

# Dark Matter and Flavor Violation

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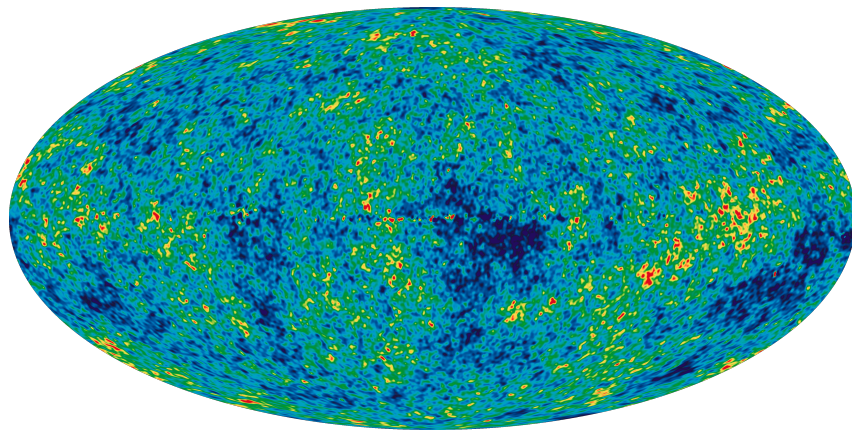
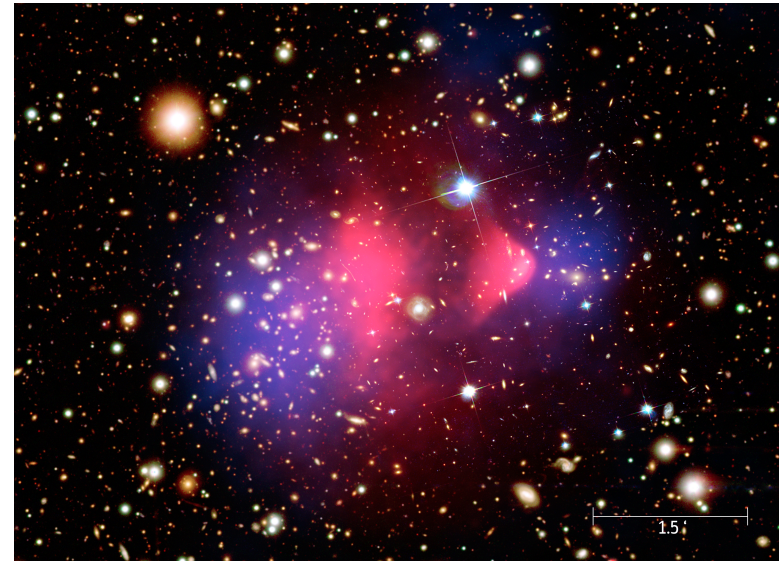
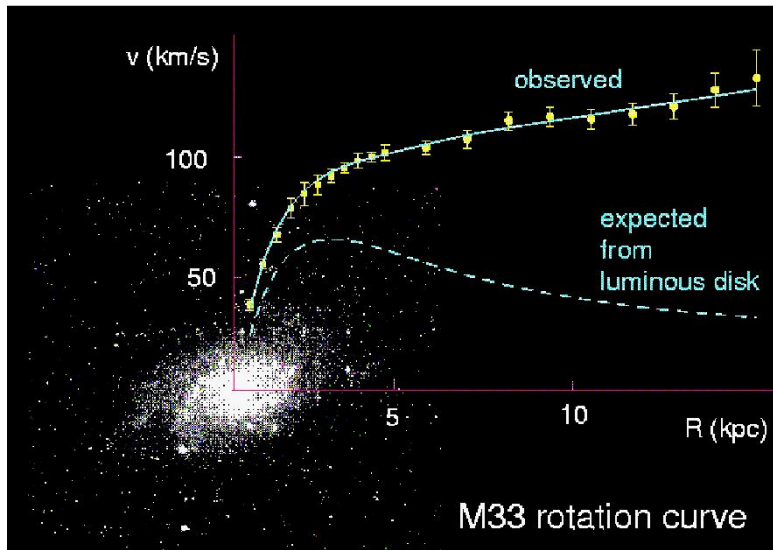
Based on work done with

Jinrui Huang (Los Alamos) and Volodymyr Takhistov (→ UCLA)

JHEP 1602 (2016) 060 [arXiv:1510.04694]

The 2nd International Conference on Charged Lepton Flavor Violation,  
Charlottesville, Virginia, June 20, 2016

# Dark Matter Evidence



Identity of dark matter?  
What is its mass?  
Possible interactions?



# Flavored Dark Matter

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- Dark matter come in multiple copies
- Non-trivial flavor structure in couplings to quarks and leptons
  - distinct signatures
- FCNC constraints
  - universal couplings
  - minimal flavor violation      Batell, Pradler, Spannowsky (2011)
  - beyond MFV: “dark minimal flavor violation”      Agrawal, Blanke, Gemmler (2014)
    - dark matter coupling: only new source of flavor violation
    - implemented in quark sector
    - lepton sector unexplored ⇒ this work

# Minimal Flavor Violation with SM gauge group

$$G_F \equiv G_{QF} \times G_{LF}$$

$$G_{QF} \equiv SU(3)_Q \times SU(3)_U \times SU(3)_D$$

D'Ambrosio, Giudice, Isidori, Strumia (2002);  
Bobeth, Ewerth, Krüger, Urban (2002)

$$G_{LF} \equiv SU(3)_L \times SU(3)_E \quad [m_\nu = 0]$$

Cirigliano, Grinstein, Isidori, Wise (2005)

lepton sector : complication from  $\nu$  mass generation

\* minimal particle content :  $G_{LF}$

\* extended particle content (N) :  $G_{LF} \times SU(3)_N$

⇒ different spurion combinations

⇒ diff. implications for LFV

For simplicity :  $m_\nu = 0$

# Beyond Minimal Flavor Violation

Quark Flavored DM:  $G_{QF} \times SU(3)_X$

Agrawal, Blanke, Gemmler (2014)

DM: Dirac fermion  $\chi \sim 3$  of  $SU(3)_X$

mediator: scalar  $\phi \sim 1$  of  $SU(3)_X$

coupling:  $\lambda \bar{d}_R \chi \phi$ ,  $\lambda \sim (3, \bar{3})$  of  $SU(3)_d \times SU(3)_X$

constraints: meson-antimeson mixing,  
K, B decays,  
.....

Lepton Flavored DM:  $G_{LF} \times SU(3)_X$

MCC, Huang, Takhistov (2015)

DM: Dirac fermion  $\chi \sim 3$  of  $SU(3)_X$

mediator: scalar  $\phi \sim 1$  of  $SU(3)_X$

coupling:  $\lambda \bar{e}_R \chi \phi$ ,  $\lambda \sim (3, \bar{3})$  of  $SU(3)_E \times SU(3)_X$

constraints: cLFV processes ( $\mu \rightarrow e \gamma, \dots$ )

# The Model - Particle Content

	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	$SU(3)_Q$	$SU(3)_U$	$SU(3)_D$	$SU(3)_L$	$SU(3)_E$	$SU(3)_\chi$
$Q_L$	<b>3</b>	<b>2</b>	1/6	<b>3</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>
$u_R$	<b>3</b>	<b>1</b>	2/3	<b>1</b>	<b>3</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>
$d_R$	<b>3</b>	<b>1</b>	-1/3	<b>1</b>	<b>1</b>	<b>3</b>	<b>1</b>	<b>1</b>	<b>1</b>
$L_L$	<b>1</b>	<b>2</b>	-1/2	<b>1</b>	<b>1</b>	<b>1</b>	<b>3</b>	<b>1</b>	<b>1</b>
$e_R$	<b>1</b>	<b>1</b>	-1	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>3</b>	<b>1</b>
$H$	<b>1</b>	<b>2</b>	1/2	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>
$\phi$	<b>1</b>	<b>1</b>	-1	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>
$\chi$	<b>1</b>	<b>1</b>	0	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>3</b>
$Y_U$	<b>1</b>	<b>1</b>	0	<b>3</b>	$\bar{\mathbf{3}}$	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>
$Y_D$	<b>1</b>	<b>1</b>	0	<b>3</b>	<b>1</b>	$\bar{\mathbf{3}}$	<b>1</b>	<b>1</b>	<b>1</b>
$Y_E$	<b>1</b>	<b>1</b>	0	<b>1</b>	<b>1</b>	<b>1</b>	<b>3</b>	$\bar{\mathbf{3}}$	<b>1</b>
$\lambda$	<b>1</b>	<b>1</b>	0	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>3</b>	$\bar{\mathbf{3}}$



