

# In-situ absolute flux constraints from FastMC studies

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# Outline

ND Parametrized Simulation/Reconstruction (Fast MC)

$$\nu e^- \rightarrow \nu e^-$$

Inverse Muon Decay

Summary and Outlook

# ND Parametrized Simulation/Reconstruction (Fast MC)

## ND Parametrized Simulation/Reconstruction (Fast MC)

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## Fast MC Basics

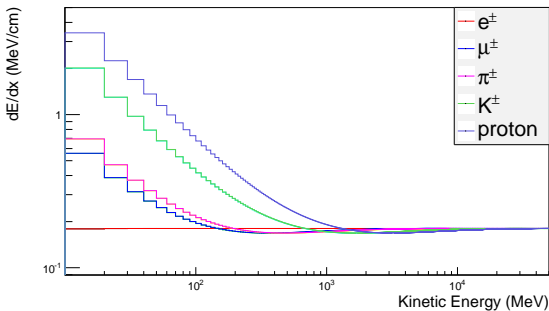
- Fast MC = Fast Detector Simulation + Fast Reconstruction
  - Originally developed by Daniel Cherdack and Rik Gran for LBNE FD. Re-use as much as possible the existing Fast MC codes. It is also a good cross check of the existing code
- The Chain: G4LBNE→GENIE→ND Fast MC→Analyzing the output ROOT files
  - G4LBNE produces the flux
  - GENIE produces the interactions with a homogeneous detector with approximately the same composition as the current design of HiResM<sub>ν</sub>
  - ND Fast MC will mimic the detector simulation and reconstruction to produce the “reconstructed” variables for downstream analysis
  - Analyzing the output “reconstructed” ROOT files for specific topics
- Use the existing NOMAD data to benchmark the whole chain

## ND specs (FGT)

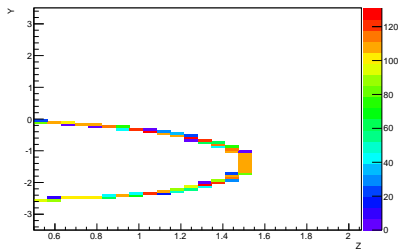
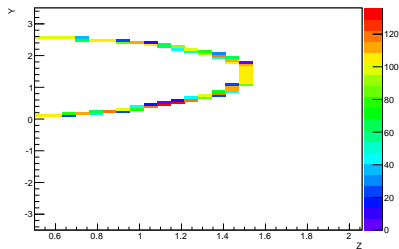
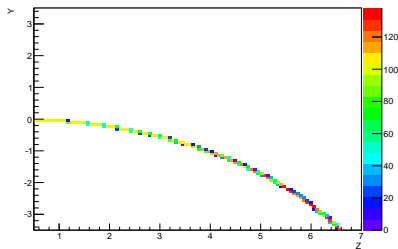
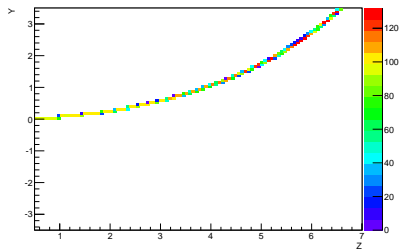
- These are defined in the configuration file:  
\$FMC\_CONFIG/FastMC\_DetParams.xml within the block of  
<param\_set name="STT\_1" >
- Internal Magnetic Volume:  $4.0 \times 4.0 \times 8.1$  m
- Tracker volume (STT):  $3.5 \times 3.5 \times 7.04$  m (**6.40 m**), density =  $0.1$  g/cm<sup>3</sup>
- Fiducial volume:  $|x, y| < 150$  cm,  $25 < z < 550$  cm
- Radiation length:  $X_0 \simeq 600$  cm
- hadronic interaction length: 1,200 cm
- Charged particle momentum resolution:  $\sigma_p/p = \frac{0.05}{\sqrt{L}} + 0.008p/\sqrt{L^5}$ ,  
where  $L$  is the track length
- Angular resolution:  $\theta_0 = \frac{13.6 \text{ MeV}}{\beta c p} z \sqrt{x/X_0} [1 + 0.038 \ln(x/X_0)]$
- EM shower energy resolution:  $\sigma_E/E = 1\% + 0.06/\sqrt{E}$
- Hadronic shower energy resolution:  $\sigma_E/E = 1\% + 0.50/\sqrt{E}$

