

Study of the optical potential parameters of $^{12}\text{C} + \text{nucleus}$

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Background

- The optical potential is an important tool to study **nucleus-nucleus interactions**.
- The optical potential is an important quantity to describe not only **elastic scattering** but also **more complicated reactions** such as inelastic scattering, breakup, and transfer reactions.

The optical potential

- **Phenomenological** and **Microscopic** potentials.
- The parameters of phenomenological potentials can be obtained by analyzing experimental data. Such as Woods-Saxon potential.
- The calculation of microscopic potentials based on the nucleon-nucleon interaction and approximation of nuclear material or nuclear structure. Such as folding potential.

Research status

- The optical potential of reactions induced by light particles have been studied a lot.
- The optical potential parameters always have **large ambiguities** for reactions between heavy ions because of **strong Coulomb interaction**, the study is far from satisfied.

Research status

- Microscopic potentials:
 - Sao Paulo Potential (SPP)
 - Phys. Rev. C 66, 014610 (2002)
 - University of Sao Paulo, Spanish.

System	E_{Lab} (MeV)
$^{16}\text{O} + ^{58}\text{Ni}$	35, 35.5, 36, 36.5, 37, 38
$^{16}\text{O} + ^{60}\text{Ni}$	35, 35.5, 36, 37, 38
$^{16}\text{O} + ^{62,64}\text{Ni}$	34, 35, 36
$^{16}\text{O} + ^{88}\text{Sr}$	43, 44, 45
$^{16}\text{O} + ^{90}\text{Zr}$	46, 47, 48
$^{16}\text{O} + ^{92}\text{Zr}$	45, 46, 47, 48
$^{16}\text{O} + ^{92}\text{Mo}$	48, 48.5, 49
$^{16}\text{O} + ^{120}\text{Sn}$	53, 54, 55
$^{16}\text{O} + ^{138}\text{Ba}$	54, 55, 56, 57
$^{16}\text{O} + ^{208}\text{Pb}$	74, 75, 76, 77, 78
$^{18}\text{O} + ^{58}\text{Ni}$	35.1, 35.5, 37.1, 38
$^{18}\text{O} + ^{60}\text{Ni}$	34.5, 35.5, 37.1, 38

System	E_{Lab} (MeV)
$p + ^{40}\text{Ca}, ^{208}\text{Pb}$	30.3
$d + ^{40}\text{Ca}, ^{208}\text{Pb}$	52
$^4\text{He} + ^{40}\text{Ca}, ^{208}\text{Pb}$	104
$^6\text{Li} + ^{12}\text{C}, ^{28}\text{Si}$	210, 318
$^6\text{Li} + ^{40}\text{Ca}, ^{58}\text{Ni}, ^{90}\text{Zr}, ^{208}\text{Pb}$	210
$^7\text{Li} + ^{12}\text{C}, ^{28}\text{Si}$	350
$^{12}\text{C} + ^{12}\text{C}$	300, 360, 1016, 1440, 2400
$^{12}\text{C} + ^{208}\text{Pb}$	1440
$^{13}\text{C} + ^{208}\text{Pb}$	390
$^{16}\text{O} + ^{16}\text{O}$	250, 350, 480, 704, 1120
$^{16}\text{O} + ^{12}\text{C}, ^{28}\text{Si}, ^{40}\text{Ca}, ^{90}\text{Zr}, ^{208}\text{Pb}$	1504
$^{40}\text{Ar} + ^{60}\text{Ni}, ^{120}\text{Sn}, ^{208}\text{Pb}$	1760

Research status

- Microscopic potentials:
 - Phys. Rev. C 87, 044605 (2013)
 - Beihang University, China
 - Incident particle: ${}^6\text{Li}, {}^7\text{Li}$
 - Target: ${}^{40}\text{Ca} \sim {}^{208}\text{Pb}$
 - $E_{\text{lab}}: 30 \sim 240 \text{ MeV}$.

$$N_r^{6\text{Li}}(E_{\text{lab}}) = (0.00424 E_{\text{lab}}/A_P + 0.423) \pm 0.068,$$

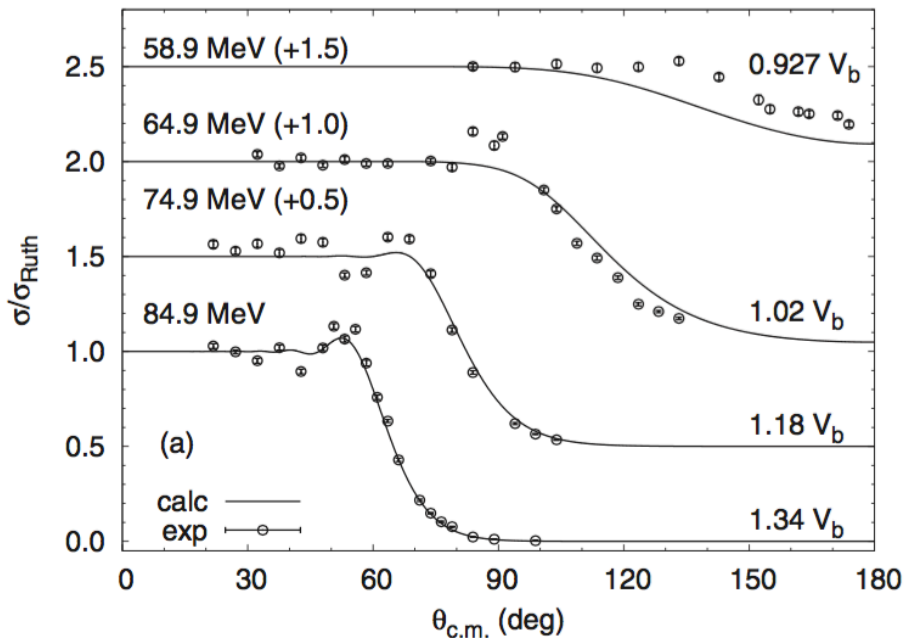
$$N_i^{6\text{Li}} = 1.22 \pm 0.17,$$

$$N_r^{7\text{Li}} = 0.489 \pm 0.096,$$

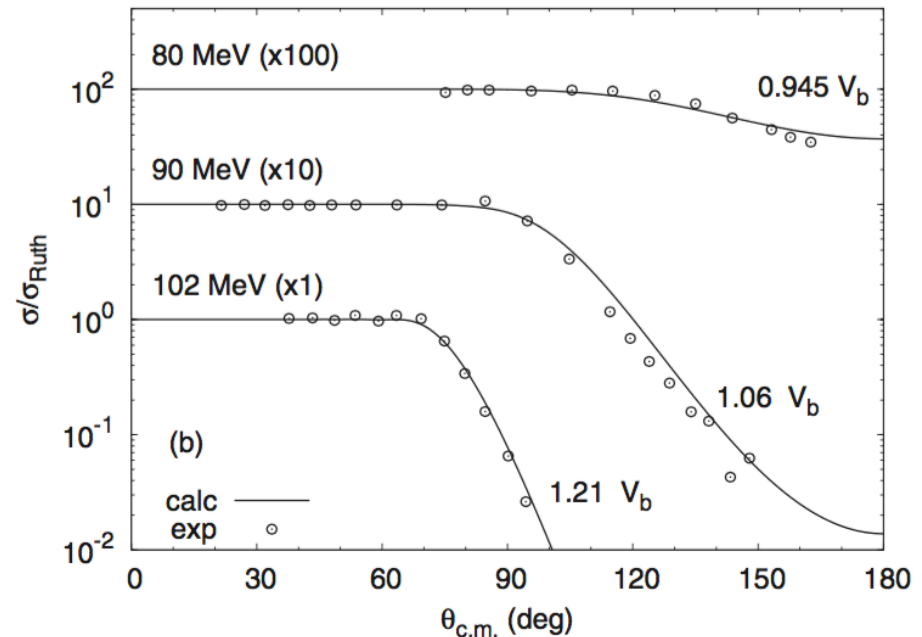
$$N_i^{7\text{Li}} = 1.28 \pm 0.22.$$

Research status

- Microscopic potentials:
 - Phys. Rev. C 87, 044605 (2013)
 - For other reaction systems



