

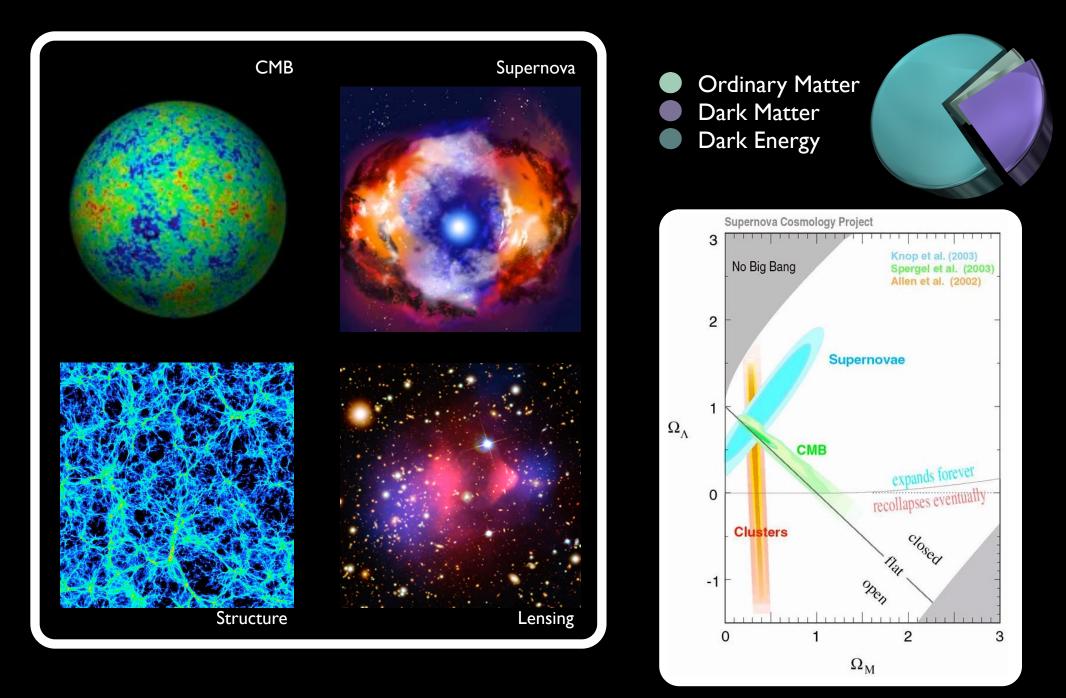
EFTs for Dark Matter

Tim M.P. Tait University of California, Irvine

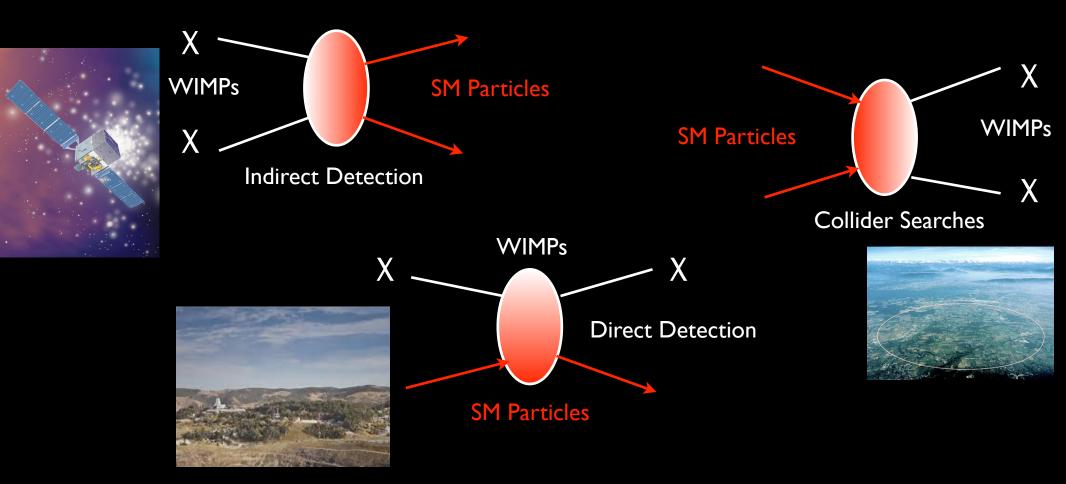


HEFT 2015 Chicago November 4, 2015

Dark Matter



Particle Probes of DM



• The common feature of particle searches for WIMPs is that all of them are determined by how WIMPs interact with the Standard Model.

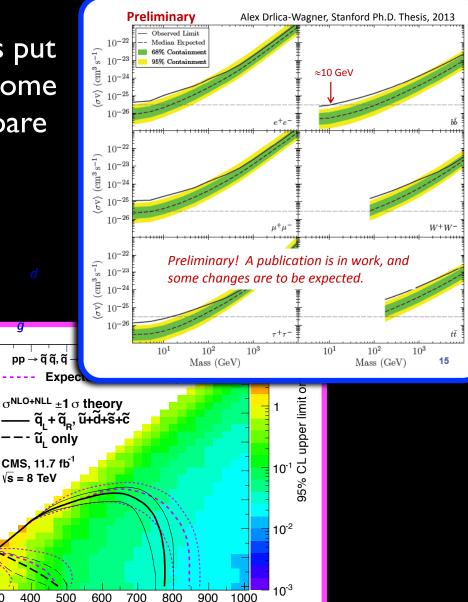
We Need (a) Theory

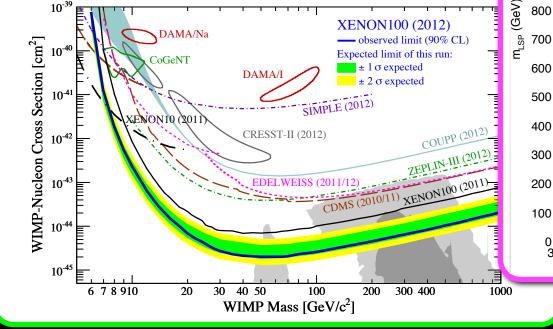
300

400

Individually, dark matter searches of all kinds put limits on different cross sections. Without some kind of theoretical structure, we can't compare them.

> But we know they are all attempts to characterize the same thing(s).

