

Fully Differential predictions for top-quark pair production at NNLO using STRIPPER

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Arxiv: 1606.03350, 1608.00765, ...

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NNLO – Cross section

$$\sigma_{h_1 h_2}(P_1, P_2) = \sum_{ab} \int_0^1 \int_0^1 dx_1 dx_2 f_{a/h_1}(x_1, \mu_F^2) f_{b/h_2}(x_2, \mu_F^2) \hat{\sigma}_{ab}(x_1 P_1, x_2 P_2; \alpha_s(\mu_R^2), \mu_R^2, \mu_F^2)$$

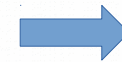
- Partonic cross section expansion in α_s at NNLO

$$\hat{\sigma}_{ab} = \hat{\sigma}_{ab}^{(0)} + \hat{\sigma}_{ab}^{(1)} + \hat{\sigma}_{ab}^{(2)}$$

- NNLO contribution

R: Real radiation
V: Virtual
C: Collinear Factorization

$$\hat{\sigma}_{ab}^{(2)} = \hat{\sigma}_{ab}^{\text{RR}} + \hat{\sigma}_{ab}^{\text{RV}} + \hat{\sigma}_{ab}^{\text{VV}} + \hat{\sigma}_{ab}^{\text{C1}} + \hat{\sigma}_{ab}^{\text{C2}}$$



Sum is Finite

Real **IR** - poles

Virtual **IR** - poles

- STRIPPER

- Subtraction scheme to consistently cancel **IR** - singularities

Subtraction/slicing schemes at NNLO

- Antenna subtraction

- $e^+e^- \rightarrow 3 \text{ jets}, pp \rightarrow 2 \text{ jets}, qq \rightarrow tt, H + \text{jet}$

[Gehrmann, GehrmannDeRidder, Glover, Heinrich '05 - '08]

[Weinzierl '08, '09]

[Currie, Gehrmann, GehrmannDeRidder, Glover, Pires, '13 -'14]

[Bernreuther, Bogner, Dekkers, '11, '14]

[Abelof, (Dekkers), GehrmannDeRidder, '11-'15]

[Abelof, GehrmannDeRidder, Maierhofer, Pozzorini, '14]

[Chen, Gehrmann, Glover, Jaquier, '15]

- Colorful subtraction

- $H \rightarrow bb, e^+e^- \rightarrow 3 \text{ jets}$

[DelDuca, Somogyi, Trocsanyi, '05 - '13]

[DelDuca, Duhr, Somogyi, Tramontano, Trocsanyi, '15]

[DelDuca et al. , '16]

- q_T – slicing

- $pp \rightarrow H, pp \rightarrow V, pp \rightarrow H + V, pp \rightarrow VV,$
 $qq \rightarrow tt$ (flavour off-diagonal)

[Catani, Grazzini, '07]

[Ferrera, Grazzini, Tramontano, '11]

[Catani, Cieri, DeFlorian, Ferrera, Grazzini, '12]

[Gehrmann, Grazzini, Kallweit, Maierhofer, Manteuffel, Rathlev, Torre, '14 -'15]

[Bonciani, Catani, Grazzini, Sargsyan, Torre; '14. '15]

- N-jettiness slicing

- $pp \rightarrow H + \text{jet}, pp \rightarrow W + \text{jet}, pp \rightarrow Z + \text{jet},$
 $pp \rightarrow H + V, pp \rightarrow \gamma\gamma$

[Gaunt, Stahlhofen, Tackmann, Walsh, '15]

[Boughezal, Focke, Giele, Liu, Petriello, '15-'16]

[Boughezal, Campbell, Ellis, Focke, Giele, Liu, Petriello, '15]

[Campbell, Ellis, Williams, '16]

Sector improved residue subtraction (STRIPPER)

SecToR Improved Phase sPacE for real Radiation

- Local subtraction scheme for NNLO (no approximations)
- First formulation [Czakon, '10, '11]
 - $pp \rightarrow tt$ [Czakon, Fiedler, Mitov; '13, '15]
(total cross section, A_{FB} at Tevatron, distributions at Tevatron) [Czakon, Fiedler, DH, Mitov; '16]
 - $pp \rightarrow H + \text{jet}$, $Z \rightarrow e^+ e^-$, Muon – decay, [Boughezal, Caola, Melnikov, Petriello, Schulze, '13 '14]
 b – decay, top – decay, single top production [Boughezal, Melnikov, Petriello, '11]
[Caola, Czernecki, Liang, Melnikov, Szafron, '14]
[Brucherseifer, Caola, Melnikov, '13, '13, '14]
- Generalization to 4 dimensions [Czakon, DH, '14]

STRIPPER – Main Idea

- Numerical cancellation of **IR** – poles between NNLO contributions
- Example: Double real radiation (most complicated)

$$\hat{\sigma}_{ab}^{\text{RR}} = \frac{1}{2\hat{s}} \frac{1}{N_{ab}} \int d\Phi_{n+2} \langle \mathcal{M}_{n+2}^{(0)} | \mathcal{M}_{n+2}^{(0)} \rangle F_{n+2}$$

1) Use selector functions to split phase space into triple and double collinear sectors

2) Use physical parametrization (angles, energies)

[Frixione, Kunszt, Signer (FKS); '95]

3) Physical sector decomposition: Factorization of non-commuting singularities

[Binoth, Heinrich; '00]

4) Generate subtraction terms

5) Laurent series in ϵ (\rightarrow numerical integration of all coefficients)

STRIPPER – General formulation

[Czakon, DH; '14]

$$\hat{\sigma}_{ab}^{(2)} = \hat{\sigma}_{ab}^{\text{RR}} + \hat{\sigma}_{ab}^{\text{RV}} + \hat{\sigma}_{ab}^{\text{VV}} + \hat{\sigma}_{ab}^{\text{C1}} + \hat{\sigma}_{ab}^{\text{C2}}$$

- Each contribution is a Laurent series in ϵ
 - Separation of independently finite contributions (check number of unresolved particles)
 - Finite contribution (all particles resolved)
 - Single unresolved $|\mathcal{M}_{n+1}^{(0)}\rangle$
 - Double unresolved $|\mathcal{M}_n^{(0)}\rangle$
 - Finite Remainder $|\mathcal{F}_n^{(1)}\rangle = |\mathcal{M}_n^{(1)}\rangle - \mathbf{Z}^{(1)}|\mathcal{M}_n^{(0)}\rangle$
- $$\hat{\sigma}_{\text{F}}^{\text{RR}}, \quad \hat{\sigma}_{\text{F}}^{\text{RV}}, \quad \hat{\sigma}_{\text{F}}^{\text{VV}}, \quad \hat{\sigma}_{\text{FR}} = \hat{\sigma}_{\text{FR}}^{\text{RV}} + \hat{\sigma}_{\text{FR}}^{\text{VV}} + \hat{\sigma}_{\text{FR}}^{\text{C2}},$$

$$\hat{\sigma}_{\text{SU}} = \hat{\sigma}_{\text{SU}}^{\text{RR}} + \hat{\sigma}_{\text{SU}}^{\text{RV}} + \hat{\sigma}_{\text{SU}}^{\text{C1}}, \quad \hat{\sigma}_{\text{DU}} = \hat{\sigma}_{\text{DU}}^{\text{RR}} + \hat{\sigma}_{\text{DU}}^{\text{RV}} + \hat{\sigma}_{\text{DU}}^{\text{VV}} + \hat{\sigma}_{\text{DU}}^{\text{C1}} + \hat{\sigma}_{\text{DU}}^{\text{C2}}$$
- Make sure that SU and DU cancel independently (\rightarrow resolved particles in 4 dimensions)