$^{12}\text{C}+^{208}\text{Pb}$



$^{16}\text{O}+^{208}\text{Pb}$

Research status

- Phenomenological potentials:
 - Phys. Rev. C 78, 014607 (2008)
 - Guangxi Normal University, China
 - modified Woods-Saxon

$$V_N(R) = \frac{V_0}{1 + \exp[(R - R_0)/a]},$$

$$V_0 = u_0[1 + \kappa(I_1 + I_2)] \frac{A_1^{1/3} A_2^{1/3}}{A_1^{1/3} + A_2^{1/3}},$$

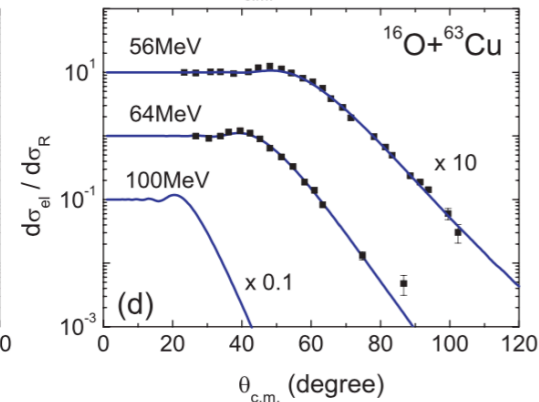
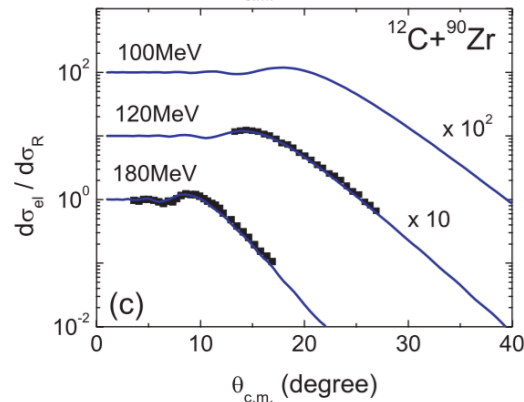
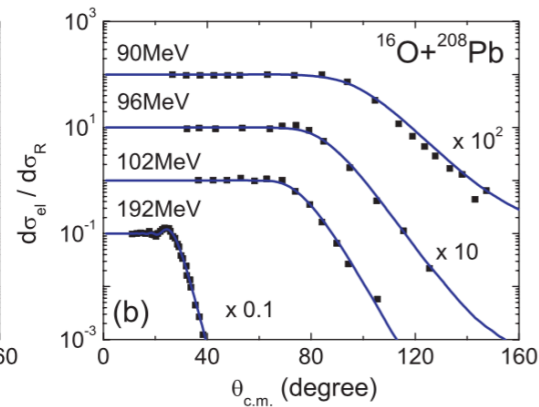
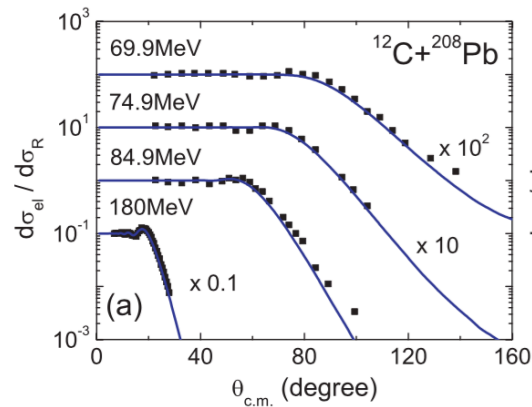
$$R_0 = r_0(A_1^{1/3} + A_2^{1/3}) + c.$$

r_0 (fm)	c (fm)	u_0 (MeV)	κ	a (fm)
1.27	-1.37	-44.16	-0.40	0.75

$$I_1 = (N_1 - Z_1)/A_1 \text{ and } I_2 = (N_2 - Z_2)/A_2$$

Research status

- Phenomenological potentials:
 - Phys. Rev. C 78, 014607 (2008)



Motivation and method

- The study for optical potential for reactions between heavy ions should be carried on.
- In this work, **Woods-Saxon (WS) parameters** will be extracted through fitting the elastic scattering angular distributions of **$^{12}\text{C} + \text{heavy ions}$** .
- The ambiguities will be overcome with volume integral.
- Formulas to infer global heavy-ion potential parameters will be summarized.

data sources

NNDC and RNB team of CIAE

Incident particle : ^{12}C

Target: ^{39}K , ^{40}Ca , ^{56}Fe , $^{90,91,92,94,96}\text{Zr}$, ^{115}In , ^{169}Tm ,
 ^{209}Bi

E_{lab} : 54 ~420 MeV

• WS parameters setting:

Woods-Saxon form:

$$V_n(r) = \frac{-V}{1 + \exp[(r - R_v)/a_v]} + i \frac{-W}{1 + \exp[(r - R_w)/a_w]}$$

$$R_i = r_i \times (A_P^{1/3} + A_T^{1/3})$$

Fixed:

$$W=35 \text{ MeV}, \quad r_w=1.15 \text{ fm}, \quad a_w=0.56 \text{ fm}, \quad r_C=1.0 \text{ fm}$$

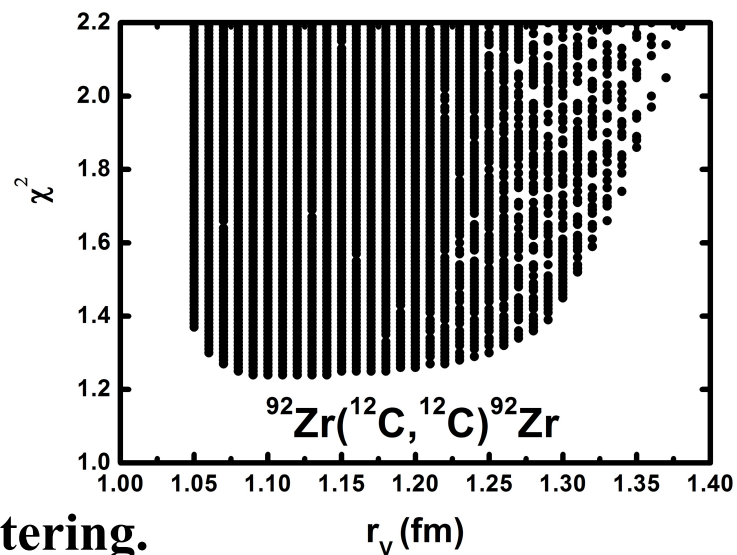
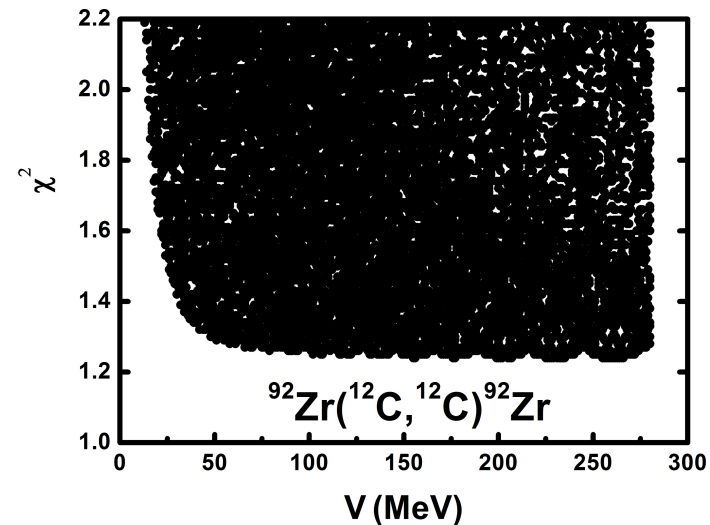
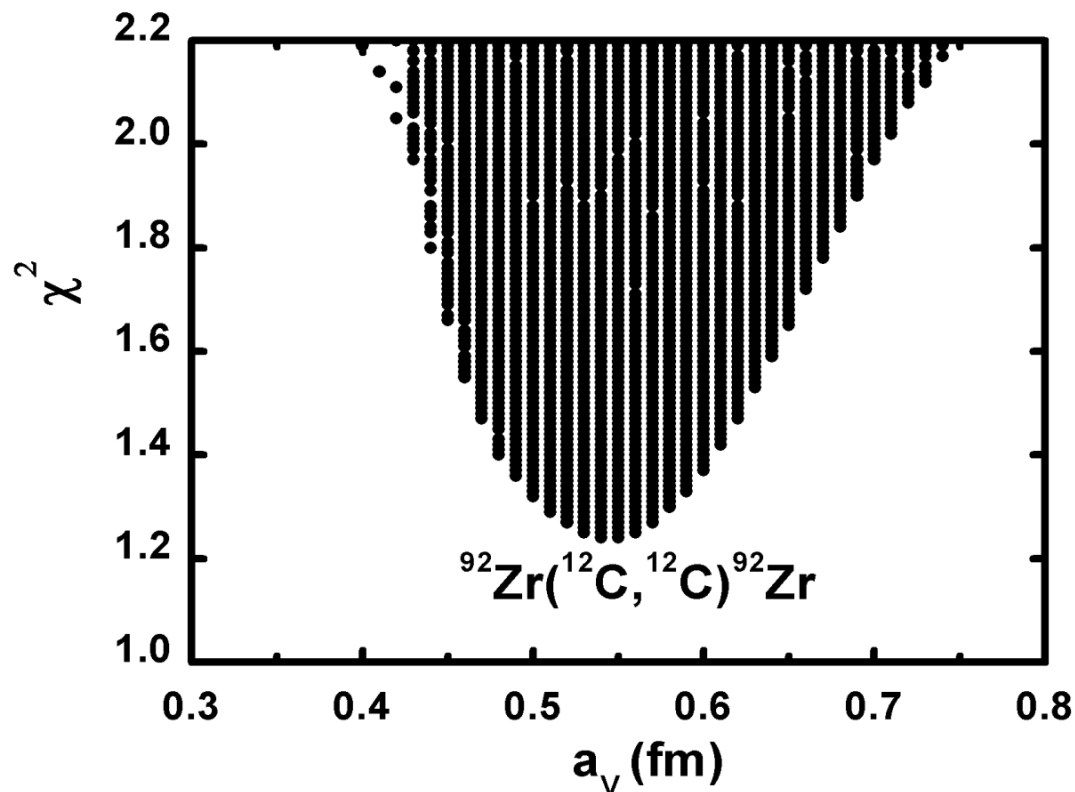
Variables :

