

# Nuclear Pasta in Supernova and Neutron Star Mergers

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U.S. DEPARTMENT OF  
**ENERGY**

Office of  
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**NUCLEI**  
Nuclear Computational Low-Energy Initiative



**INDIANA UNIVERSITY**



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# Summary



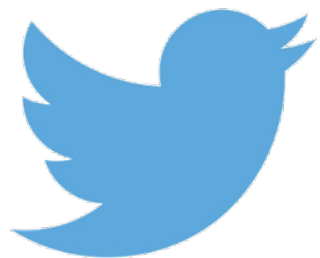
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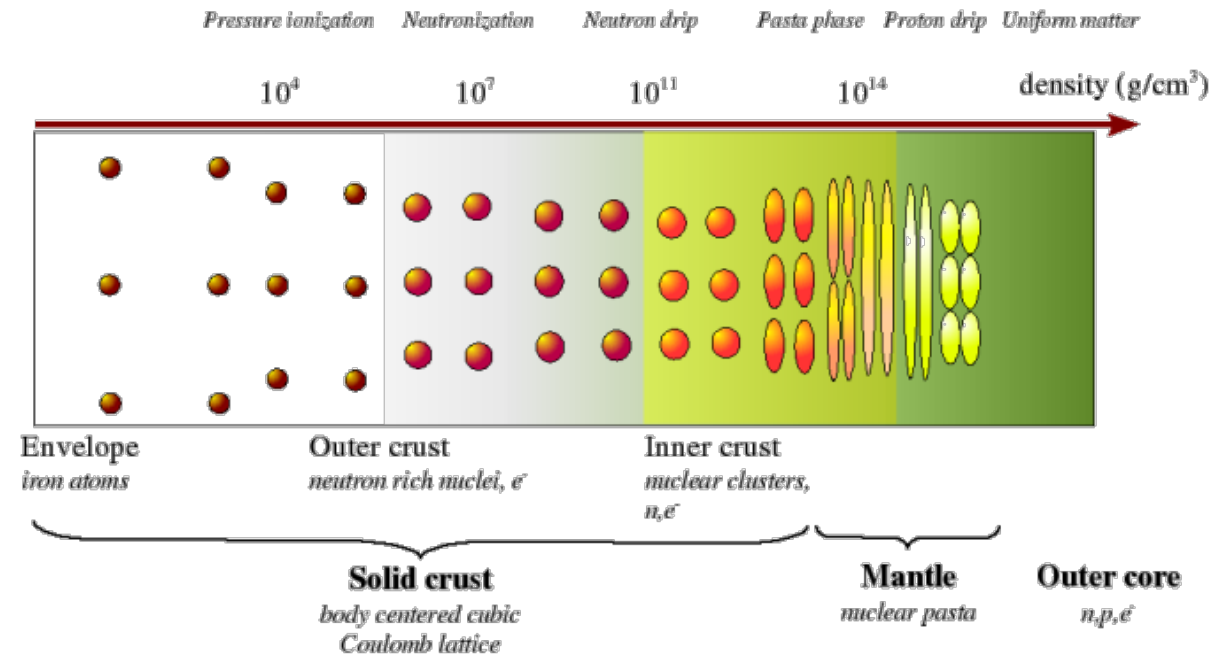
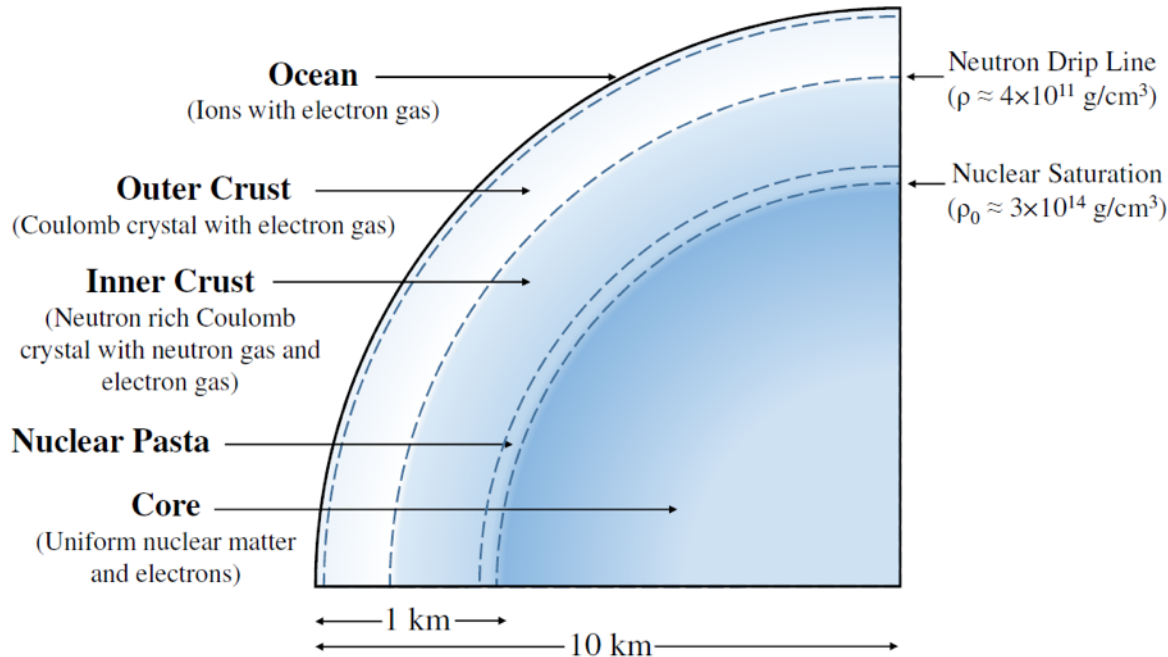
Nuclear Pasta



# Neutron Star Structure



- What's inside a neutron star?