Differential top-quark pair production at NNLO

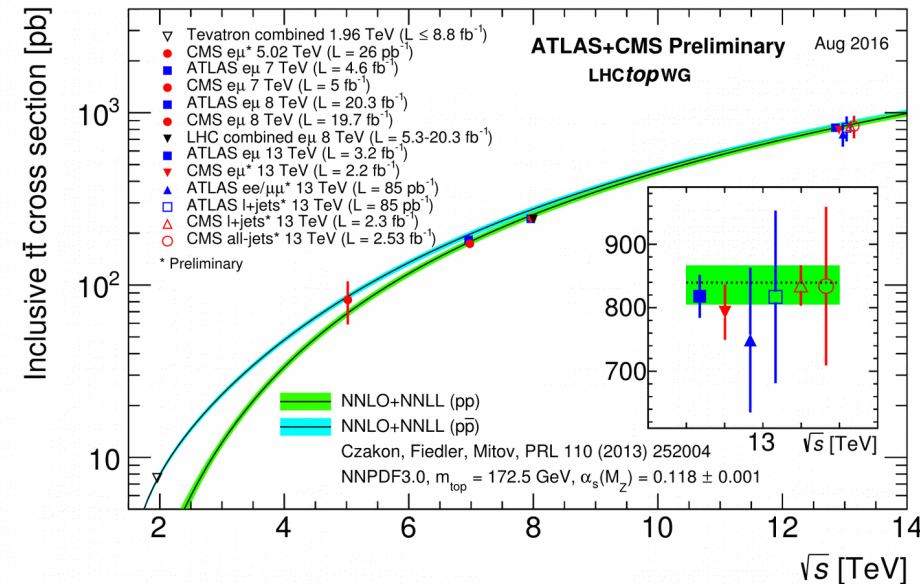
[Czakon, DH, Mitov; 2015, 2016]

Top-quark pairs at the LHC

- Total cross section measured ($\sim 7\%$)
 $\sigma_{t\bar{t}}(13\text{ TeV}) \approx (800 \pm 50)\text{pb}$
- Uncertainty of the prediction
 - LO (30%) \rightarrow NLO (15%) \rightarrow NNLO + NNLL (5%)

\rightarrow Percent - level precision required

- Precision tests of the Standard Model
- Background for many searches and processes (Higgs, New Physics,...)
- Constrain gluon PDF at high x
- ...



Scale dependence and best scale choice

[Czakon, DH, Mitov; 2016]

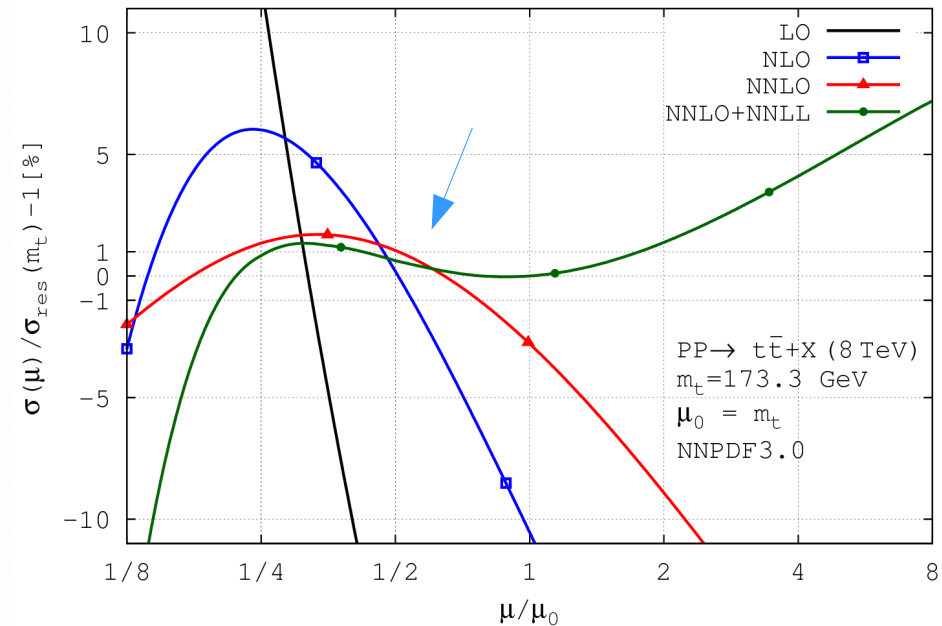
$$\sigma_{h_1 h_2}(P_1, P_2) = \sum_{ab} \int_0^1 \int_0^1 dx_1 dx_2 f_{a/h_1}(x_1, \mu_F^2) f_{b/h_2}(x_2, \mu_F^2) \hat{\sigma}_{ab}(x_1 P_1, x_2 P_2; \alpha_s(\mu_R^2), \mu_R^2, \mu_F^2)$$

- What is the “best” (dynamical) scale?
 - Difference between different dynamical scales could be as large as difference between dynamical scale and fixed scale
 - Precision predictions only possible for deliberately chosen scale
 - Comparative study of perturbative convergence based on different scales
- Selection of the “correct” scale is based on the following criteria:
 - Perturbative convergence for both total and differential cross section
 - Limiting behavior: Low p_T (m_{tt}): $\sim m_{top}$ \leftrightarrow High p_T (m_{tt}): $\sim p_T$
 - Restriction to simple functional forms studied in the past (H_T, m_{tt}, \dots)

Scale dependence – Total cross section

[Czakon, DH, Mitov; 2016]

- Look for convergence
 - Scale value which minimizes difference
 - $\text{NLO} \rightarrow \text{NNLO} \rightarrow (\text{NNLO} + \text{NNLL})$
 - Best convergence: $\mu_0 < m_{\text{top}}$
 - Little dependence on PDFset at NNLO



- Value of NNLO cross section at point of best convergence equals the NNLO+NNLL at the usual canonical scale $\mu_0 = m_{\text{top}}$
 - Therefore: Resummation has negligible impact on the total cross section at the point of fastest convergence

Scale dependence – Differential Distributions

[Czakon, DH, Mitov; 2016]

