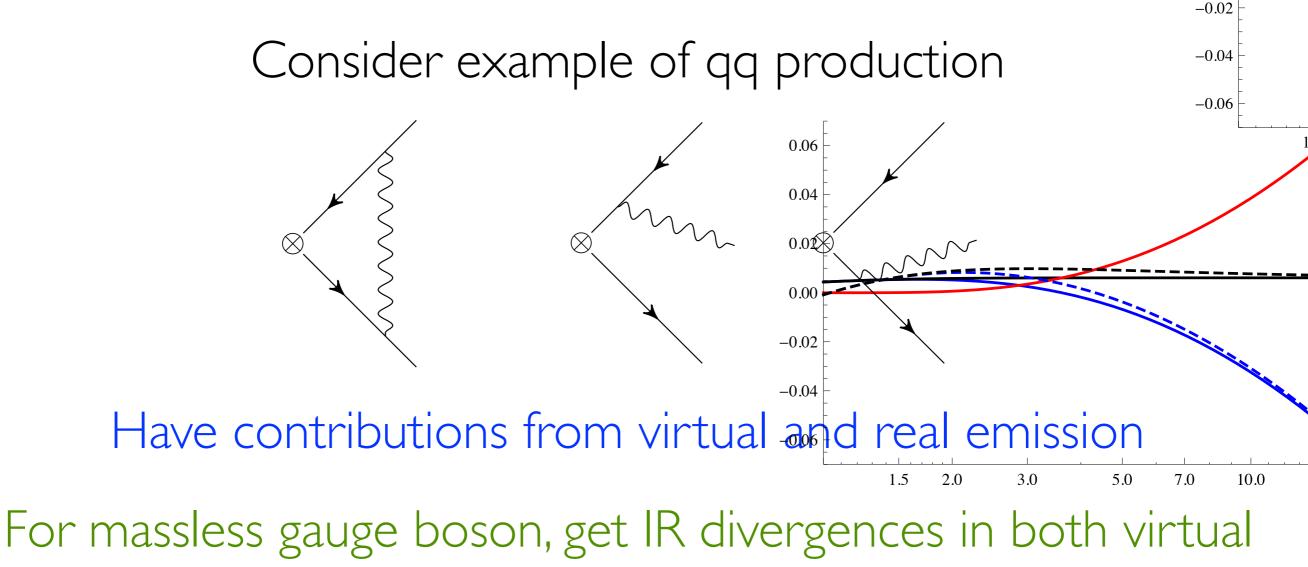
Resummation of EW Sudakov logarithms for real radiation

Work in collaboration with Nicolas Ferland 1601.07190 (JHEP)

Electroweak Sudakov logarithms arise from exchanges of electroweak gauge bosons



and real that cancel by KLN

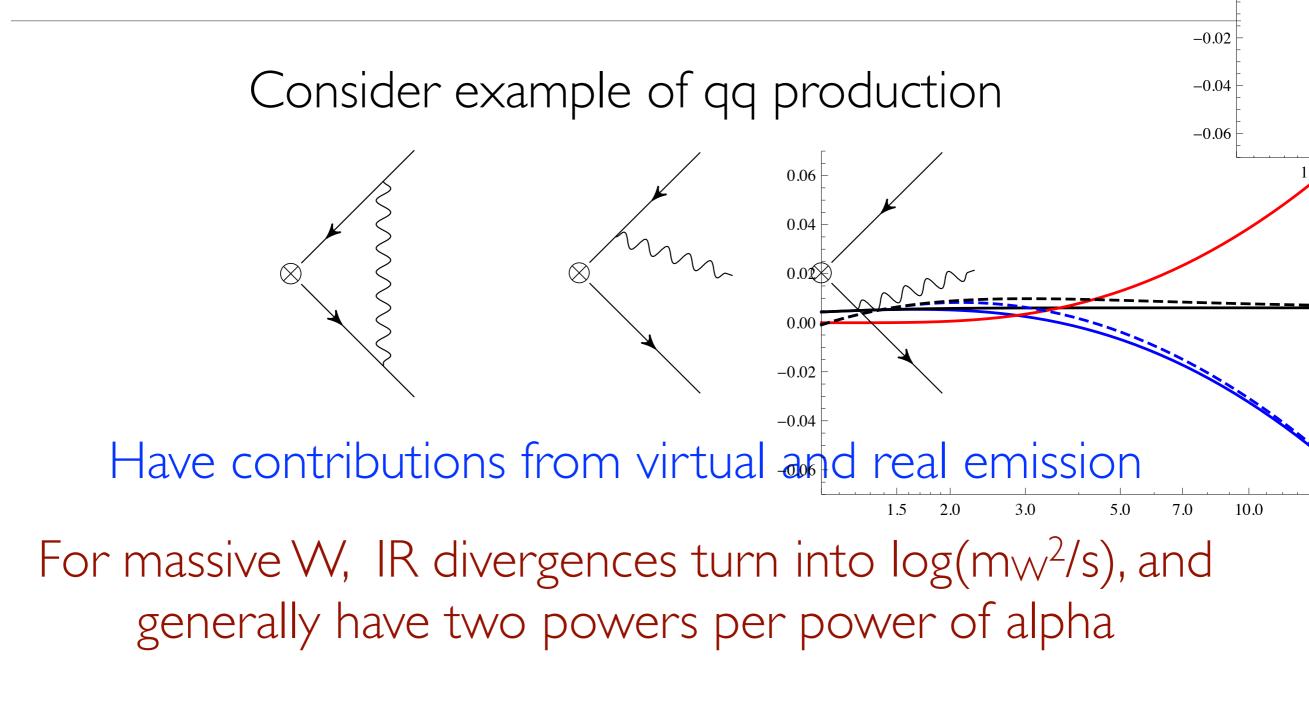
0.06

0.04

0.02

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Electroweak Sudakov logarithms arise from exchanges of electroweak gauge bosons



