

# Justifying the $\kappa$ -framework with the non-linear EFT

– Higgs Effective Field Theory workshop, Chicago 2015 –

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Ludwig-Maximilians-Universität München

November 4th - 6th, 2015



LUDWIG-  
MAXIMILIANS-  
UNIVERSITÄT  
MÜNCHEN

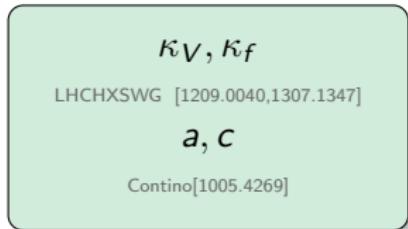


ARNOLD SOMMERFELD  
CENTER FOR THEORETICAL PHYSICS



In collaboration with G. Buchalla, O. Catà and A. Celis

# Between Run-1 and the final stages of the LHC:

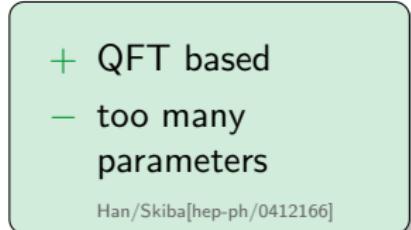
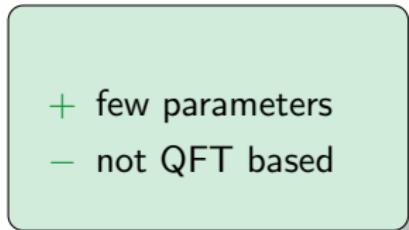
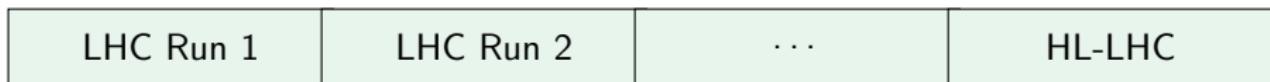
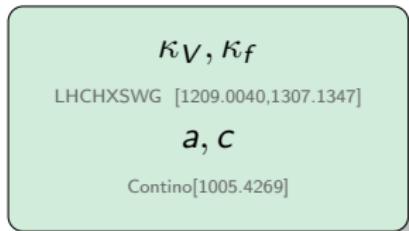


complexity

time →

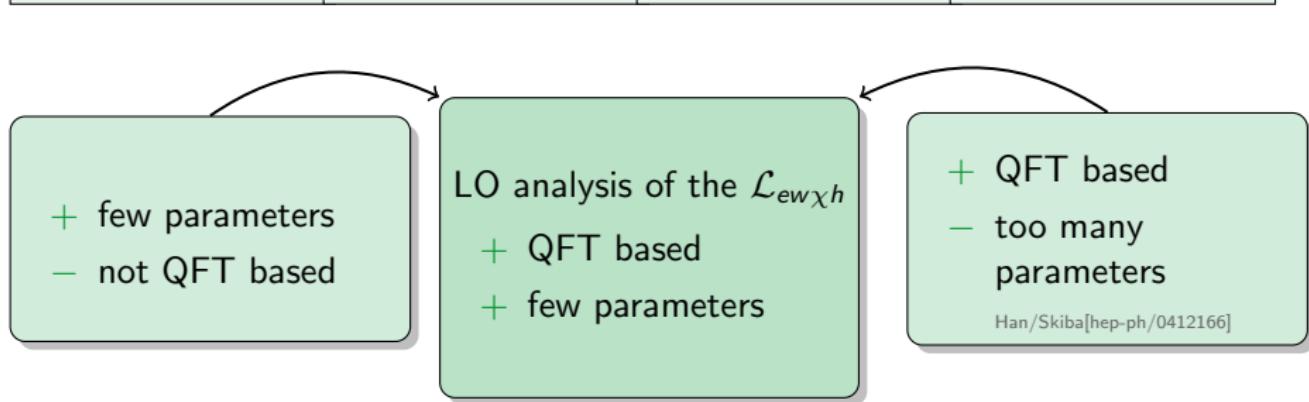
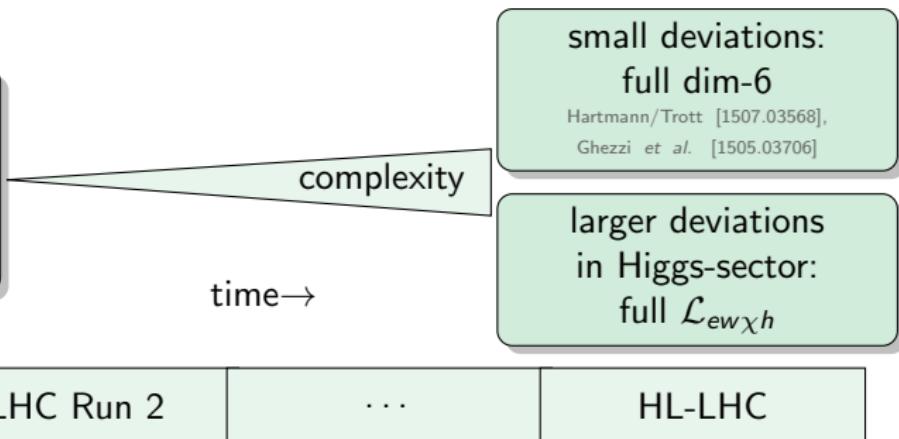