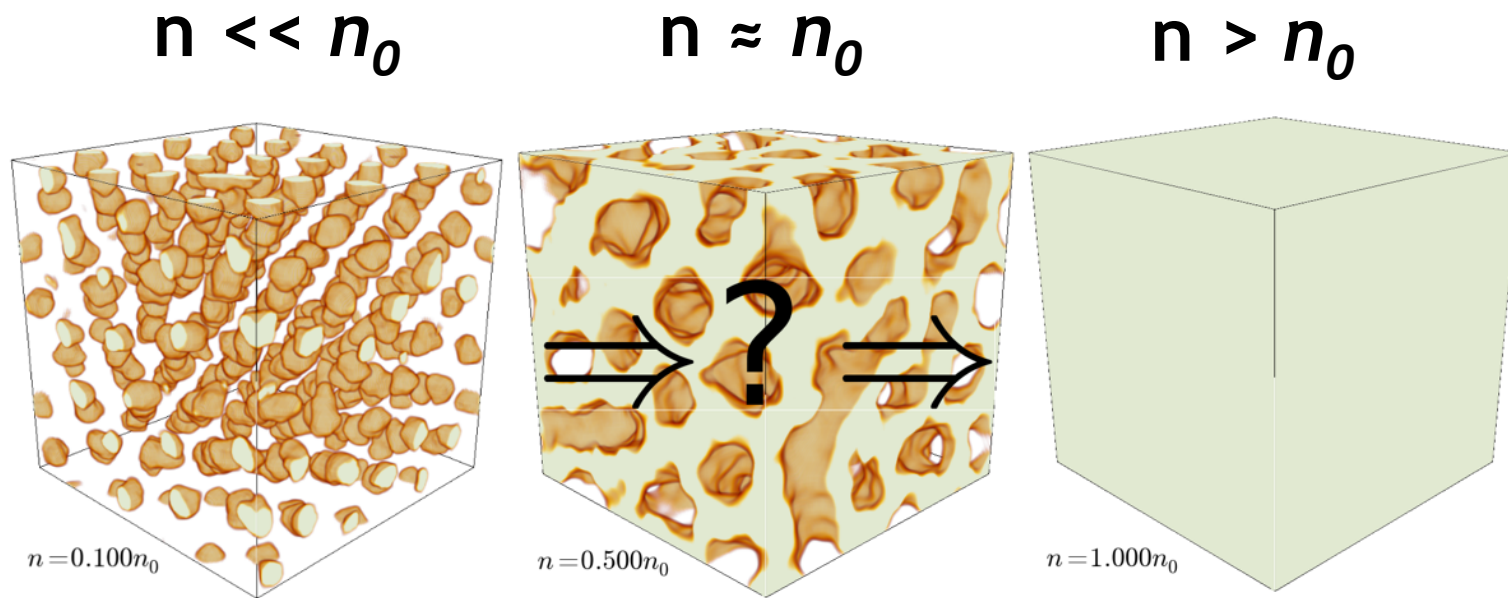


- Not just a “giant nucleus in space!”

# Nuclear Pasta



- Neutron star core is uniform nuclear matter ( $n_0 = 2.4 \times 10^{14} \text{ g cm}^{-3}$ )
- The crust is conventional, isolated nuclei
- What sort of nuclear phase transition must occur between these two phases of matter?



# Non-Spherical Nuclei



- First theoretical models of the shapes of nuclei near  $n_0$ 
  - 1983: Ravenhall, Pethick, & Wilson
  - 1984: Hashimoto, H. Seki, and M. Yamada
- *Frustration*: Competition between proton-proton Coulomb repulsion and strong nuclear attraction
- Nucleons adopt non-spherical geometries near the saturation density to minimize surface energy

Shape of Nuclei in the Crust of Neutron Star

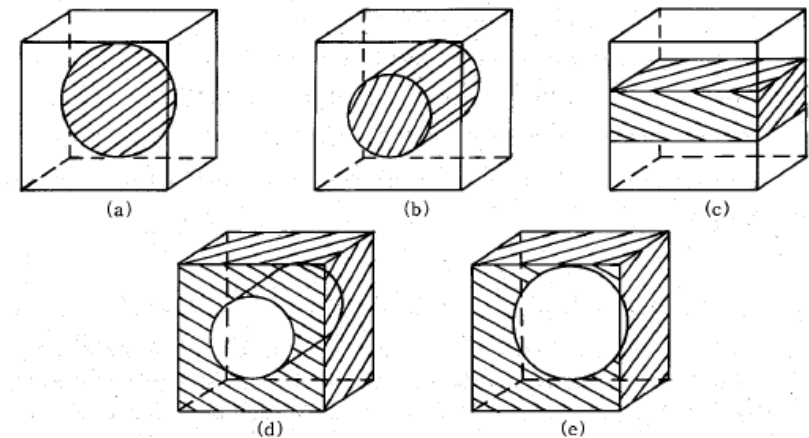
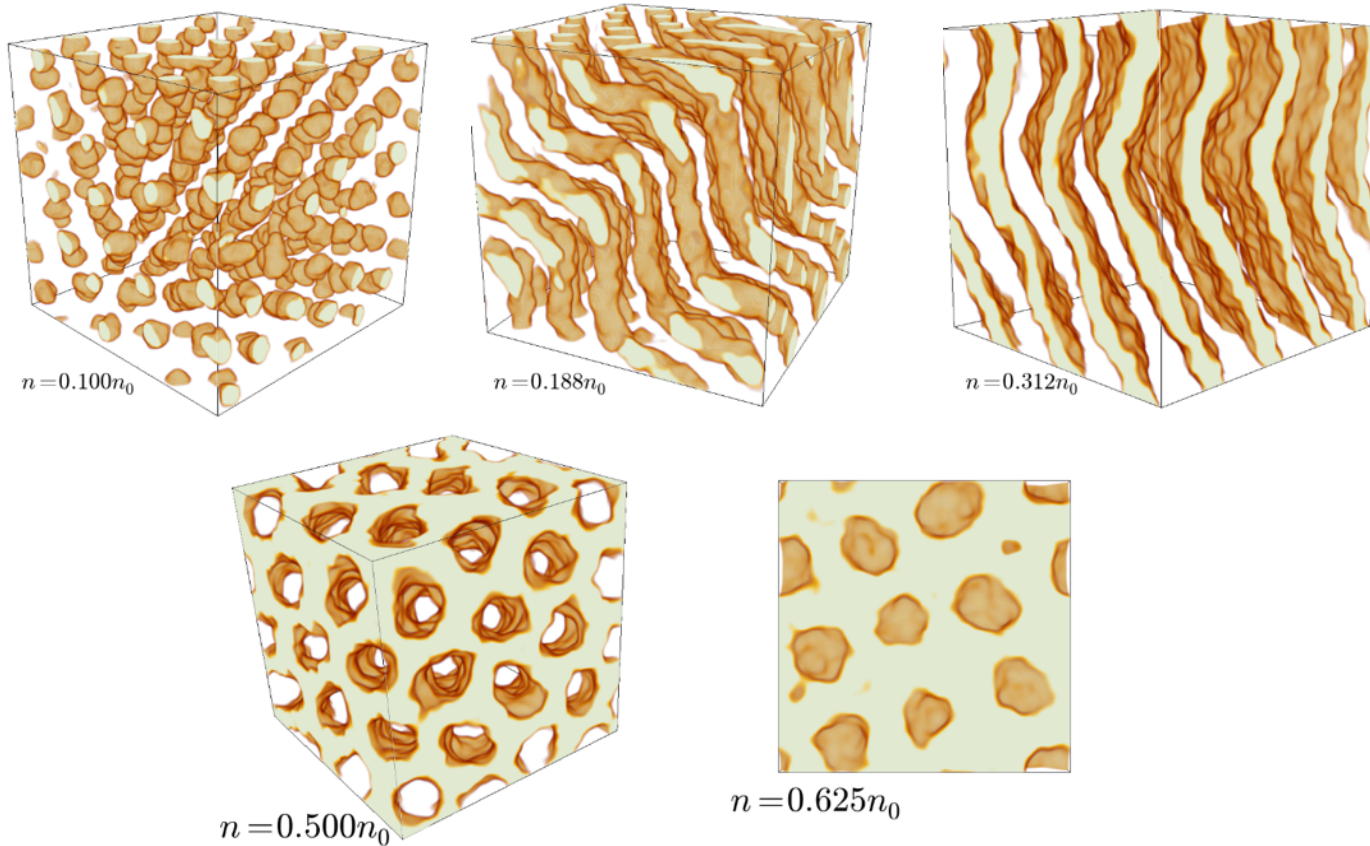


Fig. 1. Candidates for nuclear shapes. Protons are confined in the hatched regions, which we call nuclei. Then the shapes are, (a) sphere, (b) cylinder, (c) board or plank, (d) cylindrical hole and (e) spherical hole. Note that many cells of the same shape and orientation are piled up to form the whole space, and thereby the nuclei are joined to each other except for the spherical nuclei (a).

