

Relativistic approach to atomic nuclei including quasiparticle-vibration coupling

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Outline

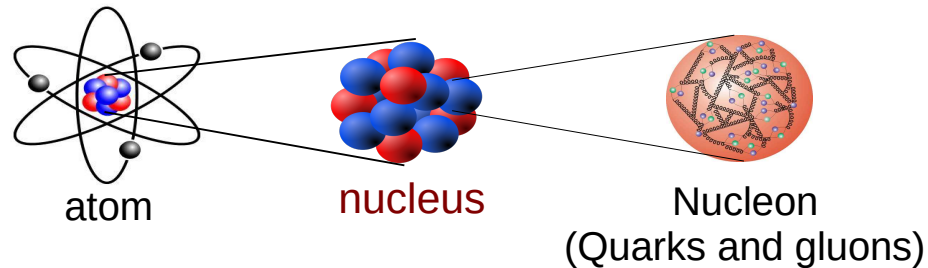
- ✦ **Introduction:**
Relativistic Nuclear Field Theory: connecting the scales of nuclear physics from Quantum Hadrodynamics to emergent collective phenomena
- ✦ **Formalism**
- ✦ **Applications to nuclear excitation modes:**
 - ★ A few results in the particle-hole neutral channel
 - ★ Response theory for spin-isospin excitations:
Gamow-Teller transitions, beta-decay half-lives and the “quenching” problem
- ✦ **Conclusion & perspectives**

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Introduction

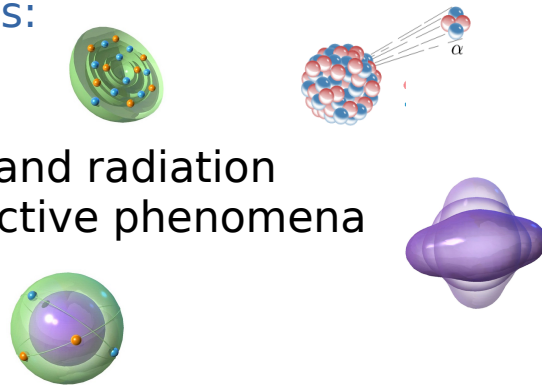
Atomic nucleus = challenging many-body system!



At the frontiers between microscopic & macroscopic worlds

★ Exhibits generic properties of many-body systems:

- ▶ shell structure
- ▶ particle-decay and radiation
- ▶ emergent collective phenomena
- ▶ superfluidity



★ Also has specific features and difficulties:

- ▶ Two types of particles (neutrons & protons) which are not structureless
- ▶ NN interaction unknown, existence of many-body forces...

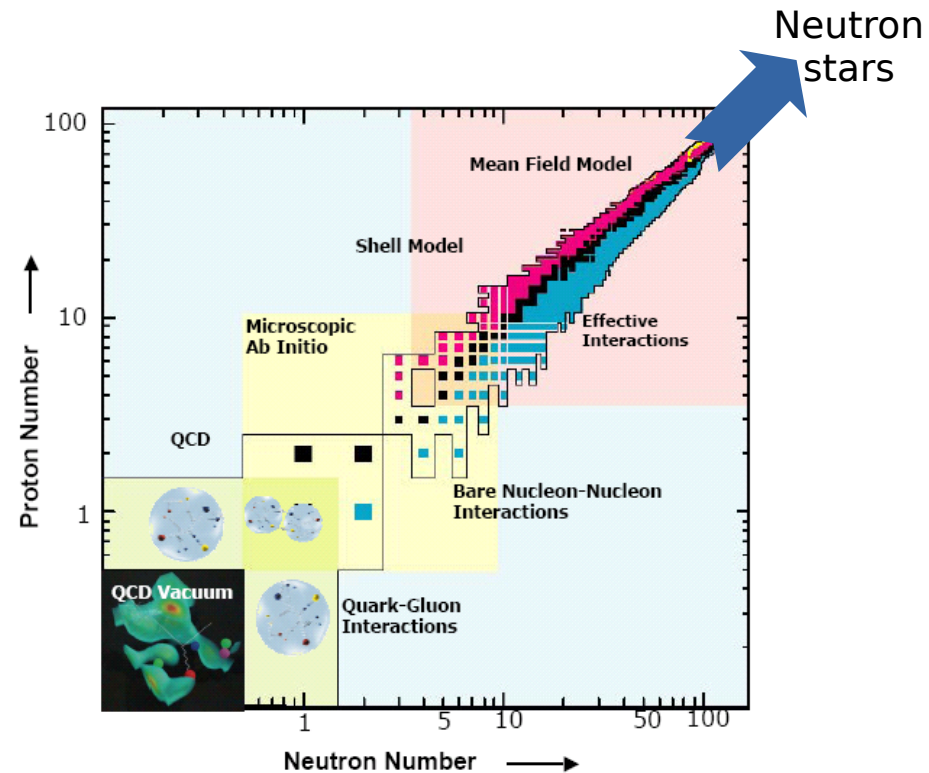



Figure: TRIUMF

Relativistic Nuclear Field Theory: foundations

→ Connects the scales from heavy mesons to the complex dynamics of heavy nuclei



Mesons

 $m_{\pi, \sigma, \omega, \rho} \sim 140-800 \text{ MeV}$



nucleons

 $S_n \sim 10 \text{ MeV}$

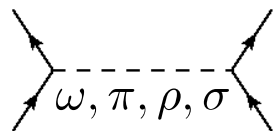


collective vibrations (phonons) $\sim \text{few MeV}$



nucleons & phonons

More correlations



Quantum Hadrodynamics (QHD)

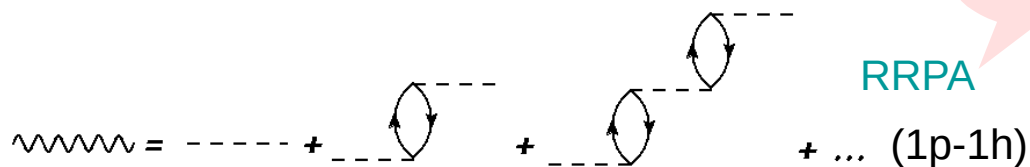
Walecka/Serot



Ring

Relativistic mean-field + superfluidity

Bogoliubov/BCS /Gorkov

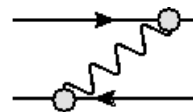


RRPA

Ring

self-consistent extensions of the Relativistic Mean-Field via Green function techniques

successive corrections in the single-particle motion and effective interaction



Argentina-Copenhagen -Milano...

Bohr-Mottelson

Nuclear Field theory - Particle-Vibration coupling

(2p-2h)

More correlations

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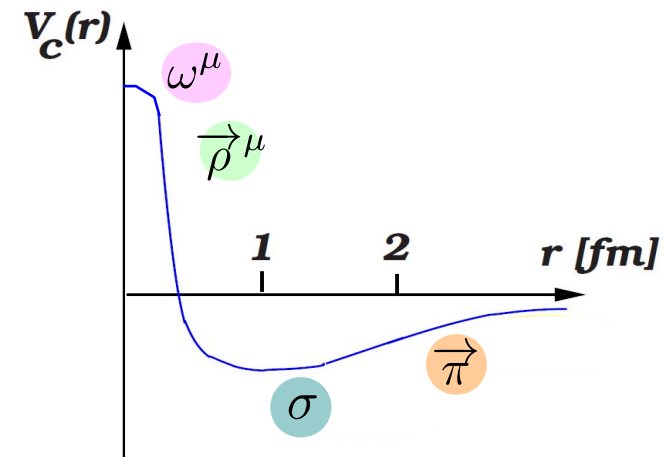
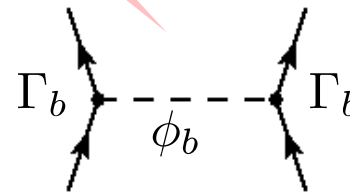
From QHD to relativistic mean field

★ Effective QHD Lagrangian:

$$\mathcal{L}_{eff} = \mathcal{L}_{Nucleons} + \mathcal{L}_{bosons} + \mathcal{L}_{int}$$

$$\phi_b = (\vec{\pi}, \sigma, \omega^\mu, \vec{\rho}^\mu, A^\mu)$$

$(J^\pi = 0^-, T = 1)$ → $\vec{\pi}$
 $(0^+, 0)$ → σ
 $(1^-, 0)$ → ω^μ
 $(1^-, 1)$ → $\vec{\rho}^\mu$



⇒ When both nucleons and mesons are quantized the equations of motion:

$$(i\gamma_\mu \partial^\mu - m - \sum_b \Gamma_b \phi_b) \psi = 0 \quad (\text{Nucleons})$$

$$(\square + m_b^2) \phi_b = \mp \bar{\psi} \Gamma_b \psi \quad (\text{Mesons})$$

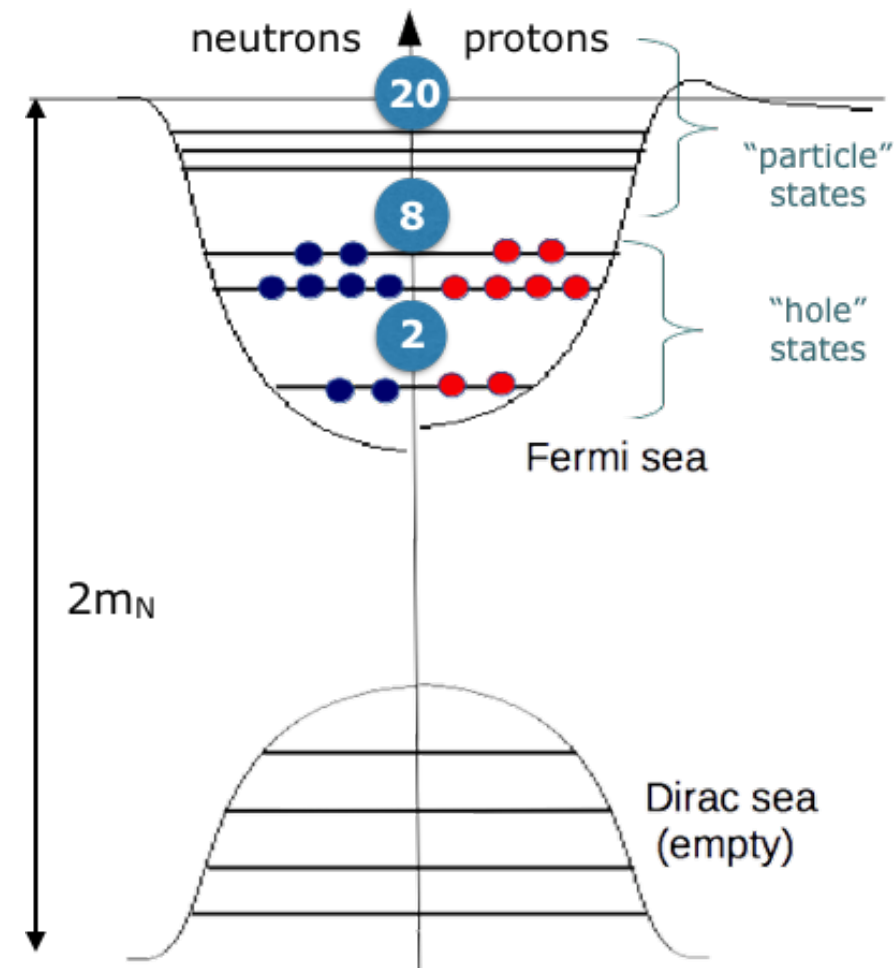
are very complicated to solve...

From QHD to relativistic mean field

★ Possible approximation: **Mean-field approximation** i.e. treat the bosons classically

$$\phi_b \rightarrow \langle \phi_b \rangle$$

⇒ the pion does not contribute in the ground state (would break parity)



⇒ EoM describe independent nucleons in classical meson fields:

$$(i\gamma_\mu \partial^\mu - m - \tilde{\Sigma}_{RMF})\psi = 0 \quad (\text{Nucleons})$$

$$(-\Delta + m_b^2)\langle \phi_b \rangle = \mp \langle \bar{\psi} \Gamma_b \psi \rangle \quad (\text{Mesons})$$

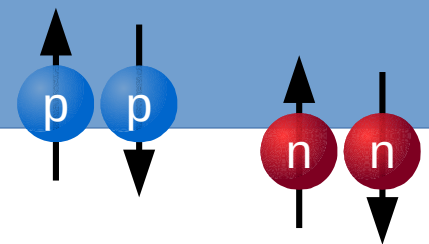
→ One-nucleon motion (propagator):

$$\text{RMF propagator} = \text{free propagator} + \text{free propagator} \circ \tilde{\Sigma}_{RMF} \circ \text{free propagator}$$

→ Static nucleonic self-energy:

$$\tilde{\Sigma}_{RMF} = \sum_b \Gamma_b \langle \phi_b \rangle = \text{Hartree}$$

From QHD to relativistic mean field



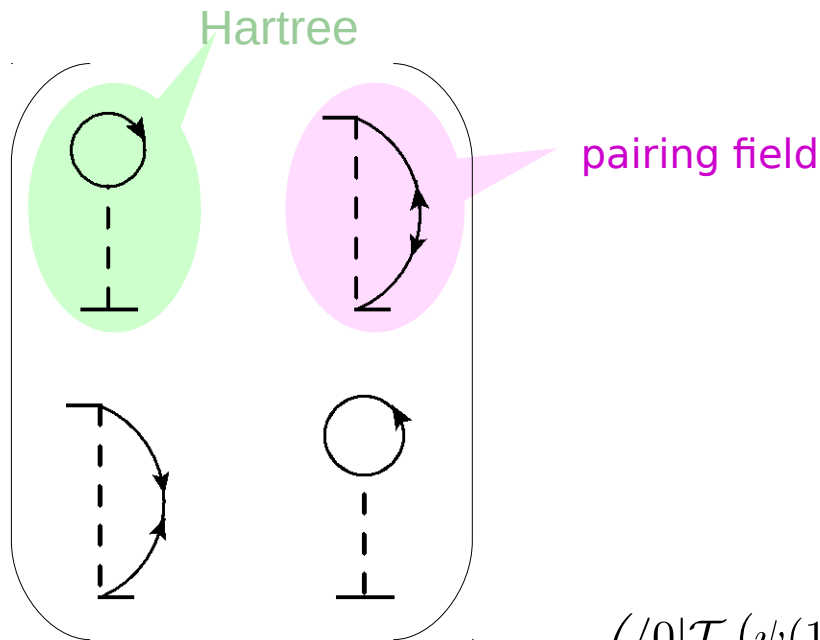
+ Superfluid pairing correlations in open-shell nuclei:

→ Introduce quasiparticles = superpositions of particles and holes (BCS/Bogoliubov)

$$\Rightarrow \begin{cases} (-\Delta + m_b^2)\langle\phi_b\rangle = \mp\langle V^T \beta \Gamma_b V^* \rangle & \text{(for bosons)} \\ \mathcal{H}_{RHB}|\psi_k^\eta\rangle = \eta E_k |\psi_k^\eta\rangle, \eta = \pm 1 & \text{(for quasi-nucleons)} \end{cases}$$

• RHB self-energy:

$$\tilde{\Sigma}_{RHB} =$$

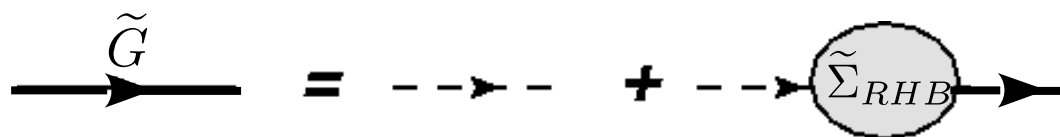


Quasiparticles and quasiholes

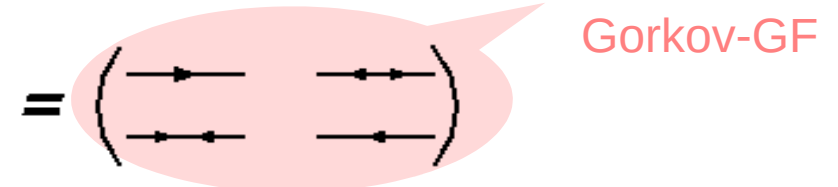
$$|\psi_k^+\rangle = \begin{pmatrix} U_k \\ V_k \end{pmatrix} \quad |\psi_k^-\rangle = \begin{pmatrix} V_k^* \\ U_k \end{pmatrix}$$



→ RHB quasiparticle propagator:

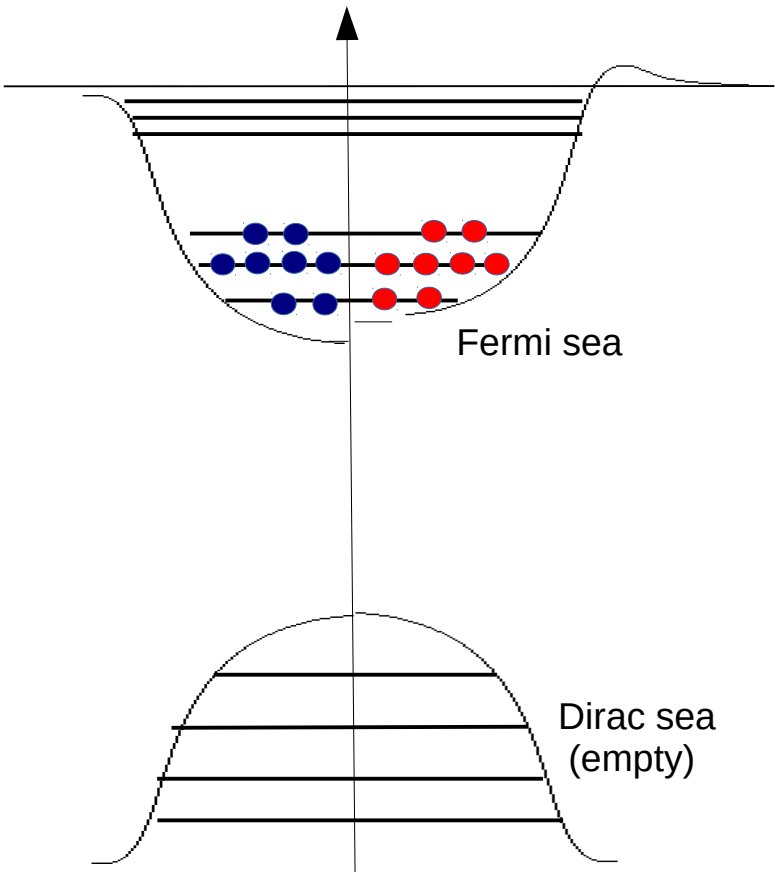


$$\begin{pmatrix} \langle 0 | \mathcal{T} (\psi(1) \bar{\psi}(2)) | 0 \rangle & \langle 0 | \mathcal{T} (\psi(1) \psi(2)) | 0 \rangle \\ \langle 0 | \mathcal{T} (\bar{\psi}(1) \bar{\psi}(2)) | 0 \rangle & \langle 0 | \mathcal{T} (\bar{\psi}(1) \psi(2)) | 0 \rangle \end{pmatrix}$$



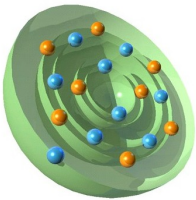
Gorkov-GF

Going beyond mean-field: quasiparticles coupled to vibrations

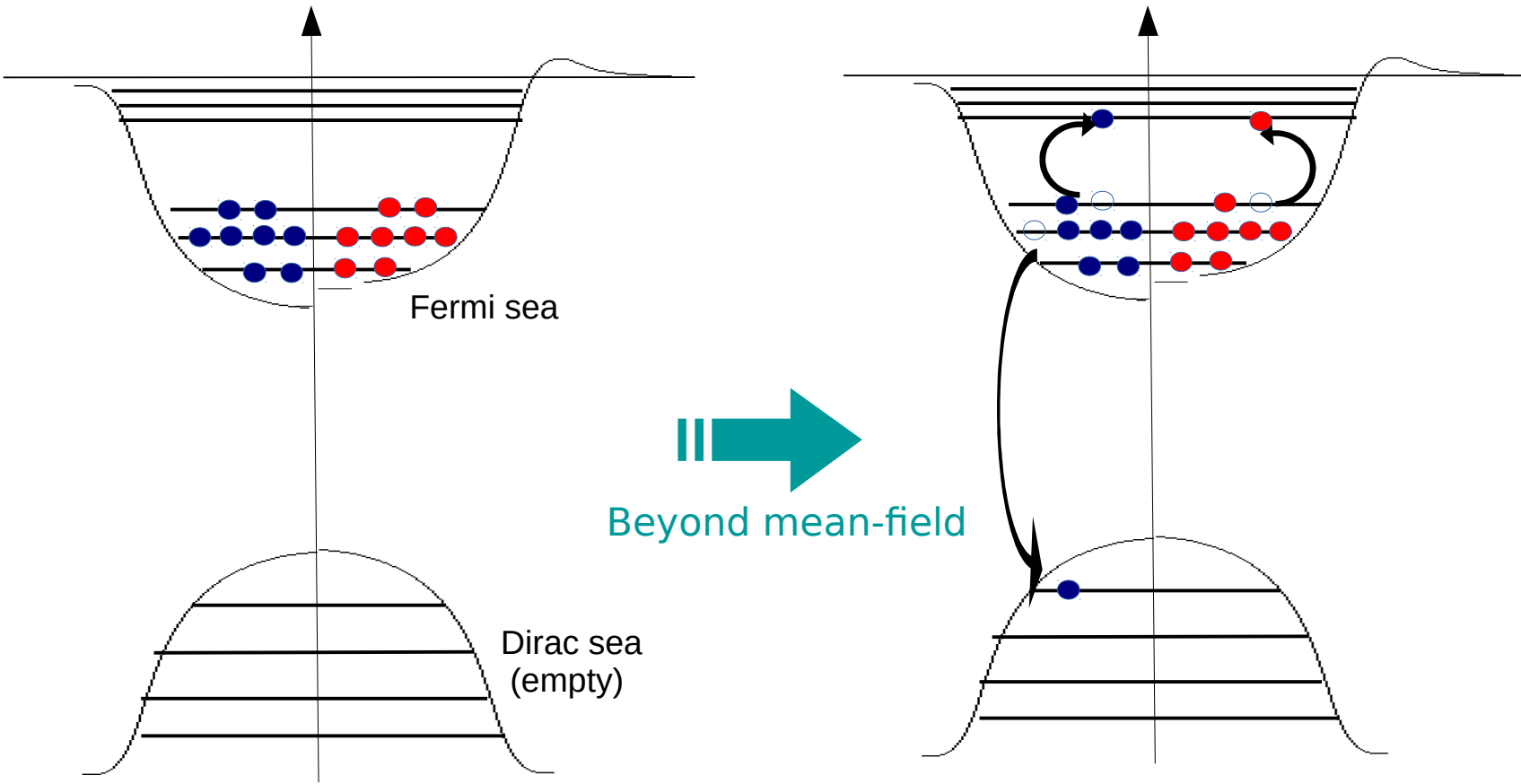


Mean-field ground-state

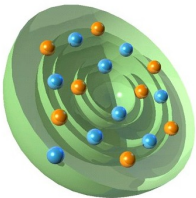
- = independent (quasi)particles
- = 0-th order approximation



Going beyond mean-field: quasiparticles coupled to vibrations



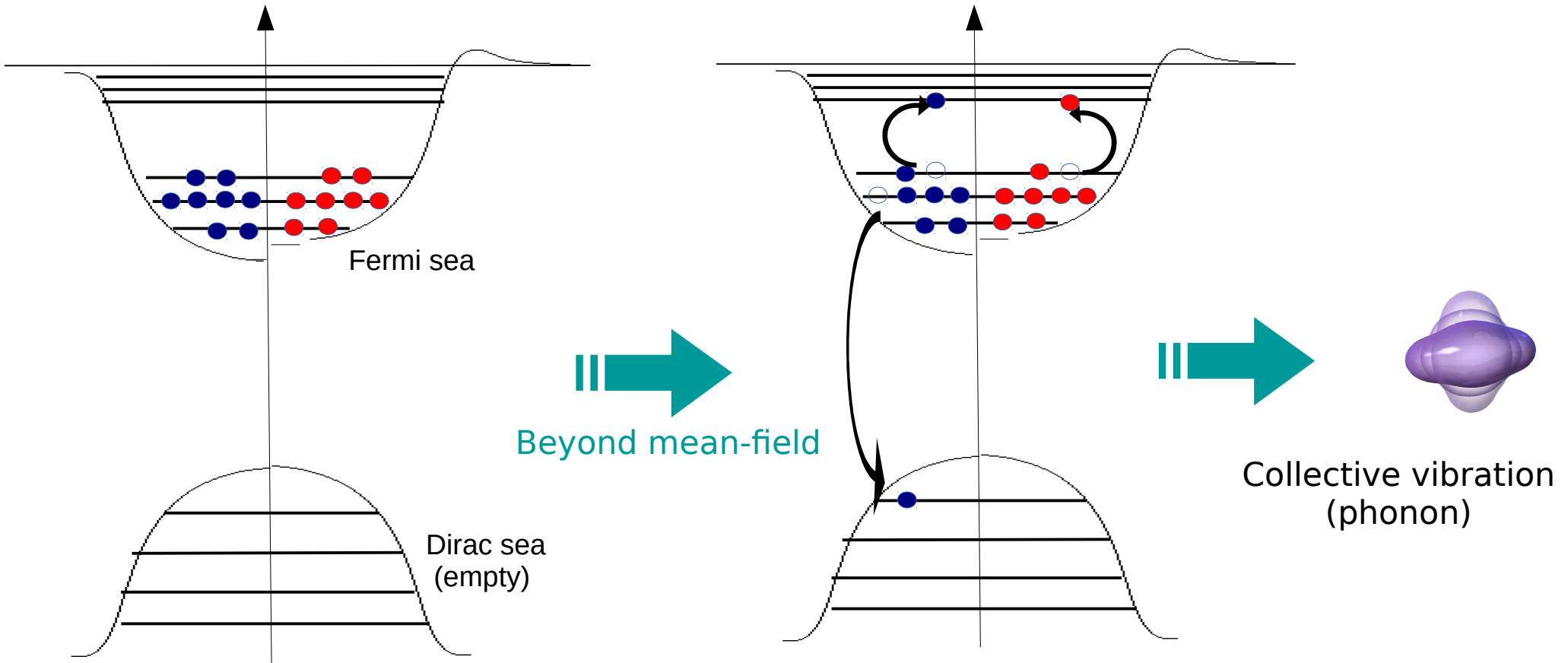
Mean-field ground-state
= independent (quasi)particles
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correlations