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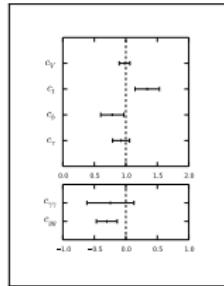
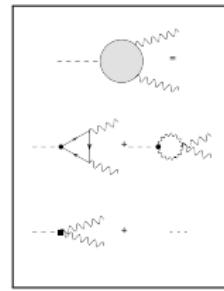
# Between Run-1 and the final stages of the LHC:

$\kappa_V, \kappa_f$   
LHCHXSWG [1209.0040,1307.1347]  
 $a, c$   
Contino[1005.4269]

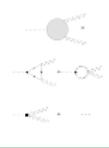


We use the electroweak chiral Lagrangian  
to analyze LHC data.

Part 1 – from  $\mathcal{L}_{ew\chi h}$  to  $\mathcal{L}_{\text{fit}}$  & the  $\kappa$ 's  
[1504.01707]



Part 2 – Fit to LHC Data  
[1511.00988]

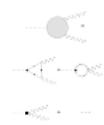


# 1. The electroweak chiral Lagrangian $\mathcal{L}_{ew\chi h}$

## assumptions

Feruglio [hep-ph/9301281], Bagger *et al.* [hep-ph/9306256], Chivukula *et al.* [hep-ph/9312317],  
Wang/Wang [hep-ph/0605104], Grinstein/Trott[0704.1505], Contino[1005.4269], Alonso *et al.* [1212.3305], ...

- A new strong sector is generating the 3 Goldstones of EWSB and the  $h$ .
- The scale of the new dynamics is given by  $f$ .
- The transverse gauge bosons and the fermions of the SM are weakly coupled.
- The pattern of symmetry breaking is  $SU(2)_L \times SU(2)_R \rightarrow SU(2)_{V=L+R}$



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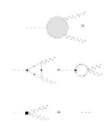
## power counting

Weinberg [Physica A96 '79]; Nyffeler/Schenk [hep-ph/9907294]; Buchalla, Catà, CK [1312.5624]

- The EFT is organized as an expansion in loops.
- This is equivalent to a counting of chiral dimensions:

$$2L + 2 = [\text{couplings}]_\chi + [\text{derivatives}]_\chi + [\text{fields}]_\chi$$

$$[\text{bosons}]_\chi = 0, \quad [\text{fermion bilinears}]_\chi = [\text{derivatives}]_\chi = [\text{weak couplings}]_\chi = 1$$



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## power counting

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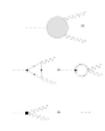
- The EFT is organized as an expansion in powers of  $1/f$
- This is equivalent to a count of dimensions

Example:

$$[gg' B_{\mu\nu} \langle UT_3 U^\dagger W^{\mu\nu} \rangle \mathcal{F}(\frac{h}{v})]_\chi = 4$$
$$\rightarrow L = 1$$

$$2L + 2 = [\text{couplings}]_\chi + [\text{derivatives}]_\chi + [\text{fields}]_\chi$$

$$[\text{bosons}]_\chi = 0, \quad [\text{fermion bilinears}]_\chi = [\text{derivatives}]_\chi = [\text{weak couplings}]_\chi = 1$$

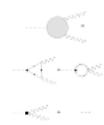


# 1. Current observables select $\mathcal{L}_{\text{fit}}$ from $\mathcal{L}_{\text{ew}\chi h}$ .

$$\begin{aligned}\mathcal{L}_{\text{ew}\chi h} = & \mathcal{L}_{\text{kin}}^{h,\Psi,\text{gauge}} + \frac{v^2}{4} \langle (D_\mu U)(D^\mu U^\dagger) \rangle (1 + F_U(h)) - \mathcal{V}(h) \\ & - v (\bar{\Psi}_f Y_{j,f} U \Psi_f + \text{h.c.}) \left(\frac{h}{v}\right)^j + \mathcal{L}_{\text{NLO}}\end{aligned}$$

