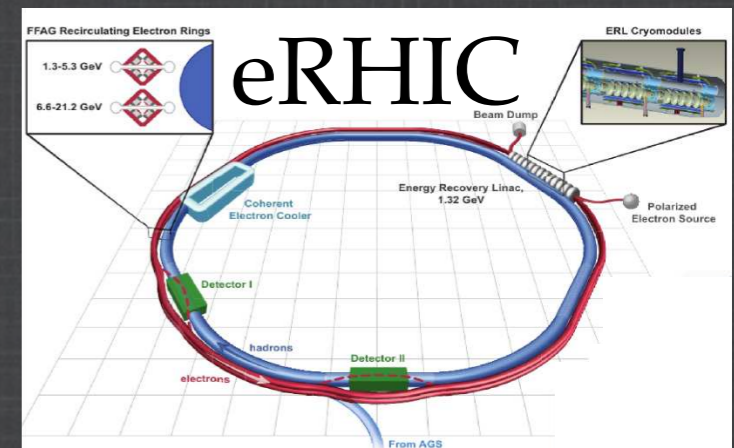


FFAGs for fundamental research

JB. Lagrange



Imperial College, UK
FNAL, USA



FFAG accelerator

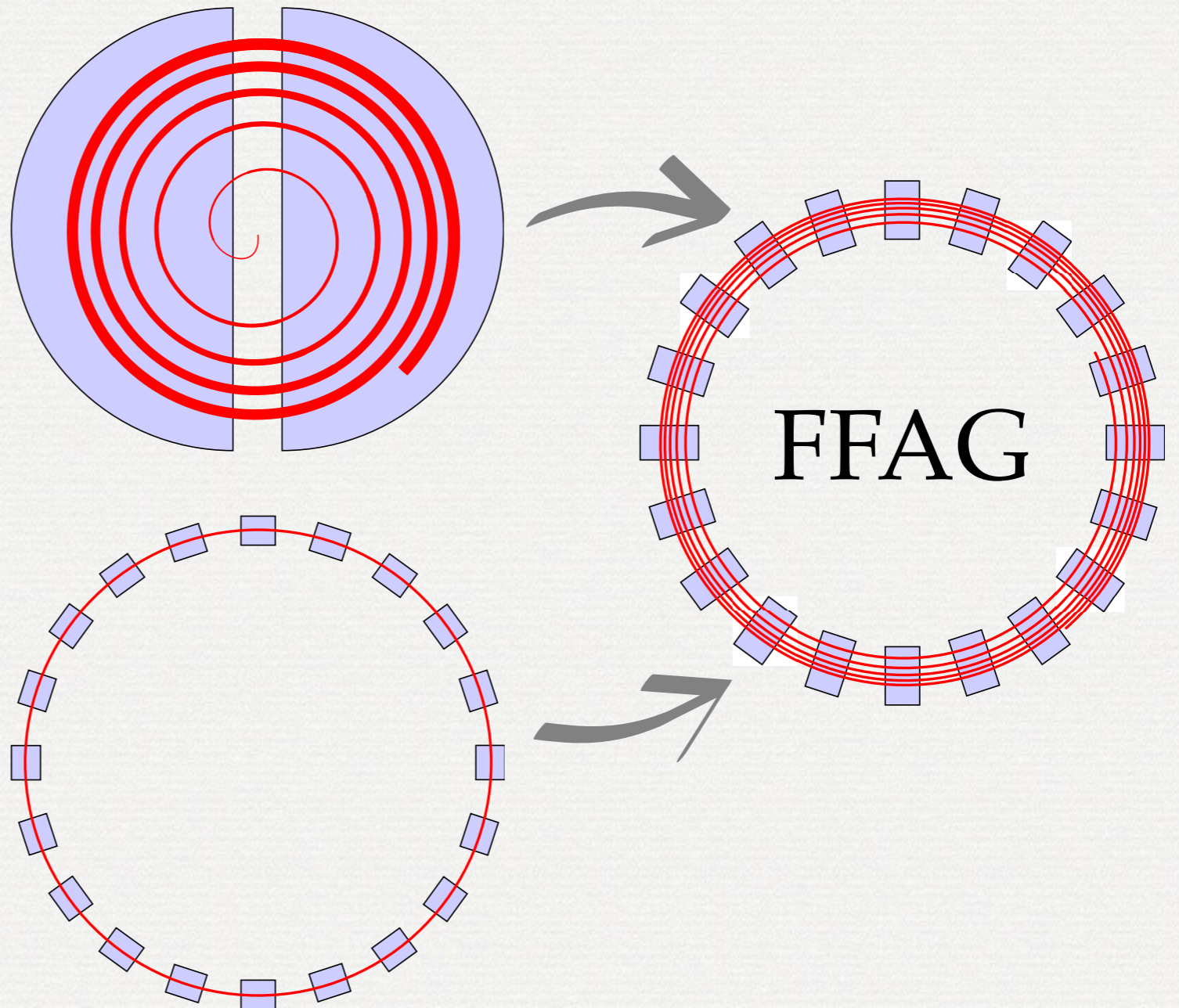
FIXED FIELD ALTERNATING GRADIENT

It combines

● a static guide field
like cyclotrons:

AND

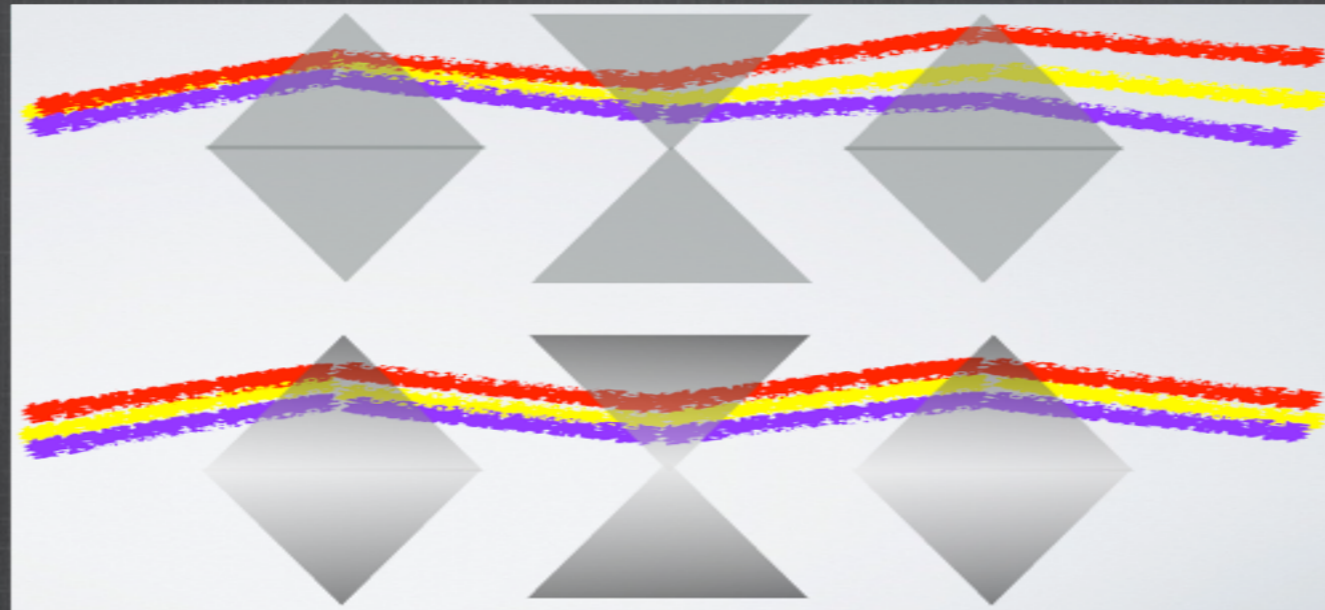
● a strong focusing.
like synchrotrons:



Zero-chromatic FFAG

Pros:

- stable optics for very large momentum spread.
- allows a good working point with a large acceptance far from harmful resonances.



Quasi-zero beam loss!

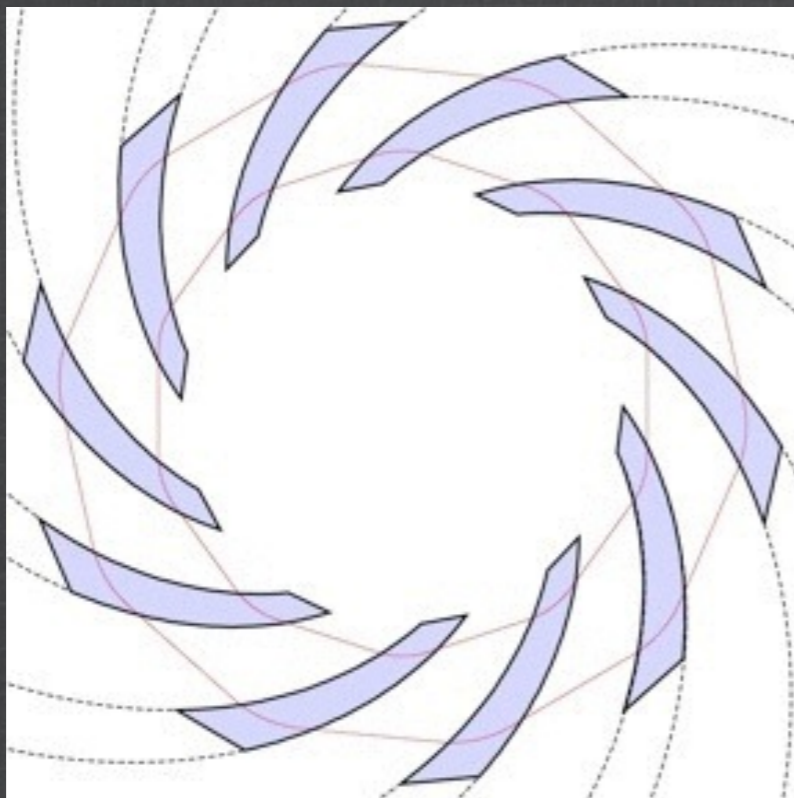
Cons:

- possibly large magnets

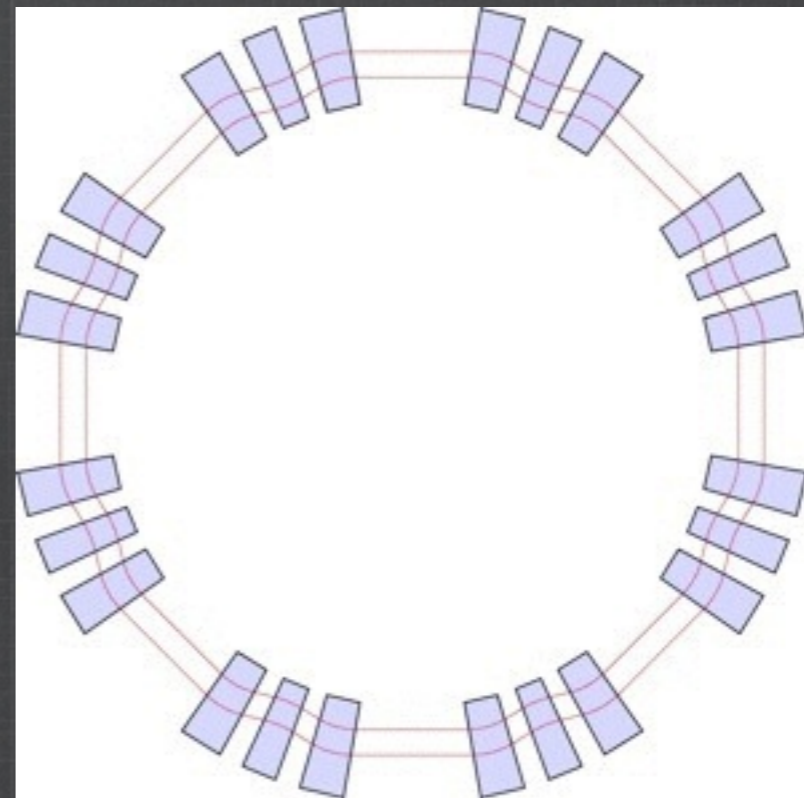
Circular scaling

Constant geometrical field index: $k = \frac{R}{\bar{B}} \frac{d\bar{B}}{dR}$

$$B(r, \theta) = B_0 \left(\frac{r}{r_0} \right)^k \cdot \mathcal{F}\left(\theta - \tan \zeta \ln \frac{r}{r_0}\right)$$



Spiral sector: $\zeta = \text{const.}$

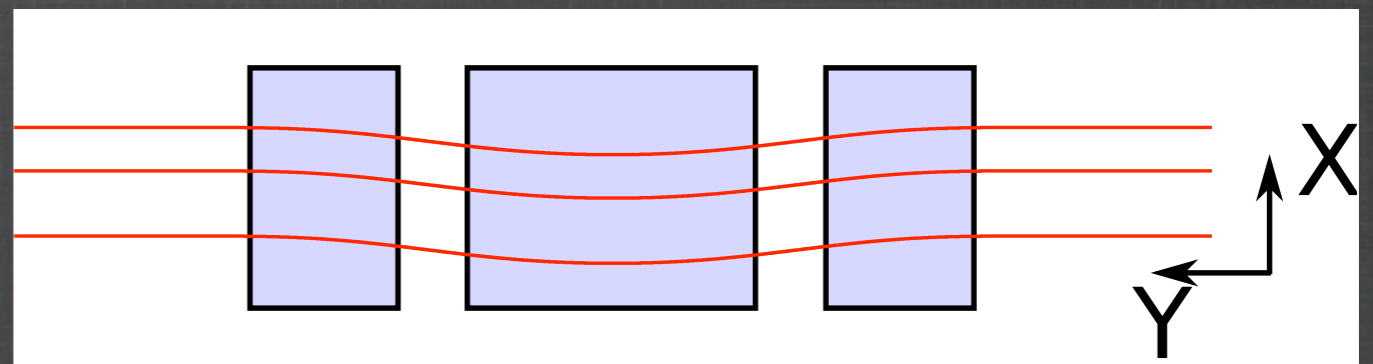
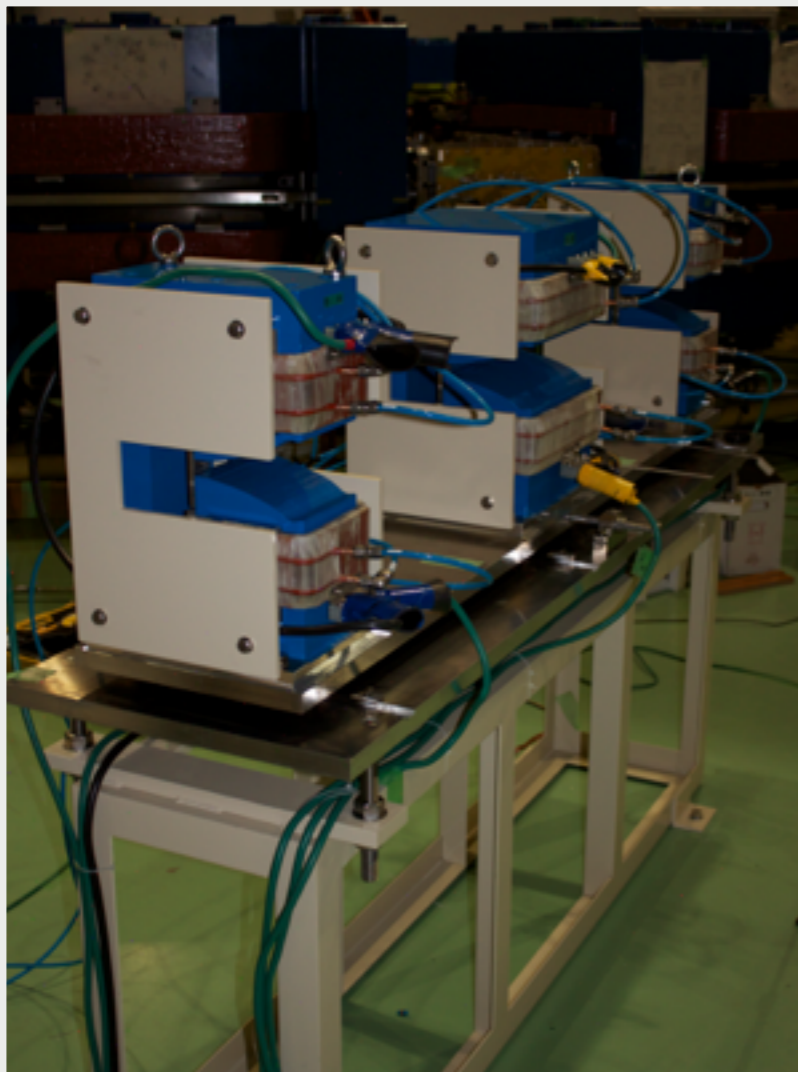


Radial sector: $\zeta = 0$

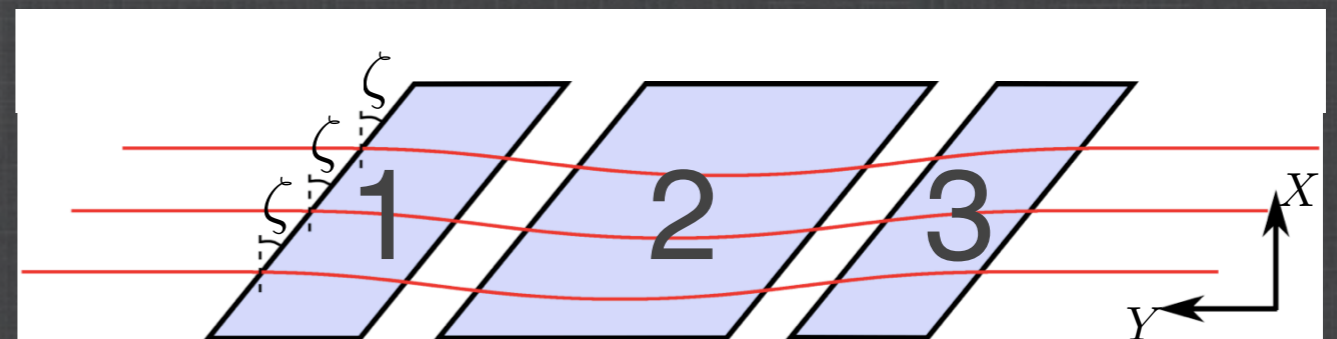
Straight scaling

Constant normalised field gradient: $m = \frac{1}{\bar{B}} \frac{d\bar{B}}{dX}$

$$B(X, Y) = B_0 e^{m(X - X_0)} \mathcal{F}(Y - (X - X_0) \tan \zeta)$$



Rectangular case: $\zeta = 0$

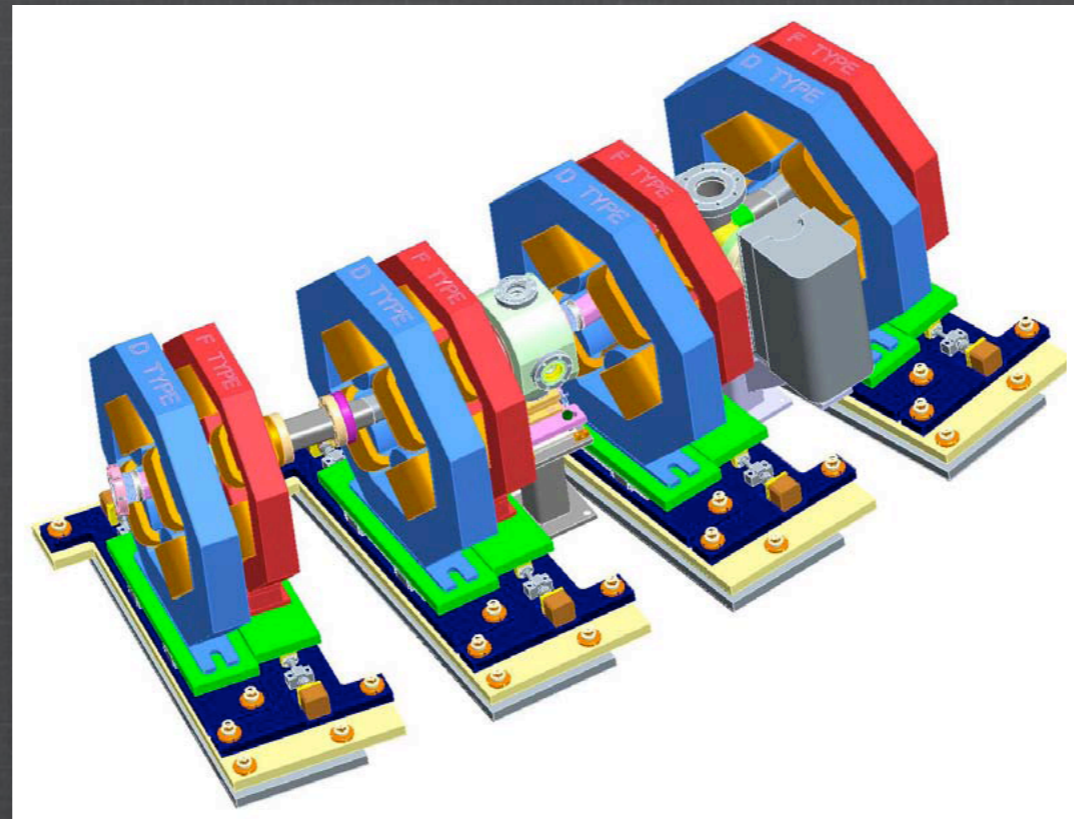


Tilted straight case: $\zeta = \text{const.}$

Linear “non-scaling” FFAG

Offset quadrupoles

- very strong focusing (small magnets)
- chromaticity



Cyclotron with synchrotron-size magnets

Outline

- Linear NS FFAG: eRHIC
- PRISM
- racetrack FFAG: nuSTORM
- “FFAG beam line”: nuPIL

