

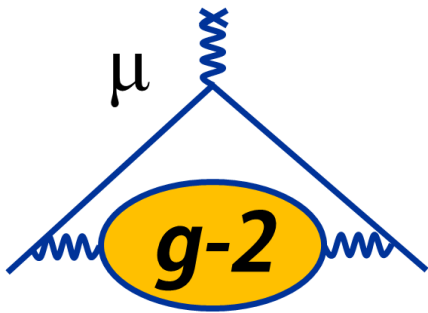
Status of the FNAL g-2 experiment

Joe Price

on behalf of the g-2 collaboration



UNIVERSITY OF
LIVERPOOL



22nd June 2016
Virginia

Outline



- Introducing the anomaly
- Theoretical predictions
- Current experimental limits
- How to measure the anomaly
- Expected improvements at FNAL
- Time scale

Magnetic moments - QM

- 1928 - Dirac combined special relativity and quantum mechanics

$$(i\gamma^\mu \partial_\mu - m) = 0$$

- Led to reinterpretation of spin $\frac{1}{2}$ particles as 4D spinors
 - Associated extra DOFs with spin, matter and anti-matter
- When placed in a field a potential-energy-like term appears, suggesting an intrinsic spin, the associated dipole moment is given by:

$$\vec{\mu} = g \frac{e}{2mc} \vec{S}$$

- g , the proportionality constant, is known as the gyromagnetic ratio
- Predicted by Dirac to be exactly 2 for spin $\frac{1}{2}$ particles

Introducing the anomaly

- 1947 Kusch-Foley experiment discovered an anomaly in the electron dipole moment

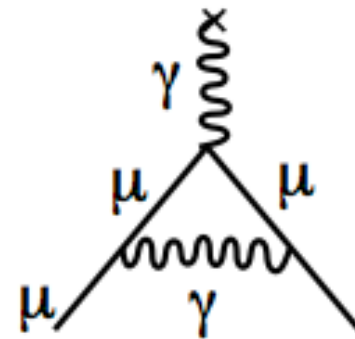
- $g_e = 2.00238(6)$

- The anomaly is parameterised via:

$$a = \frac{g - 2}{2}$$

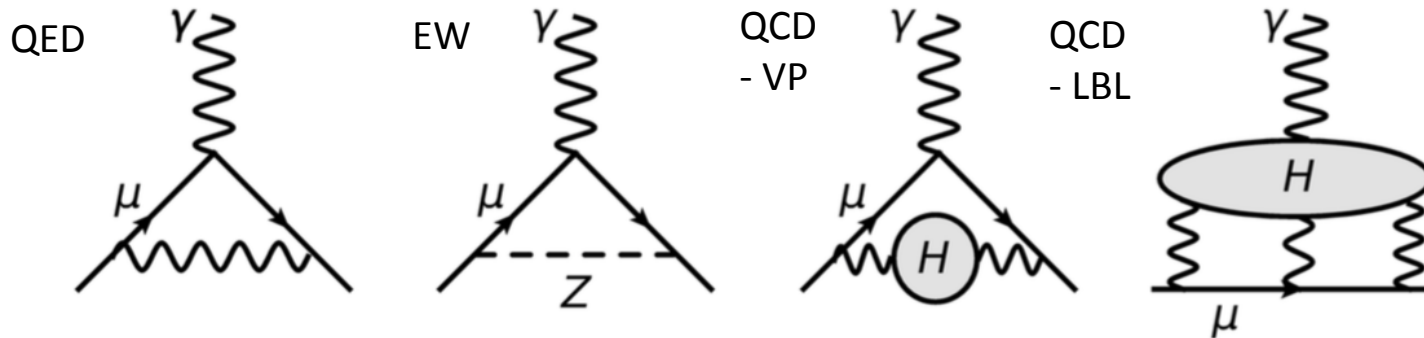
- Within a year Schwinger had calculated the first order QED correction, for electrons, but applies to muons:

$$g = 2\left(1 + \frac{\alpha}{2\pi}\right) \approx 2.00232$$



Standard model predictions

- There are higher order QED corrections, EW and QCD

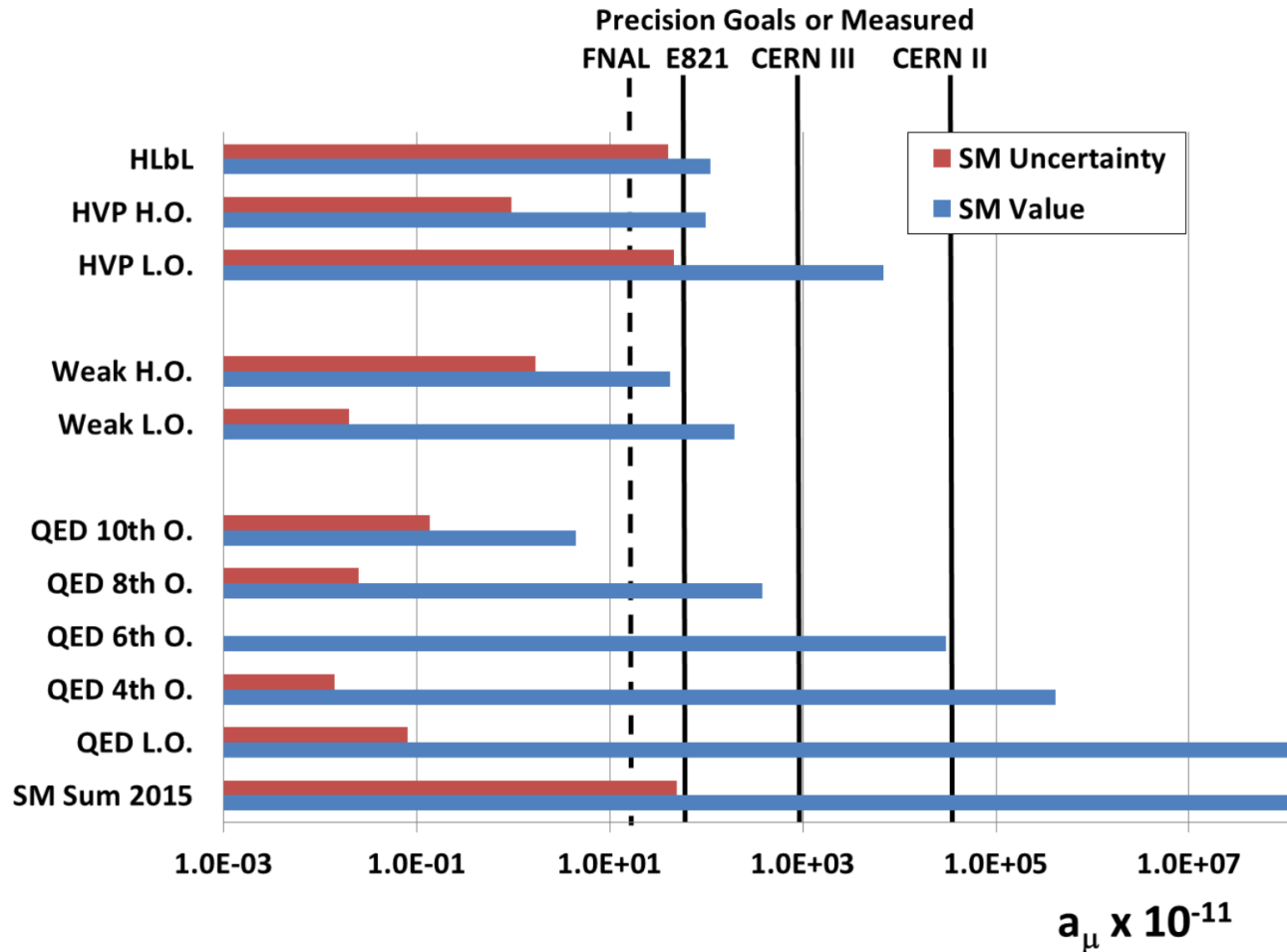


- All diagrams need to be included in calculation
- So far the best prediction is:

$$g_\mu = 2.002\,331\,841\,78(126)$$

Dirac (under 2.002), Schwinger $\sim O(1)$ QED (under 331), Kinoshita $\sim O(10)$ QED (under 841), Hadronic (under 78), EW (under 126)

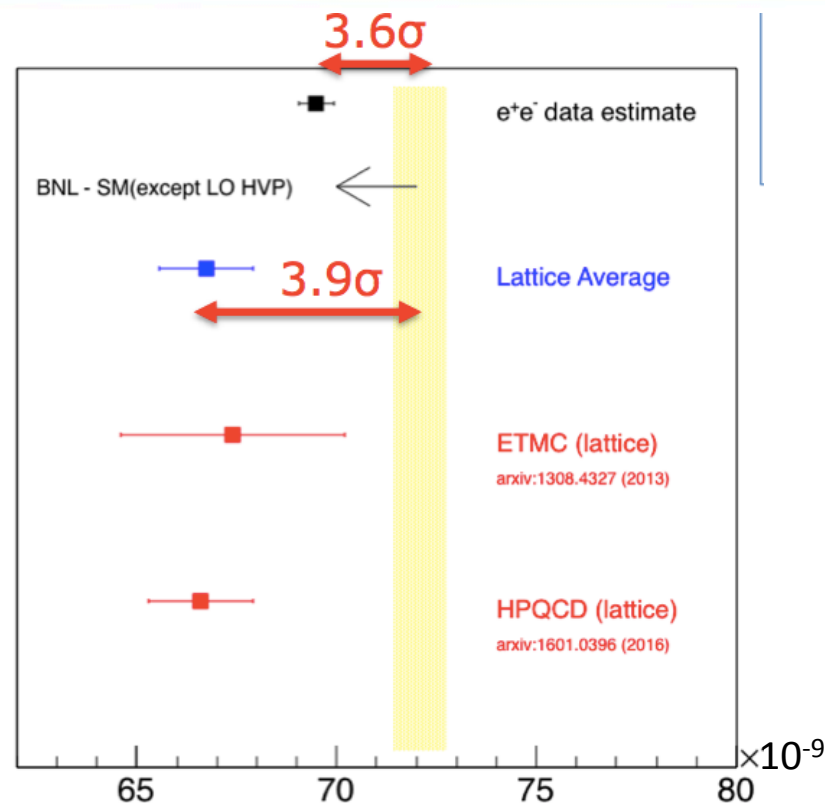
SM uncertainties



- SM uncertainty dominated by Hadronic - VP and LBL

Anticipated improvements to SM

- HVP can be tied to experimental data from e^+e^- collisions
 - New data expected from SND, CMD-3, BES-III, Belle-II...
 - Continuously updating SM prediction
- Alternative lattice calculation agrees with this prediction



- Hadronic light by light must be calculated by theory - lattice
- Factor of 2 improvement in SM calculation expected by end of data taking

