

# Preliminary combination of the KLOE08, KLOE10 and KLOE12 ISR measurements

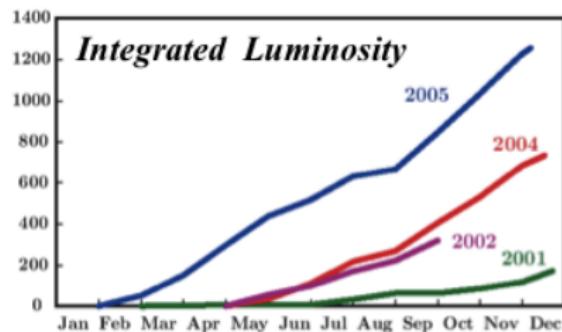
A. Keshavarzi, S. E. Müller, T. Teubner, G. Venanzoni

on behalf of the KLOE-2 collaboration

*First Workshop of the Muon g-2 Theory Initiative  
Q-Center St. Charles, 3-6 June 2017*

# DAΦNE: A $\phi$ factory

$e^+e^-$  collider with  $\sqrt{s} = m_\phi \simeq 1.02$  GeV



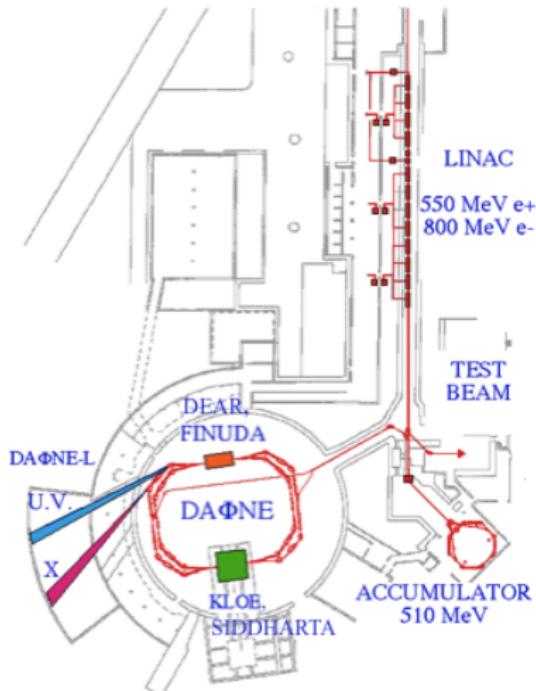
Peak luminosity  $L_{\text{peak}} = 1.4 \cdot 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$

Total KLOE int. luminosity:

$$\int L dt \sim 2.1 \text{ fb}^{-1} \text{ (2001 - 05)}$$

2006:

- ▶ Energy scan with 4 points around  $m_\phi$
- ▶  $250 \text{ pb}^{-1}$  at  $\sqrt{s} = 1 \text{ GeV}$



# KLOE:

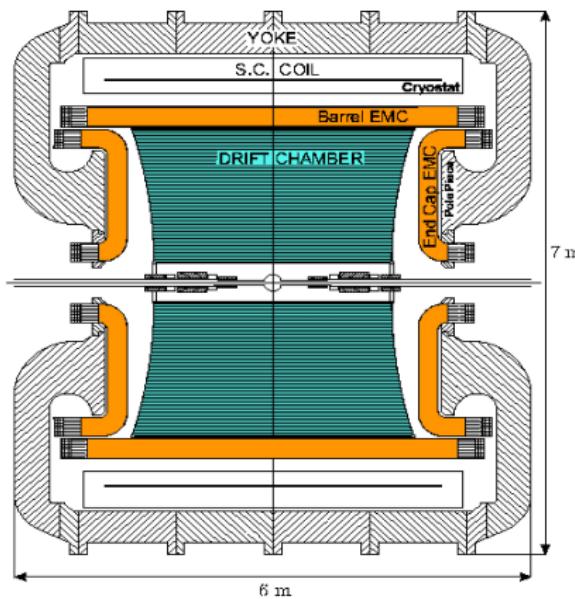
Driftchamber:



$$\sigma_{r\phi} = 150 \mu m, \sigma_z = 2 mm$$
$$\sigma_p/p = 0.4\%$$

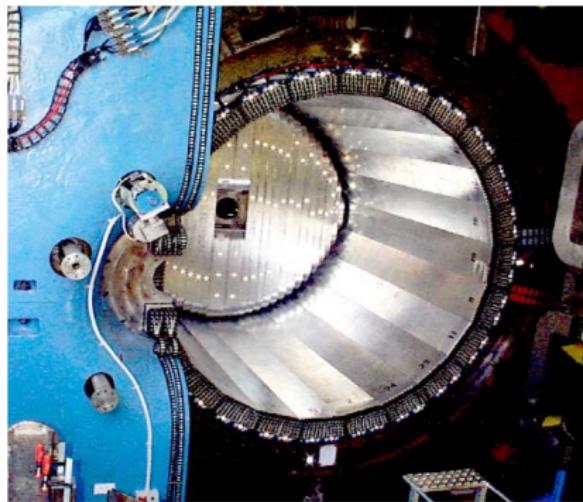
*Excellent momentum  
resolution*

KLOE Detector

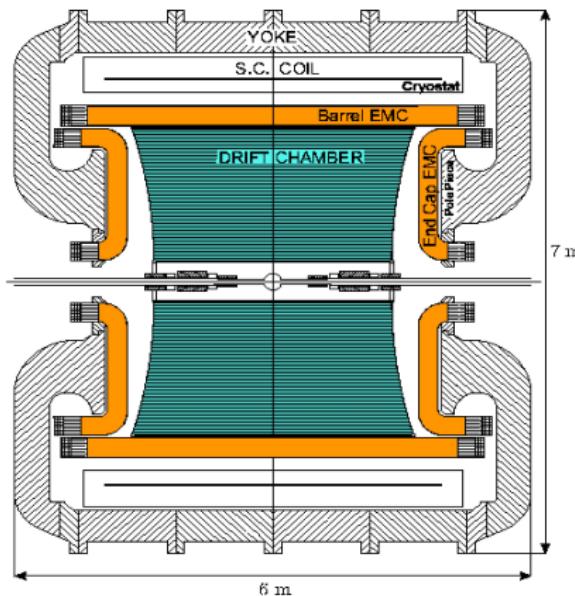


# KLOE:

## Electromagnetic Calorimeter



## KLOE Detector



$$\sigma_t = 54\text{ps}/\sqrt{E(\text{GeV})} \oplus 100\text{ps},$$
$$\sigma_E/E = 5.7\%/\sqrt{E(\text{GeV})},$$

