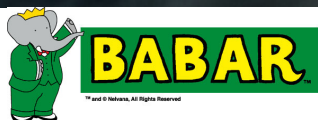


# Recent Measurements of Exclusive Hadronic Cross Sections at *BABAR* and the Implications for the Muon $g-2$ Calculation

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Meeting of the Division of Particles and Fields  
of the American Physical Society  
Fermilab, Batavia, IL  
31 July – 03 August 2017



# Outline

- The muon g-2 puzzle
- *BABAR* and ISR studies
- Recent hadronic cross section measurements

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0, \quad \pi^+\pi^-\eta \quad \text{To Be Submitted}$$

$$e^+e^- \rightarrow K_S^0K_L^0\pi^0, \quad K_S^0K_L^0\eta, \quad K_S^0K_L^0\pi^0\pi^0 \quad \text{Phys. Rev. D95 (2017) 052001.}$$

$$e^+e^- \rightarrow K_S^0K^\pm\pi^\mp\pi^0, \quad K_S^0K^\pm\pi^\mp\eta \quad \text{Phys. Rev. D95 (2017) 092005.}$$

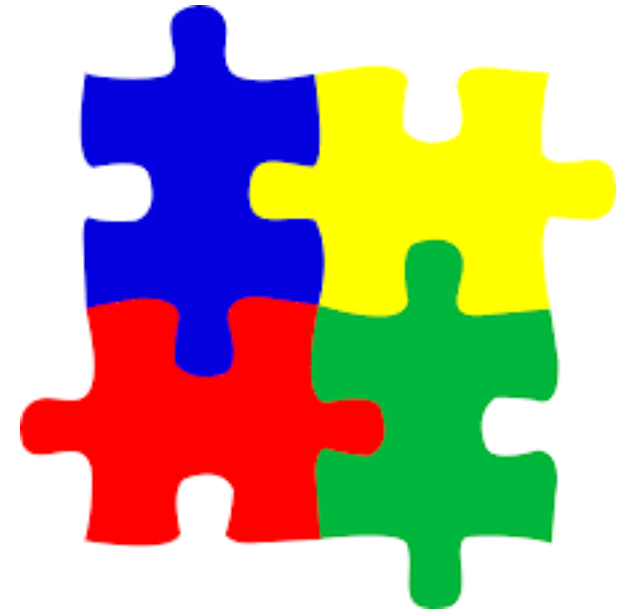
- Implications for muon g-2

# The muon g-2 puzzle

- The magnetic dipole moment for Dirac particles can be written  $\vec{\mu} = g \frac{e\hbar}{2mc} \vec{S}$ 
  - Dirac equation predicts  $g = 2$  exactly
- Corrections from higher order processes cause  $g$  to differ from 2 by a small amount. Characterize with anomalous magnetic moment:

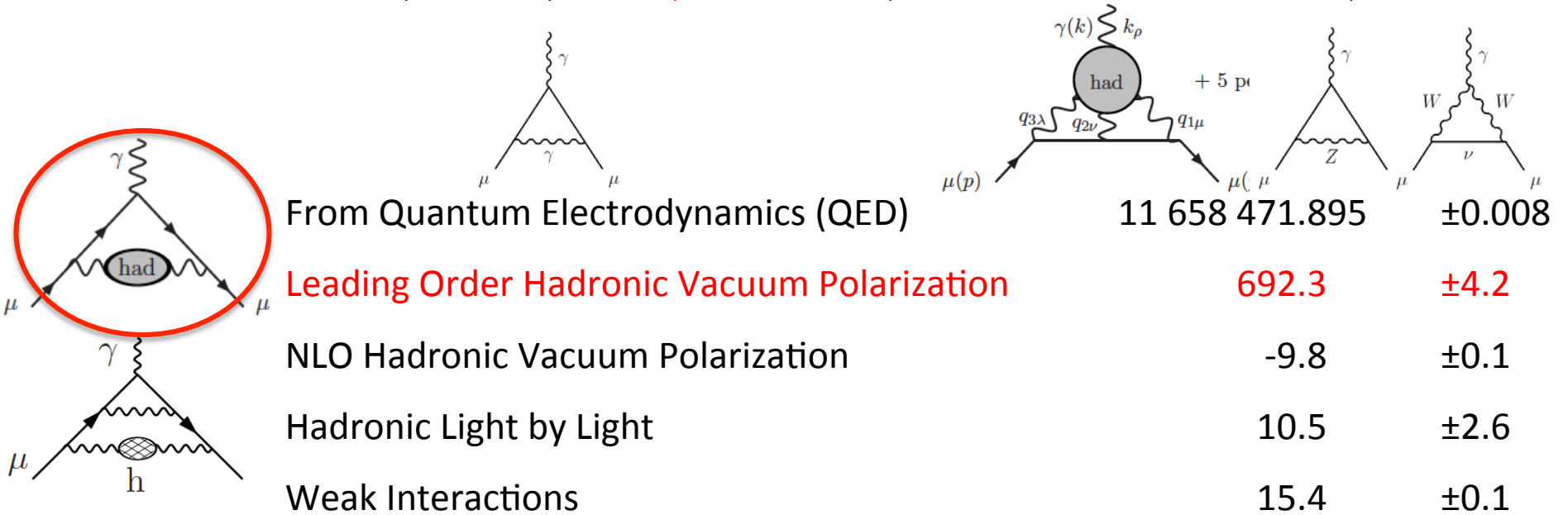
$$a_l = \frac{1}{2}(g_l - 2)$$

- For the electron, theory and experiment agree to great precision
- For the muon, they are in tension, which is the puzzle



# Status of $a_\mu$ - “before”

$$a_\mu^{theory} = a_\mu^{QED} + a_\mu^{Hadronic LO} + a_\mu^{Hadronic NLO} + a_\mu^{Hadronic LBL} + a_\mu^{Weak}$$



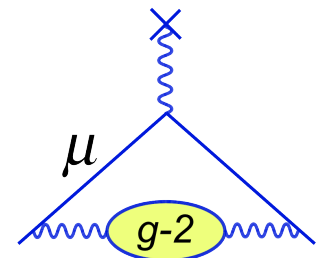
$a_\mu^{theory}$	11 659 180.2	$\pm 4.9$
$a_\mu^{experiment}$ J.P. Miller <i>et al.</i> , Ann Rev Nucl Part Sci 2012 62:237-64	11 659 208.9	$\pm 6.3$
$\Delta a_\mu = a_\mu^{experiment} - a_\mu^{theory}$	$3.6\sigma$ 28.7	$\pm 8.0$

DHMZ: Eur. Phys. J. C (2011) 71:1515

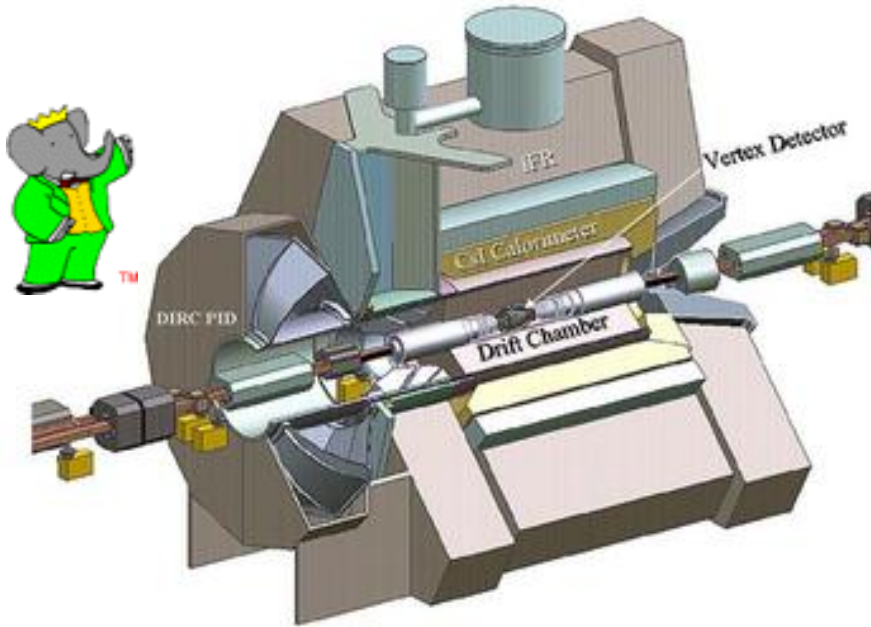
units of  $10^{-10}$

# The allure of $a_\mu$

- Longstanding tension between experiment and theory could be a hint at New Physics (NP).
- Rich muon program here at Fermilab and at J-PARC addressing the experimental side.
- Other experiments, including *BABAR*, provide inputs for the theoretical calculations, particularly at low energies where perturbative QCD runs into difficulty.



