

UBER-GRAVITY AND H₀ PROBLEM

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25 September 2017 — DarkMod — Saclay

A sunset over the ocean with a small boat on the horizon. The sky is filled with soft, colorful clouds in shades of orange, yellow, and blue. The water is calm and reflects the light from the sky.

GR, Lambda and CDM

? H_0 tension

? σ_8 tension

? void phenomenon

? missing satellite problem

GR, Lambda and CDM

? the cosmological constant problem

? why GR should govern gravity force

ENSEMBLE AVERAGE THEORY OF GRAVITY

➤ A. Einstein:

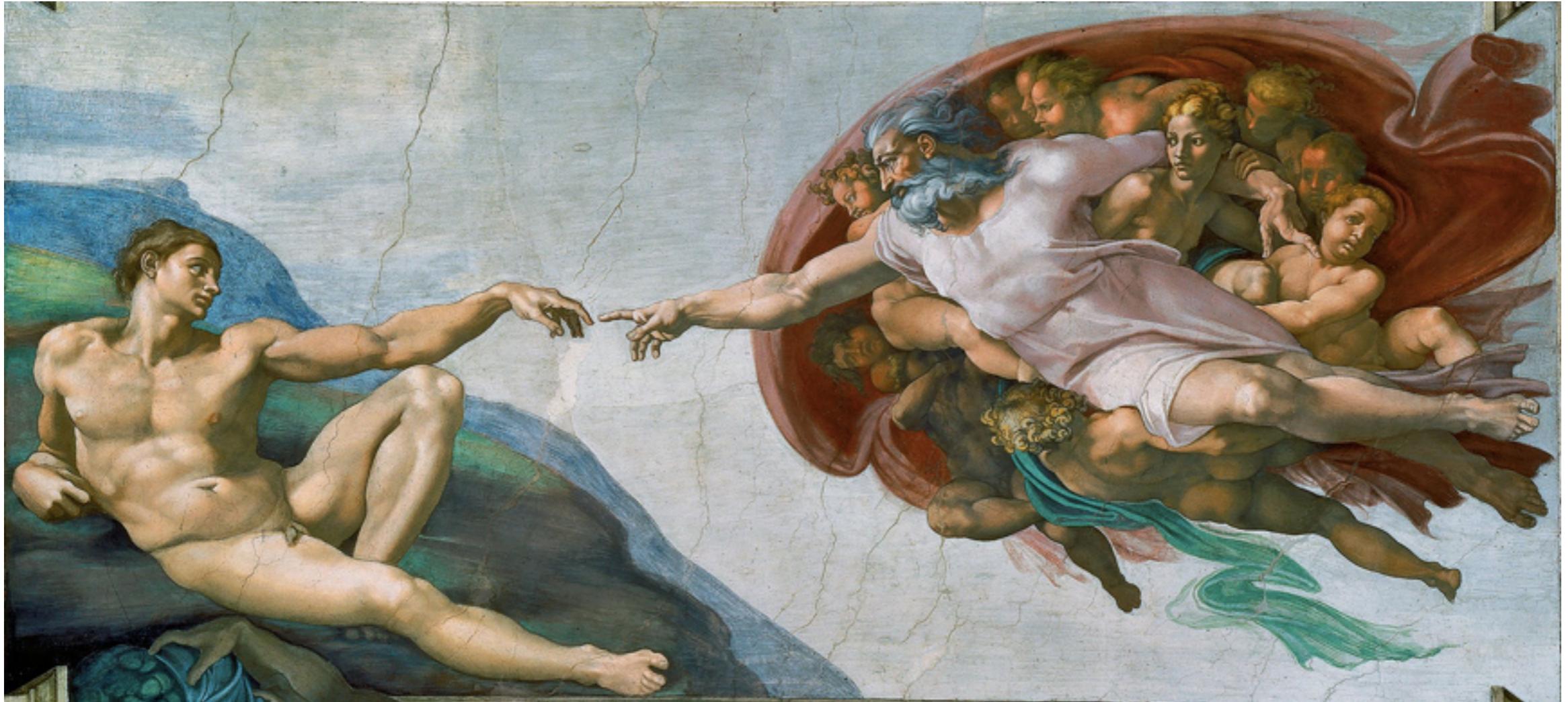
“What really interests me is whether God had any choice in the creation of the World”

A REAL STORY:



— THE FIRST DAY: IT WAS ASKED FOR A THEORY!

the creation of Adam, Michelangelo:



A. Einstein:

“What really interests me is whether God had any choice in the creation of the World”

— THEN, MANY THEORIES WERE PROPOSED BY THINKERS!

the school of Athens, Raphael:



Tessa Baker

Lovelock's theorem

Einstein-Dilaton-Gauss-Bonnet
Cascading gravity
Strings & Branes
Randall-Sundrum I & II
DGP

$$f\left(\frac{R}{\square}\right) \quad R_{\mu\nu} \square^{-1} R^{\mu\nu}$$

Lorentz violation
Hořava-Lifschitz
Conformal gravity

Higher-order

$$f(G) \quad f(R) \quad \text{General } R_{\mu\nu}R^{\mu\nu}, \square R, \text{etc.}$$

Higher dimensions

Non-local

Some degravitation scenarios

Kaluza-Klein

Generalisations of SEH

Gauss-Bonnet
Lovelock gravity

Non-action Approaches

CDT
Entanglement entropy

TeVS — Add new field content

Scalar-tensor & Brans-Dicke
Ghost condensates
Galileons
the Fab Four

KGB
Coupled Quintessence
Horndeski theories

Scalar

Chern-Simons
Cuscuton
Chaplygin gases

$f(T)$
Einstein-Cartan-Sciama-Kibble

Torsion theories

Vector

Einstein-Aether
Lorentz violation

Massive gravity

Bigravity

Tensor

EBI

Bimetric MOND

— EUREKA: THE ANSWER IS “AVERAGING”!

death of Socrates, David:



ENSEMBLE AVERAGE THEORY OF GRAVITY

➤ let's recall Einstein quote:

“What really interests me is whether God had any choice in the creation of the World”

➤ what is your answer to his question?

● no!  why not? why GR is unique?

● yes!  how can we check this “yes”?

● it is not a well-defined question!  see you at break!

ENSEMBLE AVERAGE THEORY OF GRAVITY

- what is my answer to his question?
 - my answer to this question is “yes” and “no” both!
 - “yes”: all the theoretically consistent models have been used in the creation of the World!
 - “no”: at the end there is just a “unique model” which is the “ensemble average” of all the theoretically possible models!
- based on PRD 94 (2016) 124035, arXiv:1606.01887
- for a very similar idea see also: N. Arkani-Hamed et al., PRL 117 (2016) 251801, arXiv:1607.06821

ENSEMBLE AVERAGE THEORY OF GRAVITY

\mathcal{M}

the space of all the (consistent) models for gravity!

- ▶ we take average over all the models
- ▶ to do this we need to assigned to each model a probability

$$\mathcal{M} = \sum_i p_i \mathcal{M}_i = \frac{1}{\sum_j e^{-S_j}} \times \sum_i e^{-S_i} \mathcal{M}_i$$

ENSEMBLE AVERAGE THEORY OF GRAVITY

- practically I will assign to each model a Lagrangian
- the averaged Lagrangian will be like

$$\mathcal{L} = \sqrt{-g} \left(\sum_{i=1}^N L_i e^{-\beta L_i} \right) / \left(\sum_{j=1}^N e^{-\beta L_j} \right)$$

The diagram shows four labels with arrows pointing to specific parts of the equation above:

- averaged Lagrangian**: points to the symbol \mathcal{L} .
- i'th Lagrangian**: points to the term L_i in the numerator's sum.
- its weight**: points to the exponential term $e^{-\beta L_i}$ in the numerator's sum.
- normalization factor**: points to the denominator's sum $\sum_{j=1}^N e^{-\beta L_j}$.

ENSEMBLE AVERAGE THEORY OF GRAVITY

- an example: higher order gravity
- in 4-dimension we have Ricci scalar and Gauss-Bonnet term

$$\mathcal{L} = \sqrt{-g} \left[\frac{M^2 R e^{-\beta M^2 R}}{e^{-\beta M^2 R} + e^{-\beta \alpha G}} + \frac{\alpha G e^{-\beta \alpha G}}{e^{-\beta M^2 R} + e^{-\beta \alpha G}} \right]$$

Ricci scalar

Gauss-Bonnet term

temperature of model space??

