

# Justifying the $\kappa$ -framework with the non-linear EFT

– Higgs Effective Field Theory workshop, Chicago 2015 –

Claudius Krause

Ludwig-Maximilians-Universität München

November 4th - 6th, 2015

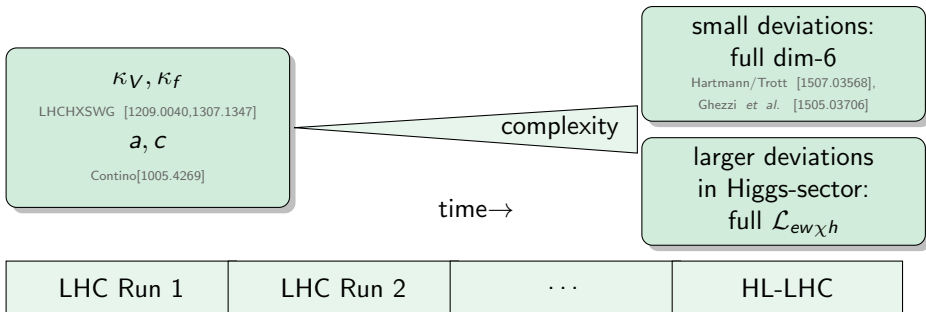


ARNOLD SOMMERFELD  
CENTER FOR THEORETICAL PHYSICS

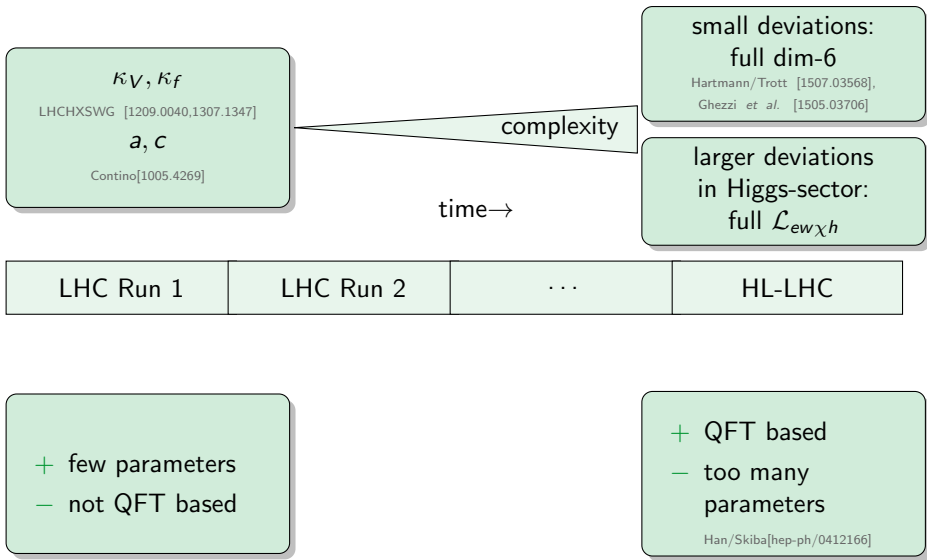


In collaboration with G. Buchalla, O. Catà and A. Celis

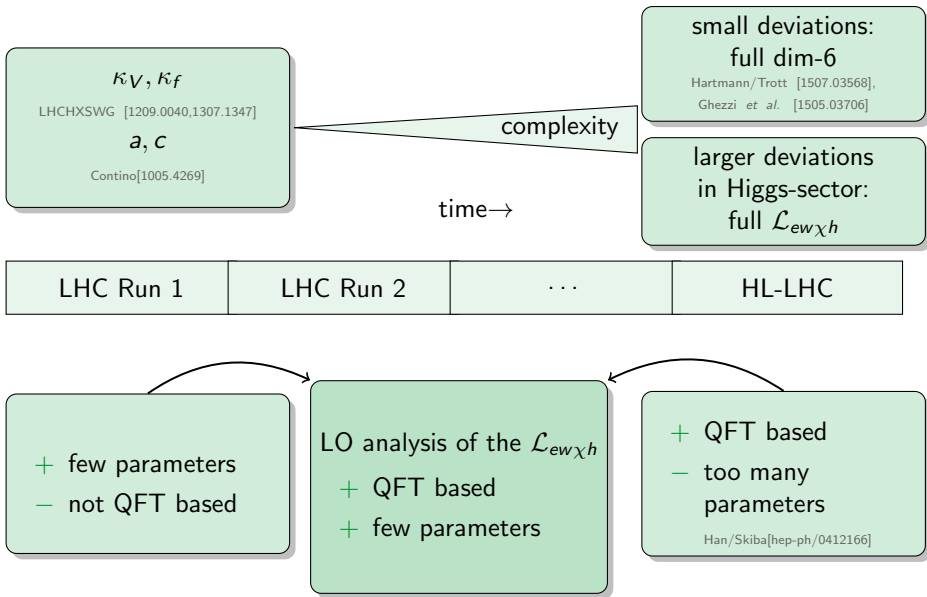
# Between Run-1 and the final stages of the LHC:



# Between Run-1 and the final stages of the LHC:

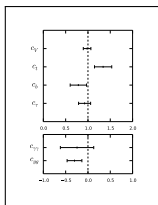
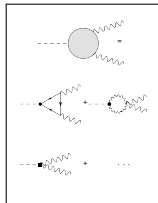


# Between Run-1 and the final stages of the LHC:



# We use the electroweak chiral Lagrangian to analyze LHC data.

Part 1 – from  $\mathcal{L}_{ew\chi h}$  to  $\mathcal{L}_{fit}$  & the  $\kappa$ 's  
[1504.01707]



Part 2 – Fit to LHC Data  
[1511.00988]

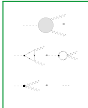


# 1. The electroweak chiral Lagrangian $\mathcal{L}_{ew\chi h}$

## assumptions

Feruglio [hep-ph/9301281], Bagger *et al.* [hep-ph/9306256], Chivukula *et al.* [hep-ph/9312317], Wang/Wang [hep-ph/0605104], Grinstein/Trott[0704.1505], Contino[1005.4269], Alonso *et al.* [1212.3305], ...

- A new strong sector is generating the 3 Goldstones of EWSB and the  $h$ .
- The scale of the new dynamics is given by  $f$ .
- The transverse gauge bosons and the fermions of the SM are weakly coupled.
