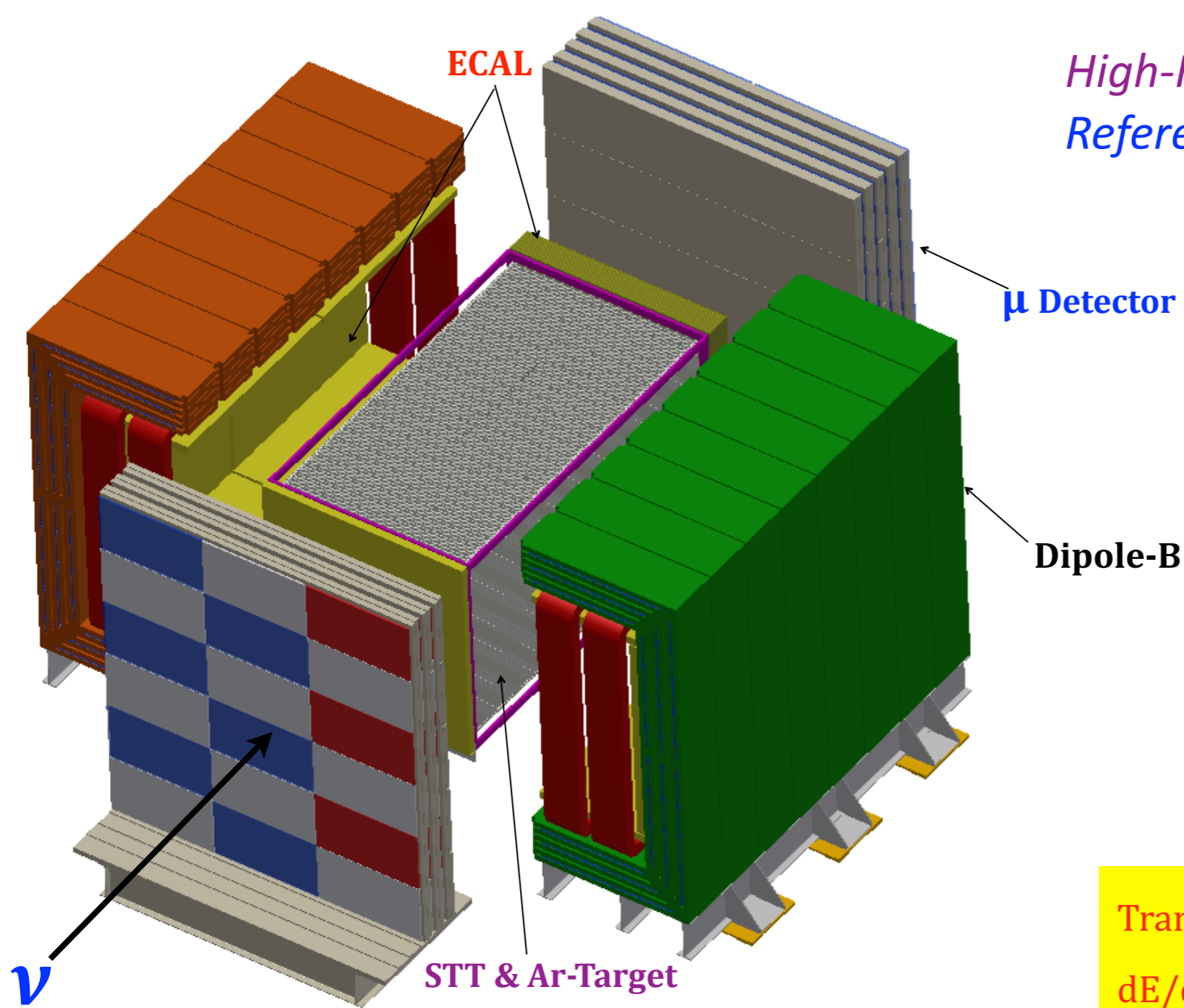


# Muons in FGT

*Xinchun Tian, Sanjib R. Mishra, Roberto Petti*

High-Resolution Fine Grain Tracker:  
Reference ND of DUNE



Transition Radiation  $\Rightarrow e^{+/-} \text{ ID} \Rightarrow \gamma$   
 $dE/dx \Rightarrow \text{Proton, } \pi^{+/-}, K^{+/-}$   
 Magnet/Muon Detector  $\Rightarrow \mu^{+/-} e^{+/-}$   
 ( $\Rightarrow$  *Absolute Flux measurement*)  
 $1X0 \sim 600 \text{ cm} / 1 \lambda \sim 1200 \text{ cm}$

- ☞  $\sim 3.5\text{m} \times 3.5\text{m} \times 6.5\text{m}$  STT ( $\rho \approx 0.1\text{gm/cm}^3$ )
- ☞  $4\pi$ -ECAL in a Dipole-B-Field (0.4T)
- ☞  $4\pi$ - $\mu$ -Detector (RPC) in Dipole and Downstream
- ☞ Pressurized Ar-target ( $\approx \times 5$  FD-Stat)  $\Rightarrow$  LAr-FD

## Muon Measurement in FGT

\*  $\nu_{\mu} \leftrightarrow \mu^{-}$ ;  $\text{anti-}\nu_{\mu} \leftrightarrow \mu^{+}$ ;

### \* $\mu$ -Momentum Measurement:

Track-reconstruction in STT:

Curvature  $\Rightarrow |\mathbf{p}|$  & “-” or “+”

Direction-cosines  $\Rightarrow$  STT Track-fit extrapolated to the vertex including  $dE/dx$

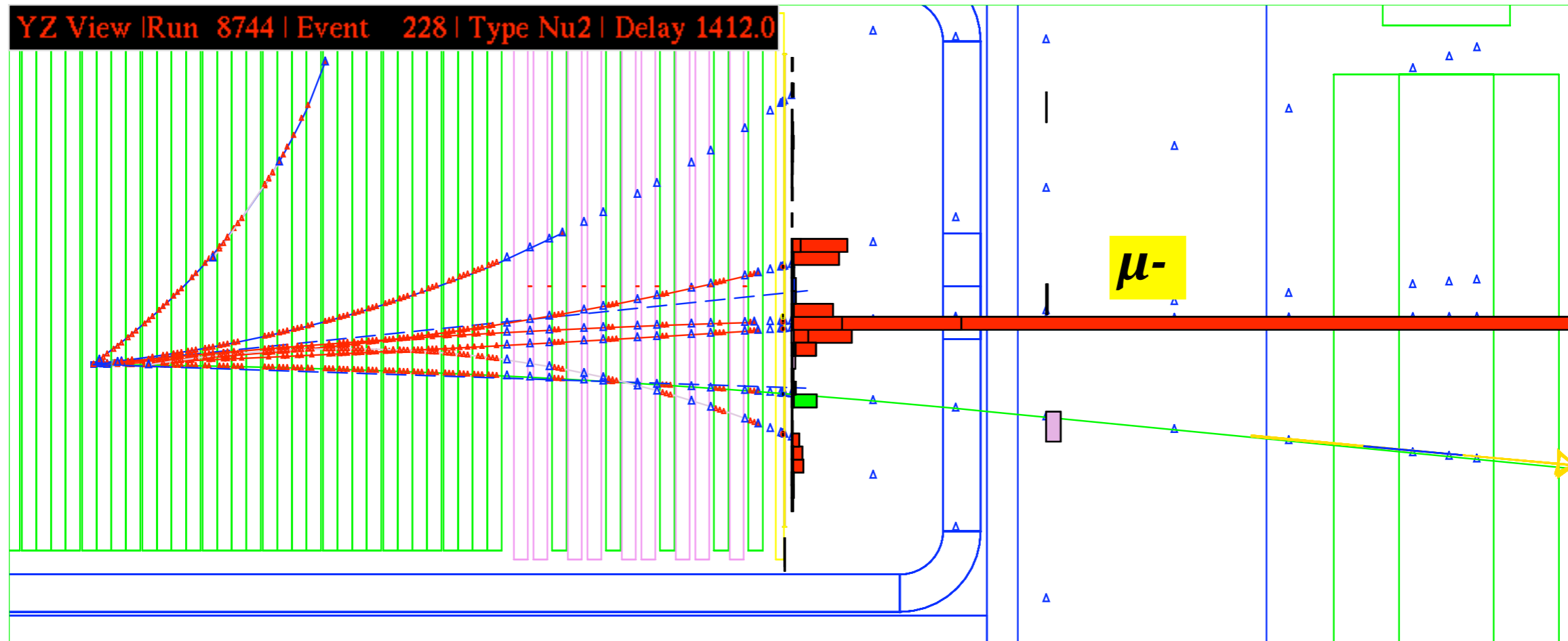
### \* $\mu$ -ID Measurement:

Track-reconstruction in the  $\mu$ -Detector (RPC)

$\mu$ -ID Detector (RPC) will have a  $4\pi$ -coverage  $\Rightarrow \mu^{+}$  .vs.  $\mu^{-}$  separation & Large-angle  $\mu$

Match the RPC-Track with the STT-Track

## A $\nu_\mu$ CC candidate in NOMAD



**Observation**  $\Rightarrow$

- (1) **Hadrons** are tracks, enabling the momentum vector measurement
- (2)  $\mu$  is kinematically separated from **Hadron-vector**  $\Rightarrow$  **Miss-PT Measurement**
- (3) **FGT** offers  $\sim x5$  higher tracking-points for hadronic tracks

