

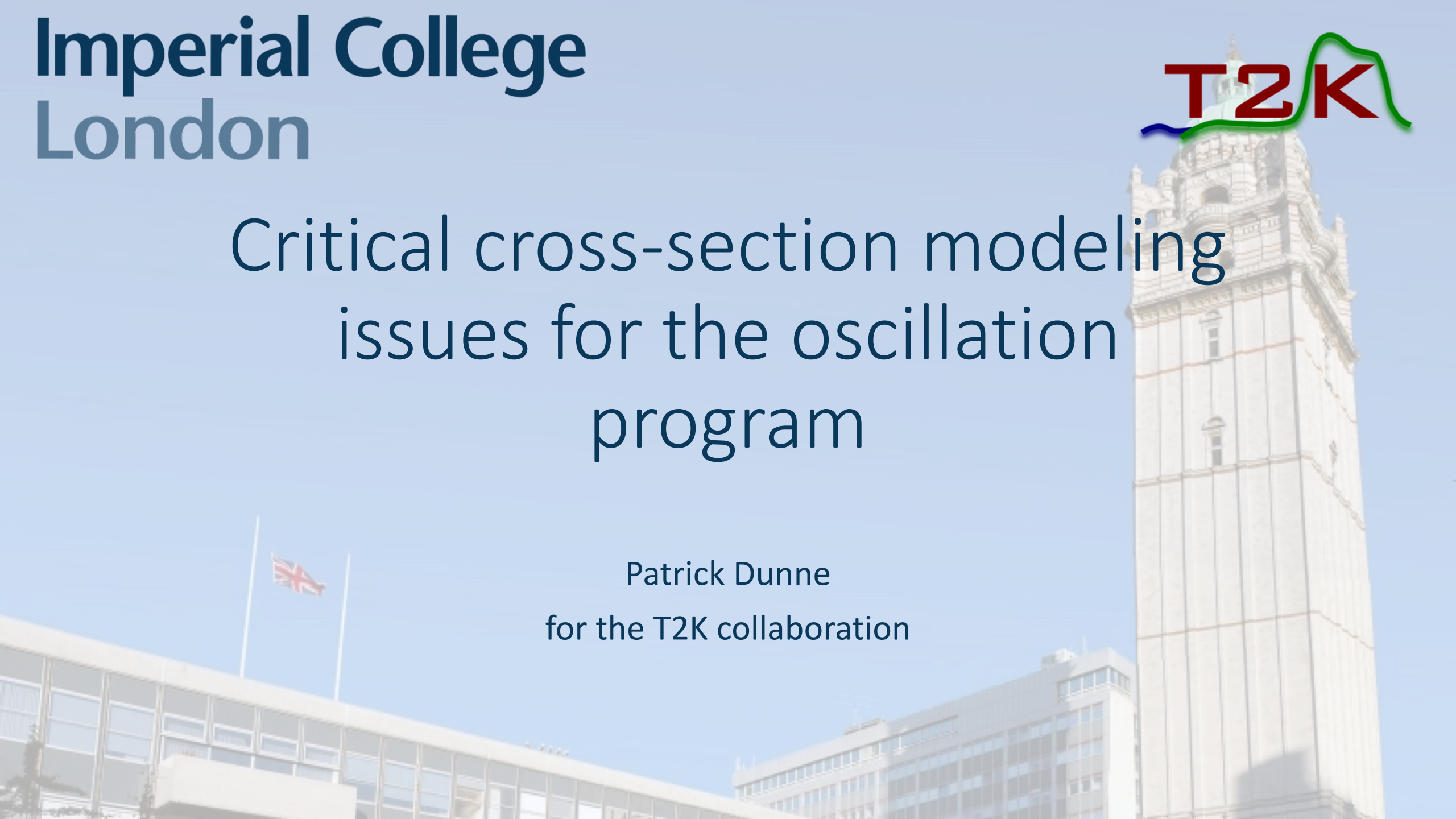
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T2K



Critical cross-section modeling
issues for the oscillation
program

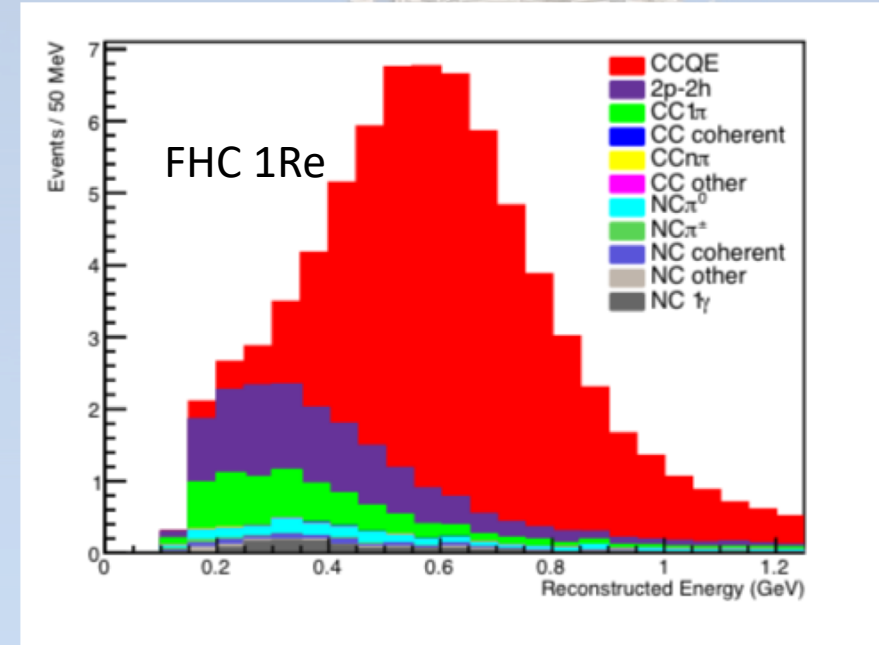
Patrick Dunne
for the T2K collaboration



Outline

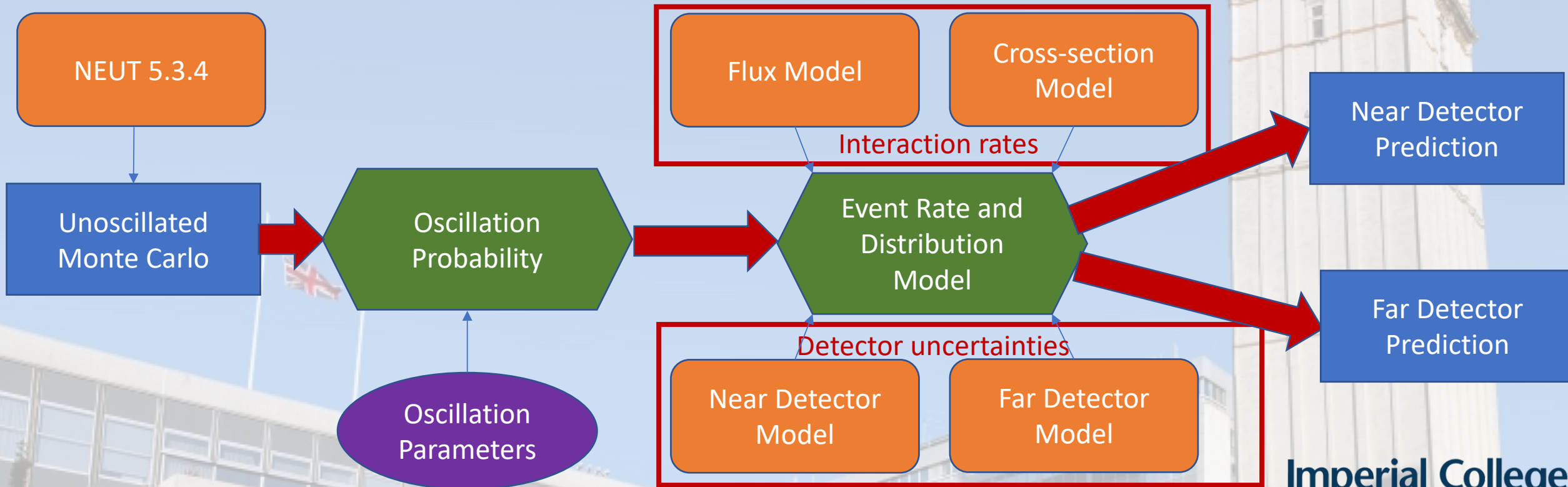
- How do cross-sections enter oscillation analyses
- Simulated data method – How do we check our model?
- Which interaction modes do we have concerns about?
- What can we do about the concerns in the future?

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Where do cross-sections enter analysis

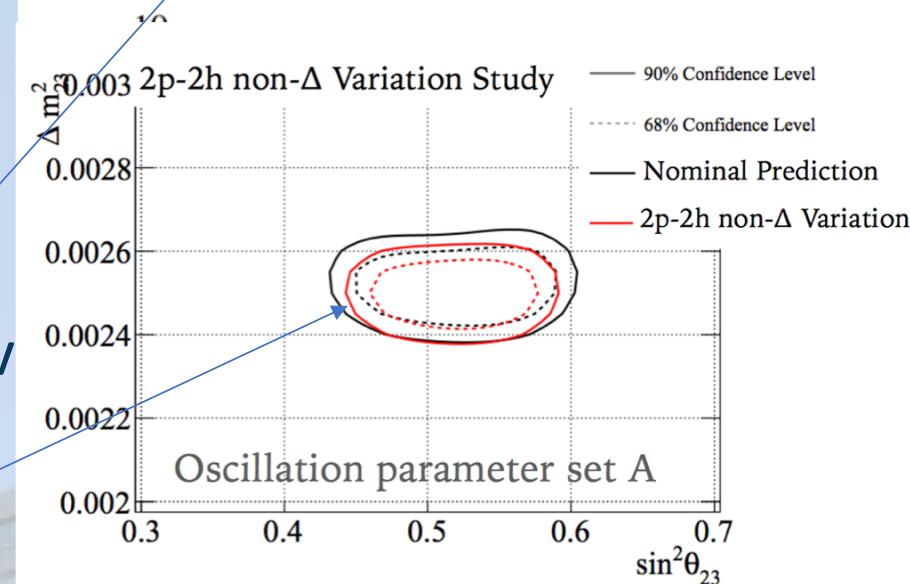
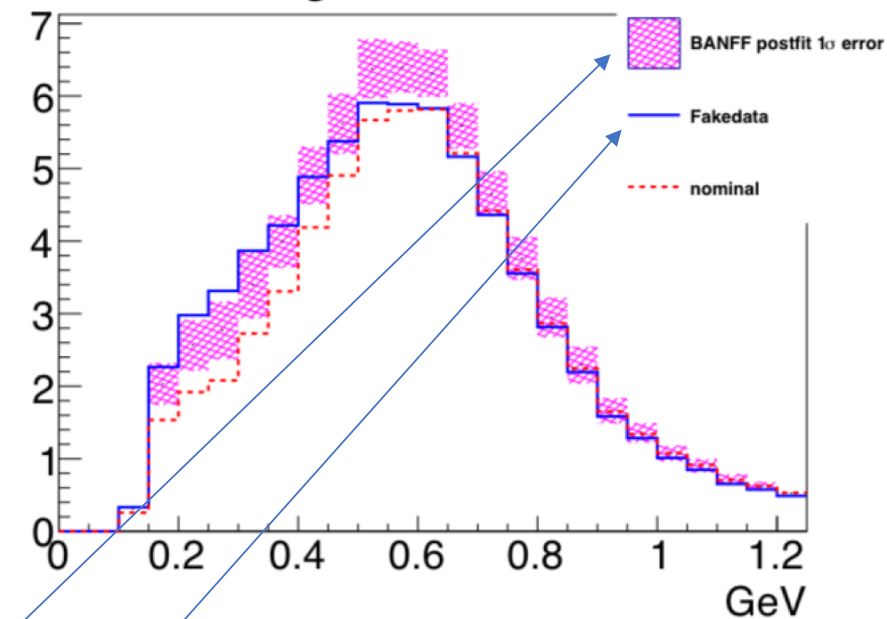
- Apply oscillation effects to Monte Carlo as a function of true E_ν
- **Construct model to predict event rates and distributions at near and far detectors**
- Need to ensure experiment can constrain non-oscillation elements of model
- Important to allow enough uncertainty to mitigate bias in case of incorrect model choice



Simulated data method

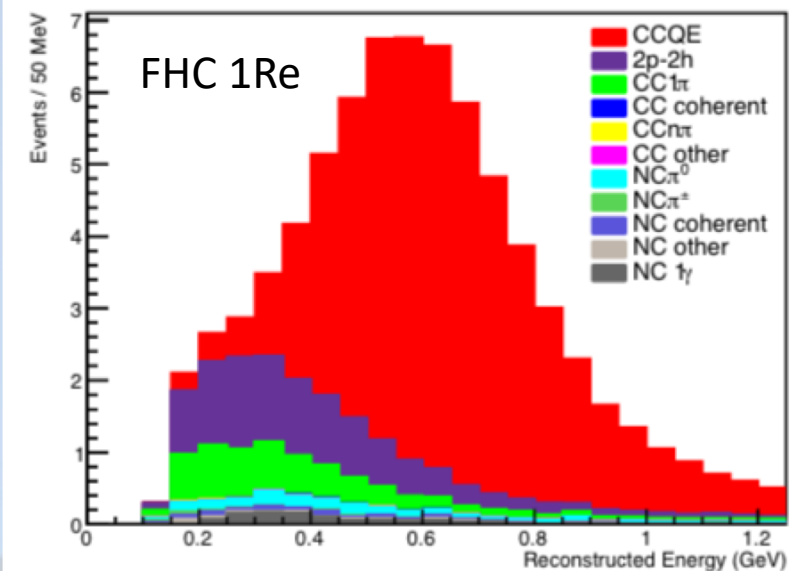
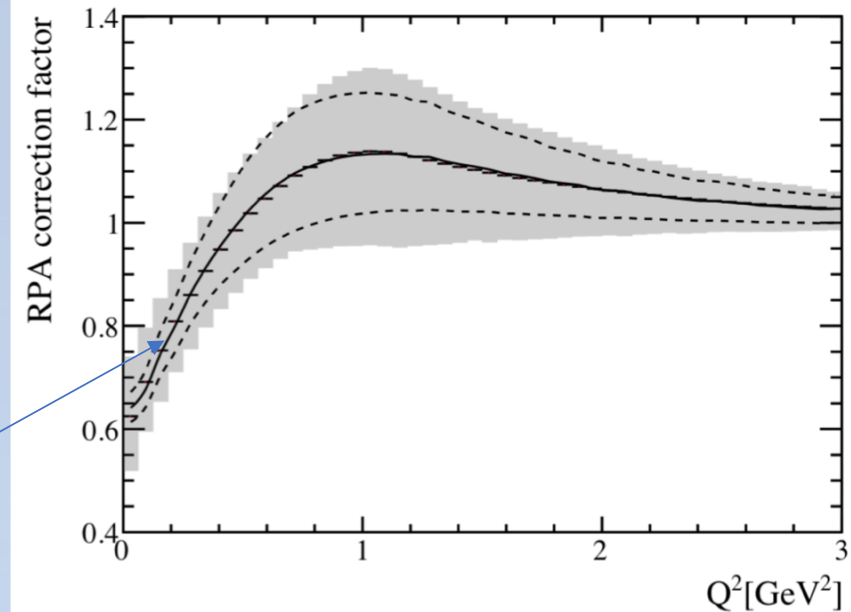
- Check robustness of results to neutrino interaction model by using our model to fit “simulated data”
- Simulated data are generated in two ways
 1. ‘Data-driven’: Inflate one interaction mode to account for differences between current model prediction and existing data
 2. Model choices: generate data using other models implemented in generator but not used in oscillation analysis and refit
- Fit simulated ND data, propagate constraint to SK
- Fit SK simulated data using ND constrained xsec model
- Compare fit to simulated data to nominal model Asimov
- If getting the interaction model wrong leads to significantly different constraints: further investigation

PDF to generate nue events



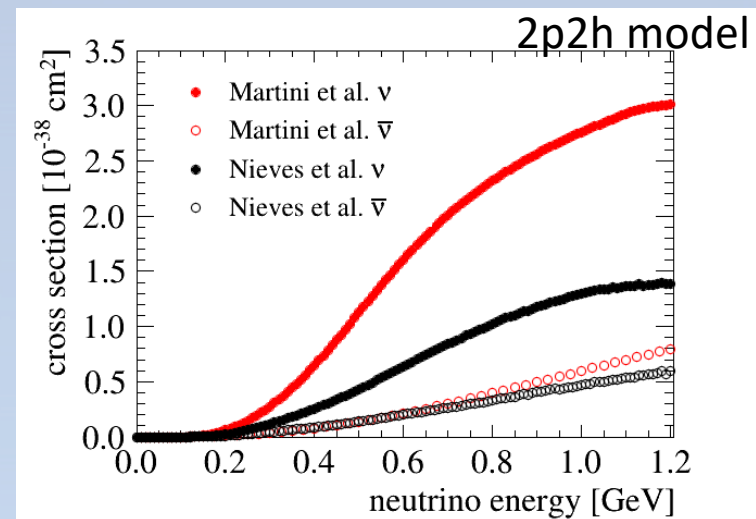
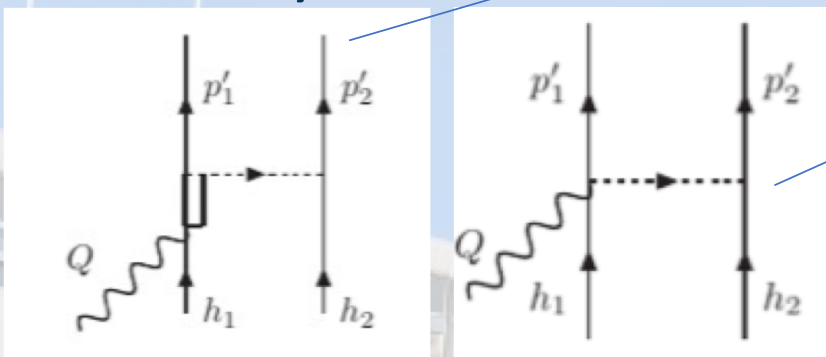
T2K Cross-section Model

- Use Neut 5.3.4
- Separate CC0pi into 1p1h and 2p2h:
 - 1p1h: Assume relativistic fermi gas plus Nieves et al RPA
 - Use effective parametrisation of uncertainty (BeRPA)
 - 2p2h: Assume Nieves et al model
- CC1pi:
 - Generate Rein-Sehgal model for resonant, non-resonant and coherent
 - Reweight to Berger-Sehgal
 - Mostly changes normalisation
- DIS: Modelled using Pythia 5.72

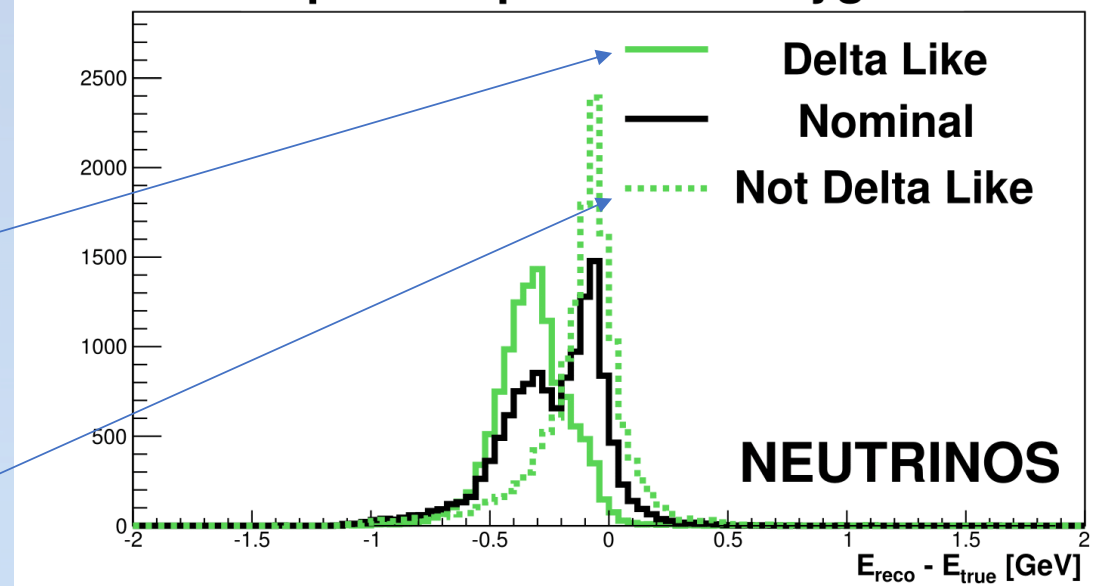


2p2h

- New 2p2h uncertainties for 2017 analysis based on Nieves et al model
- C and O normalisation vary independently
- Shape allowed to vary continuously between totally pionless-delta like and non-pionless-delta like
- Also performed Martini et al 2p2h simulated data study



2p2h Shape Dial on Oxygen

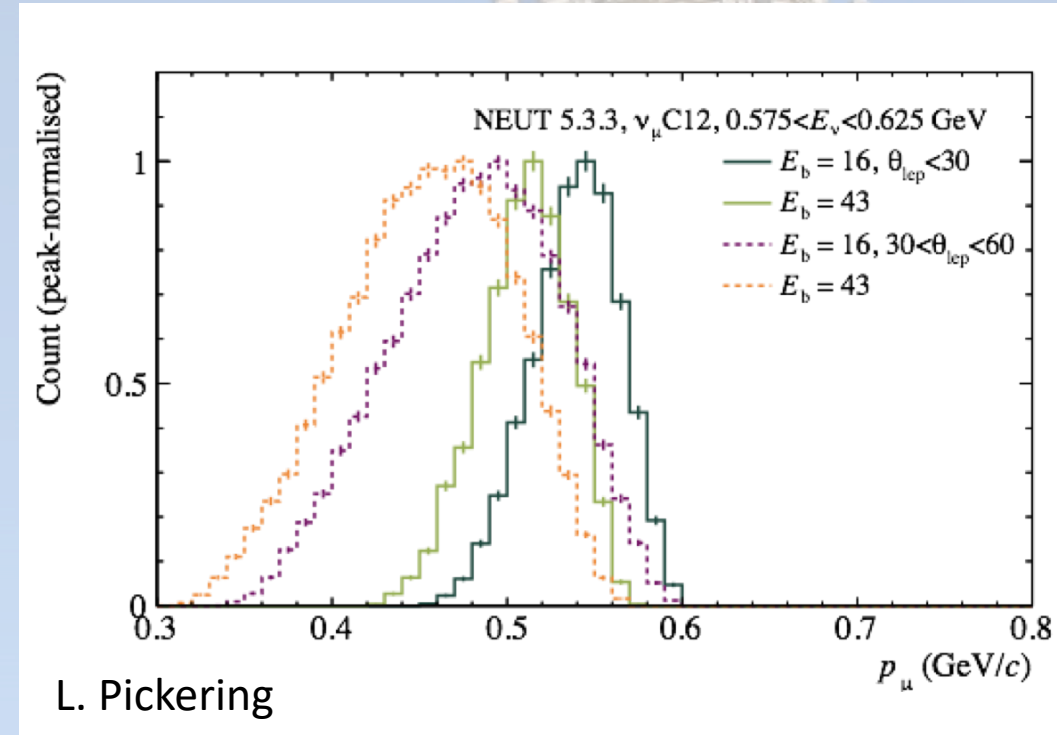


CC0pi issues

Binding Energy like effects (T2K jargon: E_b)