Sensitivity to new physics

- Anomaly is due to vacuum interactions - sensitive to new physics
- But it hasn't shown up in a_e , why expect it in a_μ ?
- Sensitivity to new physics proportional to squared mass of probe

$$\left(\frac{m_e}{m_\mu}\right)^2 \sim 4 \times 10^4$$

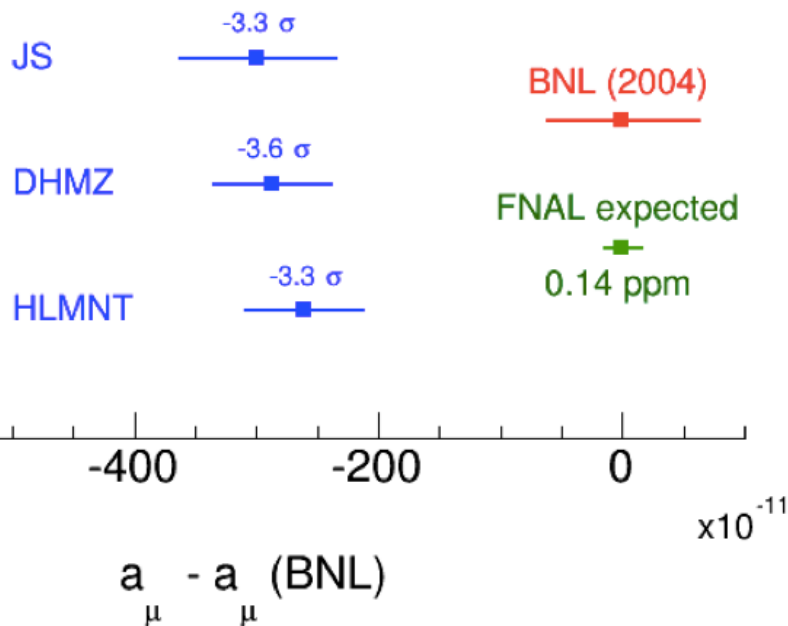
- For example EW contributes **1.3 ppm** to a_μ , but only **26 ppt** to a_e
- When using muons:
 - Relatively long lifetime means we can store muons
 - High production cross section
 - Relatively easy to polarise

Current experimental limits on a_μ

- Most precise measurement performed at BNL (1999-2001)
- Accuracy of ~ 0.5 ppm

$$a_\mu^{exp} = 116\,592\,089 (0.54)_{st} (0.33)_{sy} (0.63)_{tot} \times 10^{-11}$$

- Uncertainty is dominated by statistics



- Measurement differs from theory by $\sim 3.5 \sigma$

$$\Delta a_\mu^{(today)} = (287 \pm 80) \times 10^{-11}$$

How to measure the anomaly

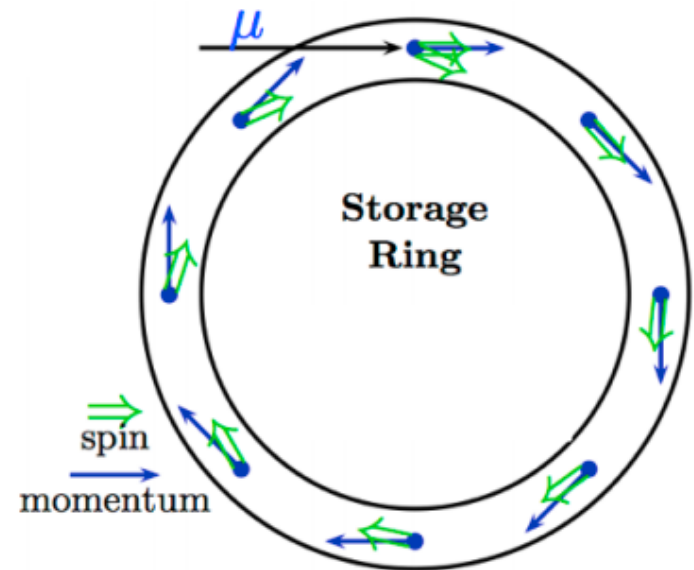
- Store longitudinally polarised muons in a dipole field
- Measure 2 quantities:
 - ω_a - the precession frequency
 - $\langle B \rangle$, the average magnetic field sampled by the muon distribution

$$\omega_a = \omega_s - \omega_c = a_\mu \frac{e \langle B \rangle}{m_\mu c}$$

Larmor Precession $\omega_s = \frac{geB}{2mc} + (1 - \gamma) \frac{eB}{\gamma mc}$ Spin Precession frequency	Thomas Precession $\omega_c = \frac{eB}{\gamma mc}$ Cyclotron frequency
---	--

~140ns

~149ns



actual precession $\times 2$

- Spin precession $> 2\pi$ per cyclotron turn

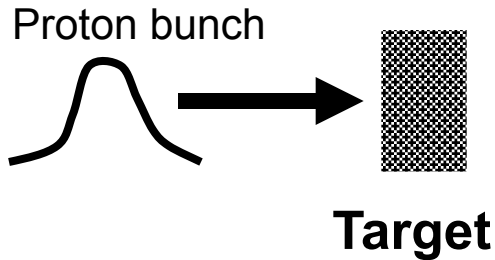
Magic momentum

- Electric quadrupoles used for vertical focusing seen as magnetic field in muon rest frame
- Assuming velocity is perpendicular to E and B fields:

$$\vec{\omega}_a = -\frac{e}{mc} \left[a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \vec{\beta} \times \vec{E} \right]$$

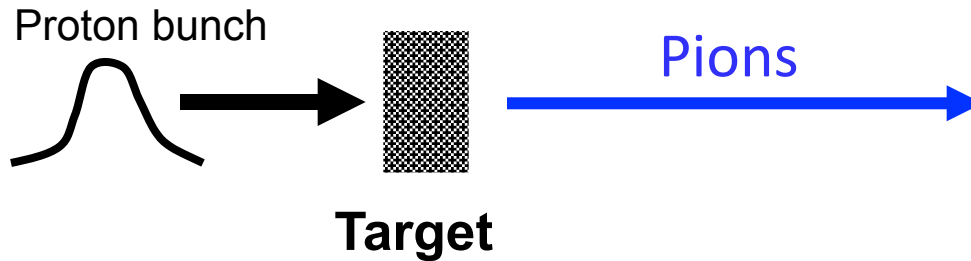
- By choosing $\gamma = 29.3$, $p_\mu = 3.09 \text{ GeV}/c^2$, $\vec{\beta} \times \vec{E}$ term is 0
- At this momentum the magnetic field alone determines the precession frequency - only need to measure B and ω_a
- Dilated muon lifetime is $64.4 \mu\text{s}$

Supplying anti-muons



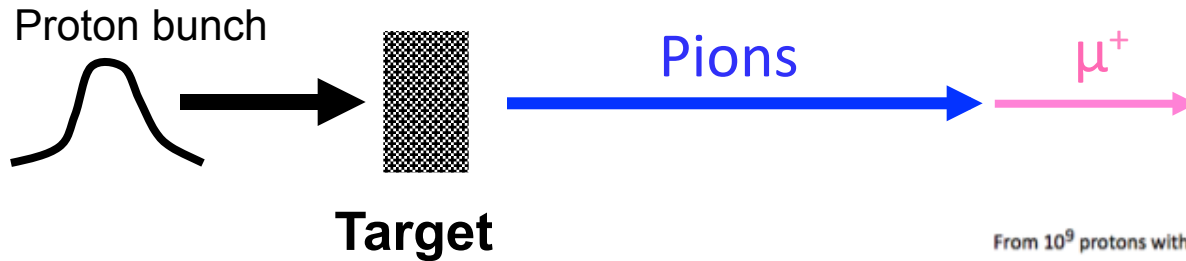
- Booster & Recycler supply 120 ns wide 8 GeV proton bunches
- Fired at pion production target

Supplying anti-muons

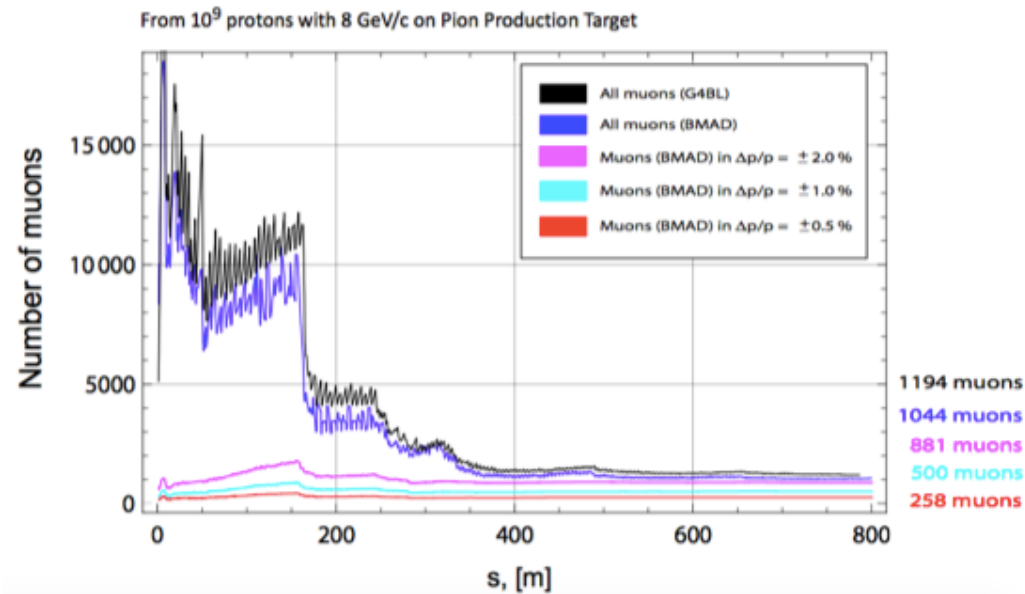
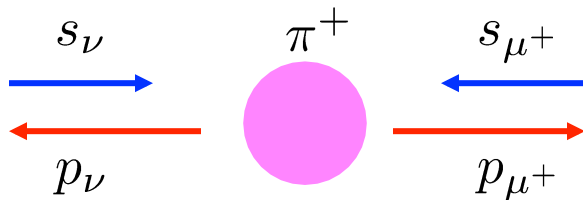


- Outgoing pions focused by a lithium lens and then momentum-selected, centred on 3.11 GeV
- The pions are then collected and sent towards the delivery ring

