

# Developments in the Theory of Flavor Mixing and Rare Decays

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# Flavor in the Standard Model and Beyond

$$\begin{aligned}\mathcal{L}_{\text{SM}} \sim & \Lambda^4 + \Lambda^2 H^2 + \lambda H^4 \\ & + \bar{\Psi} \not{D} \Psi + (D_\mu H)^2 + (F_{\mu\nu})^2 + F_{\mu\nu} \tilde{F}^{\mu\nu} \\ & + Y H \bar{\Psi} \Psi\end{aligned}$$

# Flavor in the Standard Model and Beyond

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Callouts identifying problems:

- CC problem**: Points to the  $\Lambda^4$  term.
- Hierarchy problem**: Points to the  $\Lambda^2 H^2$  term.
- Vacuum stability?**: Points to the  $\lambda H^4$  term.
- Strong CP problem**: Points to the  $F_{\mu\nu} \tilde{F}^{\mu\nu}$  term.
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- Neutrino masses**: Callout pointing to the  $\frac{1}{\Lambda} (LH)^2$  term.
- NP flavor puzzle ...**: Callout pointing to the  $\frac{1}{\Lambda^2} \sum_i \mathcal{O}_i^{\text{dim6}}$  term.

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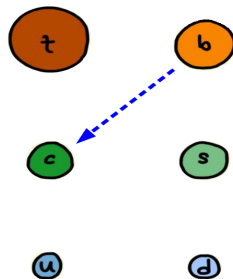
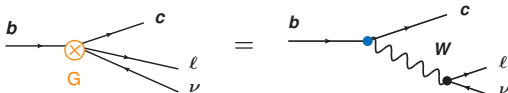
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**Q1:** What is the origin of the hierarchies in the SM sources of flavor violation?

**Q2:** Are there other sources of flavor violation beyond the SM?

# Flavor Changing Quark Decays in the SM

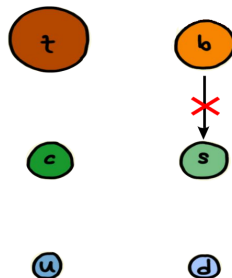
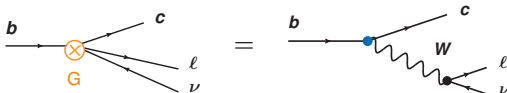
In the Standard Model, flavor changing charged current decays arise at the tree level;  
rates are suppressed by small CKM elements



$$G \sim G_F V_{cb}$$

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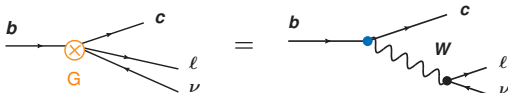
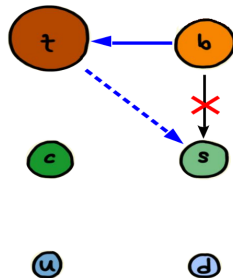


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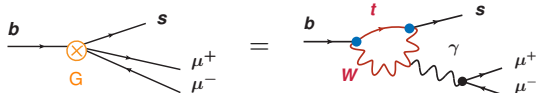
# Flavor Changing Quark Decays in the SM

In the Standard Model, flavor changing charged current decays arise at the tree level;  
rates are suppressed by small CKM elements

Flavor changing neutral current decays can arise at the loop level; they are suppressed by loop factors and small CKM elements



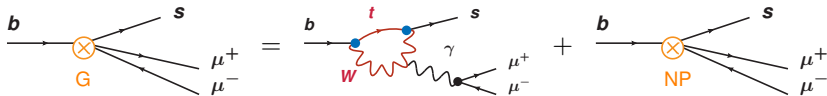
$$G \sim G_F V_{cb}$$



$$G \sim \frac{e^2}{16\pi^2} G_F \frac{m_t^2}{m_W^2} V_{tb} V_{ts}^*$$



# New Physics in B Decays



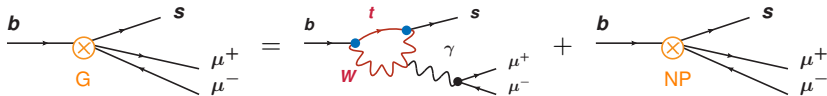
$$G \sim \frac{e^2}{16\pi^2} G_F \frac{m_t^2}{m_W^2} V_{tb} V_{ts}^* + \frac{C_{NP}}{\Lambda_{NP}^2}$$