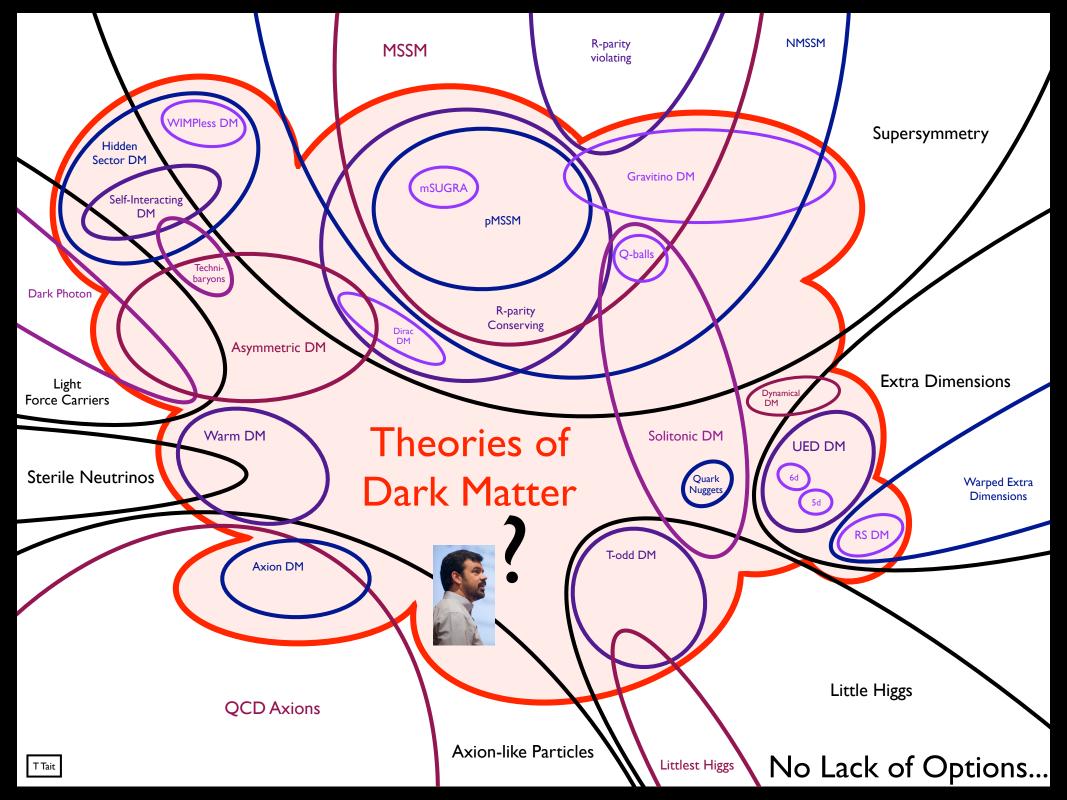


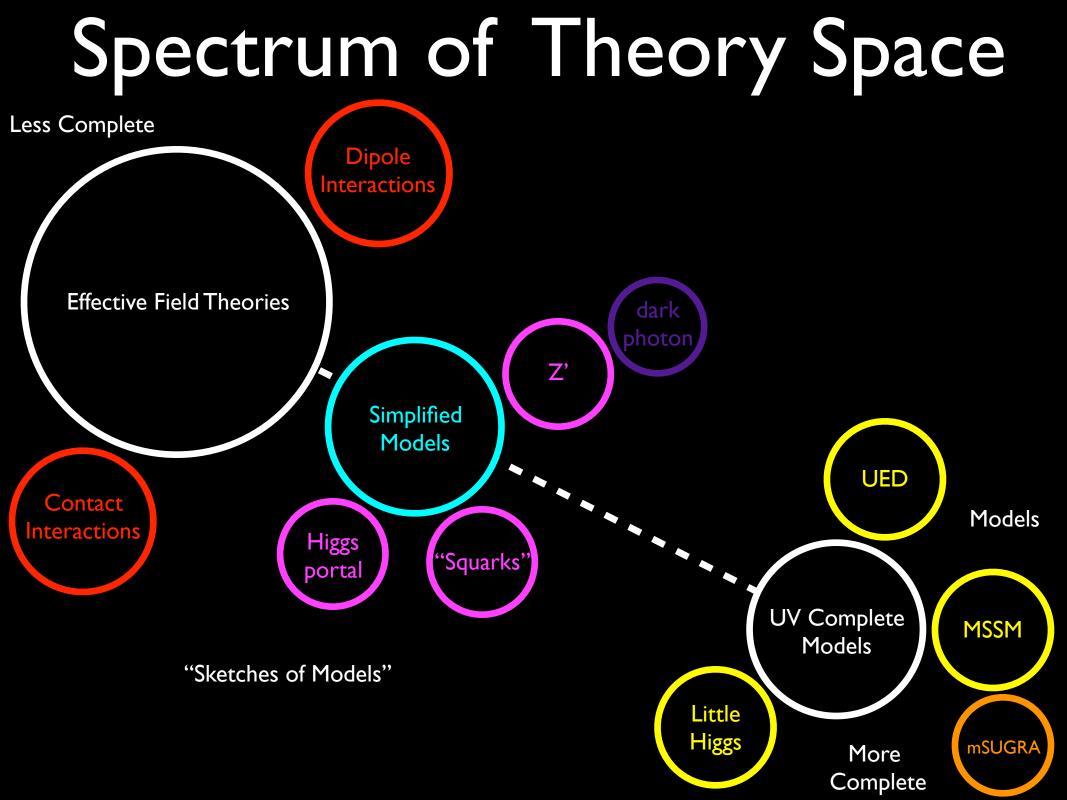


10⁻³⁹

Which theory to use?

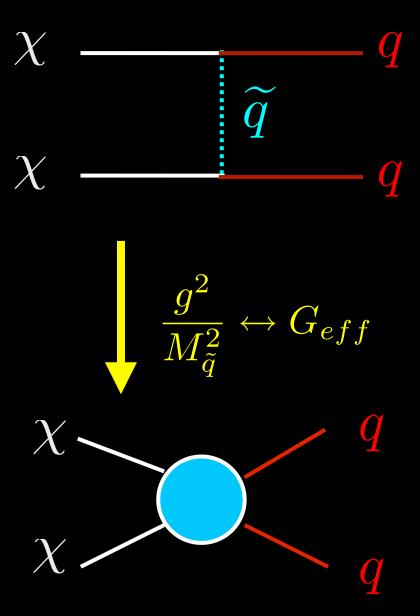
m_{squark} (GeV)





Contact Interactions

- On the "simple" end of the spectrum are theories where the dark matter is the only χ state accessible to our experiments.
- This is a natural place to start, since effective field theory tells us that many theories will show common low energy behavior when the mediating particles are heavy compared to the energies involved.
- The drawback to a less complete theory is such a simplified description will undoubtably miss out on correlations between quantities which are obvious in a complete theory.
- And it will fail to describe high energies, where one can produce more of the new particles directly.



- As an example, we can write down the operators of interest for a Majorana WIMP.
- There are 10 leading operators consistent with Lorentz and SU(3) x U(1)_{EM} gauge invariance coupling the WIMP to quarks and gluons.
- Each operator has a (separate) coefficient M* which parametrizes its strength.
- In principle, a realistic UV theory will turn on some combination of them, with related coefficients.

Goodman, Ibe, Rajaraman, Shepherd, TMPT, Yu 1005.1286 & PLB

Namo	Turno	C	Γ^{χ}	Γ^q
Name	Type	G_{χ}		1
M1	qq	$m_q/2M_*^3$	1	1
M2	qq	$im_q/2M_*^3$	γ_5	1
M3	qq	$im_q/2M_*^3$	1	γ_5
M4	qq	$m_q/2M_*^3$	γ_5	γ_5
M5	qq	$1/2M_{*}^{2}$	$\gamma_5\gamma_\mu$	γ^{μ}
M6	qq	$1/2M_{*}^{2}$	$\gamma_5\gamma_\mu$	$\gamma_5\gamma^\mu$
M7	GG	$\alpha_s/8M_*^3$	1	-
M8	GG	$i\alpha_s/8M_*^3$	γ_5	-
M9	$G\tilde{G}$	$\alpha_s/8M_*^3$	1	-
M10	$G\tilde{G}$	$i\alpha_s/8M_*^3$	γ_5	-

 $G_{\chi} \left[\bar{\chi} \Gamma^{\chi} \chi \right] G^{2}$ $\sum_{q} G_{\chi} \left[\bar{q} \Gamma^{q} q \right] \left[\bar{\chi} \Gamma^{\chi} \chi \right]$

Other operators may be rewritten in this form by using Fierz transformations.

- The various types of interactions are accessible to different kinds of experiments. (Technically meaning: the observables are unsuppressed by the small dark matter velocity in our halo, v ~ 10⁻³.
 - Spin-independent elastic scattering
 - Spin-dependent elastic scattering
 - Annihilation in the galactic halo
 - Collider Production

Goodman, Ibe, Rajaraman, Shepherd, TMPT, Yu 1005.1286 & PLB

Name	Type	G_{χ}	Γ^{χ}	Γ^q
M1	qq	$m_q/2M_*^3$	1	1
M2	qq	$im_q/2M_*^3$	γ_5	1
M3	qq	$im_q/2M_*^3$	1	γ_5
M4	qq	$m_q/2M_*^3$	γ_5	γ_5
M5	qq	$1/2M_{*}^{2}$	$\gamma_5\gamma_\mu$	γ^{μ}
M6	qq	$1/2M_{*}^{2}$	$\gamma_5\gamma_\mu$	$\gamma_5\gamma^\mu$
M7	GG	$\alpha_s/8M_*^3$	1	-
M8	GG	$i\alpha_s/8M_*^3$	γ_5	-
M9	$G\tilde{G}$	$\alpha_s/8M_*^3$	1	-
M10	$G\tilde{G}$	$i\alpha_s/8M_*^3$	γ_5	-

 $G_{\chi} \left[\bar{\chi} \Gamma^{\chi} \chi \right] G^{2}$ $\sum_{\bar{u}} G_{\chi} \left[\bar{q} \Gamma^{q} q \right] \left[\bar{\chi} \Gamma^{\chi} \chi \right]$

Other operators may be rewritten in this form by using Fierz transformations.

- The various types of interactions are accessible to different kinds of experiments. (Technically meaning: the observables are unsuppressed by the small dark matter velocity in our halo, v ~ 10⁻³.
 - Spin-independent elastic
 scattering
 - Spin-dependent elastic scattering
 - Annihilation in the galactic halo
 - Collider Production

Goodman, Ibe, Rajaraman, Shepherd, TMPT, Yu 1005.1286 & PLB

Name	Type	G_{χ}	Γ^{χ}	Γ^q
M 1	qq	$m_q/2M_*^3$	1	1
M2	qq	$im_q/2M_*^3$	γ_5	1
M3	qq	$im_q/2M_*^3$	1	γ_5
M4	qq	$m_q/2M_*^3$	γ_5	γ_5
M5	qq	$1/2M_{*}^{2}$	$\gamma_5\gamma_\mu$	γ^{μ}
M6	qq	$1/2M_{*}^{2}$	$\gamma_5\gamma_\mu$	$\gamma_5\gamma^\mu$
ightarrowM7	GG	$\alpha_s/8M_*^3$	1	-
M8	GG	$i\alpha_s/8M_*^3$	γ_5	-
M9	$G\tilde{G}$	$\alpha_s/8M_*^3$	1	_
M10	$G\tilde{G}$	$i\alpha_s/8M_*^3$	γ_5	_

 $G_{\chi} \left[\bar{\chi} \Gamma^{\chi} \chi \right] G^{2}$ $\sum_{\alpha} G_{\chi} \left[\bar{q} \Gamma^{q} q \right] \left[\bar{\chi} \Gamma^{\chi} \chi \right]$

Other operators may be rewritten in this form by using Fierz transformations.

- The various types of interactions are accessible to different kinds of experiments. (Technically meaning: the observables are unsuppressed by the small dark matter velocity in our halo, v ~ 10⁻³.
 - Spin-independent elastic scattering
 - Spin-dependent elastic scattering
 - Annihilation in the galactic halo
 - Collider Production

Goodman, Ibe, Rajaraman, Shepherd, TMPT, Yu 1005.1286 & PLB

	Name	Type	G_{χ}	Γ^{χ}	Γ^q
	M 1	qq	$m_q/2M_*^3$	1	1
	M2	qq	$im_q/2M_*^3$	γ_5	1
	M3	qq	$im_q/2M_*^3$	1	γ_5
	M4	qq	$m_q/2M_*^3$	γ_5	γ_5
	M5	qq	$1/2M_{*}^{2}$	$\gamma_5\gamma_\mu$	γ^{μ}
	M6	qq	$1/2M_{*}^{2}$	$\gamma_5\gamma_\mu$	$\gamma_5\gamma^\mu$
1	$\sim M7$	GG	$\alpha_s/8M_*^3$	1	-
	M 8	GG	$i\alpha_s/8M_*^3$	γ_5	-
	M9	$G\tilde{G}$	$\alpha_s/8M_*^3$	1	-
	M 10	$G\tilde{G}$	$i\alpha_s/8M_*^3$	γ_5	-

 $G_{\chi} \left[\bar{\chi} \Gamma^{\chi} \chi \right] G^{2}$ $\sum G_{\chi} \left[\bar{q} \Gamma^{q} q \right] \left[\bar{\chi} \Gamma^{\chi} \chi \right]$

Other operators may be rewritten in this form by using Fierz transformations.