We focus on current observables and phenomenology requires  $f > v$ , i.e.

$$\xi = v^2/f^2 < 1.$$



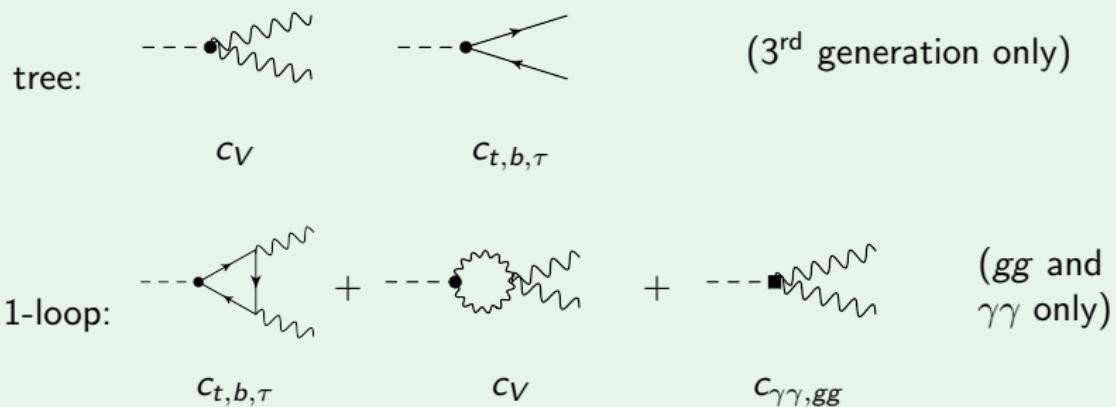
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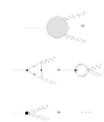
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## Single $h$ processes





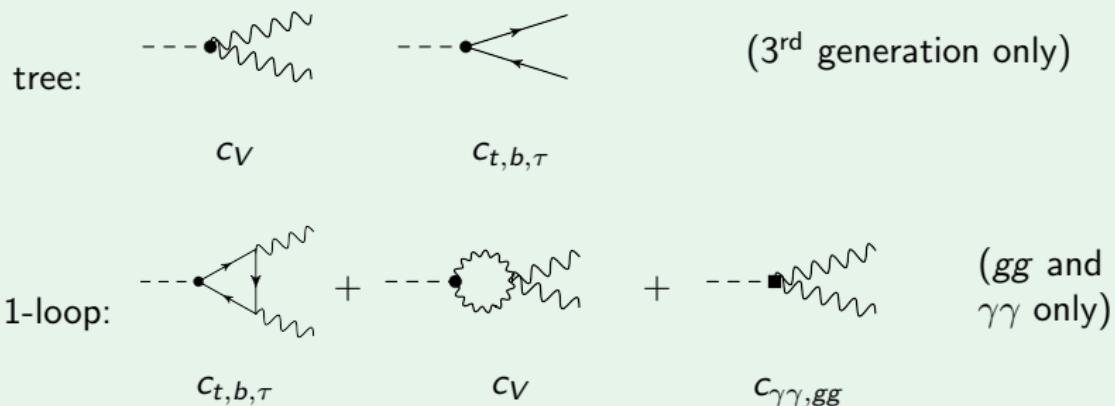
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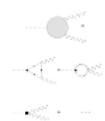
$$\begin{aligned}\mathcal{L}_{\text{fit}} = & 2cv \left( m_W^2 W_\mu^+ W^{-\mu} + \frac{1}{2} m_Z^2 Z_\mu Z^\mu \right) \left( \frac{h}{v} \right) - c_t y_t \bar{t} t h - c_b y_b \bar{b} b h - c_\tau y_\tau \bar{\tau} \tau h \\ & + \frac{e^2}{16\pi^2} c_{\gamma\gamma} F_{\mu\nu} F^{\mu\nu} \frac{h}{v} + \frac{g_s^2}{16\pi^2} c_{gg} \langle G_{\mu\nu} G^{\mu\nu} \rangle \frac{h}{v}\end{aligned}$$

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## Single $h$ processes





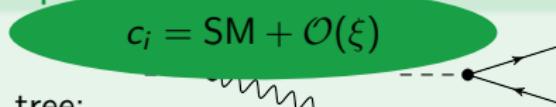
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**Single  $h$  processes**



tree:

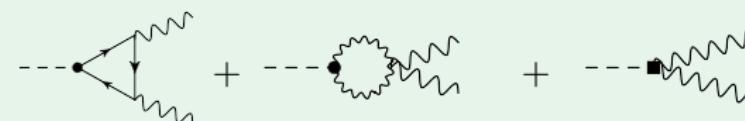
(3rd generation only)

$c_V$

$c_{t,b,\tau}$

1-loop:

( $gg$  and  
 $\gamma\gamma$  only)



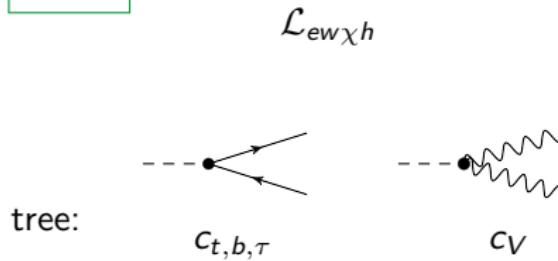
$c_{t,b,\tau}$

$c_V$

$c_{\gamma\gamma, gg}$

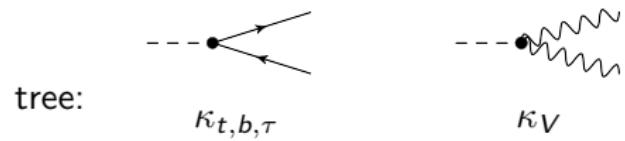


# 1. There is a relation between the electroweak chiral Lagrangian and the $\kappa$ framework.



$$\kappa_i^2 = \Gamma^i / \Gamma_{\text{SM}}^i, \quad \kappa_i^2 = \sigma^i / \sigma_{\text{SM}}^i$$

LHCHXSWG [1209.0040, 1307.1347]





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$$\mathcal{L}_{ew\chi h}$$

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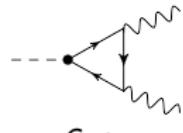


$$c_{t,b,\tau}$$



$$c_V$$

1-loop:



$$c_{t,b,\tau}$$



$$c_V$$

+

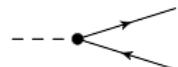


$$c_{\gamma\gamma,gg}$$

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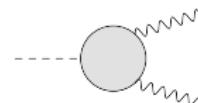


$$\kappa_{t,b,\tau}$$



$$\kappa_V$$

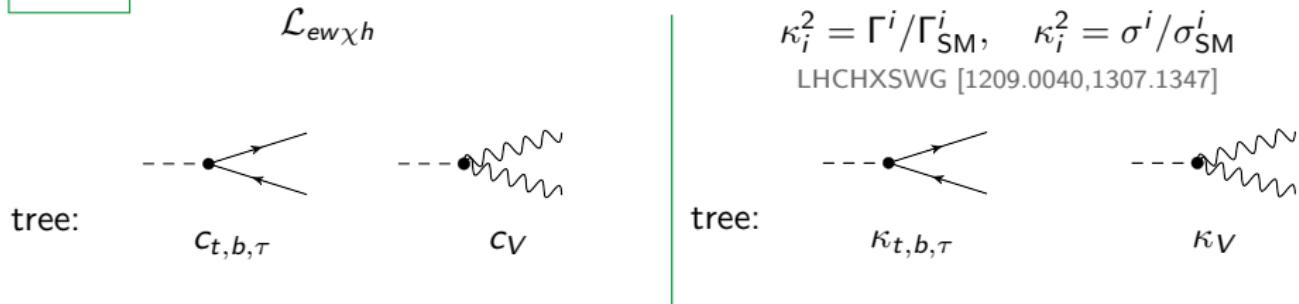
1-loop:



$$\kappa_{\gamma,g}$$



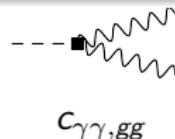
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Both have the same number of free parameters:

$$\{c_V, c_{t,b,\tau}, c_{\gamma\gamma}, c_{gg}\} \quad vs. \quad \{\kappa_V, \kappa_{t,b,\tau}, \kappa_\gamma, \kappa_g\}$$

⇒  $\kappa$ 's are QFT consistent and with small modifications directly interpretable within an EFT!