Both virtual and real sensitive to $log(m_W^2/s)$

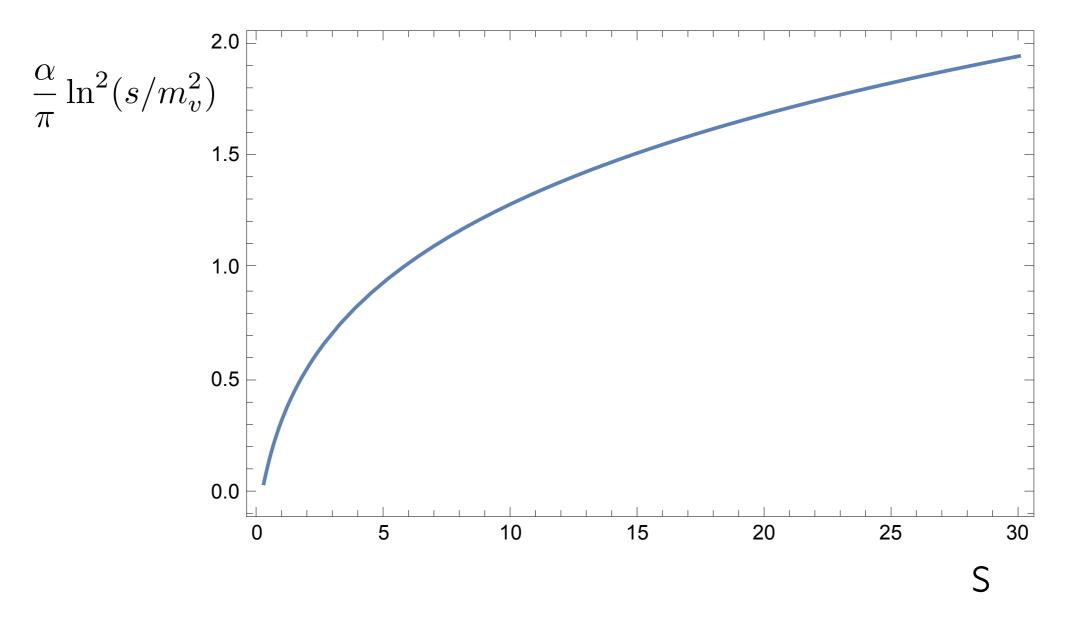
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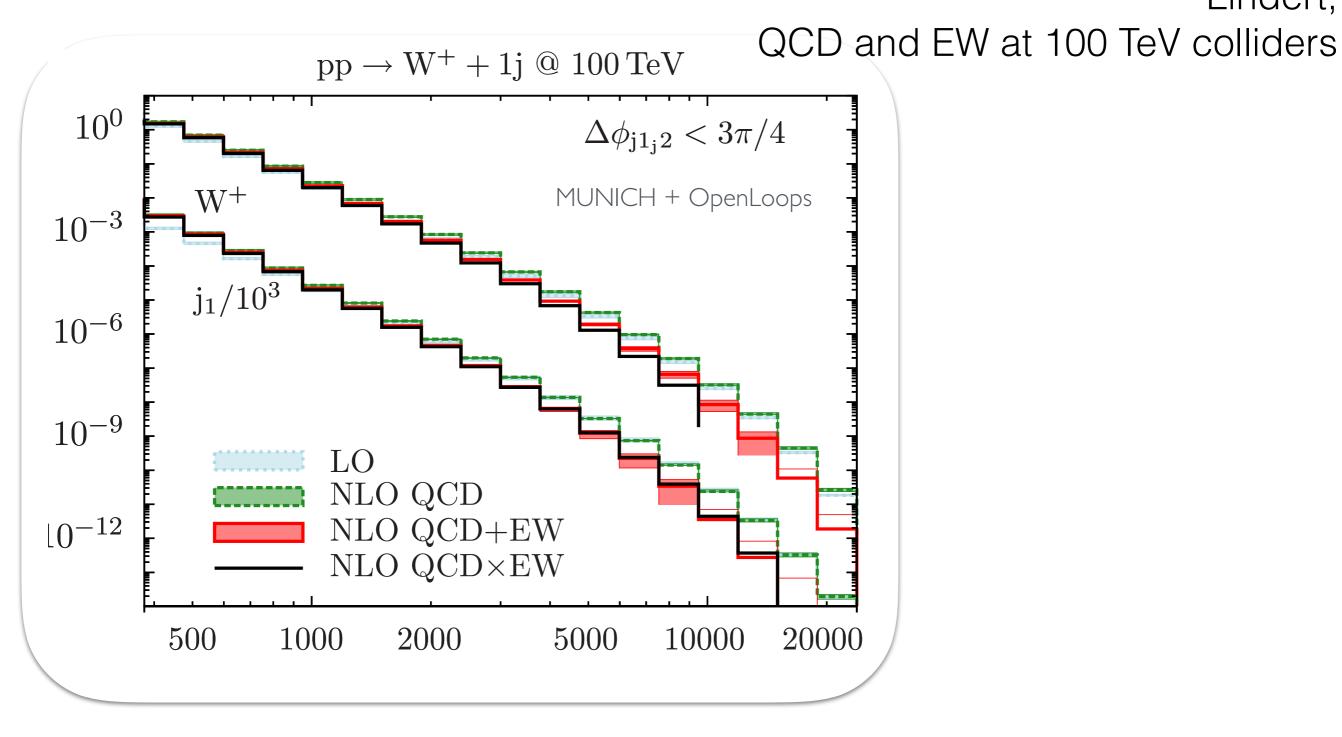
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The numerical effect of EW Sudakov logarithms becomes large at high energies