*Excellent time resolution*

# The KLOE data sets

- **KLOE05:** 60 points between 0.35 and 0.95  $\text{GeV}^2$ ,  
based on  $141.4 \text{ pb}^{-1}$  of data taken in 2001<sup>a</sup>  
(small angle photon cuts, normalization to Bhabha and PHOKHARA radiator)
- **KLOE08:** 60 points between 0.35 and 0.95  $\text{GeV}^2$ ,  
based on  $240.0 \text{ pb}^{-1}$  data taken in 2002<sup>b</sup>  
(small angle photon cuts, normalization to Bhabha and PHOKHARA radiator)
- **KLOE10:** 75 points between 0.1 and 0.85  $\text{GeV}^2$ ,  
based on  $232.6 \text{ pb}^{-1}$  data taken in 2006<sup>c</sup> with  $\sqrt{s} = 1.00 \text{ GeV}$   
(large angle photon cuts, normalization to Bhabha and PHOKHARA radiator)
- **KLOE12:** 60 points between 0.35 and 0.95  $\text{GeV}^2$ ,  
based on  $240.0 \text{ pb}^{-1}$  data taken in 2002<sup>d</sup>  
(small angle photon cuts, normalization to  $\mu\mu\gamma$  events)

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<sup>a</sup>Phys. Lett. B**606** (2005) 12

<sup>b</sup>Phys. Lett. B**670** (2009) 285

<sup>c</sup>Phys. Lett. B**700** (2011) 102

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*Superseded by KLOE08!*
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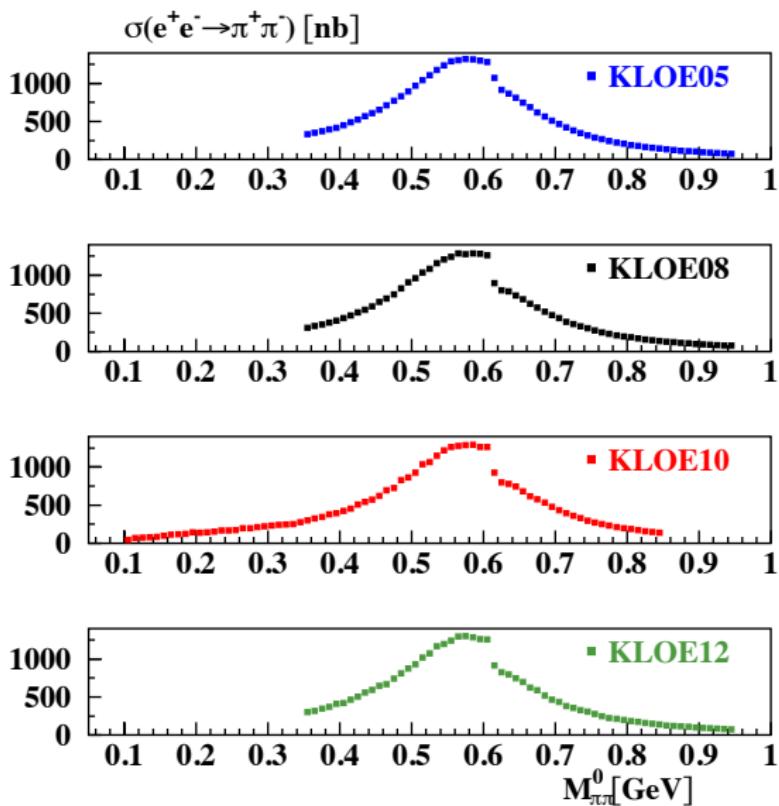
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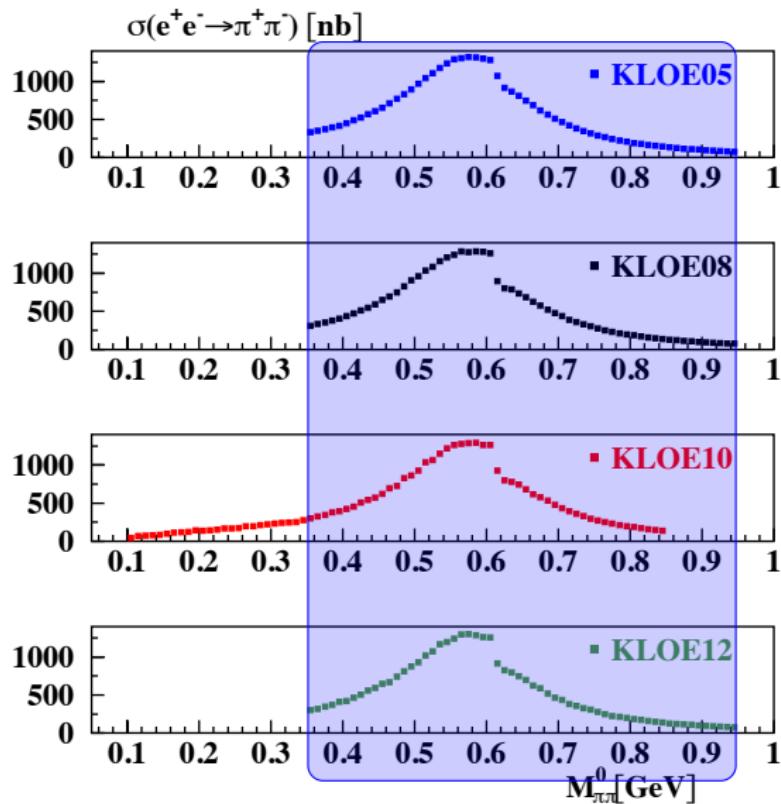
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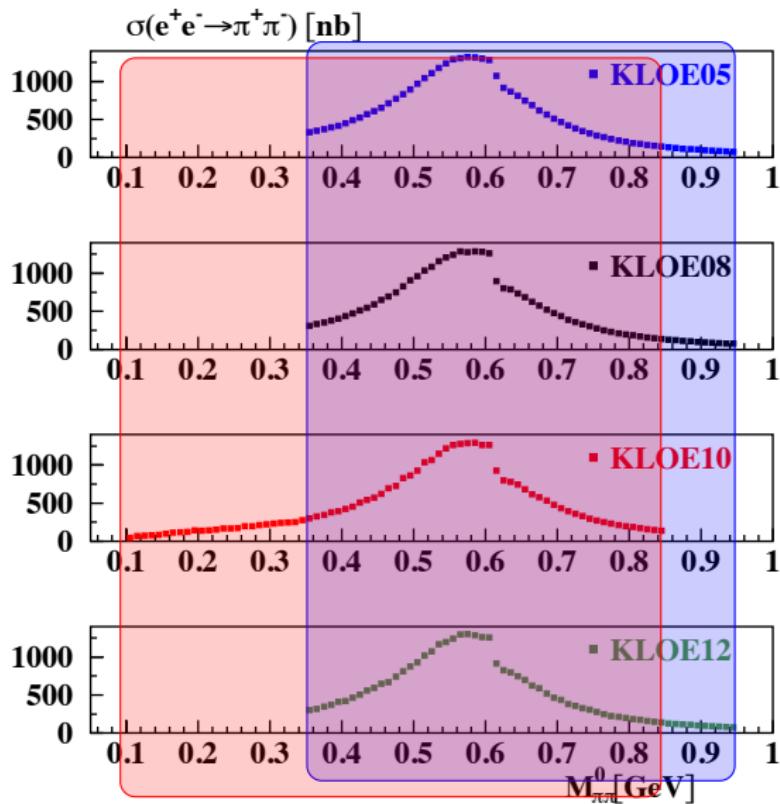
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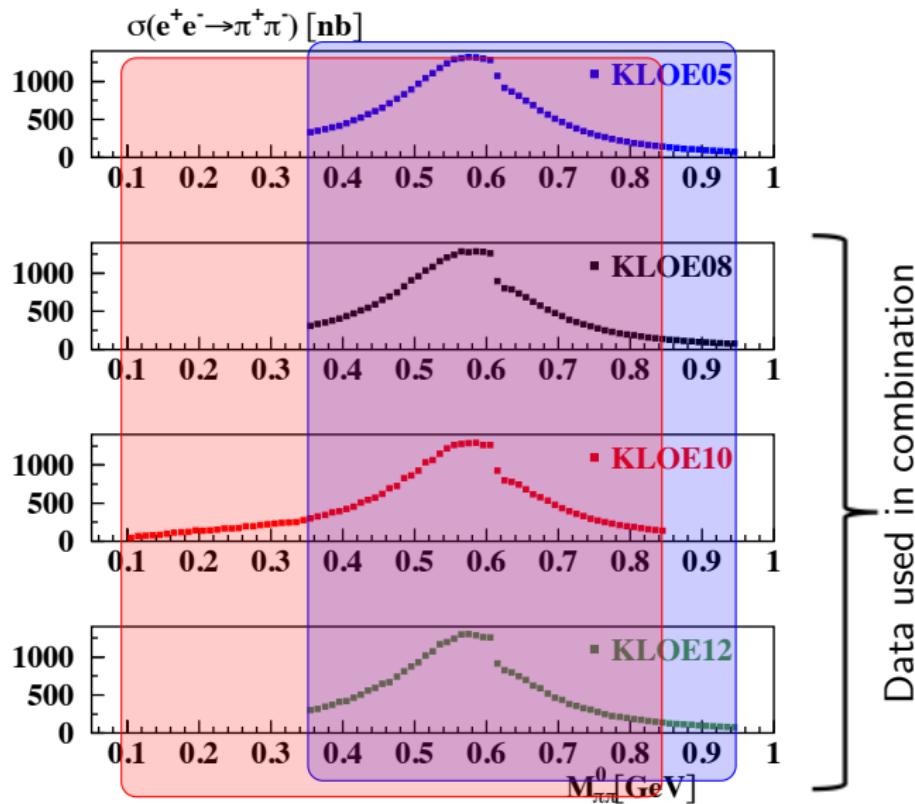
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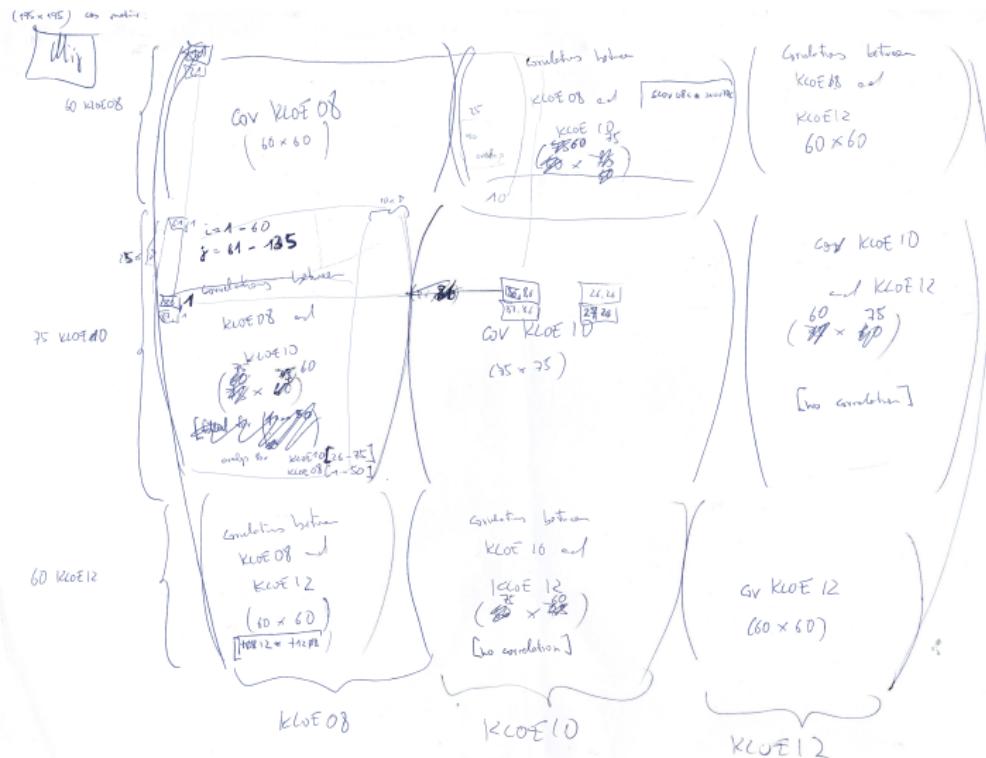


