

Extended electroweak precision fits and their implications

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LoopFest XV

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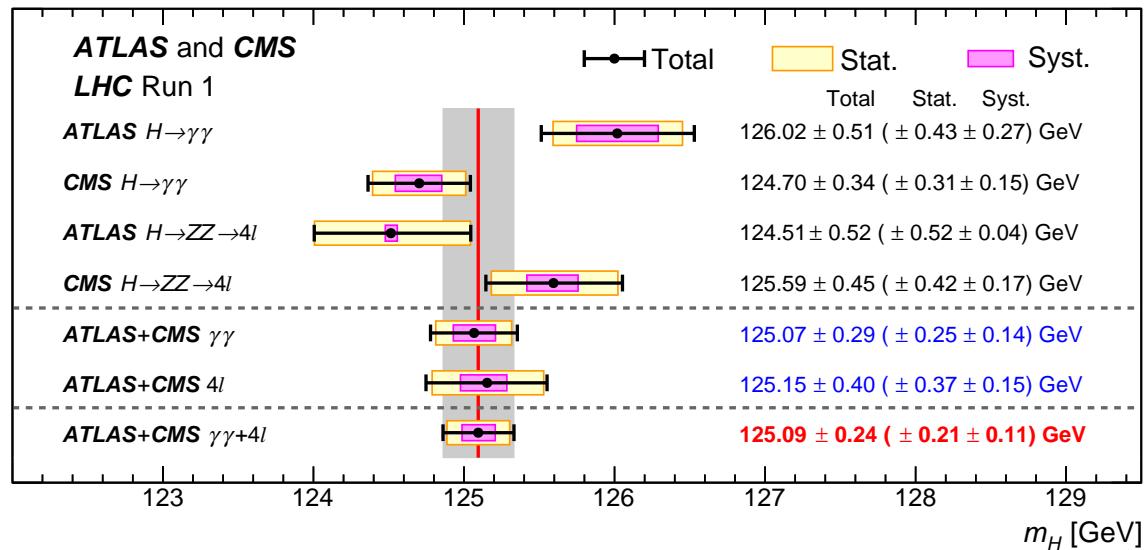
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Thanks to the extended **HEPfit** collaboration.

Electroweak precision physics in the LHC era

- LHC, Run II: after the Higgs-boson discovery
 - ↪ M_H becomes a precision electroweak (EW) parameter;
 - ↪ precision fits now probe consistency of the Standard Model (SM) and can provide indirect evidence of new physics;
 - ↪ fits can be extended to include Higgs-boson results: rates and distributions → constraints on anomalous Higgs-boson couplings;
 - ↪ actual sensitivity depends on experimental precision and theoretical accuracy.
- HEPfit: a global fit of existing electroweak precision data (EWPD) and Higgs-boson observables
 - General framework, new features
 - Results of EWPD fit, constraints on new physics
- Main results for Higgs-boson couplings and effective interactions
 - In terms of κ_i rescaling factors.
 - In terms of C_i coefficients of EFT operators.
- Outlook

LHC Run I has discovered the Higgs, measured its mass and spin . . .



ATLAS+CMS, Phys. Rev. Lett. 114, 191803

M_H is now among the EW precision observables!

Effects of New Physics can now be more clearly disentangled in both
EW observables and Higgs-boson couplings

Moreover, from decays ($H \rightarrow VV$ and $H \rightarrow f\bar{f}$)

- **Spin**: highly constrained to be $s = 0$
- **Parity**: scalar vs pseudoscalar, exploring the tensor structure of decay amplitudes

Fits of electroweak precision data

- Set of **input parameters**
 - **fixed**: G_F , α (best measured)
 - **floating**: M_Z , M_H , m_t , $\alpha_s(M_Z)$, $\Delta\alpha_{\text{had}}^{(5)}$
- **Compute EW precision observables** (EWPO), including all known higher-order corrections (in a given renormalization scheme):
 M_W , Γ_W (LEP2/Tevatron), Z-pole observables: Γ_Z , A_f , ... (LEP/SLD)
- **Perform best fit** and compare with experimental measurement: tension might signal new physics.
- Parametrize new physics effects (ex: S , T , U parameters) and constrain deviations in terms of chosen parameters.
- Several groups:
 - **GAPP** [Erler]
 - **ZFITTER**: [Akhundov, Arbuzov, S.Riemann & T.Riemann]
 - **Gfitter**: [Baak, Cúth, Haller, Hoecker, Kogler, Mönig, Schott, Stelzer]
 - Now also part of **HEPfit** → HEPfit Collaboration.
For this study: [de Blas, Ciuchini, Franco, Mishima, Pierini, L.R., Silvestrini]

HEPfit developer repository: <https://github.com/silvest/HEPfit>

HEPfit webpage: <http://hepfit.roma1.infn.it>

The screenshot shows the HEPfit website interface. At the top is a dark teal header with the "HEPfit" logo in a white box. Below it is a navigation bar with links: home, developers, samples, and documentation. The main content area features a large title: "HEPfit: a Code for the Combination of Indirect and Direct Constraints on High Energy Physics Models." Below this are four rectangular boxes, each containing a plot and a brief description:

- Higgs Physics**: A contour plot of κ_t vs κ_b with regions labeled for different processes: all, $\gamma\gamma$, WW, ZZ, and $t\bar{t}$. It includes a legend and the "HEPfit" logo.
- Precision Electroweak**: A plot of Γ vs S for $U=0$, showing contours for various models like "all", M_W , asymmetries, and Γ_z . It includes a legend and the "HEPfit" logo.
- Flavour Physics**: A plot of A_{FB} vs $q^2 [GeV^2]$ comparing SM@HEPfit, full fit, and LHCb 2015 data. It includes a legend and the "HEPfit" logo.
- BSM Physics**: A plot of $m_{\tilde{\chi}_1^0}$ vs $-m_{\tilde{\eta}_1^\pm}$ for $\tau \rightarrow \mu \gamma$ with $\delta_{23} = 0.1$. It shows current HFAG constraints and projections for Belle II at 5 ab⁻¹ and 50 ab⁻¹. It includes a legend and the "HEPfit" logo.

In this talk: EW precision physics and Higgs-boson physics

[de Blas, Ciuchini, Franco, Mishima, Pierini, L.R., Silvestrini, arXiv:1608.01509]