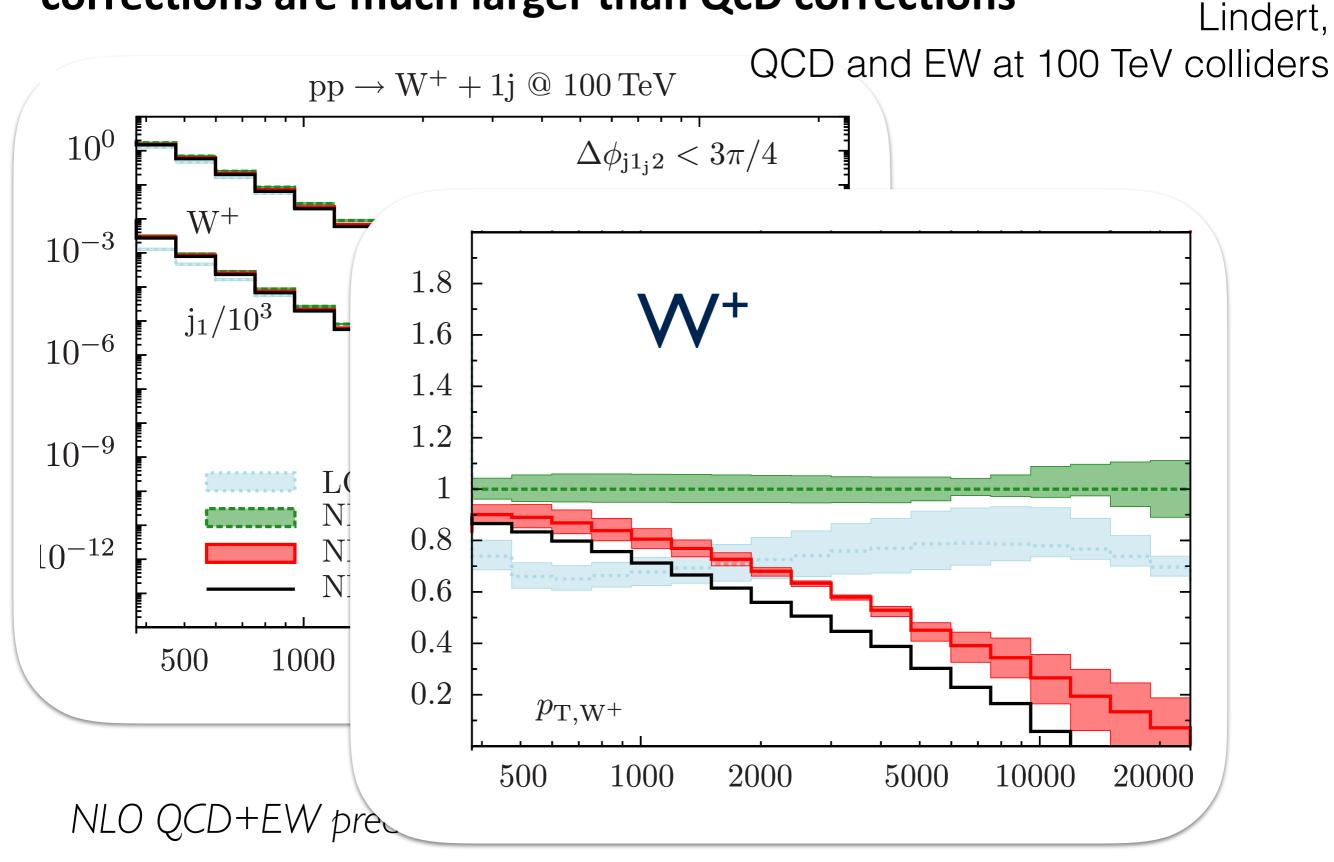
No sense in which electroweak corrections are small

Fixed order results at a future 100 TeV machine show that EW corrections are much larger than QcD corrections Lindert,



NLO QCD+EW predictions for W+jets at 100 TeV

Fixed order results at a future 100 TeV machine show that EW corrections are much larger than QcD corrections



The cancellation between virtual and real corrections is very different from the usual story in QCD

Look at "Drell-Yan" production and keep onto terms with α_2 . The coefficient of Log²(m_V²/s)/4 π is

	V	R	V+R
uu	$2/3 \alpha_2^2$	- α_2^2	$-1/3 \alpha_2^2$
dd	$2/3 \alpha_2^2$	- α_2^2	- Ι/3 α ₂ ²
ud	4/3 α ₂ ²	- α_2^2	$1/3 \alpha_2^2$
du	4/3 α ₂ ²	- α_2^2	$1/3 \alpha_2^2$
sum	4 α_2^2	- 4 α ₂ ²	0

Cancellation for completely inclusive observables (KLN)

The cancellation between virtual and real corrections is very different from the usual story in QCD

Look at "Drell-Yan" production and keep onto terms with α_2 . The double logarithmic terms are

	V	R	V+R
uu	$2/3 \alpha_2^2$	- α_2^2	-1/3 α ₂ 2
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du	4/3 α_2^2	- α_2^2	$1/3 \alpha_2^2$
sum	4 α_2^2	- 4 α_2^2	0

Cancellation only happens if we include both real and virtual corrections, and average over initial states

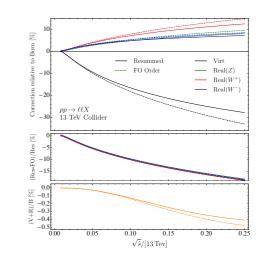
- I. Most experimental analyses are not inclusive over final states
- 2. Averaging over initial states is impossible, since beams (pdf's) are not SU(2) symmetric