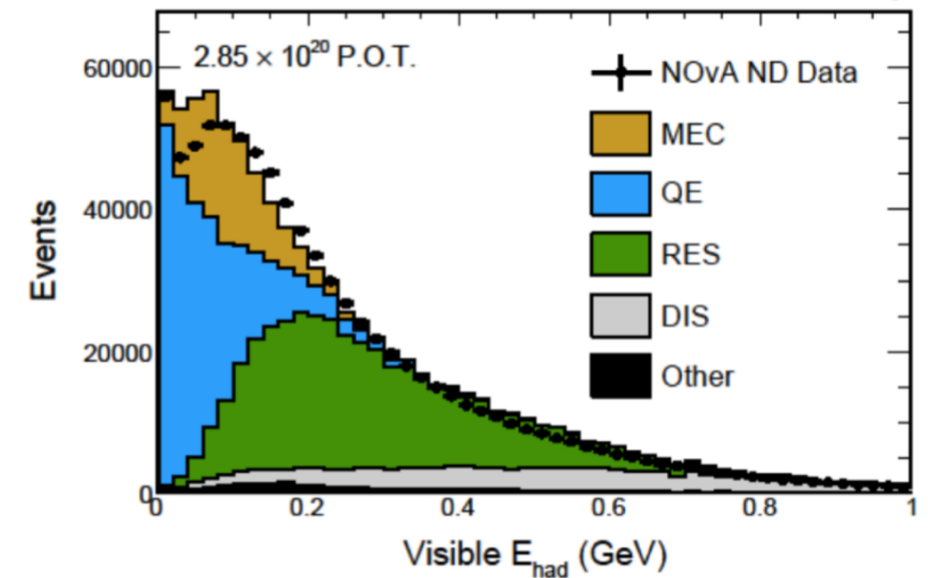


- Most cross-section systematics dealt with using reweighting
- What if the phase space you want to weight up isn't filled in original model?
- Particular problem for E_b as it shifts events up and down in energy
- T2K were unable to add variations for this in time for our analysis release last year
- E_b varied simulated data study is performed
 - Large uncertainty used to cover for several definitions of E_b : (Bodek arXiv:1801.07975)
 - Under study to reduce for future iterations

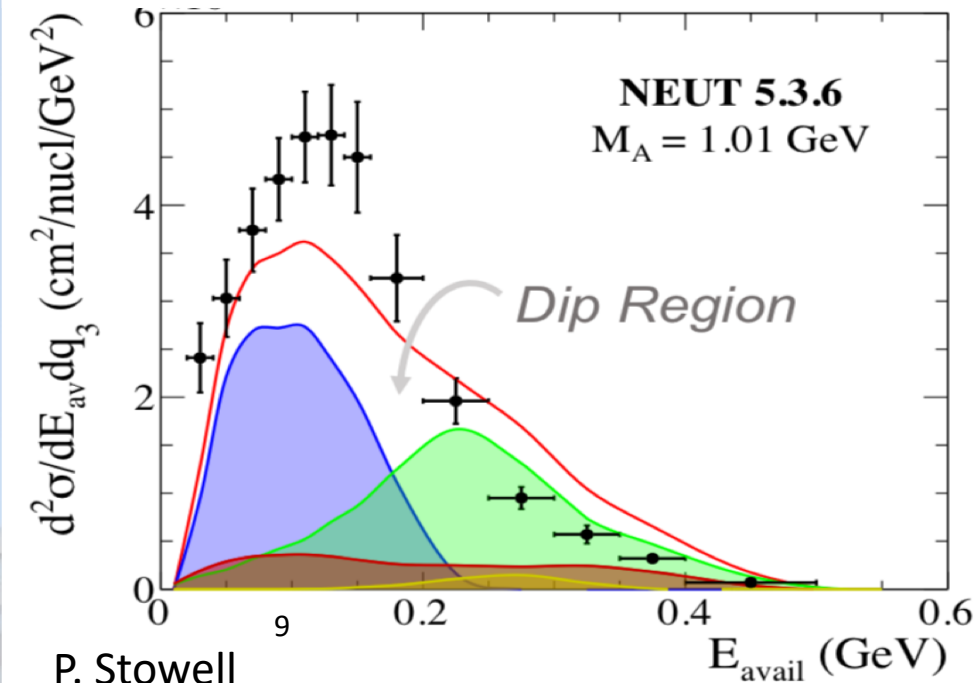


MINERvA

- MINERvA and NOvA see a discrepancy between GENIE and data in the “dip” region between CCQE and Resonant
 - Both compensate with a procedure to scaling up either 1p1h or 2p2h
- Discrepancy also seen in NEUT when compared to MINERvA data
- 1p1h and 2p2h not disambiguated by ND280
- Comparing increase to 1p1h and 2p2h needed at NuMI energy to that needed at T2K energy gives similar amount at low angles but different (lower for T2K) at high angles
- Studies imply energy dependence of discrepancy is different to our model



"Cross-sections and neutrino oscillations in NOvA",
Kirk Bays, NuFact 2017



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Non-CC0pi

CC1pi

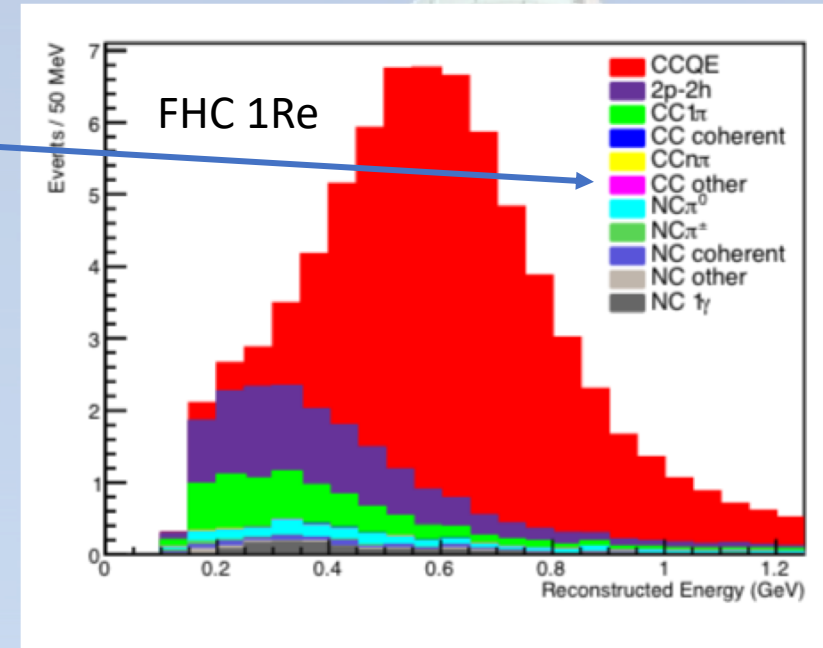


- T2K CC1pi like far detector sample sees more events than expected
 - p-value to see similar fluctuation in one of 5 samples is 12%
- Known deficiencies in CC1pi model: e.g. treatment of multiple resonances
 - New treatment of non- $\Delta(1232)$ resonance part (Minoo model) addresses some of these
 - Simulated data study has been performed
 - Simulated data study reweighted SK pion spectrum to match ND280 data-MC difference
 - See S. Dolan's talk for planned CC1pi measurements partly driven by this

Sample	Predicted Rates at SK				Observed Rates
	$\delta_{CP} = -\pi/2$	$\delta_{CP} = 0$	$\delta_{CP} = \pi/2$	$\delta_{CP} = \pi$	
CCQE 1-Ring e-like ν -mode	73.5	61.5	49.9	62.0	74
CC1pi 1-Ring e-like ν -mode	6.92	6.01	4.87	5.78	15
CCQE 1-Ring e-like $\bar{\nu}$ -mode	7.93	9.04	10.04	8.93	7
CCQE 1-Ring μ -like ν -mode	267.8	267.4	267.7	268.2	240
CCQE 1-Ring μ -like $\bar{\nu}$ -mode	63.1	62.9	63.1	63.1	68

Additional Processes

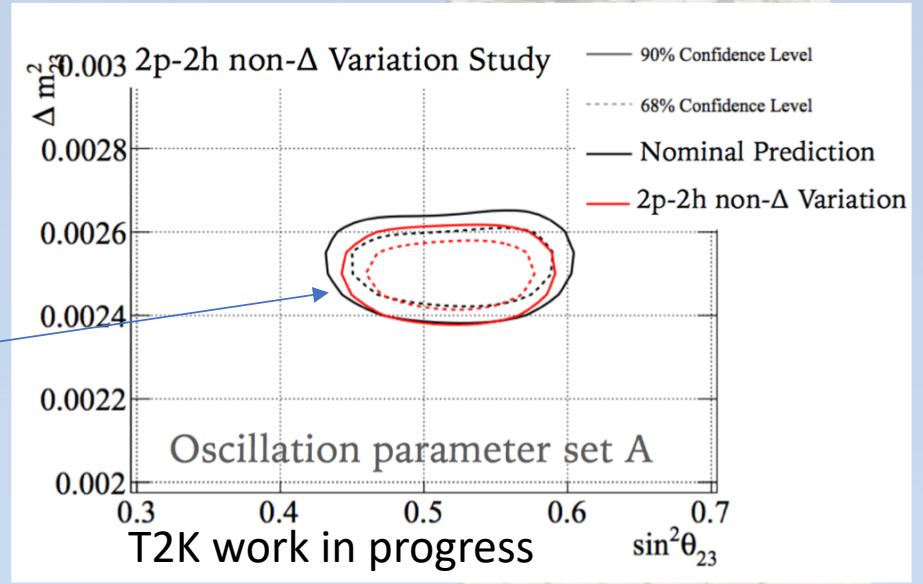
- Composed mainly of DIS and other multipion
 - Subdominant component for T2K
- T2K currently treat this with a single energy dependent normalisation uncertainty: $0.4/E_\nu$
- This parameter is starting to be pulled in fits
- Indicates that it may be time for a more advanced treatment
- T2K is considering:
 - Parton distribution function uncertainties
 - Bodek-Yang corrections
 - Hadron multiplicity uncertainties
 - Revisiting overall normalisation uncertainties
 - Work in progress by T2K not yet finalised



Effects on Analysis

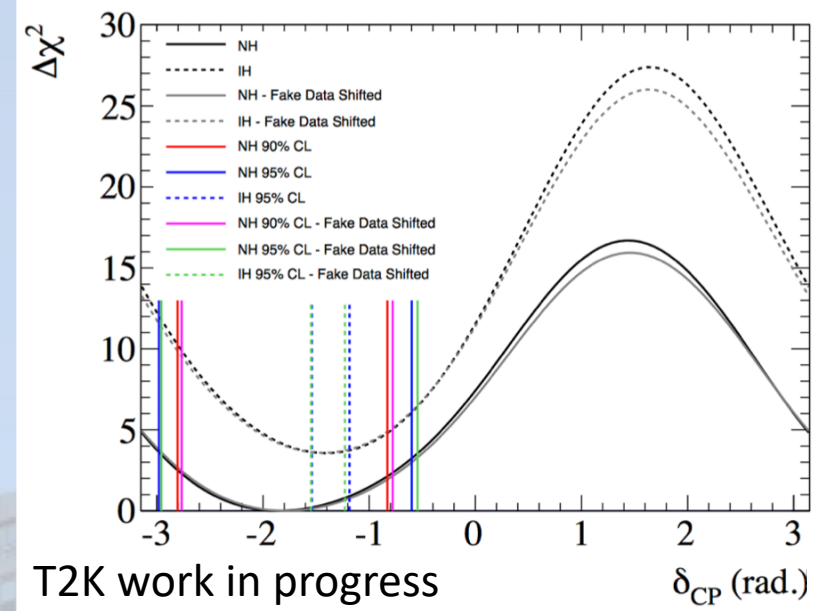
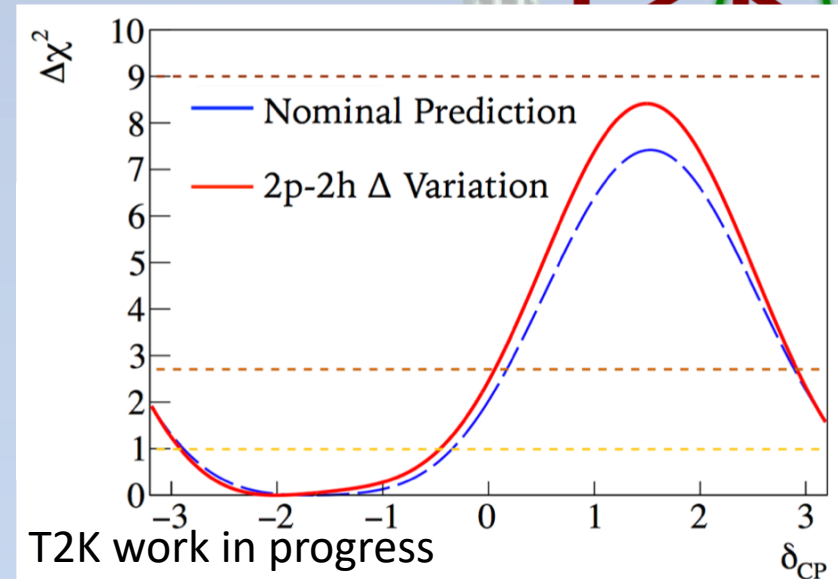
Current status

- Several simulated data studies give significant Δm^2_{32} biases
- Indicates that model doesn't have freedom to replicate reco-true energy mapping for these cases
- It is possible for simulated data to show significant bias on θ_{23} as well e.g.
- Additional systematics being added



Impact on δ_{CP}

- Need to check how changes to $\Delta\chi^2$ from simulated data studies affect statements on δ_{CP}
- Take $\Delta\chi^2$ difference observed in simulated data study (top plot) and shift observed $\Delta\chi^2$ in data (bottom plot) by that amount
- **Impact on δ_{CP} intervals is small for all simulated data sets**
- **Statement that CP conserving values are excluded at 95% CL is unaffected**



Mitigation plans

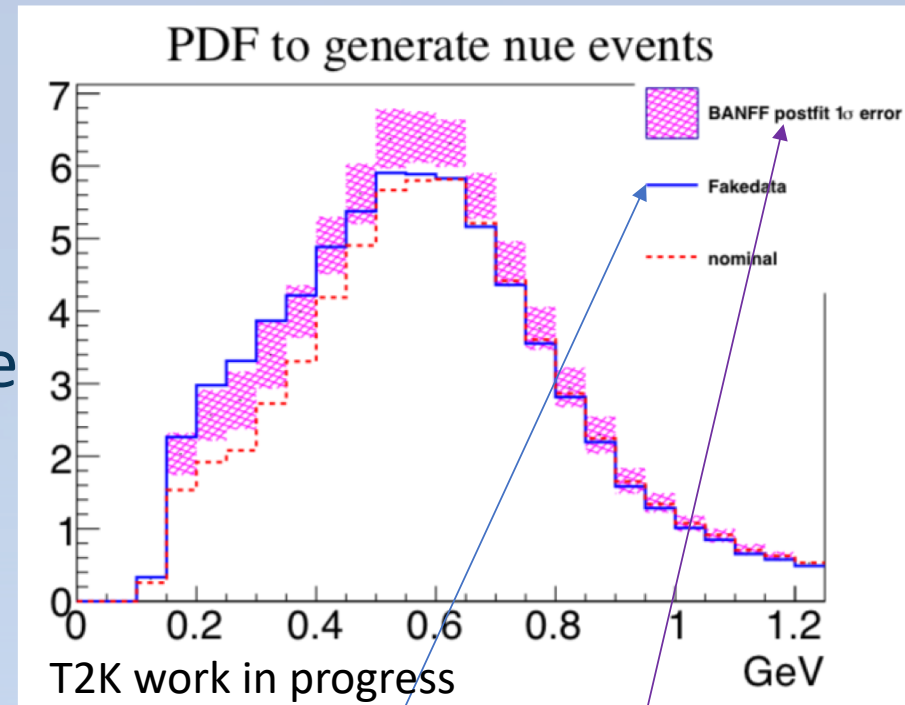
General Method:

- Biases caused by inability of model to accommodate different reco to true interaction rate mapping
- Add parameters to model to allow for that variation
 - Most simulated data sets cover known model deficiencies so variations well motivated
- In many cases, e.g. Eb, cannot currently make full theory based variation
- Add freedom to move event weights linearly from 1 to:

Number of events in bin at SK in SK simulated data

Number of events in SK bin predicted by model when fit to ND280 simulated data

- Approximates the missing freedom of the model



Mitigation plans

- Method on previous slide could be applied generically to a simulated data set
- Additionally in the case of Δm^2_{32} Gaussian smearing of post-fit contours can be done as the parameter is approximately Gaussian
 - Width chosen to be quadrature sum of biases seen in independent simulated data studies

Final sensitivity coming soon!

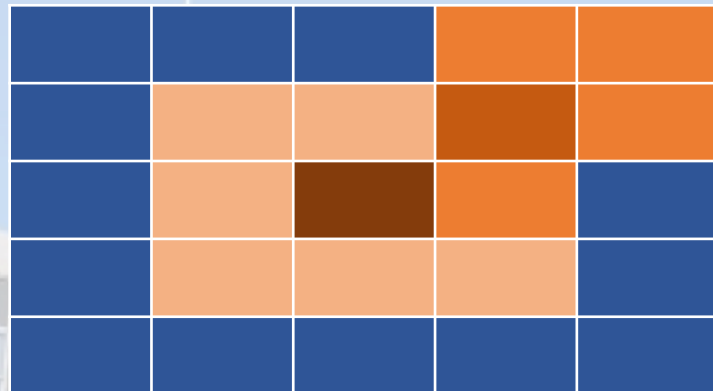
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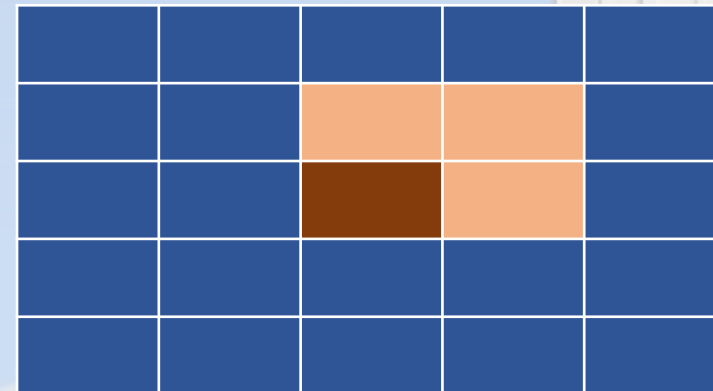
Future

What can we do in future?

- Improve interaction model: better Eb treatment planned for 2019
- A lot of issues involve unobserved hadrons: e.g. inferred kinematics (see S. Dolan)
- Several methods to get better measurements:
- Get a lower threshold detector, e.g. ND280 upgrade (see S. Dolan) or HPTPC
 - Low threshold measurements with several hadrons can constrain high threshold experiments where only highest momentum hadron is seen
- Do novel things with the one we've got, e.g. Vertex activity, Gas/wall analyses



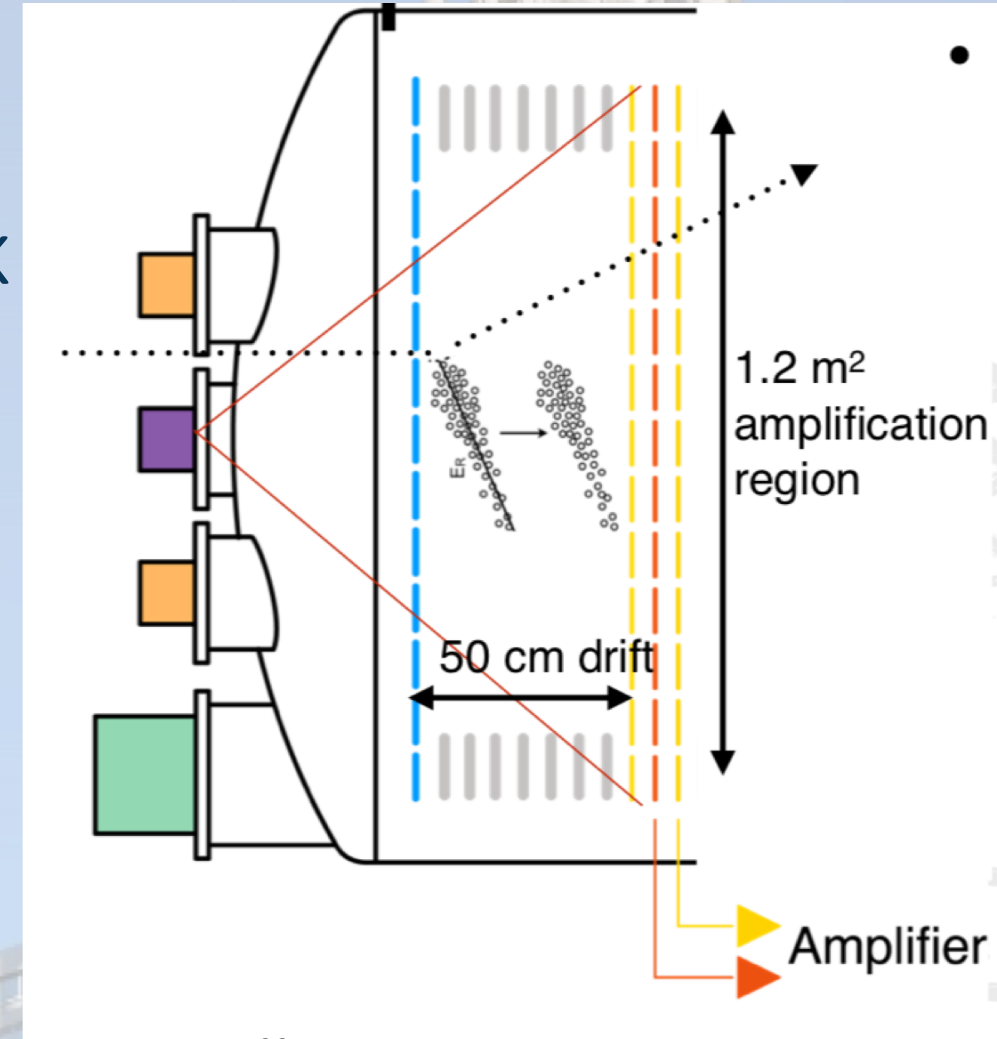
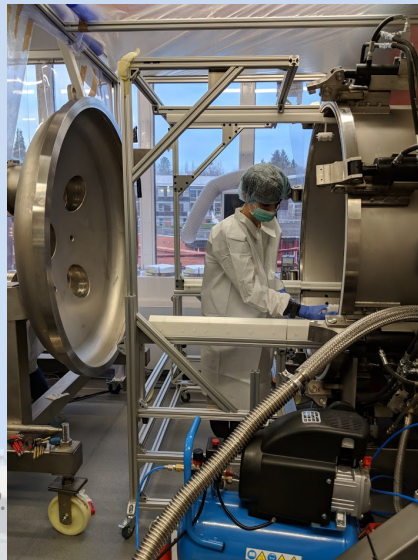
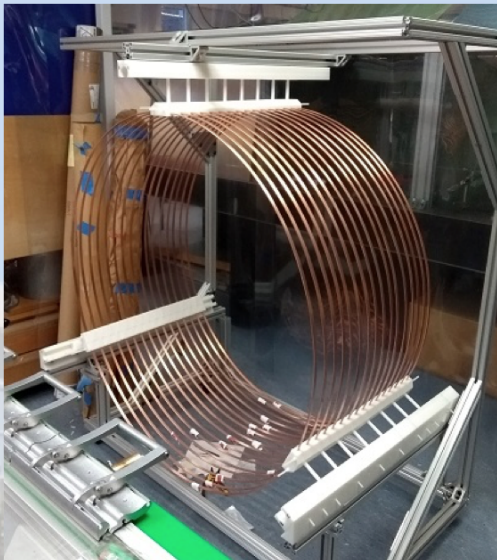
More vertex activity implies more below threshold hadrons



HPTPC



- High pressure gas TPC combines low threshold and acceptable mass
 - Proton momentum threshold ~ 50 MeV
- Can also switch between target gases
- Optically read out prototype being built in the UK
 - Design tested before on DMTPC experiment:
DOI: [10.1063/1.3700603](https://doi.org/10.1063/1.3700603)
 - Beam test due in August: CERN-SPSC-2017-030