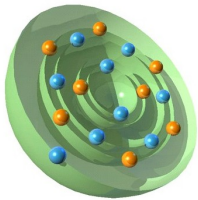


Going beyond mean-field: quasiparticles coupled to vibrations

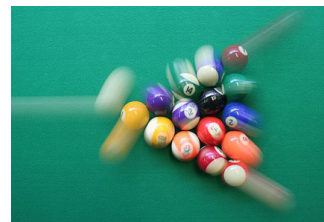


Mean-field ground-state

- = independent (quasi)particles
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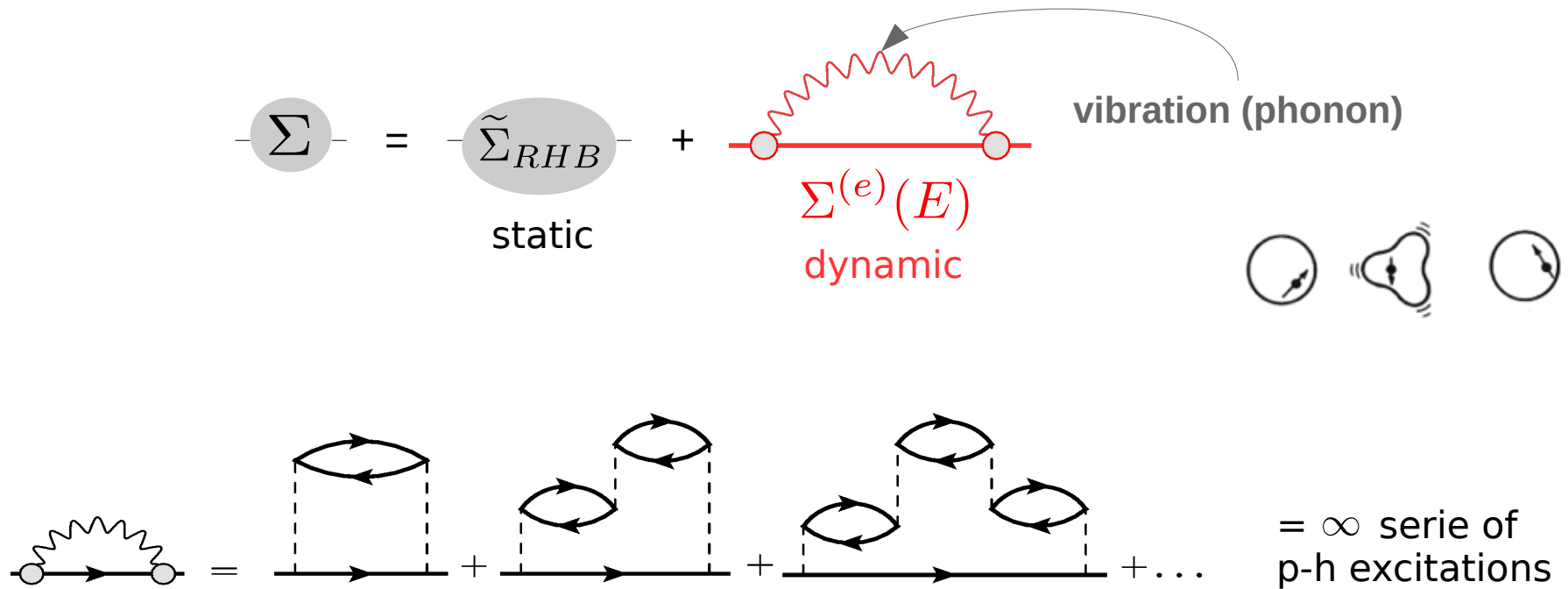


correlations

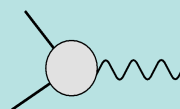


Going beyond mean-field: Quasiparticles coupled to vibrations

★ Quasiparticle-Vibration Coupling (QVC) in the nucleonic self-energy:

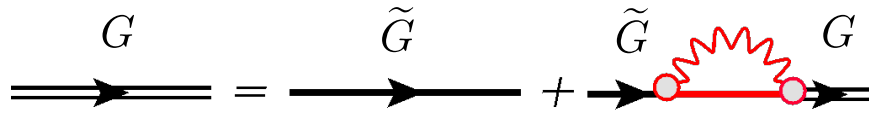


→ Allows a non perturbative treatment of the NN interaction

→ New order parameter = QVC vertex 

Going beyond mean-field: Quasiparticles coupled to vibrations

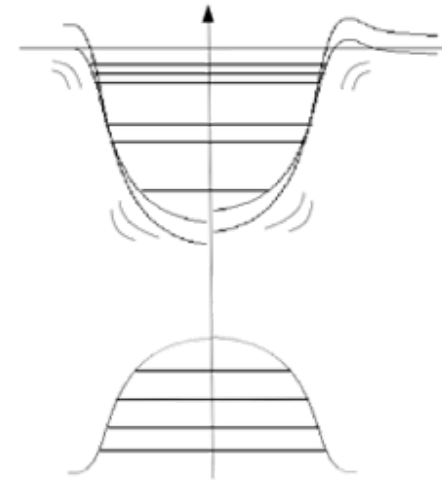
→ quasi-particle propagator:



$$G(E) = \left(\varepsilon - \mathcal{H}_{RHB} - \underbrace{\Sigma^{(e)}(E)} \right)^{-1}$$

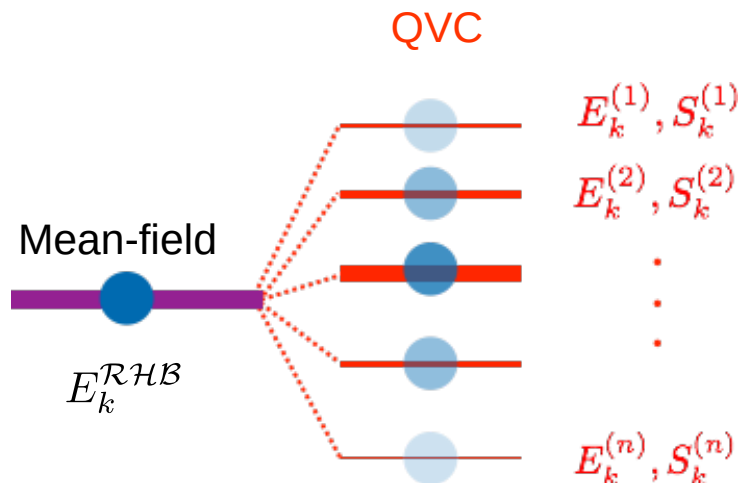
Introduces new poles

$$E_k^{(\nu)} = E_k^{\mathcal{RHB}} + \Sigma_k^{(e)}(E_k^{(\nu)})$$



$$\Sigma_{k_1 k_2}^{(e)\eta_1 \eta_2}(\varepsilon) = \sum_{\eta=\pm 1} \sum_{k, \mu} \frac{\gamma_{\mu; k_1 k}^{\eta; \eta_1 \eta} \gamma_{\mu; k_2 k}^{\eta; \eta_2 \eta^*}}{\varepsilon - \eta(E_k + \Omega_\mu - i\delta)}$$

→ fragmentation of single (quasi)particle states:



No more well defined (quasi)nucleons on single (quasi)particle shells
→ fractional occupation numbers

$$E_k^{\mathcal{RHB}} = \sum_{\nu} S_k^{(\nu)} E_k^{(\nu)}$$

$$\sum_{\nu} S_k^{(\nu)} = 1$$

Excited states: nuclear response theory

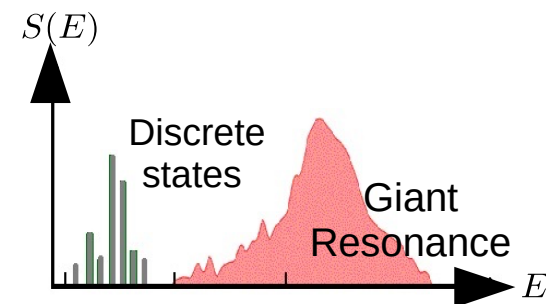
★ Response of the nucleus to an external field:



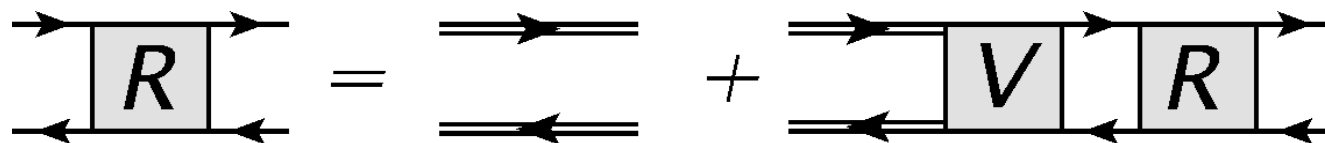
→ Transition strength:

$$S(E) = \sum_f |\langle \Psi_f | \hat{F} | \Psi_i \rangle|^2 \delta(E - E_f + E_i)$$

$$= -\frac{1}{\pi} \lim_{\Delta \rightarrow 0^+} \text{Im} \langle \Psi_i | \hat{F}^\dagger R(E + i\Delta) \hat{F} | \Psi_i \rangle$$



Response function (2-body propagator)
solution of the Bethe-Salpeter equation (BSE):



$$V = i \frac{\delta \Sigma}{\delta G}$$

effective interaction induced by the nuclear medium

Excited states: nuclear response theory

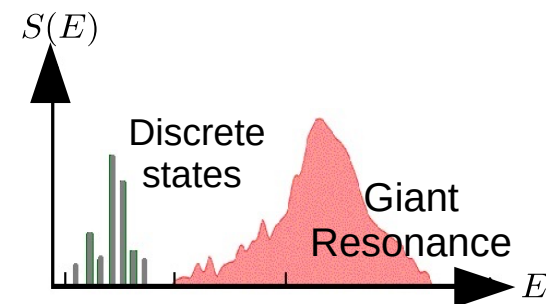
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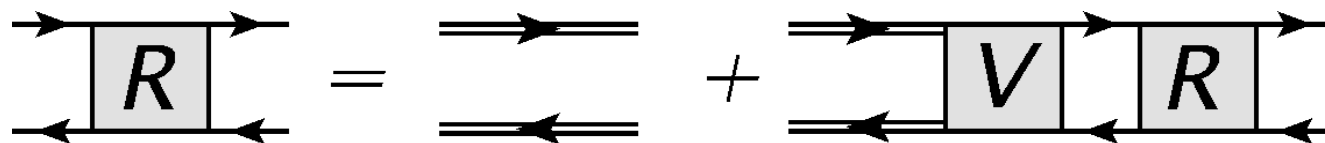
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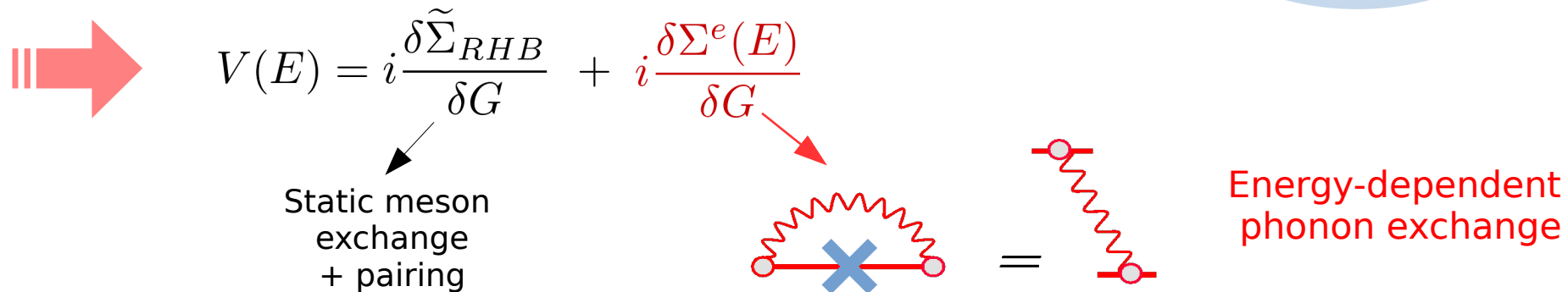


Response function (2-body propagator)
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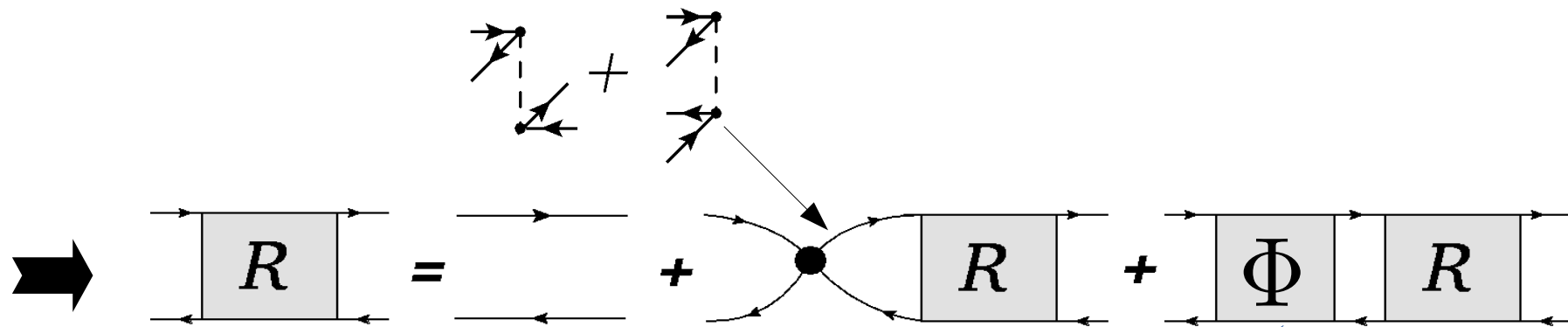


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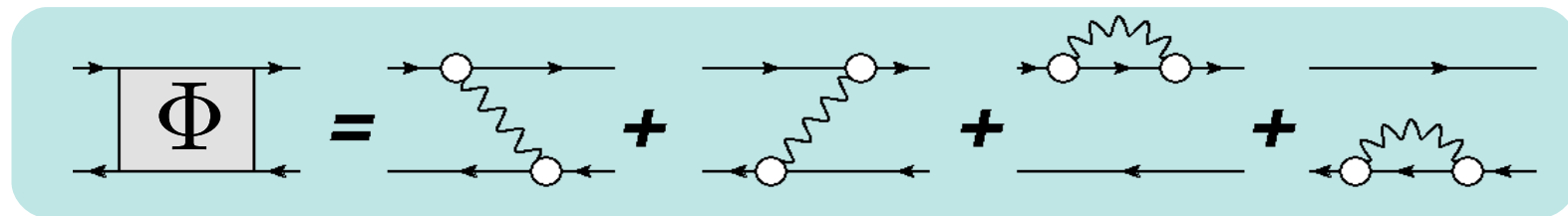
effective interaction induced by the nuclear medium



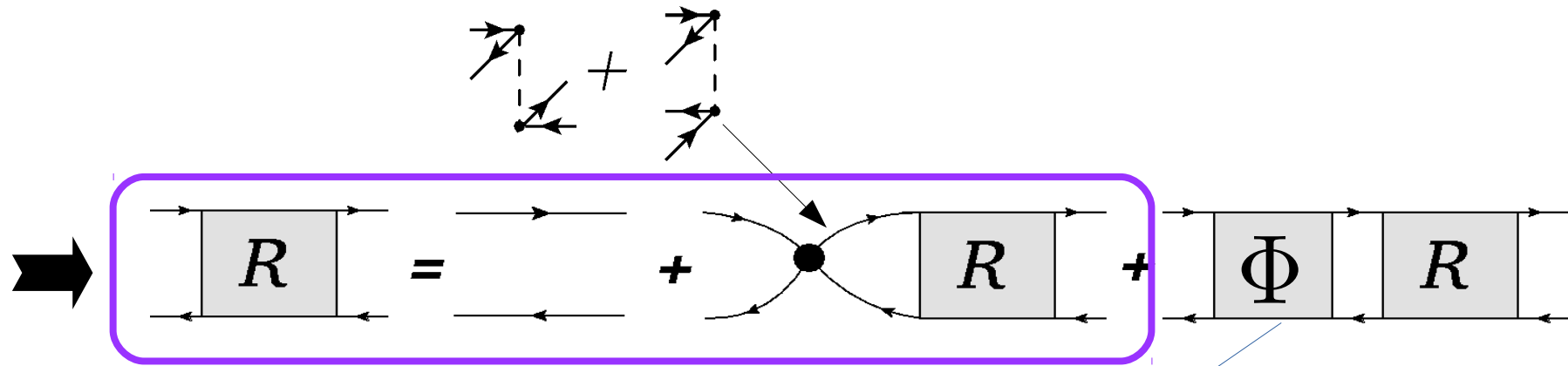
Excited states: nuclear response theory



Quasiparticle-Vibration Coupling amplitude:

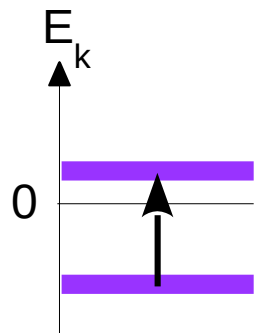
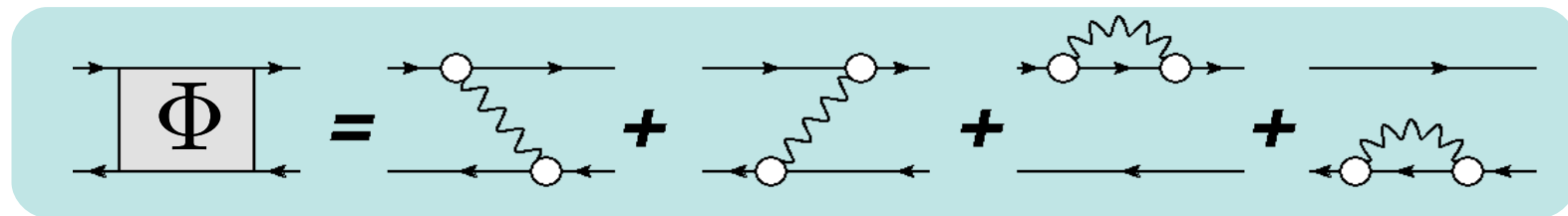


Excited states: nuclear response theory

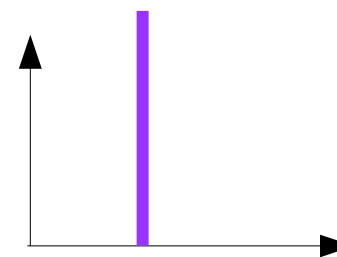


Relativistic Quasiparticle Random Phase Approximation (RQRPA)

Quasiparticle-Vibration Coupling amplitude:



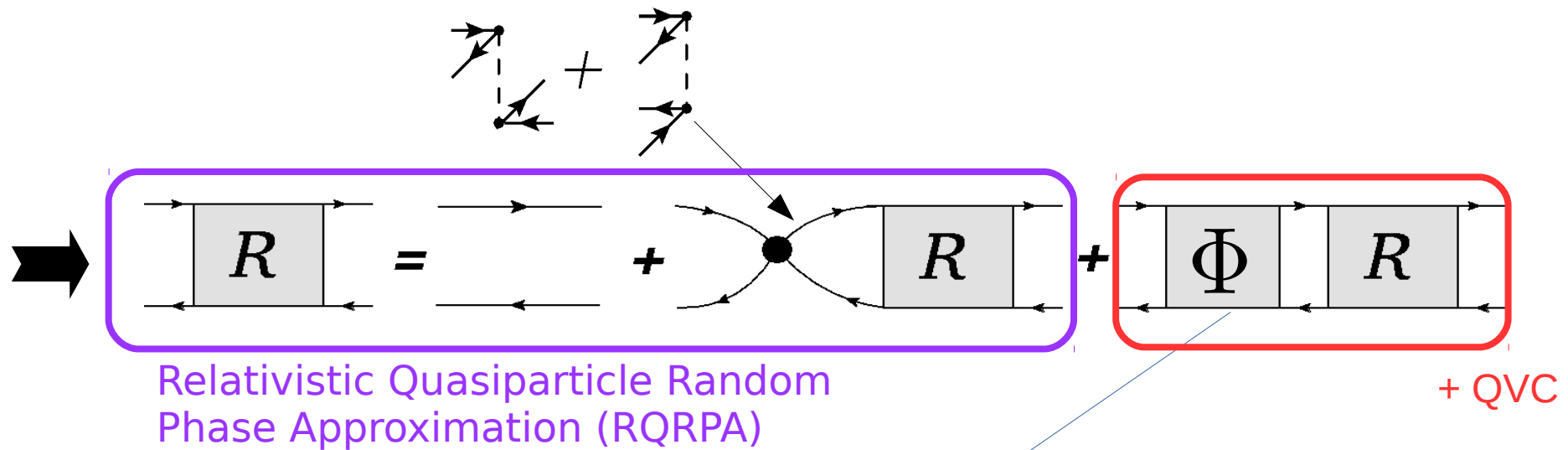
Single-particle states



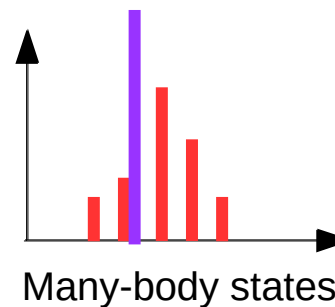
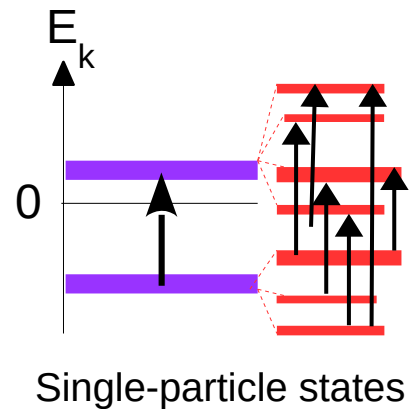
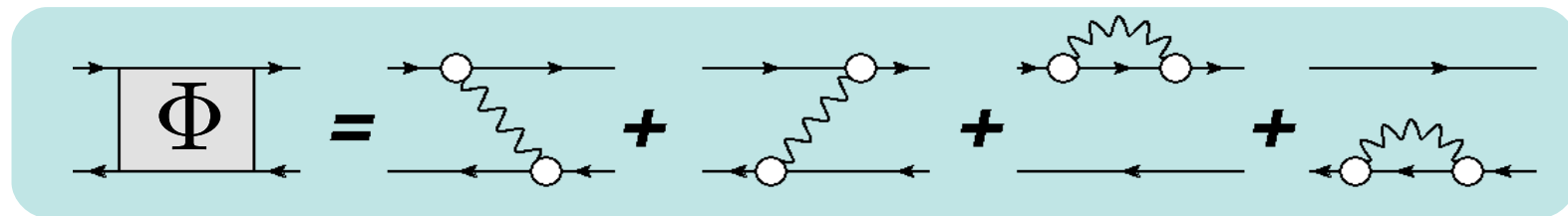
Many-body states

$1(q)p-1(q)h$ configurations

Excited states: nuclear response theory



Quasiparticle-Vibration Coupling amplitude:

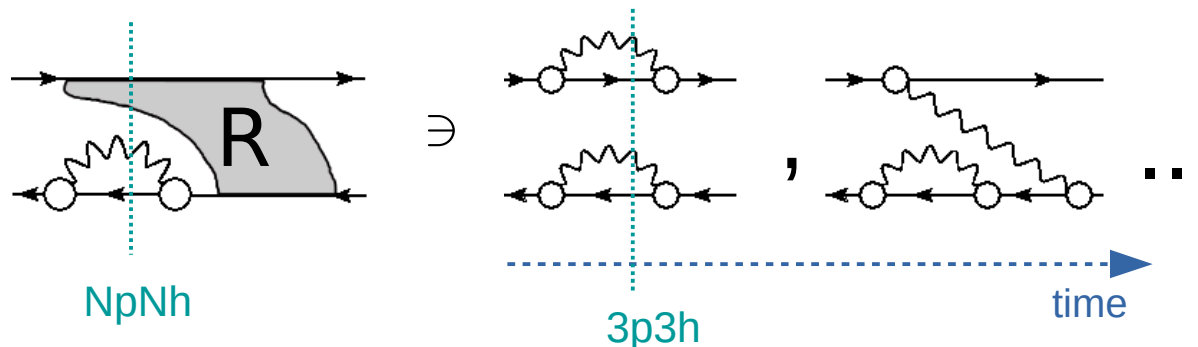


✓ spreading width

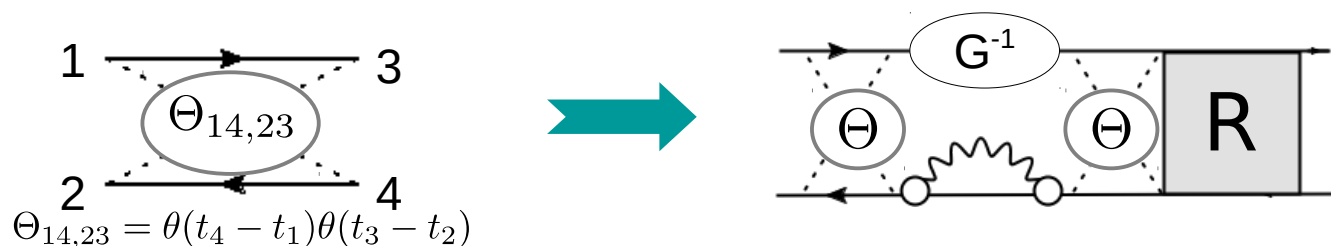
$1(q)p-1(q)h \otimes 1$ phonon configurations

Excited states: nuclear response theory

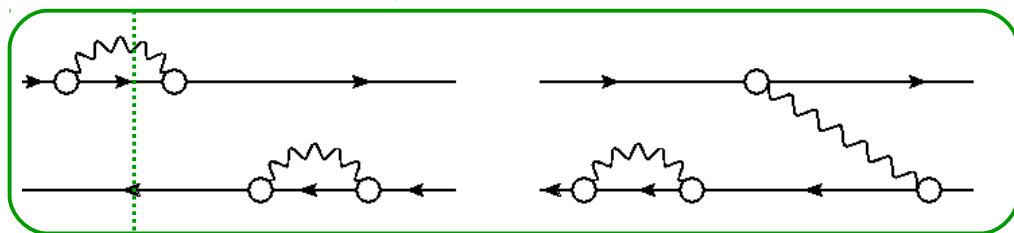
Problem: Integration over all intermediate times \Rightarrow complicated BSE (integrations do not separate), appearance of $NpNh$ configurations:



Solution: Time-Blocking Approximation [V.I. Tselyaev, Yad. Fiz. 50,1252 (1989)]

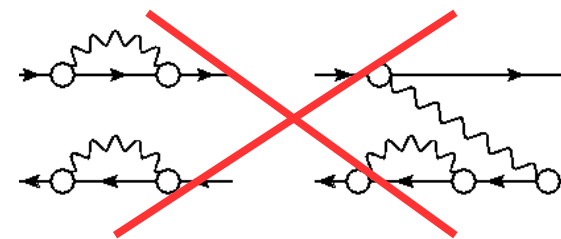


\rightarrow allowed configurations:



\rightarrow $1(q)p-1(q)h \otimes 1$ phonon i.e. $2(q)p2(q)h$
 \rightarrow spreading

\rightarrow blocked configurations: $3(q)p-3(q)h, 4(q)p4(q)h\dots$

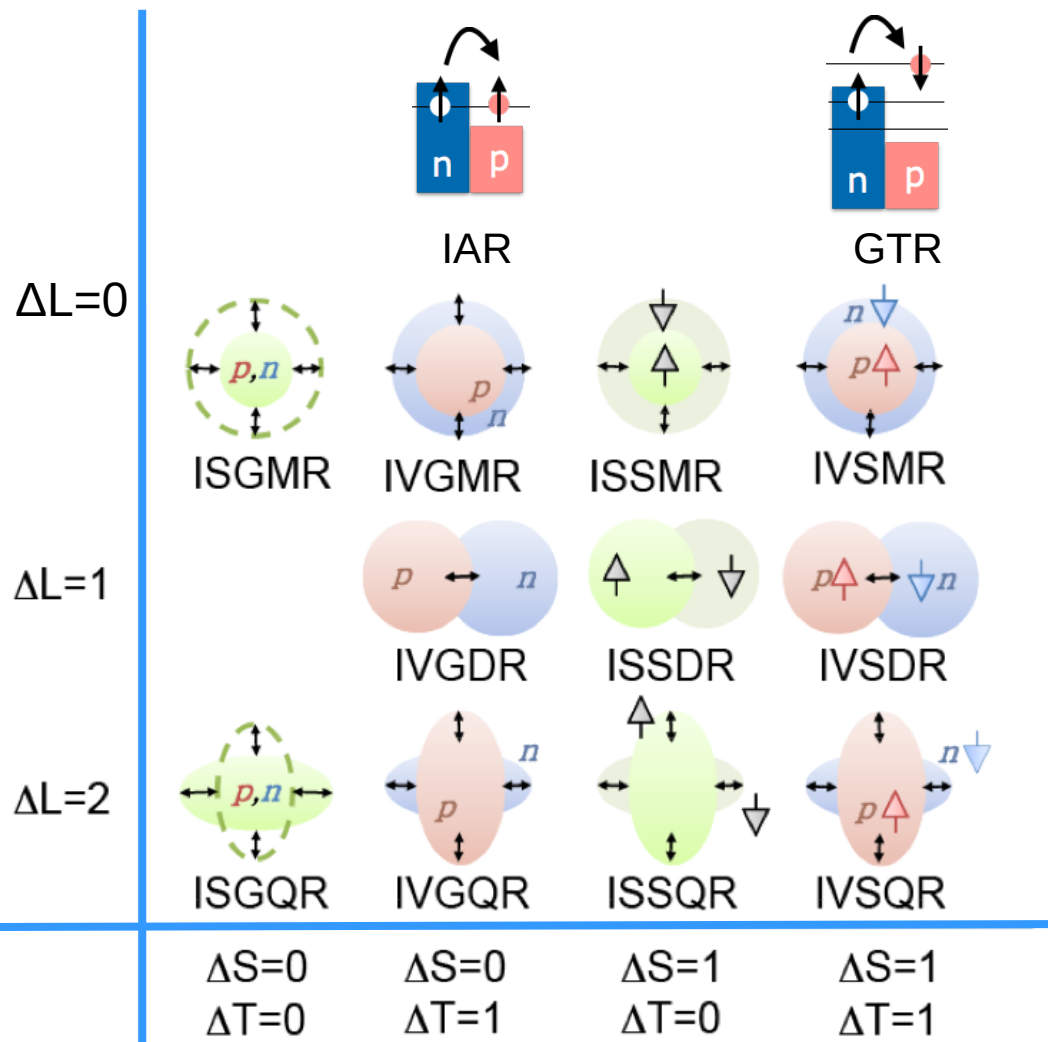


... but can be included in a next step
 (under development)

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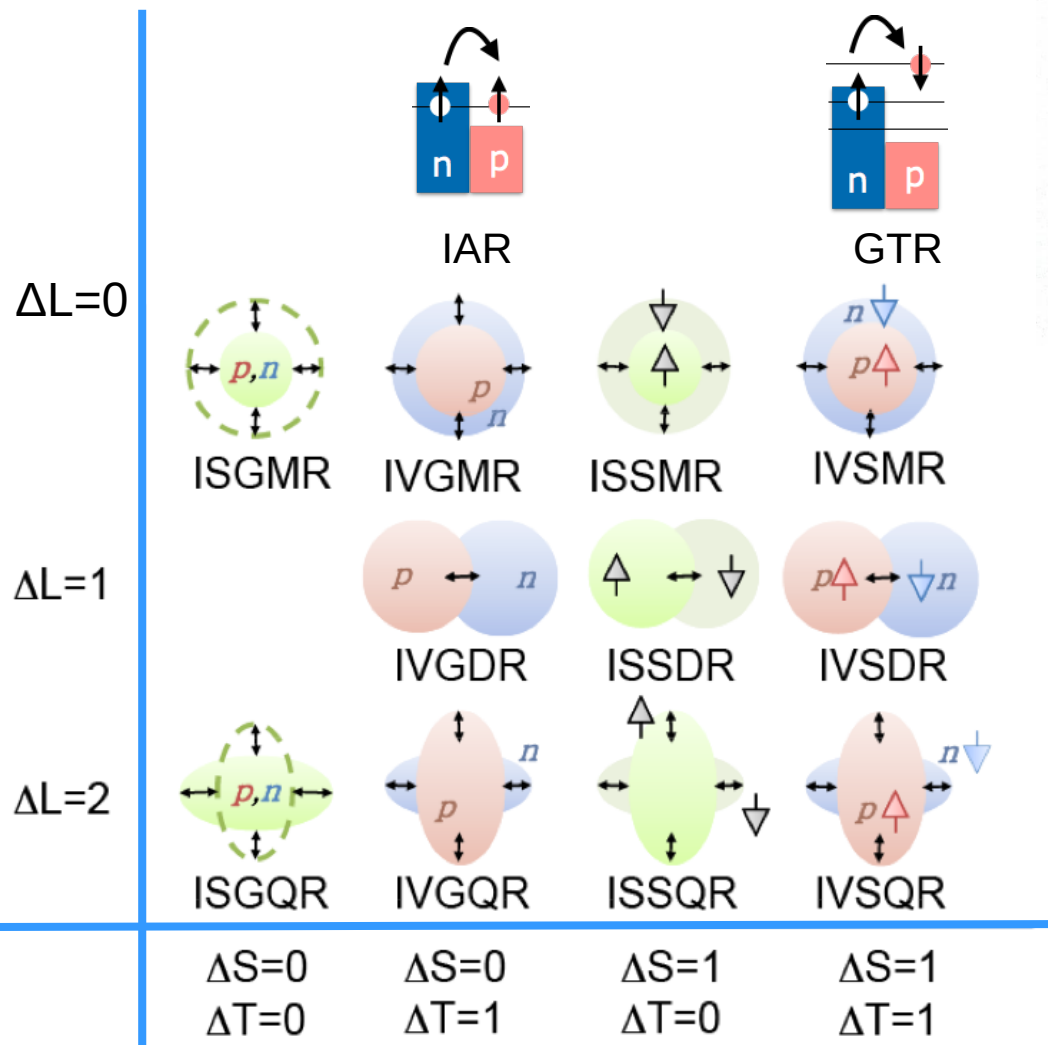
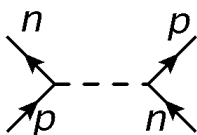
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Nuclear vibrational motion and their applications

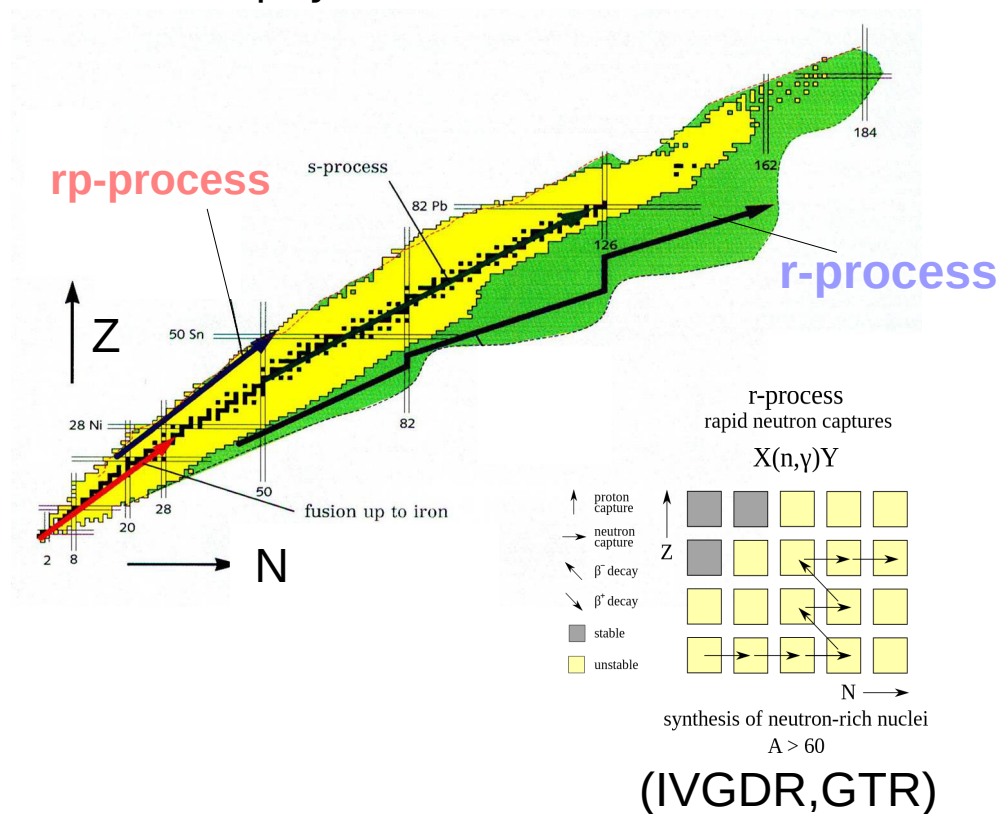


Nuclear vibrational motion and their applications

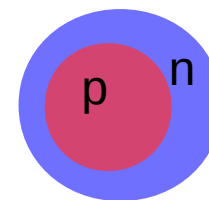
★ Channels of the nuclear interaction



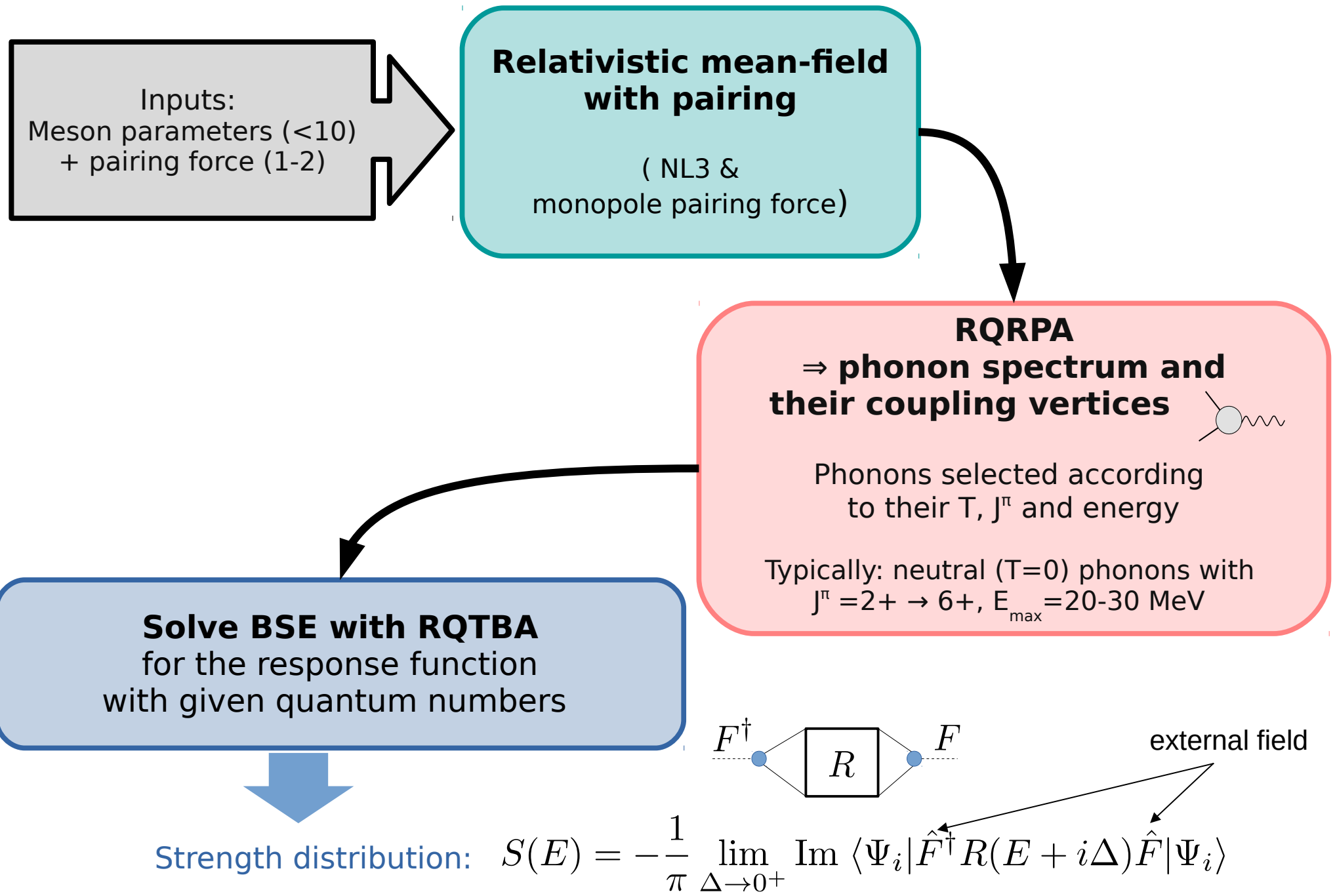
★ Astrophysics: (IAR,GTR,IVGDR...)



★ Neutron skin thickness (IVGDR,IVSGDR...)



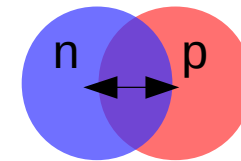
Numerical scheme



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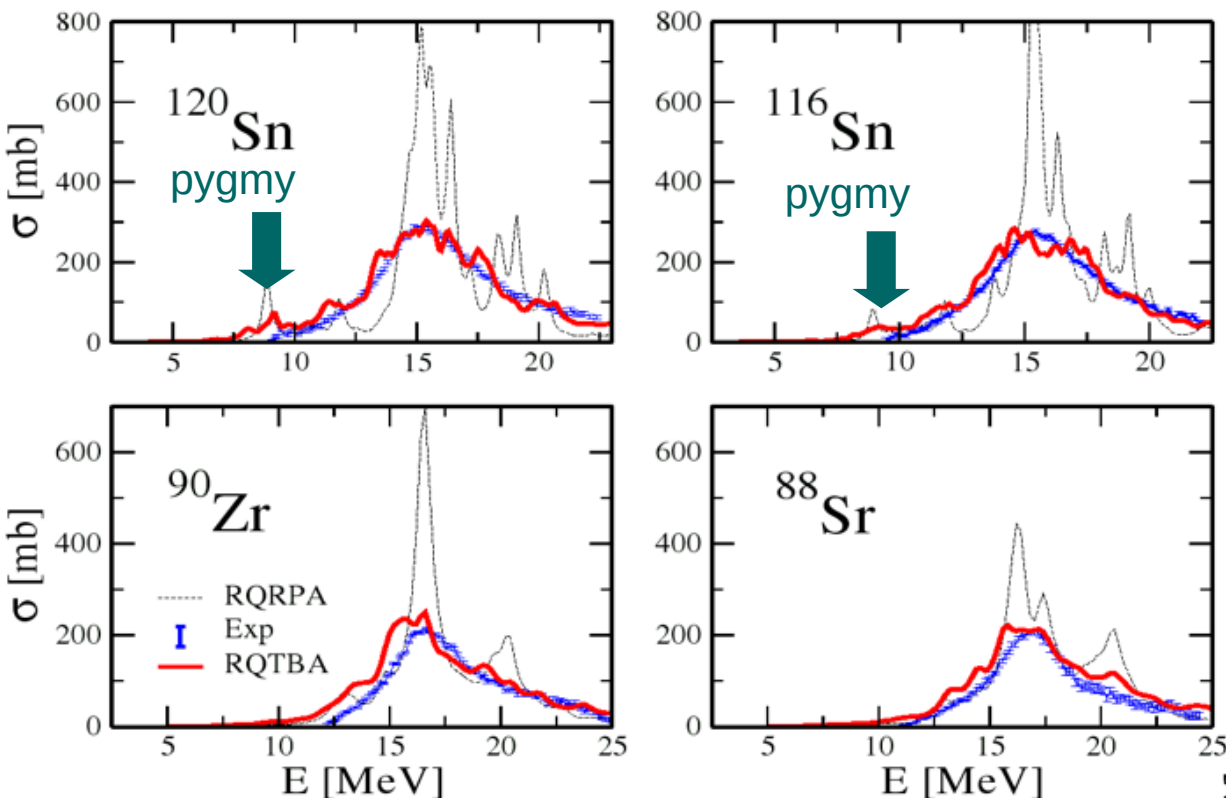
A few results in the ph neutral ($\Delta T_z=0$) channel



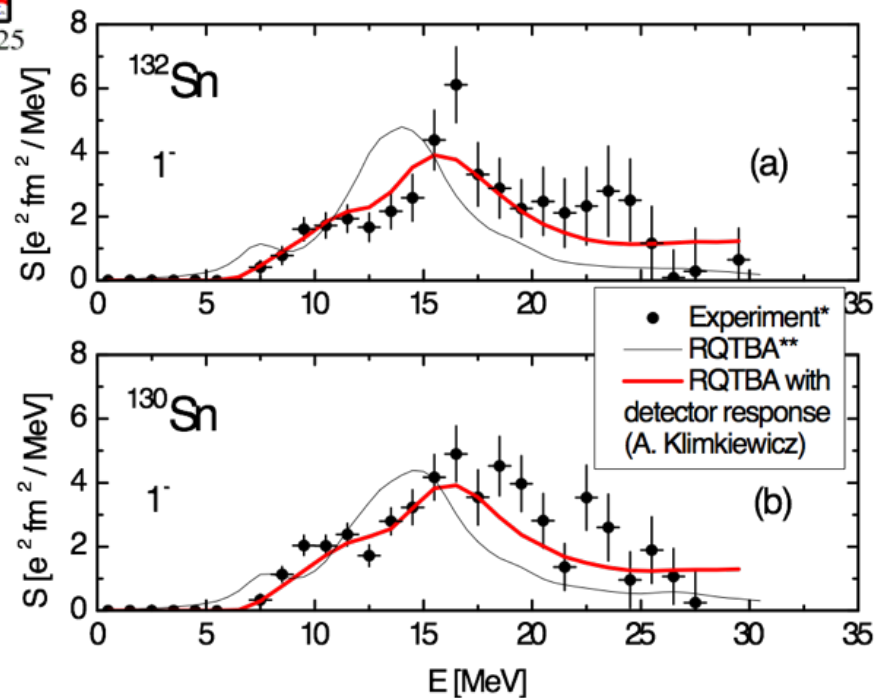
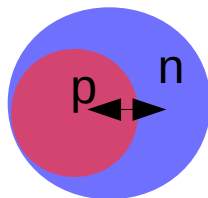
Test case: E1 (IVGDR)

Giant and pygmy resonances

Neutron-rich nuclei:

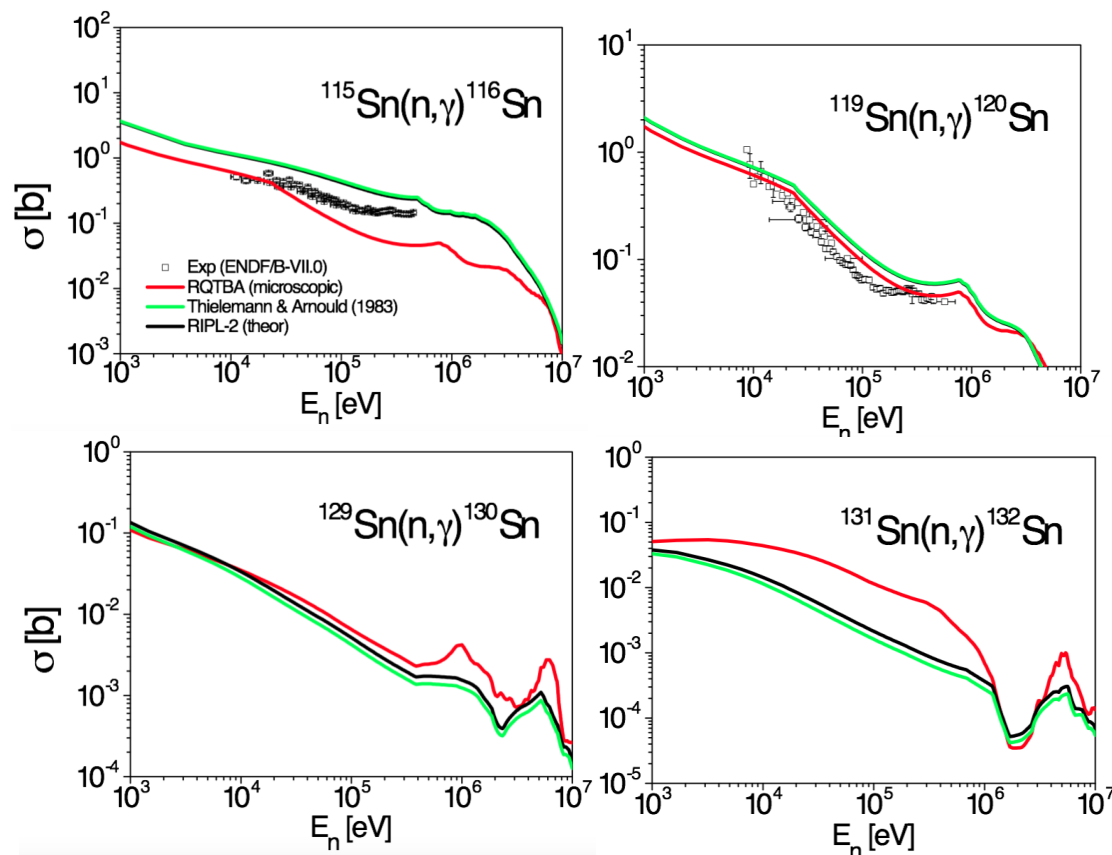


Pygmy Dipole Resonance (PDR):
Oscillation of the neutron skin against the core



- Litvinova, Ring, and Tselyaev, PRC 78, 014312 (2008)
- Adrich et al., PRL 95, 132501 (2005)
- Litvinova, Ring, Tselyaev, Langanke, PRC 79, 054312 (2009)