Review of resummed virtual



Resummation of the real



Results



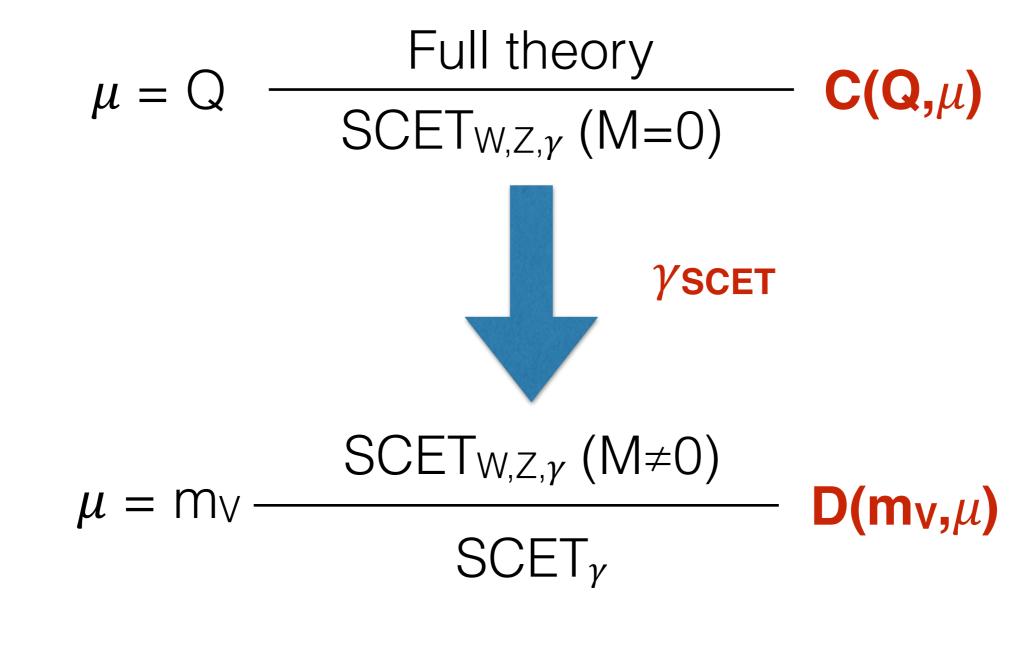
Kuhn, Penin, Smirnov ('95) Ciafaloni, Comelli ('99, '00) Fadin, Lipton, Martin, Melles ('00) Denner, Pozzorini ('91)

Logarithms arise from collinear and soft "divergences" in loop diagrams

These "divergences" are regulated by the mass of the vector boson

Can be resummed using standard SCET RGE running

Chiu, Golf, Kelley, Manohar, ('08)



Problem is completely solved at NLL' for any process

For Drell-Yan production, 7 operators in $SCET_{Z,W,\gamma}$

$$\mathcal{L} = C_{QLT} Q^T L^T + C_{QLS} Q^S L^S + C_{ULS} U^S L^S + C_{DLS} D^S L^S + C_{QES} Q^S E^S + C_{UES} U^S E^S + C_{DES} D^S E^S ,$$

with

$$F^S = \bar{F}\gamma^{\mu}F, \qquad F^T = \bar{F}\tau^a\gamma^{\mu}F$$

Q, L : left handed quark and lepton doublets U, D, E : right handed u, d, e fields

$$\mathcal{L} = C_{QLT} Q^T L^T + C_{QLS} Q^S L^S + C_{ULS} U^S L^S + C_{DLS} D^S L^S + C_{QES} Q^S E^S + C_{UES} U^S E^S + C_{DES} D^S E^S ,$$

	NLL'	LL
C(Q ,μ)	1-loop	tree
D(m ν,μ)	1-loop	tree
γ (Q, μ)	2-loop cusp 1-loop non-cusp op mixing	1-loop cusp no op mixing

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Matching onto SCET $sC_{QLT}^{(0)}(Q) = 4\pi\alpha_2$ $sC_{IFS}^{(0)}(Q) = 4\pi\alpha_1 Y_I Y_F$

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Running in SCET

$$\gamma_i(\mu) = \Gamma_i \log \frac{\mu^2}{s}$$

$$\Gamma_i = \sum_j \left[\frac{\alpha_1}{\pi} Y_j^2 + \frac{\alpha_2}{\pi} T_j^2 - \frac{\alpha_{\rm em}}{\pi} Q_j^2 \right]_i$$

$$\mathcal{L} = C_{QLT} Q^T L^T + C_{QLS} Q^S L^S + C_{ULS} U^S L^S + C_{DLS} D^S L^S + C_{QES} Q^S E^S + C_{UES} U^S E^S + C_{DES} D^S E^S ,$$