Outline

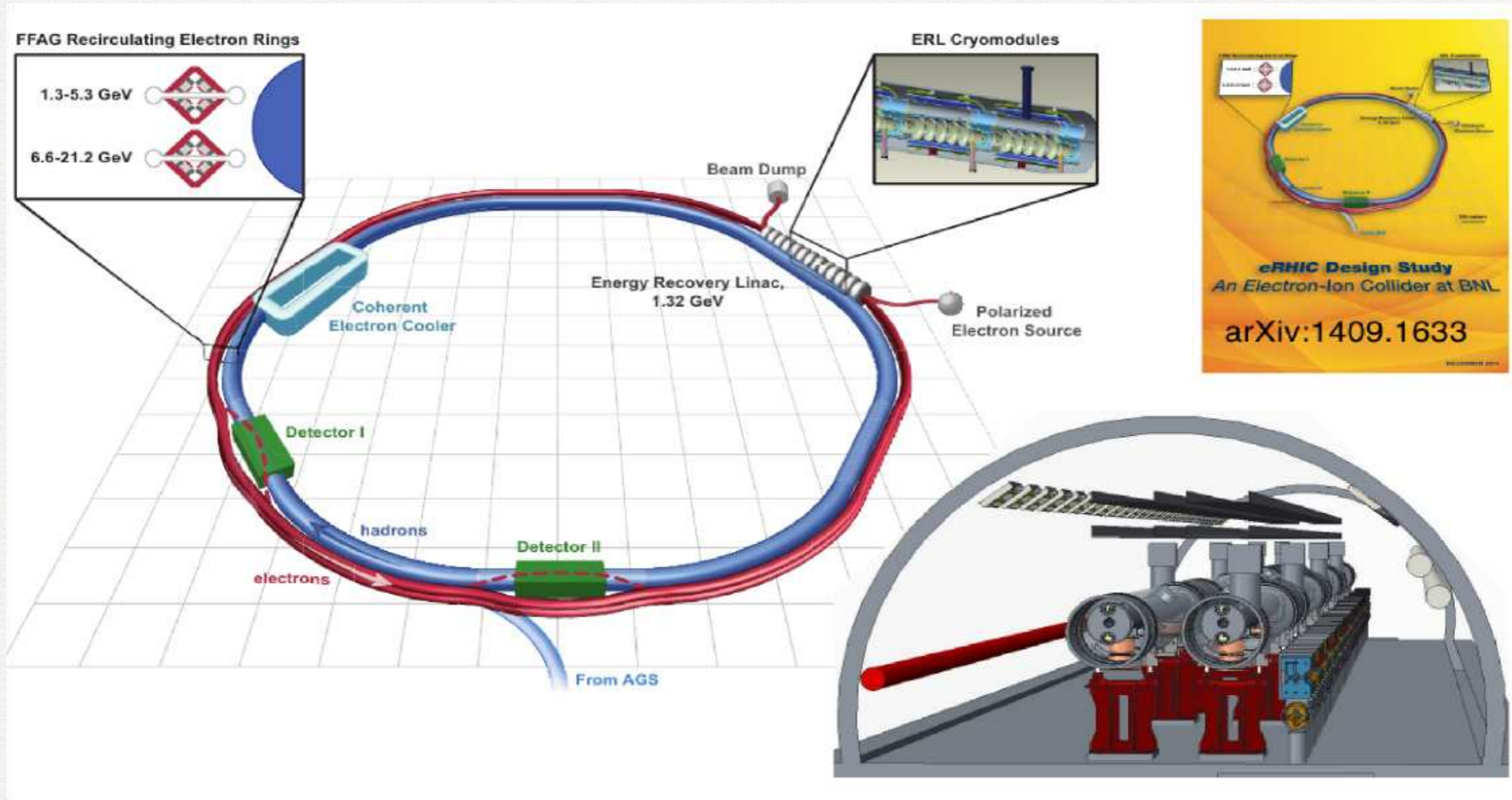
● Linear NS FFAG: eRHIC

● PRISM

● racetrack FFAG: nuSTORM

● “FFAG beam line”: nuPIL

eRHIC

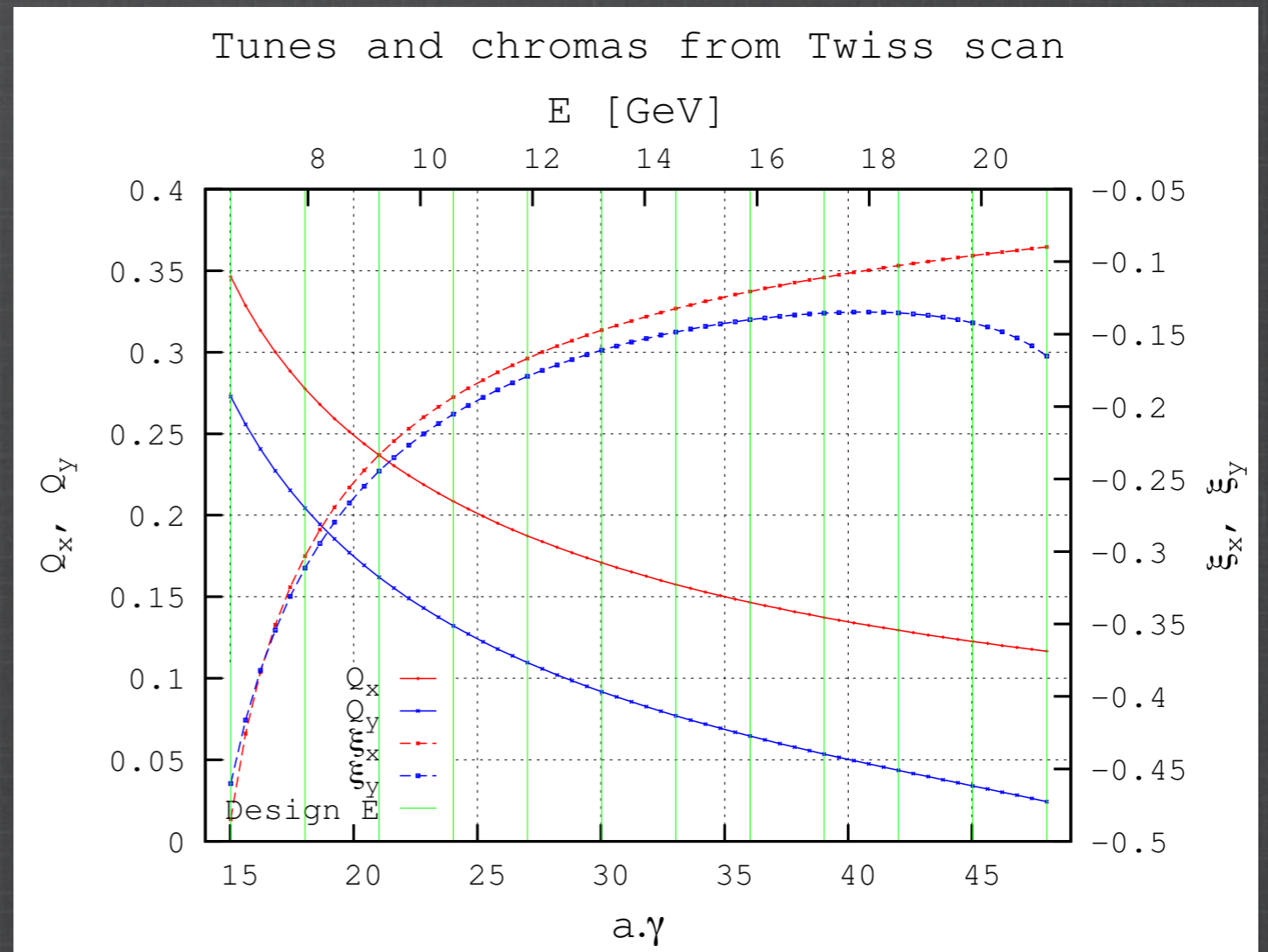
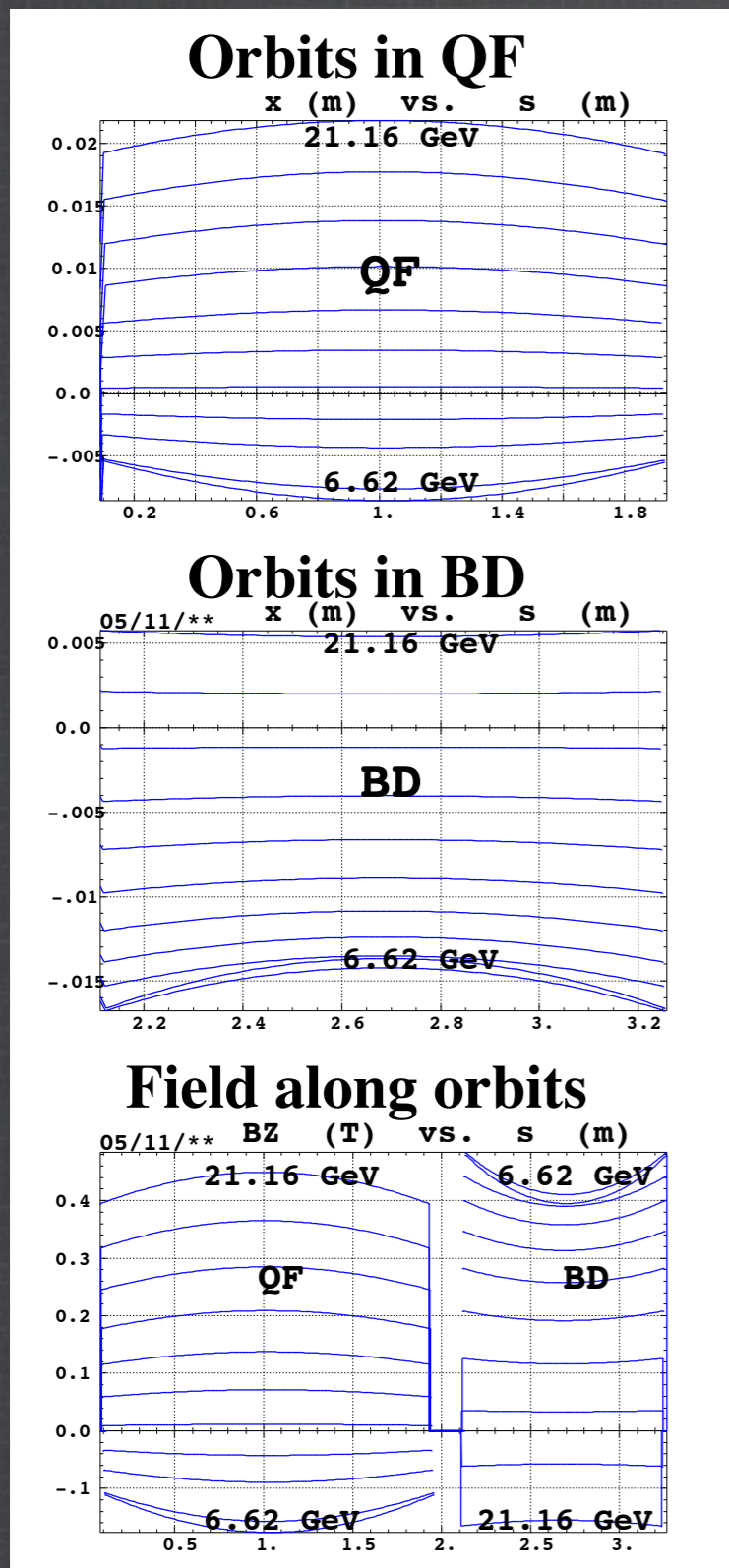


Alongside the existing RHIC, an ERL as polarised electron bunch with linear NS FFAG arcs (permanent magnets).

5 paths in FFAG1, 12 paths in FFAG2

eRHIC FFAG2

Arcs optimized to minimize synchrotron radiation



Outline

● Linear NS FFAG: eRHIC

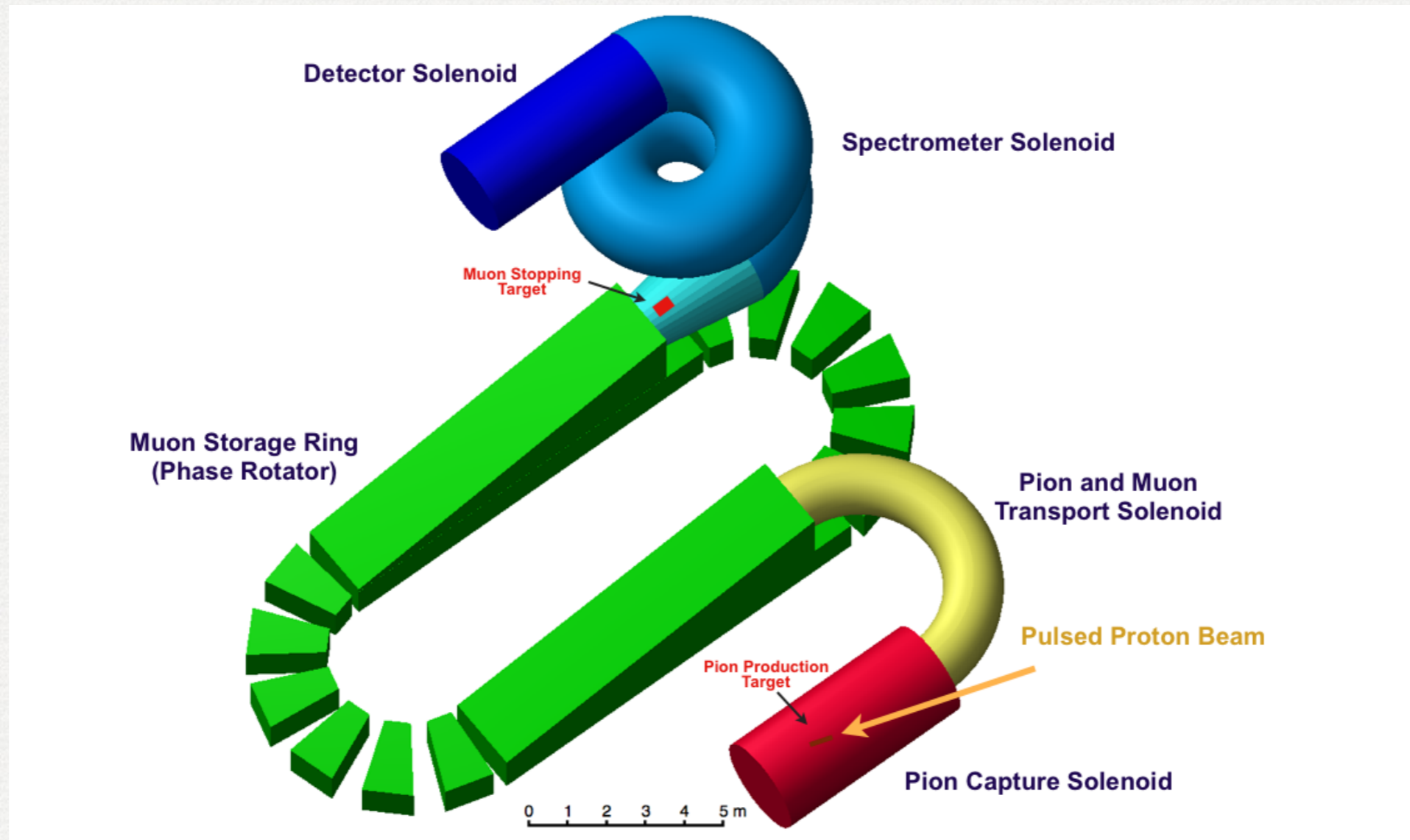
● PRISM

● racetrack FFAG: nuSTORM

● “FFAG beam line”: nuPIL

PRISM

Phase Rotated Intense Slow Muon Beam

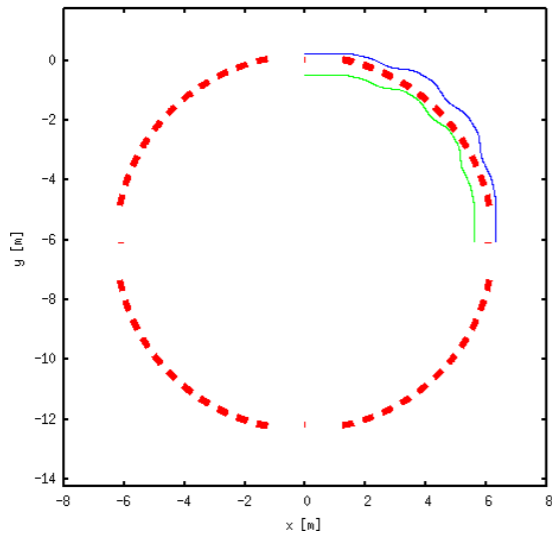


Reduce the muon energy spread by phase rotation and purify the muon beam in the ring.