# $\mu$ -CC Events in NOMAD

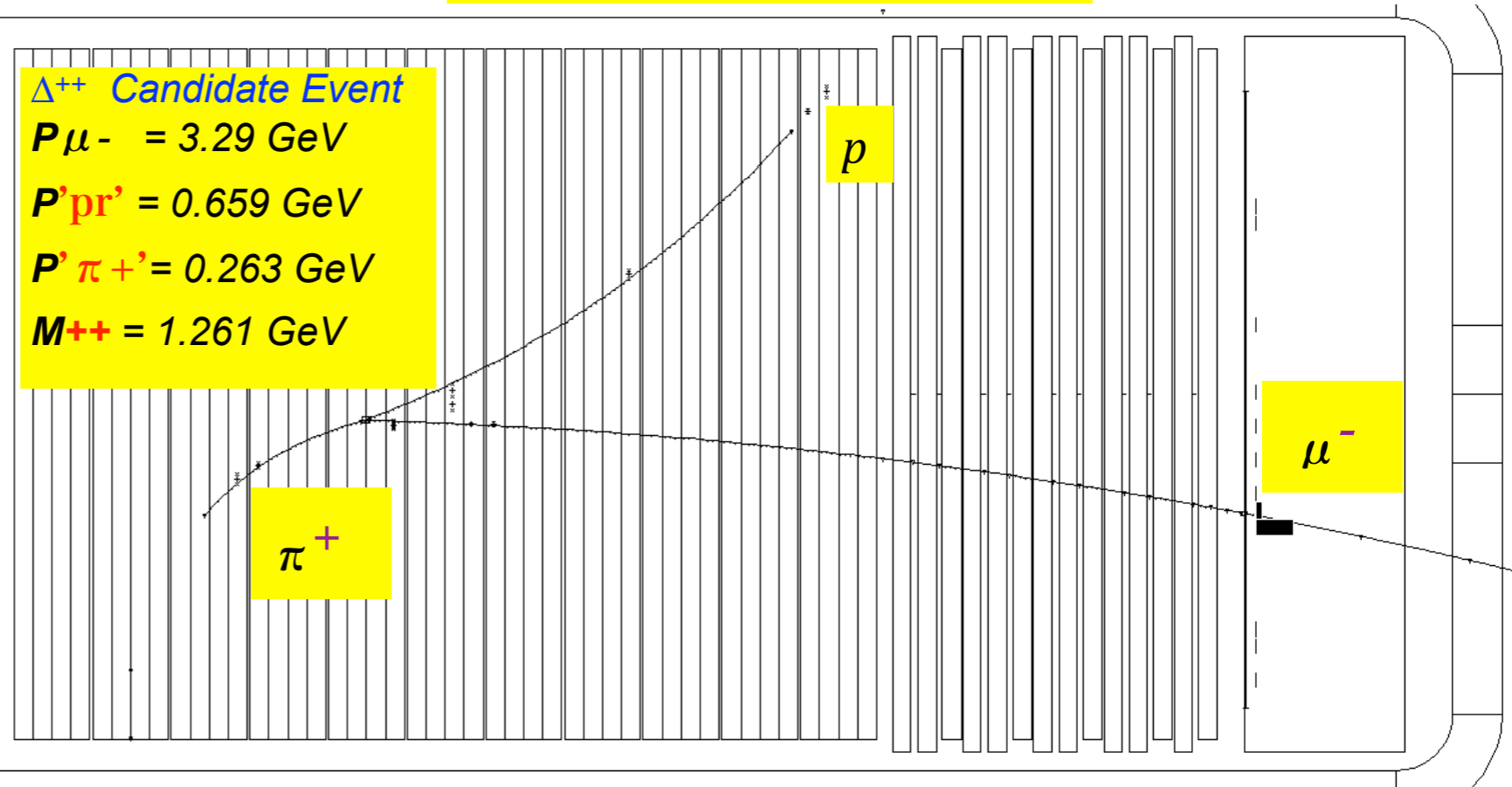
$\Delta^{++}$  Candidate Event

$$P_{\mu^-} = 3.29 \text{ GeV}$$

$$P'_{p\pi'} = 0.659 \text{ GeV}$$

$$P'_{\pi^+} = 0.263 \text{ GeV}$$

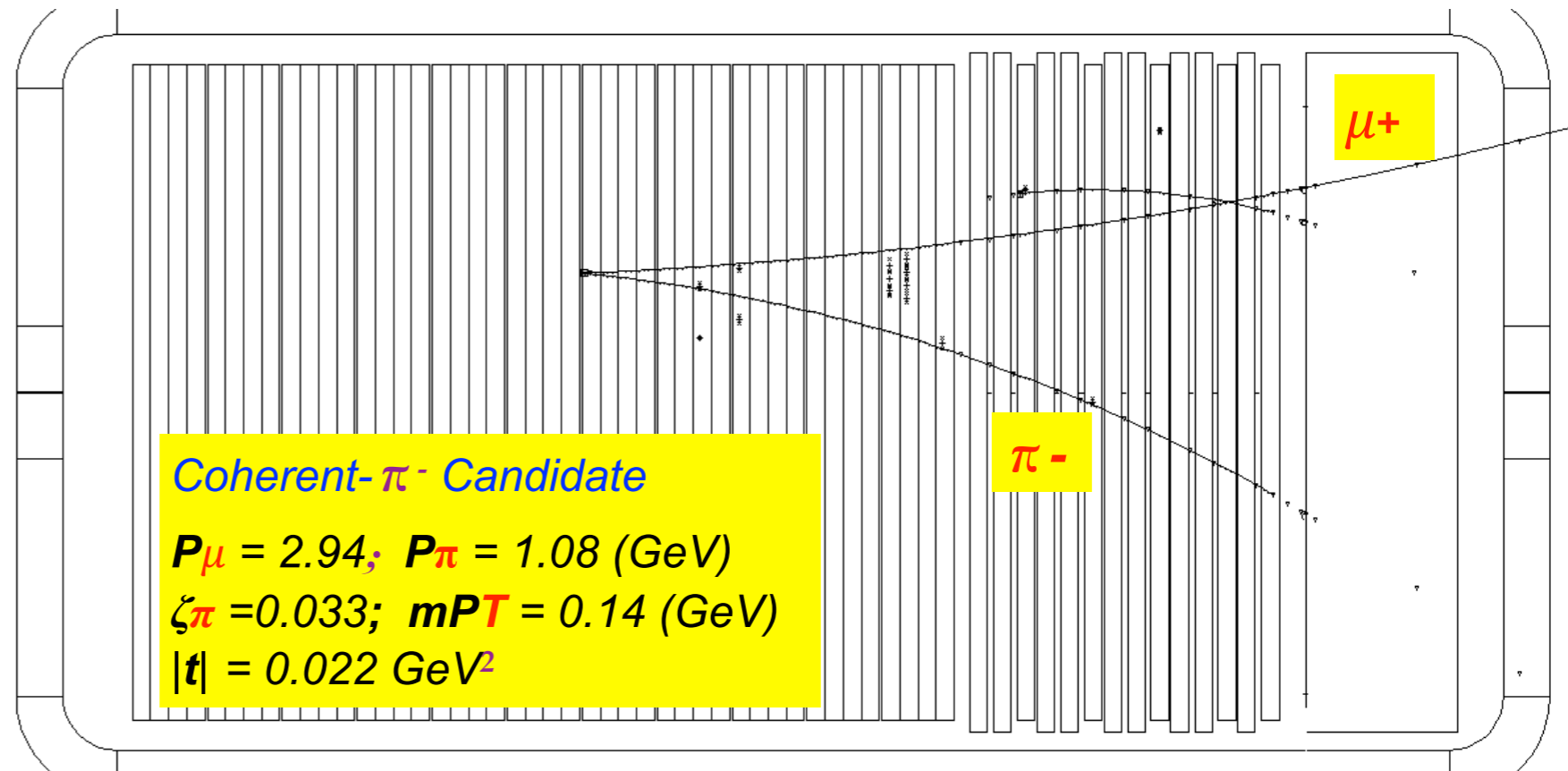
$$M^{++} = 1.261 \text{ GeV}$$



In FGT

$\times 3$  higher track-points in  $\mu$

$\sim \times 10$  higher track-points in  $p/\pi$



Coherent- $\pi^-$  Candidate

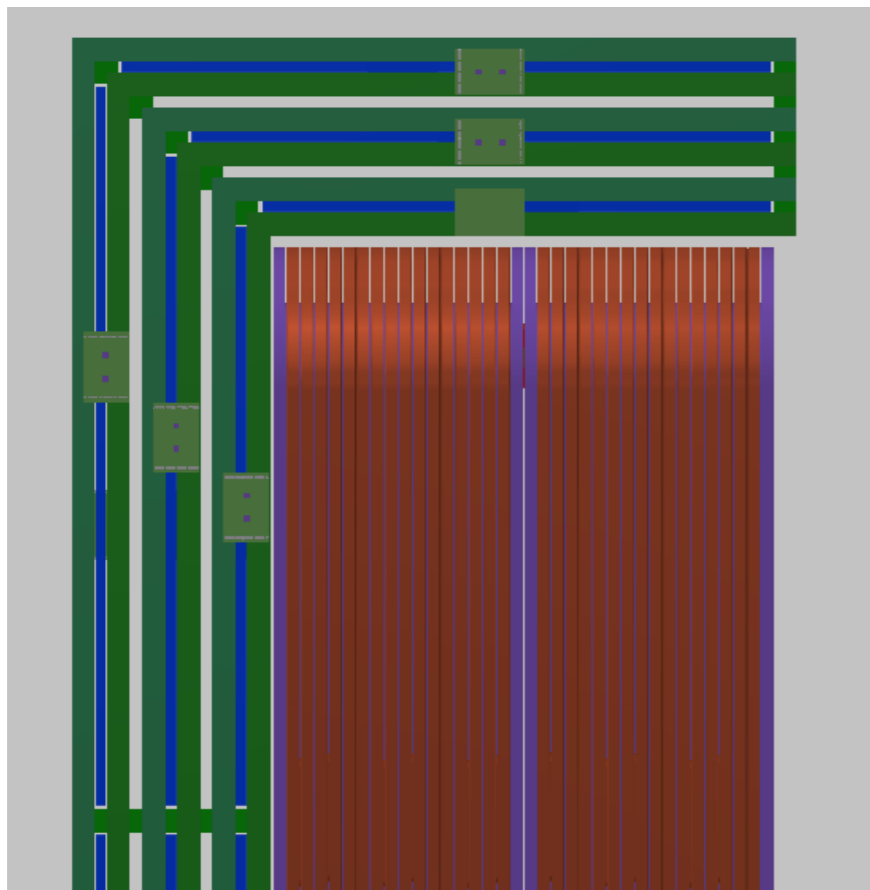
$$P_{\mu} = 2.94; P_{\pi} = 1.08 \text{ (GeV)}$$

