

$$\Gamma_{\text{DIO}} \equiv \Gamma_0 + \mathcal{O}(z^2 a^2)$$