## $dE/dx$ as a function of kinetic energy

- $dE/dx$  as a function of kinetic energy determined by a standalone G4 simulation with a homogeneous HiResM $\nu$  detector: same detector composition as in the GENIE phase.
  - Geant4  $\rightarrow$  Kinetic energy &  $dE/dx$  table  $\rightarrow$   $dE/dx$  as function of kinetic energy histograms



# Magnetic field : 4<sup>th</sup> order Runge-Kutta method, same method as used in Geant4



$$\nu e^- \rightarrow \nu e^-$$

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ND Parametrized Simulation/Reconstruction (Fast MC)

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Summary and Outlook



$\nu e^- \rightarrow \nu e^-$  1

- Cross section is extremely small

- $\sigma(\nu_{\mu,\tau} e \rightarrow \nu_{\mu,\tau} e) = \frac{G_\mu^2 m_e E_\nu}{2\pi} [1 - 4 \sin^2 \theta_W + \frac{16}{3} \sin^4 \theta_W]$

- $\sigma(\bar{\nu}_{\mu,\tau} e \rightarrow \bar{\nu}_{\mu,\tau} e) = \frac{G_\mu^2 m_e E_\nu}{2\pi} [\frac{1}{3} - \frac{4}{3} \sin^2 \theta_W + \frac{16}{3} \sin^4 \theta_W]$

- $\sigma(\nu_e e \rightarrow \nu_e e) = \frac{G_\mu^2 m_e E_\nu}{2\pi} [1 + 4 \sin^2 \theta_W + \frac{16}{3} \sin^4 \theta_W]$

- $\sigma(\bar{\nu}_e e \rightarrow \bar{\nu}_e e) = \frac{G_\mu^2 m_e E_\nu}{2\pi} [\frac{1}{3} + \frac{4}{3} \sin^2 \theta_W + \frac{16}{3} \sin^4 \theta_W]$

- $\sigma(\nu_{\mu,\tau} e \rightarrow \nu_{\mu,\tau} e) : \sigma(\bar{\nu}_{\mu,\tau} e \rightarrow \bar{\nu}_{\mu,\tau} e) : \sigma(\nu_e e \rightarrow \nu_e e) : \sigma(\bar{\nu}_e e \rightarrow \bar{\nu}_e e) = 1 : 0.854 : 6.077 : 2.547$

- 10520  $\nu e^- \rightarrow \nu e^-$  events assuming 1.2 MW beam power, 5 tons ND fiducial mass, 5 years neutrino running

- $\sigma(\nu_\mu e \rightarrow \nu_\mu e) : \sigma(\bar{\nu}_\mu e \rightarrow \bar{\nu}_\mu e) : \sigma(\nu_e e \rightarrow \nu_e e) : \sigma(\bar{\nu}_e e \rightarrow \bar{\nu}_e e) \simeq 7800 : 1690 : 845 : 184$

- A clean determination of the neutrino flux
- A clean determination of the weak mixing angle  $\sin^2 \theta_W$

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<sup>1</sup>W. Marciano and Z. Parsa, arXiv: hep-ph/0403168

## Selection Cuts

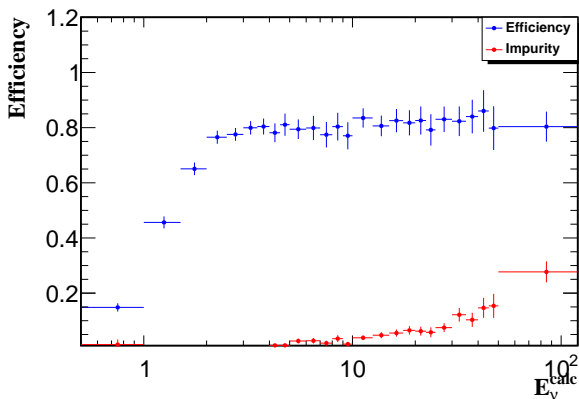
Cut	Sig.	Sig. Eff.	Back.	Back. Surv. Prob.
Fiducial	1.052e+04	1	9.747e+07	1
$p_e > 0.2 \text{ GeV}/c$ & $n_e^{\text{hits}} \geq 4$	9784	0.9301	9.607e+07	0.9856
$\mu$ -veto	9784	0.9301	3.476e+07	0.3566
$\pi^0/n/K_0$ veto	9784	0.9301	1.69e+07	0.1734
no positive track	9784	0.9301	2.961e+06	0.03038
1 negative track	8724	0.8294	2.288e+04	0.0002347
$E_e > 0.5 \text{ GeV}$ & $n_e^{\text{hits}} \geq 12$	7680	0.7301	331.5	3.401e-06
$p_e^T < 0.1 \text{ GeV}$	7677	0.7298	324.9	3.333e-06
$\theta_e < 0.1 \text{ Rad}$	7677	0.7298	324.9	3.333e-06