$$\zeta_{\pi} = 0.033; m_{PT} = 0.14 \text{ (GeV)}$$

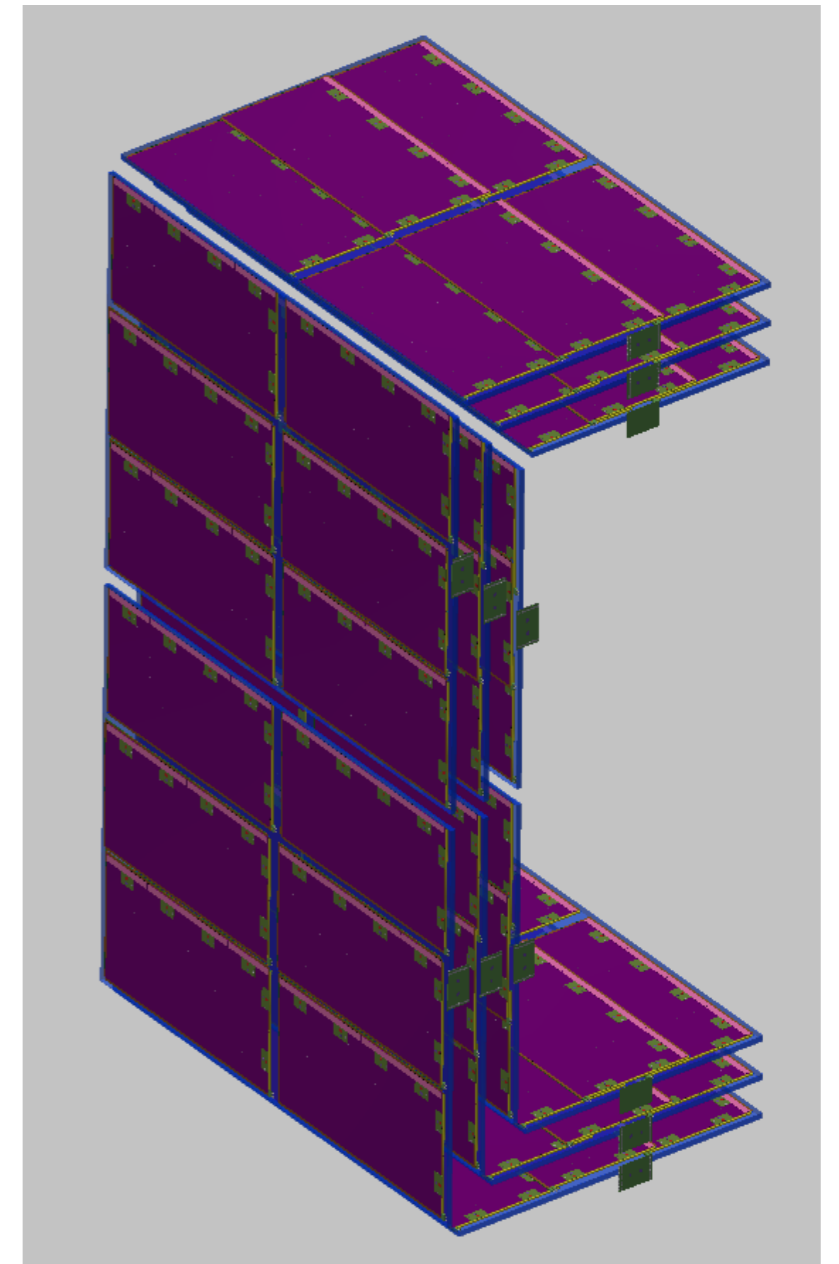
$$|t| = 0.022 \text{ GeV}^2$$

## THE MUON DETECTOR

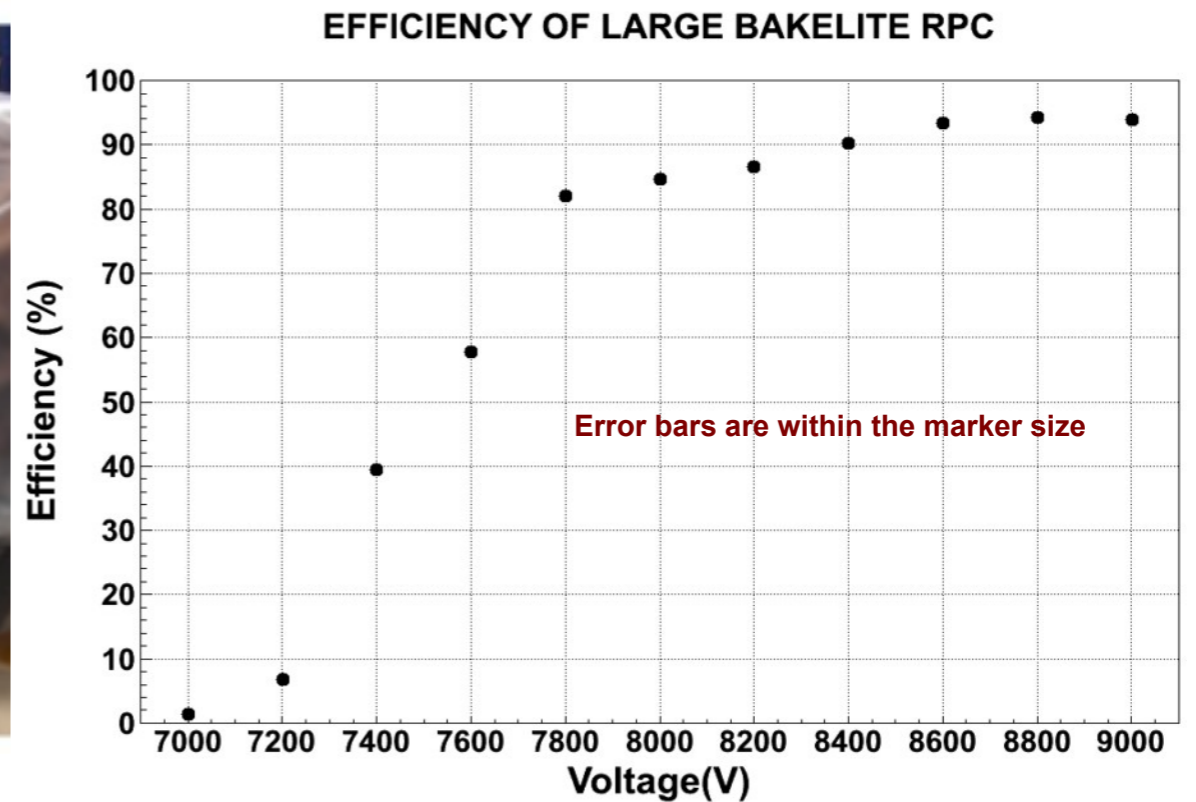
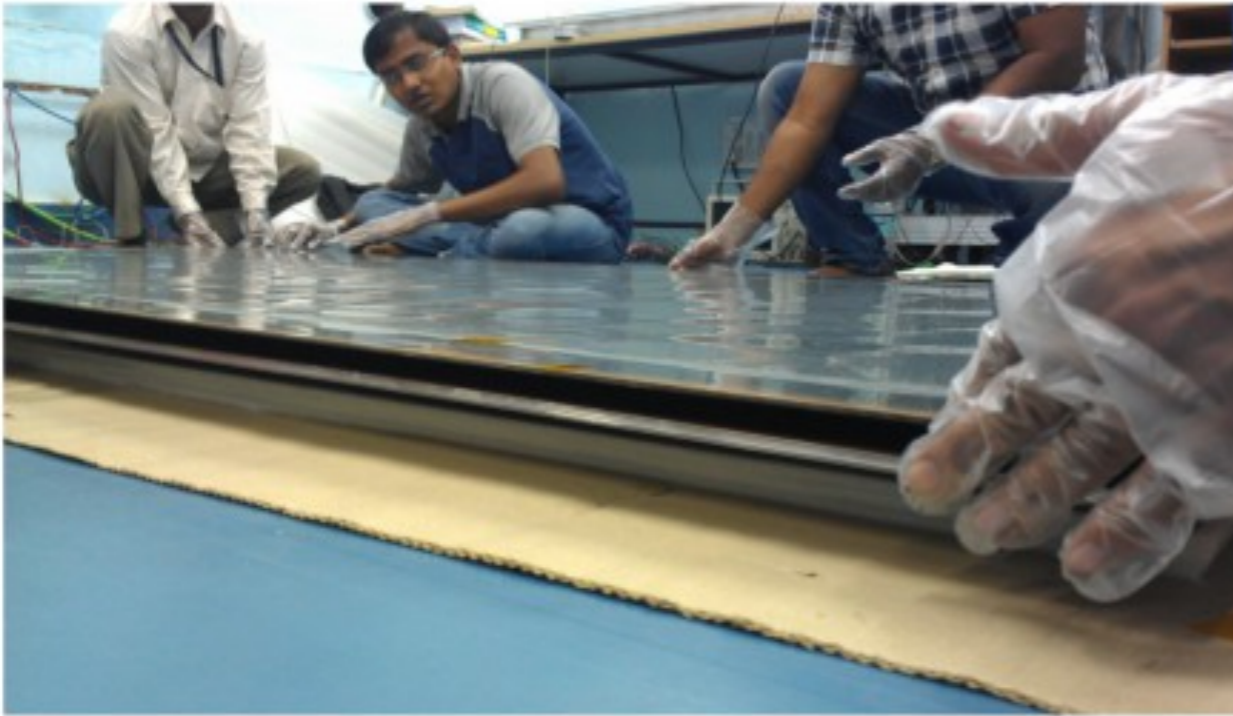
- ◆ **Glo-Sci-51** measure absolute and relative  $\nu_\mu$  and  $\bar{\nu}_\mu$  spectra separately.
  - ◆ **Glo-Sci-52** measure NC and CC cross-sections separately vs. hadronic energy
- ⇒ identify muons exiting the tracking volume **NDC-L2-34,35**
- ⇒  $4\pi$  muon detector with  $< 1$  mm space resolution
- ◆ Instrument magnet yoke (3 planes), and downstream (5 planes) and upstream (3 planes) stations
  - ◆ Bakelite RPC chambers  $2\text{m} \times 1\text{m}$  (432 in total) with 7.65 (7.5) mm X (Y) strips in avalanche or streamer mode