Summary



- We know our model is far from perfect in several areas
 - CC0pi: Inferred kinematics, MINERvA/NOvA discrepancy, theory (Eb)
 - CC1pi: Known deficiencies, improvements expected soon (Minoo model)
 - Other CC: Small contribution with simplistic treatment, will be reviewed
- We try to assess whether this matters using simulated data
- We have a procedure to add an 'effective' uncertainty for problematic simulated data studies
- Better solution is to find ways to incorporate theory driven uncertainties in the analysis

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Backup

List of all xsec parameters



CC0pi Inferred Kinematics



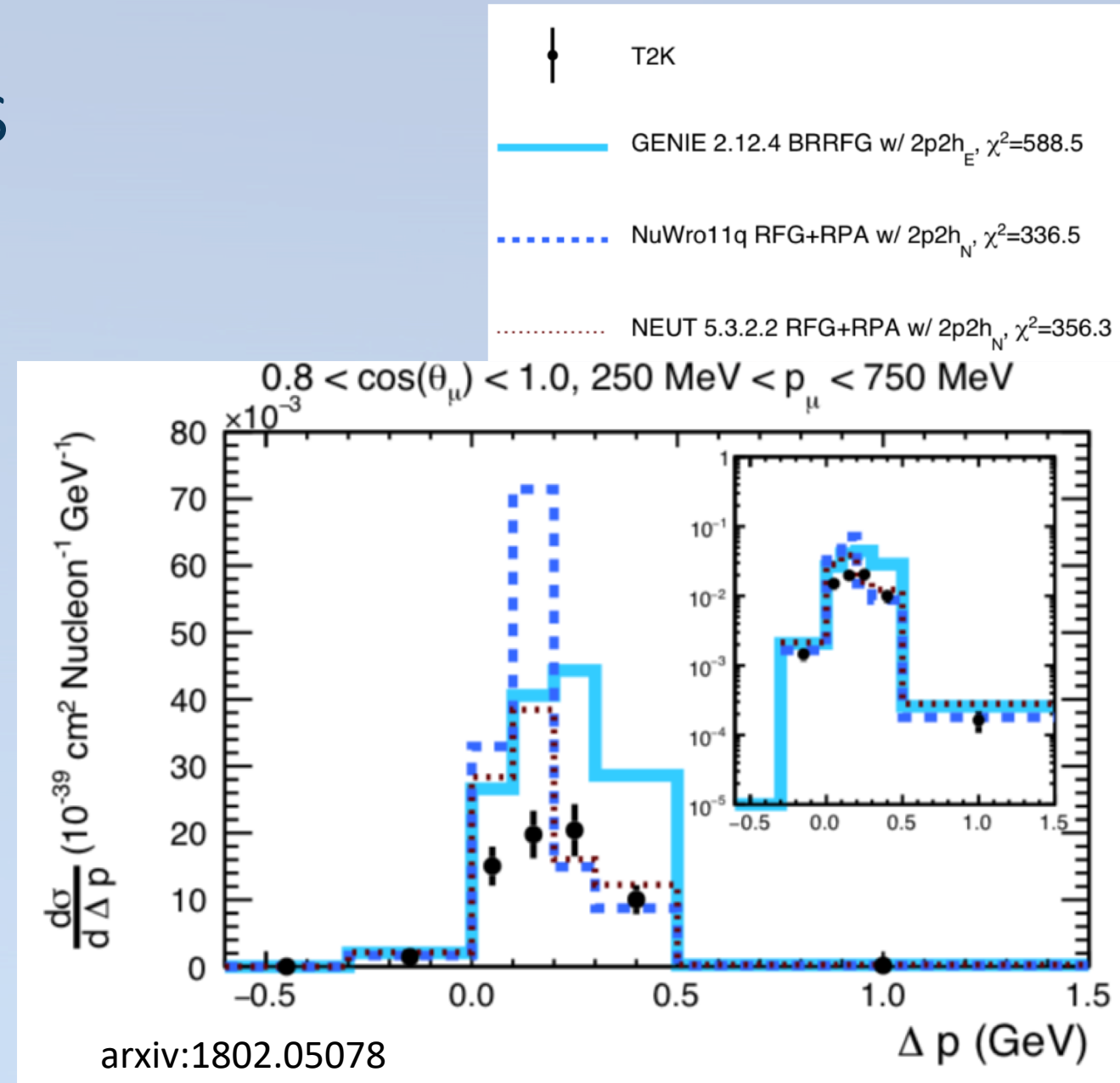
- Kinematic energy reconstruction assumes interaction mode and stationary initial nucleon
- System fully specified from lepton kinematics

$$E_\nu = \frac{m_p^2 - m_\mu^2 + 2E_\mu(m_n - E_b) - (m_n - E_b)^2}{2[(m_n - E_b) - E_\mu + p_\mu \cos\theta_\mu]}$$
$$E_p^{inferred} = E_\nu - E_\mu + m_p$$
$$\vec{p}_p^{inferred} = (-p_\mu^x, -p_\mu^y, -p_\mu^z + E_\nu)$$

- If you identify a proton in the event you can compare inferred and measured energy
- $\Delta p = |p^{\text{measured}}| - |p^{\text{inferred}}|$
- See S. Dolan's talk for more details

CC0pi Inferred Kinematics

- $\Delta p = |p^{\text{measured}}| - |p^{\text{inferred}}|$
- RFG+RPA model shows differences with data
- Present when modelled with both NEUT and GENIE
- Need to check this doesn't bias oscillation results
 - Concerning if underlying 1p1h/2p2h models are wrong
 - ND280 data driven, Benhar spectral function and Martini 2p2h model simulated data test robustness to model variations



PMNS matrix

- Ignoring overall phase, general 3x3 unitary matrix can be broken down into 3 rotation matrices and a complex phase

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{CP}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- Oscillation probability in vacuum given by:

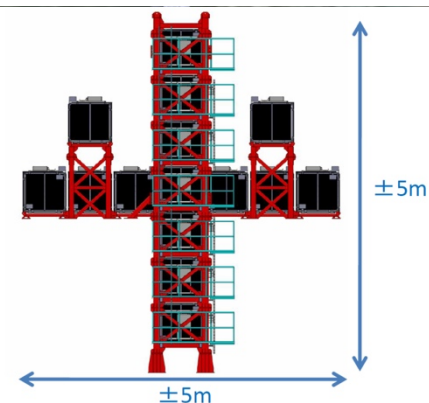
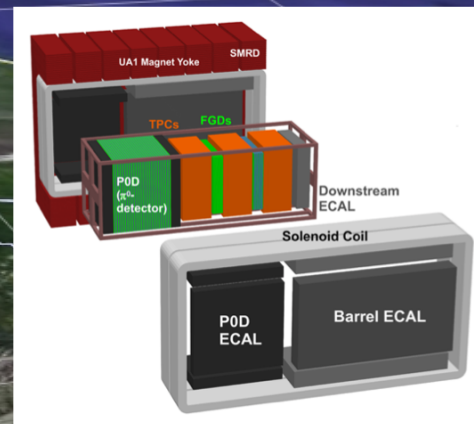
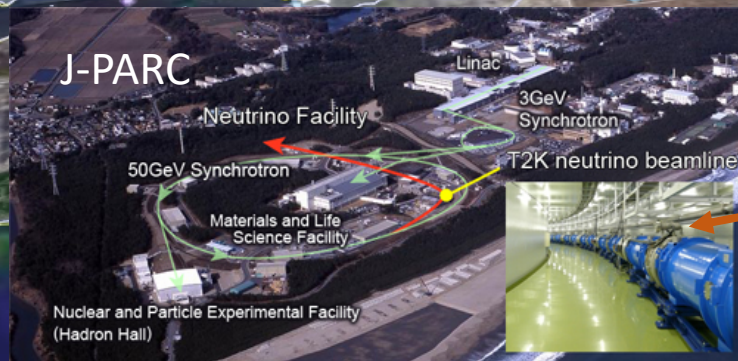
$$P_{\alpha\beta} = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2\left(\Delta m_{ij}^2 \frac{L}{4E}\right) + 2 \sum_{i>j} \text{Im}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2\left(\Delta m_{ij}^2 \frac{L}{4E}\right)$$

- Frequency of oscillation set by squared mass difference
- Relevant distance scale for experiment is L/E
- Amplitude of oscillation decided by mixing angles
- CPT symmetry implies $P(\alpha \rightarrow \beta) = P(\bar{\beta} \rightarrow \bar{\alpha})$
- Non-zero complex phase, δ_{CP} , would lead to CP violation

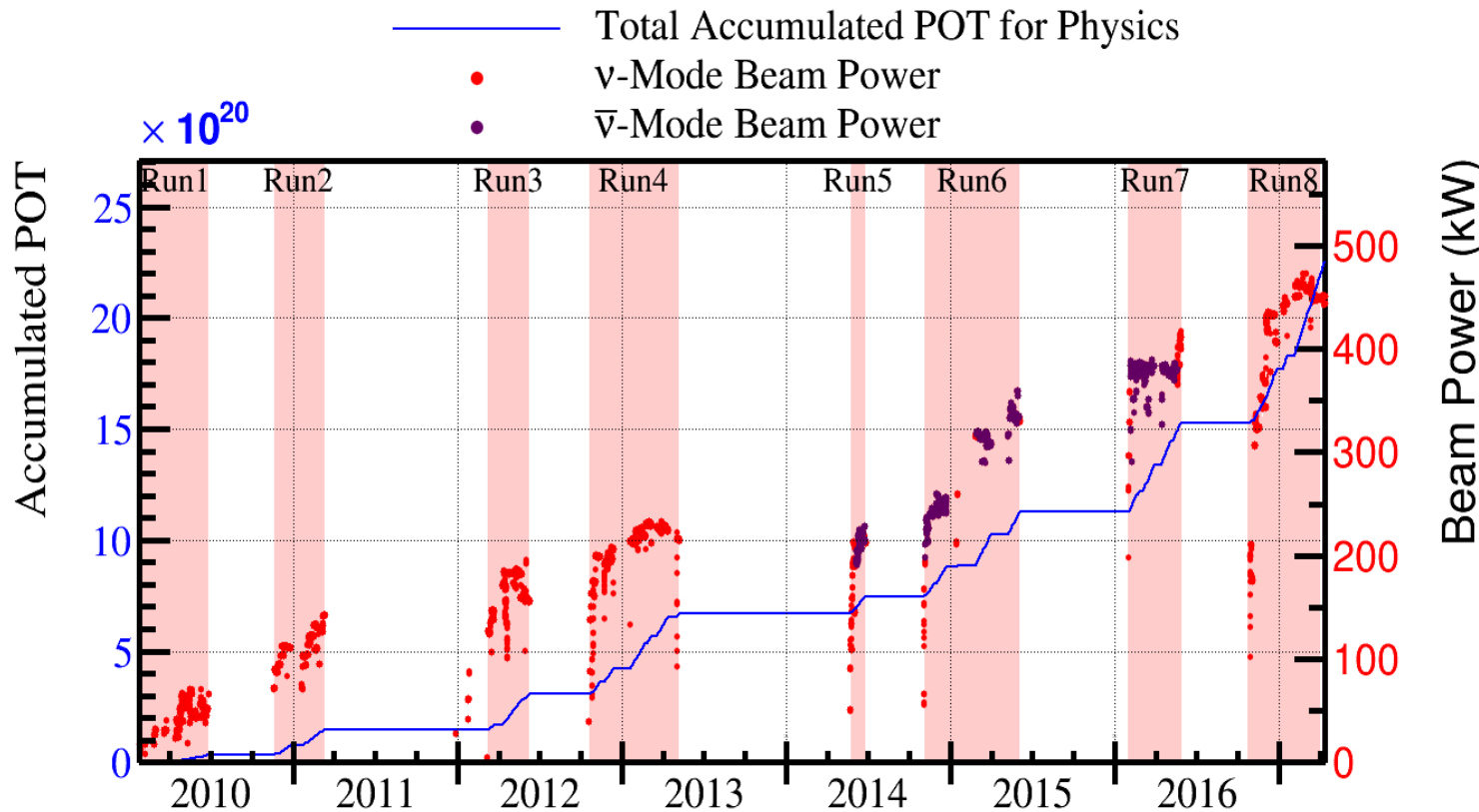
The T2K Experiment



- Muon (anti) neutrino beam generated at J-PARC
- Near detector complex 280m from target measures beam before oscillation
- Beam travels 295 km to 50 kton Super-K detector to be measured after oscillations
- ~500 researchers, 62 institutes, 11 countries

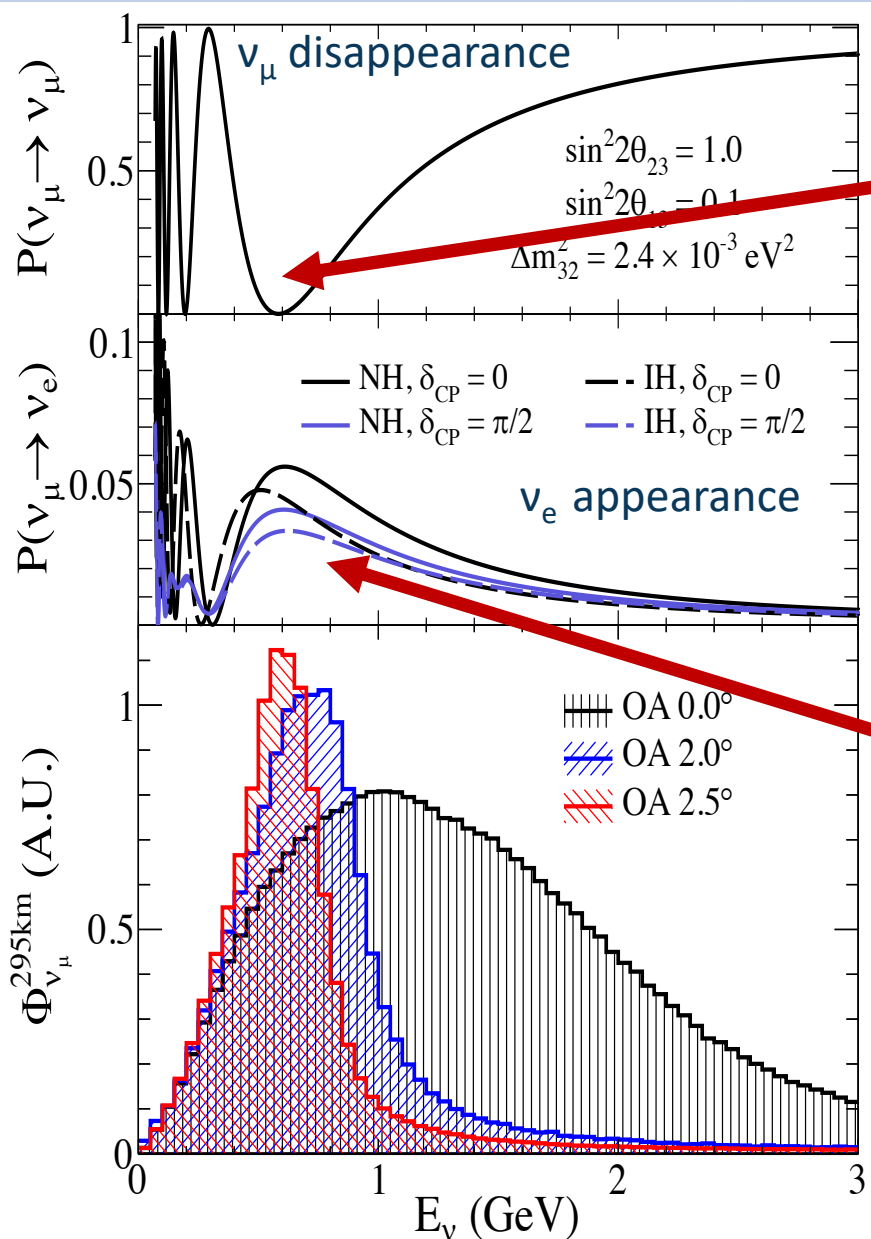


Beam operation



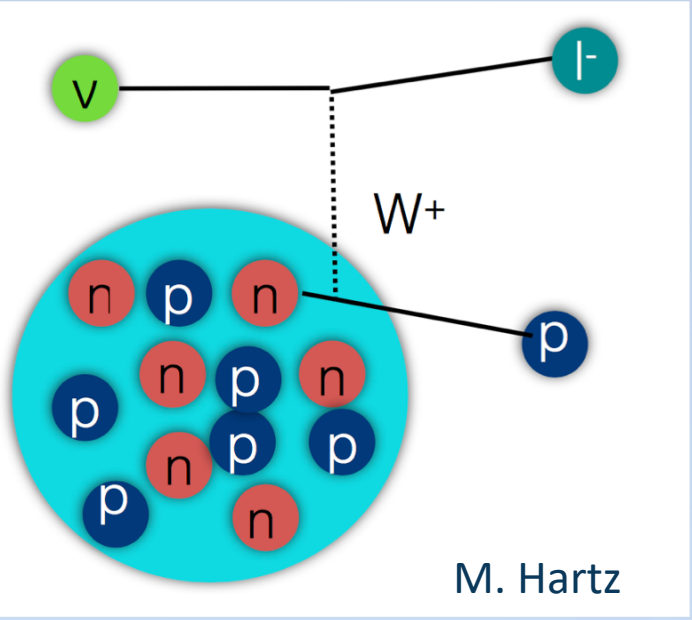
- Accumulated 14.7×10^{20} protons-on-target (POT) in neutrino mode and 7.6×10^{20} POT in antineutrino mode
 - 29% of approved T2K-I POT
- Previous results used 7.5×10^{20} POT ν -mode, 7.5×10^{20} POT $\bar{\nu}$ -mode
 - Phys. Rev. Lett. 118 (2017) no. 15, 151801
- Operated at stable beam power of **470 kW** this year
 - Enabled doubling ν -mode data

Neutrino oscillations at T2K



- Muon (anti)neutrino disappearance
 - Location of dip determined by Δm^2_{23}
 - Depth of dip determined by $\sin^2(2\theta_{23})$
- Electron (anti)neutrino appearance
 - Leading term depends on $\sin^2(\theta_{23}), \sin^2(\theta_{13})$ and Δm^2_{23}
 - Sub-leading dependance on δ_{CP}
 - $\delta_{CP} = \pi/2$: fewer neutrinos, more anti-neutrinos
 - $\delta_{CP} = -\pi/2$: more neutrinos, fewer anti-neutrinos
- Matter effects give dependence on mass hierarchy
- For 295km baseline first oscillation maximum is at 0.6 GeV

Detecting neutrinos



- Use charged-current neutrino-nucleus interactions
- Detect energetic final state lepton
 - Gives kinematic information and flavour ID
- Oscillation effects vary with E_ν
 - Recoil hadrons often below detection threshold and nuclear effects important so hard to reconstruct
- Construct variable as close to true energy as possible

- Assume quasi-elastic scattering from single bound nucleon (CCQE):

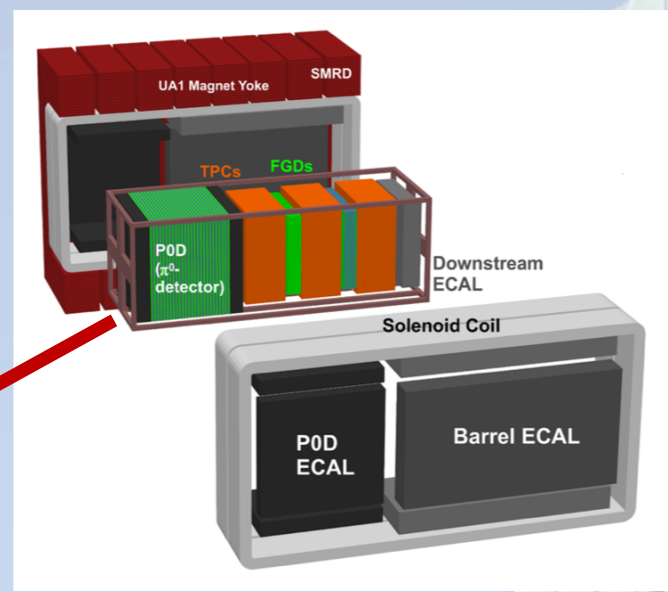
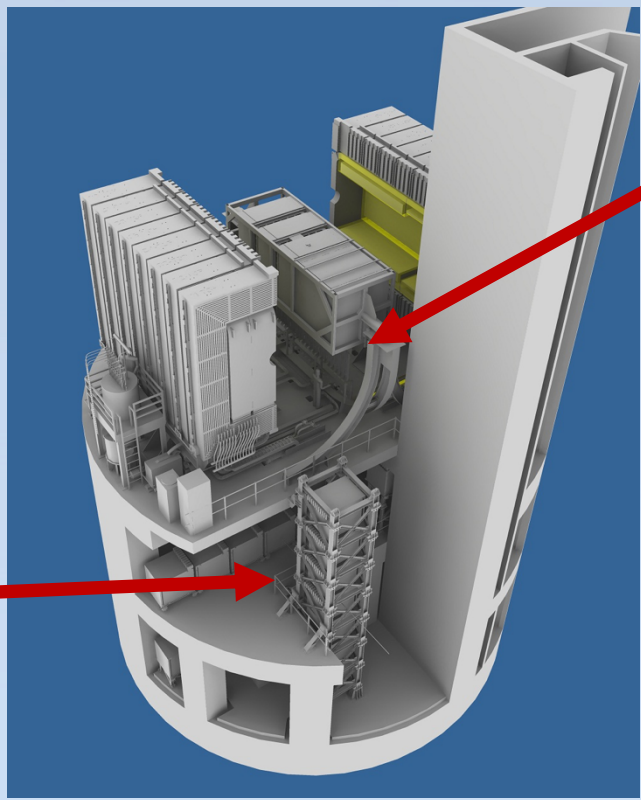
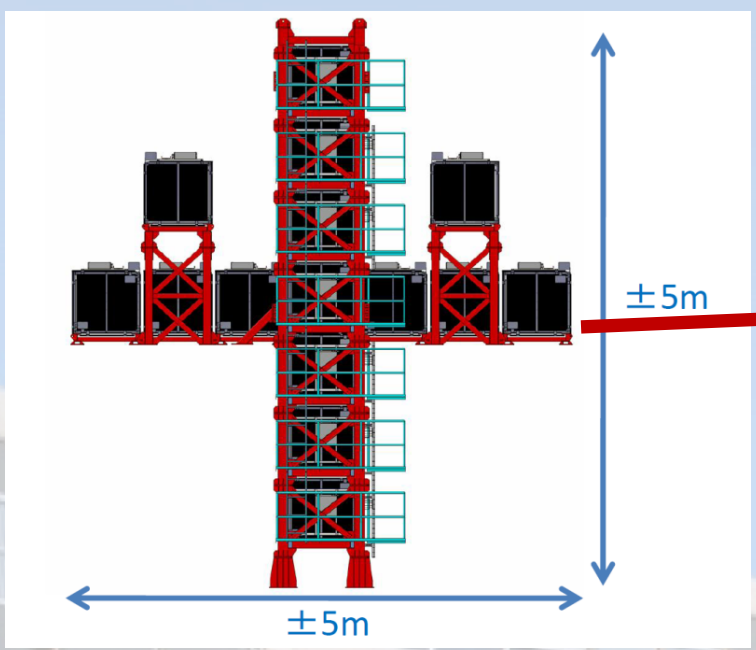
$$E_\nu^{rec} = \frac{m_p^2 - (m_n - E_b)^2 - m_e^2 + 2(m_n - E_b)E_l}{2(m_n - E_b - E_l + p_l \cos\theta_l)}$$

