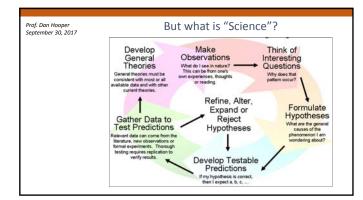
Albert Einstein and the Modern Physics Revolution

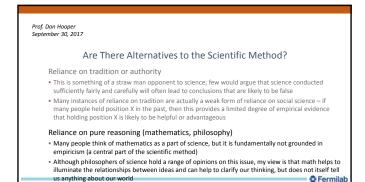
Dr. Elliott S. McCrory Saturday Morning Physics Lecture number 2 October 7, 2017

Concepts for today

- Intuition
- Transformations
- Special Relativity
- Simultaneity
- Mass equals energy
- Spacetime
- Utilizing
 - The metric system
 - Algebra
 - Star Trek
 - Trains
 - · Pole vaulters







We are guided by our intuition

- · Must be careful!
 - Ptolemeic view of the "universe" based on beliefs and on intuition
- Experience, observation and intuition are linked
- It can only takes you so far
- Intuition grows as we gain experience and make observations



Fermilal

What is Intuition?

· The ability to understand something immediately, without the need for conscious reasoning.

"We shall allow our intuition to guide us"

- a thing that one knows or considers likely from instinctive feeling rather than $% \left(1\right) =\left(1\right) \left(1\right)$ conscious reasoning.

"Your insights and intuitions as a native speaker are positively sought"

synonyms:

instinct, hunch, feeling (in one's bones), inkling, (sneaking) suspicion, idea, sense, notion;



1

Modern Physics: Our Intuition is incomplete

Much is, at first, counter-intuitive

We must develop new intuition

Terminology: A quantity is said to be

Invariant

- If different observers would obtain the same result from a measurement of this quantity.
- The mass of an object.

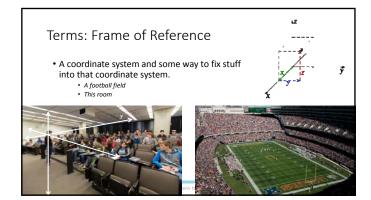
Relative

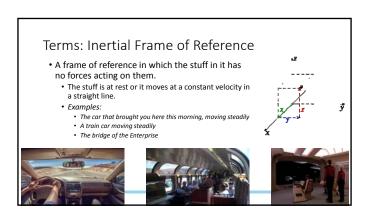
- If different observers would obtain different result from a measurement of this quantity.
 - The speed of an object.

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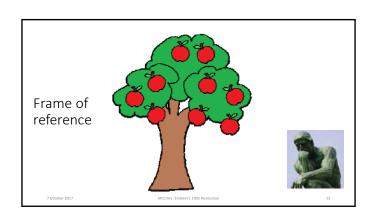


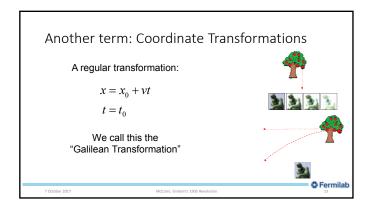
What are these symbols?

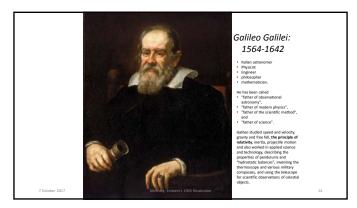
Physics Greek letters Velocity : v Beta : β

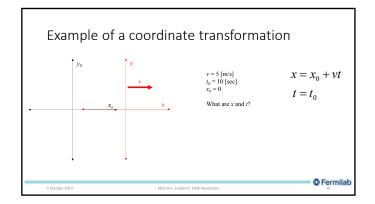
Distance : d Gamma : γ

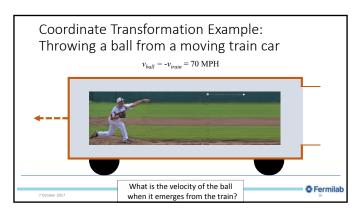
Time : *t*

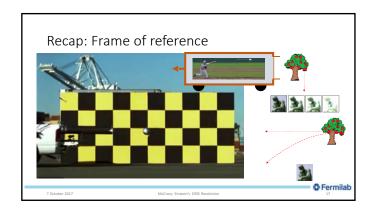


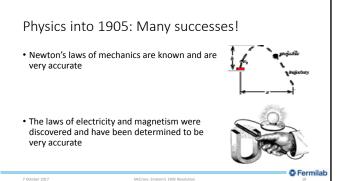












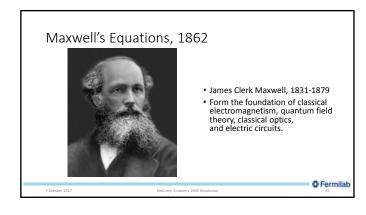


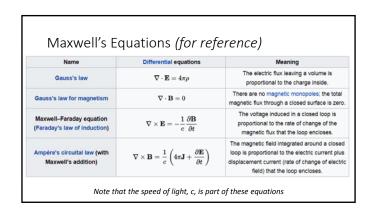
But ..