\* 166k Channels



## Full-scale RPC Prototype @ VECC (Subhsish, Zybayer )

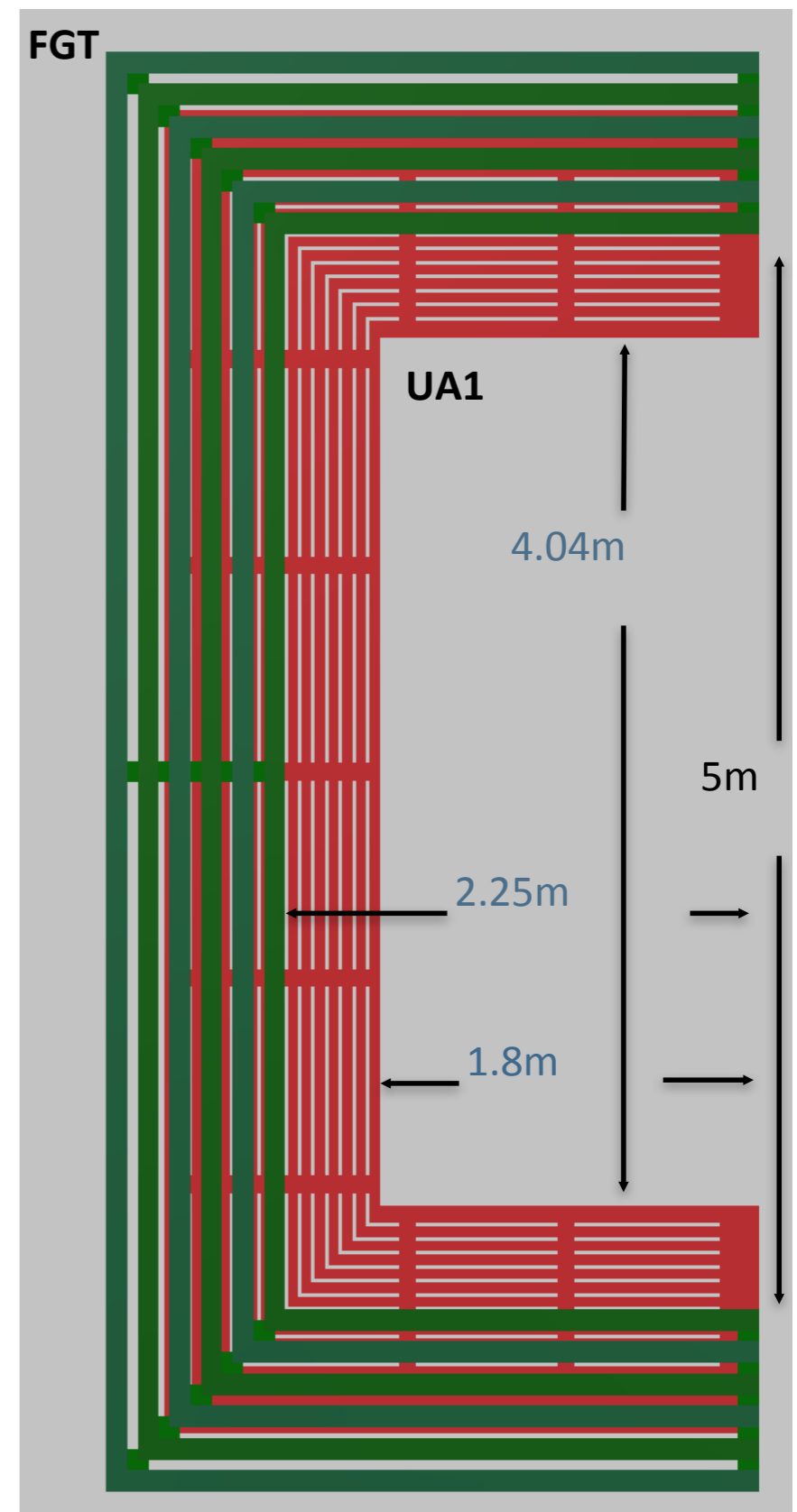
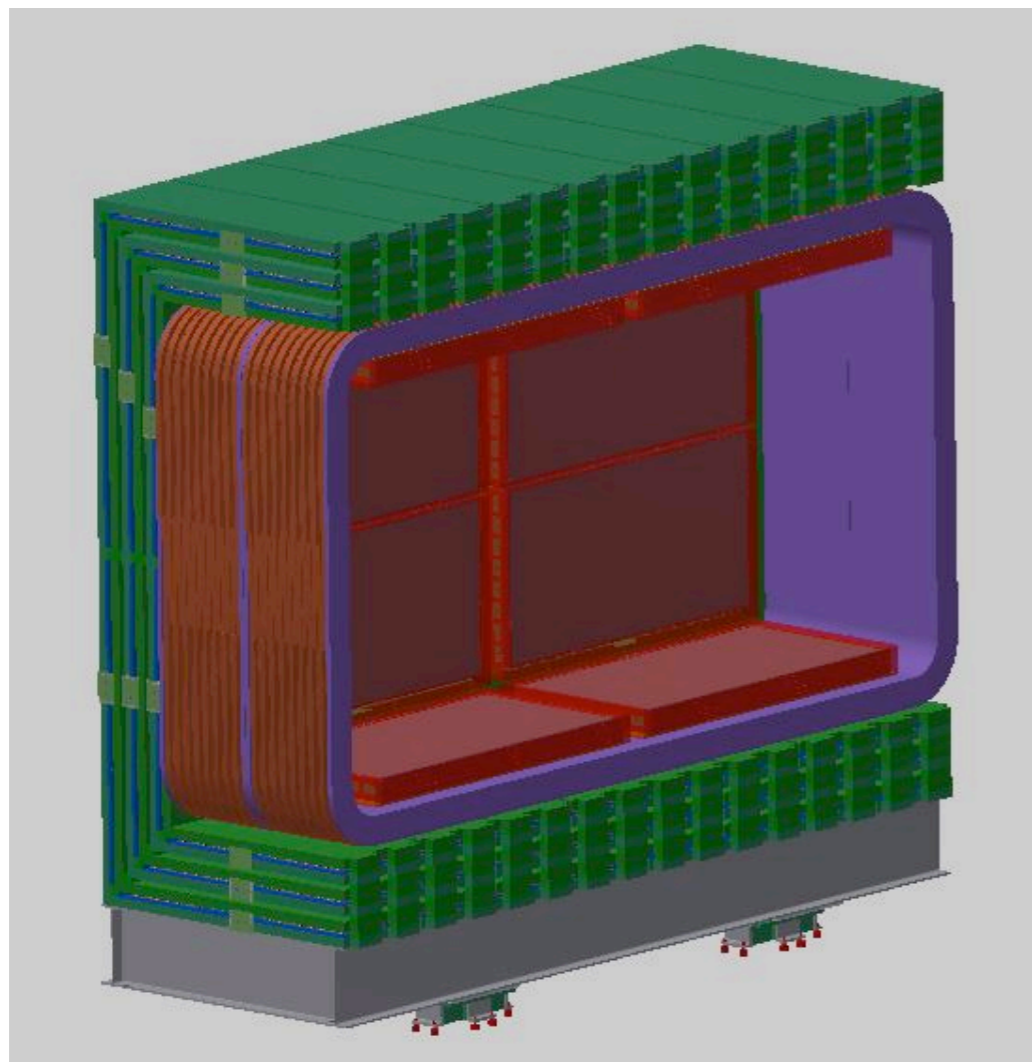


- ◆ Built  $2.4m \times 1.2m \times 2cm$  prototype (full scale) at VECC in India
- ◆ Operated in streamer mode,  $\epsilon \sim 95\%$ , noise  $< 1 Hz/cm^2$

