



BSM Theory: The SM and Beyond

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 **Fermilab**

Topics to (try to) cover

- Review of the SM its “Bugs and Features”
- Case study in BSM: SUSY
- General BSM
- Dark Matter at Colliders and in the Cosmos
- Model Building in the LHC era
- Conclusions

“In theory there is no difference between theory and practice.
But in practice there is.--Yogi Berra”

The Standard Model



Standard Model of Elementary Particles

three generations of matter (fermions)				
	I	II	III	
mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$	0
charge	2/3	2/3	2/3	0
spin	1/2	1/2	1/2	1
	u up	c charm	t top	g gluon
	d down	s strange	b bottom	γ photon
	e electron	μ muon	τ tau	Z Z boson
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson
				H Higgs

	$SU(3)_c$	$SU(2)_w$	$U(1)_Y$	
Q	3	2	$1/6$	$Q \sim (P, Y_0)$
U^c	$\bar{3}$	1	$-2/3$	
D^c	3	1	$+1/3$	$U^c \sim (P, Y_0)^c$
L	1	2	$-1/2$	
E^c	1	1	+1	
H	1	2	$1/2$	

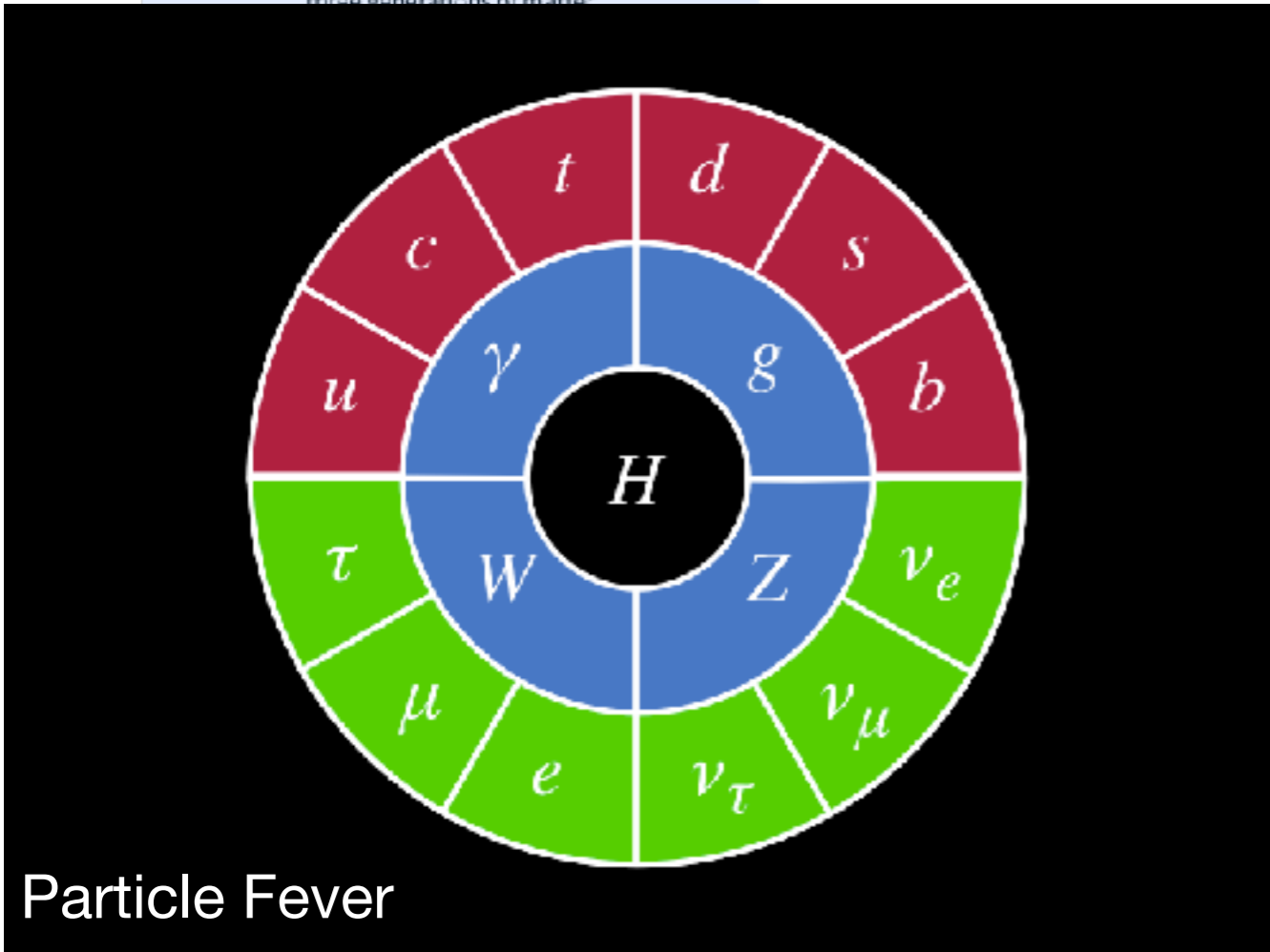
+ Gauge principle

$$D_\mu = \partial_\mu + ig_s T^a A_\mu^a + ig_2 \frac{\sigma^j}{2} W_\mu^j + ig_1 Y B_\mu$$



The Standard Model

Standard Model of Elementary Particles



Particle Fever

	$SU(3)_c$	$SU(2)_w$	$U(1)_Y$	
Q	3	2	$1/6$	$Q \sim (P_c \psi_0)$
U^c	$\bar{3}$	1	$-2/3$	
D^c	$\bar{3}$	1	$+1/3$	$U^c \sim (P_c \psi_0)^c$
L	1	2	$-1/2$	
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+ Gauge principle

$$D_\mu = \partial_\mu + ig_s T^a A_\mu^a + ig_2 \frac{\sigma^j}{2} W_\mu^j + ig_1 Y B_\mu$$



The Standard Model

$$\mathcal{L} = \mathcal{L}_0 + \mathcal{L}_1 + \mathcal{L}_2 + \mathcal{L}_3 + \mathcal{L}_4 + \mathcal{L}_5 + \mathcal{L}_6 + \dots$$