There are a few loose ends to tidy up.

A big one is contained within Maxwell's Equations of Electricity and Magnetism

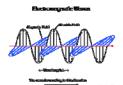
Electricity and magnetism: Maxwell's Equations





Maxwell's Equations: Powerful and accurate

- Electricity and magnetism are the same thing
- Predict the existence of light waves.
- Light is a form of electromagnetism
- Light travels with a velocity of 299,792,458 meters per second ("the speed of light", c)
- Wow! That's Fabulous!



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Maxwell's Equations: Powerful and accurate

• But Maxwell's Equations have a some strange features:

The speed of light is the same for all observers

They are not invariant under a Galilean coordinate transformation

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The Speed of Light

• It seems like* speed is relative: x' = x + vt

. . . .

 $v' = v_0 + v$

c' = c + v??

• Maxwell's Equations say that the speed of light is invariant

* Intuition

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What do Maxwell's Equations say?

- Light travels at the same speed even if the observer is moving
- Velocities do not add up in the expected way

$$v' \neq v_0 + v$$

- How's that?
 - Mathematicians to the rescue

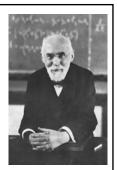
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Hendrik Lorentz (1823-1928)

- Lorentz developed a *coordinate transformation* that kept Maxwell's Equations invariant
 - By doing deep math on these complicated equations amazing!
- Maxwell's Equations are invariant under the Lorentz transformation.



♣ Fermil

Coordinate Transformations

Galilean transformation:

 $t = t_0$

Lorentz transformation:



$$x = \gamma(x_0 + vt)$$







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Understanding of Lorentz Transformations in 1905

• Even at the speed of sound, 340 m/s, this "gamma" factor is almost irrelevant:

$$\gamma = 1/\sqrt{1 - (v/c)^2}$$

$$= 1/\sqrt{1 - (340/299,792,458)^2}$$

$$= 1/\sqrt{1 - 0.99999999999357}$$

$$\gamma = 1.00000000000064$$

$$x = \gamma(x_0 + vt)$$

$$\gamma = \frac{1}{\sqrt{1 - v^2/c^2}}$$

* Intuition

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InConner Einstein's 1905 Resolution

Understanding of Lorentz Transformations in 1905

 For speeds a lot less than the speed of light, Galilean and Lorentz transformations are identical.

 $t\approx t_{0}$

$$\gamma = \frac{1}{\sqrt{1 - v^2 / c^2}}$$

$$= 1.0000000000000064$$

$$\therefore \gamma \approx 1$$

$$x \approx x_0 + vt$$

$$x = \gamma(x_0 + vt)$$
$$t = \gamma \left(t_0 + \frac{vx}{c^2} \right)$$

$$\gamma = \frac{1}{\sqrt{1 - v^2 / c^2}}$$

* Intuition

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Understanding of Lorentz Transformations in 1905

- However, for speeds close to the speed of light, Lorentz transformation predicted weird things.
 - This seemed* so radical that scientist were reluctant to accept it
 - For example, what happens when v=c?
 - Or worse: when v>c??

 $\gamma = \frac{1}{\sqrt{1 - v^2 / c^2}}$

 $x = \gamma(x_0 + vt)$

 Then there came along this patent clerk in Bern, Switzerland ...

* Intuition

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Albert Einstein (1879 – 1955)

- At age 4 (1883)
- At 23 (1902): Patent clerk
- At 26 (1905): Published 4 papers that changed everything
- At 29 (1908): Professor at U Bern
- At 36 (1915): Published The General Theory of Relativity
- At 42 (1921): Nobel Prize
- At 54 (1933): Emigrated to America
- At 76 (1955): Completes *The Meaning of Relativity*, 5th edition

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1905: Einstein's Extraordinary Year

- https://en.wikipedia.org/wiki/Annus Mirabilis papers
 - Annus Mirabilis = Extraordinary year
- Einstein published four spectacular papers, which derived explanations for:
 - 1. The Photoelectric Effect
 - Brownian Motion
 - 3. Coordinate transformations in Maxwell's Equations (Special Relativity) 🕸
 - Mass-energy equivalence ☆

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1905: Old Memes - Gone

- He introduced to humans:
 - Quantum Mechanics
 - Special Relativity
 E=mc²



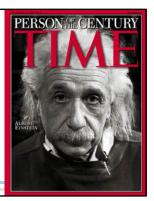
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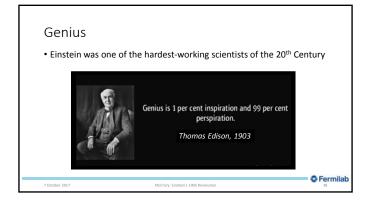
4 papers: More than a century of physics

- Each of these papers, individually, would have turned physics on its head
- All of them together from one person, in one year, is (to me) incomprehensible!