The fitting procedure → HEPfit

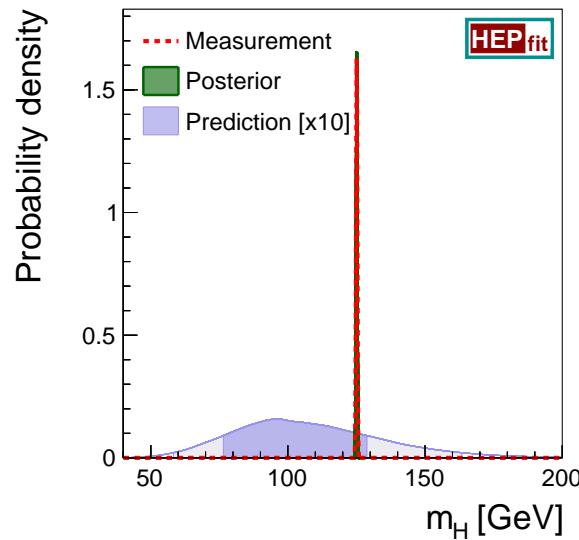
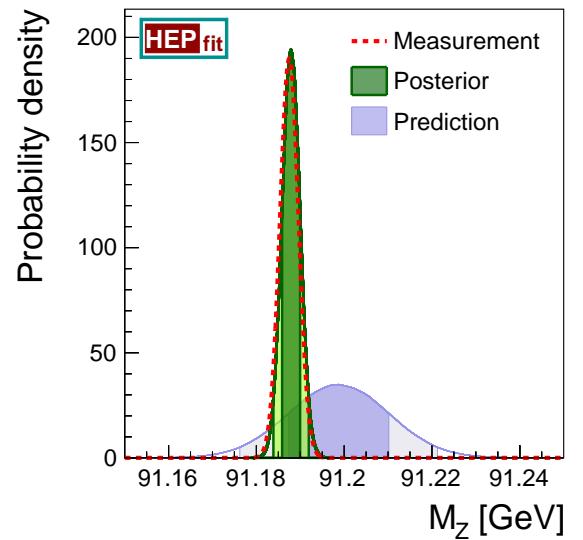
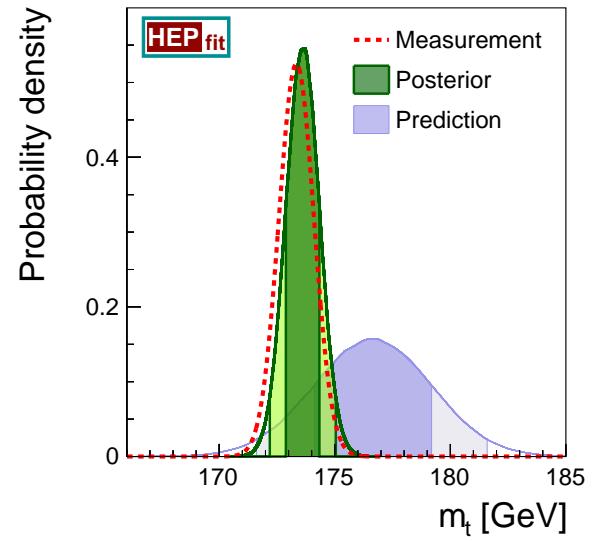
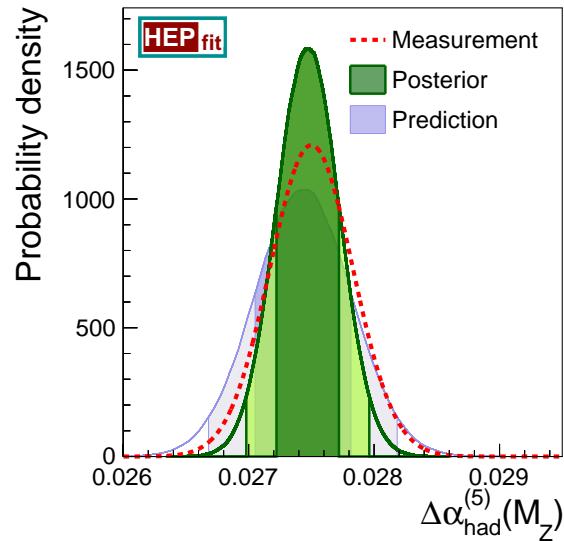
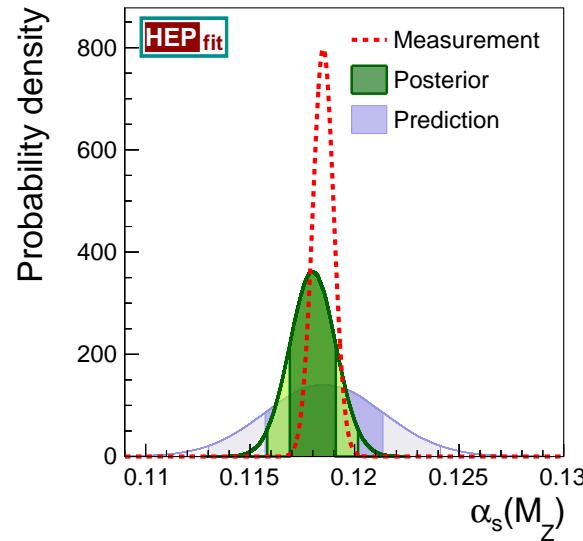
- Both electroweak and Higgs observables are calculated as a SM core plus corrections:
 - ↪ the SM cores include all existing higher order corrections [→ loops!]
 - ↪ the NP corrections are at the lowest order in all SM couplings.
- Experimental results are taken from the most recent published analyses
- The fit procedure uses BAT (Bayesian Analysis Toolkit) with flat priors for all input parameters, and posteriors calculated using a Markov Chain Monte Carlo.
(Caldwell, Kollar, Kröninger, arXiv:0808.2552+ Beaujean, Greenwald, Schulz)
- **Stand-alone or library mode to compute observables in a given model:**
 - ↪ **Implemented models:**
 - ↪ SM,
 - ↪ Oblique parameters (S, T, U), ε_i parameters, Modified $Z b\bar{b}$ couplings,
 - ↪ Modified Higgs couplings (κ_i), SMEFT ($d=6$),
 - ↪ 2HDM.
 - ↪ **Implemented observables:** EWPO, Flavor ($\Delta F = 2$, UT, B-decays).

Results of SM fit to EW precision data

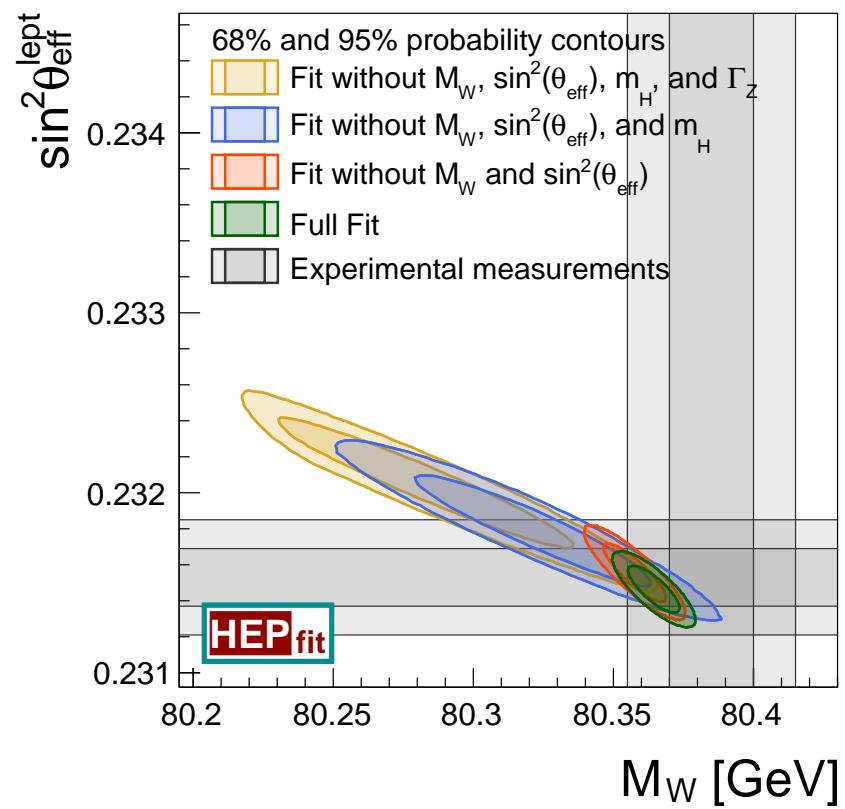
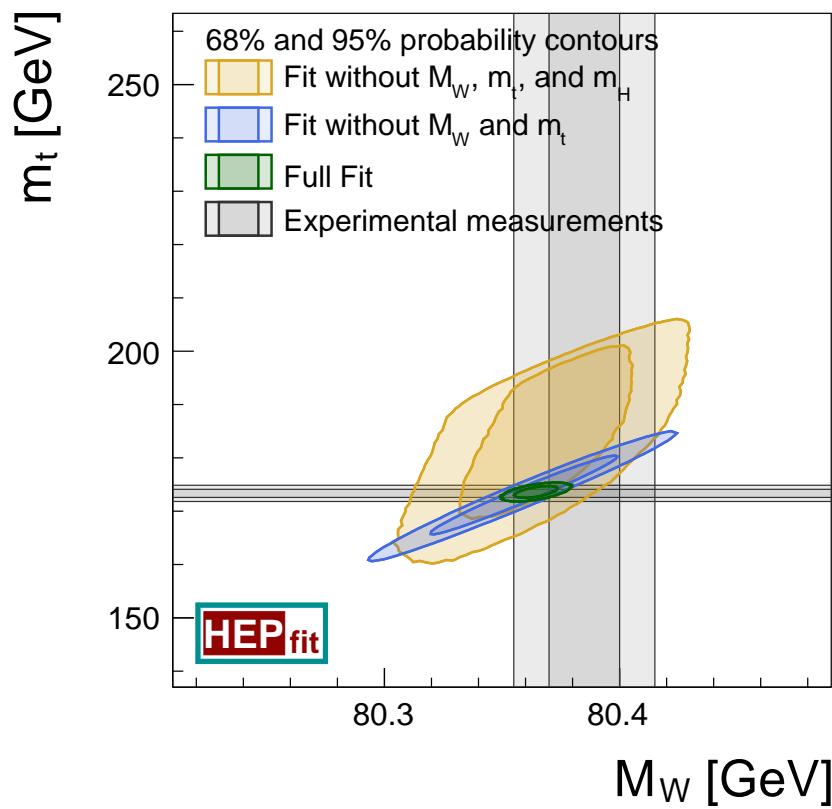
Measurement	Result	Prediction	1D Pull	nD Pull
$\alpha_s(M_Z)$	0.1179 ± 0.0012	0.1180 ± 0.0011	0.1185 ± 0.0028	-0.2
$\delta\alpha_5^{\text{had}}(M_Z)$	0.02750 ± 0.00033	0.02747 ± 0.00025	0.02743 ± 0.00038	0.04
M_Z [GeV]	91.1875 ± 0.0021	91.1879 ± 0.0020	91.199 ± 0.011	-1.0
m_t [GeV]	173.34 ± 0.76	173.61 ± 0.73	176.6 ± 2.5	-1.3
m_H [GeV]	125.09 ± 0.24	125.09 ± 0.24	102.8 ± 26.3	0.8
M_W [GeV]	80.385 ± 0.015	80.3644 ± 0.0061	80.3604 ± 0.0066	1.5
Γ_W [GeV]	2.085 ± 0.042	2.08872 ± 0.00064	2.08873 ± 0.00064	-0.2
$\sin^2 \theta_{\text{eff}}^{\text{lept}}(Q_{\text{FB}}^{\text{had}})$	0.2324 ± 0.0012	0.231464 ± 0.000087	0.231435 ± 0.000090	0.8
$P_\tau^{\text{pol}} = \mathcal{A}_\ell$	0.1465 ± 0.0033	0.14748 ± 0.00068	0.14752 ± 0.00069	-0.4
Γ_Z [GeV]	2.4952 ± 0.0023	2.49420 ± 0.00063	2.49405 ± 0.00068	0.5
σ_h^0 [nb]	41.540 ± 0.037	41.4903 ± 0.0058	41.4912 ± 0.0062	1.3
R_ℓ^0	20.767 ± 0.025	20.7485 ± 0.0070	20.7472 ± 0.0076	0.8
$A_{\text{FB}}^{0,\ell}$	0.0171 ± 0.0010	0.01631 ± 0.00015	0.01628 ± 0.00015	0.8
\mathcal{A}_ℓ (SLD)	0.1513 ± 0.0021	0.14748 ± 0.00068	0.14765 ± 0.00076	1.7
\mathcal{A}_c	0.670 ± 0.027	0.66810 ± 0.00030	0.66817 ± 0.00033	0.02
\mathcal{A}_b	0.923 ± 0.020	0.934650 ± 0.000058	0.934663 ± 0.000064	-0.6
$A_{\text{FB}}^{0,c}$	0.0707 ± 0.0035	0.07390 ± 0.00037	0.07399 ± 0.00042	-0.9
$A_{\text{FB}}^{0,b}$	0.0992 ± 0.0016	0.10338 ± 0.00048	0.10350 ± 0.00054	-2.6
R_c^0	0.1721 ± 0.0030	0.172228 ± 0.000023	0.172229 ± 0.000023	-0.05
R_b^0	0.21629 ± 0.00066	0.215790 ± 0.000028	0.215788 ± 0.000028	0.7
$\sin^2 \theta_{\text{eff}}^{ee}$	0.23248 ± 0.00052			2.1
$\sin^2 \theta_{\text{eff}}^{\mu\mu}$	0.2315 ± 0.0010			0.07
$\sin^2 \theta_{\text{eff}}^{ee}$	0.23146 ± 0.00047	0.231464 ± 0.000087	0.231435 ± 0.000090	0.1
$\sin^2 \theta_{\text{eff}}^{ee,\mu\mu}$	0.2308 ± 0.0012			-0.5
$\sin^2 \theta_{\text{eff}}^{\mu\mu}$	0.2287 ± 0.0032			-0.8
$\sin^2 \theta_{\text{eff}}^{\mu\mu}$	0.2314 ± 0.0011			-0.1

