Jet Substructures and Cross Sections in Proton and Heavy Ion Collisions

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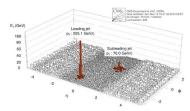
References: JHEP 1412 (2014) 061, arXiv:1509.07257, arXiv:1512.06851 and work in progress

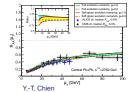
Outline

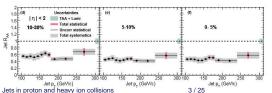
- Heavy ion collisions compared to proton collisions
 - Quark-gluon plasma (QGP)
 - Hard Probes with jets
 - Precision jet modification studies
- Resummation using Soft-Collinear Effective Theory (SCET)
 - Factorization theorem
 - Renormalization group evolution
- Medium Modification using SCET with Glauber gluons (SCET_G)
 - Medium induced splitting functions
- Results

Jet quenching in heavy ion collisions

- Hard probes of the QGP: the study of how various hard processes are affected by the presence of the medium. Traditionally,
 - J/ψ and charged hadron suppression
 - Debye screening and energy loss
 - $-R_{AA} = \frac{\sigma_{AA}}{\langle N_{coll} \rangle \ \sigma_{pp}} < 1$
 - jet quenching and dijet asymmetry
- Initial and final state energy loss can both contribute to the suppression of cross sections
- Kinematics of charged particles and jets contain limited information about the QGP
- How to disentangle the hot QGP from the cold nuclear matter effects?

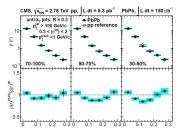


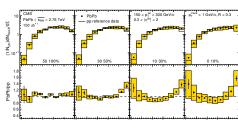




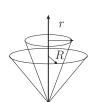
Jet modifications

- Jet substructure contains more information about the QGP
- Isolate final state effects
 - ullet jet shape: how energies are distributed in r
 - jet fragmentation function: how particles are distributed in z (or $\ln 1/z$)
 - Jet X modification factor: X_{AA}/X_{pp}





Jet shape, a classic jet substructure observable (Ellis, Kunszt, Soper)



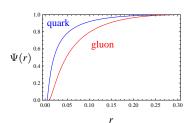
$$\Psi_J(r,R) = \frac{\sum_{r_i < r} E_{T_i}}{\sum_{r_i < R} E_{T_i}}$$

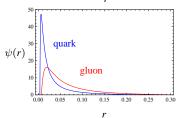
$$\langle \Psi \rangle = \frac{1}{N_J} \sum_{J}^{N_J} \Psi_J(r, R)$$

$$\psi(r, R) = \frac{d\langle \Psi \rangle}{dr}$$

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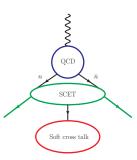
- Jet shapes probe the averaged energy distribution inside a jet
- The infrared structure of QCD induces Sudakov logarithms
- Fixed order calculation breaks down at small r
- Large logarithms of the form $\alpha_s^n \log^m r/R \ (m \le 2n)$ need to be resummed





Soft-Collinear Effective Theory (SCET)

- Effective field theory techniques are most useful when there is clear scale separation
- SCET separates physical degrees of freedom in QCD by a systematic expansion in power counting
 - Match SCET with QCD at the hard scale by integrating out the hard modes
 - Integrating out the off-shell modes gives collinear Wilson lines which describe the collinear radiation
 - The soft sector is described by soft Wilson lines along the jet directions
 - Soft-collinear decoupling holds at leading power in the Lagrangian, which leads to the factorization theorems of cross sections

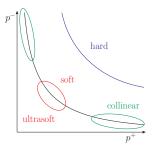


Power counting in SCET

The scaling of modes:

$$p_h: Q(1,1,1), p_c: Q(1,\lambda^2,\lambda) \text{ and } p_s: Q(\lambda,\lambda,\lambda)$$