- The various types of interactions are accessible to different kinds of experiments. (Technically meaning: the observables are unsuppressed by the small dark matter velocity in our halo, v ~ 10⁻³.
 - Spin-independent elastic
 scattering
 - Spin-dependent elastic scattering
 - Annihilation in the galactic halo
 - Collider Production

Goodman, Ibe, Rajaraman, Shepherd, TMPT, Yu 1005.1286 & PLB

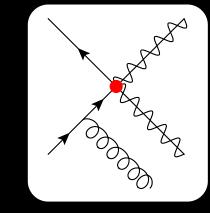
_					
	Name	Type	G_{χ}	Γ^{χ}	Γ^q
	M1	qq	$m_q/2M_*^3$	1	1
1	M2	qq	$im_q/2M_*^3$	γ_5	1
	M3	qq	$im_q/2M_*^3$	1	γ_5
	M4	qq	$m_q/2M_*^3$	γ_5	γ_5
	M5	qq	$1/2M_{*}^{2}$	$\gamma_5\gamma_\mu$	γ^{μ}
	M6	qq	$1/2M_{*}^{2}$	$\gamma_5\gamma_\mu$	$\gamma_5\gamma^\mu$
1	$^{\circ}$ M7	GG	$\alpha_s/8M_*^3$	1	-
	M 8	GG	$i\alpha_s/8M_*^3$	γ_5	-
1	M9	$G\tilde{G}$	$\alpha_s/8M_*^3$	1	_
-	M10	$G\tilde{G}$	$i\alpha_s/8M_*^3$	γ_5	-

 $G_{\chi} \left[\bar{\chi} \Gamma^{\chi} \chi \right] G^{2}$ $\sum G_{\chi} \left[\bar{q} \Gamma^{q} q \right] \left[\bar{\chi} \Gamma^{\chi} \chi \right]$

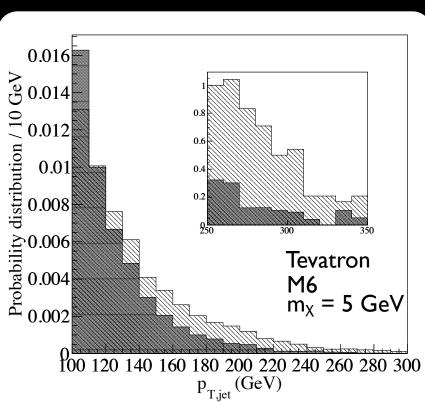
Other operators may be rewritten in this form by using Fierz transformations.

Collider Searches

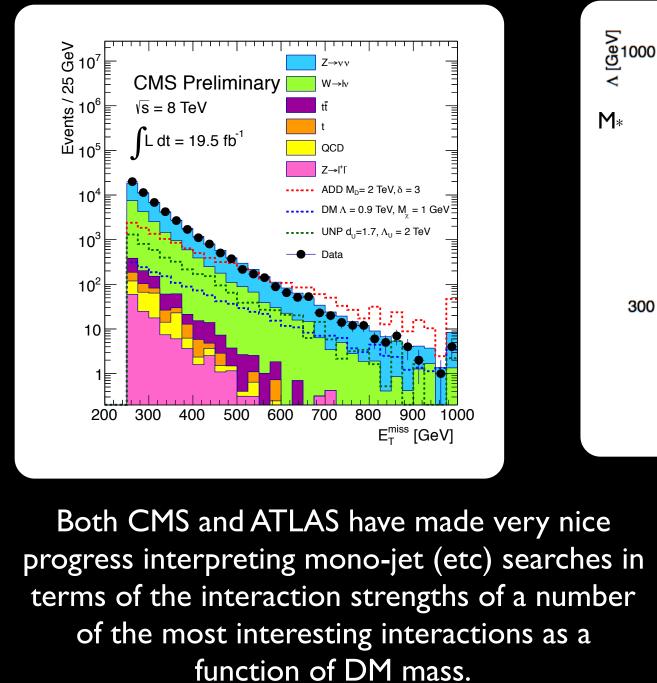
- At colliders, one searches for this type of theory by producing the dark matter directly.
- Since the detector needs something to trigger on, one looks for processes with additional final state particles, and infers the presence of dark matter based on the missing momentum it carries away from the interaction.
- There are the usual SM backgrounds from Z + jets, as well as fake backgrounds from QCD, etc.
- Contact interactions grow with energy, generically leading to a harder MET spectrum than the SM backgrounds.



Beltran, Hooper, Kolb, Krusberg, TMPT 1002.4137 & JHEP



Collider Results



CMS 2012 Vector CMS 2011 Vector 300 10^{2} 10 M, [GeV/c²] ∑ 80 1000 CMS Preliminary √s = 8 TeV dt = 19.5 fb CMS 2012 Axial Vecto CMS 2011 Axial Vector 10 10² 10[°] M, [GeV/c²]

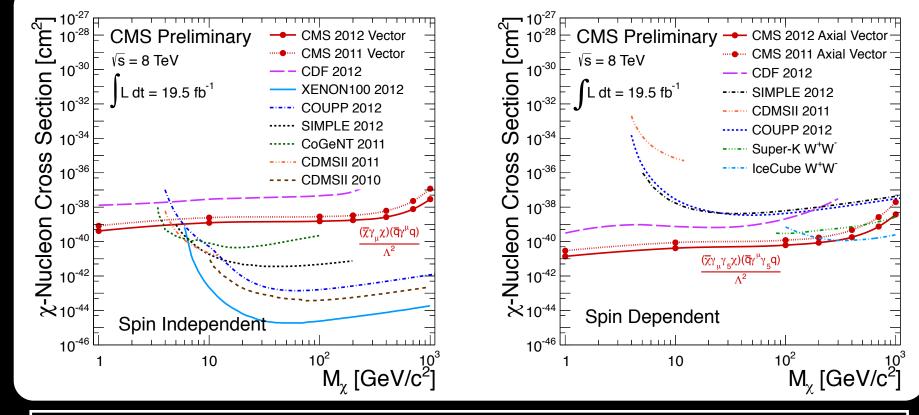
10³

CMS Preliminary

L dt = 19.5 fb⁻¹

√s = 8 TeV

Translation to Elastic Scattering

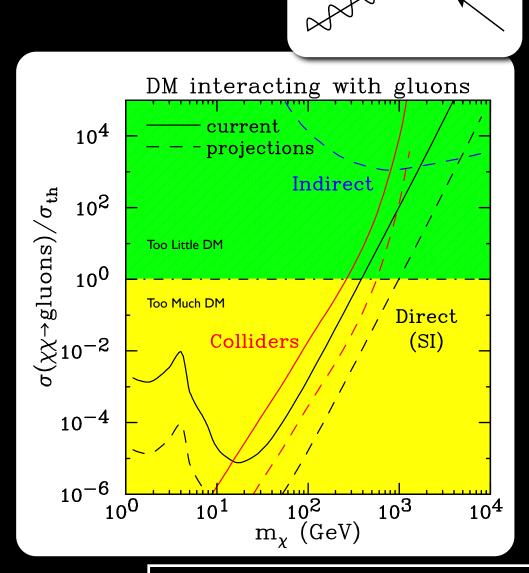


See: Goodman, Ibe, Rajaraman, Shepherd, TMPT, Yu 1005.1286 & PLB; Bai, Fox, Harnik 1005.3797 & JHEP; and lots of other papers..

- Colliders can help fill in a challenging region of low dark matter mass and spin-dependent interactions.
- Since they see individual partons, rather than the nucleus coherently, collider results offer a complementary perspective on DM interactions with hadrons.
- The translation assumes a heavy mediating particle (contact interaction).

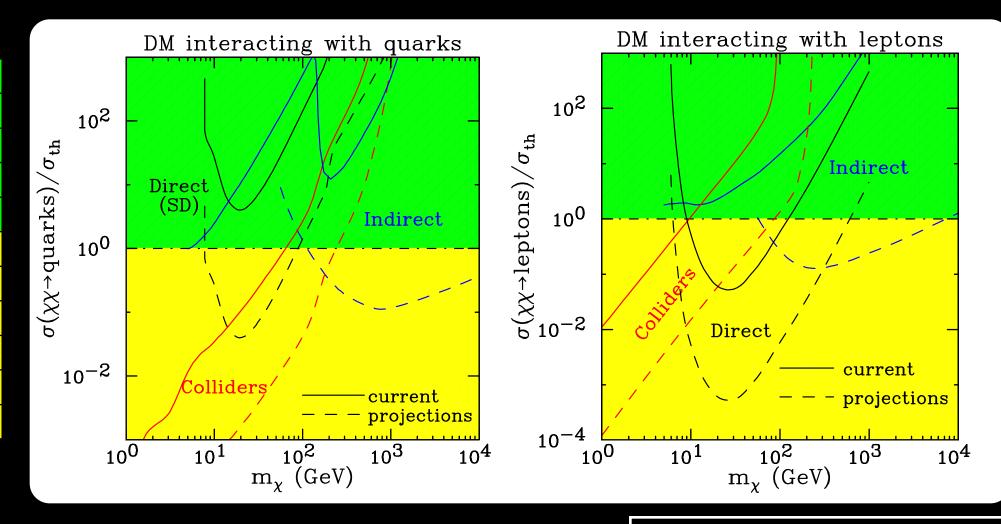
Annihilation

- We can also map interactions into predictions for WIMPs annihilating.
- For example, into continuum photons from a given tree level final state involving quarks/gluons.
- This allows us to consider bounds from indirect detection, and with assumptions, maps onto a thermal relic density.
- Colliders continue to do better for lighter WIMPs or p-wave annihilations whereas indirect detection is more sensitive to heavy WIMPs.



