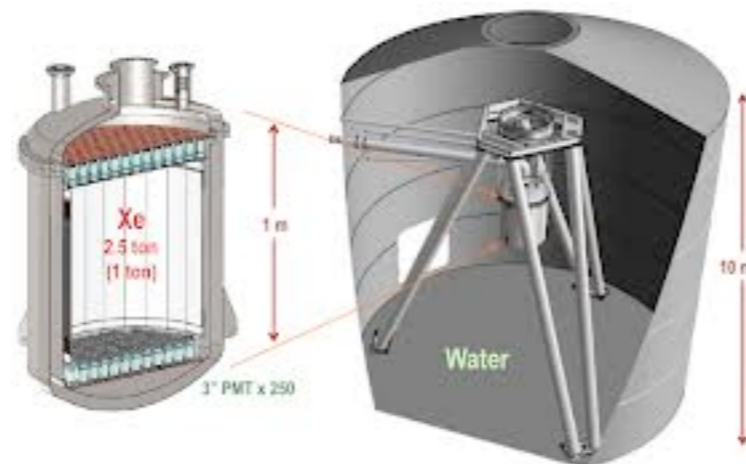
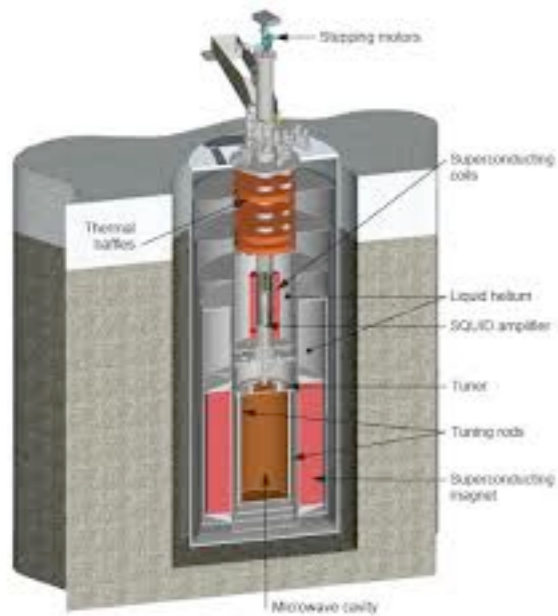


# Axions and WIMPs from natural SUSY (and where to find 'em)

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# Lots of problems with SM

- nu mass
- gauge hierarchy, why  $m(h)$  so small
- strong CP: why 3 not 4 light pions from QCD?
- dark matter?
- dark energy?
- baryogenesis?

SUSY either solves or improves all of these

# But where is SUSY

- LHC:  $m(\text{gluino}) > 1.9 \text{ TeV}$
- LHC:  $m(t_1) > 0.85 \text{ TeV}$
- $m(h) \sim 125 \text{ GeV}$
- compare: Barbieri-Giudice naturalness:  
 $m(\text{gluino}) < 350 \text{ GeV}$
- is SUSY unnatural? Is SUSY dead?

# No

- BG naturalness computed in multi-parameter effective theories
- In more fundamental theories (e.g. SUGRA) all soft terms inter-dependent: computed as multiples of more fundamental gravitino mass  $m(3/2)$
- Then large cancellations in fine-tuning computation (e.g. focus point SUSY, but now via all soft terms)
- More conservative measure:  $\Delta_{EW}$

$$m_Z^2/2 = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \sim -m_{H_u}^2 - \Sigma_u^u - \mu^2$$

naturalness: no large unnatural cancellations on RHS

then:

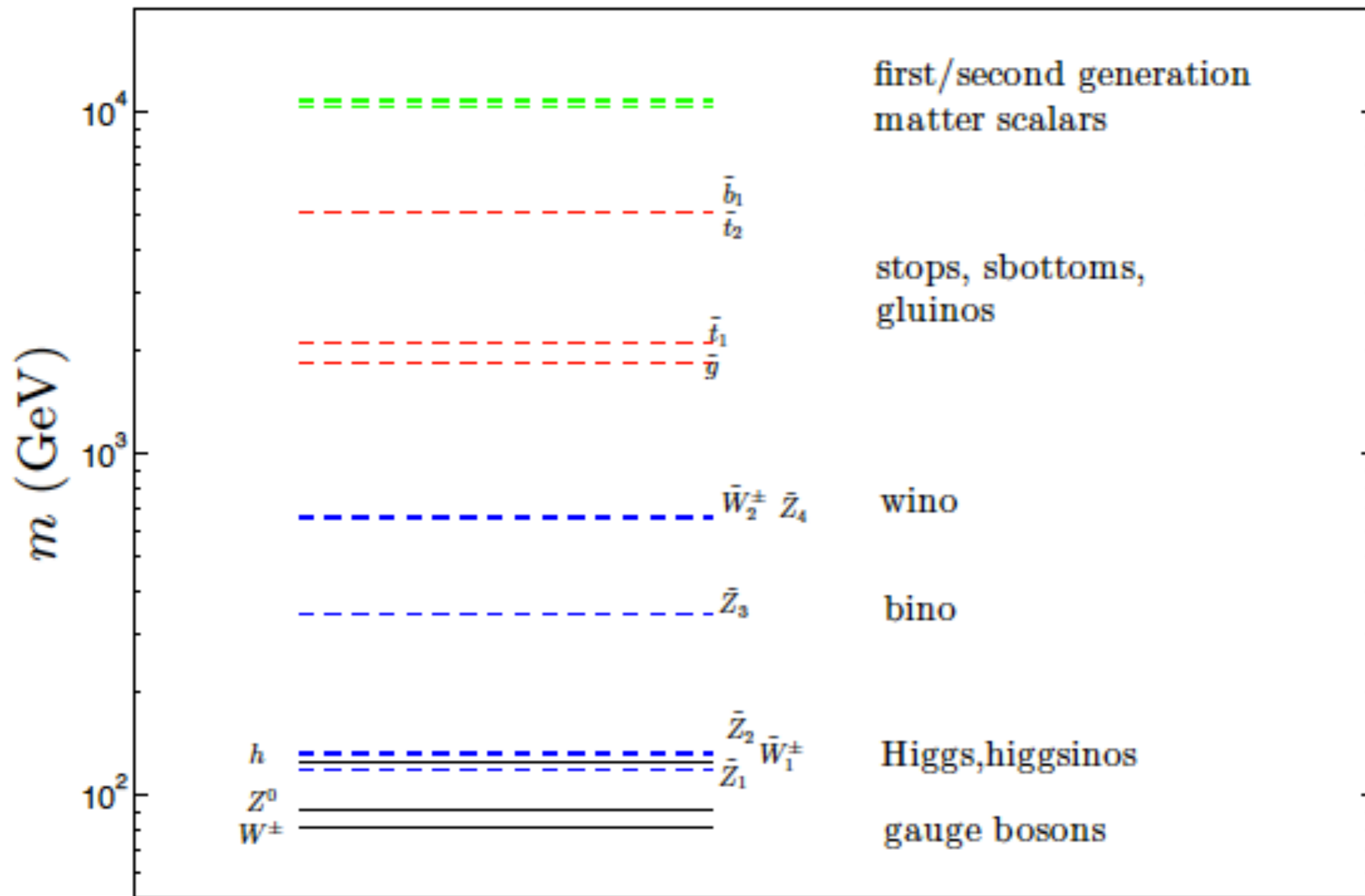
- $\mu \sim 100 - 200 \text{ GeV}$
- $m_{H_u}^2$  can be driven to natural via large top Yukawa
- radiative corrections not too large

naturalness: only higgsinos need be  $\sim 100\text{-}200 \text{ GeV}$

higgsino is LSP

higgsino-like WIMP  $\sim 100\text{-}200 \text{ GeV}$  thermally  
underproduced as DM

# Typical spectrum for low $\Delta_{EW}$ models



There is a Little Hierarchy, but it is **no problem**

$$\mu \ll m_{3/2}$$

SUSY  $\mu$  problem:  $\mu$  term is SUSY, not SUSY breaking:  
expect  $\mu \sim M(\text{Pl})$  but phenomenology requires  $\mu \sim m(\text{Z})$