$$V=20-280 \text{ MeV}, \quad \text{step: } 1 \text{ MeV}$$

$$r_v=0.70-1.40 \text{ fm}, \quad \text{step: } 0.01 \text{ fm}$$

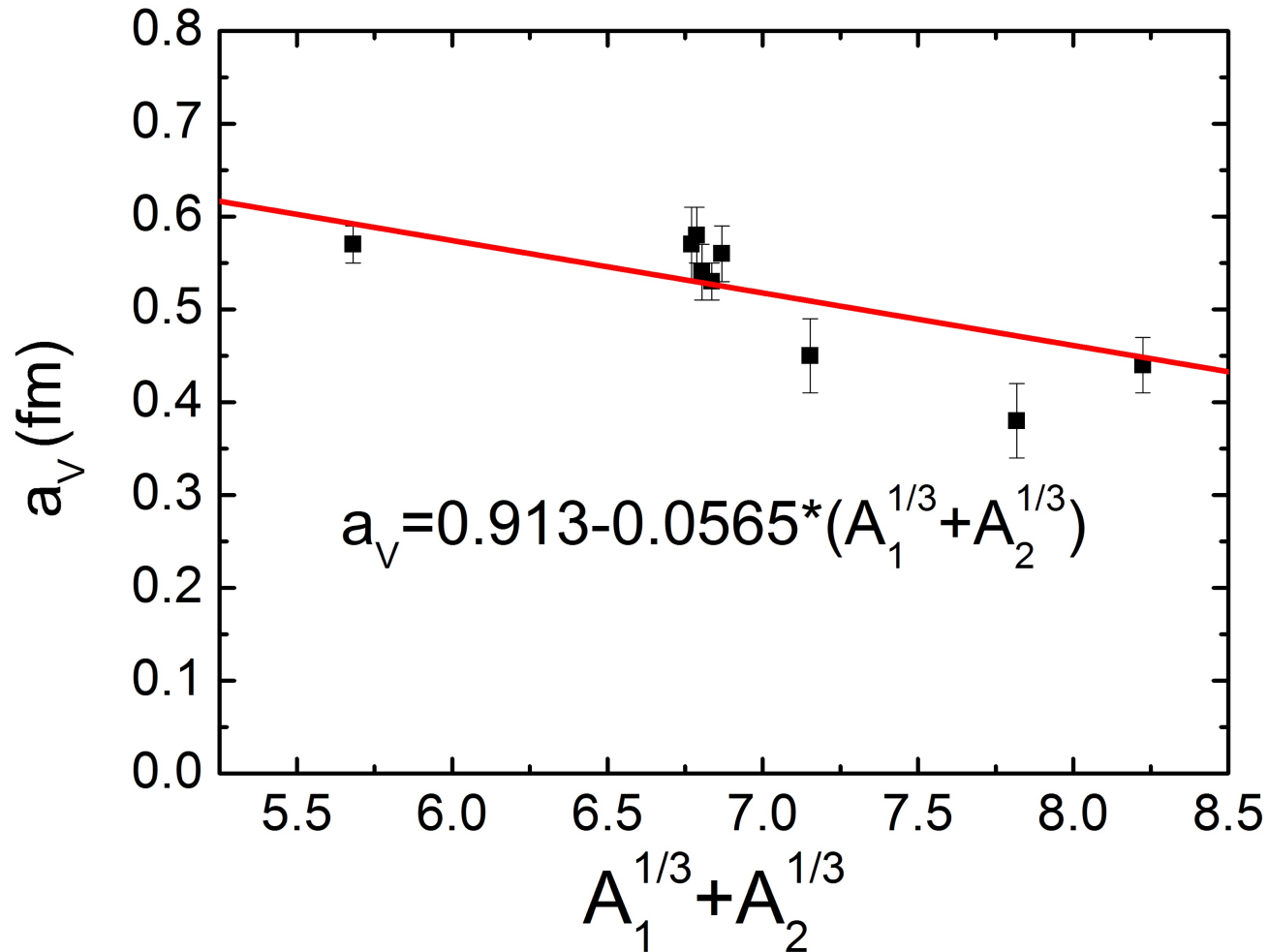
$$a_v=0.30-0.80 \text{ fm}, \quad \text{step: } 0.01 \text{ fm}$$

• Result for a_V



χ^2 versus V , r_V , a_V for $^{12}\text{C} + ^{92}\text{Zr}$ elastic scattering.