## The covariance matrix

The  $(195 \times 195)$  covariance matrix for the  $60 + 75 + 60$  data points:

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$$\left( \begin{array}{c|cc|c} \dots & \dots & \dots & \dots \\ \dots & \dots & \dots & \dots \\ \text{KLOE08} & \dots & \text{KLOE0810} & \dots \\ 60 \times 60 & \dots & 60 \times 75 & \dots \\ \dots & \dots & \dots & \dots \\ \dots & \dots & \dots & \dots \\ \hline \dots & \dots & \dots & \dots \\ \dots & \dots & \dots & \dots \\ \dots & \dots & \dots & \dots \\ \text{KLOE1008} & \dots & \text{KLOE10} & \dots \\ 75 \times 60 & \dots & 75 \times 75 & \dots \\ \dots & \dots & \dots & \dots \\ \dots & \dots & \dots & \dots \\ \hline \dots & \dots & \dots & \dots \\ \dots & \dots & \dots & \dots \\ \text{KLOE1208} & \dots & \text{KLOE1210} & \dots \\ 60 \times 60 & \dots & 60 \times 75 & \dots \\ \dots & \dots & \dots & \dots \end{array} \right)$$

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The  $(195 \times 195)$  covariance matrix for the  $60 + 75 + 60$  data points:

<p>.....</p> <p>.....</p> <p>KLOE08 <math>60 \times 60</math></p> <p>.....</p> <p>.....</p>	<p>.....</p> <p>.....</p> <p>.....</p> <p>KLOE0810 <math>60 \times 75</math></p> <p>.....</p> <p>.....</p>	<p>.....</p> <p>.....</p> <p>.....</p> <p>KLOE0812 <math>60 \times 60</math></p> <p>.....</p> <p>.....</p>
<p>.....</p> <p>.....</p> <p>.....</p> <p>KLOE1008 <math>75 \times 60</math></p> <p>.....</p> <p>.....</p>	<p>.....</p> <p>.....</p> <p>.....</p> <p>KLOE10 <math>75 \times 75</math></p> <p>.....</p> <p>.....</p>	<p>.....</p> <p>.....</p> <p>.....</p> <p>KLOE1012 <math>75 \times 60</math></p> <p>.....</p> <p>.....</p>
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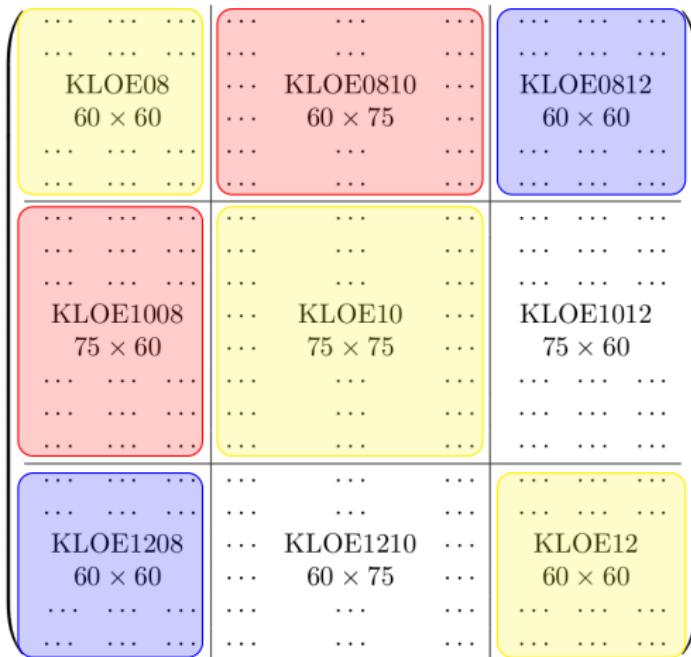
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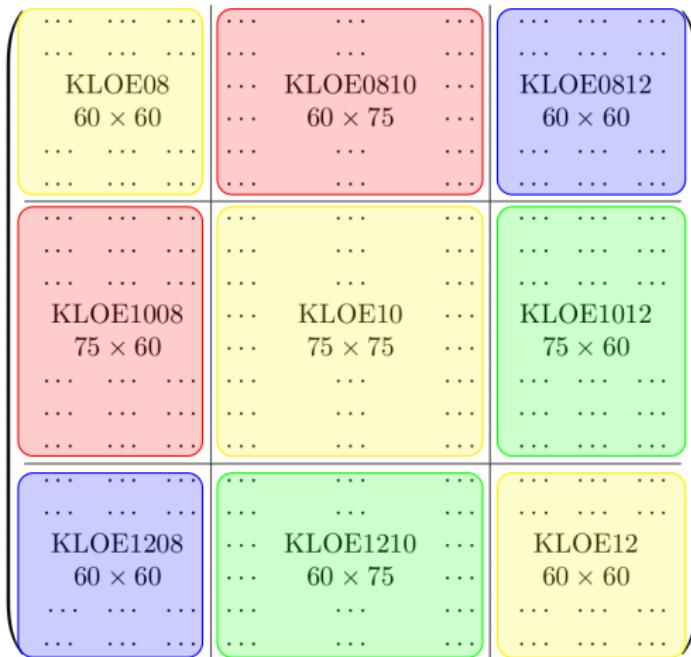
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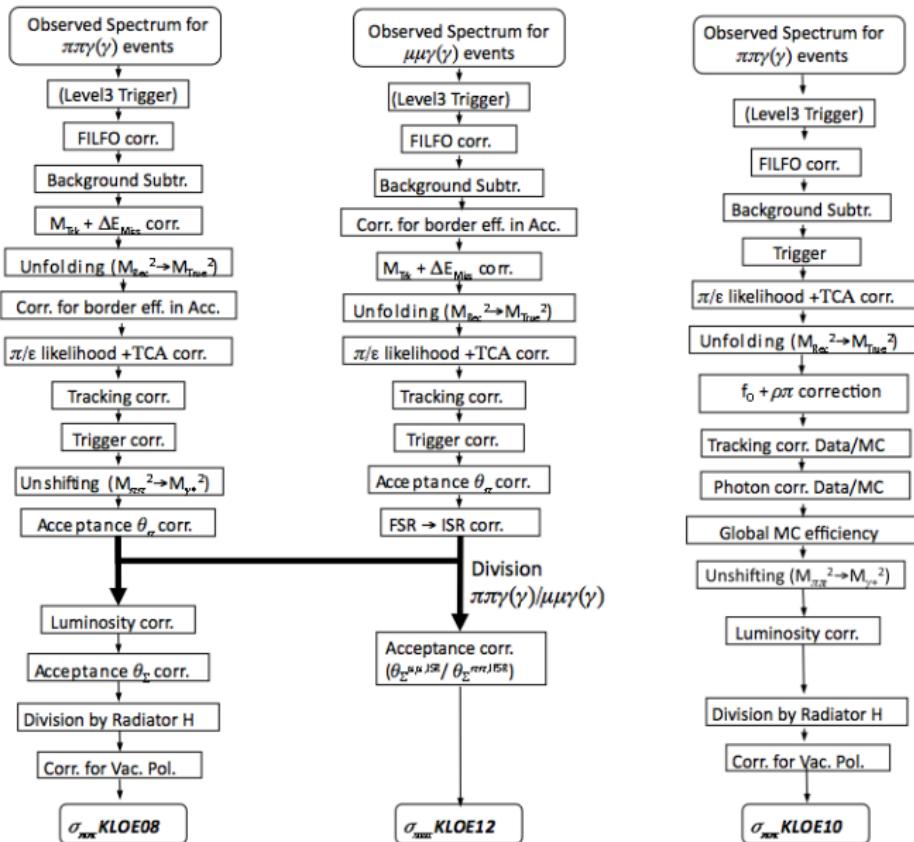