- $\mu_{\text{ID}}$ :
  - $\mu_{\text{ID}} = 60\%$  @  $p_\mu \in [0.2, 0.6] \text{ GeV}/c$ ,
  - $\mu_{\text{ID}} = 80\%$  @  $p_\mu \in [0.6, 1.0] \text{ GeV}/c$ ,
  - $\mu_{\text{ID}} = 95\%$  @  $p_\mu > 1.0 \text{ GeV}/c$ .
- $\pi^0$  veto: Require  $p_\gamma < 0.08 \text{ GeV}$ ,
- neutron veto: Require  $T_n < 0.25 \text{ GeV}$ ,
- $K_0$  veto: Require  $T_{K_0} < 0.25 \text{ GeV}$ ,
- TRD efficiency applied: 90% for electron,  $10^{-3}$  for  $\mu^\pm, \pi^\pm, K^\pm$ , etc.

$\nu e^- \rightarrow \nu e^-$  efficiency as a function of  $E_{\text{calc}}$ 

- Average signal efficiency is 73% (7677 signal events passing the cuts) with 4% background

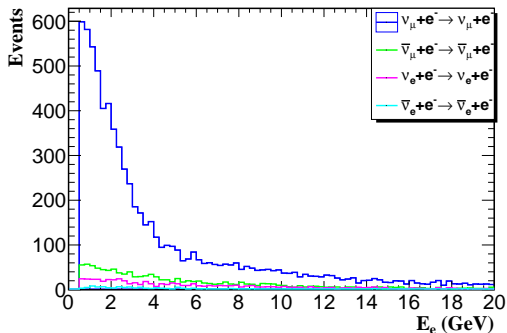
$$E_{\nu}^{\text{calc}} = \frac{(M_e E_e - M_e^2)}{M_e - E_e + E_e \cos \theta_e} \quad (1)$$

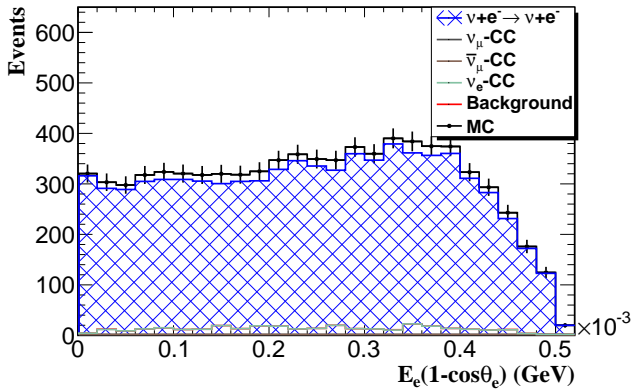


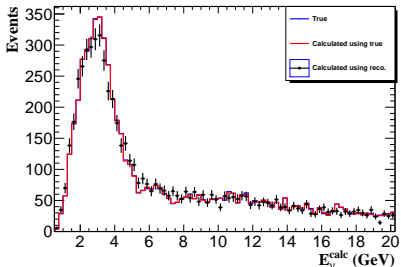
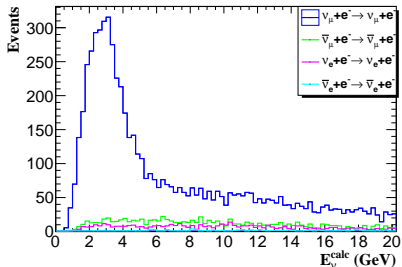
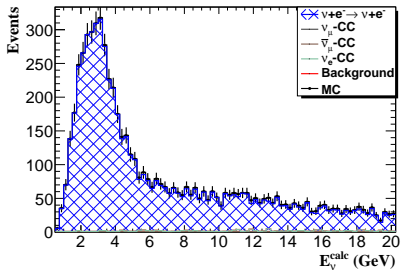
## $\nu e \rightarrow \nu e$ composition

Energy Range	$\nu_\mu$	$\bar{\nu}_\mu$	$\nu_e$	$\bar{\nu}_e$
0.5-5.0 GeV	0.907	0.085	0.006	0.001
5.0-10 GeV	0.624	0.345	0.022	0.009
> 10 GeV	0.624	0.332	0.026	0.017