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Physics: Velocity (v), Distance (d) and Time (t)

Hint: Use the units

v = d/t

[meters per second] = [meters] ÷ [second]

d = vt

 $[m] = [m/s] \times [s]$

t = d/v

 $[s] = [m] \div [m/s]$

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And now

Special Relativity

"On the Electrodynamics of Moving Bodies"

891

Special Relativity

3. Zur Elektrodynamik bewegter Körper; von A. Einstein.

Daß die Elektrodynamik Maxwells — wie dieselbe gegenwärtig aufgefaßt zu werden pflegt — in ihrer Anwendung auf bewegte Körper zu Asymmetrien führt, welche den Phänomenen nicht anzuhaften scheinen, ist bekannt. Man denke z.B. an

Einstein stipulated

- The laws of nature are the same in all inertial frames of reference.
 - Intuition
- The speed of light in the vacuum is the same in all inertial frames of reference.
 - Recognized as a (crazy?) feature of Maxwell's Equations

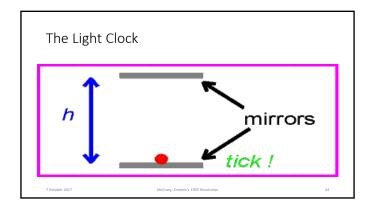
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What can we predict* from these two assumptions?

Let invent a new type of clock and see

* Scientific method



Time = distance / velocity

$$t = 2h/v$$

$$t = 2h/c$$

$$h = \frac{1}{2}tc$$

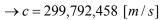
The clock ticks at a rate of 2h/c seconds

For a clock that ticks every t seconds, the mirrors are $\frac{1}{2}tc$ apart

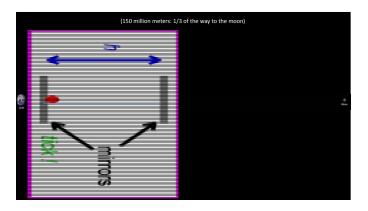
For the clock to tick at 1 second $h = \frac{1}{2}tc$

$$h = \frac{1}{2}c$$

$$h=\frac{1}{2}C$$

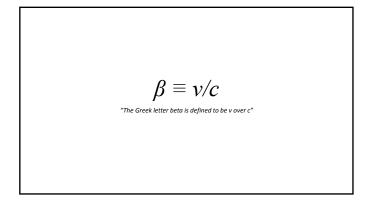


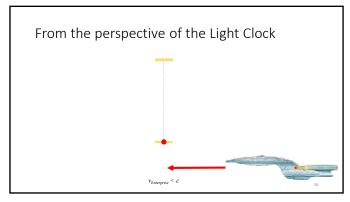
$$h = 149,896,229$$
 [m]

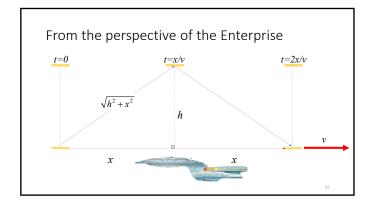


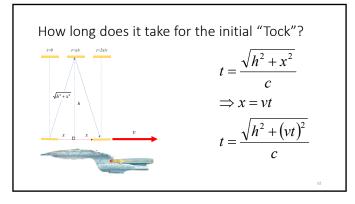
Remember, we assumed

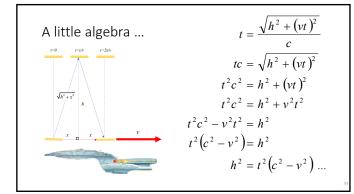
The speed of light is the same for all observers

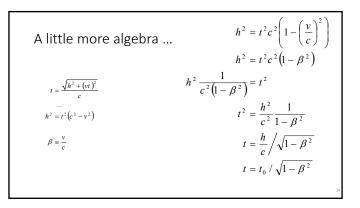


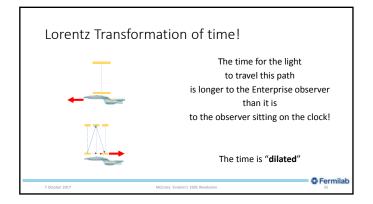












$$t = \frac{t_0}{\sqrt{1 - \beta^2}}$$

Wow! That's Fantastic!

Dilate

v.tr.

To make wider or larger; cause to expand. *v.intr.*

- 1. To become wider or larger; expand.
- **2.** To speak or write at great length on a subject ; expatiate.

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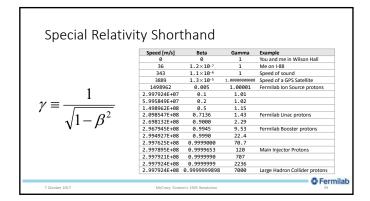
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& Fermila

In other words ...