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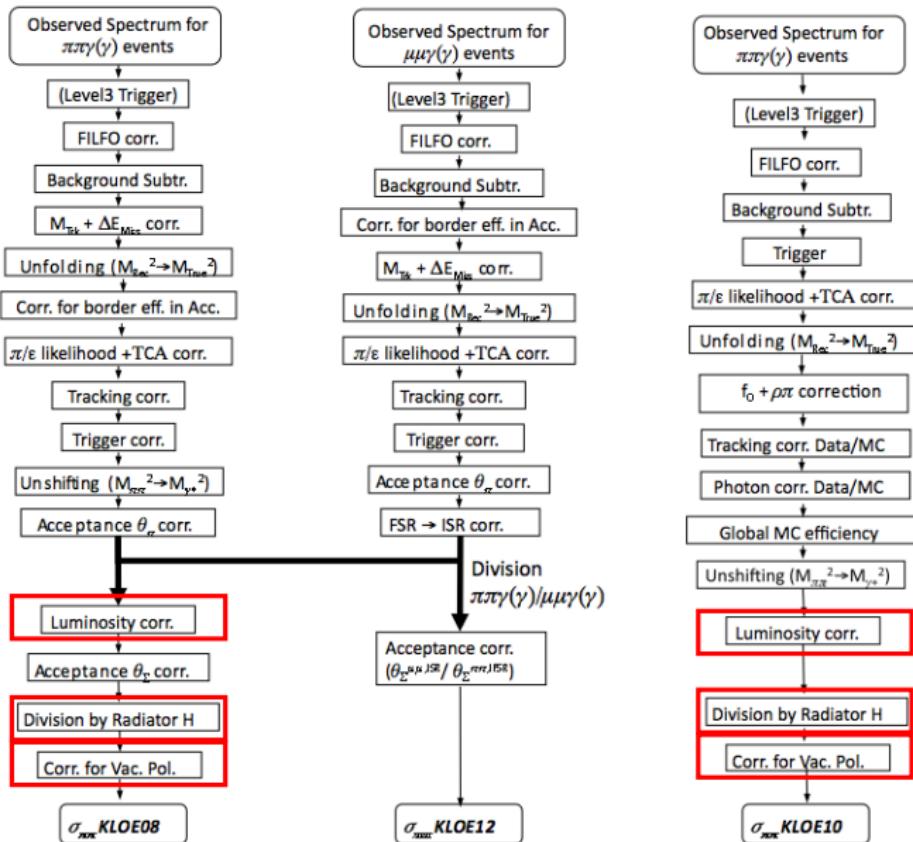
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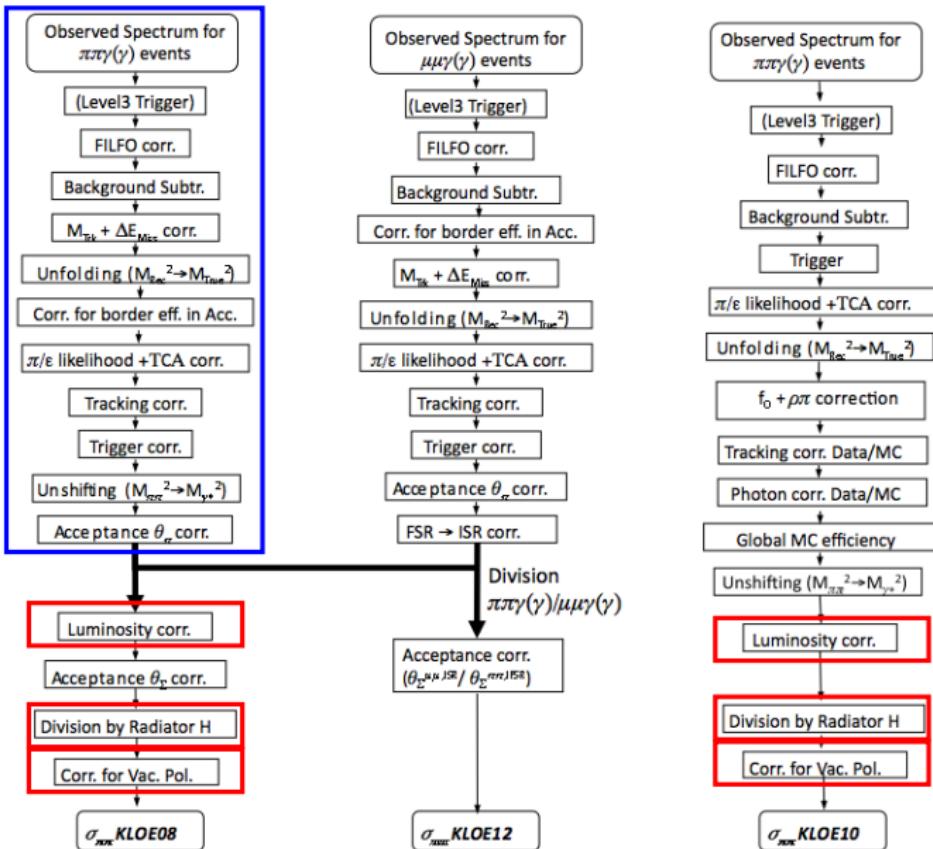
# The analysis flow



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## The elements of the covariance matrices

- Diagonal matrix blocks are composed from the statistical covariance matrices of the individual measurements and the fully bin-per-bin-correlated systematic contributions
- Syst. correlations between KLOE08 and KLOE10 analyses because both analyses share identical radiative corrections (Luminosity, radiator function and vacuum polarization correction)
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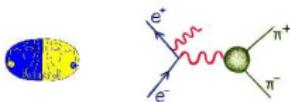
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# The PPG2014 covariance matrices



## KLOE ppg 2014 web page

Combination of **KLOE12**, **KLOE10**, **KLOE08** measurements, see for details S. Mueller, contribution to Mini-Proceedings, 15th meeting of the Working Group on Rad. Corrections and MC Generators for Low Energies, <http://arxiv.org/abs/1406.4639>

- Data files of the bare cross section  $\sigma(e^+e^- \rightarrow \pi^+\pi^-)$  (which includes FSR and excludes VP) are organized in a 195 dim Vector as follows:
  - [KLOE08 \(1:60\)](#)
  - [KLOE10 \(61:135\)](#)
  - [KLOE12 \(136:195\)](#)

Please note that KLOE08 and KLOE10 has been obtained correcting the Vacuum Polarization with Fred Jegerlehner 2003 routine ([VP03](#)). If you want to apply your Vacuum Polarization correction (For example Fred's new one [VP12](#)) you should multiply vector components (1:135) for VP12/VP03.

### • Statistical errors (195x195 matrix):

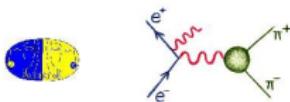
- [lspp\\_covstat\\_KLOE081012.dat](#). Covariance matrix for  $\sigma(e^+e^- \rightarrow \pi^+\pi^-)$ . [\[README\]](#)
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27 Feb 2015 [G.V.](#)

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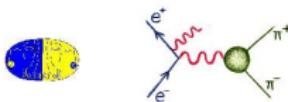
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F. Ignatov (25.5.2016):

- Syst. covariance matrix has negative eigenvalues

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27 Feb 2015 [G.V.](#)

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- Syst. covariance matrix has negative eigenvalues

**Don't use!**

# The PPG2017 covariance matrices (Preliminary!)

During the (re-) evaluation of the covariance matrices, the following updates have been applied to the KLOE data sets:

- The analyses have been updated with respect to the precision of input parameters and fundamental constants
- The data are not rounded to prevent precision loss due to rounding cut-off
- KLOE08 and KLOE10 data have been corrected for vacuum polarization using an updated routine (real and imaginary part)
  - this results in a reduction of the corresponding  $a_{\mu}^{\pi\pi}$ -value by  $0.6 - 0.7 \times 10^{-10}$
- An improved error analysis for the KLOE12 data resulted in a slight decrease of the systematic uncertainty