Supplying anti-muons



- In the delivery ring the pions decay to negative helicity anti-muons

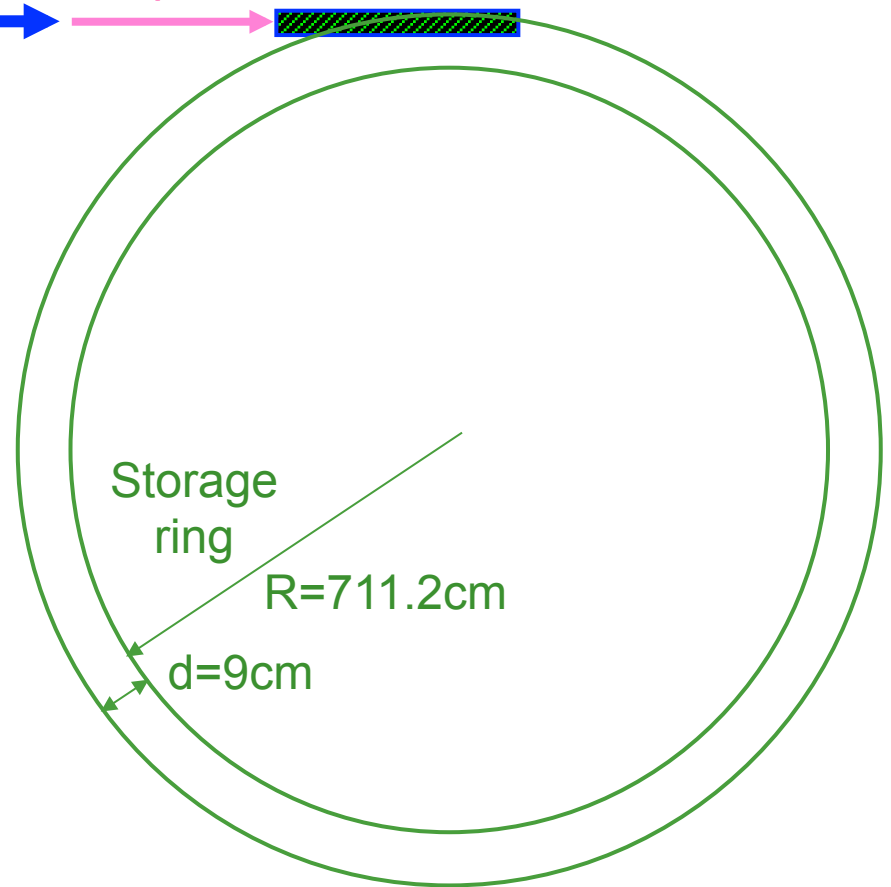


- 2 independent simulations of polarisation and phase space of beam

Supplying anti-muons



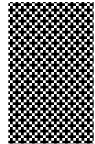
- Storage ring is 14m diameter toroidal C-magnet of 1.45T
- Inflector magnet nullifies the storage ring field for incoming muons



Supplying anti-muons



Proton bunch

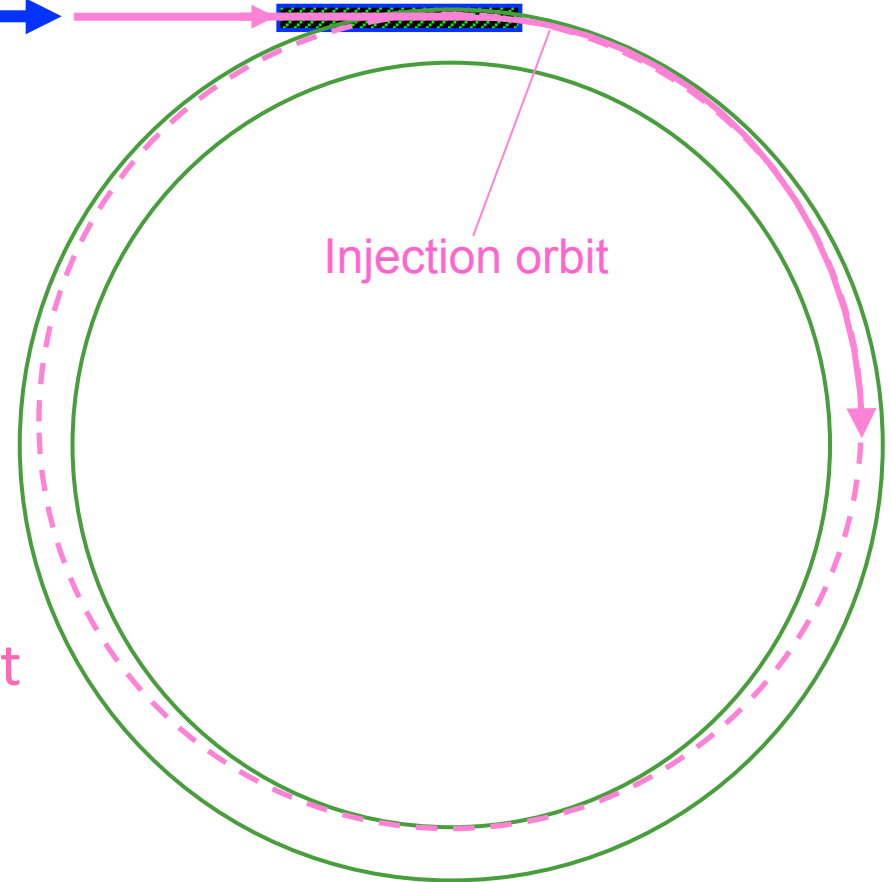


Target

Pions



μ^+



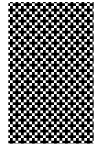
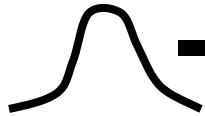
- Storage ring is 14m diameter toroidal C-magnet of 1.45T

- Inflector magnet nullifies the storage ring field for incoming muons

- Muons that pass through the inflector are not on the ideal orbit

Supplying anti-muons

Proton bunch

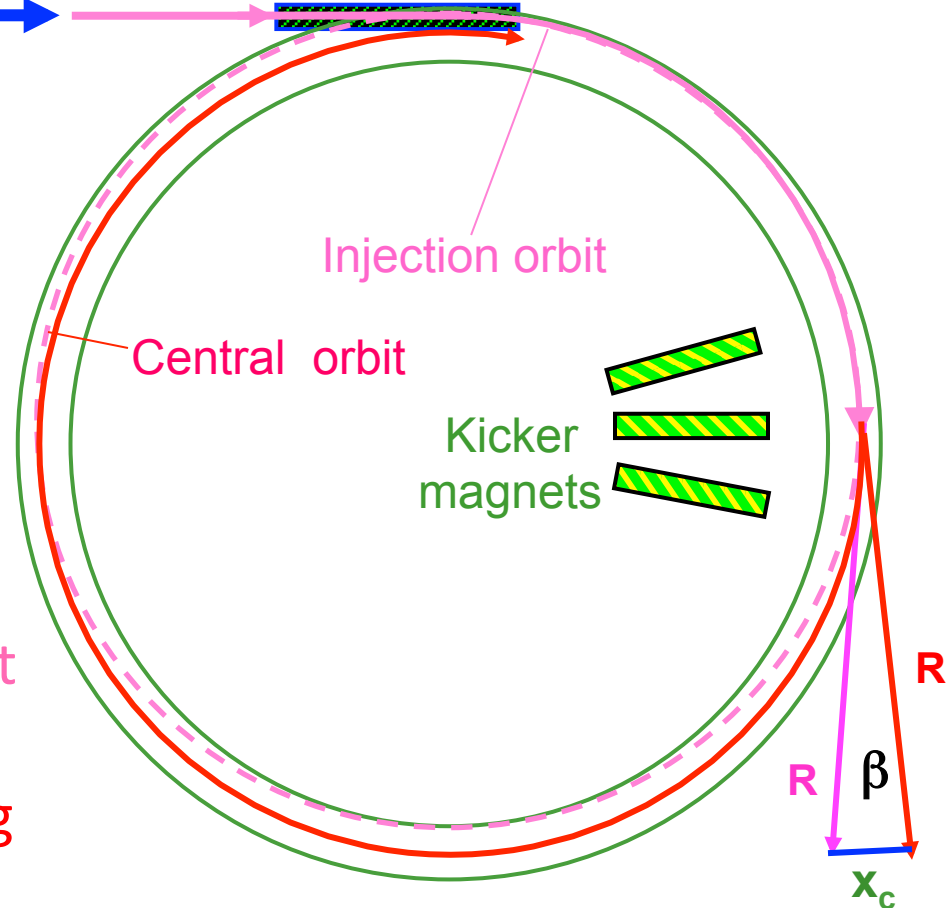


Target

Pions



μ^+



- Storage ring is 14m diameter toroidal C-magnet of 1.45T

- Inflector magnet nullifies the storage ring field for incoming muons

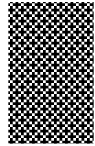
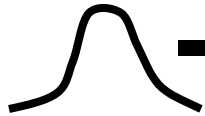
- Muons that pass through the inflector are not on the ideal orbit

