

Low- ν Flux

Lu Ren

University of Pittsburgh

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Outline

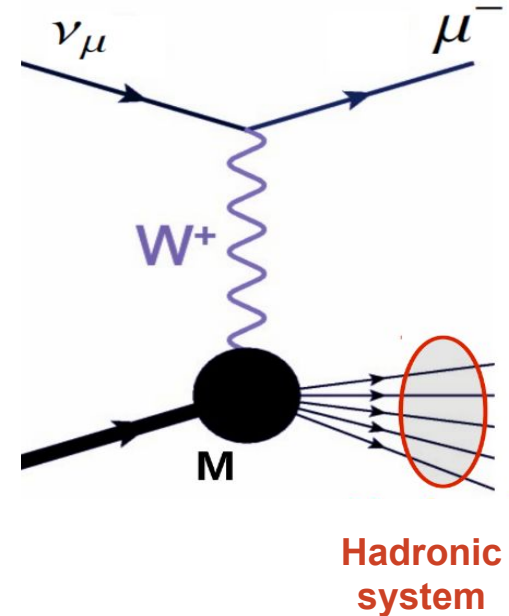
- Reminder of low- ν method
- Flux uncertainty
 - Overview
 - Cross section model
 - FSI model
 - Energy scales
- Summary

Sample

- Input flux (same as NDTF dst samples')
- Target: CH2
- Sample sizes: 500,000 charged-current events per sample
- MC model details
 - GENIE 2.12.6
 - Study uses Nieves model MEC (circa MINERvA 2017)
 - Comparing with MINERvA (GENIE 2.8.4 With RPA, Nieves MEC and CC1pi reweighted)

Reminder of Low- ν Method

- Relies on the information from hadron energy
 - $\nu = E_{Had} = E_\nu - E_\mu$
- $\frac{d\sigma^{\nu,\bar{\nu}}}{d\nu} = A(1 + \frac{B^{\nu,\bar{\nu}}}{A} \frac{\nu}{E} - \frac{C^{\nu,\bar{\nu}}}{A} \frac{\nu^2}{2E^2})$
- In the limit $\frac{\nu}{E} \rightarrow 0$
 - Cross sections are **constants** -- independent of neutrino energy
 - **Small ν/E dependent** correction
$$S^{\nu(\bar{\nu})}(\nu_0, E) = \frac{\sigma^{\nu(\bar{\nu})}(\nu < \nu_0, E)}{\sigma^{\nu(\bar{\nu})}(\nu < \nu_0, E \rightarrow \infty)}$$
 - Flux normalized with external world data
 - cross section

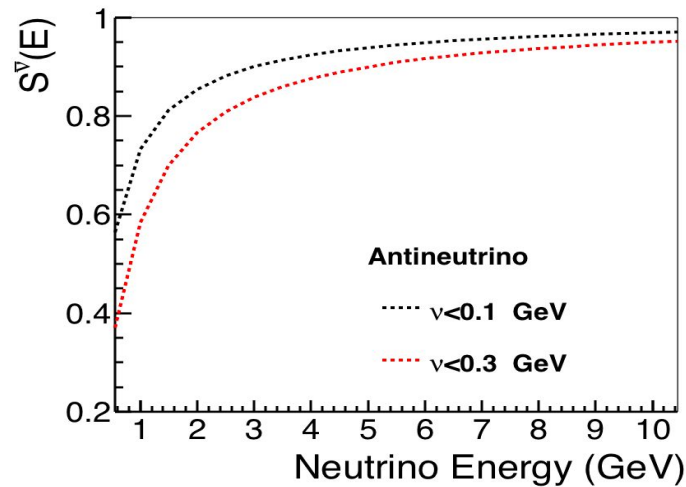
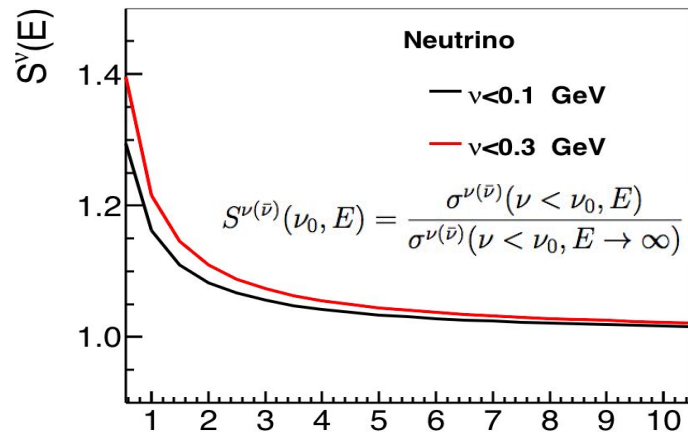


Low- ν Flux

- Use truth information to extract low- ν flux
 - **Inclusive sample** $N^\nu(E_\nu)$
 - CC events in neutrino energy range <10 GeV
 - **Flux sample** $F^\nu(E_\nu)$
 - Inclusive sample with $\nu < 0.1$ GeV
 - **Model correction** $S^{\nu, \nu < \nu_0}(E_\nu)$
 - **Normalization** H^ν
 - At Ev bin 9-10 GeV

$$\sigma^\nu(E_\nu) = \frac{N^\nu(E_\nu)}{F^\nu(E_\nu)} * \frac{S^{\nu, \nu < \nu_0}(E_\nu)}{H^\nu}$$

$$\Phi^\nu(E_\nu) = \frac{F^\nu(E_\nu) * H^\nu}{S^{\nu, \nu < \nu_0}(E_\nu)}$$



Flux Uncertainty Estimation Method

- Extract low- ν flux with single parameter shifted:

$$\Phi(E_\nu) = \frac{F(E_\nu) * H}{S^{\nu < \nu_0}(E_\nu)} \longrightarrow \Phi'(E'_\nu) = \frac{F'(E'_\nu) * H'}{S^{\nu < \nu_0}(E_\nu)}$$

- Shape uncertainty from
 - **Model correction S**: when $\nu < 0.1$ GeV, QEL and MEC contribute (small, MEC \ll QEL, ignore this for now)
 - **Flux sample F(E ν)**