- a_V versus $R_0=(A_1^{1/3}+A_2^{1/3})$



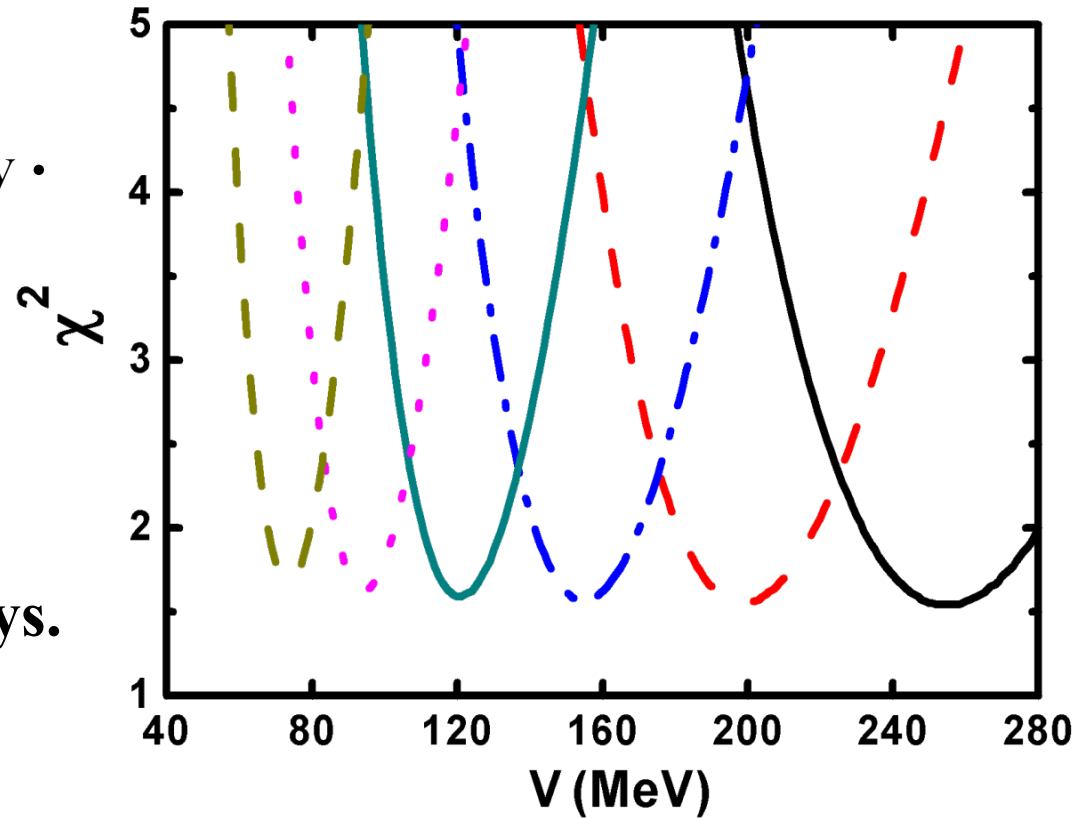
- Optical potential ambiguities

Each curve in picture corresponding to different r_V .

$$V \times \exp(R_V/a_V) = \text{const}$$

$$R_V = r_V(A_1^{1/3} + A_2^{1/3})$$

The **const** can be obtained with the parameters of valleys.

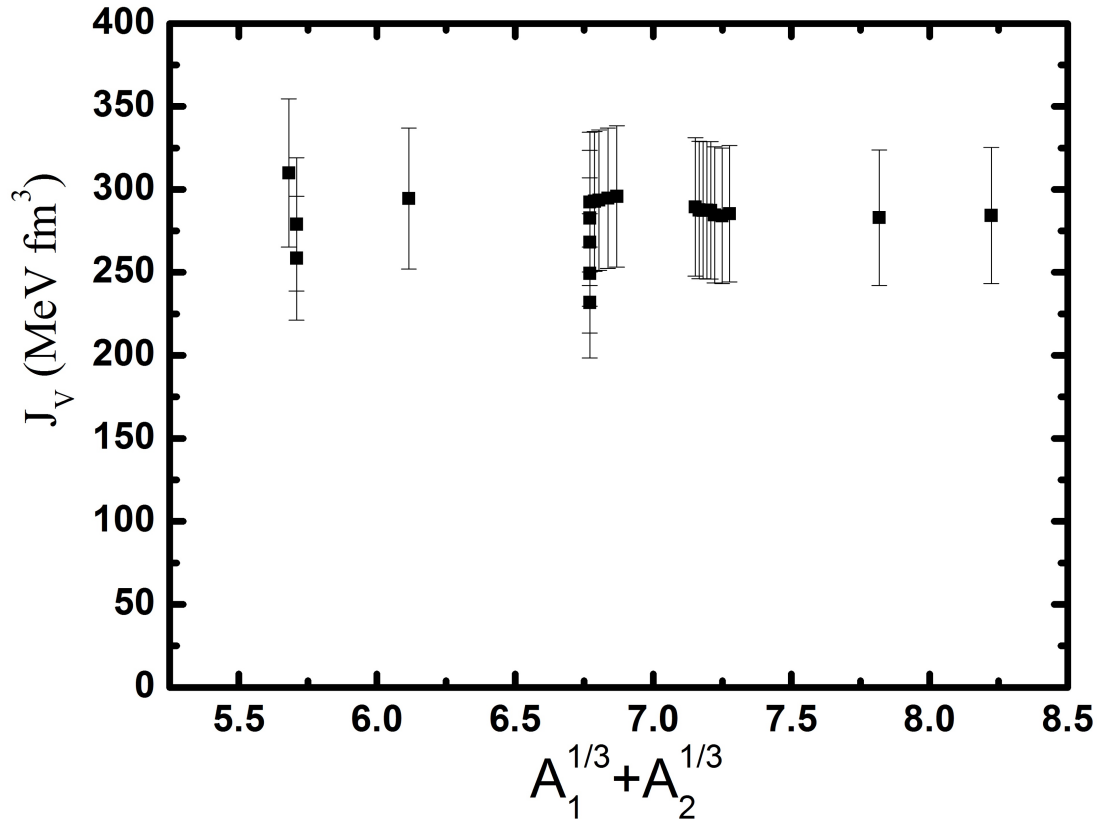


$^{12}\text{C} + ^{94}\text{Zr}$ elastic scattering

- **Volume integral**

$$J_V = -\frac{4\pi}{A_P A_T} \int V(r) r^2 dr$$

V(r) employed the double folding form.



- Calculation

$$V \times \exp(R_v/a_v) = \text{const}$$

+

$$J_V = -\frac{4\pi}{A_p A_T} \int V(r) r^2 dr$$

$$V_n(r) = \frac{-V}{1 + \exp[(r - R_v)/a_v]}$$

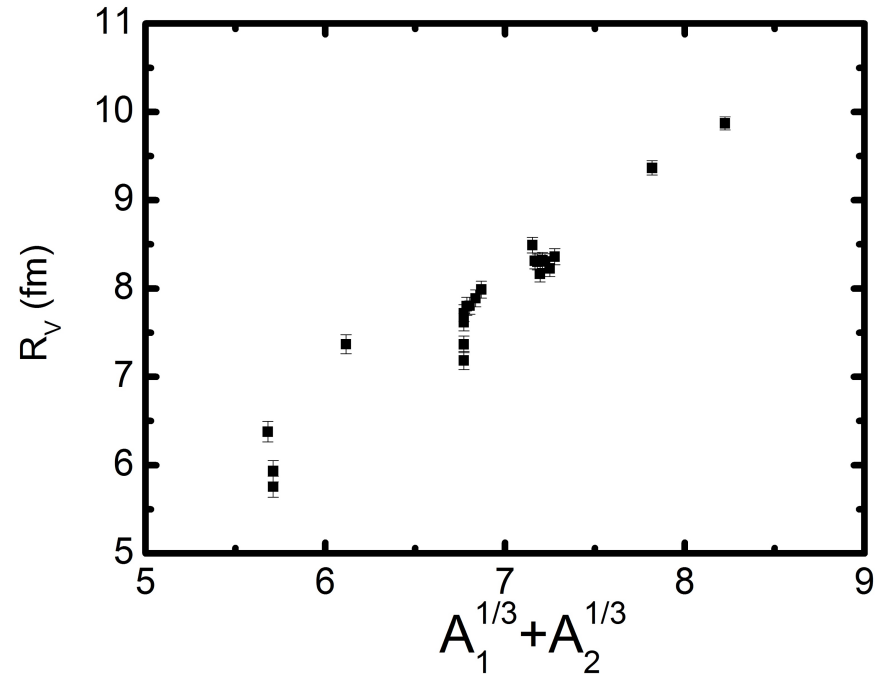
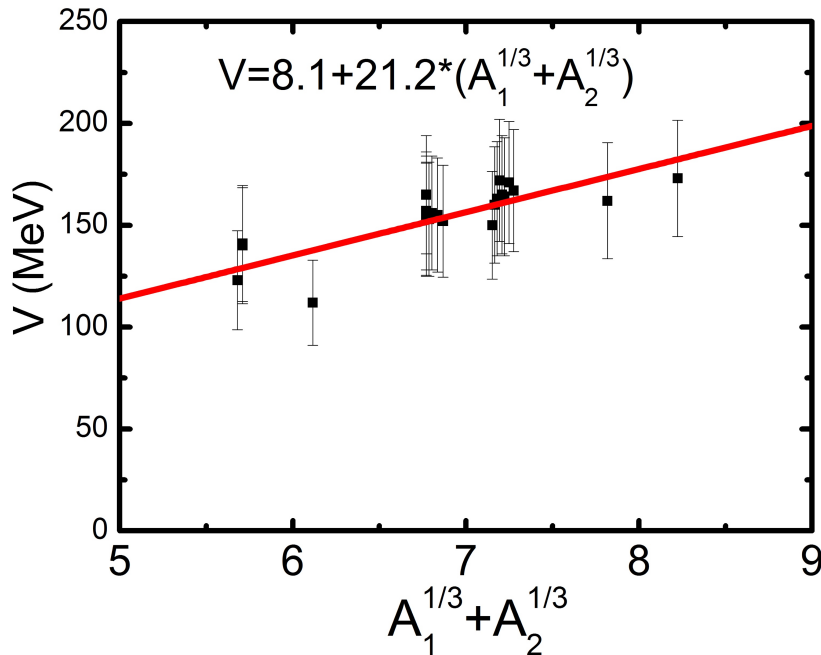