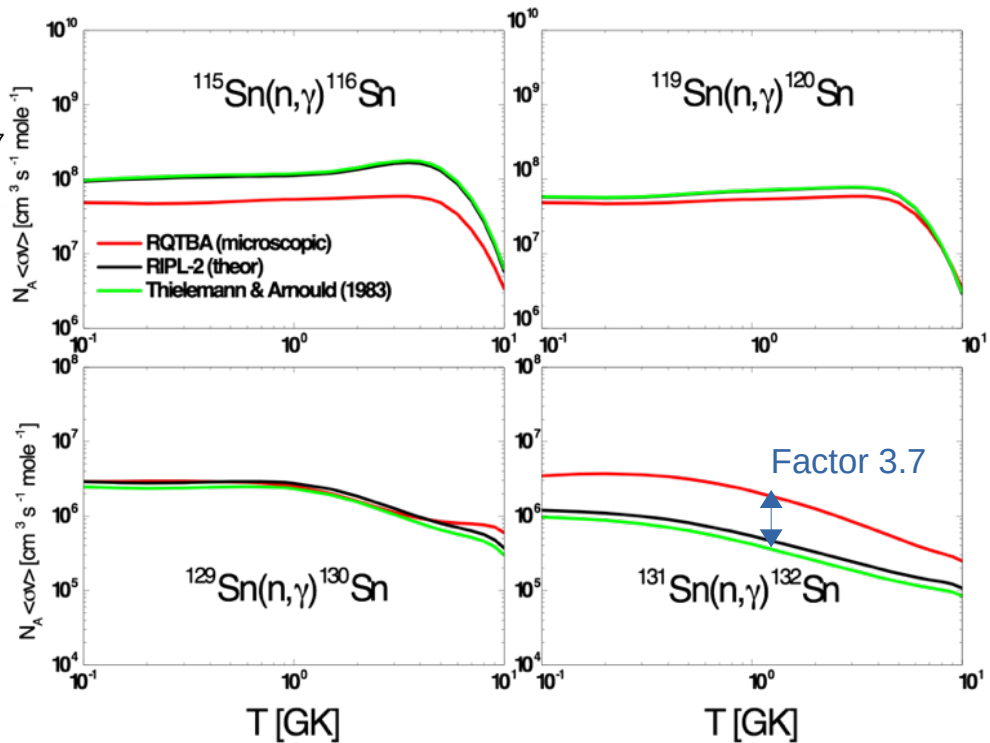
A few results in the ph neutral ($\Delta T_z=0$) channel



(n, γ) stellar reaction rates



Microscopic structure is important, especially when PDR is at the neutron threshold



Radiative neutron capture in the Hauser-Feshbach model: standard Lorentzians vs microscopic structure

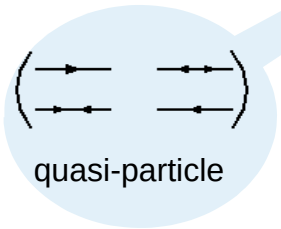
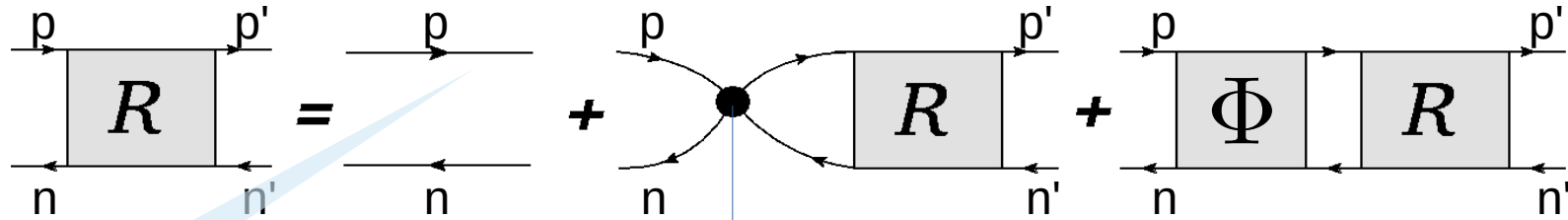
E. Litvinova et al., Nucl. Phys. A 823, 26 (2009).

Outline

- ✦ **Introduction:**
Relativistic Nuclear Field Theory: connecting the scales of nuclear physics from Quantum Hadrodynamics to emergent collective phenomena
- ✦ **Formalism**
- ✦ **Applications to nuclear excitation modes:**
 - ★ A few results in the particle-hole neutral channel
 - ★ Response theory for spin-isospin excitations:
Gamow-Teller transitions, beta-decay half-lives and the “quenching” problem
- ✦ **Conclusion & perspectives**

Response theory for isospin-transfer modes

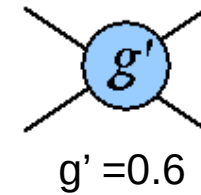
★ Response in the ph proton-neutron channel:



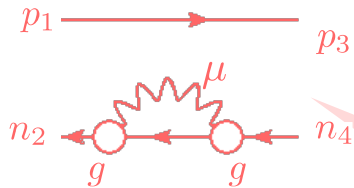
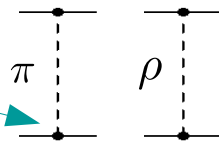
isovector interaction

$$\tilde{V} = V_\pi + V_\rho + V_{\delta\pi}$$

Landau-Migdal contact term

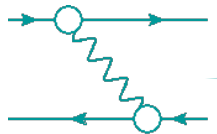
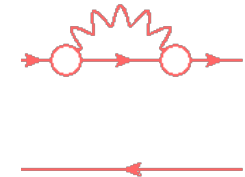


free-space coupling constant

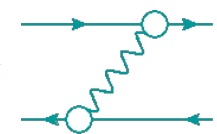


$$\Phi_{p_1 n_4, n_2 p_3}^\eta(\omega) =$$

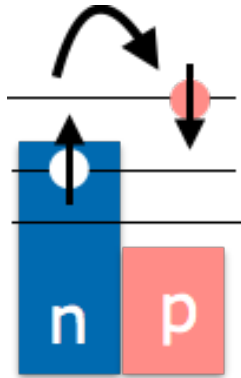
$$\sum_{\mu\xi} \delta_{\eta\xi} \left[\delta_{p_1 p_3} \sum_{n_6} \frac{g_{\mu; n_6 n_2}^{\eta; -\xi} g_{\mu; n_6 n_4}^{\eta; -\xi*}}{\eta\omega - E_{p_1} - E_{n_6} - \Omega_\mu} + \delta_{n_2 n_4} \sum_{p_5} \frac{g_{\mu; p_1 p_5}^{\eta; \xi} g_{\mu; p_3 p_5}^{\eta; \xi*}}{\eta\omega - E_{p_5} - E_{n_2} - \Omega_\mu} \right]$$



$$\left[\frac{g_{\mu; p_1 p_3}^{\eta; \xi} g_{\mu; n_2 n_4}^{\eta; -\xi*}}{\eta\omega - E_{p_3} - E_{n_2} - \Omega_\mu} - \frac{g_{\mu; p_1 p_3}^{\eta; \xi*} g_{\mu; n_4 n_2}^{\eta; -\xi}}{\eta\omega - E_{p_1} - E_{n_4} - \Omega_\mu} \right]$$



Gamow-Teller transitions in Nickel isotopes (Ni → Cu)



$$F_{GT^-} = \sum_n \begin{pmatrix} \sigma_{(n)}^i & 0 \\ 0 & \sigma_{(n)}^i \end{pmatrix} \tau_{-}^{(n)}$$

$$\Delta T_z = -1$$

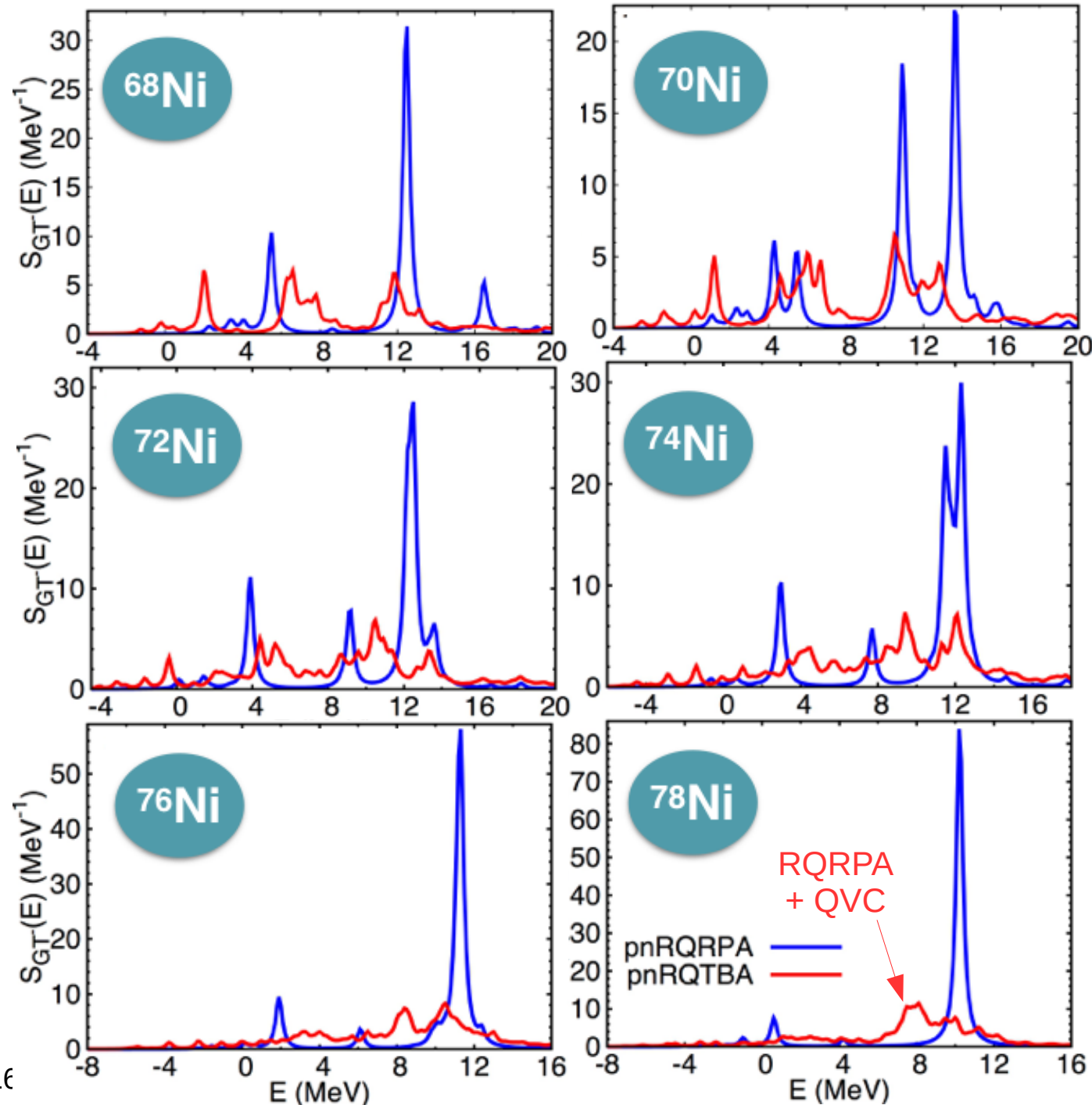
$$\Delta S = 1$$

$$\Delta L = 0$$

QPVC brings fragmentation of the strength and distribution over a larger energy range

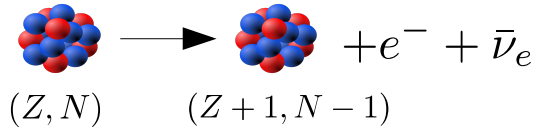
(Smearing $\Delta = 200$ keV)

C. R. and E. Litvinova EPJA 52, 205 (2016)



Low-energy GT strength and β -decay half-lives

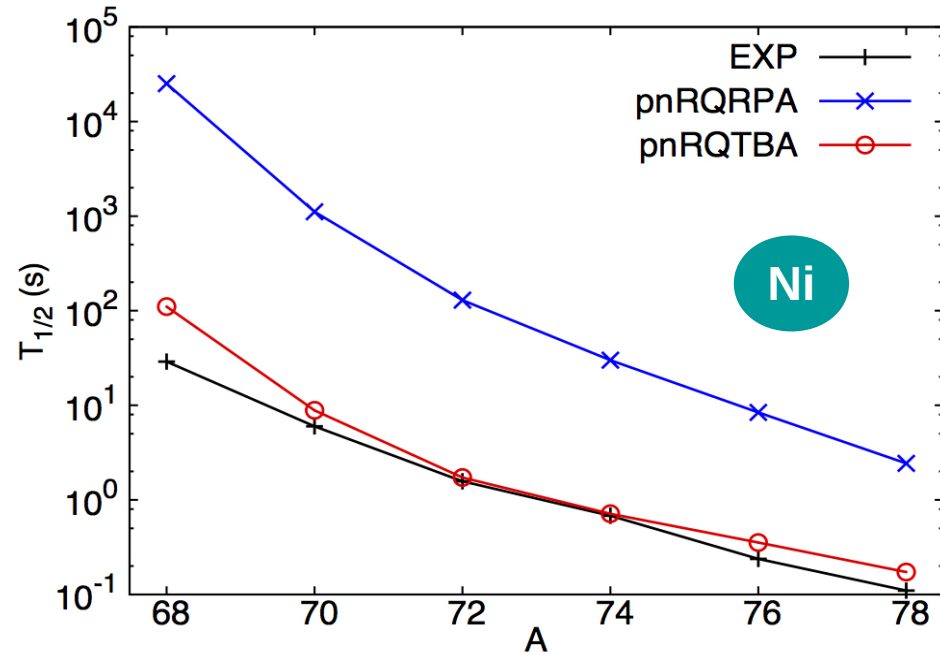
★ Half-lives and low-energy strength:



$$\frac{1}{T_{1/2}} = \frac{g_a^2}{D} \int^{Q_\beta} f(Z, Q_\beta - E) S(E) dE$$

With $g_a = 1$

Leptonic phase-space factor



→ big improvement due to QVC!



- ^{68}Ni and ^{70}Ni : appearance of strength in the Q_β window due to QVC → finite lifetime
- ^{78}Ni : more strength with RQRPA but located at higher energies → smaller lifetime with QVC due to phase space factor

Gamow-Teller transitions and the “quenching” problem

● “Quenching problem”:

The observed GT strength (\sim up to the GR region) in nuclei is \sim 30-40% less than the model independent Ikeda sum rule: $S_- - S_+ = 3(N-Z)$

$$S_- = \sum B(GT^-) \quad \begin{array}{|c|c|} \hline \text{n} & \text{p} \\ \hline \end{array} \quad S_+ = \sum B(GT^+) \quad \begin{array}{|c|c|} \hline \text{n} & \text{p} \\ \hline \end{array}$$


\Rightarrow some strength is pushed at high energies \rightarrow possible mechanisms?

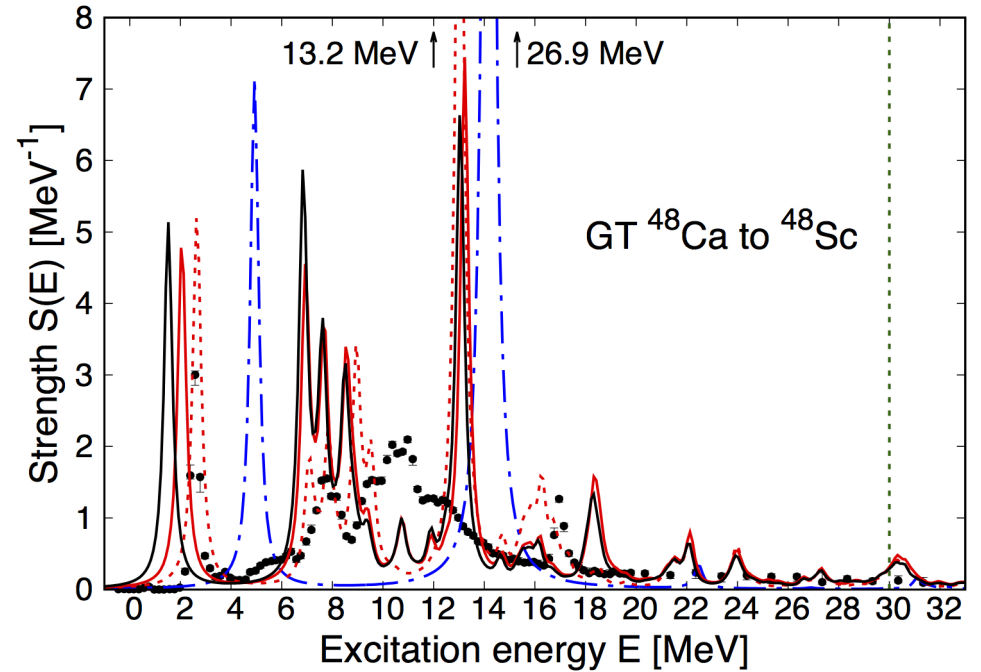
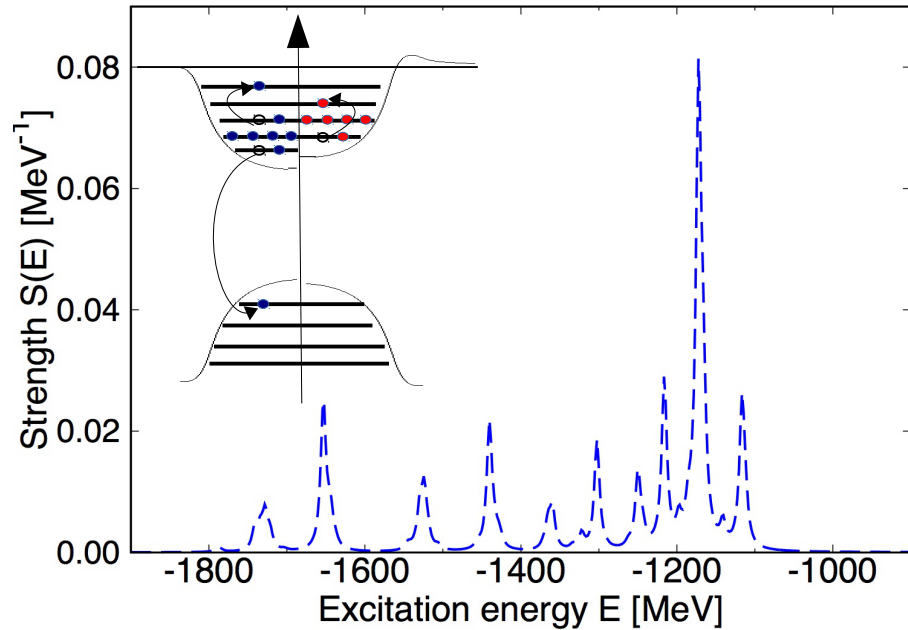
- ★ Coupling of 1p1h to Δ baryon (believed to be small)
- ★ Coupling of 1p1h to higher-order configurations such as 2p2h, 3p3h... (Believed to be the most important)

\Rightarrow important to introduce complex configurations in large model spaces

At present with RNFT+TBA:

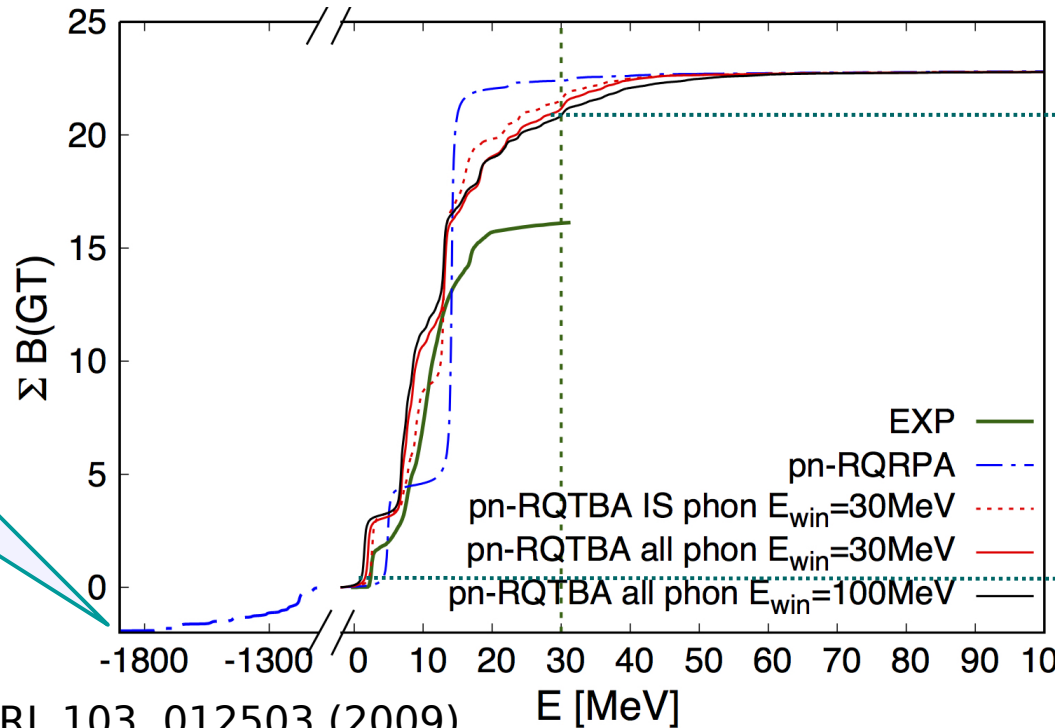
- ✓ 2(q)p-2(q)h configurations
- ✓ in an energy window from 30 MeV up to \sim 100 MeV in light or doubly magic nuclei

Gamow-Teller transitions and the “quenching” problem



+ transitions from the Fermi sea to the Dirac sea (~8%)

[N. Paar et al., PRC 69, 054303]

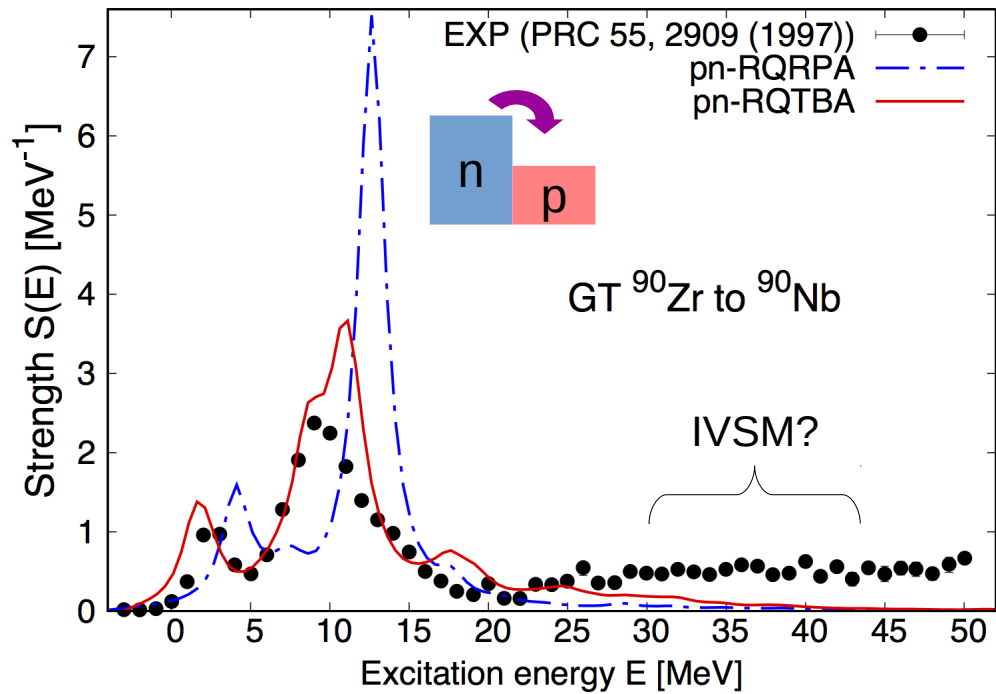


Up to 30 MeV: ~91% (vs 98% in RQRPA) of the total GT_strength

→ RQRPA strength naturally “quenched” due to complex configurations

But not enough... (exp: 71%)