Matching onto SCET Running in SCET

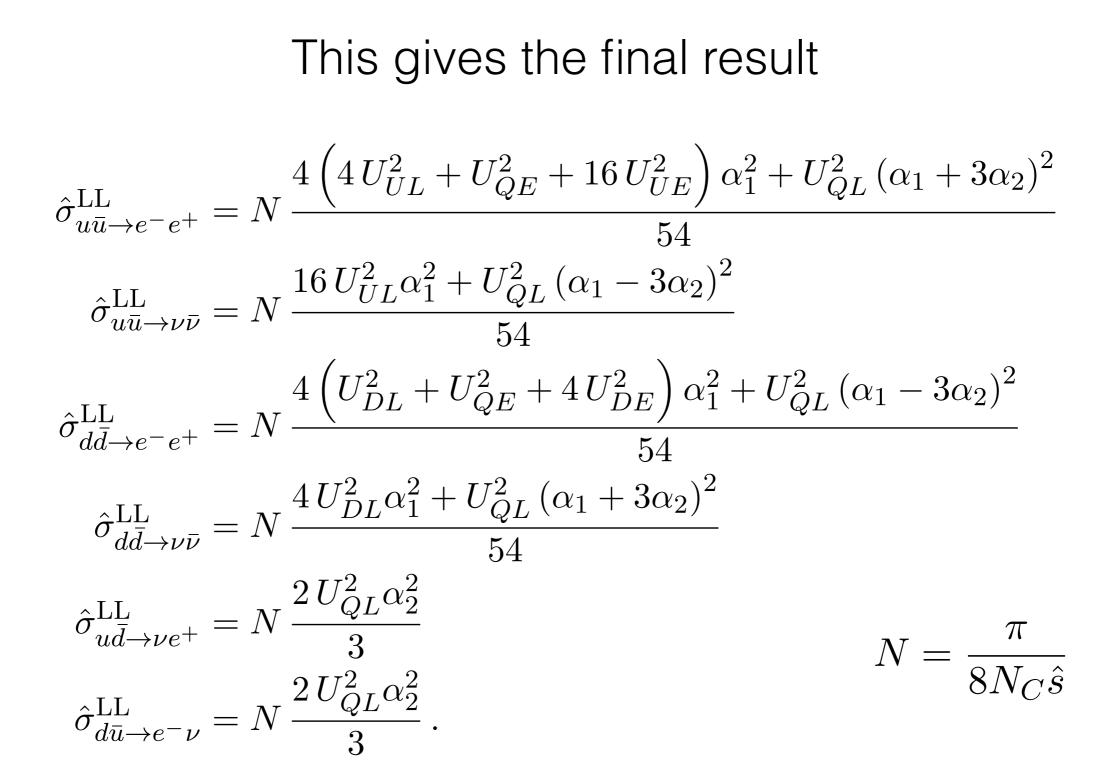
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Summation of logarithms

$$C_i(m_V) = U_i^{\text{LL}}(m_V, Q)C_iQ)$$
$$U_i^{\text{LL}}(m_V, Q) = \exp\left[-\Gamma_i \log^2 \frac{m_V}{Q}\right]$$





Fadin, Lipton, Martin, Melles ('00) Baur ('06)

There are good arguments that the resummation of the real is not as important as that of the virtual

W emission rates from jets Slide from M. Mangano at CERN workshop on 100 TeV 0.4 $\sigma(jj+nW)/\sigma(jj+(n-1)W) = \sigma(jjW)/\sigma(jj)$ with $max[p_T(jet)] > p_{T,min}$ 0.3 $\sigma(jjWW)/\sigma(jjW)$ 0.2 $\sigma(jjWWW)/\sigma(jjWW)$ 0.1 0.0 5 15 20 10 $\mathbf{0}$ $p_{T,min}$ (TeV)

Conclusion: substantial increase of W production at large energy, but W-emission probability small enough that fixed-order PT is likely the most reliable way to model rates and kinematics

But real radiation of W and Z bosons has double logarithmic sensitivity, just as the virtual corrections

For completely SU(2) symmetric observables (for example production with gg in initial state) the sum over all real emissions has the same logarithms as virtual corrections

A priori no reason why real double logarithmic sensitivity should be less for real than for virtual

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For completely SU(2) symmetric observables (for example production with gg in initial state) the sum over all real emissions has the same logarithms as virtual corrections

A priori no reason why real double logarithmic sensitivity should be less for real than for virtual

Very important to understand EW Sudakov logarithms for real radiation

Let's first rewrite the virtual corrections for a pure SU(2) theory

$$\hat{\sigma}_{q_1^H q_2^H \to \ell_1^H \ell_2^H}^{\text{LL}} = \hat{\sigma}_{q_1^H q_2^H \to \ell_1^H \ell_2^H}^B \Delta_{q_1^H q_2^H \ell_1^H \ell_2^H}^{\text{SU}(2)} \left(m_V^2, s; s \right)$$

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Born cross-section

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no-branching of 4f system between s and my²

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Born cross-section Born cross-section no-branching of 4f system between s and m_{V}^{2}

0

The expressions can easily be written down explicitly

$$\hat{\sigma}_{q^{H}q^{H} \to \ell^{H}\ell^{H}}^{B} = N \frac{8\alpha_{2}^{2}\left(T_{q^{H}}^{3}T_{\ell^{H}}^{3}\right)^{2}}{3} \qquad \hat{\sigma}_{q_{1}^{L}q_{2}^{L} \to \ell_{1}^{L}\ell_{2}^{L}}^{B} = N \frac{2\alpha_{2}^{2}}{3}$$

$$\Delta_{q_{1}^{H}q_{2}^{H}\ell_{1}^{H}\ell_{2}^{H}}^{SU(2)}\left(m_{V}^{2}, s; s\right) = \exp\left[-\frac{A_{q_{1}^{H}q_{1}^{H}\ell_{1}^{H}\ell_{2}^{H}}{2}\ln^{2}\frac{m_{V}^{2}}{s}\right] \qquad A_{q_{1}^{H}q_{1}^{H}\ell_{1}^{H}\ell_{2}^{H}}^{SU(2)} = \frac{\alpha_{2}}{2\pi}\sum_{i}T_{i}^{2}$$

$$\hat{\sigma}_{q_1^H q_2^H \to \ell_1^H \ell_2^H}^{\text{LL}} = \hat{\sigma}_{q_1^H q_2^H \to \ell_1^H \ell_2^H}^B \Delta_{q_1^H q_2^H \ell_1^H \ell_2^H}^{\text{SU}(2)} \left(m_V^2, s; s \right)$$