- Q is at the hard scale which is the energy of the jet
- λ is the power counting parameter ($\lambda \approx m_J/Q$)
- QCD = $\mathcal{O}(\lambda^0) + \mathcal{O}(\lambda^1) + \cdots$ in SCET
- $Q\lambda$ is the jet scale which is significantly lower than Q



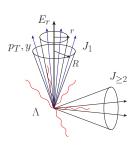
Jet shapes have dominant contributions from the collinear sector

$$\Psi(r) = \frac{E_c^{< r} + E_s^{< r}}{E_c^{< R} + E_s^{< R}} = \frac{E_c^{< r}}{E_c^{< R}} + \mathcal{O}(\lambda)$$

- Soft contributions are power suppressed
- For high p_T and narrow jets, power corrections are small and the leading power contribution is a very good approximation of the full QCD result

Factorization theorem for jet shapes in proton collisions (Chien et al)

 Without loss of generality, we demonstrate the calculation in e⁺e⁻ collisions since the initial state radiation in proton collisions contributes as power corrections



 The factorization theorem for the differential cross section of the production of N jets with p_{Ti}, y_i, the energy E_r inside the cone of size r in one jet, and an energy cutoff Λ outside all the jets is the following,

$$\frac{d\sigma}{dp_{T_i}dy_idE_r} = H(p_{T_i}, y_i, \mu)J_1^{\omega_1}(E_r, \mu)J_2^{\omega_2}(\mu)\dots S_{1,2,\dots}(\Lambda, \mu)$$

For the differential jet rate (without measuring E_r)

$$\frac{d\sigma}{dp_{T_{i}}dy_{i}} = H(p_{T_{i}}, y_{i}, \mu)J_{1}^{\omega_{1}}(\mu)J_{2}^{\omega_{2}}(\mu)\dots S_{1,2,\dots}(\Lambda, \mu)$$

- $J_1^{\omega}(E_r, \mu) = \sum_{X_c} \langle 0|\bar{\chi}_{\omega}(0)|X_c\rangle \langle X_c|\chi_{\omega}(0)|0\rangle \delta(E_r \hat{E}^{< r}(X_c, \text{algorithm}))$
 - X_c is constrained within jets by the corresponding jet algorithm
 - the energy outside jets is power suppressed
- The factorization theorem has a product form instead of a convolution

Factorization theorem for jet shapes (continued)

The averaged energy inside the cone of size r in jet 1 is the following,

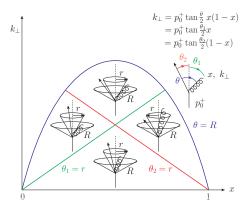
$$\langle E_r \rangle_{\omega} = \frac{1}{\frac{d\sigma}{dp_{T_i}dy_i}} \int dE_r E_r \frac{d\sigma}{dp_{T_i}dy_i dE_r} = \frac{H(p_{T_i}, y_i, \mu) J_{E, T_1}^{\omega_1}(\mu) J_2^{\omega_2}(\mu) \dots S_{1,2,\dots}(\Lambda, \mu)}{H(p_{T_i}, y_i, \mu) J_1^{\omega_1}(\mu) J_2^{\omega_2}(\mu) \dots S_{1,2,\dots}(\Lambda, \mu)} = \frac{J_{E, r_1}^{\omega_1}(\mu) J_{E, r_2}^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)}{J_1^{\omega_1}(\mu) J_2^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)} = \frac{J_{E, r_2}^{\omega_1}(\mu) J_{E, r_2}^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)}{J_1^{\omega_1}(\mu) J_2^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)} = \frac{J_{E, r_2}^{\omega_1}(\mu) J_{E, r_2}^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)}{J_1^{\omega_2}(\mu) J_2^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)} = \frac{J_{E, r_2}^{\omega_1}(\mu) J_2^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)}{J_1^{\omega_2}(\mu) J_2^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)} = \frac{J_{E, r_2}^{\omega_1}(\mu) J_2^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)}{J_1^{\omega_2}(\mu) J_2^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)} = \frac{J_{E, r_2}^{\omega_1}(\mu) J_2^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)}{J_1^{\omega_2}(\mu) J_2^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)} = \frac{J_{E, r_2}^{\omega_1}(\mu) J_2^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)}{J_1^{\omega_2}(\mu) J_2^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)} = \frac{J_{E, r_2}^{\omega_1}(\mu) J_2^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)}{J_1^{\omega_2}(\mu) J_2^{\omega_2}(\mu) \dots J_{1, r_2, \dots}(\Lambda, \mu)} = \frac{J_{E, r_2}^{\omega_1}(\mu) J_2^{\omega_2}(\mu) J_$$