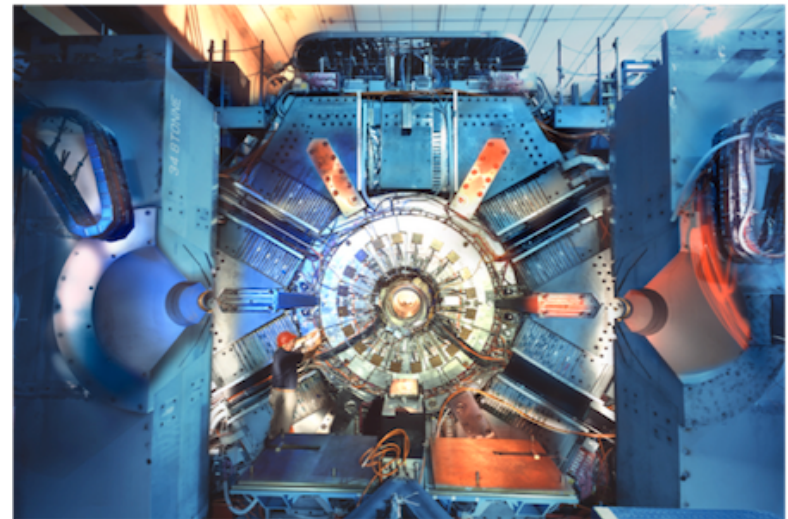
# The *BABAR* Experiment at SLAC



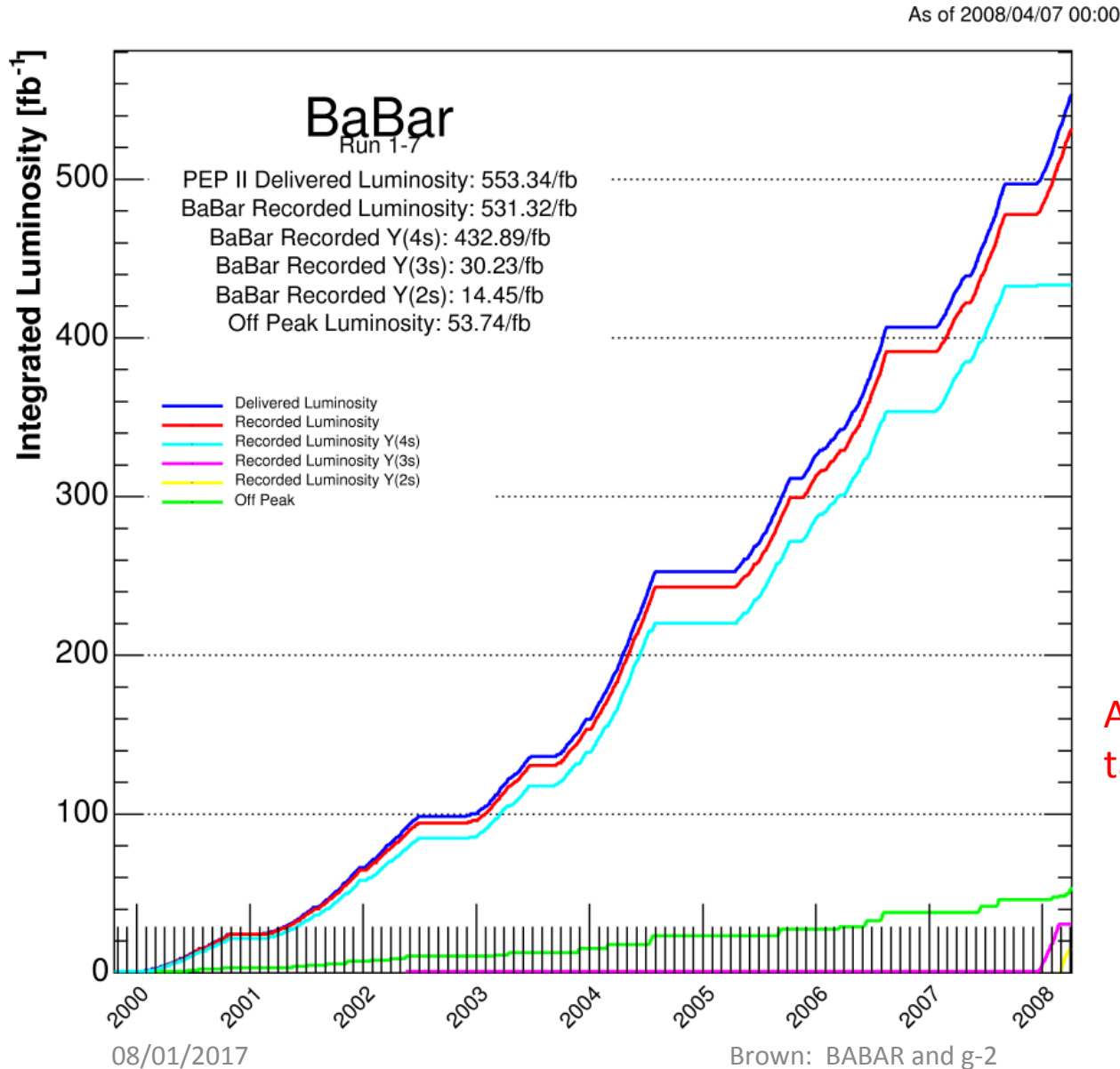
- Asymmetric-energy beams for boost
- Modern/state of the art detector
- 5 cylindrical subdetectors with a 40-layer drift chamber
- Excellent electromagnetic calorimetry
- Multiple measurements for particle identification
- Excellent momentum resolution

- Primarily designed for study of *CP*-violation in *B* meson decays
- Quality and general-purpose design make it suitable for a large variety of studies

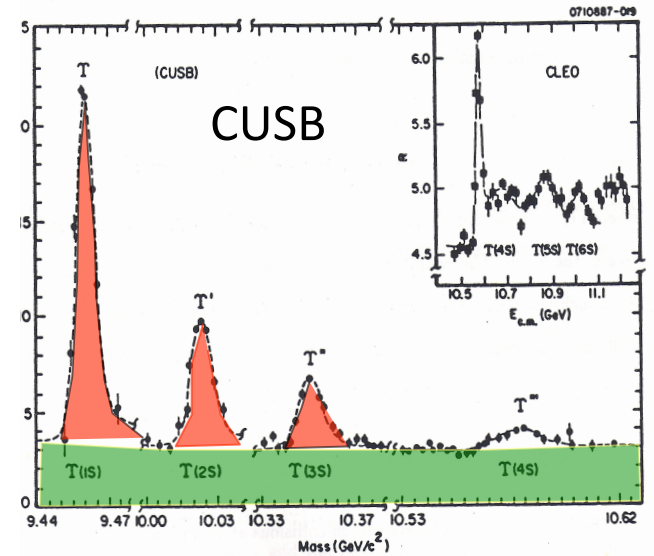
NIM A479,1 (2002),  
update: NIM A729, 615 (2013)