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This is precisely the result how a parton shower would predict an exclusive (no extra V radiation) DY cross-section

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Exclusive = Born x (no-branching Prob)

Since emission of massive V has resolution t > m_V^2 no branching probability (Sudakov) is from s=Q² to m_V^2

From a no-branching probability one can of course derive a branching probability

$$P_{\rm br}(m_V^2, s) = 1 - P_{\rm no-br}(m_V^2, s)$$

from which one can write

$$\hat{\sigma}_{q_1^H q_2^H \to \ell_1^H \ell_2^H + nV}^{\text{LL}} = \hat{\sigma}_{q_1^H q_2^H \to \ell_1^H \ell_2^H}^B \left[1 - \Delta_{q_1^H q_2^H \ell_1^H \ell_2^H}^{\text{SU}(2)} \left(m_V^2, s; s \right) \right]$$

The probability to emit a gauge boson with resolution t is

$$\hat{\sigma}_{q_{1}^{H}q_{2}^{H} \to \ell_{1}^{H}\ell_{2}^{H} + nV}^{\text{LL}} = \hat{\sigma}_{q_{1}^{H}q_{2}^{H} \to \ell_{1}^{H}\ell_{2}^{H}}^{B} \int_{m_{V}^{2}}^{s} \mathrm{d}k_{T}^{2} \frac{\mathrm{d}}{\mathrm{d}k_{T}^{2}} \Delta_{q_{1}^{H}q_{2}^{H}\ell_{1}^{H}\ell_{2}^{H}}^{\text{SU}(2)} \left(k_{T}^{2}, s; s\right)$$

$$\hat{\sigma}_{q_1^H q_2^H \to \ell_1^H \ell_2^H + nV}^{\text{LL}} = \hat{\sigma}_{q_1^H q_2^H \to \ell_1^H \ell_2^H}^B \int_{m_V^2}^{s} \mathrm{d}k_T^2 \frac{\mathrm{d}}{\mathrm{d}k_T^2} \Delta_{q_1^H q_2^H \ell_1^H \ell_2^H}^{\text{SU}(2)} \left(k_T^2, s; s\right)$$

Inclusive σ only sensible if measurement not SU(2) violating

If specifying the flavors, have to define an exclusive real crosssection, with fixed number of emission

This requires an extra no-branching probability

$$\Delta_{q_1^H q_2^H \ell_1^H \ell_2^H V}^{\mathrm{SU}(2)} \left(m_V^2, k_T^2; s \right) \equiv \Delta_V \left(m_V^2, k_T^2; \hat{k}_T^2 \right) \Delta_{q_1^H q_2^H \ell_1^H \ell_2^H}^{\mathrm{SU}(2)} \left(m_V^2, k_T^2; s \right)$$

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no-branching of extra V from k_T to m_V

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Putting this together one gets the final exclusive real radiation result

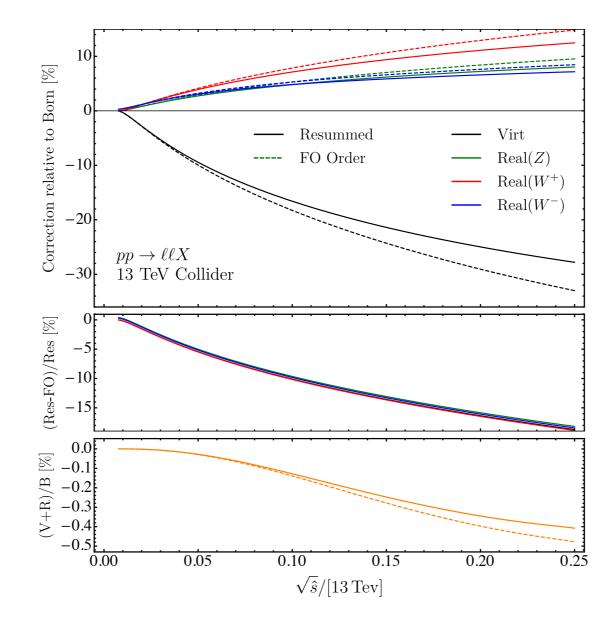
$$\hat{\sigma}_{q_{1}^{H}q_{2}^{H} \to \ell_{1}^{H}\ell_{2}^{H} + V}^{\text{LL}} = \hat{\sigma}_{q_{1}^{H}q_{2}^{H} \to \ell_{1}^{H}\ell_{2}^{H}}^{B} \int_{m_{V}^{2}}^{s} \mathrm{d}k_{T}^{2} \frac{\mathrm{d}}{\mathrm{d}k_{T}^{2}} \left[\Delta_{q_{1}^{H}q_{2}^{H}\ell_{1}^{H}\ell_{2}^{H}}^{\text{SU}(2)} \left(k_{T}^{2}, s; s\right) \right] \Delta_{q_{1}^{H}q_{2}^{H}\ell_{1}^{H}\ell_{2}^{H}V}^{\text{SU}(2)} \left(m_{V}^{2}, k_{T}^{2}; s\right)$$

Taking into account the full SU(2) x U(1) structure and writing the result in terms of W, Z, one finds