# 1. The $\kappa$ framework cannot be recovered as a limit of the SMEFT (dim 6).

Full dimension 6 Grzadkowski *et al.* [1008.4884]:

LO:

example:  $h \rightarrow Z\gamma$

$$\text{SM} + \text{SM} + \mathcal{O}\left(\frac{v^2}{\Lambda^2}\right) + \dots$$

The diagram shows a series of Feynman diagrams for the decay of a scalar particle  $h$  into a  $Z$  boson and a photon ( $Z\gamma$ ). The first term is the Standard Model (SM) contribution, shown as a triangle loop with a vertical wavy line entering from the left. The second term is also labeled 'SM' and shows a more complex loop with multiple internal lines. The third term is labeled  $\mathcal{O}\left(\frac{v^2}{\Lambda^2}\right)$  and includes a box-like diagram with a wavy line entering from the left. Ellipses indicate higher-order terms.



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LO:

$$\text{SM} + \text{SM} + \mathcal{O}\left(\frac{v^2}{\Lambda^2}\right) + \dots$$

Diagram: A sum of three terms. The first is the Standard Model (SM) vertex. The second is the SM vertex with a loop. The third is the SM vertex with a box. All diagrams involve a dashed line and a wavy line.

example:  $h \rightarrow Z\gamma$

LO + NLO:

$$\text{SM} + \mathcal{O}\left(\frac{v^2}{\Lambda^2}\right) + \mathcal{O}\left(\frac{v^2}{16\pi^2\Lambda^2}\right) + \mathcal{O}\left(\frac{v^2}{16\pi^2\Lambda^2}\right) + \dots$$

Diagram: A sum of four terms. The first is the SM vertex with a box. The second is the SM vertex with a loop and a box. The third is the SM vertex with a box and a loop. All diagrams involve a dashed line and a wavy line.



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$$\begin{array}{c} \text{---} \quad \text{---} \\ \diagdown \quad \diagup \\ \text{SM} \end{array} + \begin{array}{c} \text{---} \quad \text{---} \\ \diagup \quad \diagdown \\ \text{SM} \end{array} + \begin{array}{c} \text{---} \quad \text{---} \\ \diagup \quad \diagup \\ \mathcal{O}(\frac{v^2}{\Lambda^2}) \end{array} + \dots$$

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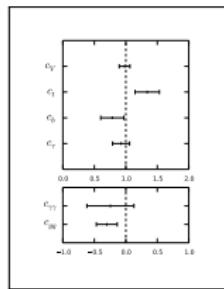
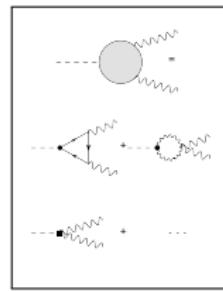
Additional assumption of weakly coupled UV Einhorn/Wudka[1307.0478]:

$$\begin{array}{c} \text{---} \quad \text{---} \\ \diagdown \quad \diagup \\ \text{SM} + \mathcal{O}(\frac{v^2}{16\pi^2\Lambda^2}) \end{array} + \begin{array}{c} \text{---} \quad \text{---} \\ \diagup \quad \diagdown \\ \mathcal{O}(\frac{v^2}{16\pi^2\Lambda^2}) \end{array} + \begin{array}{c} \text{---} \quad \text{---} \\ \diagup \quad \diagup \\ \mathcal{O}(\frac{v^2}{16\pi^2\Lambda^2}) \end{array} + \dots$$

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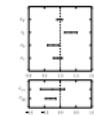
Part 2 – Fit to LHC Data  
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## 2. We performed a Bayesian fit to LHC data.

Bayes Theorem:

$$\left( \begin{array}{c} \text{posterior pdf} \\ \text{probability of the} \\ \text{parameters, given data} \end{array} \right) = \text{prior} \times \left( \begin{array}{c} \text{Likelihood} \\ \text{probability of data,} \\ \text{given the parameters} \end{array} \right)$$



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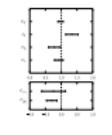
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flat prior in

- $c_V \in [0.5, 1.5]$
- $c_{f=t,b,\tau} \in [0, 2]$
- $c_{\gamma\gamma} \in [-1.5, 1.5]$
- $c_{gg} \in [-1, 1]$

Likelihood

- given by the code **Lilith**  
Beroni/Dumont[1502.04138]
- using **DB 15.09**  
[ATLAS-CONF-2015-044,  
CMS-PAS-HIG- 15-002]