- Level uncertainty mainly from **inclusive sample**
 - Relative normalization (shape) to cross section at 9-10 GeV

$$H = \frac{N(10)}{F(10)} * \frac{S^{\nu < \nu_0}(10)}{\sigma(10)} \longrightarrow H' = \frac{N'(10)}{F'(10)} * \frac{S^{\nu < \nu_0}(10)}{\sigma(10)}$$

- Depend on **N(10)** / **F(10)**

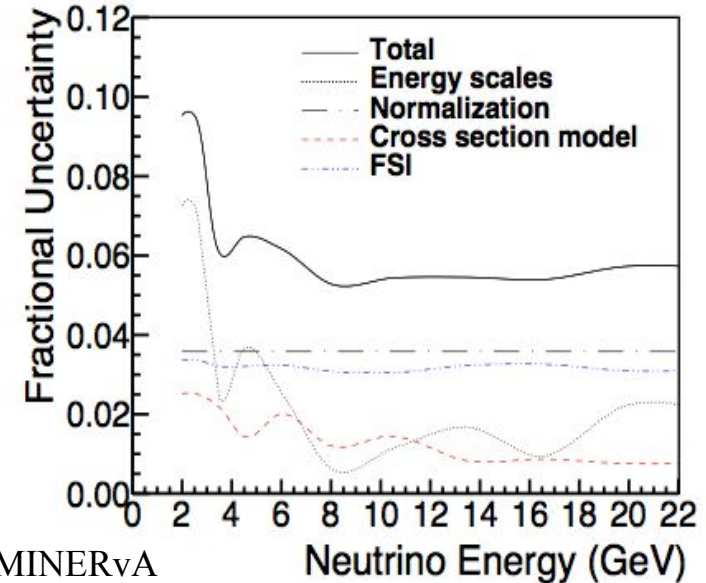
$$\sigma(10) = \frac{N(10)}{F(10)} * \frac{S^{\nu < \nu_0}(10)}{H}$$

$$\sigma(10) = \frac{N'(10)}{F'(10)} * \frac{S^{\nu < \nu_0}(10)}{H'}$$

Flux Uncertainty Estimation Method

L. Ren et al., Phys.Rev. D95 (2017) no.7, 072009

- Sources of uncertainty (separately evaluate pieces)
 - Cross section model
 - GENIE(CCQE, RES, DIS)
 - 2p2h
 - RPA
 - GENIE FSI model
 - Energy scales
 - Normalization (not included- shape only)
- Using truth information, does not include
 - Backgrounds
 - Negligible for neutrino, <1% for antineutrino flux in MINERvA
 - Smearing effect
- Comparing with MINERvA
 - MINERvA uses ν cut 0.3-2 GeV, here uses ν cut 0.1 GeV
 - MINERvA normalizes at 12-22 GeV, here normalizes at 9-10 GeV



Components of Flux Uncertainty

- Cross section model
 - GENIE(CCQE, RES, DIS)
 - 2p2h
 - RPA (recap)
- GENIE FSI model
- Energy scales (recap)
- Summary of flux uncertainties

Cross Section Model Uncertainties in GENIE

- Table from MINERvA
- Differences from MINERvA
 - Show MaCCQE uncertainty (+25% / -15%), which is removed by MINERvA
 - $rvn1\pi$: 1σ is +/-50% (GENIE recommended) instead of 15% in MINERvA
 - VeCFFCCQEshape not included due to technical problem (<0.6% in MINERvA)

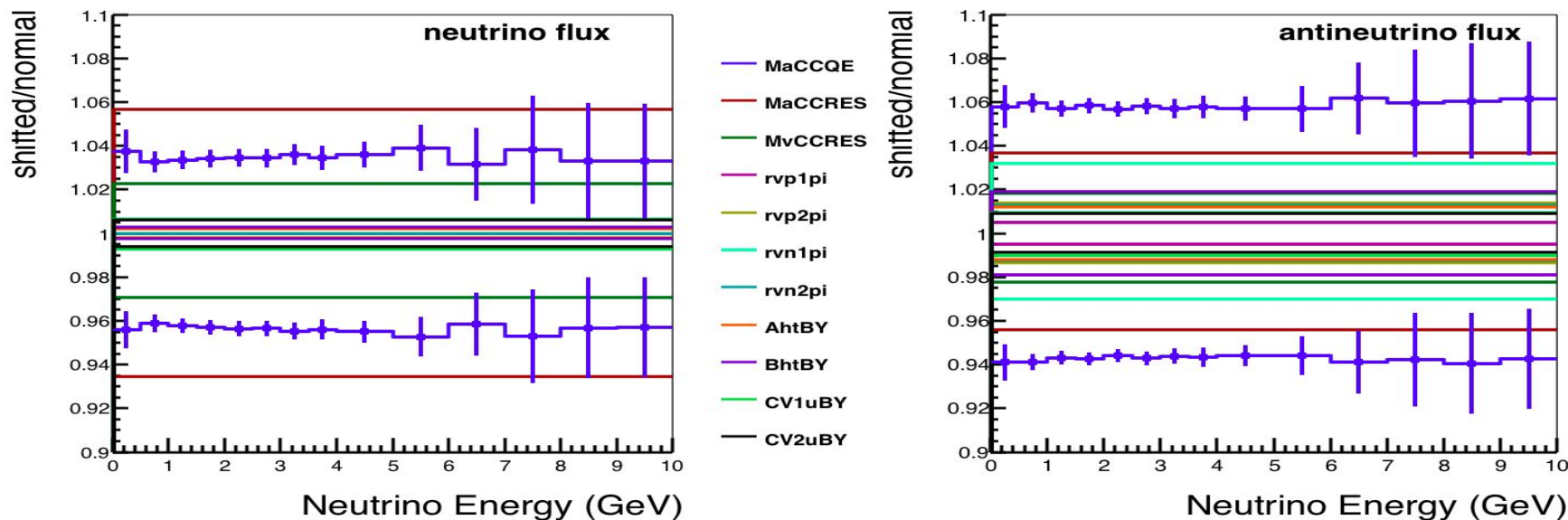
GENIE Knob name	Description	1σ
MaRES	adjust M_A in Rein-Sehgal cross section	$\pm 20\%$
MvRES	adjust M_v in Rein-Sehgal cross section	$\pm 10\%$
Rvp1pi	1 pi production from νp non-resonant interactions	$\pm 50\%$
Rvn1pi	1 pi production from νn non-resonant interactions	$\pm 15\%$
Rvp2pi	2 pi production from νp non-resonant interactions	$\pm 50\%$
Rvn2pi	2 pi production from νn non-resonant interactions	$\pm 50\%$
VeCFFCCQEshape	Changes from BBBA to dipole	on or off
AhtBY	Bodek-Yang parameter A_{HT}	$\pm 25\%$
BhtBY	Bodek-Yang parameter B_{HT}	$\pm 25\%$
CV1uBY	Bodek-Yang parameter C_{V1u}	$\pm 30\%$
CV2uBY	Bodek-Yang parameter C_{V2u}	$\pm 40\%$