- The pattern of symmetry breaking is  $SU(2)_L \times SU(2)_R \rightarrow SU(2)_{V=L+R}$



# 1. The electroweak chiral Lagrangian $\mathcal{L}_{ew\chi h}$

## assumptions

Feruglio [hep-ph/9301281], Bagger *et al.* [hep-ph/9306256], Chivukula *et al.* [hep-ph/9312317], Wang/Wang [hep-ph/0605104], Grinstein/Trott[0704.1505], Contino[1005.4269], Alonso *et al.* [1212.3305], ...

- A new strong sector is generating the 3 Goldstones of EWSB and the  $h$ .
- The scale of the new dynamics is given by  $f$ .
- The transverse gauge bosons and the fermions of the SM are weakly coupled.
- The pattern of symmetry breaking is  $SU(2)_L \times SU(2)_R \rightarrow SU(2)_{V=L+R}$

## power counting

Weinberg [Physica A96 '79]; Nyffeler/Schenk [hep-ph/9907294]; Buchalla, Catà, CK [1312.5624]

- The EFT is organized as an expansion in loops.
- This is equivalent to a counting of chiral dimensions:

$$2L + 2 = [\text{couplings}]_\chi + [\text{derivatives}]_\chi + [\text{fields}]_\chi$$

$$[\text{bosons}]_\chi = 0, \quad [\text{fermion bilinears}]_\chi = [\text{derivatives}]_\chi = [\text{weak couplings}]_\chi = 1$$

# 1. The electroweak chiral Lagrangian $\mathcal{L}_{ew\chi h}$

## assumptions

Feruglio [hep-ph/9301281], Bagger *et al.* [hep-ph/9306256], Chivukula *et al.* [hep-ph/9312317], Wang/Wang [hep-ph/0605104], Grinstein/Trott[0704.1505], Contino[1005.4269], Alonso *et al.* [1212.3305], ...