## THE DIPOLE MAGNET

*Design by BARC: Sanjay Malhotra & team*

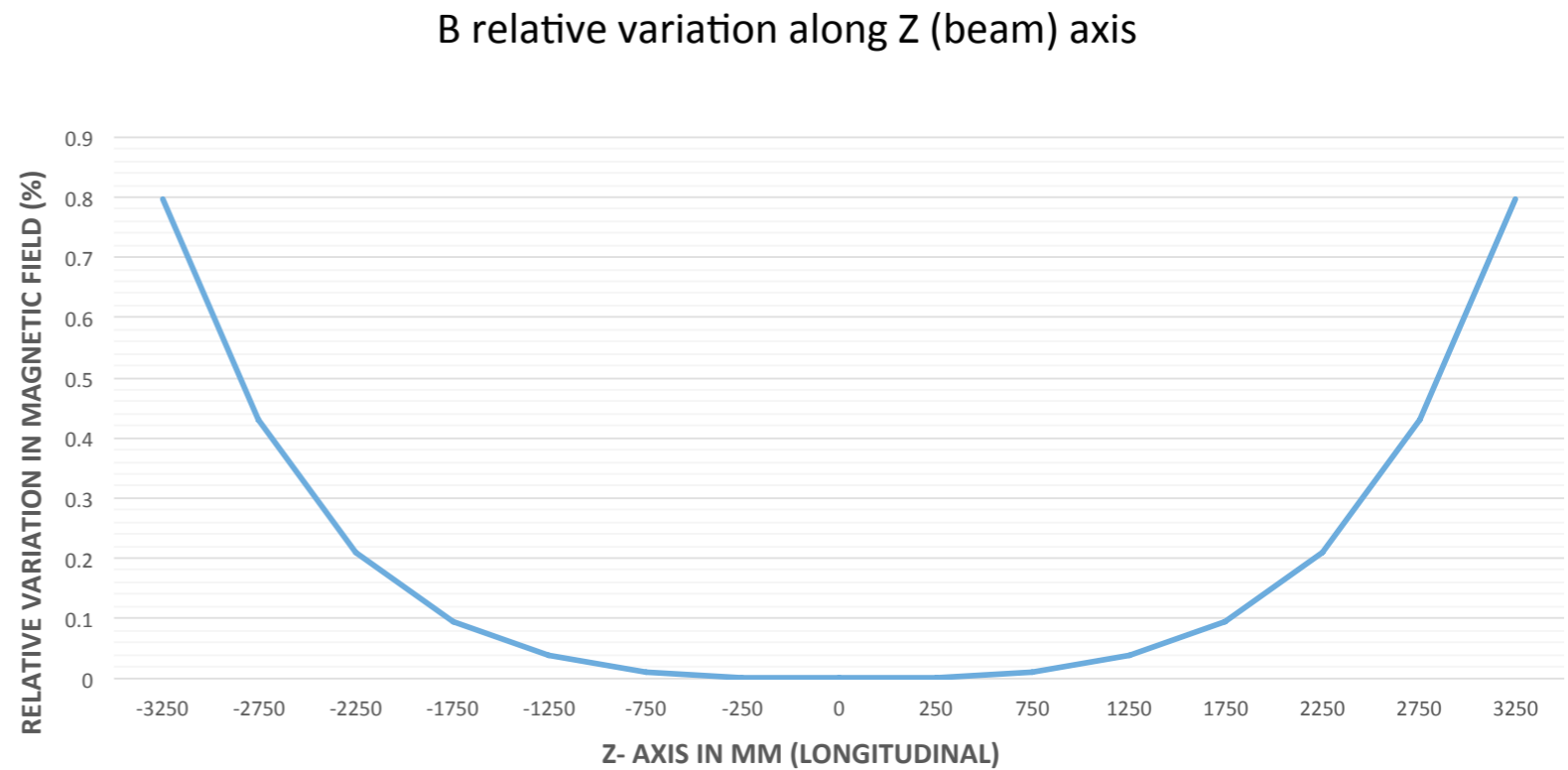
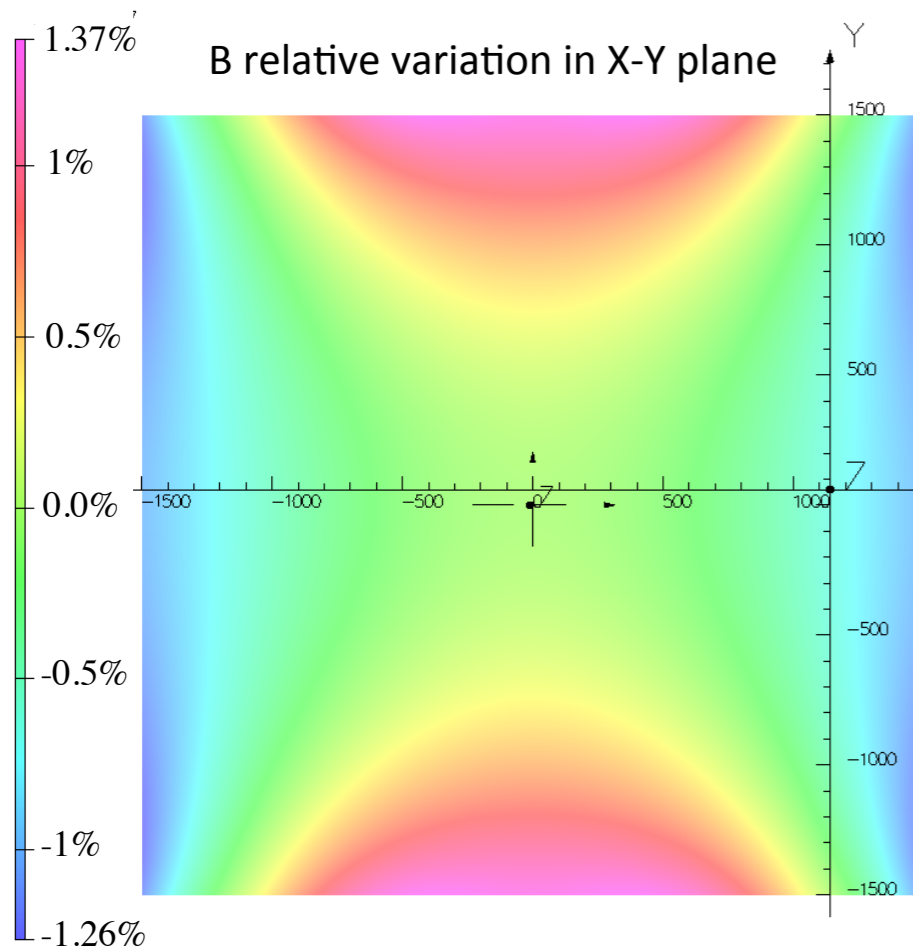
- ◆ *Design based on established UA1/NOMAD/T2K magnet*
- ◆ *Magnetic volume  $4.5\text{m} \times 4.5\text{m} \times 8.1\text{m}$ , nominal  $B=0.4\text{ T}$*
- ◆ *Return yoke with 8+8 "C" sections:  
 $6 \times 100\text{ mm}$  steel plates, 50 mm gaps (960 tons)*
- ◆ *4 vertical Cu coils (150 tons) made of 8 double pancake*
- ◆ *Power requirement for nominal field 2.43 MW,  
water flow for coil cooling 20 l/s*