Gamow-Teller transitions and the “quenching” problem



GT strength only:

0-50 MeV:

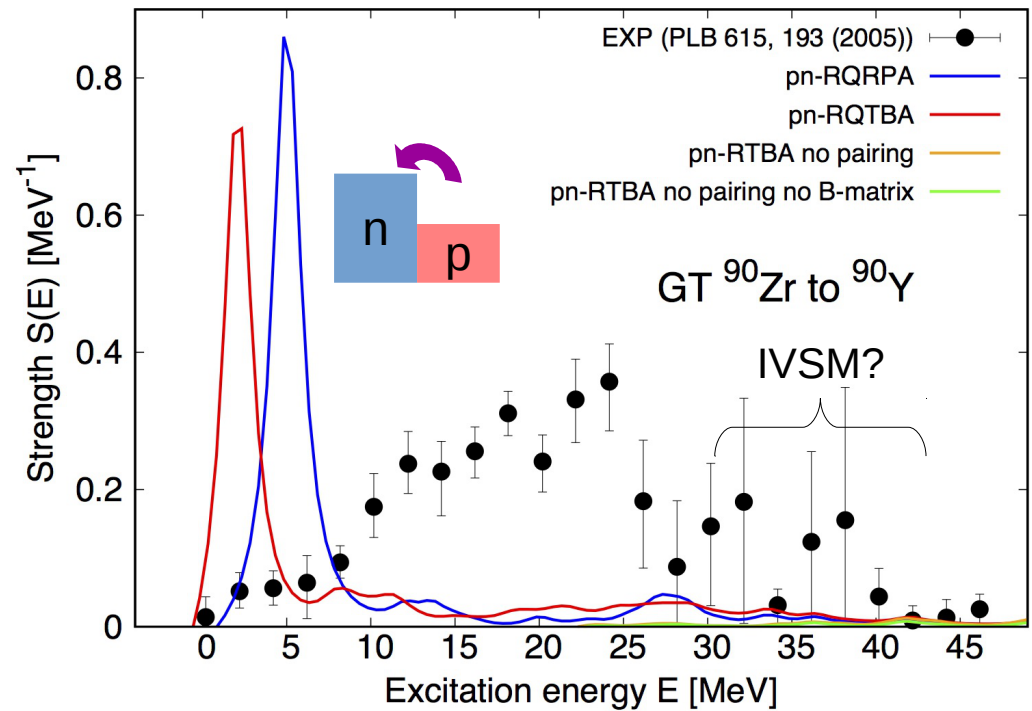
$$S_{-}^{EXP} \sim 29.3$$

$$S_{-}^{RQTBA} \sim 30.35$$

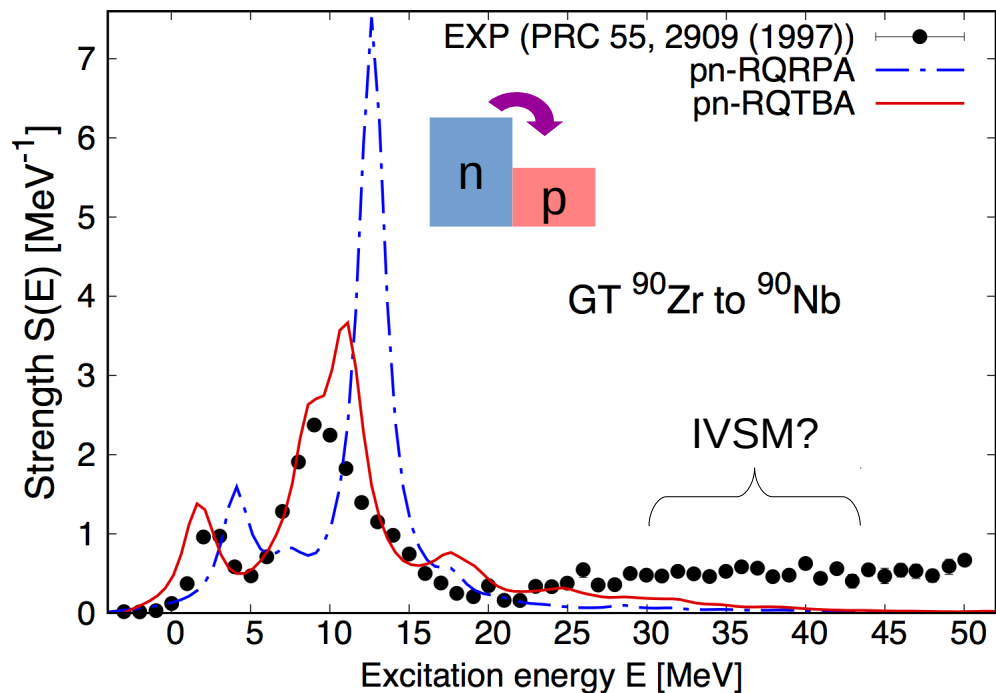
0-32 MeV:

$$S_{+}^{EXP} \sim 2.9$$

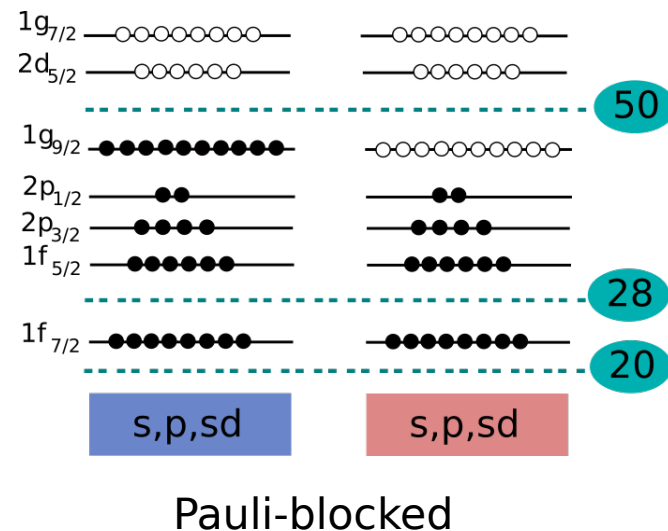
$$S_{+}^{RQTBA} \sim 2.54$$



Gamow-Teller transitions and the “quenching” problem



Schematic mean-field - no pairing:



GT strength only:

0-50 MeV:

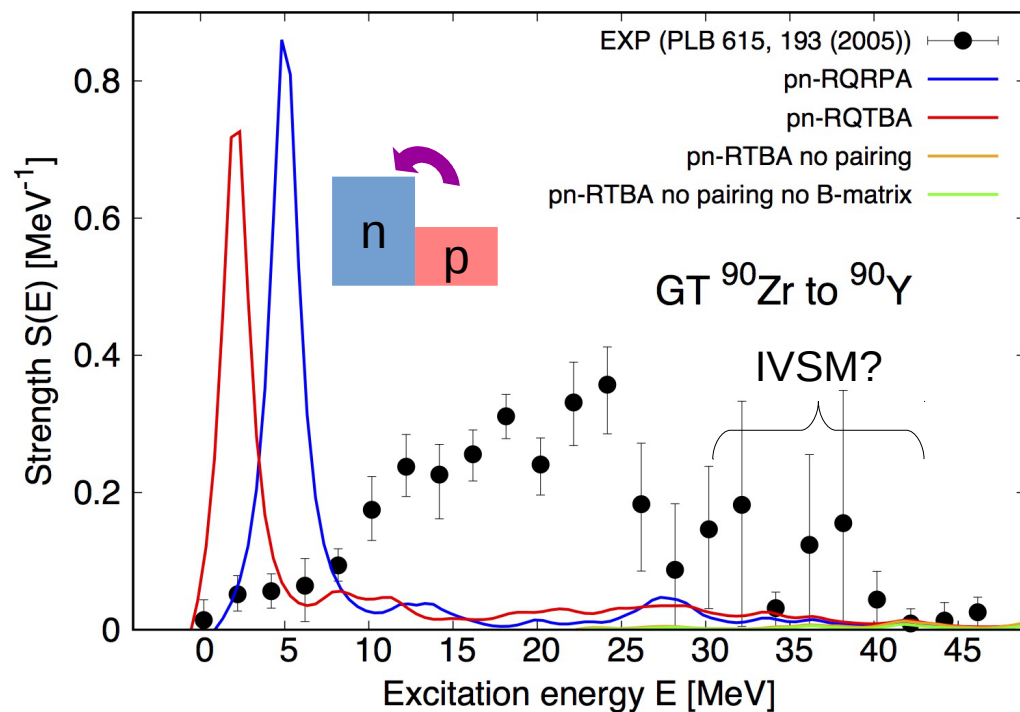
$$S_{-}^{EXP} \sim 29.3$$

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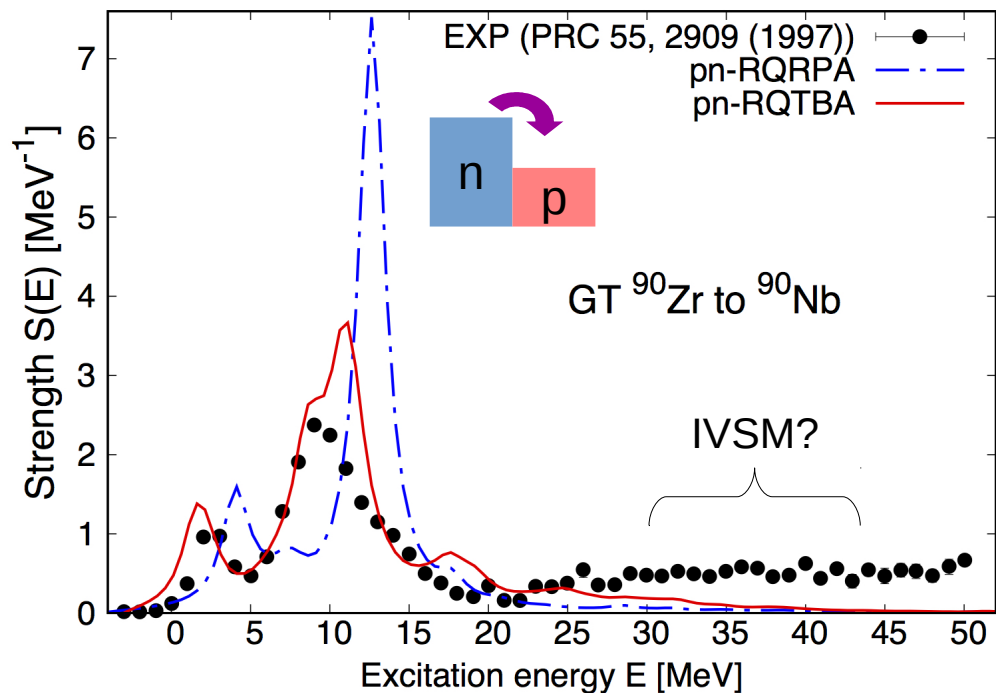
0-32 MeV:

$$S_{+}^{EXP} \sim 2.9$$

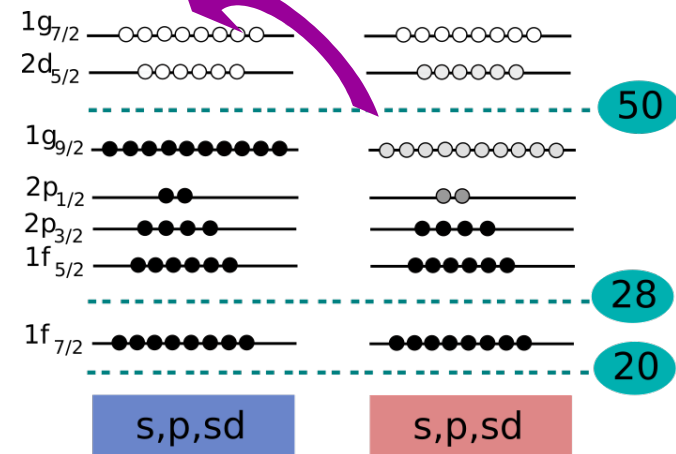
$$S_{+}^{RQTBA} \sim 2.54$$



Gamow-Teller transitions and the “quenching” problem



Schematic mean-field with pairing:



GT strength in β^+ channel caused by ground-state correlations (pairing here). But need further fragmentation \rightarrow GSC induced by QVC ?

GT strength only:

0-50 MeV:

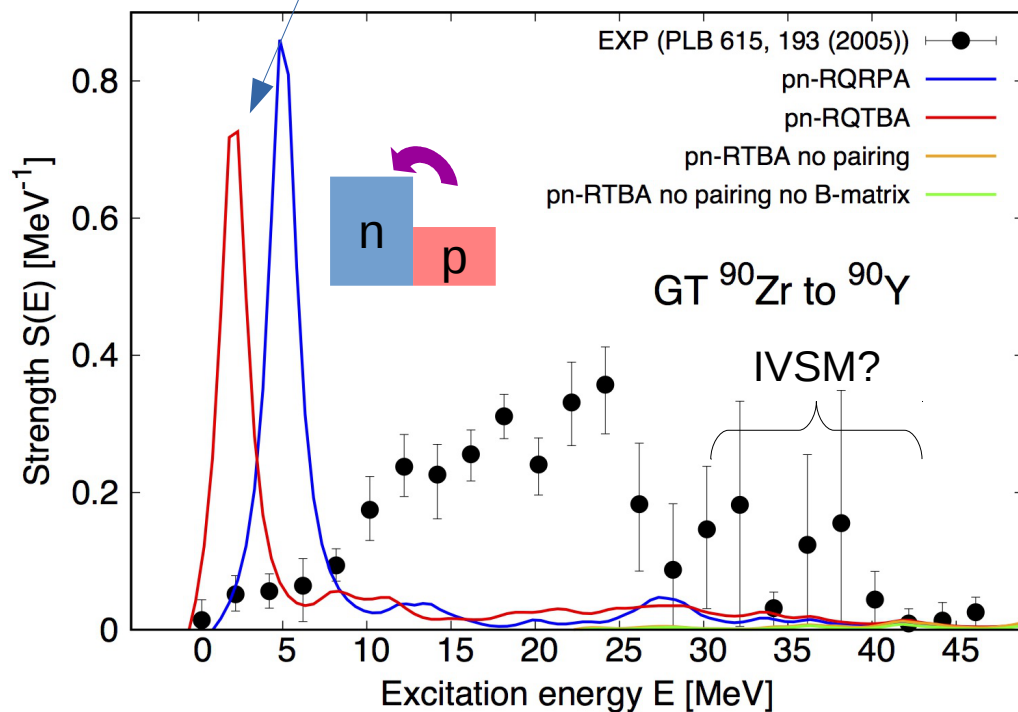
$$S_{-}^{EXP} \sim 29.3$$

$$S_{-}^{RQTBA} \sim 30.35$$

0-32 MeV:

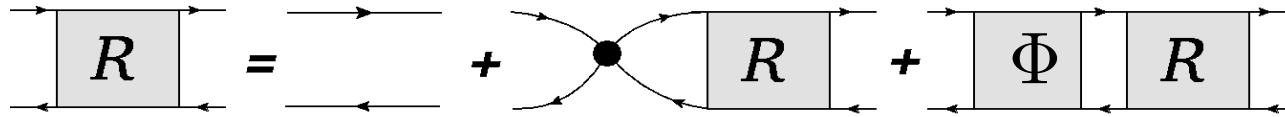
$$S_{+}^{EXP} \sim 2.9$$

$$S_{+}^{RQTBA} \sim 2.54$$

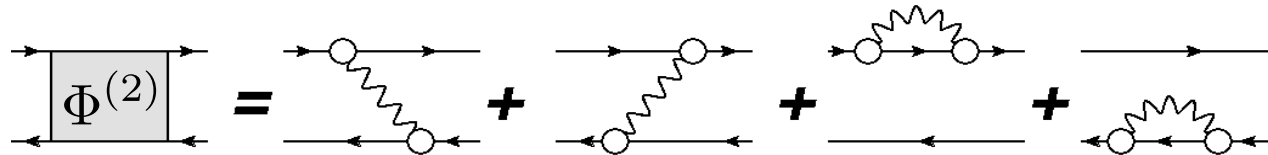


...Ongoing developments in the RNFT

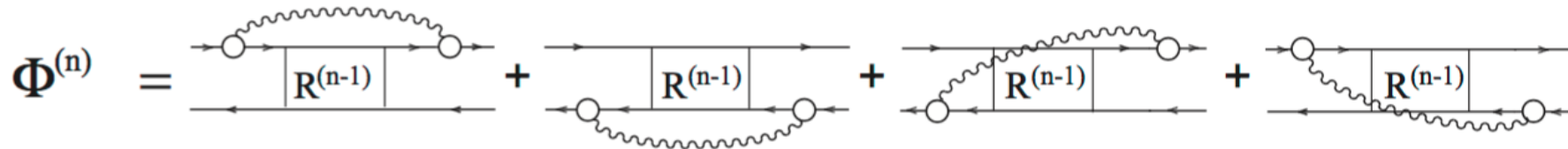
- ★ Inclusion of higher-order Np-Nh configurations in the response



RNFT + TBA:



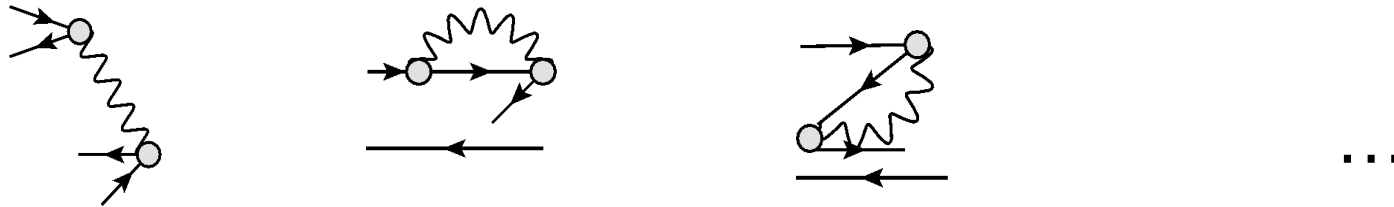
Extension:



E. Litvinova, Phys. Rev. C 91, 034332 (2015)

→ important for an accurate description of fine details of the transition strength

- ★ Ground-state correlations induced by QVC = backward going diagrams



→ important for e.g. (n,p) strength in neutron-rich nuclei / (p,n) strength in proton-rich nuclei

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Conclusion, perspectives

→ Conclusions:

- ★ The RNFT is a powerful framework for the microscopic description of mid-mass to heavy nuclei, which allows the account for complex configurations of nucleons in a large model space.
- ★ It has been quite successful in the description of neutral excitations.
- ★ It appears promising in the spin-isospin channel (description of both the low-energy strength and overall distribution to higher excitation energy).
- ★ However, in its present formulation (time-blocking approximation) it is often not sufficient.

→ Perspectives:

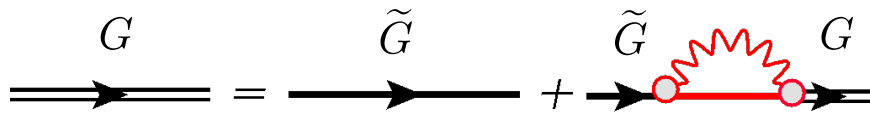
- ★ Inclusion of higher-order configurations and ground-state correlations
- ★ Application to double-charge exchange and double-beta decay ($2\nu\beta\beta$ and $0\nu\beta\beta$)
- ★ Together with RNFT in the neutral channel, this framework provides a high-quality and consistent description of both phases of the r-process nucleosynthesis, (n,γ) and β -decay \Rightarrow implementation in astrophysical modeling
- ★ Long-term goals: inclusion of the Fock term, start from bare interaction...
- ★ Other ongoing developments at WMU: coupling to continuum and extension to finite temperature (Ph.D. of H. Wibowo), description of neutral pairing vibrations (Ph.D of I. Egorova)

Thank you!

**This work is supported by US-NSF Grants
PHY-1404343 and PHY-1204486**

Next step beyond mean-field: Quasiparticles coupled to vibrations

→ quasi-particle propagator:

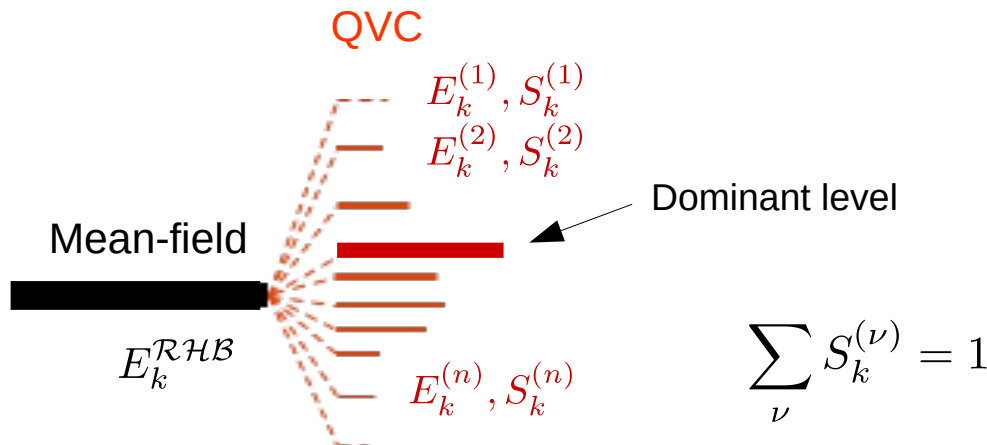


$$G(E) = \left(\varepsilon - \mathcal{H}_{RHB} - \underbrace{\Sigma^{(e)}(E)} \right)^{-1}$$

Introduces new poles

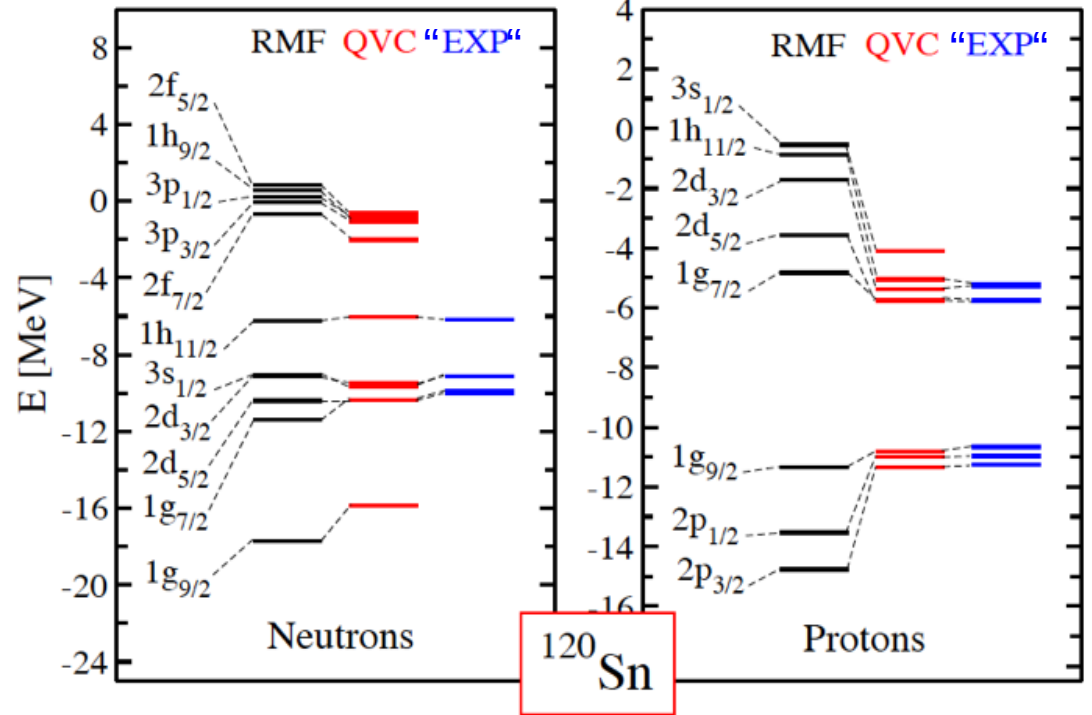
$$E_k^{(\nu)} = E_k^{\mathcal{RHB}} + \Sigma_k^{(e)}(E_k^{(\nu)})$$

→ fragmentation of single (quasi)particle states:



Dominant level:

(coupling to T=0 phonons w/ $J^\pi = 2^+, 3^-, 4^+, 5^-, 6^+$)