- A new strong sector is generating the 3 Goldstones of EWSB and the  $h$ .
- The scale of the new dynamics is given by  $f$ .
- The transverse gauge bosons and the fermions of the SM are weakly coupled.
- The pattern of symmetry breaking is  $SU(2)_L \times SU(2)_R \rightarrow SU(2)_{V=L+R}$

## power counting

Weinberg [Physica A96 '79], Nuyts [hep-th/0009152], Barbella, Catà, CK [1312.5624]

- The EFT is organized as an expansion in  $\frac{E}{\Lambda}$ .
- This is equivalent to a counting of the number of derivatives and fields.

Example:

$$[gg' B_{\mu\nu} \langle UT_3 U^\dagger W^{\mu\nu} \rangle \mathcal{F}(\frac{h}{v})]_{\chi} = 4 \\ \rightarrow L = 1$$

$$2L + 2 = [\text{couplings}]_{\chi} + [\text{derivatives}]_{\chi} + [\text{fields}]_{\chi}$$

$$[\text{bosons}]_{\chi} = 0, \quad [\text{fermion bilinears}]_{\chi} = [\text{derivatives}]_{\chi} = [\text{weak couplings}]_{\chi} = 1$$





# 1. Current observables select $\mathcal{L}_{\text{fit}}$ from $\mathcal{L}_{\text{ew}\chi h}$ .

$$\mathcal{L}_{\text{ew}\chi h} = \mathcal{L}_{\text{kin}}^{h,\Psi,\text{gauge}} + \frac{v^2}{4} \langle (D_\mu U)(D^\mu U^\dagger) \rangle (1 + F_U(h)) - \mathcal{V}(h) \\ - v (\bar{\Psi}_f Y_{j,f} U \Psi_f + \text{h.c.}) \left(\frac{h}{v}\right)^j + \mathcal{L}_{\text{NLO}}$$

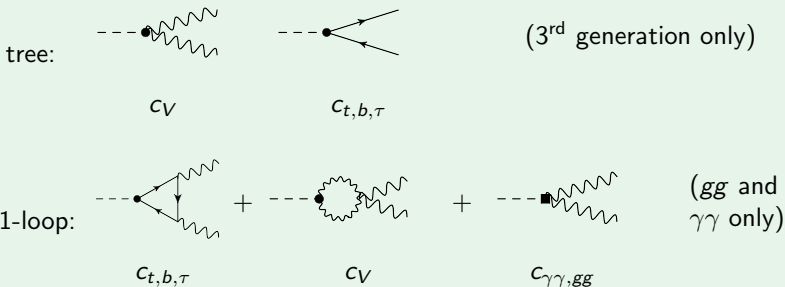
We focus on current observables and phenomenology requires  $f > v$ , i.e.  
 $\xi = v^2/f^2 < 1$ .

# 1. Current observables select $\mathcal{L}_{\text{fit}}$ from $\mathcal{L}_{\text{ew}\chi h}$ .

$$\mathcal{L}_{\text{ew}\chi h} = \mathcal{L}_{\text{kin}}^{h,\Psi,\text{gauge}} + \frac{v^2}{4} \langle (D_\mu U)(D^\mu U^\dagger) \rangle (1 + F_U(h)) - \mathcal{V}(h) \\ - v (\bar{\Psi}_f Y_{j,f} U \Psi_f + \text{h.c.}) \left(\frac{h}{v}\right)^j + \mathcal{L}_{\text{NLO}}$$

We focus on **current observables** and phenomenology requires  $f > v$ , i.e.  $\xi = v^2/f^2 < 1$ .