## *Muon Momentum Reconstruction using Curvature in the B-Field*

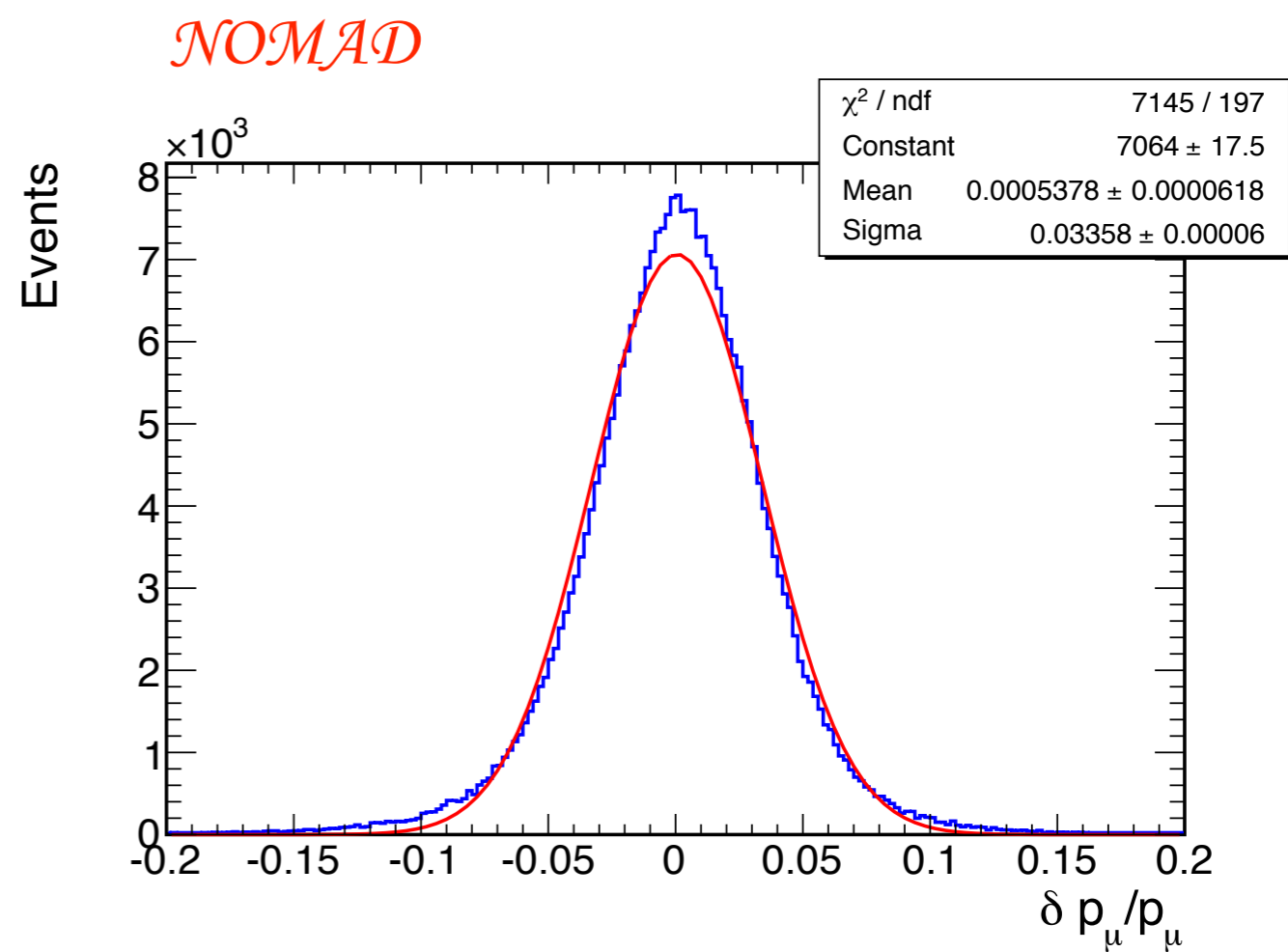
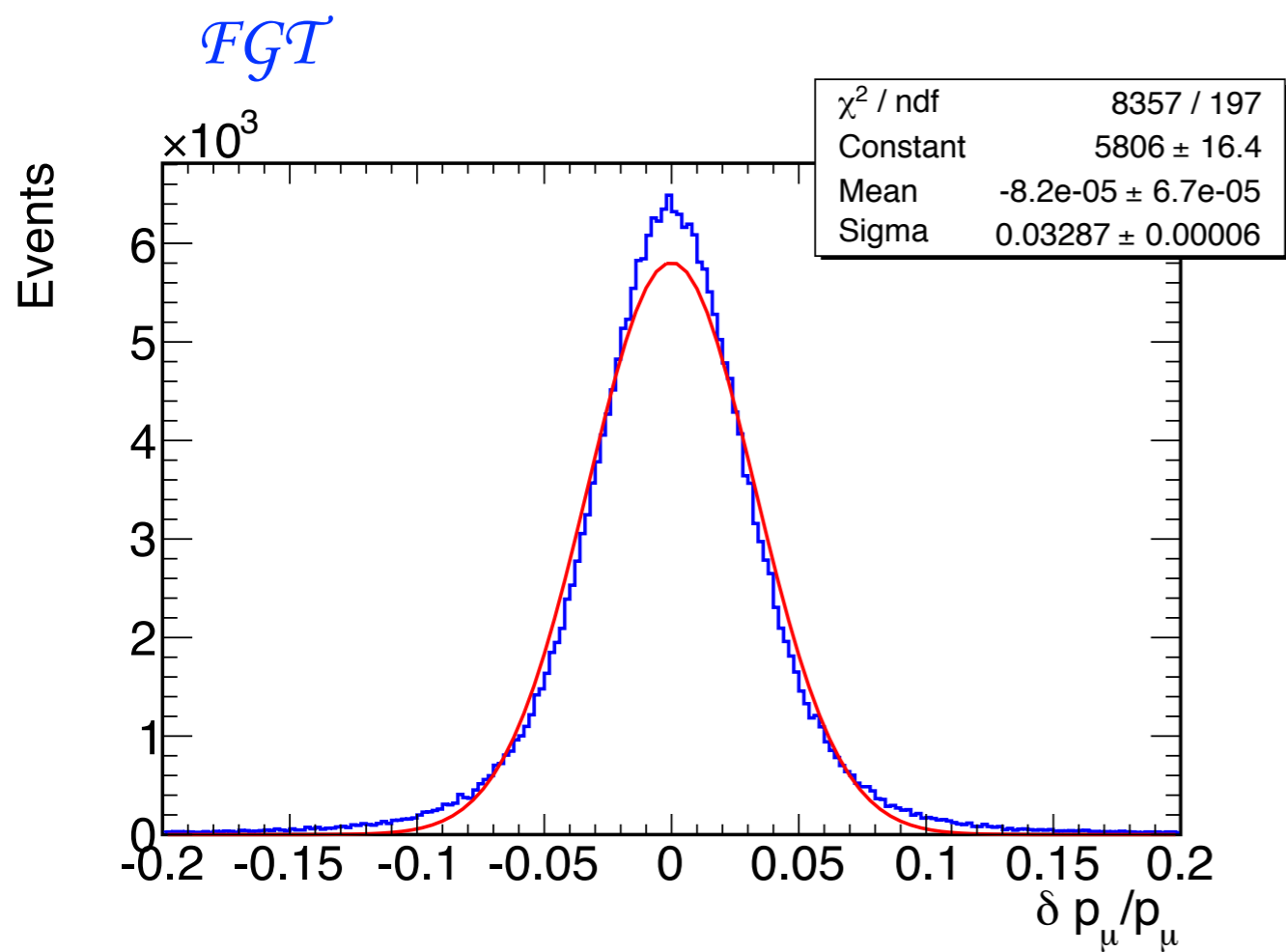
- \* Need a uniform B-Field with  
*Good design uniformity (  $\sim 1\%$  variation over the volume of  $3.5\text{m} \times 3.5\text{m} \times 6.5\text{m}$ )*
- \* Detailed B-Field **map-variations** measured **with  $\leq 10\%$  precision**  
 $\Rightarrow$  B-Field known to  $\sim 0.1\%$  precision
- \* Continual monitoring of the B-Field during operation  
 $\Rightarrow$  Built in instrumentation in the field volume, especially the edges & yokes



BARC, India

- ◆ *B uniformity in  $3.5m \times 3.5m \times 7m$  tracking volume better than 2% (field simulations)*
- ◆ *Maximal deformation of C yoke 1.16 mm, maximal buckling of bobbin 1 mm*
- ◆ **Glo-Sci-51,23** *measure absolute and relative  $\nu_\mu, \nu_e$  and  $\bar{\nu}_\mu, \bar{\nu}_e$  spectra separately.*
  - $\implies$  *Low- $\nu$  technique for relative fluxes requires muon energy scale to  $< 0.2\%$*
  - $\implies$  *B field mapping to better than 1% matches the requirement*

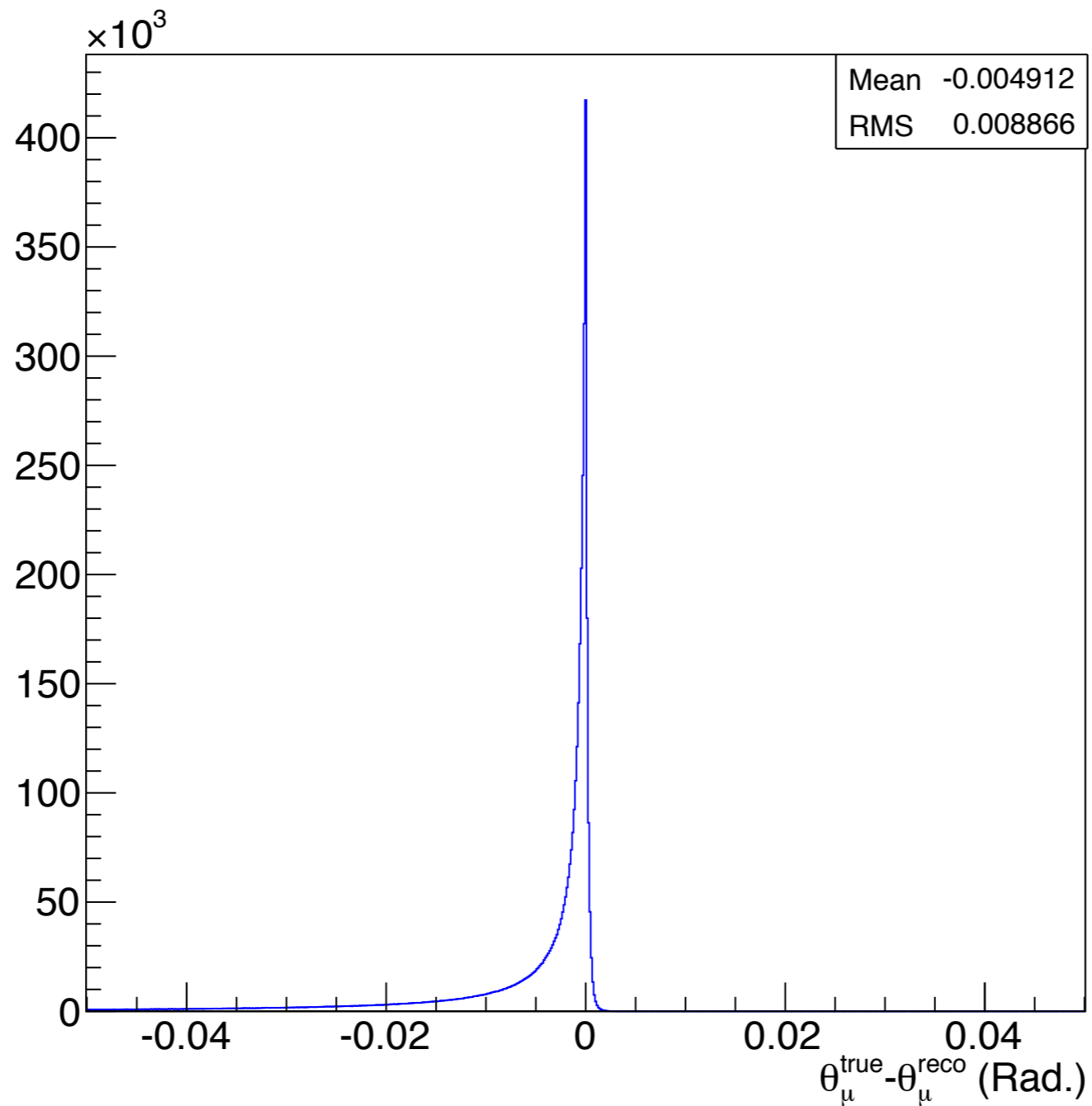
# Muon Momentum Resolution in FGT



## *Muon Angular ( $\theta$ ) Resolution in FGT*

\* Resolution depend on “p”

$\langle \Delta\theta \rangle \sim 1 \text{ mad}$  for the LBNF-spectrum [Fig. will be updated]



## *Measurement of Muons, $\mu^+$ & $\mu^-$ , at Large Angles*

\* Need to measure muons emitted at large angles

\* At the 1<sup>st</sup> oscillation maximum (2—3 GeV):

| $\theta$ -Cut | % $\nu_{\mu}$ -CC |
|---------------|-------------------|
| $>60^\circ$   | $\sim 11\%$       |

\* At the 2<sup>nd</sup> oscillation maximum (0.5—1 GeV):

| $\theta$ -Cut | % $\nu_{\mu}$ -CC |
|---------------|-------------------|
| $>60^\circ$   | $\sim 37\%$       |

$\Rightarrow$  *Imperative to measure muons at large angles*

\* With  $4\pi$   $\mu$ -ID coverage, FGT will measure large-angle muons without any discernible loss of efficiency compared to, say,  $\theta < 60^\circ$

## *Muon Efficiency in FGT (Prelim.)*

Efficiencies from Fast-MC; cross-checked against NOMAD  
Purity, in  $P < 1$  GeV, estimated from Fast-MC (prelim.)