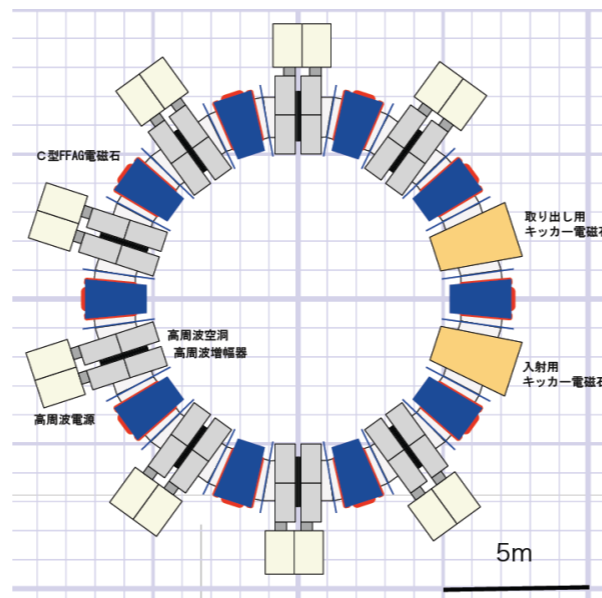
PRISM ring requirements

- Compact ring (circumference ~ 40 m).
- Long drift spaces required for injection/ extraction.
- Very large transverse acceptance (30 000 mm.mrad in horizontal, 3000 mm.mrad in vertical)
- Large momentum acceptance ($68 \text{ MeV} / c \pm 20\%$)

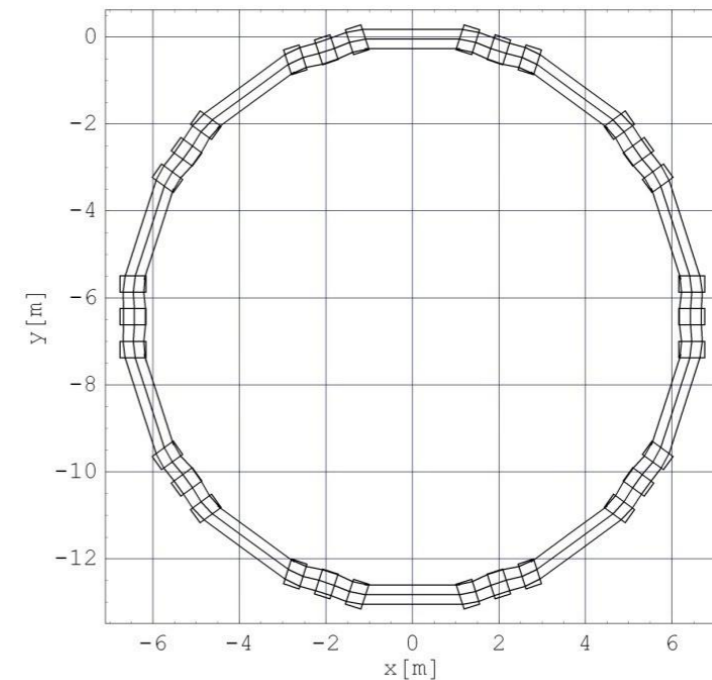
PRISM FFAG ring designs



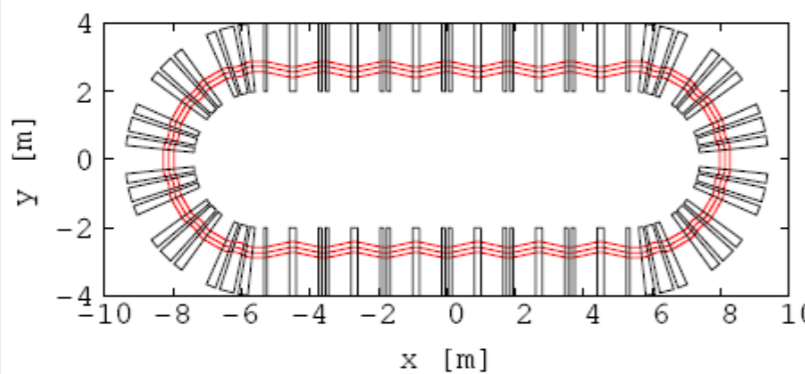
Scaling Superperiodic



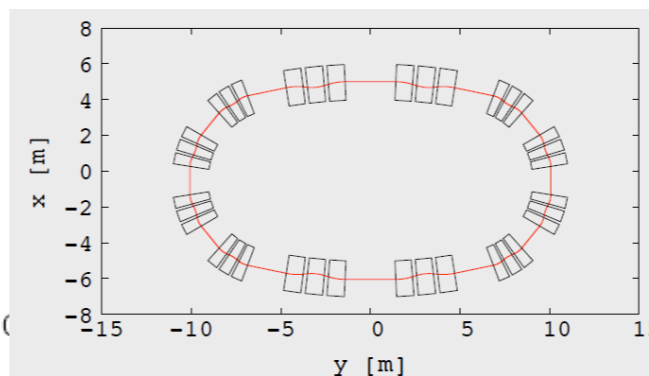
Reference design



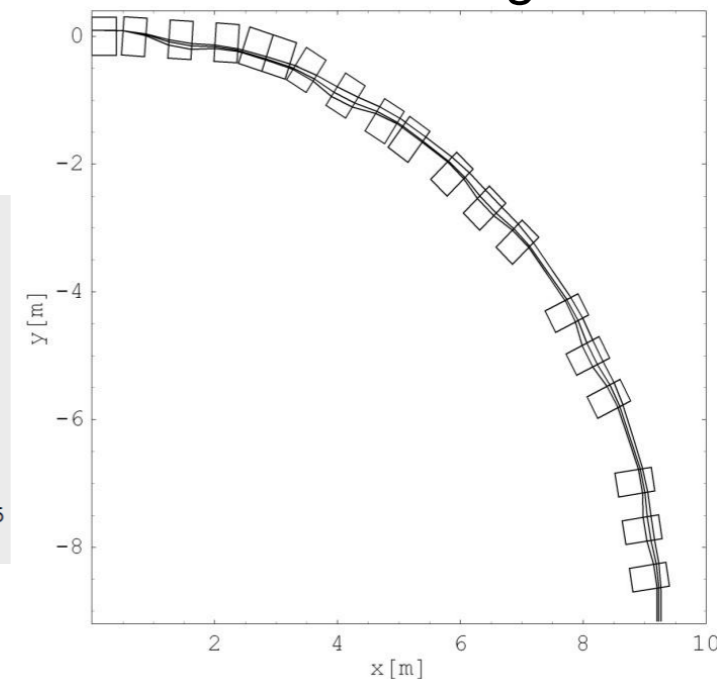
Non-Scaling



Advanced scaling FFAG



"Egg-shaped"



Advanced NS-FFAG

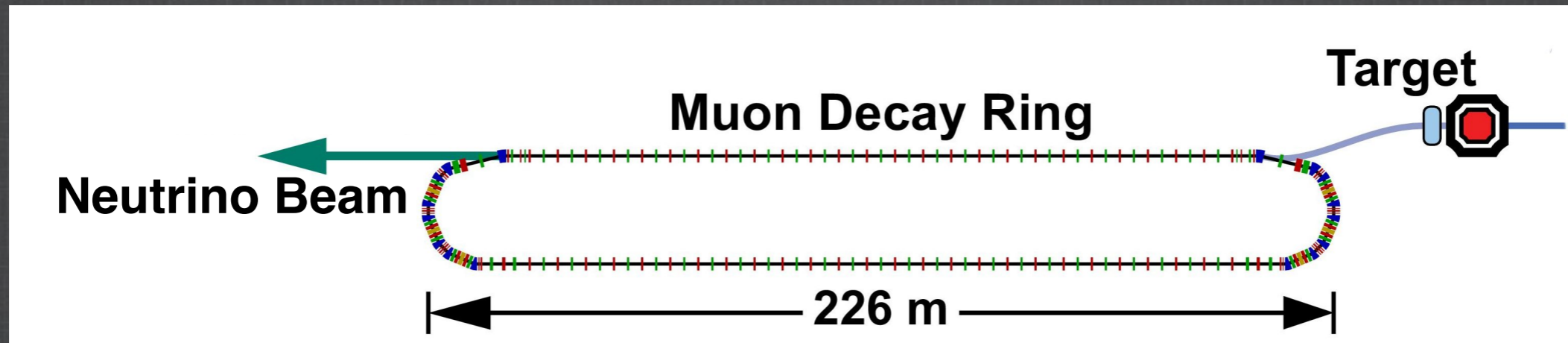
Outline

● Linear NS FFAG: eRHIC

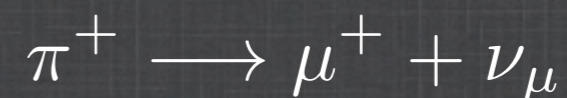
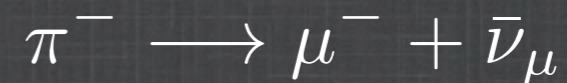
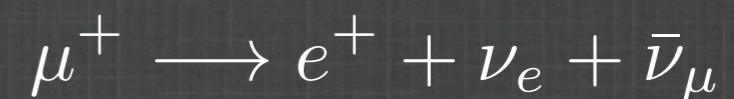
● PRISM

● racetrack FFAG: nuSTORM

● “FFAG beam line”: nuPIL



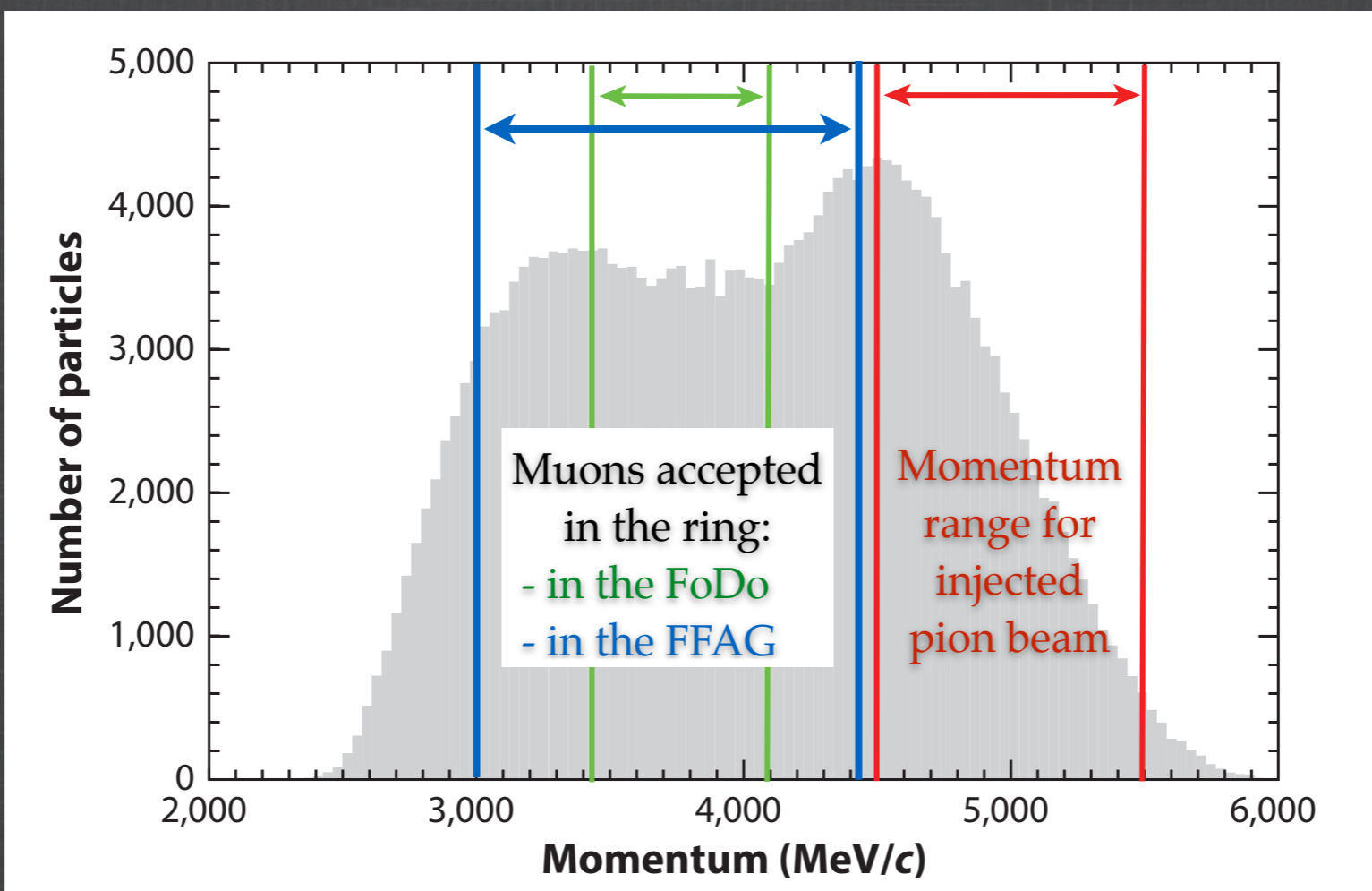
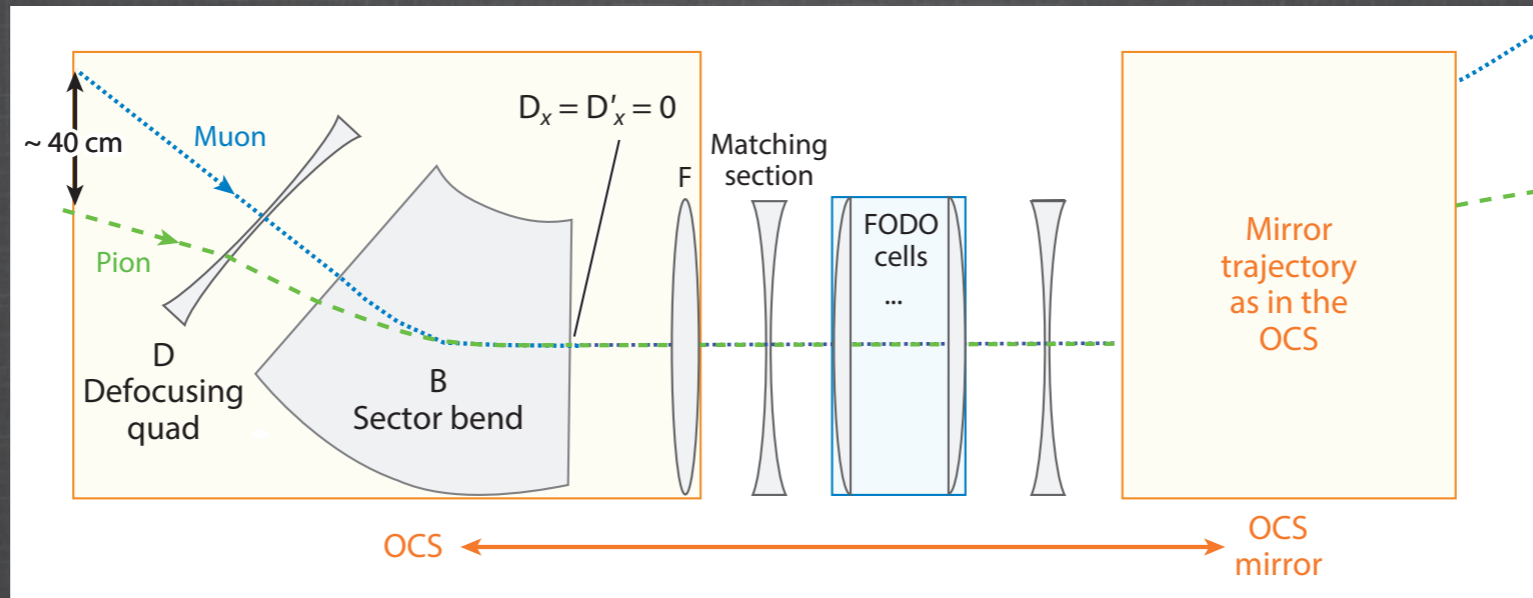
1. Facility to provide a muon beam for precision neutrino interaction physics
2. Study of sterile neutrinos
3. Accelerator & Detector technology test bed
 - Potential for intense low energy muon beam
 - Enables μ decay ring R&D (instrumentation) & technology demonstration platform
 - Provides a neutrino Detector Test Facility
 - Test bed for a new type of conventional neutrino beam



Facility

- 100 kW target station (designed for 400 kW)
 - 120 GeV protons from MI (FNAL), or 100 GeV protons from SPS (CERN)
 - Horn to collect pions (π^+ or π^-)
 - Target material: Inconel
 - 10^{21} protons on target over 4-5 years (3×10^{18} useful muon decays)
- Collection and transport
 - Chicane to select charge of pions
 - Stochastic injection
- Racetrack decay ring
 - large aperture FODO or FFAG.

Stochastic injection

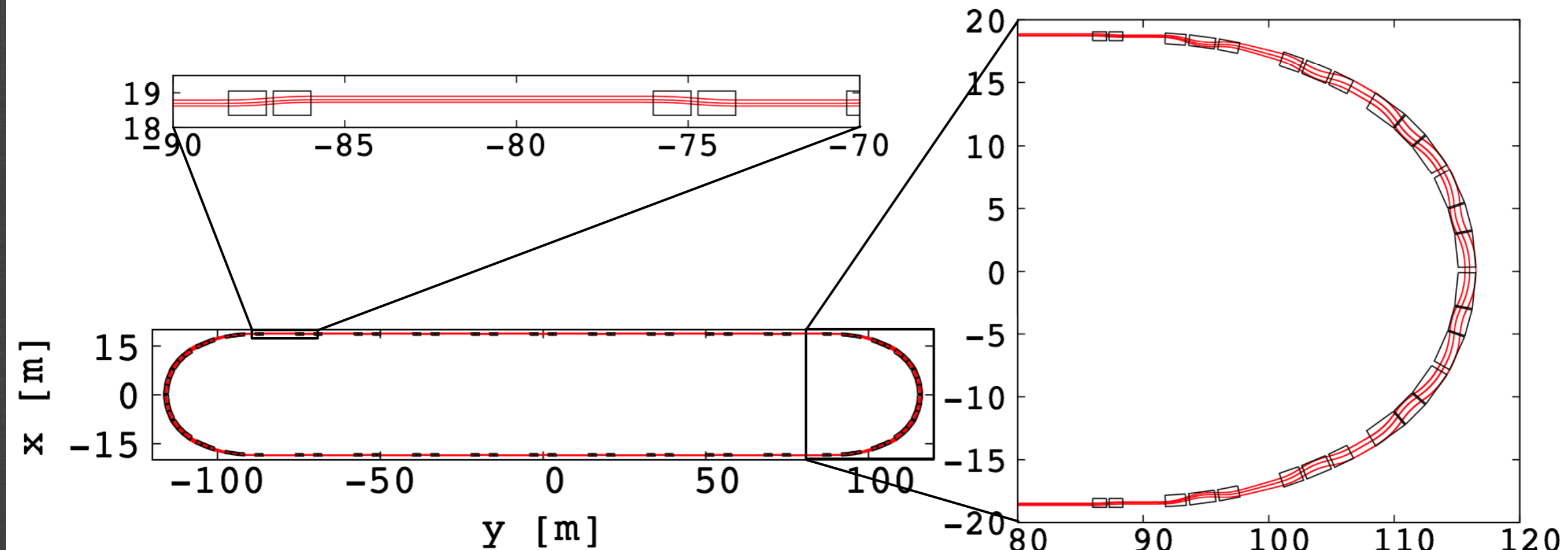


ν STORM Racetrack FFAG

Constraints:

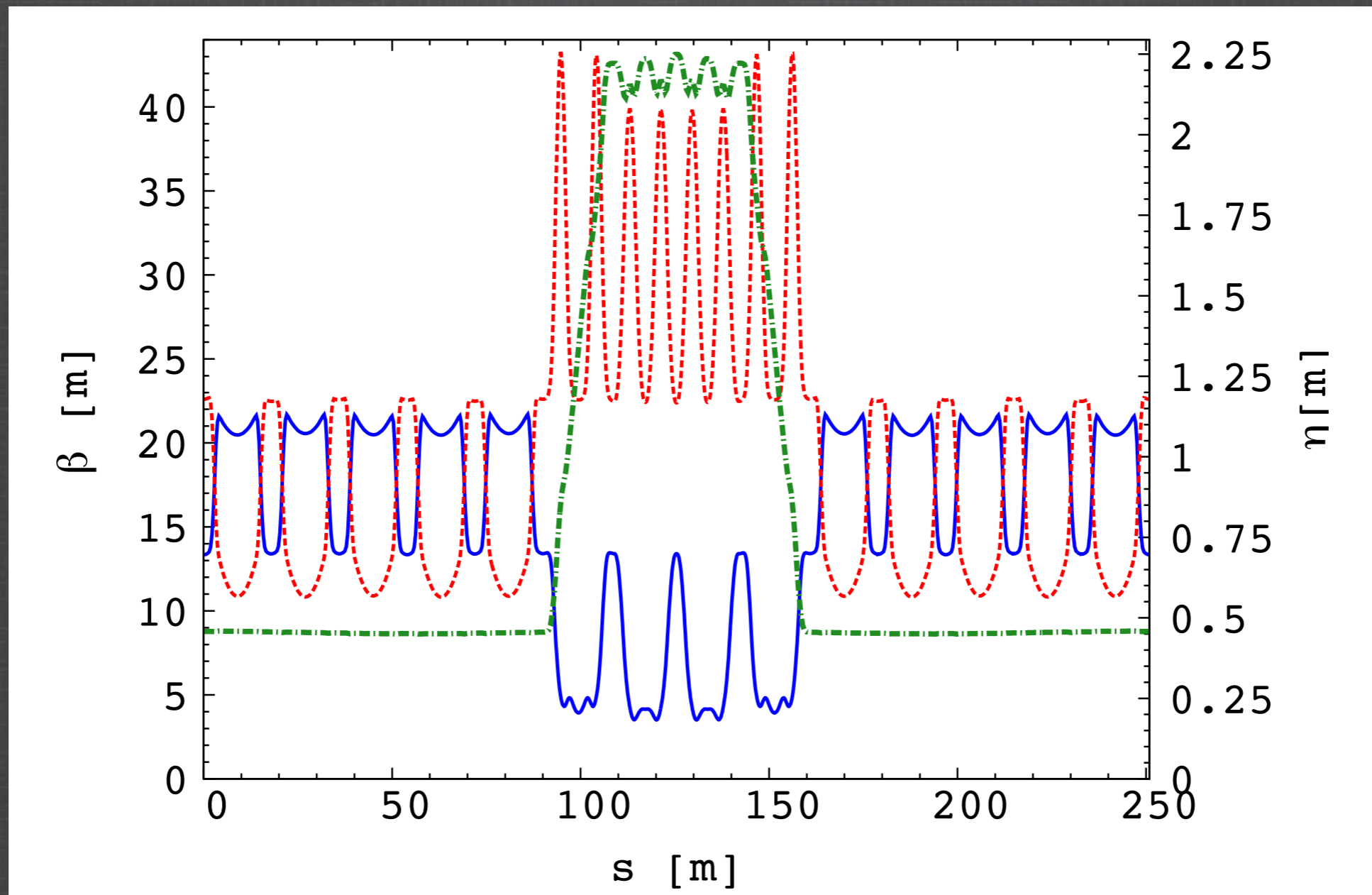
- in the straight part, the scallop effect must be as small as possible to collect the maximum number of neutrinos at the far detector.
- Stochastic injection: in the dispersion matching section, a drift length of 2.6 m is necessary to install a septum.
- to keep the ring as small as possible, SC magnets in the arcs are considered. Normal conducting magnets in the straight part are used.
- large transverse acceptance is needed in both planes: $1 (2) \pi$ mm.rad.

Quadruplet lattice



Quadruplet lattice

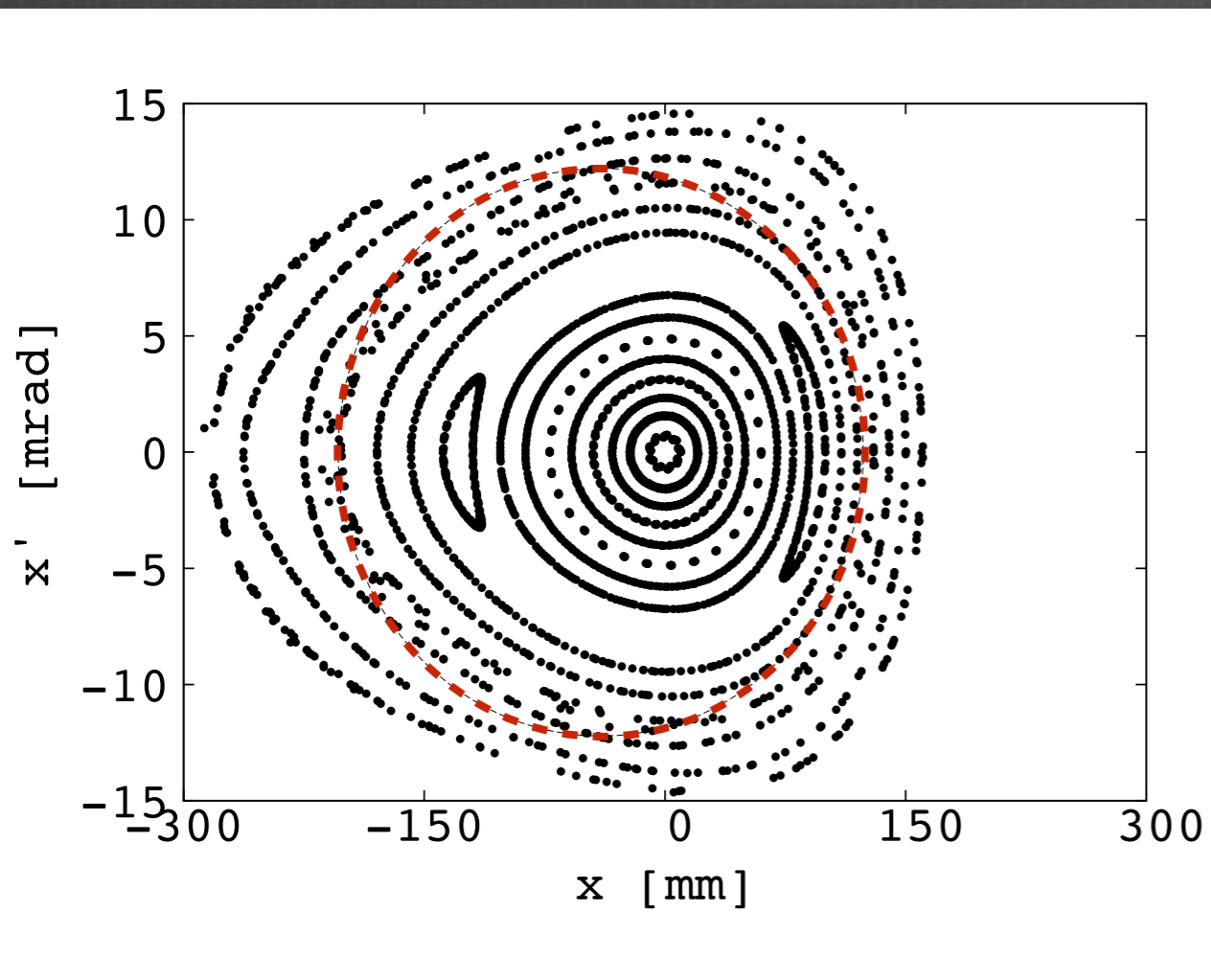
Beta-functions and dispersion at matching momentum



Horizontal (plain blue), vertical (dotted red) beta-functions and dispersion (mixed green) for half of the ring.

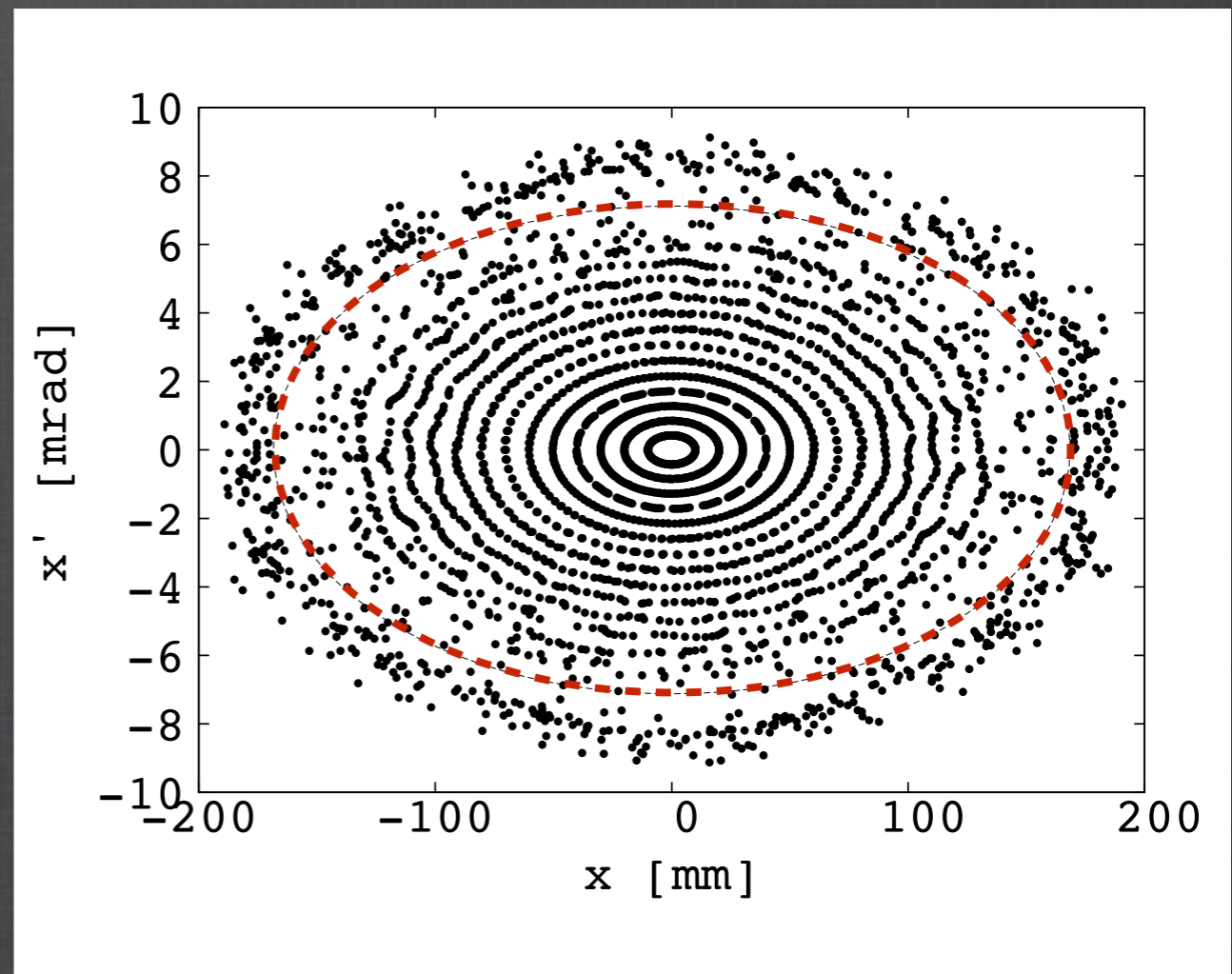
Quadruplet lattice

Transverse acceptance



Maximum horizontal stable
amplitude over 100 turns

(Dotted ellipse represents 2π .mm.rad)

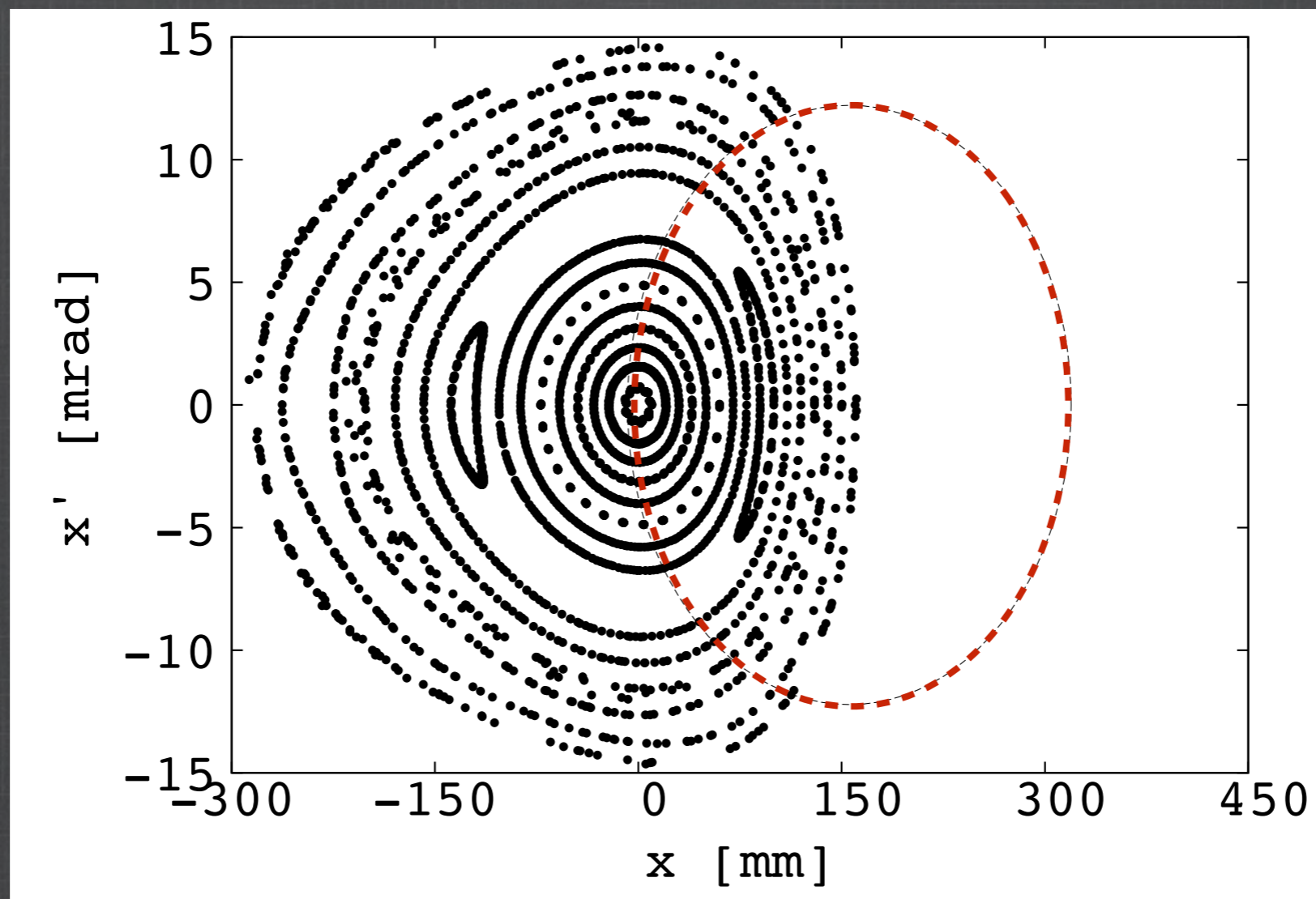


Maximum vertical stable
amplitude over 100 turns

(Dotted ellipse represents 1.2π .mm.rad)

Quadruplet lattice

Muon capture efficiency



Maximum horizontal stable amplitude over 100 turns
 (Dotted ellipse represents 2π .mm.rad 5 GeV/c pion beam position)

Hybrid lattice

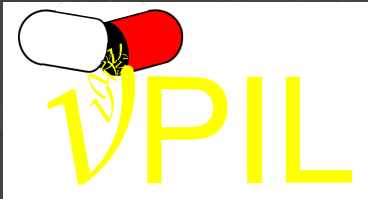
zero-dispersion (chromatic!) straight capture section
with FFAG arcs and straight zero-chromatic FFAG:

- increase muon capture efficiency of full FFAG lattice
- reduce chromaticity of FoDo lattice.

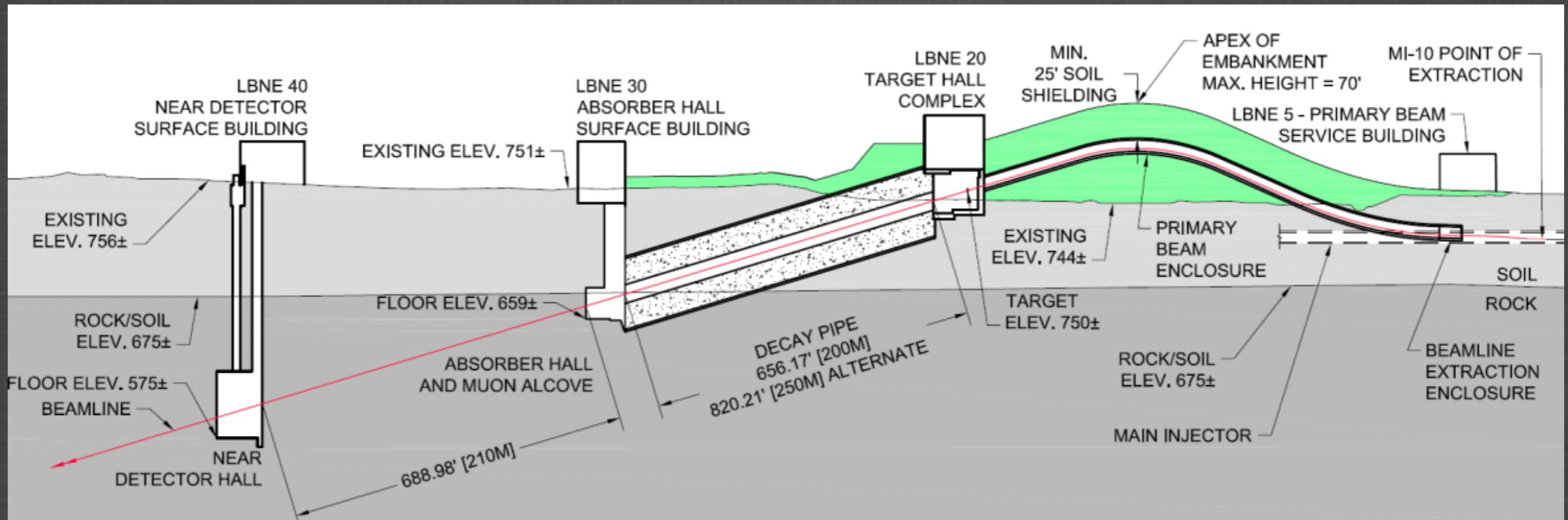
To be implemented

Outline

- Linear NS FFAG: eRHIC
- PRISM
- racetrack FFAG: nuSTORM
- “FFAG beam line”: nuPIL



LBNE baseline



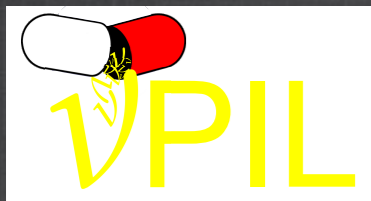
(LBNE Letter of Intent, Jan 2015)

Decay pipe:

- 6 (4?) m diameter,
- filled with Helium,
- 7 m of concrete around the pipe to shield it.

