

# Global fit of top quark EFT to data



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arXiv:1506.08845

*Higgs Effective Field Theories workshop, Chicago, November 2015*

# The Standard Model EFT

Why bother with Effective Field Theory?

- All measurements more or less consistent with SM
- Resurgence of model-independent frameworks to go beyond SM

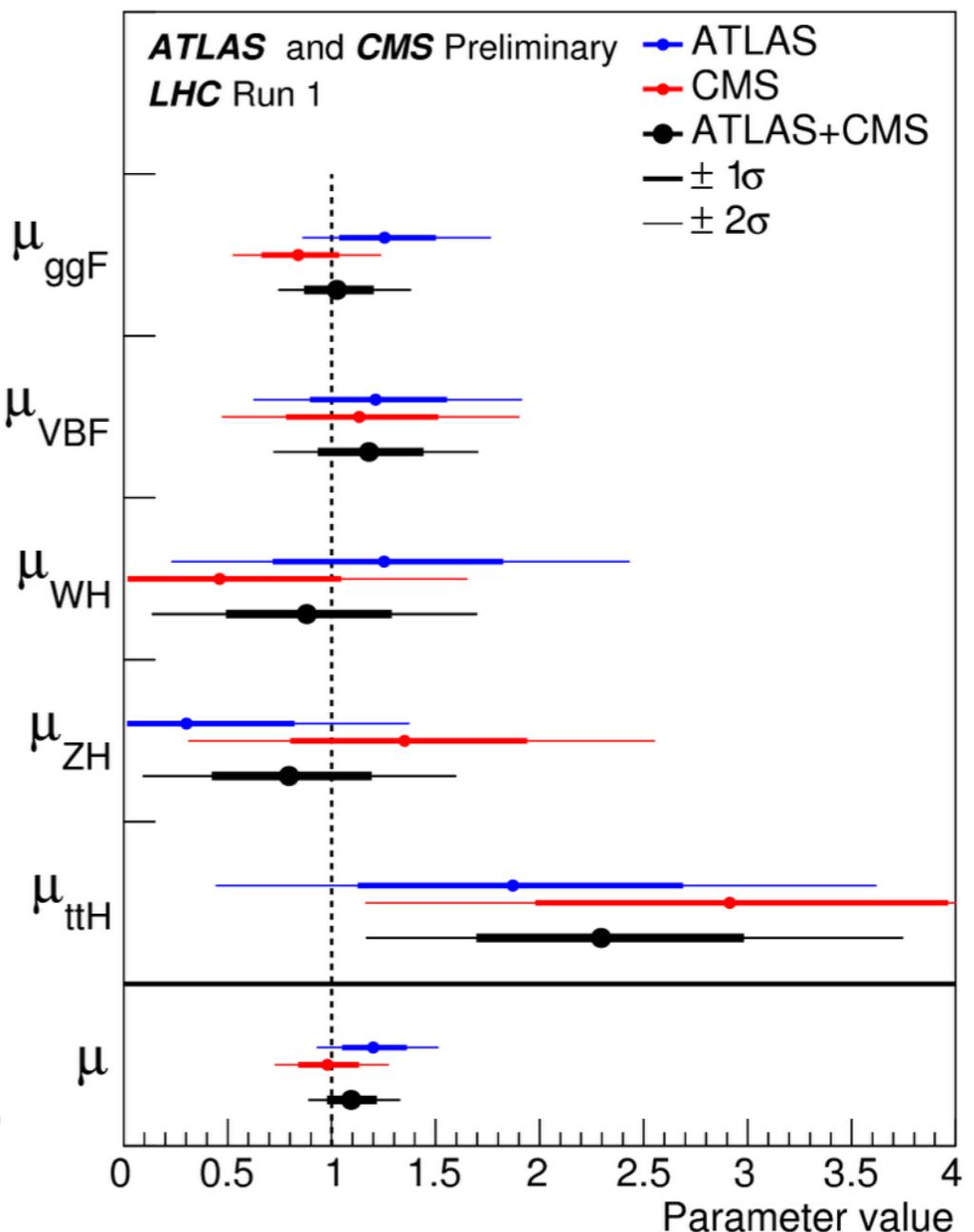
( *$\kappa$  framework, anomalous couplings, form factors...*)

- Merits of EFT: completely general, can be matched to UV completions, radiative corrections calculable etc.
- If there is new physics, looks like it decouples

$$\mathcal{O}^{d_i}(E) = \mathcal{O}^{d_i}(\Lambda)(E/\Lambda)^{d_i-4}$$

Wilson, Rev. Mod. Phys. 55, 583 (1983)

Appelquist & Carazzone, Phys. Rev. D11, 28565 (1973)



**Any decoupled new physics (at high scale) = A higher-dimensional operator (at low scale)**

# The Standard Model EFT

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} \sum_i C_i O_i(G_\mu^a, W_\mu^I, B_\mu, \Phi, q_L, u_R, d_R, l_L, e_R) + \mathcal{O}(\Lambda^{-4})$$

see e.g.

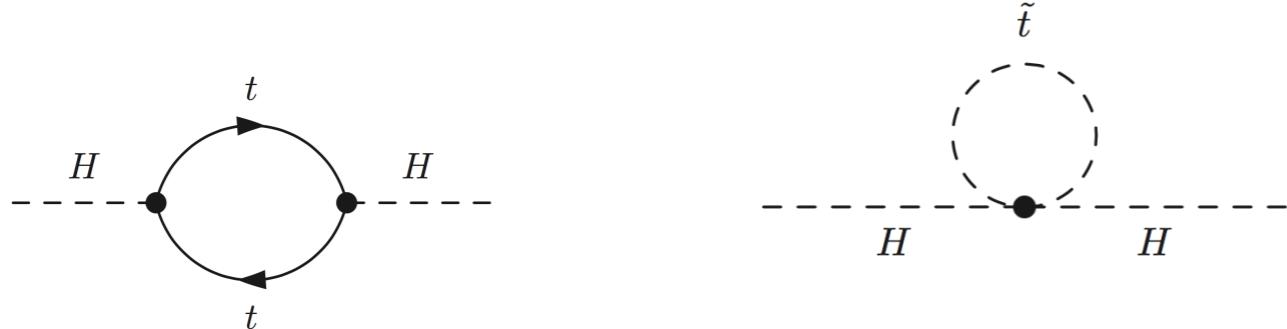
Gripaios & Sutherland, 1309.7822	Hayreter & Valencia, 1304.6976	Henning, Lu & Murayama, 1412.1837
Buchalla, Cata & Krause 1312.5624		Alonso, Jenkins, Manohar & Trott 1312.2014
Aguilar, Bouzas, Larios, 1509.06431	Chiang & Huo 1505.06334	Gupta, Pomarol & Riva 1405.0181
	Ellis, Sanz & You 1410.7703	Lehman 1410.4193
Corbett, Eboli, Goncalves, Gonzalez-Fraile, Plehn & Rauch 1505.05516		Englert & Spannowsky 1408.5147
Pierce, Thaler & Wang hep-ph/0609049	Djouadi 1208.3436	Efrati, Falkowski & Soreq 1503.07872
Wells & Zhang 1406.6070	de Blas, Chala & Santiago 1507.00757	Berthier & Trott 1508.05060
Degrande 1308.6323	Alonso, Gavela, Merlo, Rigolin & Yepes 1202.3305	Dawson, Lewis & Zeng 1409.6299
	Delgado, Dobado, Herrero, Sanz-Cillero 1404.2866	Elias-Miró, Espinosa, Masso & Pomarol 1302.5661
Low, Lykken & Shaughnessy 1207.1093		Greiner, Willenbrock & Zhang 1104.3102
Contino, Ghezzi, Grojean, Muhlleitner & Spira 1303.3876		Grojean, Salvioni, Schlaffer & Weiler, 1312.3317
Azatov, Contino, Panico & Son 1502.00539		Gavela, Kanshin, Machado & Saa 1409.1571

# Why top EFT?

## DIRECTLY:

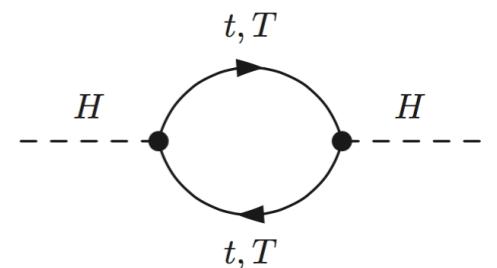
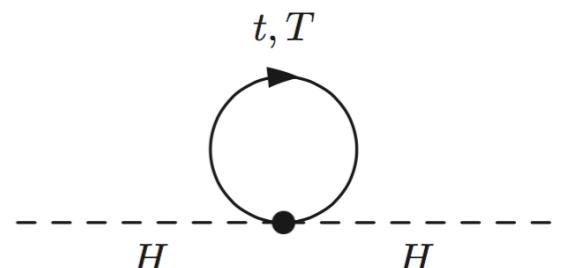
Top plays a special role in most scenarios of electroweak symmetry breaking:

- SUSY: Top partners cancel UV divergences in  $m_h$  (if light enough)



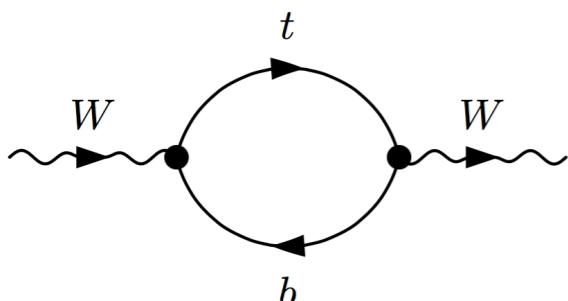
$$\delta m_H^2 = -\frac{|\lambda_F|^2}{8\pi^2} [\Lambda_{UV}^2 + \dots] \quad \delta m_{\tilde{H}}^2 = 2 \times \frac{|\lambda_S|^2}{16\pi^2} [\Lambda_{UV}^2 + \dots]$$