- Main guidance is perturbative convergence to discriminate between scales

- Invariant mass distribution

$$\mu_0 = H_T/4 \quad \checkmark$$

$$H_T = \sqrt{m_t^2 + p_{Tt}^2} + \sqrt{m_{\bar{t}}^2 + p_{T\bar{t}}^2}$$

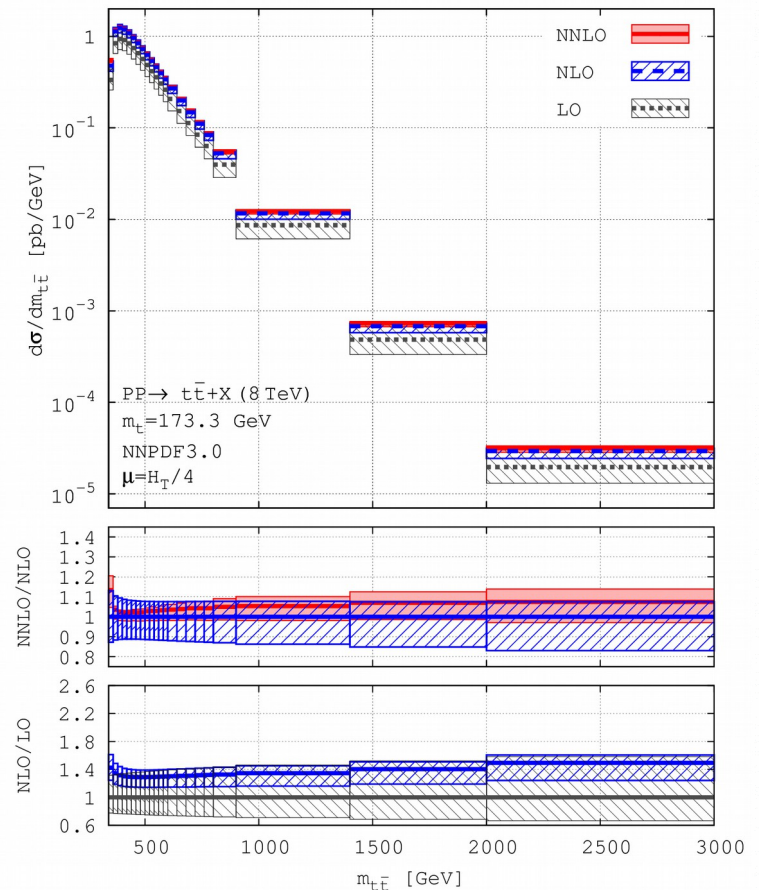
- Limiting behaviour

$$\mu_0(p_T \rightarrow 0) \rightarrow m_t/2$$

$$\mu_0(p_T \rightarrow \infty) \rightarrow (p_{T,t} + p_{T,\bar{t}})/4$$

- Scales based on the invariant mass itself

$$\mu \propto m_{t\bar{t}} \quad \times$$



Scale dependence – Differential Distributions

[Czakon, DH, Mitov; 2016]

- Main guidance is perturbative convergence to discriminate between scales

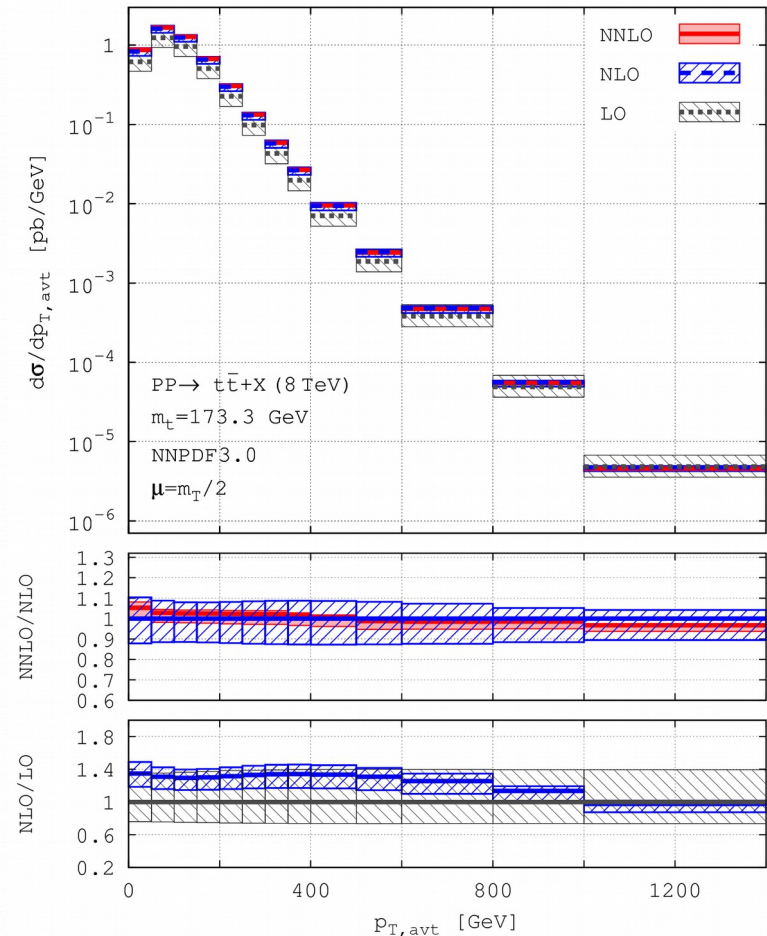
- Choose individual scales for top and antitop p_T
- Transverse mass scale

$$\mu_0 = \frac{1}{2}m_T(t/\bar{t}) = \frac{1}{2}\sqrt{m_t^2 + p_{T,t/\bar{t}}^2}$$

- Average distributions afterwards



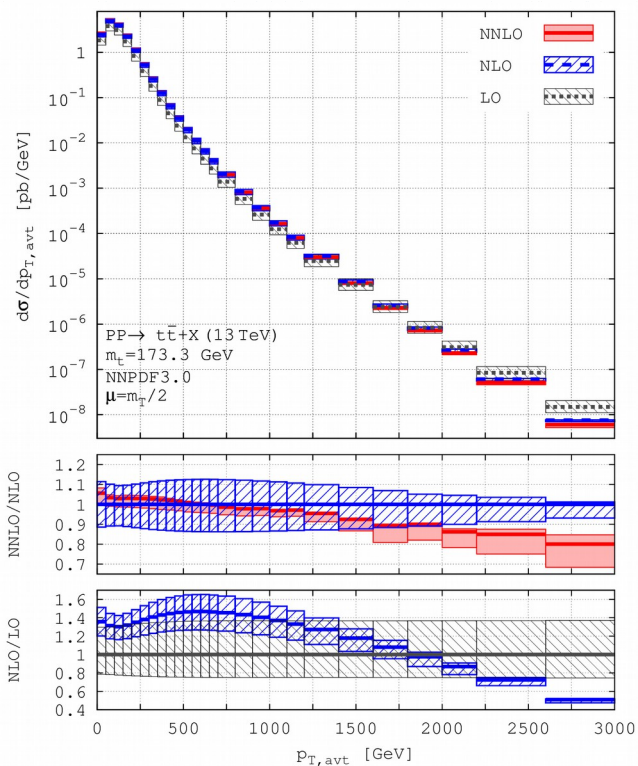
Different scale choices for different observables