DM Complementarity, arXiv:1305.1605

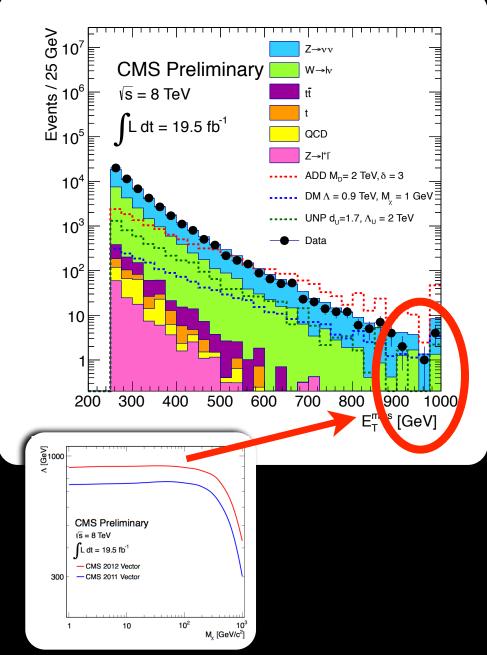
Quarks & Leptons



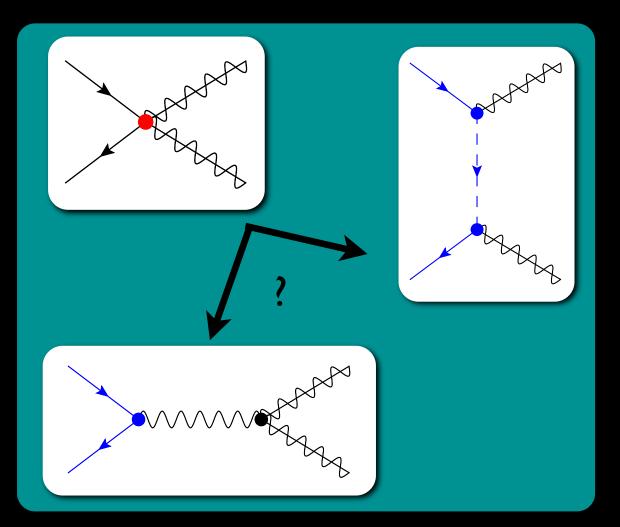
DM Complementarity, arXiv: 1305.1605

How Effective a Theory?

- We should worry a little bit about whether what we are doing makes sense.
- The bounds on the scale of the contact interaction are ~ I TeV, and we know that LHC collisions are capable of producing higher energies.
- For the highest energy events, we might be using the wrong theory description.
- It is difficult to be quantitative about precisely where the EFT breaks down, because the energies probed by the LHC depend on the parton distribution functions. [The answer is time-dependent in that sense.]

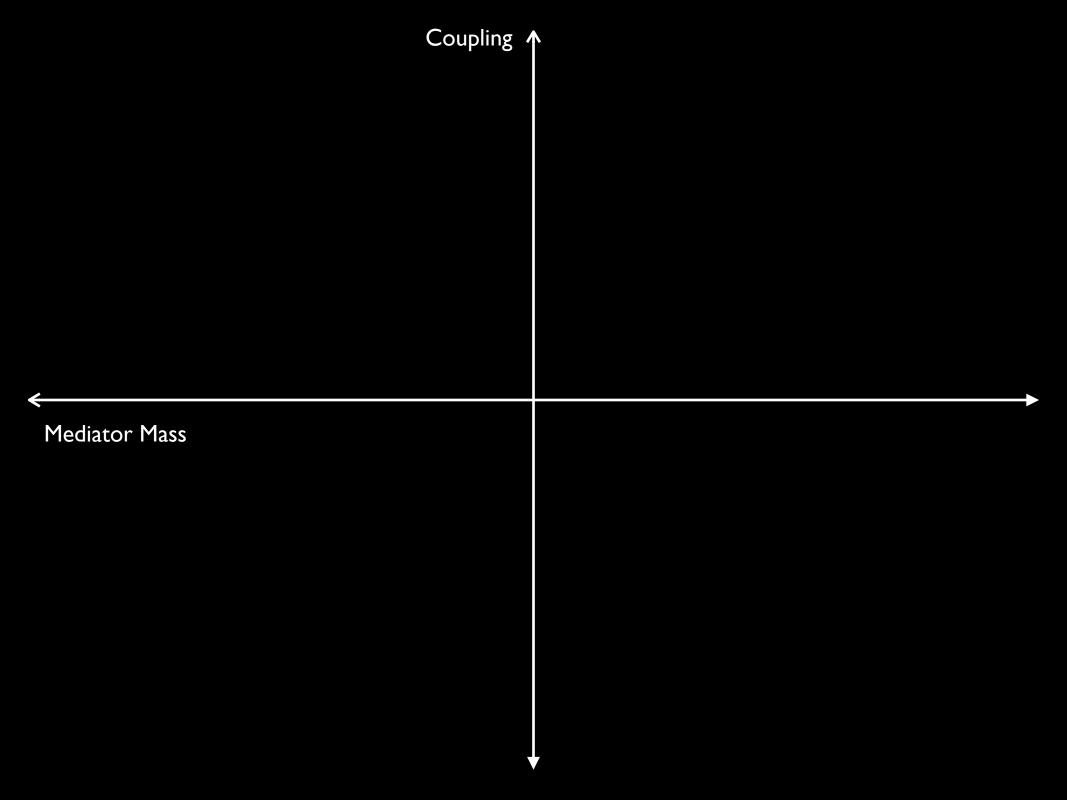


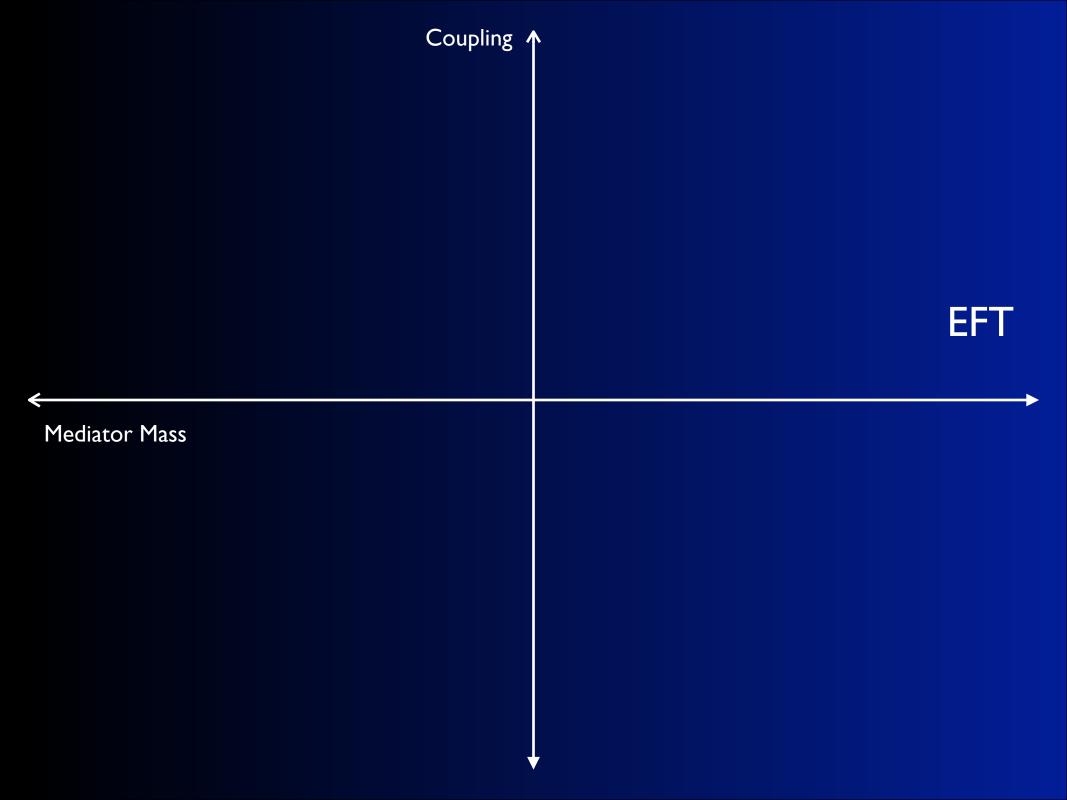
Simplified Models?