- Little Higgs and friends: Spin-1/2 top partners with large T-t mixing

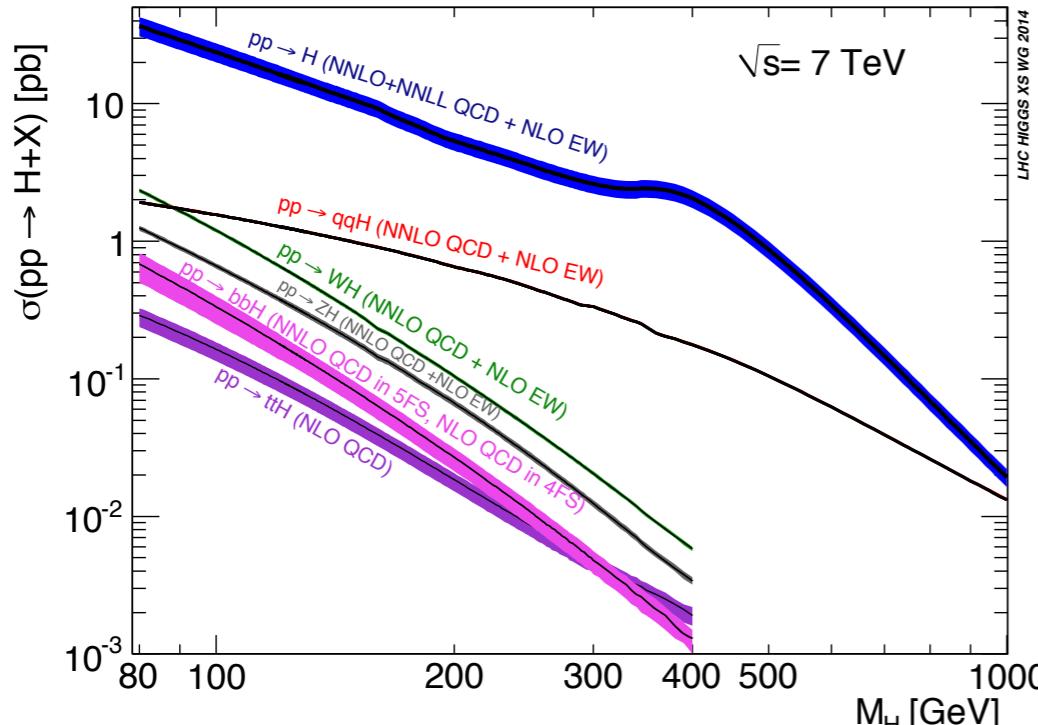


## INDIRECTLY:

Large effects in electroweak measurements: ripe for deviations



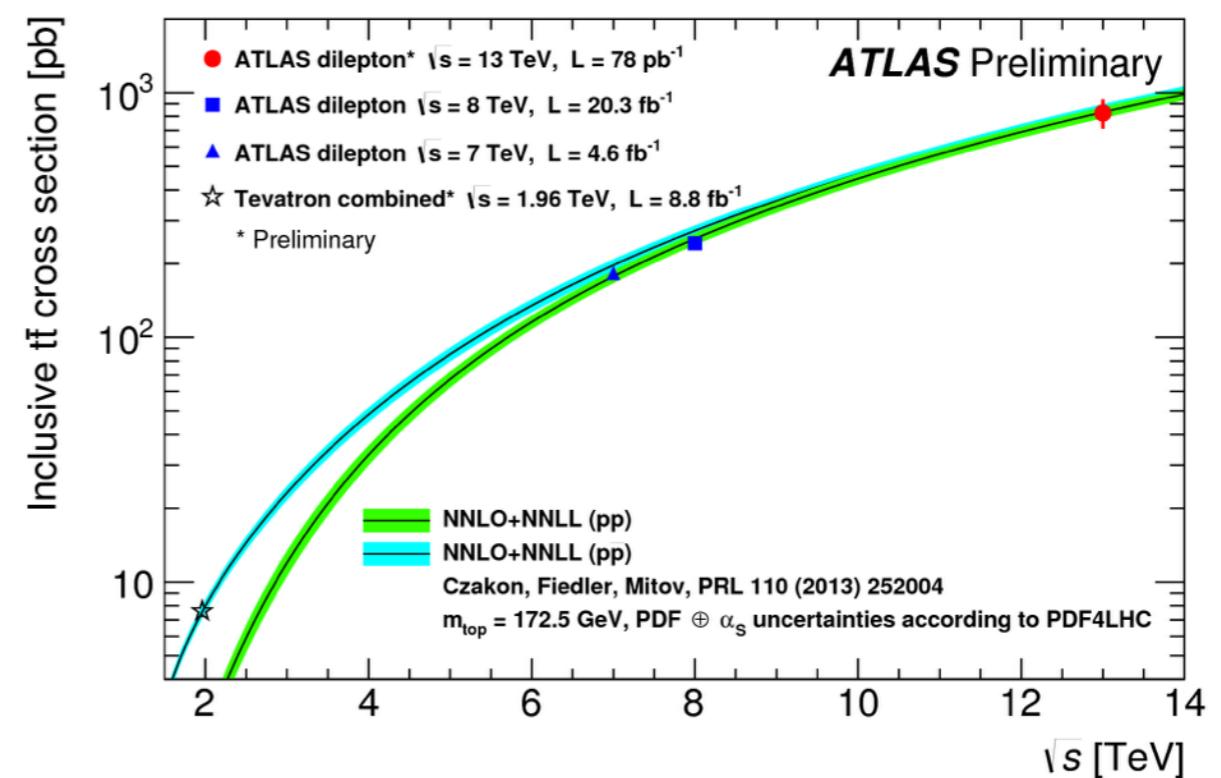
# Why top EFT?



8 million top quarks produced!

LHC run 1:  
 4.57  $\text{fb}^{-1}$  @ 7 TeV  
 20.3  $\text{fb}^{-1}$  @ 8 TeV

→ 550,000 Higgs produced (before BRs!)



EFT: Which Lagrangian best describes the currently available data?







# The PROFESSOR method

Brief detour: MC tuning

- Every MC event generator comes with many free parameters that must be tuned in order to describe the data



Different approaches:



Tune by hand (!?)

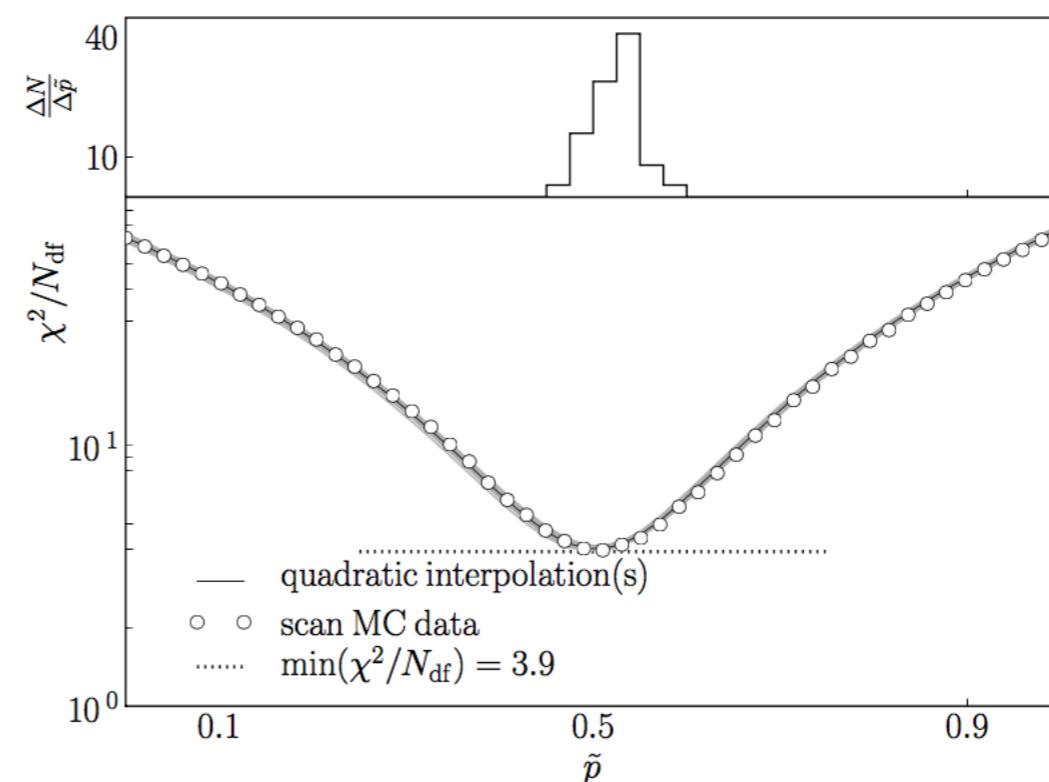
Brute force computation ( $N^D$ )

## Parameterisation-based tuning:

Buckley et al. 0907.2973

Parameterise MC response

Fit to data → Optimal 'tune'



# The PROFESSOR method

- Sample a set of points in the N-dimensional parameter space of  $\{C_i\}$
- Construct *parameterising* function  $f_b(\{C_i\})$  which models change in MC w.r.t Wilson coefficient

$$|\mathcal{M}_{\text{tot}}|^2 = |\mathcal{M}_{\text{SM}}|^2 + 2\Re \{\mathcal{M}_{\text{SM}}\mathcal{M}_{D6}^*\} + |\mathcal{M}_{D6}|^2 \longrightarrow f_b(\{C_i\}) = \alpha_0^b + \sum_i \beta_i^b C_i + \sum_{i \leq j} \gamma_{ij}^b C_i C_j$$

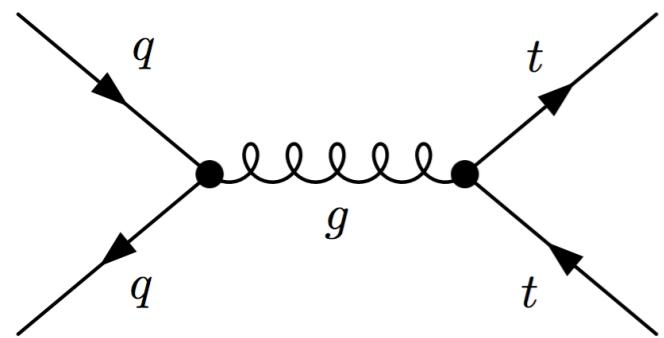
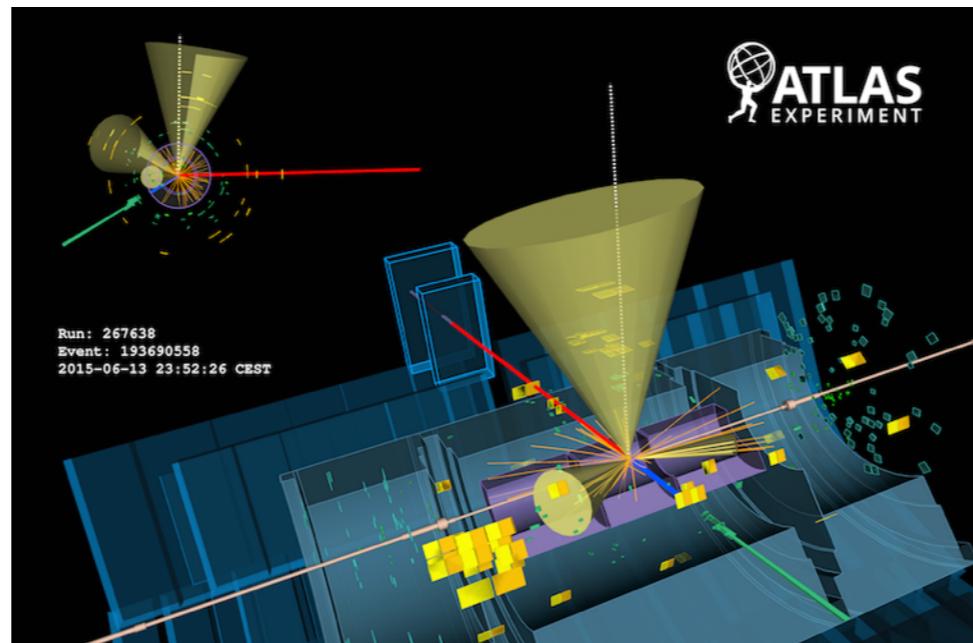

- Construct goodness-of-fit between  $f_b(\{C_i\})$  and data

$$\chi^2(\mathbf{C}) = \sum_{\mathcal{O}} \sum_{i,j} \frac{(f_i(\mathbf{C}) - E_i)\rho_{i,j}(f_j(\mathbf{C}) - E_j)}{\sigma_i \sigma_j}$$

- Minimise it!