# The *BABAR* Running Era



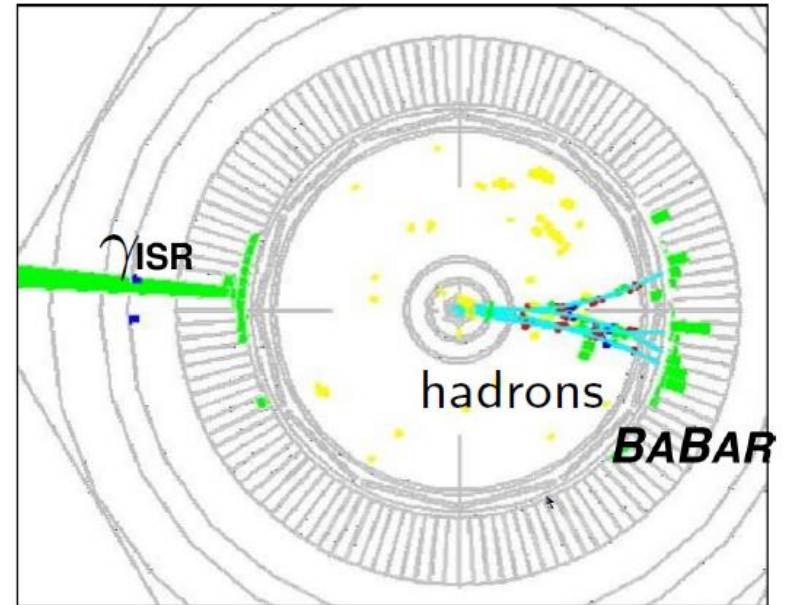
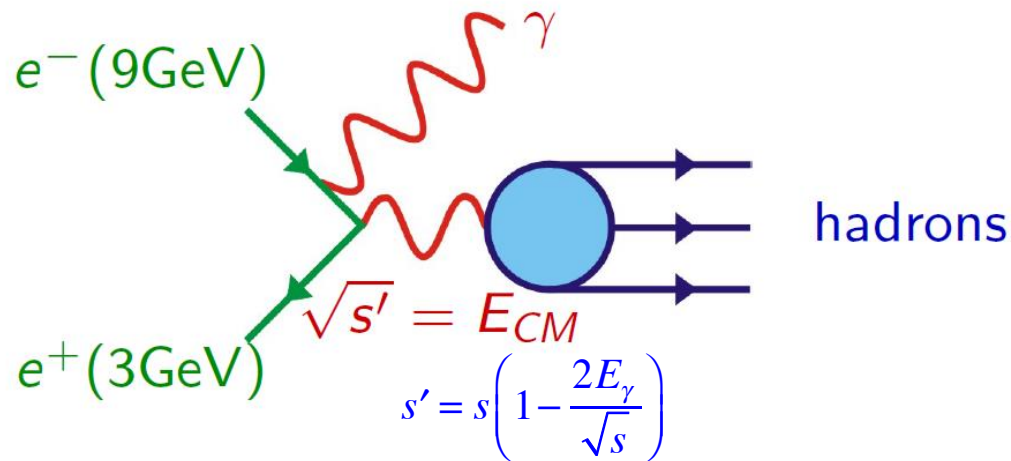
7 Runs over the course of 9 years



Analyses here use  $\sim 470 \text{ fb}^{-1}$  of data taken near 4S

- First collisions with BaBar  
May 26, 1999
- Final data taken 12:43 p.m.,  
April 7, 2008

# ISR Method



- Photon emitted by electron or positron – Initial State Radiation (ISR)
  - Carries away energy - allows “scan” of energies for remaining system
  - Easily identified back-to-back topology
  - High acceptance, even at threshold
  - Exploited heavily at *BABAR* for large number of hadronic cross sections

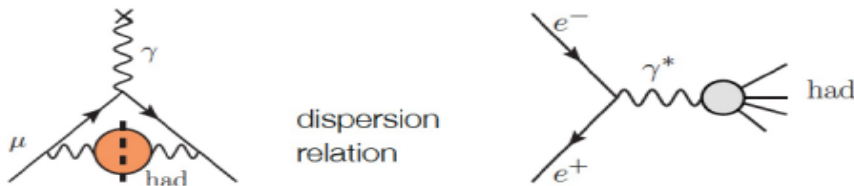
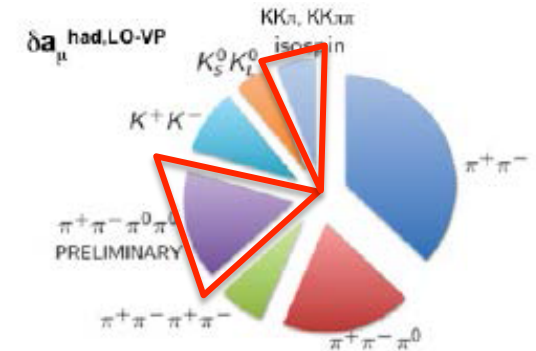
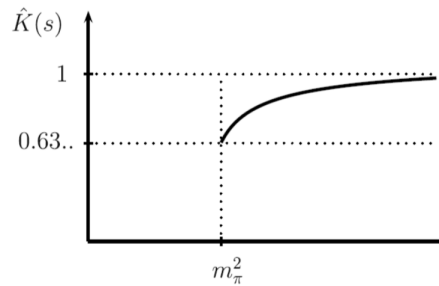


# BABAR ISR Contributions

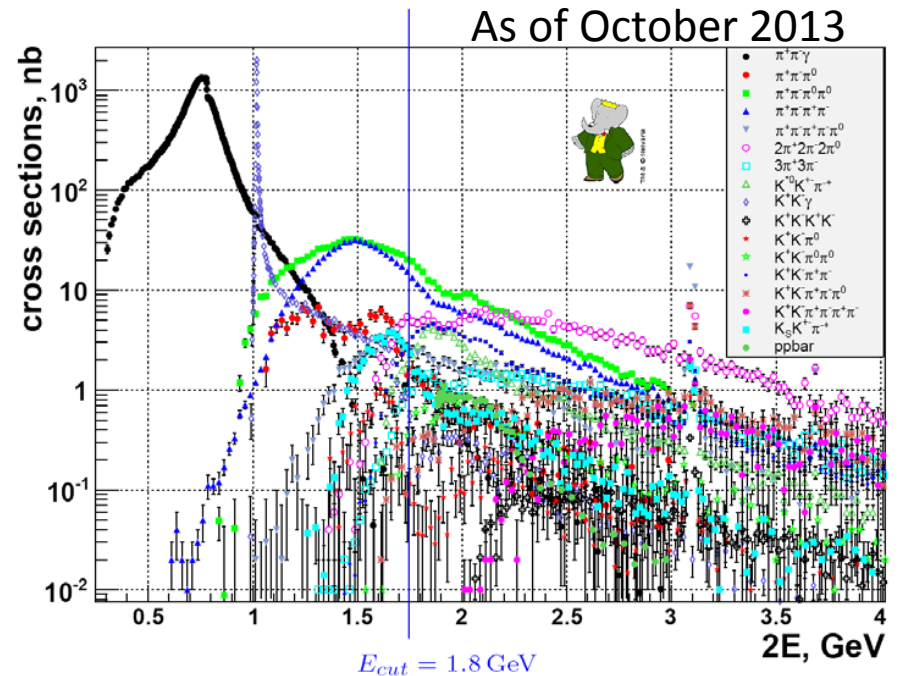
Calculate via dispersion relation integral.  
 Lowest CM energies contribute most

$$\alpha_{\mu}^{\text{Hadronic LO}} = \left( \frac{\alpha m_{\mu}}{3\pi} \right)^2 \int_{m_{\pi}^2}^{\infty} \frac{\hat{K}(s)}{s^2} R_{\text{HAD}}(s) ds$$

$$R_{\text{HAD}}(s) = \frac{\sigma(e^+e^- \rightarrow \text{HAD})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$