# The Model - Lagrangian

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$$\begin{aligned}\mathcal{L} = & \mathcal{L}_{SM} + i\bar{\chi}\not{\partial}\chi - m_\chi\bar{\chi}\chi \\ & - (\lambda_{ij}\bar{e}_R^i\chi_j\phi + \text{h.c.}) \\ & + (D_\mu\phi)^\dagger(D^\mu\phi) - m_\phi^2\phi^\dagger\phi \\ & + \lambda_{H\phi}(\phi^\dagger\phi)(H^\dagger H) + \lambda_{\phi\phi}(\phi^\dagger\phi)^2\end{aligned}$$

flavor  
violating  
interactions

# Dark Matter Stability

$$\mathcal{O}_{DM} \sim \chi \cdots \bar{\chi} \cdots \phi \cdots \phi^\dagger \cdots L \cdots \bar{L} \cdots e_R \cdots \bar{e}_R \\ \cdots \gamma_E \cdots \gamma_E^\dagger \cdots \lambda \cdots \lambda^\dagger \cdots G$$

↳  $SU(3)_c$  inv  
rendering  $\mathcal{O}_{DM}$  inv.  
under  $G_{EW}$

Inv. under flavor  $SU(3)$ :

$$N_\lambda - N_{\bar{\lambda}} = 0 \pmod{3}$$

$$SU(3)_L: N_L - N_{\bar{L}} + N_{\gamma_E} - N_{\gamma_E^\dagger} = 0 \pmod{3}$$

$$SU(3)_E: N_E - N_{\bar{E}} - N_{\gamma_E} + N_{\gamma_E^\dagger} + N_\lambda - N_{\lambda^\dagger} = 0 \pmod{3}$$

$$SU(3)_\chi: N_\chi - N_{\bar{\chi}} + N_\lambda - N_{\lambda^\dagger} = 0 \pmod{3}$$

$$\Rightarrow N_\chi - N_{\bar{\chi}} + N_L - N_{\bar{L}} + N_E - N_{\bar{E}} = 0 \pmod{3}$$

# Dark Matter Stability

$$O_{\text{decay}} : N_\chi = 1, \quad N_{\bar{\chi}} = N_\phi = N_{\phi^\dagger} = 0$$

$$\Rightarrow 1 + N_L - N_{\bar{L}} + N_E - N_{\bar{E}} = 0 \pmod{3}$$

can still be satisfied.  $\Rightarrow$  DM stability: need additional symm.

cf. Quark flavored DM : Batell, Pradler, Spannowsky (2011);  
Agrawal, Blanke, Gemmler (2014)

$$\text{e.g. } \mathbb{Z}_2 : \begin{array}{ll} \phi, \chi & - \\ \text{SM} & + \end{array}$$

inv. under QCD & G<sub>RF</sub> & SU(3)<sub>χ</sub>

$$\Rightarrow N_\chi - N_{\bar{\chi}} - N_\phi - N_{\phi^\dagger} = 0 \pmod{3}$$

$$\text{For } O_{\text{decay}} : 1 \neq 0 \pmod{3}$$

$\Rightarrow$  automatic  $\mathbb{Z}_3$  stabilizing symmetry

• argument works for both MFV and BMFV

# Model Assumptions

## MFV limit:

$$(i) \text{ } SU(3)_X \equiv SU(3)_E : \quad \lambda_{ij} = (\alpha \mathbb{1} + \beta [Y_E^\dagger Y_E])_{ij}$$
$$\mathcal{M}_{ij} = (m_X \mathbb{1} + \Delta_m [Y_E^\dagger Y_E])_{ij}$$

$$(ii) \text{ } SU(3)_X = SU(3)_L : \quad \lambda_{ij} = (Y_E)_{ij}$$
$$\mathcal{M}_{ij} = (m_X \mathbb{1} + \Delta_m [Y_E^\dagger Y_E])_{ij}$$

## BMFV

$\lambda_{ij}$  : unrestricted

$$\mathcal{M}_{ij} = (m_X \mathbb{1} + \Delta_m [\lambda^\dagger \lambda])_{ij}$$

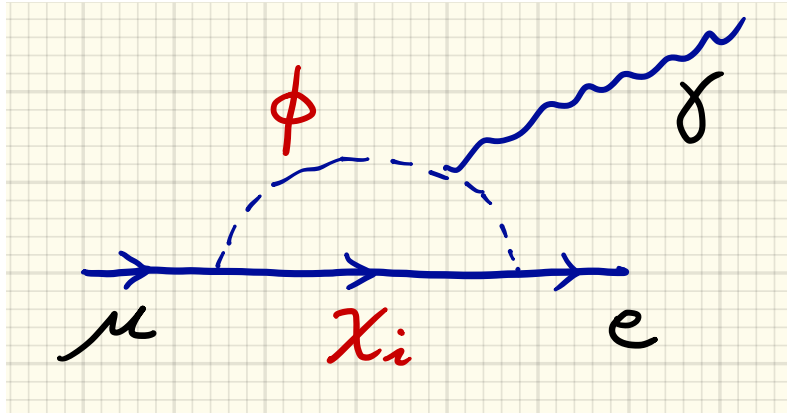
RG induced mass splitting:  $\Delta_m \sim \frac{1}{16\pi^2} \ln\left(\frac{m_X^2}{\Lambda^2}\right)$ ,  $\Lambda$ :  $SU(3)_X$  breaking scale

assume near degenerate  $m_{X_a} \simeq m_X$ ,  $a=1,2,3$

$m_\phi > m_X$  w/  $\phi \rightarrow \chi \bar{e}_R$  (100%)



# Constraints: cLFV



Current exp limit:

$$\text{Br}(\mu \rightarrow e \gamma) < 5.7 \times 10^{-13}$$

(MEG @ PSI, 90% CL)

$$\text{Br}(\mu \rightarrow e \gamma) \propto \frac{1}{G_F^2 m_\phi^4} \left[ \sum_{i=1}^3 (\lambda_{1i}^* \lambda_{2i}) F\left(\frac{m_{\chi_i}^2}{m_\phi^2}\right) \right]^2$$