Cross Section Model Uncertainties in GENIE

- Dominated by MaRES, MaCCQE
 - MaCCQE not included in summary plots
- Most are level uncertainty propagated from the 9-10 GeV bin of inclusive sample.
- Only MaCCQE affect the shape of flux ($\nu < 0.1\text{GeV}$)
 - Including smearing effect might introduce shift of shape from other systematics

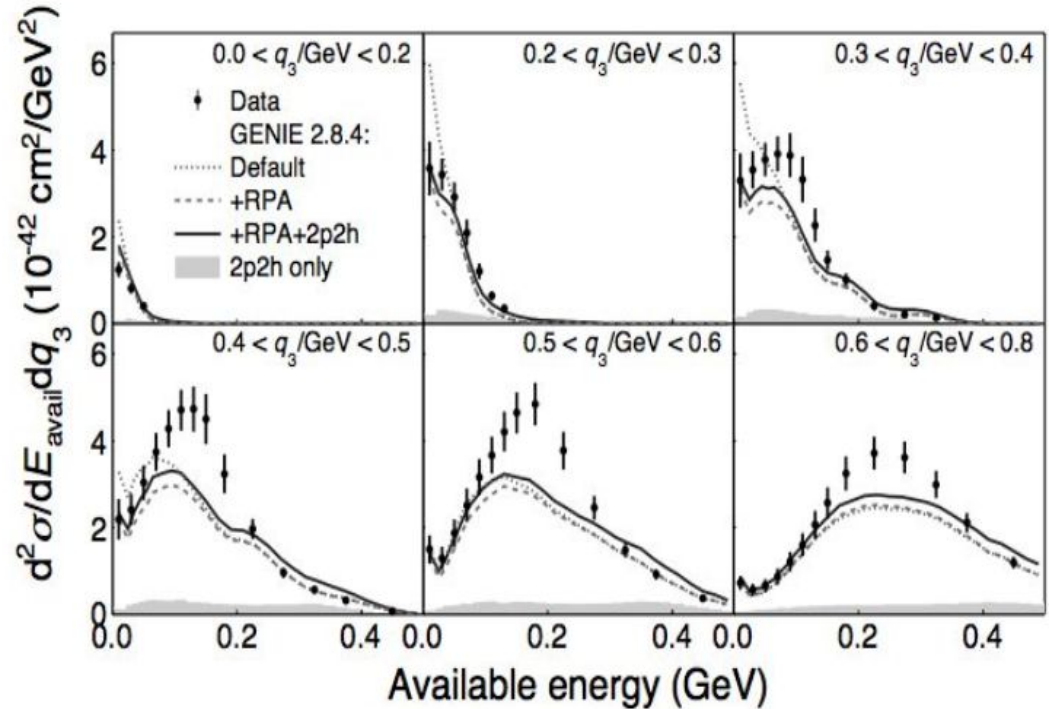
$$\Phi'(E'_\nu) = \frac{F'(E'_\nu) * H'}{S^{\nu < \nu_0}(E'_\nu)}$$

$$H' = \frac{N'(10)}{F'(10)} * \frac{S^{\nu < \nu_0}(10)}{\sigma(10)}$$



MINERvA's 2p2h Uncertainty

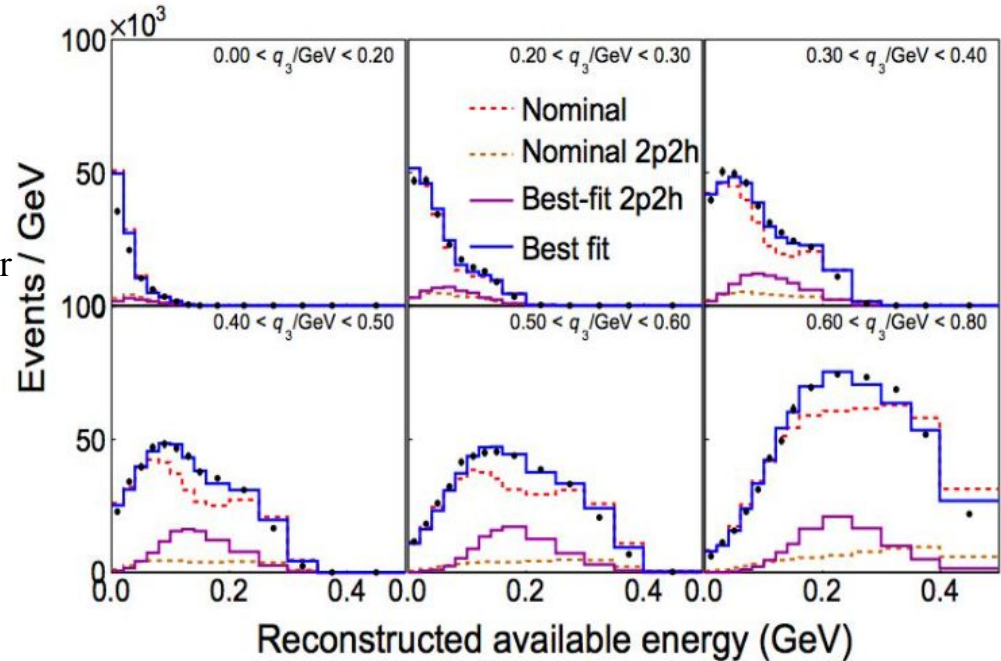
- MINERvA measured differential cross section at low 3-momentum transfer region for neutrino
- Available energy
 - $\sim E_{\text{had}}$ (visible energy- not including neutron energy)
- Implementing Nieves 2p2h and RPA improves agreement with data
- 2p2h uncertainty
 - Remaining data MC difference