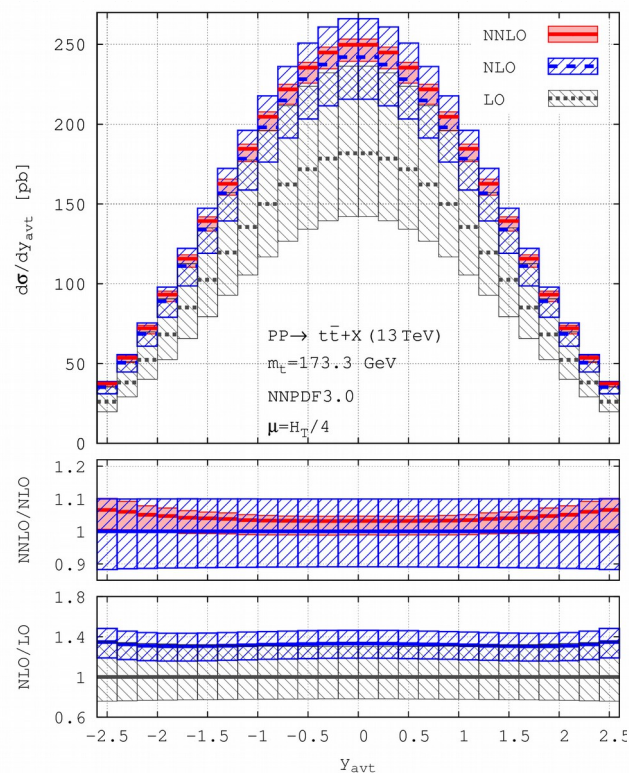
Differential Distributions @ 13 TeV

[Czakon, DH, Mitov; 2016]

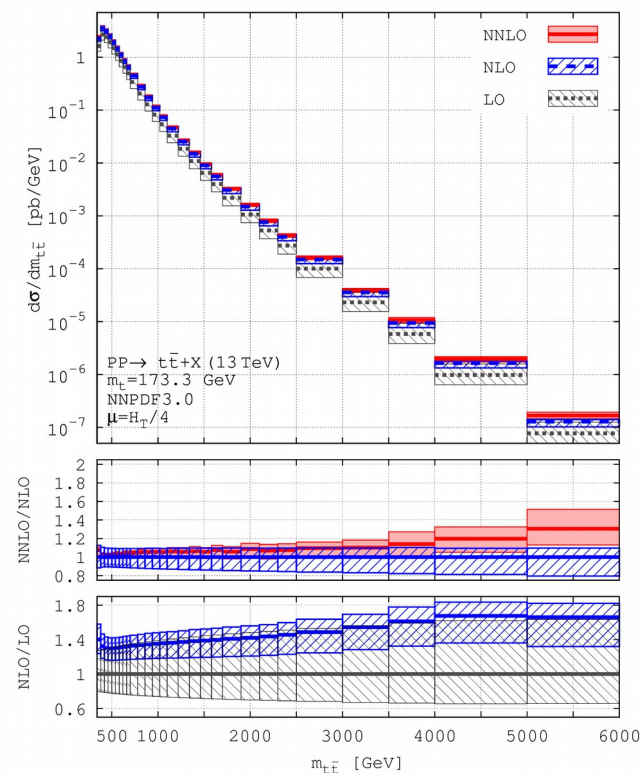
PT of the top



Rapidity of the top



Invariant mass



Dynamical scales → extended kinematical regime

- Comparison with data → Good agreement

Bump hunting in top-pair events (Example: 750 GeV)

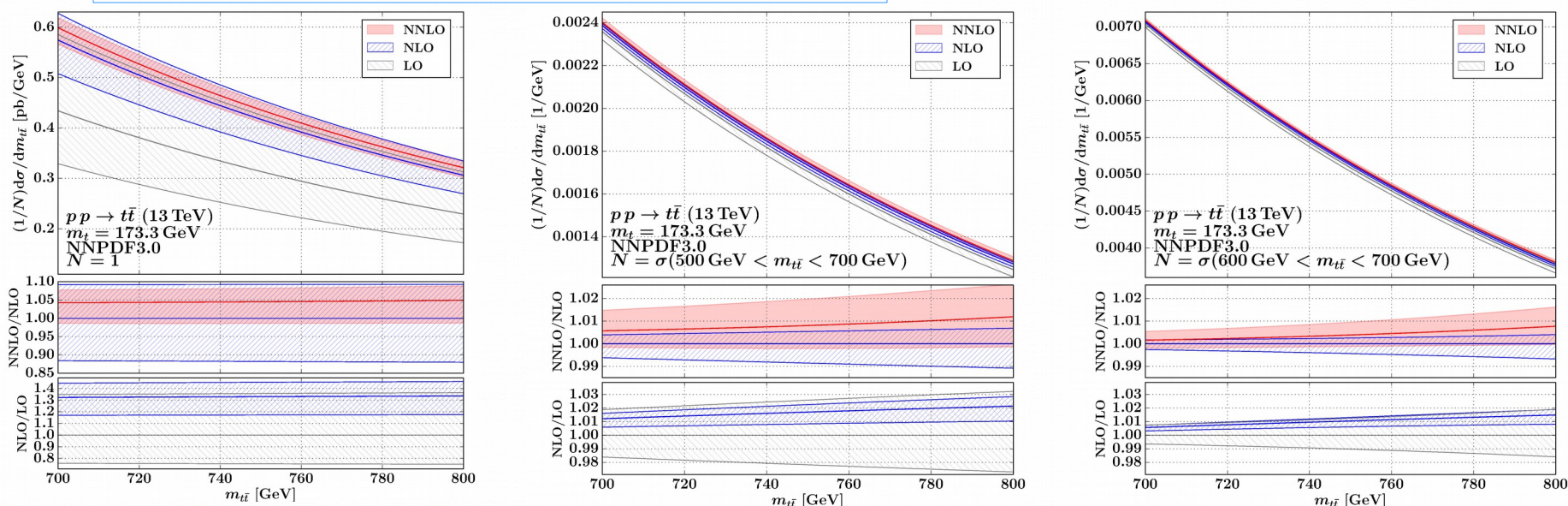
[Czakon,DH, Mitov; 2016]

Bumps in top-pair invariant mass distribution

[Czakon, DH, Mitov; 2016]