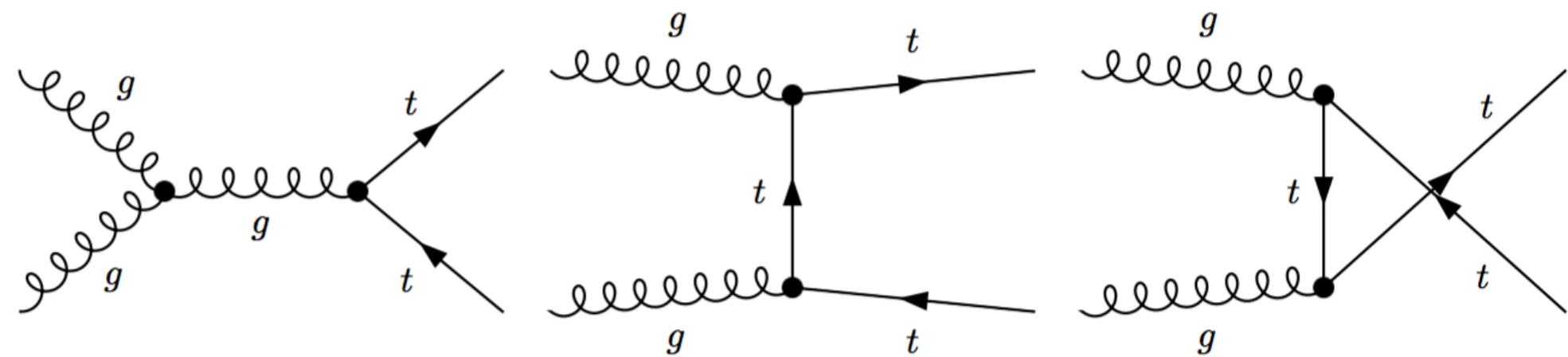
**GOAL: Global fit of all relevant operators  
in top quark production & decay to  
available data from Tevatron & LHC**

# Top pair production



85% of Tevatron cross-section

~ 90% of LHC cross-section



# Top pair production

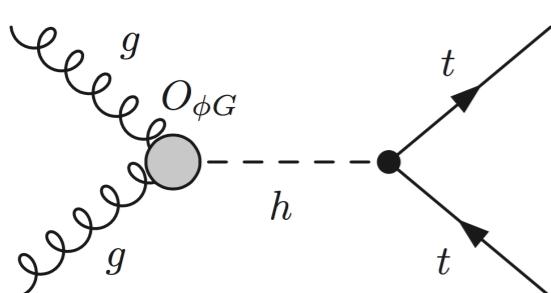
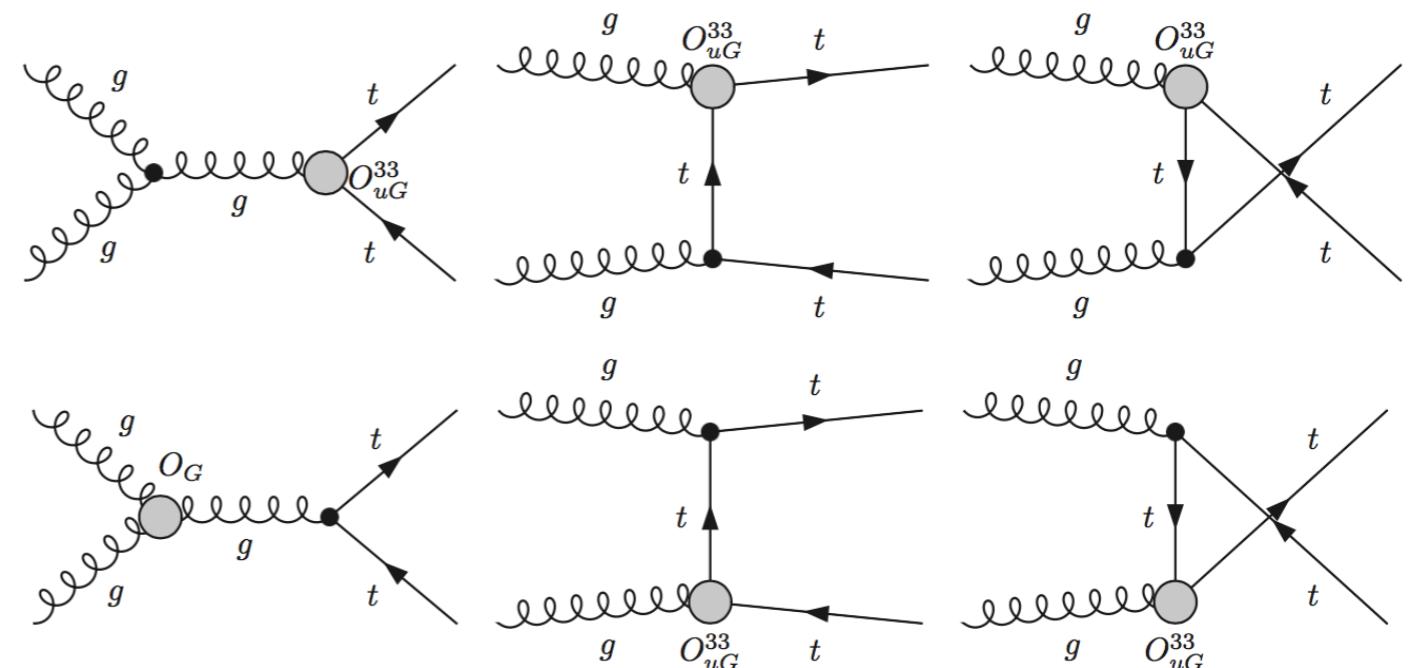
At dimension-six

$$|\mathcal{M}_{\text{tot}}|^2 = |\mathcal{M}_{\text{SM}}|^2 + 2\Re \{\mathcal{M}_{\text{SM}}\mathcal{M}_{D6}^*\} + |\mathcal{M}_{D6}|^2$$

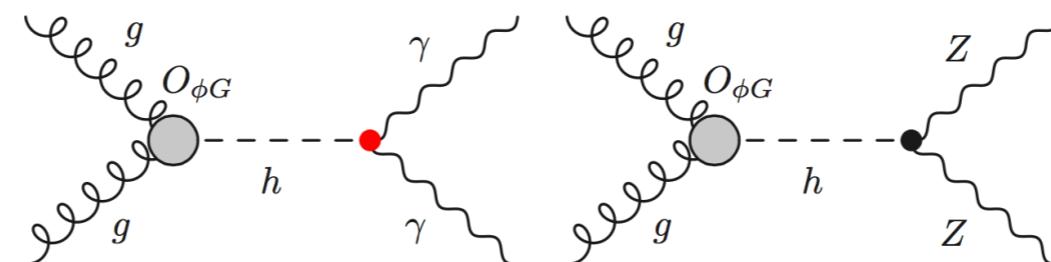
$$O_{uG} = (\bar{q}\sigma^{\mu\nu}\lambda^A u)\tilde{\phi}G_{\mu\nu}^A$$

$$O_G = f_{ABC}G_\mu^{A\nu}G_\nu^{B\lambda}G_\lambda^{C\mu}$$

$$O_{\phi G} = \frac{1}{2}(\phi^\dagger\phi)G_{\mu\nu}^A G^{A\mu\nu} \text{ ??}$$

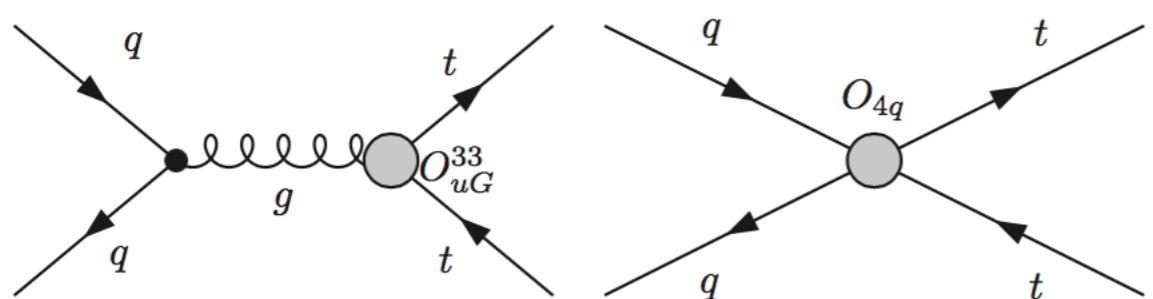


No constraint here, but can probe in Higgs physics



*Corbett et al. 1505.05516*

# Top pair production



*Kamenik, Shu & Zupan, 1107.5257*

*Zhang and Willenbrock, 1008.3869*

*Degrade, Gerard, Grojean,  
Maltoni & Servant, 1010.6304*

$$O_{qq}^1 = (\bar{q}\gamma_\mu q)(\bar{q}\gamma^\mu q)$$

$$O_{qq}^3 = (\bar{q}\gamma_\mu \tau^I q)(\bar{q}\gamma^\mu \tau^I q)$$

$$O_{uu} = (\bar{u}\gamma_\mu u)(\bar{u}\gamma^\mu u)$$

$$O_{qu}^8 = (\bar{q}\gamma_\mu T^A q)(\bar{u}\gamma^\mu T^A u)$$

$$O_{qd}^8 = (\bar{q}\gamma_\mu T^A q)(\bar{d}\gamma^\mu T^A d)$$

$$O_{ud}^8 = (\bar{u}\gamma_\mu T^A u)(\bar{d}\gamma^\mu T^A d)$$



$$O_u^1 = 3(2O_{qq}^{(1)1331} + O_{uu}^{1331}) - (O_{qq}^{(1)1133} + O_{qq}^{(3)1133} + O_{uu}^{1133})$$