UBER-GRAVITY

- based on “Uber-Gravity and the CPP”, arXiv:1703.02052
- a generalization of EAT-of-Gravity for all analytical functions of $f(R)$. so we have

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UBER-GRAVITY

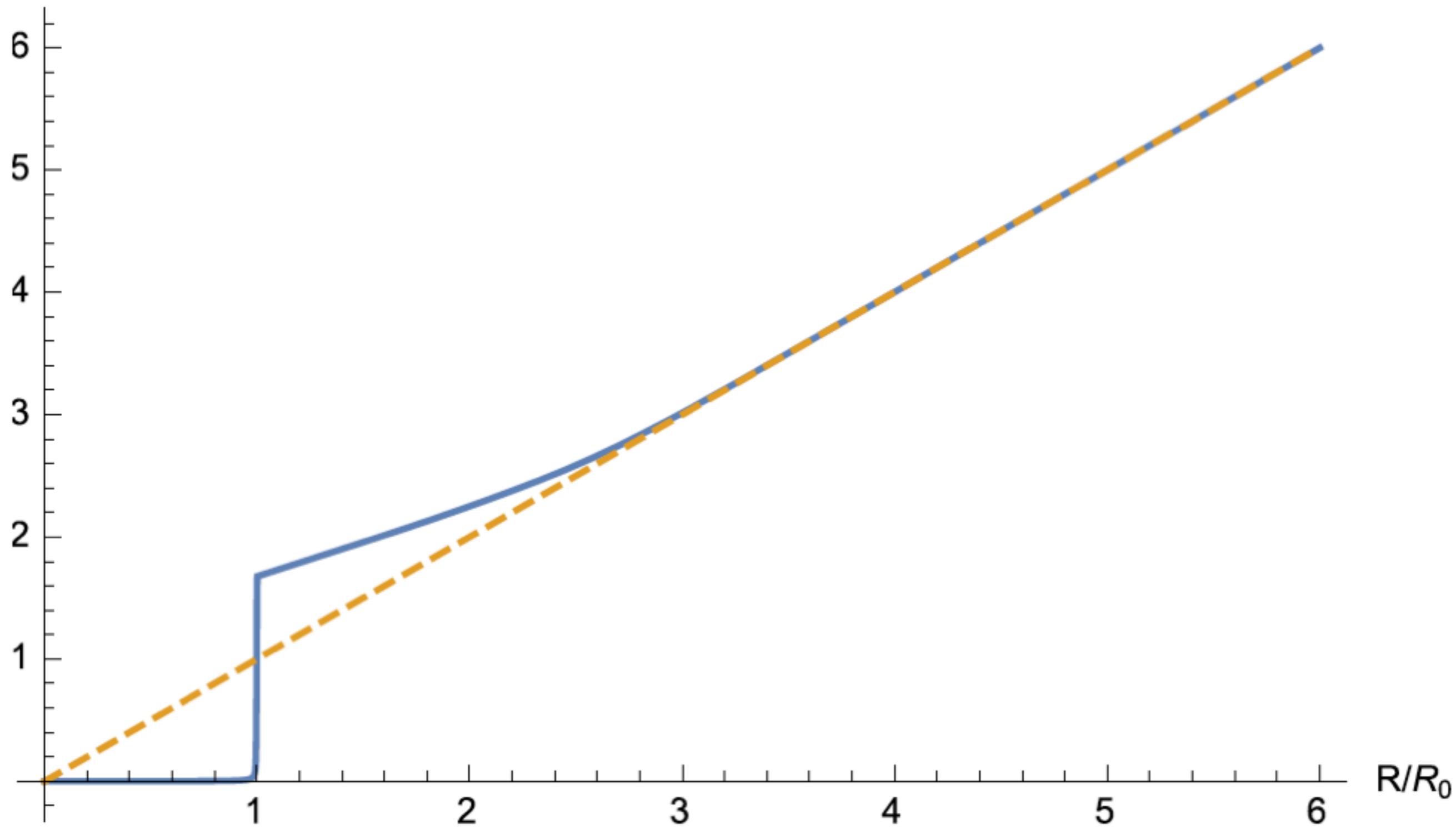
- ▶ based on “Uber-Gravity and the CPP”, arXiv:1703.02052
- ▶ a generalization of EAT-of-Gravity for all analytical functions of $f(R)$. so we have

$$\mathbb{M} = \{R^n \mid \forall n \in \mathbb{N}\}$$

$$\mathcal{L} = \left(\sum_{n=1}^{\infty} \bar{R}^n e^{-\beta \bar{R}^n} \right) / \left(\sum_{n=1}^{\infty} e^{-\beta \bar{R}^n} \right)$$

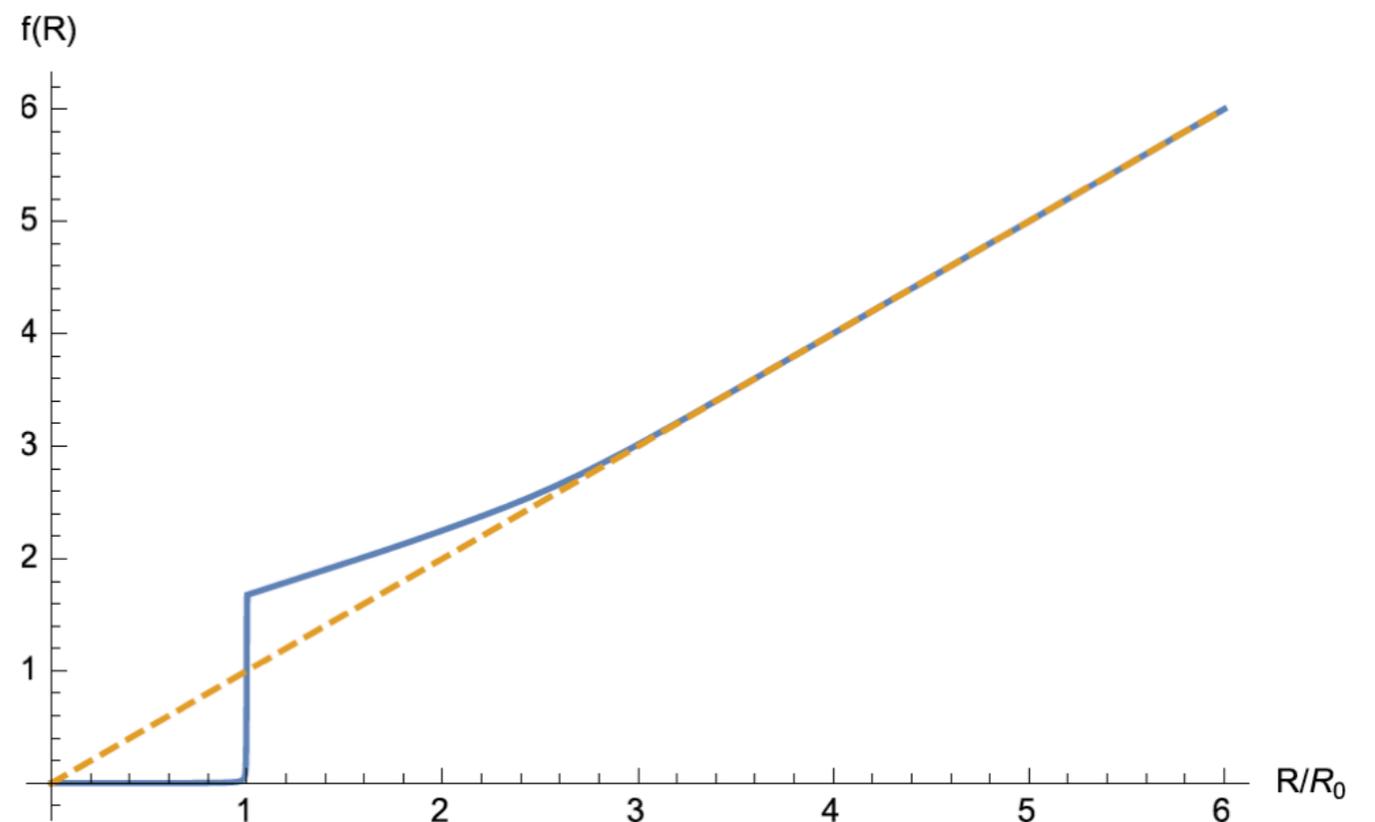
UBER-GRAVITY

$f(R)$



UBER-GRAVITY: UNIVERSAL PROPERTIES

- for high-curvature regime it reduces to GR
- for intermediate-curvature regime it predicts stronger gravity than GR
- it is vanishing for low-curvature regime ($R < R_0$)
- there is a sharp transition at R_0