Above  $\sim 2$  GeV, theory can use perturbative QCD.  
 Below that, rely on experimental input. *BABAR* providing significant inputs



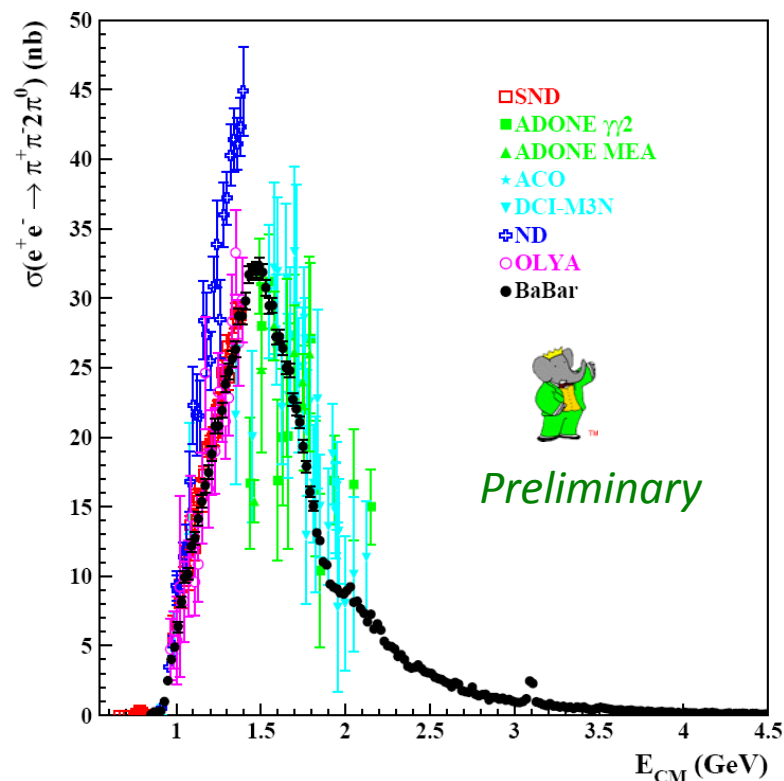
# Study of $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$

To Be Submitted

- Resolves tensions among previous results
- Large signal (over 150,000 events)
- Larger energy range than previous results
- Biggest background from  $e^+e^- \rightarrow \pi^+\pi^-3\pi^0$ 
  - Background measured from data

**Impact:**

Greatly improved uncertainties.  $\sim 3.3\%$  for energies less than 1.8 GeV



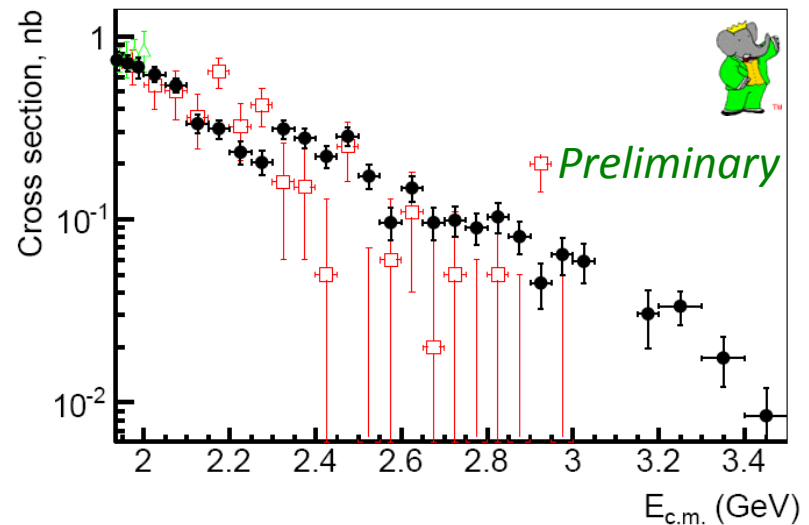
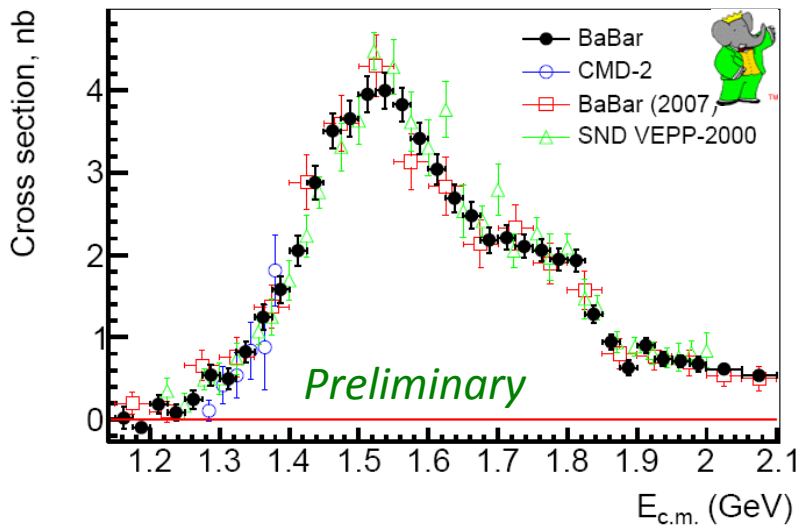
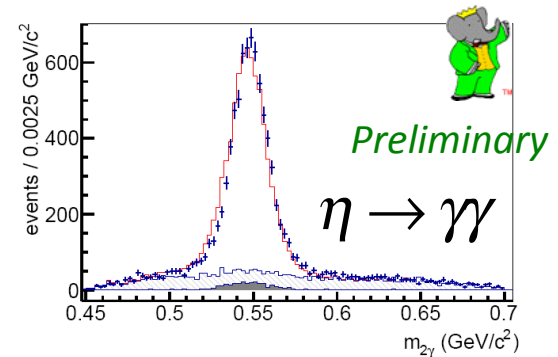
$$a_{\mu}^{\pi^+\pi^-\pi^0\pi^0} = (17.9 \pm 0.1 \pm 0.6) \times 10^{-10}$$

BABAR Preliminary

# Study of $e^+e^- \rightarrow \pi^+\pi^-\eta$

To Be Submitted

- Reconstruct via  $\eta \rightarrow \gamma\gamma$  decay
- Highest energy range for this mode
- Most precise measurement
- $\sim 8,000$  signal events

