

What does a non-vanishing neutrino mass have to say about the strong CP problem?

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- A new solution with **testable experimental implications at the LHC** (and beyond): smallness of neutrino masses \Rightarrow smallness of the CP-violating parameter $\bar{\theta}$, below the experimental bound $\bar{\theta} < 10^{-10}$.
- Model: A model of **fertile** right-handed neutrinos at the electroweak scale (EW- ν_R model) involving **mirror fermions**. All the ingredients for a strong CP solution already contained in the EW- ν_R model. Mixing between mirror quarks and SM quarks via a Higgs **singlet** \Rightarrow contribution to $\bar{\theta}$ proportional to the **neutrino masses** \Rightarrow naturally small! Experimental implications in the search for mirror quarks!

The Strong CP problem

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- This contributes to the **Electric Dipole Moment of the neutron**:
 $d_n \approx 2.5 \times 10^{-16} \bar{\theta} e - cm$. Experimentally: $|d_n| < 2.9 \times 10^{-26} e - cm!$

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 - Several axion-less scenarios were proposed.

What does a neutrino mass have to do with all that stuff?

The EW-scale ν_R model

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 - Seesaw: $m_\nu \sim m_D^2/M_R$; M_R .

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- Yukawa interactions with quarks:

$$\mathcal{L}_{mass} = g_u \bar{q}_L \tilde{\Phi}_2 u_R + g_d \bar{q}_L \Phi_2 d_R + g_{u^M} \bar{q}_R^M \tilde{\Phi}_{2M} u_L^M + g_{d^M} \bar{q}_R^M \Phi_{2M} d_L^M + H.c.$$

$$\mathcal{L}_{mixing} = g_{Sq} \bar{q}_L \phi_S \bar{q}_R^M + g_{Su} \bar{u}_L^M \phi_S u_R + g_{Sd} \bar{d}_L^M \phi_S d_R + H.c.$$

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- Extra global symmetries: $U(1)_{SM} \times U(1)_{MF}$ (to prevent some unwanted couplings for consistency). These contain the **chiral symmetries**: $U(1)_{A,SM} \times U(1)_{A,MF} \Rightarrow \mathcal{L}_{mixing}$ is invariant under: $q \rightarrow \exp(i\alpha_{SM}\gamma_5)q$; $q^M \rightarrow \exp(i\alpha_{MF}\gamma_5)q^M$; $\phi_S \rightarrow \exp(-i(\alpha_{SM} + \alpha_{MF}))\phi_S$.

Neutrino mass and Strong CP

- **Chiral rotations:** $\theta_{QCD} \rightarrow \theta_{QCD} - (\alpha_{SM} + \alpha_{MF})$. Can be rotated to **zero!** Next, compute $ArgDetM$ (actually $\theta_{Weak} = ArgDet(\mathcal{M}_u \mathcal{M}_d)$)

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- Mass matrices: $\mathcal{M}_u = \begin{pmatrix} m_u & |g_{Sq}|v_S \exp(i\theta_q) \\ |g_{Su}|v_S \exp(i\theta_u) & M_u \end{pmatrix},$

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- Straightforward calculations give:

$$\bar{\theta} = \theta_{Weak} \approx \frac{-(r_u \sin(\theta_q + \theta_u) + r_d \sin(\theta_q + \theta_d))}{1 - r_u \cos(\theta_q + \theta_u) - r_d \sin(\theta_q + \theta_d)}$$

$$r_u = \frac{|g_{Sq}| |g_{Su}| v_S^2}{m_u M_u} = \left(\frac{|g_{Sq}| |g_{Su}|}{g_{S_l}^2} \right) \left(\frac{m_D^2}{m_u M_u} \right)$$

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- Putting in some reasonable numbers

$$\theta_{Weak} < -10^{-8} \left\{ \left(\frac{|g_{Sq}| |g_{Su}|}{g_{SI}^2} \right) \sin(\theta_q + \theta_u) + \left(\frac{|g_{Sq}| |g_{Sd}|}{g_{SI}^2} \right) \sin(\theta_q + \theta_d) \right\}$$

Neutrino mass and Strong CP: Experimental implications

- The EW-scale ν_R model: (a) satisfies the EW-precision data, e.g. positive contributions to S from mirror fermions get cancelled by negative contributions from triplet scalars; (b) Two very distinct scenarios (**Dr Jekyll** and **Mr Hyde**) that can accommodate, in terms of signal strengths, the 125-GeV scalar; (c) Constraints from $\mu \rightarrow e\gamma$ and $\mu 2e$ conversion imply $g_{SI} < 10^{-4} \Rightarrow$ Decays of **mirror leptons** at **DISPLACED VERTICES!**

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- Another important collider implication: **Like-sign dileptons** from ν_R decays at **DISPLACED VERTICES.**

Neutrino mass and Strong CP: Experimental implications

- The EW-scale ν_R model: (a) satisfies the EW-precision data, e.g. positive contributions to S from mirror fermions get cancelled by negative contributions from triplet scalars; (b) Two very distinct scenarios (**Dr Jekyll** and **Mr Hyde**) that can accommodate, in terms of signal strengths, the 125-GeV scalar; (c) Constraints from $\mu \rightarrow e\gamma$ and $\mu 2e$ conversion imply $g_{SI} < 10^{-4} \Rightarrow$ Decays of **mirror leptons** at **DISPLACED VERTICES!**
- To satisfy $\bar{\theta} < 10^{-10}$, one requires $|g_{Sq}| \sim |g_{Su}| \sim |g_{Sd}| \sim 0.1g_{SI} \Rightarrow$ Decays of **mirror quarks** at **DISPLACED VERTICES!**
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- Other implications are under investigation.

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- There seems to be a **collusion** between **neutrino physics** and **QCD** to make **Strong CP great again!** **Stay tune!**

Some papers

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- Searches: S. Chakdar, K. Ghosh, V. Hoang, P. Q. Hung and S. Nandi, Phys. Rev. D **93**, no. 3, 035007 (2016) doi:10.1103/PhysRevD.93.035007 [arXiv:1508.07318 [hep-ph]], S. Chakdar, K. Ghosh, V. Hoang, P. Q. Hung and S. Nandi, Phys. Rev. D **95**, no. 1, 015014 (2017) doi:10.1103/PhysRevD.95.015014 [arXiv:1606.02500 [hep-ph]].

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- Need to restore the Custodial Symmetry! Another triplet Higgs scalar $\xi = (3, Y/2 = 0)$ such that

$$\chi = \begin{pmatrix} \chi^0 & \xi^+ & \chi^{++} \\ \chi^- & \xi^0 & \chi^+ \\ \chi^{--} & \xi^- & \chi^{0*} \end{pmatrix}$$

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- Note: The magnitude of the magnetic moment for the electron or muon is $\mu = (1 + a) \frac{q}{2m}$ where $a = \frac{g-2}{2}$. $a^{(4)} \sim \frac{1}{45} \left(\frac{m}{m_{heavy}}\right)^2 \left(\frac{\alpha}{\pi}\right)^2$. For $m_{heavy} \sim 200 \text{ GeV}$, $a_e^{(4)} \sim 10^{-18}$ and $a_\mu^{(4)} \sim 10^{-14}$.

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- Under the custodial symmetry group $SU(2)_D$, these **10 physical degrees of freedom** decompose as

$$\text{five-plet (quintet)} \rightarrow H_5^{\pm\pm}, H_5^{\pm}, H_5^0;$$

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$$\text{two singlets} \rightarrow H_1^0, H_1^{0'}$$

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- These scalars make important contributions to the electroweak precision parameters which offset those of the mirror fermions!