E. Litvinova, PRC 85, 021303(R) (2012)

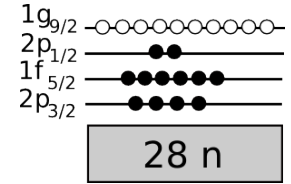
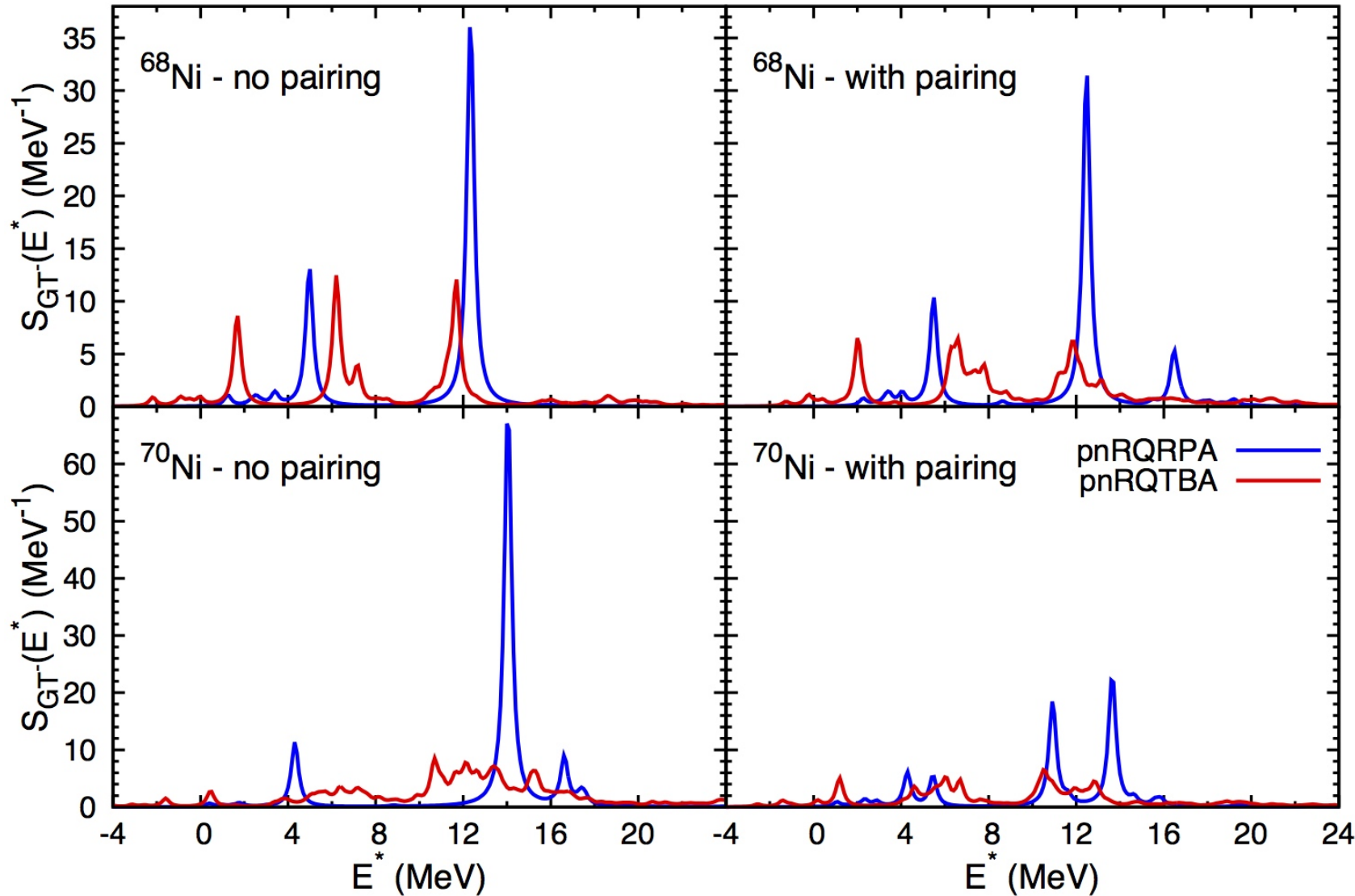
Spectroscopic factors in ^{120}Sn :

(nlj) ν	S^{th}	" S^{exp} "
2d _{5/2}	0.32	0.43
1g _{7/2}	0.40	0.60
2d _{3/2}	0.53	0.45
3s _{1/2}	0.43	0.32
1h _{11/2}	0.58	0.49
2f _{7/2}	0.31	0.35
3p _{3/2}	0.58	0.54

! model dependence...

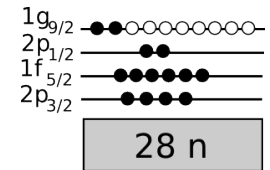
Gamow-Teller resonance in Nickel

Effect of pairing correlations on the strength distribution:



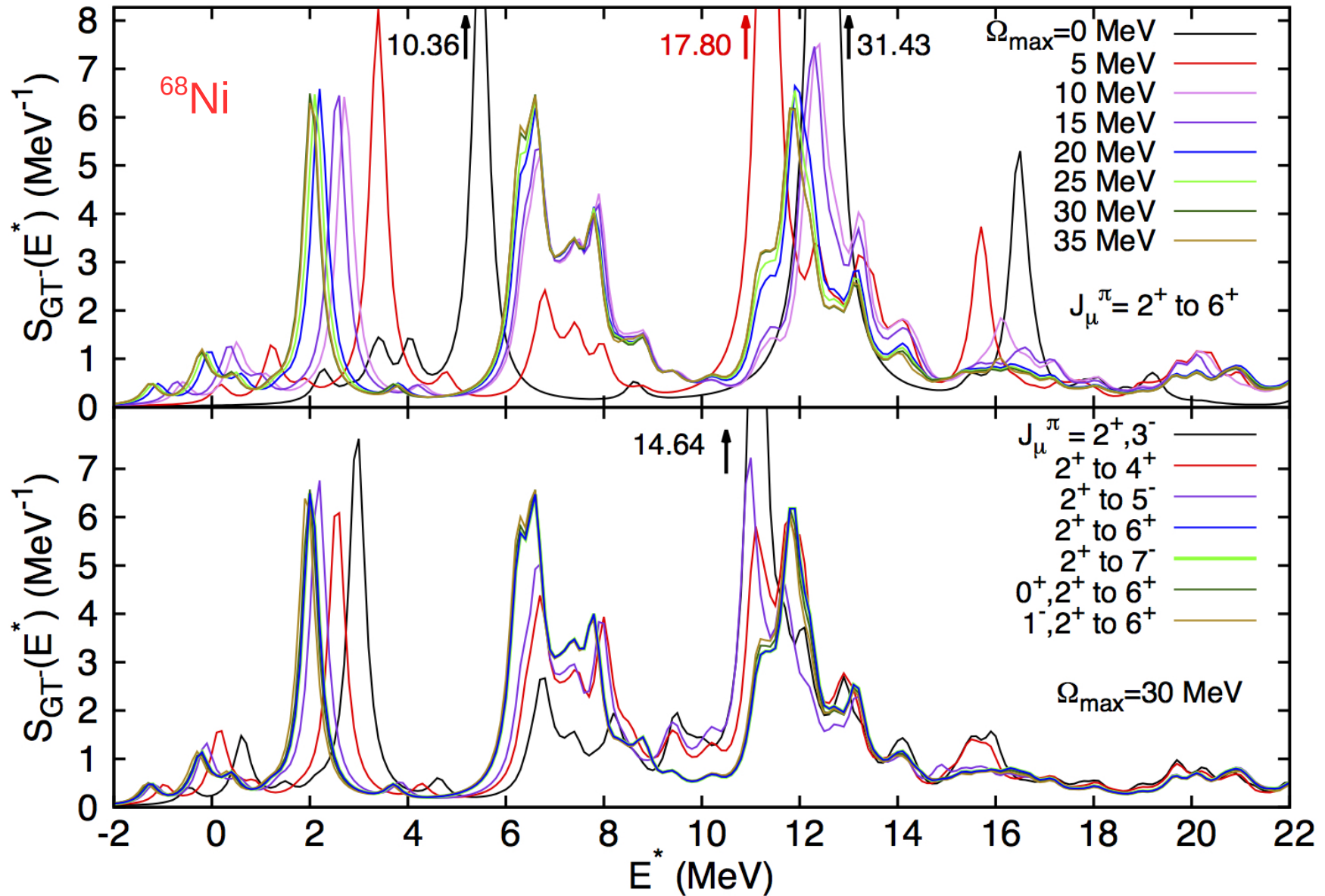
Pairing can bring fragmentation at the QRPA level (Landau damping)

QPVC brings spreading effects



Gamow-Teller transitions in Nickel isotopes (Ni → Cu)

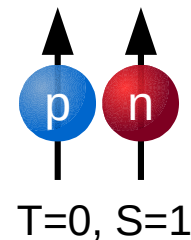
Convergence of the strength according to the phonon spectrum (neutral phonons only):



Low-energy GT strength and beta-decay half-lives

★ Problem with QRPA description: the beta-decay half-lives are systematically overestimated.

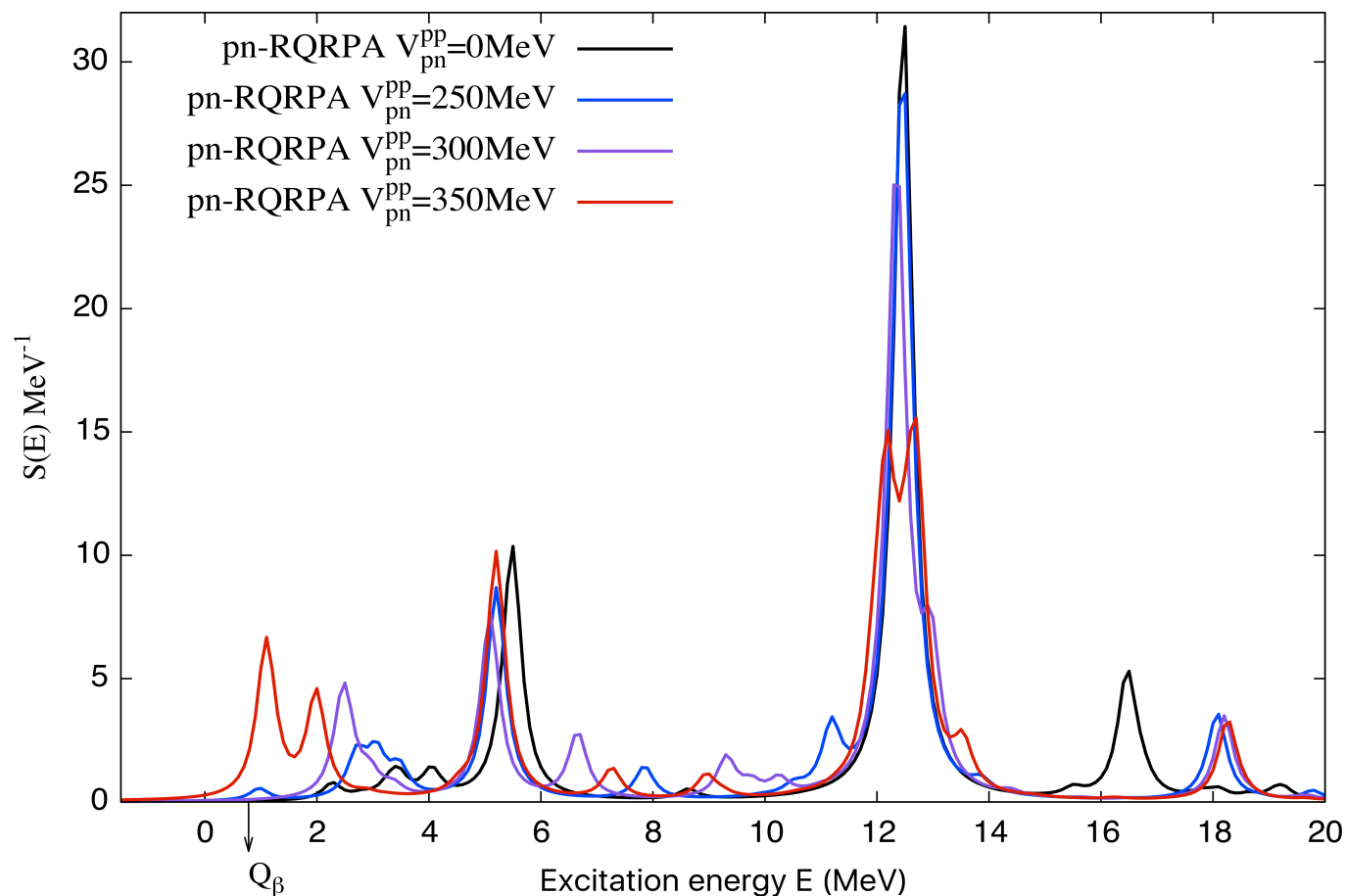
→ issue overcome by considering T=0 pn-pairing



But this type of pairing is not well understood
(no deuteron condensate → T=0 pairing is dynamic (?)...)
And not well constrained ...

→ often treated phenomenologically with an additional static pn residual interaction in the particle-particle channel.

→ Example in ^{68}Ni :



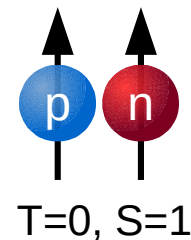
⇒ Lack of
predictive power

Low-energy GT strength and beta-decay half-lives

★ Problem with QRPA description: the beta-decay half-lives are systematically overestimated.

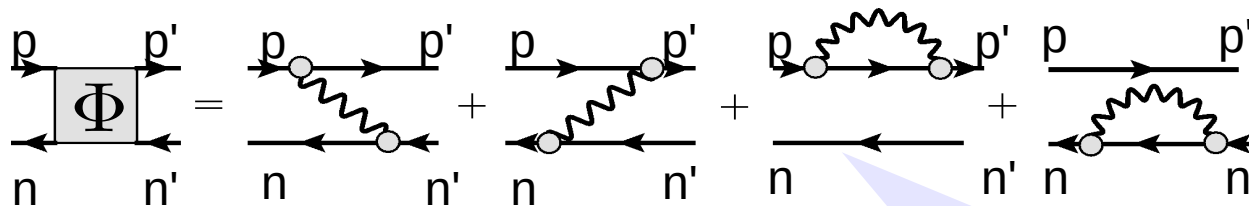
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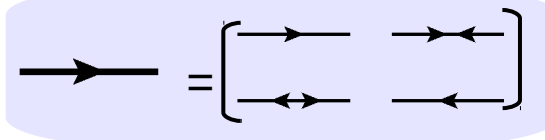


→ often treated phenomenologically with an additional static pn residual interaction in the particle-particle channel.

⇒ Goal: evaluate the effect of QVC on the half-lives and provide a possible microscopic mechanism for pn-pairing:

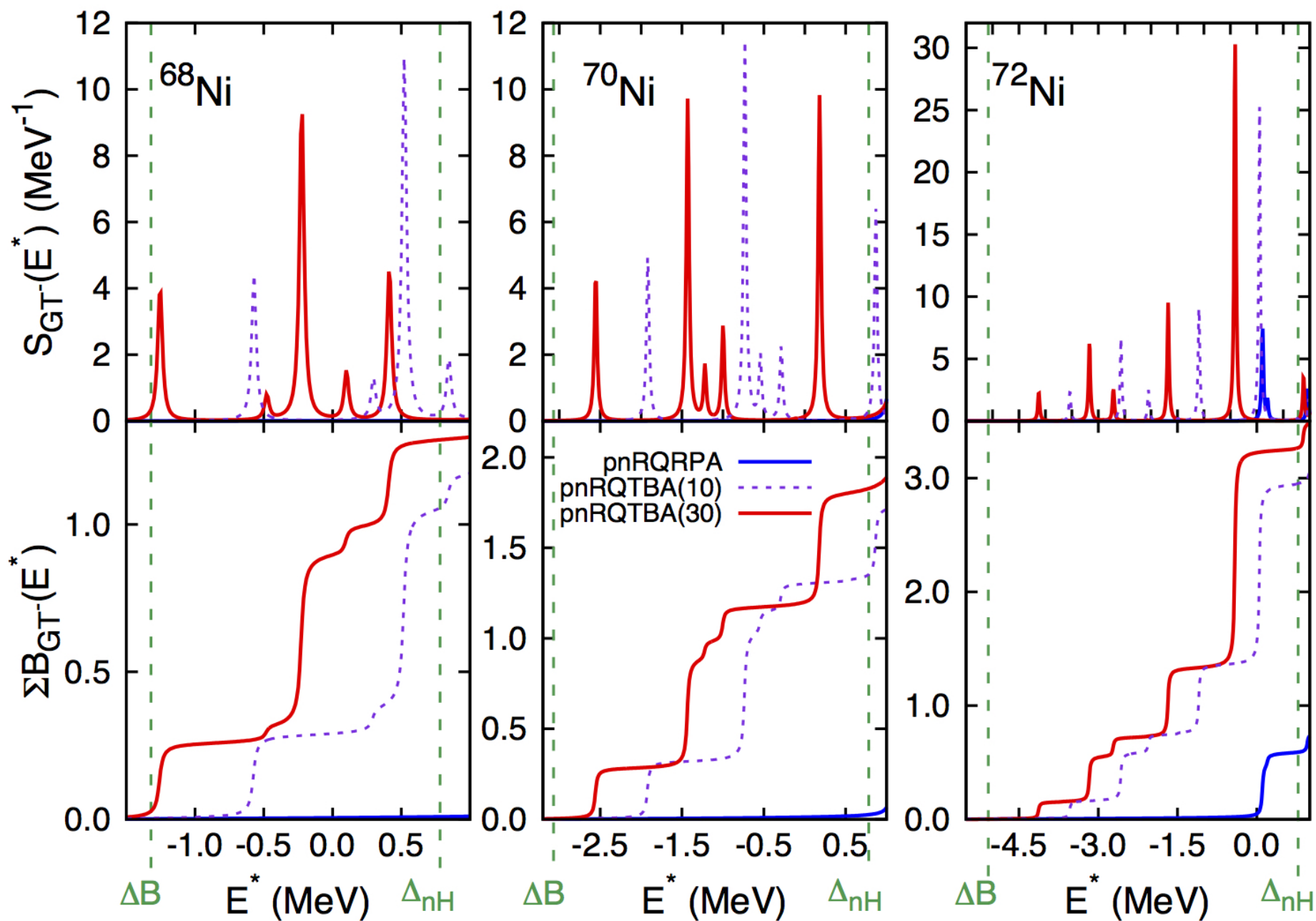


Quasiparticle = superposition of particles and holes:

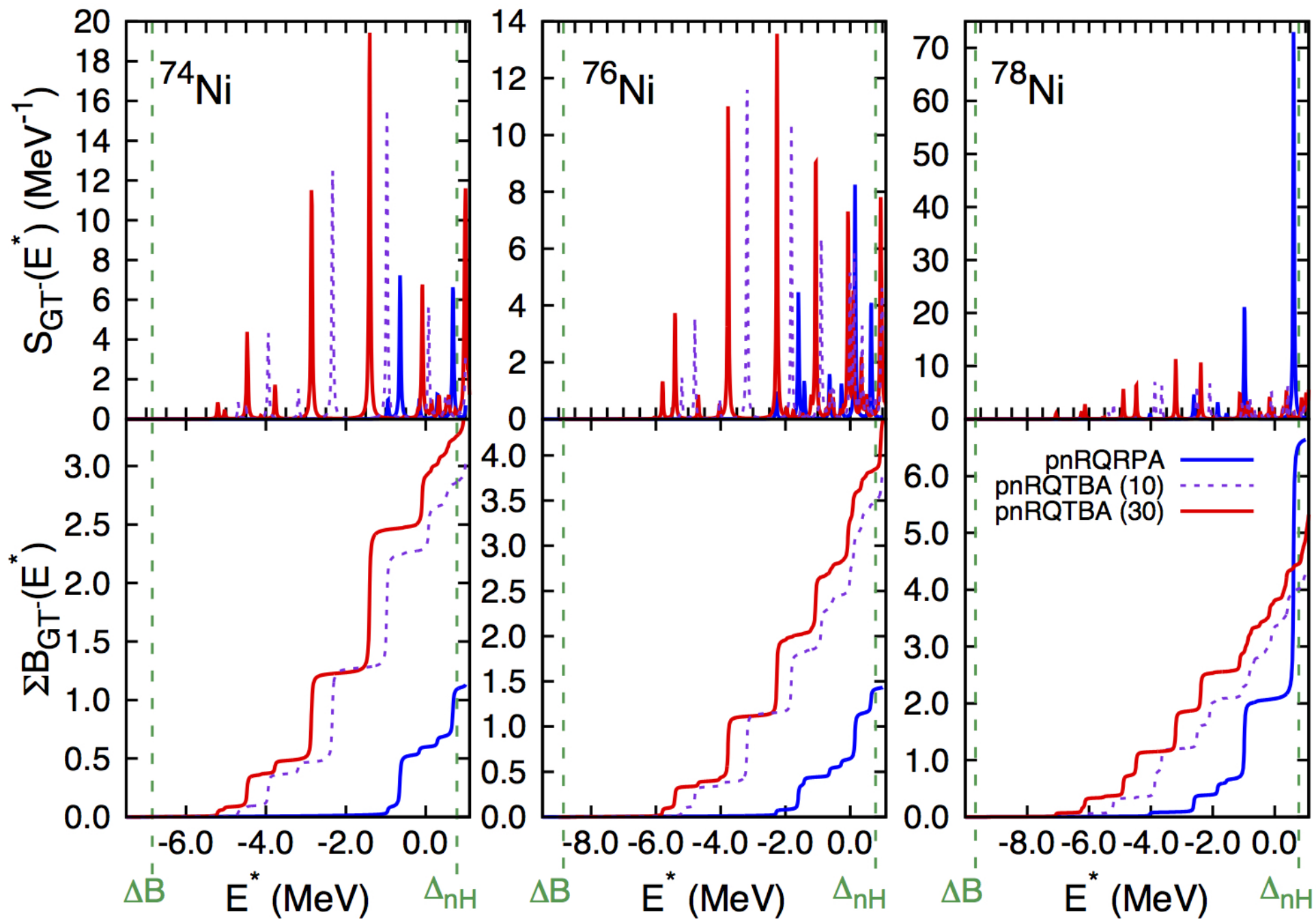


- QVC generates a pn effective interaction in the particle-hole and particle-particle channels.
- QVC can provide an underlying mechanism for dynamical proton-neutron pairing