measure  
precisely

calculate precisely  
the SM contribution

get information on  
NP coupling and scale

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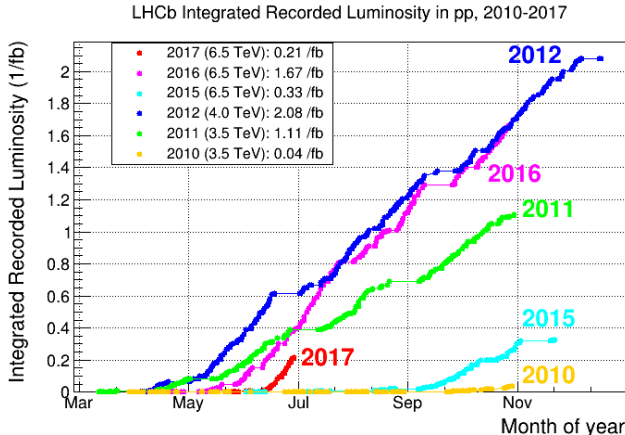
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Anomalies in B decays could establish a new scale in particle physics

# LHC is a “b-factory”



more than  $\sim 10^{12}$  b quarks produced in the LHCb detector so far

$\Rightarrow$  unique sensitivity to many b decays

SM predictions for b hadron decays require non-perturbative input

- 1 form factors ( $\rightarrow$  lattice QCD)
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clever way to reduce/eliminate hadronic uncertainties:  
lepton flavor universality (LFU) tests

$$R_{D^{(*)}} = \frac{BR(B \rightarrow D^{(*)} \tau \nu)}{BR(B \rightarrow D^{(*)} \ell \nu)}$$

LFU ratios of  
charged current decays

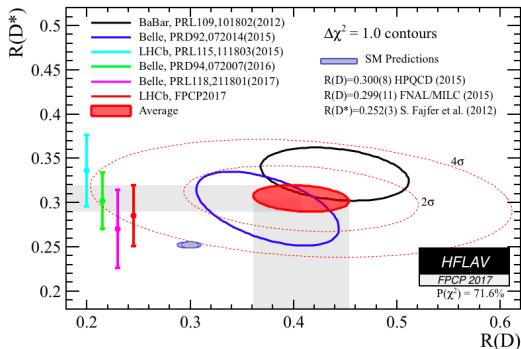
$$R_{K^{(*)}} = \frac{BR(B \rightarrow K^{(*)} \mu \mu)}{BR(B \rightarrow K^{(*)} e e)}$$

LFU ratios of  
neutral current decays

$R_D$  and  $R_{D^*}$

# The Experimental Situation

world average from the heavy flavor averaging group



$$R_D = \frac{BR(B \rightarrow D\tau\nu)}{BR(B \rightarrow D\ell\nu)}$$

$$R_{D^*} = \frac{BR(B \rightarrow D^*\tau\nu)}{BR(B \rightarrow D^*\ell\nu)}$$

$$\ell = \mu, e \quad (\text{BaBar/Belle})$$

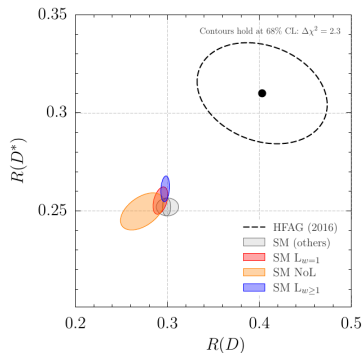
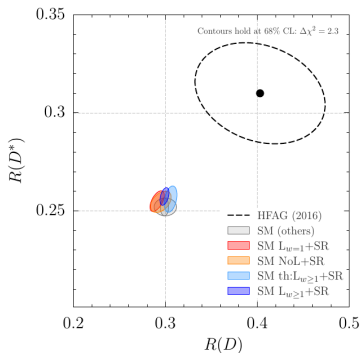
$$\ell = \mu \quad (\text{LHCb})$$

$$R_D^{\text{exp}} = 0.407 \pm 0.039 \pm 0.024, \quad R_{D^*}^{\text{exp}} = 0.304 \pm 0.013 \pm 0.007$$

discrepancies with the SM by  $2.3\sigma$  and  $3.4\sigma$ , respectively

# Standard Model Predictions for $R_D$ and $R_{D^*}$

Bernlochner, Ligeti, Papucci, Robinson 1703.05330



heavy quark expansion +  $B \rightarrow D^{(*)} \ell \nu$  data + lattice input + QCD sum rule input