# The PPG2017 covariance matrices (Preliminary!)

After the updates on the cross section data, the following values for  $a_\mu^{\pi\pi}$  are obtained:

**KLOE08:**  $\Delta a_\mu^{\pi\pi}[0.35 - 0.95 \text{ GeV}^2] = (386.6 \pm 3.3) \times 10^{-10}$

was:  $\Delta a_\mu^{\pi\pi}[0.35 - 0.95 \text{ GeV}^2] = (387.2 \pm 3.4) \times 10^{-10}$

**KLOE10:**  $\Delta a_\mu^{\pi\pi}[0.10 - 0.85 \text{ GeV}^2] = (477.8 \pm 7.0) \times 10^{-10}$

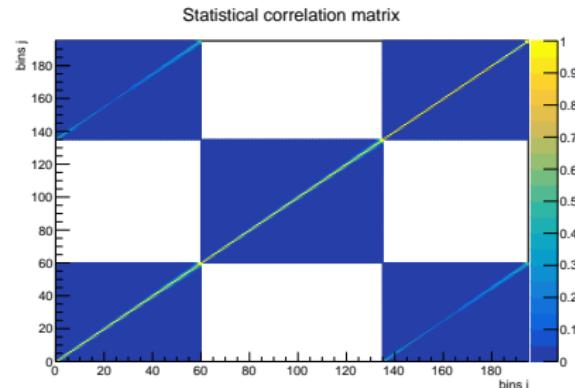
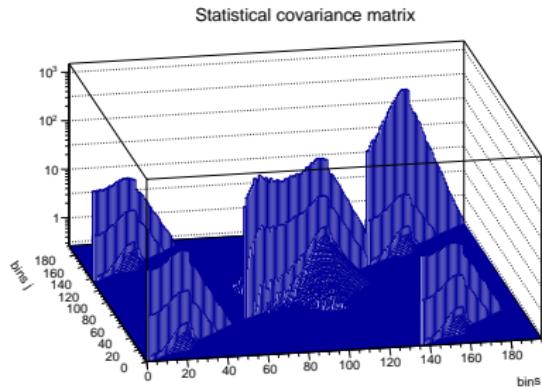
was:  $\Delta a_\mu^{\pi\pi}[0.10 - 0.85 \text{ GeV}^2] = (478.5 \pm 7.0) \times 10^{-10}$

**KLOE12:**  $\Delta a_\mu^{\pi\pi}[0.35 - 0.95 \text{ GeV}^2] = (385.1 \pm 2.6) \times 10^{-10}$

was:  $\Delta a_\mu^{\pi\pi}[0.35 - 0.95 \text{ GeV}^2] = (385.1 \pm 2.9) \times 10^{-10}$

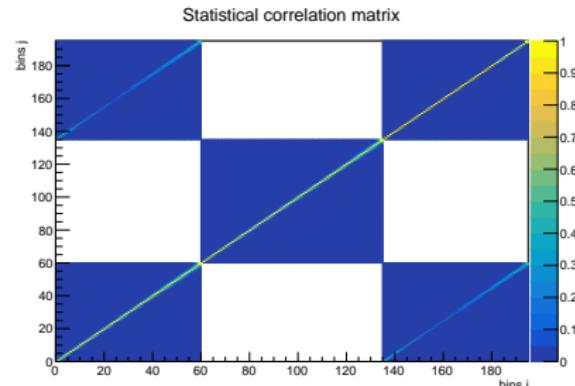
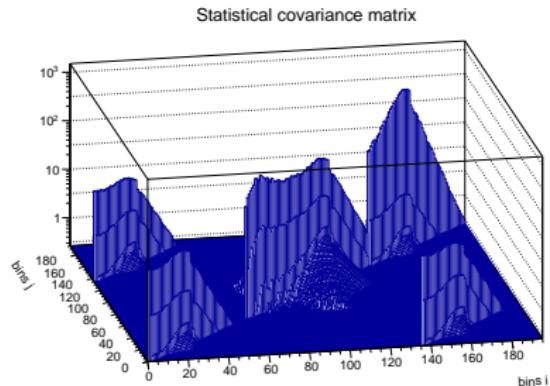
# The PPG2017 covariance matrices (Preliminary!)

Statistical covariance and correlation matrix:

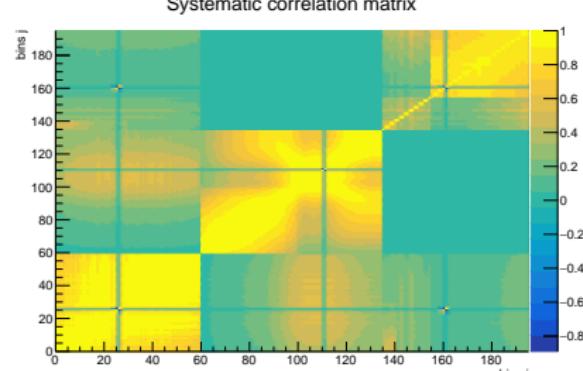
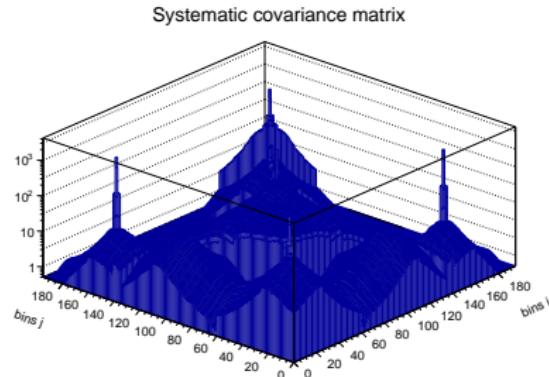


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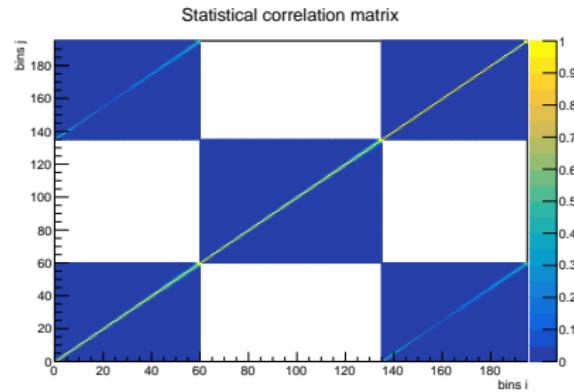
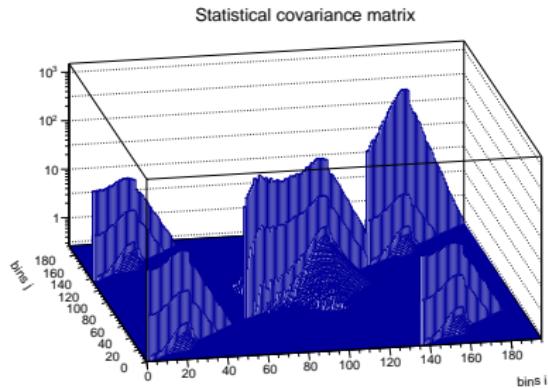