- NMSSM:  $\mu \sim m(3/2)$ ; beware singlets!
- Giudice–Masiero:  $\mu$  forbidden by some symmetry:  
generate via Higgs coupling to hidden sector
- **Kim–Nilles**: invoke SUSY version of DFSZ axion  
solution to strong CP:

KN: PQ symmetry forbids  $\mu$  term,  
but then it is generated via PQ breaking

Little Hierarchy due to mismatch between  
PQ breaking and SUSY breaking scales?

$$\mu \sim \lambda f_a^2 / M_P$$

$$m_{3/2} \sim m_{hid}^2 / M_P$$

$$f_a \ll m_{hid}$$

**Higgs mass tells us where  
to look for axion!**

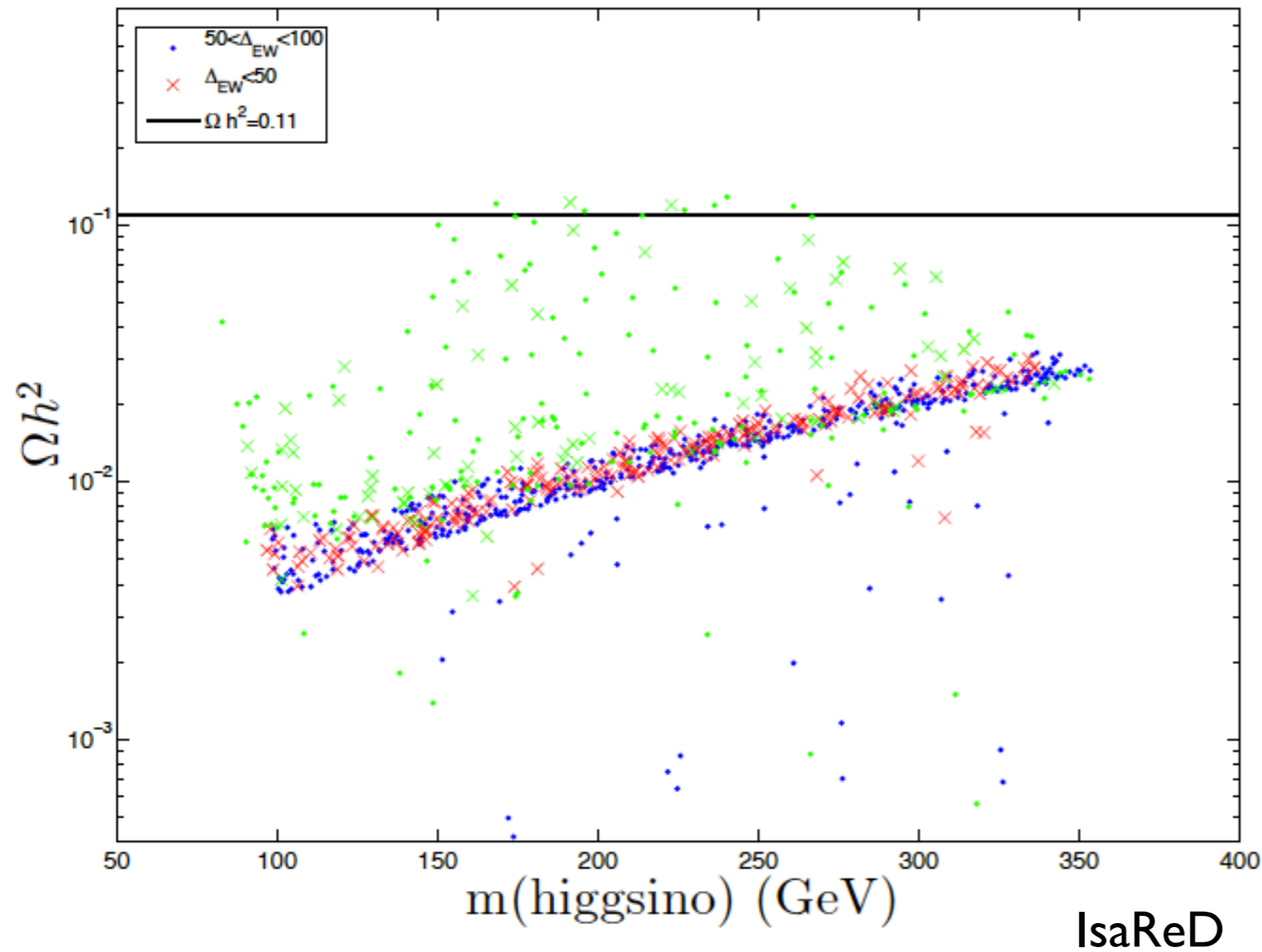
$$m_a \sim 6.2 \mu\text{eV} \left( \frac{10^{12} \text{ GeV}}{f_a} \right)$$

bounds from naturalness (3%)	BG/DG	Delta_EW
mu	350 GeV	350 GeV
gluino	400-600 GeV	5000 GeV
t1	450 GeV	3000 GeV
sq/sl	550-700 GeV	10-20 TeV

h(125) and LHC limits are perfectly compatible with 3-10% naturalness: **no crisis!**



# Mainly higgsino-like WIMPs thermally underproduce DM



green: excluded;  
red/blue: allowed

HB, Barger, Mickelson

Factor of 10–15 too low

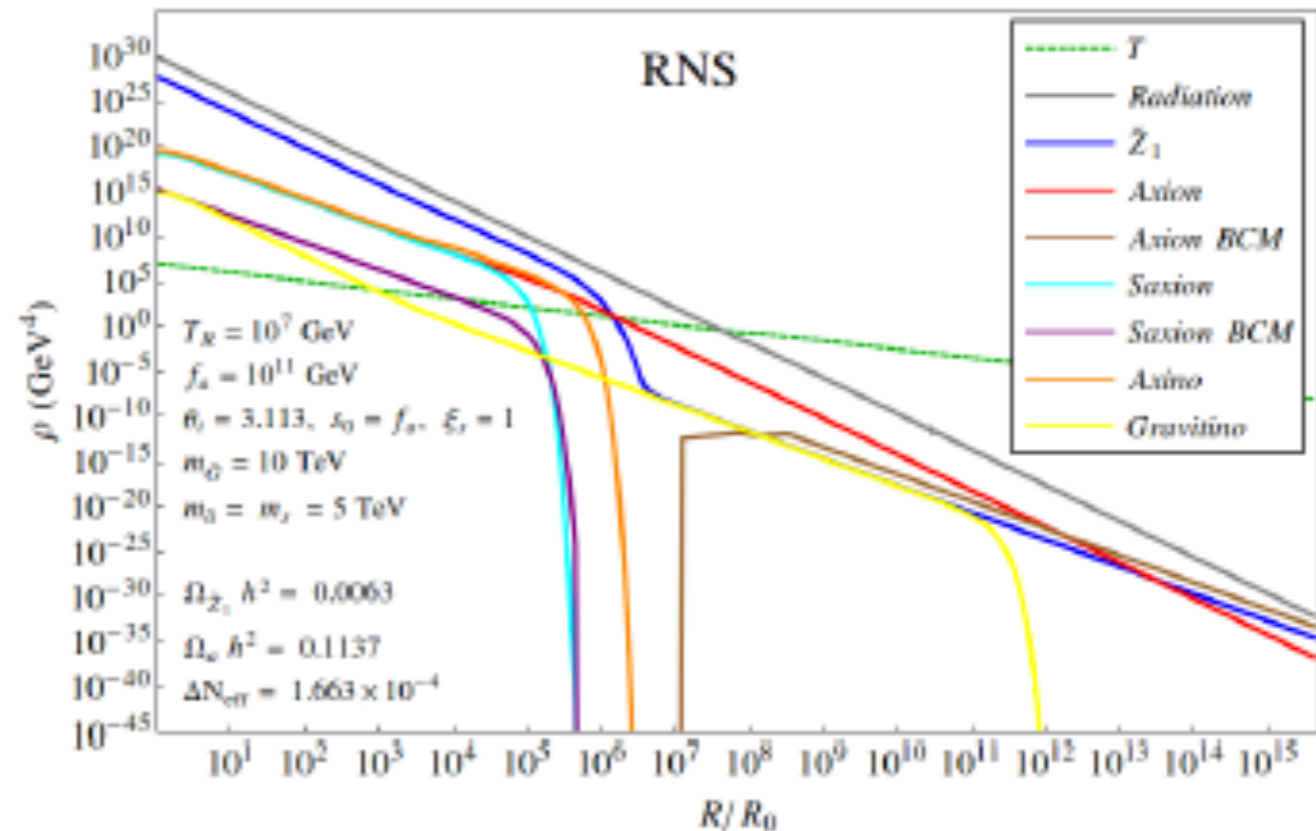
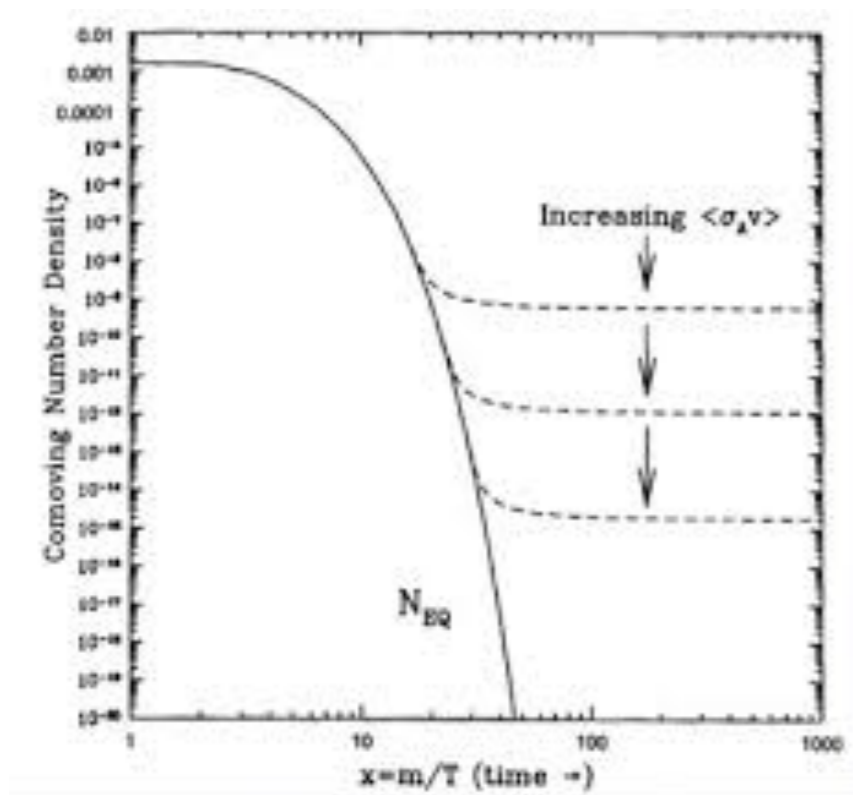
# mixed axion-neutralino production in early universe