# Nuclear Pasta



*Shape of Nuclei in the Crust of Neutron Star*

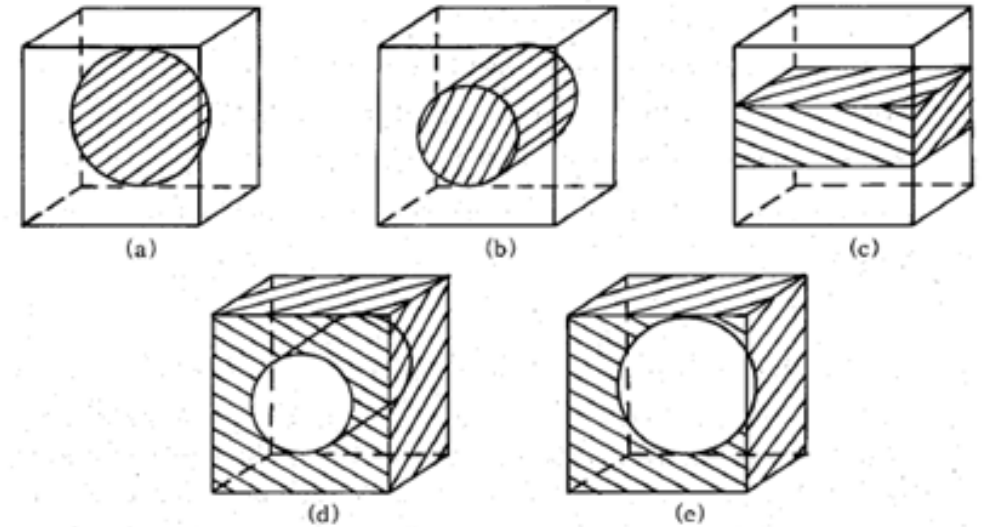


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# Classical Pasta Formalism



- **Classical Molecular Dynamics** with IUMD on Big Red II

$$V_{np}(r_{ij}) = ae^{-r_{ij}^2/\Lambda} + [b - c]e^{-r_{ij}^2/2\Lambda}$$

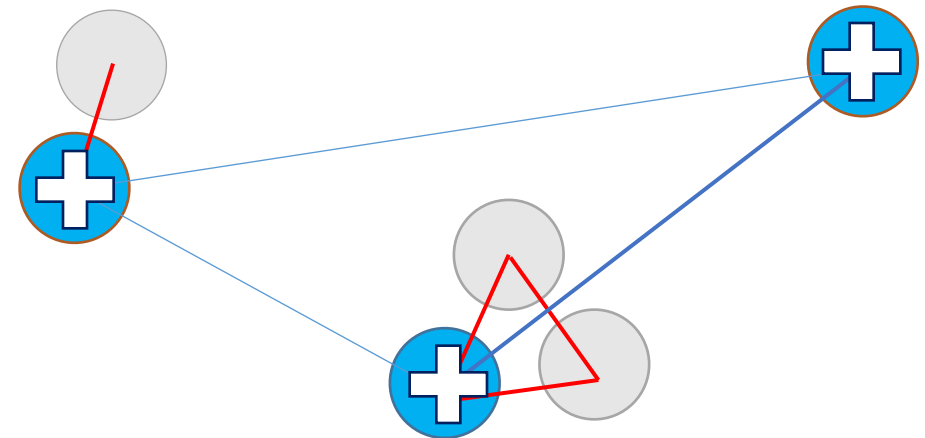
$$V_{nn}(r_{ij}) = ae^{-r_{ij}^2/\Lambda} + [b + c]e^{-r_{ij}^2/2\Lambda}$$

$$V_{pp}(r_{ij}) = ae^{-r_{ij}^2/\Lambda} + [b + c]e^{-r_{ij}^2/2\Lambda} + \frac{\alpha}{r_{ij}}e^{-r_{ij}/\lambda}$$

$a$	$b$	$c$	$\Lambda$	$\lambda$
110 MeV	-26 MeV	24 MeV	1.25 fm <sup>2</sup>	10 fm

- Short range **nuclear** force
- Long range **Coulomb** force

Nucleus	Monte-Carlo $\langle V_{tot} \rangle$ (MeV)	Experiment (MeV)
<sup>16</sup> O	-7.56 ± 0.01	-7.98
<sup>40</sup> Ca	-8.75 ± 0.03	-8.45
<sup>90</sup> Zr	-9.13 ± 0.03	-8.66
<sup>208</sup> Pb	-8.2 ± 0.1	-7.86



# Classical Pasta Formalism



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Density

$b$	$c$	$\Lambda$	$\lambda$
MeV	24 MeV	1.25 fm <sup>2</sup>	10 fm

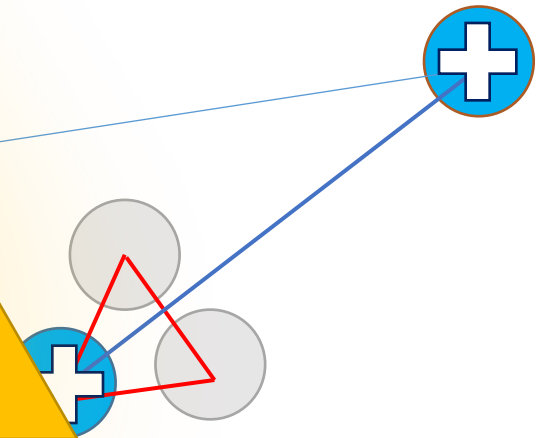


range **nuclear** force  
range **Coulomb** force

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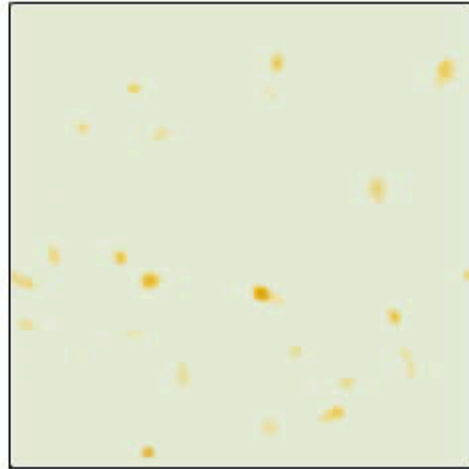
Proton Fraction