- New 2016 world average for $\alpha_s(M_Z)$ (previously: $\alpha_s(M_Z) = 0.1185 \pm 0.0005$)
- Succesful comparison with both ZFITTER and Gfitter.

Good agreement between direct and indirect determination of the values of the input parameters



Good agreement between direct and indirect determination of the values of the input parameters



EW precision, example of future projections

Present

Observable	Exp. Error	Theor. Error
M_W [MeV]	15	4
$\sin^2 \theta_{\text{eff}}^l$ [10^{-5}]	16	4.5
Γ_Z [MeV]	2.3	0.5
R_b [10^{-5}]	66	15

Future

Observable	ILC	FCC-ee	CEPC	Theor. Error
M_W [MeV]	3-4	1	3	1
$\sin^2 \theta_{\text{eff}}^l$ [10^{-5}]	1	0.6	2.3	1.5
Γ_Z [MeV]	0.8	0.1	0.5	0.2
R_b [10^{-5}]	14	6	17	5-10

[A. Freitas, arXiv:1604.00406]

$(\delta m_t = 50 \text{ MeV}, \delta \alpha_s = 0.001, \delta M_Z = 2.1 \text{ MeV}, \delta(\Delta\alpha) \simeq 5 \cdot 10^{-5})$

ILC [e^+e^- , $\sqrt{s}=90\text{-}500$ GeV] → hep-ph/0106315, arXiv:1306.6352

FCC-ee [e^+e^- , $\sqrt{s}=90\text{-}400$ GeV] → arXiv:1308.6176

CEPC [e^-p , $\sqrt{s}=90\text{-}250$ GeV] → IHEP-CEPC-DR-2015-01

→ Theoretical errors may become leading source of error

Limits on beyond SM physics from EW precision data and Higgs-boson data

Parametrizing indirect evidence of new physics beyond the SM (BSM) in a **model-independent** way via

- Oblique corrections (ex.: S,T,U parameters)
- Non-standard $Zb\bar{b}$ couplings
- Non-standard Higgs couplings
- SM effective field theory (SMEFT)

Oblique parameters, S, T, U

[Peskin and Takeuchi, Phys. Rev. D46 (1992) 381] Dominant effects of NP in gauge-boson vacuum polarization corrections,

$$\begin{aligned}\alpha S &= 4e^2 \left[\Pi_{33}^{NP'}(0) - \Pi_{3Q}^{NP'}(0) \right] \\ \alpha T &= \frac{e^2}{s_W^2 c_W^2 M_Z^2} \left[\Pi_{11}^{NP}(0) - \Pi_{33}^{NP}(0) \right] \\ \alpha U &= 4e^2 \left[\Pi_{11}^{NP'}(0) - \Pi_{33}^{NP'}(0) \right]\end{aligned}$$

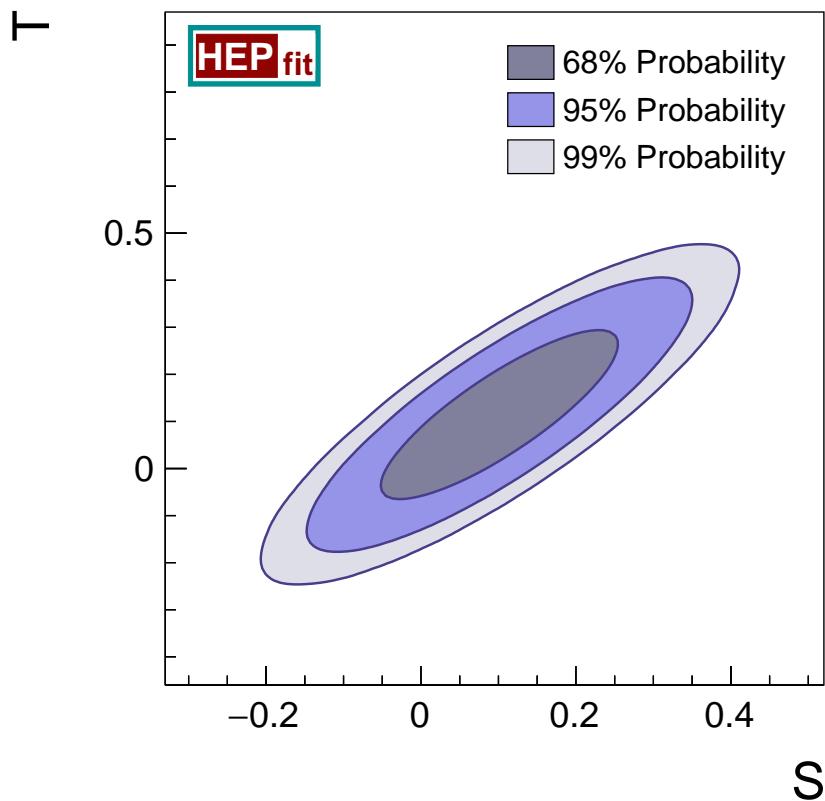
NP contributions to given EWPO (linearized in terms of S, T, U)

$$O = O_{\text{SM}} + O_{\text{NP}}(S, T, U)$$

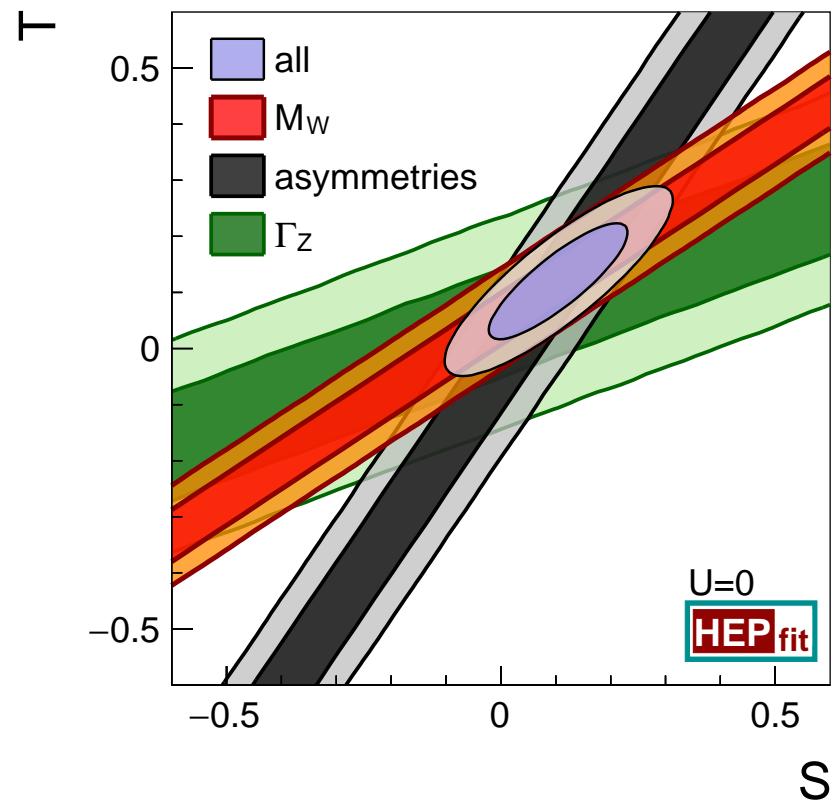
$U \rightarrow$ NP contributions to M_W and Γ_W

$U \ll S, T$ in many NP models (linearly realized EWSB) $\rightarrow U = 0$

Equivalently: use $\varepsilon_{1,2,3,b}$ parameters [Altarelli, Barbieri, Phys. Lett. B253 (1991) 161]



	Fit result	correlations	
S	0.09 ± 0.10	1.00	
T	0.10 ± 0.12	0.86	1.00
U	0.01 ± 0.09	-0.054	-0.81
			1.00

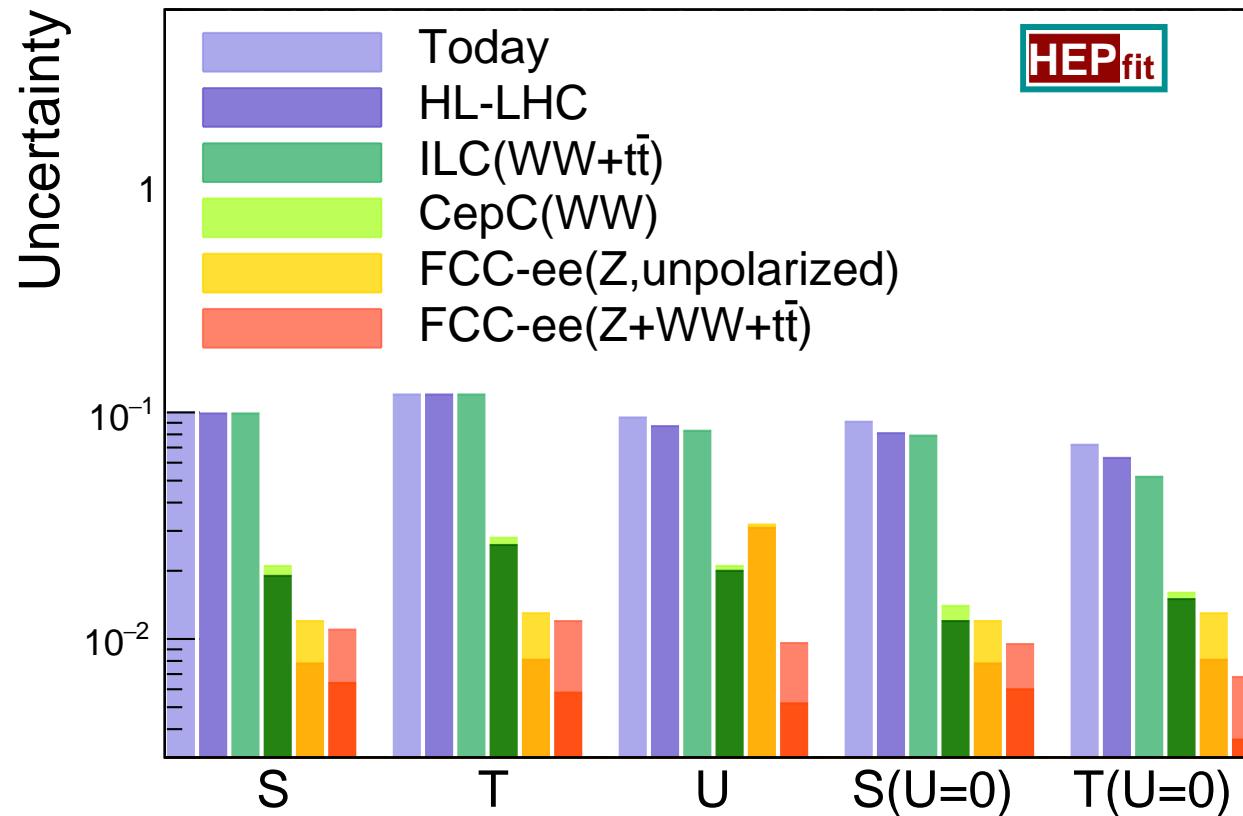


	Fit result	correlations	
S	0.10 ± 0.08	1.00	
T	0.12 ± 0.07	0.86	1.00

blue shaded areas \rightarrow 68%, 95%, 99%

blue shaded areas \rightarrow 68%, 95%

Projected sensitivity to EW oblique parameters at a glance:



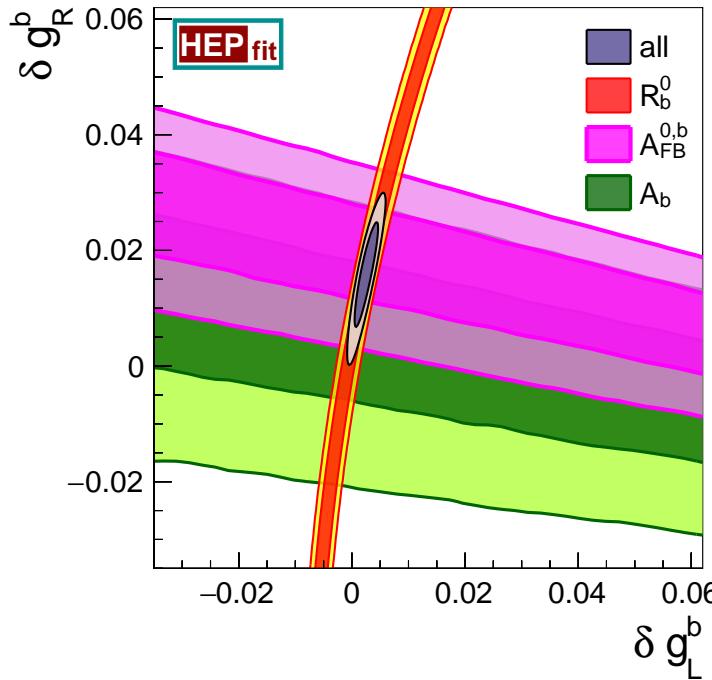
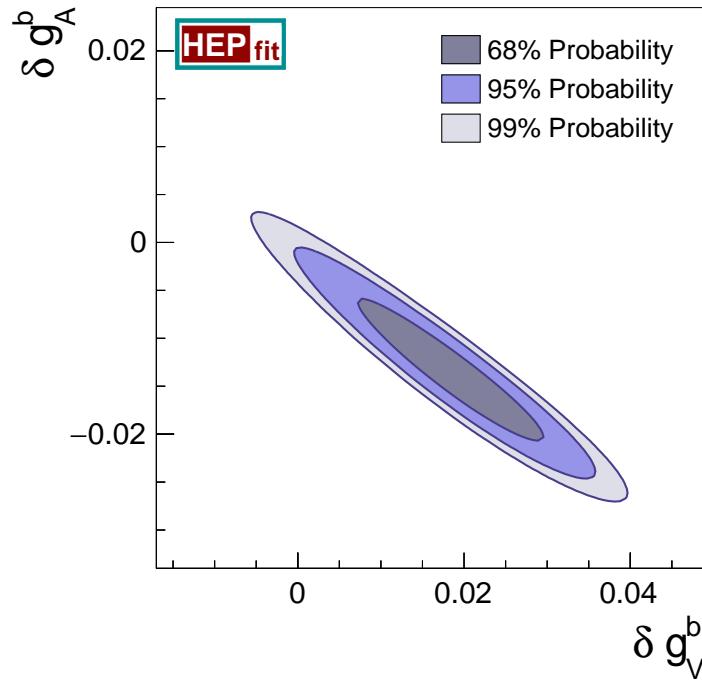
FCCee: several projected runs

	Z pole	WW threshold	HZ threshold	$t\bar{t}$ threshold	above $t\bar{t}$ threshold
\sqrt{s} [GeV]	90	160	240	350	> 350
\mathcal{L} [ab^{-1}/yr]	86	15	3.5	1.0	1.0
Years of run	0.3/2.5	1	3	0.5	3
Events	$10^{12}/10^{13}$	6×10^7	2×10^6	2×10^5	7.5×10^4

Non-standard $Zb\bar{b}$ couplings

Tension in $A_{\text{FB}}^{0,b}$ (pull of EWPO fit $\rightarrow 2.8\sigma$)

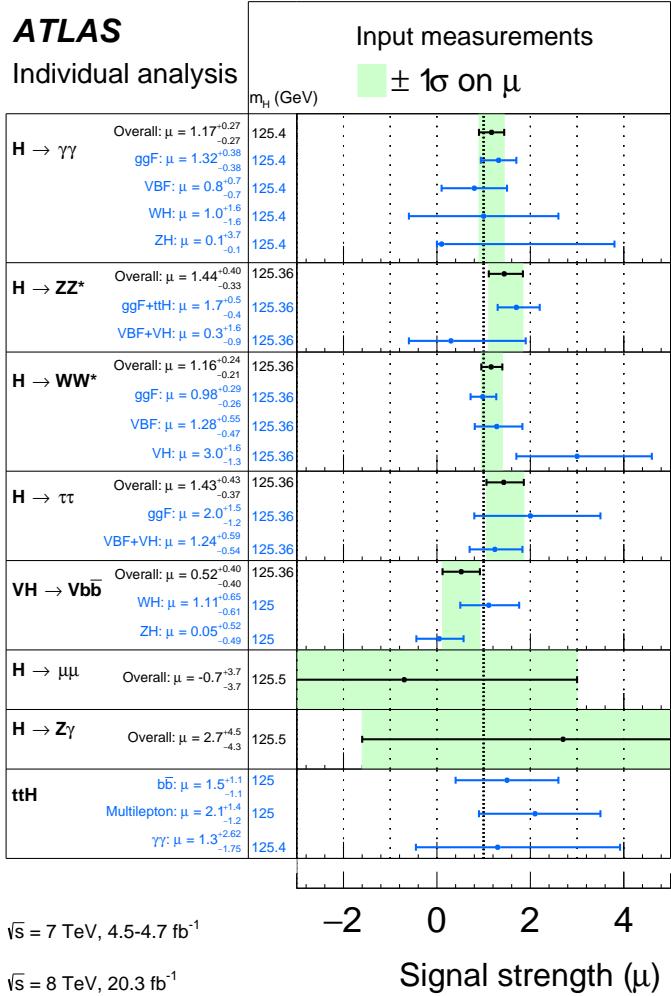
$$A_{\text{FB}}^{0,b} = \frac{3}{4} A_e A_b , \quad A_f = \frac{2 \operatorname{Re} \frac{g_V^f}{g_A^f}}{1 + (\operatorname{Re} \frac{g_V^f}{g_A^f})^2} \longrightarrow g_i^b = g_{i,\text{SM}}^b + \delta g_i^b \quad (\text{i=V,A,L,R})$$



$$\begin{aligned} \delta A_{\text{FB}}^{0,b}, \delta A_b &\propto g_{L,\text{SM}}^b \delta g_R^b - g_{R,\text{SM}}^b \delta g_L^b \\ \delta R_b &\propto g_{R,\text{SM}}^b \delta g_R^b + g_{L,\text{SM}}^b \delta g_L^b \end{aligned}$$

	Fit result	correlations	
δg_R^b	0.016 ± 0.006	1.00	
δg_L^b	0.003 ± 0.001	0.90	1.00
δg_V^b	0.018 ± 0.007	1.00	
δg_A^b	-0.013 ± 0.005	-0.98	1.00

Higgs couplings analysis



ATLAS: arXiv:1507.04548

$$\mu = \sum_i w_i r_i \quad \text{where}$$

$$w_i = \frac{[\sigma \times \text{Br}]_i}{[\sigma_{\text{SM}} \times \text{Br}_{\text{SM}}]_i}$$

$$r_i = \frac{\epsilon_i [\sigma_{\text{SM}} \times \text{Br}_{\text{SM}}]_i}{\sum_j \epsilon_j^{\text{SM}} [\sigma_{\text{SM}} \times \text{Br}_{\text{SM}}]_j}$$

$$\sigma_i = \sigma_i^{\text{SM}} + \delta\sigma_i$$

$$\Gamma_j = \Gamma_j^{\text{SM}} + \delta\Gamma_j$$

$\sigma_i^{\text{SM}}, \Gamma_j^{\text{SM}} \rightarrow$ YR of HXSWG

$\delta\sigma_i \rightarrow$ FR+Madgraph+Kfactors

$\delta\Gamma_j \rightarrow$ eHdecay

hγγ: ATLAS(1408.7084), CMS(1407.0558)

hττ: ATLAS(1501.04943), CMS(1401.5041)

hZZ: ATLAS(1408.5191), CMS(1412.8662)

hWW: ATLAS(1412.2641, 1506.06641),
CMS(1312.1129)

hb: ATLAS(1409.6212, 1503.05066),
CMS(1310.3687, 1408.1682),
CDF (1301.6668), D0 (1303.0823)

Non-standard Higgs-boson couplings

Minimal assumptions (inspired by strong-dynamics EWSB models):

- ↪ only one Higgs boson below the cutoff Λ ;
- ↪ custodial symmetry approximately realized;
- ↪ corrections from new physics flavor-diagonal and universal;
- ↪ no NP corrections in Hgg , $H\gamma\gamma$, $HZ\gamma$ loop-induced couplings.

Ex.: [Contino, Grojean, Moretti, Piccinini,Rattazzi](#), JHEP 1005 (2010) 089

$$\mathcal{L}_{\text{eff}} = \frac{v^2}{4} \text{tr} \left(D_\mu \Sigma^\dagger D^\mu \Sigma \right) \left(1 + 2\kappa_V \frac{h}{v} + \dots \right) - m_i \bar{f}_L^i \left(1 + 2\kappa_f \frac{h}{v} + \dots \right) f_R^i$$

where $\Sigma(x) = \exp i\sigma^a \chi^a(x)/v \rightarrow$ longitudinal W/Z polarizations.

Defining: $\kappa_X = g_X/g_X^{\text{SM}}$ ($\text{SM} \rightarrow \kappa_X = 1$),

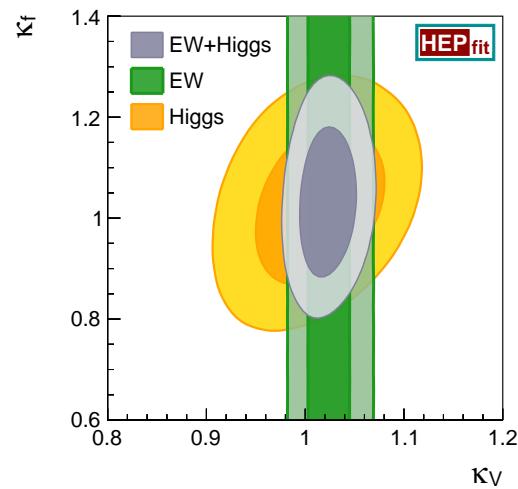
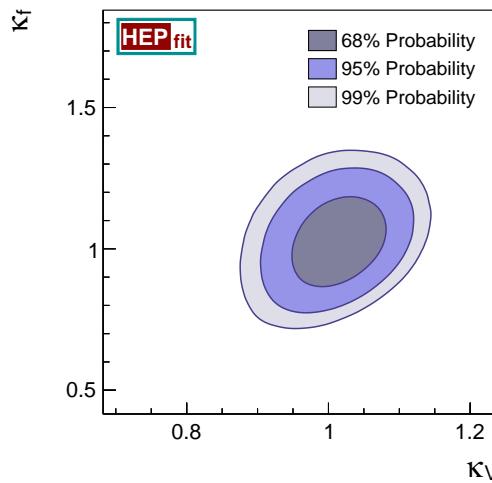
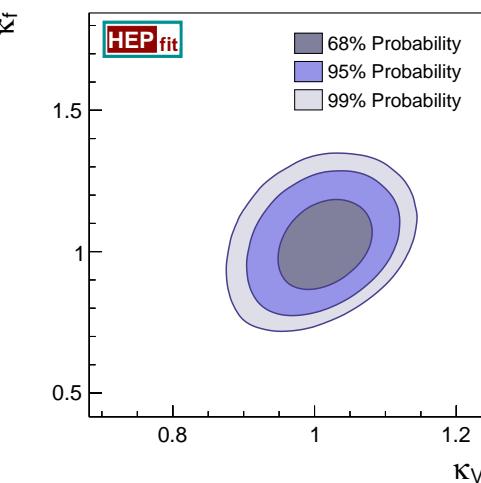
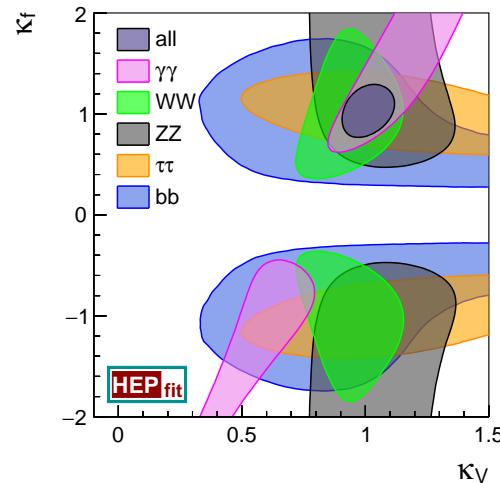
$\kappa_V \rightarrow$ rescaling of all hVV couplings

$\kappa_f \rightarrow$ rescaling of all hff couplings

Considering both κ_V and κ_f

Higgs only

	68%	95%	correlation	
κ_V	1.01 ± 0.04	[0.93, 1.10]	1.00	
κ_f	1.03 ± 0.10	[0.83, 1.23]	0.31	1.00

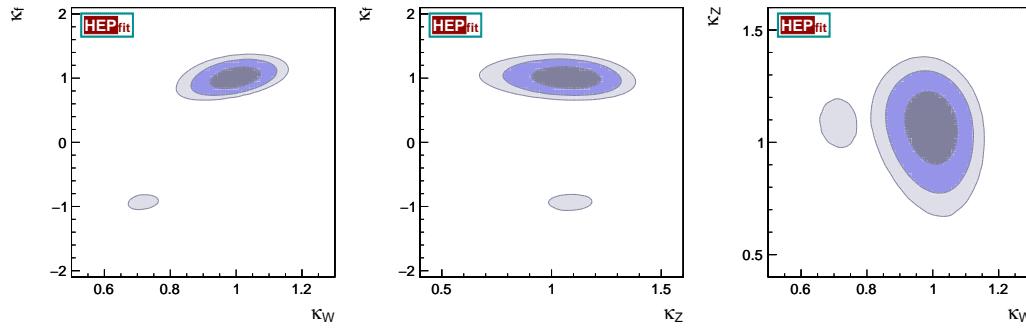


Higgs+EWPO

	68%	95%	correlation	
κ_V	1.02 ± 0.02	[0.99, 1.06]	1.00	
κ_f	1.03 ± 0.10	[0.85, 1.23]	0.14	1.00

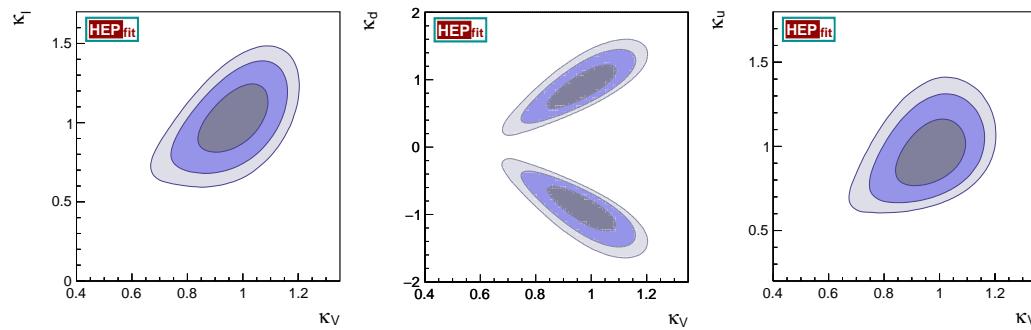
Zooming into κ_V and κ_f . . .

Custodial symmetry
 $(\kappa_V \rightarrow \kappa_W, \kappa_Z)$



	68%	95%	correlation		
κ_W	1.00 ± 0.05	$[0.89, 1.10]$	1.00		
κ_Z	1.07 ± 0.11	$[0.85, 1.27]$	-0.17	1.00	
κ_f	1.01 ± 0.11	$[0.80, 1.22]$	0.41	-0.14	1.00

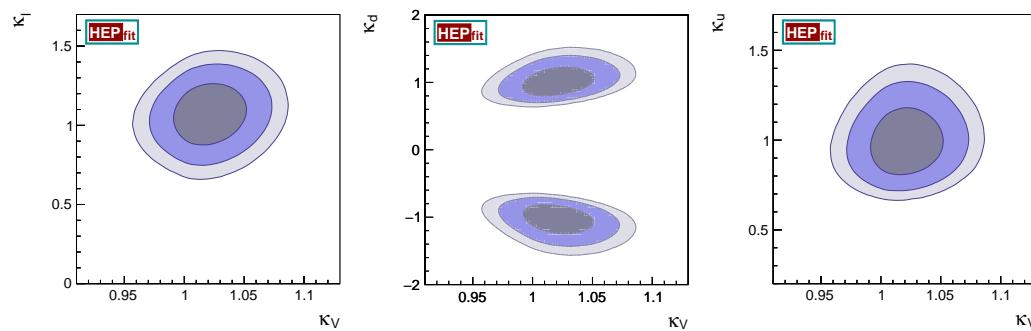
Higgs only



Flavor universality
 $(\kappa_f \rightarrow \kappa_u, \kappa_d, \kappa_l)$

	68%	95%	correlation		
κ_V	0.97 ± 0.08	$[0.80, 1.13]$	1.00		
κ_l	1.01 ± 0.14	$[0.73, 1.30]$	0.54	1.00	
κ_u	0.97 ± 0.13	$[0.73, 1.25]$	0.42	0.41	1.00
κ_d	0.91 ± 0.21	$[0.48, 1.35]$	0.81	0.61	0.77
					1.00

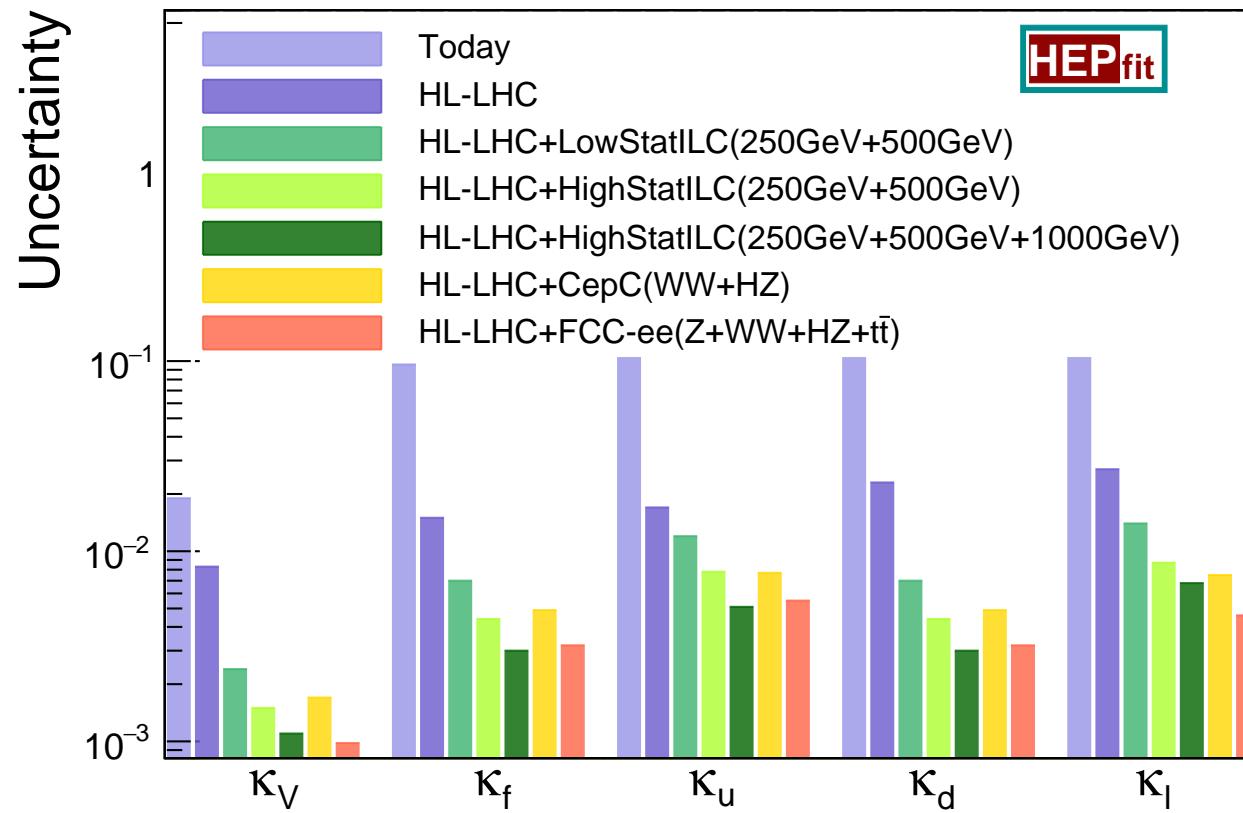
Higgs only



Higgs+EWPO

	68%	95%	correlation		
κ_V	1.02 ± 0.02	$[0.99, 1.06]$	1.00		
κ_l	1.07 ± 0.12	$[0.82, 1.32]$	0.15	1.00	
κ_u	1.01 ± 0.12	$[0.79, 1.27]$	0.10	0.24	1.00
κ_d	1.01 ± 0.13	$[0.76, 1.30]$	0.31	0.38	0.78
					1.00

Projected sensitivity to κ_i parameters at a glance:



SM Effective Field Theories

Systematic extension of the SM Lagrangian by $d > 4$ operators,

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum_{d>4} \frac{1}{\Lambda^{d-4}} \mathcal{L}_d, \quad \text{with} \quad \mathcal{L}_d = \sum_i C_i \mathcal{O}_i, \quad [\mathcal{O}_i] = d,$$

including **effects in NP on EWPO** and **SM Higgs-boson coupling**, but also **allowing for new structures**.

Consider:

- $d = 6$ operators only, obeying SM gauge symmetry, L and B conservation
- one Higgs doublet of $SU(2)_L$, linearly realized SSB
- assuming flavor universality: **59 operators**
[basis by Grzadkowski et al., JHEP 1010 (2010) 085]
- CP even and with at least one Higgs: **27 operators**
- contributing to the observables considered: **17 operators**
- with a specific model in mind: running $C_i(\Lambda) \rightarrow C_i(\Lambda_{\text{EW}})$ more meaningful
- otherwise take $C_i = C_i(\Lambda_{\text{EW}})$, no running included

$$\mathcal{O}_{HG} = (H^\dagger H) G_{\mu\nu}^A G^{A\mu\nu}$$

$$\mathcal{O}_{HW} = (H^\dagger H) W_{\mu\nu}^I W^{I\mu\nu}$$

$$\mathcal{O}_{HB} = (H^\dagger H) B_{\mu\nu} B^{\mu\nu}$$

$$\mathcal{O}_{HWB} = (H^\dagger \tau^I H) W_{\mu\nu}^I B^{\mu\nu}$$

$$\mathcal{O}_{HD} = (H^\dagger D^\mu H)^* (H^\dagger D_\mu H)$$

$$\mathcal{O}_{H\square} = (H^\dagger H) \square (H^\dagger H)$$

bosonic operators

→ corrections to:

- oblique parameters
- hVV
- WWZ and $WW\gamma$

$$\mathcal{O}_{HL}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{L} \gamma^\mu L)$$

$$\mathcal{O}_{HL}^{(3)} = (H^\dagger i \overleftrightarrow{D}_\mu^I H)(\bar{L} \tau^I \gamma^\mu L)$$

$$\mathcal{O}_{He} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{e}_R \gamma^\mu e_R)$$

$$\mathcal{O}_{HQ}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{Q} \gamma^\mu Q)$$

$$\mathcal{O}_{HQ}^{(3)} = (H^\dagger i \overleftrightarrow{D}_\mu^I H)(\bar{Q} \tau^I \gamma^\mu Q)$$

$$\mathcal{O}_{Hu} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{u}_R \gamma^\mu u_R)$$

$$\mathcal{O}_{Hd} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{d}_R \gamma^\mu d_R)$$

$$\mathcal{O}_{Hud} = i(\tilde{H}^\dagger D_\mu H)(\bar{u}_R \gamma^\mu d_R)$$

single-fermionic-vector-current
operators

→ corrections to:

- $h f \bar{f}$
- $V f \bar{f}$

single-fermionic-scalar-current
operators

$$\begin{aligned}\mathcal{O}_{eH} &= (H^\dagger H)(\bar{L} e_R H) \\ \mathcal{O}_{uH} &= (H^\dagger H)(\bar{Q} u_R \tilde{H}) \\ \mathcal{O}_{dH} &= (H^\dagger H)(\bar{Q} d_R H)\end{aligned}$$

→ corrections to:

- oblique parameters
- Yukawa couplings
- $h f \bar{f}$

four-fermion operator

$$\mathcal{O}_{LL} = (\bar{L} \gamma^\mu L)(\bar{L} \gamma^\mu L)$$

→ corrections to:

- G_F extraction from μ decay

Notice: $V f \bar{f}$ and indirect effects (e.g. G_F) strongly constrained by EW precision observables.

Upon SSB, direct effect on Higgs-boson couplings

$$\mathcal{L}_{\text{Higgs}} = \mathcal{L}_{hVV} + \mathcal{L}_{hff} + \mathcal{L}_{hVff} + \mathcal{L}_{hTff}$$

each term contains the interactions to either vector bosons or fermions.

Ex.1: \mathcal{L}_{hVV} contains all the non-fermionic interactions with the SM vector bosons,

$$\begin{aligned} \mathcal{L}_{hVV} = & h \left(g_{hZZ}^{(1)} Z_{\mu\nu} Z^{\mu\nu} + g_{hZZ}^{(2)} Z_\nu \partial_\mu Z^{\mu\nu} + g_{hZZ}^{(3)} Z_\mu Z^\mu - \right. \\ & + g_{hAA} A_{\mu\nu} A^{\mu\nu} + g_{hZA}^{(1)} Z_{\mu\nu} A^{\mu\nu} + g_{hZA}^{(2)} Z_\nu \partial_\mu A^{\mu\nu} - \\ & + g_{hWW}^{(1)} W_{\mu\nu}^+ W^{-\mu\nu} + \left(g_{hWW}^{(2)} W_\nu^+ D_\mu W^{-\mu\nu} + (g_{hWW}^{(2)})^* W_\nu^- D_\mu W^{+\mu\nu} \right) \\ & \left. + g_{hWW}^{(3)} W_\mu^+ W^{-\mu} + g_{hGG} \text{Tr} [G_{\mu\nu} G^{\mu\nu}] \right) \end{aligned}$$

where (both directly and indirectly $\rightarrow G_F$, field renormalization, ...),

$$C_{HG} \rightarrow g_{hGG}$$

$$C_{HW} \rightarrow g_{hWW}^{(1)}$$

$$C_{HW}, C_{HB}, C_{HWB} \rightarrow g_{hZZ}^{(1)}, g_{hZA}^{(1)}, g_{hAA}^{(1)}$$

$$C_{HD} \rightarrow g_{hZZ}^{(3)}$$

while Ex. 2: \mathcal{L}_{hff} contains the interactions with the fermions only:

$$\mathcal{L}_{hff} = h \sum_f g_{hff} \overline{f_L} f_R + \text{h.c.}$$

where,

$$C_{eH} \rightarrow g_{h\tau\tau}$$

$$C_{uH} \rightarrow g_{hcc}, g_{htt}$$

$$C_{dH} \rightarrow g_{hbb}$$

The corresponding rescaling factors $\kappa_V = \frac{g_{hVV}}{g_{hVV}^{SM}}$ and $\kappa_f = \frac{g_{hff}}{g_{hff}^{SM}}$, are

$$\kappa_Z = 1 + \delta_h + \frac{1}{2} \frac{v^2}{\Lambda^2} C_{HD} - \frac{1}{2} \delta_{G_F}$$

$$\kappa_W = 1 + \delta_h - \frac{1}{2} (c_W^2 - s_W^2) (4 s_W c_W \frac{v^2}{\Lambda^2} C_{HWB} + c_W^2 \frac{v^2}{\Lambda^2} C_{HD} + \delta_{G_F})$$

$$\kappa_f = 1 + \delta_h - \frac{1}{2} \delta_{G_F} - \frac{v}{m_f} \frac{v^2}{\Lambda^2} \frac{C_{fH}}{\sqrt{2}}$$