- Kicker magnets move the beam into the centre of the storage ring

$x_c \sim 77\text{mm}$
 $\beta \sim 10\text{mrad}$

Supplying anti-muons

Proton bunch

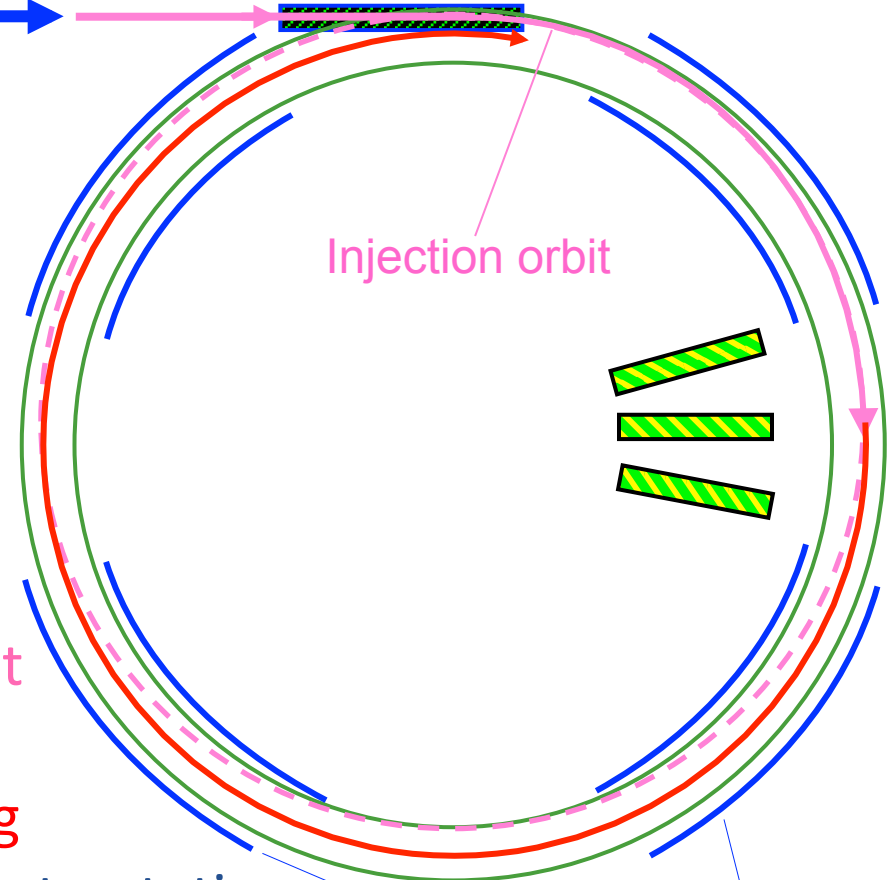


Target

Pions



μ^+



Injection orbit

Electric Quadrupoles

- Storage ring is 14m diameter toroidal C-magnet of 1.45T

- Inflector magnet nullifies the storage ring field for incoming muons

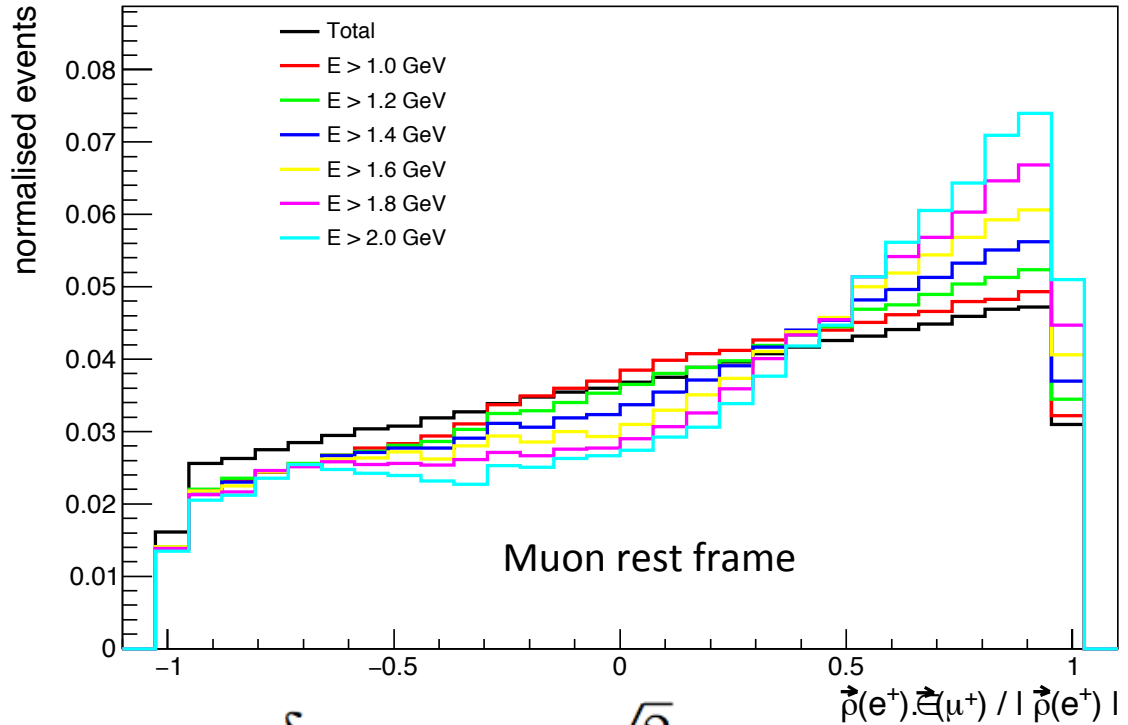
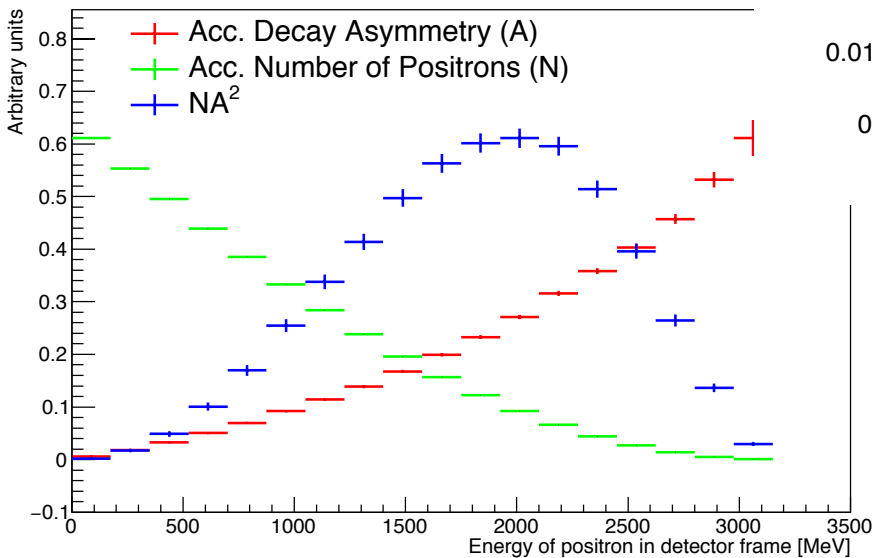
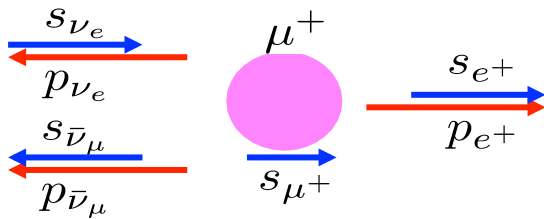
- Muons that pass through the inflector are not on the ideal orbit

- Kicker magnets move the beam into the centre of the storage ring

- Muons focused vertically with electrostatic quadrupoles - improves statistics

Muon decay

e^+ preferentially emitted in direction of the μ^+ spin

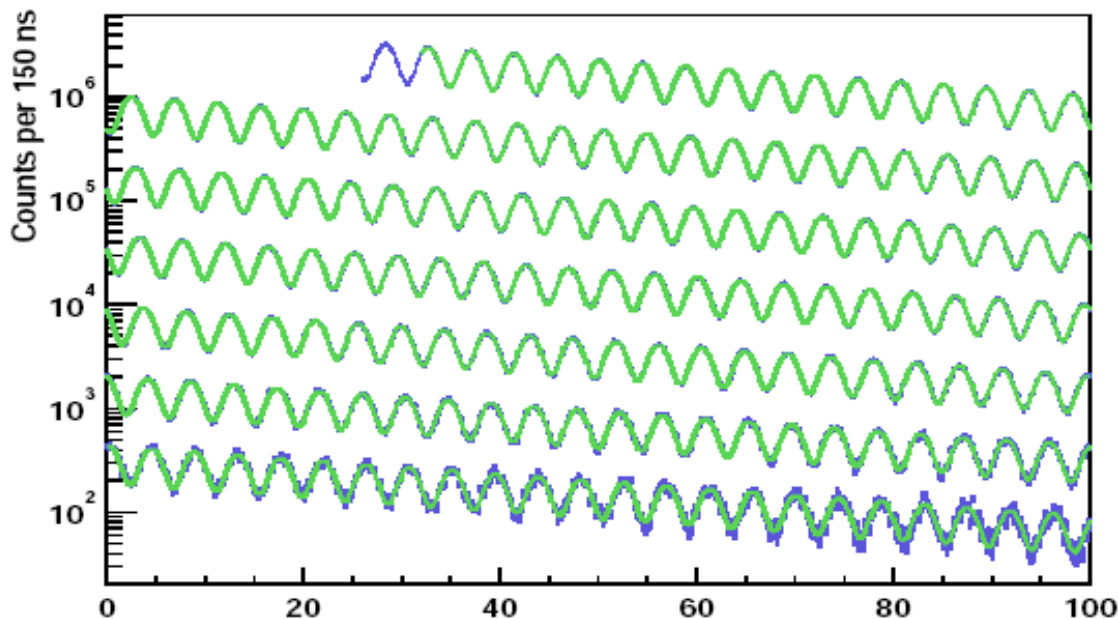


$$\frac{\delta\omega_a}{\omega_a} = \frac{\sqrt{2}}{2\pi f_a \tau_\mu \sqrt{NA^2}}$$

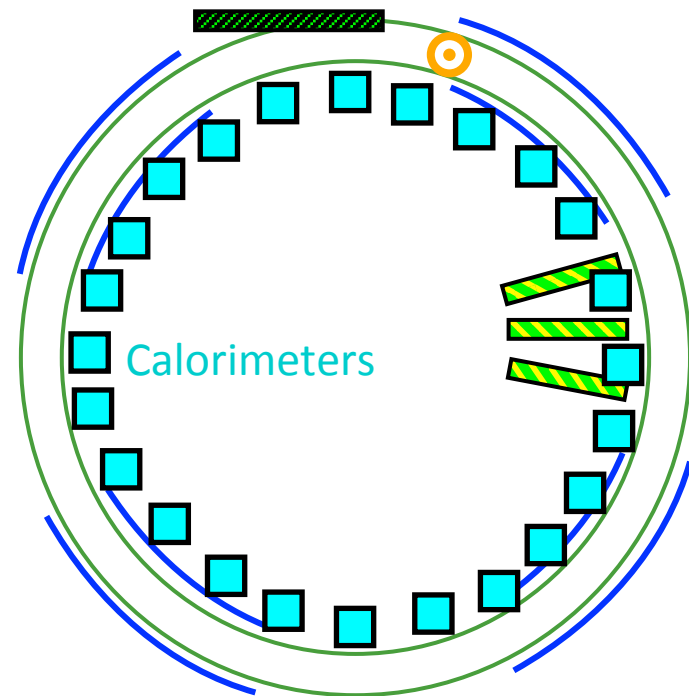
- Asymmetry is larger for higher energy positrons
- Optimal cut at $\sim E > 1.8 \text{ GeV}$

Calorimeters

- 24 calorimeters are placed around ring
- They measure the e^+ from the μ decay
- Number of higher energy positrons oscillates as spin points towards/away from calorimeters

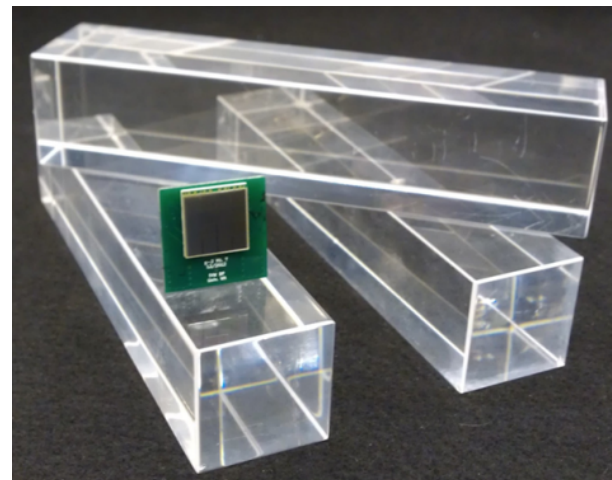
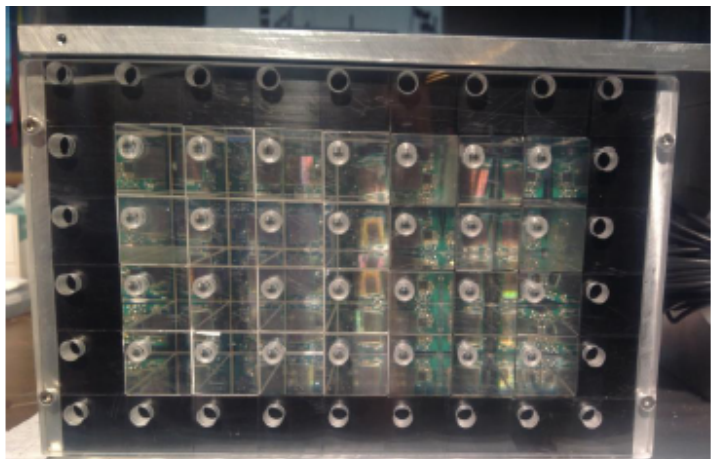


$$N_e(t) \simeq N_0 e^{-\frac{t}{\gamma\tau}} [1 - A \cos(\omega_a t + \phi_a)]$$