Temperature





Gold Nucleus  
For Scale

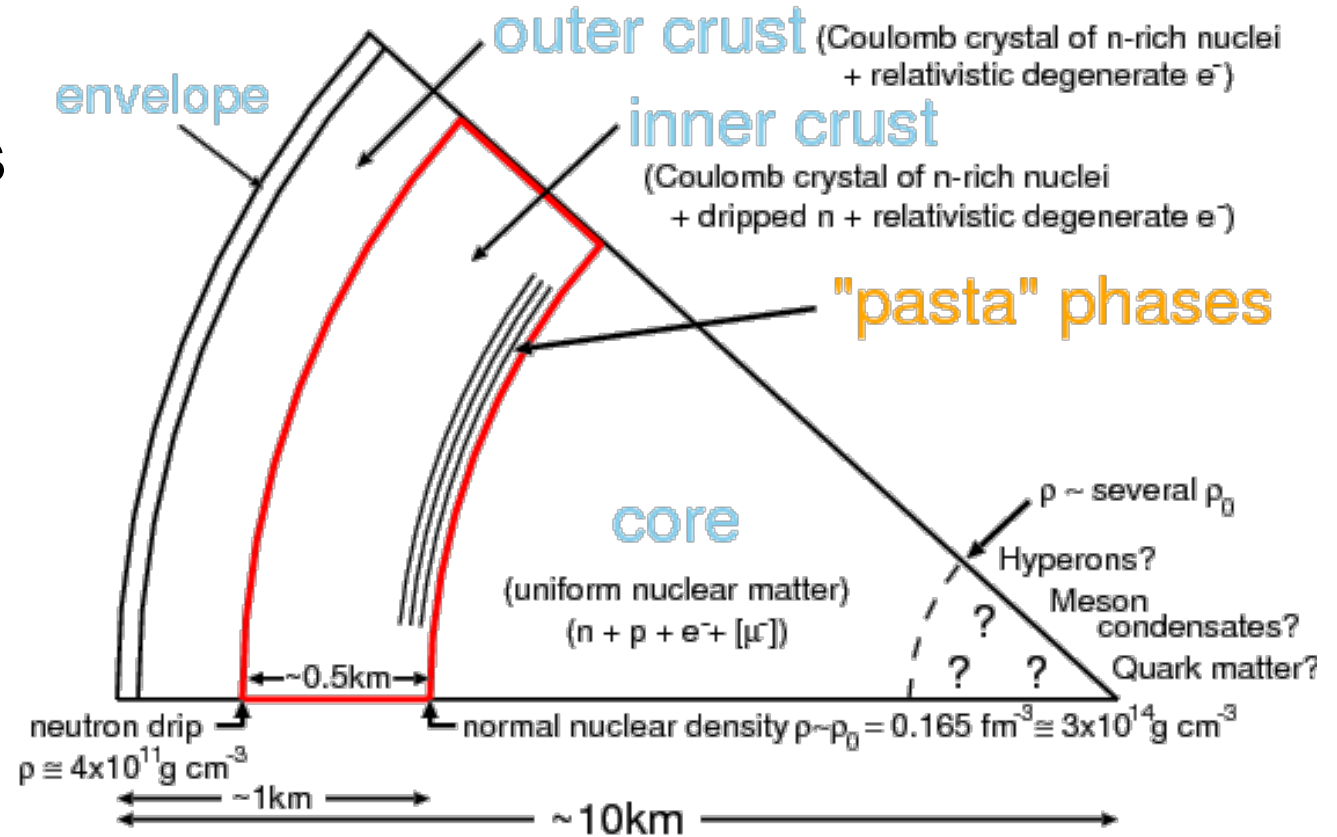


$$n = 0.1200 \text{fm}^{-3}$$

# Phases of Pasta



- Where does pasta form?
  - 1) Inner crust of neutron stars

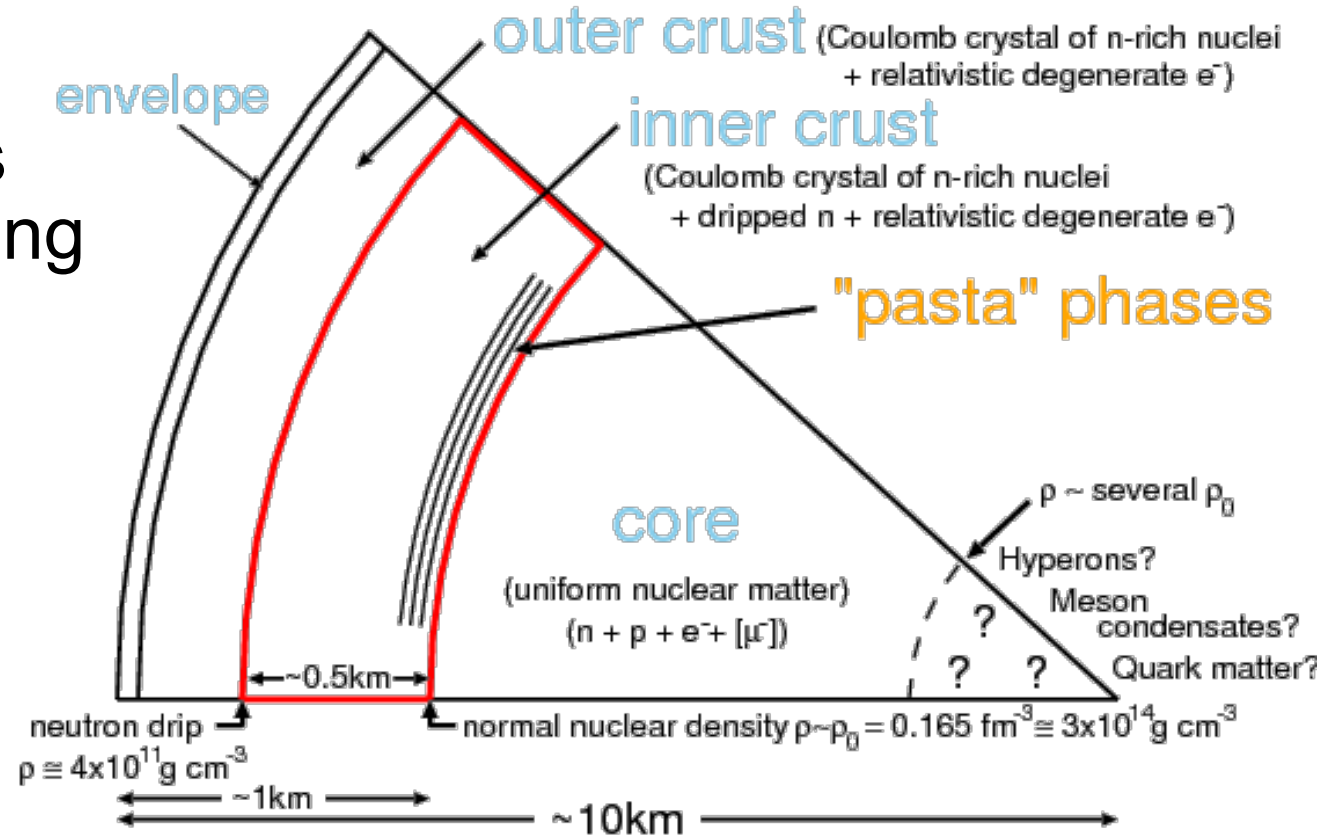


(Watanabe et al. 2011)

# Phases of Pasta



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(Watanabe et al. 2011)

# Phases of Pasta



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... but that's not interesting
- Under what conditions does pasta form?