V and R_v

- Result --V, R_V

$$V = 8.1 + 21.2 \times (A_1^{1/3} + A_2^{1/3}) (\text{MeV})$$

$$R_V = 1.345 \times (A_1^{1/3} + A_2^{1/3}) - 0.002 \times (E - E_C) - 1.318 (\text{fm})$$



• Formulas

$$V = 8.1 + 21.2 \times (A_1^{1/3} + A_2^{1/3}) (\text{MeV})$$

$$R_V = 1.345 \times (A_1^{1/3} + A_2^{1/3}) - 0.002 \times (E - E_C) - 1.318 \text{ (fm)}$$

$$a_V = 0.913 - 0.0565 \times (A_1^{1/3} + A_2^{1/3}) \text{ (fm)}$$

$$W = 35 \text{ (MeV)}$$

$$R_W = 1.15 \times R_0 \text{ (fm)}$$

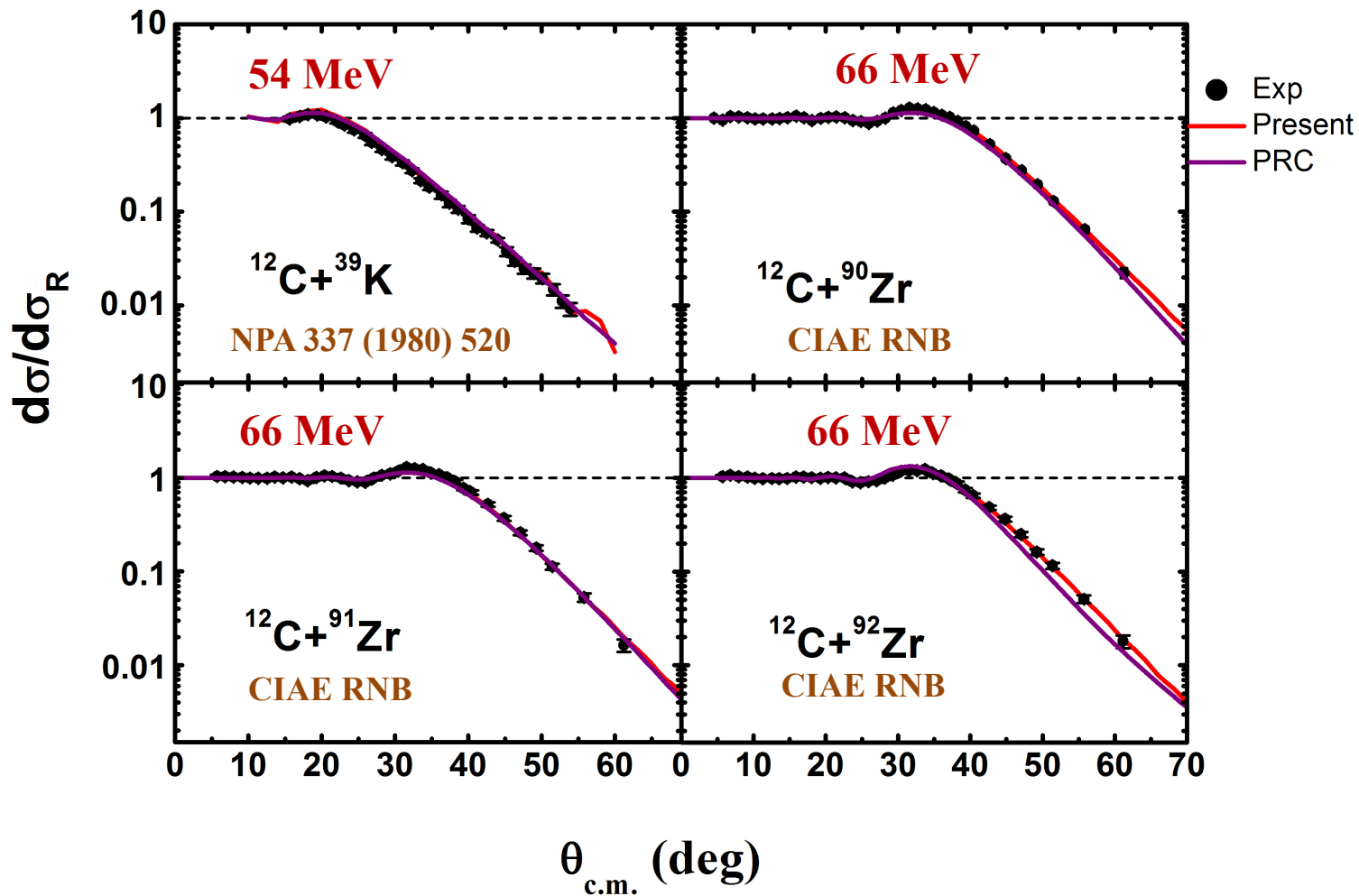
$$a_W = 0.56 \text{ (fm)}$$

$$R_C = 1.00 \times (A_1^{1/3} + A_2^{1/3}) (\text{fm})$$

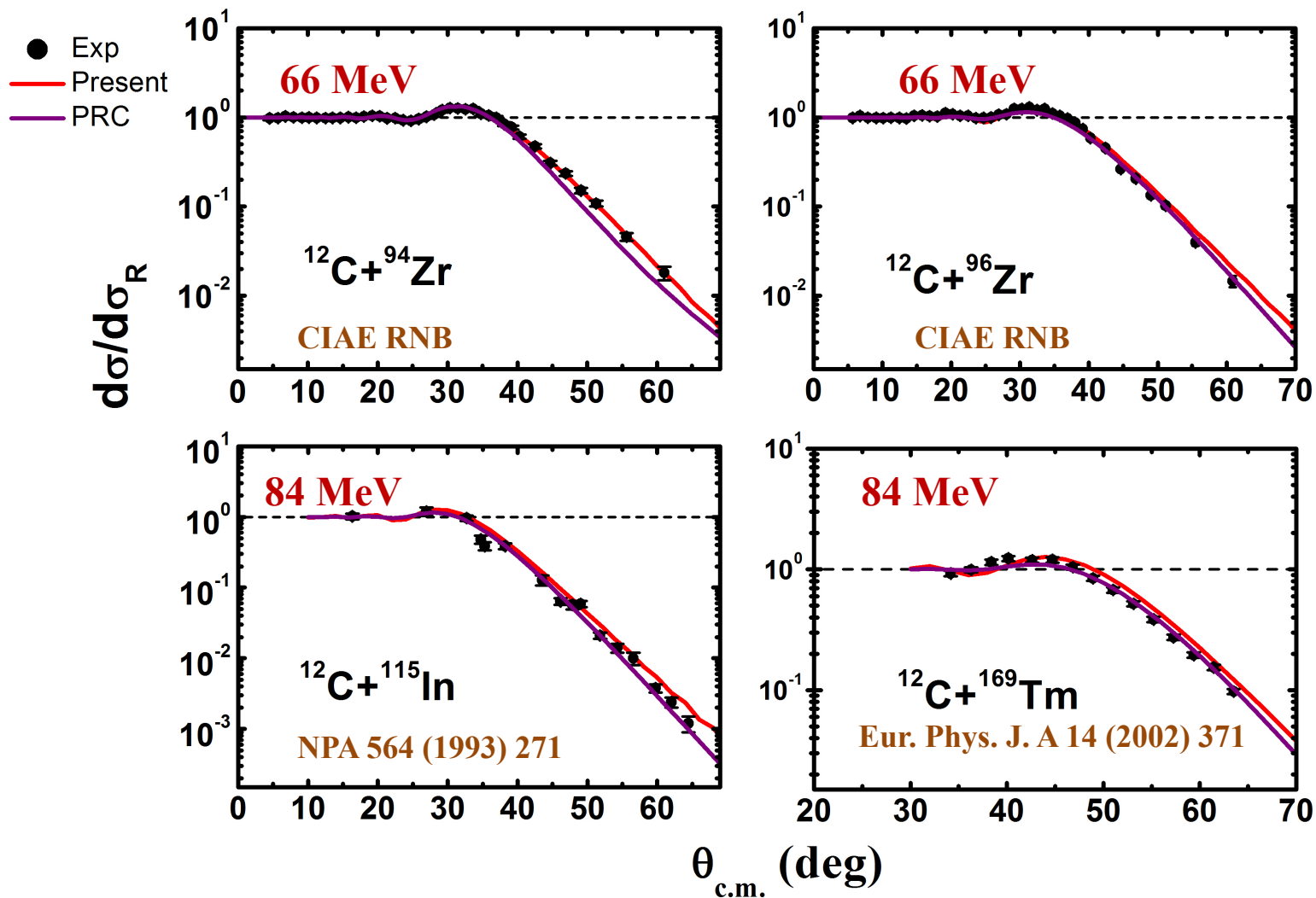
$$\bullet E_C = \frac{6Z_P Z_T e^2}{5R_C}$$