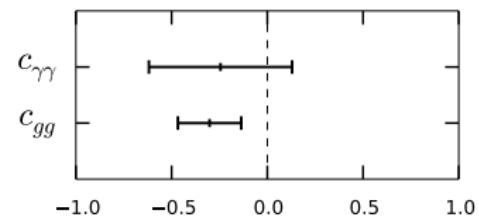
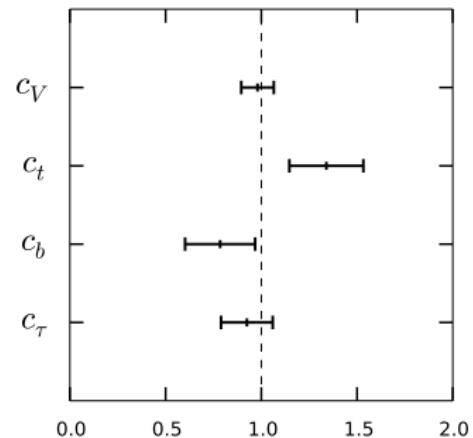
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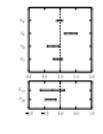
Results:

$$\begin{pmatrix} c_V \\ c_t \\ c_b \\ c_\tau \\ c_{\gamma\gamma} \\ c_{gg} \end{pmatrix} = \begin{pmatrix} 0.98 & \pm & 0.08 \\ 1.37 & \pm & 0.22 \\ 0.83 & \pm & 0.19 \\ 0.95 & \pm & 0.14 \\ -0.41 & \pm & 0.38 \\ -0.31 & \pm & 0.16 \end{pmatrix}$$

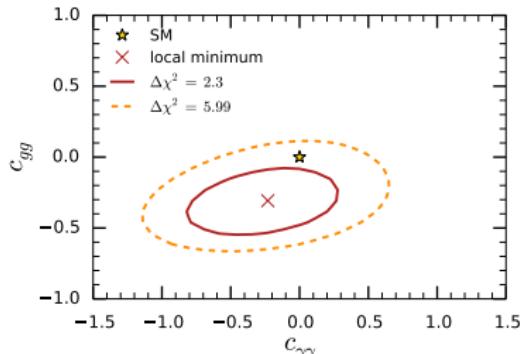
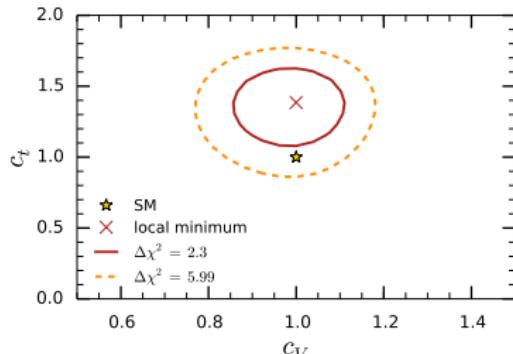
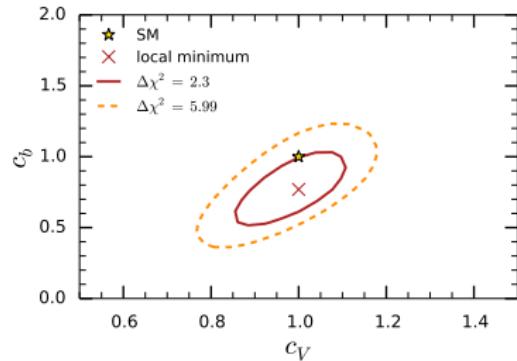
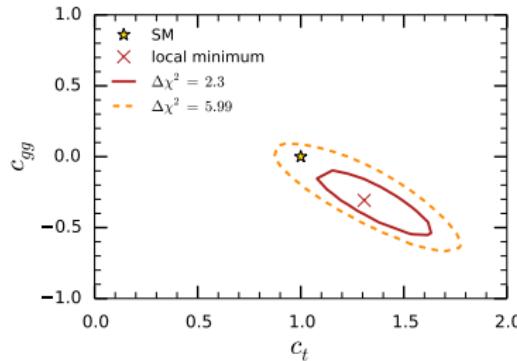
$$\rho_{ij} = \frac{\text{cov}(c_i, c_j)}{\sigma_i \sigma_j} =$$

$$\begin{pmatrix} 1.0 & 0.09 & 0.68 & 0.42 & 0.33 & 0.06 \\ . & 1.0 & 0.16 & 0.01 & -0.43 & -0.73 \\ . & . & 1.0 & 0.59 & -0.07 & 0.24 \\ . & . & . & 1.0 & -0.07 & 0.18 \\ . & . & . & . & 1.0 & 0.32 \\ . & . & . & . & . & 1.0 \end{pmatrix}$$