- neutralinos: thermally produced (TP) or NTP via  $\tilde{a}$ ,  $s$  or  $\tilde{G}$  decays
  - re-annihilation at  $T_D^{s,\tilde{a}}$
- axions: TP, NTP via  $s \rightarrow aa$ , bose coherent motion (BCM)
- saxions: TP or via BCM
  - $s \rightarrow gg$ : entropy dilution
  - $s \rightarrow SUSY$ : augment neutralinos
  - $s \rightarrow aa$ : dark radiation ( $\Delta N_{eff} < 1.6$ )
- axinos: TP
  - $\tilde{a} \rightarrow SUSY$  augments neutralinos
- gravitinos: TP, decay to SUSY

usual picture

=>

mixed axion/WIMP



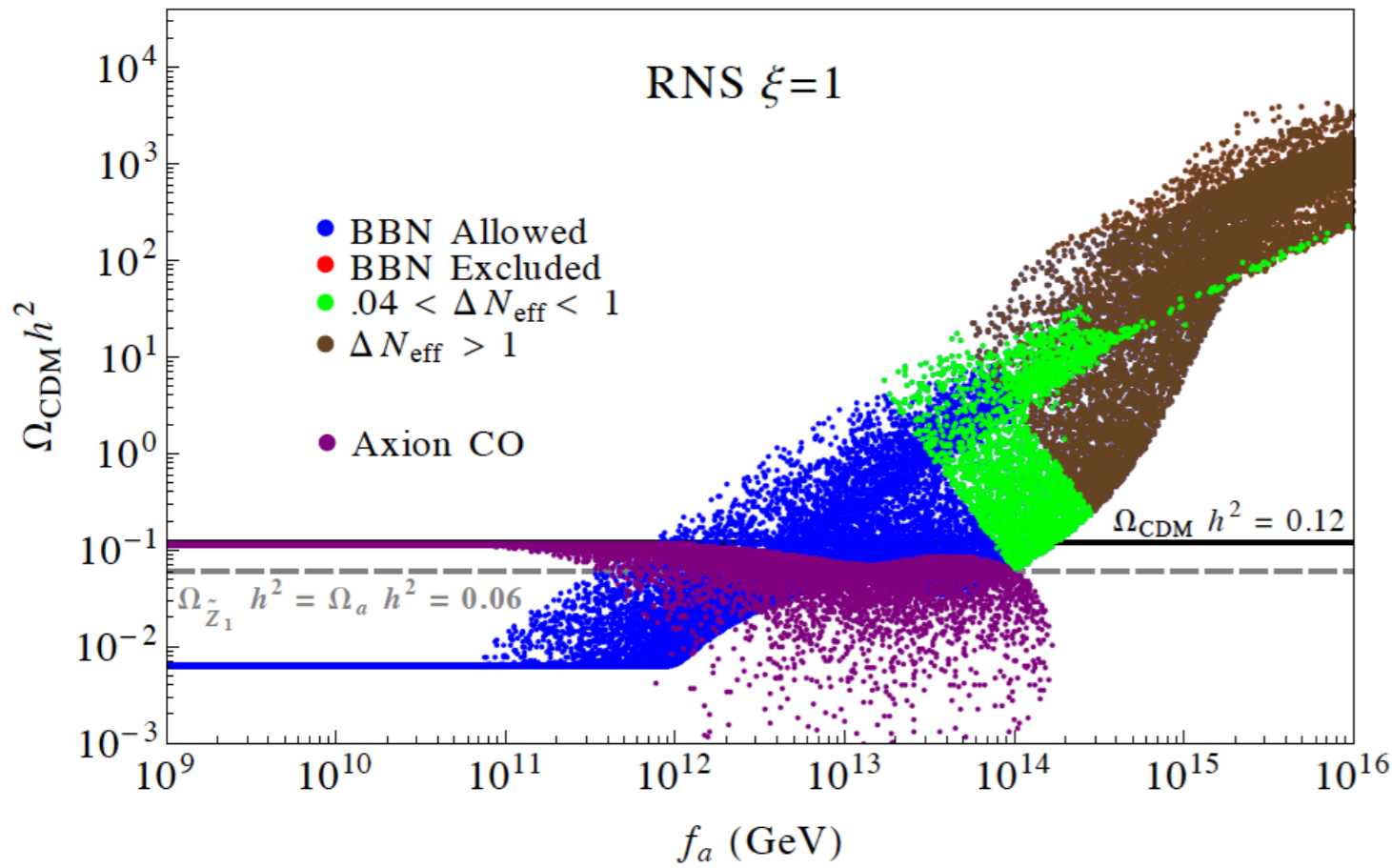