$\mathcal{L}_0 = \Lambda^4$ The cosmological constant...hard to measure @LHC

$\mathcal{L}_1 = \mu^3 \Phi$ Need a gauge singlet scalar, none in SM.

$\mathcal{L}_2 = \pm \mu^2 |H|^2$ Mass term of SM Higgs

$\mathcal{L}_3 = \mu \xi \eta$ Fermion mass term. Sterile neutrinos?

$$\mathcal{L}_4 = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \bar{Q} \not{D} Q + |D_\mu H|^2 - \lambda |H|^4 + y H Q U^c + \dots$$

Gauge kinetic terms, fermion kinetic terms, Higgs self-coupling, Yukawa couplings

The Standard Model

$$\mathcal{L} = \mathcal{L}_0 + \mathcal{L}_1 + \mathcal{L}_2 + \mathcal{L}_3 + \mathcal{L}_4 + \mathcal{L}_5 + \mathcal{L}_6 + \dots$$

Come back to these later

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Gauge kinetic terms, fermion kinetic terms, Higgs self-coupling, Yukawa couplings

The Standard Model

The SM contains 18 **physical** parameters, the Lagrangian contains many more e.g.

$$Y_u^{ij} Q_i U_j^c H + Y_d^{ij} Q_i D_j^c \tilde{H}$$

$Y_{u,d} : 3 \times 3 \mathbb{C}$ matrix $\Rightarrow 2 \times 18$ params

The quark kinetic terms ($\bar{Q} \not{D} Q$ etc.) have $U(3)^3$ broken to $U(1)_B$

Can make 26 field redefinitions to
alter parameters

27 gens. \rightarrow 1 gens

$$36 - 26 = 10$$

**6 quark masses, 3 angles
and 1 phase of CKM**

The Standard Model

What are the 18 **physical** parameters?
 How do we explain them?



$$g_1, g_2, g_3 \quad (\alpha, \sin \theta_W, \alpha_S)$$

3

$$\langle H \rangle \equiv v, \lambda_h$$

2

$$m_{e, \mu, \tau}$$

3

= 18

$$m_{u, d, c, s, b, t}$$

6

$$V_{CKM} \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

4

$$\theta_{QCD}, m_{\nu_e, \nu_\mu, \nu_\tau}, V_{PMNS}$$

1+3+4

(Depends on neutrino mass model)