UBER-GRAVITY: A SIMPLIFIED MODEL

$$f(R) = \begin{cases} \bar{R}^n & R \leq R_0 \\ \bar{R} + e^{-(\bar{R}-0.7)} & R_0 < R \end{cases}$$

we focus on low-curvature regime. we have

$$(n - 2)\bar{R}^n + 3n R_0^{-1} \square \bar{R}^{n-1} = \kappa^2 T$$

and for $R = \text{const.}$ we have

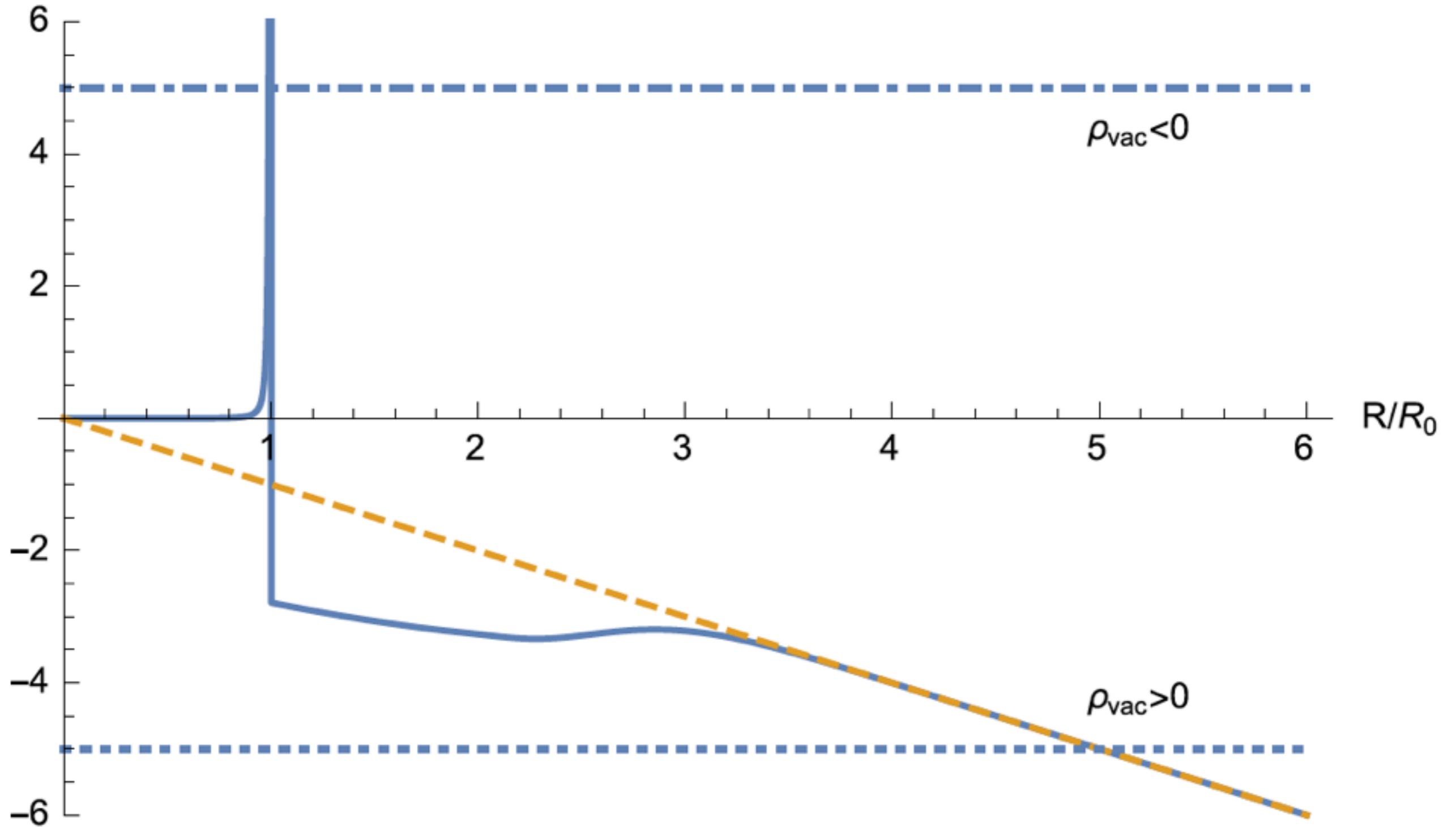
$$\frac{R}{R_0} = \left(\frac{\kappa^2 T}{n - 2} \right)^{\frac{1}{n}}$$

which means for $n \rightarrow \infty$ results in $R \rightarrow R_0$!!

this means there is no need to fine-tuning since this model is not sensitive to vacuum energy.

UBER-GRAVITY: FULL MODEL

trace





? H_0 tension

? void phenomenon

? σ_8 tension

? missing satellite problem

Uber-Gravity

LAMBDA XOR CDM MODEL:

note: this part has been done in collaboration with

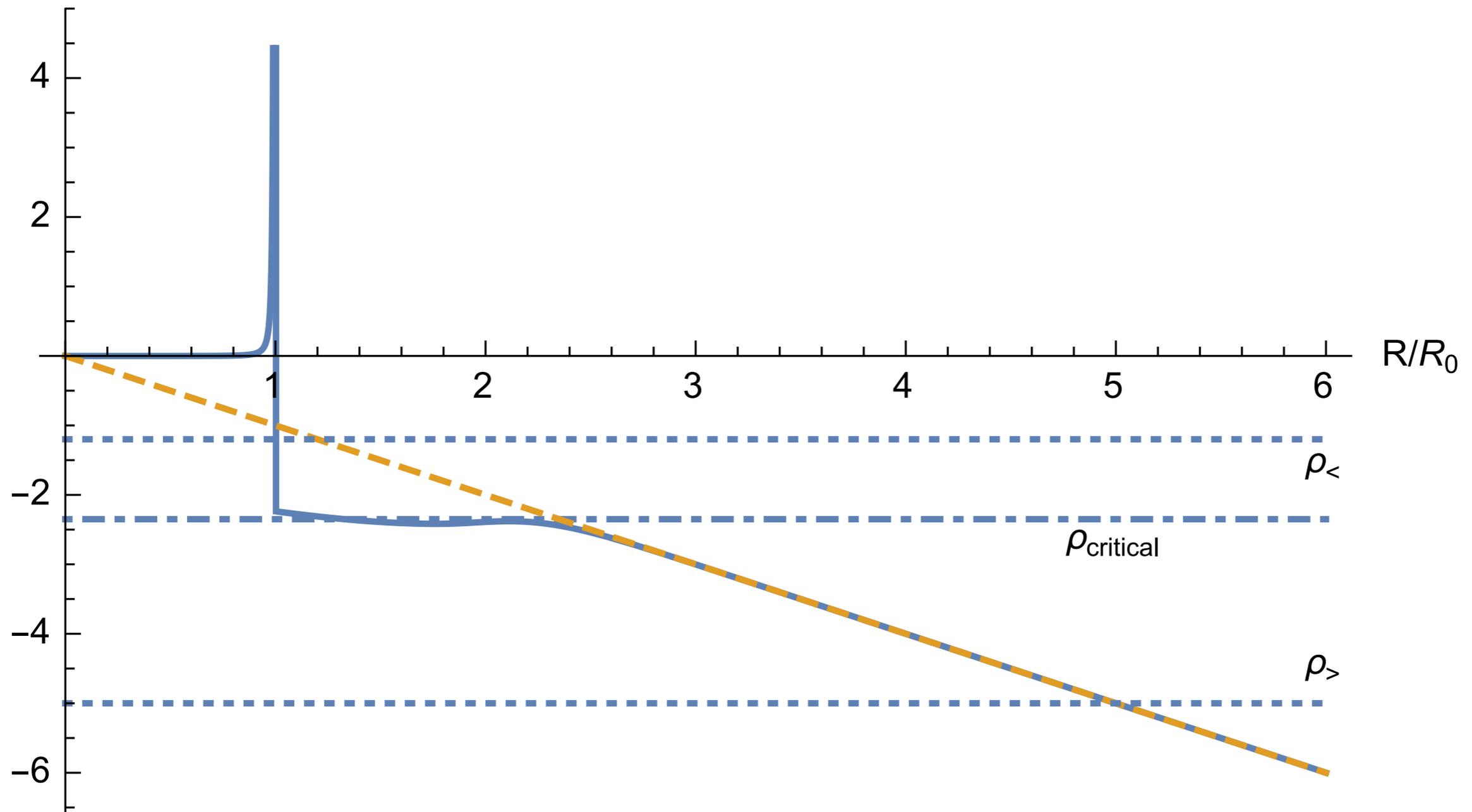
Shant Baghram

Sharif University of Technology, Tehran, Iran



UBER-GRAVITY: FULL MODEL

trace



LAMBDA XOR CDM MODEL:

- based on uber-gravity model we suggest the following cosmological model:

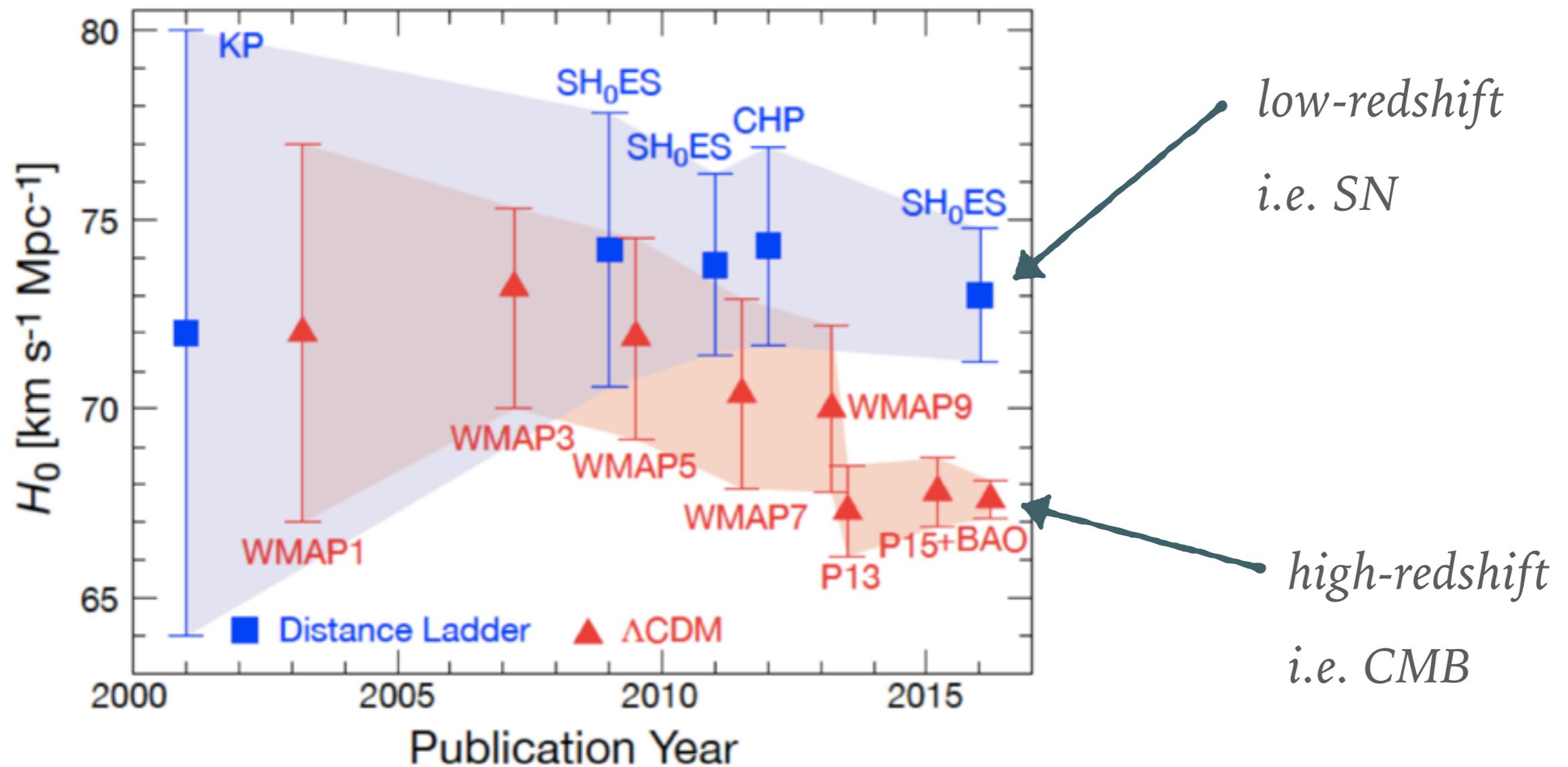
$$\text{Gravity} = \begin{cases} \text{de Sitter} & \rho < \rho_{critical} \\ \text{GR} + \text{CDM} & \rho > \rho_{critical} \end{cases}$$

which is dubbed as “either Lambda or CDM”:

$\Lambda \oplus \text{CDM}$ MODEL

LAMBDA XOR CDM MODEL: BACKGROUND

The Hubble Constant



LAMBDA XOR CDM MODEL: BACKGROUND

A 2.4% Determination of the Local Value of the Hubble Constant

Adam G. Riess (Johns Hopkins U. & Baltimore, Space Telescope Sci.) *et al.*, Apr 5, 2016. 31 pp.

Published in *Astrophys.J.* 826 (2016) no.1, 56

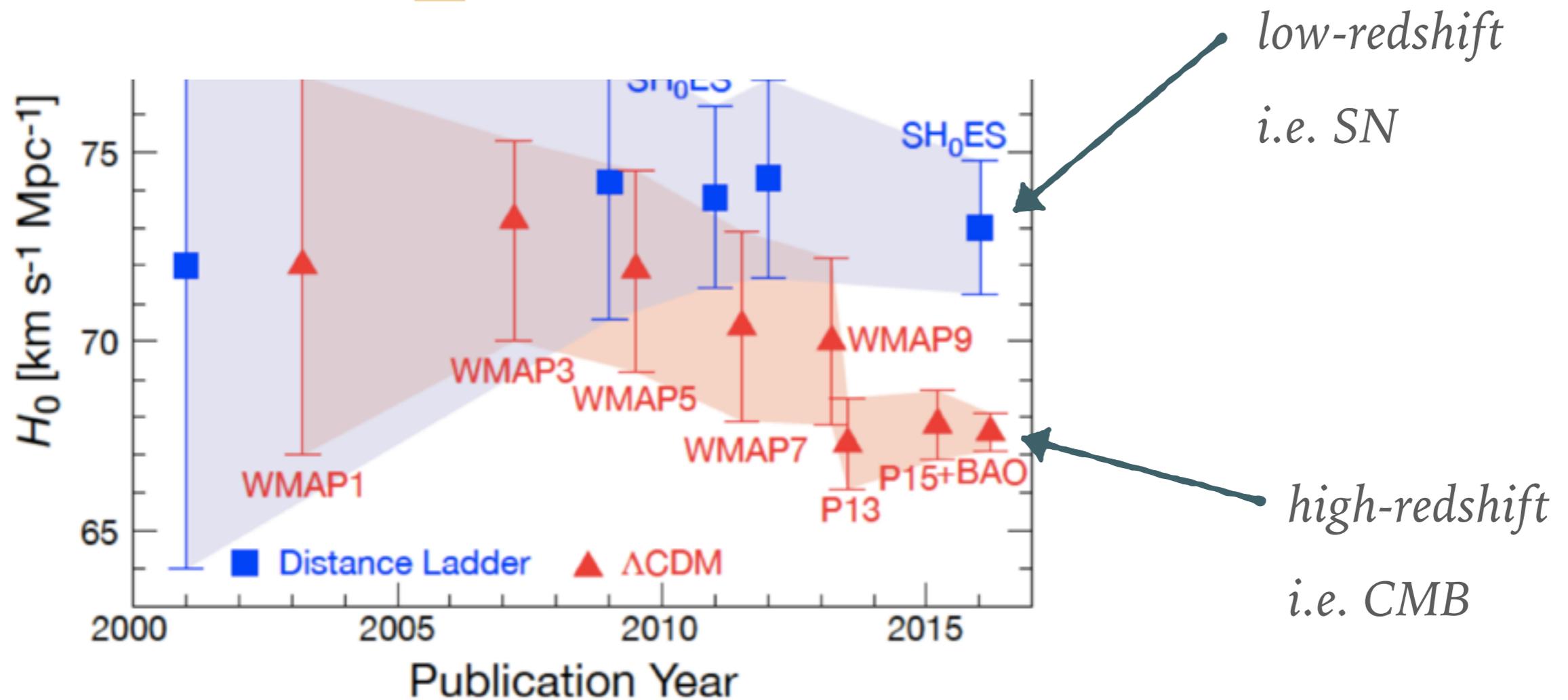
DOI: [10.3847/0004-637X/826/1/56](https://doi.org/10.3847/0004-637X/826/1/56)

e-Print: [arXiv:1604.01424](https://arxiv.org/abs/1604.01424) [astro-ph.CO] | [PDF](#)