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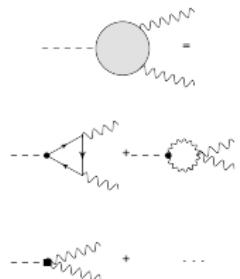


# Conclusions

- ① The electroweak chiral Lagrangian analysis at leading order [1504.01707]

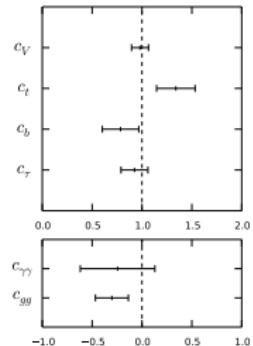
- ▶ justifies the  $\kappa$  framework
- ▶ is suitable for current LHC analyses,  
since it is based on EFT and has rel. few parameters.

This is in contrast to the dim-6 analysis, where new physics effects arise at NLO.



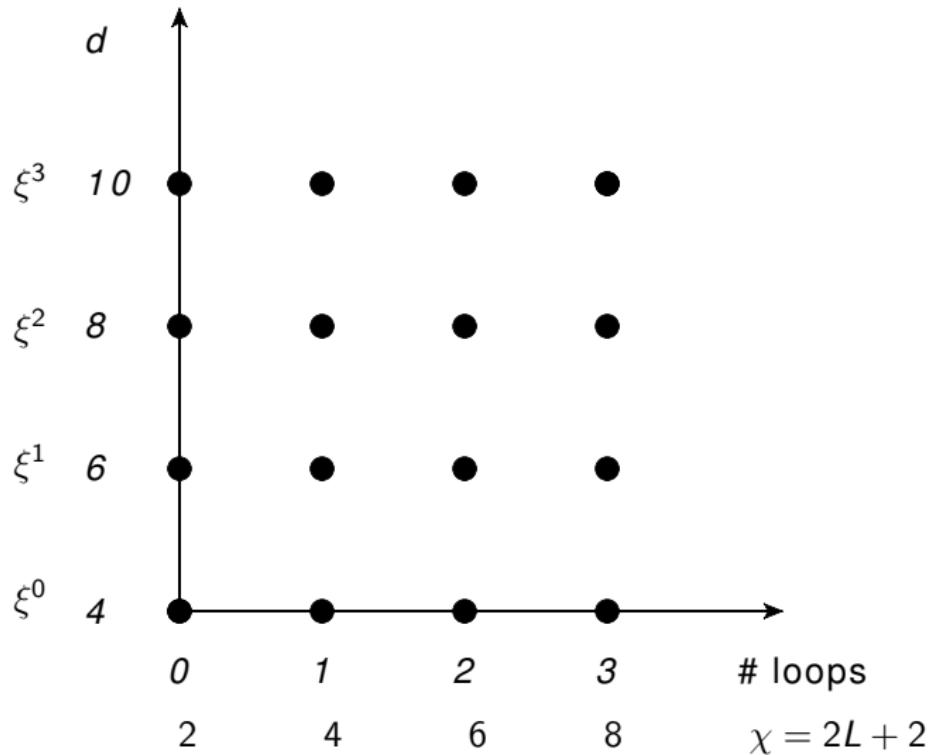
- ② We fitted the set  $\{c_V, c_t, c_b, c_\tau, c_{\gamma\gamma}, c_{gg}\}$  to LHC data:  
[1511.00988]

$$\begin{pmatrix} c_V \\ c_t \\ c_b \\ c_\tau \\ c_{\gamma\gamma} \\ c_{gg} \end{pmatrix} = \begin{pmatrix} 0.98 & \pm & 0.08 \\ 1.37 & \pm & 0.22 \\ 0.83 & \pm & 0.19 \\ 0.95 & \pm & 0.14 \\ -0.41 & \pm & 0.38 \\ -0.31 & \pm & 0.16 \end{pmatrix}$$