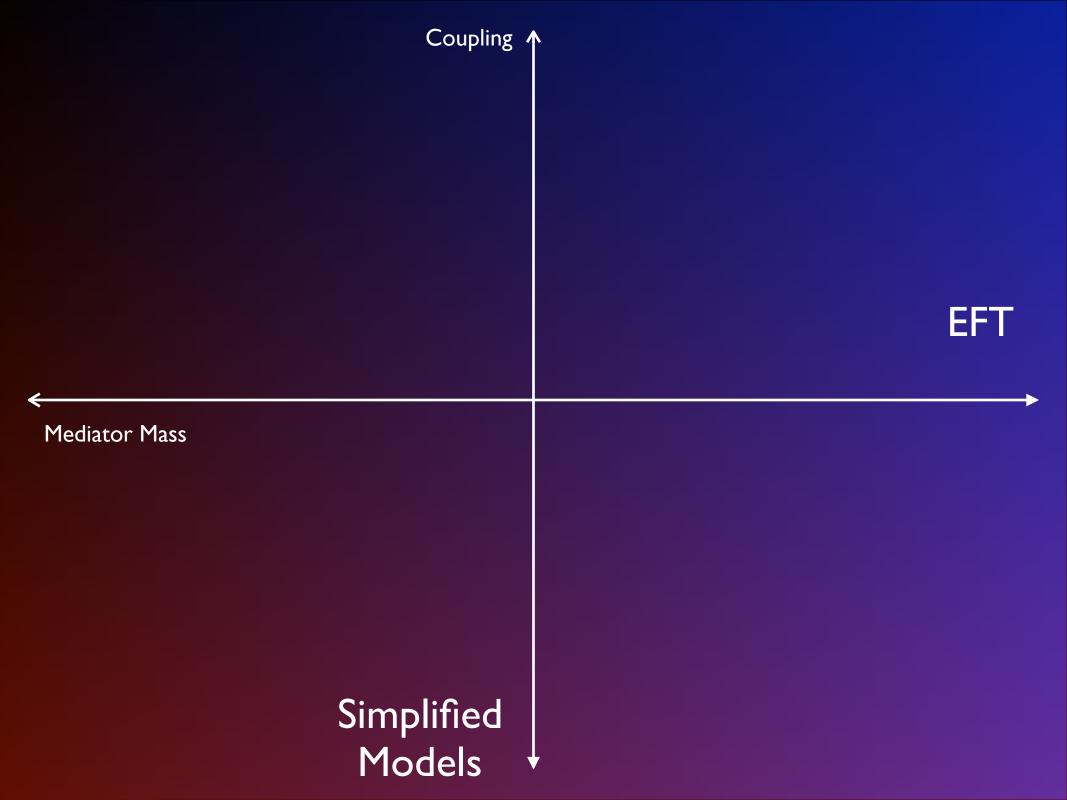


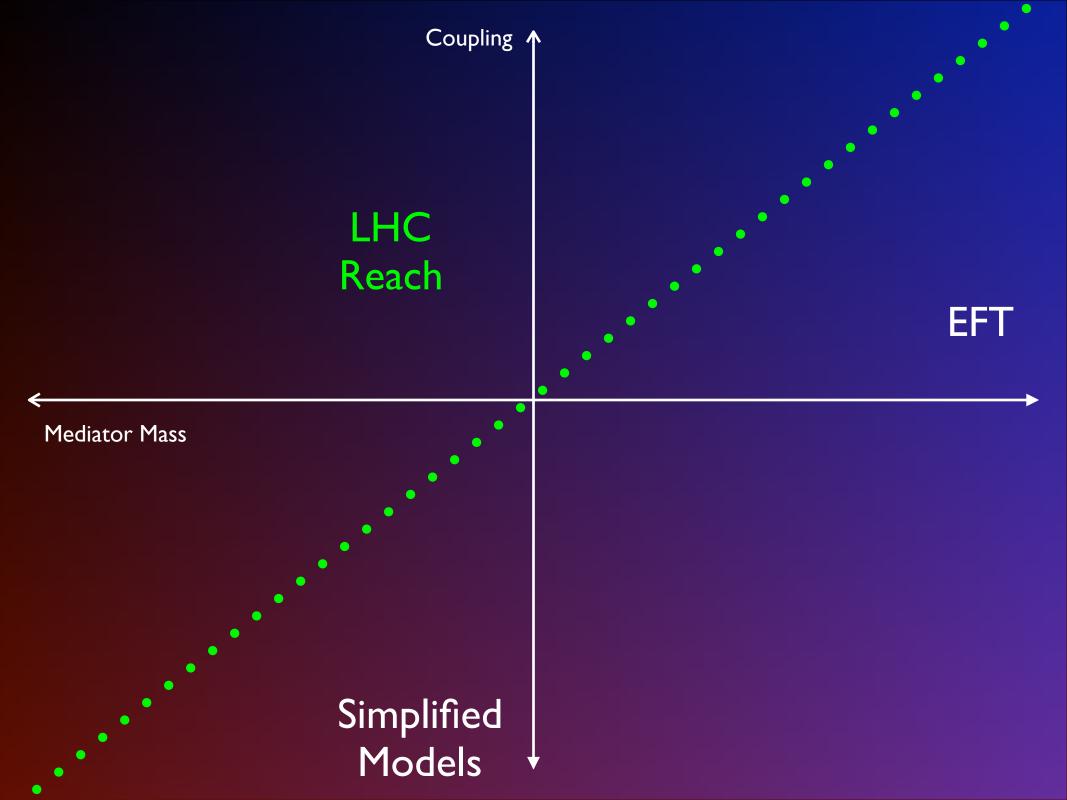
"s-channel" mediators are not protected by the WIMP stabilization symmetry. They can couple to SM particles directly, and their masses can be larger or smaller than the WIMP mass itself. "t-channel" mediators are protected by the WIMP stabilization symmetry. They must couple at least one WIMP as well as some number of SM particles. Their masses are greater than the WIMP mass (or else the WIMP would just decay into them).

One strategy is to try to write down some theories with mediators explicitly included.









At this point, one typically hears a lot of fuzzy, qualitative, and often just plain absurd statements, such as:

I. "The effective field theory doesn't work at the LHC"

At this point, one typically hears a lot of fuzzy, qualitative, and often just plain absurd statements, such as:

- I. "The effective field theory doesn't work at the LHC"
- 2. "The higher energies of Run II will cause the EFT to break down."

At this point, one typically hears a lot of fuzzy, qualitative, and often just plain absurd statements, such as:

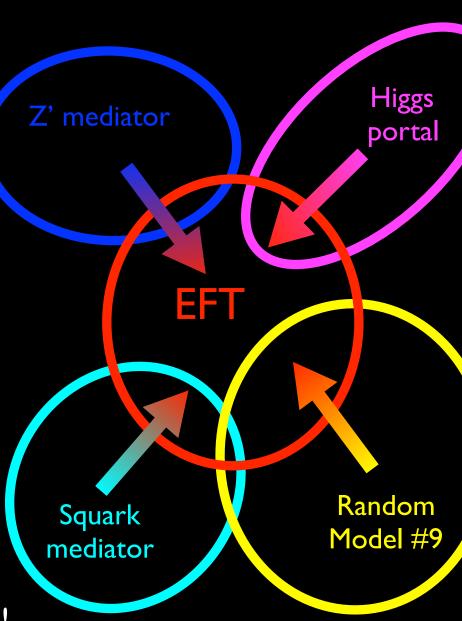
- I. "The effective field theory doesn't work at the LHC"
- 2. "The higher energies of Run II will cause the EFT to break down."
- 3. "The parameter space of the EFT is already ruled out."

At this point, one typically hears a lot of fuzzy, qualitative, and often just plain absurd statements, such as:

- I. "The effective field theory doesn't work at the LHC"
- 2. "The higher energies of Run II will cause the EFT to break down."
- 3. "The parameter space of the EFT is already ruled out."
- 4. "The early work on EFTs has brain-washed people."

I. "EFT Doesn't Work at LHC"

- A lot of the discussion is driven by conflation of a particular simplified model with the EFT itself.
 - This is inspired to some extent by the fact that the EFT is the universal large mass limit of any simplified model.
 - One should remember that the EFT is a superset of a limit of all simplified models: any one of them does not typically characterize all of them.
 - It is logistically impossible to rule out application of the EFT *in general* based on one *specific* model.
 - Instead, this reminds us that the EFT cannot itself describe all the possibilities!



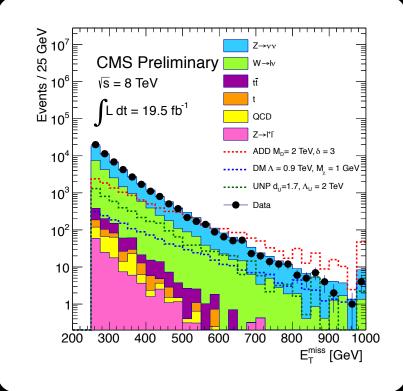
I. "EFT Doesn't Work at LHC"

- So what can we learn from the EFT itself?
- The EFT is an expansion in energy: E / M*.
 - If E is too large, loop contributions to the observables will contribute as much as the tree level, and the theory ceases to be predictive.
 - Where that happens for fixed M* is somewhere around:

 $E \gtrsim 4\pi M_*$

(We can argue about whether this should be 4π or 2π or some other number. One is as indefensible as another.)

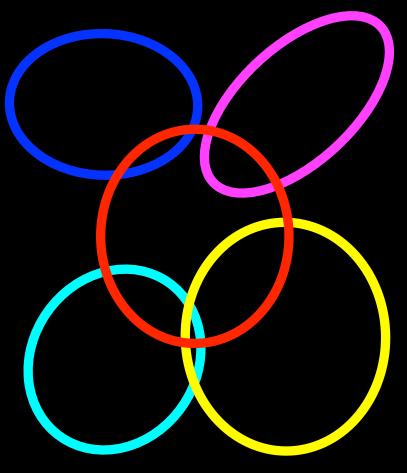
 For the Run I limits of M* ~ I TeV, this forbids us from using events with energies larger than about 10 TeV.