P. A. Rodrigues et al., Phys. Rev. Lett. 116, 071802 (2016)

MINERvA's 2p2h Uncertainty

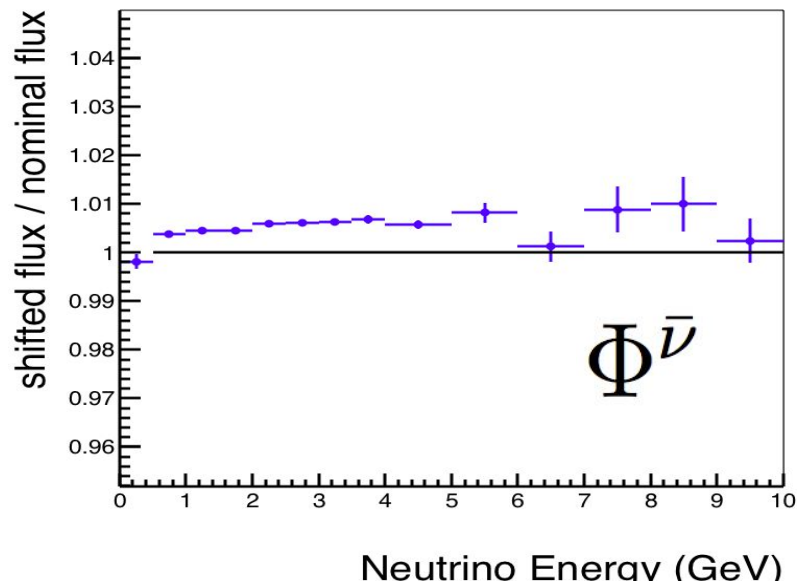
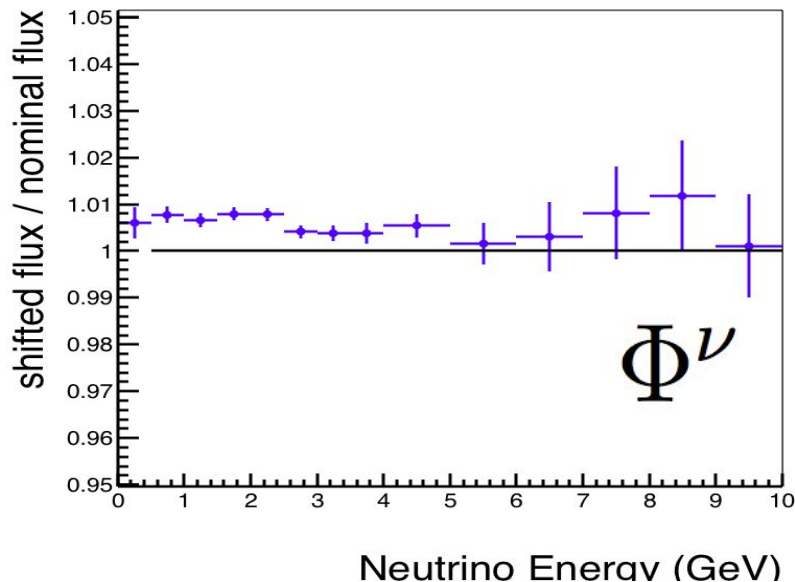
- MINERvA 2-step fit for low- ν flux:
 - (q_3 , Eavail) fit to data
 - Nominal vs best fit
 - Initial state reweighting
 - reweight nn/pp/np event to further improve the agreement with data
 - Small effect, not included in this study
- Apply in the region
 - $q_3 < 0.8$ GeV
 - To both neutrino and antineutrino
 - MINERvA is working on antineutrino version



Ref: MINERvA internal document by P. A. Rodrigues

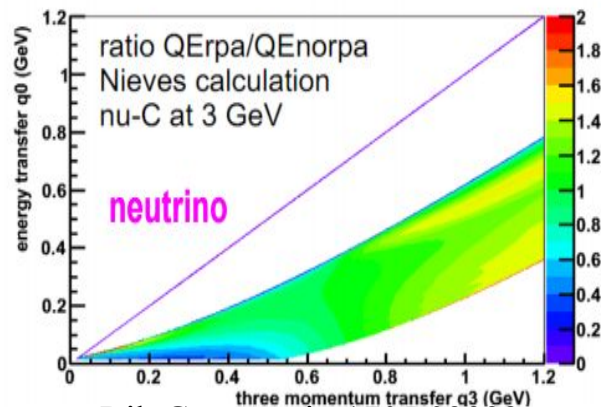
2p2h Model Uncertainty

- MC sample size increased for this study
- <1% effect on flux
- Similar as MINERvA

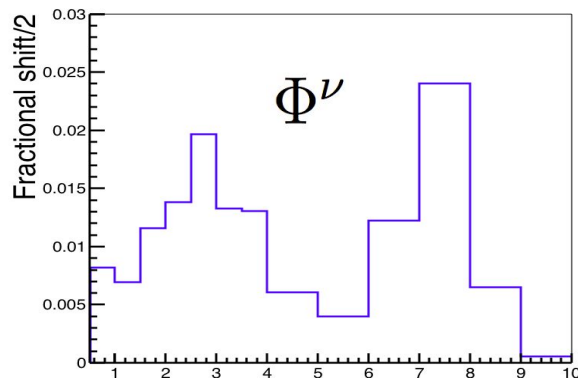


RPA (recap)

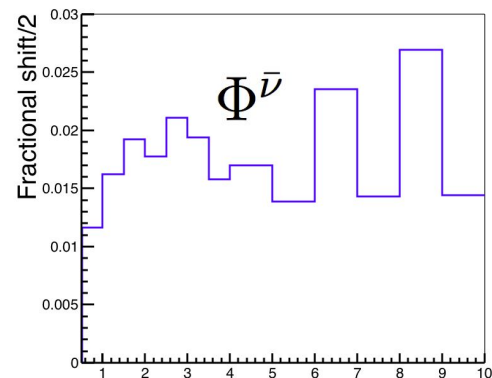
- Shown at collaboration meeting in August
<https://indico.fnal.gov/event/13293/session/7/contribution/83/material/slides/0.pdf>
- MINERvA's prescription
 - Reweight QE events with 2D weight (q_0 vs q_3): QE RPA / QE no RPA
 - Extract low- ν flux with RPA weight, and take half of the change in flux as an uncertainty
 - Uncertainty of $< 2.5\%$ for neutrino and antineutrino flux (MINERvA: $< 1.5\%$)
 - Large statistical error above 6 GeV