- Only uses **particle masses**, **lepton kinematics** and **nuclear model**

Near detectors

INGRID

- On-axis detector
- Monitors beam direction and constrains flux



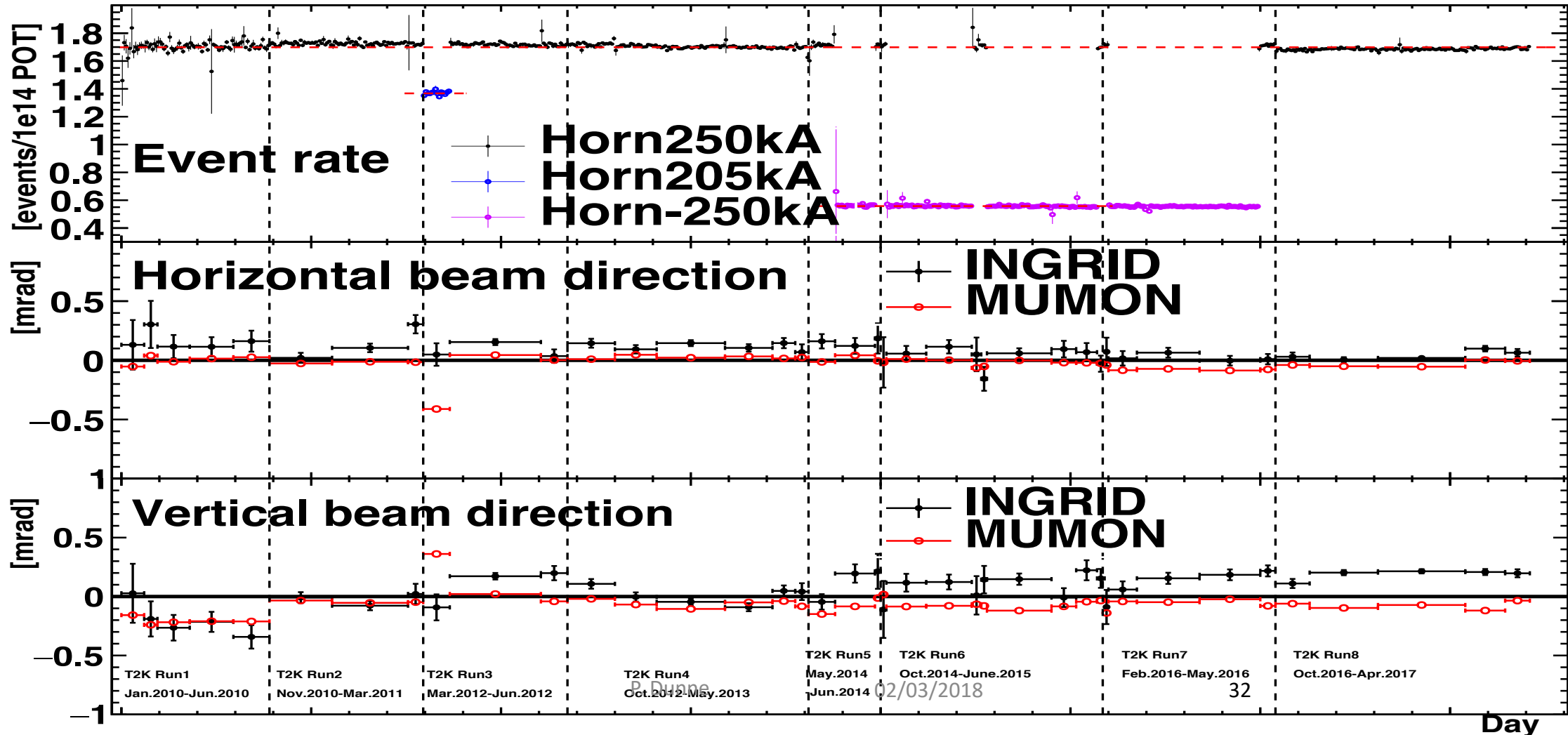
ND280

- 2.5° off-axis (same as Super-K)
- Constrains cross-section and flux uncertainties

INGRID



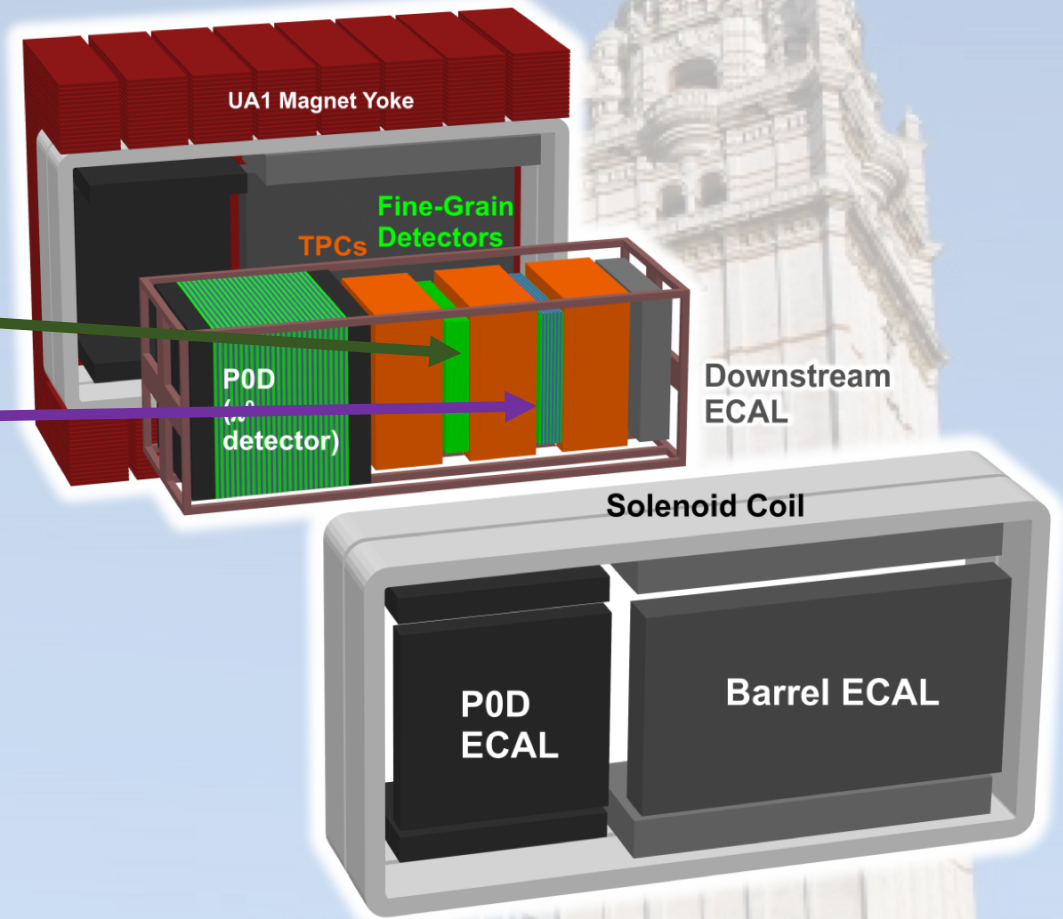
- Design beam direction tolerance 1 mrad



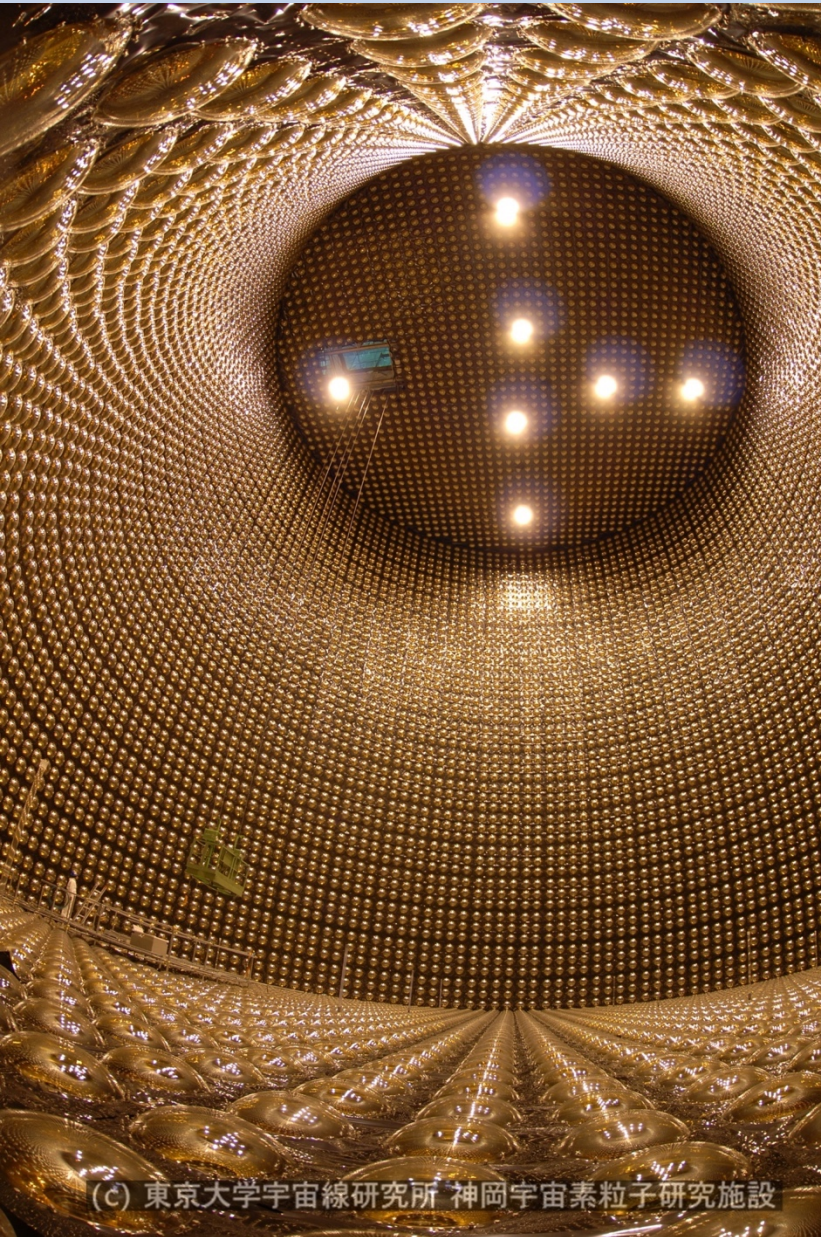
ND280



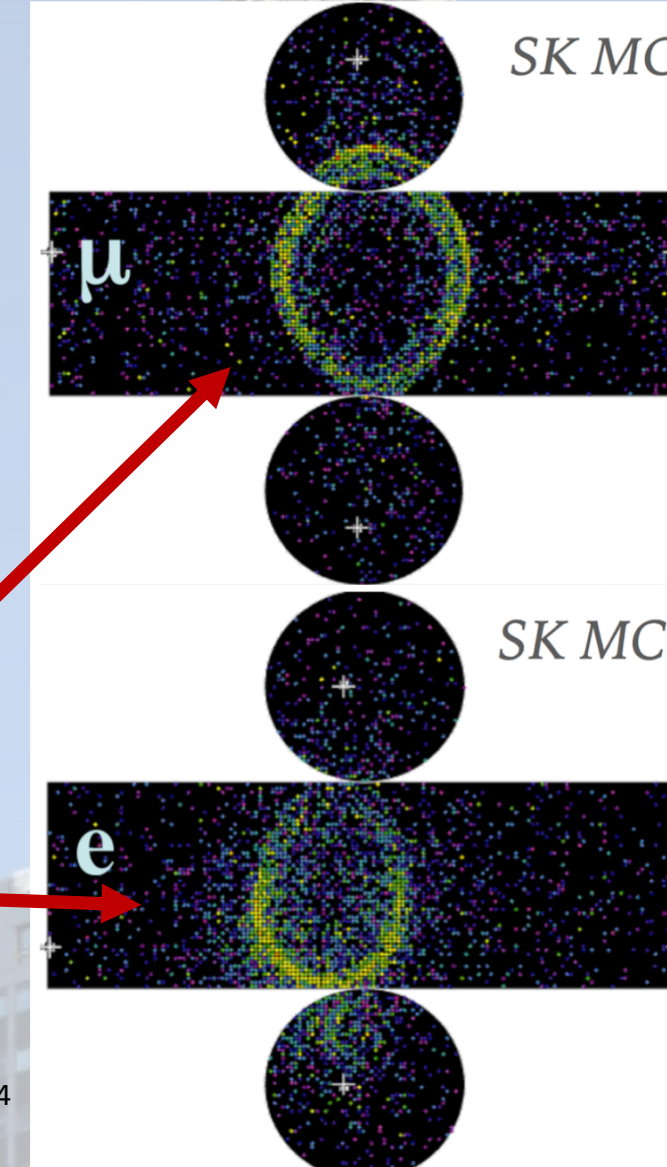
- Measures neutrinos before they oscillate
- Two fine-grained detector (FGD) targets
 - FGD1 – Active carbon target
 - FGD2 – Active carbon and passive water layers (same nucleus as SK)
- **Magnet + three TPCs**
 - Refurbished 0.2T UA1 magnet
 - Particle charge + momentum from curvature
 - Particle ID From dE/dx – 0.2% mis-ID rate



Super-K



- 50 kt water-Cherenkov detector
- 11,000 20" PMT inner detector
 - 40% photo-coverage
- 2,000 8" PMT outer detector
 - Cosmic veto/exiting particles
- Not magnetised
- Particle ID via Cherenkov ring pattern:
 - **Muons** produce **sharp** rings
 - **Electrons** scatter more → **fuzzier** rings



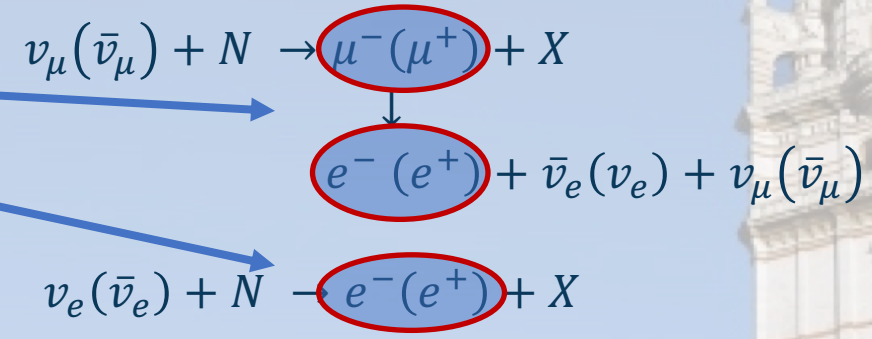
ND280 samples and selection

- ND280 aims to constrain cross-section and flux uncertainties
- Separate samples for **FGD1** and **FGD2**: allows separation of Carbon and Oxygen
- Separate samples by particle content: attempt to isolate interaction modes
- **SK is not magnetised so neutrino contamination of antineutrino beam is important to constrain**

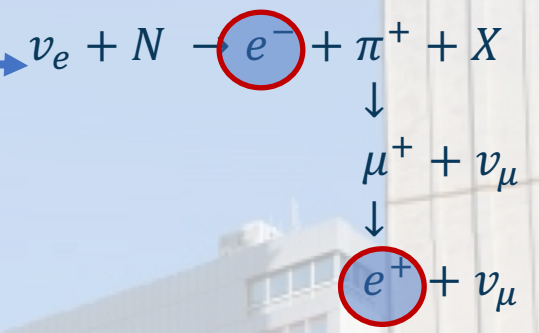
	FGD1			FGD2		
ν events in neutrino mode	CC0pi	CC1pi	CCNpi	CC0pi	CC1pi	CCNpi
$\bar{\nu}$ events in antineutrino mode	CC1track		CCNtrack	CC1track		CCNtrack
ν events in antineutrino mode	CC1track		CCNtrack	CC1track		CCNtrack

SK samples

- Looking for ν_μ disappearance and ν_e appearance
 - Neutrino mode:
 - 1 μ -like ring, ≤ 1 decay electron
 - 1 e-like ring, 0 decay electrons
 - Antineutrino mode:
 - 1 μ -like ring, ≤ 1 decay electron
 - 1 e-like ring, 0 decay electrons
- All four samples target charged-current quasi-elastic (CCQE) interactions

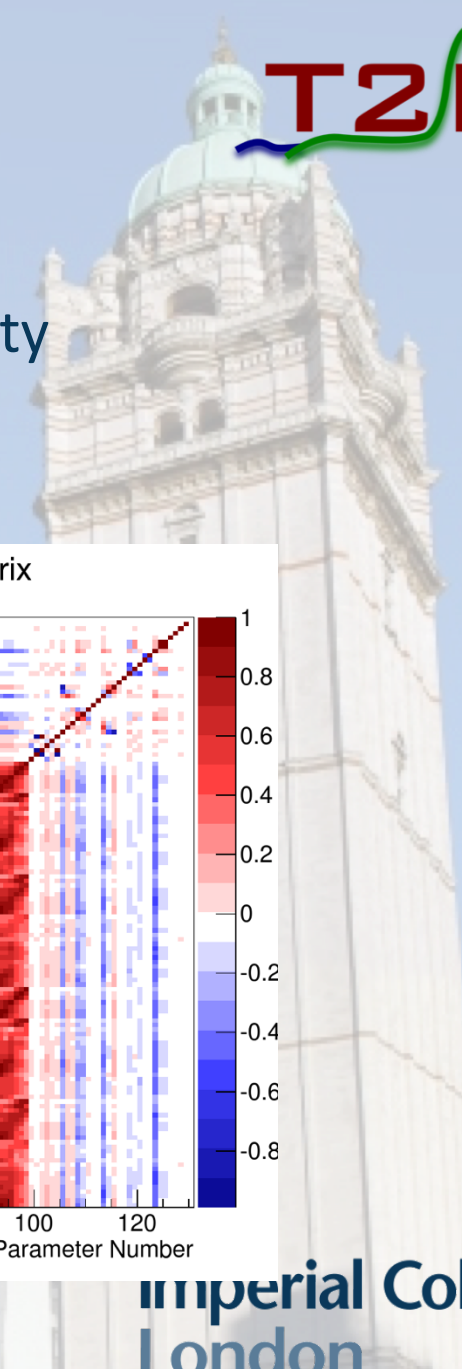


- Recently we also include neutrino mode sample targeting charged-current interactions with an additional pion
 - Neutrino mode: 1 e-like ring, 1 decay electron
 - Reconstructed energy formula adjusted accordingly



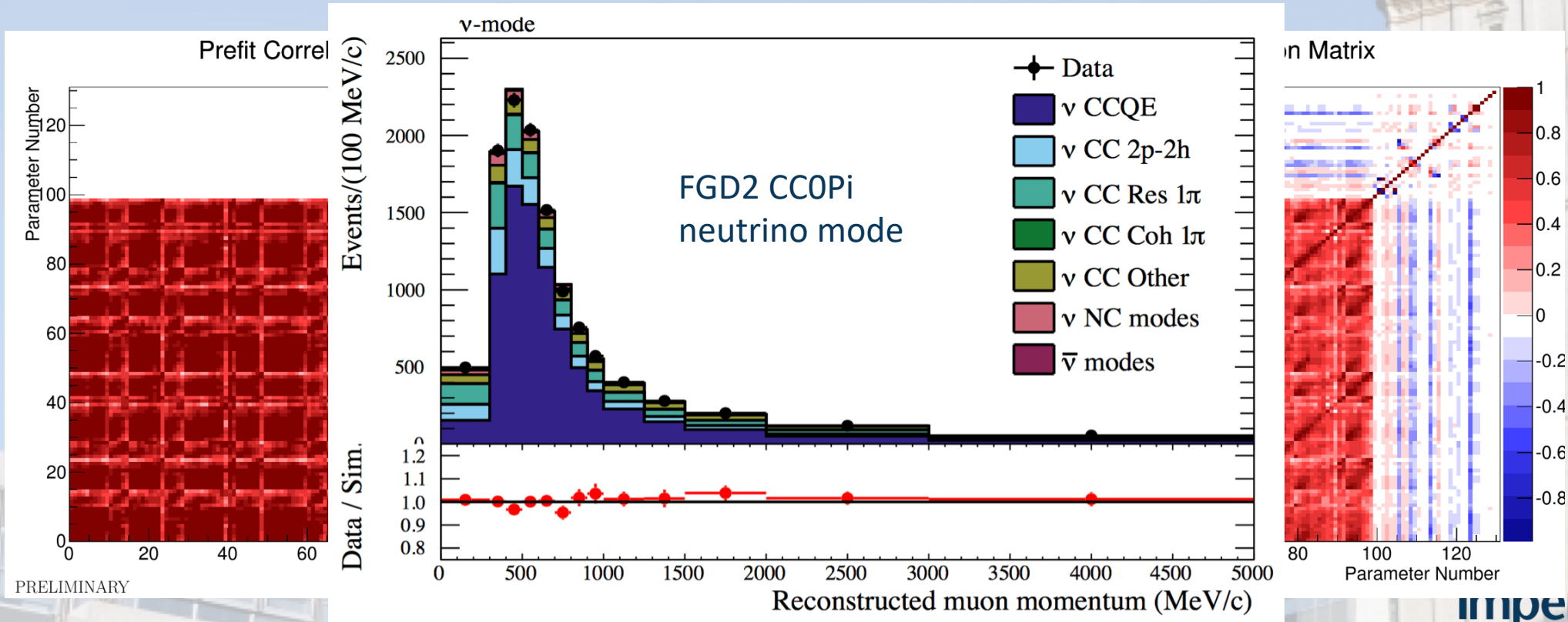
- Combination of new sample and increased FV equates to **30% increase in event rate** for same POT in neutrino mode

Near Detector Fit Results



Near detector fit results

- Flux and cross-section parameters have similar effects
 - ND Fit leads to significant anti-correlation reducing overall uncertainty
- Fit reproduces data well (p-value 0.47)