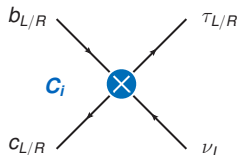
$$R_D^{\text{SM}} = 0.299 \pm 0.003, \quad R_{D^*}^{\text{SM}} = 0.257 \pm 0.003$$

(see also Fajfer, Kamenik, Nisandzic 1203.2654; Bailey et al. 1503.07237;  
Na et al. 1505.03925; Bigi, Gambino 1606.08030)



# Model Independent New Physics Analysis

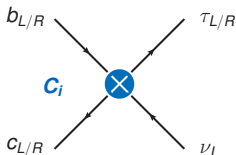
$$\mathcal{H}_{\text{eff}} = \frac{4G_F}{\sqrt{2}} V_{cb} \mathcal{O}_{V_L} + \frac{1}{\Lambda^2} \sum_i C_i \mathcal{O}_i$$



$\mathcal{O}_i = 4$  fermion contact interactions with  
vector, scalar or tensor currents

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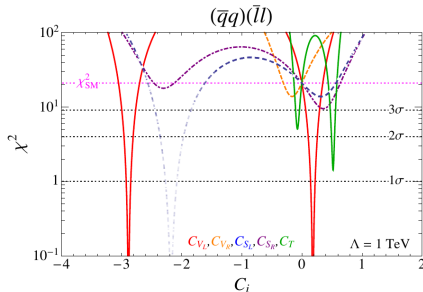
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rescaling of the **SM operator** fits the data best

combinations of operators are also possible



Freytsis, Ligeti, Ruderman 1506.08896

# Implications for the New Physics Scale

unitarity bound	$\frac{4\pi}{\Lambda_{\text{NP}}^2} (\bar{c}\gamma_\nu P_L b)(\bar{\tau}\gamma^\nu P_L \nu)$	$\Lambda_{\text{NP}} \simeq 8.4 \text{ TeV}$
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generic tree	$\frac{1}{\Lambda_{\text{NP}}^2} (\bar{c}\gamma_\nu P_L b)(\bar{\tau}\gamma^\nu P_L \nu)$	$\Lambda_{\text{NP}} \simeq 2.4 \text{ TeV}$
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MFV tree	$\frac{1}{\Lambda_{\text{NP}}^2} V_{cb} (\bar{c}\gamma_\nu P_L b)(\bar{\tau}\gamma^\nu P_L \nu)$	$\Lambda_{\text{NP}} \simeq 0.5 \text{ TeV}$
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(MFV = Minimal Flavor Violation)

# Many Constraints on New Physics Models

- ▶ constraints from  $B \rightarrow \tau \nu$  and  $B \rightarrow K \nu \nu$  etc.
- ▶ the  $B_c \rightarrow \tau \nu$  rate and the total  $B_c$  life-time strongly constrain scalar explanations of  $R_D$  and  $R_{D^*}$

Li, Yang, Zhang 1605.09308; Alonso, Grinstein, Martin Camalich 1611.06676

- ▶ in many models strong constraints are obtained from  $pp \rightarrow \tau \tau$  searches at the LHC

Faroughy, Greljo, Kamenik 1609.07138

- ▶ in many models one finds strong constraints from  $Z$  couplings,  $W$  couplings, or tau decays, etc. that are modified at the loop level

Feruglio, Paradisi, Pattori 1606.00524 + 1705.00929

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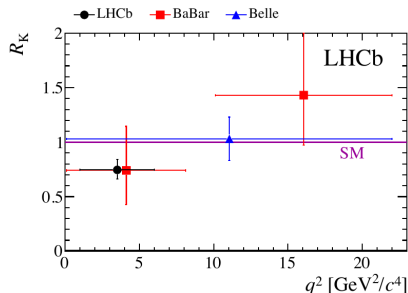
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Feruglio, Paradisi, Pattori 1606.00524 + 1705.00929