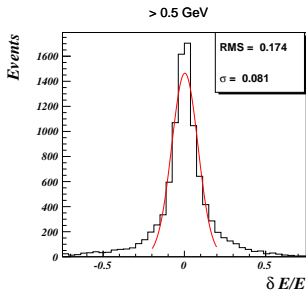
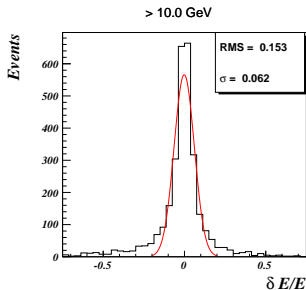
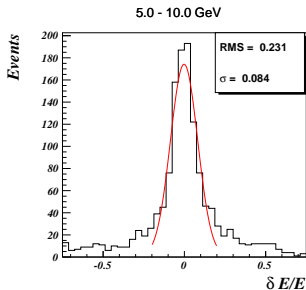
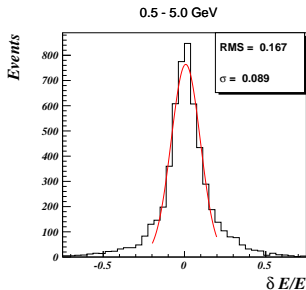
**Table:** Flux composition in different energy range.



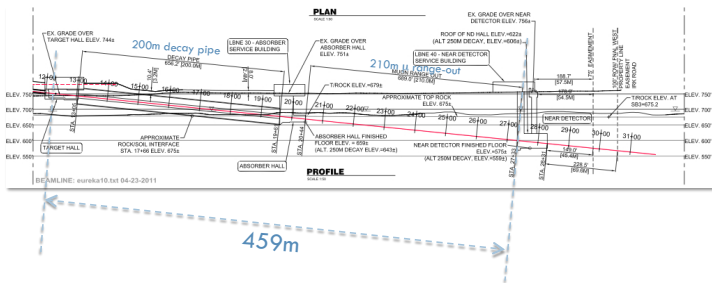
$Z_e$  distribution

$E_{\nu}^{\text{calc}}$ 

# Energy resolution - nominal angular resolution



## Effect of the beam divergence

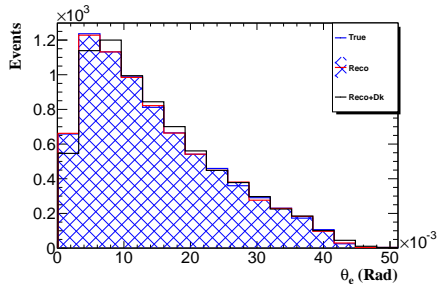
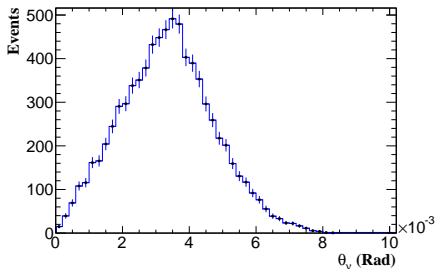


- 459 m<sup>[2]</sup> = distance from upstream end of proton target to upstream end of ND hall
- Target is 9 m downstream of upstream end of target hall
- Target hall + 200 m decay pipe + absorber + 210 m of rock for muon range out

<sup>2</sup>574 m in current engineering drawing

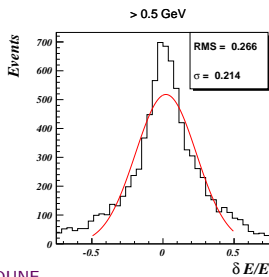
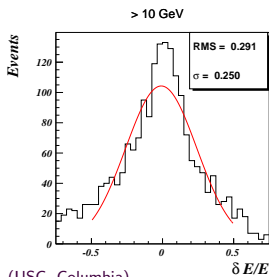
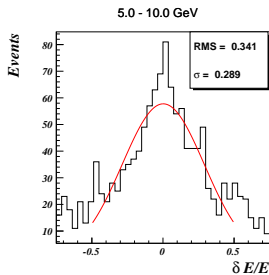
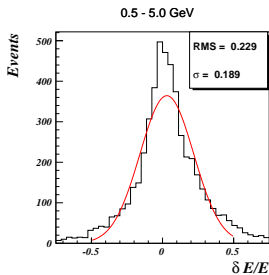