PRELIMINARY

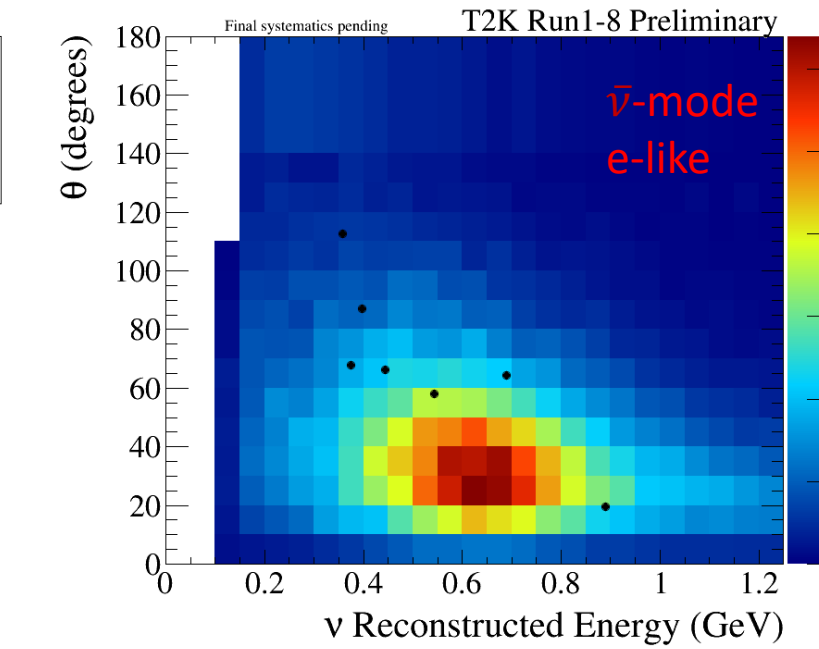
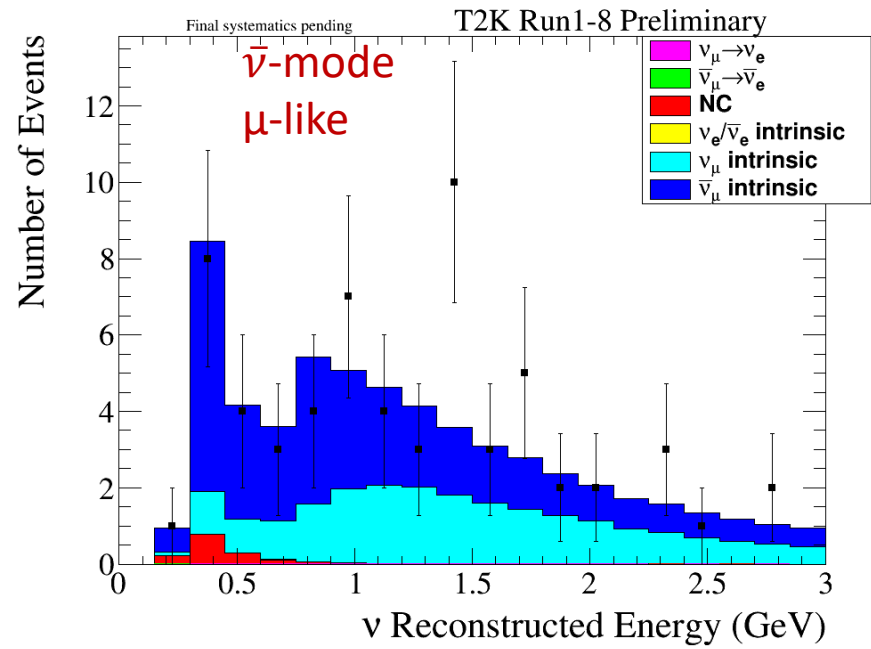
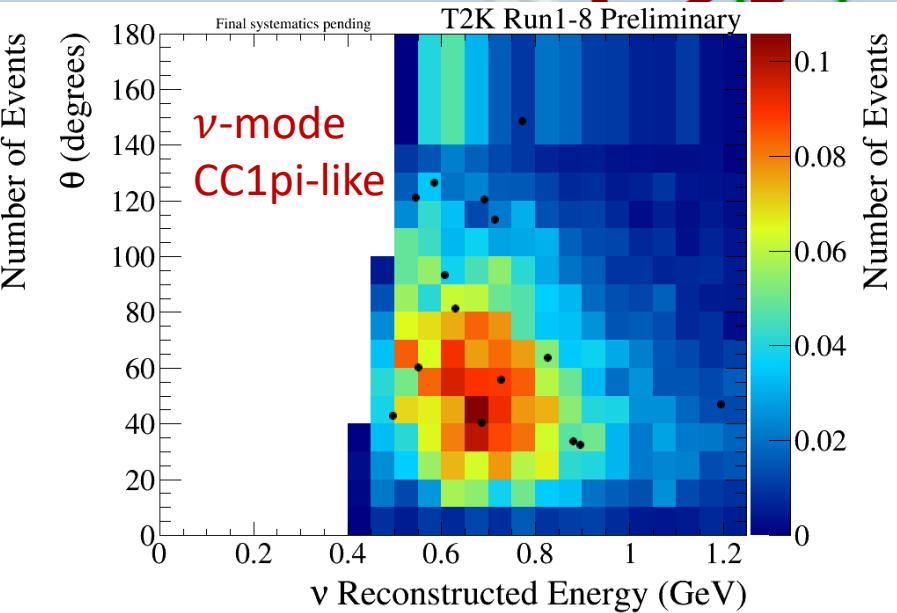
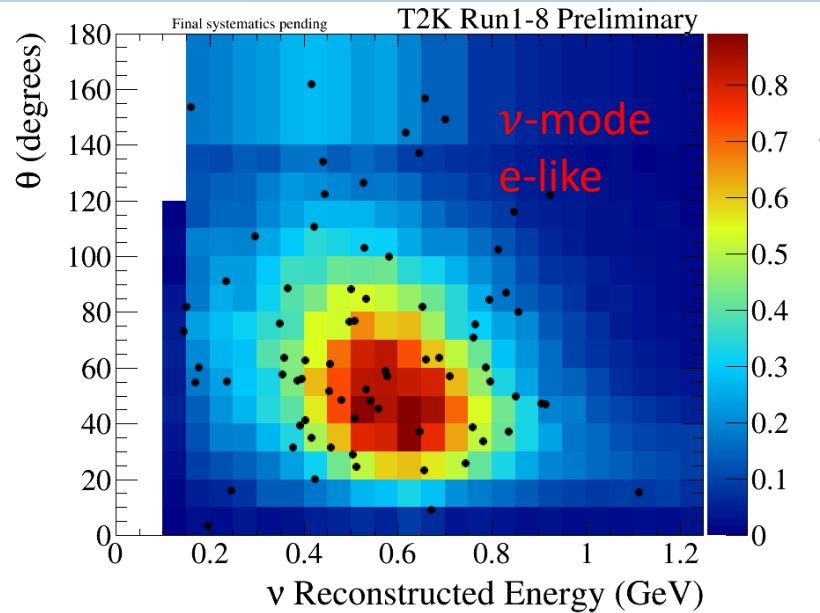
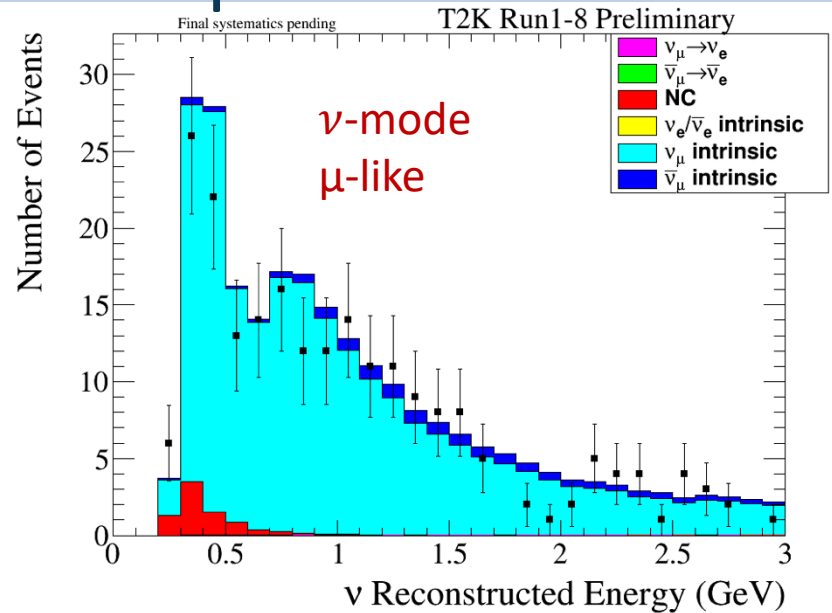
Predicted and observed Super-K event rates



Sample	Predicted Rates				Observed Rates
	$\delta_{CP} = -\pi/2$	$\delta_{CP} = 0$	$\delta_{CP} = \pi/2$	$\delta_{CP} = \pi$	
CCQE 1-Ring e-like ν -mode	73.5	61.5	49.9	62.0	74
CC1 π 1-Ring e-like ν -mode	6.92	6.01	4.87	5.78	15
CCQE 1-Ring e-like $\bar{\nu}$ -mode	7.93	9.04	10.04	8.93	7
CCQE 1-Ring μ -like ν -mode	267.8	267.4	267.7	268.2	240
CCQE 1-Ring μ -like $\bar{\nu}$ -mode	63.1	62.9	63.1	63.1	68

- Other oscillation parameters at set A values: maximal θ_{23}
- Number of events observed generally agrees with oscillated predictions
 - e-like sample rates are most consistent with $\delta_{CP} = -\pi/2$ hypothesis
 - μ -like sample rates consistent within statistical and systematic errors
 - CC1 π rate shows large upwards fluctuation
 - p-value for fluctuation of this size in at least 1 of 5 samples: 11.9%

SK spectra



Size of systematic uncertainties



Error Source	% Errors on predicted event rates, Osc. Parameters as for rates					
	1R μ -like		1R e-like			
	ν -mode	$\bar{\nu}$ -mode	ν -mode	$\bar{\nu}$ -mode	ν -mode CC1 π	ν -mode/ $\bar{\nu}$ -mode
SK Detector	1.86	1.51	3.03	4.22	16.69	1.60
SK FSI+SI+PN	2.20	1.98	3.01	2.31	11.43	1.57
ND280 const. flux & xsec	3.22	2.72	3.22	2.88	4.05	2.50
$\sigma(\nu_e)/\sigma(\bar{\nu}_e)$	0.00	0.00	2.63	1.46	2.62	3.03
NC1 γ	0.00	0.00	1.08	2.59	0.33	1.39
NC Other	0.25	0.25	0.14	0.33	0.98	0.18
Total Systematic Error	4.40	3.76	6.10	6.51	20.94	4.77

- Total error in the 4-7% range (except CC1 π)
- Errors constrained by ND280 contribute 3-4% uncertainties
- Error on ν -mode / $\bar{\nu}$ -mode ratio 4.8%
 - important for CP violation

Far Detector Event Rate Predictions and Uncertainties

Oscillation parameters used for predictions

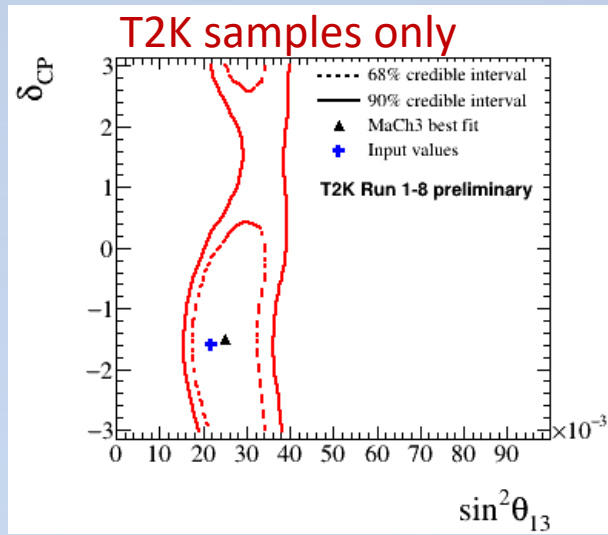


- Define two sets of oscillation parameter values used for event rate and sensitivity predictions
- Parameters generally at previous T2K 2013 best fit values

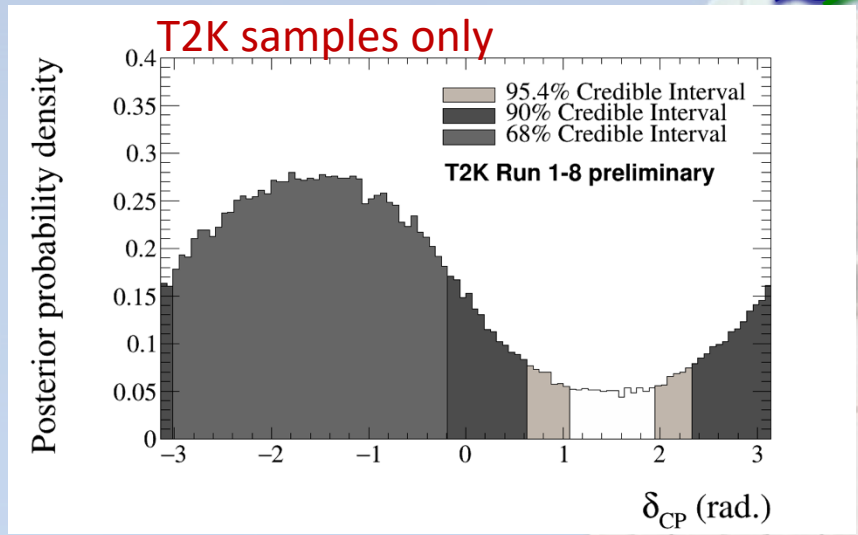
	Set A	Set B
$\sin^2\theta_{12}$	0.304	0.304
$\sin^2\theta_{23}$	0.528	0.45
$\sin^2\theta_{13}$	0.0219	0.0219
Δm^2_{12}	$7.53 \times 10^{-5} \text{ eV}^2$	$7.53 \times 10^{-5} \text{ eV}^2$
Δm^2_{23}	$2.509 \times 10^{-3} \text{ eV}^2$	$2.509 \times 10^{-3} \text{ eV}^2$
δ_{CP}	-1.601	0

Sensitivities

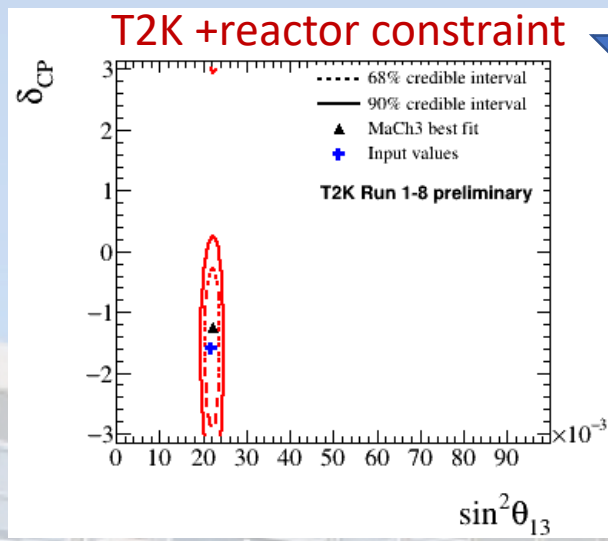
Set A sensitivity



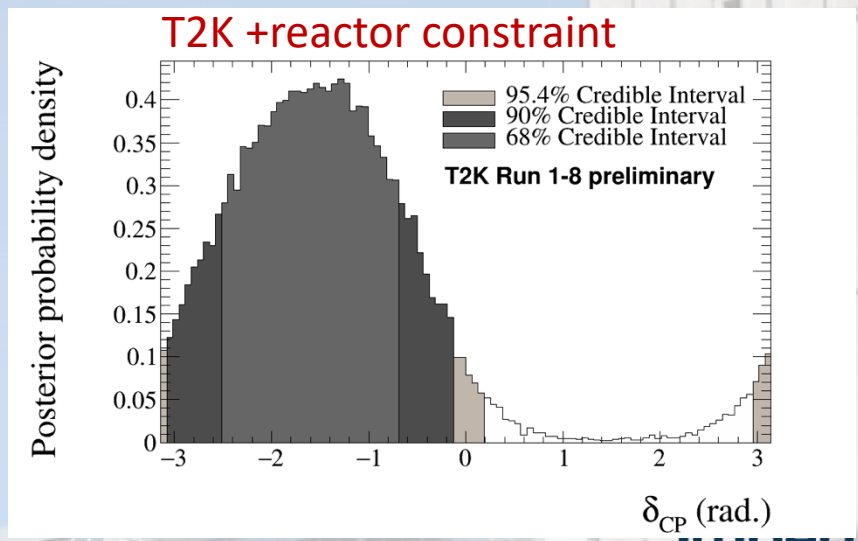
Integrate out $\sin^2\theta_{13}$ dependence



Impose reactor constraint on $\sin^2(2\theta_{13})$ (PDG 2016)

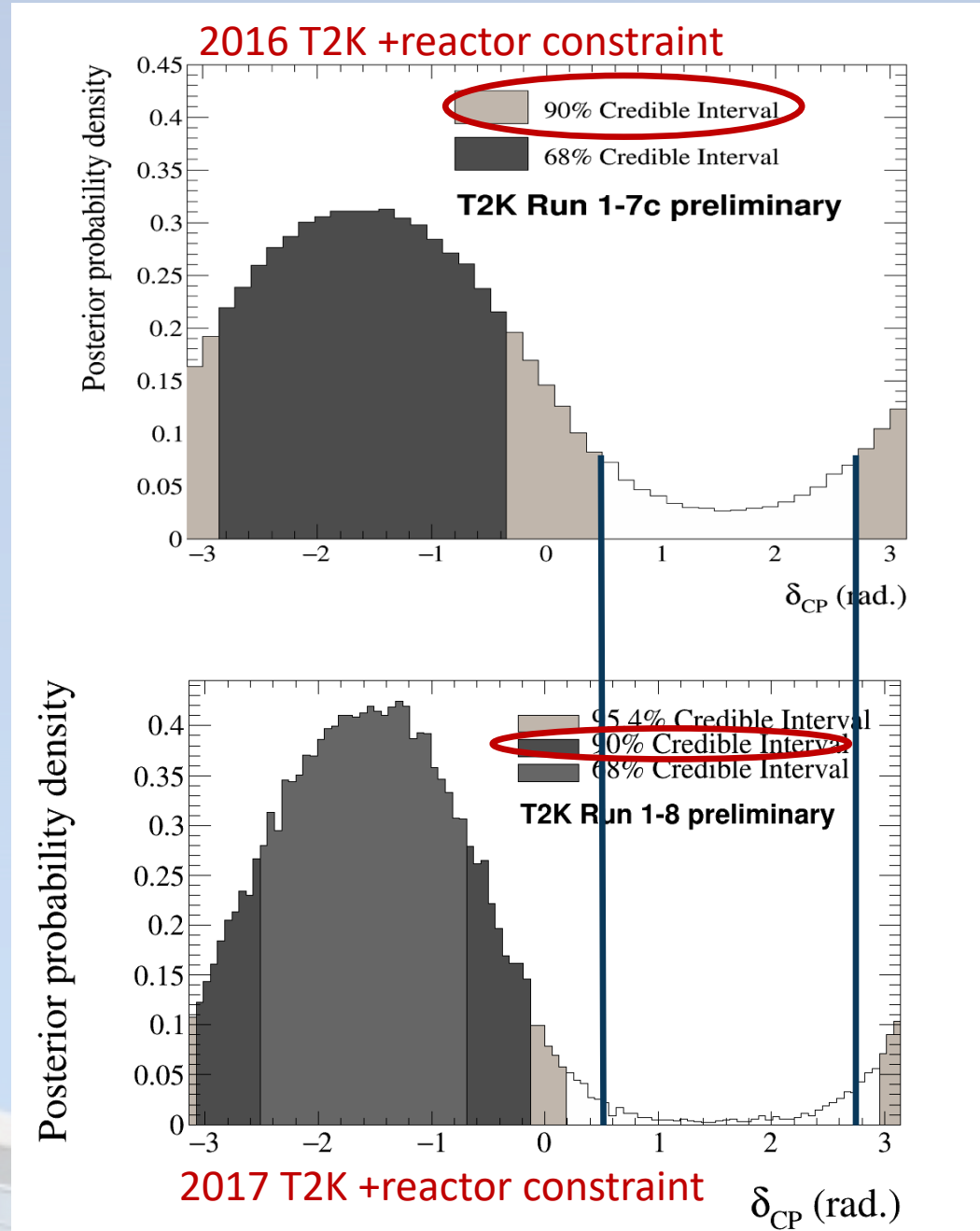


Integrate out $\sin^2\theta_{13}$ dependence



Comparison to Summer 2016 sensitivity

T2K

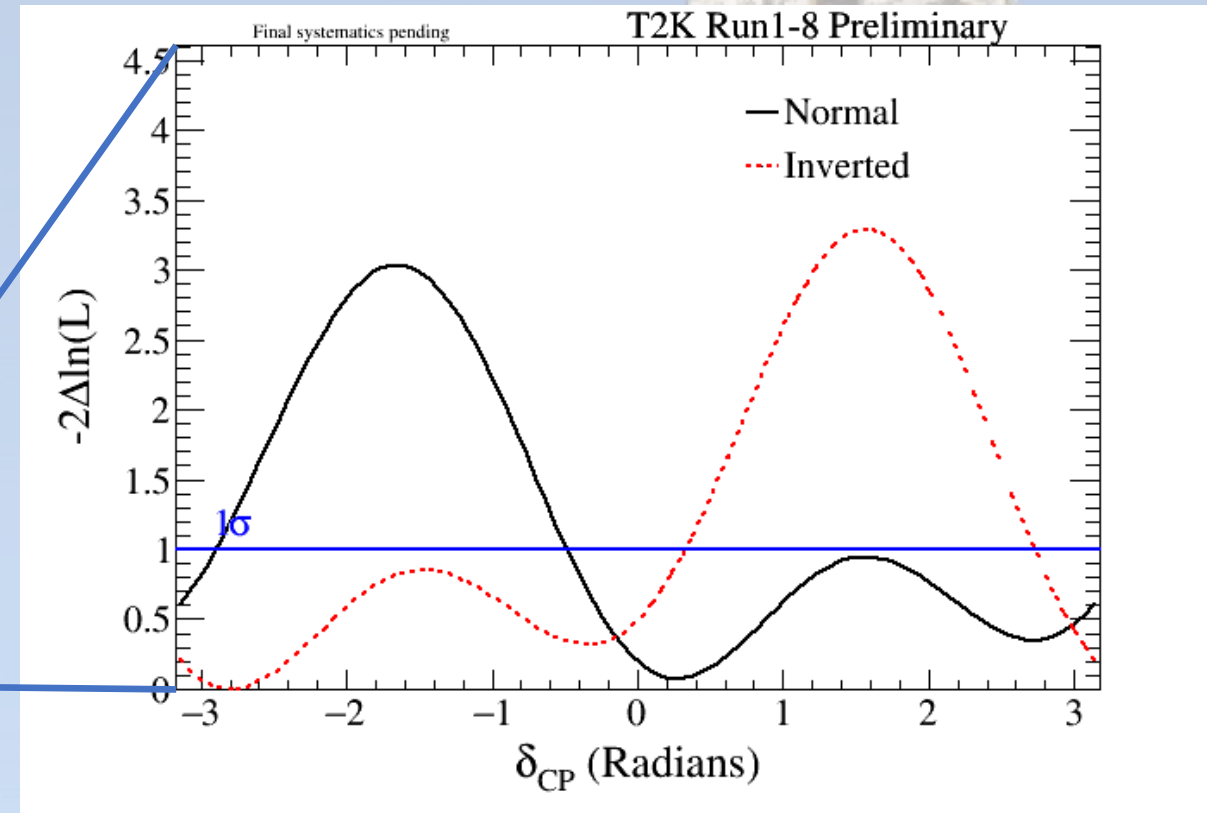
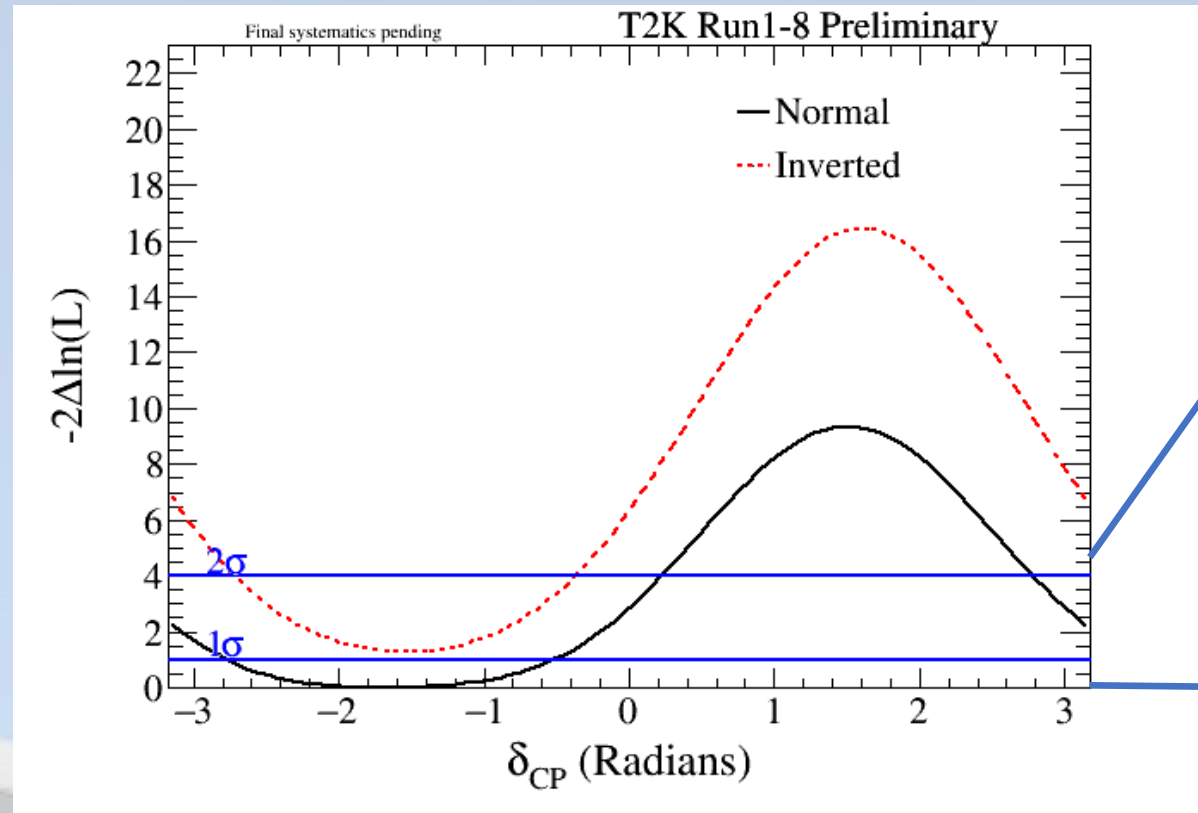