→ model building is non-trivial

$R_K$  and  $R_{K^*}$

# Experimental Situation

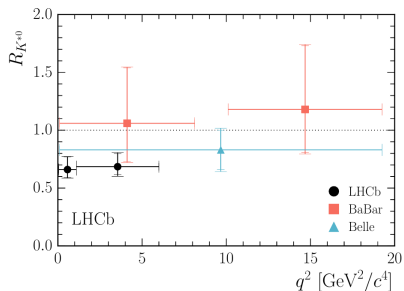


$$R_{K^{(*)}} = \frac{BR(B \rightarrow K^{(*)} \mu \mu)}{BR(B \rightarrow K^{(*)} e e)}$$

$$R_K^{[1,6]} = 0.745_{-0.074}^{+0.090} \pm 0.036$$

$$R_{K^*}^{[0.045, 1.1]} = 0.66_{-0.07}^{+0.11} \pm 0.03$$

$$R_{K^*}^{[1.1, 6]} = 0.69_{-0.07}^{+0.11} \pm 0.05$$



3 observables  
deviating by  $\sim 2\sigma - 2.5\sigma$   
from the SM predictions

$$R_{K^{(*)}} = 1$$



# Standard Model Predictions for $R_K$ and $R_{K^*}$

$$R_{K^{(*)}} = 1 + \mathcal{O}\left(\frac{m_\mu^2}{q^2}\right) \times \left(1 + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}}{m_b}\right) + \mathcal{O}(\alpha_s)\right) + \mathcal{O}\left(\frac{\alpha_{\text{em}}}{\pi} \log^2\left(\frac{m_e^2}{m_\mu^2}\right)\right)$$

phase space  
(tiny effect)

hadronic corrections  
(tiny effect)

QED corrections  
(soft and collinear  
photon emission)

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Bordone, Isidori, Pattori 1605.07633

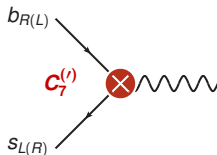
$$R_K^{[1,6]} = 1.00 \pm 0.01, \quad R_{K^*}^{[1,1,6]} = 1.00 \pm 0.01, \quad R_{K^*}^{[0.045,1.1]} = 0.91 \pm 0.03$$

- ▶ QED corrections are well modeled by Monte Carlo
- ▶ additional corrections at low  $q^2$  from  $B \rightarrow K^* \eta (\rightarrow ee\gamma)$

# Model Independent New Physics Analysis

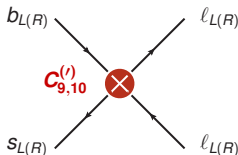
$$\mathcal{H}_{\text{eff}} = \mathcal{H}_{\text{eff}}^{\text{SM}} - \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e^2}{16\pi^2} \sum_i \left( C_i \mathcal{O}_i + C'_i \mathcal{O}'_i \right)$$

magnetic dipole operators



$$C_7^{(\prime)} (\bar{s} \sigma_{\mu\nu} P_{R(L)} b) F^{\mu\nu}$$

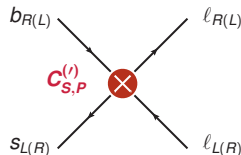
semileptonic operators



$$C_9^{(\prime)} (\bar{s} \gamma_\mu P_{L(R)} b) (\bar{\ell} \gamma^\mu \ell)$$

$$C_{10}^{(\prime)} (\bar{s} \gamma_\mu P_{L(R)} b) (\bar{\ell} \gamma^\mu \gamma_5 \ell)$$

scalar operators



$$C_S^{(\prime)} (\bar{s} P_{R(L)} b) (\bar{\ell} P_{L(R)} \ell)$$

# Anatomy of the New Physics Effect

✗ dipole operators do not break lepton flavor universality

✗ scalar operators are strongly constrained by  $B_s \rightarrow \ell^+ \ell^-$

WA, Niehoff, Straub 1702.05498; Alonso, Grinstein, Martin Camalich 1407.7044

✓ semi-leptonic operators are required

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- ✓ semi-leptonic operators are required

parity of the final state mesons implies:

right-handed quark currents result  
in an anti-correlation of  $R_K$  and  $R_{K^*}$

left-handed quark currents result  
in a correlation of  $R_K$  and  $R_{K^*}$

Hiller, Schmaltz 1411.4773

# Fits to Wilson Coefficients

WA, Stangl, Straub 1704.05435

Coeff.	best fit	$1\sigma$	$2\sigma$	pull
$C_9^\mu$	-1.56	$[-2.12, -1.10]$	$[-2.87, -0.71]$	$4.1\sigma$
$C_{10}^\mu$	+1.20	$[+0.88, +1.57]$	$[+0.58, +2.00]$	$4.2\sigma$
$C_9^e$	+1.54	$[+1.13, +1.98]$	$[+0.76, +2.48]$	$4.3\sigma$
$C_{10}^e$	-1.27	$[-1.65, -0.92]$	$[-2.08, -0.61]$	$4.3\sigma$

suppress the muon rate with  $C_9^\mu < 0$  or  $C_{10}^\mu > 0$   
or enhance the electron rate with  $C_9^e > 0$  or  $C_{10}^e < 0$   
(or linear combinations)

see also Capdevila, Crivellin, Descotes-Genon, Matias, Virto 1704.05340;