## Single $h$ processes



# 1. Current observables select $\mathcal{L}_{\text{fit}}$ from $\mathcal{L}_{\text{ew}\chi h}$ .

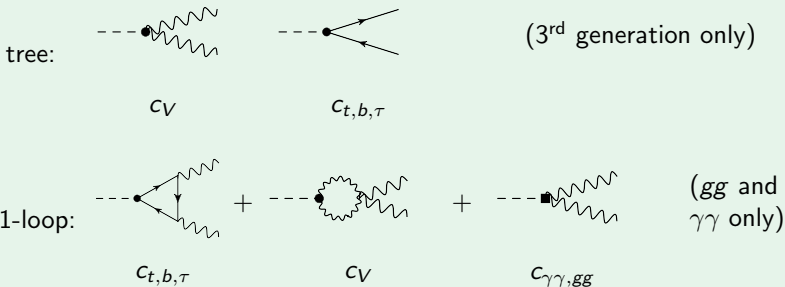
$$\mathcal{L}_{\text{fit}} = 2c_V (m_W^2 W_\mu^+ W^{-\mu} + \frac{1}{2} m_Z^2 Z_\mu Z^\mu) \left(\frac{h}{v}\right) - c_t y_t \bar{t} t h - c_b y_b \bar{b} b h - c_\tau y_\tau \bar{\tau} \tau h$$

$$+ \frac{e^2}{16\pi^2} c_{\gamma\gamma} F_{\mu\nu} F^{\mu\nu} \frac{h}{v} + \frac{g_s^2}{16\pi^2} c_{gg} \langle G_{\mu\nu} G^{\mu\nu} \rangle \frac{h}{v}$$

We focus on **current observables** and phenomenology requires  $f > v$ , i.e.

$$\xi = v^2/f^2 < 1.$$

## Single $h$ processes



# 1. Current observables select $\mathcal{L}_{\text{fit}}$ from $\mathcal{L}_{\text{ew}\chi h}$ .

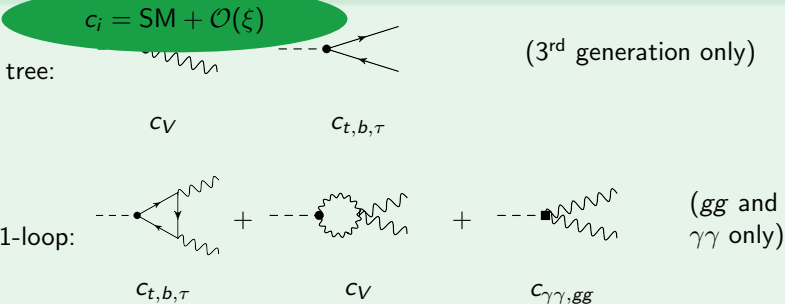
$$\mathcal{L}_{\text{fit}} = 2c_V (m_W^2 W_\mu^+ W^{-\mu} + \frac{1}{2} m_Z^2 Z_\mu Z^\mu) \left(\frac{h}{v}\right) - c_t y_t \bar{t} t h - c_b y_b \bar{b} b h - c_\tau y_\tau \bar{\tau} \tau h$$

$$+ \frac{e^2}{16\pi^2} c_{\gamma\gamma} F_{\mu\nu} F^{\mu\nu} \frac{h}{v} + \frac{g_s^2}{16\pi^2} c_{gg} \langle G_{\mu\nu} G^{\mu\nu} \rangle \frac{h}{v}$$

We focus on current observables and phenomenology requires  $f > v$ , i.e.

$$\xi = v^2/f^2 < 1.$$

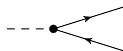
Single  $h$  processes



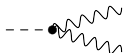
# 1. There is a relation between the electroweak chiral Lagrangian and the $\kappa$ framework.