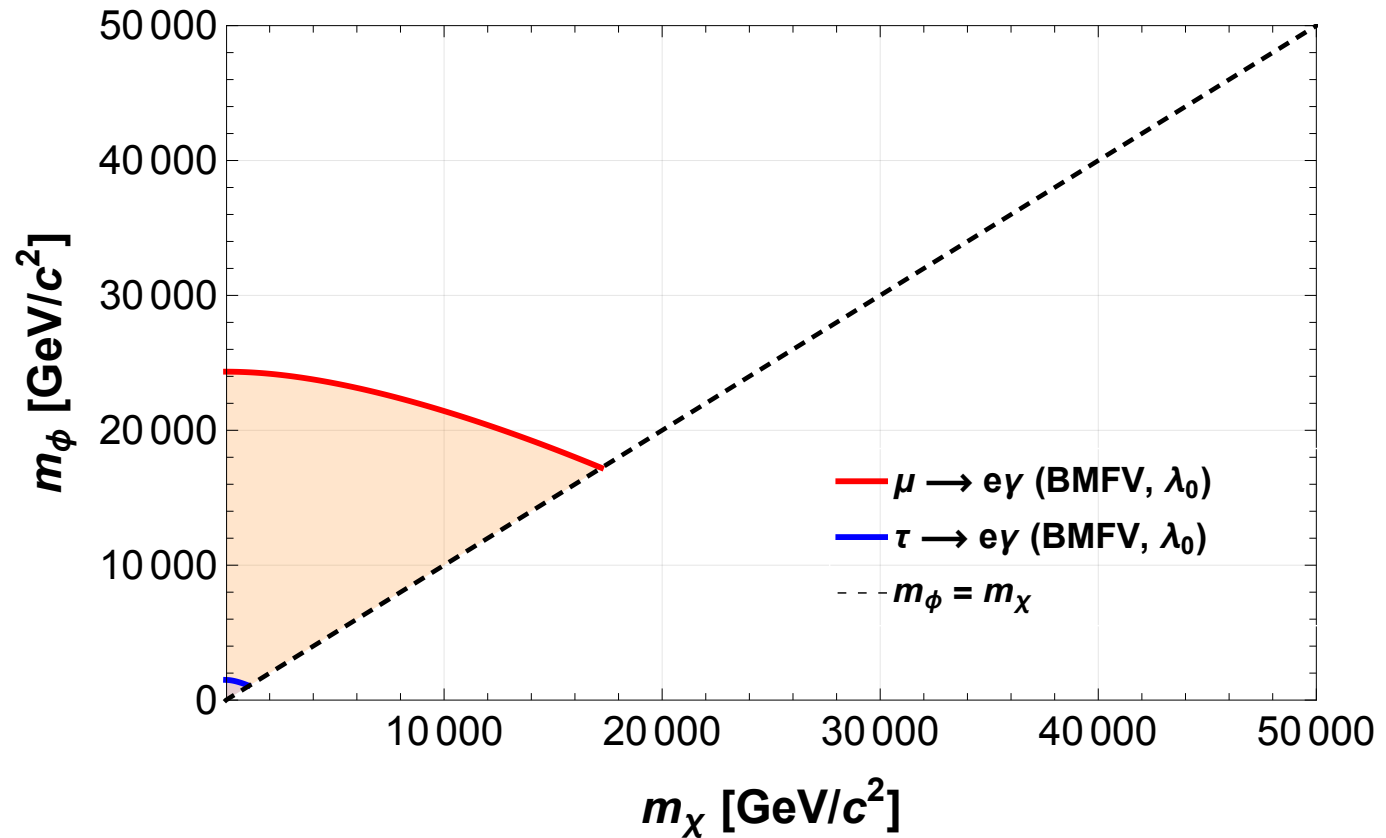
$$\chi = (\chi_1, \chi_2, \chi_3)$$

$$F(x) \sim (1 - 6x + \dots)(1 - x)^{-4}$$

# Constraints: cLFV

“democratic”  
coupling matrix:

$$\lambda_0 = \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}$$

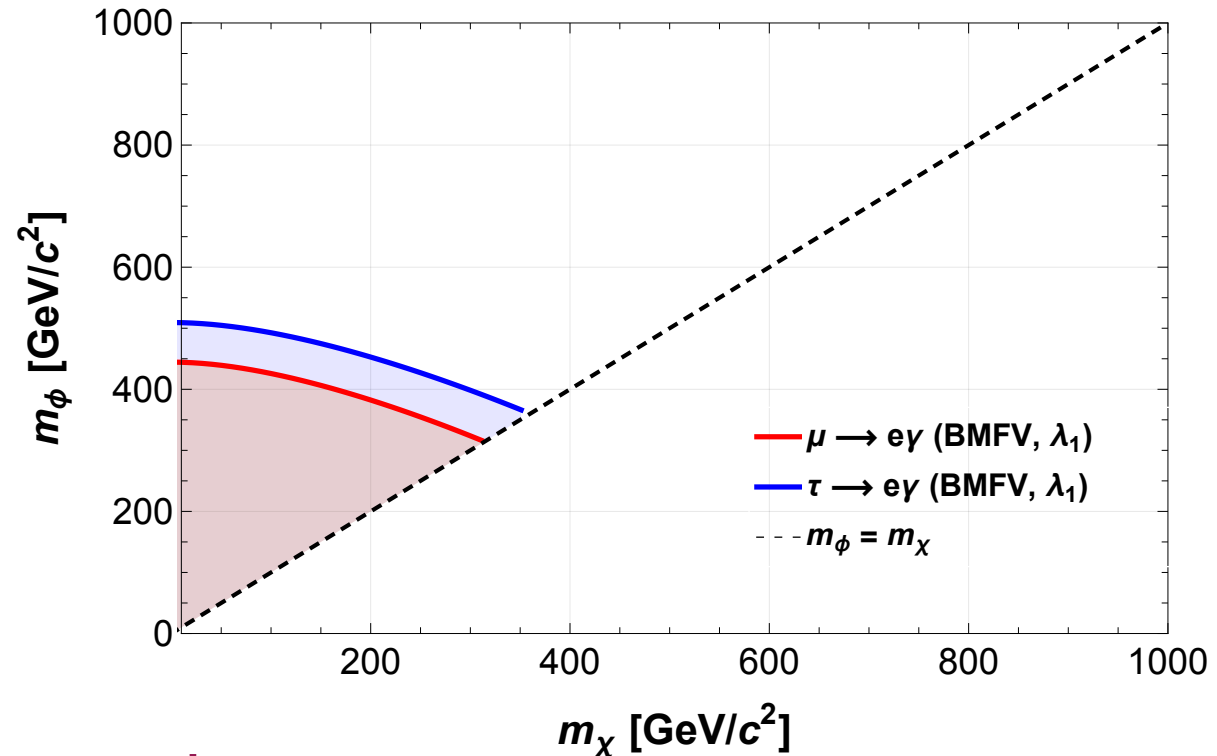


Rather tightly constrained

# Constraints: cLFV

Special form of coupling matrix:

$$\lambda_1 = \begin{pmatrix} 1 & 0 & 10^{-\frac{3}{2}} \\ 0 & 1 & 10^{-\frac{3}{2}} \\ 10^{-\frac{1}{2}} & 10^{-\frac{1}{2}} & 1 \end{pmatrix}$$



Constraints can be loosened

O(1) off diagonal couplings possible, e.g.

$$\lambda_2 = \begin{pmatrix} 0 & 1 & 10^{-\frac{3}{2}} \\ 1 & 0 & 10^{-\frac{3}{2}} \\ 10^{-\frac{1}{2}} & 10^{-\frac{1}{2}} & 0 \end{pmatrix}$$

# Constraints: Muon (g-2)

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$$a_{\mu}^{\text{exp}} \equiv \frac{g_{\mu} - 2}{2} \equiv \frac{\mu_{\mu}}{(e\hbar/2m_{\mu})} - 1 = (11659208.9 \pm 6.3) \times 10^{-10}$$

$$a_{\mu}^{\text{SM}} = (11659182.8 \pm 4.9) \times 10^{-10}$$

$$a_{\mu}^{\text{diff}} = a_{\mu}^{\text{exp}} - a_{\mu}^{\text{SM}} = (26.1 \pm 8.0) \times 10^{-10}$$

**BMFV:**

$$\delta a_{\mu} = -\frac{m_{\mu}^2}{192\pi^2 m_{\phi}^2} \left[ \sum_{i=1}^3 (\lambda_{2i}^* \lambda_{2i}) \right] F_1(x)$$

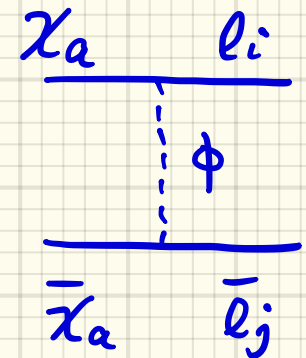
contributions  $< 0 \Rightarrow$  increase the discrepancy



# Constraints: Relic Abundance

multiple DM species w/ distinct masses:

self-annihilation  $\chi_a \bar{\chi}_a \rightarrow l_i \bar{l}_j$



$$\langle \sigma v \rangle_{\chi_a \bar{\chi}_a} \sim \lambda_{ia}^* \lambda_{ja} \lambda_{ia} \lambda_{ja}^* \frac{m_{\chi_a}^2}{(m_{\chi_a}^2 + m_\phi^2)^2}$$