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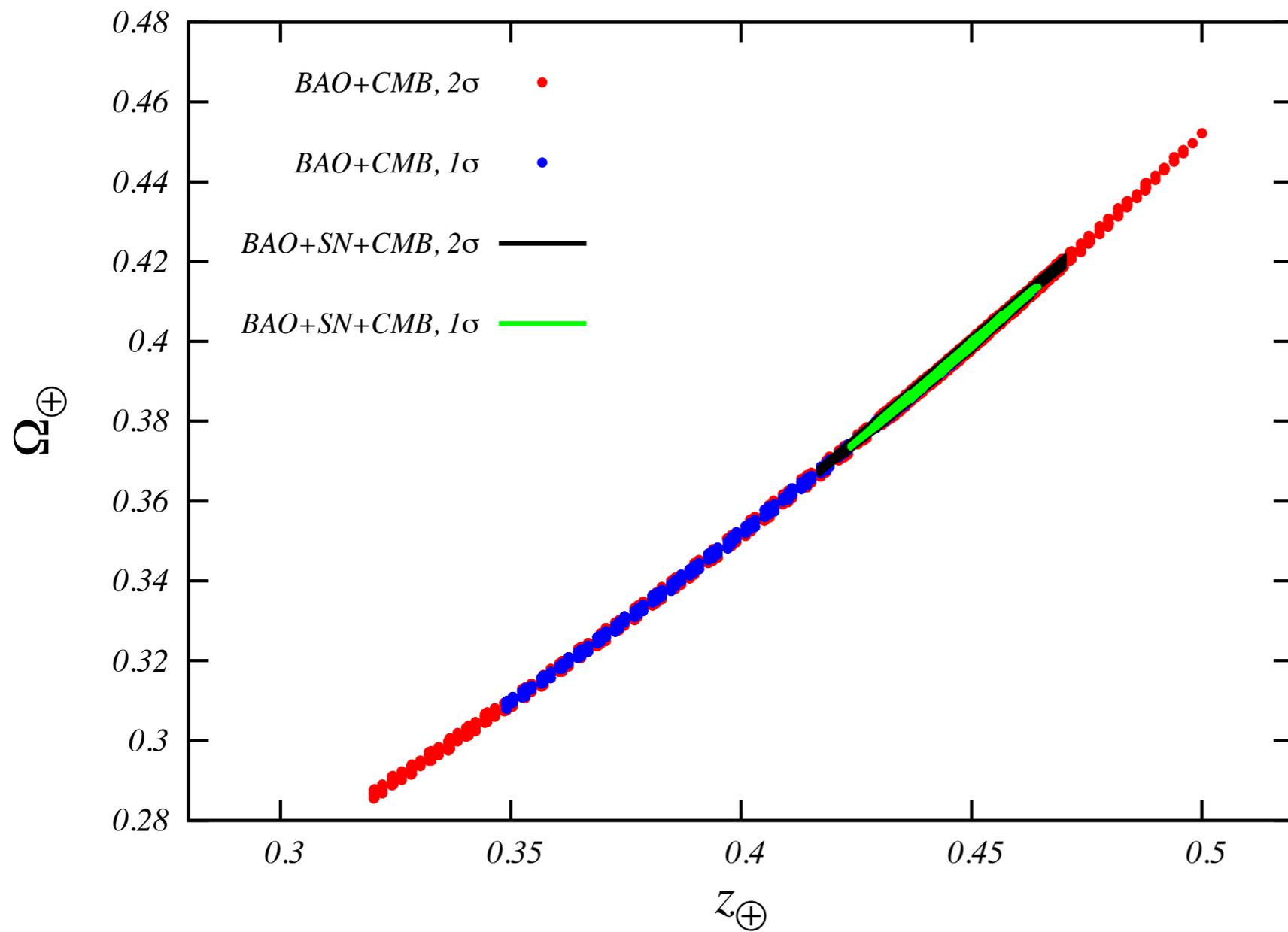
LAMBDA XOR CDM MODEL: BACKGROUND

$$E^2(z) \equiv \left(\frac{H(z)}{H_0^{low}} \right)^2 = \begin{cases} 1 & z < z_{\oplus} \\ \Omega_{m,\oplus} \left(\frac{1+z}{1+z_{\oplus}} \right)^3 & z > z_{\oplus} \end{cases}$$

$$\chi(z) = \frac{c}{H_0^{low}} \left[\int_0^{z_{\oplus}} dz + \int_{z_{\oplus}}^z \frac{dz}{\left(\Omega_{m,\oplus} \left(\frac{1+z}{1+z_{\oplus}} \right)^3 \right)^{1/2}} \right]$$