For the observer on the Enterprise <u>and</u> the observer on the mirrors to see the light to go between the mirrors the same way, ...

The passage of time on the Enterprise has to be slower than the passage of time on the mirrors!



Recap: Time dilation

$$t = \gamma t_0$$

The time observed on the moving clock is longer than the observer's clock

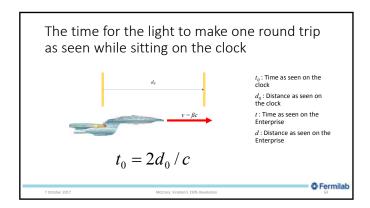
$$t_0 = t / \gamma$$

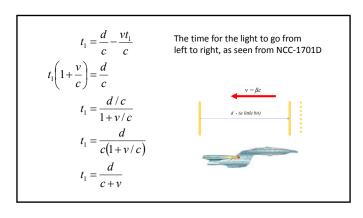
The time on the observer's clock is shorter than the moving clock

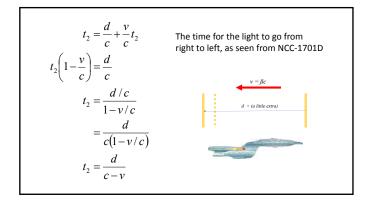
How long is one second, as seen from the Earth, on the Enterprise for v=0.25c ? *

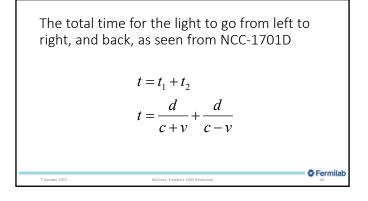
A. 0.9682B. 3.1416C. 0.7071D. 1.0328E. 1.1412*ST.THG Technical Manual "High relativative speeds are to be avoided unless absolutely necessary; impulse power should be limited to a maximum of $\frac{1}{2}$ lightwapped of the control of the

Light Clock also leads to length contraction $d = d_0 / \gamma$









We'll use this:

$$\left(\frac{1}{a-b} + \frac{1}{a+b}\right) = \left(\frac{a+b}{(a-b)(a+b)} + \frac{a-b}{(a-b)(a+b)}\right)$$
$$= \left(\frac{2a}{(a-b)(a+b)}\right)$$
$$= \frac{2a}{a^2 - b^2}$$

$$t = \frac{d}{c - v} + \frac{d}{c + v}$$

$$= d\left(\frac{2c}{c^2 - v^2}\right)$$

$$= \frac{2cd}{c^2\left(1 - \frac{v^2}{c^2}\right)}$$

$$= \frac{2d}{c}\left(\frac{1}{(1 - \beta^2)}\right)$$

$$= \frac{2d}{c}\left(\frac{1}{2\gamma^2}\right)$$

$$= \frac{2d}{c}\left(\frac{1}{2\gamma^2}\right)$$

$$= \frac{2d}{c}\left(\frac{1}{2\gamma^2}\right)$$

$$= \frac{2d}{c}\left(\frac{1}{2\gamma^2}\right)$$

$$= \frac{ct}{2\gamma^2}$$

$$d = \frac{ct}{2\gamma^2}$$

$$d = \frac{d}{d} = \frac{d}{d}$$

$$d = \frac{d}{d} = \frac{d}{d}$$

Special Relativity Summary

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A nice velocity $v = 0.866 \ c$ $\beta = 0.866$ $\gamma = 1/\sqrt{1-(0.866)^2}$ $= 1/\sqrt{1-.749956}$ $\approx 1/\sqrt{1-0.75}$ = 1/0.5 = 2 Questions?

Simultaneity



- Noun form of "simultaneous"
- Two events happen simultaneously when you see/observe that they have occurred at the same time.
- The fact that the speed of light is the same to all observers means that our intuitive understanding of simultaneity needs to be extended.
 - Let's see why

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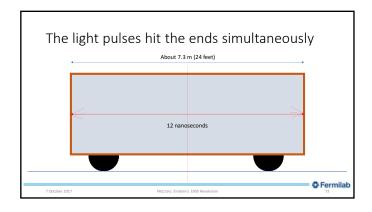


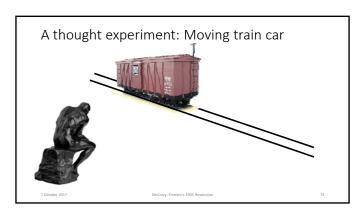
A thought experiment: Stationary train car

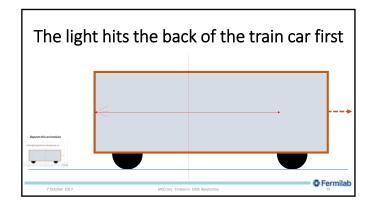
7.3 m (24 feet)