Not a big problem at Run I... (even in the limit $4\pi \rightarrow 1!$)

2. "EFT Doesn't Work at Run 2"

- Uhh... Again:
 - One single simplified model cannot rule out the applicability of the EFT in general.
 - The EFT itself breaks down for energies much higher than the interaction scale M*.
- Run II projections are for bounds on M* which are around 2-3 TeV. (Obviously this involves things like the fake MET rate, so mileage may vary).
- If you believe the mediator must have a mass less than a few TeV and/or very small couplings, the EFT won't describe it.
- If you think it could be heavier, it might.

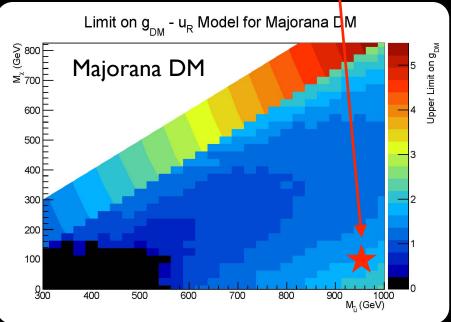


3."The EFT Describes Models Which are Already Ruled Out"

- It's true that for any given simplified model, one may find that the LHC limits apply for large couplings and widths.
 - Watch for hidden assumptions like setting couplings equal which needn't be.
- Sometimes other searches give better limits.
- For example, a Z' mediator with large coupling to light quarks can be bounded by dijet resonance searches.
- In general, one can find regions of parameter space where the EFT is a good description of weakly-ish coupled models with heavy-ish mediators.

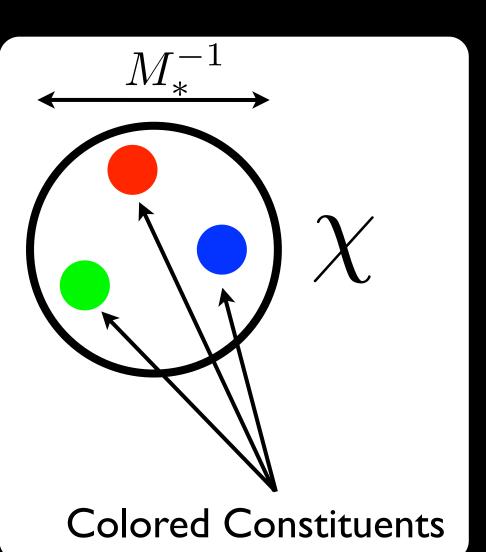
Direct searches for the mediator are actually somewhat weaker than mono-jet bounds here.

DiFranzo, Nagao, Rajaraman, TMPT arXiv: I 308.2679



A Composite WIMP?

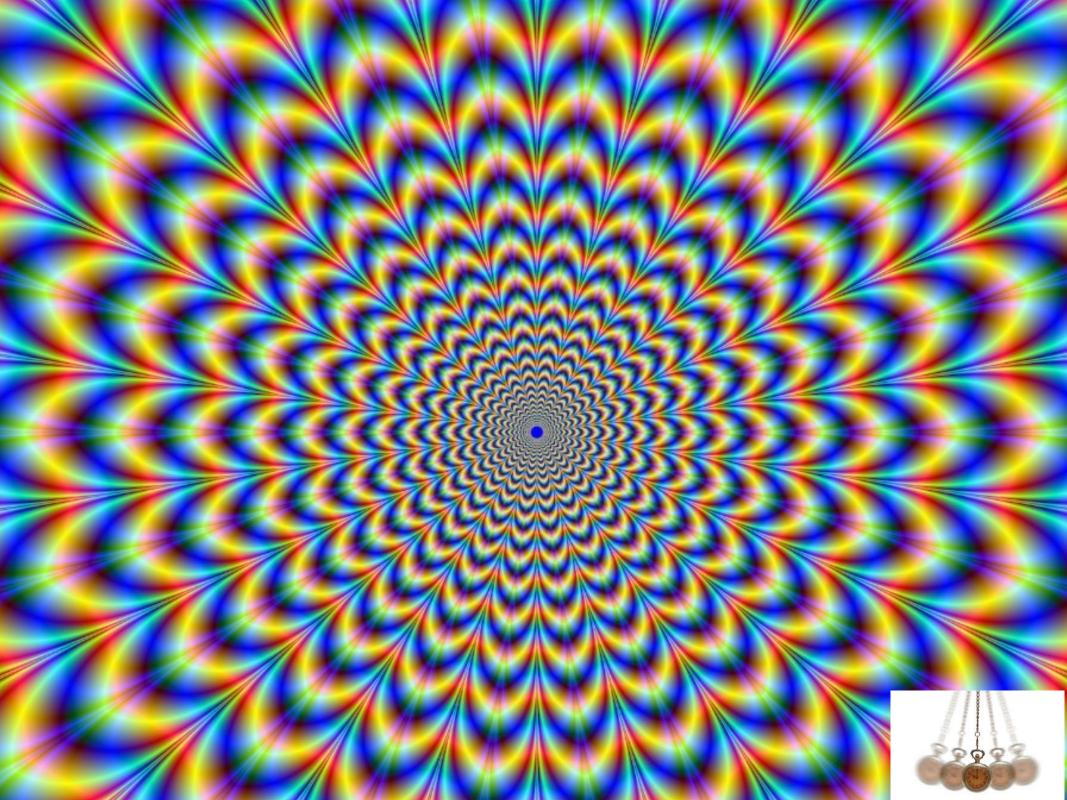
 \bigcirc



- There are cases where an EFT still says something even when there is no perturbative simplified model that can describe the physics.
- If the dark matter is a (neutral) confined bound state (confined by some dark gauge force, say) of colored constituents, we should expect its coupling to quarks and gluons to be represented by higher dimensional operators whose strength is characterized by the new confinement scale.
- Bounds on EFTs constrain the dark confinement scale -- the "radius" of the dark matter.

4. "The EFT has brain-washed people."

- I actually don't have any evidence that this is not true.
- Let's settle it once and for all experimentally:

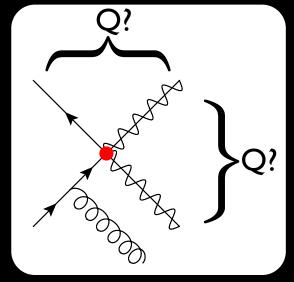


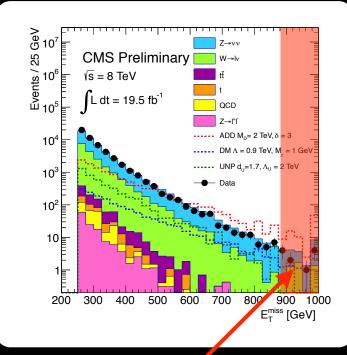
4. "The EFT has brain-washed people."

- I actually don't have any evidence that this is not true.
- Let's settle it once and for all experimentally:
 - None of you are currently clucking like a chicken, so I think it is safe to declare this particular experiment a failure.

Truncation

- A good idea which I think Andrea will shortly describe in some detail is to present EFT bounds using "truncation".
- The idea is to exclude the events with the largest momentum transfer from the bound, since they are the most likely to be badly modeled by the EFT.
- If one imagines a simple t-channel or s-channel model, two different quantities ("Q") characterize the momentum through the implicit propagator.
 - The EFT can't tell you which one to use.
 - (Neither really can be measured anyway).
- Events with Q larger than some cut value Q_{cut} are excluded from the analysis bounding M*.

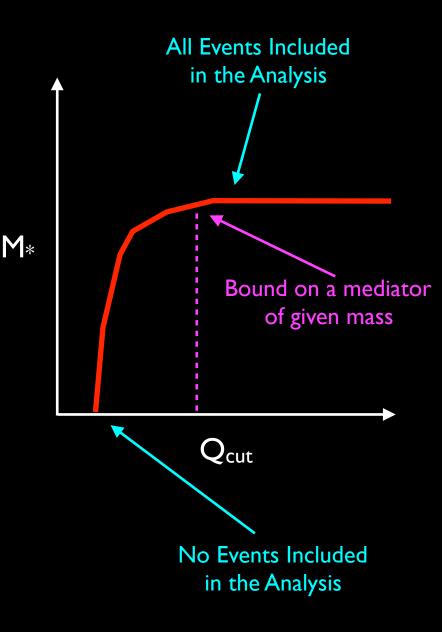




Exclude these Events for $Q_{cut} = 900$ GeV.

Truncation

- Probably the most useful way to present results would be to show the resulting bound on M* as a function of Q_{cut}.
- That way, the end user can decide (based on the masses of the particles in her theory) what value of Q_{cut} is appropriate, and find the conservative limit on her model.
- (And of course dedicated searches for mediators will be important, too).
- This the final recommendation made by the "ATLAS/CMS Dark Matter Forum", 1507.00966 for presenting the results in terms of EFT parameterizations.