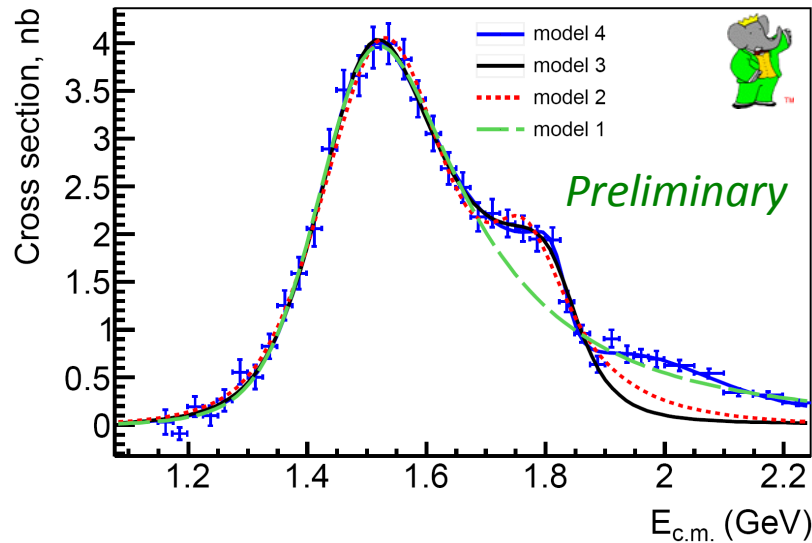


$$a_{\mu}^{\pi^+\pi^-\eta} = (1.19 \pm 0.02 \pm 0.06) \times 10^{-10}$$

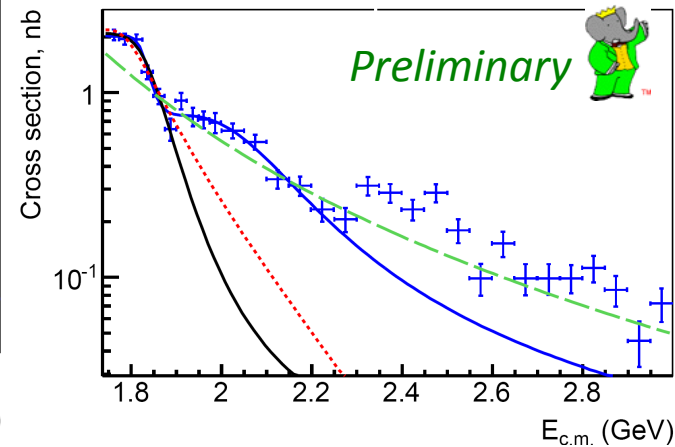
BABAR Preliminary

# Study of $e^+e^- \rightarrow \pi^+\pi^-\eta$

To Be Submitted



Vector Dominance Model fits  
- detailed information on dynamics



model 1:  $\rho(770) - \rho(1450)$  fits  $E_{CM} < 1.7$  GeV

model 2:  $\rho(770) - \rho(1450) - \rho(1700)$  fits  $< 1.9$  GeV

model 3:  $\rho(770) - \rho(1450) + \rho(1700)$  fits  $< 1.9$  GeV

model 4:  $\rho(770) - \rho(1450) + \rho(1700) + \rho(2150)$  fits  $< 2.2$  GeV

relative phases  $0$  (+) and  $180^\circ$  (-)

Implications for  
both  $a_\mu$  and  
hadronic  $\tau$  decays!

# Modes with Kaons

$K_S^0$  reconstructed as a pair of opposite charge tracks with a displaced vertex via its decay  $K_S^0 \rightarrow \pi^+ \pi^-$

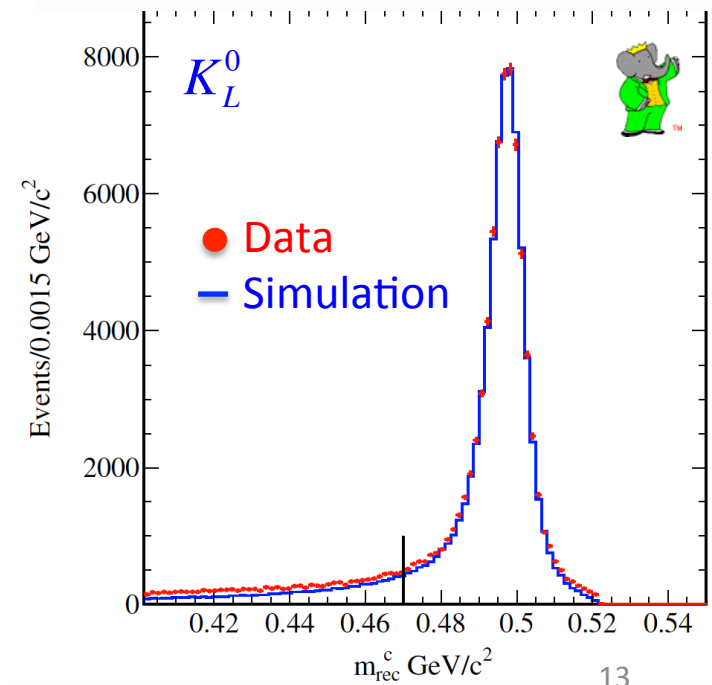
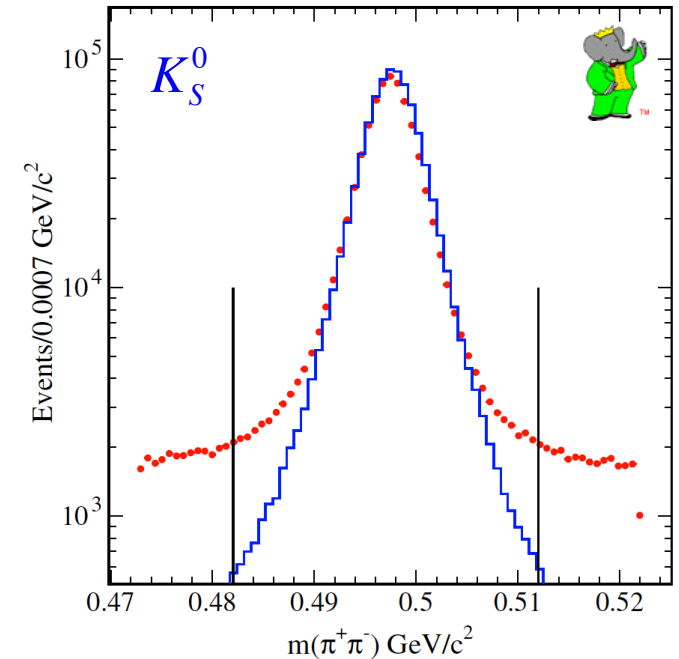
$K_L^0$  identified as an isolated energy cluster in the calorimeter, cluster shape not consistent with a photon.

- Validated via

$$e^+e^- \rightarrow \gamma\phi \rightarrow \gamma K_S^0 K_L^0$$

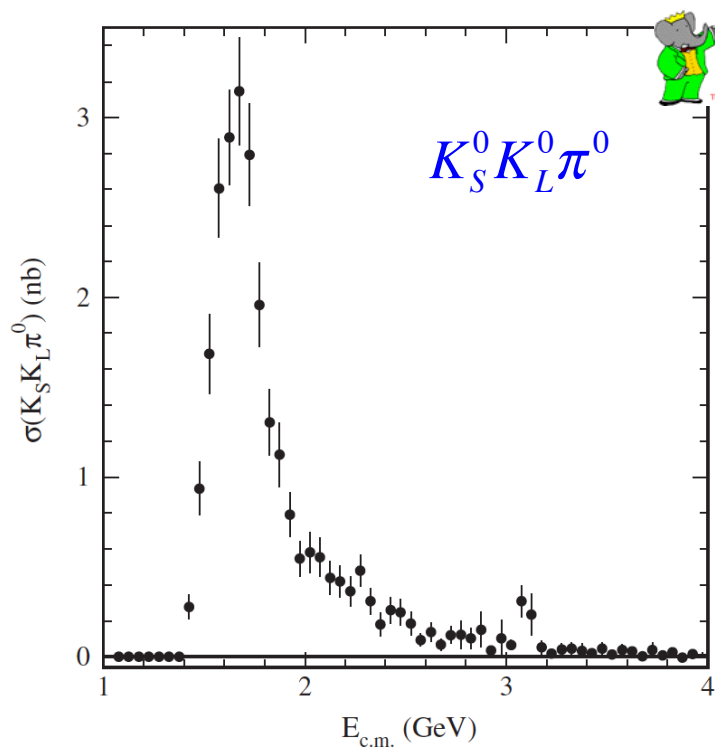
PRD89 0092002 (2014)

$K^\pm$  identified via standard charged-particle PID system utilizing specific ionization, timing, Cerenkov radiation, calorimetry