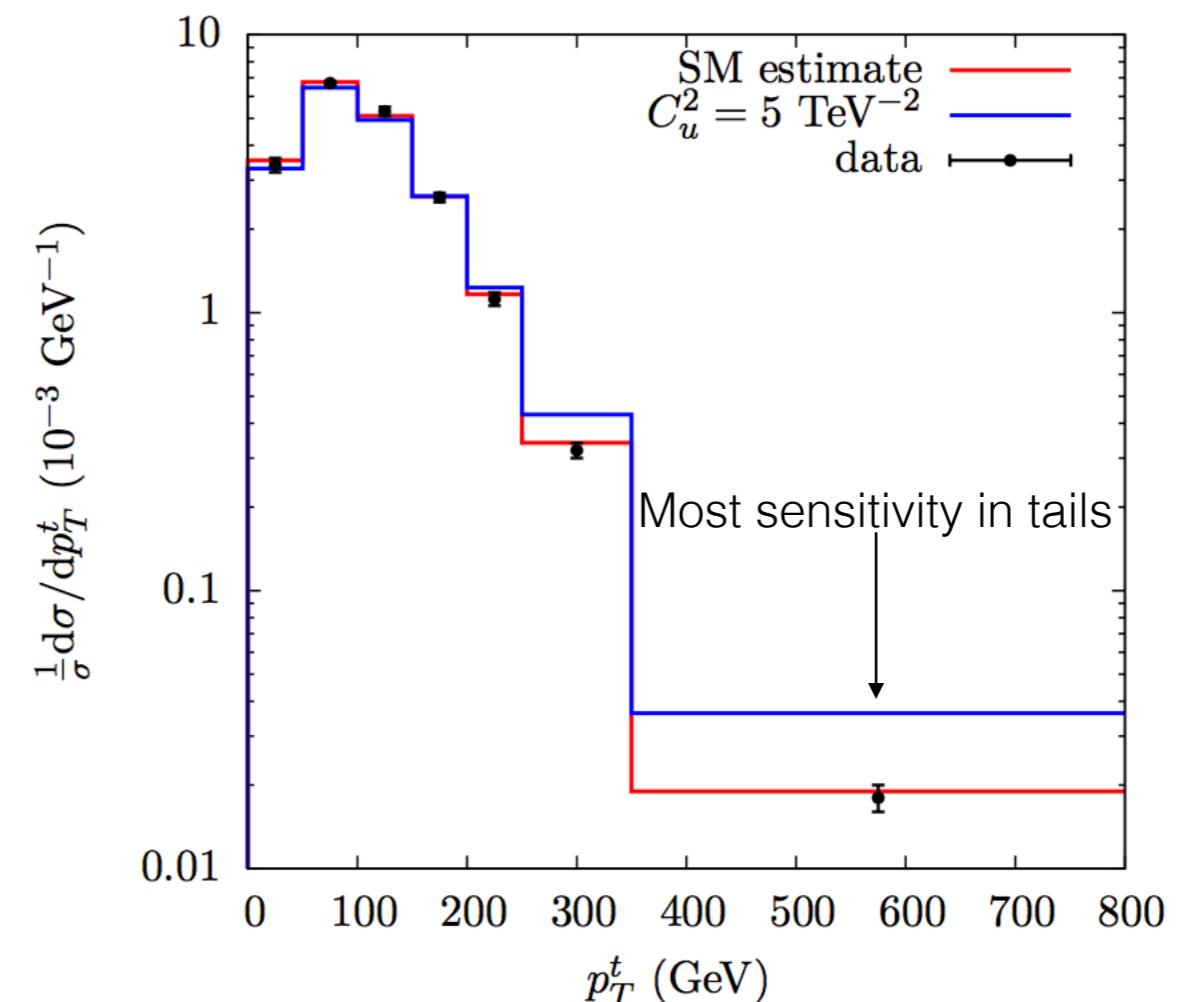
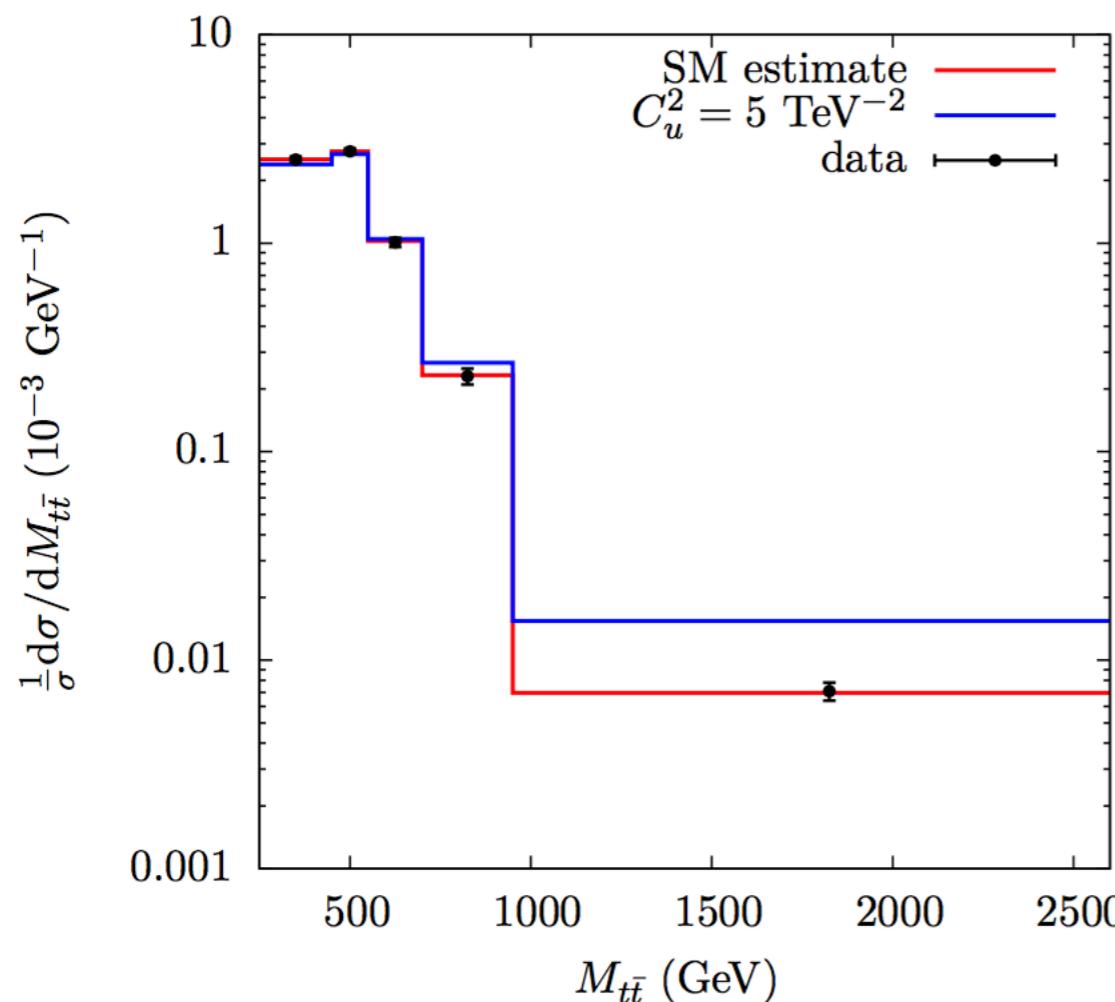
$$O_u^2 = -(O_{qu}^{(8)1133} + O_{qu}^{(8)3311})$$

$$O_d^1 = 3(O_{qq}^{(3)1331} - O_{qq}^{(1)1331}) + (O_{qq}^{(3)1133} - O_{qq}^{(1)1133}) + 6O_{ud}^{(8)3311}$$