KJ Bae, HB, Lessa, Serce

much of parameter space is axion-dominated  
with 10-15% WIMPs



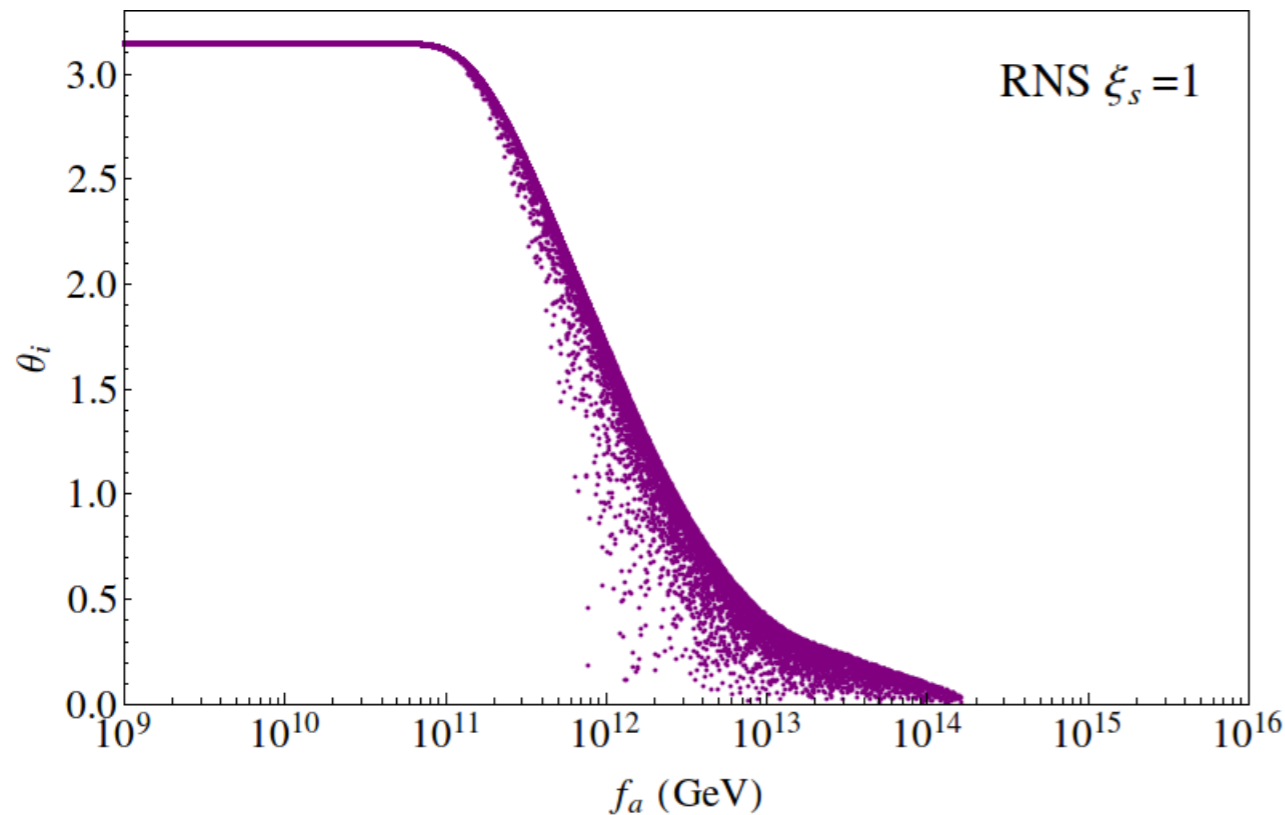
$\Rightarrow$



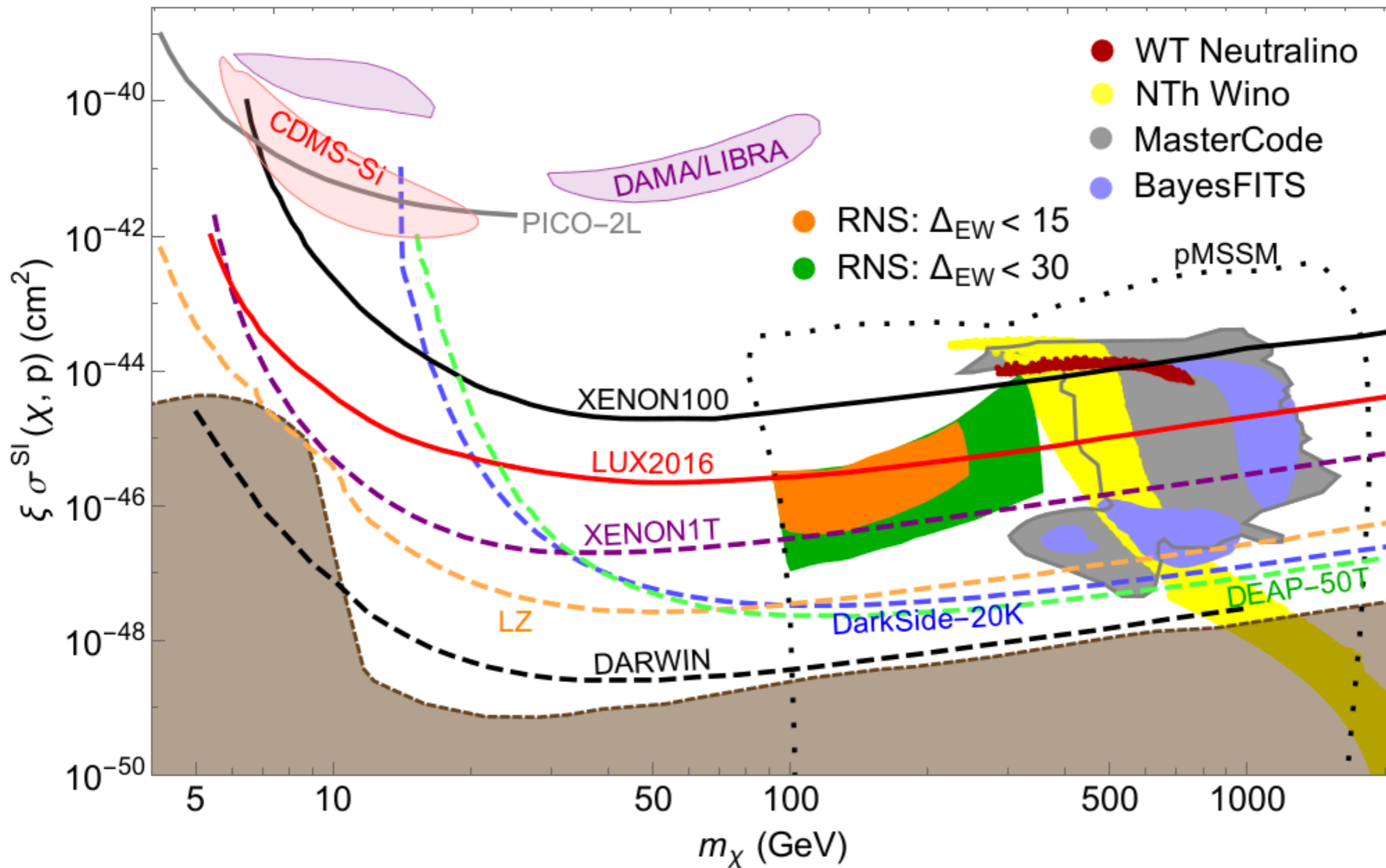


higgsino abundance

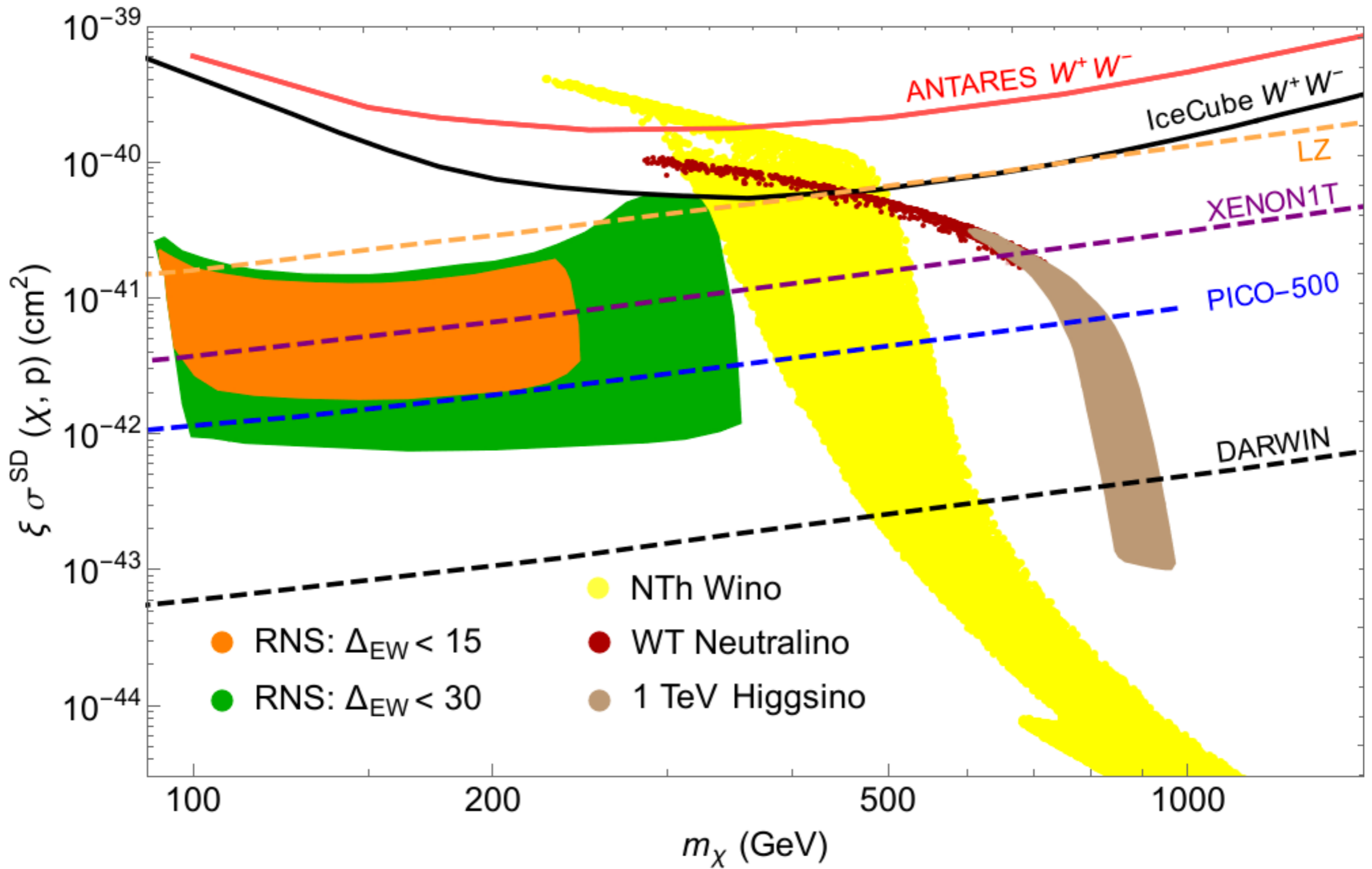
axion abundance



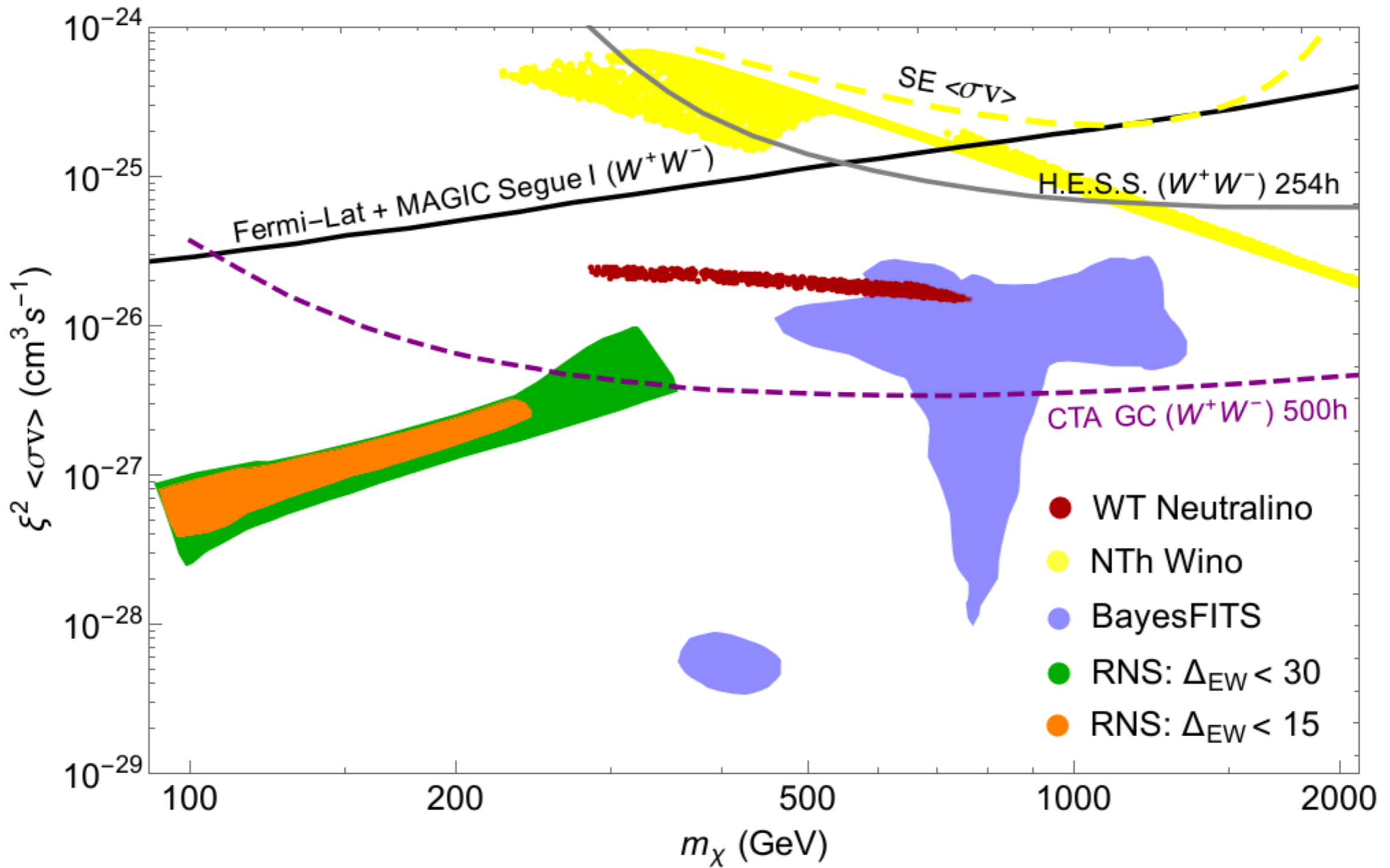
mainly axion CDM  
 for  $f_a < \sim 10^{12}$  GeV;  
 for higher  $f_a$ , then  
 get increasing wimp  
 abundance



may need n-ton scale noble liquid detector  
 because may be fewer target WIMPs if  
 most DM=axions