# Neutrino's intrinsic $p_T$ ( $\theta_\nu$ )

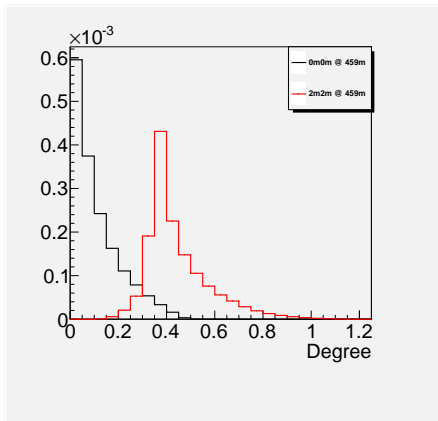


- The beam  $p_T$  can be measured precisely with coherent pion production

# Energy resolution - nominal angular resolution + neutrino intrinsic angle

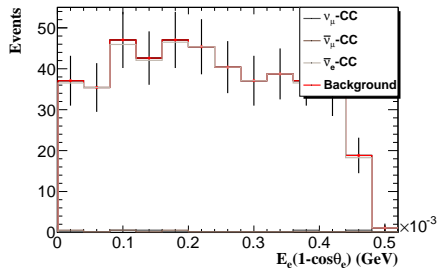
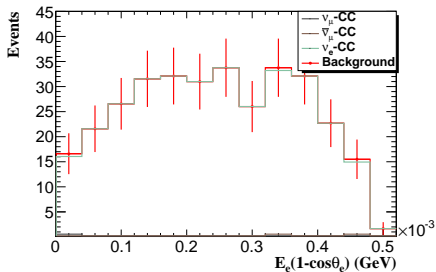


## Neutrino's intrinsic $p_T$ ( $\theta_\nu$ )



- We can reduce the effect of the beam divergence by considering the correlation between the electron angle and the vertex location (i.e. final uncertainty should be smaller).

# $e^-$ vs $e^+$ sample background



- $e^+/e^-$  separation in B field allows to calibrate in-situ symmetric backgrounds (from data).

## ND Requirements for $\nu e^- \rightarrow \nu e^-$ Scattering

- Low density medium to track  $e^\pm$  -  $\rho \sim 0.1 \text{ g/cm}^3$
- Transition Radiation :  $e^\pm$
- $dE/dx$  :  $\pi^\pm$ ,  $K^\pm$  and proton
- Magnet : + .vs. -
- Large statistics to reach  $\sim 3\%$  statistical precision
- Excellent momentum and angular resolution

# Inverse Muon Decay

ND Parametrized Simulation/Reconstruction (Fast MC)

$$\nu e^- \rightarrow \nu e^-$$

Inverse Muon Decay

Summary and Outlook

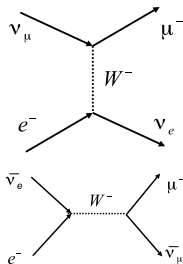
Inverse Muon Decay <sup>3</sup>

$$\frac{d\sigma(\nu_l e \rightarrow l \nu_e)}{dy} = \frac{G_\mu^2}{\pi} (2m_e E_\nu - (m_l^2 - m_e^2)) \quad (2)$$

$$\frac{d\sigma(\bar{\nu}_e e \rightarrow l \bar{\nu}_l)}{dy} = \frac{G_\mu^2}{\pi} (2m_e E_\nu (1-y)^2 - (m_l^2 - m_e^2)(1-y)) \quad (3)$$

$$y = \frac{E_l - \frac{m_l^2 + m_e^2}{2m_e}}{E_\nu} \quad (4)$$

$$0 \leq y \leq y_{\max} = 1 - \frac{m_l^2}{2m_e E_\nu + m_e^2} \quad (5)$$



- Cross section is extremely small

- $\sigma(\nu_\mu e^- \rightarrow \mu^- \nu_e) \simeq 3\sigma(\bar{\nu}_\mu e^- \rightarrow \mu^- \bar{\nu}_\mu) \simeq \frac{2G_\mu^2 m_e E_\nu}{\pi} \simeq 1.5 \times 10^{-41} (E_\nu/\text{GeV}) \text{ cm}^2$