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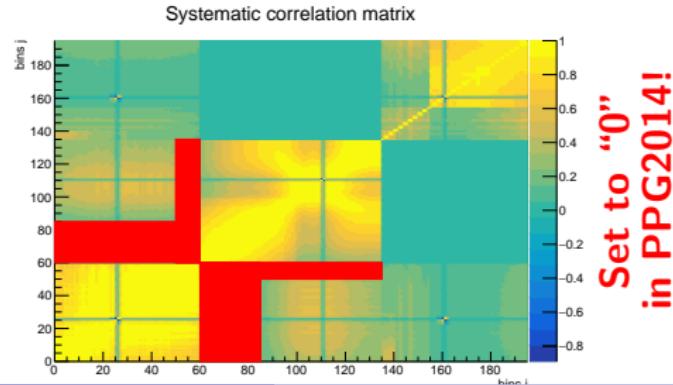
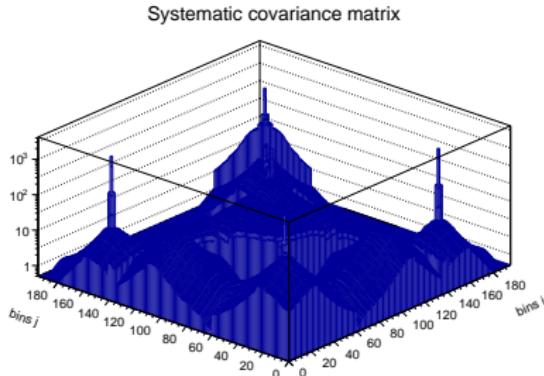


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Statistical covariance and correlation matrix:



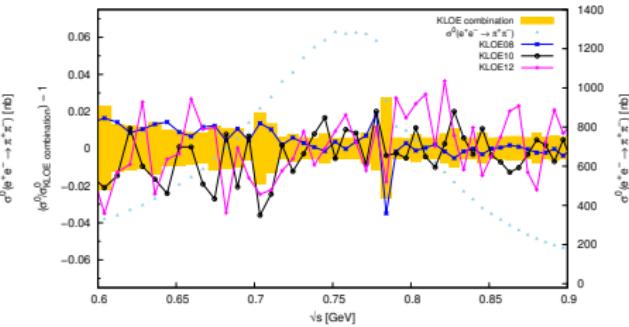
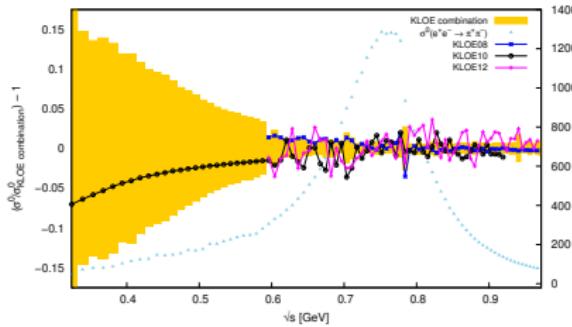
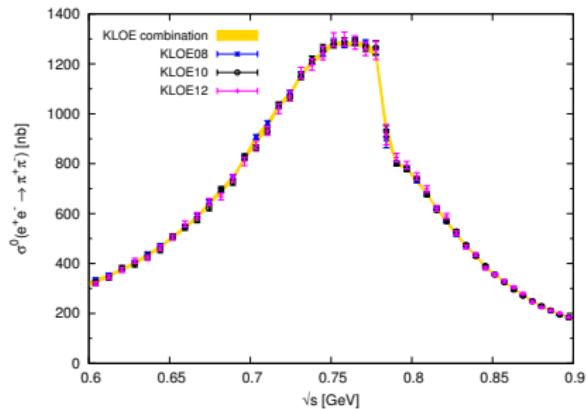
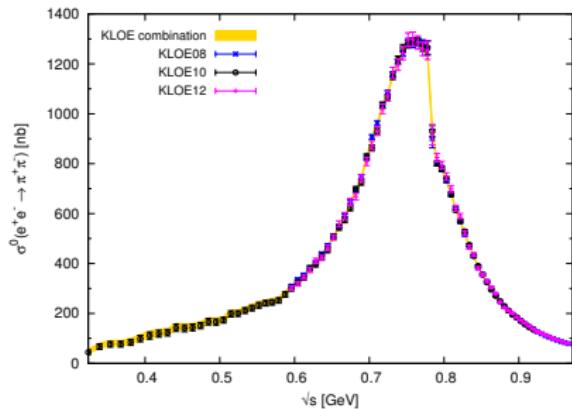
Systematic covariance and correlation matrix:



Set to "0"  
in PPG2014!

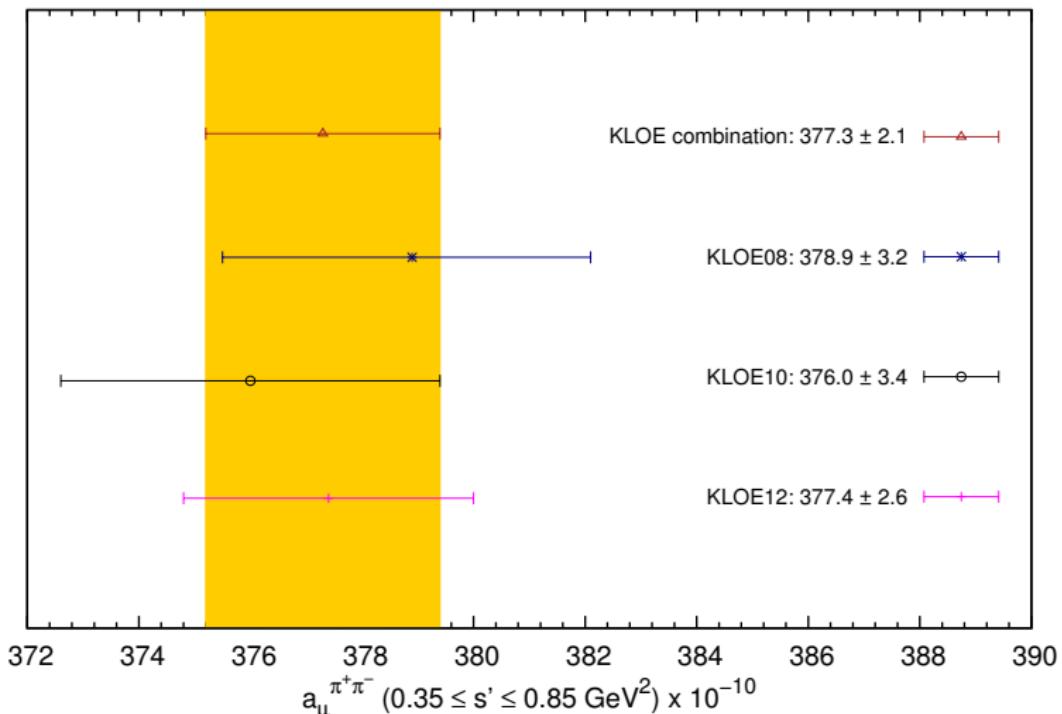
# Preliminary combination of KLOE data sets