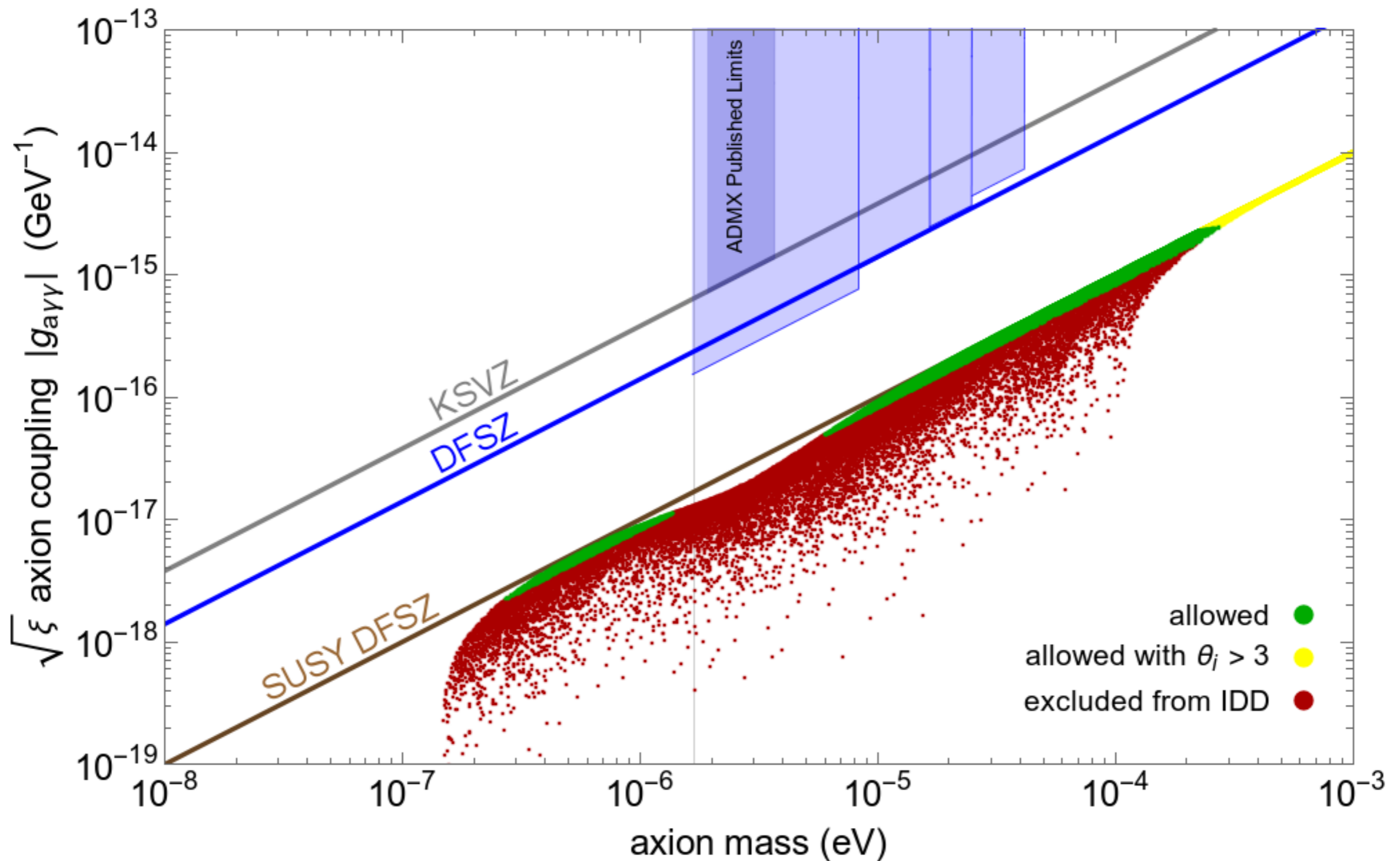


spin-dependent WIMP detection

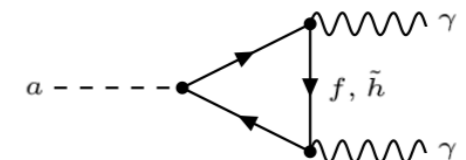


IDD- rate goes like square of depleted abundance





SUSY DFSZ axion: large range in  $m(a)$  but coupling reduced  
 may need to probe broader and deeper!



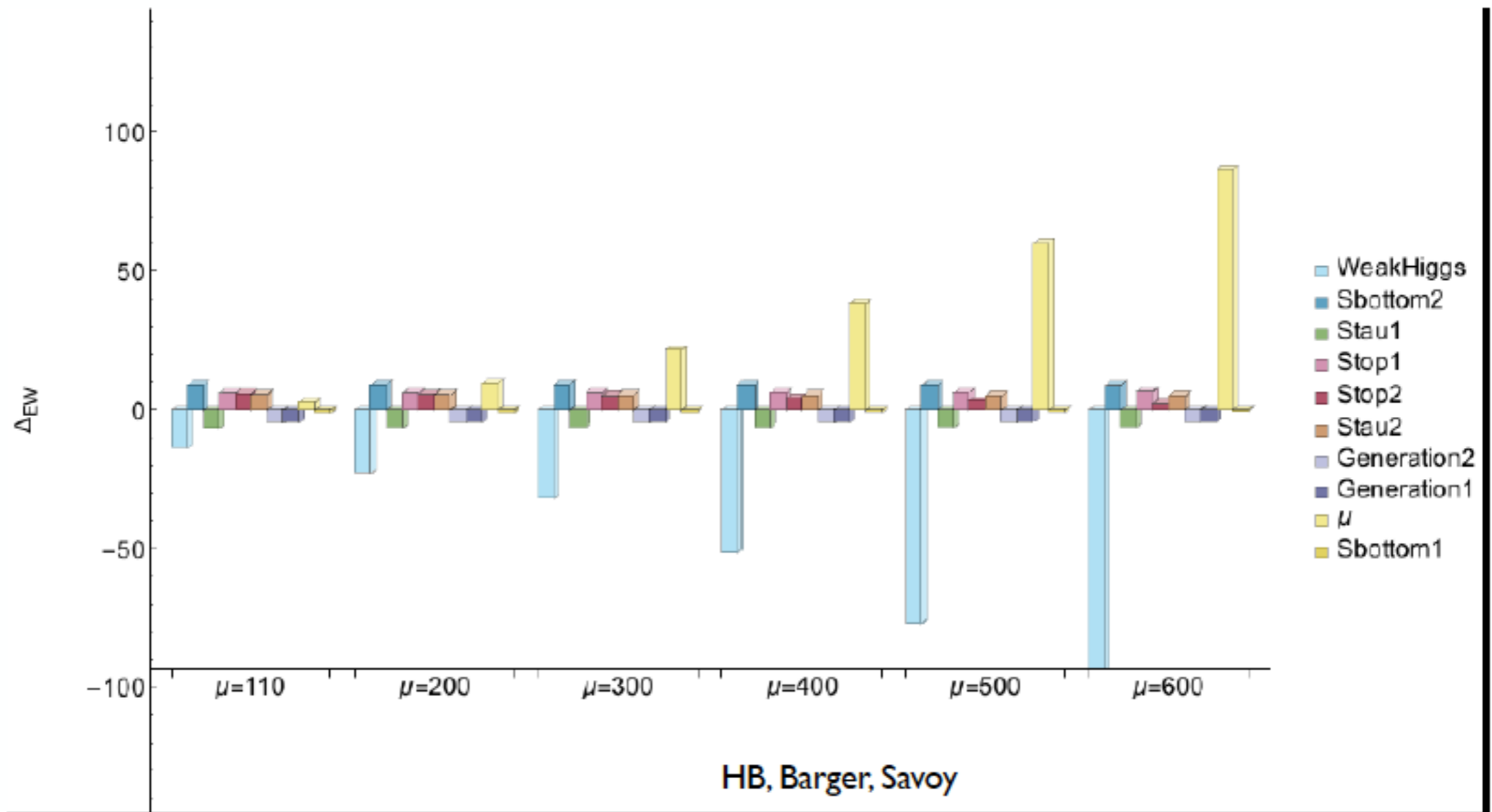
# summary slide

- Solve gauge hierarchy (SUSY)
- Solve strong CP (axion)
- Solve SUSY  $\mu$  problem (SUSY DFSZ axion)
- Allow/generate Little Hierarchy [ $\mu \ll m(\text{soft})$  ]
- Expect mixed higgsino/(SUSY) DFSZ axion DM
- Higgsino should be probed by ton scale DD search
- $m(a)$  for SUSY DFSZ axion spread across vast range
- $a$ - $\gamma$ - $\gamma$  coupling reduced compared to non-SUSY DFSZ
- Deeper and broader probes in axion  $p$ -space are required/encouraged
- Cost? see my experimental colleagues...

# Conclusions:

- SUSY very much alive: natural for  $m_{\tilde{\mu}} \sim 100\text{--}200$  GeV
- EW naturalness: higgsino-like WIMP
- QCD naturalness: axion
- SUSY  $\mu$  problem/Little Hierarchy: SUSY DFSZ axion
- DM=higgsino-like WIMP+DFSZ axion admixture?
- n-ton SI noble liquid detectors should probe all p-space
- axions: must probe broader and deeper!
- (HL)-LHC: maybe see SUSY, maybe not
- HE-LHC33 TeV may be required
- ILC is ideal for light higgsinos

# How much is too much fine-tuning?



Visually, large fine-tuning has already developed by  $\mu \sim 350$  or  $\Delta_{EW} \sim 30$

higgsinos should be accessible to ILC!