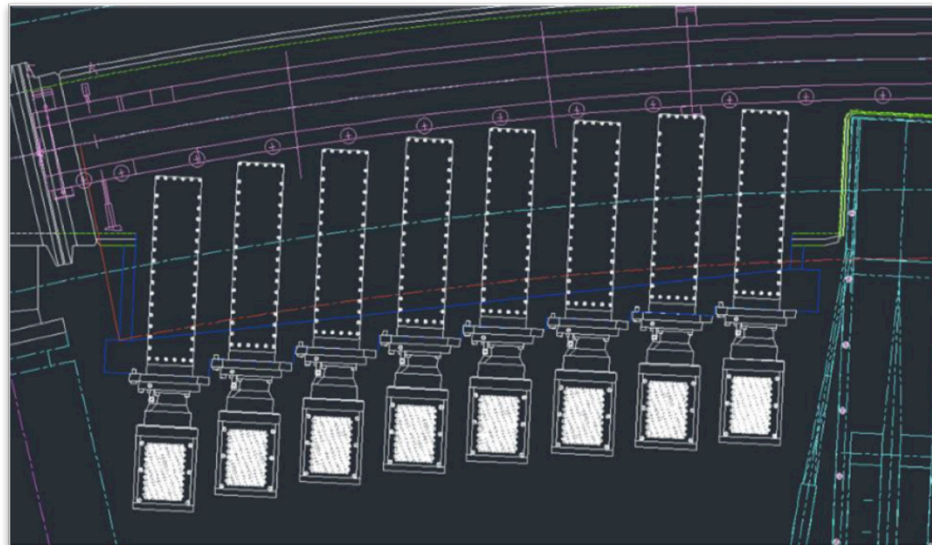
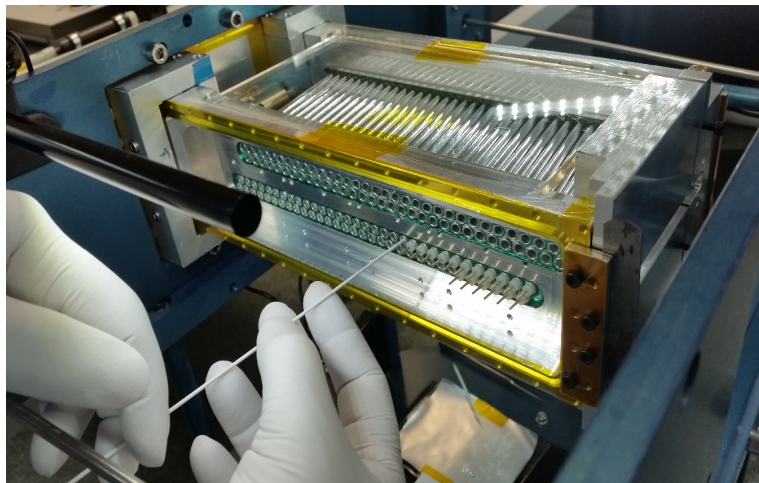
- Perform 5 parameter fit to arrival time spectrum - same as in BNL experiment

Calorimeters



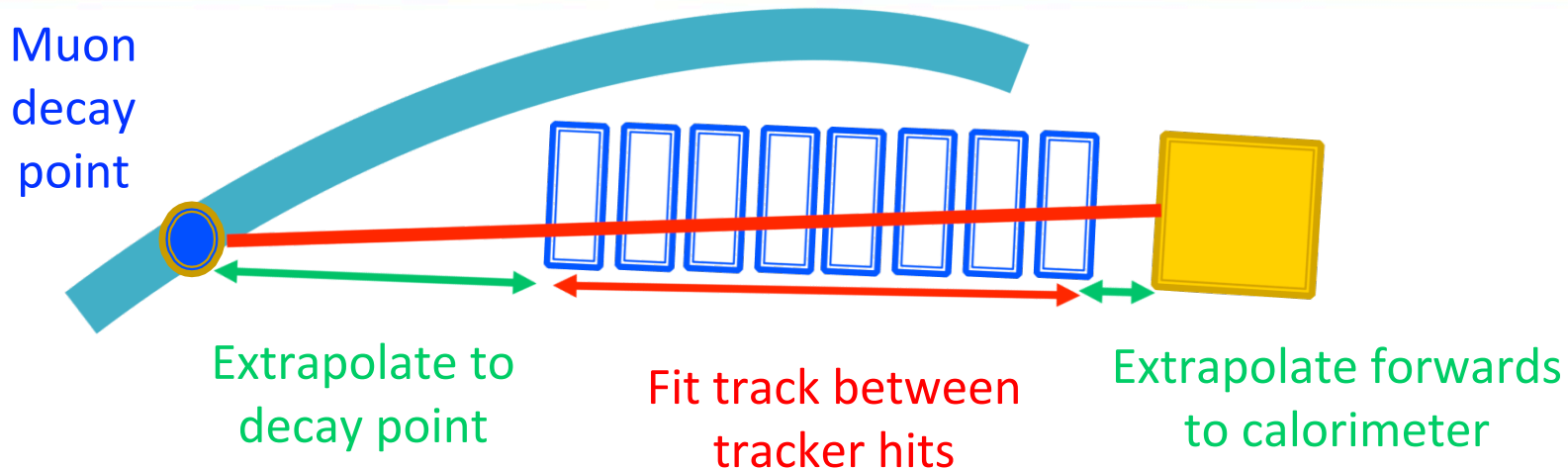
- Each consists of 6 by 9 array of PbF_2 crystals
 - Multiple test beams at SLAC with 28 crystals
- Each crystal is 2.5 x 2.5 x 14cm $\sim (15X_0)$
- Improvement in gain - event rate changes 4 orders of magnitude over 700 μs fill
- Increased segmentation reduces pile up
- Readout by SiPM

Trackers



- 3 trackers - each with 8 modules
- Placed in front of calorimeters
- Each module 128 straws filled with Ar-Ethane
- $\sim 100 \mu\text{m}$ radial resolution
- Major improvements on tracking for E989
 - Allow extrapolation to decay point / into calorimeters

Improvements from trackers



- Measuring beam profile during spill allows reduction in several key systematics:

Decay point

- Magnetic field seen by muons
- Beam dynamics corrections
- Precession plane tilt

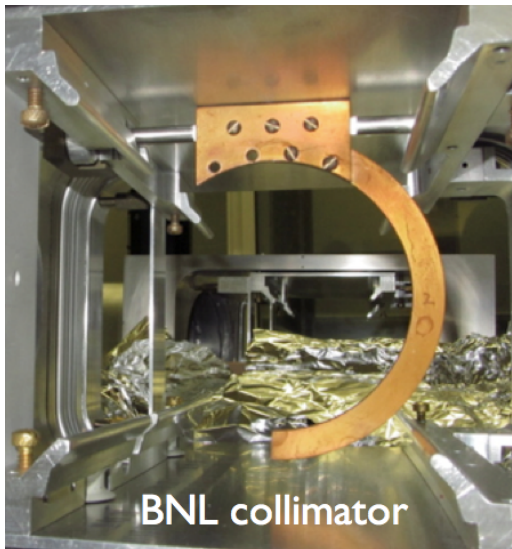
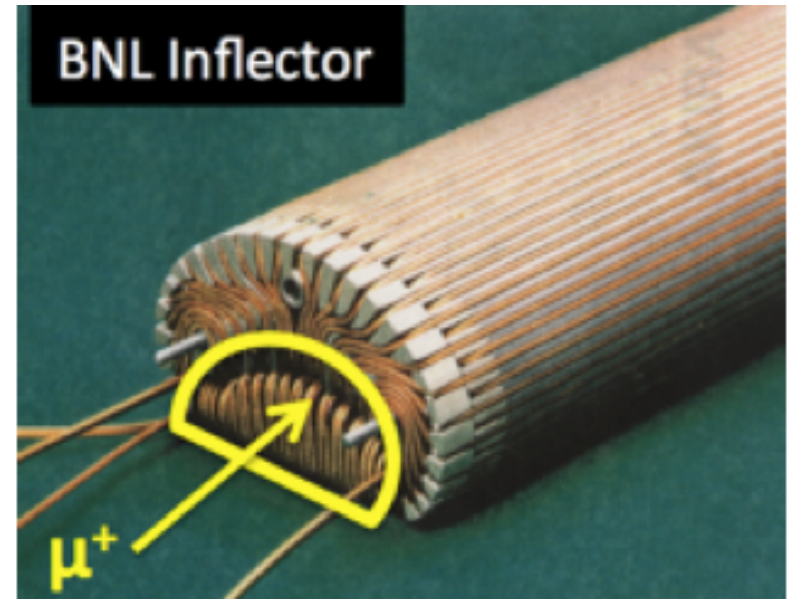
Calorimeter matching

- Pileup correction
- Calorimeter gain stability

- Additional improvement in vertical measurement - EDM

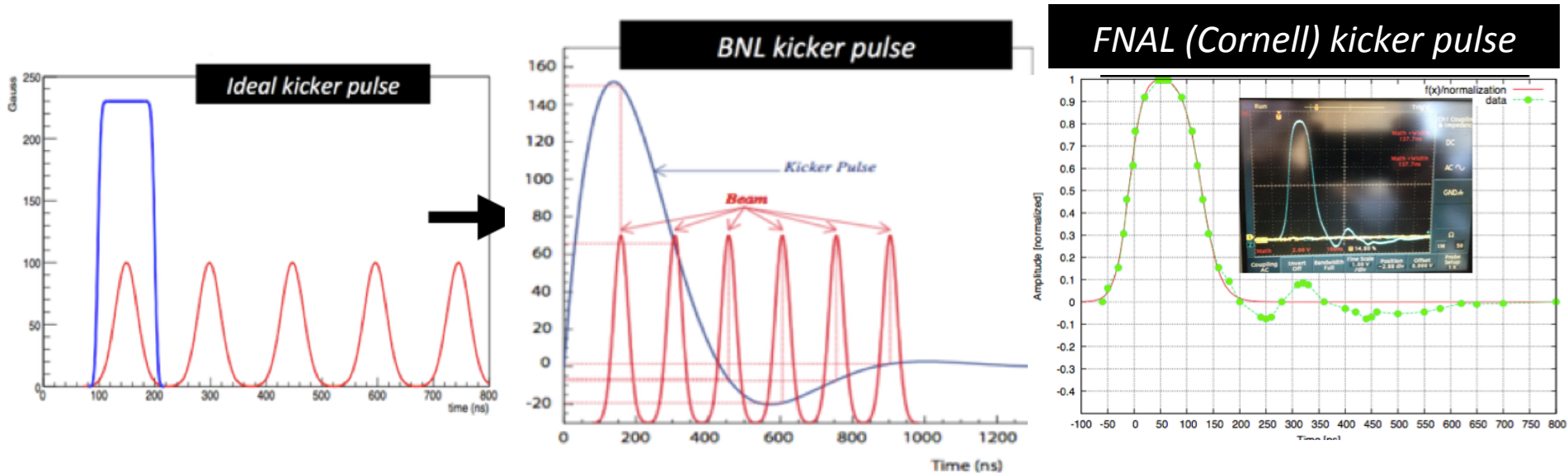
Inflector / collimator

- Inflector actively cancels magnetic fringe field so that muons are injected tangentially
- New inflector scheduled for 2018 running period