$$O_d^2 = -(O_{qu}^{(8)1133} + O_{qd}^{(8)3311}),$$

**SUMMARY:** 6 constrainable operators in top pair production

# Top pair production

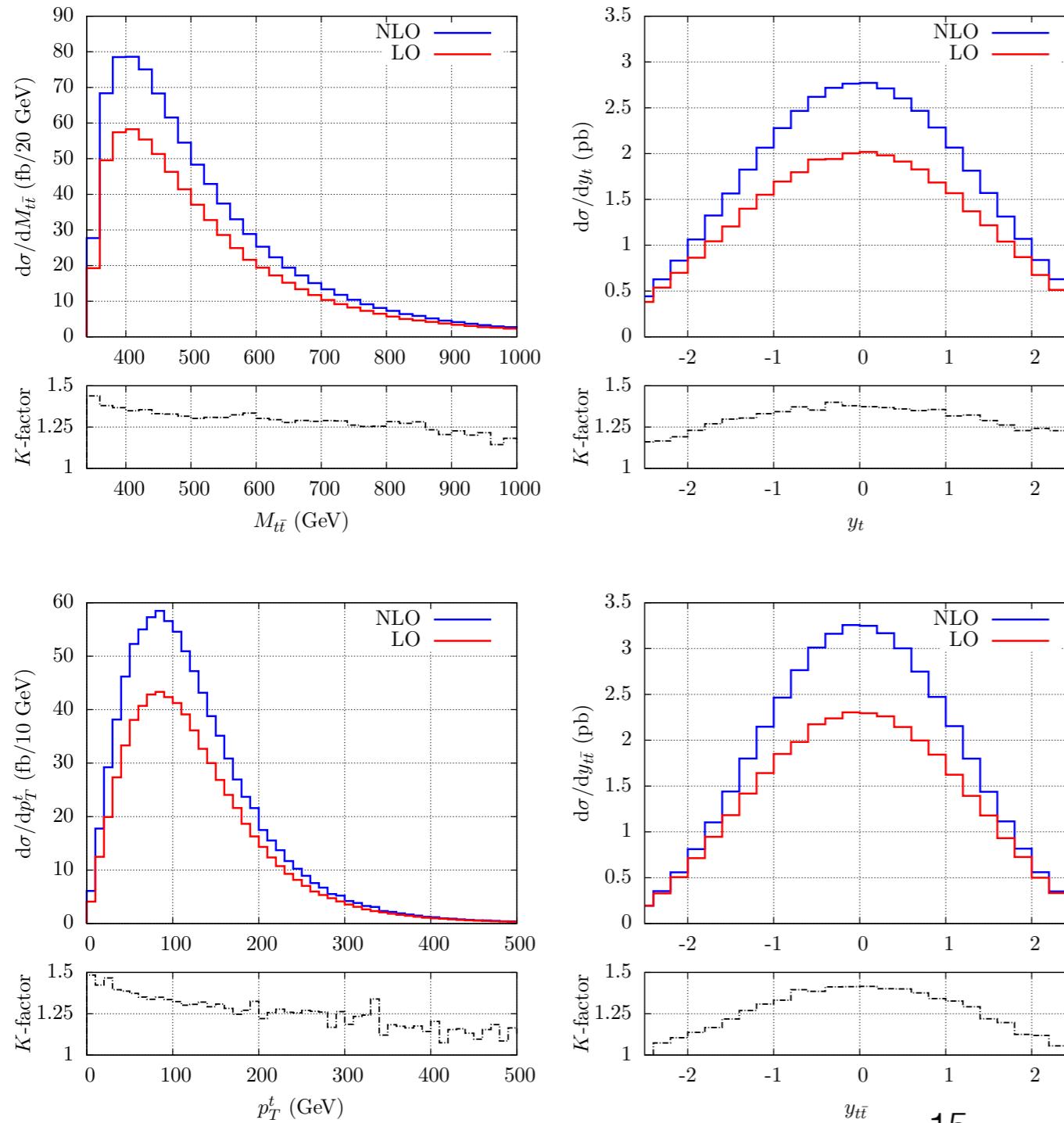


Small effect on shapes

# NLO corrections

Known to be large ( $\sim 1.6$ ) for top pair production

*Nason, Dawson & Ellis Nucl.Phys. B303 (1988) 607*



Re-weight SM piece to  
NLO estimate to model  
higher-order effects

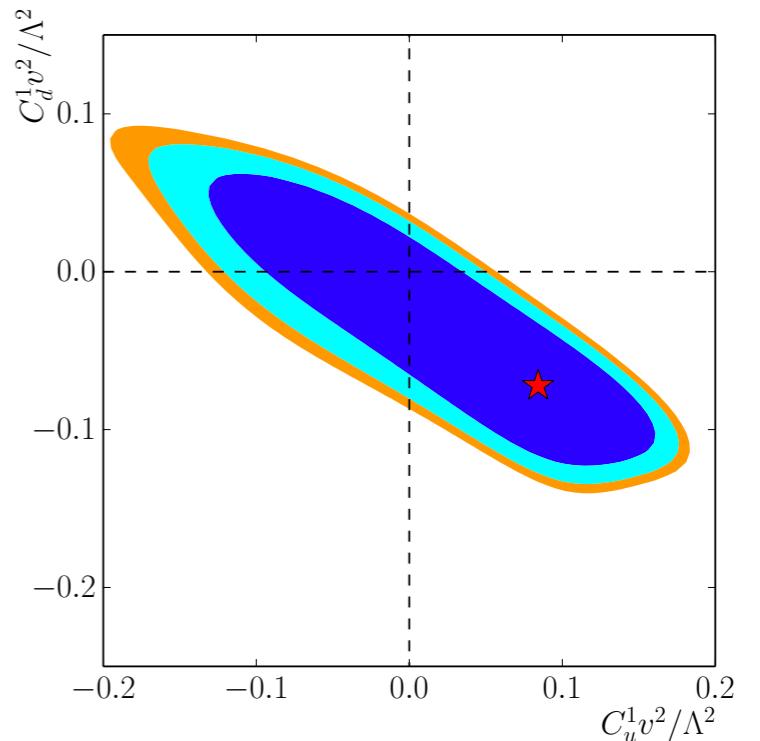
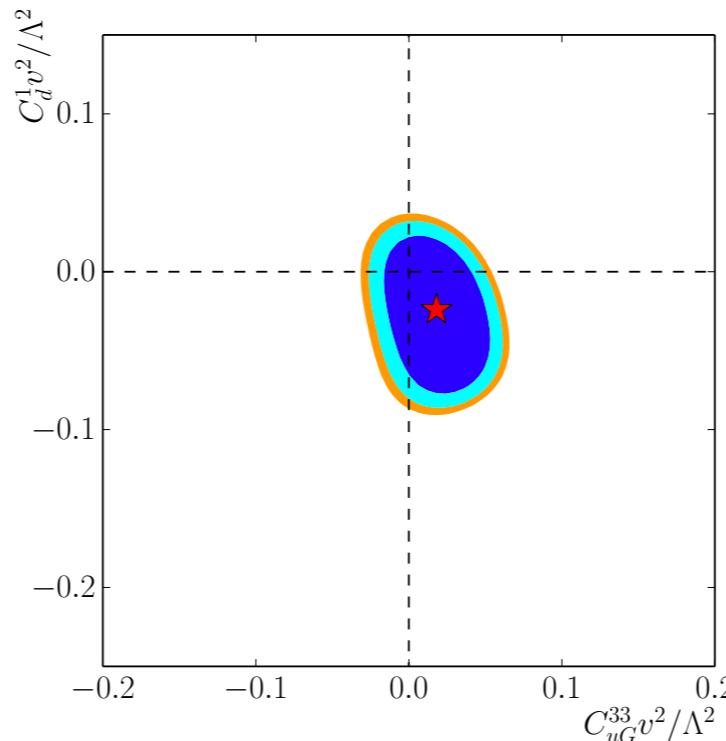
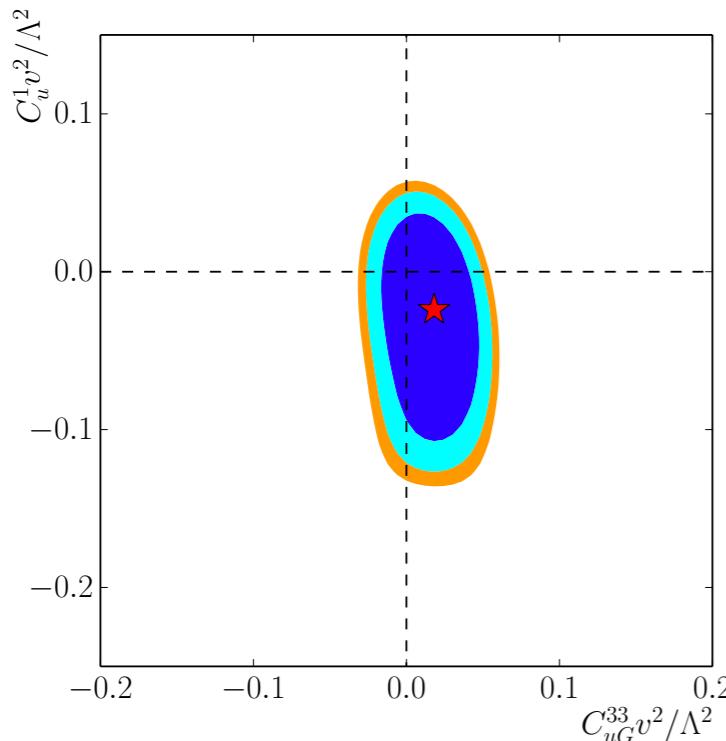
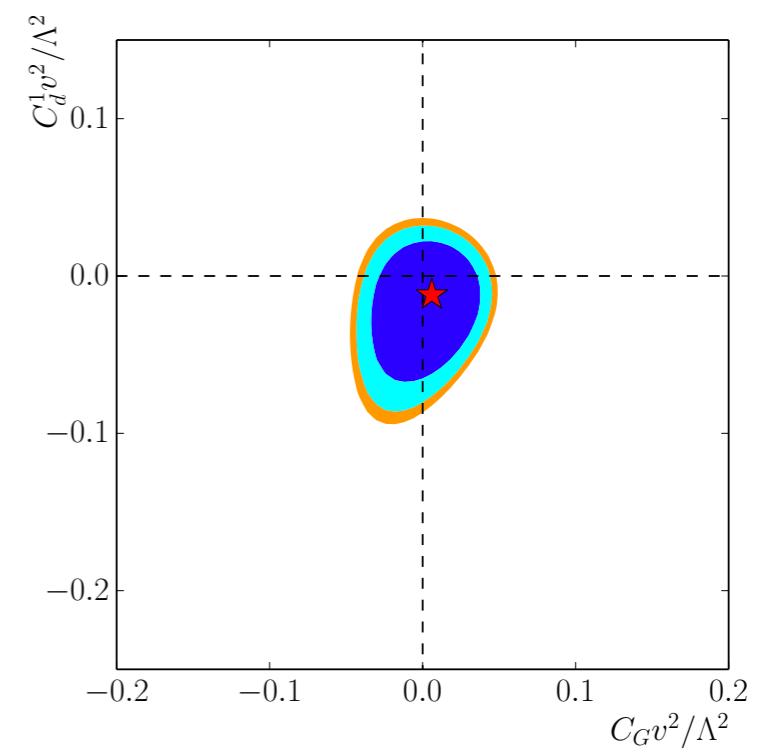
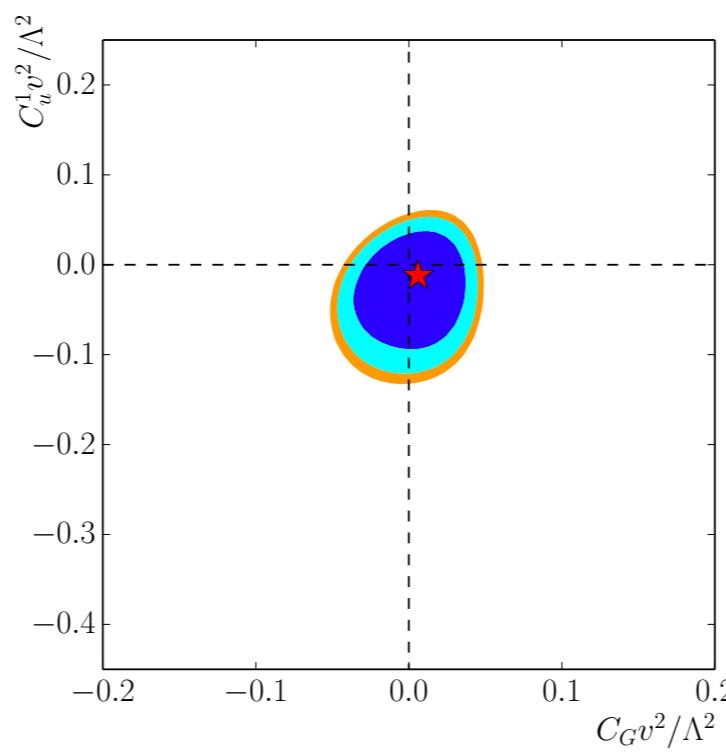
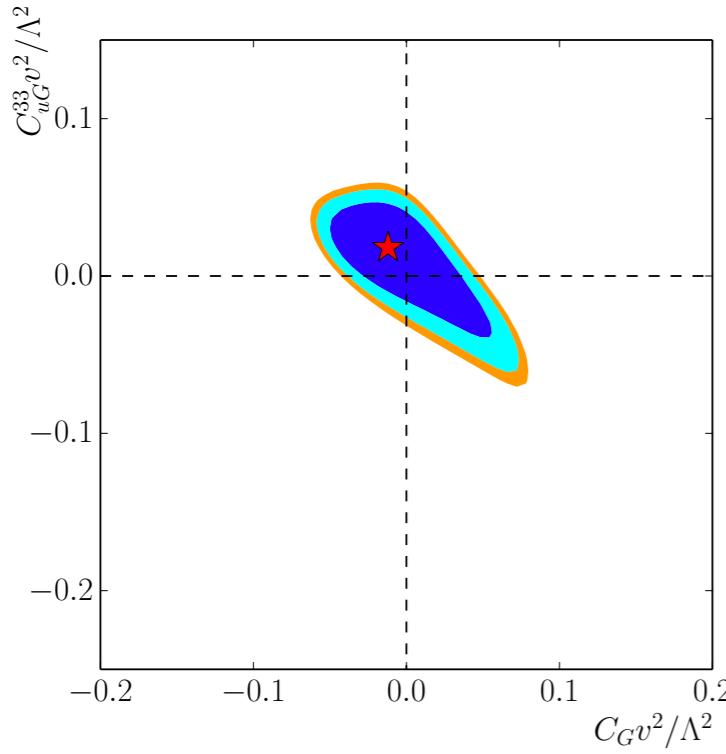
Scale + PDF  
uncertainties  
added linearly  
(maximally  
correlated)