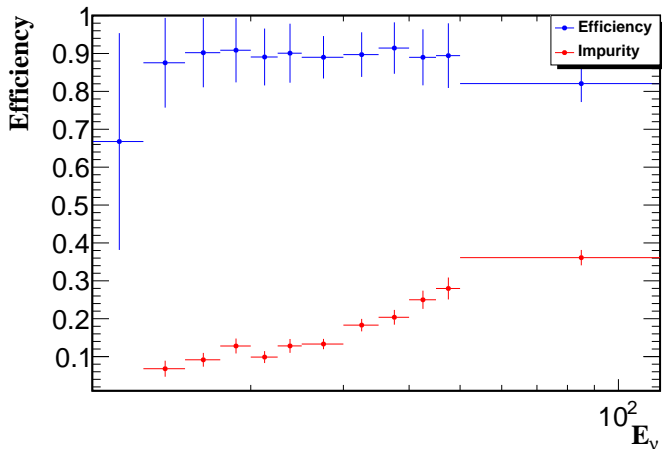
- Threshold  $E_\nu \geq \frac{m_l^2 - m_e^2}{2m_e} \simeq 10.9 \text{ GeV}$
- 5360  $\sigma(\nu_\mu e^- \rightarrow \mu^- \nu_e)$  events assuming 1.2 MW beam power, 5 tons ND fiducial mass, 5 years neutrino running
- A clean determination of the neutrino flux

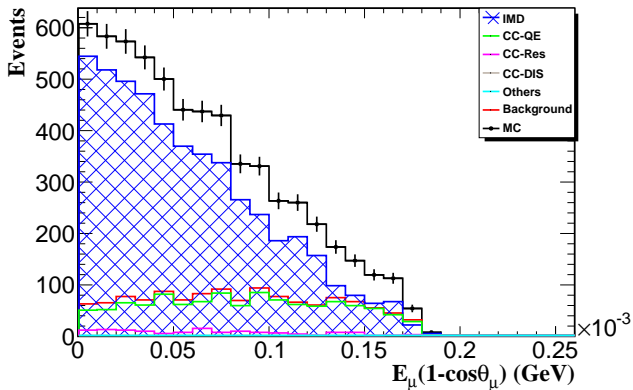
<sup>3</sup>W. Marciano and Z. Parsa, arXiv: hep-ph/0403168

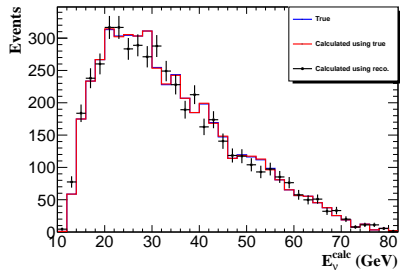
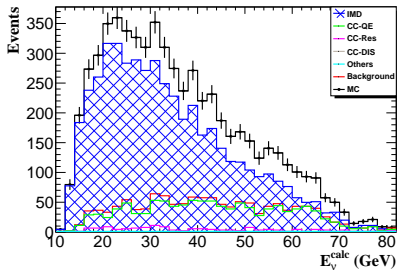
## Cut Table

Cut	Sig.	Sig. Eff.	Back.	Back. Surv. Prob.
Fiducial	5357	1	6.505e+07	1
$p_\mu > 0.2 \text{ GeV}/c$ & $n_e^{\text{hits}} \geq 12$	5357	1	6.281e+07	0.9655
$\mu$ -ID	5091	0.9502	5.648e+07	0.8683
$\pi^0/n/K_0$ veto	5091	0.9502	3.148e+07	0.484
no second track	5091	0.9502	2.02e+06	0.03106
$E_\mu > 10.9$	4960	0.9258	1709	2.627e-05
$p_\mu^T < 0.15 \text{ GeV}$	4960	0.9258	1699	2.612e-05
$\theta_\mu < 0.005 \text{ Rad}$	4960	0.9258	1699	2.612e-05
$\mathcal{Z}_\mu < 0.00025$	4960	0.9258	1699	2.612e-05
$\mathcal{N}\mathcal{N} > 0.20$	4881	0.9112	1253	1.926e-05

