

$$Z = \int [dU] \prod_f \det(D[U] + m_f) e^{-S_g[U]}$$