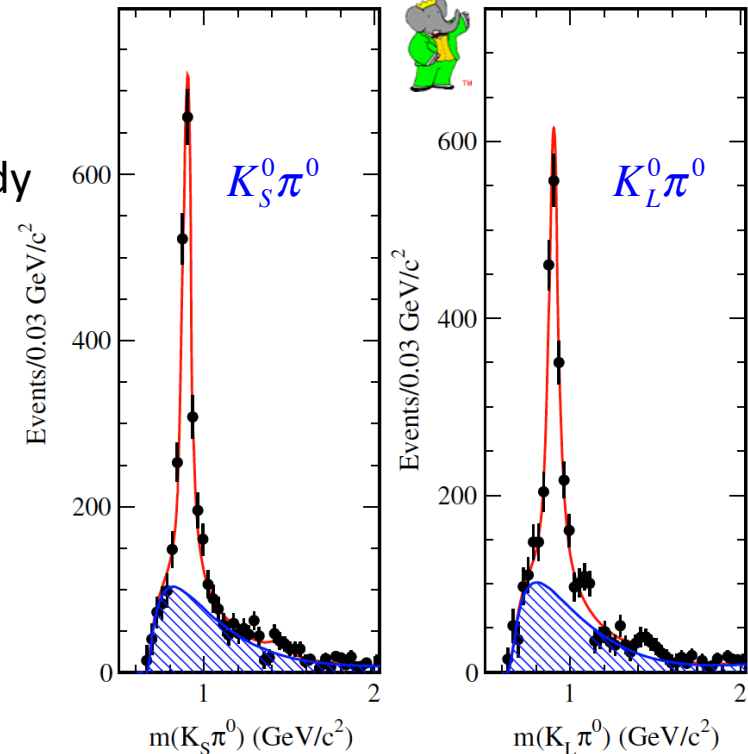


# Study of $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ , $K_S^0 K_L^0 \eta$ , $K_S^0 K_L^0 \pi^0 \pi^0$

Phys. Rev. D95 (2017) 052001.



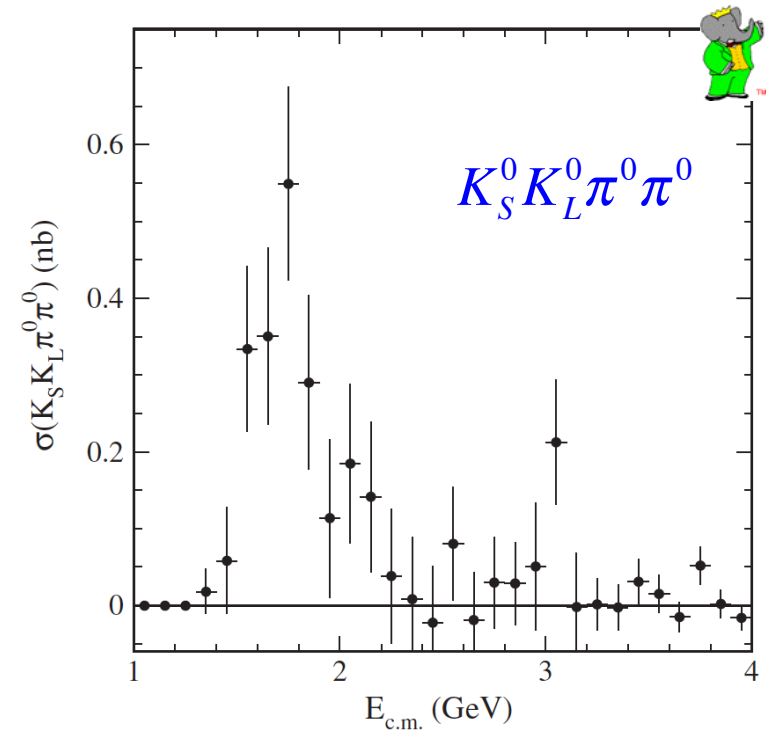
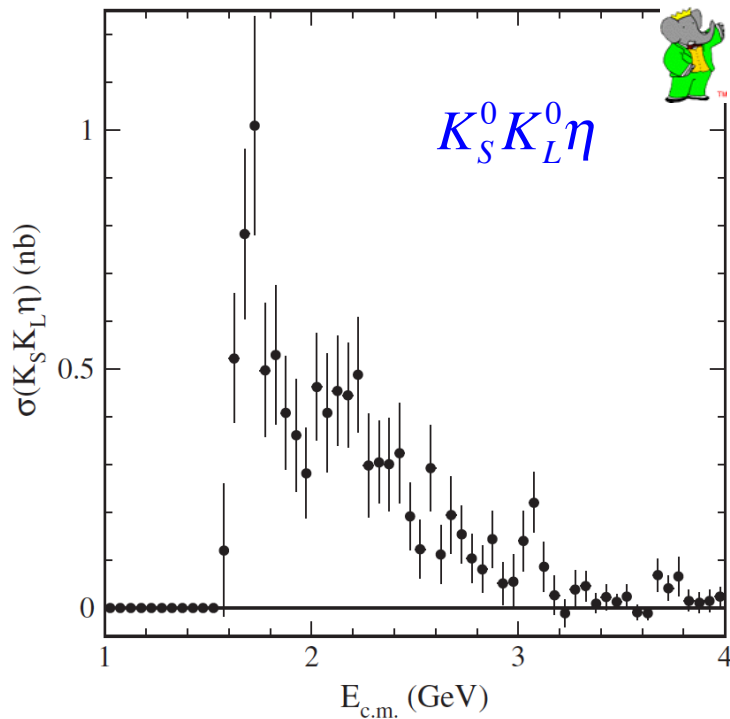
Extensive study  
of **resonant**  
**substructure**.



Improved energy range and cross-section uncertainties.  
First observation for  $J/\psi$  decays to these states

# Study of $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ , $K_S^0 K_L^0 \eta$ , $K_S^0 K_L^0 \pi^0 \pi^0$

Phys. Rev. D95 (2017) 052001.