# Phases of Pasta



- Where does pasta form?

1) Inner crust of neutron stars  
... but that's not interesting

- Under what conditions does pasta form?

1) Temperature:  $T \lesssim 10 \text{ MeV}$

2) Density:  $0.1 n_0 \lesssim n \lesssim 1.0 n_0$

3) Proton Fraction:  $0.1 \lesssim Y_e$

(Sonoda et al., 2008)

(Schuetrumpf et al. 2013)

(Caplan et al., in prep)

# Phases of Pasta



- Where does pasta form?
  - 1) Inner crust of neutron stars  
... but that's not interesting
  - 2) Supernova?
  - 3) Neutrons star mergers?
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# Phases of Pasta



- Where does pasta form?

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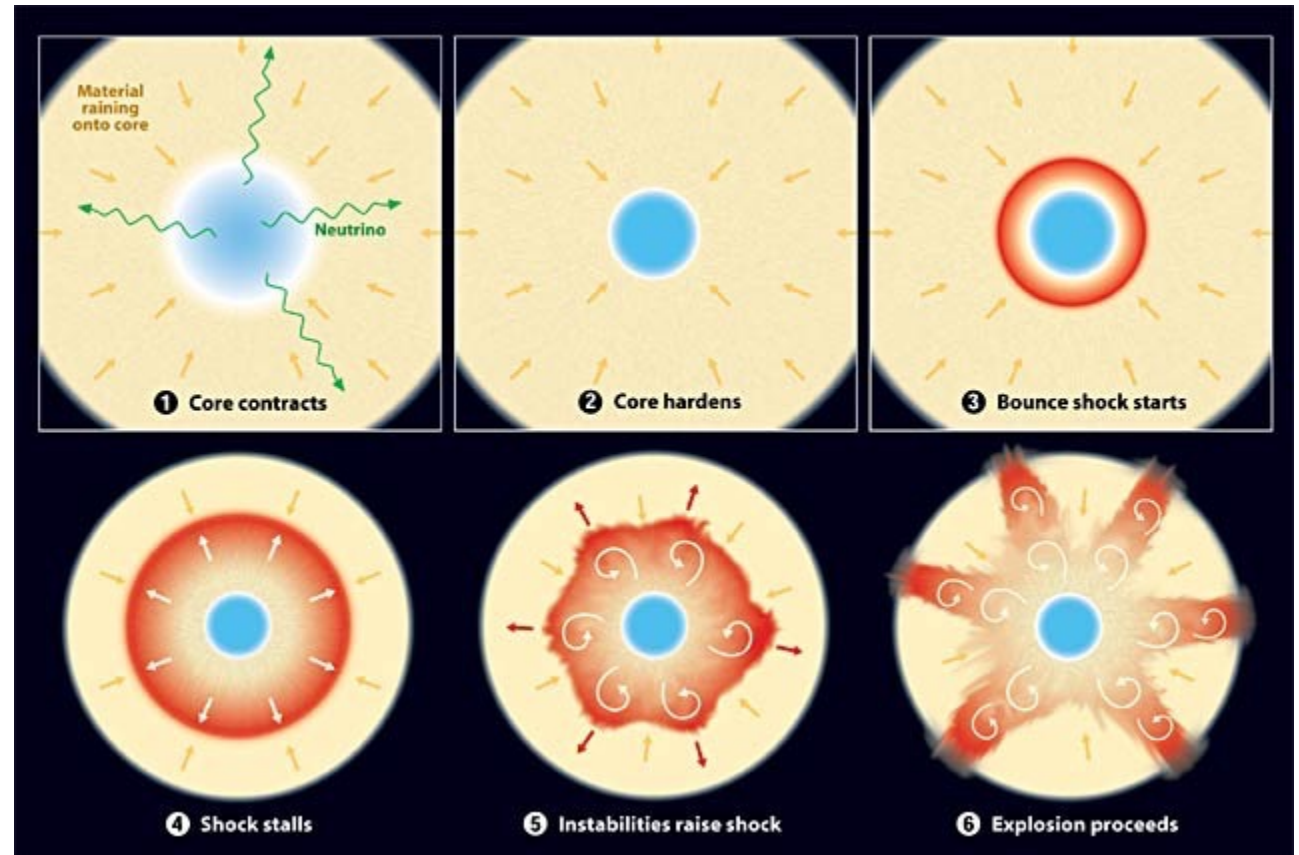
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Where in **these** do we find **these conditions**?