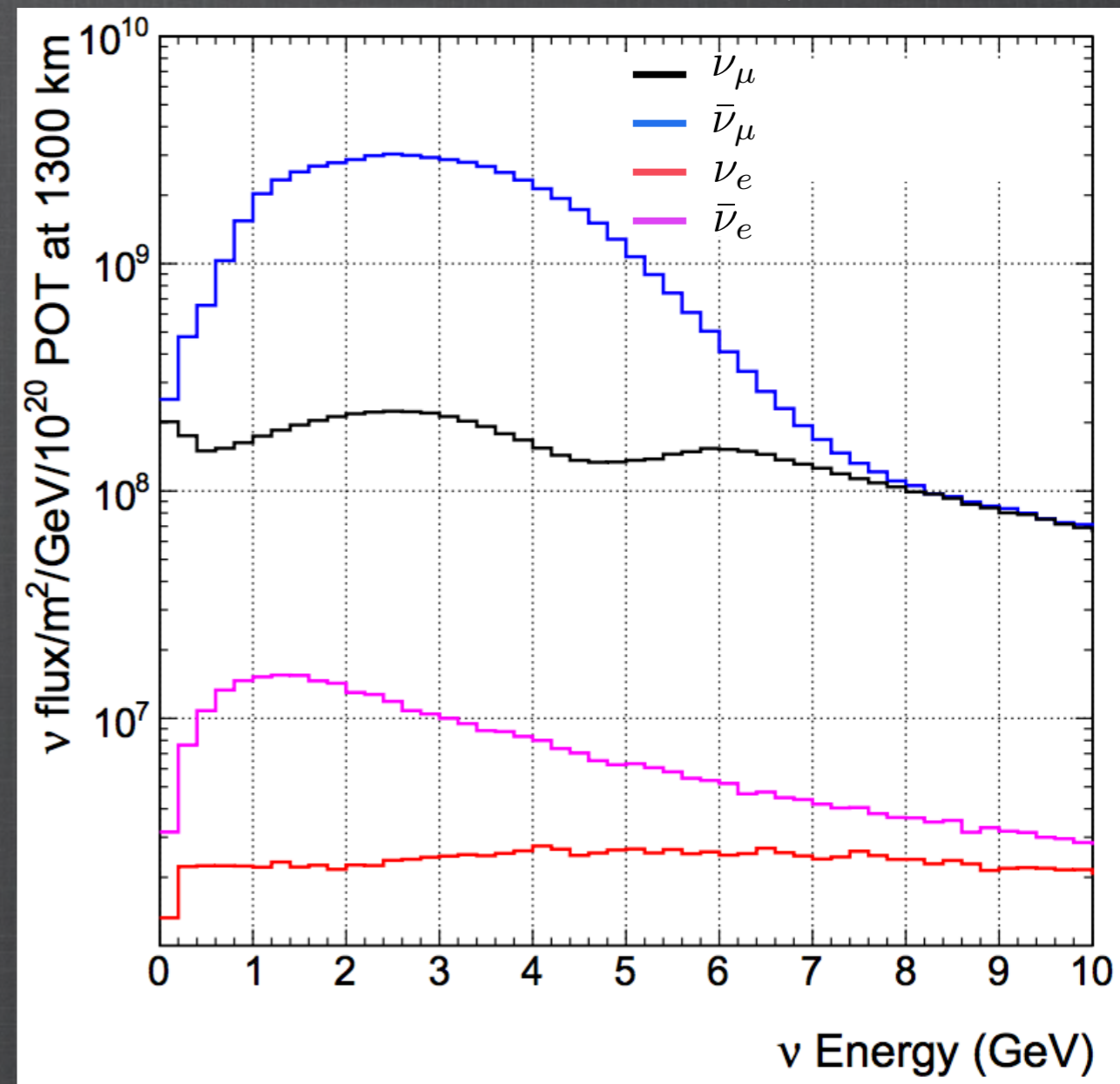
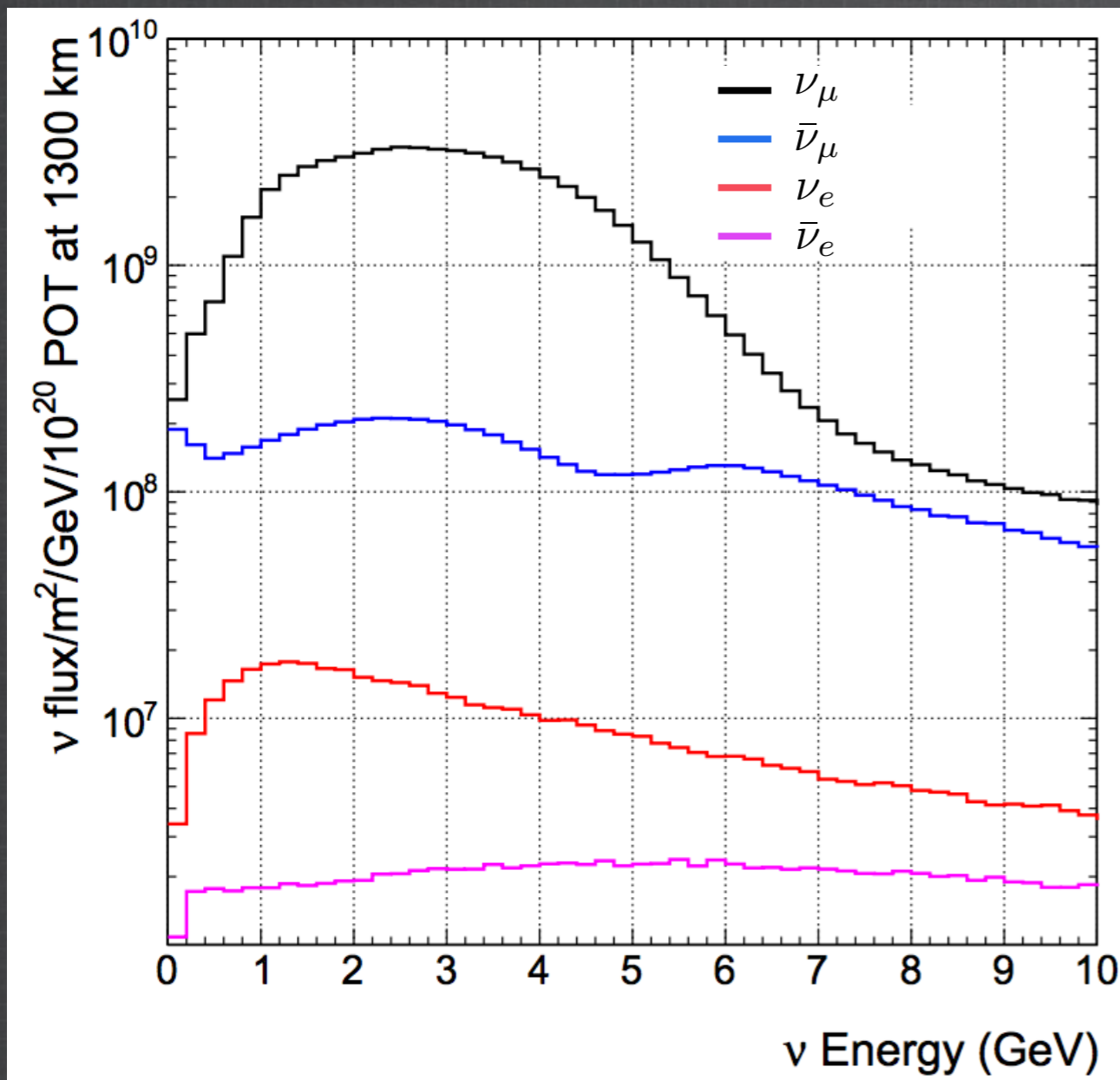


20 m diameter tunnel!

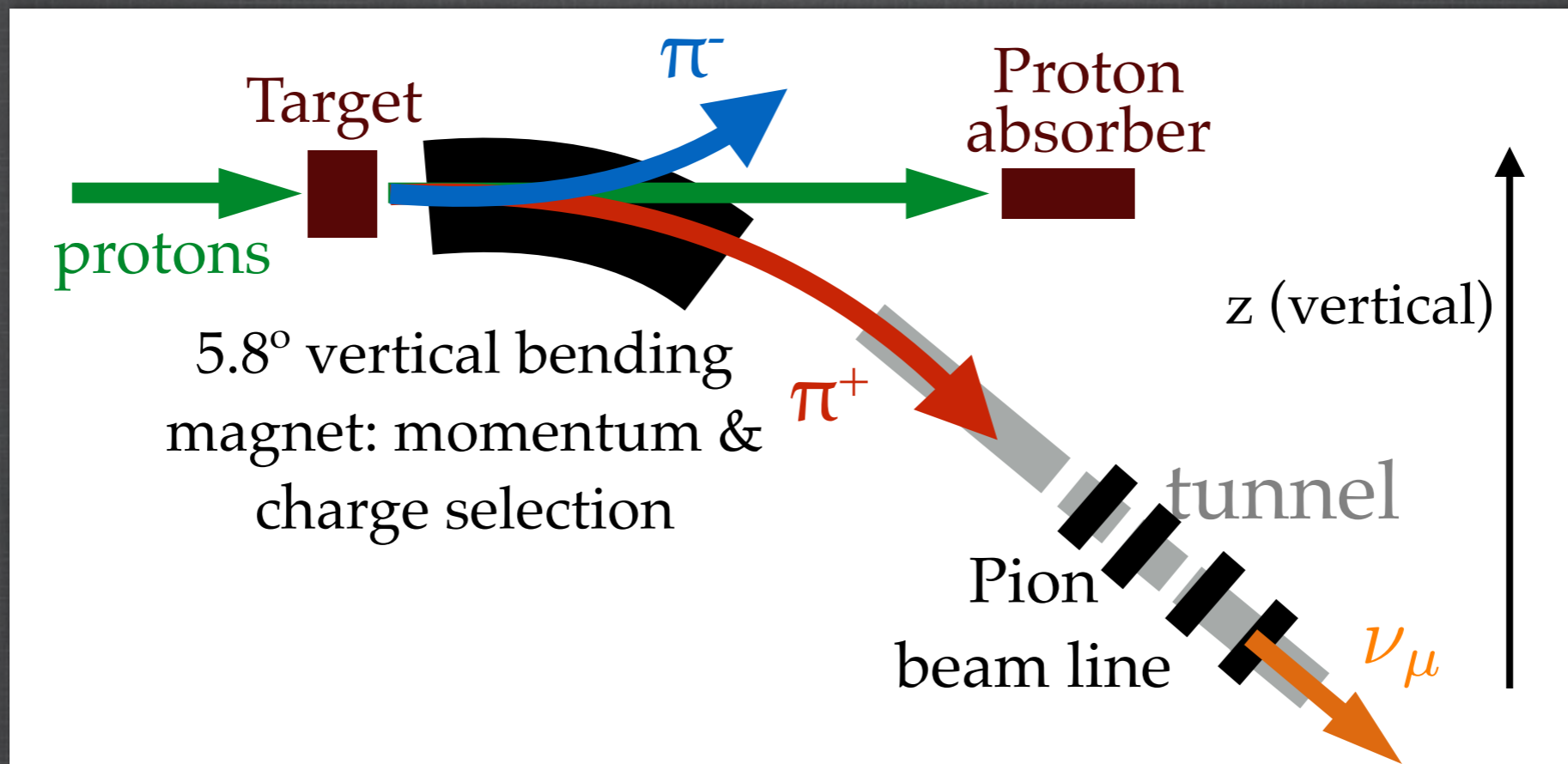


Neutrino Flux at DUNE

(CDR-Physics Volume)



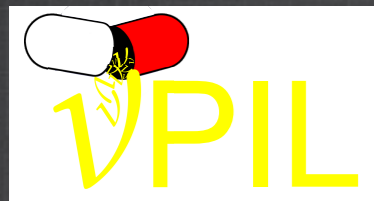
Inevitable background from wrong-sign particles decay
(DUNE detector not magnetized: rely on high-resolution imaging to statistically discriminate neutrinos from anti-neutrinos.)



Pion beam line

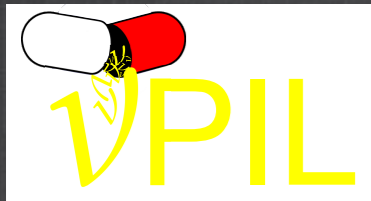
- clean, well known flux
- smaller tunnel (conventional pion beam line)
- Detector does not need to be magnetised

➔ **nuPIL (Neutrinos from Pion Injection Line)**

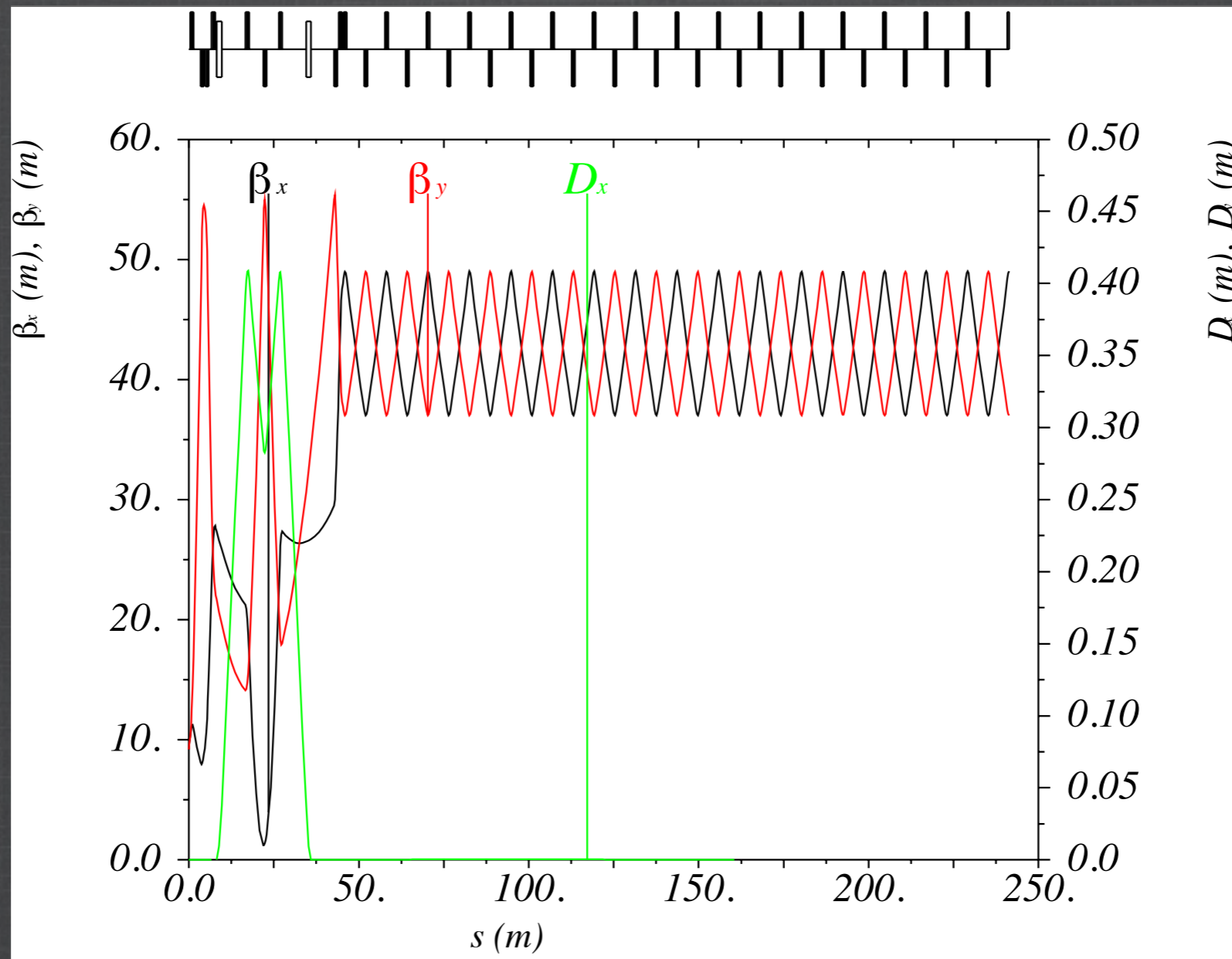
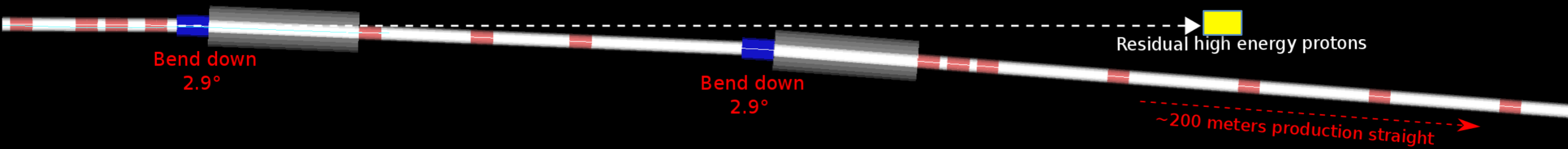


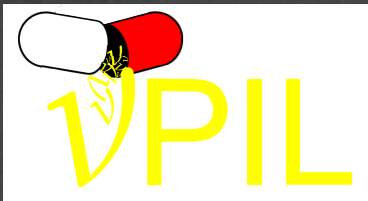
General Parameters

- Very large momentum acceptance (pions $7 \text{ GeV} / c \pm 50\%$)
- Large transverse acceptance (2000 mm.mrad in both planes)
- Normal conducting range (KEK radiation hard coils)
- C-shape magnet