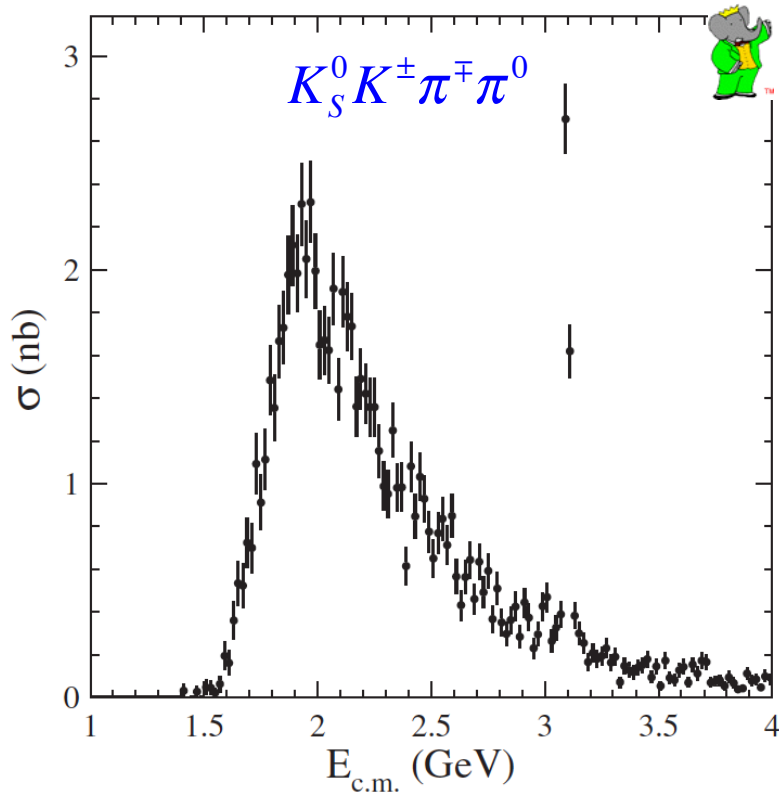


Very significant contribution from  $\phi\eta$

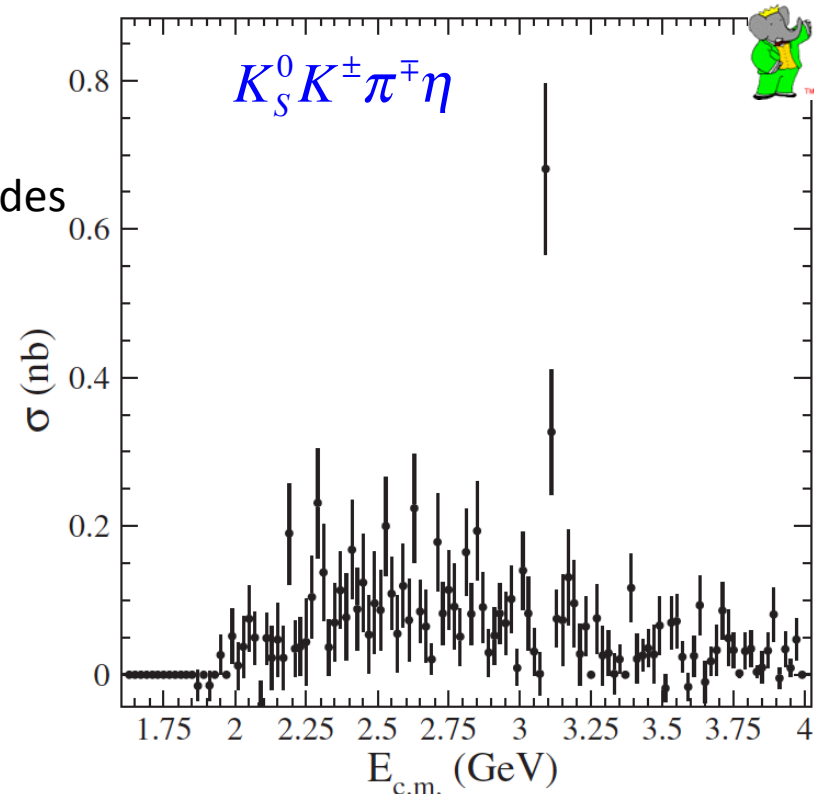
No significant contribution from  $K^* K^*$

# Study of $e^+e^- \rightarrow K_S^0 K^\pm \pi^\mp \pi^0$ , $K_S^0 K^\pm \pi^\mp \eta$

Phys. Rev. D95 (2017) 092005.



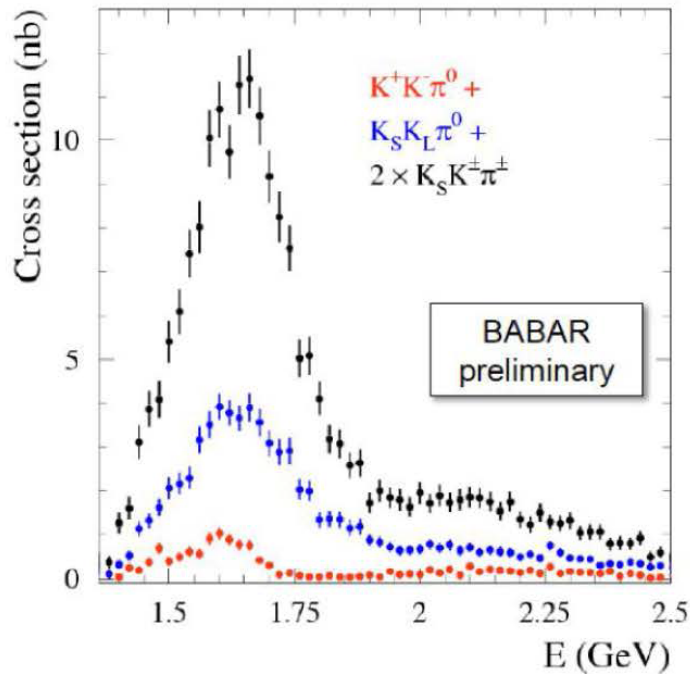
Completing  
the  $KK\pi$  modes



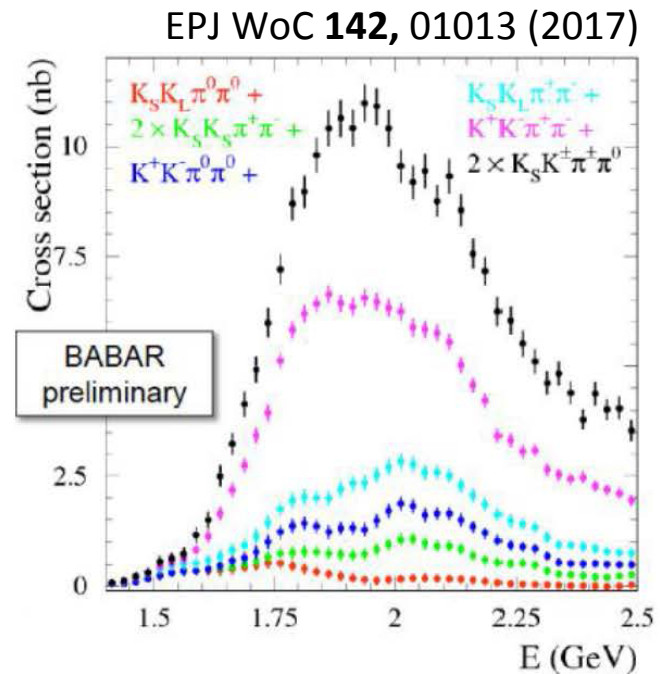
Significant contributions from  $J/\psi$  obvious