- Minimize theory uncertainty \rightarrow choose appropriate normalization

NNLO scale + (approx.) PDF uncertainty added in quadrature

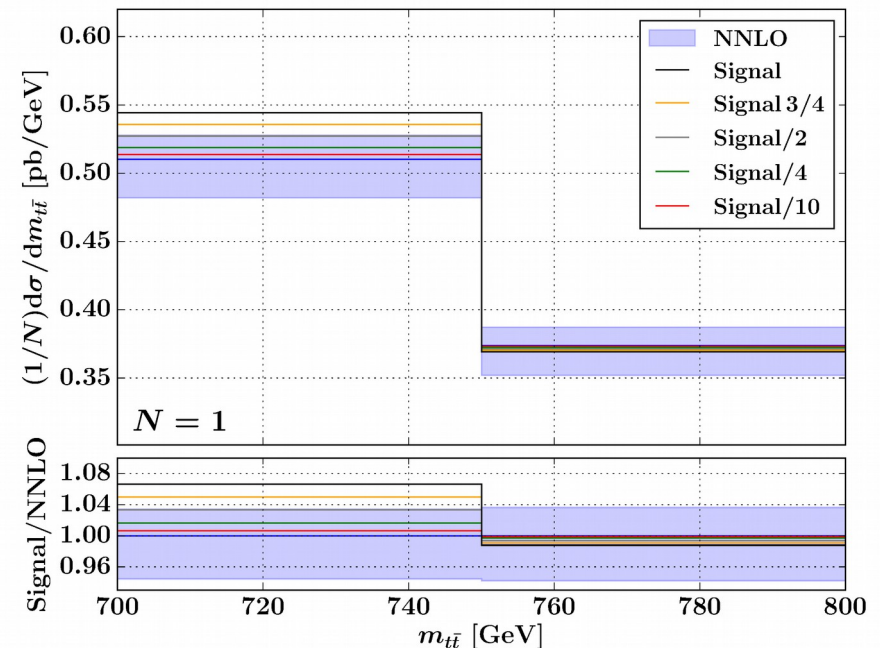
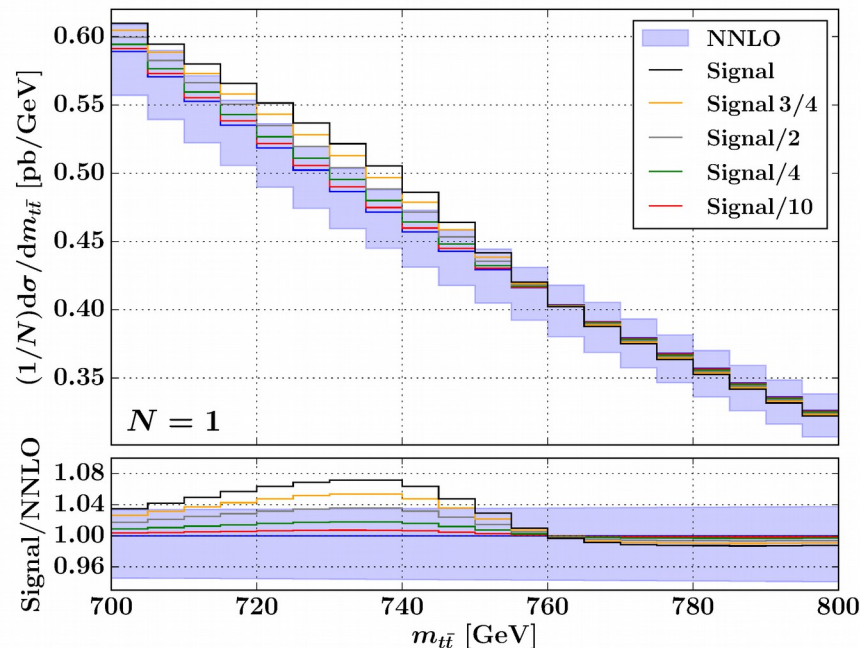


- Trade off between experimental uncertainty and theory uncertainty to choose N
- Minimize dependence on the top-mass $\ll 1\%$, checked at NLO
- Analytic fit of the distribution allows flexible rebinning

Bumps in top-pair invariant mass distribution

[Czakon, DH, Mitov; 2016]

- Discriminate Signal from Background

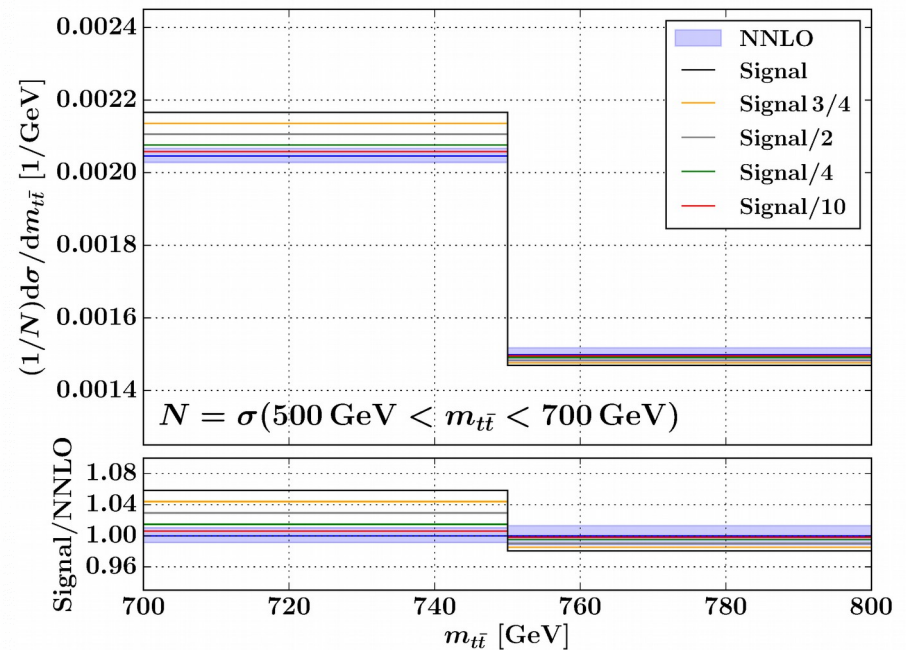
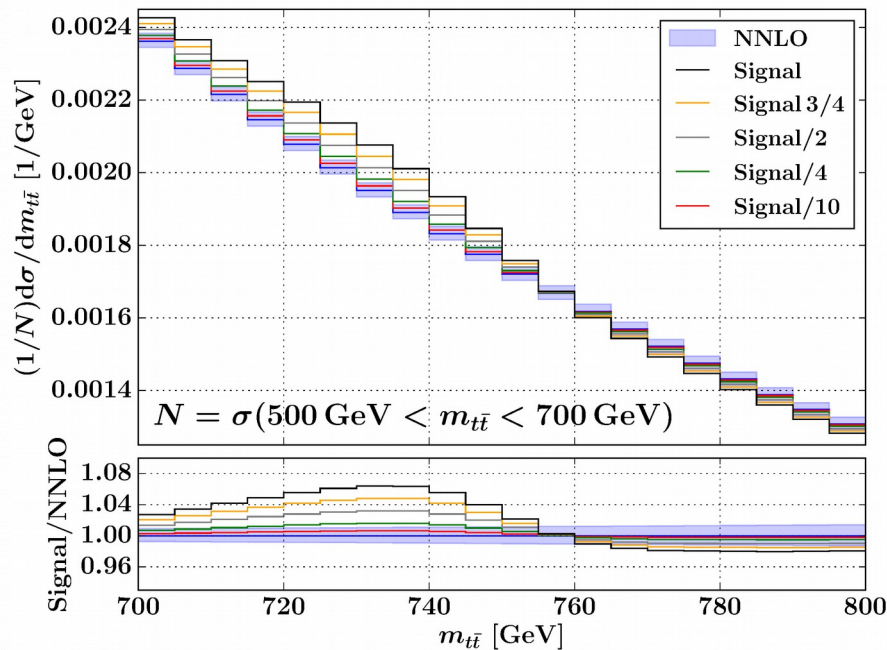