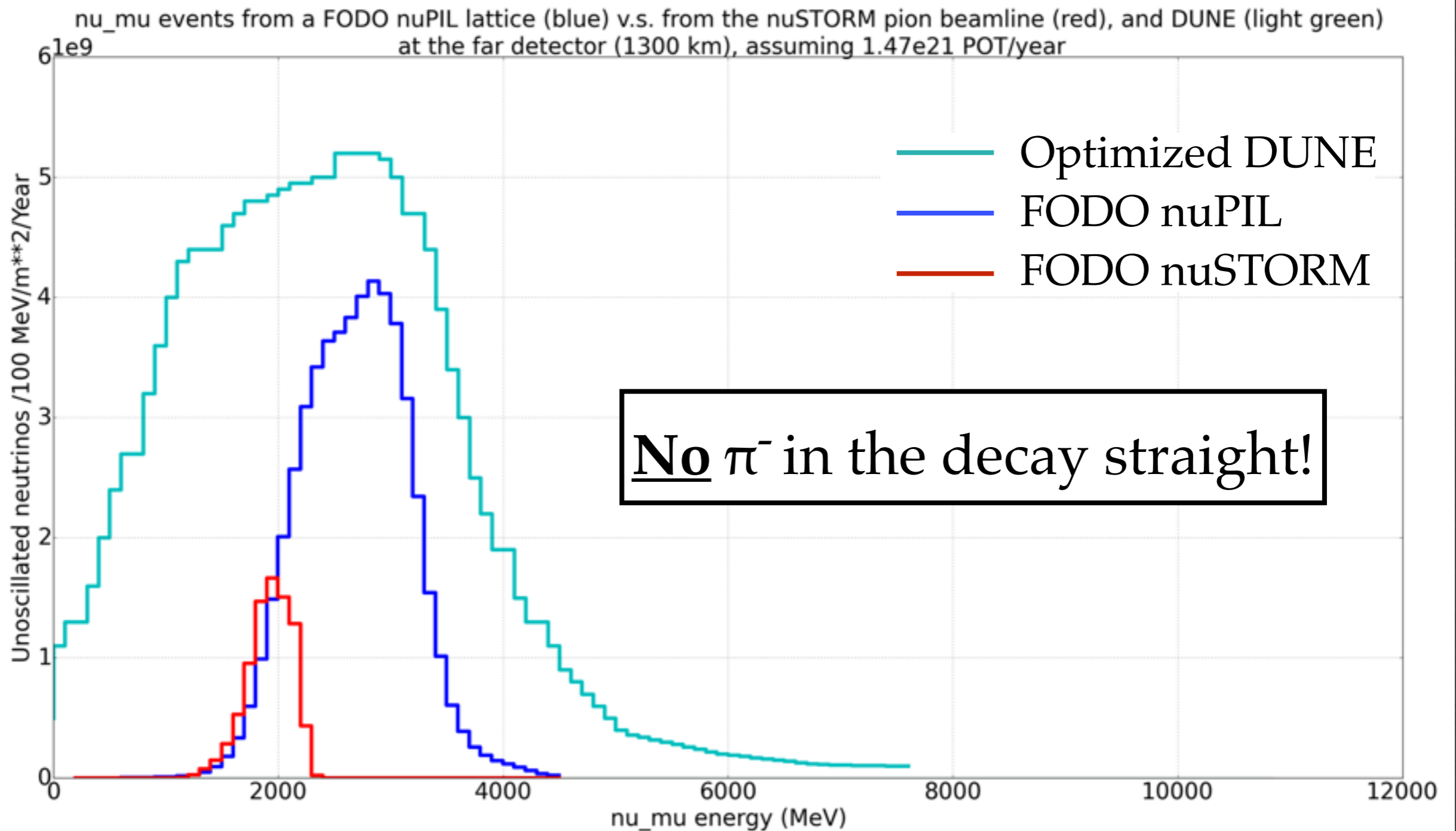


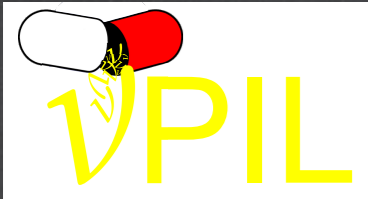
FODO design



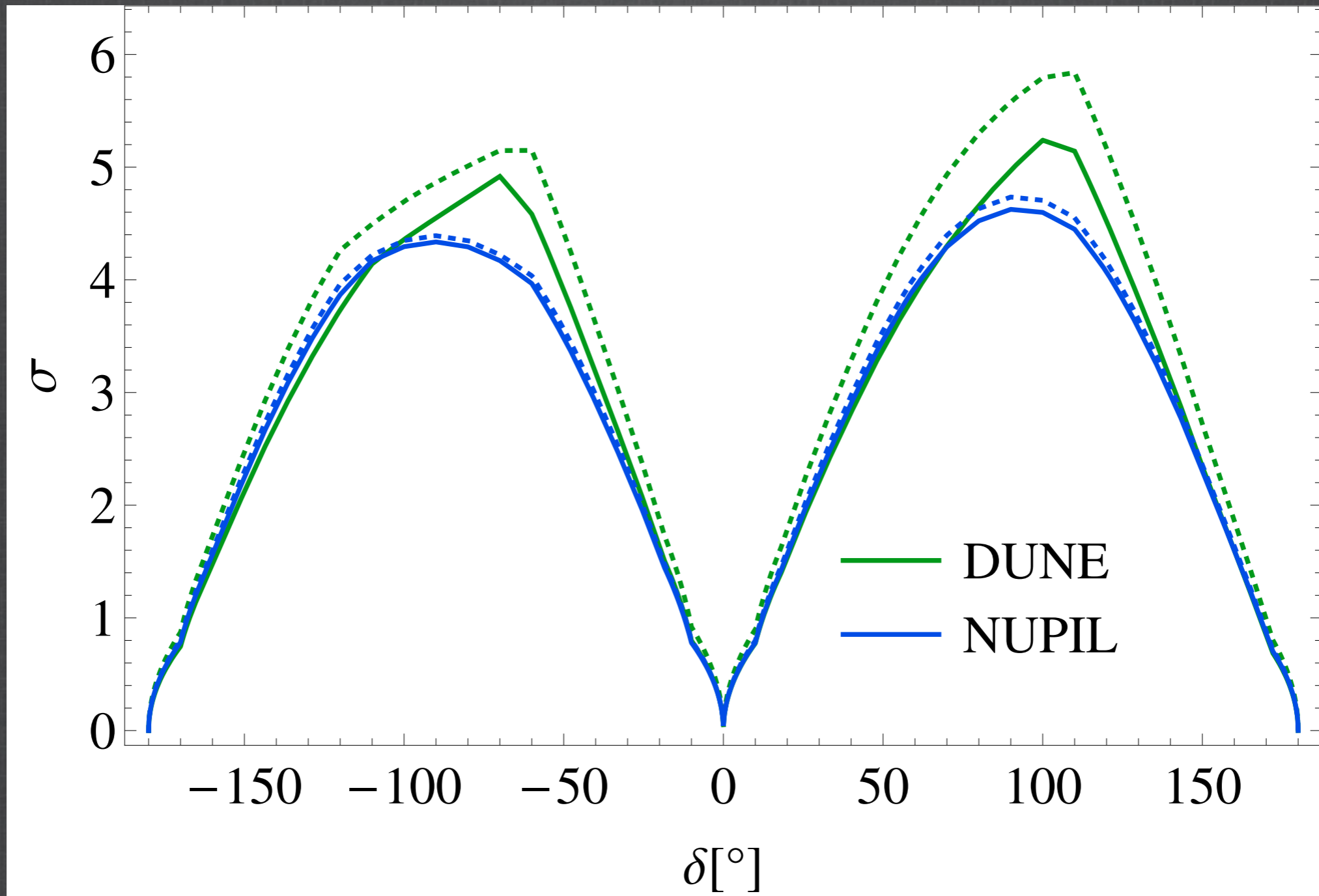


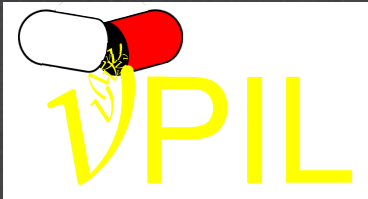
FODO design Flux



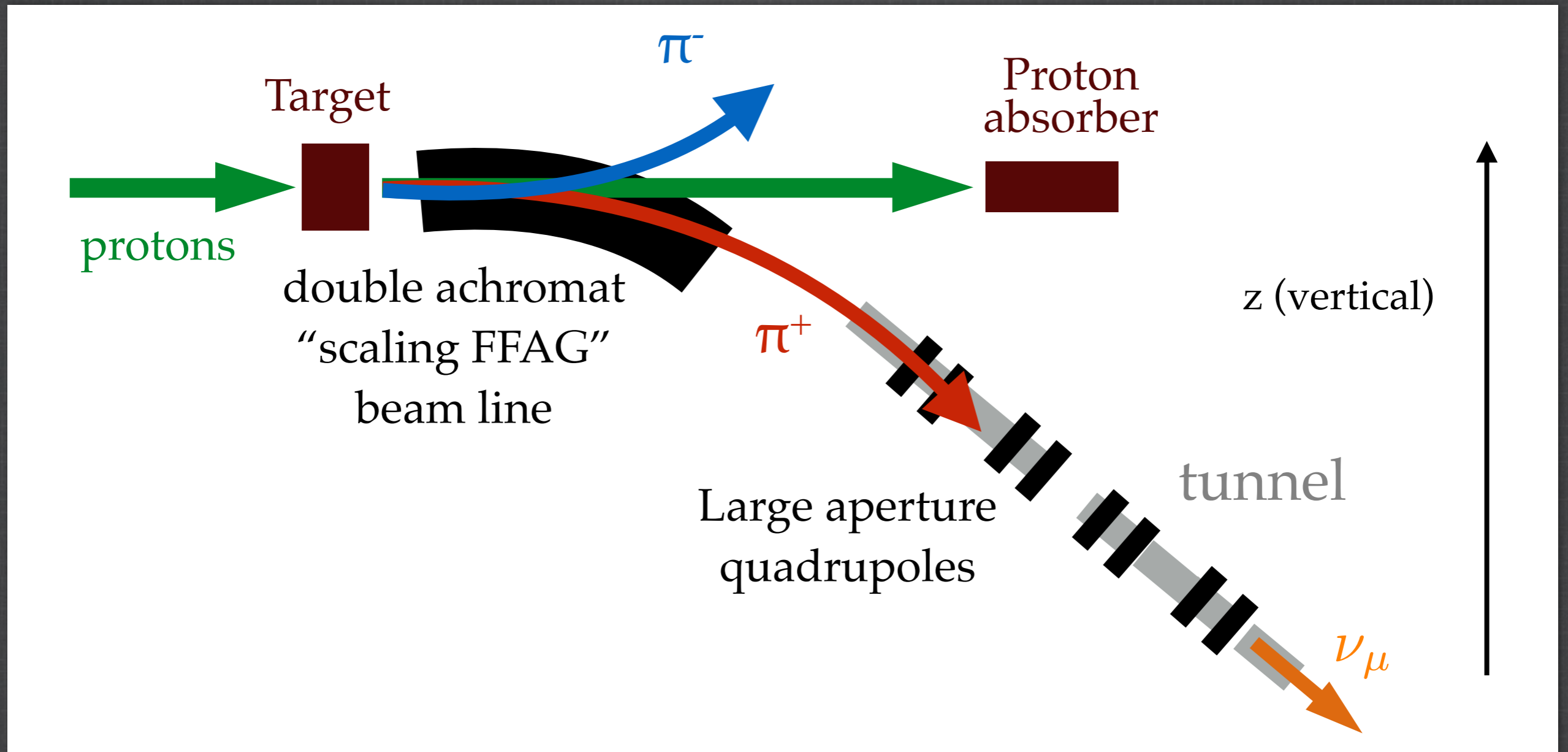


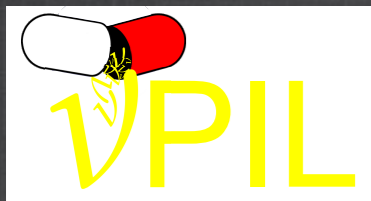
FODO design Sensitivity



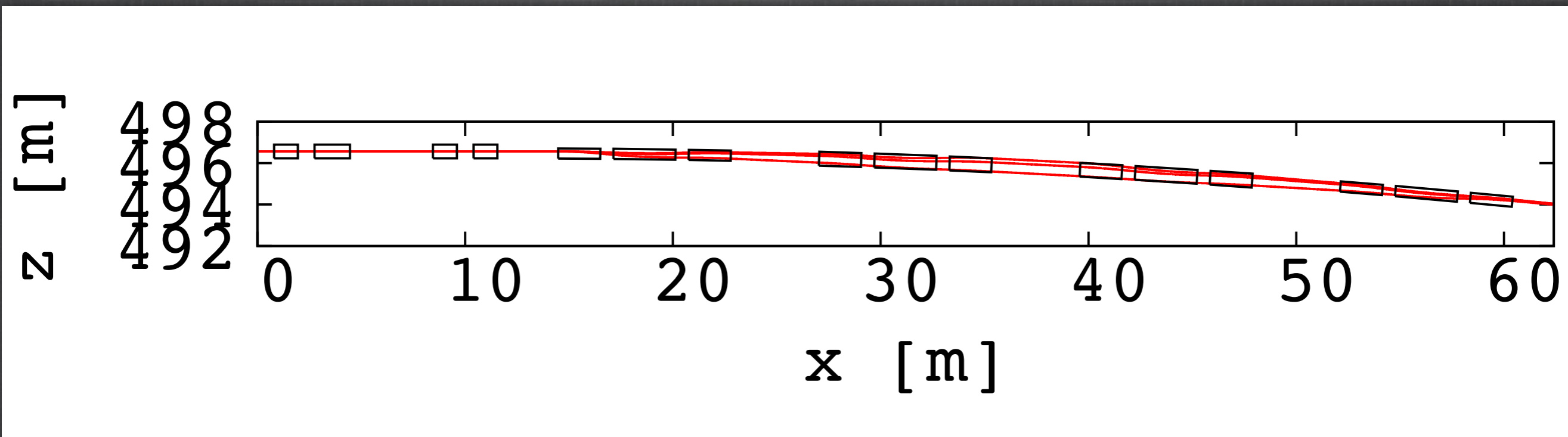


Hybrid design concept

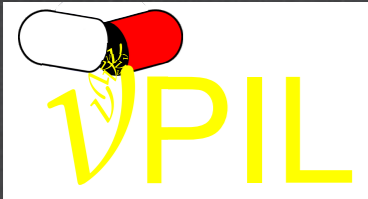




Double achromat FFAG beam line

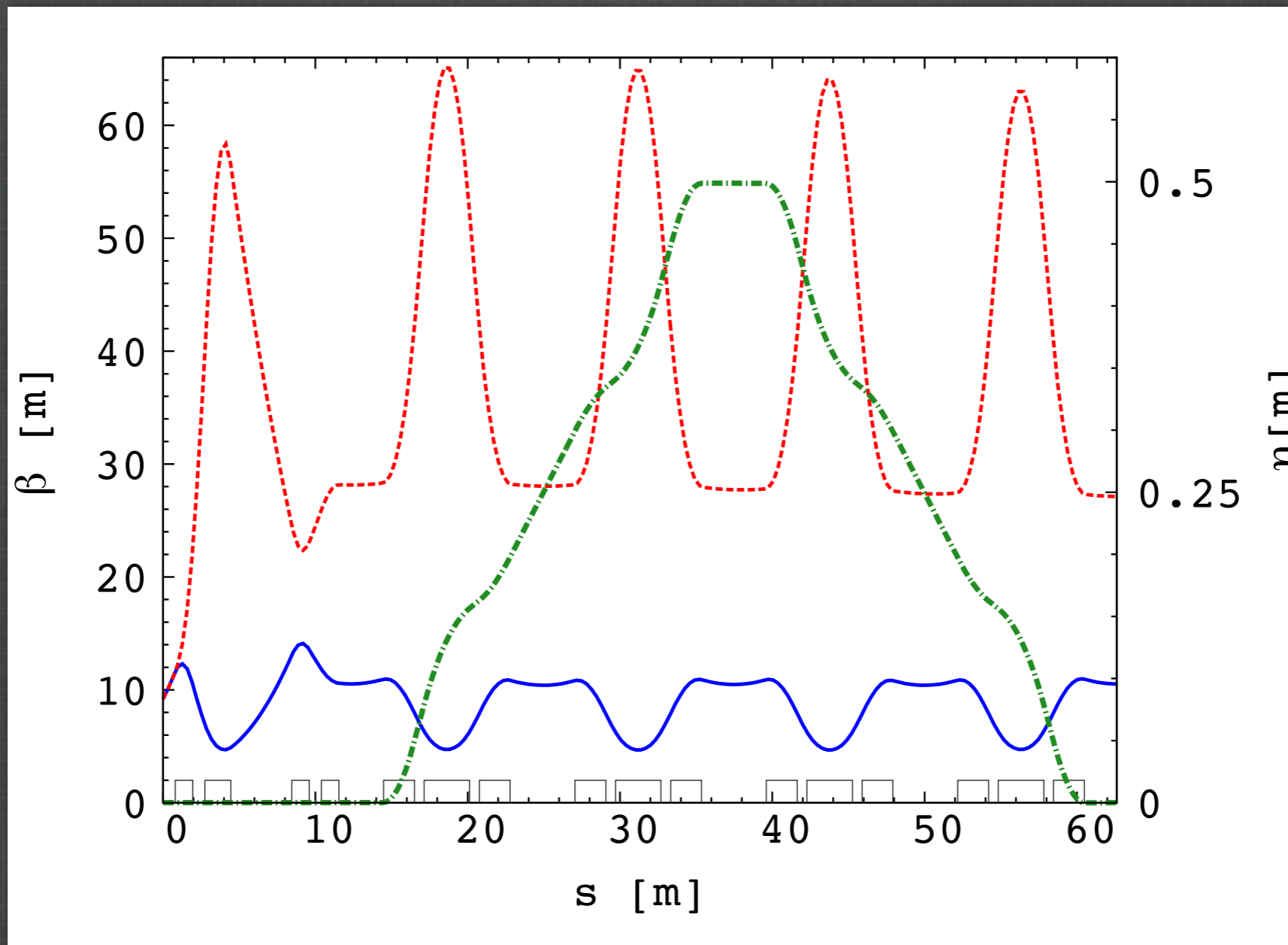


- Pions trajectories 3.5 GeV/c & 10.5 GeV/c
- $B_{\max} < 1.7$ T, excursion < 67 cm.
- k -value = 1988, $r_{\text{av}} = 496.5$ m, $L_{\text{beam line}} = \sim 60$ m.

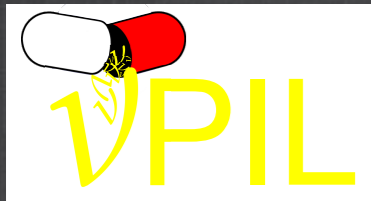


double achromat FFAG beam line

Beta-functions and dispersion at matching momentum

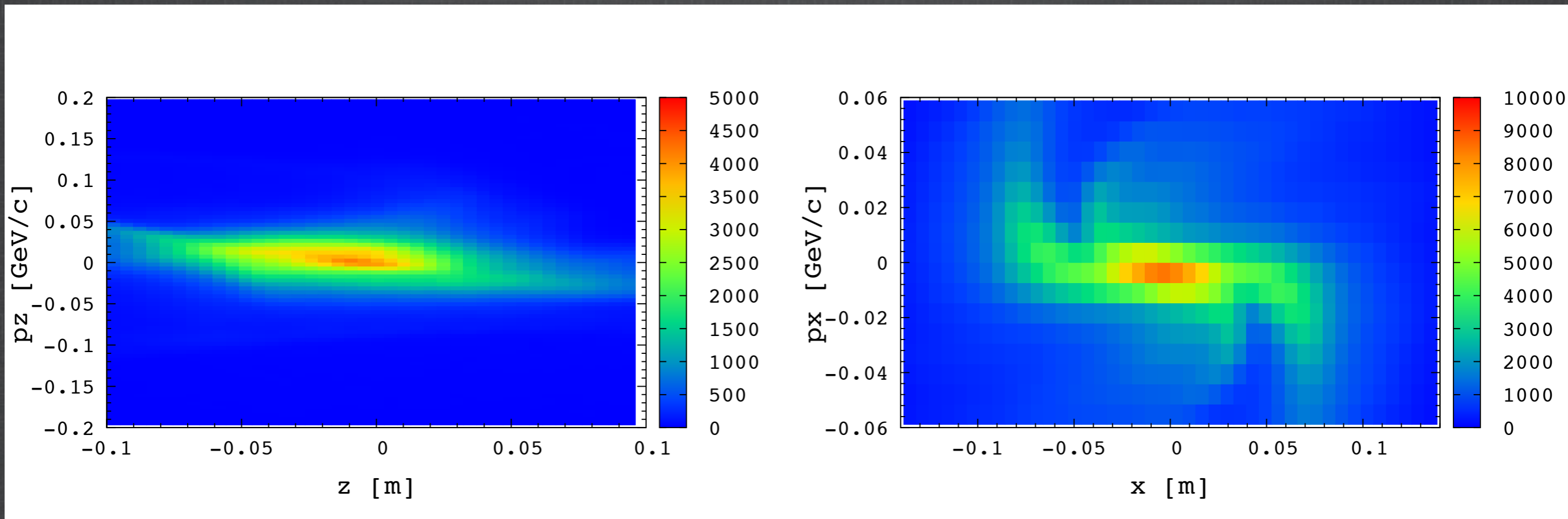


Horizontal (plain blue), vertical (dotted red) beta-functions and dispersion (mixed green).