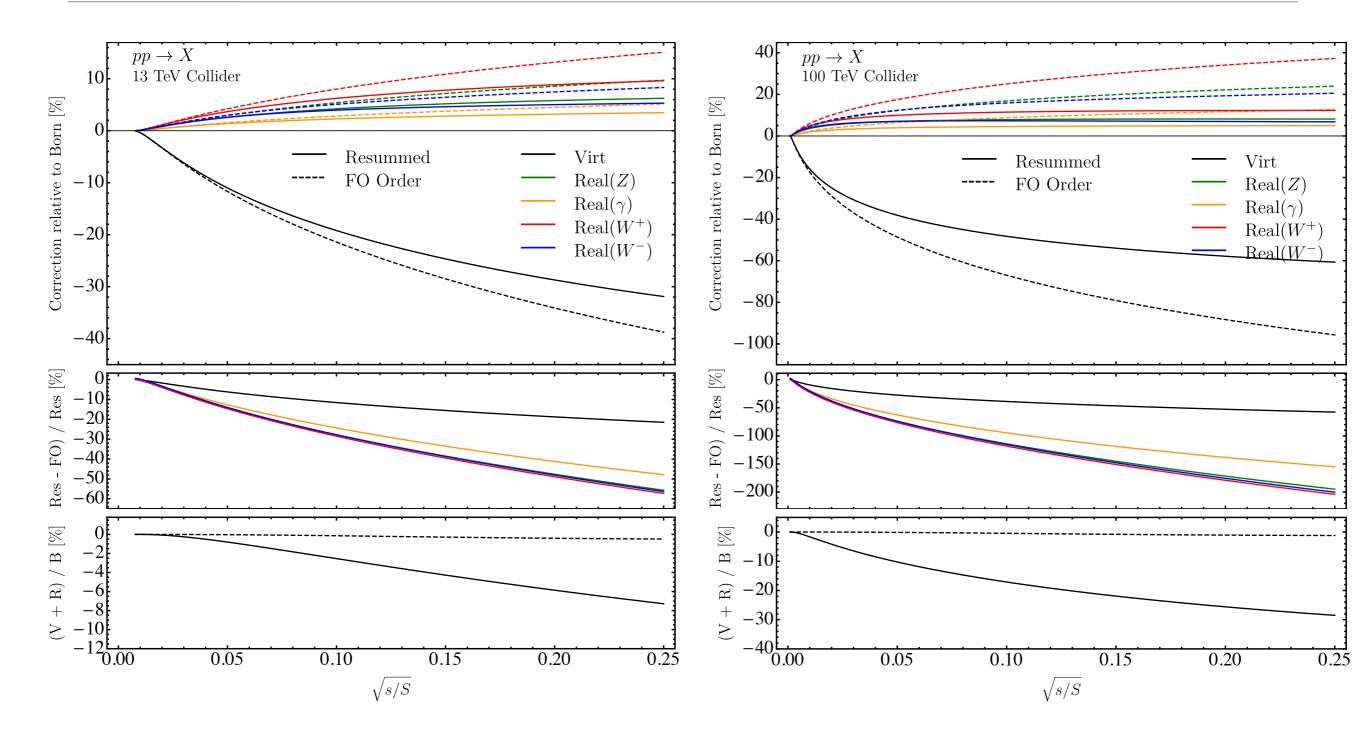
Z boson

$$\hat{\sigma}_{q_{1}^{H}q_{2}^{H} \to \ell_{1}^{H}\ell_{2}^{H}+Z}^{\text{LL}} = \hat{\sigma}_{q_{1}^{H}q_{2}^{H} \to \ell_{1}^{H}\ell_{2}^{H}}^{B} \Delta_{q_{1}^{H}q_{2}^{H}\ell_{1}^{H}\ell_{2}^{H}}\left(m_{V}^{2}, s; s\right) \Delta_{q_{1}^{H}q_{2}^{H}\ell_{1}^{H}\ell_{2}^{H}}^{\text{em}}\left(\Lambda^{2}, m_{V}^{2}; s\right) \qquad (4.42)$$

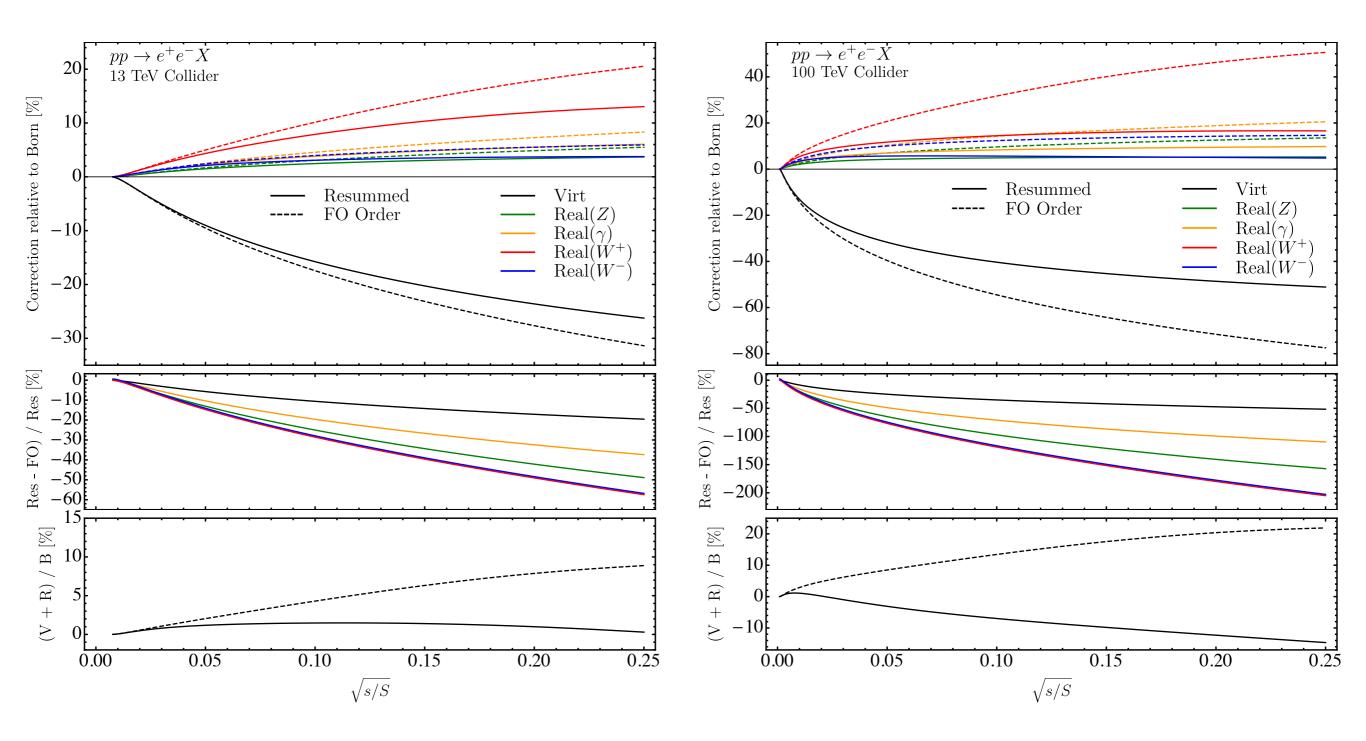
$$\times \int_{m_{V}^{2}}^{s} \frac{\mathrm{d}k_{T}^{2}}{k_{T}^{2}} \ln \frac{s}{k_{T}^{2}} \left(s_{W}^{2} A_{q_{1}^{H}q_{2}^{H}\ell_{1}^{H}\ell_{2}^{H}}^{U(1)} - A_{q_{1}^{H}q_{2}^{H}\ell_{1}^{H}\ell_{2}^{H}}^{\text{mixing}} \sqrt{\Delta_{W}(m_{V}^{2}, k_{T}^{2}; k_{T}^{2})} + c_{W}^{2} A_{q_{1}^{H}q_{2}^{H}\ell_{1}^{H}\ell_{2}^{H}}^{W^{3}} \Delta_{W}(m_{V}^{2}, k_{T}^{2}; k_{T}^{2})\right)$$