$\mathcal{L}_{ew\chi h}$



$C_{t,b,\tau}$

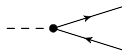


$C_V$

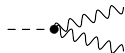
tree:

$$\kappa_i^2 = \Gamma^i / \Gamma_{SM}^i, \quad \kappa_i^2 = \sigma^i / \sigma_{SM}^i$$

LHCHXSWG [1209.0040,1307.1347]



$\kappa_{t,b,\tau}$



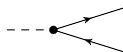
$\kappa_V$

tree:

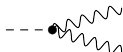
# 1. There is a relation between the electroweak chiral Lagrangian and the $\kappa$ framework.



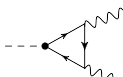
$\mathcal{L}_{ew\chi h}$



$C_{t,b,\tau}$



$C_V$



$C_{t,b,\tau}$



$C_V$



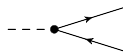
$C_{\gamma\gamma,gg}$

tree:

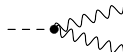
1-loop:

$$\kappa_i^2 = \Gamma^i / \Gamma_{SM}^i, \quad \kappa_i^2 = \sigma^i / \sigma_{SM}^i$$

LHCHXSWG [1209.0040,1307.1347]



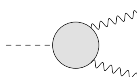
$\kappa_{t,b,\tau}$



$\kappa_V$

tree:

1-loop:

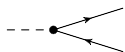


$\kappa_{\gamma,g}$

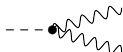
# 1. There is a relation between the electroweak chiral Lagrangian and the $\kappa$ framework.



$\mathcal{L}_{ew\chi h}$



$C_{t,b,\tau}$

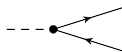


$C_V$

tree:

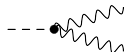
$$\kappa_i^2 = \Gamma^i / \Gamma_{SM}^i, \quad \kappa_i^2 = \sigma^i / \sigma_{SM}^i$$

LHCHXSWG [1209.0040,1307.1347]



$\kappa_{t,b,\tau}$

tree:



$\kappa_V$

Both have the same number of free parameters:

$$\{C_V, C_{t,b,\tau}, C_{\gamma\gamma}, C_{gg}\} \quad \text{vs.} \quad \{\kappa_V, \kappa_{t,b,\tau}, \kappa_\gamma, \kappa_g\}$$

$\Rightarrow$   $\kappa$ 's are QFT consistent and with small modifications directly interpretable within an EFT!



$C_{\gamma\gamma,gg}$

# 1. The $\kappa$ framework cannot be recovered as a limit of the SMEFT (dim 6).

Full dimension 6 Grzadkowski *et al.* [1008.4884]:

example:  $h \rightarrow Z\gamma$

LO:







# 1. The $\kappa$ framework cannot be recovered as a limit of the SMEFT (dim 6).

Full dimension 6 Grzadkowski *et al.* [1008.4884]:

example:  $h \rightarrow Z\gamma$

LO:

$$\begin{array}{ccccccc}
 \text{---} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} \\
 & \text{SM} & + & \text{SM} & + & \mathcal{O}\left(\frac{v^2}{\Lambda^2}\right) & + \dots
 \end{array}$$

LO + NLO:

$$\begin{array}{ccccccc}
 \text{---} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} \\
 \text{SM} + \mathcal{O}\left(\frac{v^2}{\Lambda^2}\right) & + & \mathcal{O}\left(\frac{v^2}{16\pi^2\Lambda^2}\right) & + & \mathcal{O}\left(\frac{v^2}{16\pi^2\Lambda^2}\right) & + & \dots
 \end{array}$$



# 1. The $\kappa$ framework cannot be recovered as a limit of the SMEFT (dim 6).

Full dimension 6 Grzadkowski *et al.* [1008.4884]:

example:  $h \rightarrow Z\gamma$

LO:

$$\begin{array}{ccccccc}
 \text{---} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} & \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{array} & + & \text{---} & \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{array} & + & \text{---} & \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{array} & + & \dots \\
 & \text{SM} & & + & \text{SM} & & + & \mathcal{O}\left(\frac{v^2}{\Lambda^2}\right) & & & 
 \end{array}$$