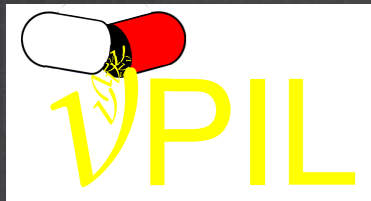


double achromat FFAG beam line

$\sim 2.9 \cdot 10^6$ particles (distribution from the horn) \longrightarrow 42.6% survival

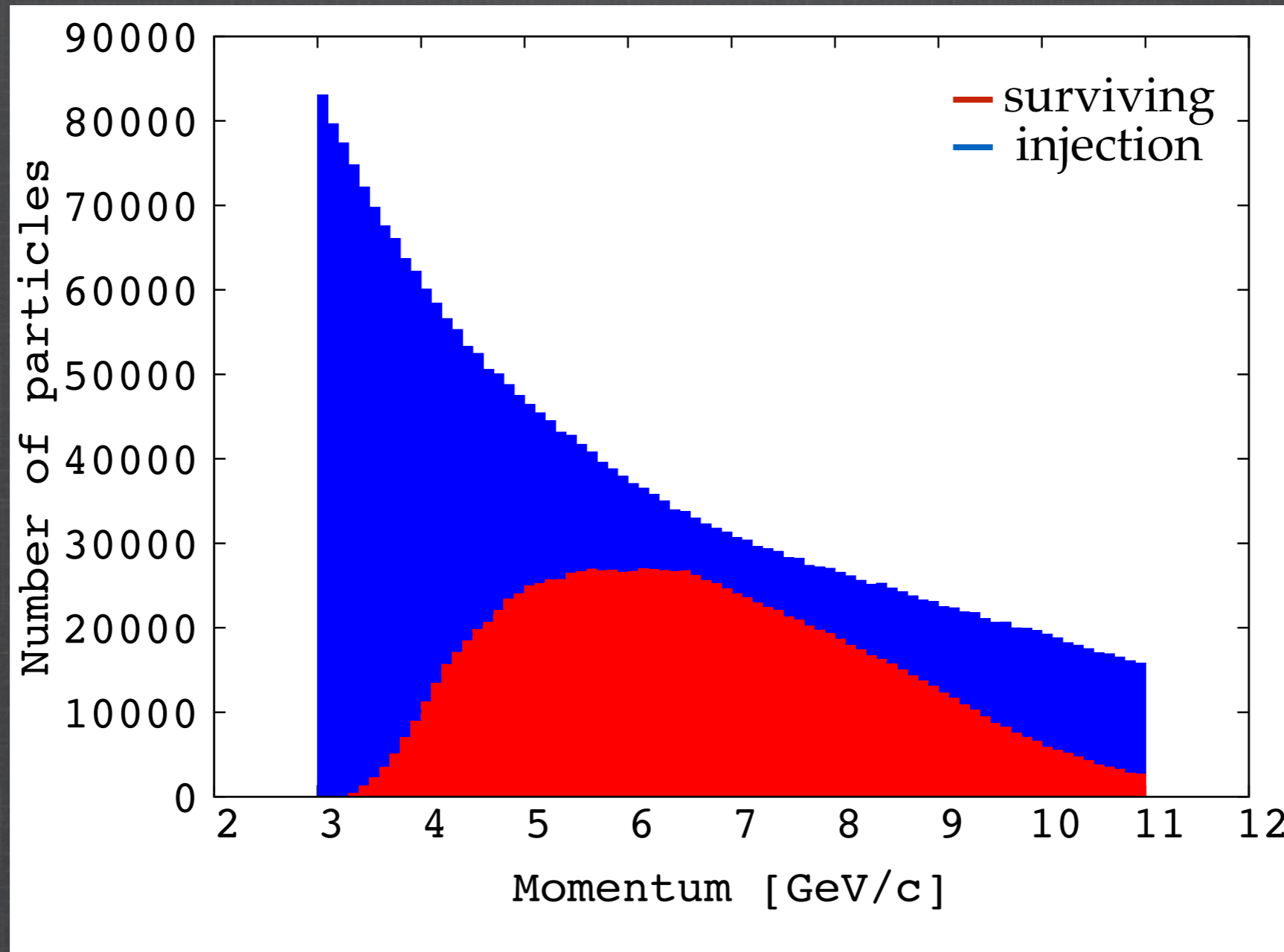


Surviving particles in vertical (left) and horizontal (right) phase spaces

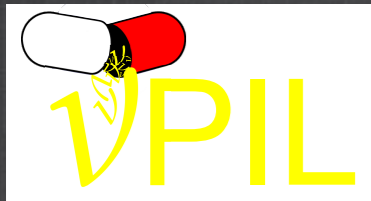


double achromat FFAG beam line

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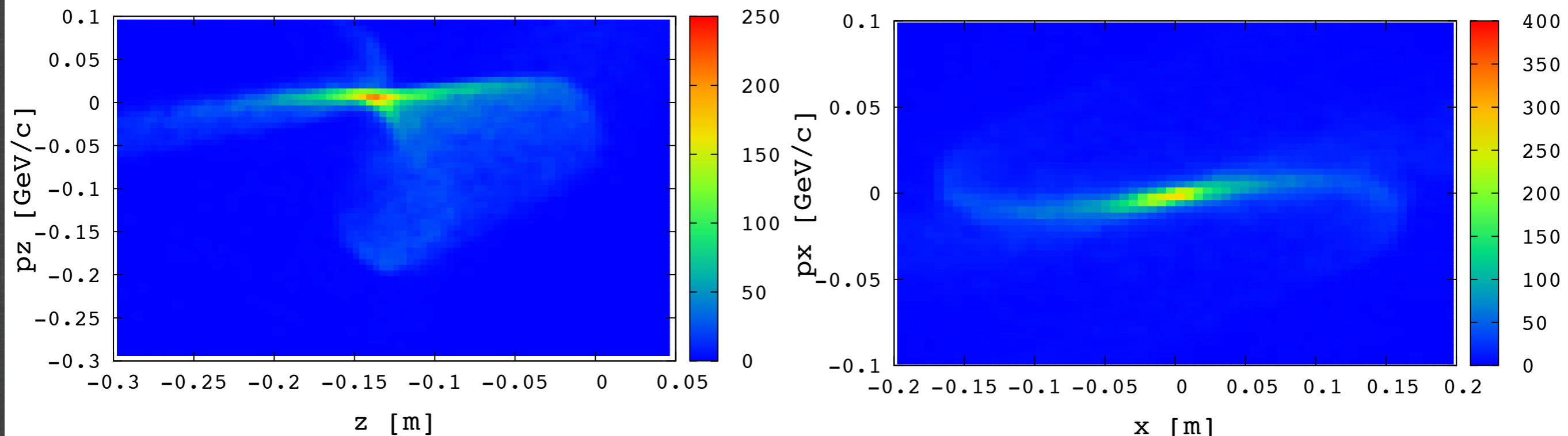
Momentum range at the injection (blue) and for the surviving particles (red) after tracking.



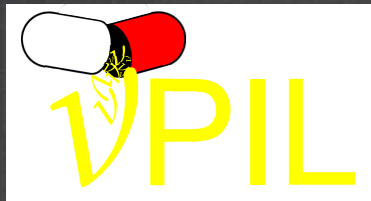
double achromat FFAG beam line

Wrong Sign Survival

$\sim 1.1 \cdot 10^6$ particles (distribution from the horn) \longrightarrow 3.2% survival



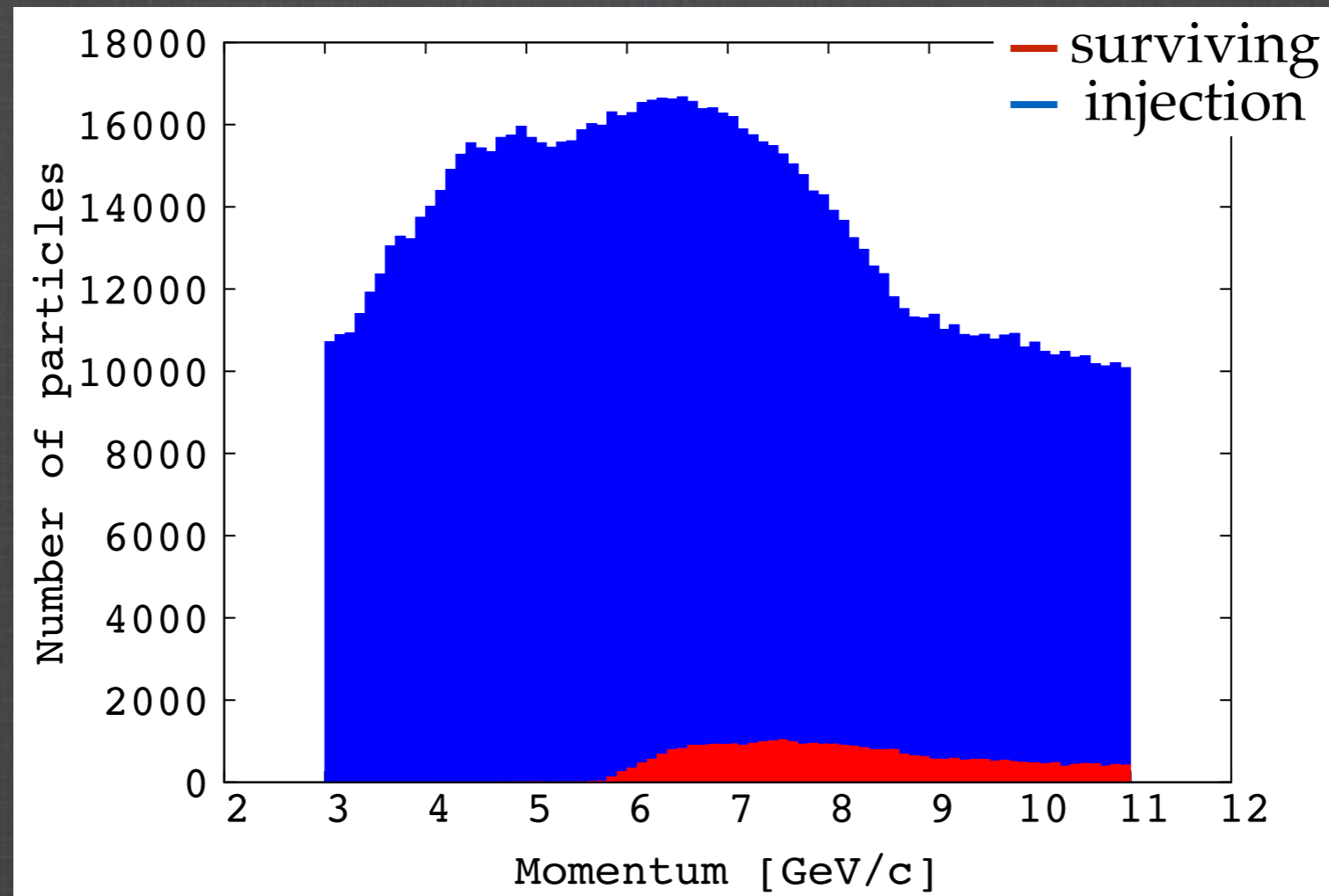
Surviving particles in vertical (left) and horizontal (right) phase spaces



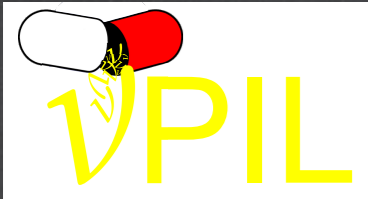
double achromat FFAG beam line

Wrong Sign Survival

$\sim 1.1 \cdot 10^6$ particles (distribution from the horn) \rightarrow 3.2% survival

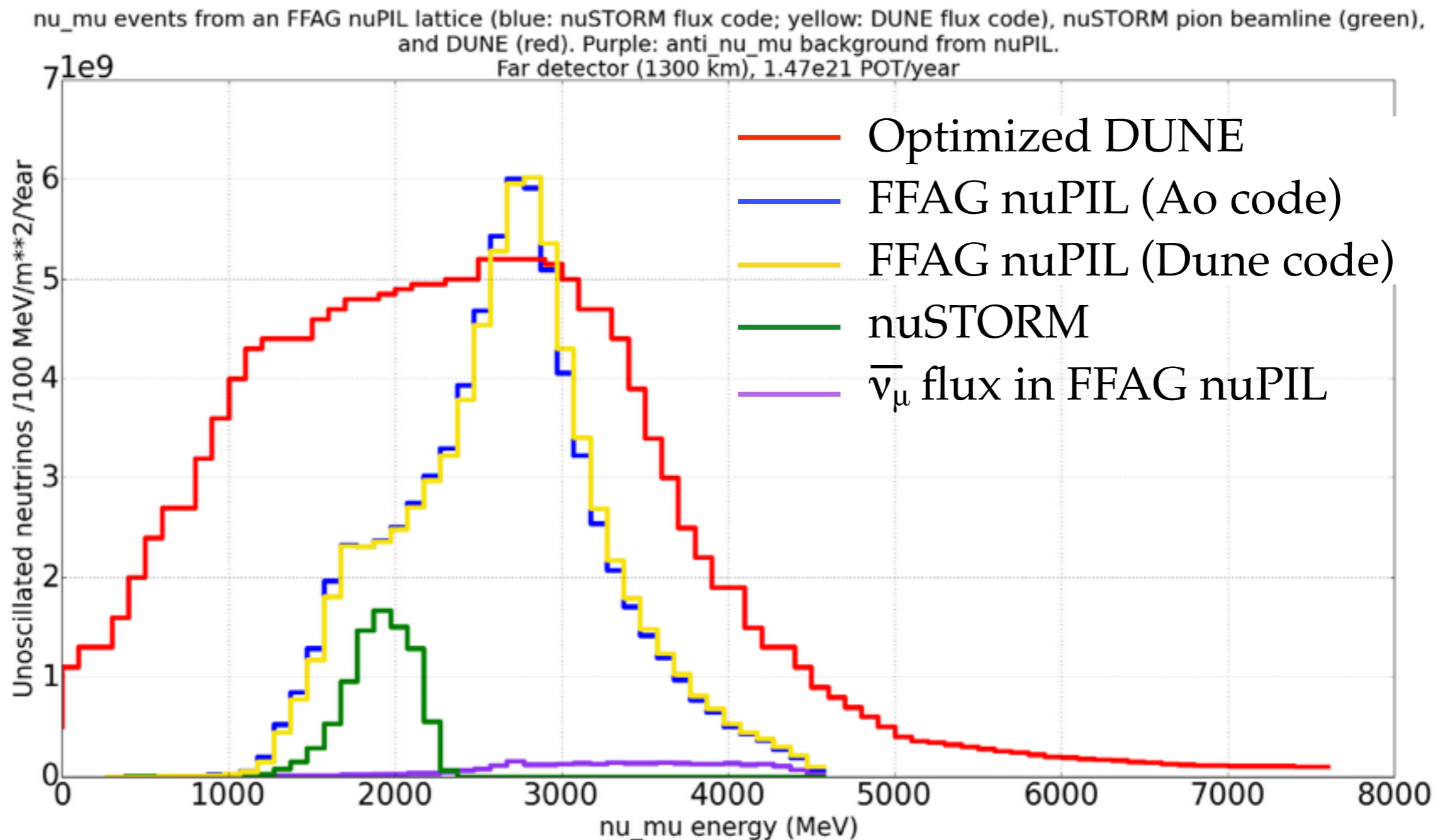


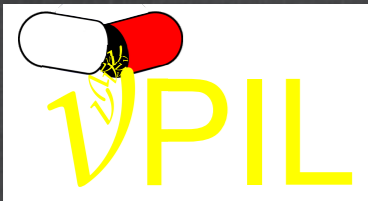
Momentum range at the injection (blue) and for the surviving particles (red) after tracking.