- Signal Model (BSM) from [Hespel, Maltoni, Vryonidou 2016] \rightarrow 1.1 pb
- Significance depends on the bin-width

Bumps in top-pair invariant mass distribution

[Czakon, DH, Mitov; 2016]

- Discriminate Signal from Background

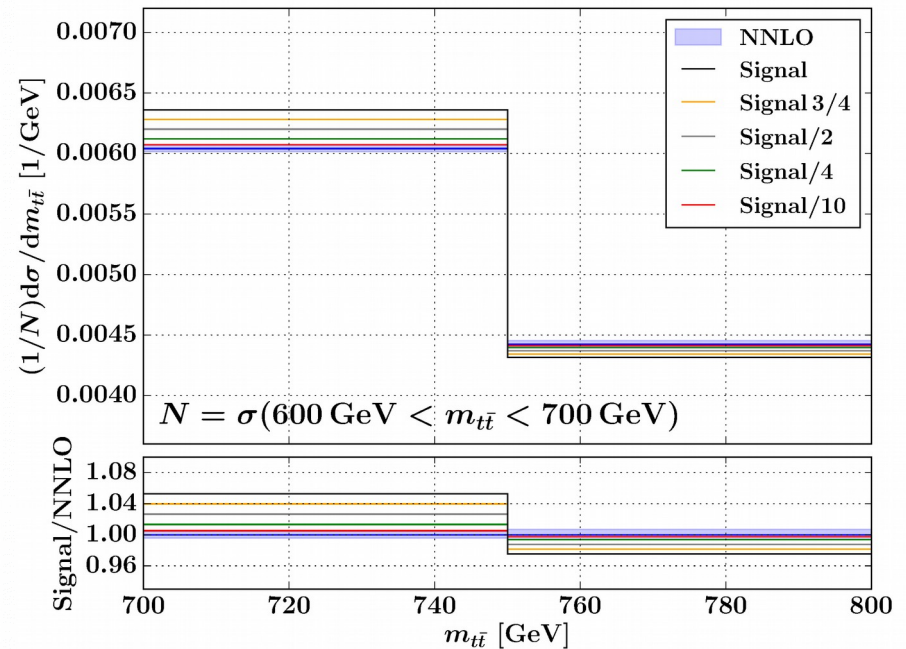
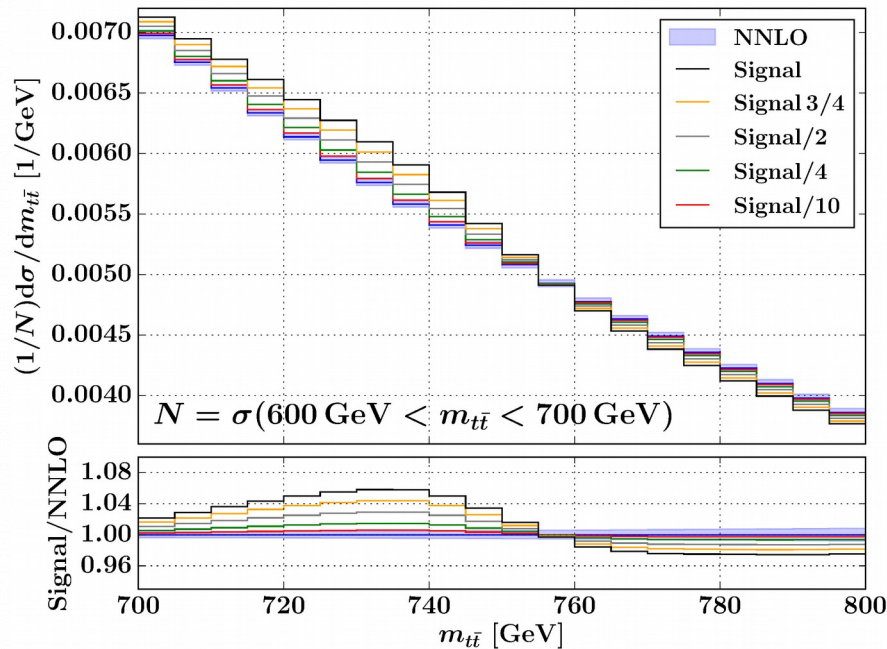


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Bumps in top-pair invariant mass distribution

[Czakon, DH, Mitov; 2016]