Using the obtained covariance matrices, the KLOE data are combined using an bias-free iterative linear  $\chi^2$  minimisation (Talk by A. Keshavarzi)



# Preliminary combination of KLOE data sets

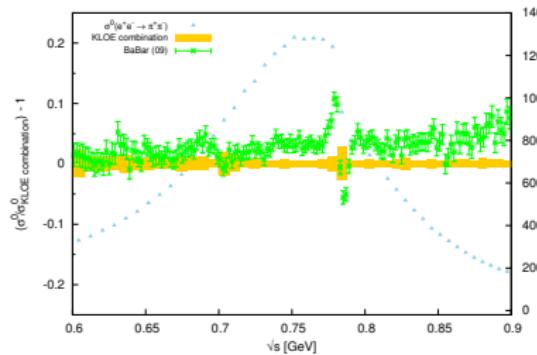
Estimates of  $\Delta a_{\mu}^{\pi\pi}$  in the range  $0.35 \leq s' \leq 0.85 \text{ GeV}^2$  for the different KLOE analyses and the prel. combination:



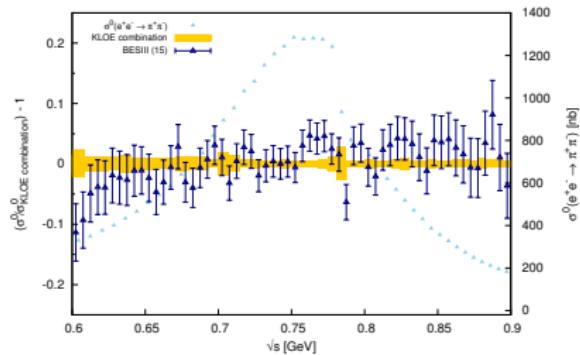
# Preliminary combination of KLOE data sets

Comparison with data from other experiments:

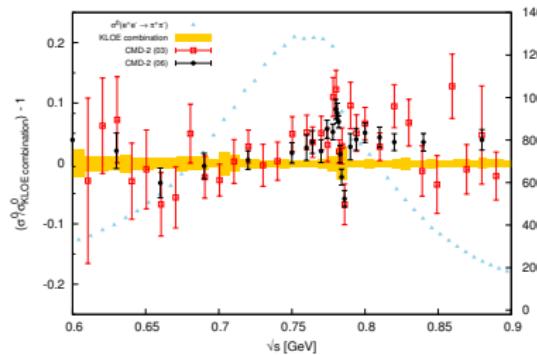
Comp. with BaBar



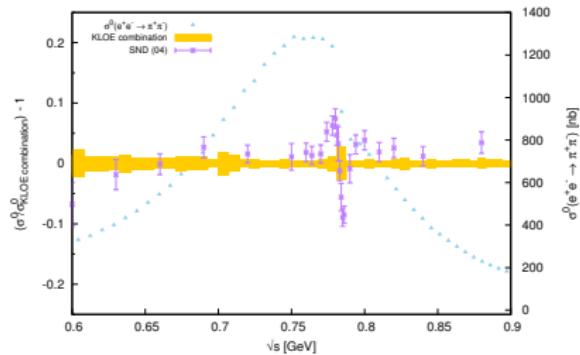
Comp. with BESIII



Comp. with CMD

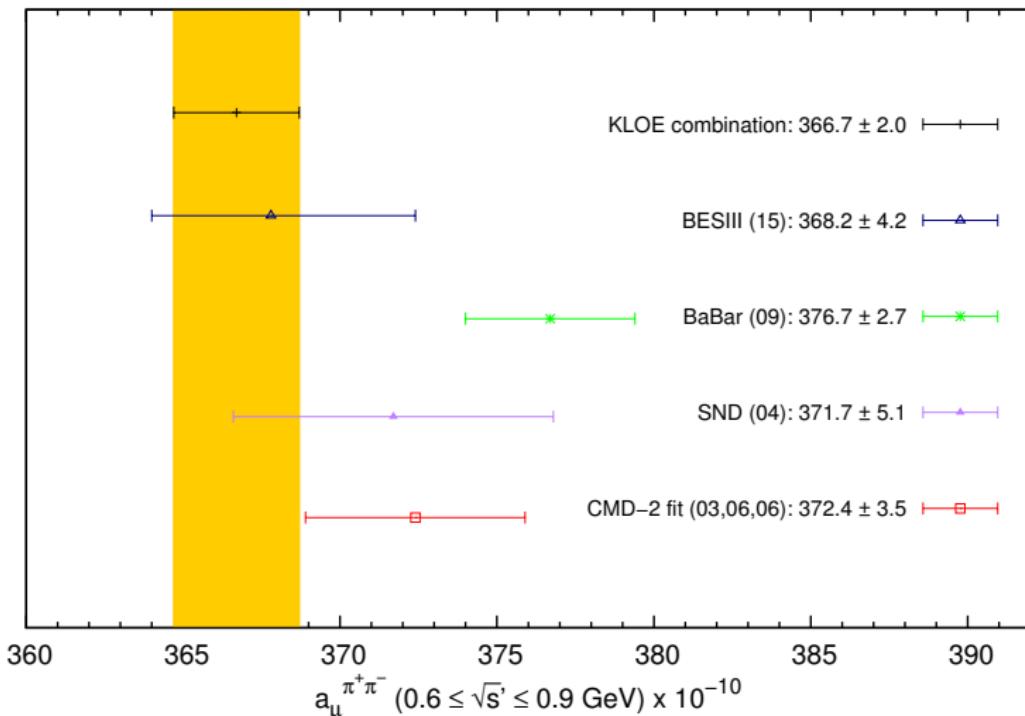


Comp. with SND



# Preliminary combination of KLOE data sets

Estimates of  $\Delta a_\mu^{\pi\pi}$  in the range  $0.6 \leq \sqrt{s'} \leq 0.9$  GeV for different experiments:



## Summary and Conclusion

- We have re-evaluated the  $195 \times 195$  statistic and systematic covariance matrices for the three KLOE ISR analyses KLOE08, KLOE10 and KLOE12
- Using these covariance matrices, a preliminary combined estimate in the range between 0.1 and 0.95  $\text{GeV}^2$  has been constructed
- Results are currently evaluated by the KLOE-2 collaboration, after final blessing will be put on the KLOE ppg-webpage:  
<http://www.lngs.infn.it/kloe/ppg/>
- This work has been started and greatly profited from discussions within the framework of the Radio MonteCarLOW group  
<https://www.lngs.infn.it/wg/sihad/>

## SPARE SLIDES

## Zoom around the $\rho - \omega$ region:

