

# Soft Gluon Resummation at NNLL Accuracy for Associated $t\bar{t}H$ Production at the LHC

Vincent Theeuwes

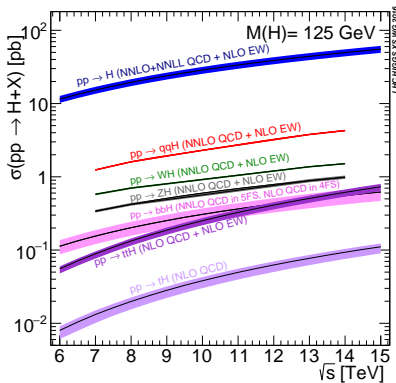
University at Buffalo  
The State University of New York

In Collaboration with: Anna Kulesza, Leszek Motyka, Tomasz Stebel

DPF, 07-26-2017

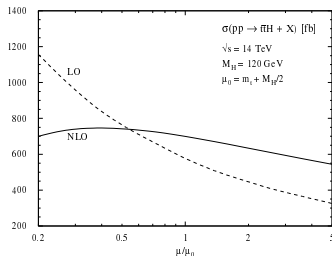
# Importance of $pp \rightarrow t\bar{t}H$

- A Higgs boson found with a mass of 125 GeV
- Precision study needed to determine if it is SM Higgs
- Direct way to access Yukawa coupling



# Current status of $pp \rightarrow t\bar{t}H$

- QCD Corrections up to NLO [*Beenakker et al. , '02*] [*Dawson et al. , '02*]
- Matched to parton showers by: aMC@NLO [*Frederix et al. , '11*], PowHel [*Garzelli et al. , '11*], Sherpa [*Hoeche et al., '12*], POWHEG-BOX [*Hartanto et al. , '14*]
- Electroweak correction [*Frixione et al. , '14,'15*][*Zhang et al., '14*]
- Including top decays [*Denner, Feger, '15*]
- Absolute threshold at NLL [*Kulesza, Motyka, Stebel, VT, '15*]
- NNLL in SCET, expansion [*Broggio, Ferroglia, Pecjak, Yang, '15*] and resummation [*Broggio, Ferroglia, Pecjak, Yang, '16*]

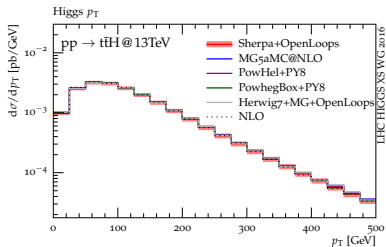


[*Beenakker et al. , '02*]

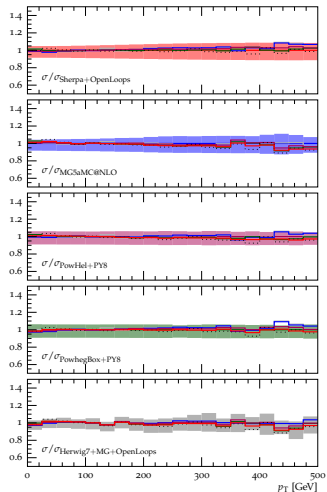
# Parton showers

NLO matched to parton showers by:

- aMC@NLO [Frederix et al. , '11]
- PowHel [Garzelli et al. , '11]
- Sherpa [Hoeche et al., '12]
- POWHEG-BOX [Hartanto et al. , '14]

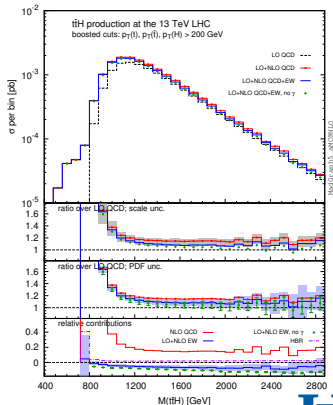
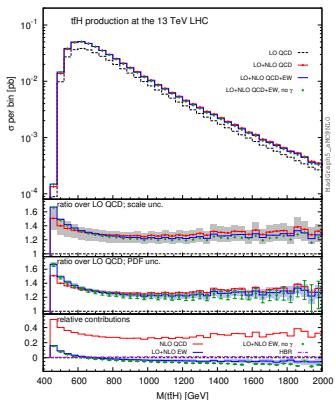


[YR4 , '16]



# Electroweak corrections

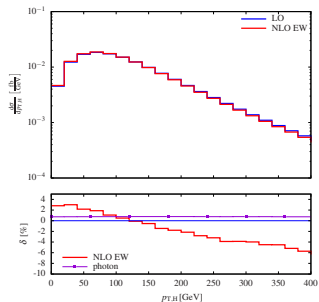
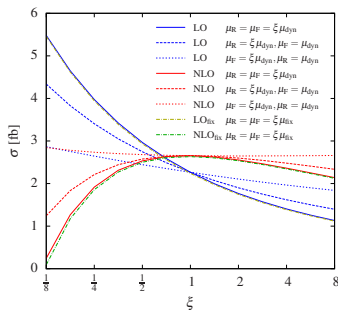
- Electroweak correction [Frixione et al. , '14,'15][Zhang et al., '14]
- Contributions not proportional to Yukawa
- 1-2% corrections to inclusive cross section
- Larger corrections in certain regions of phase space



[Frixione et al. , '15]

# Top decay

- Including top decays [Denner, Feger, '15]
- Combined with electroweak corrections [Denner, Lang, Pellen, Uccirati, '16]



[YR4, '16] [Denner, Lang, Pellen, Uccirati, '16]

# Background processes

- $pp \rightarrow t\bar{t}V$  (Electroweak correction)
- $pp \rightarrow t\bar{t}VV'$
  
- $pp \rightarrow t\bar{t}b\bar{b}$  (Flavor scheme)
- $pp \rightarrow t\bar{t} + X$  (Double counting with massless  $b\bar{b}$ )

# Why resummation for $t\bar{t}H$ ?

## Gains

- NNLO corrections out of reach
- Resummation can help reduce scale uncertainty
- Good process to start:
  - Simple color structure
  - Massive particles  $\rightarrow$  no final state collinear divergences



# Why resummation for $t\bar{t}H$ ?

## Gains

- NNLO corrections out of reach
- Resummation can help reduce scale uncertainty
- Good process to start:
  - Simple color structure
  - Massive particles  $\rightarrow$  no final state collinear divergences

## Pitfalls

- $2 \rightarrow 3$  phase space suppressed near threshold ( $\sigma \propto \beta^4$ )
- Small corrections from near absolute threshold

# Definition of Threshold

Threshold variable  $\hat{\tau} = \frac{Q^2}{\hat{s}}$

$Q^2$ : the invariant mass final state particles

$$1 - \hat{\tau} = 1 - \frac{Q^2}{\hat{s}}$$

$$\sim \frac{\text{energy of the emitted gluons}}{\text{total available energy}}$$

The IR divergences lead to logarithms:

$$(1 - \hat{\tau})^{-1-2\epsilon} = -\frac{1}{2\epsilon} \delta(1 - \hat{\tau}) + \left( \frac{1}{1 - \hat{\tau}} \right)_+ - 2\epsilon \left( \frac{\log(1 - \hat{\tau})}{1 - \hat{\tau}} \right)_+$$

$$\alpha_s^n \left( \frac{\log^m(1 - \hat{\tau})}{1 - \hat{\tau}} \right)_+$$

# Mellin Transform

Mellin transform is used with respect to  $\tau$  (needed for factorization of phase space):

$$\begin{aligned}\tilde{\sigma}_{pp \rightarrow t\bar{t}H}(N) &\equiv \int_0^1 d\tau \tau^{N-1} \sigma_{pp \rightarrow t\bar{t}H}(\tau, \mu_R, \mu_F) \\ &= \sum_{i,j} \tilde{f}_{i/p}(N+1, \mu_F) \tilde{f}_{j/p}(N+1, \mu_F) \tilde{\sigma}_{ij \rightarrow t\bar{t}H}(N, \mu_R, \mu_F)\end{aligned}$$

- $\tilde{f}_{i/p}(N+1, \mu_F)$ : Mellin transform with respect to  $x$
- $\tilde{\sigma}_{ij \rightarrow t\bar{t}H}(N, \mu_R, \mu_F)$ : Mellin transform with respect to  $\hat{\tau}$

$\log^n(1 - \hat{\tau}) \Rightarrow \log^n N$  and threshold  $\hat{\tau} \rightarrow 1 \sim N \rightarrow \infty$

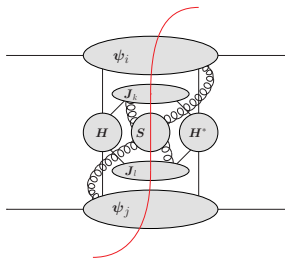
First application for  $2 \rightarrow 3$  in Mellin space

# General factorization

In general cross section factorizes into:

$$\hat{\sigma}_{ij \rightarrow kl \dots} = H_{ij \rightarrow kl \dots, IJ} \otimes \psi_i \otimes \psi_j \otimes S_{JI} \otimes J_k \otimes J_l \dots$$

- $H_{ij \rightarrow kl, IJ}$  Hard function
- $\psi_{i,j}$  Initial state collinear emission
- $J_{k,l, \dots}$  Final state collinear emission
- $S_{JI}$  Soft emission



Each of these functions is computed through renormalization group equations

# Orders of Resummation

Large logarithms  $\log N \equiv L$  for  $N \rightarrow \infty$

Perturbation needs to be reordered in  $\alpha_s$  and  $L$ :

$$\tilde{\sigma} \sim \tilde{\sigma}_{LO} \times \mathcal{C}(\alpha_s) \exp [Lg_1(\alpha_s L) + g_2(\alpha_s L) + \alpha_s g_3(\alpha_s L) + \dots]$$

With orders of precision:       $\Downarrow$                        $\Downarrow$                        $\Downarrow$

LL                      NLL                      NNLL

$\Downarrow$                        $\Downarrow$                        $\Downarrow$

$\alpha_s^n \log^{n+1}(N)$        $\alpha_s^n \log^n(N)$        $\alpha_s^{n+1} \log^n(N)$

Exponential functions are universal for initial state emission

*[Kodaira, Trentadue, '82][Sterman, '87][Catani, d'Emilio, Trentadue, '88][Catani, Trentadue, '89]*

# Soft anomalous dimension

## Soft anomalous dimension

Calculated at the hand of UV divergences of eikonal integrals

$$\Gamma_{ij \rightarrow klB, IJ}^{(1)} = -C_{IJ}^{ab} \text{Res} \{ \omega^{ab} \} - \Gamma_{ij \rightarrow C}^{(1)} \delta_{IJ}$$

- $I$  and  $J$ : color indices
- $a$  and  $b$ : colored particle indices
- $C_{IJ}^{ab}$ : color factor of the exchange
- $\omega^{ab}$ : UV divergent terms of eikonal integrals

# Soft wide-angle

[Kidonakis et al., '97-'01]

$$\begin{aligned} \tilde{S}_{ij \rightarrow kl} \left( \frac{Q}{\mu N} \right) &= \bar{P} \exp \left[ \int_Q^{Q/N} \frac{dq}{q} \Gamma_{ij \rightarrow kl}^\dagger (\alpha_s(q^2)) \right] \tilde{S}_{ij \rightarrow kl} \\ &\quad \times P \exp \left[ \int_Q^{Q/N} \frac{dq}{q} \Gamma_{ij \rightarrow kl} (\alpha_s(q^2)) \right] \end{aligned}$$

Path-order exponential solved at NNLL accuracy by

[Buras, '80][Ahrens, Ferroglia, Neubert, Pecjak, Yang, '10]

$$\mathbf{U}_R = \left( \mathbf{1} + \frac{\alpha_s(Q/\bar{N})}{\pi} \mathbf{K} \right) \left[ \left( \frac{\alpha_s(Q)}{\alpha_s(Q/\bar{N})} \right)^{\frac{\vec{\lambda}^{(1)}}{2\pi b_0}} \right]_D \left( \mathbf{1} - \frac{\alpha_s(Q)}{\pi} \mathbf{K} \right)$$

$$K_{IJ} = \delta_{IJ} \lambda_I^{(1)} \frac{b_1}{2b_0^2} - \frac{(\Gamma_R^{(2)})_{IJ}}{2\pi b_0 + \lambda_I^{(1)} - \lambda_J^{(1)}}$$

# Hard Matching Coefficient (Schematically)

$$H(\alpha_s) = H^{(0)} + \frac{\alpha_s}{\pi} H^{(1)} + \dots$$

$$S(\alpha_s(Q/\bar{N})) = S^{(0)} + \frac{\alpha_s(Q/\bar{N})}{\pi} S^{(1)} + \dots$$

- Soft and collinear functions computed
- Virtual contribution split into color channels from modified version of PowHel [*Garzelli, Kardos, Papadopoulos, Trócsányi, '11*]
- Average has been confirmed using:  
PowHeg-Box [*Hartanto, Jäger, Reina, Wackerroth, '15*]  
aMC@NLO [*Hirschi, Frederix, Frixione, Garzelli, Maltoni, Pittau, '11*]
- Include Coulomb correction  $\frac{1}{\beta_{34}}$



# Matching to Fixed Order

## Resummed Cross Section

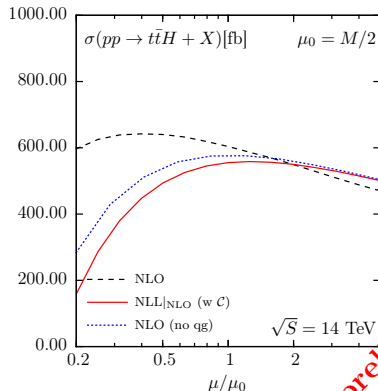
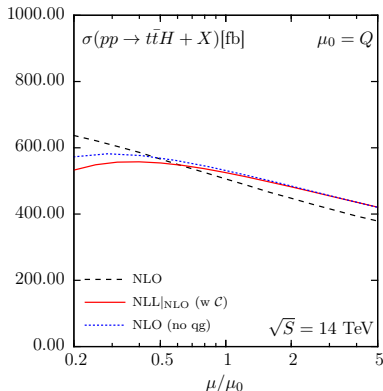
$$\begin{aligned}
 \sigma^{(\text{NLO+NLL})}(\tau) &= \sigma^{(\text{NLO})}(\tau) \\
 &+ \int_{\text{CT}} \frac{dN}{2\pi i} \tau^{-N} \tilde{f}_{g/p}(N+1) \tilde{f}_{g/p}(N+1) \\
 &\times \left[ \tilde{\sigma}^{(\text{NLL})}(N) - \tilde{\sigma}^{(\text{NLL})}(N)|_{(\text{NLO})} \right]
 \end{aligned}$$

Matching to fixed order required to avoid double counting.

# Results

[Kulesza, Motyka, Stebel, VT, in preparation]

PDFs used: PDF4LHC

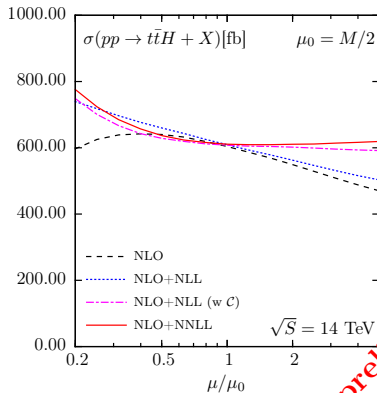
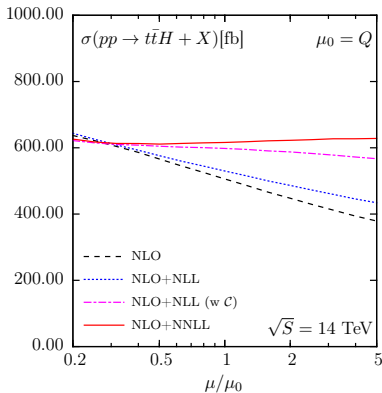


preliminary

# Results

[Kulesza, Motyka, Stebel, VT, in preparation]

PDFs used: PDF4LHC

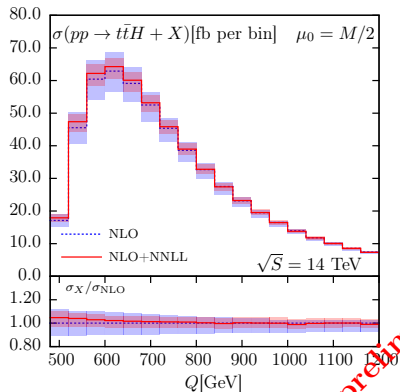
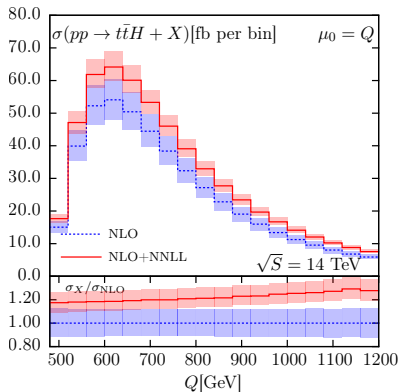


preliminary

# Results

[Kulesza, Motyka, Stebel, VT, in preparation]

PDFs used: PDF4LHC

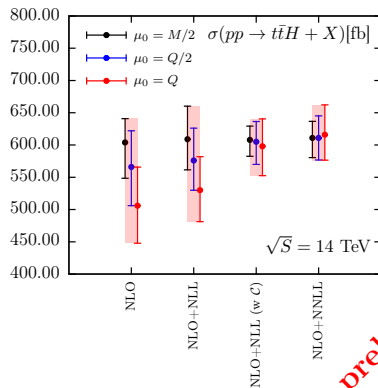
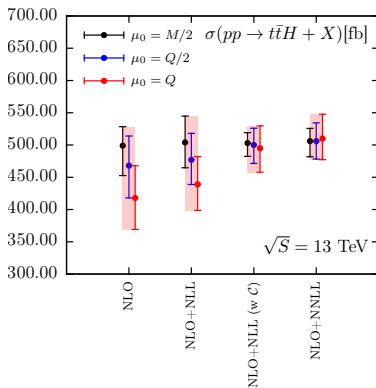


preliminary

# Results

[Kulesza, Motyka, Stebel, VT, in preparation]

PDFs used: PDF4LHC

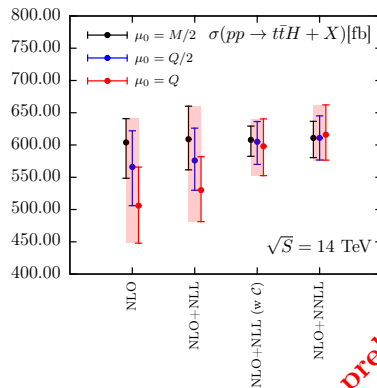
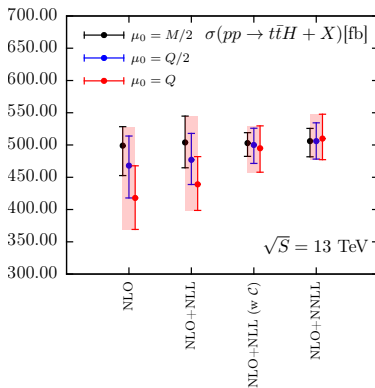


**preliminary**

# Results

[Kulesza, Motyka, Stebel, VT, in preparation]

PDFs used: PDF4LHC



**preliminary**

Thank you for your attention