$$\bullet R_V = r_V \times (A_1^{1/3} + A_2^{1/3})$$

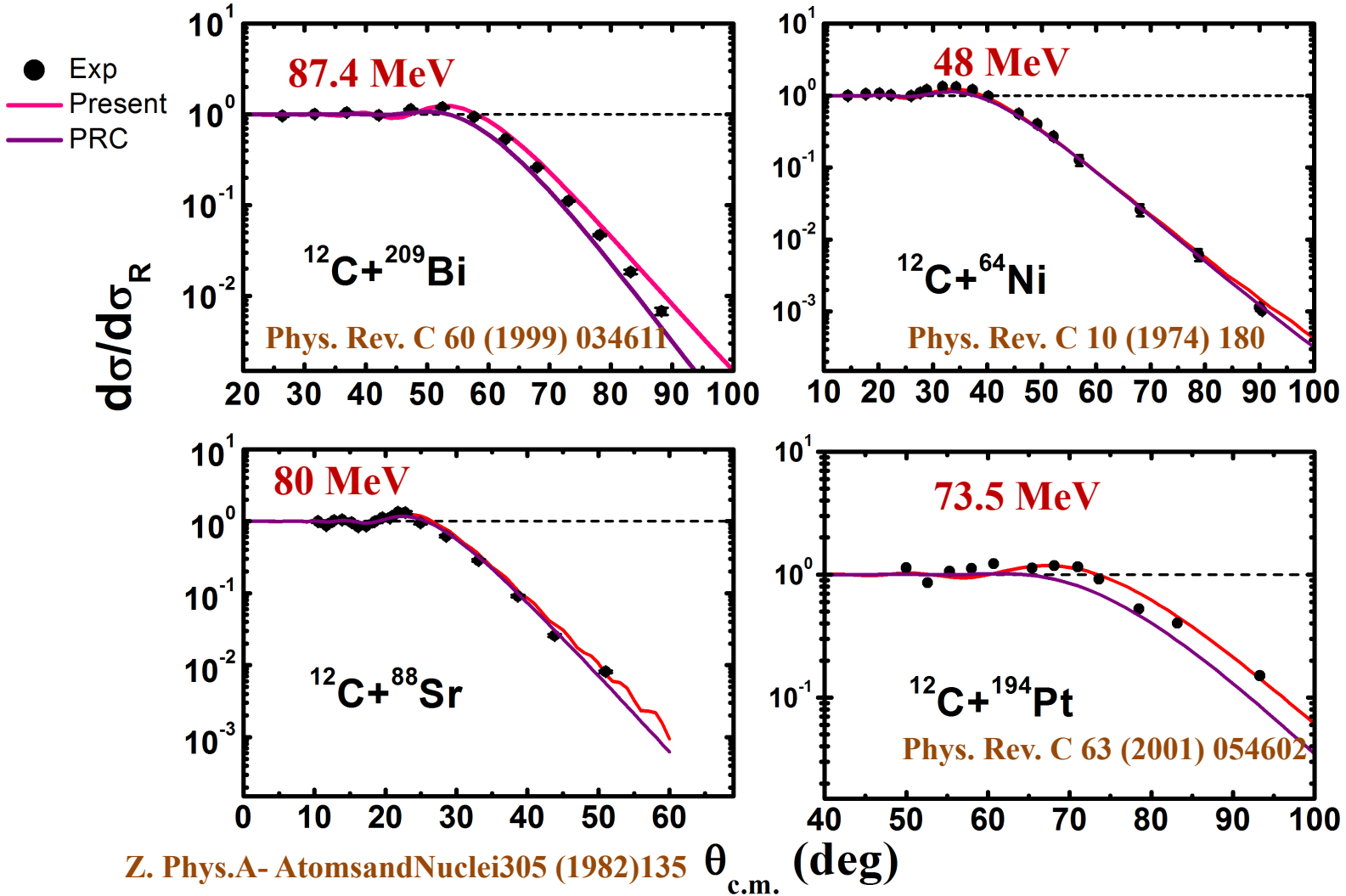
• Verification



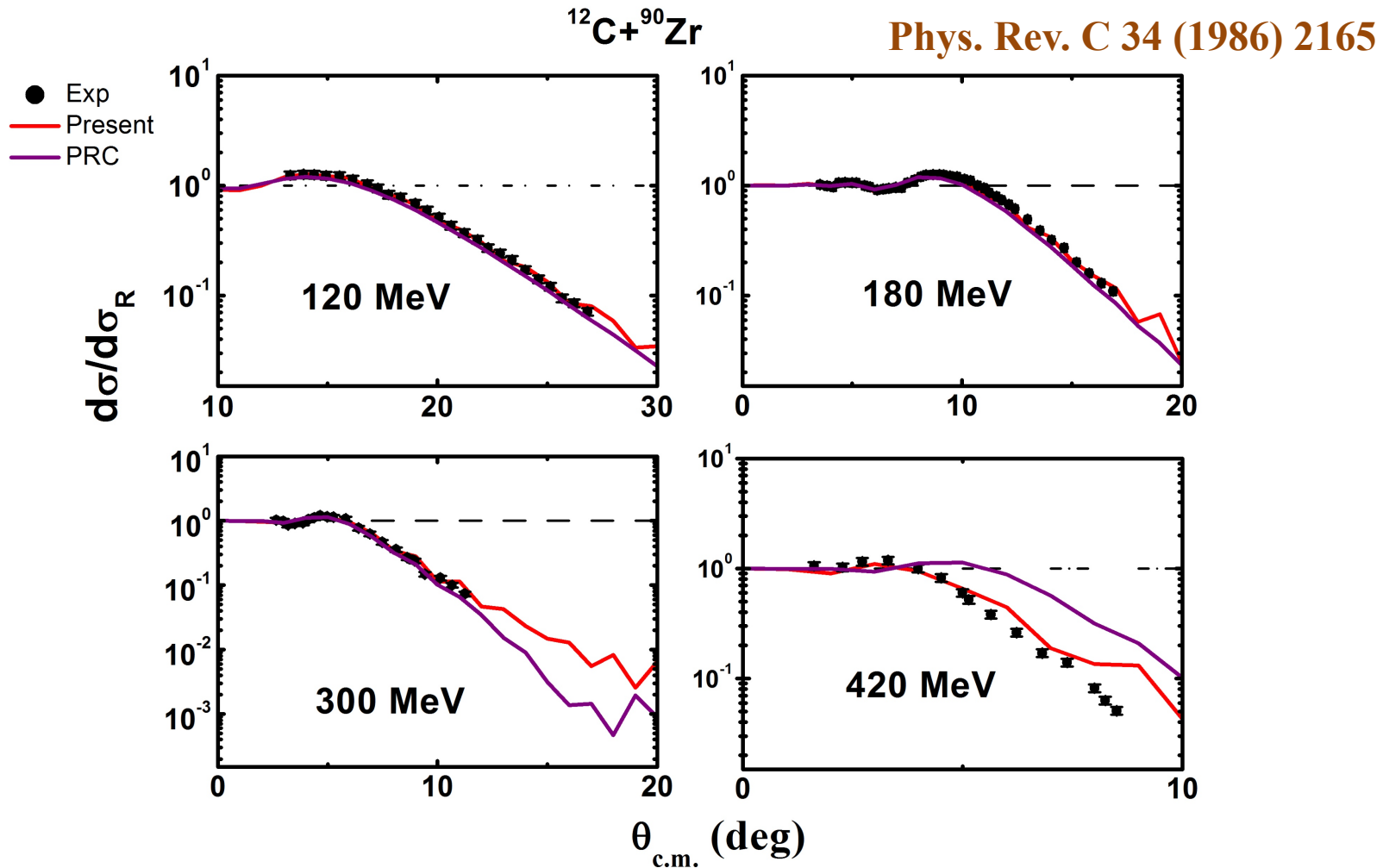
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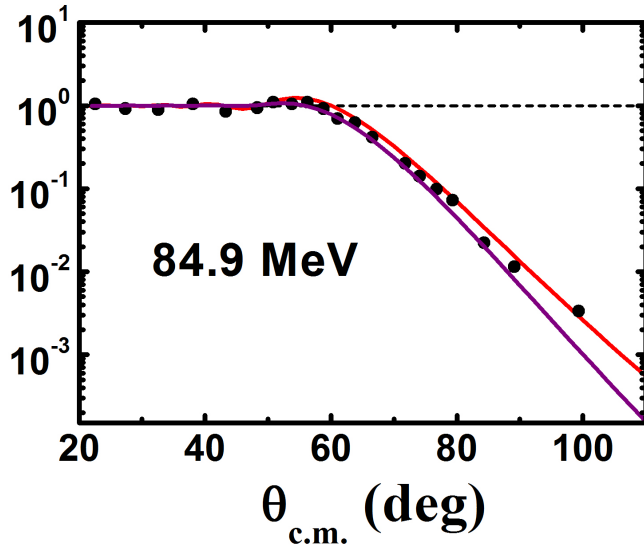
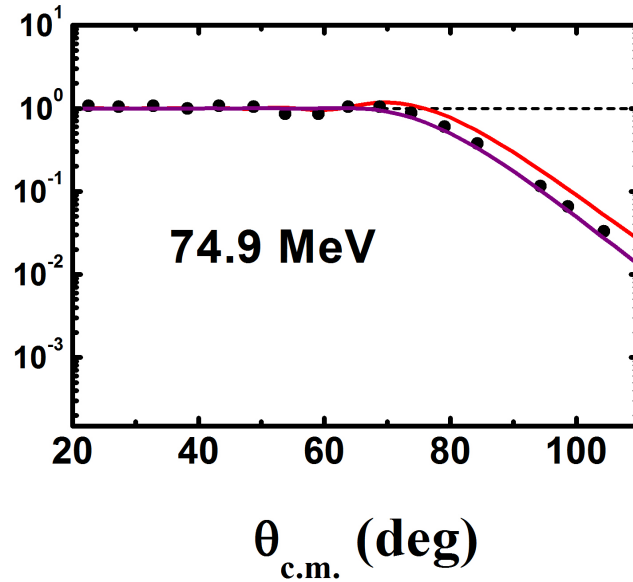
