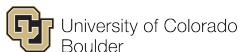


# Study of meson spectroscopy of a lattice SU(4) gauge BSM model.

**Venkitesh Ayyar**<sup>1</sup> Thomas Degrand<sup>1</sup> Daniel Hackett<sup>1</sup>  
William Jay<sup>1</sup> Ethan Neil<sup>1,3</sup> Benjamin Svetitsky<sup>2</sup> Yigal Shamir<sup>2</sup>.

<sup>1</sup>University of Colorado, Boulder, <sup>2</sup>Tel Aviv University, <sup>3</sup>RIKEN-BNL Research Center.



## TaCo collaboration

Tue, Aug 1, DPF 2017, Fermilab, Batavia, IL, USA.

Work supported by grants from the DOE.

Computational work done using resources provided by Fermilab and local Janus cluster.



# Hierarchy problem

## Unaesthetic features of SM

- Higgs potential introduced for SSB.
- Higgs is light ( $\sim 100\text{GeV}$ ) compared to  $\Lambda_{Planck}$ .
- Higgs is a scalar.

## Higgs mass Hierarchy problem

- Higgs mass  $\sim \Lambda_{EW}$ .
- Any coupling to the Higgs introduces corrections  $O(\Lambda_{UV}^2)$  to Higgs mass, due to radiative corrections.
- At higher scales, parameters have to be fine-tuned to get observed Higgs mass.

Is Higgs a composite pNGB in a new strong sector?

# Composite Higgs <sup>2</sup>

- Introduce a new strong sector (Hypercolor).
- Induce chiral symmetry breaking to get pNGBs one of which is the Higgs.
- Symmetry breaking  $G \rightarrow H$ , with Higgs doublet in the  $G/H$  coset.
- Weak sector  $SU(2)_L \times U(1)_Y \subset H$ .
- Higgs potential generated dynamically by coupling to SM fields.

## Partial compositeness <sup>1</sup>

- Linear couplings of top quark to a baryon in the new sector gives fermion mass.

Ferretti-Karateev in 2014 classified UV completions.

<sup>2</sup>Dugan, Georgi, Kaplan, Nucl. Phys. B254, 299 (1985)

<sup>1</sup>Kaplan, Nuclear Physics B365, (1991)

# Ferretti's model(1404.7137)

- UV completion with partial compositeness.
- $SU(4)$  gauge theory with 2 representations.

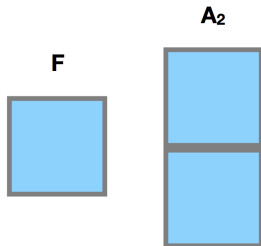
## Fermion content

- 5 sextet( $A_2$ ) Majorana fermions.
- 6 fundamental( $F$ ) Weyl fermions.

## Symmetry breaking

- $SU(5)/SO(5)$  in  $A_2$  rep.
- $(SU(3)_L \times SU(3)_R) / SU(3)$  in  $F$  rep.

The Higgs doublet lives in the  $SU(5)/SO(5)$  coset.



## Our Lattice model

SU(4) gauge theory with modified fermion content

- 2 flavors of sextet  $A_2$  Dirac fermions.
- 2 flavors of fundamental  $F$  Dirac fermions.

### Symmetry breaking

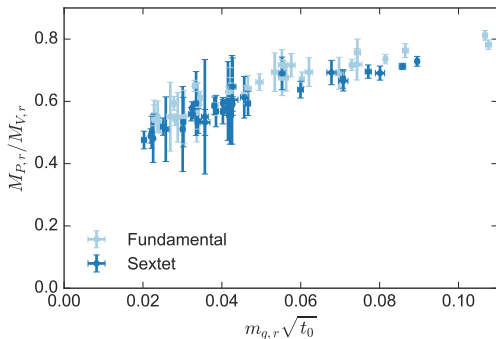
- $SU(4)/SO(4)$  in  $A_2$  rep.
- $(SU(2)_L \times SU(2)_R) / SU(2)$  in  $F$  rep.
  
- 3 coupling constants :  $\beta, \kappa_4, \kappa_6$ .
- Expected to capture qualitative features of Ferretti's model.

## Lattice details

- Simulations on lattice sizes  $16^3 \times 32$  and  $16^3 \times 18$ .
- About 40 ensembles.
- Multi-rep MILC code by Yigal Shamir
- Studied Pseudo-scalar and vector mesons.
- Extract meson masses using two-point correlation functions.
- Using Wilson flow method to set the scale.

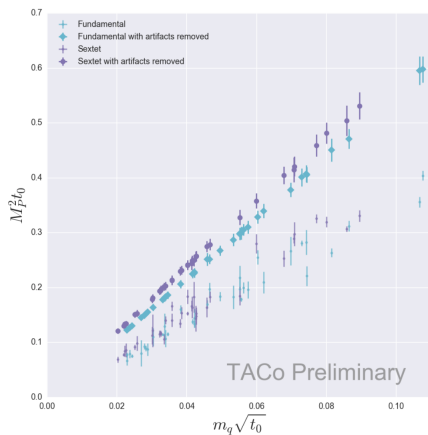
## Ensemble overview

- Lattice results obtained in terms of lattice spacing  $a$ .
- Using Wilson flow scale  $t_0$  to remove  $a$  dependence.
- Look at  $M_P/M_V$  vs  $m_q$ .
- Quark mass  $m_q$  obtained using Axial Ward identity.
- Relatively heavy mesons.
- Similar behavior for both representations.