LO + NLO:

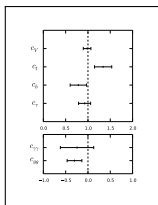
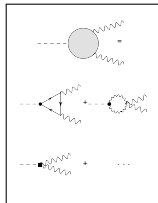
$$\begin{array}{ccccccc}
 \text{---} & \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{array} & + & \text{---} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} & + & \text{---} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} & + & \dots \\
 \text{SM} + \mathcal{O}\left(\frac{v^2}{\Lambda^2}\right) & & + & \mathcal{O}\left(\frac{v^2}{16\pi^2\Lambda^2}\right) & & + & \mathcal{O}\left(\frac{v^2}{16\pi^2\Lambda^2}\right) & & & 
 \end{array}$$

Additional assumption of weakly coupled UV Einhorn/Wudka[1307.0478]:

$$\begin{array}{ccccccc}
 \text{---} & \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{array} & + & \text{---} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} & + & \text{---} & \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} & + & \dots \\
 \text{SM} + \mathcal{O}\left(\frac{v^2}{16\pi^2\Lambda^2}\right) & & + & \mathcal{O}\left(\frac{v^2}{16\pi^2\Lambda^2}\right) & & + & \mathcal{O}\left(\frac{v^2}{16\pi^2\Lambda^2}\right) & & & 
 \end{array}$$

# We use the electroweak chiral Lagrangian to analyze LHC data.

Part 1 – from  $\mathcal{L}_{ew\chi h}$  to  $\mathcal{L}_{fit}$  & the  $\kappa$ 's  
[1504.01707]



Part 2 – Fit to LHC Data  
[1511.00988]



## 2. We performed a Bayesian fit to LHC data.

Bayes Theorem:

$$\left( \begin{array}{l} \text{posterior pdf} \\ \text{probability of the} \\ \text{parameters, given data} \end{array} \right) = \text{prior} \times \left( \begin{array}{l} \text{Likelihood} \\ \text{probability of data,} \\ \text{given the parameters} \end{array} \right)$$



## 2. We performed a Bayesian fit to LHC data.

Bayes Theorem:

$$\left( \begin{array}{l} \text{posterior pdf} \\ \text{probability of the} \\ \text{parameters, given data} \end{array} \right) = \text{prior} \times \left( \begin{array}{l} \text{Likelihood} \\ \text{probability of data,} \\ \text{given the parameters} \end{array} \right)$$

flat prior in

- $c_V \in [0.5, 1.5]$
- $c_{f=t,b,\tau} \in [0, 2]$
- $c_{\gamma\gamma} \in [-1.5, 1.5]$
- $c_{gg} \in [-1, 1]$

Likelihood

- given by the code `Lilith`  
Bernon/Dumont[1502.04138]
- using DB 15.09  
[ATLAS-CONF-2015-044,  
CMS-PAS-HIG- 15-002]



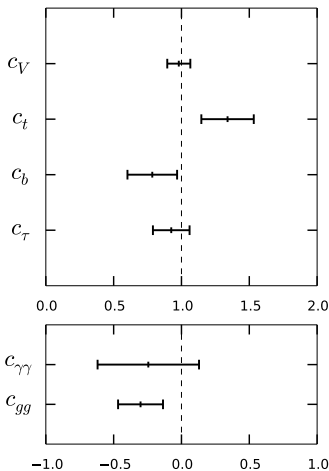
## 2. We performed a Bayesian fit to LHC data.