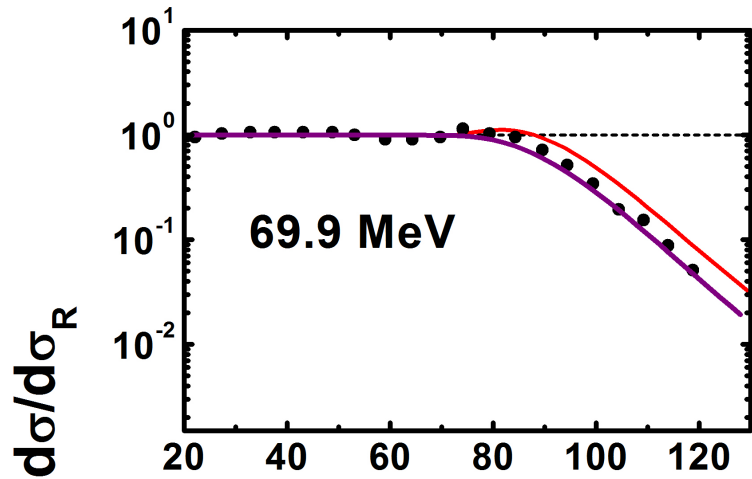
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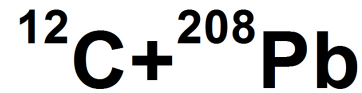
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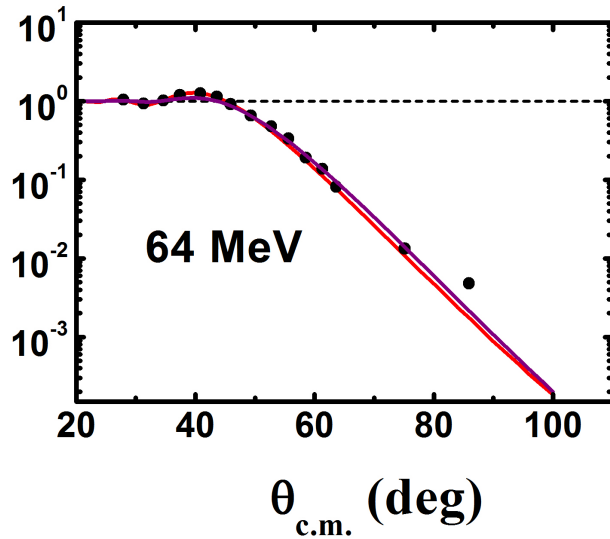
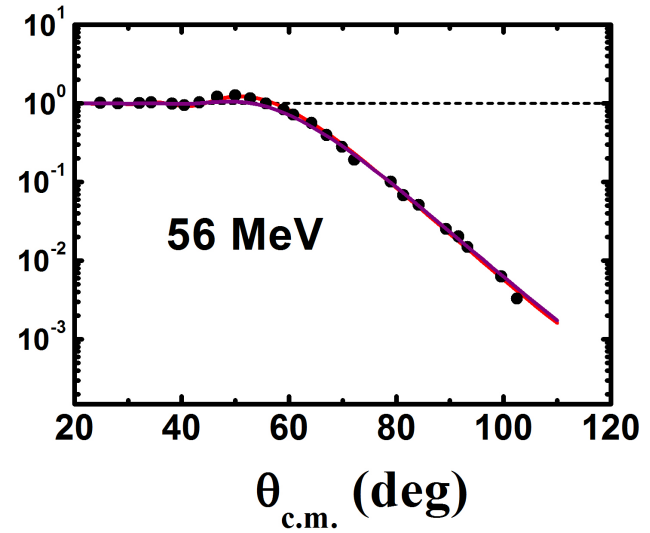
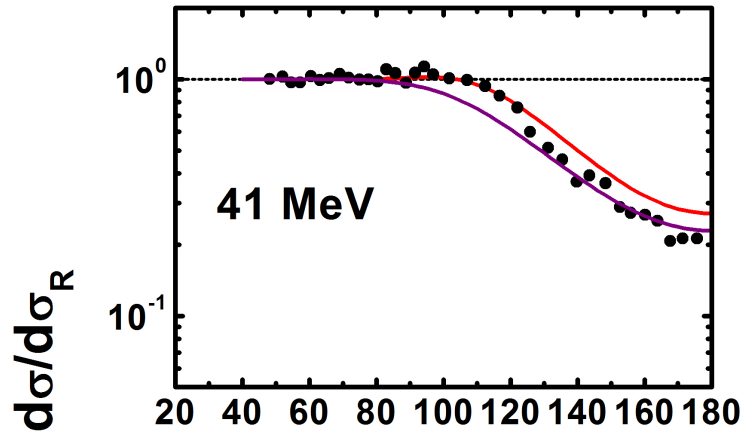