Set A vs Set B sensitivity



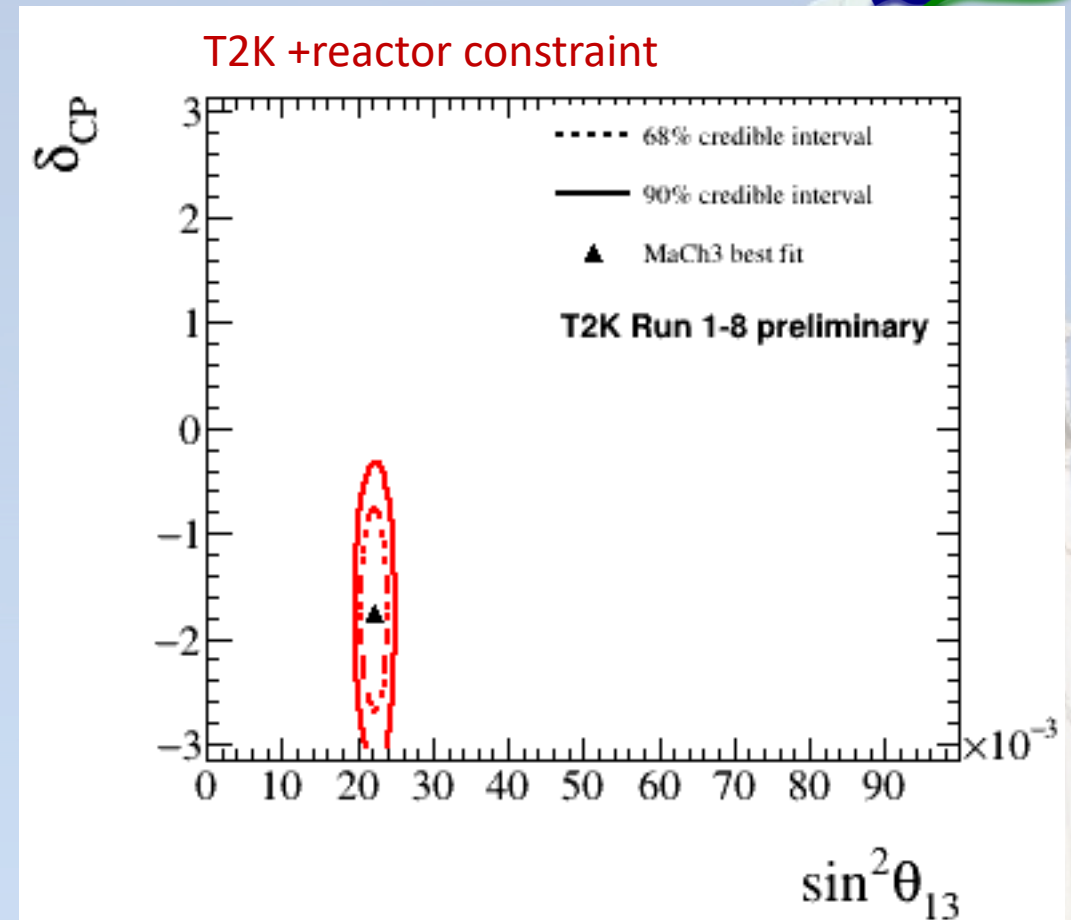
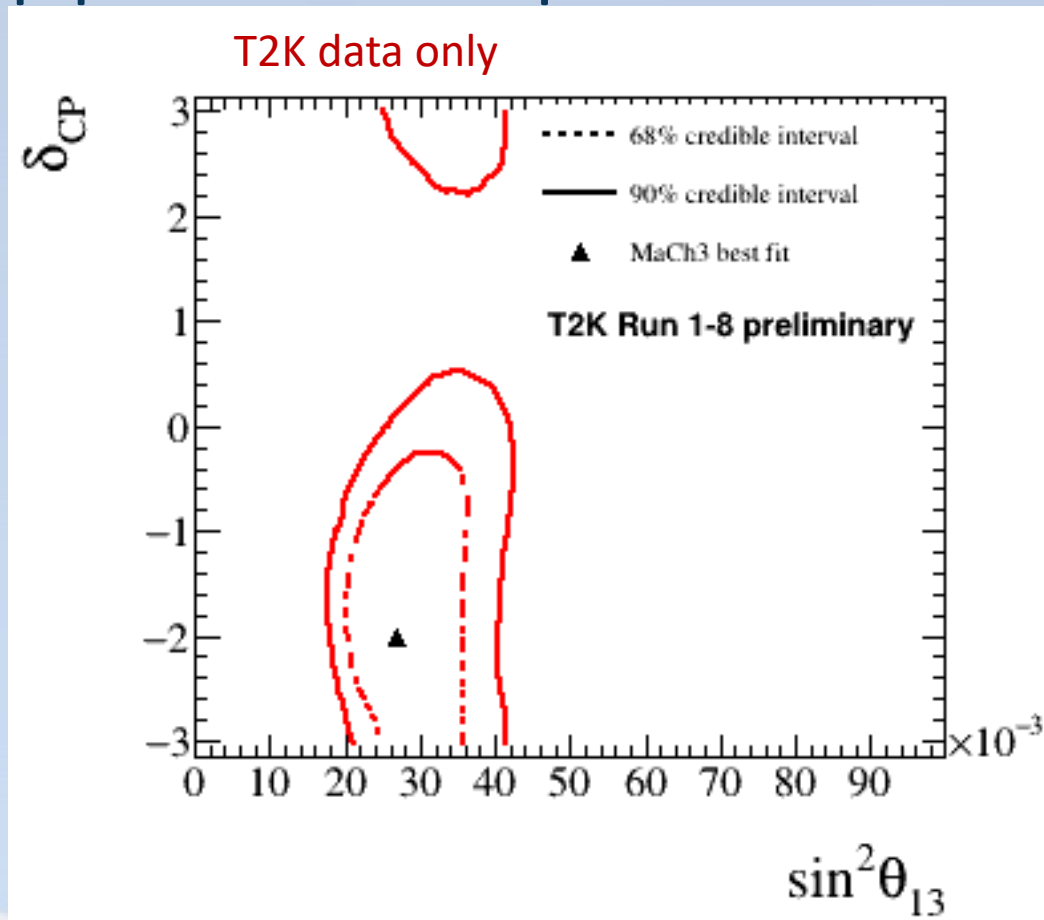
Set A: $\sin^2\theta_{23}=0.528$, $\delta_{CP} = -1.601$

Set B: $\sin^2\theta_{23}=0.45$, $\delta_{CP} = 0$



Data results

Appearance parameter constraints

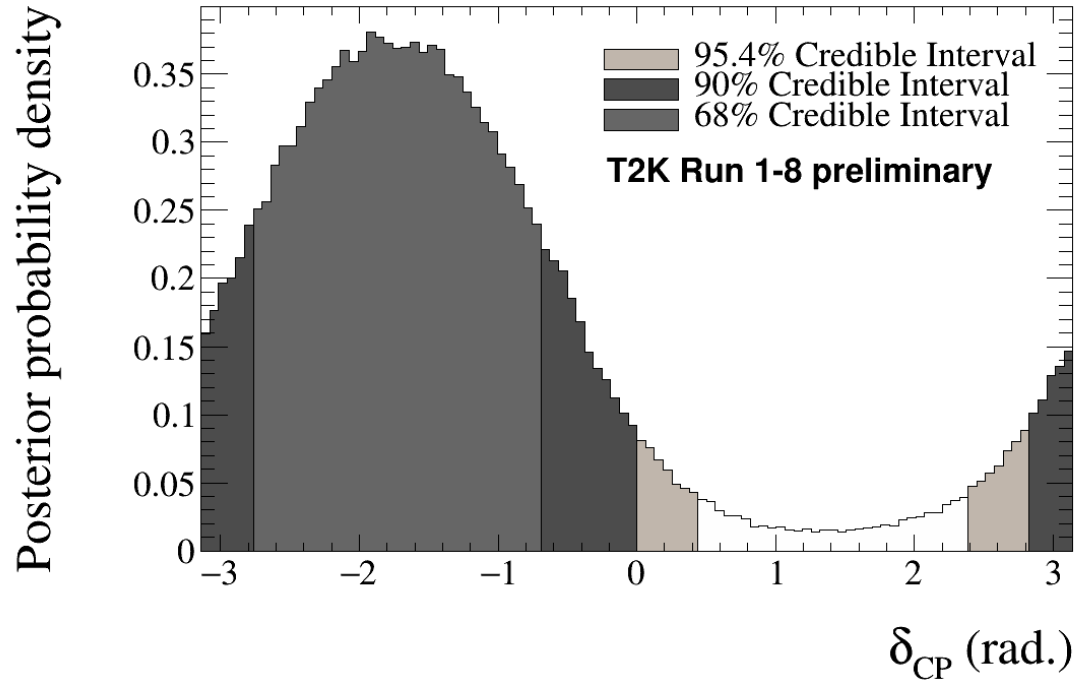


- T2K value for $\sin^2 \theta_{13}$ is consistent with PDG 2016 average (0.0219)

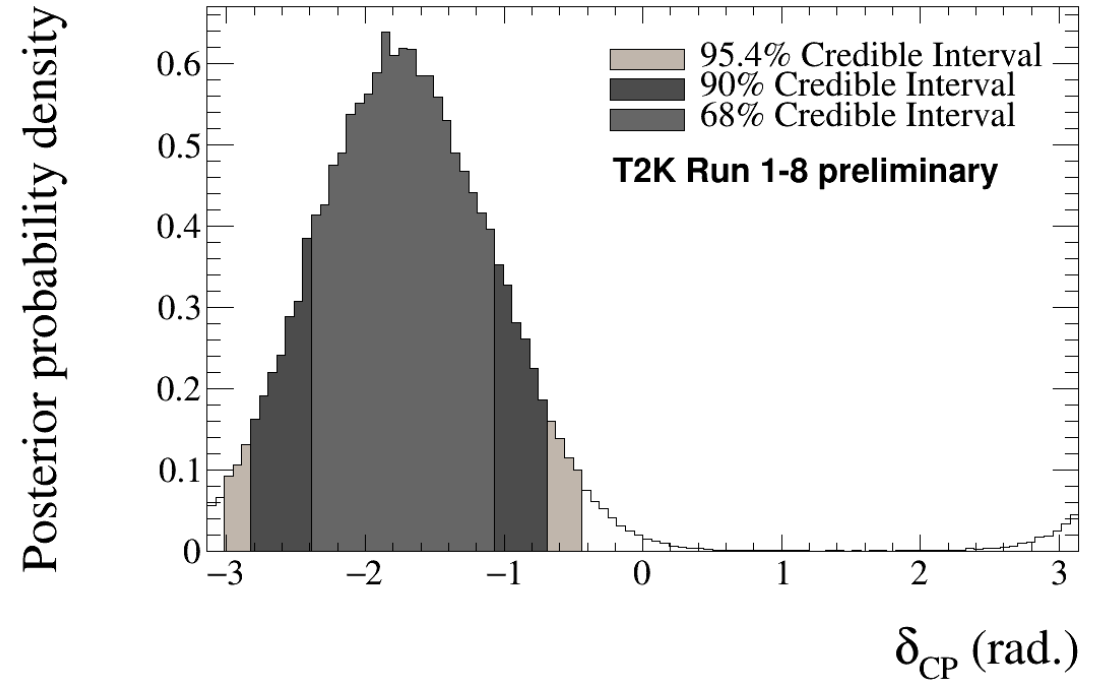
δ_{CP} Constraint



T2K data only

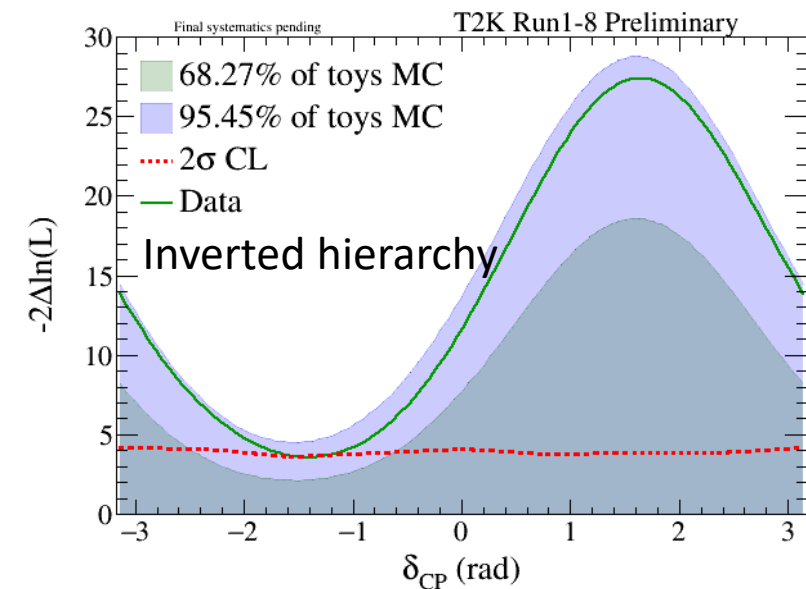
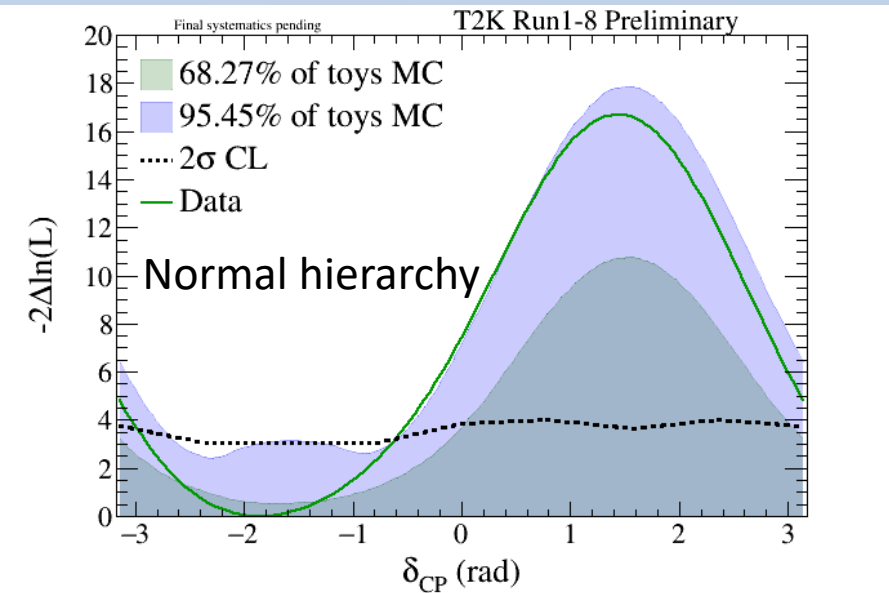


T2K + reactor constraint



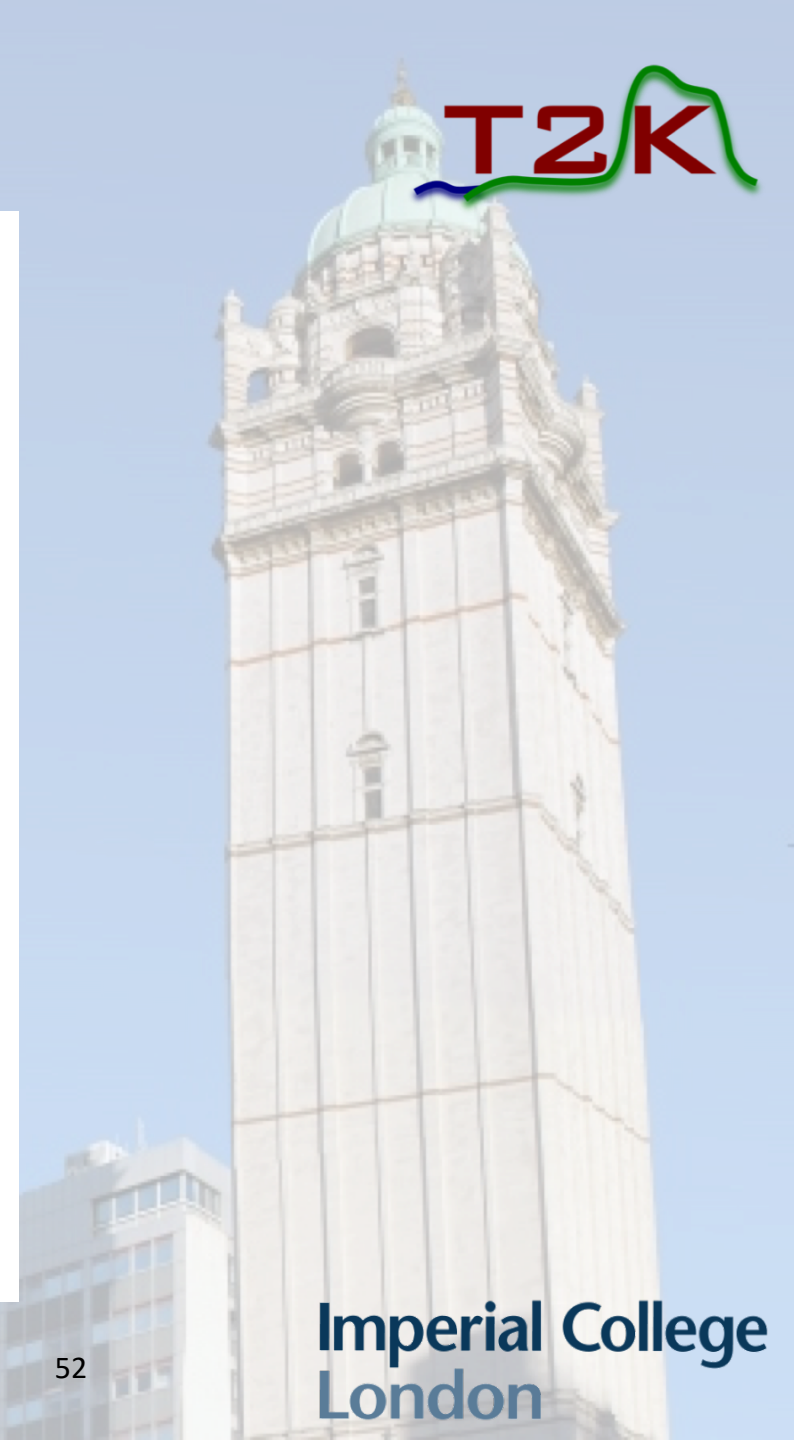
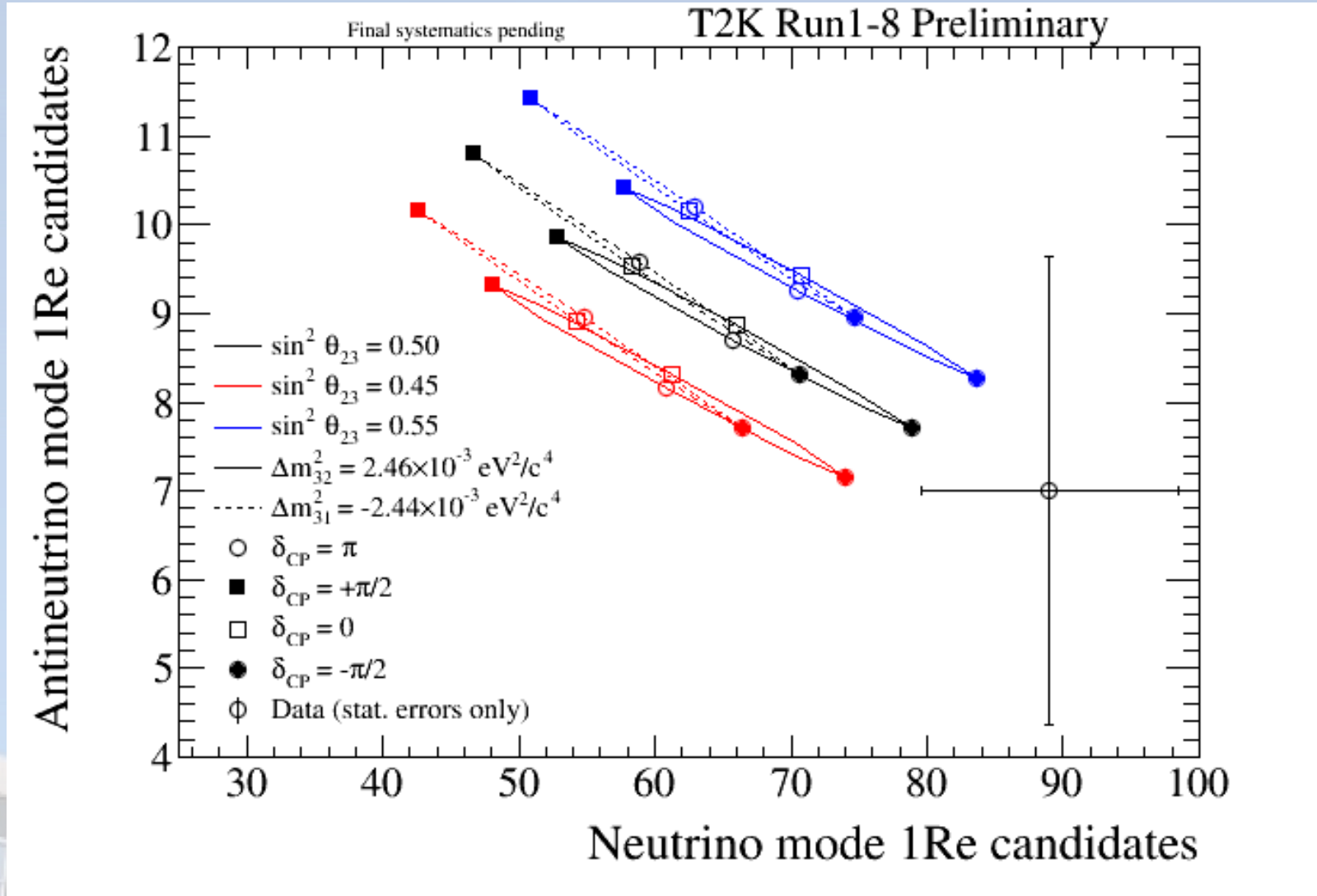
- CP conserving values outside 2σ (95.4%) interval for T2K+reactor constraint