Rik Gran, arxiv:1705.02932



Neutrino Enerav (GeV)



Neutrino Enerav (GeV)

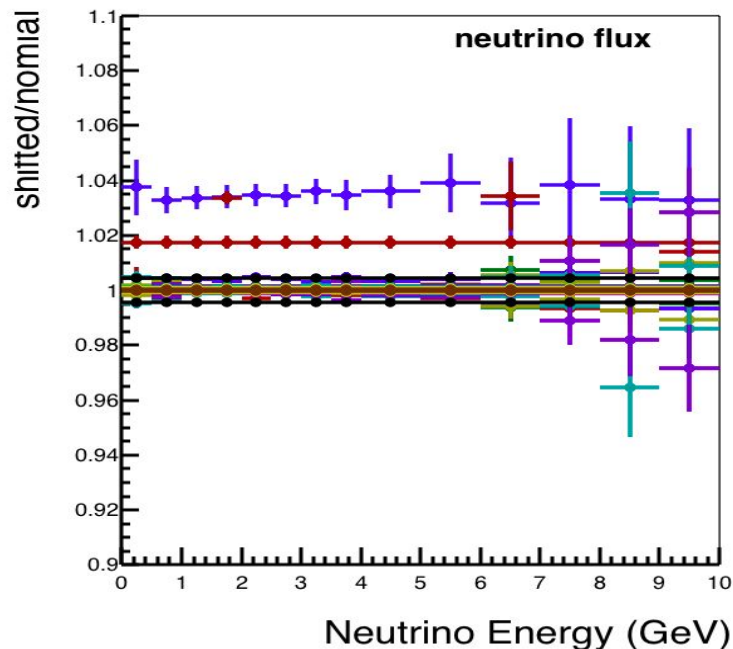
GENIE FSI Model Uncertainty

- MINERvA FSI uncertainties
- Differences from MINERvA
 - Bottom 3 uncertainties and AGKYxF1pi not included due to technical issue (<1% in MINERvA)

GENIE Knob name	Description	1 σ
MFP_N	mean free path for nucleons	$\pm 20\%$
FrCex_N	nucleon fates - charge exchange	$\pm 50\%$
FrElas_N	nucleon fates - elastic	$\pm 30\%$
Frinel_N	nucleon fates - inelastic	$\pm 40\%$
FrAbs_N	nucleon fates - absorption	$\pm 20\%$
FrPiProd_N	nucleon fates - pion production	$\pm 20\%$
MFP_pi	mean free path for pions	$\pm 20\%$
FrCEx_pi	pion fates - charge exchange	$\pm 50\%$
FrElas_pi	pion fates - elastic	$\pm 10\%$
Frinel_pi	pion fates - inelastic	$\pm 40\%$
FrAbs_pi	pion fates - absorption	$\pm 30\%$
FrPiProd_pi	pion fates - pion production	$\pm 20\%$
AGKYxF1pi	AGKY hadronization model x_F	$\pm 20\%$
Theta_Delta2Npi	Δ decay angular distribution	on/off
RDecBR1gamma	Res decay branching ratio to gamma	$\pm 50\%$
EFNUCR	Increase/decrease to nuclear size for low energy hadrons(± 0.6 fm).	
FZONE	Change formation time by 50%	
Hadronization_Alt1	Change AGKY model to do a simple phase space decay of hadrons.	

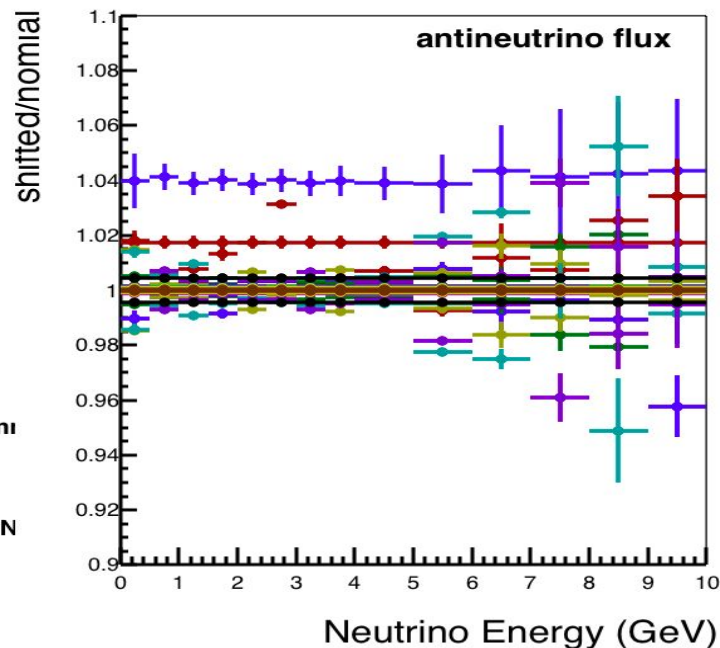
GENIE FSI Uncertainty

- Dominated by mean free path for nucleons
- Similar as MINERvA, $\sim 1\%$ larger