- Collimators help eliminate off magic momentum muons
- Increased thickness of collimators w.r.t E821 for better beam cleaning efficiency

Kickers



- Muon beam does not enter ring in central orbit
- To place the beam into the central orbit a quick magnetic field burst (kick) is supplied
- Change in angle of ~ 10.8 mrad
- Pulse must be shorter than 149ns - orbit time
- Vacuum chambers with kickers being installed this summer/fall

Improvements summary - ω_a

Category	E821 [ppb]	E989 Improvement Plans	Goal [ppb]
Gain changes	120	Better laser calibration low-energy threshold	20
Pileup	80	Low-energy samples recorded calorimeter segmentation	40
Lost muons	90	Better collimation in ring	20
CBO	70	Higher n value (frequency) Better match of beamline to ring	< 30
E and pitch	50	Improved tracker Precise storage ring simulations	30
Total	180	Quadrature sum	70

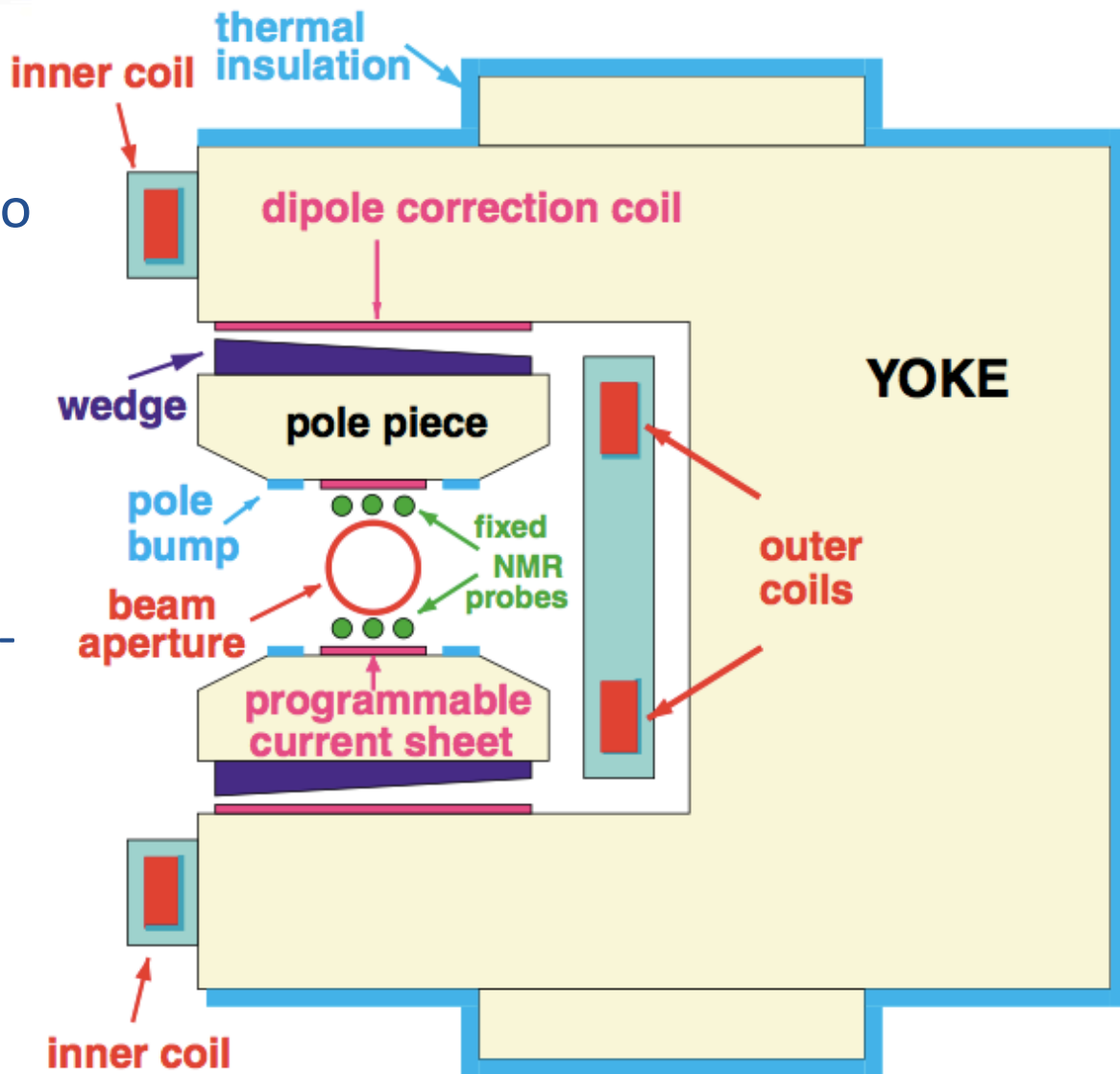
Magnetic field - goals

- BNL achieved $\sim 1\text{-}2\text{ppm}$ deviation when averaged around azimuth
- FNAL aiming for factor of 2 improvement in homogeneity

Source of uncertainty	R99 [ppb]	R00 [ppb]	R01 [ppb]	E989 [ppb]
Absolute calibration of standard probe	50	50	50	35
Calibration of trolley probes	200	150	90	30
Trolley measurements of B_0	100	100	50	30
Interpolation with fixed probes	150	100	70	30
Uncertainty from muon distribution	120	30	30	10
Inflector fringe field uncertainty	200	–	–	–
Time dependent external B fields	–	–	–	5
Others †	150	100	100	30
Total systematic error on ω_p	400	240	170	70
Muon-averaged field [Hz]: $\tilde{\omega}_p/2\pi$	61 791 256	61 791 595	61 791 400	–

Magnetic field - shimming

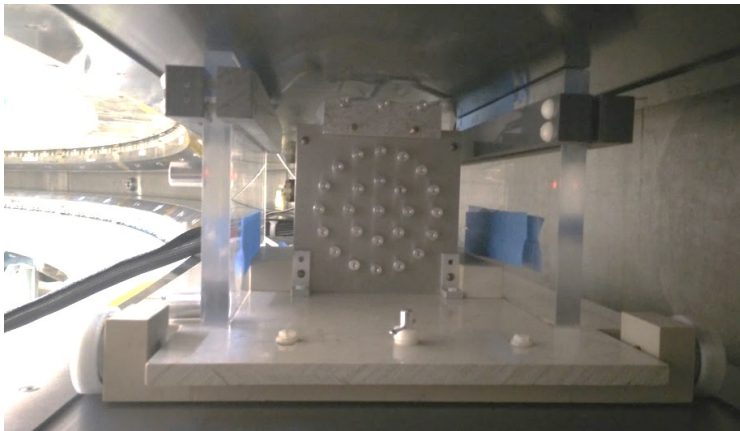
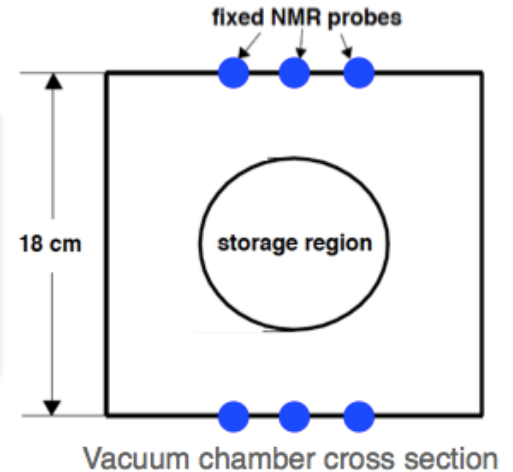
- Multiple passive and active shimming tools
- Insert thin wedges into air gap to distort field
- Use to adjust field shape up to the decupole term
- $\pm 1^\circ\text{C}$ gives ± 40 ppm field strength change - so temperature monitored precisely



Magnetic field - monitoring

- Field monitored by fixed NMR probes and NMR trolley

- ~400 probes constantly monitor field just outside storage region (in air)
- Insensitive to field shape drifts inside SR

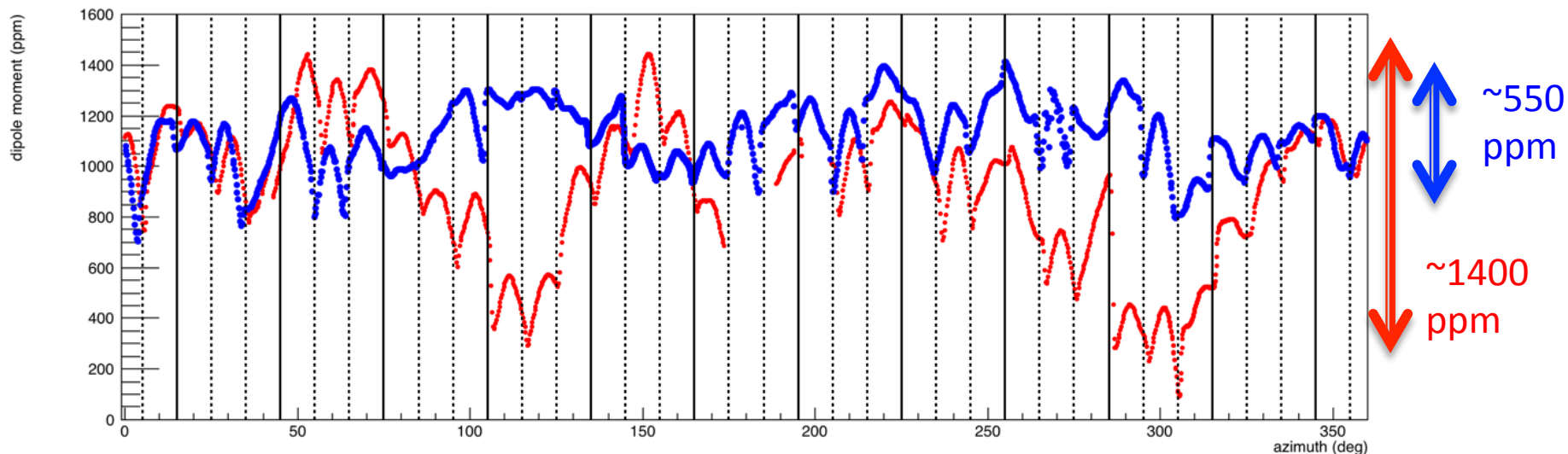
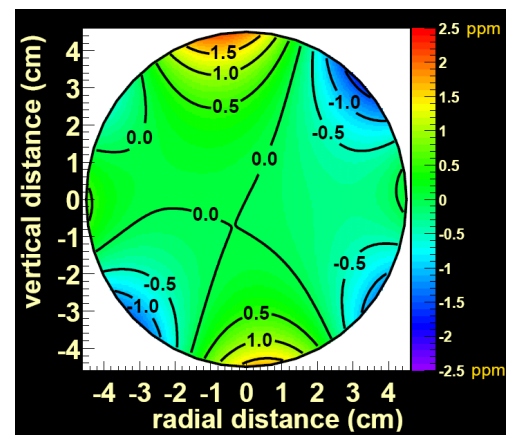


- Matrix of 25 NMR probes pulled around ring to measure field as felt by muons
- 4 Position sensors give 25 μm resolution

- Overall calibration with MRI facility (Argonne) via spherical probe

Current status - field

- Target level of <1 ppm in uniformity
- Coarse shimming complete - Variation down from 1400 ppm (October) to 550 ppm (Feb)
- Fine tuning completed end of summer



Uncertainty budget - ω_p



Source of uncertainty	R99 [ppb]	R00 [ppb]	R01 [ppb]	E989 [ppb]
Absolute calibration of standard probe	50	50	50	35
Calibration of trolley probes	200	150	90	30
Trolley measurements of B_0	100	100	50	30
Interpolation with fixed probes	150	100	70	30
Uncertainty from muon distribution	120	30	30	10
Inflector fringe field uncertainty	200	–	–	–
Time dependent external B fields	–	–	–	5
Others †	150	100	100	30
Total systematic error on ω_p	400	240	170	70
Muon-averaged field [Hz]: $\tilde{\omega}_p/2\pi$	61 791 256	61 791 595	61 791 400	–

- † Higher multipoles, trolley temperature (≤ 50 ppb/ $^{\circ}$ C) and power supply voltage response (400 ppb/V, $\Delta V=50$ mV), and eddy currents from the kicker.