# Supernova



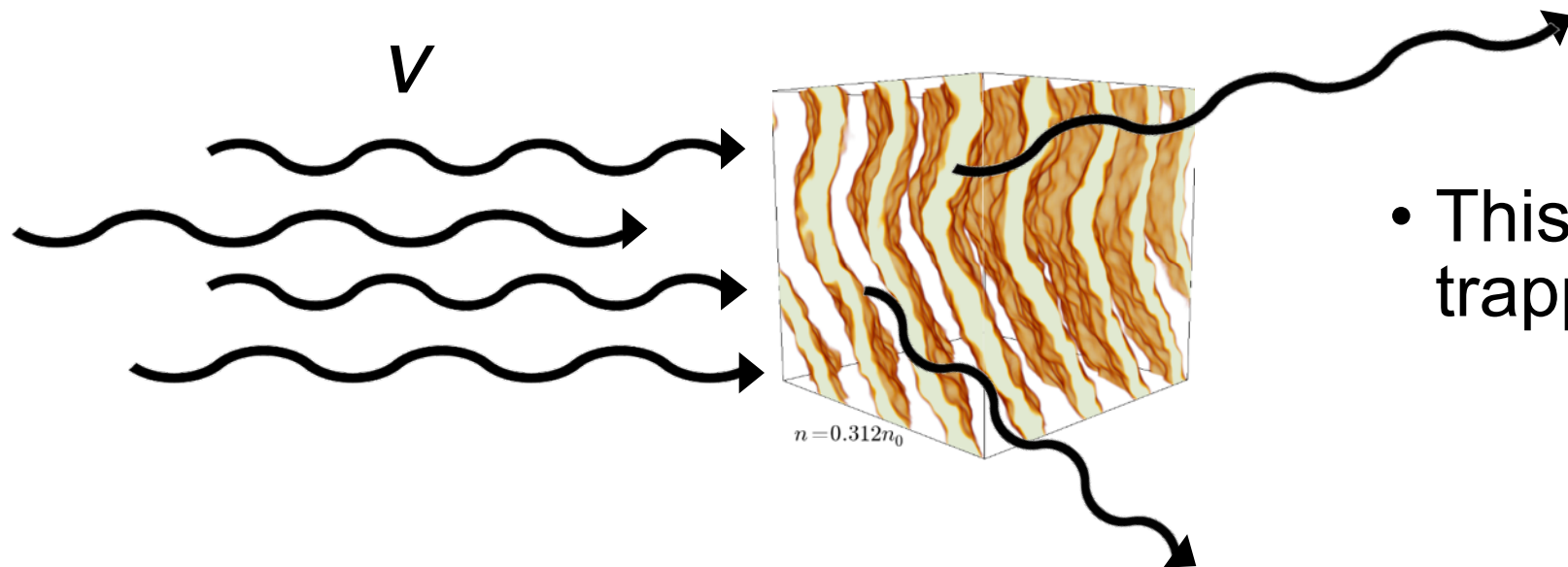
- Pasta has been studied for its role in supernova
- When the core collapses to form a proto-neutron star, it *deleptonizes*.
- The flux of  $10^{58}$  neutrinos from the core interacts with the infalling gas, blowing off the outer layers



# Supernova



- Pasta has been studied for its role in supernova
- Pasta 'pieces' have a separation comparable to neutrino wavelengths, so neutrinos can scatter coherently from pasta



- This makes pasta opaque, trapping neutrinos

# Supernova



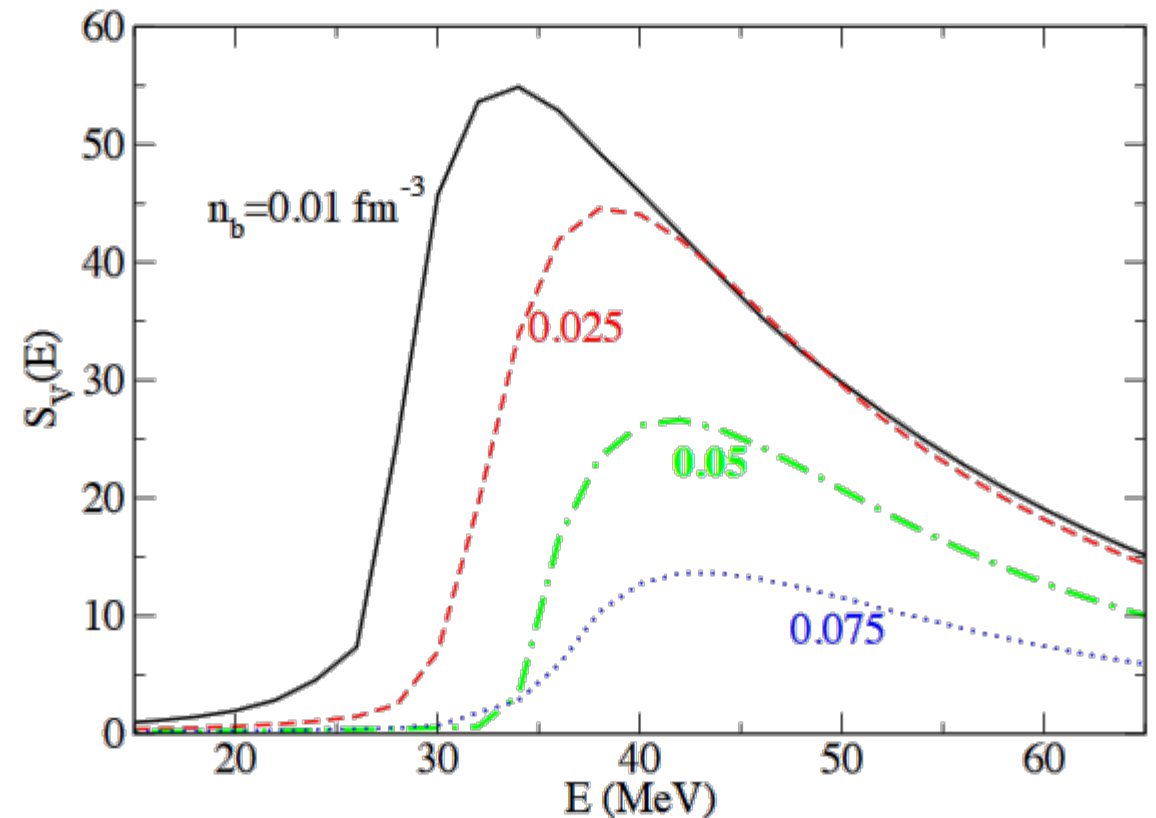
- We calculate the opacity of pasta, or mean free path, from molecular dynamics simulations

$$S_i(\mathbf{q}) = \langle \rho_i^*(\mathbf{q}, t) \rho_i(\mathbf{q}, t) \rangle_t - \langle \rho_i^*(\mathbf{q}, t) \rangle_t \langle \rho_i(\mathbf{q}, t) \rangle_t$$

$$\rho_i(\mathbf{q}, t) = N_i^{-1/2} \sum_{j=1}^{N_i} e^{i\mathbf{q} \cdot \mathbf{r}_j(t)}$$

$$\lambda_t^{-1} = \sigma_t^0 \rho_n \langle S(E_\nu) \rangle$$

(Horowitz et al., 2004)  
(Caplan et al., 2017)