Results:

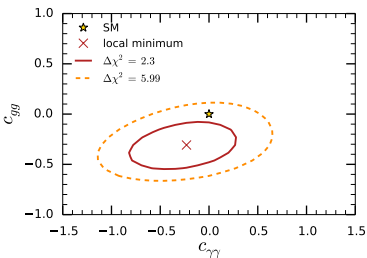
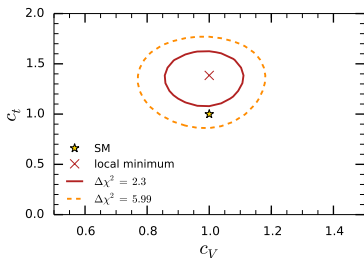
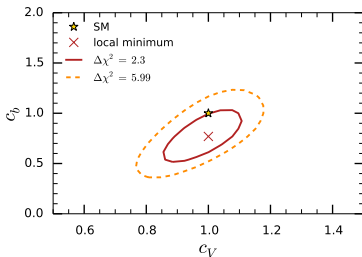
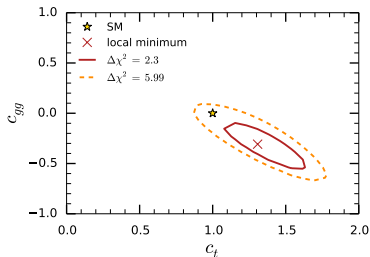
$$\begin{pmatrix} c_V \\ c_t \\ c_b \\ c_\tau \\ c_{\gamma\gamma} \\ c_{gg} \end{pmatrix} = \begin{pmatrix} 0.98 & \pm & 0.08 \\ 1.37 & \pm & 0.22 \\ 0.83 & \pm & 0.19 \\ 0.95 & \pm & 0.14 \\ -0.41 & \pm & 0.38 \\ -0.31 & \pm & 0.16 \end{pmatrix}$$

$$\rho_{ij} = \frac{\text{cov}(c_i, c_j)}{\sigma_i \sigma_j} =$$

$$\begin{pmatrix} 1.0 & 0.09 & 0.68 & 0.42 & 0.33 & 0.06 \\ . & 1.0 & 0.16 & 0.01 & -0.43 & -0.73 \\ . & . & 1.0 & 0.59 & -0.07 & 0.24 \\ . & . & . & 1.0 & -0.07 & 0.18 \\ . & . & . & . & 1.0 & 0.32 \\ . & . & . & . & . & 1.0 \end{pmatrix}$$



## 2. We performed a Bayesian fit to LHC data.

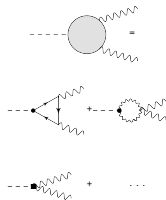


# Conclusions

- ④ The electroweak chiral Lagrangian analysis at leading order [1504.01707]

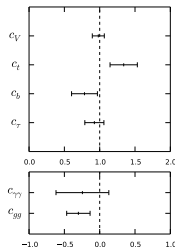
- ▶ justifies the  $\kappa$  framework
- ▶ is suitable for current LHC analyses, since it is based on EFT and has rel. few parameters.

This is in contrast to the dim-6 analysis, where new physics effects arise at NLO.



- ② We fitted the set  $\{c_V, c_t, c_b, c_\tau, c_{\gamma\gamma}, c_{gg}\}$  to LHC data: [1511.00988]