NNLO available  
for total cross-  
sections

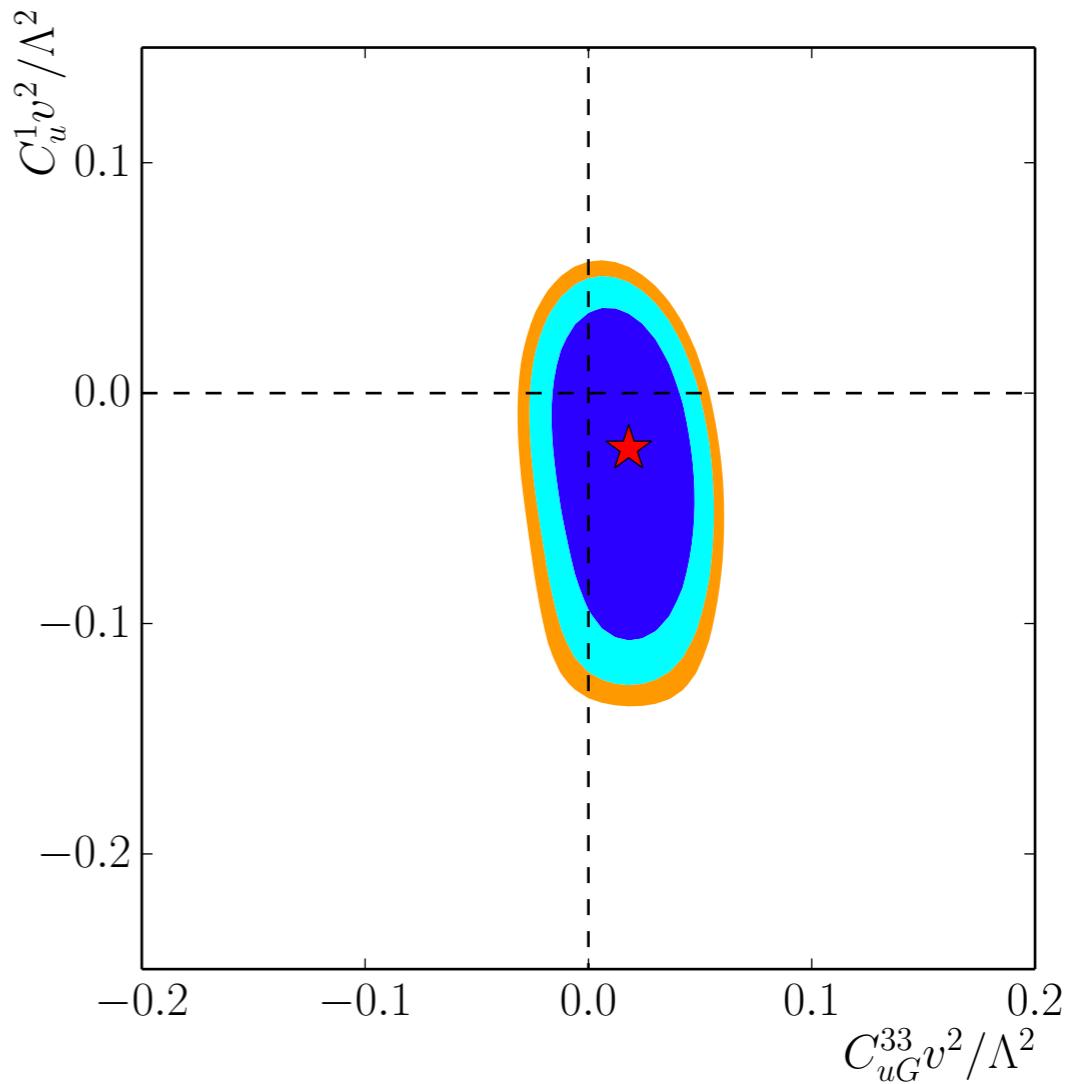
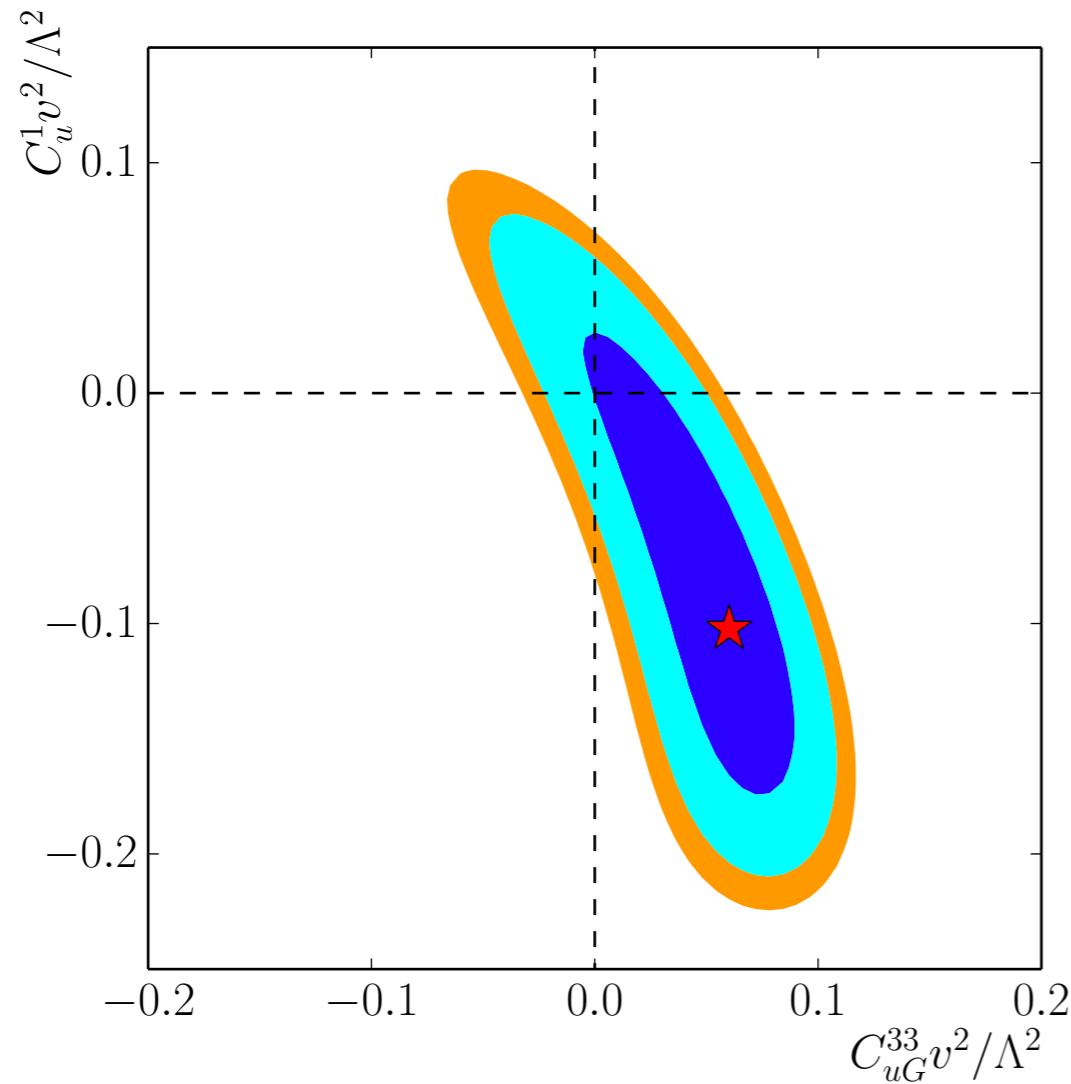
(and differential on the way)

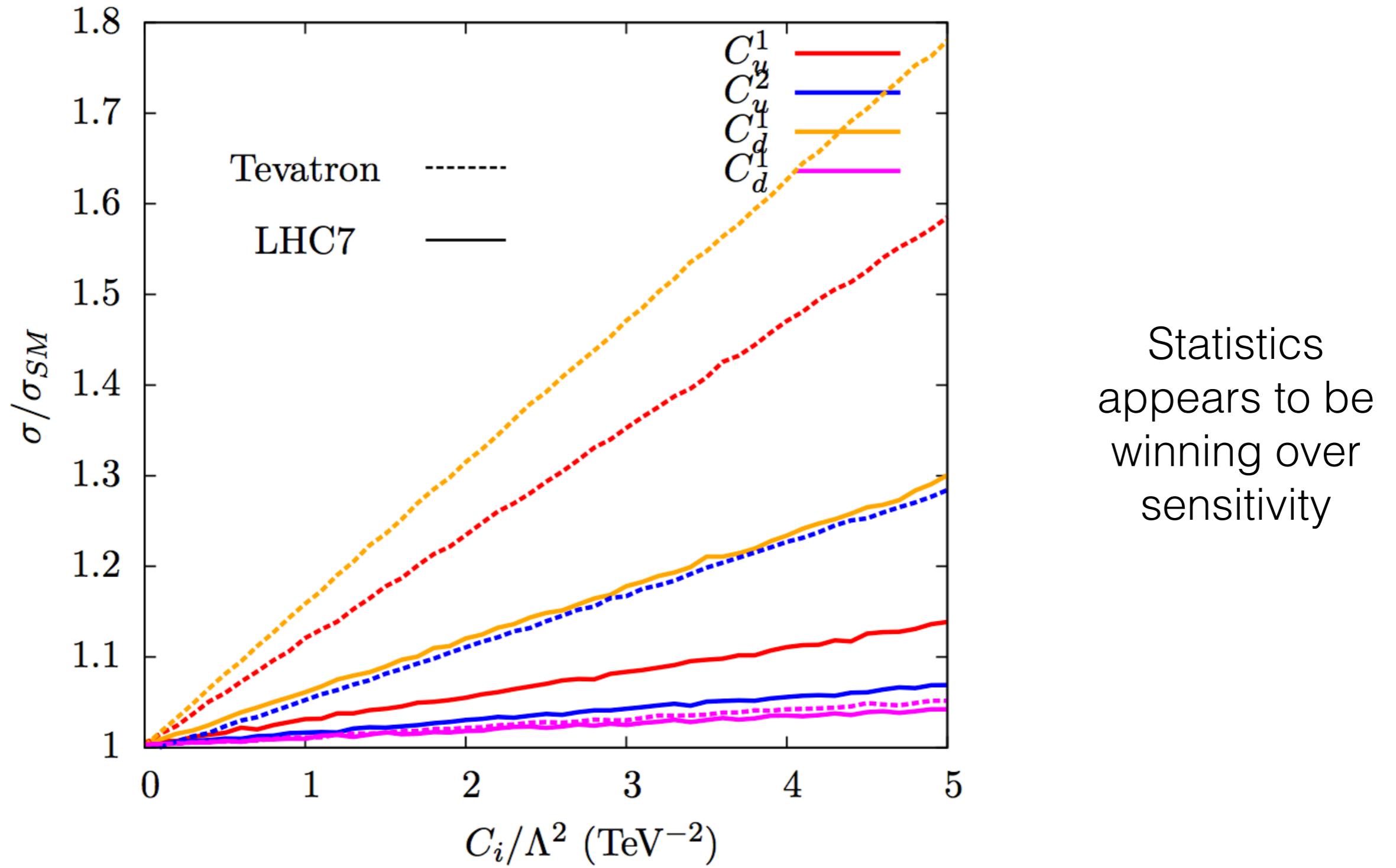
*Butterworth et al.  
arXiv:1101.0538*

# Selected correlations



# Tevatron-LHC complementarity





0 1 2 3

Measurement

ATLAS 7 TeV  $p_T(t)$ ATLAS 7 TeV  $m(t, \bar{t})$ ATLAS 7 TeV  $|y(t, \bar{t})|$ CDF  $m(t, \bar{t})$ CMS 7 TeV  $p_T(t)$  (dilepton)CMS 7 TeV  $m(t, \bar{t})$  (dilepton)CMS 7 TeV  $y(t)$  (dilepton)CMS 7 TeV  $p_T(t)$  (lepton+jets)CMS 7 TeV  $m(t, \bar{t})$  (lepton+jets)CMS 7 TeV  $y(t)$  (lepton+jets)CMS 8 TeV  $p_T(t)$  (dilepton)CMS 8 TeV  $m(t, \bar{t})$  (dilepton)CMS 8 TeV  $y(t)$  (dilepton)CMS 8 TeV  $p_T(t)$  (lepton+jets)CMS 8 TeV  $m(t, \bar{t})$  (lepton+jets)CMS 8 TeV  $y(t)$  (lepton+jets)D $\emptyset$   $p_T(t)$ D $\emptyset$   $m(t, \bar{t})$ D $\emptyset$   $y(t)$  $\chi^2/\text{bin}$ 