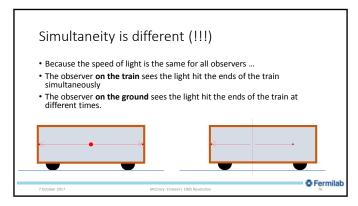
A light pulse

19 nanoseconds

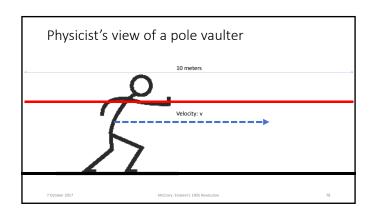


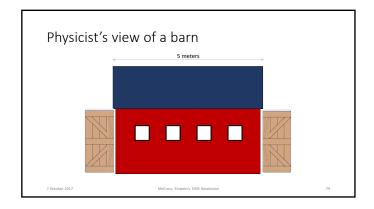


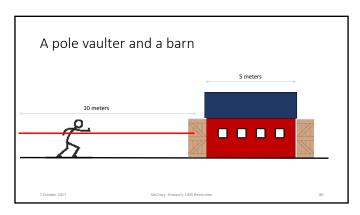


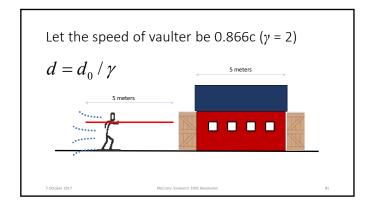


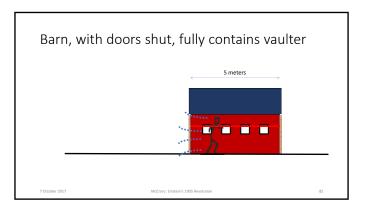
Scientists tried to disprove counter-intuitive aspects of Special Relativity

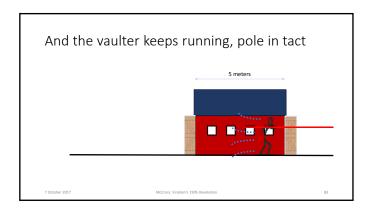


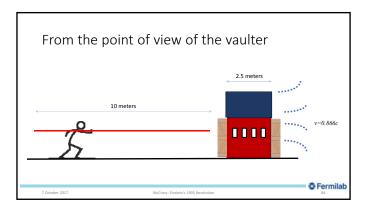


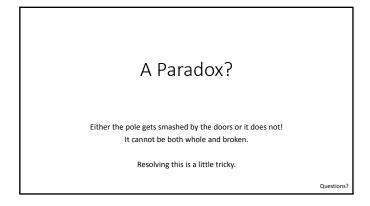


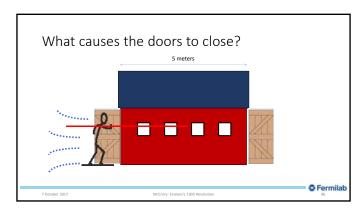












causality

nour

The relationship between cause and effect.

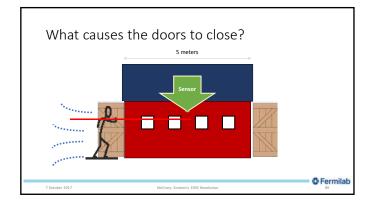
causal

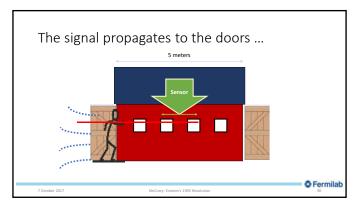
adjective

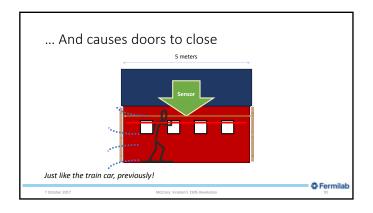
Relating to or acting as a cause.

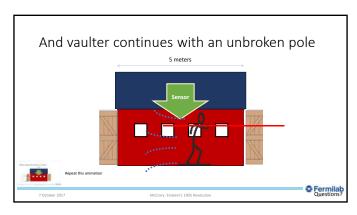
Causality can travel no faster than the speed of light

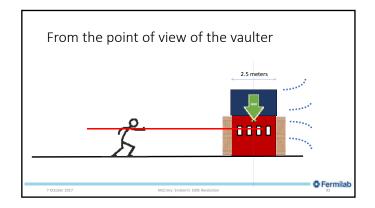
So, let's use a light-based signal to cause the doors to close