Gamow-Teller resonance in Nickel

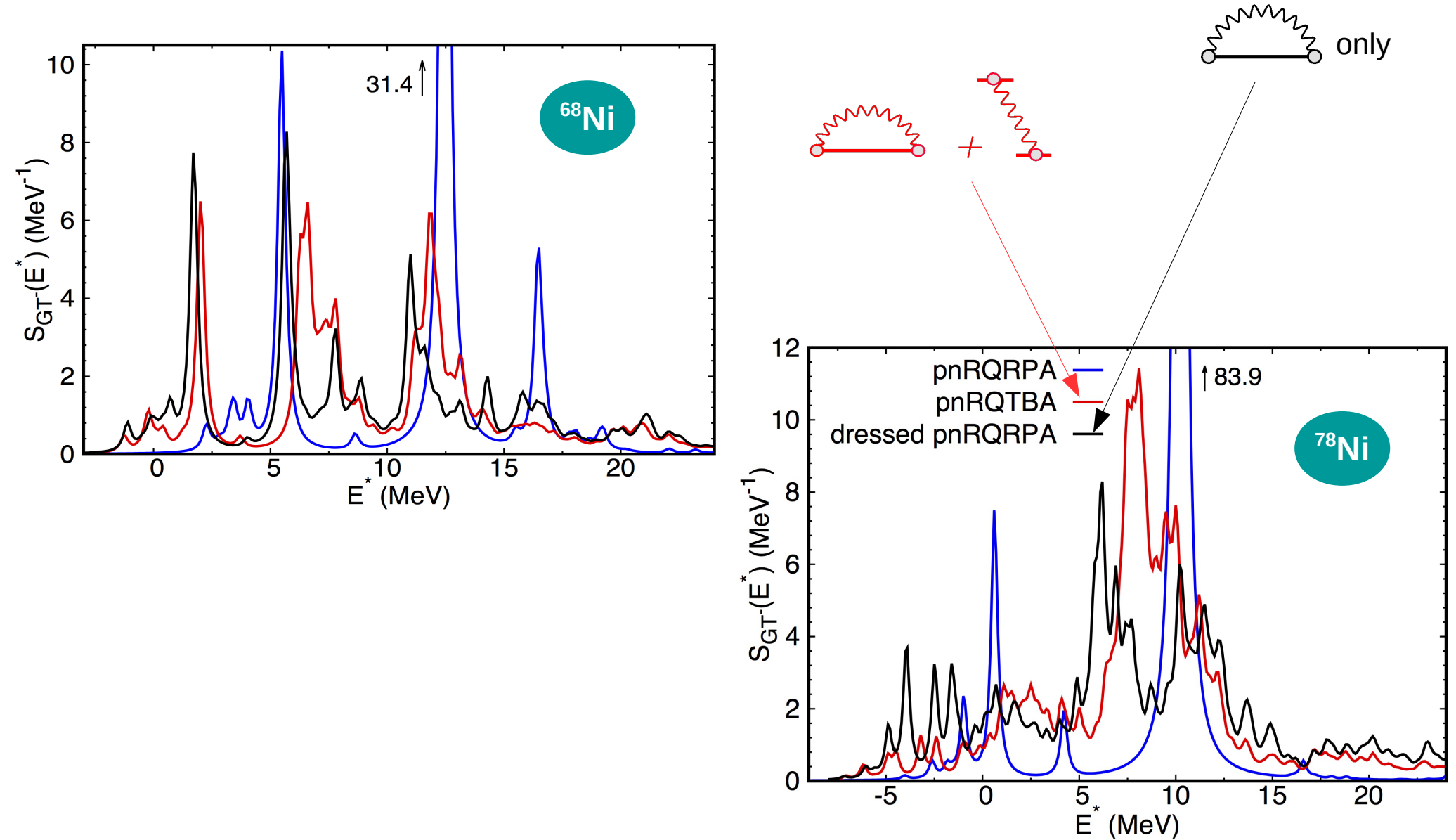


Gamow-Teller resonance in Nickel

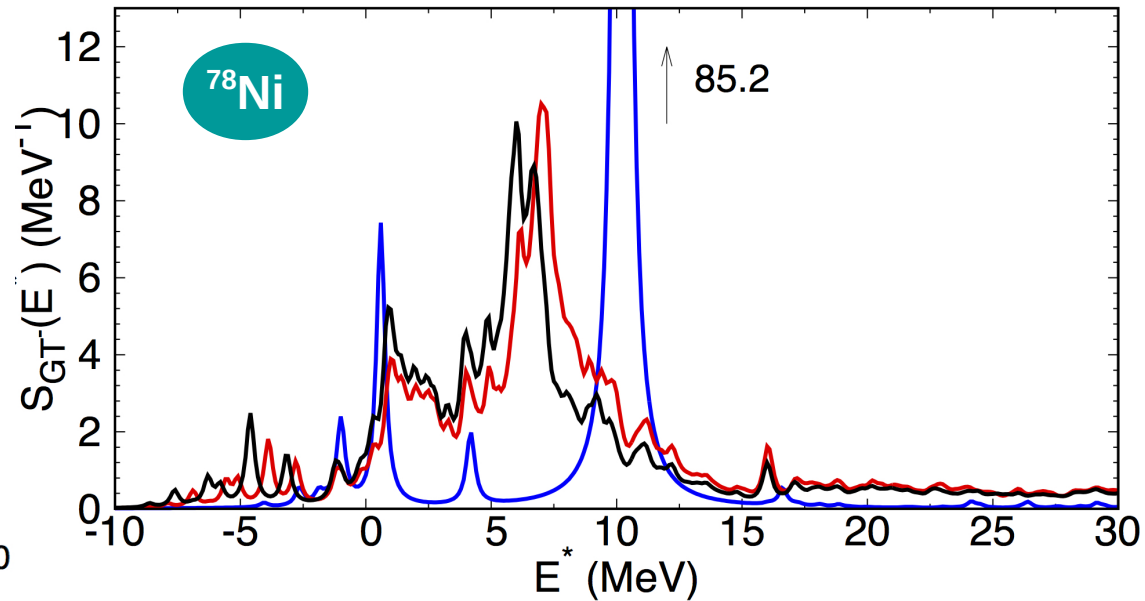
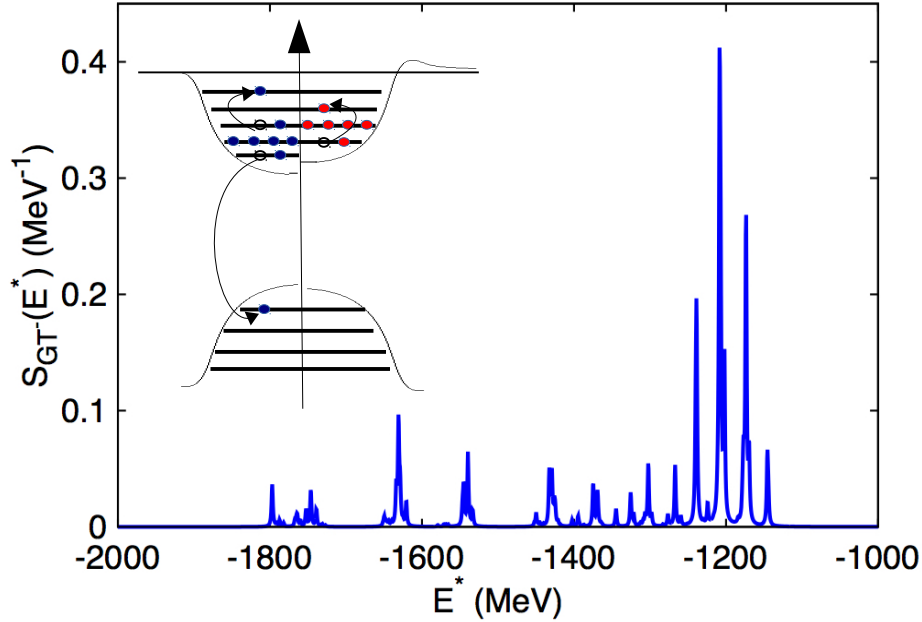


Gamow-Teller transitions in Nickel isotopes (Ni \rightarrow Cu)

★ Effect of phonon-exchange interaction vs self-energy insertions:

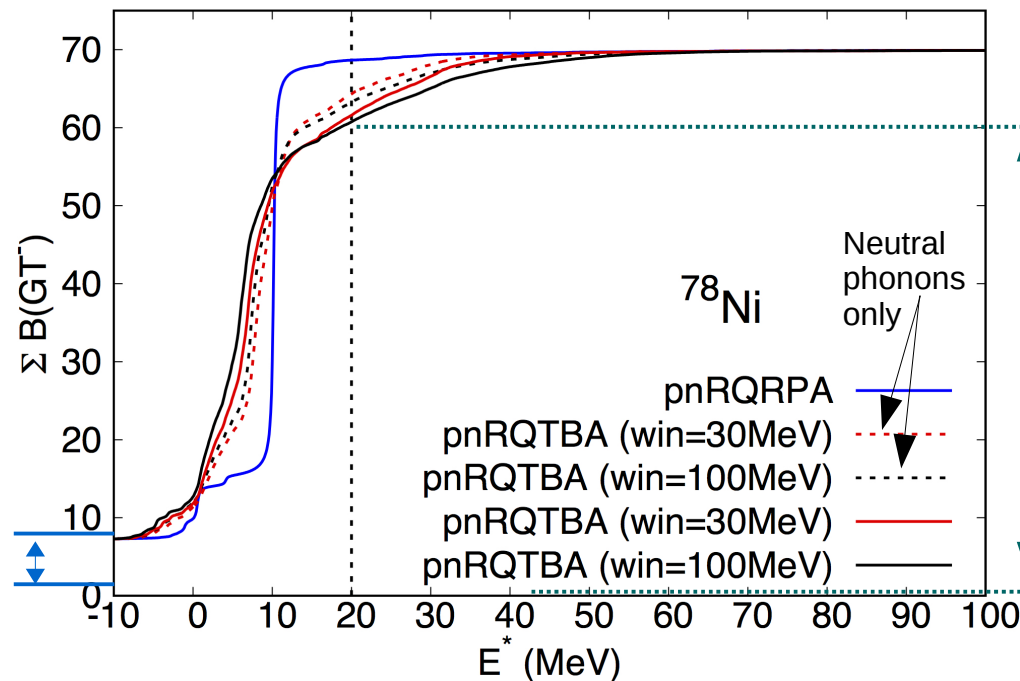


Gamow-Teller transitions and the “quenching” problem



+ transitions from the Fermi sea to the Dirac sea (~10%)

[N. Paar et al., PRC 69, 054303]

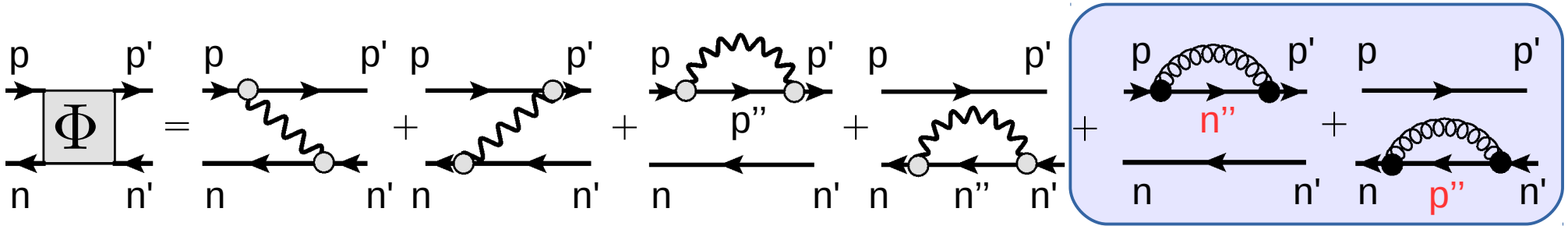


Up to the GR region: ~81% (vs 97% in RQRPA) of the total GT_- strength

→ RQRPA strength naturally “quenched” due to complex configurations

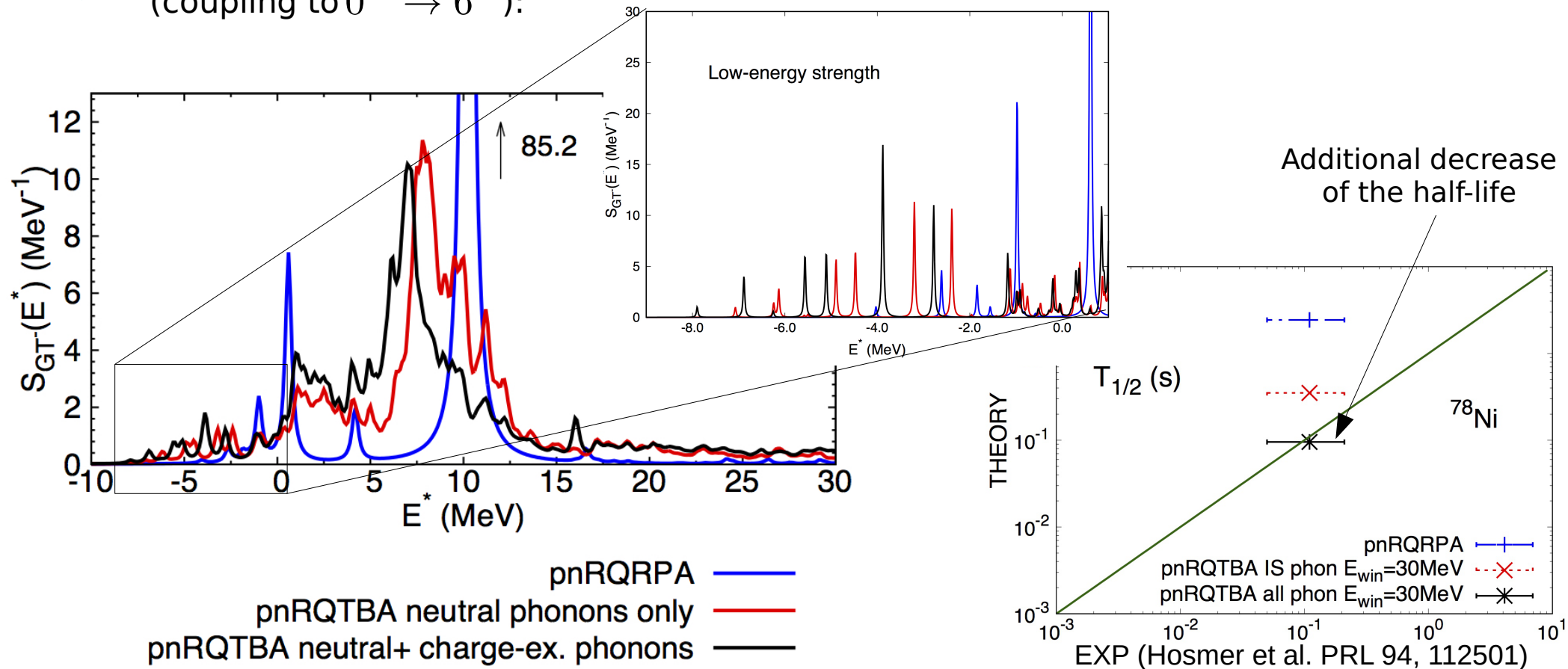
New-developments: coupling to charge-exchange phonons

Existence of low-energy isospin-flip modes which can couple to single-nucleon degrees of freedom \rightarrow additional terms in the effective interaction:

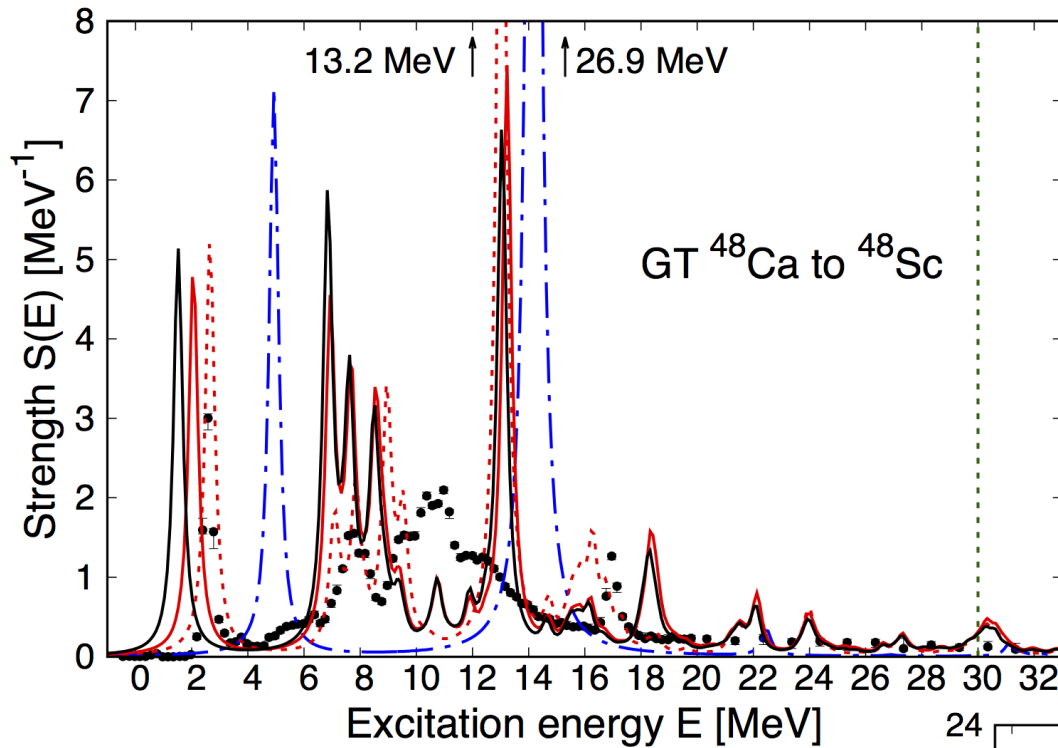


(No extra phonon-exchange term because of charge conservation)

Effect on the nuclear response in ^{78}Ni :
(coupling to $0^\pm \rightarrow 6^\pm$):



Gamow-Teller transitions and the “quenching” problem



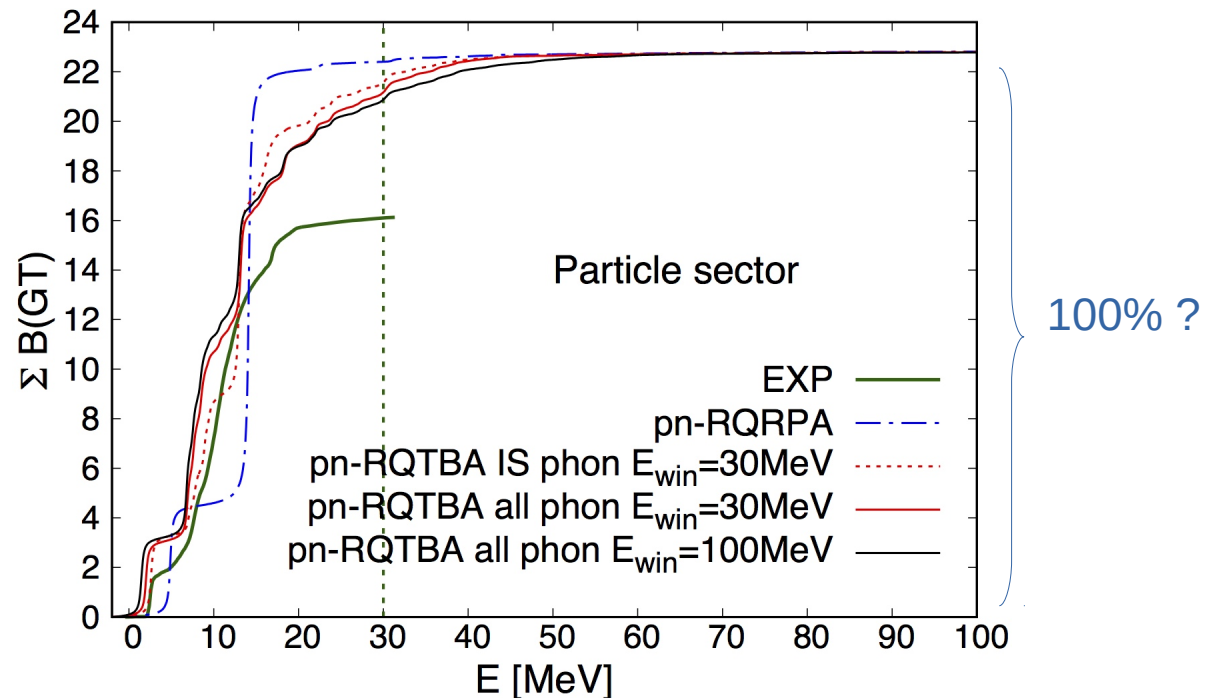
with QVC:

- more detailed description of the transition strength due to 2p-2h configurations
- “quenching” of the RPA strength in the experimental energy window due to fragmentation and redistribution

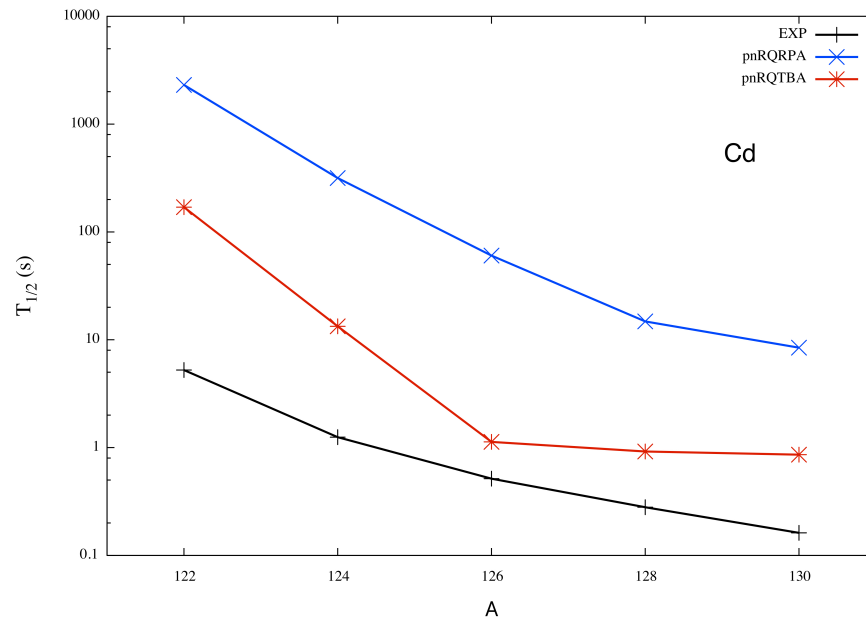
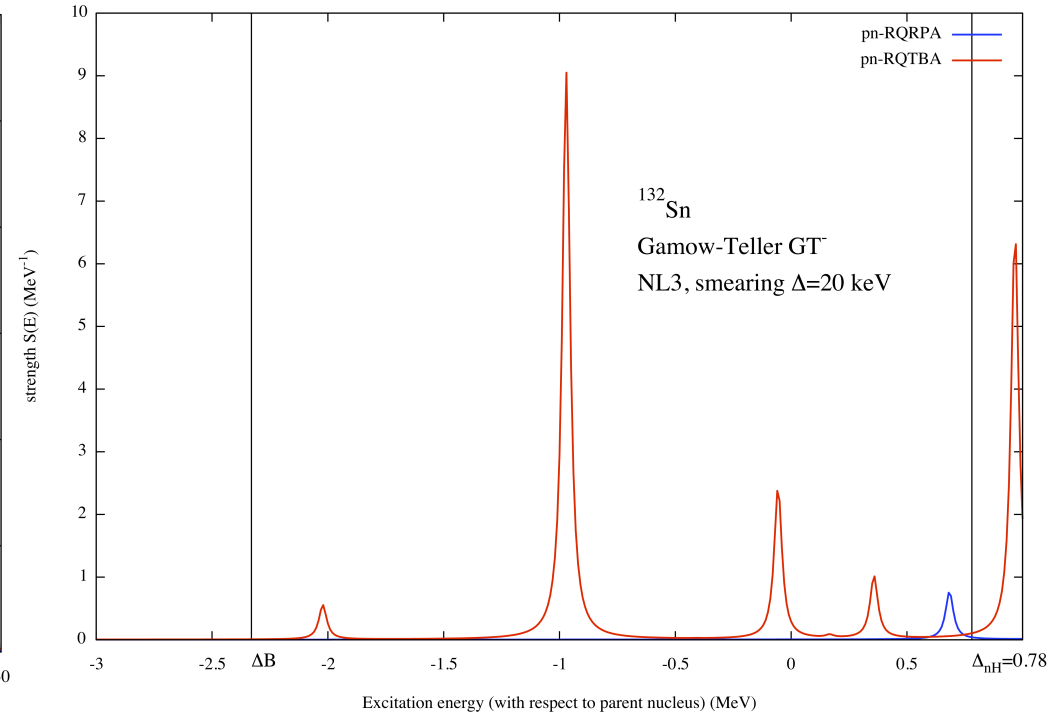
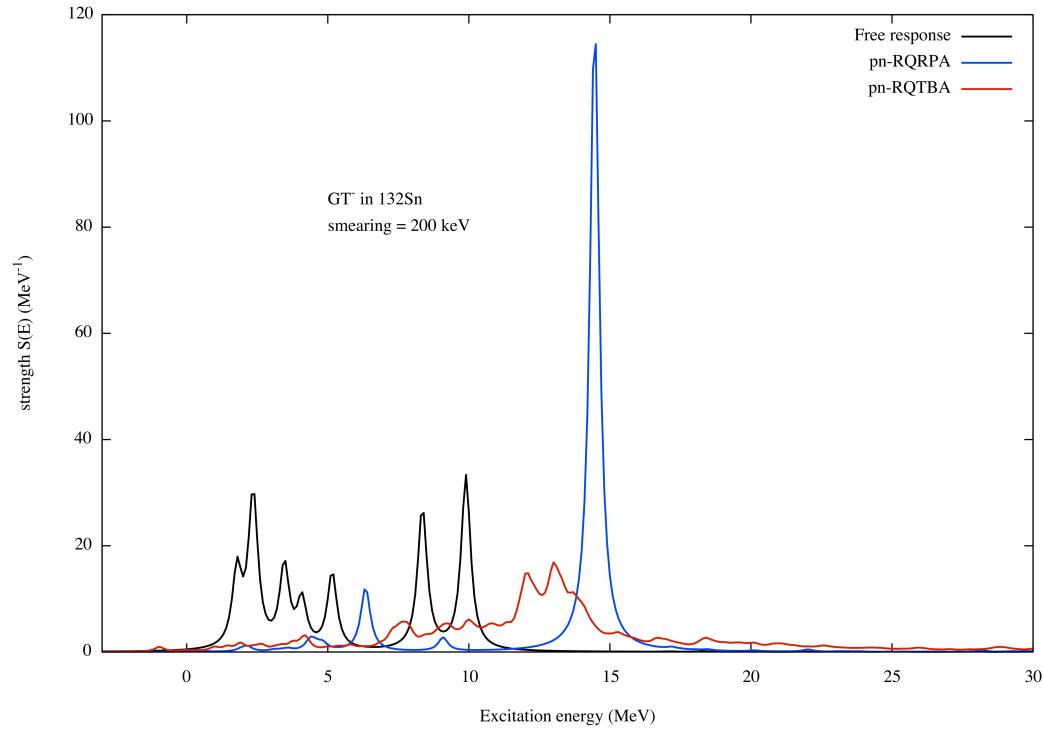
But not enough...

At 30 MeV:

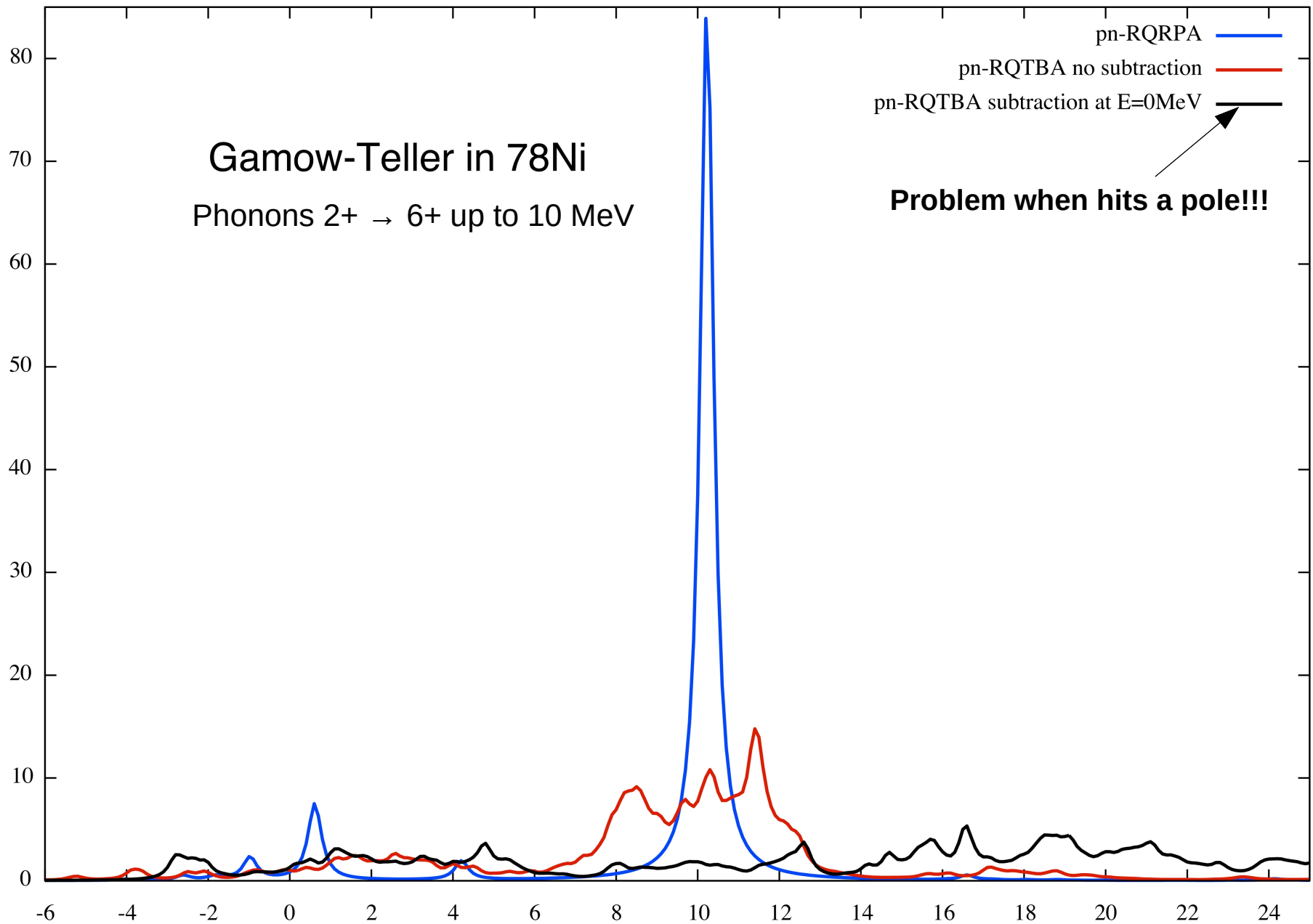
- RQRPA: quasi-saturated (98%)
- RQTBA: 91%
- Exp: $\sim 71\%$



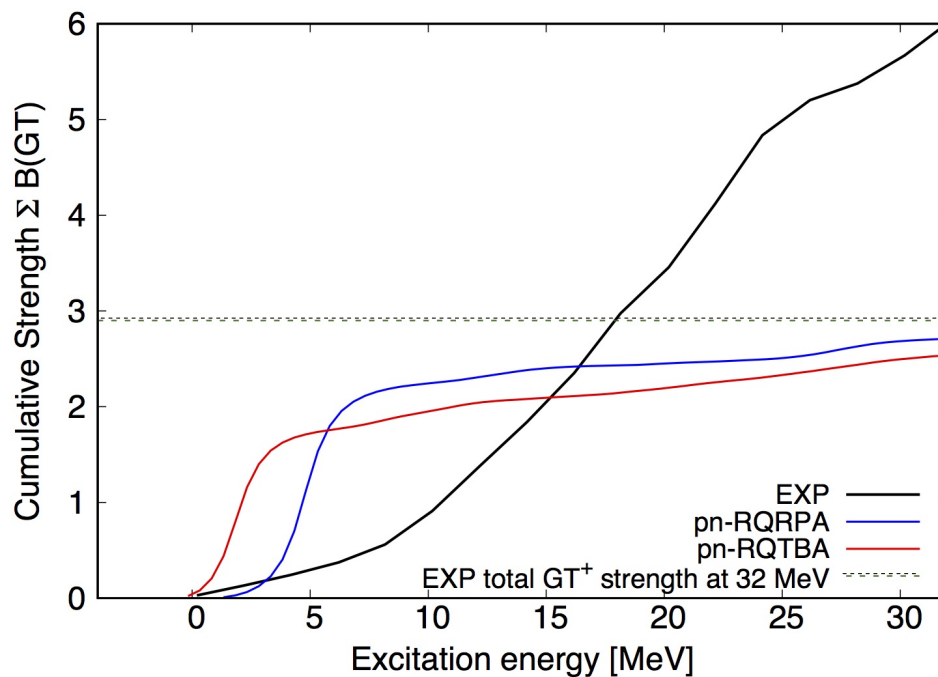
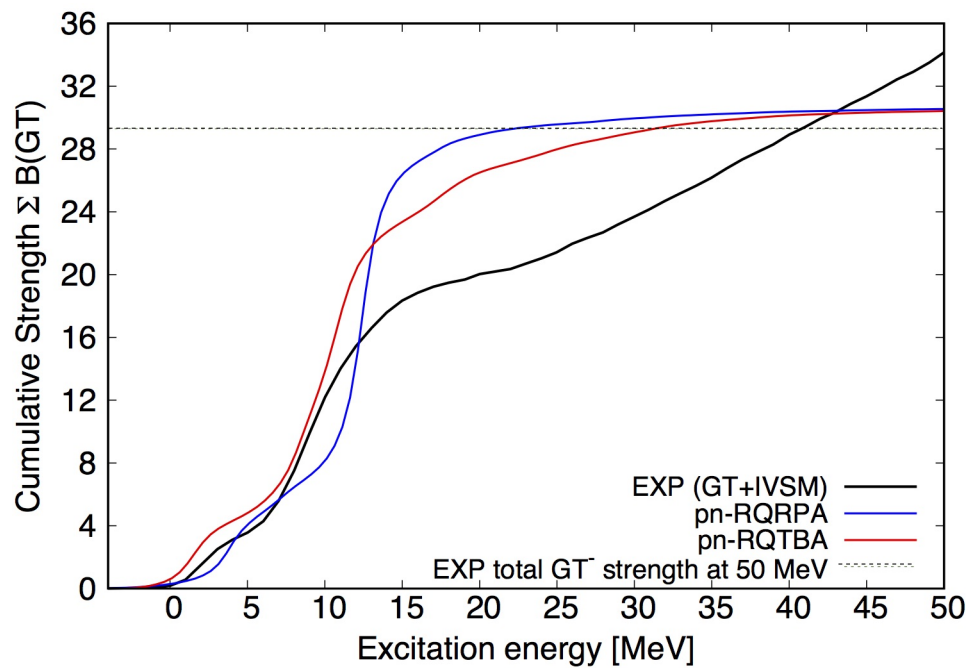
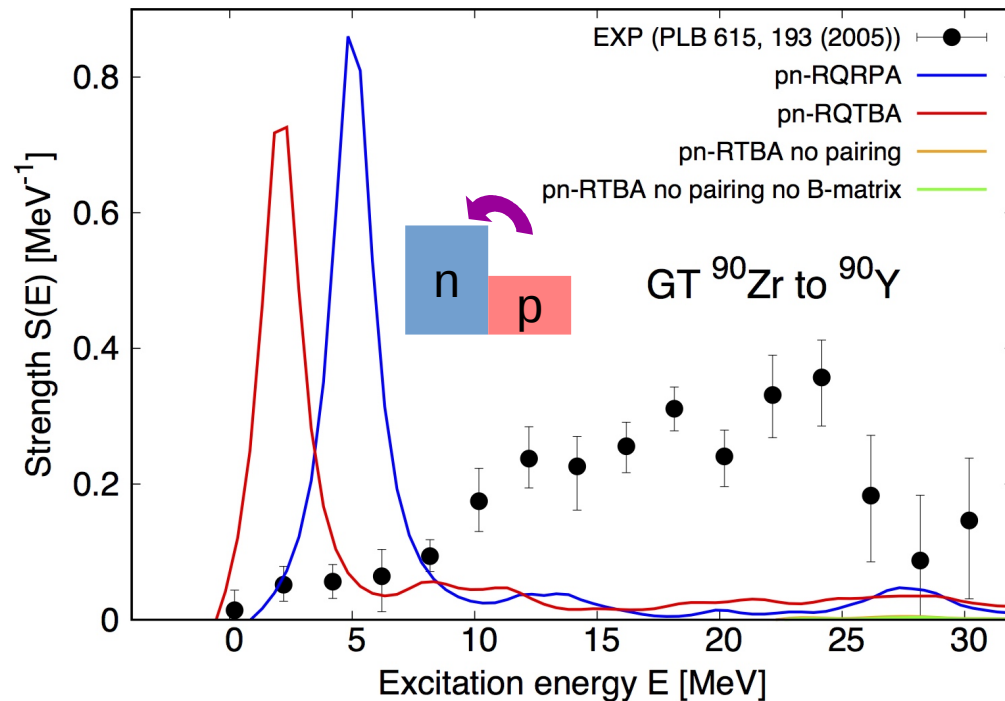
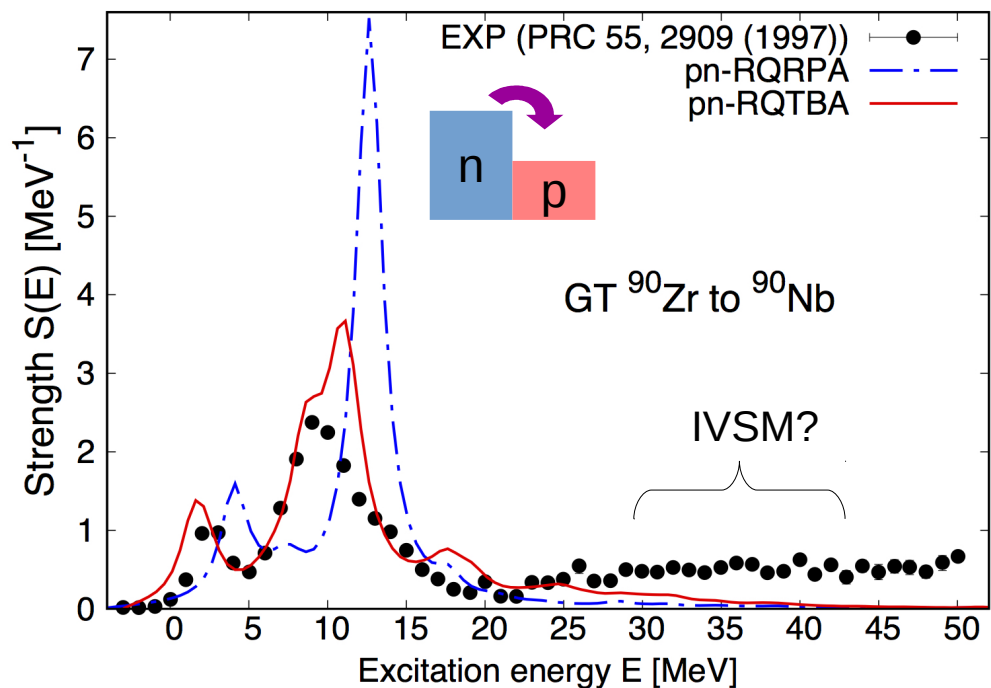
Other GT strengths and beta-decay half-lives



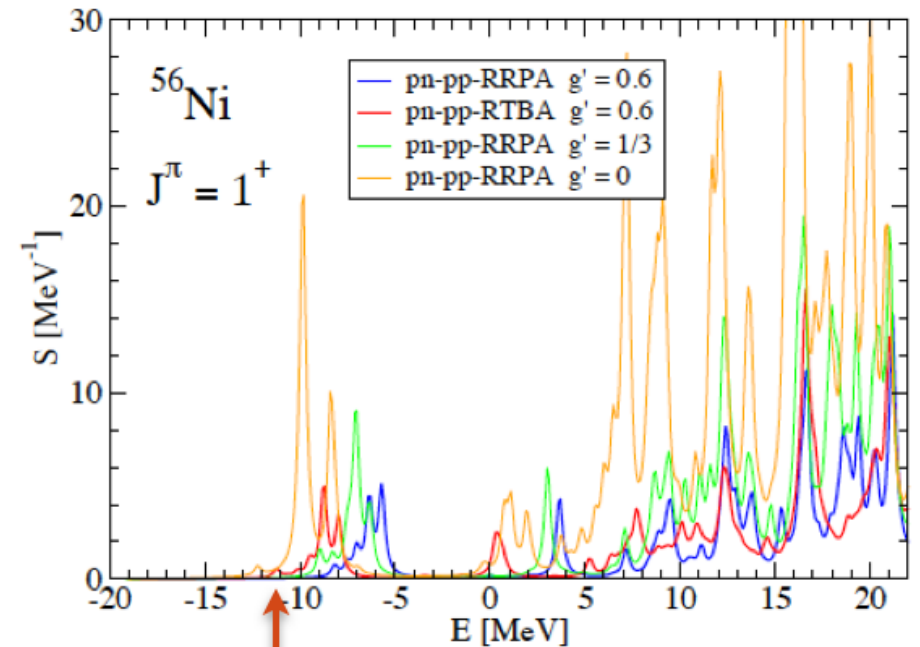
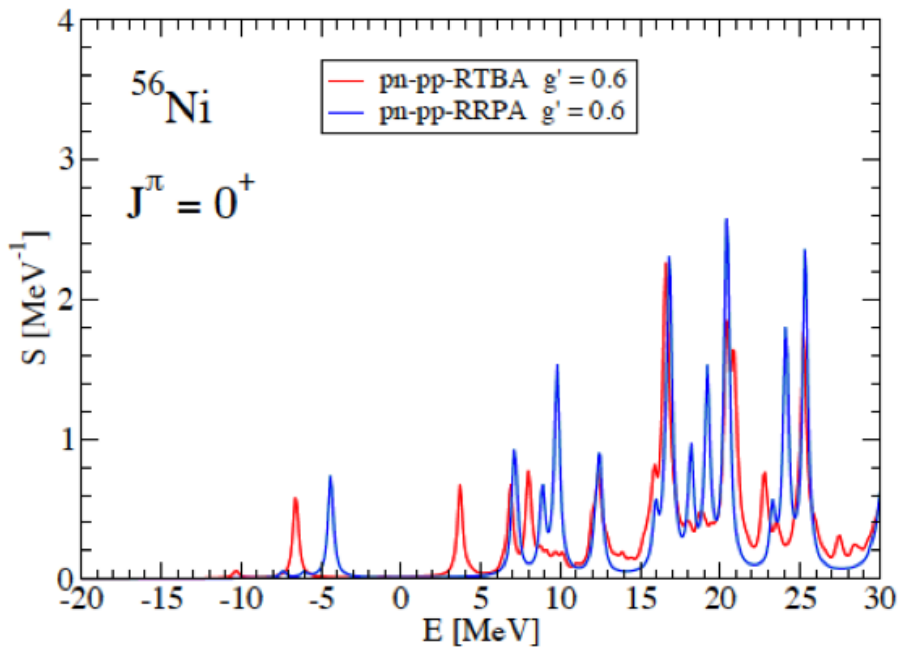
Gamow-Teller in ^{78}Ni



Gamow-Teller transitions and the “quenching” problem



Response in proton-neutron particle-particle (deuteron transfer) channel: quest for deuteron condensate and pn-pairing

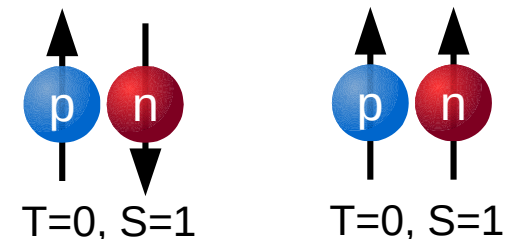


Ground state of ^{58}Cu (odd-odd)

E.L., C. Robin, I. Egorova, arXiv:1612:09182

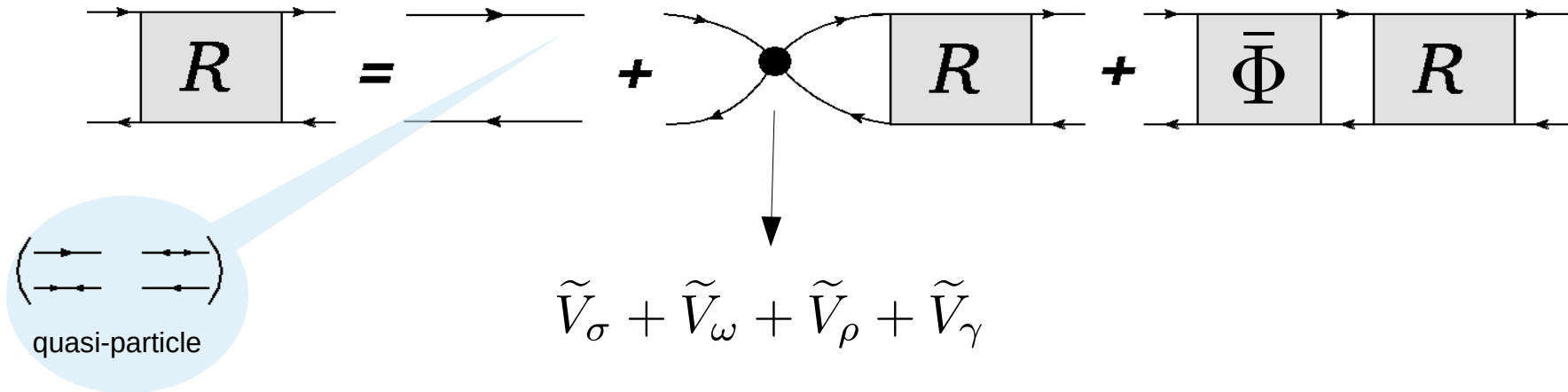
- Spectra of **odd-odd nuclei** including their ground states can be calculated in **pn-pp-RTBA**
- Presently in medium-mass $N=Z$ nuclei **no deuteron condensate** is found at realistic values of g' , but the low-lying excitation modes are collective and can mediate $T=1$ and $T=0$ **proton-neutron dynamical pairing**

Work in progress



A few results in the ph neutral ($\Delta T_z=0$) channel

★ Response in the neutral ph channel:



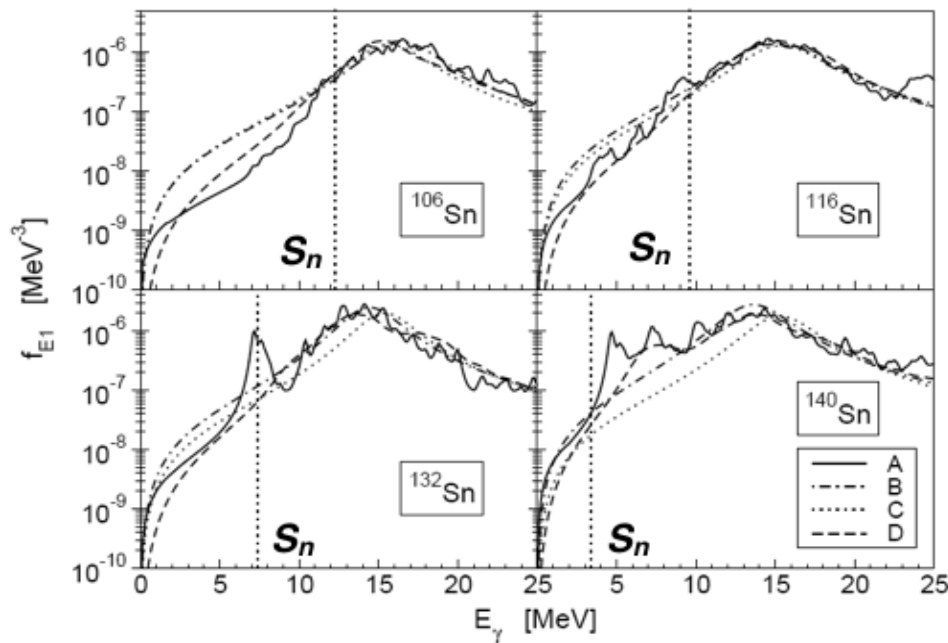
Diagrammatic equation for the vertex function Φ :

$$\Phi_{k_1 k_4, k_2 k_3}^\eta(\omega) = \sum_{\mu \xi} \delta_{\eta \xi} \left[\delta_{k_1 k_3} \sum_{k_6} \frac{\gamma_{\mu; k_6 k_2}^{\eta; -\xi} \gamma_{\mu; k_6 k_4}^{\eta; -\xi*}}{\eta\omega - E_{k_1} - E_{k_6} - \Omega_\mu} + \delta_{k_2 k_4} \sum_{k_5} \frac{\gamma_{\mu; k_1 k_5}^{\eta; \xi} \gamma_{\mu; k_3 k_5}^{\eta; \xi*}}{\eta\omega - E_{k_5} - E_{k_2} - \Omega_\mu} - \left(\frac{\gamma_{\mu; k_1 k_3}^{\eta; \xi} \gamma_{\mu; k_2 k_4}^{\eta; -\xi*}}{\eta\omega - E_{k_3} - E_{k_2} - \Omega_\mu} + \frac{\gamma_{\mu; k_3 k_1}^{\eta; \xi*} \gamma_{\mu; k_4 k_2}^{\eta; -\xi}}{\eta\omega - E_{k_1} - E_{k_4} - \Omega_\mu} \right) \right]$$

The role of the low-lying dipole strength (pygmy dipole resonance)

Microscopic strength and conventional GDR parametrizations

- A** ————— RQTBA
- B** - - - - - Lorentzian fit to RQTBA
- C** Lorentzian fit to Exp.: J.J. Cowan, F.-K. Thielemann, J.W. Truran, Phys. Rep. 208, 267 (1991)
- D** - - - - - Skyrme+QRPA, S. Gorieli, E. Khan, NPA 706, 217 (2002)

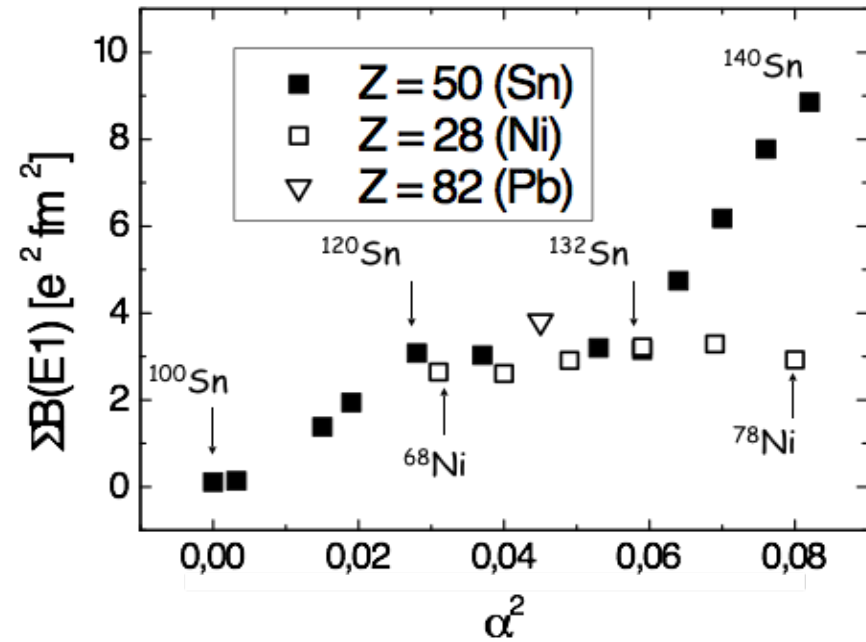


E. L., H.P. Loens, K. Langanke et al., Nucl. Phys. A 823, 26 (2009)

Total PDR strength vs asymmetry parameter α :

$$\alpha = (N-Z)/A$$

RQTBA systematics:
nearly linear dependence on α
with deviations around shell
closures with intruder orbits



E. L., P. Ring, V. Tselyaev, K. Langanke, Phys. Rev. C 79, 054312 (2009)