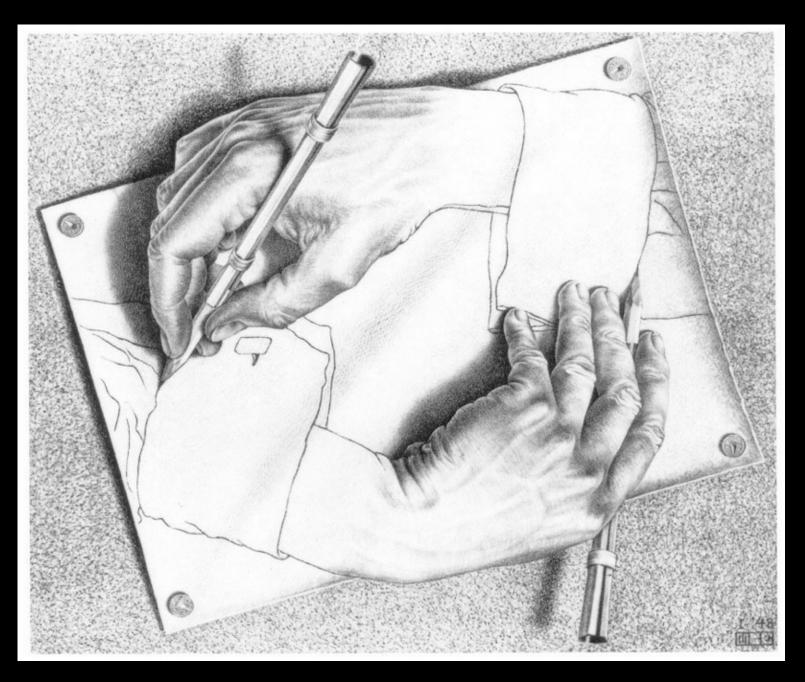
Outlook

- EFTs have been used to describe dark matter interactions. They sometimes provide a convenient framework and have offered some insights into how different kinds of searches fit together.
- There is a fair amount of confusion related to the fact that they break down at large energies.
 - If we're interested in a particular simplified model, we should study that model and forget about the EFT.
 - The EFT remains useful for the rest, including ones we didn't think of.
- Higgs physics successfully uses EFTs to describe both its coupling to gluons and to parameterize physics beyond the Standard Model.
- A lot of this currently is (rightly) focused on Higgs decays, for which the expansion parameter is m_h / M_{*}.
- But as data increases, it will be tempting to turn to high energy processes, as often these have a larger lever arm to constrain new physics.

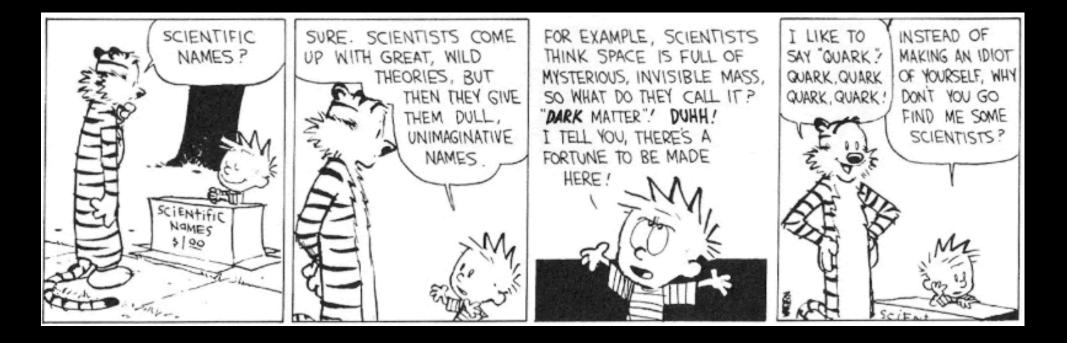
Outlook

- All of the complaints/criticisms (valid and not) of the DM results are likely to come up for Higgs analysis at that point.
- In that regime, some of the experience from dark matter will hopefully be useful:
 - When new particles are light, simplified models can help describe regions that are pathological from the EFT standpoint.
 e.g. Brehmer, Freitas, Lopez-Val, Plehn 1510.03443
 - EFT results can be presented in such a way that the user can make the most of them, via truncation or some other sliding analysis cut.
 - From my experience, it would be useful to "get ahead of the curve" and cultivate a useful way to think of the EFT results before you are forced to rant and rave the way I am today.
- EFTs are powerful tools and Higgs physics is a beautiful place to make use of them!

From Sketch to Life



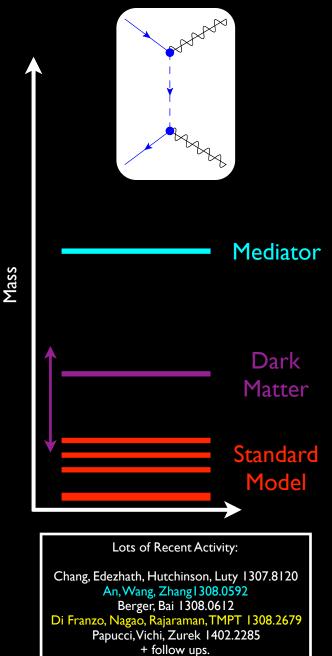
Sketches of <u>....</u>



Bonus Material

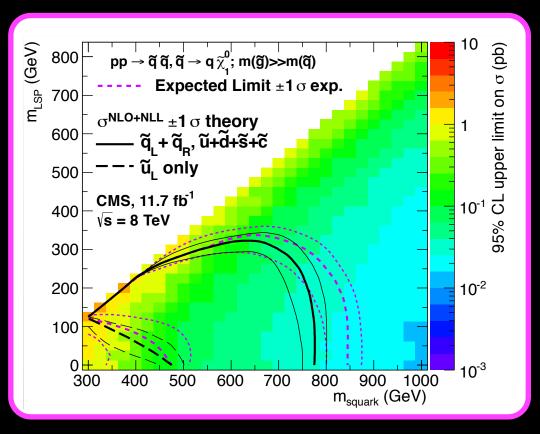
Simplified Model

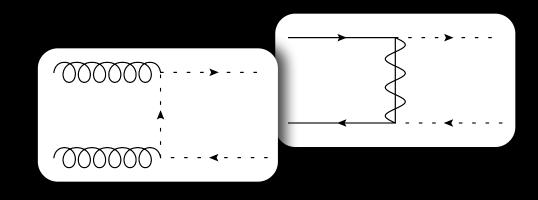
- Moving toward a more complete theory, we can also consider a model containing the dark matter as well as the most important particle mediating its interaction with the Standard Model.
- For example, if we are interesting in dark matter interacting with quarks, we can sketch a theory containing a colored scalar particle which mediates the interaction.
- This theory looks kind of like a little part of a SUSY model, but has more freedom in terms of choosing couplings, etc.
- There are basically three parameters to this model: the mass of the dark matter, the mass of the mediator, and the coupling strength with quarks.



ũ_R Model

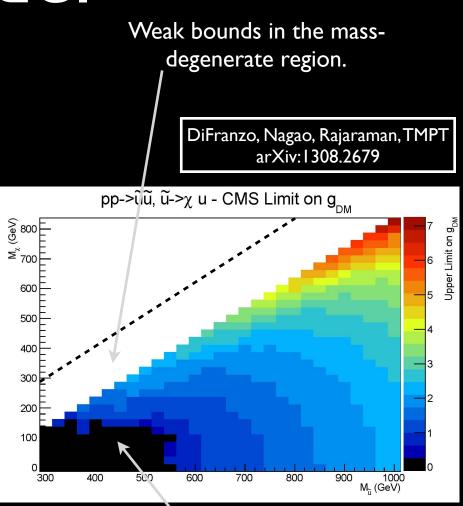
- To start with, consider a theory where a Dirac DM particle couples to right-handed up-type quarks.
- At colliders, the fact that the mediator is colored implies we can produce it at the LHC using the strong nuclear force (QCD; mostly from initial gluons) or through the interaction with quarks.
- Once produced, the mediator will decay into an ordinary quark and a dark matter particle.
- This is effectively a simplified model the collaborations already consider in searching for squark-like particles.





ũ_R Model

- In order to avoid strong flavor constraints, we implement minimal flavor violation by promoting the colored mediator to a flavor triplet.
- MFV would suggest that the first two generations have almost equal couplings, but is more agnostic about the coupling of the top quark to its mediator.
- Similarly, the masses of the first two generation mediators should be close to degenerate, and there is more freedom for the top-mediator.
- In the parameter plane of the mass of the dark matter and mass of the mediators, we can determine a limit on the coupling strength in the plane of the masses of the dark matter and the mediators.



QCD production saturates the CMS limits, resulting in no allowed value of g.

All mediator masses and couplings assumed equal.

ũ_R Model

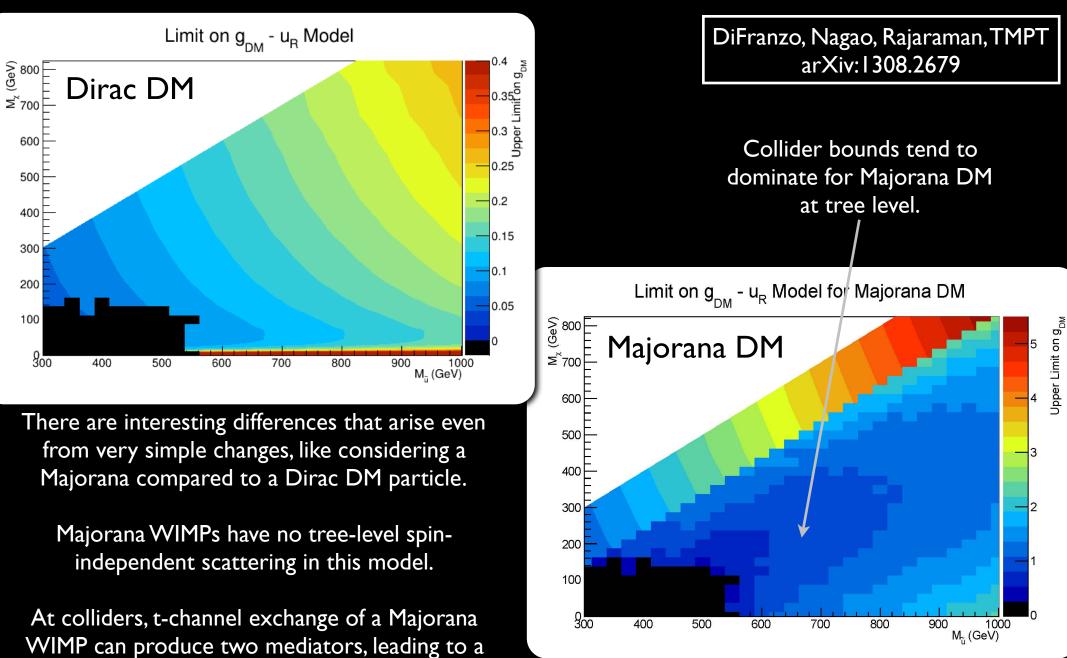
- A Dirac WIMP also has spin-independent scattering with nucleons. For most of the parameter space, there are bounds from the Xenon-100 experiment. (And LUX has recently improved these bounds by roughly a factor of two for dark matter masses around 100 GeV).
- Elastic scattering does not rule out any parameter space, but it does impose much stricter constraints on the coupling in the regions the LHC left as allowed.