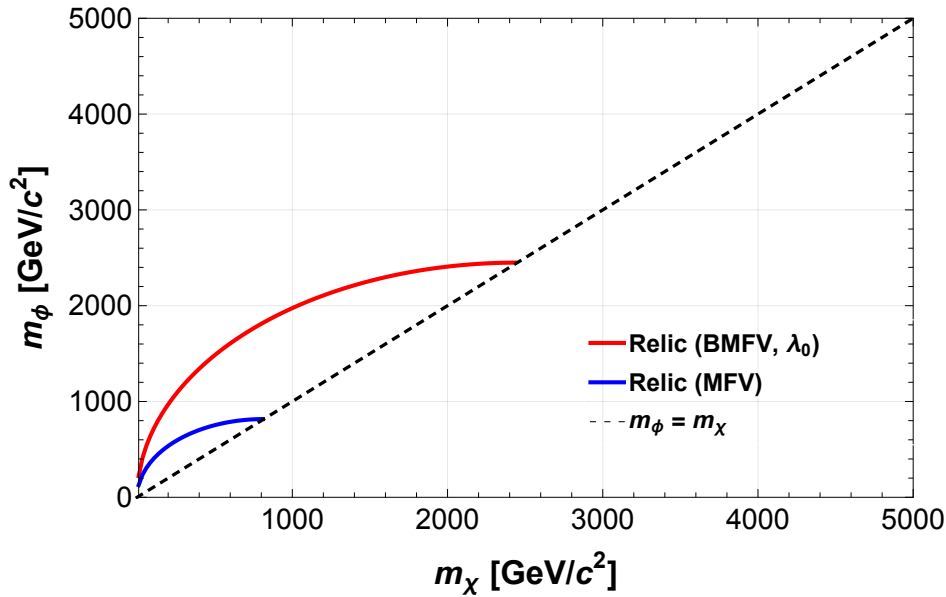
Highly degenerate DM species:  $m_{\chi_a} \simeq m_{\chi_b} \simeq m_{\chi_c}$

$\chi_a l_i \rightarrow \chi_b l_j$  fast  $\Rightarrow$  co-annihilation dominates

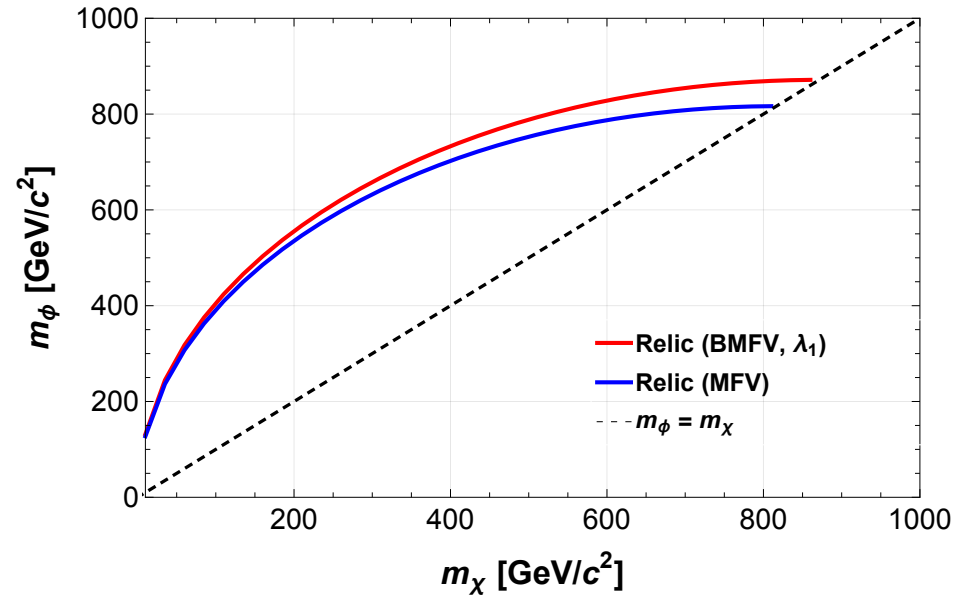
$$\langle \sigma v \rangle_{\text{eff}} \sim \sum_{i,j=e,\mu,\tau} \left[ \sum_{a,b=1,2,3} \langle \sigma v \rangle_{\chi_a \bar{\chi}_b \rightarrow l_i \bar{l}_j} \right]$$

correct relic abundance  $\Rightarrow \langle \sigma v \rangle_{\text{eff}} = 2.2 \times 10^{-26} \text{ cm}^3/\text{s}$

# Constraints: Relic Abundance



BMFV ( $\lambda_0$ ): more channels opened up



BMFV ( $\lambda_1$ ): similar to MFV

# Constraints: DM Direct Detection

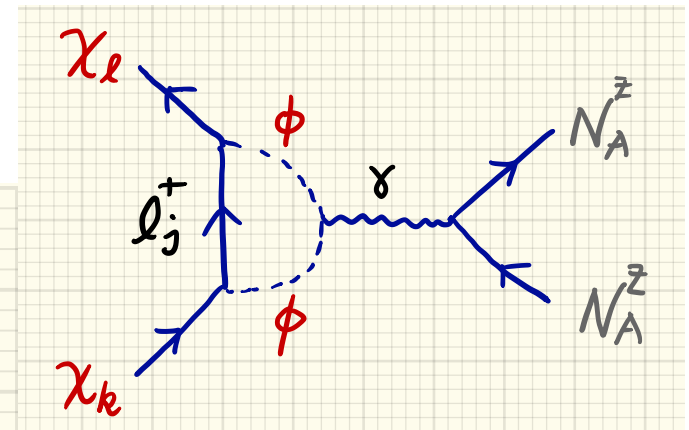
- no direct tree-level couplings of lepton flavored DM to target nucleus
  - DM scattering off target electrons at tree-level Kopp, Niro, Schwetz, Zupan (2009)
  - through photon exchange at one loop: **dominant!**

DM-nucleon cross section:

$$\sigma_{\chi}^N = \sum_{j=e,\mu,\tau} C_j^2 e^2 \left(\frac{Z}{A}\right)^2 \frac{\mu^2}{\pi}$$

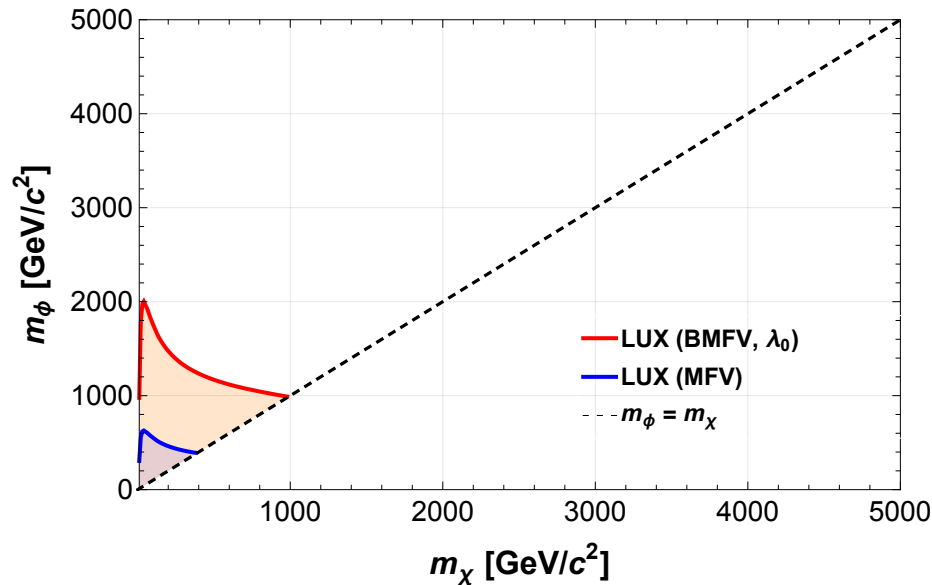
$$C_j \propto \frac{e}{m_\phi^2} \left[ \sum_{k,l=1}^3 (\lambda_{jk}^* \lambda_{jl}) \right] \left[ 1 + \frac{2}{3} \ln\left(\frac{m_{l_j}^2}{m_\phi^2}\right) \right]$$