- $J^{\omega}_{E,r}(\mu)=\int dE_r E_r J^{\omega}(E_r,\mu)$ is referred to as the jet energy function
- Nice cancelation between the hard, unmeasured jet and soft functions
- The integral jet shape, averaged over all jets, is the following

$$\langle \Psi \rangle = \frac{1}{\sigma_{\rm total}} \sum_{i=q,g} \int_{PS} dp_T dy \frac{d\sigma}{dp_T dy} \Psi^i_\omega \ , \ \text{where} \ \Psi_\omega = \frac{J_{E,r}(\mu)/J(\mu)}{J_{E,R}(\mu)/J(\mu)} = \frac{J_{E,r}(\mu)}{J_{E,R}(\mu)}$$

- ratio of sums equals weighted ratios (not sum of ratios)
- $\frac{a_1+a_2+...}{b_1+b_2+...} = \frac{1}{\sum_i b_i} (b_1 \frac{a_1}{b_1} + b_2 \frac{a_2}{b_2} + ...)$
- Using the collinear SCET Feynman rules, the jet energy function $J_{E,r}(\mu)$ and its anomalous dimension are calculated at $\mathcal{O}(\alpha_s)$ for both quark jets and gluon jets

Jet energy function



- $J_{E,r}^{\omega}(\mu) = \sum_{X_c} \langle 0|\bar{\chi}_{\omega}(0)|X_c\rangle\langle X_c|\chi_{\omega}(0)|0\rangle \hat{E}^{< r}(X_c)$
- At O(α_s), the phase space integrals in the jet energy function calculations are illustrated
- The axis is fixed and along the jet direction

$$\frac{dJ_{E,r}^g(r,R,\mu)}{d\ln\mu} = \left[-C_F \Gamma_{\text{cusp}} \ln \frac{\omega^2 \tan^2 \frac{R}{2}}{\mu^2} - 2\gamma_{Jq} \right] J_{E,r}^q(r,R,\mu)$$

$$\frac{dJ_{E,r}^g(r,R,\mu)}{d\ln\mu} = \left[-C_A \Gamma_{\text{cusp}} \ln \frac{\omega^2 \tan^2 \frac{R}{2}}{\mu^2} - 2\gamma_{Js} \right] J_{E,r}^g(r,R,\mu)$$

The anomalous dimensions of the jet energy functions are

$$\gamma_{Jq} = -3C_F$$
, $\gamma_{Jg} = -\beta_0 = -\frac{11}{3}C_A + \frac{4}{3}T_F n_f$

• $\langle E_r \rangle_{\omega}$ and Ψ_{ω} are renormalization group invariant

$$\Psi_{\omega} = rac{J_{E,r}(\mu)}{J_{E,R}(\mu)} = rac{J_{E,r}(\mu_{j_r})}{J_{E,R}(\mu_{j_R})} U_J(\mu_{j_r}, \mu_{j_R})$$

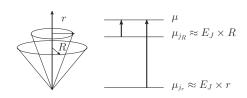
- Identify the natural scale μ_{j_r} to eliminate large logarithms in $J_{E,r}(\mu_{j_r})$
- The RG evolution kernel $U_J(\mu_{j_r},\mu_{j_R})$ resums the large logarithms