● Exp
— Present
— PRC

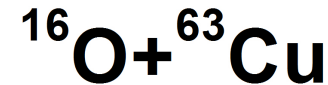


Phys. Rev. C 87 (2013) 044605

• Verification

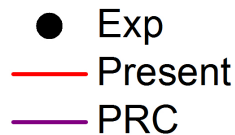
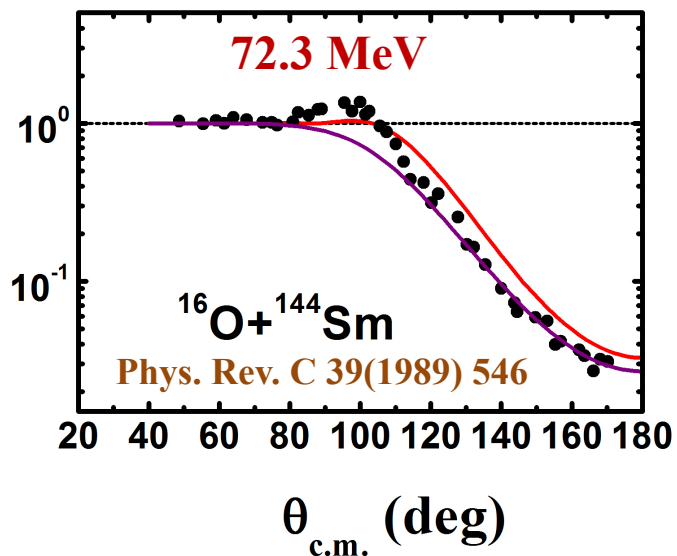
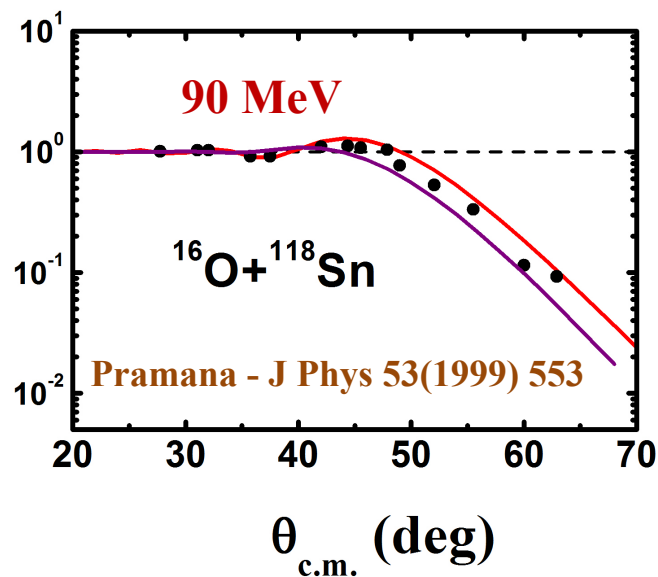
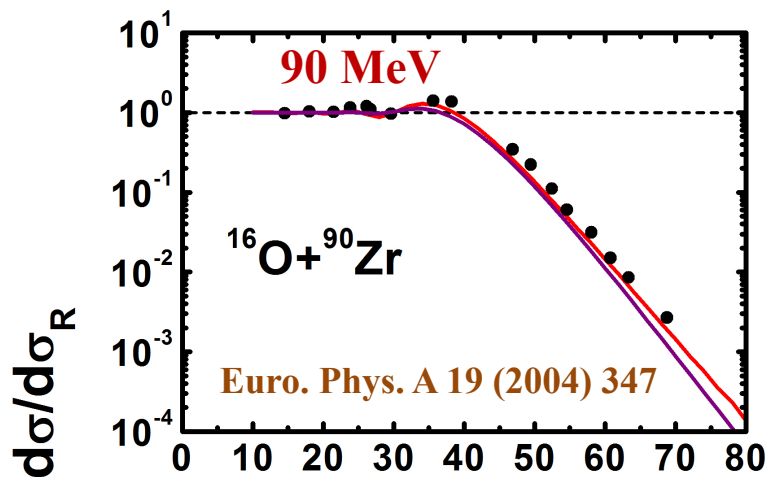


● Exp
— Present
— PRC



Phys. Rev. C 50 (1994) 3033

• Verification



Summary

- Woods-Saxon parameters for reactions induced by ^{12}C were obtained, and the formulas were summarized.
- The formulas can reproduce a lot of ^{12}C and $^{16}\text{O}+$ heavy ions' experimental data.
- More data will be introduced to test the applicability of the formulas in the future.

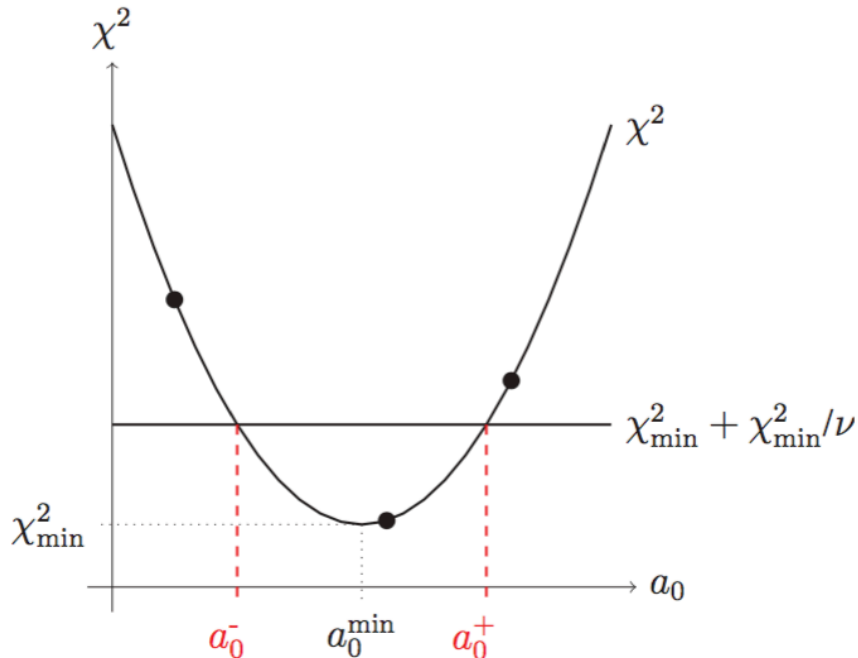
THANKS

• Uncertainty of a_{ν}

$$\hat{\chi}^2 = \chi_{\min}^2 + \frac{\chi_{\min}^2}{\nu}, \quad (6)$$

was calculated, where ν denotes the number of degrees of freedom. The intersection of $\hat{\chi}^2$ with the χ^2 envelope gives the two values a_0^-, a_0^+ , as shown in Fig. 5, resulting in an error

$$\Delta a_0 = \frac{a_0^+ - a_0^-}{2}.$$



Phys. Rev. C 78, 034614 (2008)

ν denotes the number of degrees of freedom.

- E_C : Columb correction

PHYSICAL REVIEW C 79, 024615 (2009)

PHYSICAL REVIEW C 94, 014619 (2016)

where E_C is the Coulomb correction to the incident energy [5,8,15]:

$$E_C = \frac{6Z_P Z_T e^2}{5R_C}, \quad (4)$$