$$\mu = \frac{m_\chi m_N}{(m_\chi + m_N)}$$

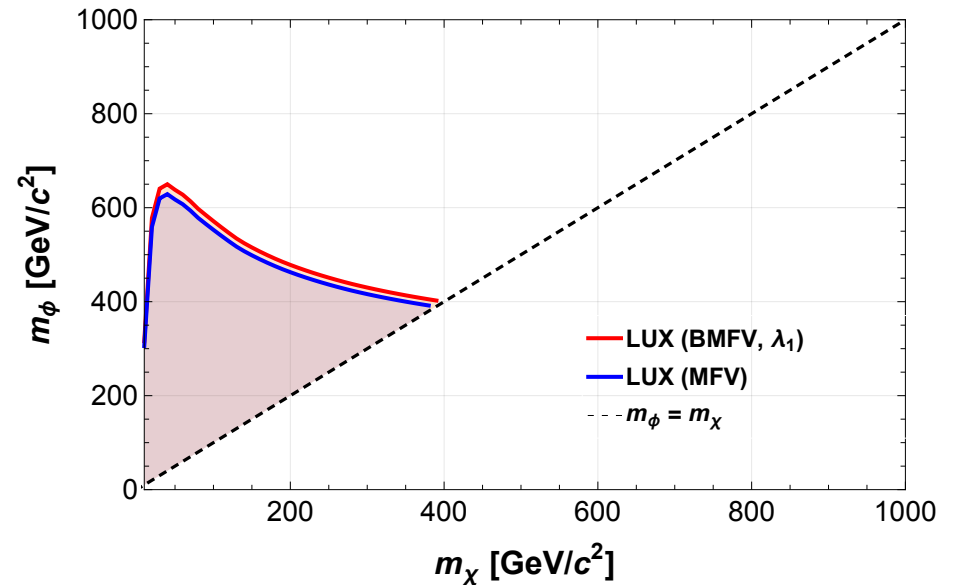


# Constraints: DM Direct Detection

LUX: Xenon,  $A = 129$ ,  $Z = 54$



BMFV ( $\lambda_0$ ): more channels opened up



BMFV ( $\lambda_1$ ): similar to MFV

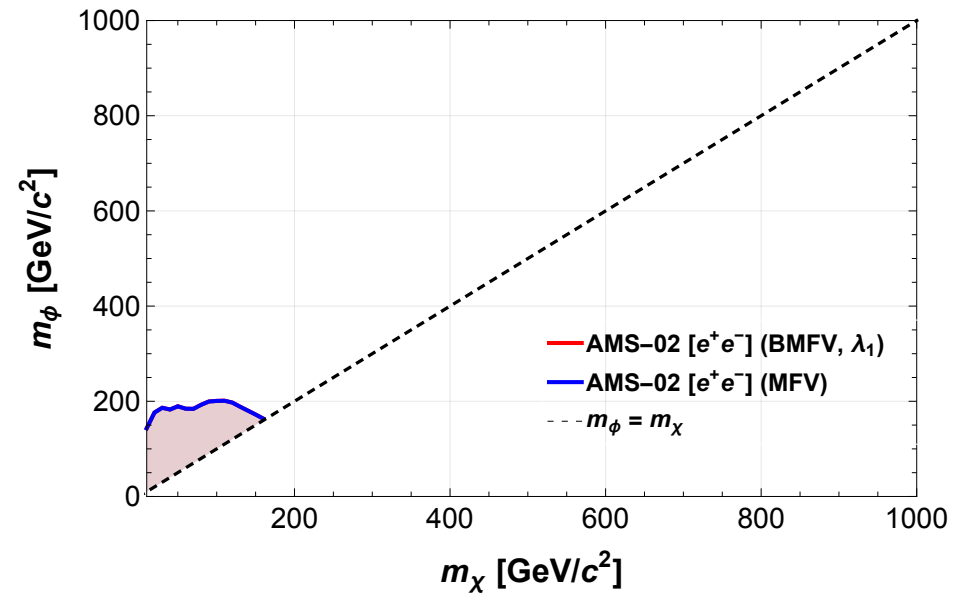
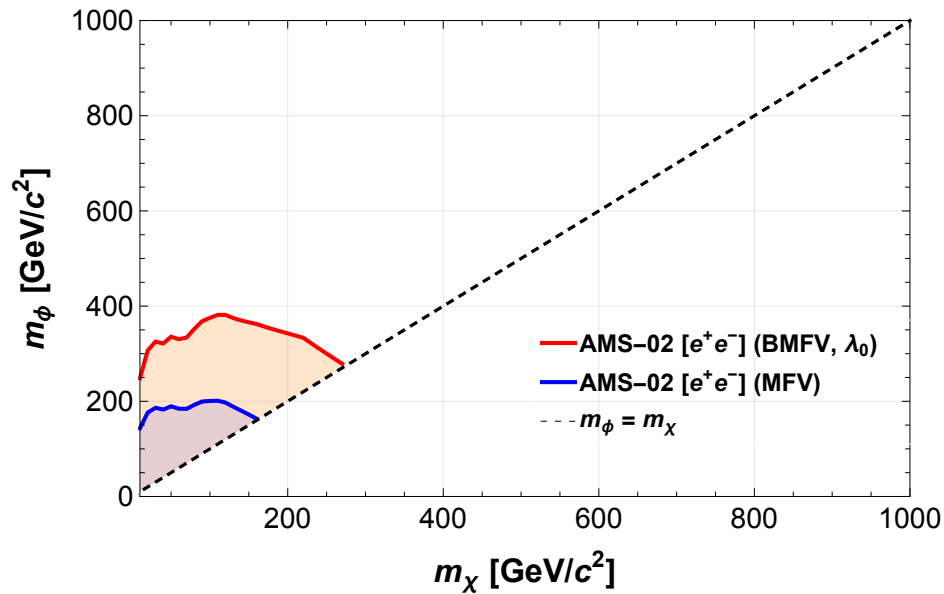


# Constraints: Indirect Detection - AMS

AMS-02 positron excess:

DM annihilation

$$\chi_a \bar{\chi}_b \rightarrow e^+ e^-$$



# Constraints: Indirect Detection - Fermi-LAT

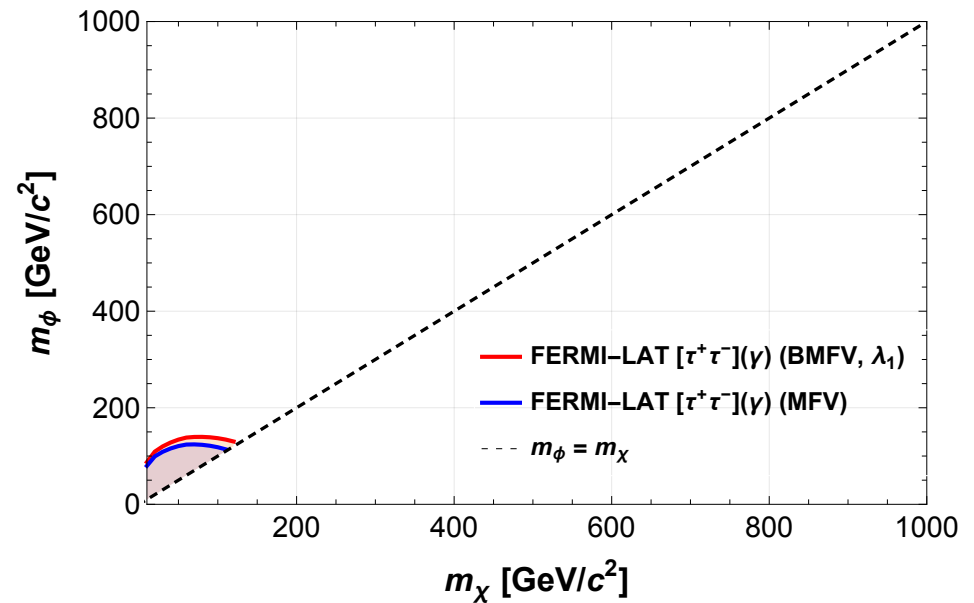
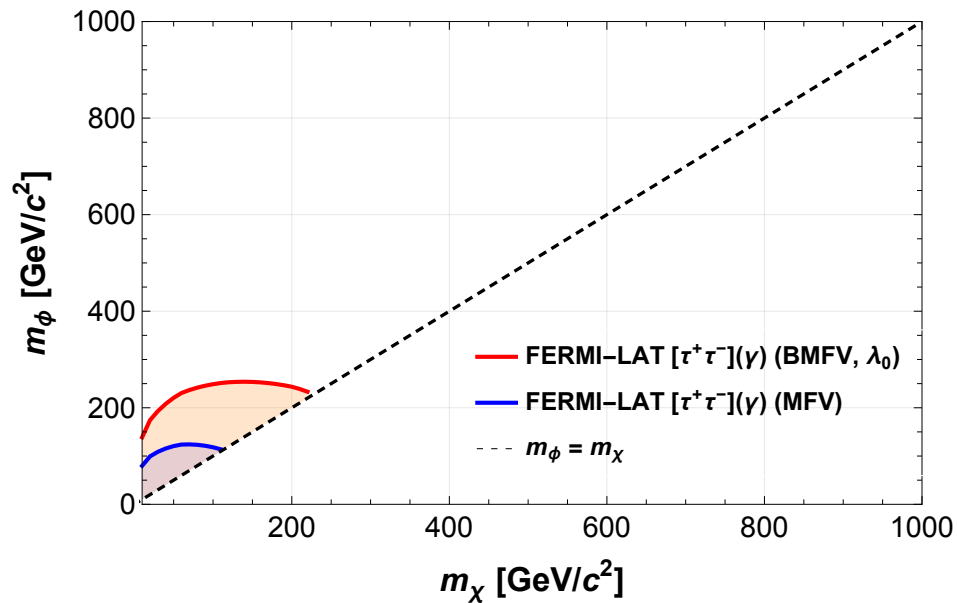
$\gamma$ -ray source:

$$\chi_a \bar{\chi}_b \rightarrow l_i^+ l_j^- \rightarrow \gamma$$

$$\chi_a \bar{\chi}_b \rightarrow \tau^+ \tau^-$$

$$\tau \rightarrow \pi^+ \pi^0 \nu$$

└─  $\gamma\gamma$



# @ Hadron Collider

Drell-Yang Production of  $\phi$ :

$$pp \rightarrow x \bar{x} l^+ l^-$$

signature:

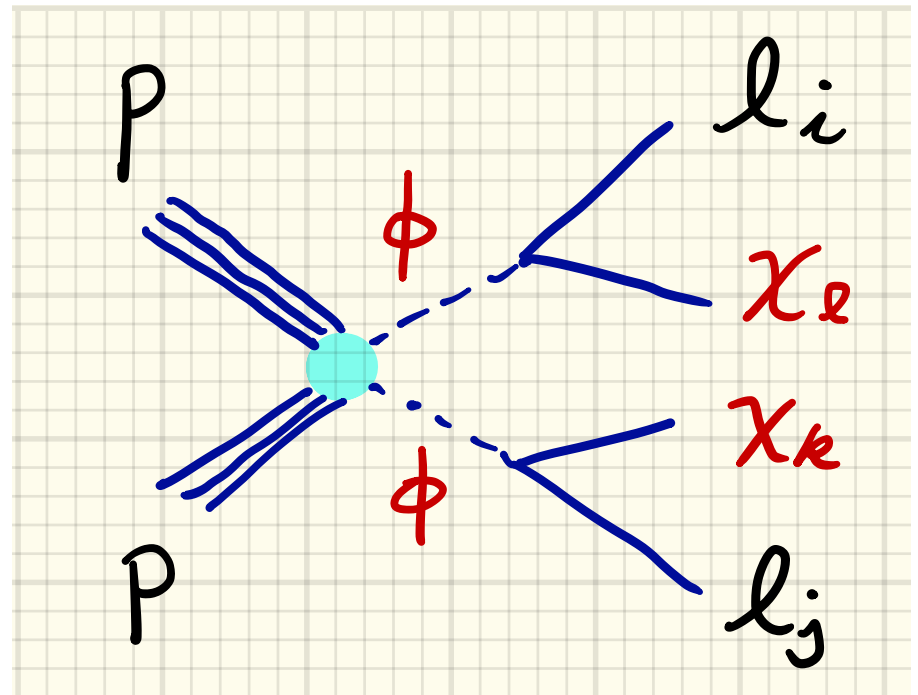
$$l^+ l^- + \text{MET}$$

cf. SUSY Slepton searches

for multi-flavor final states  
(e.g.  $e^\pm \mu^\mp$ )