Natural scales

• The quark jet energy function at $\mathcal{O}(\alpha_s)$ is the following

$$\begin{split} \frac{2}{\omega}J_{E,r}^q &= \frac{\alpha_s C_F}{2\pi} \left[\frac{1}{2} \ln^2 \frac{\omega^2 \tan^2 \frac{r}{2}}{\mu^2} - \frac{3}{2} \ln \frac{\omega^2 \tan^2 \frac{r}{2}}{\mu^2} - 2 \ln X \ln \frac{\omega^2 \tan^2 \frac{r}{2}}{\mu^2} + 2 - \frac{3\pi^2}{4} \right. \\ &\quad + 6X - \frac{3}{2}X^2 - \left(\frac{1}{2}X^2 - 2X^3 + \frac{3}{4}X^4 + 2X^2 \log X \right) \tan^2 \frac{R}{2} \right], \text{ where } X = \frac{\tan \frac{r}{2}}{\tan \frac{R}{2}} \approx \frac{r}{R} \end{split}$$

• The scale $\mu_{j_r} = \omega \tan \frac{r}{2} \approx E_J \times r$ eliminates large logarithms in $J_{E,r}^q$ at $\mathcal{O}(\alpha_s)$

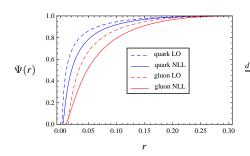


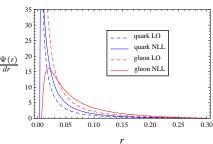
RG evolution between μ_{j_r} and μ_{j_R} resums $\log \mu_{j_r}/\mu_{j_R} = \log r/R$

Resummed jet energy functions

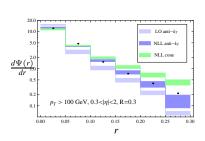
• $\log r/R$ are resummed using the RG kernels in SCET (i=q,g)

$$\begin{split} \Psi_{\omega}^{i}(r,R) &= \frac{J_{r}^{iE}(r,R,\mu_{j_{r}})}{J_{R}^{iE}(R,\mu_{j_{R}})} \exp[-2 C_{i} S(\mu_{j_{r}},\mu_{j_{R}}) + 2 A_{J^{i}}(\mu_{j_{r}},\mu_{j_{R}})] \left(\frac{\mu_{j_{r}}^{2}}{\omega^{2} \tan^{2} \frac{R}{2}}\right)^{C_{i} A_{\Gamma}(\mu_{j_{R}},\mu_{j_{r}})} \\ S(\nu,\mu) &= -\int_{\alpha_{s}(\nu)}^{\alpha_{s}(\mu)} d\alpha \frac{\Gamma_{\text{cusp}}(\alpha)}{\beta(\alpha)} \int_{\alpha_{s}(\nu)}^{\alpha} \frac{d\alpha'}{\beta(\alpha')}, \quad A_{X}(\nu,\mu) = -\int_{\alpha_{s}(\nu)}^{\alpha_{s}(\mu)} d\alpha \frac{\gamma_{X}(\alpha)}{\beta(\alpha)} \end{split}$$

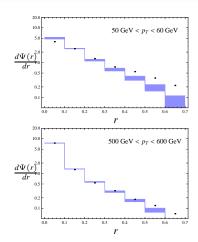




Comparison with the CMS data at 2.76 and 7 TeV



- The difference for jets reconstructed using different jet algorithms is of $\mathcal{O}(r/R)$
- Bands are theory uncertainties estimated by varying μ_{i_r} and μ_{i_R}
- In the region $r \approx R$ we may need higher fixed order calculations and include power corrections



- NLL, anti- k_T , R = 0.7
- For low p_T jets, power corrections have significant contributions