- \*  $P > 1$  GeV: Efficiency  $\sim \sim 95\%$ ; Purity  $\sim 99\%$
- \*  $P \in [0.6, 1]$  GeV: Efficiency  $\sim \sim 80\%$ ; Purity  $\sim 80\%$
- \*  $P \in [0.3, 0.6]$  GeV: Efficiency  $\sim \sim 60\%$ ; Purity  $\sim 70\%$

*in situ Constraint on the  $E_{\mu}$ -scale*

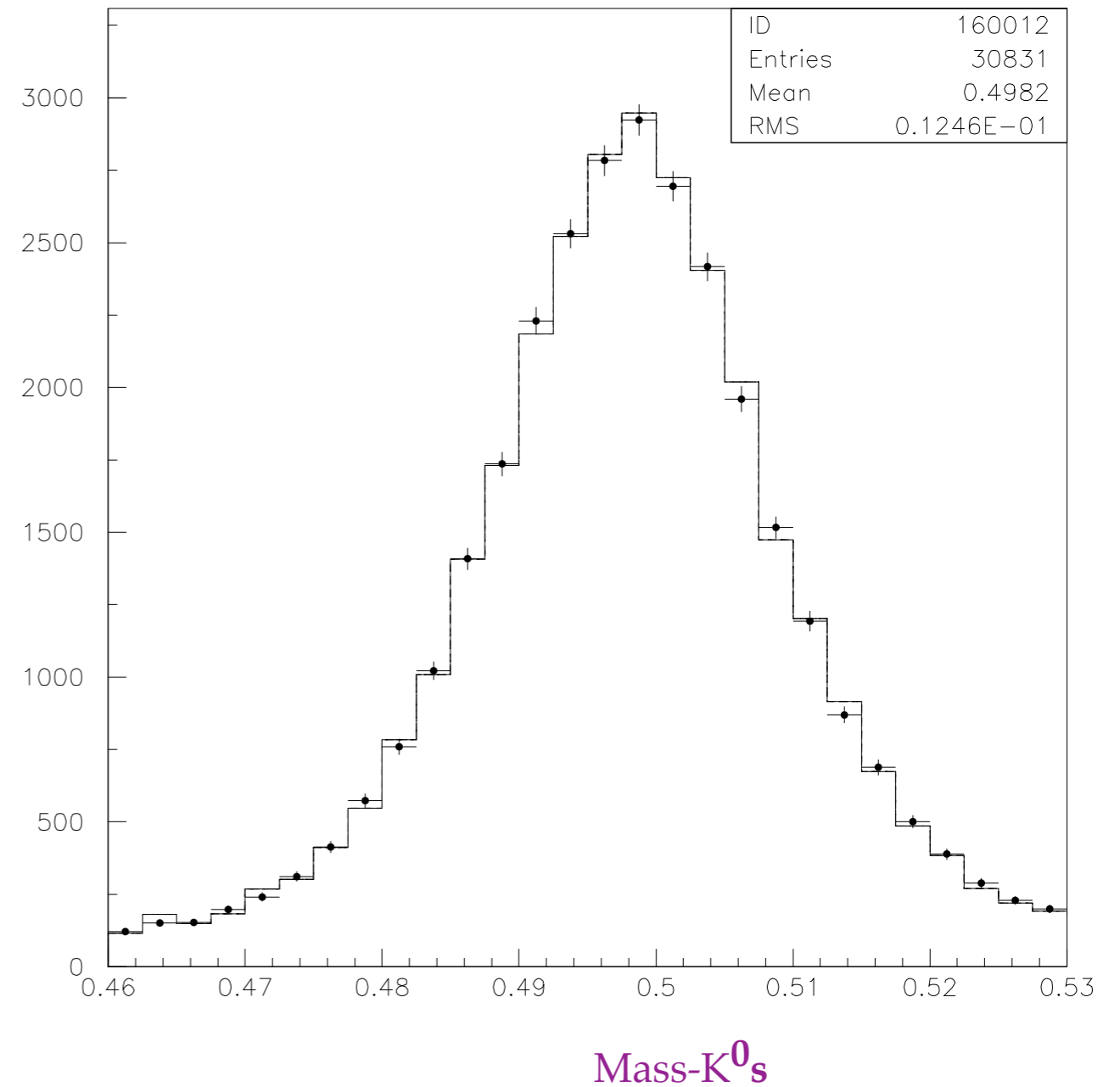
\* Measure  $K^0_s$  produced in the  $\nu$ -interactions

Expect  $> 750,000$  reconstructed  $K^0_s$

\* Constrain the error on the  $|p|$ -from-curvature

Expect an error  $< 0.1\%$  on the momentum energy scale

- \* Measurement of the Mass- $K^0_s \Rightarrow$   
in situ constraint on the *Energy-scale*
- \* NOMAD, 32k  $K^0_s \Rightarrow$   
error on the  $|p|$ -scale  $< 0.2\%$





## *in situ Constraint on the $E_\mu$ -efficiency*

### \* Measure the beam Muons

(1) Using the Up-stream Mu-ID module & Up-Stream ECAL module with Barrel, or Down-stream ECAL -&- RPC-in-Yoke or RPC-in-Down-stream  
⇒ Define the muon entering the detector (Denominator)

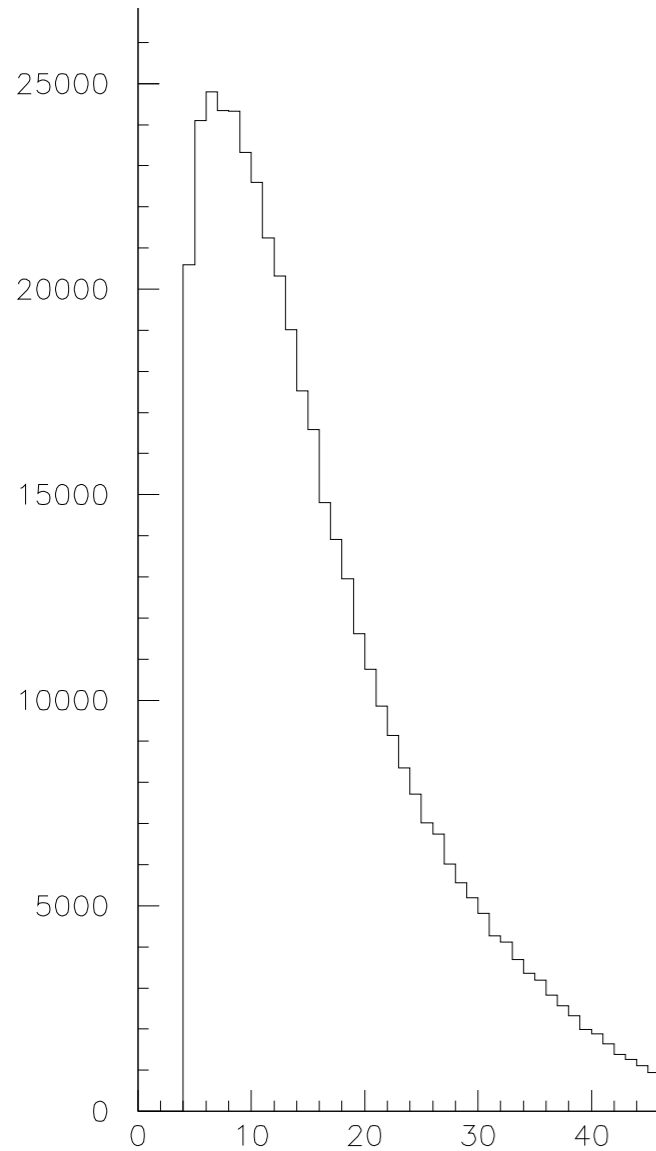
(2) Reconstruct these muons using STT and mu-ID (Numerator)

(3) Compute the Efficiency = Numerator/Denominator as a function of  $E_\mu$

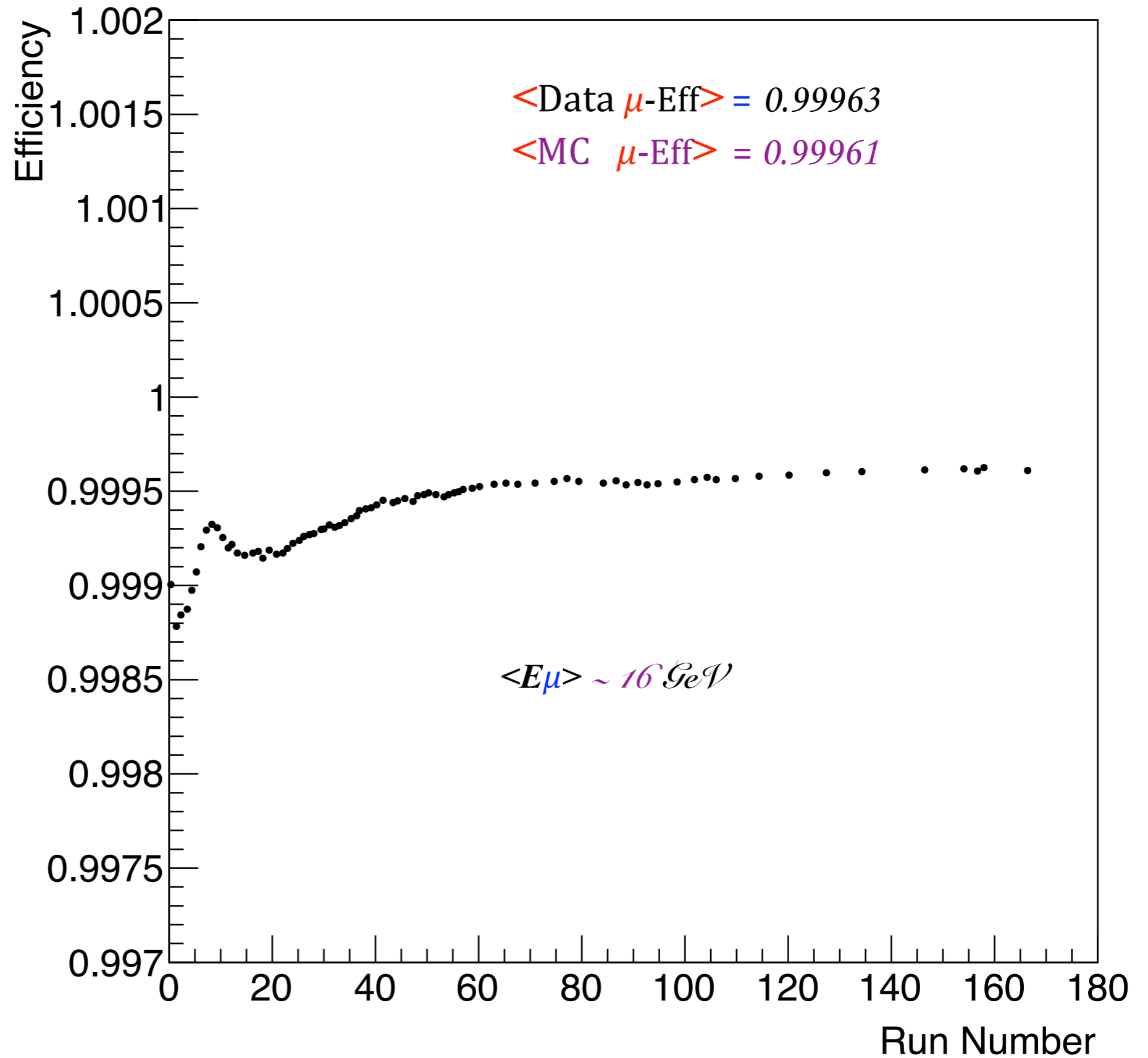
(4) Repeat this with the corresponding MC-Simulation