# Total $KK\pi(\pi)$ cross section



Courtesy  
V. Druzhinin



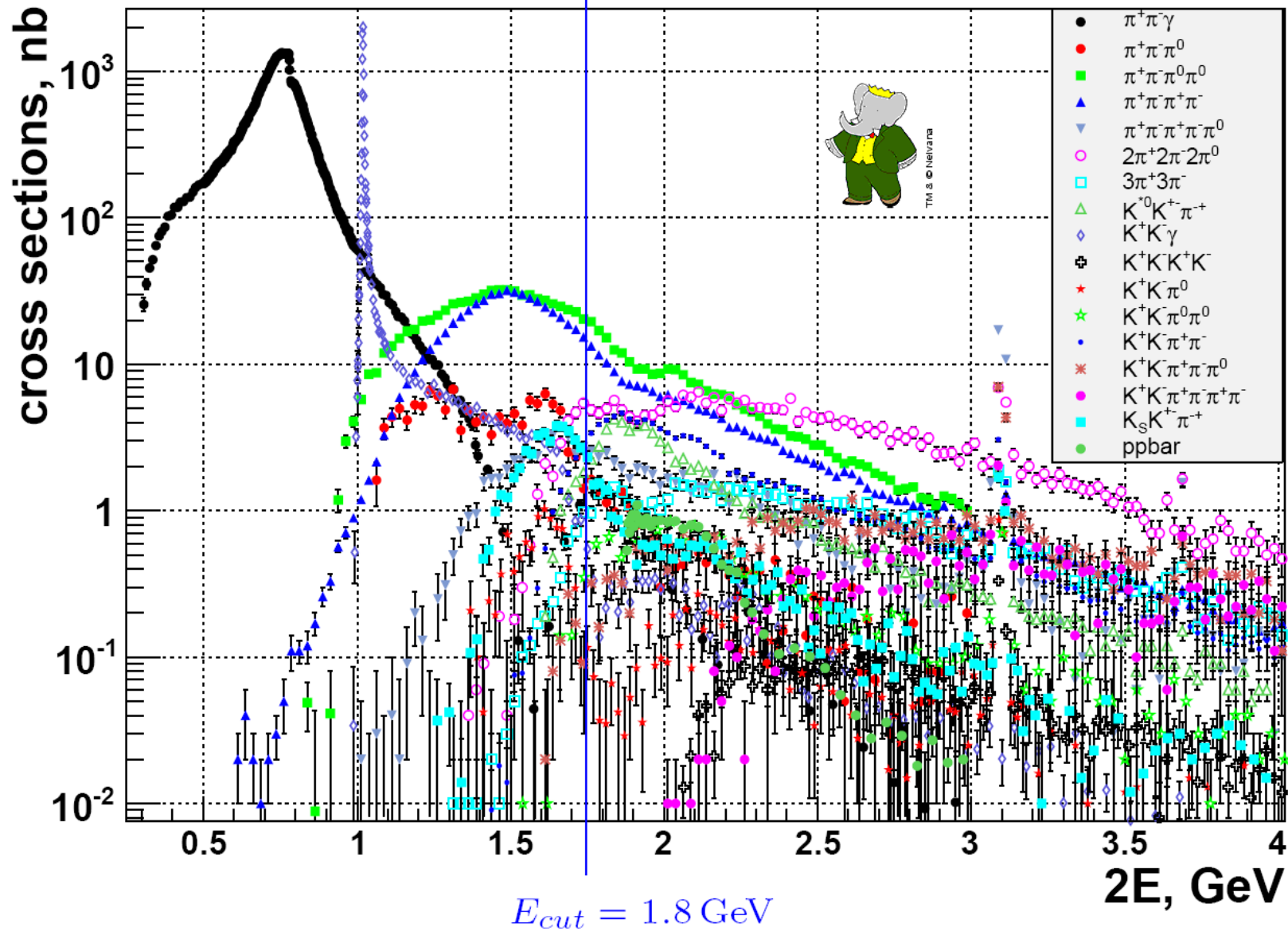
- All possible modes now measured by BABAR
- No more need to rely on isospin arguments
- Improves precision on inputs to g-2 calculations

$$a_\mu^{KK\pi} = (2.45 \pm 0.15) \times 10^{-10}$$

$$a_\mu^{KK\pi\pi} = (0.85 \pm 0.05) \times 10^{-10}$$

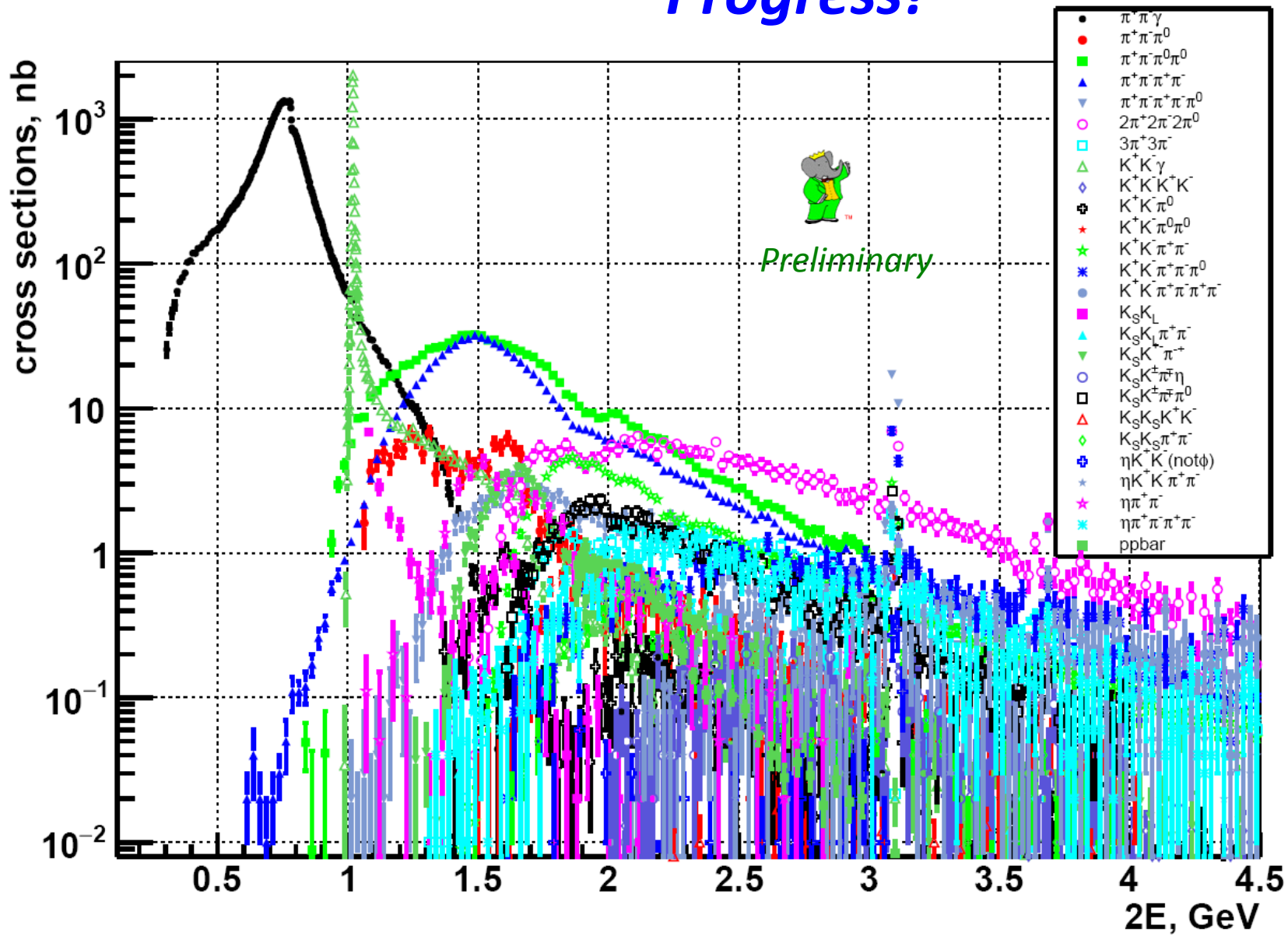
Progress!

~2013



Courtesy Fedor V. Ignatov, via J. Chauveau

# Progress!



# Now

Courtesy Fedor V. Ignatov, via J. Chauveau

# Status of $a_\mu$ – “after”

$$a_\mu^{theory} = a_\mu^{QED} + a_\mu^{Hadronic LO} + a_\mu^{Hadronic NLO} + a_\mu^{Hadronic NNLO} + a_\mu^{Hadronic LBL} + a_\mu^{Weak}$$

From Quantum Electrodynamics (QED)	11 658 471.885	±0.004
Leading Order Hadronic Vacuum Polarization	692.8	±3.3
	<i>Before:</i> 692.3	±4.2
NLO Hadronic Vacuum Polarization	-9.87	±0.09
NNLO Hadronic Vacuum Polarization	1.24	±0.01
→ Hadronic Light by Light	10.5	±2.6
Weak Interactions	15.4	±0.1

$a_\mu^{theory}$	11 659 181.9	±4.2
$a_\mu^{experiment}$	11 659 208.9	±6.3
$\Delta a_\mu = a_\mu^{experiment} - a_\mu^{theory}$	3.6σ	27.0 ±7.6

M. Davier, arXiv 1612.02743 (2017).

units of  $10^{-10}$

# Summary and Conclusions

- *BABAR* has made considerable use of the ISR technique to study  $e^+e^-$  annihilation across a broad energy range.
  - Including several new hadronic modes reported here.
- Important to improve our knowledge of muon  $g-2$ 
  - the puzzle continues, more input needed!
  - More on the way! Stay Tuned.