● 0.17 ppm will be reduced to 0.07 ppm

Improvements summary - ω_p

Category	E821 [ppb]	Main E989 Improvement Plans	Goal [ppb]
Absolute field calibration	50	Special 1.45 T calibration magnet with thermal enclosure; additional probes; better electronics	35
Trolley probe calibrations	90	Plunging probes that can cross calibrate off-central probes; better position accuracy by physical stops and/or optical survey; more frequent calibrations	30
Trolley measurements of B_0	50	Reduced position uncertainty by factor of 2; improved rail irregularities; stabilized magnet field during measurements*	30
Fixed probe interpolation	70	Better temperature stability of the magnet; more frequent trolley runs	30
Muon distribution	30	Additional probes at larger radii; improved field uniformity; improved muon tracking	10
Time-dependent external magnetic fields	–	Direct measurement of external fields; simulations of impact; active feedback	5
Others †	100	Improved trolley power supply; trolley probes extended to larger radii; reduced temperature effects on trolley; measure kicker field transients	30
Total systematic error on ω_p	170		70

- *Improvements due to more uniformly shimmed magnetic field
- Others - higher multipoles, temperature unc., voltage response and eddy current from kickers

Additional measurements

- As well as measuring the anomalous magnetic moment can additionally search for **electric dipole moment**

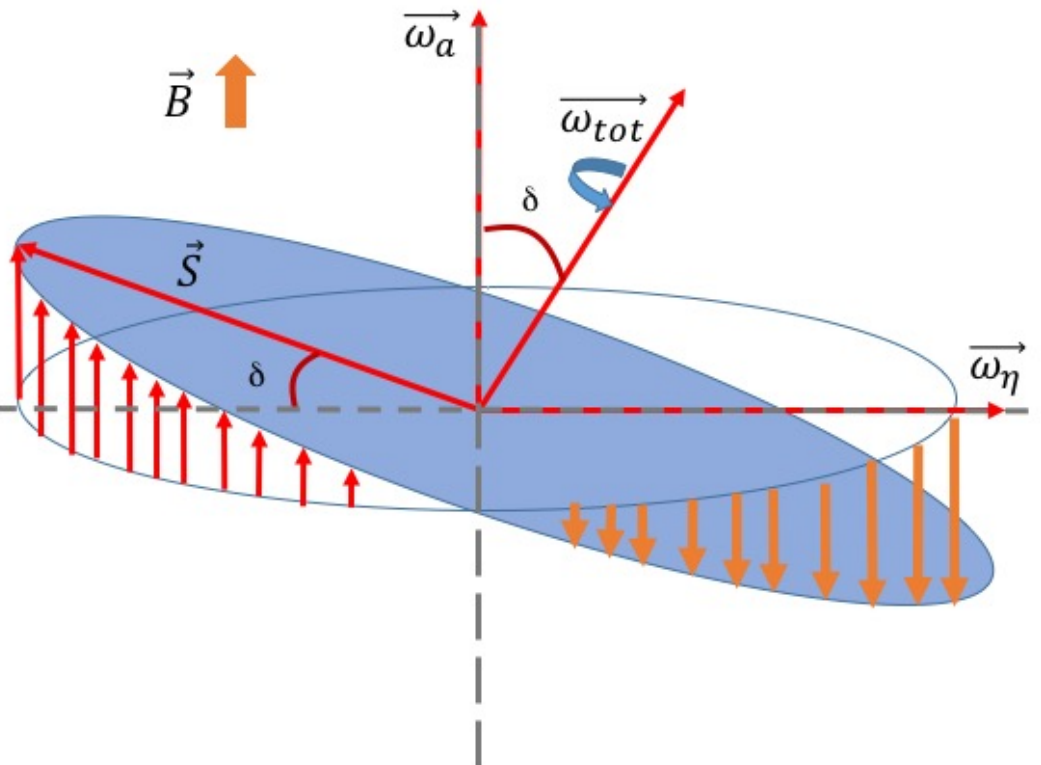
$$\vec{d}_\mu = \frac{\eta}{2} \frac{e\hbar}{2m_\mu c} \vec{S}$$

- Precession plane tilts towards centre of ring

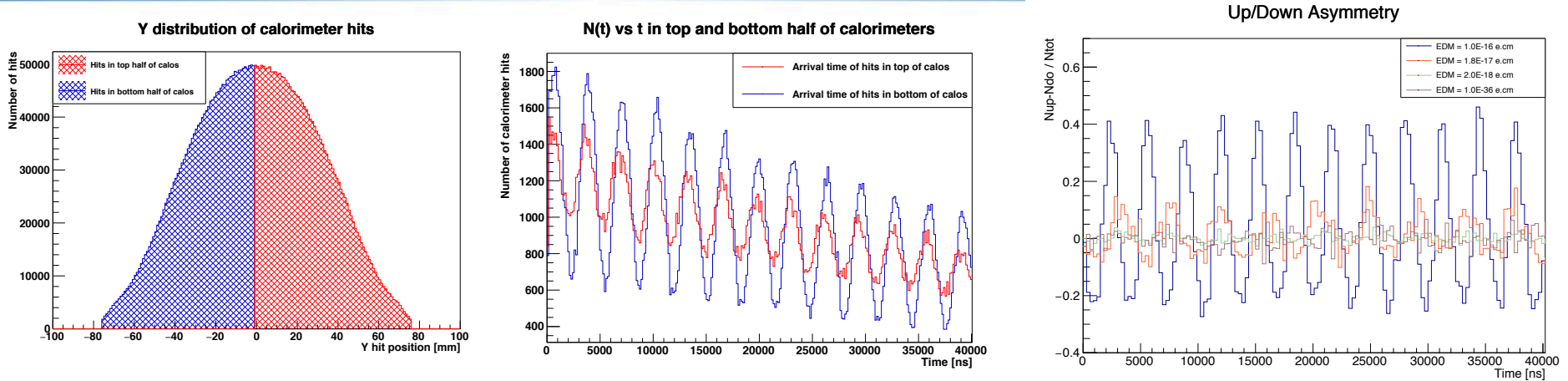
- Increase in precession frequency

$$\omega_{tot} = \sqrt{\omega_a^2 + \omega_\eta^2}$$

- Vertical oscillation is 90° out of phase with a_μ oscillation

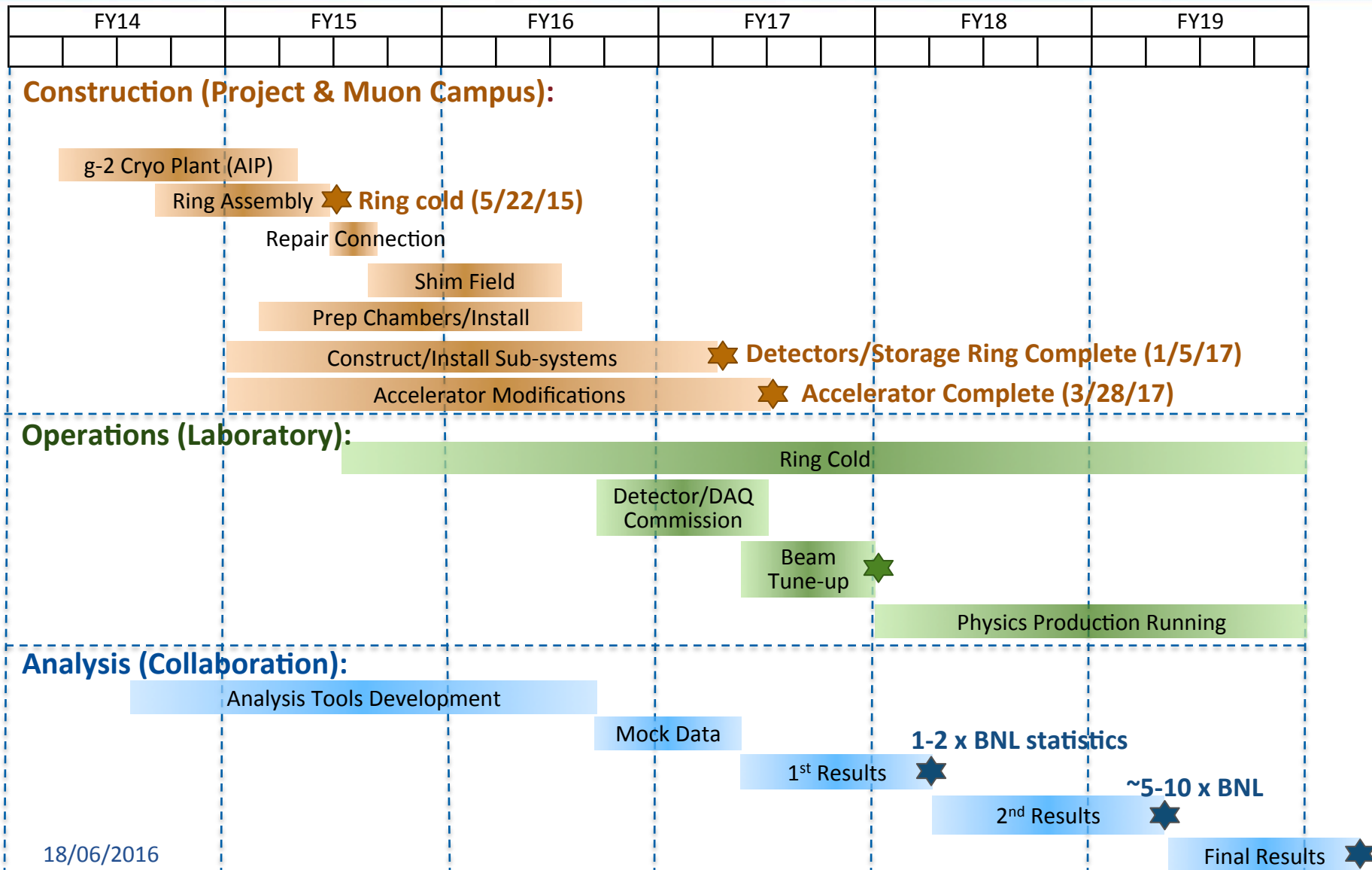


EDM sensitivity



- Amplitude of vertical oscillation proportional to d_{μ}
- Current limit $|d_{\mu}| < 1.8 \times 10^{-19}$ e.cm
- Improvement from statistics compared to BNL
 - Trackers operational for full early part of spill
- Vertical position from trackers
- Aiming for sensitivity at $|d_{\mu}| \sim 10^{-21}$ e.cm