(5) Compare (3) with (4) : Check on the absolute  $E_\mu$ -efficiency

# Checking the $E_\mu$ -efficiency in NOMAD using the "Flattop" Muons



$4 \leq E_\mu \leq 40 \text{ GeV}$



... in order of increasing  $E_\mu$   $\gg$

*A final separation of  $\nu\mu \Rightarrow \mu$  from the non-prompt  $\pi^{+-} / K^{+-} \Rightarrow \mu$*

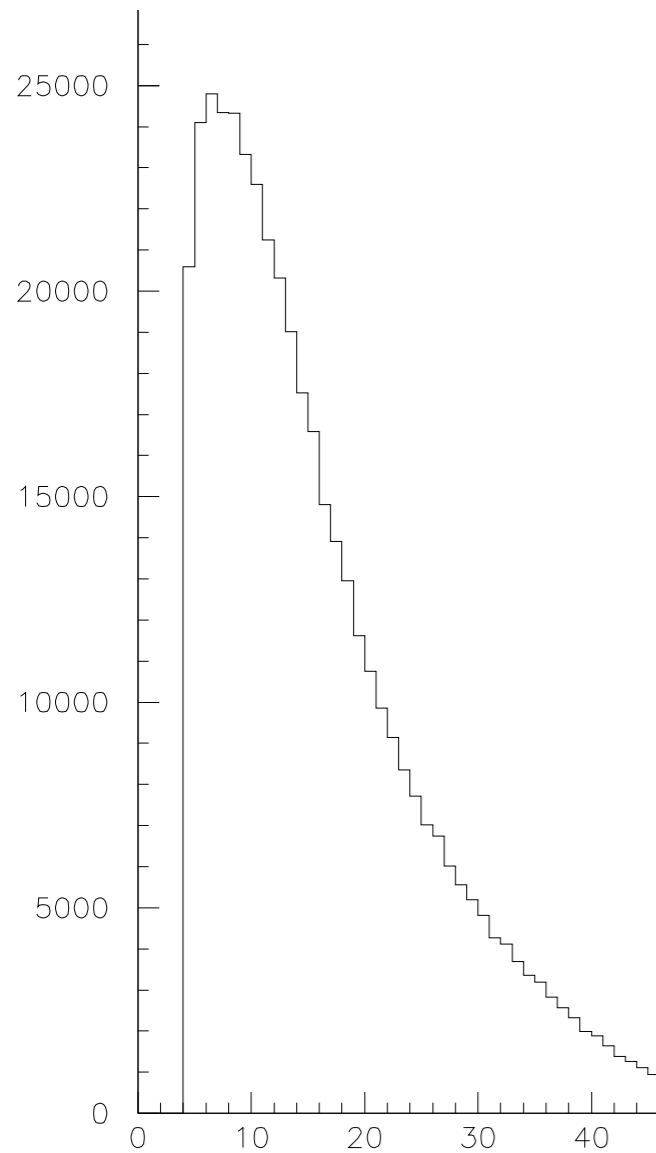
\* Use the Lepton-Hadron isolation to reduce the remaining impurity (later)

## Outlook

- (1) Measure  $E_\mu$  with  $\sim 3.5\%$  resolution
- (2) 100% distinction between  $\mu^-$  vs.  $\mu^+$  in  $\sim 0.3 - 50 \text{ GeV}$
- (3) B-field design allows the  $|E_\mu|$ -scale to be measured to  $\sim 0.1\%$  precision
- (4) in situ measurement of 0.75M  $K^0_s$  checks the  $|E_\mu|$ -scale to  $\sim 0.1\%$  precision
- (5) Absolute efficiency of the  $\mu$ -reconstruction will be checked using the Beam- $\mu$  using the built-in redundancy offered by the  $4\pi$  coverage by ECAL & RPC with  $< 0.1\%$  precision
- (6) Measure large-angle muons, e.g.  $\theta > 60^\circ$ , without loss of efficiency/bias compared to low-angle muons  $\leftarrow$  Important for the 2nd oscillation maximum

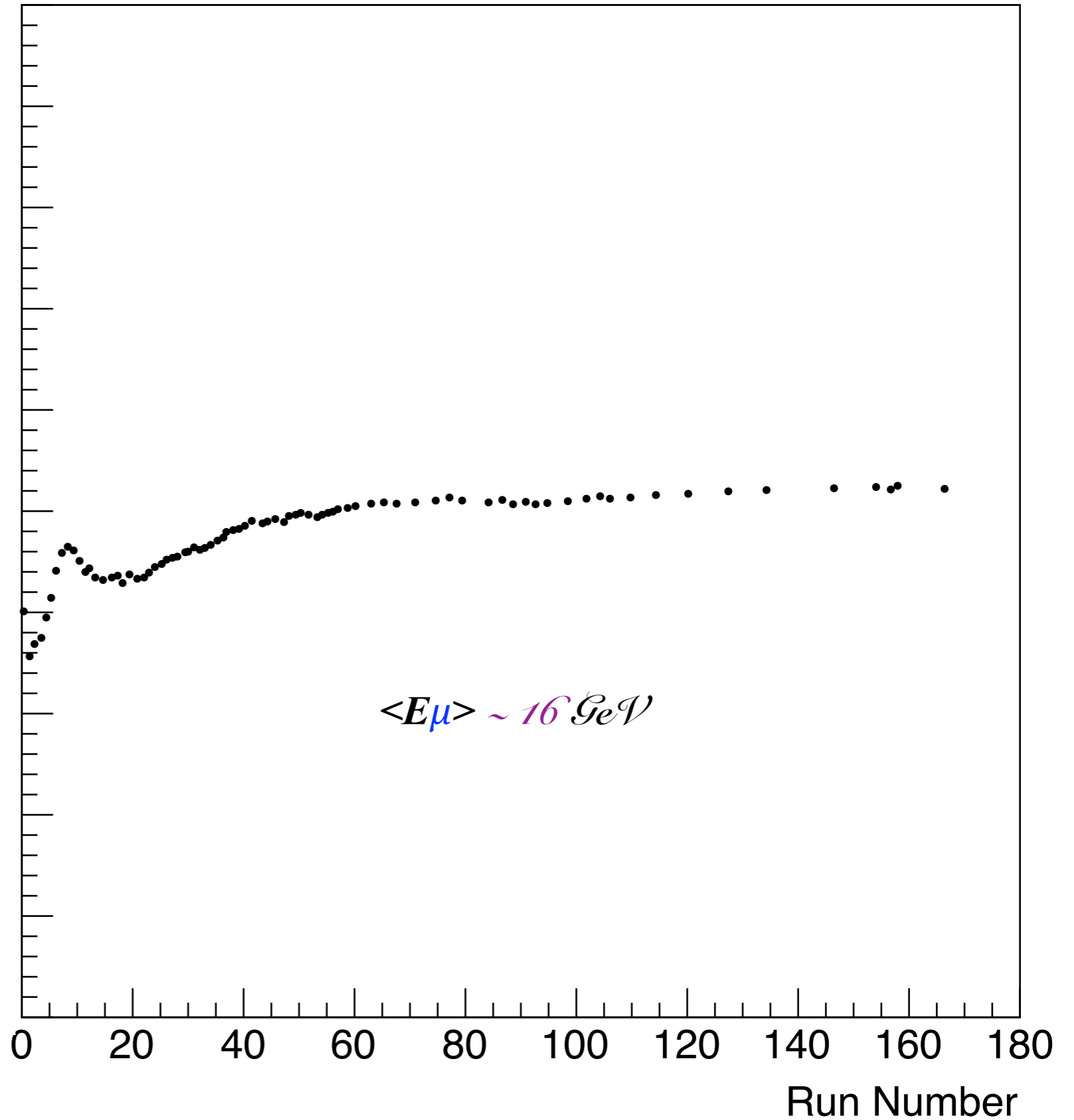
*Backup*

# Checking the $E_\mu$ -efficiency in NOMAD using the “Flattop” Muons



$4 \leq E_\mu \leq 40 \text{ GeV}$

Efficiency



$\langle E_\mu \rangle \sim 16 \text{ GeV}$

... depend on  $E_\mu, \theta_\mu \gg$