# Global $\chi^2$

Differential distributions



Total rates



Measurement

ATLAS 7 TeV lepton+jets

ATLAS 7 TeV dilepton

ATLAS 7 TeV lepton+tau

ATLAS 7 TeV lepton w/o b-jets

ATLAS 7 TeV lepton w/ b-jets

ATLAS 7 TeV tau+jets

ATLAS 7 TeV  $t\bar{t}, Z\gamma, WW$ 

ATLAS 8 TeV dilepton

ATLAS 8 TeV lepton+jets

CMS 7 TeV all hadronic

CMS 7 TeV dilepton

CMS 7 TeV lepton+jets

CMS 7 TeV lepton+tau

CMS 7 TeV tau+jets

CMS 8 TeV dilepton

Tevatron combined

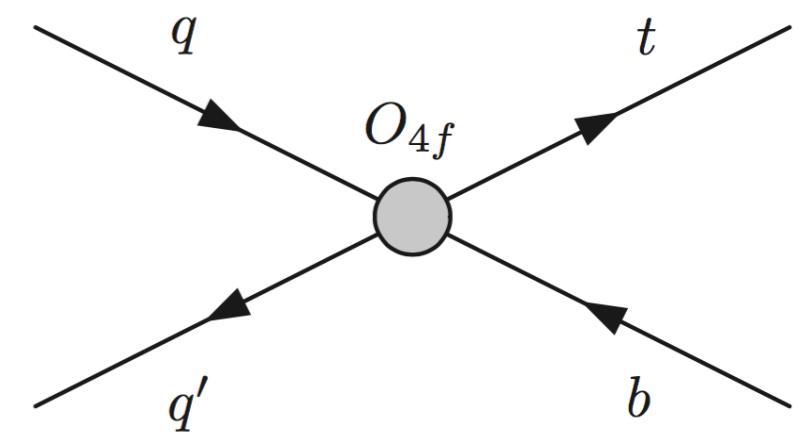
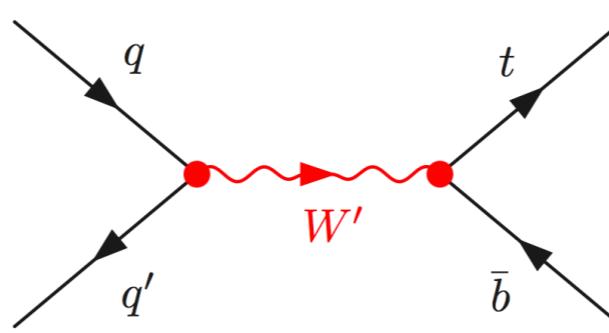
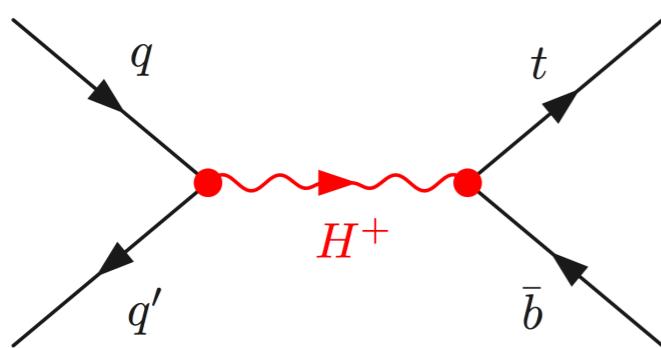
 $\chi^2/\text{bin}$ 

0 1 2 3

0 1 2 3

# Single-top production

Single top in simple BSM models:



$$O_{qq}^3 = (\bar{q}\gamma_\mu\tau^I q)(\bar{q}\gamma^\mu\tau^I q) \quad \mathcal{M}_{D6} \sim C_i v^2/\Lambda^2$$

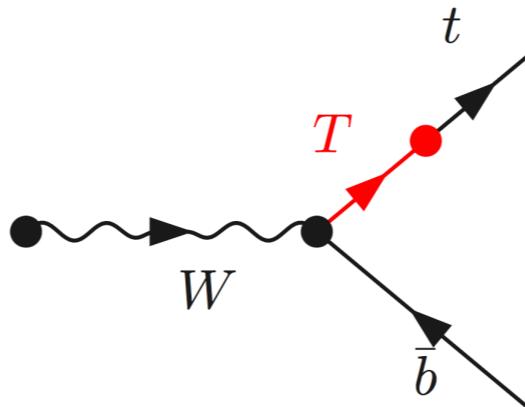
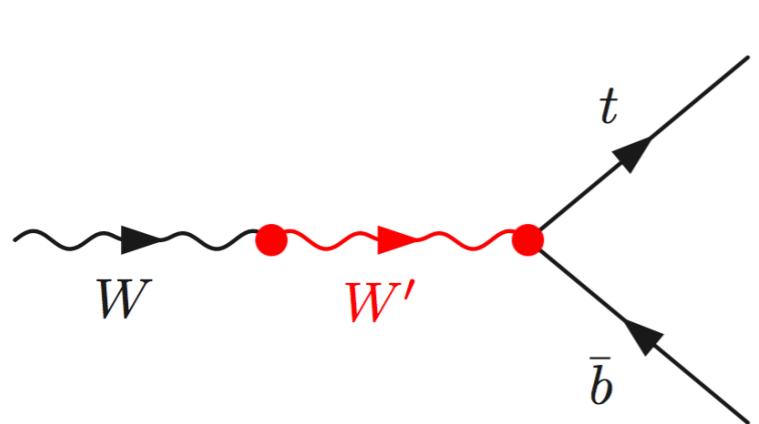
~~$$O_{qq}^1 = (\bar{q}\gamma_\mu q)(\bar{q}\gamma^\mu q)$$~~

~~$$O_{qu}^1 = (\bar{q}\gamma_\mu q)(\bar{u}\gamma^\mu u)$$~~

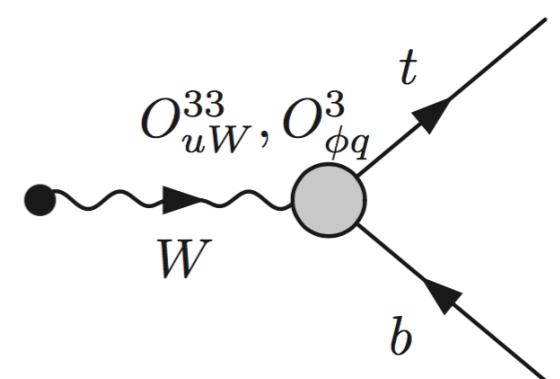
$$\mathcal{M}_{D6} \sim C_i m_t m_b / \Lambda^2$$

# Single-top production

Single top in simple BSM models:



in low-energy limit:



Relation to anomalous couplings:

$$O_{uW}^{33} = (\bar{q}\sigma^{\mu\nu}\tau^I u)\tilde{\phi}W_{\mu\nu}^I$$



$$\mathcal{L}_{Wtb} = \frac{g}{\sqrt{2}}\bar{b}\gamma^\mu(V_L P_L + V_R P_R)tW_\mu^- + \frac{g}{\sqrt{2}}\bar{b}i\sigma^{\mu\nu}(g_L P_L + g_R P_R)tW_\mu^- + h.c.$$

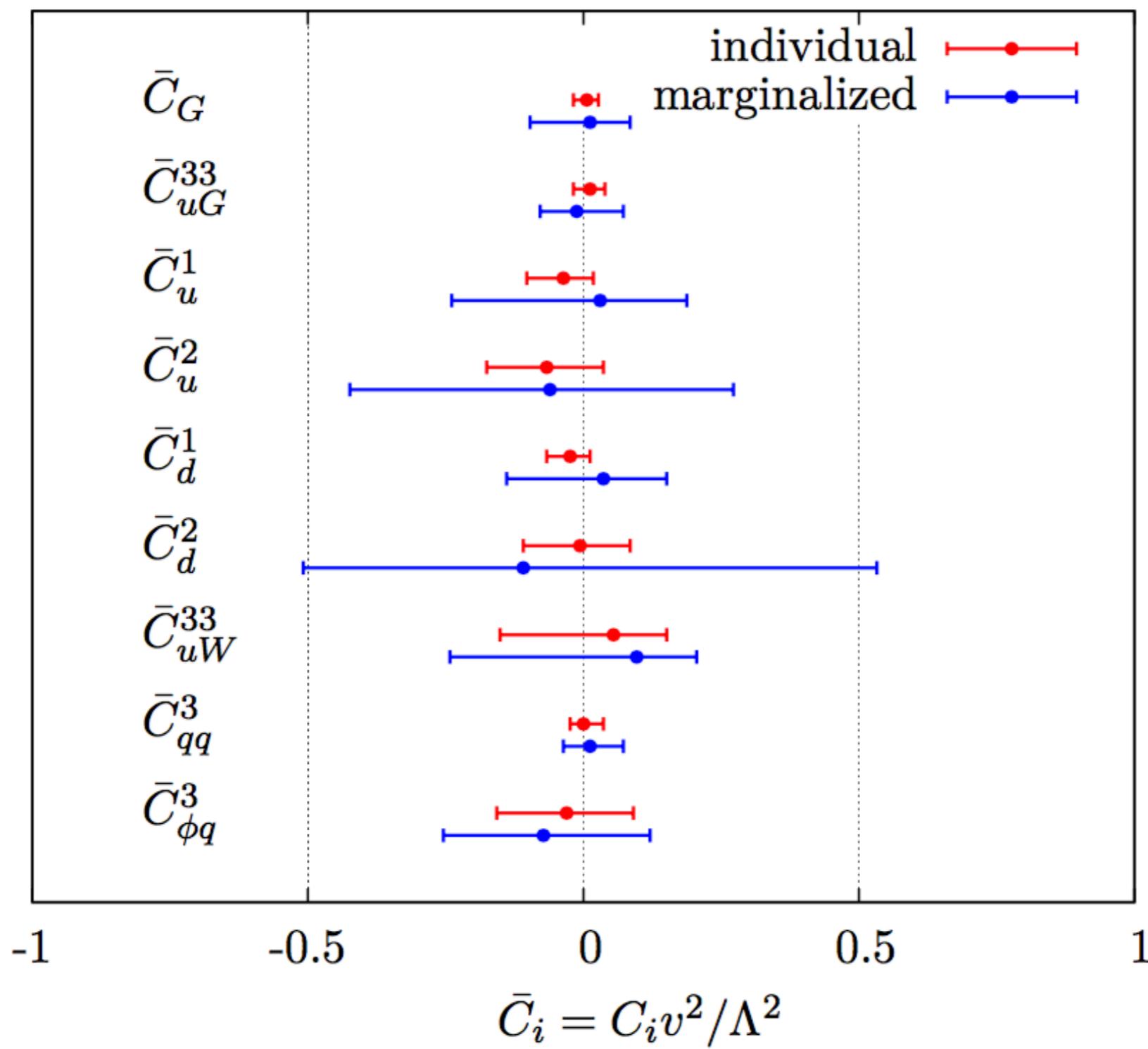
$$O_{\phi q}^3 = i(\phi^\dagger \tau^I \overleftrightarrow{D}_\mu \phi)(\bar{q}\gamma^\mu \tau^I q)$$