Constraint vs sensitivity

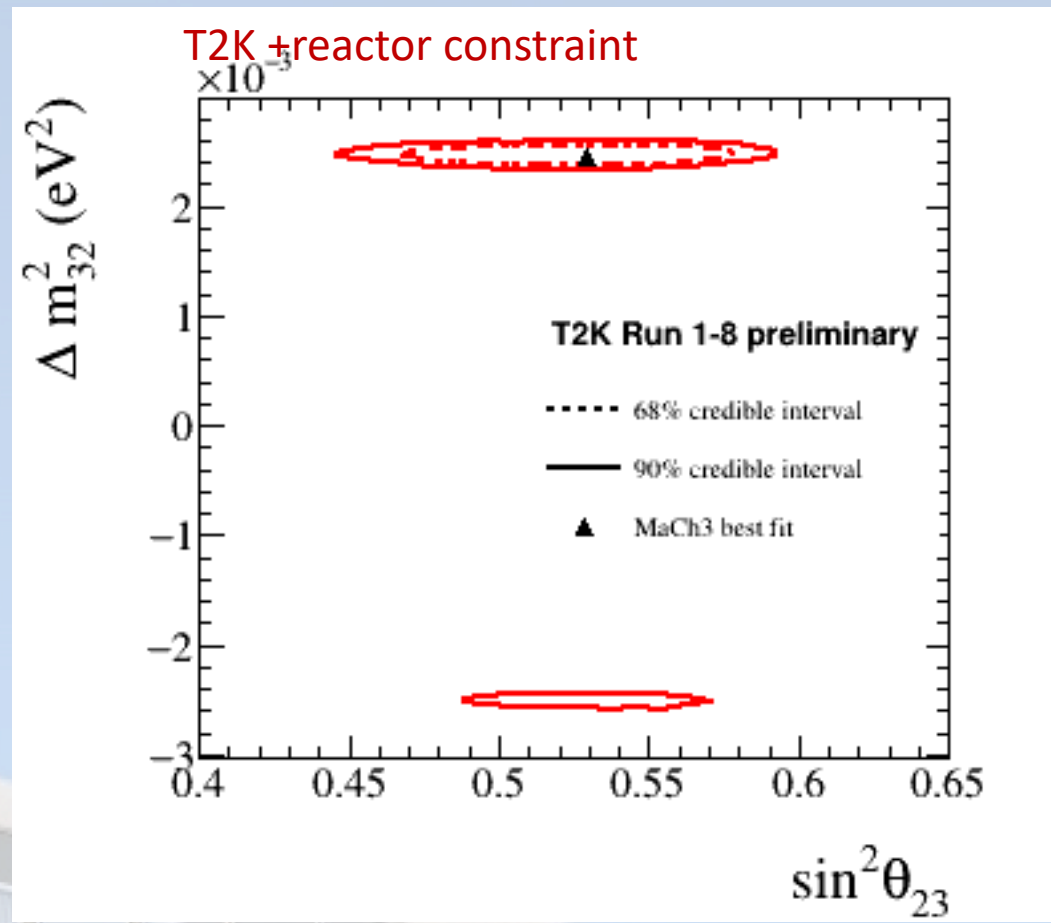


- Observed constraint stronger than predicted sensitivity
- Studied how likely this was to happen
- Generated many toy data sets with statistical and systematic fluctuations around $\delta_{CP} = -\pi/2$, normal hierarchy (NH)
- Ran fits to these spectra to determine δ_{CP} constraint
- Observed constraint falls within 95.45% for most δ_{CP} points
- 30% of experiments **exclude** $\delta_{CP} = 0$ at 2σ
- 25% of experiments **exclude** $\delta_{CP} = \pi$ at 2σ

Biprobability plots



Octant and hierarchy preferences



- Result consistent with maximal $\sin^2 \theta_{23}$
- Preference for normal hierarchy
- Systematics may change due to simulated data studies

Posterior probabilities (T2K + reactor constraint)			
	$\sin^2 \theta_{23} < 0.5$	$\sin^2 \theta_{23} > 0.5$	Sum
NH ($\Delta m_{23}^2 > 0$)	0.193	0.674	0.868
IH ($\Delta m_{23}^2 < 0$)	0.026	0.106	0.132
Sum	0.219	0.781	

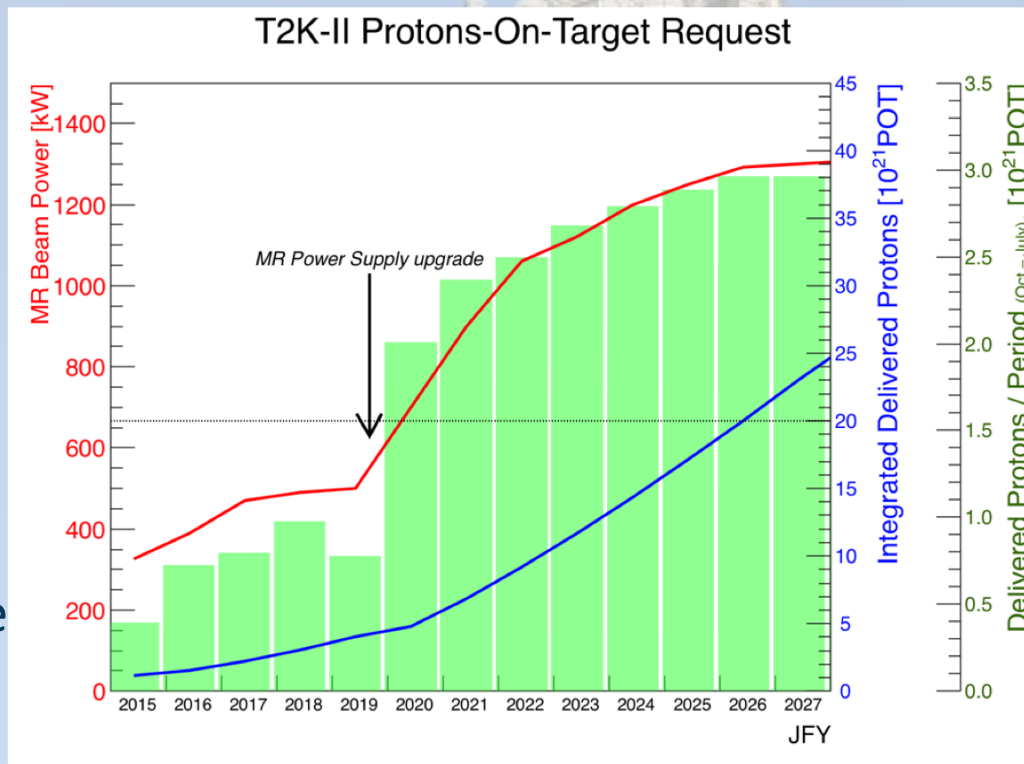
Future plans

T2K-II

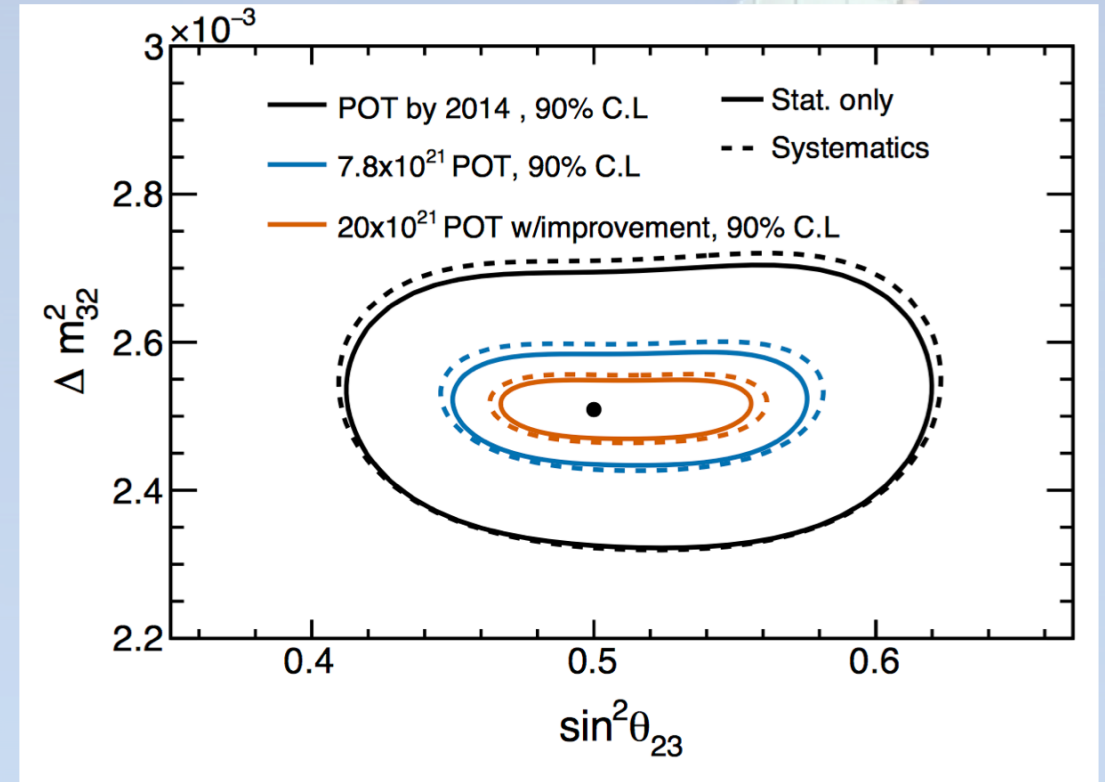
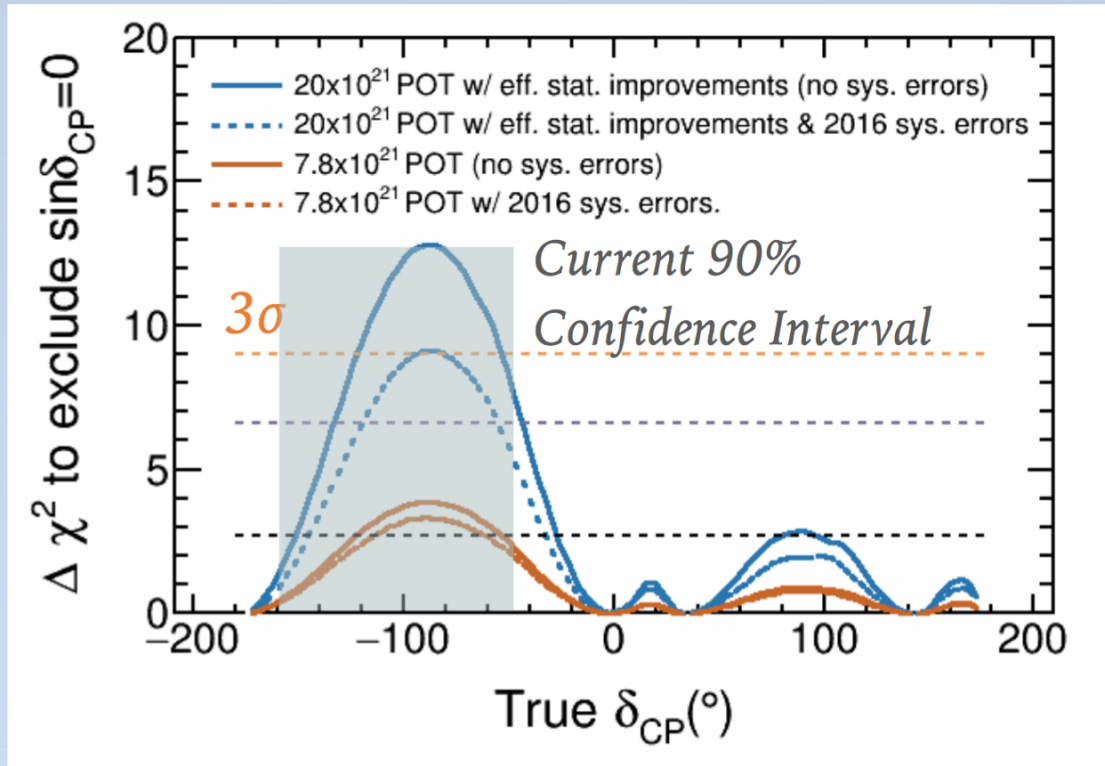
- T2K target protons on target (POT) is 7.8×10^{21}
- T2K-II is a proposal to extend target to 20.0×10^{21} POT by ~2026
 - Upgrade Main Ring power supply to increase from 0.4- \rightarrow 1 Hz running
 - Beam power increase up to 1.3 MW

Other beam and detector upgrades

- **Neutrino horns will run at 320 kA from next year**
 - Reduces wrong sign contamination in antineutrino mode
- ND280 will be upgraded to improve high-angle acceptance
 - More similar to SK improving cross-section constraint
- SK will be refurbished during Summer 2018 to allow Gd addition in 2019/2020
 - Gd enables neutron tagging



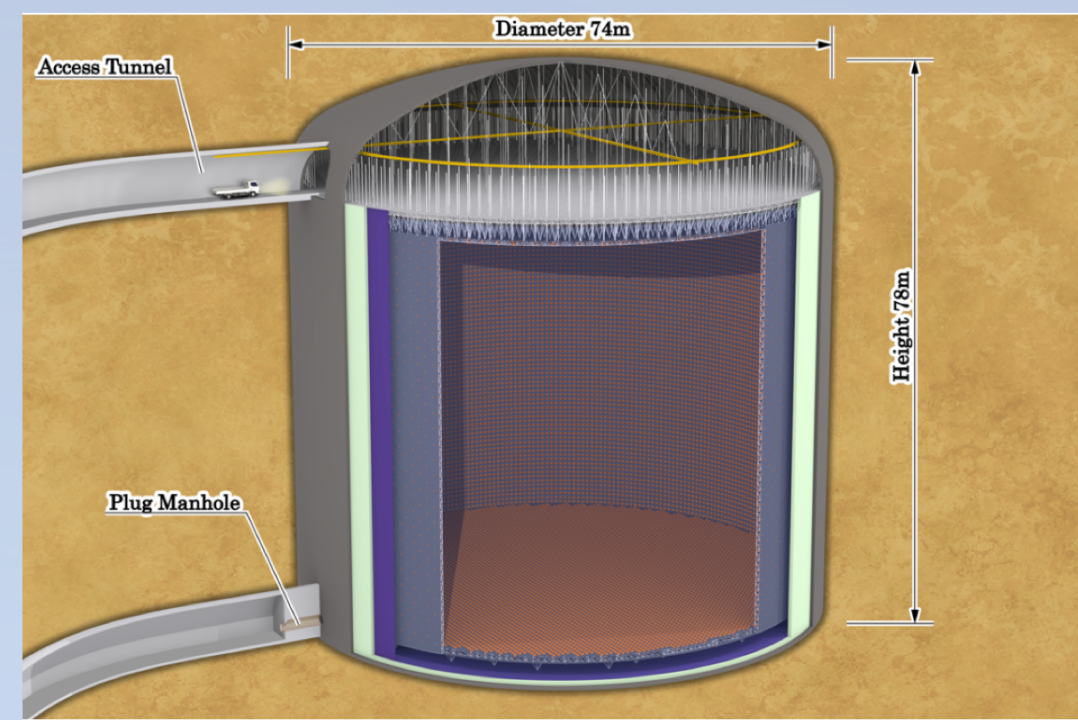
T2K-II sensitivity



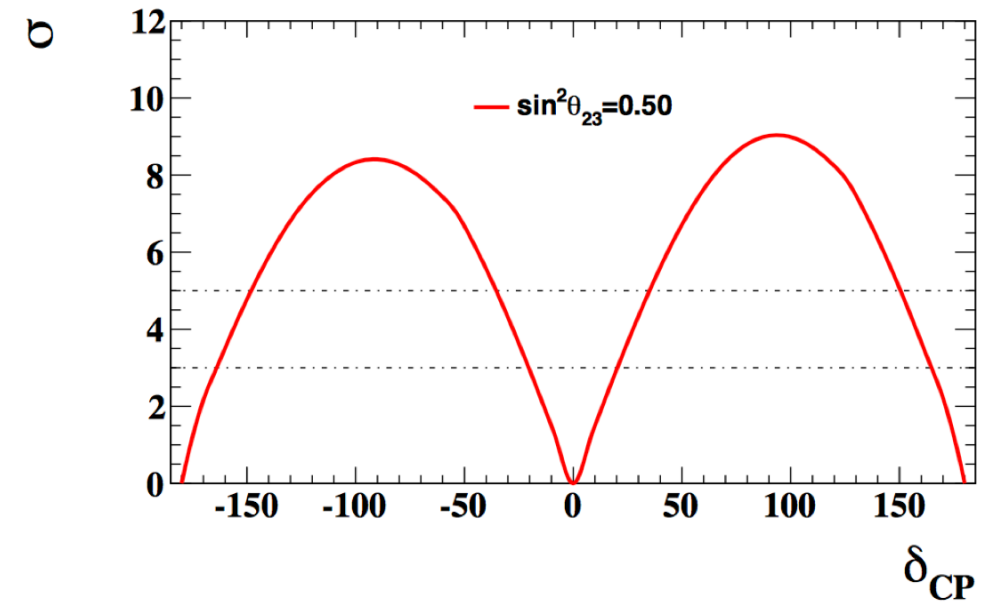
- If current preferred δ_{CP} is true T2K-II has potential for 3σ discovery
- Size of systematic uncertainties has large effect on sensitivity

Hyper-K

- Larger successor experiment to Super-K
- 187 kton fiducial volume (7x T2K design)
- 1300 kW beam power (2x T2K design)
- Aiming for 5σ δ_{CP} observation unless value is unfavourable
- Possibility to build second tank in Korea at second oscillation maximum
 - Oscillation effects look different
 - Reduces systematic sensitivity and breaks degeneracies
- Also gives world leading proton decay measurements and supernova neutrino sensitivity
- Aim for physics data taking in 2026

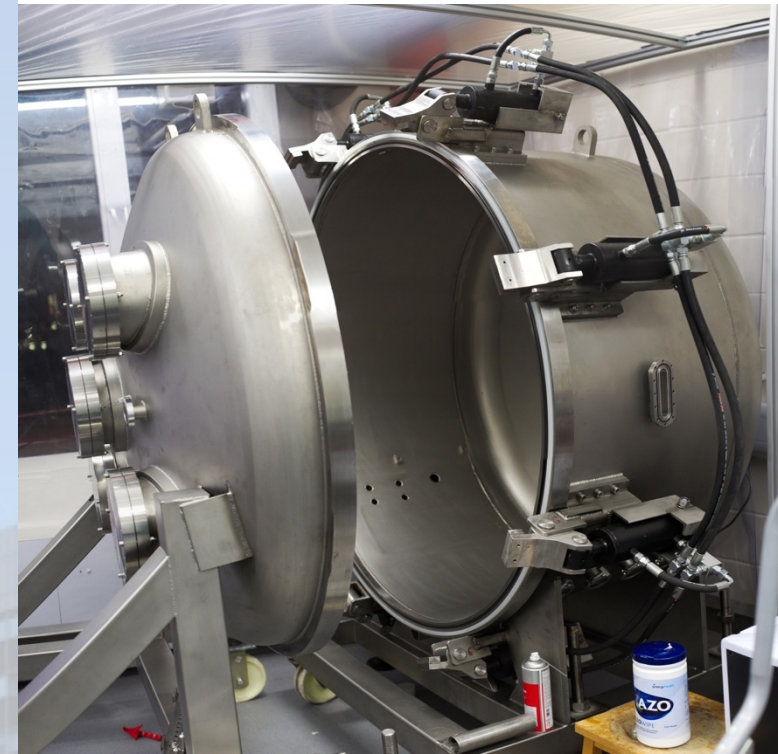
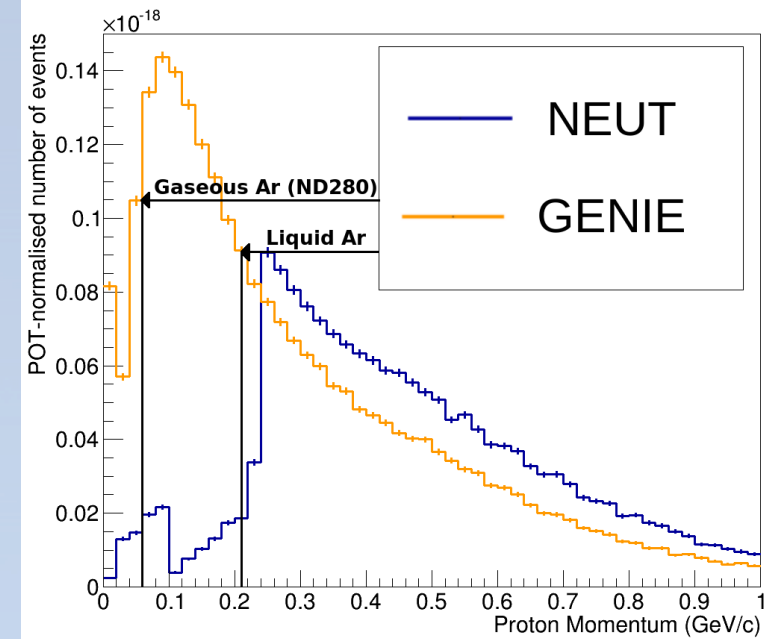


Normal mass hierarchy

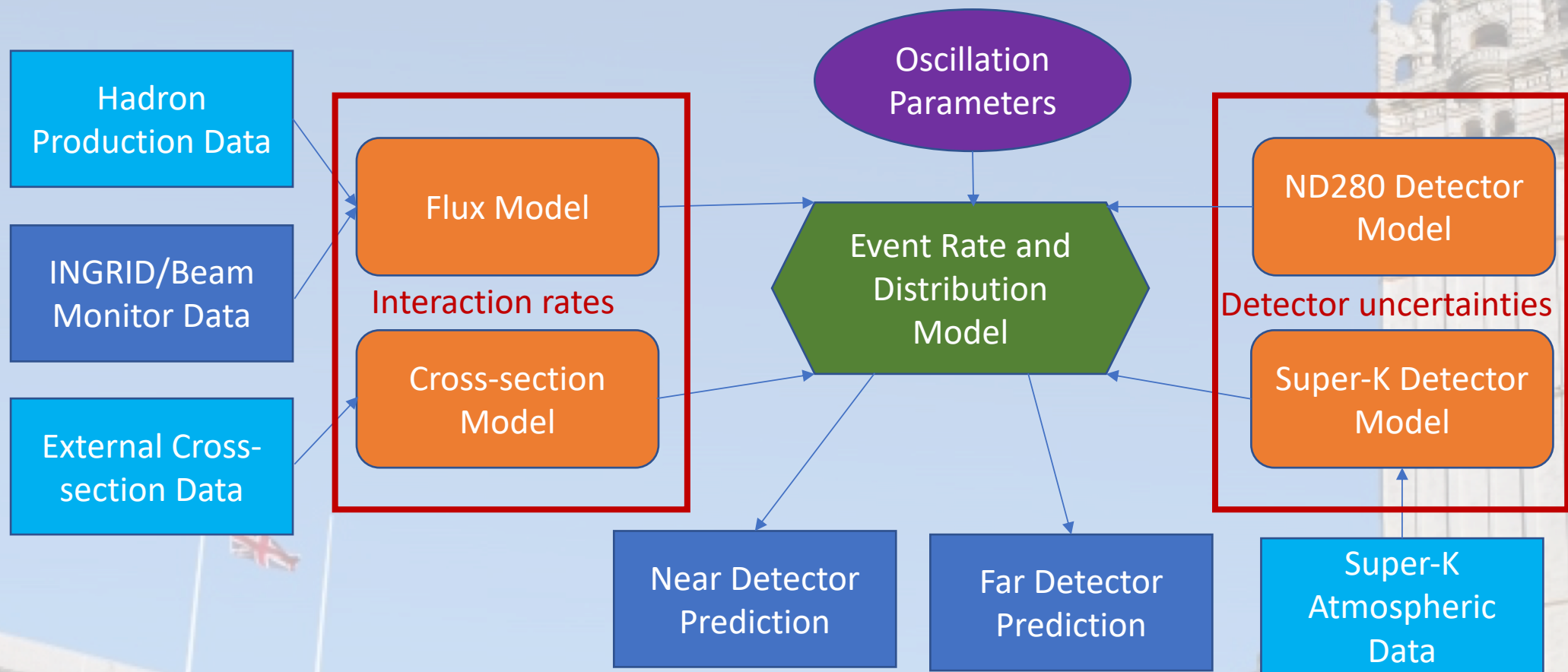


HPTPC – High Pressure TPC

- Reducing systematics key to future oscillation measurements
 - DUNE & HK aim for $\sim 1\%$
- Current MC generators give different predictions just outside accessible energy range
- Gaseous target has much lower threshold
 - Gas density usually too low for high interaction rate
- Try high pressure gas
- Building 5 bar prototype TPC at RHUL
 - Beam test at CERN planned for next year