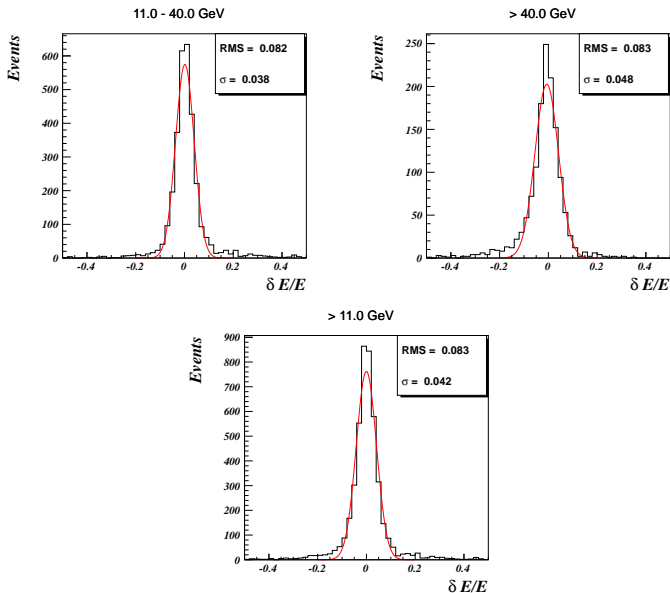


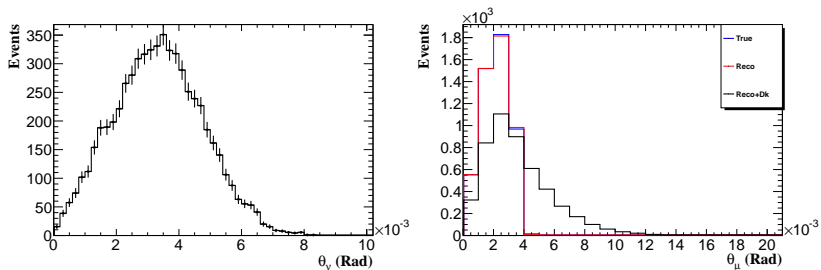
IMD efficiency as a function of  $E_\nu$  W/ NN cut

$Z_\mu$  distribution W/ NN cut

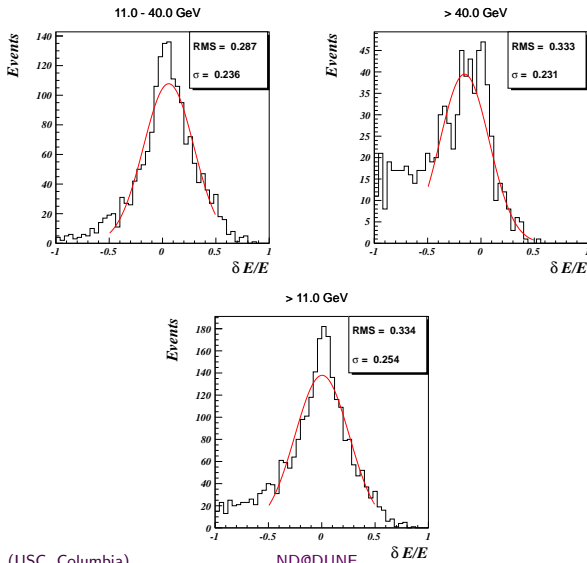
$E_{\nu}^{\text{true}}$  vs  $E_{\nu}^{\text{calc}}$  w/ NN cut


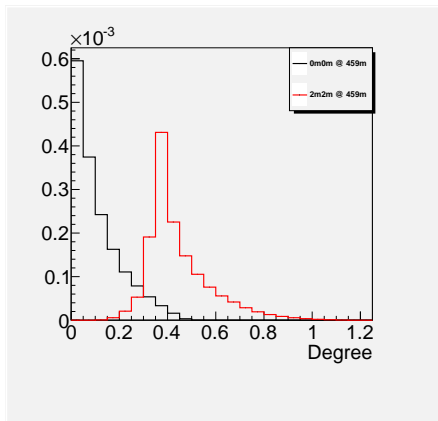
# Energy resolution - nominal angular resolution



Neutrino Intrinsic  $p_T$  ( $\theta_\nu$ )

# Energy resolution - nominal angular resolution + neutrino intrinsic angle

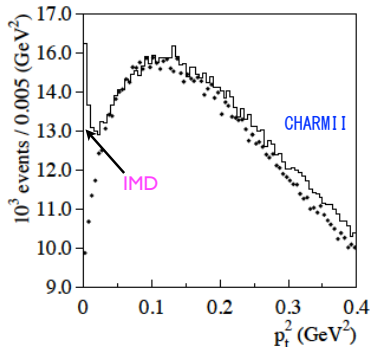
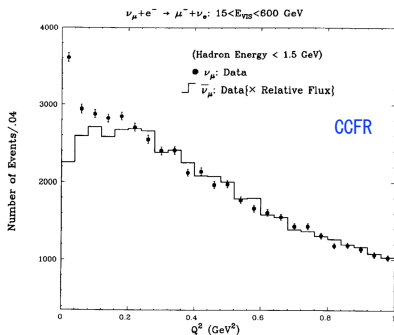


Neutrino's intrinsic  $p_T$  ( $\theta_\nu$ )

- We can reduce the effect of the beam divergence by considering the correlation between the electron angle and the vertex location (i.e. final uncertainty should be smaller).