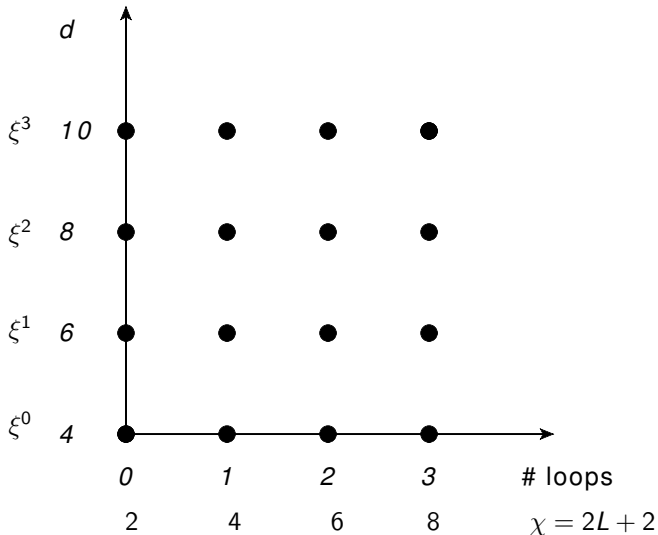
$$\begin{pmatrix} c_V \\ c_t \\ c_b \\ c_\tau \\ c_{\gamma\gamma} \\ c_{gg} \end{pmatrix} = \begin{pmatrix} 0.98 & \pm & 0.08 \\ 1.37 & \pm & 0.22 \\ 0.83 & \pm & 0.19 \\ 0.95 & \pm & 0.14 \\ -0.41 & \pm & 0.38 \\ -0.31 & \pm & 0.16 \end{pmatrix}$$



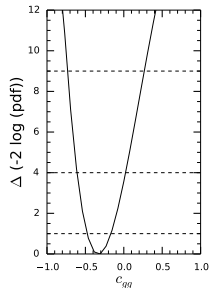
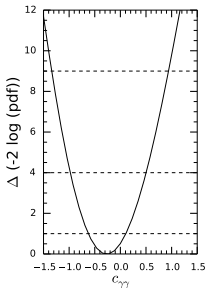
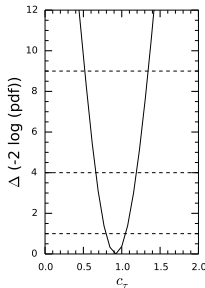
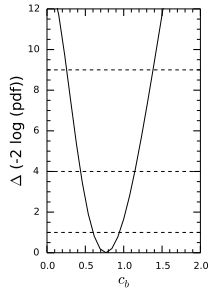
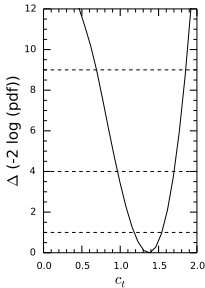
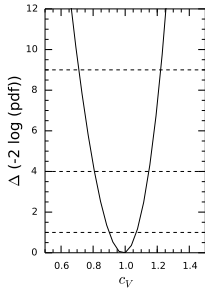


# Backup

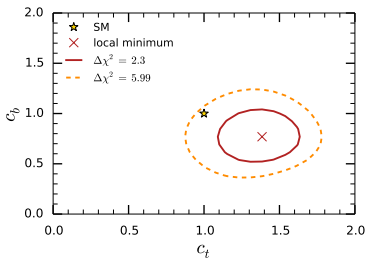
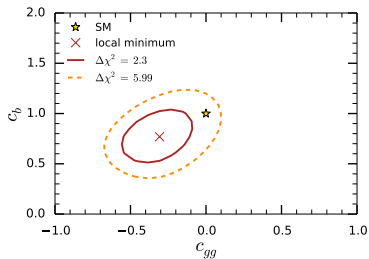
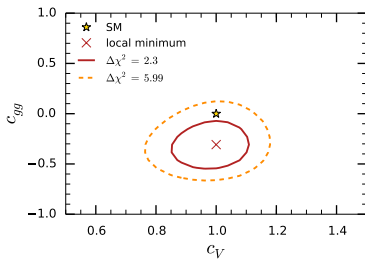
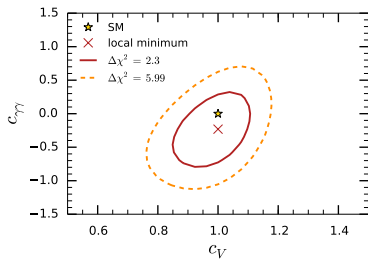
## The difference between expansions in canonical and chiral dimensions:



# $\Delta\chi^2$ for the one-dimensional marginalized pdf:



## Further 2-dim plots



## Further 2-dim plots