# Leading order ChiPt

- Upto leading order in ChiPt,  $M_{pi}^2 \sim m_q$ .
- Removed lattice artifacts obtained using Wilson ChiPt.
- Linear behavior for both reps.



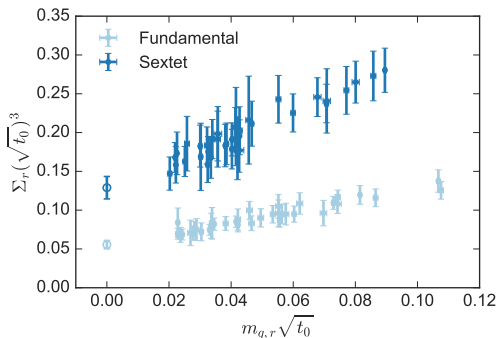


## Comparison with NLO ChiPT

- Useful to compare lattice results to NLO ChiPT.
- Multirep NLO ChiPT worked out by DeGrand, Goltermann, Neil, Shamir (1605.07738).
- $M_{P4}, F_{P4}, M_{P6}, F_{P6}$  depend on a set of low energy constants(LECs).
- Simultaneous fit to all four quantities.
- Find a good fit ( $\chi^2/DOF \sim 0.5$ )

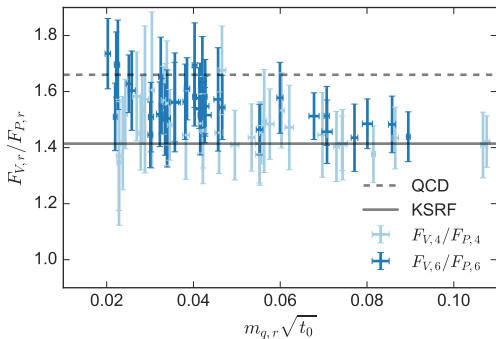
# Condensates

- Two condensates, one for each representation.
- Compute it indirectly using  $\hat{\Sigma}_r = \frac{M_{P,r}^2 F_{P,r}^2}{2m_{q,r}}$
- Chiral limit values computed using ChiPt.
- Condensate ratio  $\Sigma_6/\Sigma_4$ 
  - ▶ Lattice calc  $\rightarrow 2.2$
  - ▶ Large N scaling  $\rightarrow \frac{\dim(A_2)}{\dim(F)} \sim \frac{N^2/2}{N} \sim 2$ .



## Decay constants

- KSRF <sup>3,4</sup>related  $F_V$  and  $F_P$  using current algebra and vector meson dominance.  
 $F_V = \sqrt{2}F_P$ .
- Can compare  $F_V$  and  $F_P$  in a fixed representation.
- QCD experiment:  $F_V/F_P = 216\text{MeV}/130\text{MeV} = 1.66$ .
- For both reps, our results similar to QCD.



<sup>3</sup>Kawarabayashi and Suzuki, PRL 16, 255 (1966).

<sup>4</sup>Riyazuddin and Fayyazuddin, PRL 147, 1071 (1966).

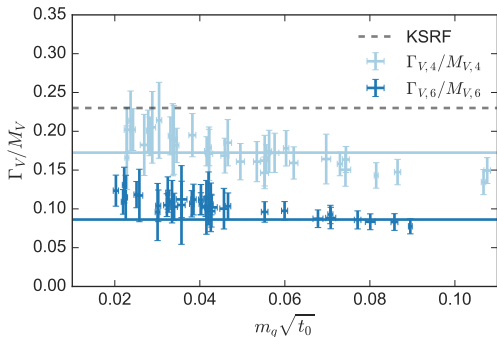
## Decay widths

- KSRF also predicted coupling strength  

$$g_{VPP} = \frac{M_V}{F_P}.$$
- Allows tree-level estimation of vector decay width:  

$$\Gamma_V = g_{VPP}^2 M_V / 48\pi.$$
- KSRF prediction  

$$\frac{\Gamma_V}{M_V} \sim \frac{M_V^2}{48\pi F_P^2}.$$
- $\frac{\Gamma_V}{M_V} \text{ QCD} = 0.19.$
- Our states narrower than QCD.
- $\frac{\Gamma_{V6}}{M_{V6}} = 0.13$  ,  $\frac{\Gamma_{V4}}{M_{V4}} = 0.18.$



# Conclusions and Outlook

## Conclusions

- Zero temperature study of lattice SU(4) gauge theory BSM model with fermions in multiple reps.
- Meson spectroscopy data consistent with ChiPT.
- KSRF relations hold similar to QCD.
- Theory appears QCD-like.

## Future direction

- Baryon spectroscopy.
- Coupling between the two irreps.
  - ▶ LECs unconstrained.
  - ▶ Greater precision might help constrain these.
- Existence of exotic pNGB  $\zeta$  meson.
  - ▶ Theory has non-anomalous  $U(1)_A$
  - ▶ SSB  $\implies$  scalar, singlet  $\zeta$  meson.

# THANK YOU

# Back-up slides

## Wilson flow to set the scale

- Wilson flow: a smearing technique to smooth-out configurations.
- Also, a method to set the scale<sup>5</sup>.
- $t_0 \langle E(t_0) \rangle = M(N)$ , where  $E(t) = \frac{1}{4} G_{t,\mu\nu} G_{t,\mu\nu}$ .
- For QCD (N=3),  $M = 0.3$ , corresponding to  $\sqrt{t_0} = 0.14 fm$ .
- For SU(4),  $t_0 \langle E(t_0) \rangle = 0.3 \times \frac{4}{3} = 0.4$ ,

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<sup>6</sup>M. Luscher, JHEP 08, 071 (2010)