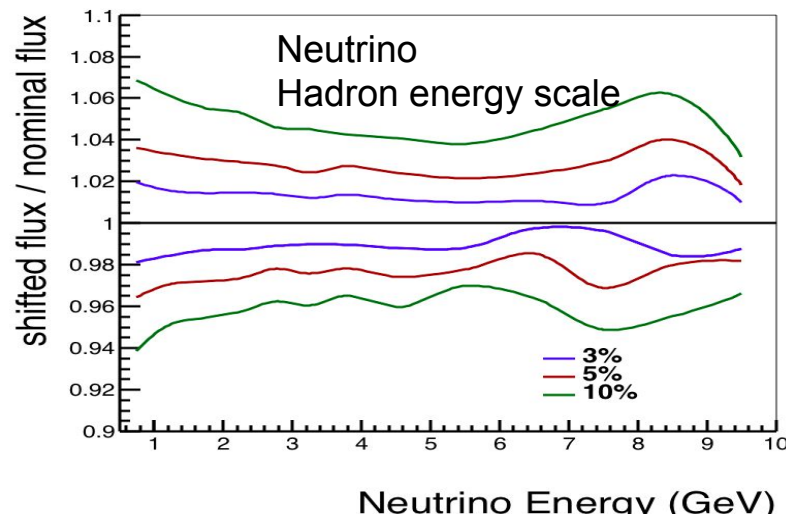
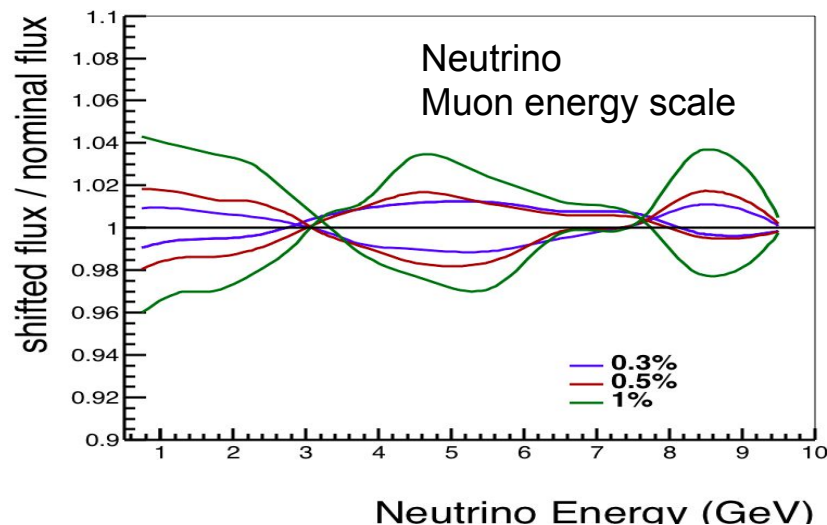
Legend:

- MFP_N
- MFP_pi
- FrAbs_N
- FrAbs_pi
- FrCEX_N
- FrCEX_pi
- FrElas_N
- FrElas_pi
- FrInel_N
- FrInel_pi
- RDecBR1gam1
- FrPiProd_pi
- FrPiProd_N
- Theta_Delta2N



Energy scales (recap)

- Shown at collaboration meeting in August
<https://indico.fnal.gov/event/13293/session/7/contribution/83/material/slides/0.pdf>
- Muon energy scale has larger effect than hadron energy scale
- Assume both are 1% in the following slides

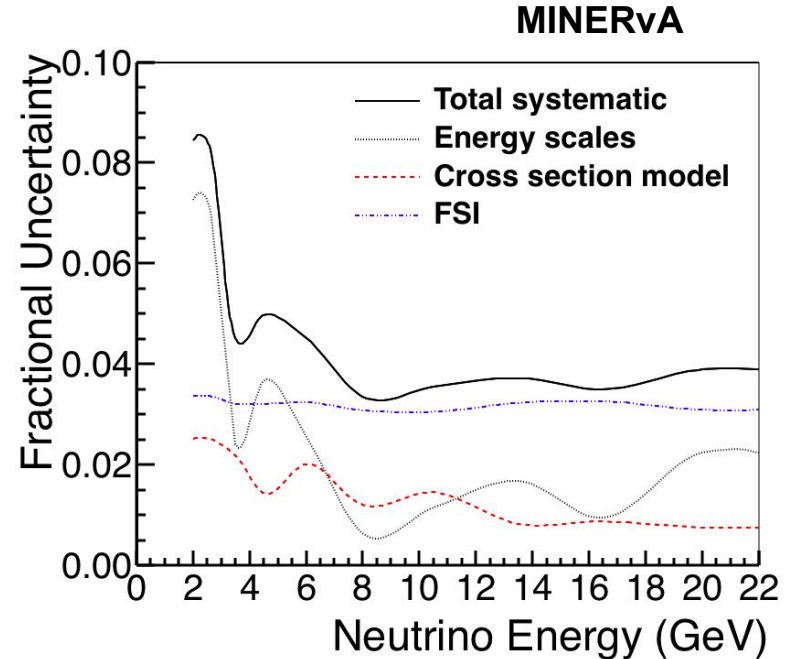
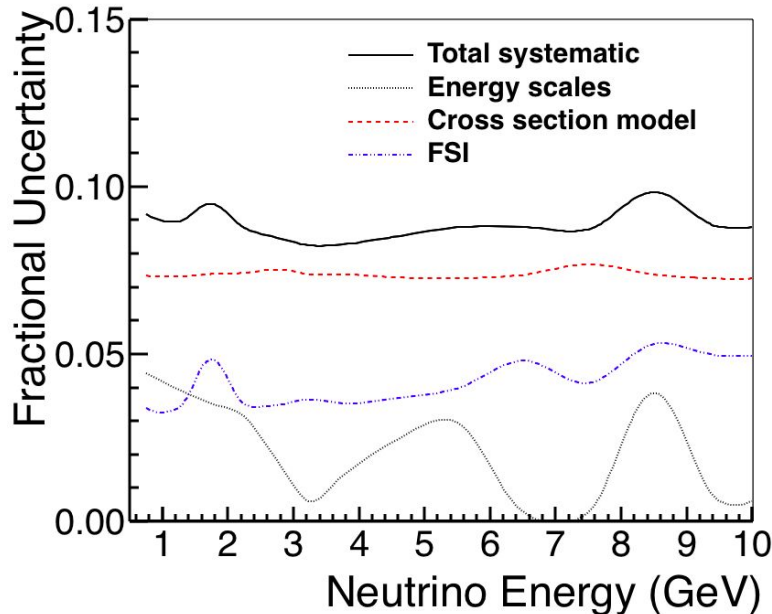