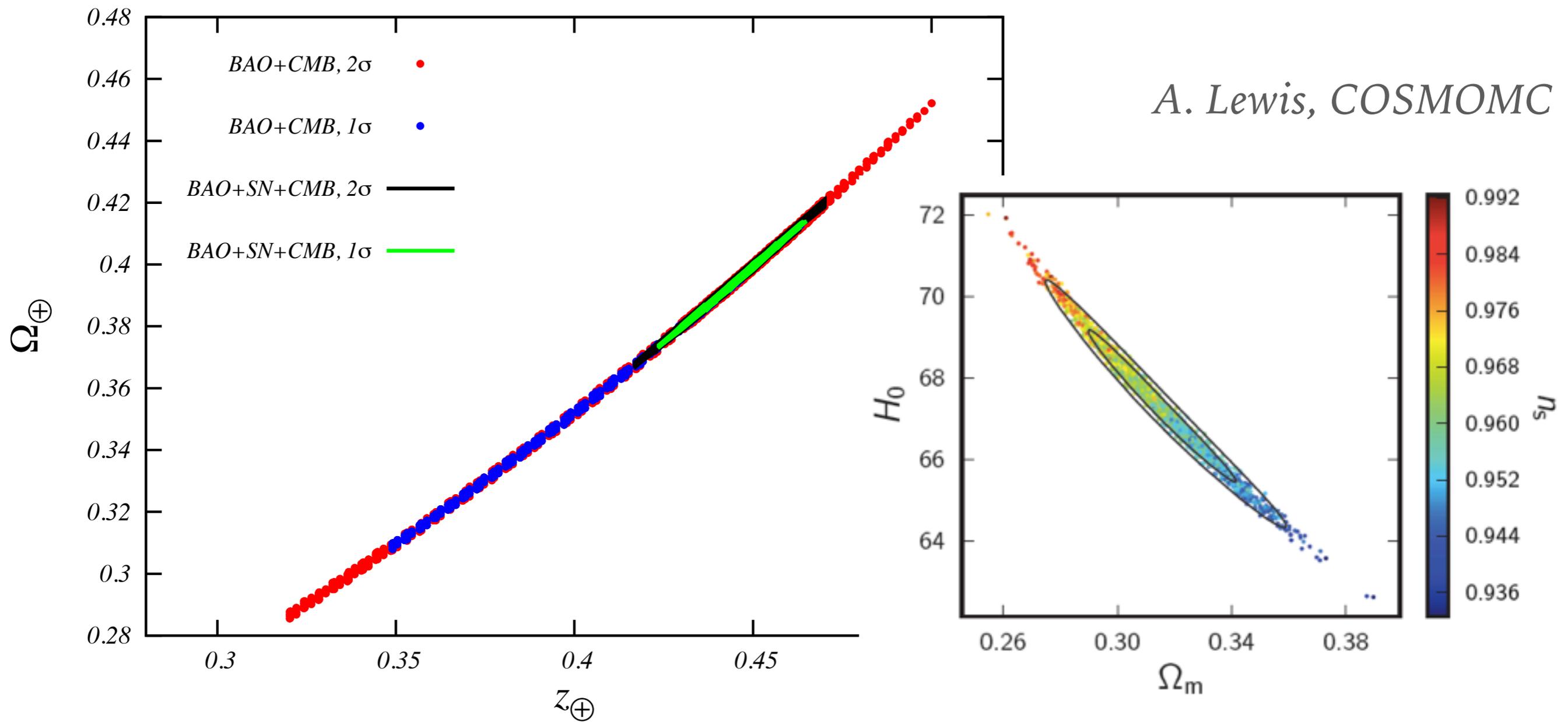
LAMBDA XOR CDM MODEL: BACKGROUND

by fitting LxorCDM with background data including SN, BAO and 1st CMB peak



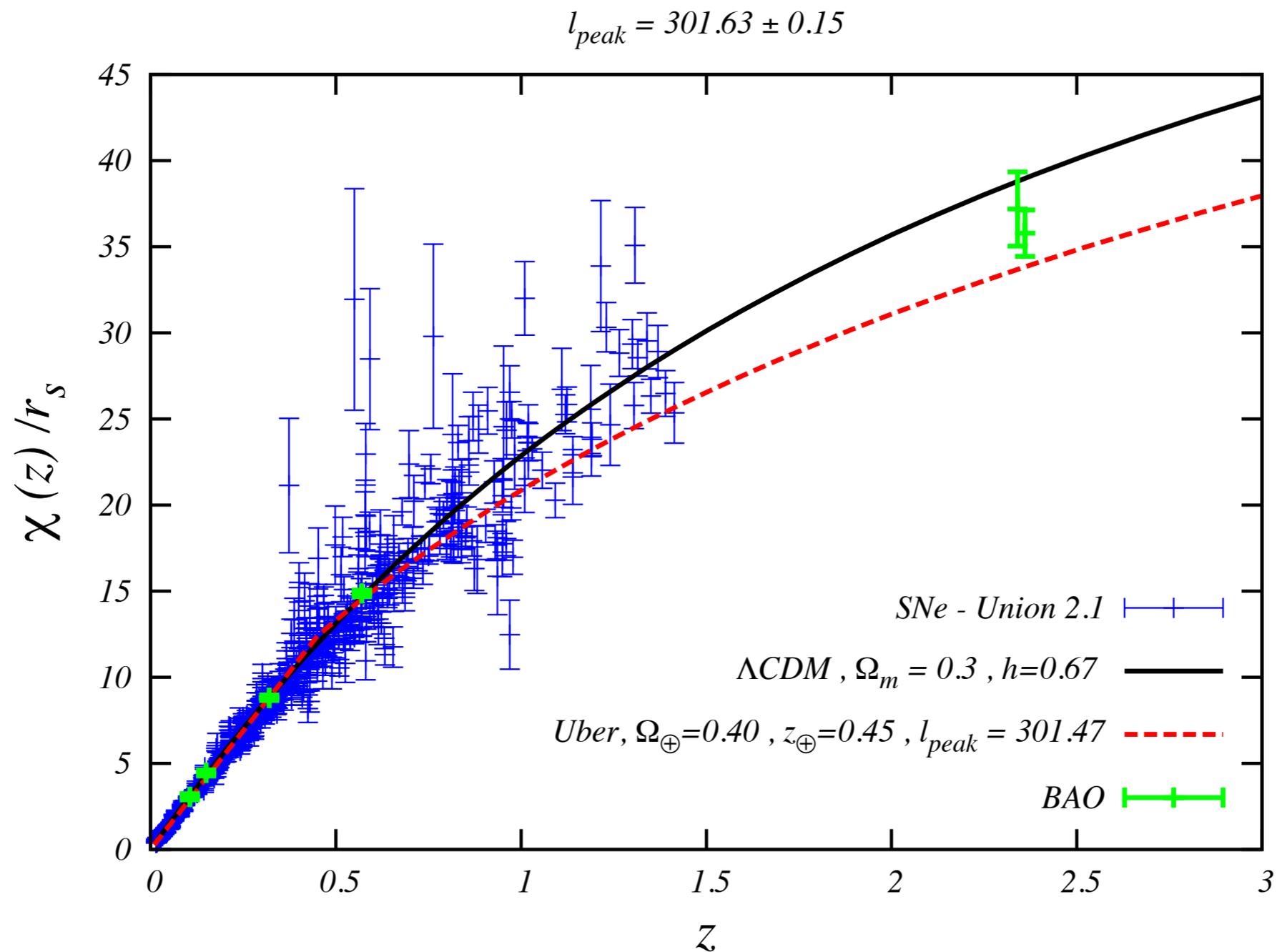
LAMBDA XOR CDM MODEL: BACKGROUND

by fitting *LxorCDM* with background data including SN, BAO and 1st CMB peak



LAMBDA XOR CDM MODEL: BACKGROUND

by fitting $L_{xor}CDM$ with background data including SN, BAO and 1st CMB peak



LAMBDA XOR CDM MODEL: BACKGROUND

- flat LxorCDM has 3 free parameters Ω_m , H_0 and $z_{\text{transition}}$ which are related to R_0 and β in original uber-gravity model!
- we fixed $H_0 = 73$ km/sec/Mpc reported by Riess et al.
- we minimize χ^2 for z_t and Ω_m
- χ^2 is comparable with number of data points!

- LxorCDM automatically solves H_0 problem which was not obvious at the first look!

✓ H_0 tension

? void phenomenon

? σ_8 tension

? missing satellite problem

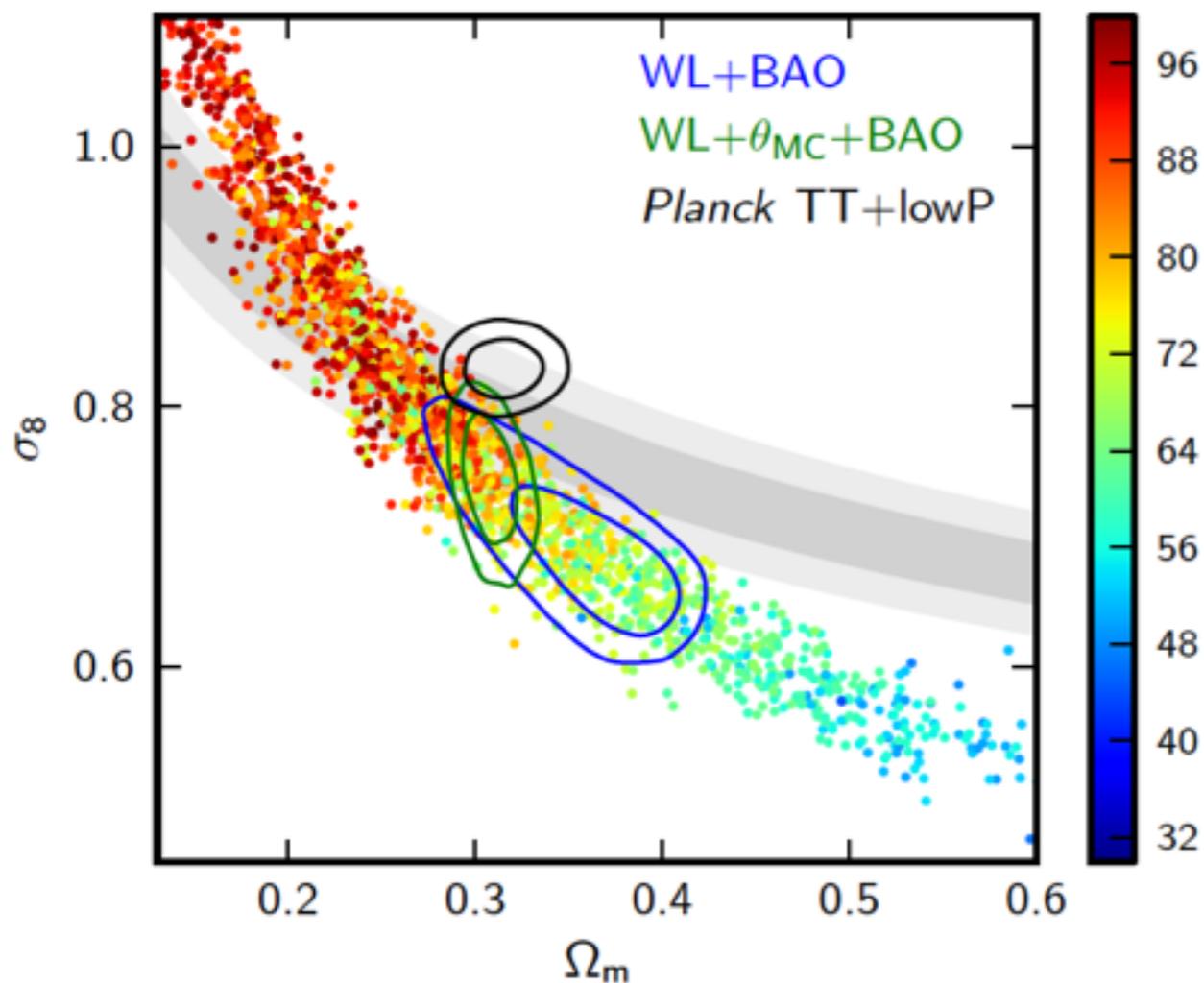
Lambda xor CDM (*background* analysis)

(Uber-Gravity)

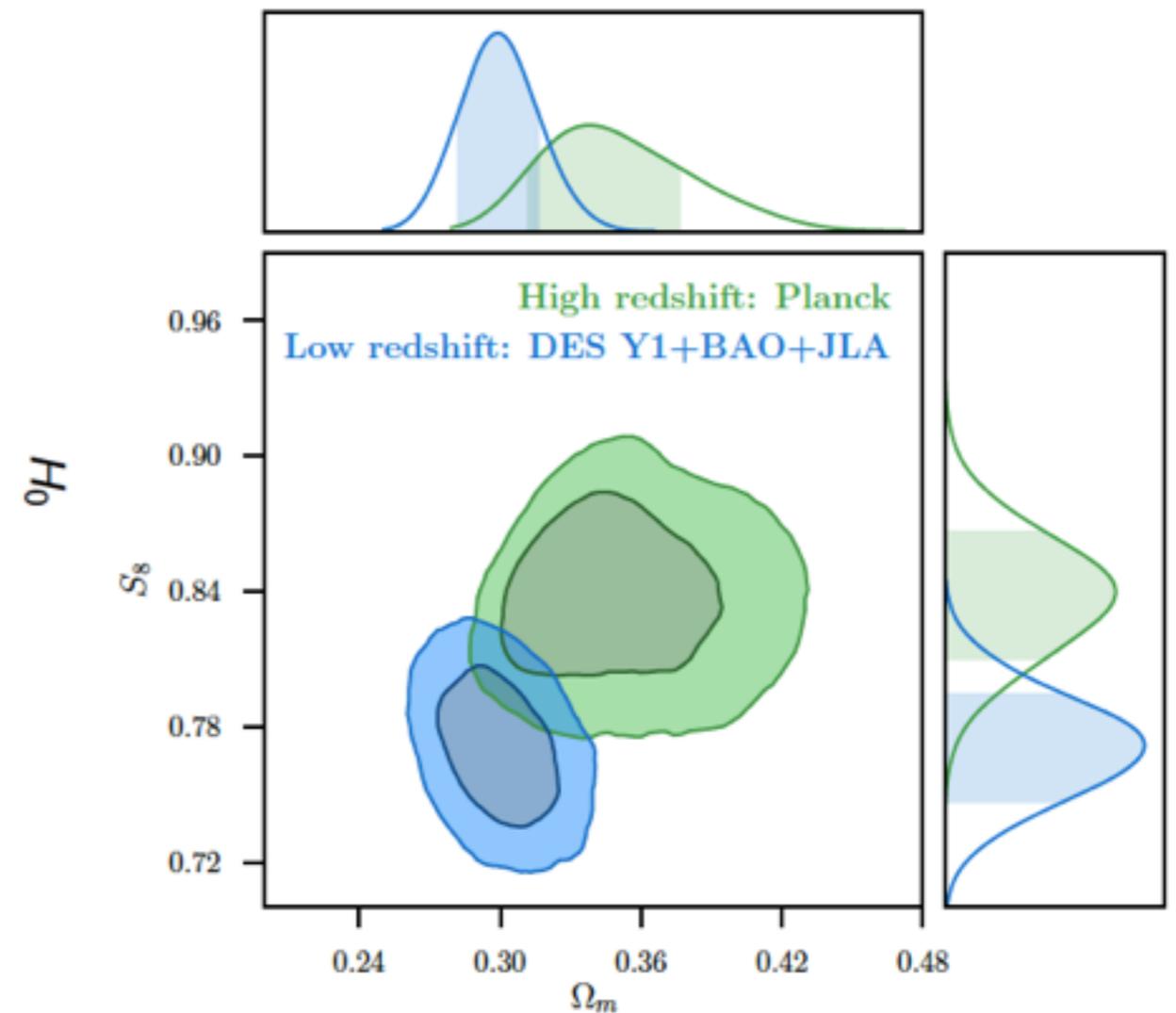
LAMBDA XOR CDM MODEL: LINEAR PERTURBATIONS

► σ_8 problem:

“Cosmic map reveals a not-so-lumpy Universe”, Nature on DES!