where

$\delta_h \rightarrow$ NP corrections to h wave-function renormalization

$\delta_{G_F} \rightarrow$ NP corrections to G_F

95% bounds on coefficients of d=6 interactions

→ Fitting one operator at a time

	Only EW	Only Higgs	EW + Higgs
Operator (O_i)	C_i/Λ^2 [TeV $^{-2}$] at 95%	C_i/Λ^2 [TeV $^{-2}$] at 95%	C_i/Λ^2 [TeV $^{-2}$] at 95%
$O_{HG} = (H^\dagger H) G_{\mu\nu}^A G^{A\mu\nu}$	--	[-0.005, 0.009]	[-0.005, 0.009]
$O_{HW} = (H^\dagger H) W_{\mu\nu}^I W^{I\mu\nu}$	--	[-0.033, 0.015]	[-0.033, 0.015]
$O_{HB} = (H^\dagger H) B_{\mu\nu} B^{\mu\nu}$	--	[-0.009, 0.004]	[-0.009, 0.004]
$O_{HWB} = (H^\dagger \tau^I H) W_{\mu\nu}^I B^{\mu\nu}$	[-0.010, 0.004]	[-0.008, 0.017]	[-0.007, 0.005]
$O_{HD} = (H^\dagger D^\mu H)^* (H^\dagger D_\mu H)$	[-0.032, 0.006]	[-1.38, 1.35]	[-0.032, 0.005]
$O_{H\square} = (H^\dagger H) \square (H^\dagger H)$	--	[-1.12, 1.72]	[-1.12, 1.72]
$O_{HL}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{L} \gamma^\mu L)$	[-0.006, 0.011]	--	[-0.006, 0.011]
$O_{HL}^{(3)} = (H^\dagger i \overleftrightarrow{D}_\mu^I H) (\bar{L} \tau^I \gamma^\mu L)$	[-0.013, 0.006]	[-0.64, 0.49]	[-0.013, 0.006]
$O_{He} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{e}_R \gamma^\mu e_R)$	[-0.017, 0.006]	--	[-0.017, 0.006]
$O_{HQ}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{Q} \gamma^\mu Q)$	[-0.025, 0.046]	[-4.3, 1.3]	[-0.025, 0.046]
$O_{HQ}^{(3)} = (H^\dagger i \overleftrightarrow{D}_\mu^I H) (\bar{Q} \tau^I \gamma^\mu Q)$	[-0.011, 0.016]	[-0.35, 0.18]	[-0.011, 0.016]
$O_{Hu} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{u}_R \gamma^\mu u_R)$	[-0.069, 0.088]	[-1.9, 2.2]	[-0.069, 0.088]
$O_{Hd} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{d}_R \gamma^\mu d_R)$	[-0.160, 0.058]	[-6.2, 7]	[-0.160, 0.058]
$O_{eH} = (H^\dagger H) (\bar{L} e_R H)$	--	[-0.053, 0.027]	[-0.053, 0.027]
$O_{uH} = (H^\dagger H) (\bar{Q} u_R \tilde{H})$	--	[-0.350, 0.510]	[-0.350, 0.510]
$O_{dH} = (H^\dagger H) (\bar{Q} d_R H)$	--	[-0.036, 0.086]	[-0.036, 0.086]
$O_{LL} = (\bar{L} \gamma^\mu L) (\bar{L} \gamma^\mu L)$	[-0.010, 0.023]	[-1.970, 1.260]	[-0.010, 0.023]

↪ see also **Corbett, Eboli, Gonçalves, Gonzales-Fraile, Plehn, Rauch**, arXiv:1505.0551

95% bounds on coefficients of d=6 interactions

→ Fitting all EW operators at the same time

Operator (O_i)	One at a time	Combined
	C_i/Λ^2 [TeV $^{-2}$] at 95%	C_i/Λ^2 [TeV $^{-2}$] at 95%
$O_{HL}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{L}\gamma^\mu L)$	[-0.006, 0.011]	[-0.012, 0.036]
$O_{HL}^{(3)} = (H^\dagger i \overleftrightarrow{D}_\mu^I H)(\bar{L}\tau^I\gamma^\mu L)$	[-0.013, 0.006]	[-0.064, 0.009]
$O_{He} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{e}_R\gamma^\mu e_R)$	[-0.017, 0.006]	[-0.026, 0.014]
$O_{HQ}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{Q}\gamma^\mu Q)$	[-0.025, 0.046]	[-0.106, 0.070]
$O_{HQ}^{(3)} = (H^\dagger i \overleftrightarrow{D}_\mu^I H)(\bar{Q}\tau^I\gamma^\mu Q)$	[-0.011, 0.016]	[-0.189, -0.001]
$O_{Hu} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{u}_R\gamma^\mu u_R)$	[-0.069, 0.088]	[-0.220, 0.420]
$O_{Hd} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{d}_R\gamma^\mu d_R)$	[-0.160, 0.058]	[-1.180, -0.150]
$O_{LL} = (\bar{L}\gamma^\mu L)(\bar{L}\gamma^\mu L)$	[-0.010, 0.023]	[-0.084, 0.030]

Only 8 combinations of EW operators can be fitted at the same time: drop O_{HWB} and O_{HD} [↪ e.g. [Falkowski, Riva, arXiv:1411.0669](#)]

95% bounds on scale of new physics Λ

	Only EW	Only Higgs	EW + Higgs
Operator (O_i)	Λ [TeV] $ C_i = 1$	Λ [TeV] $ C_i = 1$	Λ [TeV] $ C_i = 1$
$O_{HG} = (H^\dagger H) G_{\mu\nu}^A G^{A\mu\nu}$	--	12	12
$O_{HW} = (H^\dagger H) W_{\mu\nu}^I W^{I\mu\nu}$	--	5.9	5.9
$O_{HB} = (H^\dagger H) B_{\mu\nu} B^{\mu\nu}$	--	12	12
$O_{HWB} = (H^\dagger \tau^I H) W_{\mu\nu}^I B^{\mu\nu}$	11	8.2	12
$O_{HD} = (H^\dagger D^\mu H)^* (H^\dagger D_\mu H)$	5.9	0.9	6
$O_{H\square} = (H^\dagger H) \square (H^\dagger H)$	--	0.8	0.8
$O_{HL}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{L} \gamma^\mu L)$	10	—	10
$O_{HL}^{(3)} = (H^\dagger i \overleftrightarrow{D}_\mu^I H) (\bar{L} \tau^I \gamma^\mu L)$	9.4	1.3	9.7
$O_{He} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{e}_R \gamma^\mu e_R)$	8.2	—	8.2
$O_{HQ}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{Q} \gamma^\mu Q)$	5.0	0.5	5.0
$O_{HQ}^{(3)} = (H^\dagger i \overleftrightarrow{D}_\mu^I H) (\bar{Q} \tau^I \gamma^\mu Q)$	8.6	1.8	8.7
$O_{Hu} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{u}_R \gamma^\mu u_R)$	3.5	0.7	3.5
$O_{Hd} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{d}_R \gamma^\mu d_R)$	2.7	0.4	2.7
$O_{eH} = (H^\dagger H) (\bar{L} e_R H)$	--	4.7	4.7
$O_{uH} = (H^\dagger H) (\bar{Q} u_R H)$	-- 1.5	1.5	—
$O_{dH} = (H^\dagger H) (\bar{Q} d_R H)$	--	3.7	3.7
$O_{LL} = (\bar{L} \gamma^\mu L) (\bar{L} \gamma^\mu L)$	7.9	0.9	7.9

→ For $|C_i| \simeq 1$ NP is beyond LHC reach, need perturbative C_i .

95% bounds on scale of new physics Λ - Present vs Future

	95% present bound on		95% future bound on	
Coefficient	$\frac{C_i}{\Lambda^2}$ [TeV $^{-2}$] ($C_i = \pm 1$)	Λ [TeV] ($C_i = \pm 1$)	$\frac{C_i}{\Lambda^2}$ [TeV $^{-2}$] ($C_i = \pm 1$)	Λ [TeV] ($C_i = \pm 1$)
C_{HWB}	[0.009, 0.003]	12	[0.0001, 0.0001]	93
C_{HD}	[0.027, 0.004]	6.6	[0.0005, 0.0005]	45
$C_{HL}^{(1)}$	[0.005, 0.012]	9.9	[0.0003, 0.0003]	56
$C_{HL}^{(3)}$	[0.011, 0.005]	10	[0.0002, 0.0002]	70
C_{He}	[0.015, 0.007]	8.6	[0.0003, 0.0003]	58
$C_{HQ}^{(1)}$	[0.027, 0.043]	5.3	[0.0018, 0.0018]	24
$C_{HQ}^{(3)}$	[0.011, 0.015]	9.1	[0.0005, 0.0005]	44
C_{Hu}	[0.071, 0.081]	3.7	[0.0035, 0.0035]	17
C_{Hd}	[0.14, 0.070]	2.9	[0.0046, 0.0046]	15
C_{LL}	[0.0096, 0.023]	7.3	[0.0003, 0.0003]	61

→ Precision ($\times 10$) → reach $\Lambda \simeq 100$ TeV

↪ Controlling the theoretical uncertainty will be crucial →
parameters, NLO HEFT, ...

Outlook

- The SM offers a incredibly solid theoretical framework that we can use to extract indications of new physics.
- **Indirect evidence of new physics** from Higgs-boson and EW precision measurements can come **from the synergy between**
 - accurate theoretical prediction,
 - a systematic approach to the study of new effective interactions,
 - the intuition and experience of many years of Beyond SM searches!
- **Increasing the precision** of input parameters could allow to **test higher scales of new physics**: a factor of 10 in precision could give access to scales as high as 100 TeV.
- **Identifying and controlling the main sources of theoretical error** become very important for future developments.
- **Direct evidence of new physics can boost this process**, as the discovery of a Higgs-boson has prompted and guided us in this new era of LHC physics.