Summary of Flux Uncertainty for Neutrino

- Assume both muon and hadron energy scales to be 1%
- Dominated by cross section model
 - GENIE (MaRES etc.) : level uncertainty propagate from inclusive sample ($\sim 7\%$)

$$\Phi'(E'_\nu) = \frac{F'(E'_\nu) * H'}{S^{\nu < \nu_0}(E_\nu)}$$

$$H' = \frac{N'(10)}{F'(10)} * \frac{S^{\nu < \nu_0}(10)}{\sigma(10)}$$

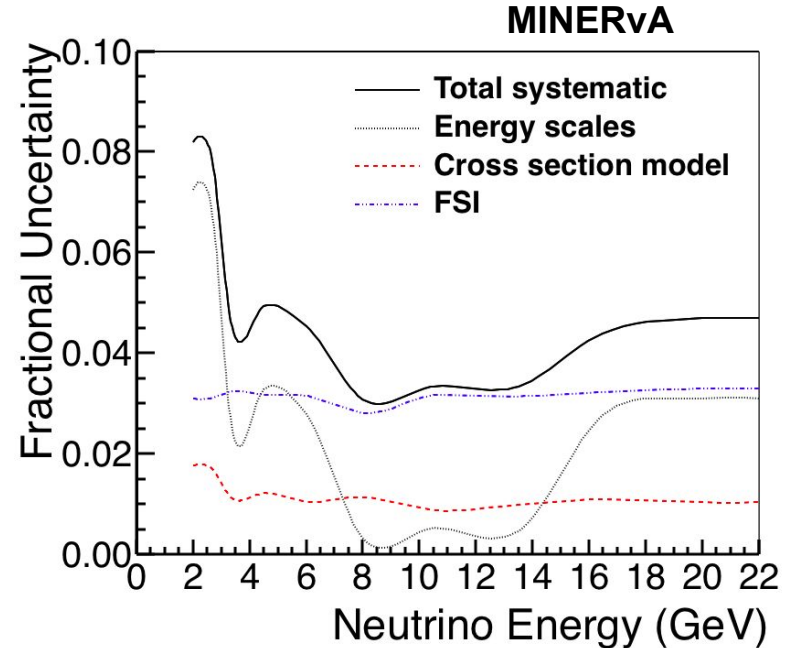
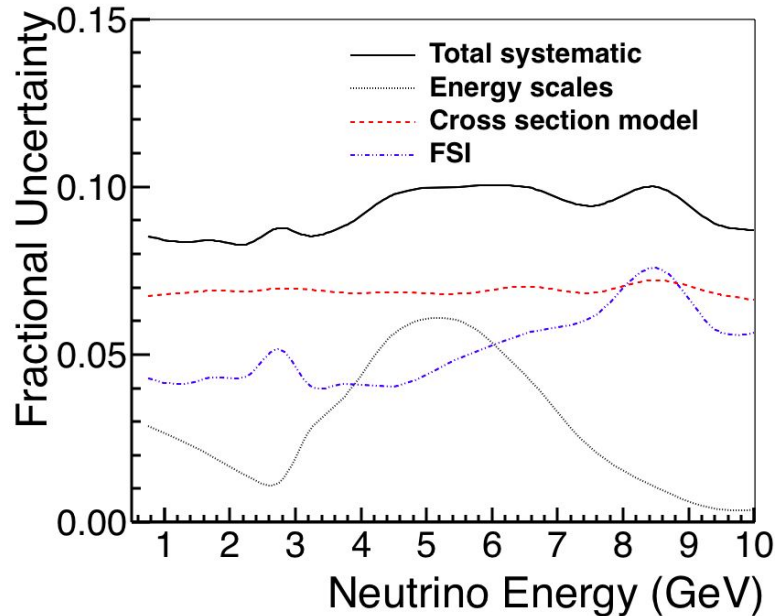


Summary of Flux Uncertainty for Antineutrino

- Assume both muon and hadron energy scales to be 1%
- Dominated by cross section model
 - GENIE (MaRES etc.) : level uncertainty propagate from inclusive sample ($\sim 7\%$)

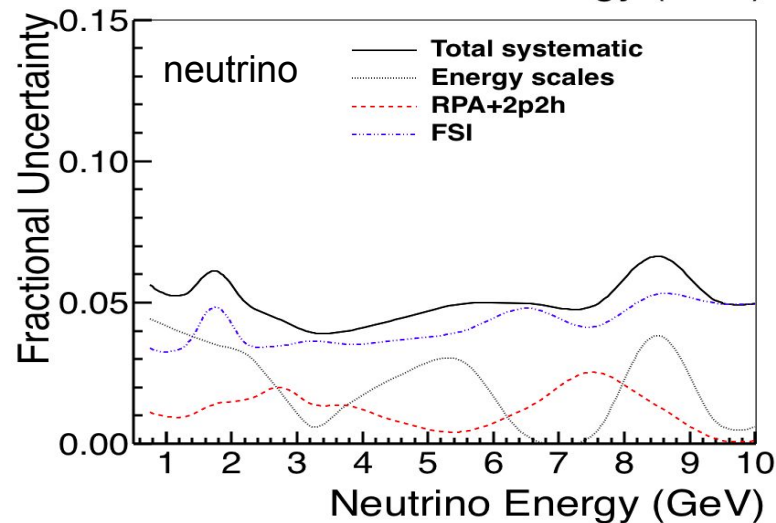
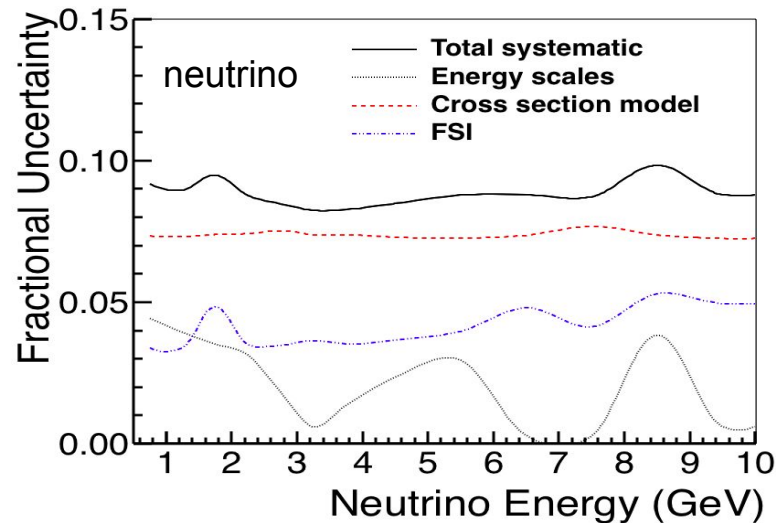
$$\Phi'(E'_\nu) = \frac{F'(E'_\nu) * H'}{S^{\nu < \nu_0}(E_\nu)}$$