Limit on $g_{DM} - u_{R}$ Model (GeV) on g_r ≥[×]700 E 0.25 ا 10.2 600 500 0.15 400 300 0.1 200 0.05 100 600 700 800 900 400 500 1000 M_~ (GeV)

DiFranzo, Nagao, Rajaraman, TMPT arXiv: 1308.2679

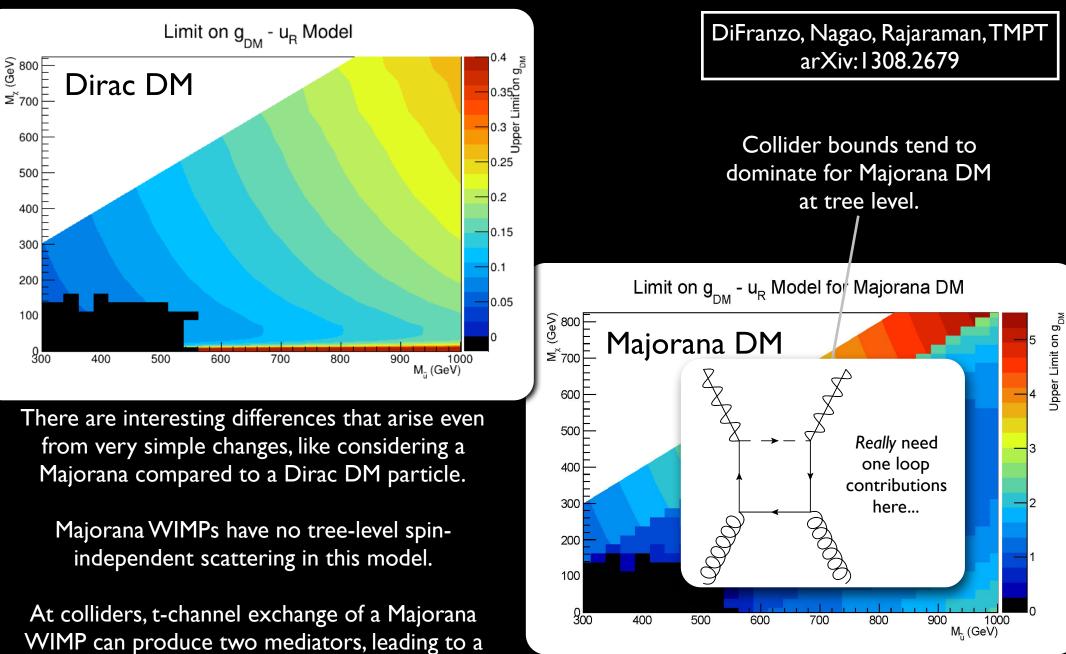
Traditional direct detection searches peter out for masses below about 10 GeV.

ũ_R Model: Results



PDF-friendly qq initial state.

\tilde{u}_R Model: Results

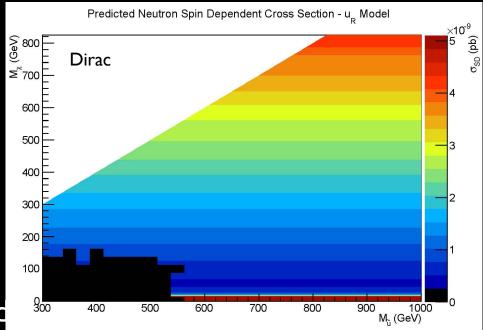


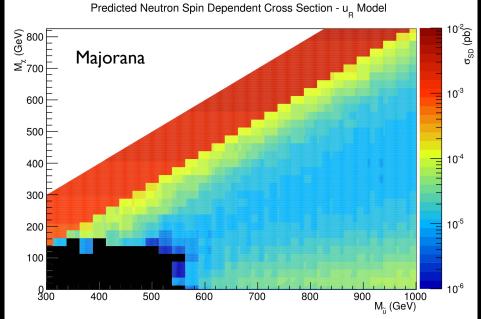
PDF-friendly qq initial state.

ũ_R Model: Forecasts

- Now that we understand the current bounds, we can forecast what this implies for future searches.
- For example, we can plot the largest spin-dependent cross sections that are consistent with the LHC constraints and Xenon-100 in this simplified model.
- Again, Dirac versus Majorana dark matter look very different from one another!

DiFranzo, Nagao, Rajaraman, TMPT arXiv: 1308.2679

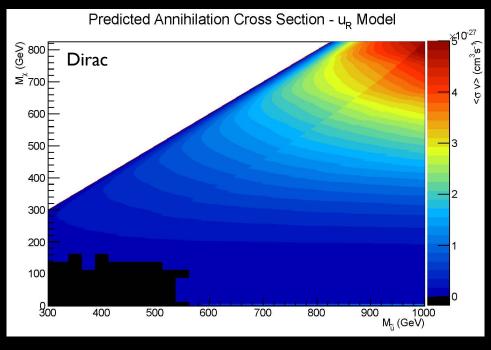


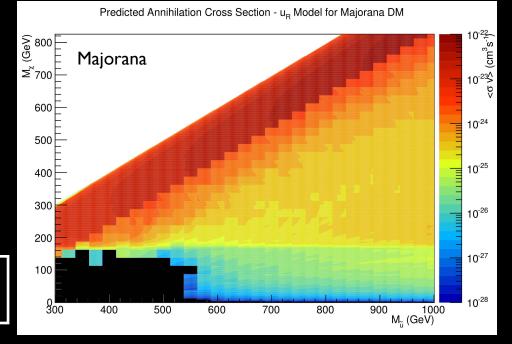


ũ_R Model: Forecasts

- Similarly, we can forecast for the annihilation cross section.
- The Fermi LAT does not put very interesting constraints at the moment, but it is very close to doing so. Limits from dwarf satellite galaxies are likely to be relevant in the near future for Majorana DM.
- We can also ask where in parameter space this simple module would lead to a thermal relic with the correct relic density.

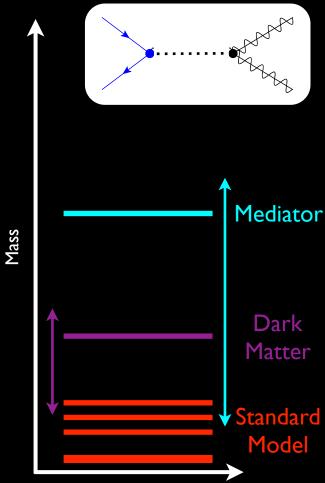
DiFranzo, Nagao, Rajaraman, TMPT arXiv: I 308.2679





S-Channel: Scalar

- A singlet scalar could be real or complex.
- Scalar couplings are chirality flipping. The scalar mediator consistent with MFV couples proportionally to Yukawa couplings.
- In the SM, the only relevant parameters are the masses, and the degree of mixing with the SM Higgs through electroweak breaking.
- If the SM is extended to a two (or more) Higgs doublet model, the coupling to up-quarks, down-quarks, and/or leptons become decorrelated.
- Much like the Higgs itself, there can be important coupling to gluons induced at loop level.

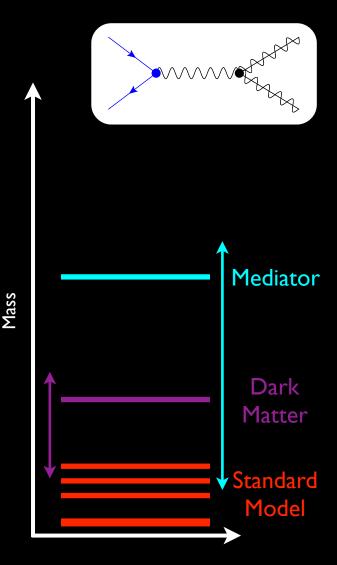


Buckley, Feld, Goncalves 1410.6497 Harris, Khoze, Spannowsky, Williams 1411.0535 + others

S-Channel : Vector

- Vector models have more parameters consistent with MFV.
- uR, dR, qL, eR, IL all have family-universal but distinct charges, as does H.
 - We would like to be able to write down the SM Yukawa interactions.
 - Quarks need not have universal couplings.
- There could be kinetic mixing with $U(I)_{Y}$.
- There is a dark Higgs sector. It may not be very important for LHC phenomenology.
- Gauge anomalies must cancel, which also may not be very important for LHC phenomenology.

Parameters: $\{M_{\mathrm{DM}}, g, M_{Z'}, z_q, z_u, z_d, z_\ell, z_e, z_H, \eta\}$ +



How Effective a Theory?

s = 8 Te

- There is a large literature asking how simplified models match up with the EFT, starting with some of the original EFT papers themselves.
- Pushing the mass of the mediator higher for fixed EFT coupling corresponds to assuming the mediator is more strongly coupled.
- Depending on how they are implemented, there a constraints from pro dijet resonance searc searches for dilepton