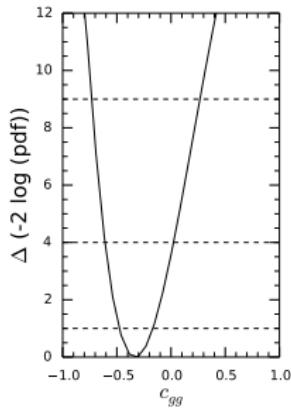
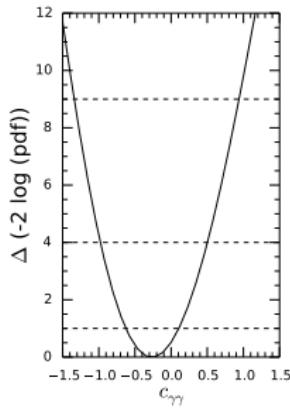
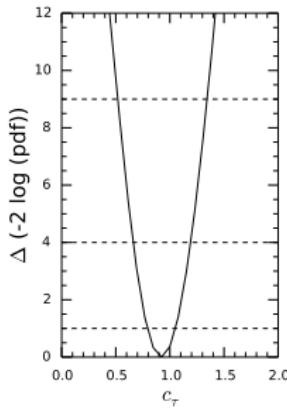
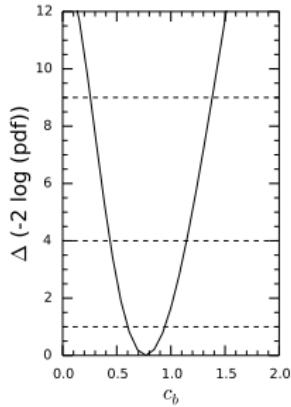
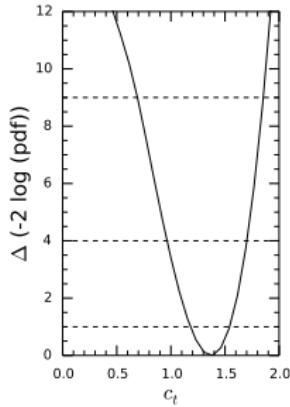
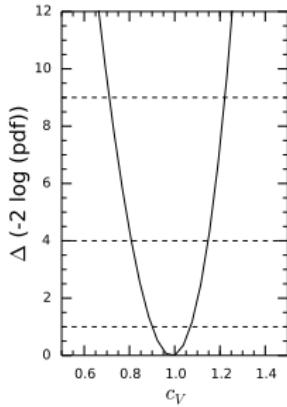


# Backup

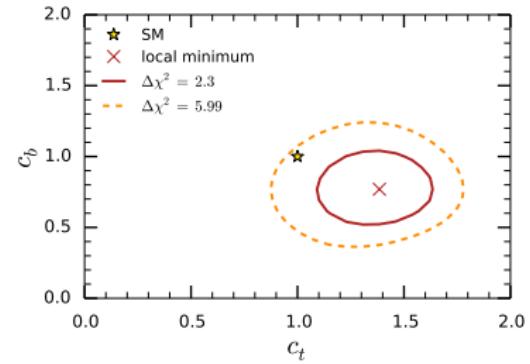
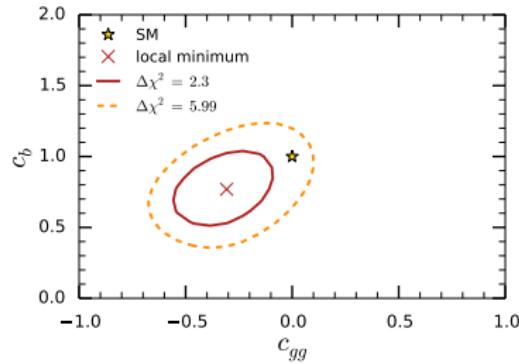
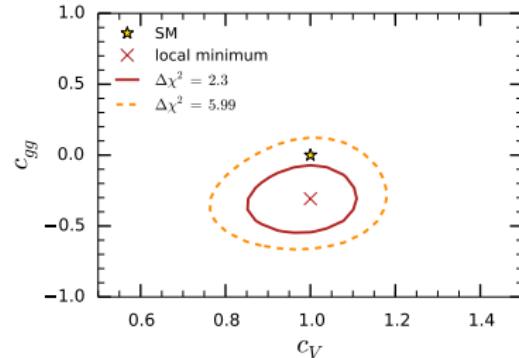
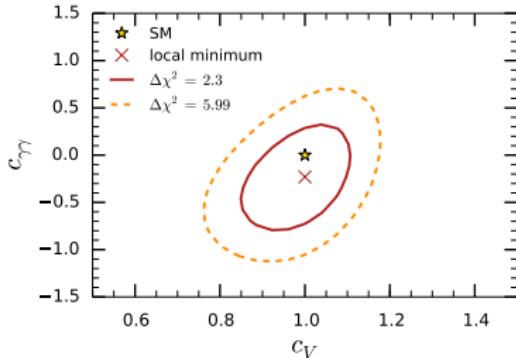
# The difference between expansions in canonical and chiral dimensions:



# $\Delta\chi^2$ for the one-dimensional marginalized pdf:



# Further 2-dim plots



# Further 2-dim plots