Schedule



Summary



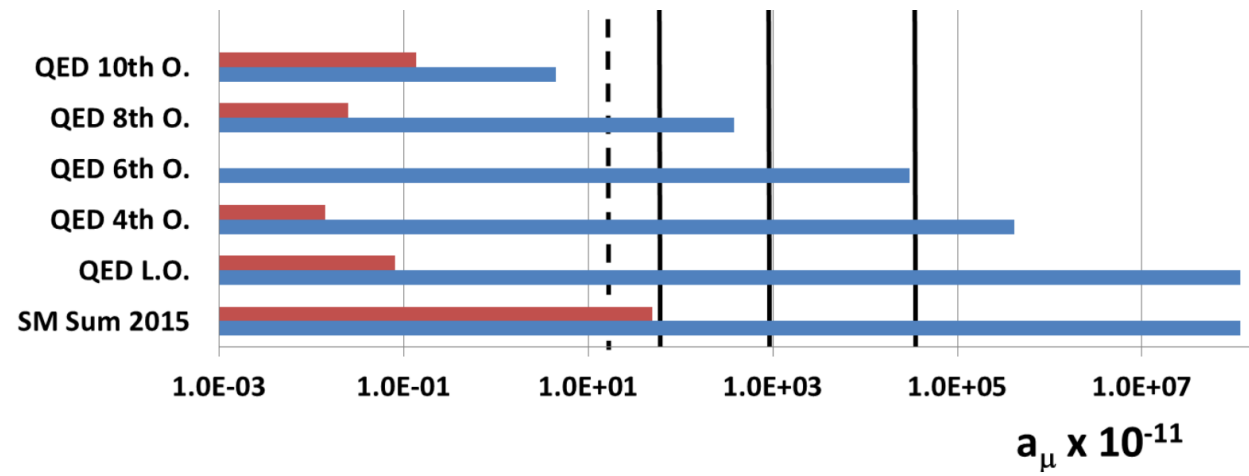
- a_μ sensitive to new physics
- Discrepancy shows no signs of going away with improved theory
- Main experimental improvement from increased stats
 - Expecting 21 times more data $\sim 1.5 \times 10^{11}$ muons
 - Available due to improved facilities at FNAL
- Additional improvements in experimental uncertainties
 - Improved uniformity in B field, calibration procedures, ...
 - New calorimeters, trackers, kickers, ...
- Data taking starts in summer 2017



● backups...

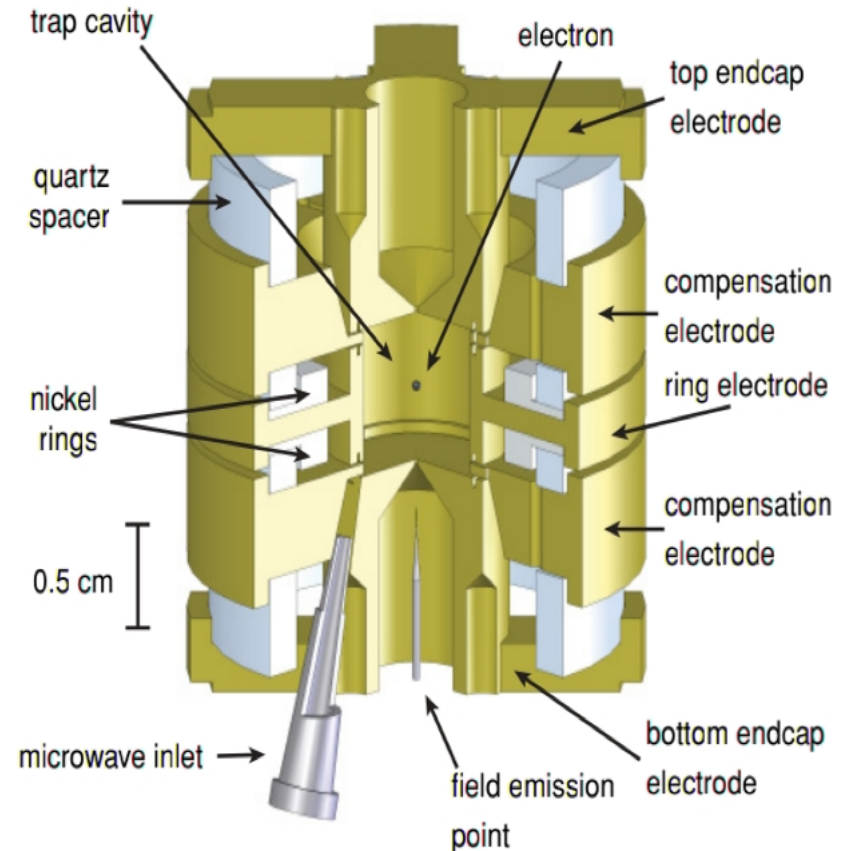


		VALUE ($\times 10^{-11}$)	UNITS
	QED ($\gamma + \ell$)	$116\,584\,718.951 \pm 0.009 \pm 0.019 \pm 0.007 \pm 0.077$	α
	HVP(lo) [20]	$6\,923 \pm 42$	
	HVP(lo) [21]	$6\,949 \pm 43$	
HLbL	HVP(ho) [21]	-98.4 ± 0.7	
HVP H.O.	HLbL	105 ± 26	
HVP L.O.	EW	154 ± 1	
Total SM [20]		$116\,591\,802 \pm 42_{\text{H-LO}} \pm 26_{\text{H-HO}} \pm 2_{\text{other}} (\pm 49_{\text{tot}})$	
Weak H.O.	Total SM [21]	$116\,591\,828 \pm 43_{\text{H-LO}} \pm 26_{\text{H-HO}} \pm 2_{\text{other}} (\pm 50_{\text{tot}})$	
Weak L.O.			



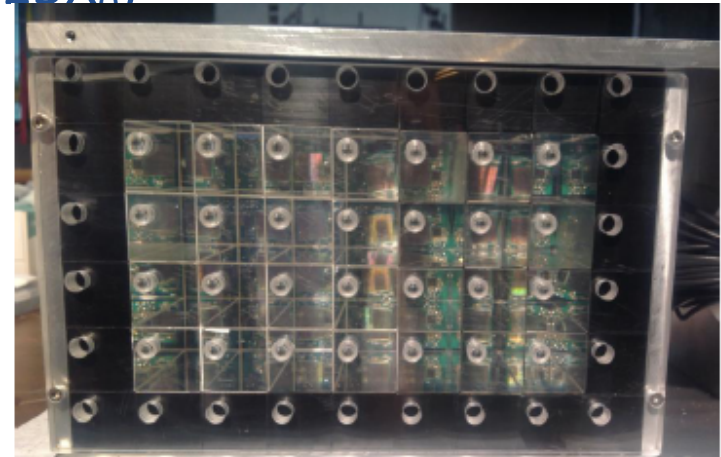
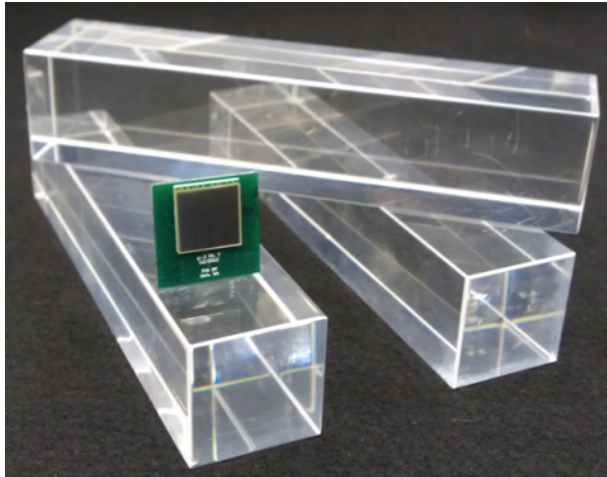
Electron anomaly

- Measurement of a_e is measured to $\sim 1\text{ppb}$
- Experiment utilized Penning trap - homogeneous axial B field quadrupole E field
- One of the most precisely measured properties in fundamental particle physics
- Excellent agreement with SM



Calorimeters

- Each consists of 6 by 9 array of crystals
- Each crystal is $2.5 \times 2.5 \times 14\text{cm} \sim (15X_0)$



Magnetic moments - Classical

- A magnetic moment in a magnetic field will experience a torque

$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

$$\vec{F} = \nabla \vec{\mu} \cdot \vec{B}$$

$$U = \vec{\mu} \cdot \vec{B}$$

$$\vec{\mu} = \frac{e}{2mc} \vec{L}$$

Brookhaven systematics - ω_a

$\sigma_{\text{syst}} \omega_a$	R99	R00	R01
	(ppm)	(ppm)	(ppm)
Pileup	0.13	0.13	0.08
AGS background	0.10	0.01	‡
Lost Muons	0.10	0.10	0.09
Timing Shifts	0.10	0.02	‡
E-field and pitch	0.08	0.03	‡
Fitting/Binning	0.07	0.06	‡
CBO	0.05	0.21	0.07
Gain Changes	0.02	0.13	0.12
Total for ω_a	0.3	0.31	0.21

- For R01 the AGS, timing shifts, E field and vertical oscillations and fitting/binning equaled 0.11ppm

Brookhaven systematics - ω_p

TABLE XI: Systematic errors for the magnetic field for the different run periods. [†]Higher multipoles, trolley temperature and its power supply voltage response, and eddy currents from the kicker.

Source of errors	R99	R00	R01
	[ppm]	[ppm]	[ppm]
Absolute calibration of standard probe	0.05	0.05	0.05
Calibration of trolley probes	0.20	0.15	0.09
Trolley measurements of B_0	0.10	0.10	0.05
Interpolation with fixed probes	0.15	0.10	0.07
Uncertainty from muon distribution	0.12	0.03	0.03
Inflector fringe field uncertainty	0.20	–	–
Others [†]	0.15	0.10	0.10
Total systematic error on ω_p	0.4	0.24	0.17
Muon-averaged field [Hz]: $\tilde{\omega}_p/2\pi$	61 791 256	61 791 595	61 791 400

HVP



- Same data for α_{EM} calculation in SM fits as for HVP
- For the BNL result to match the SM prediction Hadronic estimate would have to be incorrect by 6σ
- If HVP was out by 6σ then Higgs mass starts to become incompatible

based on arxiv: 0809:4062