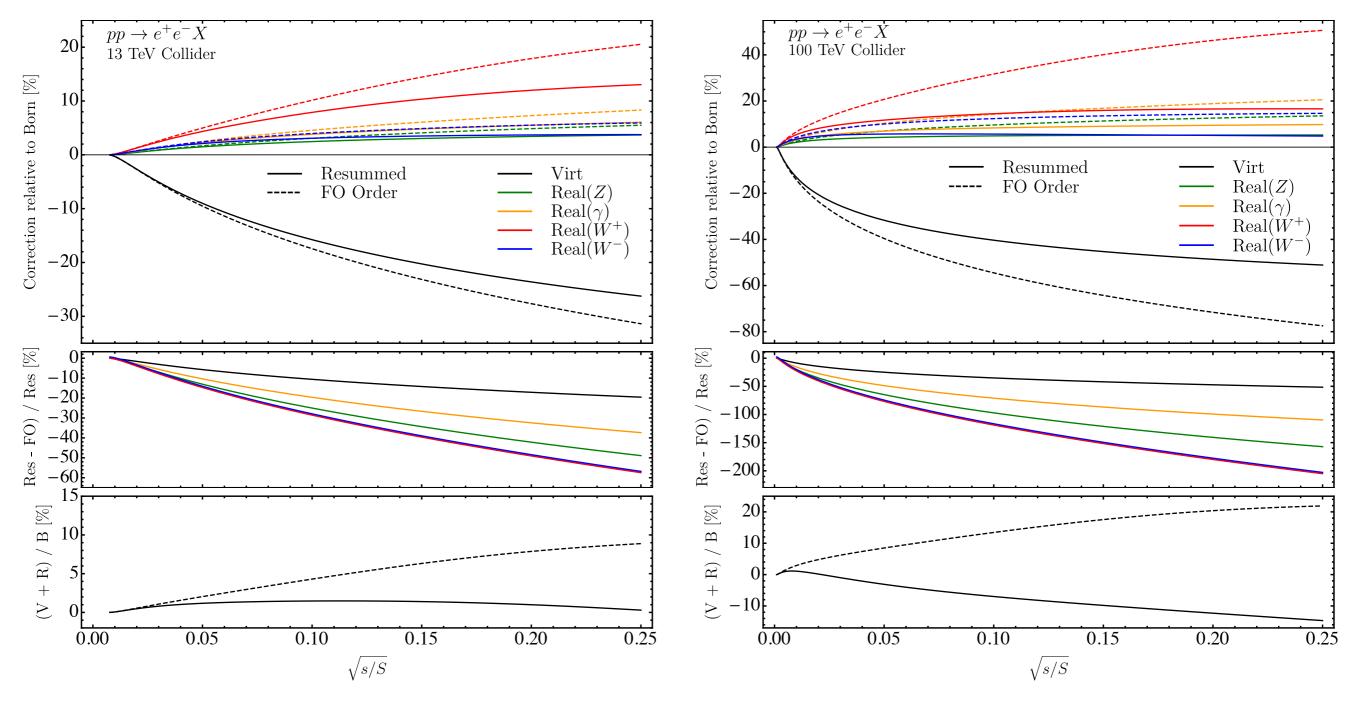
The results clearly indicate that resummation for the real is at least as important as for the virtual



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We have results for all possible leptonic final states in paper

We have first results on the LL resummation for real radiation, working on making these results fully differential

Can obtain analytical results for the resummation of the real radiation

EW Sudakov logarithms are as important for real as for virtual

Currently working on fully exclusive implementation of above results

Also working on parton shower like approach, which can take into account arbitrary number of emissions

Absolutely crucial to do this for 100 TeV machine

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