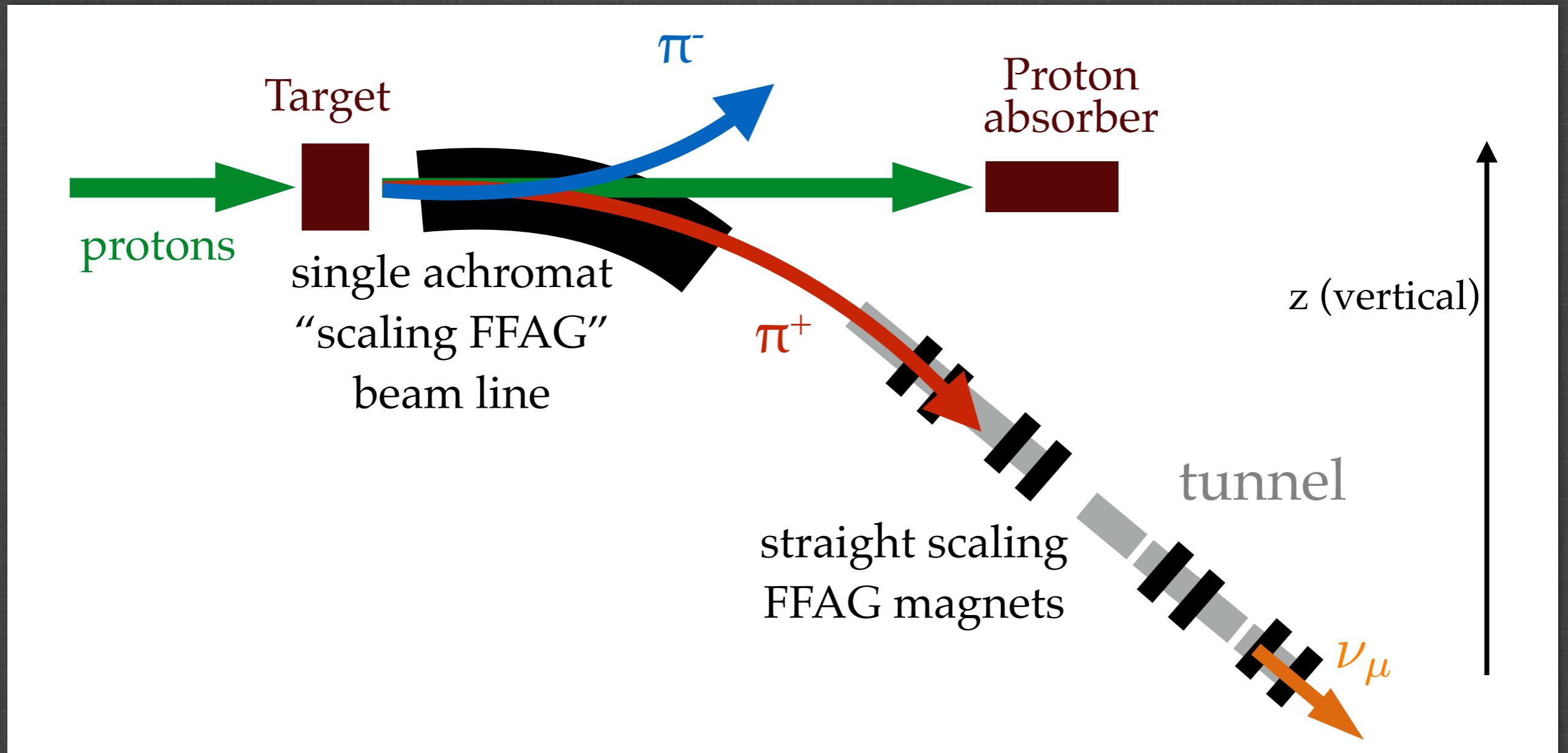
double achromat FFAG beam line

Flux

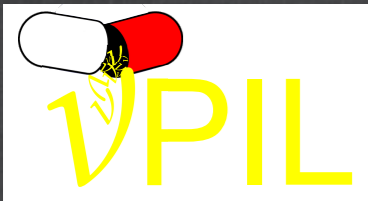




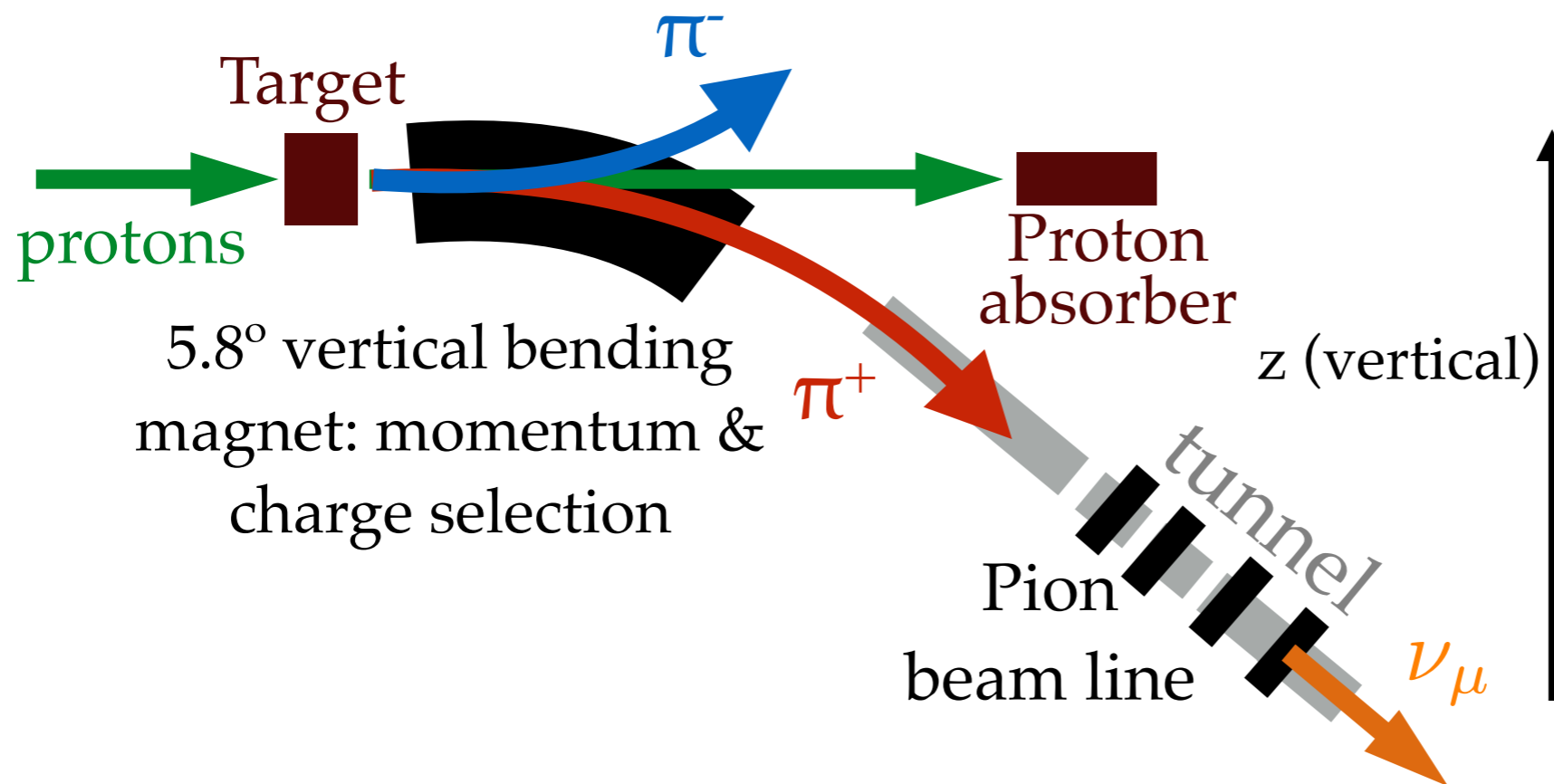
Full FFAG design concept

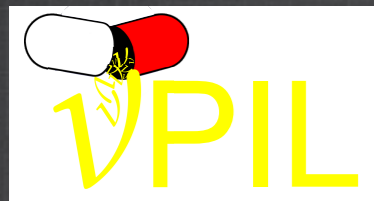


To be implemented

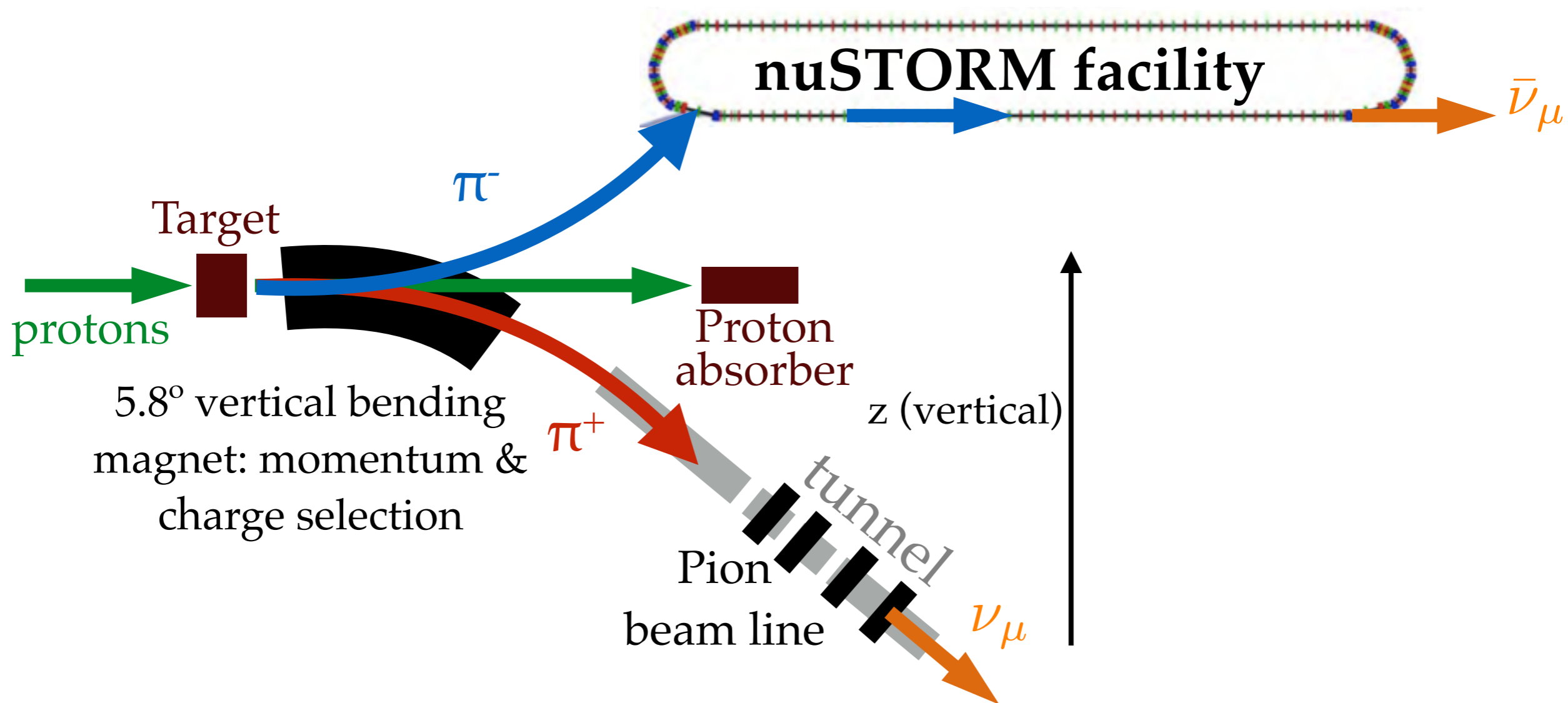


Going even further...

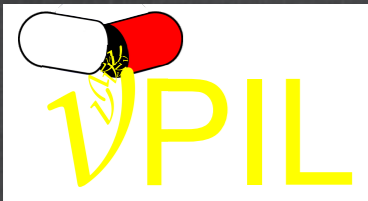




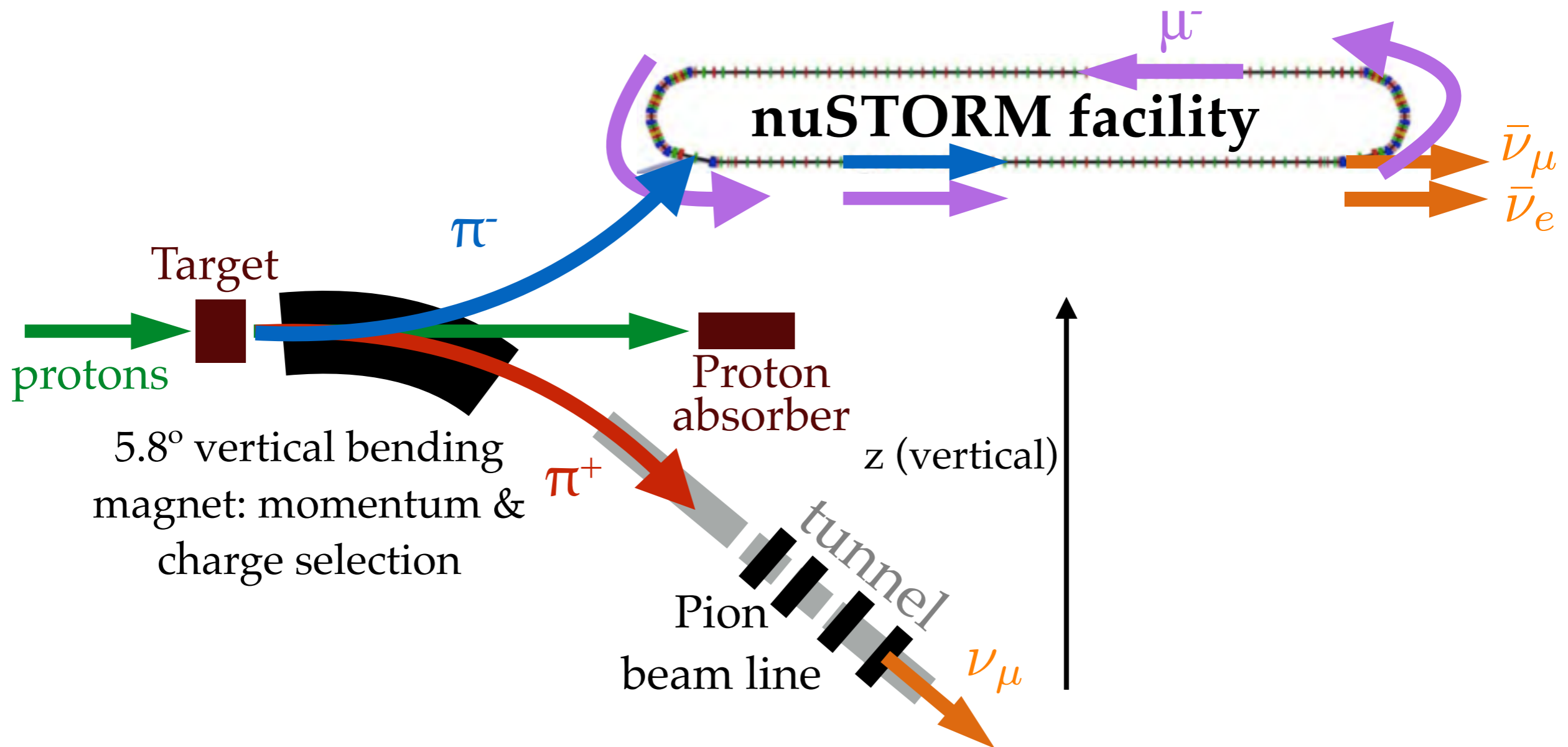
nuPIL AND nuSTORM?



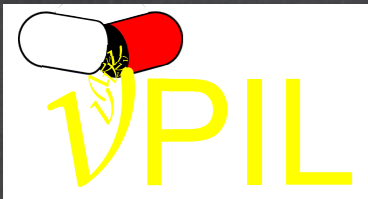
The wrong-sign pions could be used for Short Baseline experiments (i.e. nuSTORM).



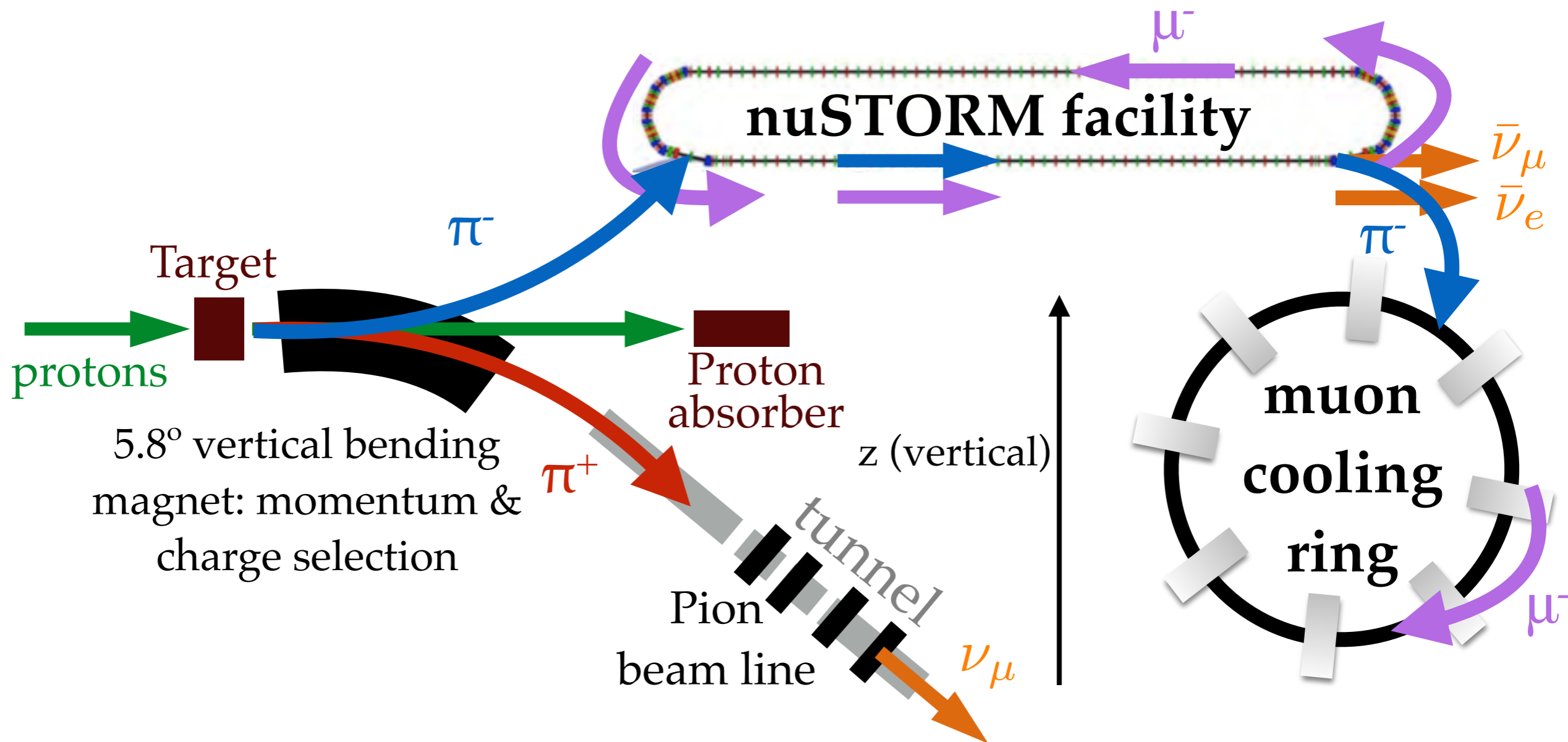
nuPIL AND nuSTORM?



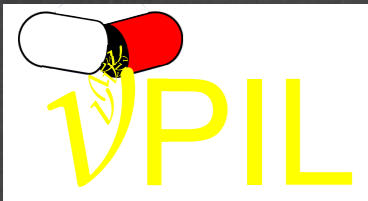
The wrong-sign pions could be used for Short Baseline experiments (i.e. nuSTORM).



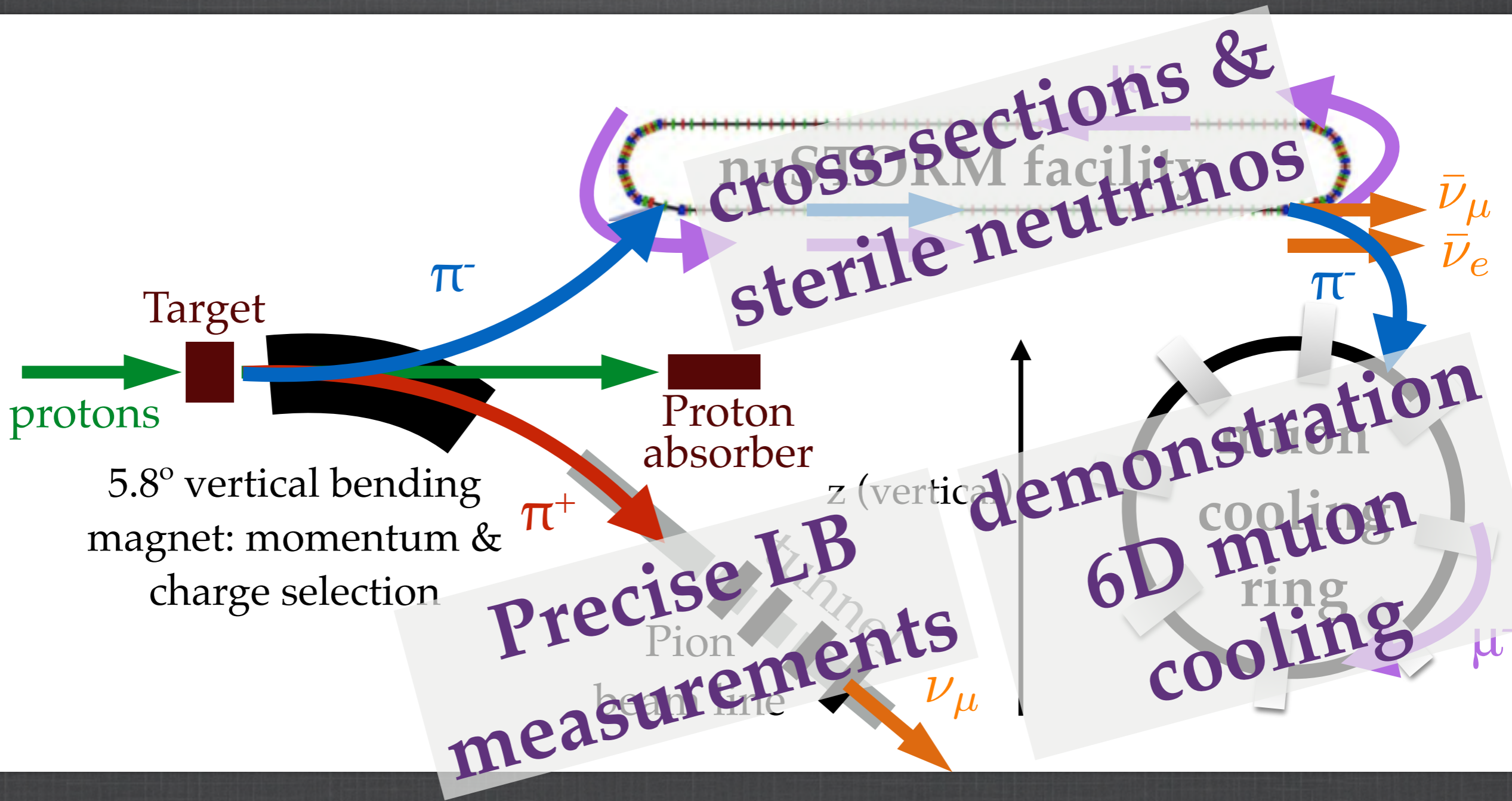
nuPIL AND nuSTORM, AND Rubbiatron?



Muon cooling experiment (C. Rubbia's ring) could also be implemented!



nuPIL AND nuSTORM, AND Rubbiatron?



Muon cooling experiment (C. Rubbia's ring) could also be implemented!

Thank you for your attention