- Discriminate Signal from Background



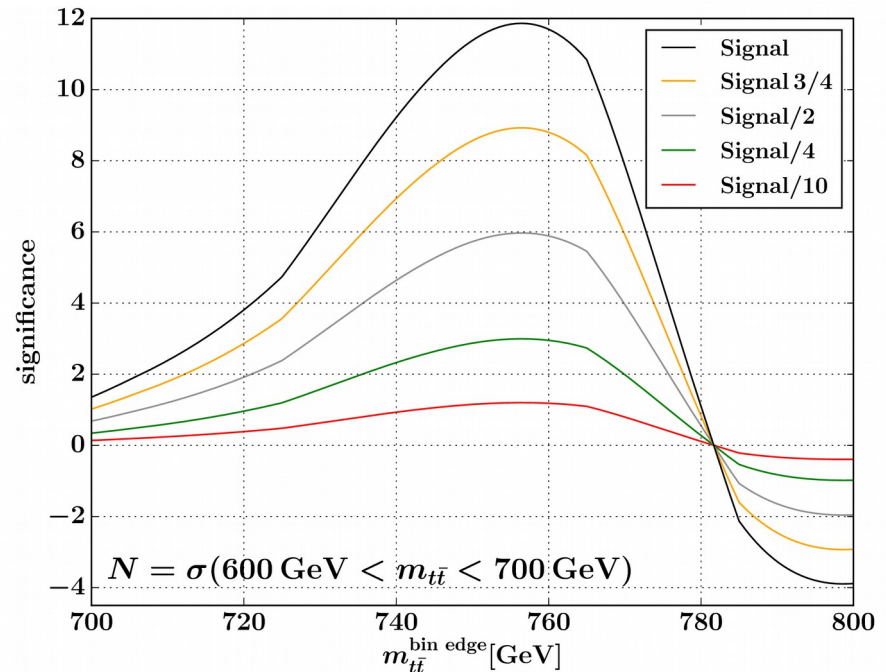
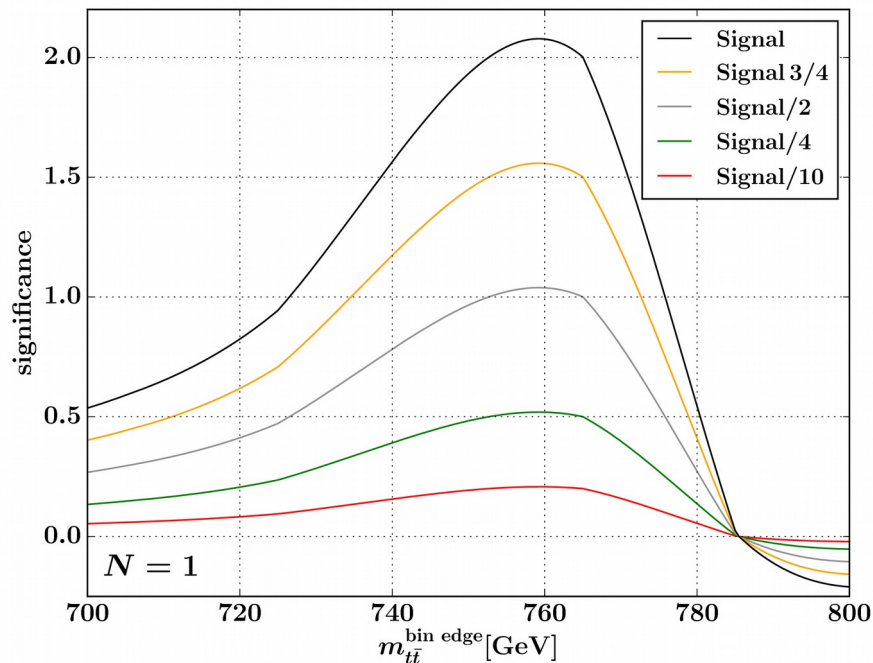
- Signal Model (BSM) from [Hespel, Maltoni, Vryonidou 2016] $\rightarrow 1.1 \text{ pb}$
- Significance depends on the bin-width

Bumps in top-pair invariant mass

[Czakon, DH, Mitov; 2016]

- Discriminate Signal from Background
 - Significance depends on the position of the bin as well

$$\text{significance} = \frac{(\text{SM} + \text{BSM})_{\text{central}} - (\text{pure SM})_{\text{central}}}{(\text{pure SM})_{\text{error}}}$$



Summary and Outlook

- Implementation of the Sector improved residue subtraction (STRIPPER)
- Applied to differential top-quark pair productions
 - High quality predictions for LHC at 8 TeV and 13 TeV
 - Precision could be used for new physics searches (Example at 750 GeV)
- Outlook
 - Combine NNLO-QCD with NLO-EW (published soon, in collaboration with Pagani, Tsinikos and Zaro)
 - Include top-quark decays at NNLO

Back Up Slides

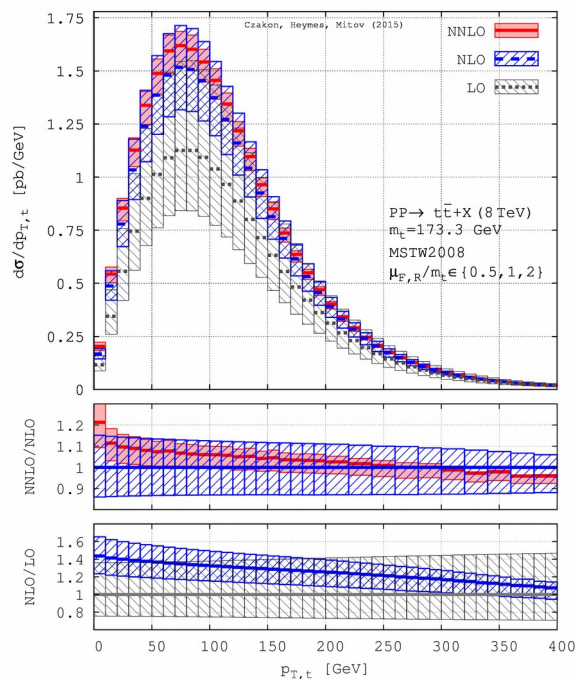
STRIPPER - Implementation

- General purpose event generator for NNLO computation
- Based on four-dimensional formulation of the subtraction scheme
- Complete independent implementation
- SM tree-level matrix elements are included [vanHameren, Bury; '09, '15]
- **Process independent:** User has to interface the one-loop and two-loop **finite** contributions
- **Speed:** Monte Carlo over processes and polarizations
- Simultaneous computation of:
 - Different PDF sets (LHAPDF interface)
 - Different renormalization and factorizations scales
 - Different observables

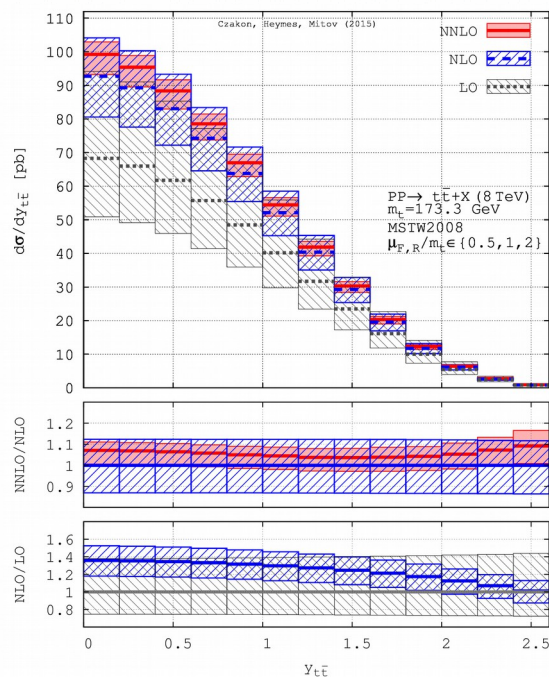
Differential Distributions @ 8 TeV

[Czakon, DH, Mitov; published 2015]