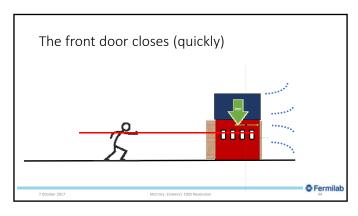


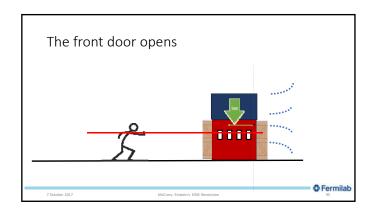


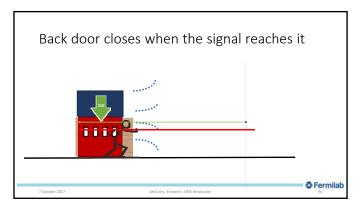


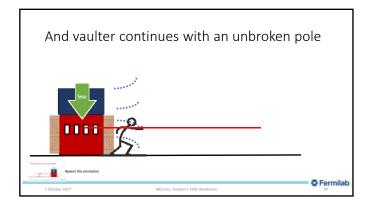


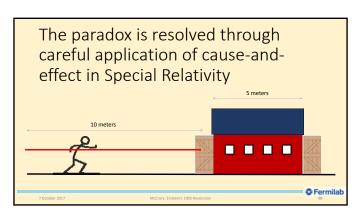












More on this apparent paradox ...

• https://en.wikipedia.org/wiki/Ladder paradox

• YouTube: "Relativity 5b - pole and barn paradox", by viascience.
• https://www.youtube.com/watch?v=0TU1tKTOlj4

At first, this seemed counter-intuitive

We have improved our intuition

Equivalence of mass and energy

"Does the Inertia of a Body Depend Upon Its Energy Content?"

639

13. Ist die Trägheit eines Körpers von seinem
Energieinhalt abhängig?
von A. Einstein.

Die Resultate einer jüngst in diesen Annalen von mir
publizierten elektrodynamischen Untersuchung!) führen zu einer
sehr interessanten Folgerung, die hier abgeleitet werden soll.
Ich legte dort die Maxwell-Hertzschen Gleichungen für
den leeren Raum nebst dem Maxwellschen Ausdruck für die
elektromagnetische Energie des Raumes zugrunde und außer-

Special Relativity: $E = mc^2$ • It is possible to derive this formula using algebra

• Energy = force × distance

• Force = the change in the momentum of an object

• Lorentz transformations of time (that is, the velocity)

• But it is easier (and cleaner) to use calculus

• http://www.emc2-explained.info/Emc2/Deriving.htm

$$E = mc^2$$

Derived using only math (mostly algebra) and the two conjectures:

- 1. The laws of nature are the same in all inertial frames of reference.
- 2. The speed of light in the vacuum is the same in all inertial frames of reference.

Mind: Blown! Wonderful Theoretical Fun!

Energy and mass are the same thing



An aside: Our nomenclature at Fermilab

• Physicists at Fermilab set the speed of light equal to one

$$E = m$$

- This is only a change in units
- Emphasizing even more clearly that energy is the same thing as mass

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McCrory: Einstein's 1905 Revolution



What does this mean? $E = mc^2$

• What is the energy of 1 gram of matter?

 $E = 0.001 \text{ [kg]} \times (2.998 \times 10^8 \text{ [m/s]})^2$ $E = 1 \times 10^{-3} \times 8.988004 \times 10^{16} \text{ [kg m²/sec²]}$ $E = 8.988004 \times 10^{13} \text{ [Joules]}$ $E \approx 90 \text{ Terajoules}$

- → Burning 691,538 gallons of gasoline
- → Exploding 42,964,554 pounds (21.5 kilo-tons (kT)) of TNT

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Crory: Einstein's 1905 Revolution



First atomic bomb: Hiroshima (USA, fission)

- Hiroshima bomb: 63 Terajoules [6.3 imes 10 13 Joules] (15 kT)
- Equivalent to about 0.7 grams of matter converted to energy





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Largest bomb: Tsar Bomba (USSR, fusion)

- Tsar Bomba: 240 Petajoules [2.4 imes 10 17 joules] (57 MT)
 - 3800 times larger than Hiroshima bomb
 - Converted about 2.7 kg of matter into energy





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How do we know Special Relativity is accurate? No Lorentz violations could be measured thus far, and exceptions in which positive results were reported have been refuted or lack further confirmations.

Everyday uses of Special Relativity

• Global Positioning System (GPS)

• Muon Decay

GPS is based on very accurate clocks

• GPS clock ticks must be known to an accuracy of 20-30 nanoseconds
• ~5 meters on the road.

• GPS satellites are constantly moving relative to Earthly observers
• These clocks move a little more slowly
• Special Relativity predictions ... next slide

• GPS also gets substantial corrections from General Relativity

An aside — GPS and General relativity

The satellite is in micro-gravity

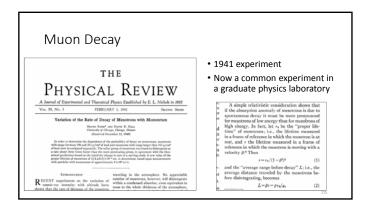
The receiver is in Earth gravity

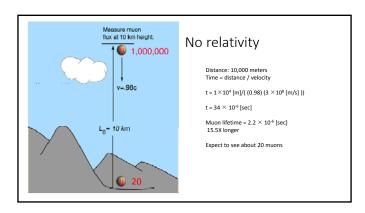
General Relativity:

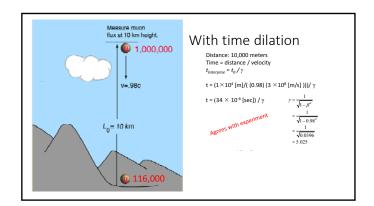
Earth clock runs 38 microseconds slower per day

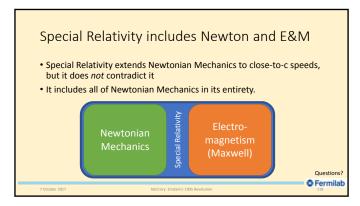
5.4% bigger effect than Special Relativity

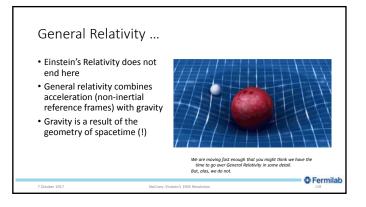
About a mile of error per day



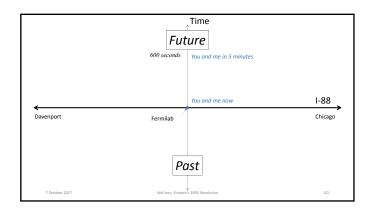


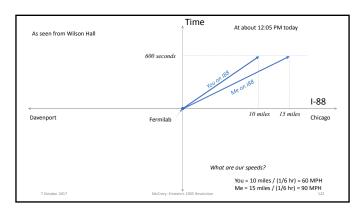


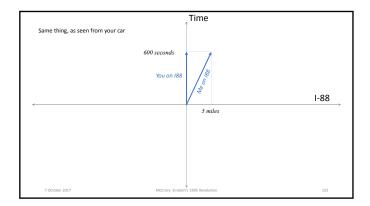


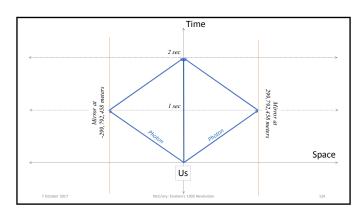


Spacetime

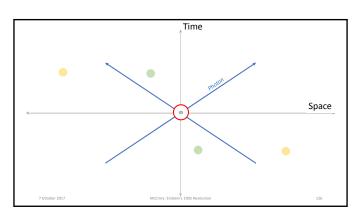


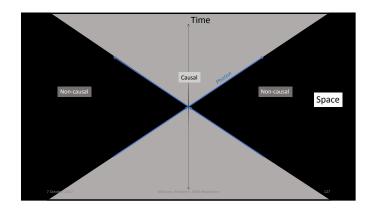


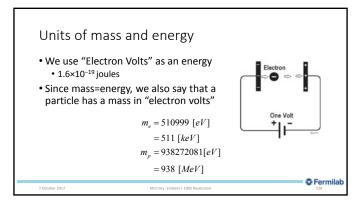




Causality: The fastest a signal can travel is *c*



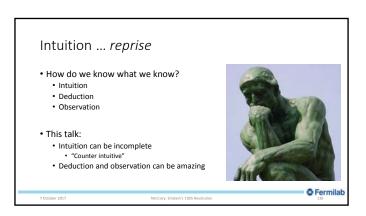




Converting between energy and mass

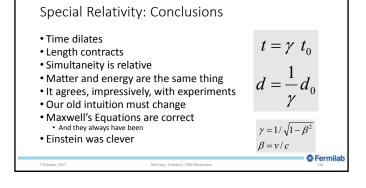
• When two particles collide at high energy, the result has a lot of energy

• Often (usually) this energy becomes mass.



In other words, Special Relativity is

A triumph of the Scientific Method



Conclusions

Weary, though fascinated!

- Einstein was one of the greatest minds ever
- 1905: Four papers changed humans' understanding of the physical
- Special Relativity: Old intuition of space and time must be adjusted
- Algebra is cool

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Relativity does not end here

General relativity

- Einstein's life's work
- Space is warped by mass
- Mass moves according to how space is warped
- Mind-blowing predictions:
 Precession of the orbit of Mercury
 - Light is bent by a gravity field Black holes
 - Expansion of the universe Gravity waves

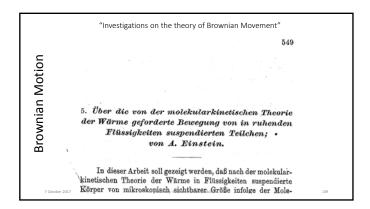
That's all, folks!