Cao, Wudka & Yuan 0704.2809

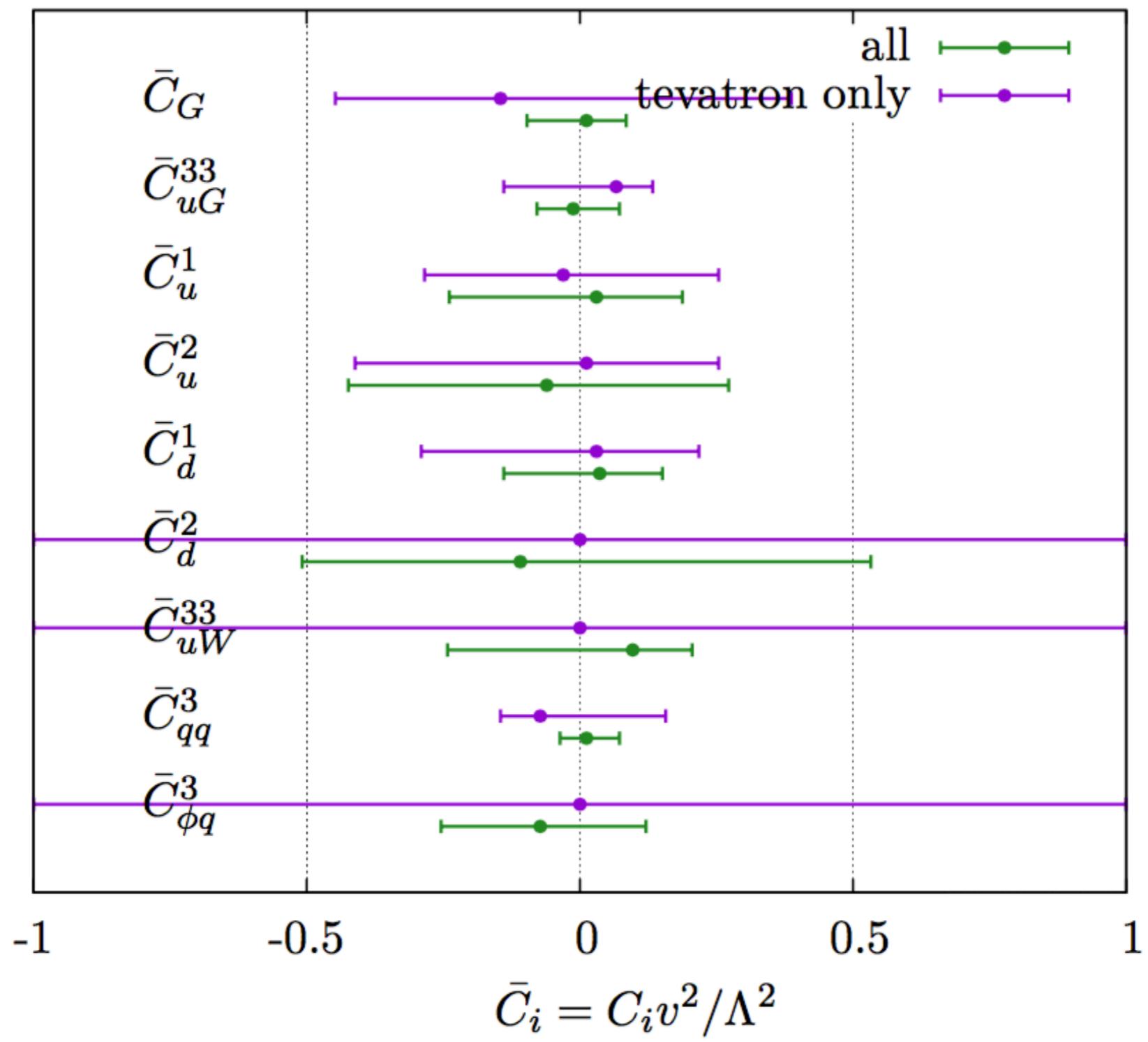
Aguilar-Saavedra 0803.3810

**SUMMARY:** 3 constrainable operators in single top production

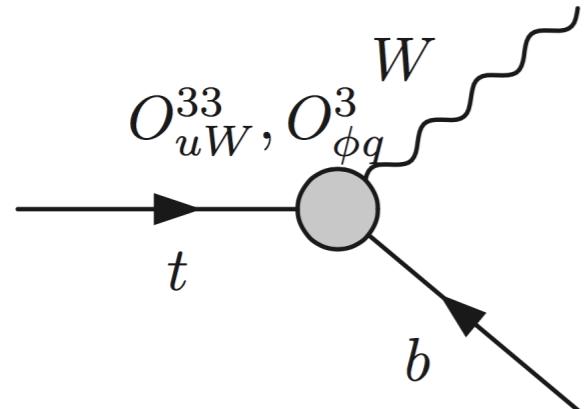
# Bottom-line constraints



# Tevatron vs. LHC



# Decay observables



$$F_0 = \frac{m_t^2}{m_t^2 + 2M_W^2} - \frac{4\sqrt{2}C_{uW}^{33}v^2}{\Lambda^2 V_{tb}} \frac{m_t M_W(m_t^2 - M_W^2)}{(m_t^2 + 2M_W^2)^2}$$

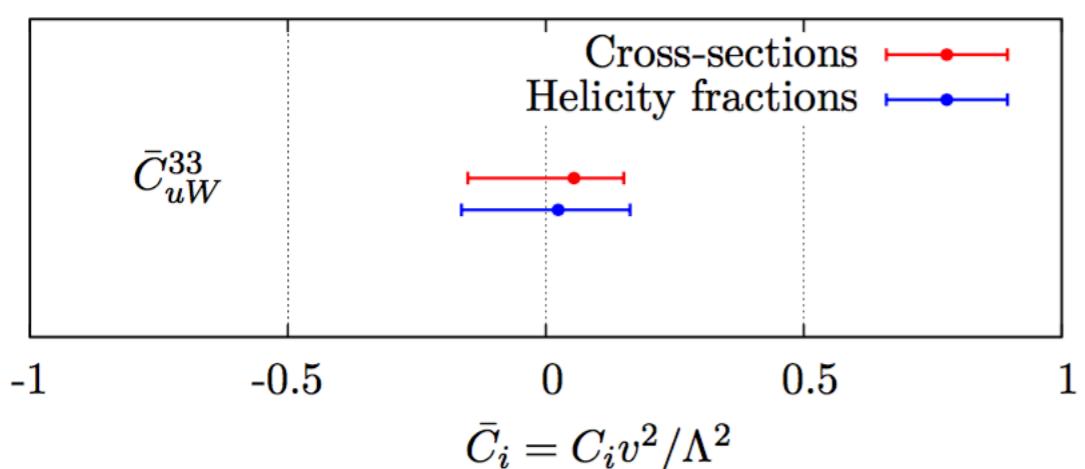
$$F_L = \frac{2M_W^2}{m_t^2 + 2M_W^2} + \frac{4\sqrt{2}C_{uW}^{33}v^2}{\Lambda^2 V_{tb}} \frac{m_t M_W(m_t^2 - M_W^2)}{(m_t^2 + 2M_W^2)^2}$$

$$F_R \simeq 0$$

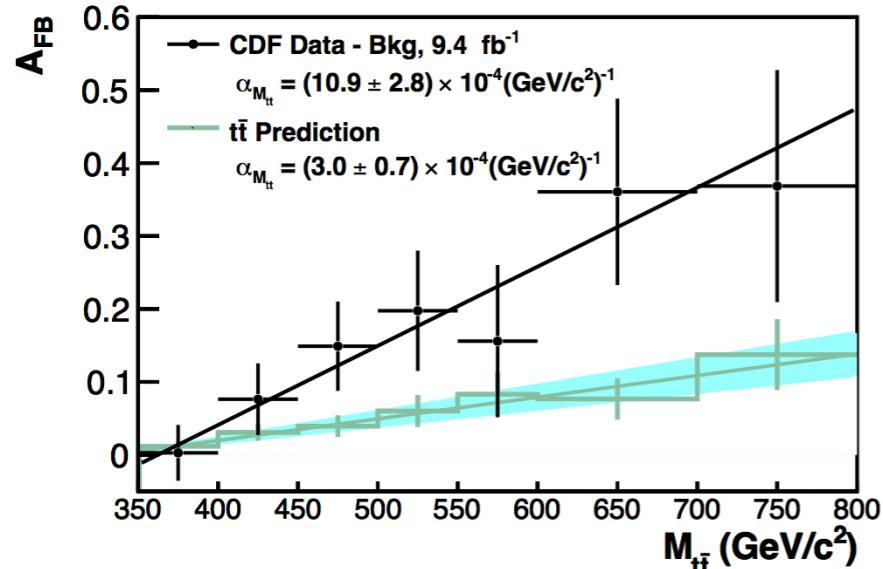
In SM:  $F_0 \approx 0.66$ ,  $F_L \approx 0.33$ ,  $F_R \approx 0$

Stable against  
higher-order  
corrections

Do angular observables give better bounds than total cross-sections?



# Charge asymmetries



$$A_{FB} = \frac{N(\Delta y > 0) - N(\Delta y < 0)}{N(\Delta y > 0) + N(\Delta y < 0)}$$

A<sub>FB</sub> (more or less) explained by large NNLO QCD

*Czakon, Fiedler & Mitov, 1411.3007*

Is there any room for {C<sub>i</sub>}?

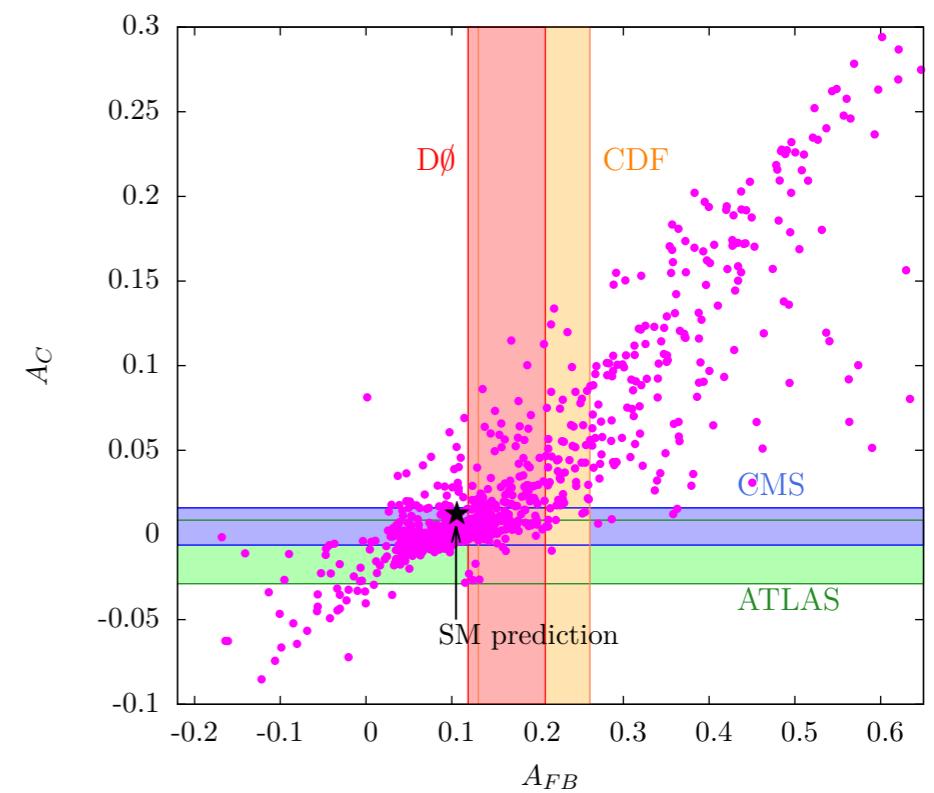
*Hewett, Sheldon, Spannowsky, Tait, Takeuchi 1103.4618*

In EFT language: A<sub>FB</sub> ~ (C<sup>1</sup><sub>u</sub> - C<sup>2</sup><sub>u</sub>) × Λ<sup>-2</sup>

*Zhang and Willenbrock 1008.3869*

correlated with

$$A_C = \frac{N(\Delta|y| > 0) - N(\Delta|y| < 0)}{N(\Delta|y| > 0) + N(\Delta|y| < 0)}$$



# Summary and outlook

Global fit of dimension-six operators to top quark production and decay data

Fitting methods borrowed from Monte Carlo tuning techniques

Run 1 data: Few surprises, all results in agreement with SM, all  $\{C_i\} = 0$  within 95% confidence intervals

Not shown here: Higher-order processes ( $t\bar{t}Z$ ,  $t\bar{t}\gamma$ ), and decay observables (but similar conclusions apply)

## ***Reasons to be cheerful:***

NNLO distributions in top pair production soon to be available, reduction in scale uncertainties

Plenty of room for surprises at run 2.

**All non-resonant new physics is a higher-dimensional operator!**