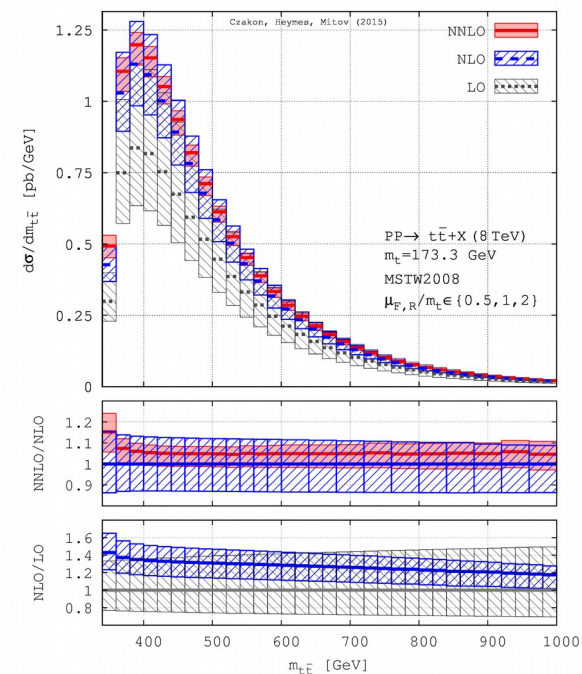
P_T of the top



Rapidity of the top-pair



Invariant mass

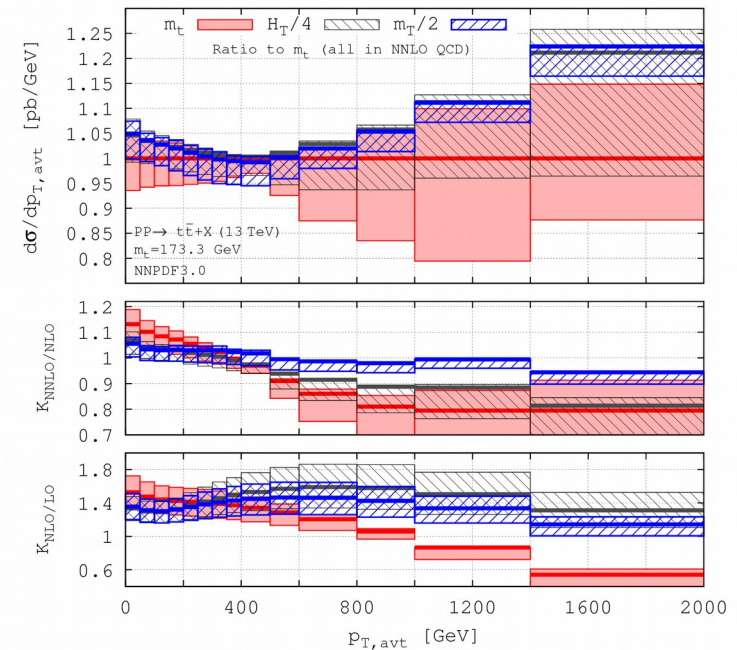


- NNLO has important impact (Good perturbative convergence)
- Good agreement with data → [CMS 2015, ATLAS 2015]
- **However:** Results with fixed scales applicable only to limited kinematical range

Scale dependence – Differential Distributions

[Czakon, DH, Mitov; 2016]

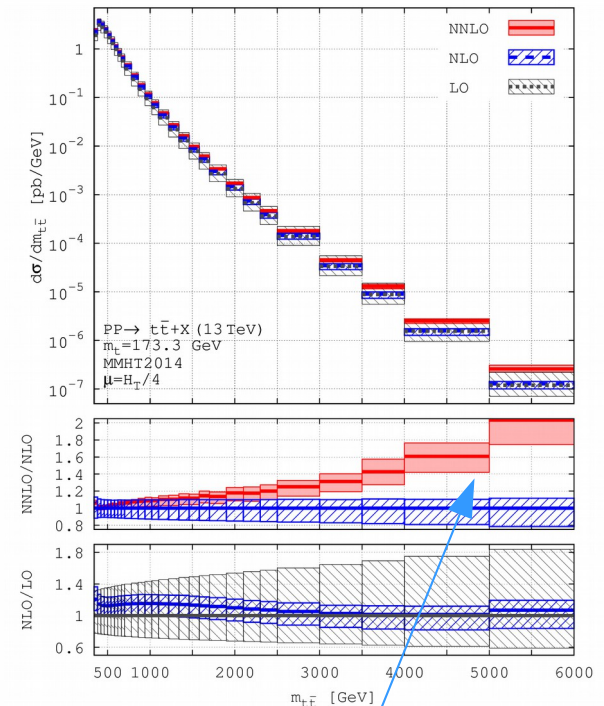
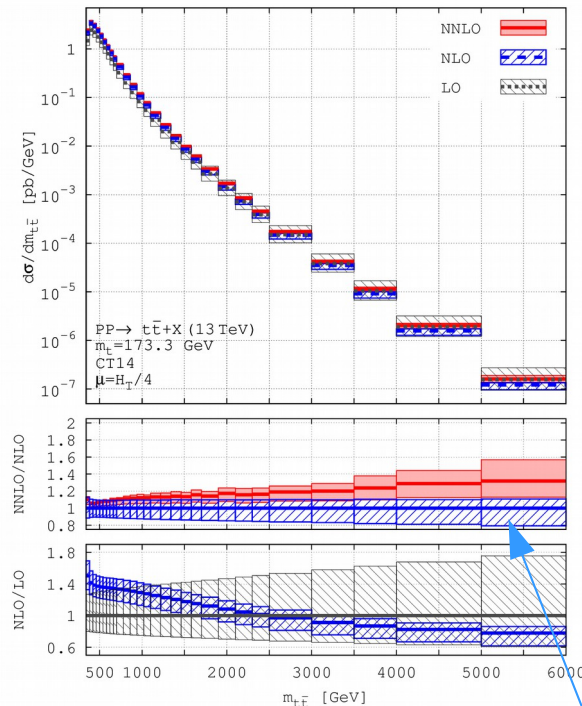
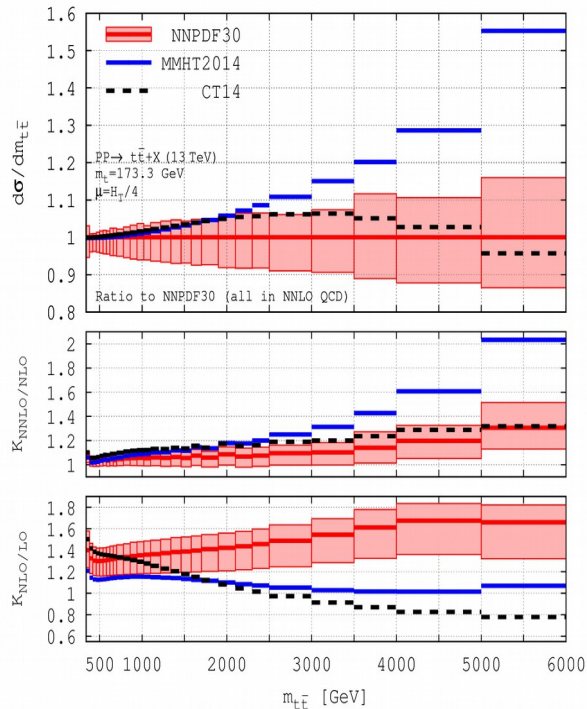
- Comparison between different scale choices
 - Difference within uncertainty
 - Main impact on scale dependence at high values and the K-factor
- Independence of PDF sets has been checked



Differential Distributions @ 13 TeV

[Czakon, DH, Mitov; 2016]

- PDF - dependence



Large PDF error in the multi TeV region

- Useful to constrain PDF sets