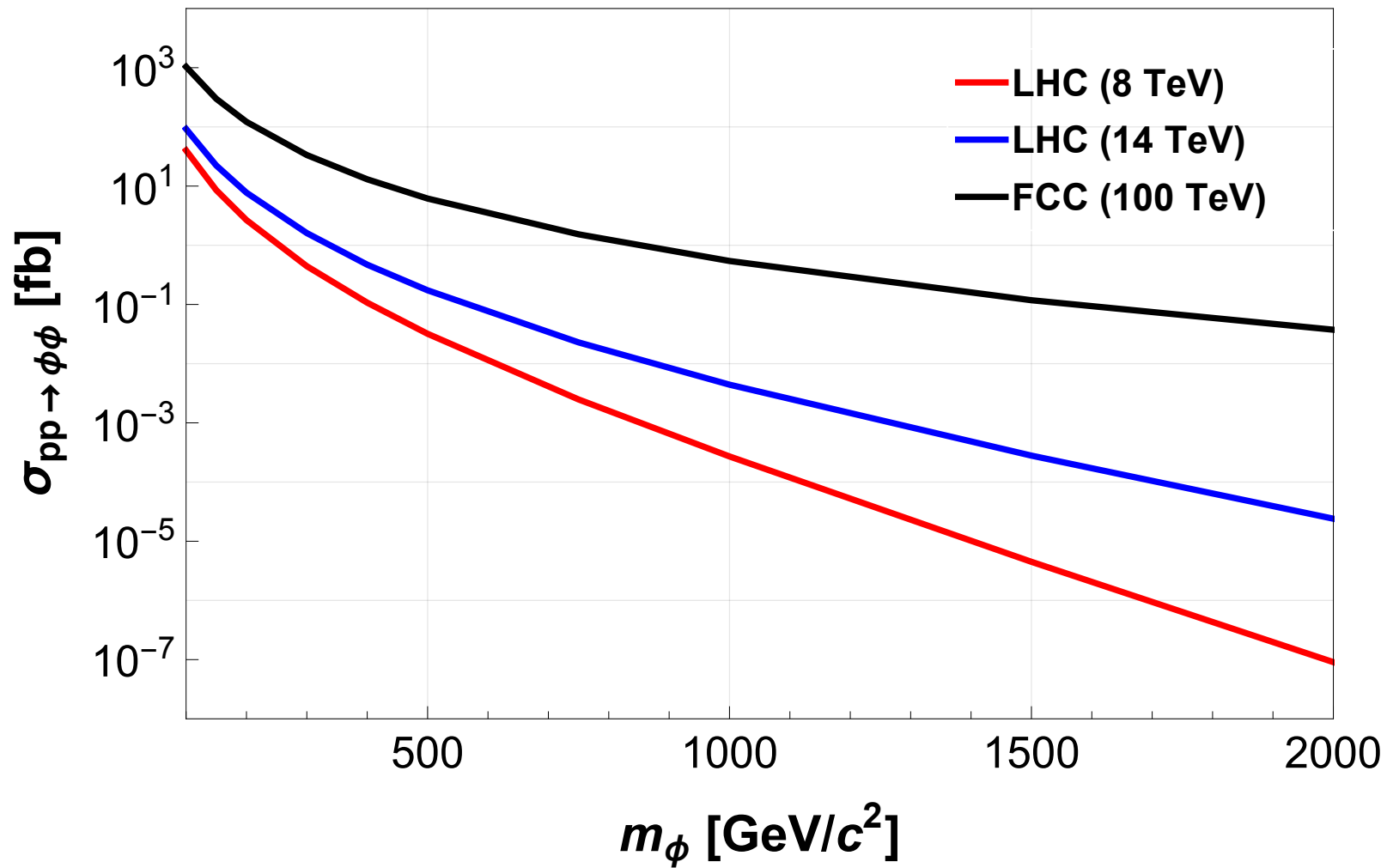
⇒ chargino production  
in SUSY

⇒ different event topologies

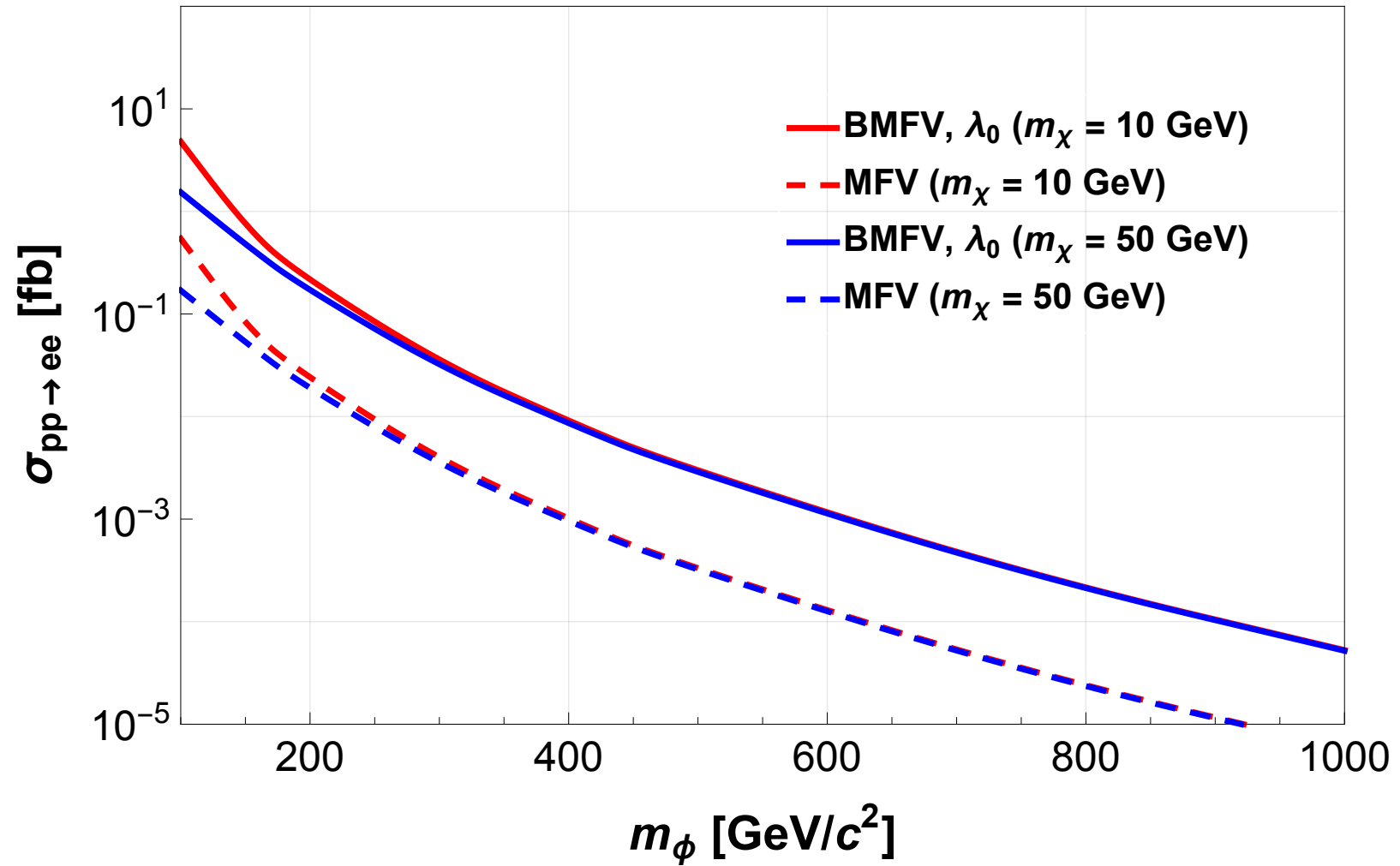


# @ Hadron Collider

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# @ Hadron Collider



# @ Lepton Collider

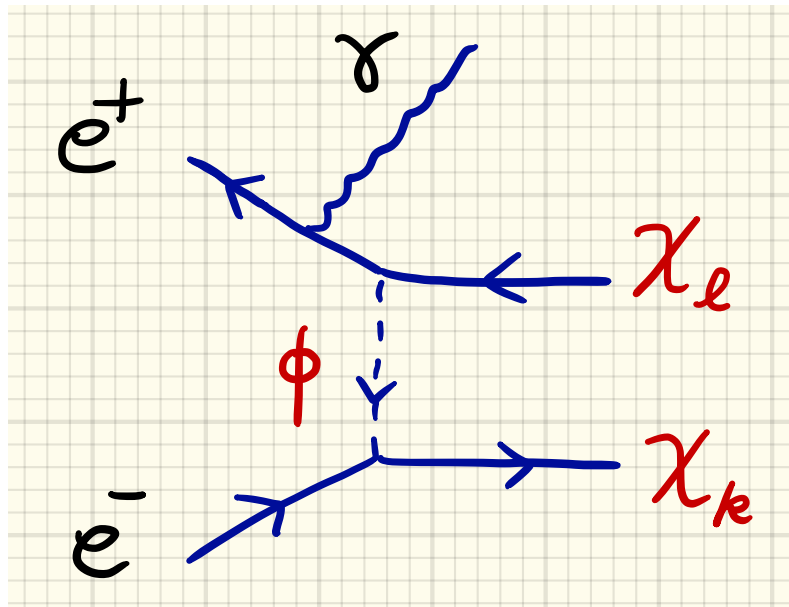
## LEP

- best discovery channel

$$e^+ e^- \rightarrow \chi \bar{\chi} \gamma$$

signature:  $\gamma + \text{MET}$

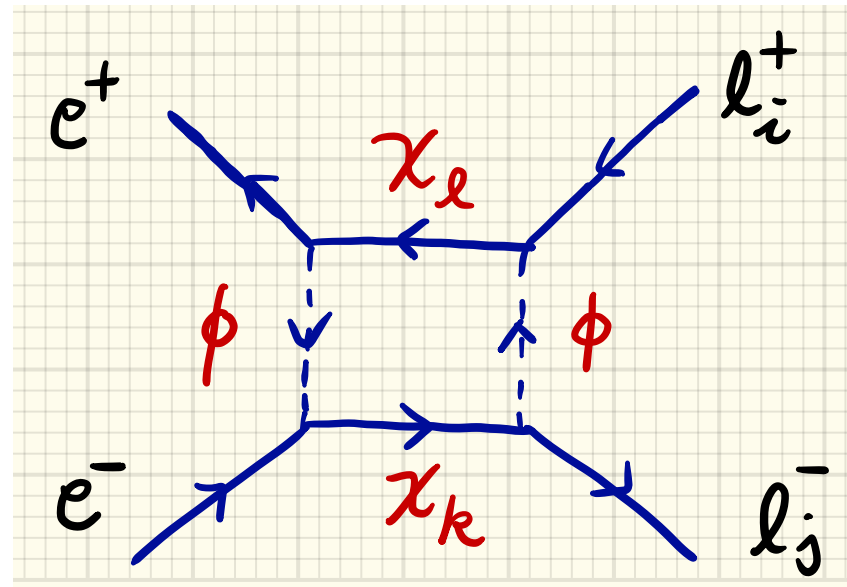
background:  $e^+ e^- \rightarrow Z \gamma$   
 $\hookrightarrow \nu \bar{\nu}$