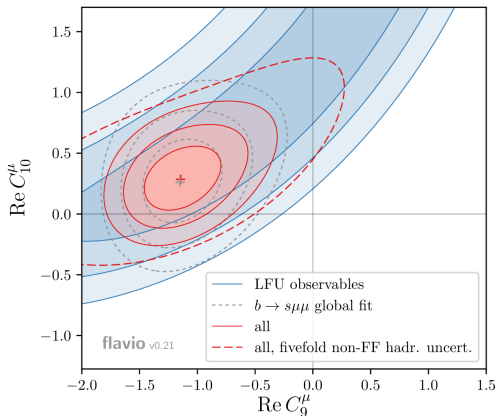
D'Amico, Nardecchia, Panci, Sannino, Strumia, Torre, Urbano 1704.05438;

Hiller, Nisandzic 1704.05444; Geng, Grinstein, Jager, Martin Camalich, Ren, Shi 1704.05446;

Ciuchini, Coutinho, Fedele, Franco, Paul, Silvestrini, Valli 1704.05447;

(+ many others, apologies for the omission...)

# Compatibility with Other $b \rightarrow s\mu\mu$ Anomalies



WA, Stangl, Straub 1704.05435

WA, Niehoff, Stangl, Straub 1703.09189

(+ many others ...)

the LFU observables are  
**fully compatible** with other  
anomalies that are seen in  
 $b \rightarrow s\mu\mu$  transitions  
("P'\_5 and friends")

Best description of all  
anomalies by:

**new physics in final states  
with muons**

$$C_9^\mu(\bar{s}\gamma_\mu P_L b)(\bar{\mu}\gamma^\mu \mu)$$

**SM-like final states with  
electrons**

# Implications for the New Physics Scale

unitarity bound  $\frac{4\pi}{\Lambda_{\text{NP}}^2} (\bar{s}\gamma_\nu P_L b)(\bar{\mu}\gamma^\nu \mu)$   $\Lambda_{\text{NP}} \simeq 120 \text{ TeV} \times (C_9^{\text{NP}})^{-1/2}$

generic tree  $\frac{1}{\Lambda_{\text{NP}}^2} (\bar{s}\gamma_\nu P_L b)(\bar{\mu}\gamma^\nu \mu)$   $\Lambda_{\text{NP}} \simeq 35 \text{ TeV} \times (C_9^{\text{NP}})^{-1/2}$

MFV tree  $\frac{1}{\Lambda_{\text{NP}}^2} V_{tb} V_{ts}^* (\bar{s}\gamma_\nu P_L b)(\bar{\mu}\gamma^\nu \mu)$   $\Lambda_{\text{NP}} \simeq 7 \text{ TeV} \times (C_9^{\text{NP}})^{-1/2}$

generic loop  $\frac{1}{\Lambda_{\text{NP}}^2} \frac{1}{16\pi^2} (\bar{s}\gamma_\nu P_L b)(\bar{\mu}\gamma^\nu \mu)$   $\Lambda_{\text{NP}} \simeq 3 \text{ TeV} \times (C_9^{\text{NP}})^{-1/2}$

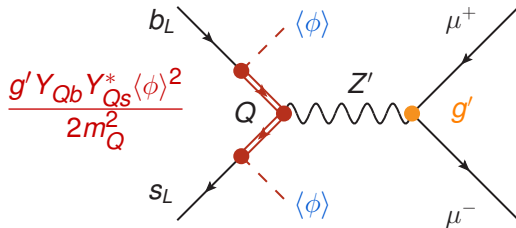
MFV loop  $\frac{1}{\Lambda_{\text{NP}}^2} \frac{1}{16\pi^2} V_{tb} V_{ts}^* (\bar{s}\gamma_\nu P_L b)(\bar{\mu}\gamma^\nu \mu)$   $\Lambda_{\text{NP}} \simeq 0.6 \text{ TeV} \times (C_9^{\text{NP}})^{-1/2}$



# My Favorite Model

$Z'$  based on gauging  $L_\mu - L_\tau$   
with effective flavor violating couplings to quarks