$$H' = \frac{N'(10)}{F'(10)} * \frac{S^{\nu < \nu_0}(10)}{\sigma(10)}$$



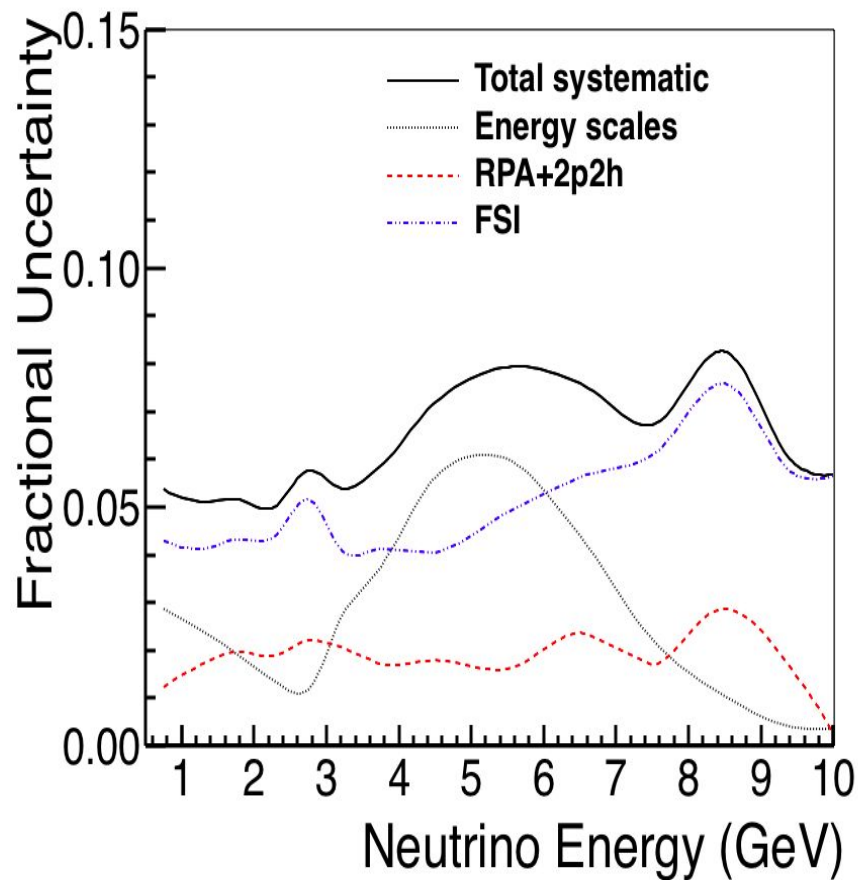
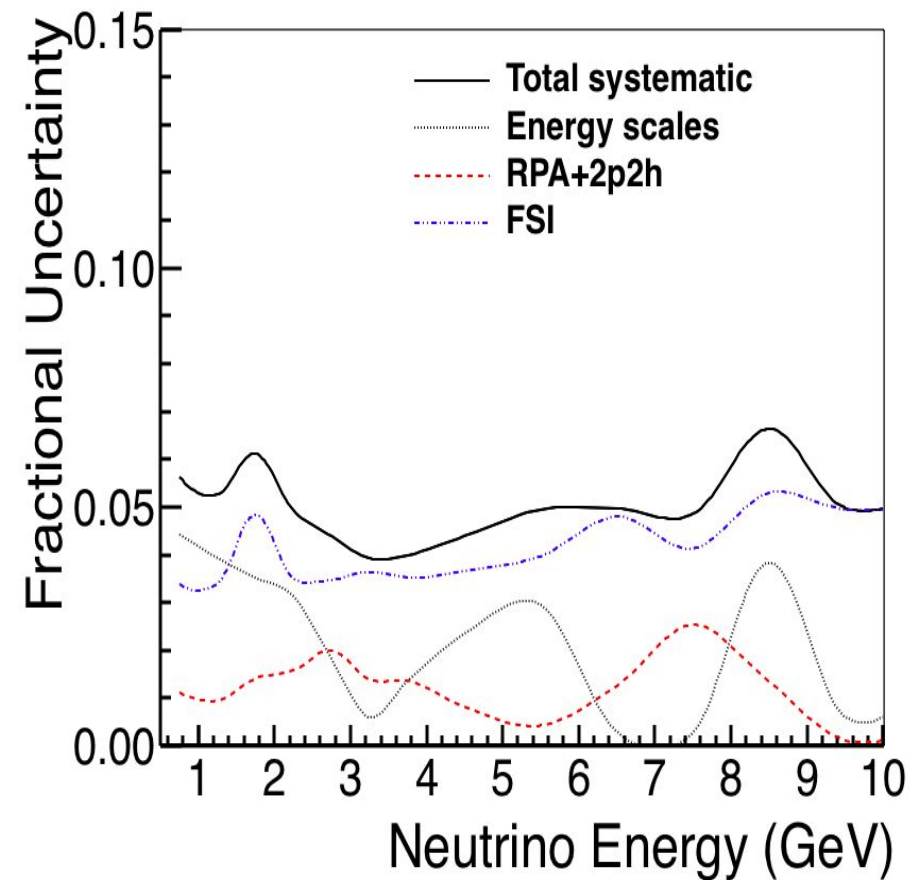
Conclusions

- Estimated low- ν flux uncertainty
 - Cross section model (GENIE, 2p2h, RPA)
 - GENIE FSI model
 - Energy scales
- Assume energy scales of 1% for both muon and hadron, we obtain total uncertainty of $\sim 10\%$ which is dominated by GENIE cross section model uncertainty (largest is MaRES)
- To improve
 - Change the way of external normalization to minimize or remove the level uncertainty coming from inclusive sample (GENIE model)
 - Better understanding of MaRES
 - Better understanding of GENIE FSI model



Backup

Remove GENIE Cross Section Model Uncertainty



Side Study: Effect of Neutron / FSI on Flux

- GENIE FSI model affect neutron number, which has large effect on flux shape
- Inclusive and flux samples w/ and /o FSI or Neutron K.E.
- With FSI, neutron makes $\sim 40\%$ flux shape difference (blue)
- Without FSI, much flat flux (green)