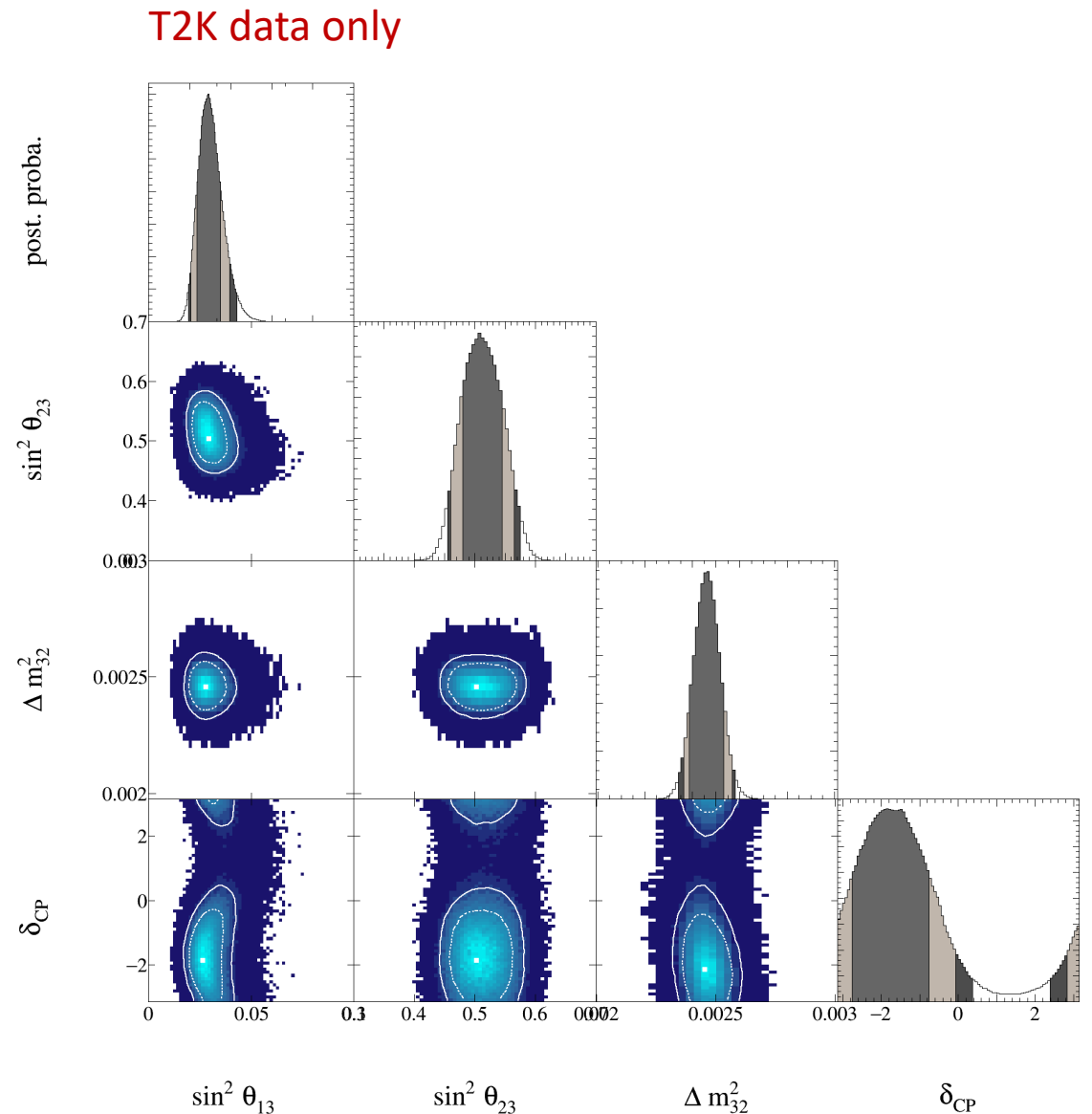
Model constraints



Triangle plots



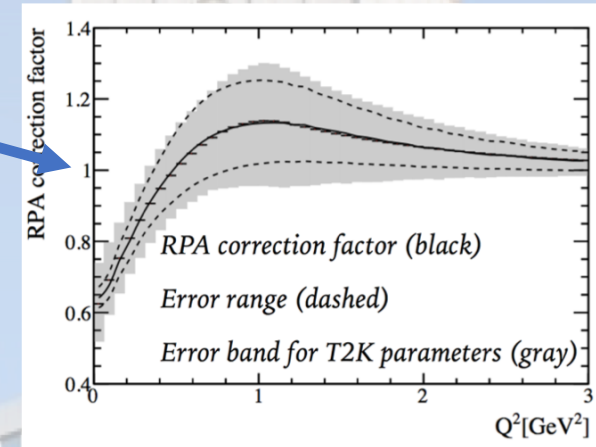
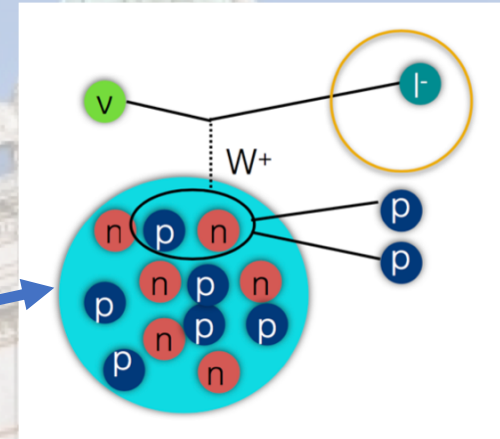
- Markov chain fit used by Bayesian analysis has all values of all parameters for all steps
- Allows study of effect of all combinations of parameters without extra fits



Changes to model this year – Cross section

T2K

- NEUT neutrino interaction MC generator has been significantly improved in recent years:
 - New tune of pion production model to external hydrogen and deuterium data
 - **Inclusion of multi-nucleon scattering processes: Valencia 2p-2h model**
(Phys. Rev. C83 (2011) 045501)
 - Improvements to the CCQE model:
Included the effect of long-range nucleus correlations
(calculated using random phase approximation, **RPA**)
- Analysis now includes new parametrisations of the uncertainties on these processes



more on ν_μ disappearance



- ν_μ disappearance probability in vacuum

$$\begin{aligned}
 P(\nu_\mu \rightarrow \nu_\mu) = & 1 - (c_{13}^4 \sin^2 2\theta_{23} + s_{23}^2 \sin^2 2\theta_{13}) \sin^2 \Delta_{atm} \\
 & + \left\{ c_{13}^2 (c_{12}^2 - s_{13}^2 s_{23}^2) \sin^2 2\theta_{23} + s_{12}^2 s_{23}^2 \sin^2 2\theta_{13} - c_{13} \sin 2\theta_{13} \sin 2\theta_{23} \sin 2\theta_{12} \cos \delta \right\} \\
 & \times \left\{ \frac{1}{2} \sin 2\Delta_{solar} \sin 2\Delta_{atm} + 2 \sin^2 \Delta_{solar} \sin^2 \Delta_{atm} \right\} \\
 & - \left\{ \sin^2 2\theta_{12} (c_{23}^2 - s_{13}^2 s_{23}^2)^2 + s_{13}^2 \sin^2 2\theta_{23} (1 - c_\delta^2 \sin^2 2\theta_{12}) \right. \\
 & + 2s_{13} \sin 2\theta_{12} \cos 2\theta_{12} \sin \theta_{23} \cos 2\theta_{23} c_\delta \\
 & \left. - \frac{1}{2} c_{13} \sin 2\theta_{13} \sin 2\theta_{23} \sin 2\theta_{12} \cos \delta s_{23}^2 s_{12}^2 \right. \\
 & \left. + \sin^2 2\theta_{23} c_{13}^2 (c_{12}^2 - s_{13}^2 s_{12}^2) + s_{13}^2 s_{23}^2 \sin^2 2\theta_{13} \right\} \times \sin^2 \Delta_{solar} \quad (26)
 \end{aligned}$$

$$\begin{aligned}
 s_{ij} &= \sin \theta_{ij} \\
 c_{ij} &= \cos \theta_{ij} \\
 c_\delta &= \cos \delta \\
 \Delta_{atm} &= \frac{\Delta m_{13}^2 L}{4 E_\nu} \\
 \Delta_{solar} &= \frac{\Delta m_{21}^2 L}{4 E_{\nu\mu}}
 \end{aligned}$$

T2K: $L = 295 \text{ km}$, E_ν peaks at $\sim 0.6 \text{ GeV}$ $\rightarrow \sin^2 \Delta_{solar} \sim 0$, $\sin 2\Delta_{atm} \sim 0$

$$P(\nu_\mu \rightarrow \nu_\mu) \sim 1 - \left(\underbrace{\cos^4 \theta_{13} \cdot \sin^2 2\theta_{23}}_{\text{Leading-term}} + \underbrace{\sin^2 2\theta_{13} \cdot \sin^2 \theta_{23}}_{\text{Next-to-leading}} \right) \cdot \sin^2 \frac{\Delta m_{31}^2 \cdot L}{4E}$$

ν_μ disapp. probability depends on $\sin^2 2\theta_{13}$ $\sin^2 \theta_{23}$ to second order
 \rightarrow Can be used in combination with known $\sin^2 2\theta_{13}$ to resolve the θ_{23} octant

ν_e appearance probability with 1st order matter effect



$$P(\nu_\mu \rightarrow \nu_e) \approx 4c_{13}^2 s_{13}^2 s_{23}^2 \sin^2 \Delta_{31} \left(1 + \frac{2a}{\Delta m_{31}^2} (1 - 2s_{13}^2) \right)$$

Leading including matter effect

$$+ 8c_{13}^2 s_{12} s_{13} s_{23} (c_{12} c_{23} \cos \delta - s_{12} s_{13} s_{23}) \cos \Delta_{32} \sin \Delta_{31} \sin \Delta_{21}$$

CP conserving

$$- 8c_{13}^2 c_{12} c_{23} s_{12} s_{13} s_{23} \sin \delta \sin \Delta_{32} \sin \Delta_{31} \sin \Delta_{21}$$

CP violating

$$+ 4s_{12}^2 c_{13}^2 (c_{12}^2 c_{23}^2 + s_{12}^2 s_{23}^2 s_{13}^2 - 2c_{12} c_{23} s_{12} s_{23} s_{13} \cos \delta) \sin^2 \Delta_{21}$$

Solar

$$- 8c_{13}^2 s_{13}^2 s_{23}^2 (1 - 2s_{13}^2) \frac{aL}{4E} \cos \Delta_{32} \sin \Delta_{31}$$

Matter effect (small)

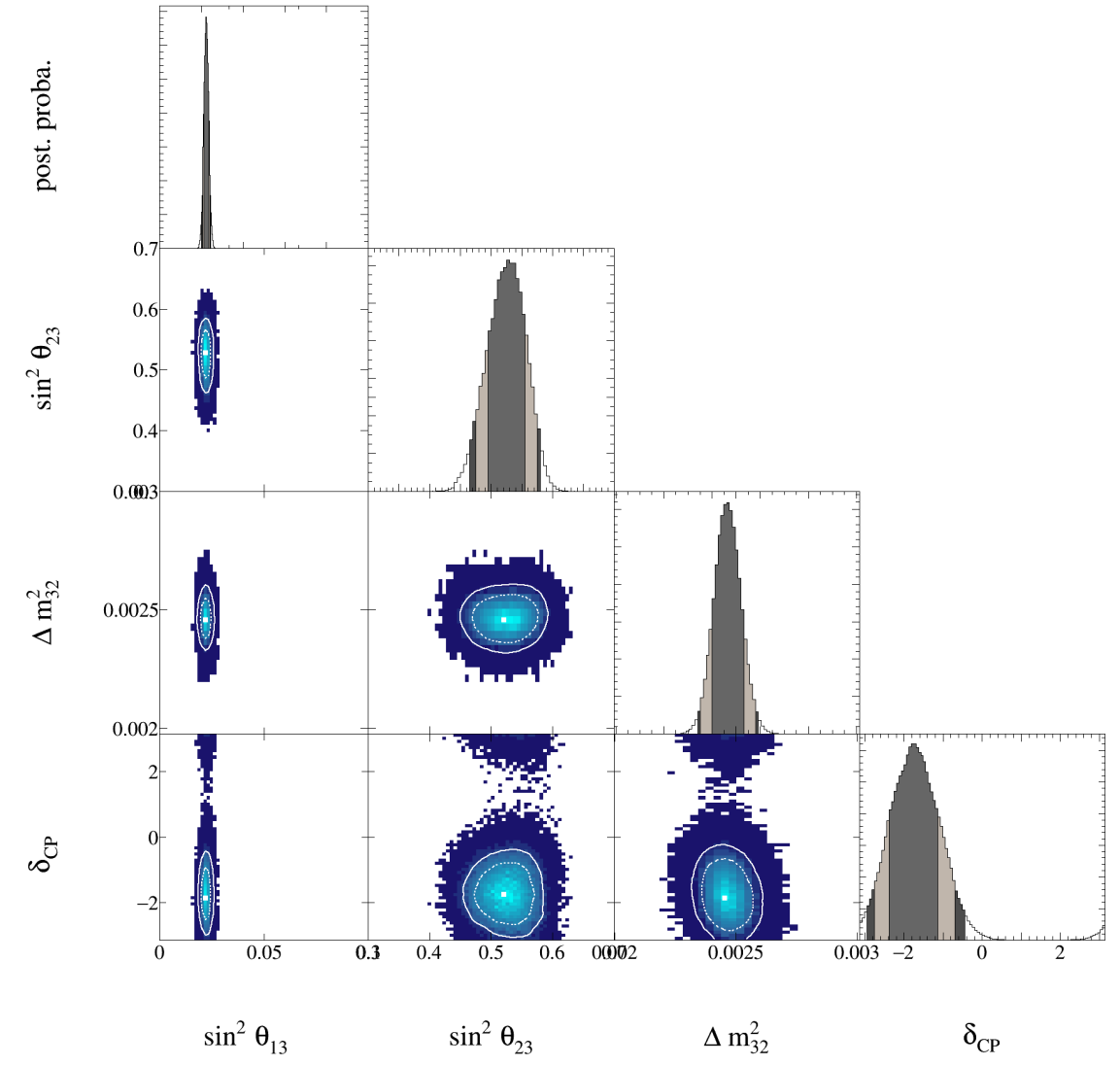
$$c_{ij} = \cos \theta_{ij}, s_{ij} = \sin \theta_{ij}$$

$$\Delta_{ij} = \Delta m_{ij}^2 \frac{L}{4E_\nu}$$

$$a \equiv 2\sqrt{2}G_F n_e E = 7.56 \times 10^{-5} \text{eV}^2 \frac{\rho}{\text{gcm}^{-3}} \frac{E}{\text{GeV}}$$

replace δ by $-\delta$ and a by $-a$ for $P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$

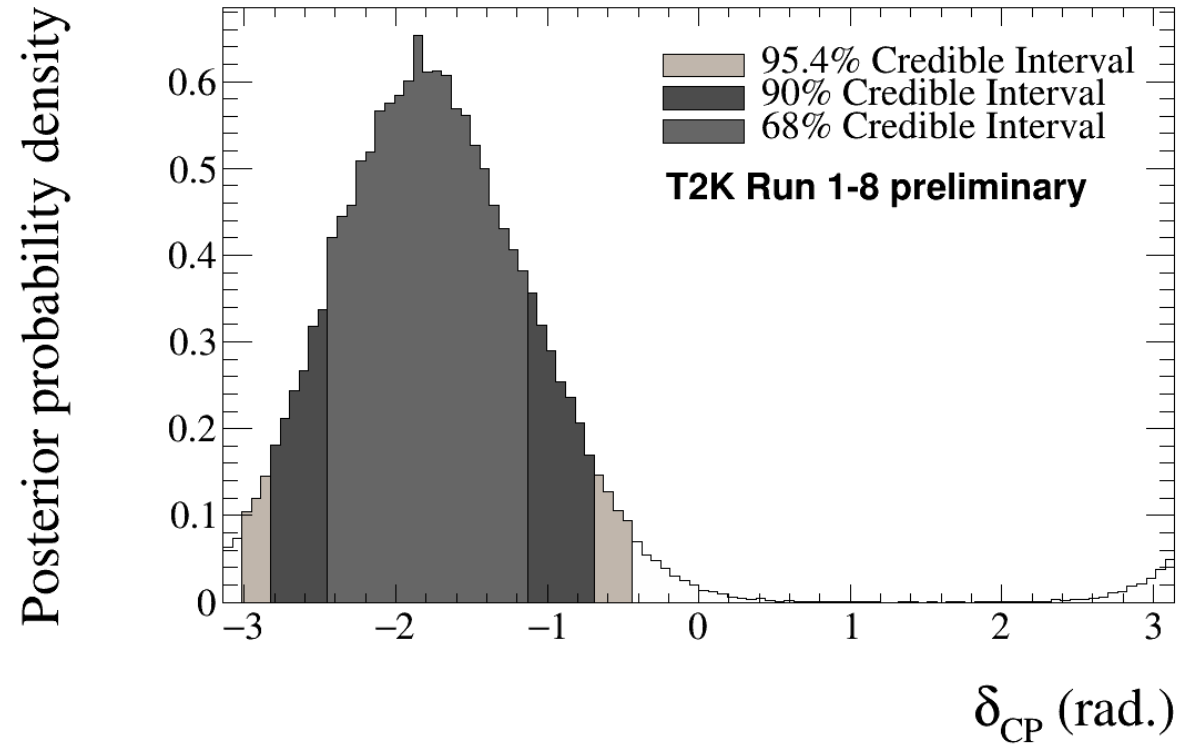
T2K + reactor constraint



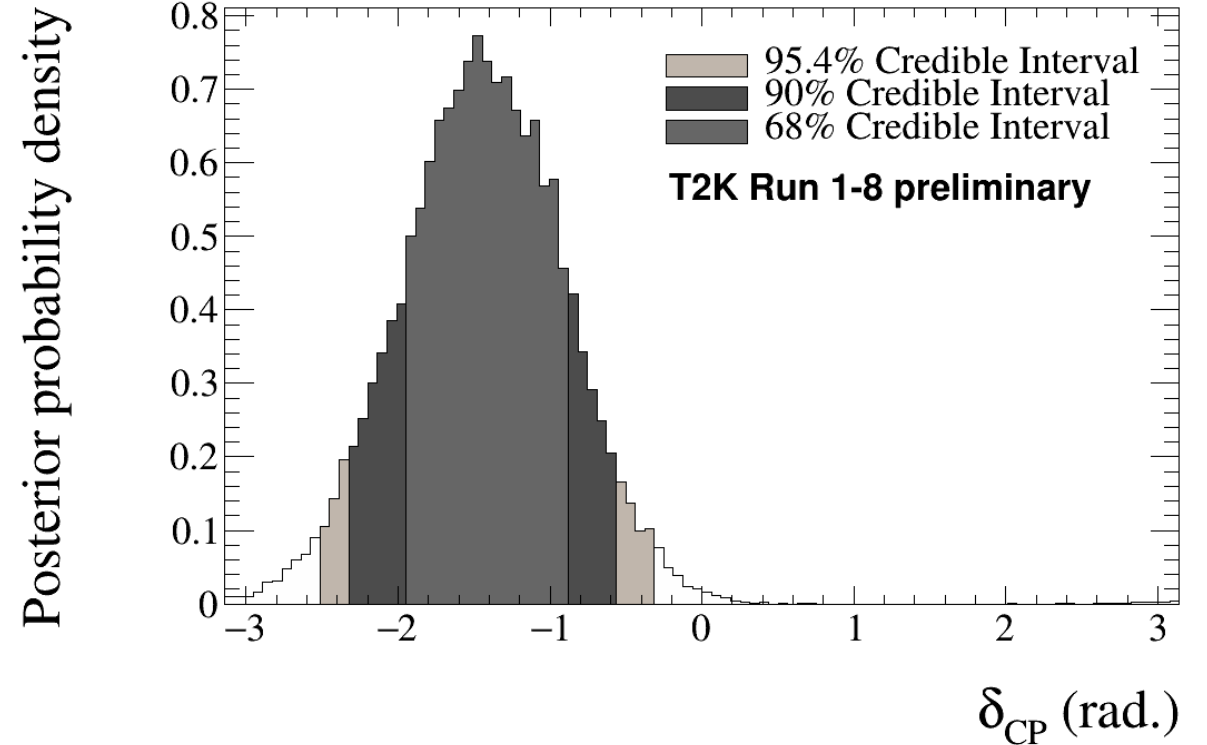
Dcp split by hierarchy- T2K+reactor



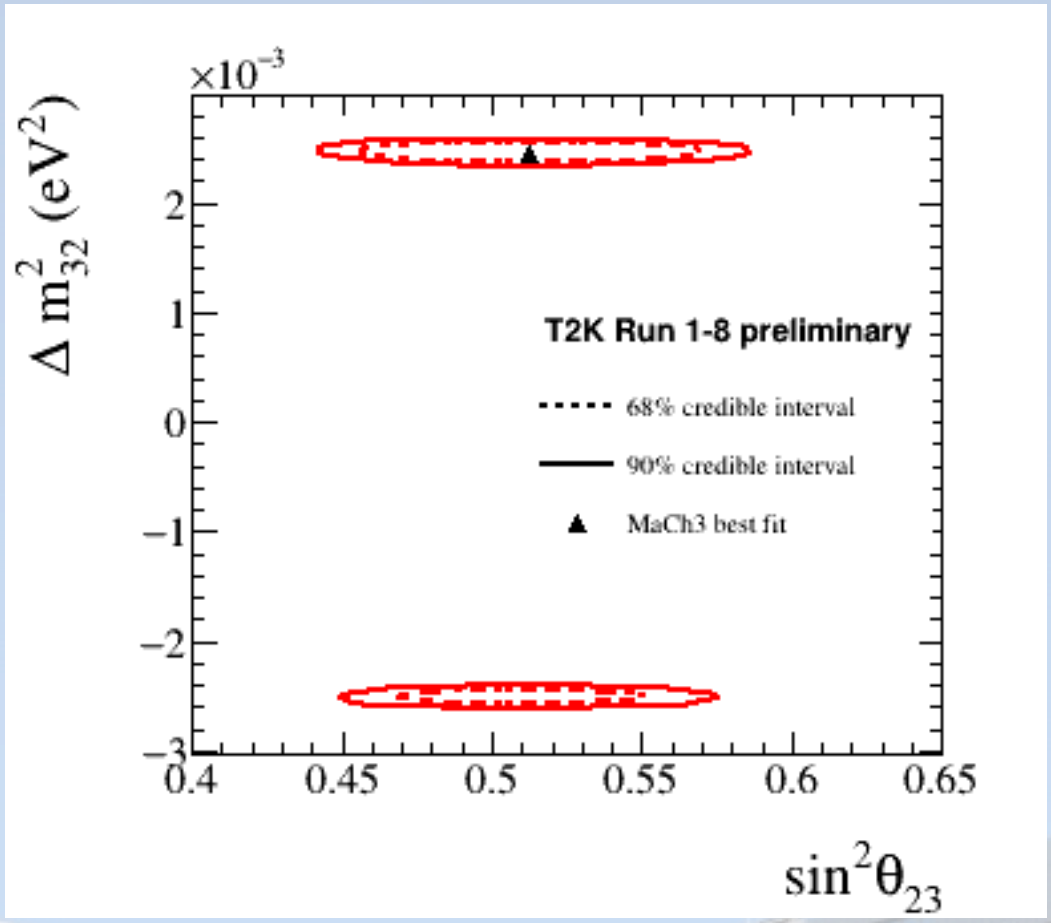
Normal hierarchy



Inverted hierarchy



T2K data only disappearance parameters



Current status – TN331 not approved version

- Results from last August presented with final systematics pending due to non-negligible biases in ND280 data driven simulated data
- Effect on θ_{13} and δ_{CP} appears very small
- Largish effects on Δm^2_{23} and θ_{23}
- Update:
 - Investigation underway
 - Additional systematics being added to analysis
 - Still not expecting much impact on θ_{13} and δ_{CP}