WA, Gori, Pospelov, Yavin 1403.1269; WA, Yavin 1508.07009



$$C_9 = \frac{Y_{Qb} Y_{Qs}^*}{2m_Q^2}$$

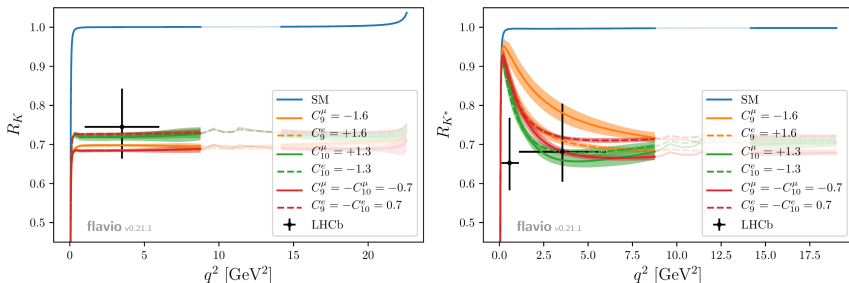
**Q**: heavy vector-like fermions with mass  $\sim 1 - 10$  TeV  
 $\phi$ : scalar that breaks  $L_\mu - L_\tau$

- ▶ The LFU ratios  $R_{D^{(*)}}$  and  $R_{K^{(*)}}$  are theoretically clean probes of new sources of flavor violation.
- ▶ Experimental uncertainties are still statistics dominated.
- ▶ With more data from LHCb and Belle II we will be able to understand if these are signs of new physics!

Back Up

# The low $q^2$ Bin in $R_{K^*}$

WA, Stangl, Straub 1704.05435



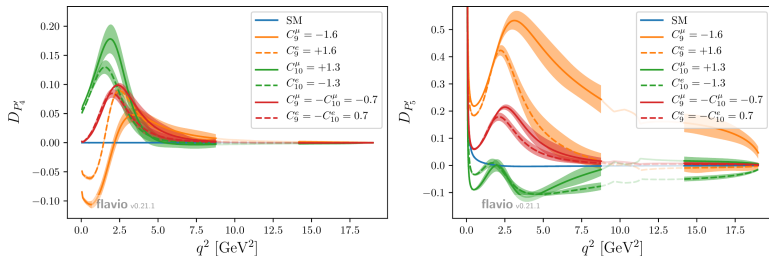
$B \rightarrow K^* \ell^+ \ell^-$  decays at low  $q^2$  are dominated by the (lepton flavor universal) **photon pole**  $B \rightarrow K^* \gamma$

→ Effect of (heavy) new physics in  $R_{K^*}$  gets **diluted at low  $q^2$** .

This behavior is not seen in the data (yet?).

# Distinguishing New Physics Scenarios

WA, Stangl, Straub 1704.05435



$$D_{P'_i} = P'_i(B \rightarrow K^* \mu \mu) - P'_i(B \rightarrow K^* e e) \quad (\text{WA, Yavin 1508.07009})$$

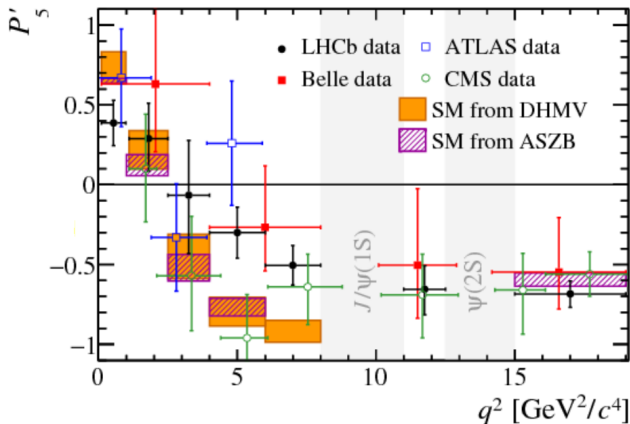
(for additional proposals of angular LFU tests see e.g.

Capdevila, Descotes-Genon, Matias, Virto 1605.03156

Serra, Silva Coutinho, van Dyk 1610.08761)

**LFU differences of angular observables** can be used to distinguish between different new physics explanations

# The $P'_5$ Anomaly



ASZB = WA, Straub 1411.3161 + Bharucha, Straub, Zwicky 1503.05534

DHMV = Descotes-Genon, Hofer, Matias, Virto 1510.04239

(talk by Tim Gershon at Moriond EW 2017)