Jet shapes in heavy ion collisions

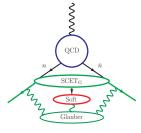
More generally, the jet energy function can be calculated from integrating the splitting functions over appropriate phase spaces. At the leading-order splitting,

$$J_{E,r}^{i}(\mu) = \sum_{i,k} \int_{PS} dx dk_{\perp} \left[\frac{dN_{i \to jk}^{vac}}{dx d^{2}k_{\perp}} + \frac{dN_{i \to jk}^{med}}{dx d^{2}k_{\perp}} \right] E_{r}(x, k_{\perp})$$

 The medium induced splitting functions are calculated numerically using SCET_G with realistic hydrodynamic QGP models

SCET with Glauber gluons (SCET_G)

- The Glauber region of phase space is the other relevant mode
- SCET_G was constructed from SCET bottom up (Idilbi et al, Vitev et al)
 - Glauber gluon momentum scales as $p_G : Q(\lambda^2, \lambda^2, \lambda)$
 - Glauber gluons are off-shell modes providing momentum transfer transverse to the jet direction
 - Glauber gluons are treated as background fields generated from the colored charges in the QGP



- In principle, Glauber gluons interact with both the collinear and the soft modes
- However, jet shapes have dominant contributions from the collinear sector so the Glauber-collinear interaction is the most relevant

Jet shapes in heavy ion collisions (continued)

Jet shapes get modified through the modification of jet energy functions

$$\Psi(r) = \frac{J_{E,r}^{vac} + J_{E,r}^{mea}}{J_{E,R}^{vac} + J_{E,R}^{med}} = \frac{\Psi^{vac}(r)J_{E,R}^{vac} + J_{E,r}^{mea}}{J_{E,R}^{vac} + J_{E,R}^{med}}$$

- Large logarithms in $\Psi^{vac}(r) = J_{E,r}^{vac}/J_{E,R}^{vac}$ have been resummed
- There are no large logarithms in $J_{E,r}^{med}$ due to the LPM effect
- The RG evolution of medium-modified jet energy functions is unchanged
- However, with the use of small R's in heavy ion collisions, there is significant jet energy loss which leads to the suppression of jet production cross sections
- Jet-by-jet shapes are averaged with the jet cross sections

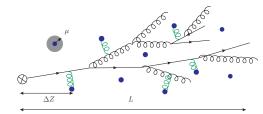
$$\frac{d\sigma^k}{d\eta dp_T} = \langle N_{\text{bin}} \rangle \sum_{ijX} \int dx_1 dx_2 f_i^A(x_1, \mu) f_j^A(x_2, \mu) \frac{d\sigma_{ij \to kX}}{dx_1 dx_2 d\eta dp_T}$$

$$\left. rac{d\sigma_{AA}^i}{d\eta dp_T}
ight|_{p_T} = \left. rac{d\sigma_{pp}^i}{d\eta dp_T}
ight|_{rac{p_T}{1-\epsilon_i}} rac{1}{1-\epsilon_i}$$

• With cold nuclear matter effects in nuclear parton distributions

Multiple scattering in a medium

- Coherent multiple scattering and induced bremsstrahlung are the qualitatively new ingredients in the medium parton shower
- Interplay between several characteristic scales:
 - Debye screening scale μ
 - $\bullet \ \ {\rm Parton \ mean \ free \ path \ } \lambda$
 - Radiation formation time τ
- From thermal field theory and lattice QCD calculations, an ensemble of quasi particles with debye screened potential and thermal masses is a reasonable parameterization of the medium properties



$$\frac{1}{\sigma_{el}} \frac{d\sigma_{el}}{d^2 q_\perp} = \frac{\mu^2}{\pi (q_\perp^2 + \mu^2)^2}$$