# $\nu_\mu N\text{-CC}$ background to IMD

- $\nu_\mu N\text{-CC}$  background to IMD dominated by low- $y$  interactions, largely QE
  - The nuclear effects in CCQE, in particular the FSI which can dramatically increase the number of 1 track events
- A measure of this background is  $\bar{\nu}_\mu N\text{-CC}$  (No IMD in  $\bar{\nu}_\mu$ ), but with  $\sim 5\%$  precision
- CCFR (S. R. Mishra *et al.* Phys. Lett. B 252, 170 (1990)):  $\pm 5.2\%$  with  $|E_\nu| \cong 100$  GeV
- Charm II (P. Vilain *et al.* Phys. Lett B 364, 121 (1995)):  $\pm 5.6\%$  with  $|E_\nu| \cong 23$  GeV
- Measure 2-track  $\nu_\mu N\text{-CC}$  ( $\mu^- + X$ ) to constrain the background when  $E_x \sim 0 \Rightarrow (\mu^-, 0)$





# $\nu_\mu N\text{-CC}$ background to IMD - Constraints from $\mu^+$ and $\mu^- + X$

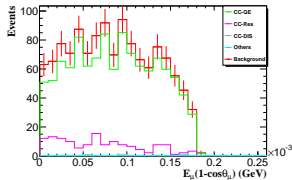
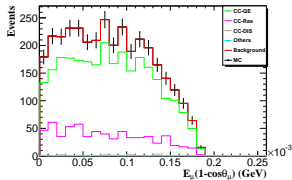
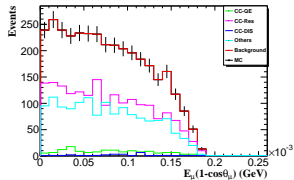
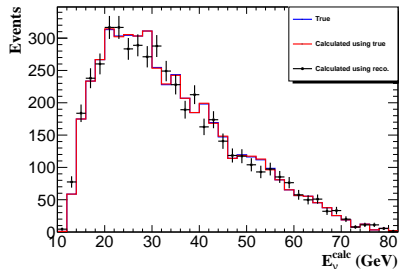
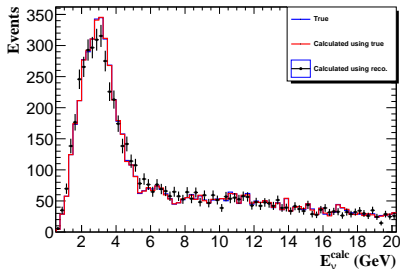


Figure: IMD background

Figure:  $\mu^+$  IMD-likeFigure:  $\mu^- + X$  IMD-like

## Neutrino Electron NC scattering + IMD



# ND Requirements for IMD

- $dE/dx$  :  $\pi^\pm$ ,  $K^\pm$  and proton
- Magnet : + .vs. -
- MuID :  $\mu$
- Large statistics
- Excellent momentum and angular resolution

# Near Detector Options

## Fine Grained Tracker

- Pros

- Angular resolution  $\sim 2$  mrad,  $e^\pm$  ID: transition radiation + dE/dx + ECAL,  $\mu$  ID, Charge measurement: B field,  $e^+$  vs.  $e^-$  separation:  $\rho \sim 0.1$  g/cm<sup>3</sup>

- Cons

- Statistics

## Liquid Argon TPC

- Pros

- Large statistics,  $e^\pm$  ID: dE/dx + e.m. shower (calorimetry),  $e/\gamma$  separation

- Cons

- Containment .vs. pile-up, angular resolution, B field?

## Gaseous Argon TPC

- Pros

- Angular resolution  $\sim$  mrad,  $e^\pm$  ID: dE/dx + ECAL,  $\mu$  ID, Charge measurement: B field,  $e^+$  vs.  $e^-$  separation:  $\rho \sim 0.04$  g/cm<sup>3</sup>

- Cons

- VERY low statistics (fiducial mass  $\sim 0.5$  t), pile-up vs. outside backgrounds

# Summary and Outlook

ND Parametrized Simulation/Reconstruction (Fast MC)

$$\nu e^- \rightarrow \nu e^-$$

Inverse Muon Decay

Summary and Outlook

# Summary and Outlook

- Absolute neutrino flux determination
  - Neutrino electron NC scattering:
    - Signal efficiency is  $\sim 73\%$  with 4% background
    - Can measure the flux to 2% level
  - IMD:
    - Signal efficiency is  $\sim 91\%$  with 20% background
    - Can measure the absolute flux to 3% precision for  $E_\nu > 11$  GeV
- Ongoing analysis
  - Coherent  $\pi^\pm$
  - Beam dispersion