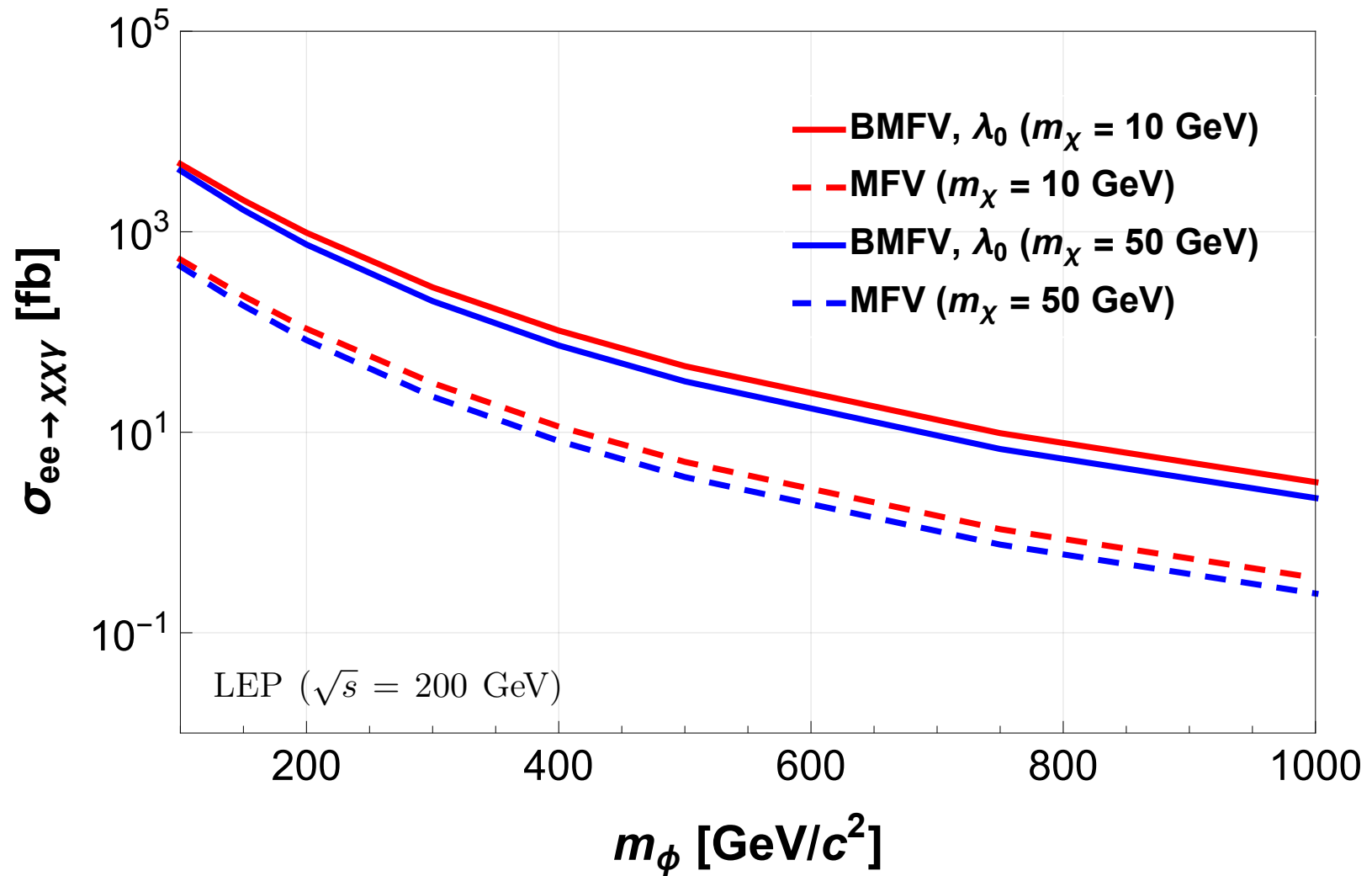
- fermion pair production

$\Rightarrow$  testing flavor violating couplings (e.g.  $e^+ e^- \rightarrow \mu^+ e^-$ )

$\Rightarrow$  signature: multi-flavor lepton final state



# @ Lepton Collider



# Decaying DM

- Without the additional stabilizing symmetry:

$$\chi \rightarrow \text{lepton} + \text{meson}$$

- e.g.

$$\left(\frac{\lambda Y_D Y_U^\dagger}{\Lambda^2}\right) \chi \bar{e}_R d_R \bar{u}_R \implies \chi \rightarrow e^+ \pi^-$$

$$\left(\frac{\lambda Y_E Y_D}{\Lambda^2}\right) \chi d_R \bar{L} \bar{Q} = \left(\frac{\lambda Y_E Y_D}{\Lambda^2}\right) \chi d_R \{\bar{\nu}_L \bar{d}_L - \bar{e}_L \bar{u}_L\} \implies \chi \rightarrow \bar{\nu} \pi^0, \chi \rightarrow e^+ \pi^-$$

$$\left(\frac{\lambda Y_E Y_U^\dagger}{\Lambda^2}\right) \chi \bar{u}_R \bar{L} \bar{Q} = \left(\frac{\lambda Y_E Y_U^\dagger}{\Lambda^2}\right) \chi \bar{u}_R \{\bar{\nu}_L d_L - \bar{e}_L u_L\} \implies \chi \rightarrow \bar{\nu} \pi^0, \chi \rightarrow e^+ \pi^-$$

$$\left(\frac{\lambda Y_E^\dagger}{\Lambda^2}\right) \chi e_R \bar{L} \bar{L} = \left(\frac{\lambda Y_E^\dagger}{\Lambda^2}\right) \chi e_R \{\bar{\nu}_L e_L - \bar{e}_L \bar{\nu}_L\} \implies \chi \rightarrow \bar{\nu} e^+ e^-$$

Mimic RPV  
neutralino  
decays

- DM lifetime

$$\tau_\chi \sim 10^{26} \text{s} \left( \frac{1}{f(\lambda, \lambda^\dagger, Y, Y^\dagger)} \right)^2 \left( \frac{\text{TeV}}{m_\chi} \right)^5 \left( \frac{\Lambda}{10^{15} \text{ GeV}} \right)^4$$

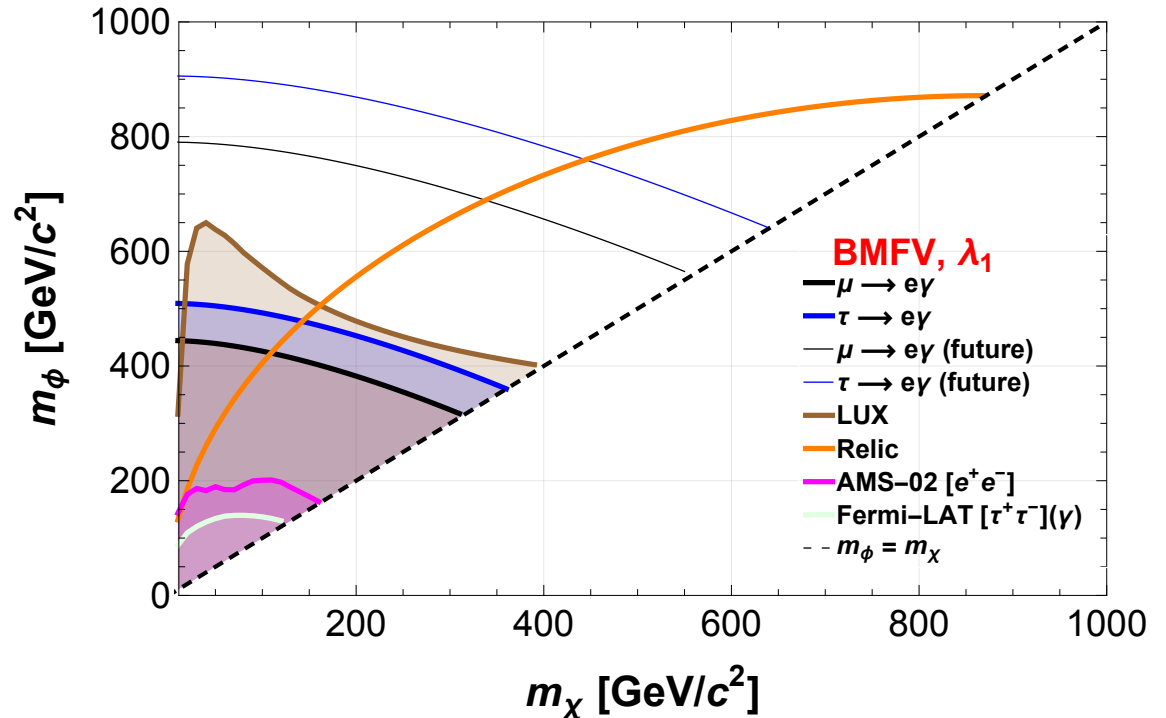
- c.f. age of the universe

$$\tau_{univ.} \sim 4.3 \times 10^{17} \text{s}$$

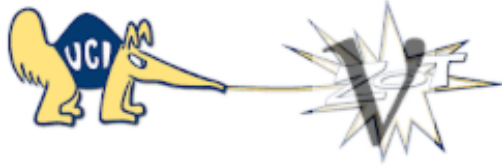


# Summary

- Lepton Flavored DM: beyond MFV with  $SU(3)_\chi$
- Contrast to quark flavored DM case: no automatic stabilizing symmetry
- Most stringent constraints from cLFV processes
- Interesting collider signatures
- UV Theory of (B)MFV?



# 26th International Workshop on Weak Interactions and Neutrinos (WIN2017)



6/19 - 24/2017

University of California, Irvine



Please check back soon for details!

<http://www.physics.uci.edu/WIN2017/index.html>

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