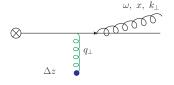
Landau-Pomeranchuk-Migdal effect

• The hierarchy between τ and λ determines the degree of coherence between multiple scatterings

$$au = rac{x \, \omega}{(q_{\perp} - k_{\perp})^2}$$
 v.s. λ



•
$$\tau \ll \lambda$$
: Bethe-Heitler incoherence limit



Medium induced splitting functions calculated using SCET_G (Ovanesyan et al)

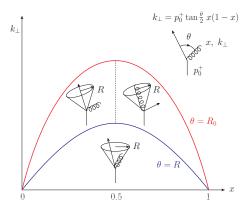
$$\frac{dN_{q\to qg}^{med}}{dxd^2k_{\perp}} = \frac{C_F\alpha_s}{\pi^2} \frac{1}{x} \int_0^L \frac{d\Delta z}{\lambda} \int d^2q_{\perp} \frac{1}{\sigma_{el}} \frac{d\sigma_{el}}{d^2q_{\perp}} \frac{2k_{\perp} \cdot q_{\perp}}{k_{\perp}^2(q_{\perp} - k_{\perp})^2} \left[1 - \cos\left(\frac{(q_{\perp} - k_{\perp})^2 \Delta z}{x\omega}\right) \right]$$

• $\frac{dN^{med}}{dxd^2k_\perp}
ightarrow$ finite as $k_\perp
ightarrow 0$: the LPM effect

•
$$\frac{dN^{vac}}{dxd^2k_{\perp}}
ightarrow \frac{1}{k_{\perp}}$$
 as $k_{\perp}
ightarrow 0$

Large angle bremsstrahlung takes away energy, resulting parton energy loss

Jet energy loss

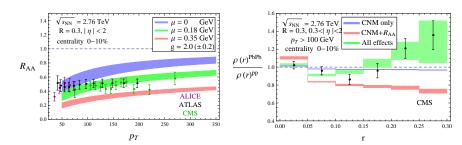


• For a parton shower constrained within radius R_0 ($\mathcal{O}(1)$), the averaged energy outside the leading anti- k_T jet of size R is the jet energy loss

Medium Modifications using SCETG

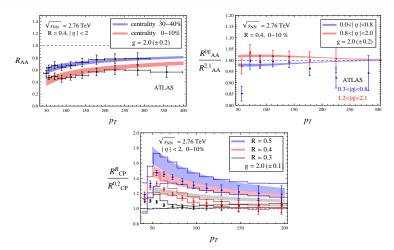
 The jet axis is not necessarily along the original parton direction

Results



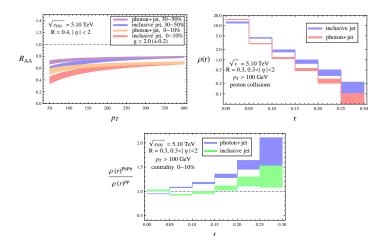
- The plots are the ratios between the jet cross sections and differential jet shapes in lead-lead and proton collisions
- Jet shapes are insensitive to cold nuclear matter effects
- Gluon jets are more suppressed which increases the quark jet fraction
- · Jet-by-jet the shape is broadened

Results



 The plots shows the dependence of jet cross section suppressions on centrality, jet rapidity and jet radius

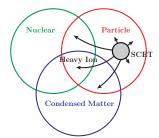
Results



 Predictions for jet shapes and cross sections at 5 TeV for inclusive and photon-tagged jets

Conclusions and outlooks

- Jet shapes in proton and heavy ion collisions are calculated within the same framework
 - Promising agreement with data and phenomenological applications
- The modification of jet shapes is a combination of cross section suppression and jet-by-jet broadening
- · Work in progress and future work
 - Calculate jet fragmentation function modifications
 - Construct SCET at finite temperature
 - Modification of other jet substructure observables more sensitive to soft physics



- The physics of heavy ion collisions is a multi-disciplinary subject
- The study of jet quenching is a unique opportunity to probe non-perturbative QCD physics with perturbative objects
- SCET can make important contributions in these new territories!