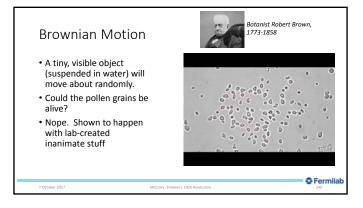
These slides:

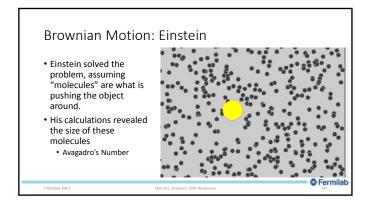
- 1. https://smp.fnal.gov
- 2. "Session I: Fall 2017"

The other 1905 Einstein papers were also profound

Brownian Motion







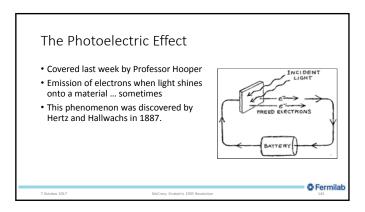
"On a Heuristic Point of View about the Creation and Conversion of Light"

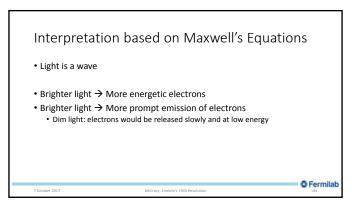
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6. Über einen

die Erzeugung und Verwandlung des Lichtes
betreffenden heuristischen Gesichtspunkt;
von A. Einstein.

Zwischen den theoretischen Vorstellungen, welche sich die
Physiker über die Gase und andere ponderable Körper gebildet haben, und der Maxwellschen Theorie der elektromagnetischen Prozesse im sogenannten leeren Raume besteht

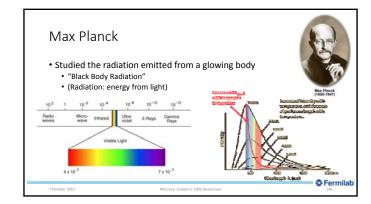




Observations

- In 1902, Lenard observed that the energy of individual emitted electrons increased with the *color* of the light, but not the intensity.
- Furthermore, when the color was blue enough, electrons would be emitted instantly

7 October 2017 McCrony: Einstein's 1905 Revolution 145



How to fit this frequency curve? • Assume that electromagnetic energy could be emitted only in quantized form • He introduced a new constant, h: E = hv• h is Planck's constant, 6.62607×10⁻³⁴ [Joules seconds] • v ("nu") is the frequency of the radiation.

(mathematically) of this assumption, but they did not (particularly) like what this meant!

Max Planck and Einstein

- Einstein showed that Planck's assertion, that light is made up of particles, would resolve the photoelectric effect
- Light comes in quanta, and they behave like particles in the Photoelectric effect
- These particles (now called "photons") hit electrons in the atoms of the metal and can only kick them out if the energy of the photos is high enough

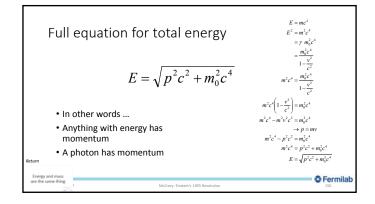
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Wave/particle duality

- The photoelectric effect helped to propel the then-emerging concept of wave–particle duality in the nature of light.
- Light simultaneously possesses the characteristics of both waves and particles, each being manifested according to the circumstances.
- \bullet It was soon realized that particles with mass also have a wavelength

Crober 2017 McCross Statistics 1905 Resolution 140



An aside: No new physics in 20th Century?

- One school of thought:

 - One school of thought:

 Classical mechanics could cope with highly complex problems involving macroscopic situations

 Thermodynamics and kinetic theory were well established

 Geometrical and physical optics could be understood in terms of electromagnetic waves

 Conservation laws for energy and momentum (and mass) were widely accepted

 t was generally accepted that all the important laws of physics had been discovered

 Research would be concerned with clearing up minor problems and particularly with improvements of method and measurement.
- However, A. A. Michelson's in his 1899 lectures Light Waves and Their Uses:
 What would be the use of extreme refinement in the science of measurement?
 L. Jall fitture discovery must lie [here].
 The more important fundamental laws and facts of physical science have all been discovered, and these are now so firmly established that the possibility of their ever being supplanted in consequence of new discoveries is exceedingly remote.
 Nevertheless, it has been found that there are apparent exceptions to most of these laws, and this is particularly true when the observations are pushed to a limit, i. e., whenever the circumstances of experiment are such that carterine cases can be examined. Such examination almost surely leads, not to the overthrow of the law, but to the discovery of other facts and laws whose action produces the apparent exceptions.

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McCrory: Einstein's 1905 Revolution

Some perspective on Annus Miralilis

- Worked as an examiner at the Patent Office in Bern, Switzerland
 - Limited access to scientific reference materials,
 - Co-worker: "[Einstein] could not have found a better sounding board for his ideas in all of Europe".
- Einstein tackles some of the era's most important physics questions
- These papers solved the primary scientific problems of the era:
 - Lord Kelvin lecture titled "Nineteenth-Century Clouds over the Dynamical Theory of Heat and Light"
 - Michelson–Morley experiment
 Black body radiation.
 - Coordinate transformation of Maxwell's Equations.