Planck 2015



DES 2017

LAMBDA XOR CDM MODEL: LINEAR PERTURBATIONS

in perturbation theory we need to find the redshift where the “total density” touches the critical density:

$$\bar{\rho}(z) \left[1 + \delta(k, z) \right] = \rho_{critical}$$

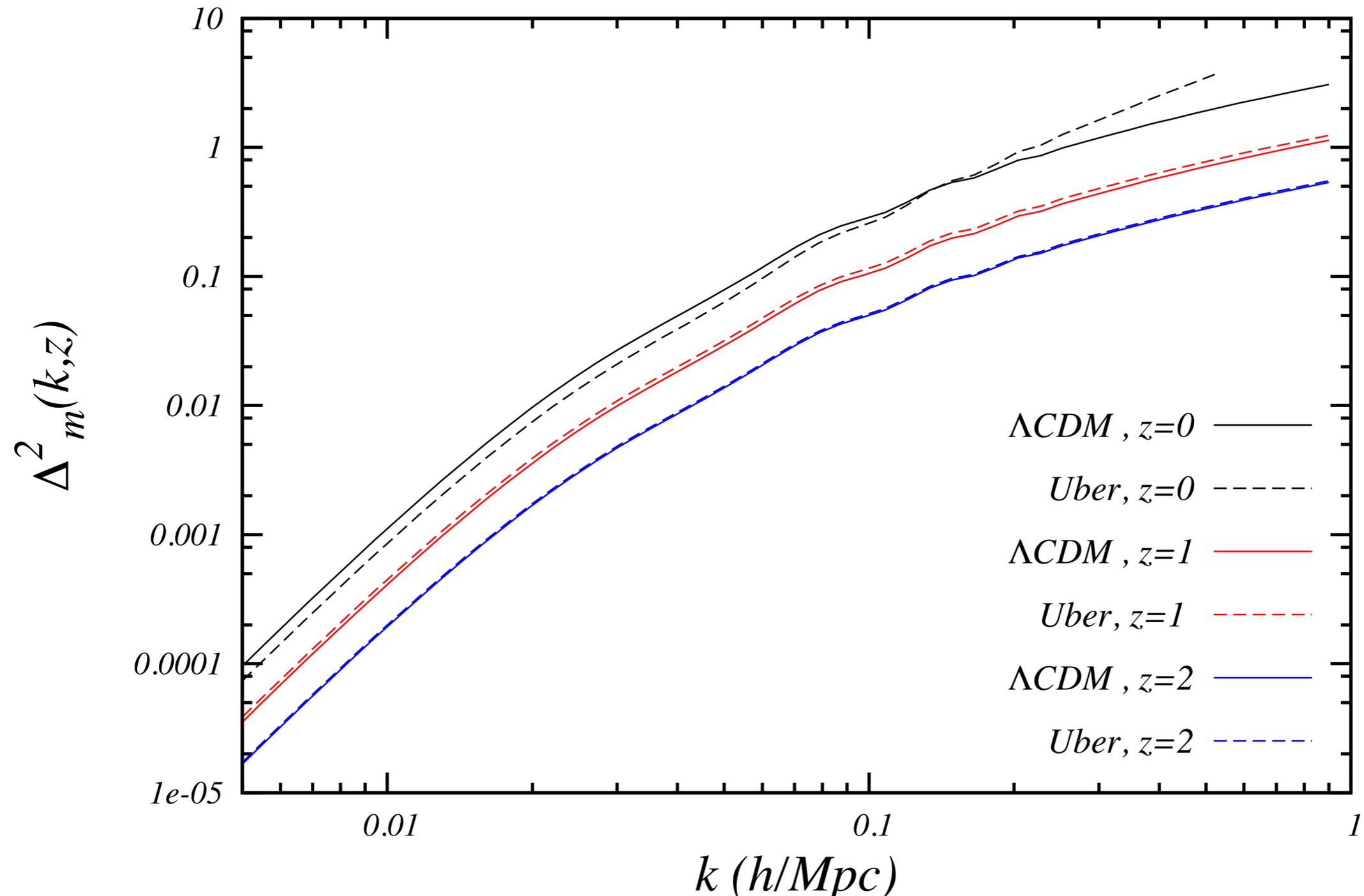
which is equivalent to:

$$X^3 + A(k) X^2 = X_{\oplus}^3$$

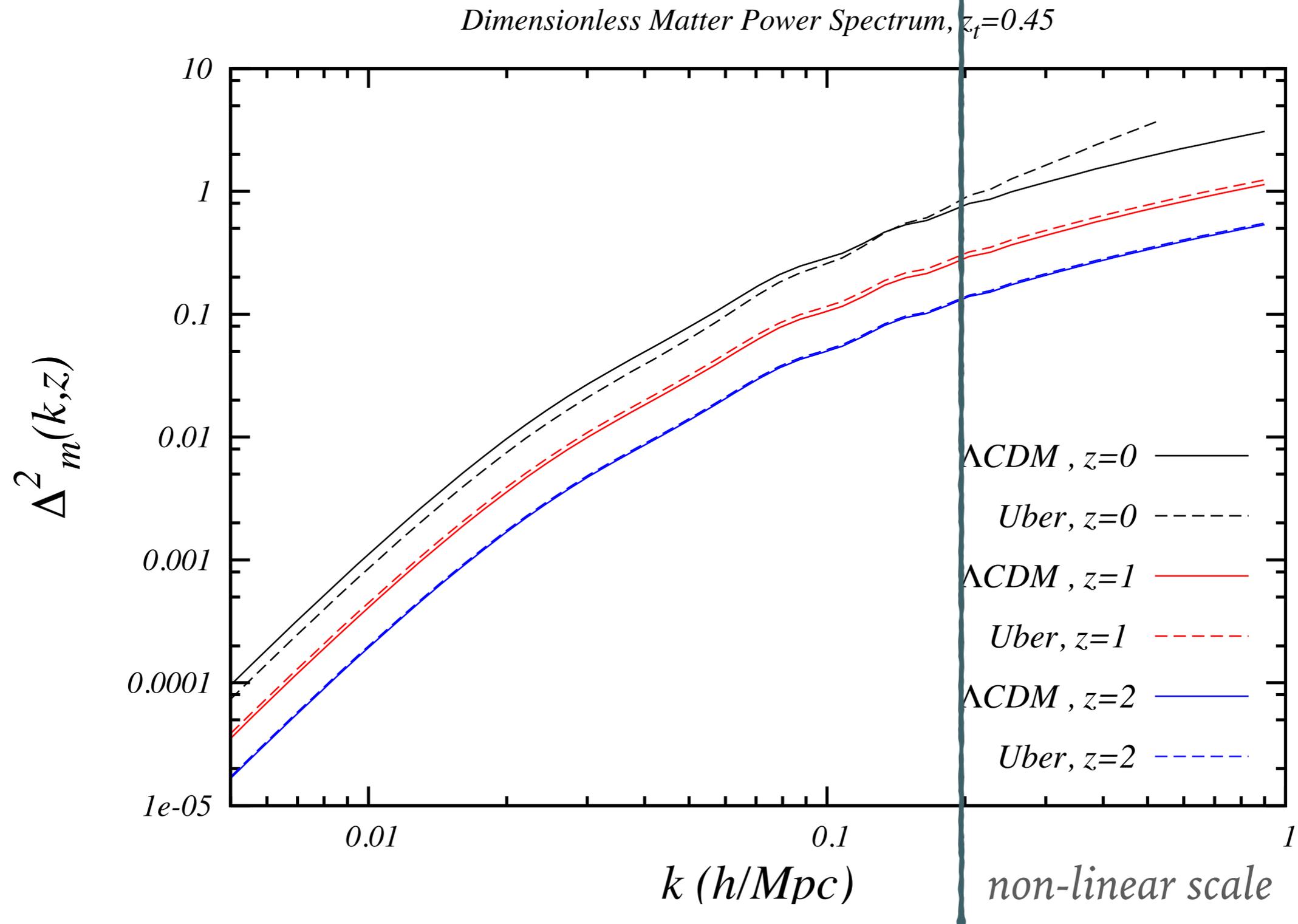
for $X = 1 + z$ in deep CDM era!