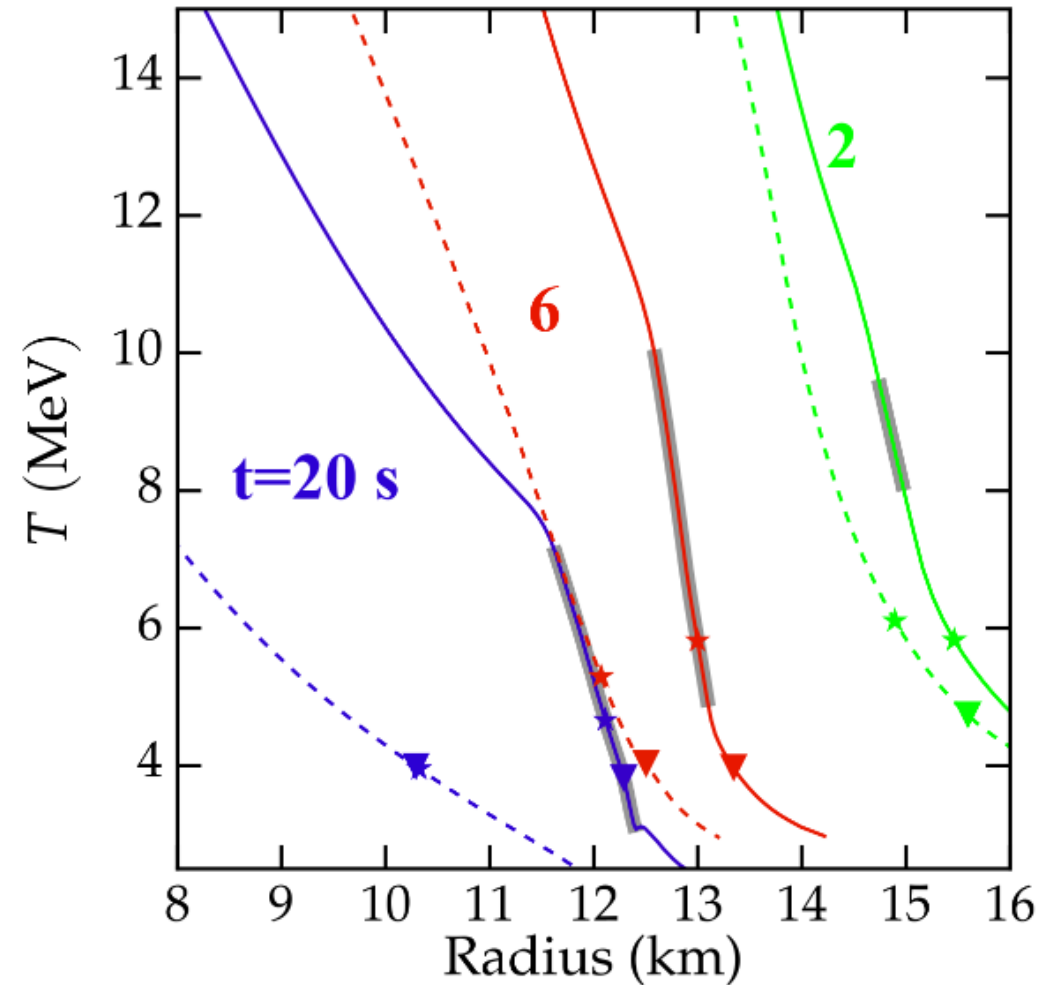


(Horowitz et al., 2016)

# Supernova



- What happens when you include pasta opacity in supernova simulations?
- 1D Simulation of supernova with pasta (solid) and without pasta (dashed)
- Pasta gives supernova a hotter, extended atmosphere.
- What does this do to neutrino luminosities?

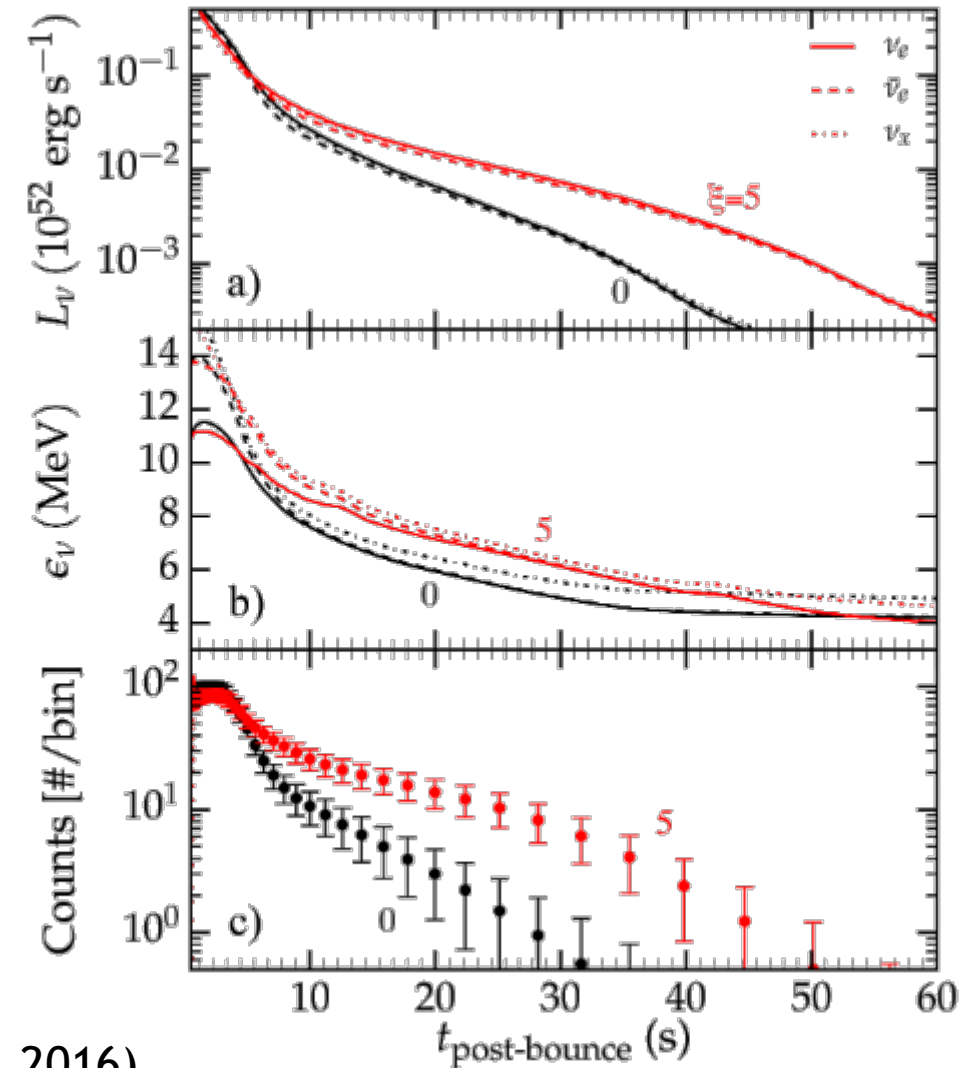


(Horowitz et al., 2016)

# Supernova



- What does this do to neutrino luminosities?
- Well, we observed  $\sim 20$  neutrinos from SN1987A. With SuperK, we expect several thousand detections.
- Pasta has a distinct effect on supernova neutrino signals:
  - More energetic neutrinos at later times
  - More neutrinos at late times after core collapse



(Horowitz et al., 2016)

# Open Questions

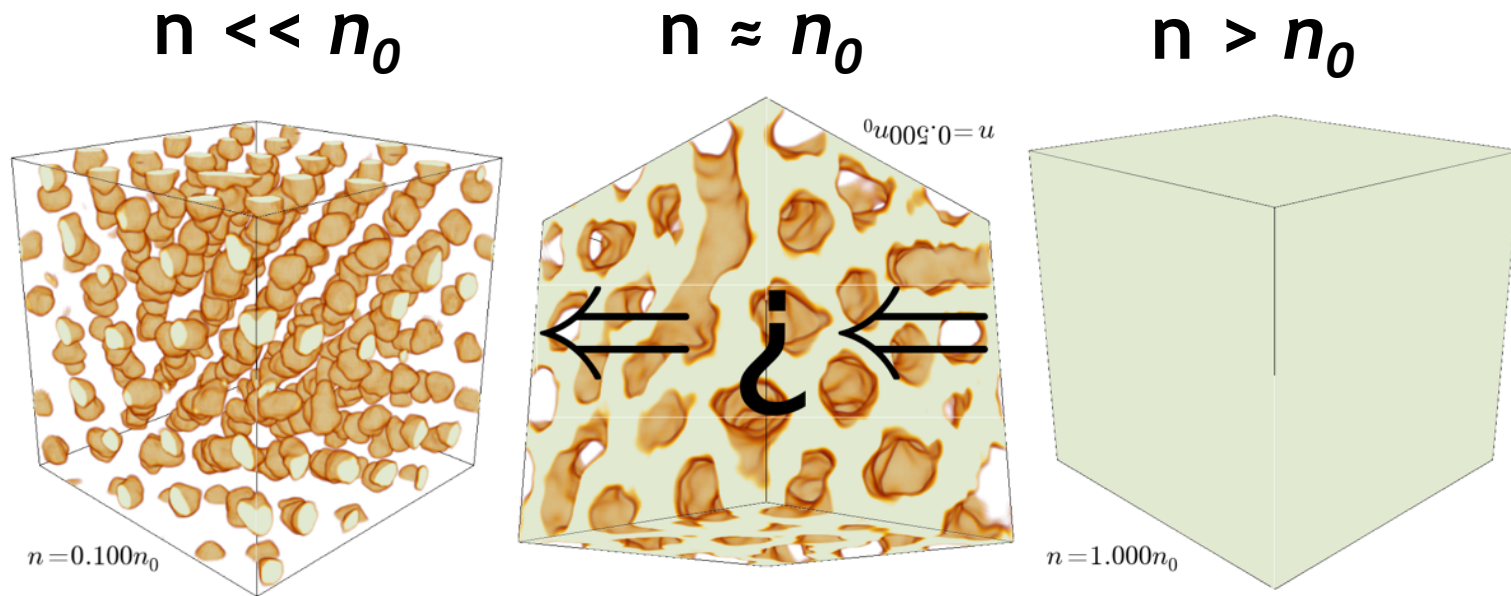


- What is the neutrino opacity of pasta?
- What effect does this neutrino opacity have on supernova?
- Certainly, the enhanced neutrino opacity should affect the proton fraction of the pasta. This is material that is hot, dense, and neutron rich, and may undergo the r-process. How does pasta change the r-process?

# Neutron Star Mergers



- What about neutron star mergers?
- It's like a supernova run in reverse...
- Ejecta may pass through pasta phases

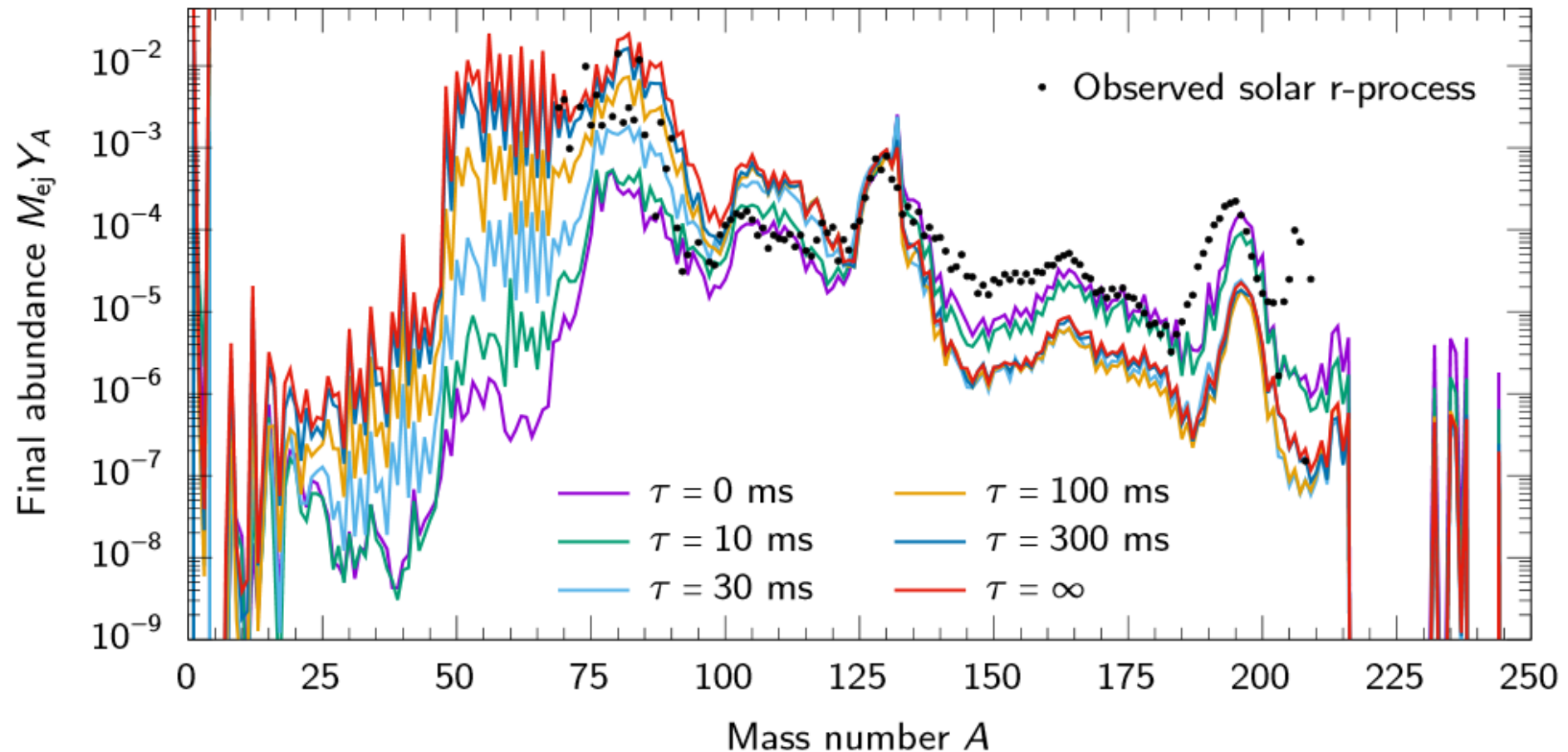




# Neutron Star Mergers



- One recent result (Lippuner, 2017), the lifetime of the hypermassive NS in a merger strongly effects r-process yields



# Forging Connections

- Theory can provide the modified neutrino opacities for pasta matter.
- Can simulation/nuclear reaction network codes be modified to study the effect that pasta plays on the ejecta?