# Little Hierarchy from radiative PQ breaking? exhibited within context of MSY model

Murayama, Suzuki, Yanagida (1992);  
Gherghetta, Kane (1995)

Choi, Chun, Kim (1996)

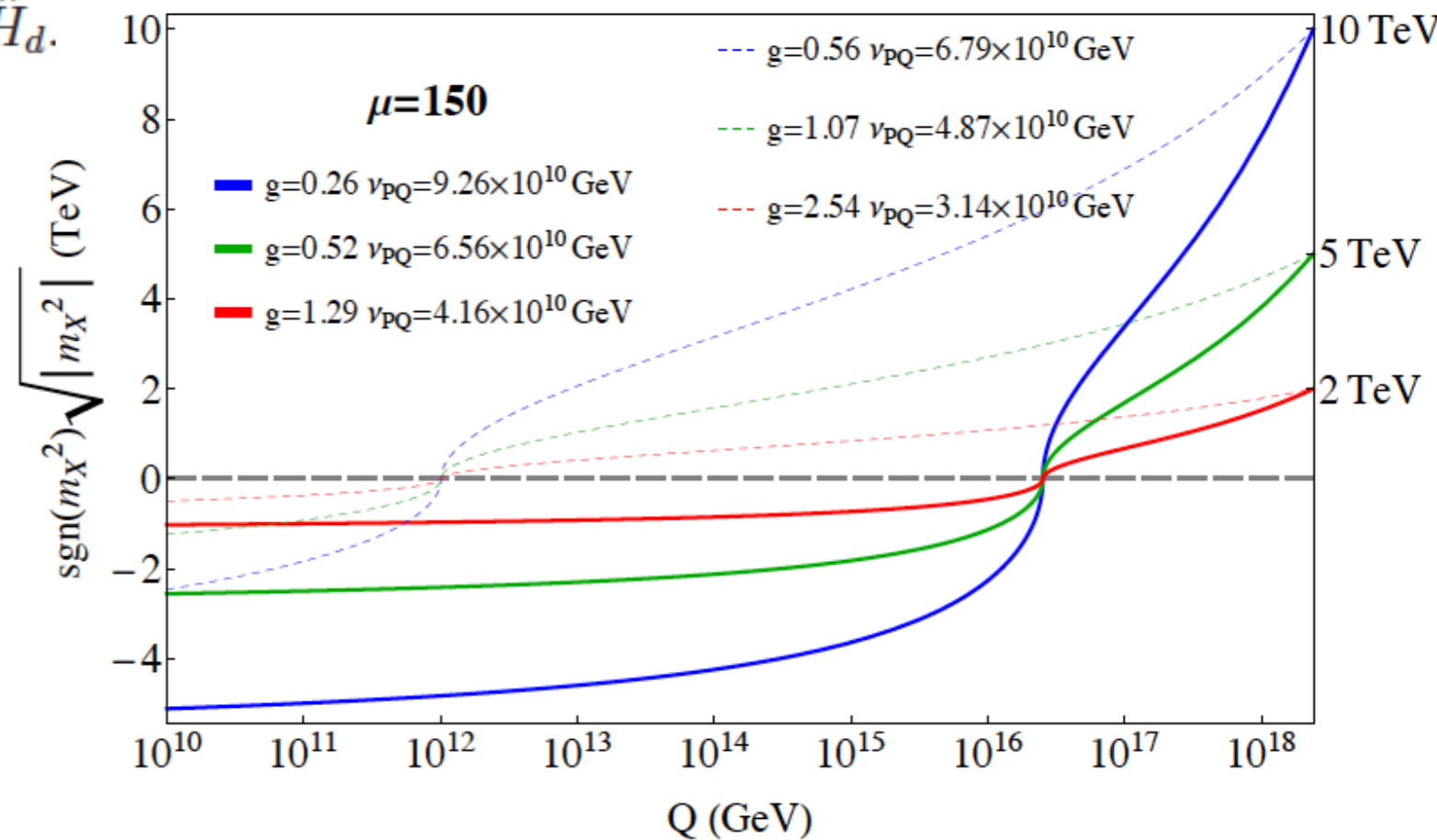
Bae, HB, Serce, PRD91 (2015) 015003

augment MSSM with PQ charges/fields:

$$\hat{f}' = \frac{1}{2} h_{ij} \hat{X} \hat{N}_i^c \hat{N}_j^c + \frac{f}{M_P} \hat{X}^3 \hat{Y} + \frac{g}{M_P} \hat{X} \hat{Y} \hat{H}_u \hat{H}_d.$$

$$M_{N_i^c} = v_X h_i |_{Q=v_X}$$

$$\mu = g \frac{v_X v_Y}{M_P}.$$

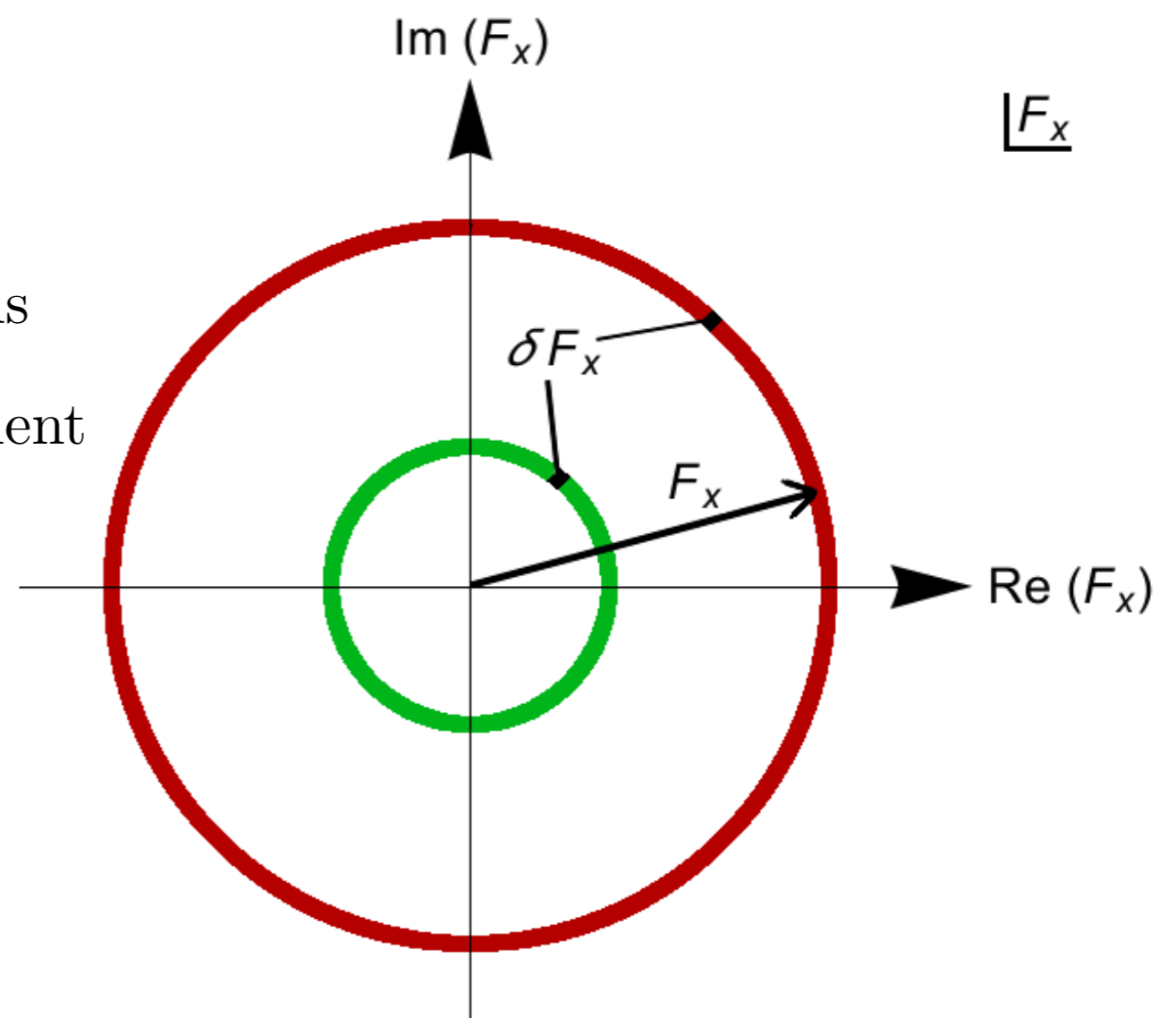


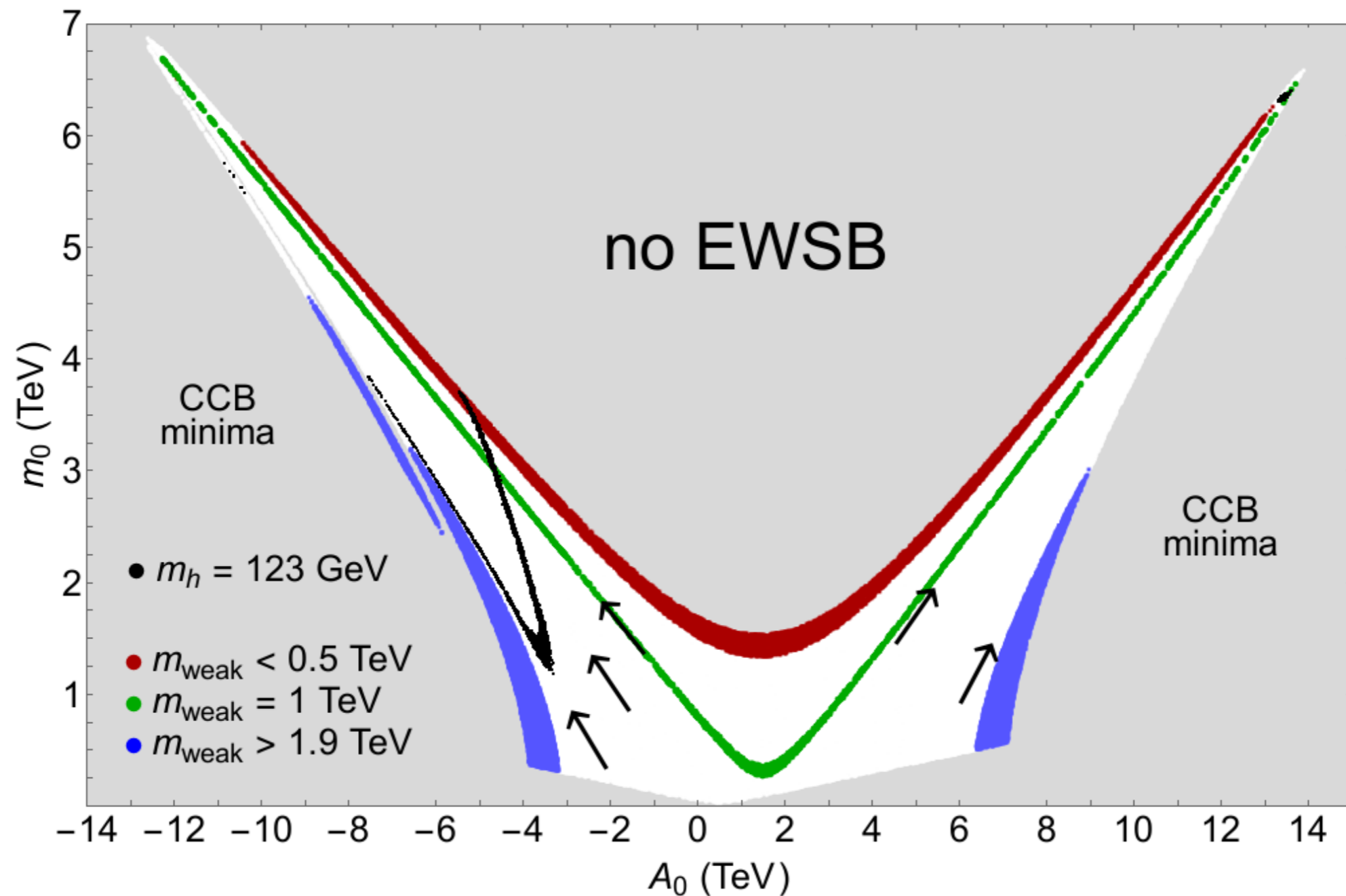
Large  $m_{3/2}$  generates small  $\mu \sim 100 - 200$  GeV!

# Why do soft terms take on values needed for natural (barely-broken) EWSB? string theory landscape?

- assume model like MSY/CCK where  $\mu \sim 100$  GeV
- then  $m(\text{weak})^2 \sim |m_{H_u}^2|$
- If all values of SUSY breaking field  $\langle F_X \rangle$  equally likely, then mild (linear) statistical draw towards large soft terms