LAMBDA XOR CDM MODEL: LINEAR PERTURBATIONS

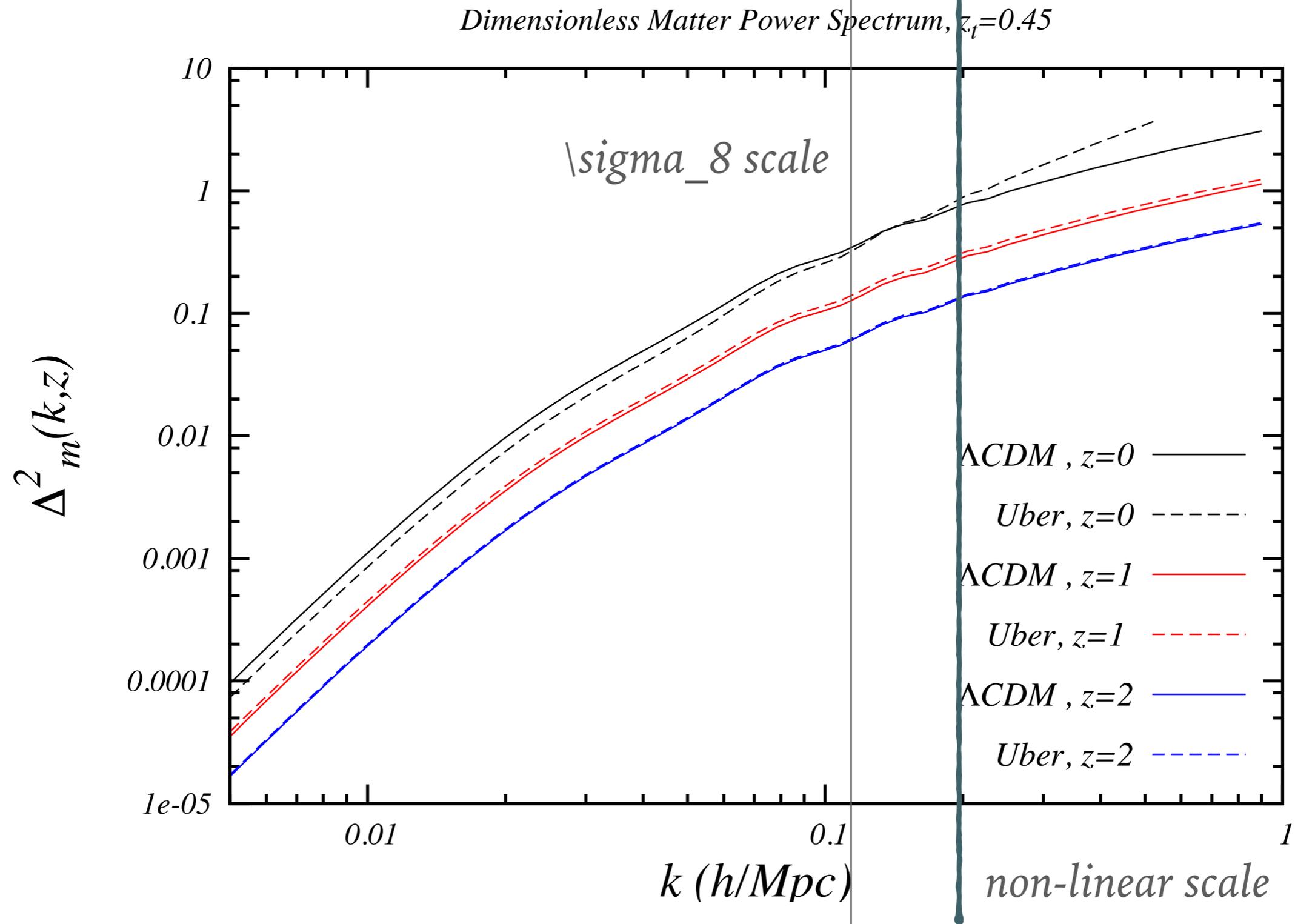
Dimensionless Matter Power Spectrum, $z_t=0.45$



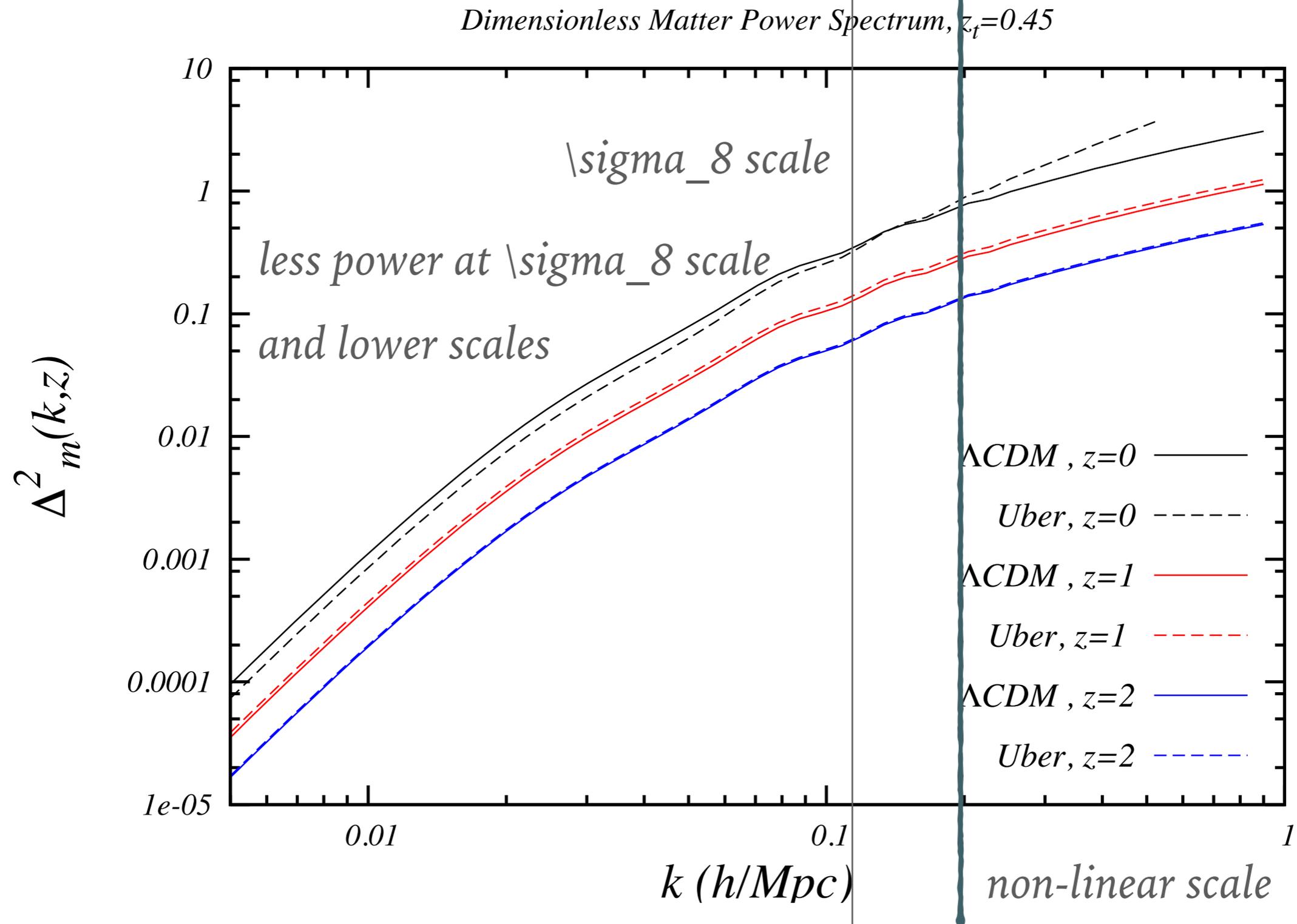
LAMBDA XOR CDM MODEL: LINEAR PERTURBATIONS



LAMBDA XOR CDM MODEL: LINEAR PERTURBATIONS



LAMBDA XOR CDM MODEL: LINEAR PERTURBATIONS



LAMBDA XOR CDM MODEL: LINEAR PERTURBATIONS

- σ_8 problem or less power problem?
- did “Lambda xor CDM” solve the σ_8 problem?
- note 1: we predict less power for σ_8 scale which is a good hint for our model!
- note 2: however we should be very careful that σ_8 scale is not well-defined in our model which predicts a scale-dependent matter power spectrum!
- note 3: we need to re-analyze all the data which gives σ_8 tension from scratch in our model.

✓ H_0 tension

? void phenomenon

? σ_8 tension

? missing satellite problem

Lambda χ CDM (*linear perturbation analysis*)

(Uber-Gravity)

✓ H_0 tension

? void phenomenon

? σ_8 tension

? missing satellite problem

Λ xor CDM

(background, linear perturbation and non-linear analysis)

(Uber-Gravity)

? a fundamental way to define probabilities