- This is balanced by anthropic requirement of weak scale  $m_{\text{weak}} \sim 100$  GeV

*Anthropic selection of  $m_{\text{weak}} \sim 100$  GeV:*  
If  $m_W$  too large, then weak interactions  $\sim (1/m_W^4)$  too weak  
weak decays, fusion reactions suppressed  
elements not as we know them

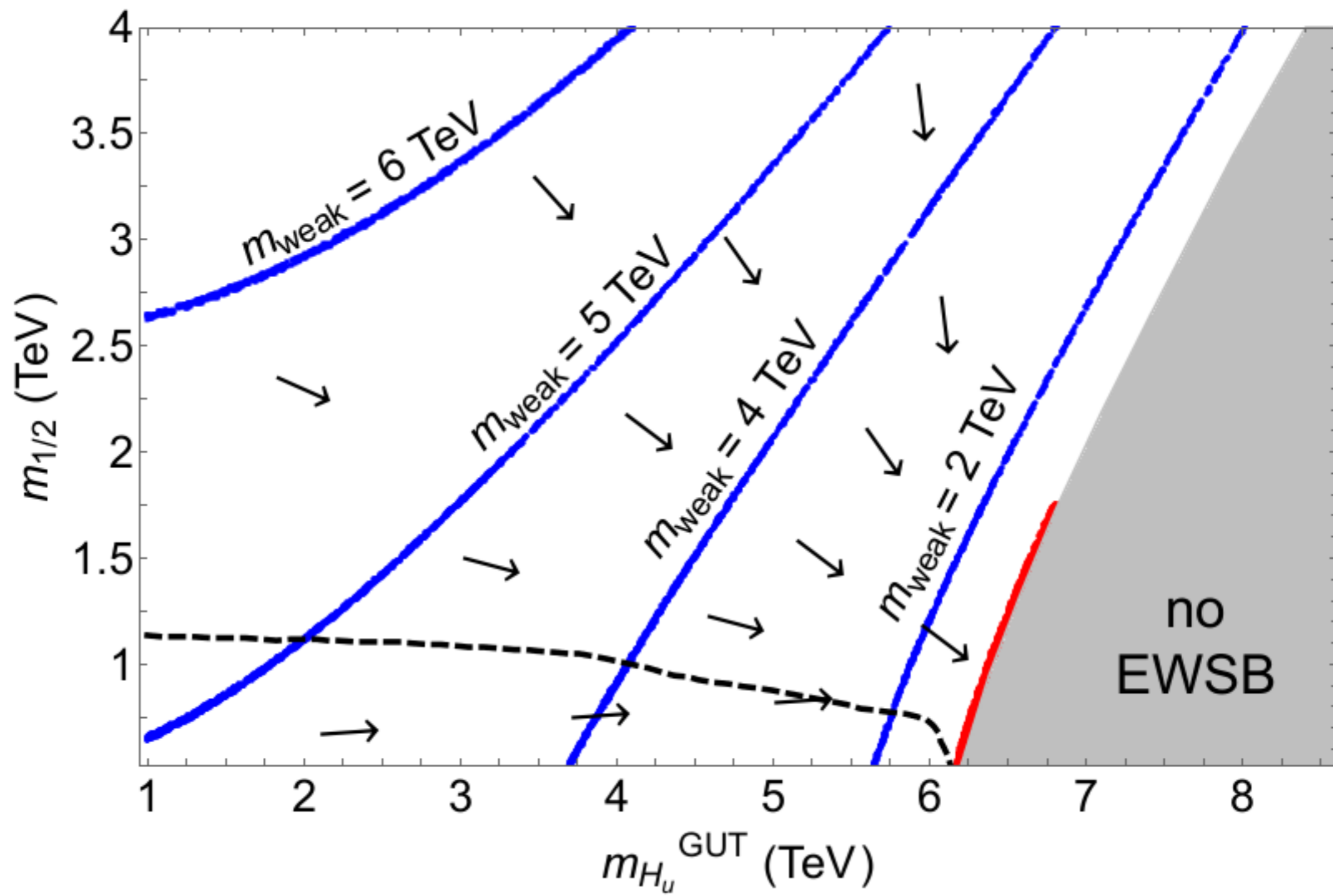




statistical draw to large soft terms balanced by anthropic draw toward red ( $m(\text{weak}) \sim 100$  GeV): then  $m(\text{Higgs}) \sim 125$  GeV and natural SUSY spectrum!

Giudice, Rattazzi, 2006

HB, Barger, Savoy, Serce, PLB758 (2016) 113



statistical/anthropic draw toward FP-like region