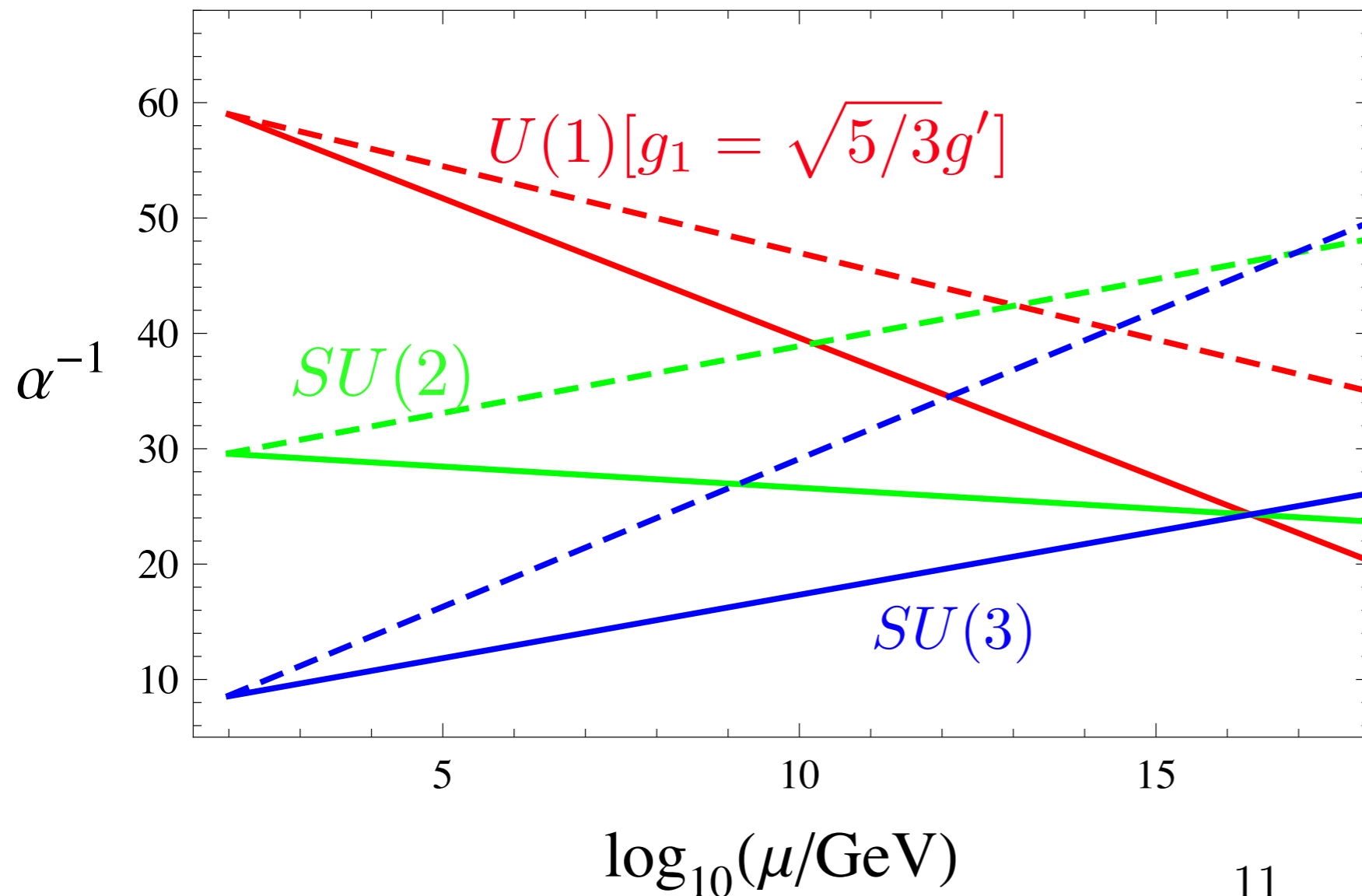
Bugs and Features

Gauge coupling unification

1 generation of SM matter fits into $\bar{\mathbf{5}}, \mathbf{10}$ of SU(5)

SM + N fits into $\mathbf{16}$ of SO(10)

$$\frac{d}{dt} \alpha_i^{-1} = -\frac{b_i}{2\pi}$$



SM

$$b_i = (-41/10, 19/6, 7)$$

MSSM

$$(b_1, b_2, b_3) = (-33/5, -1, 3)$$

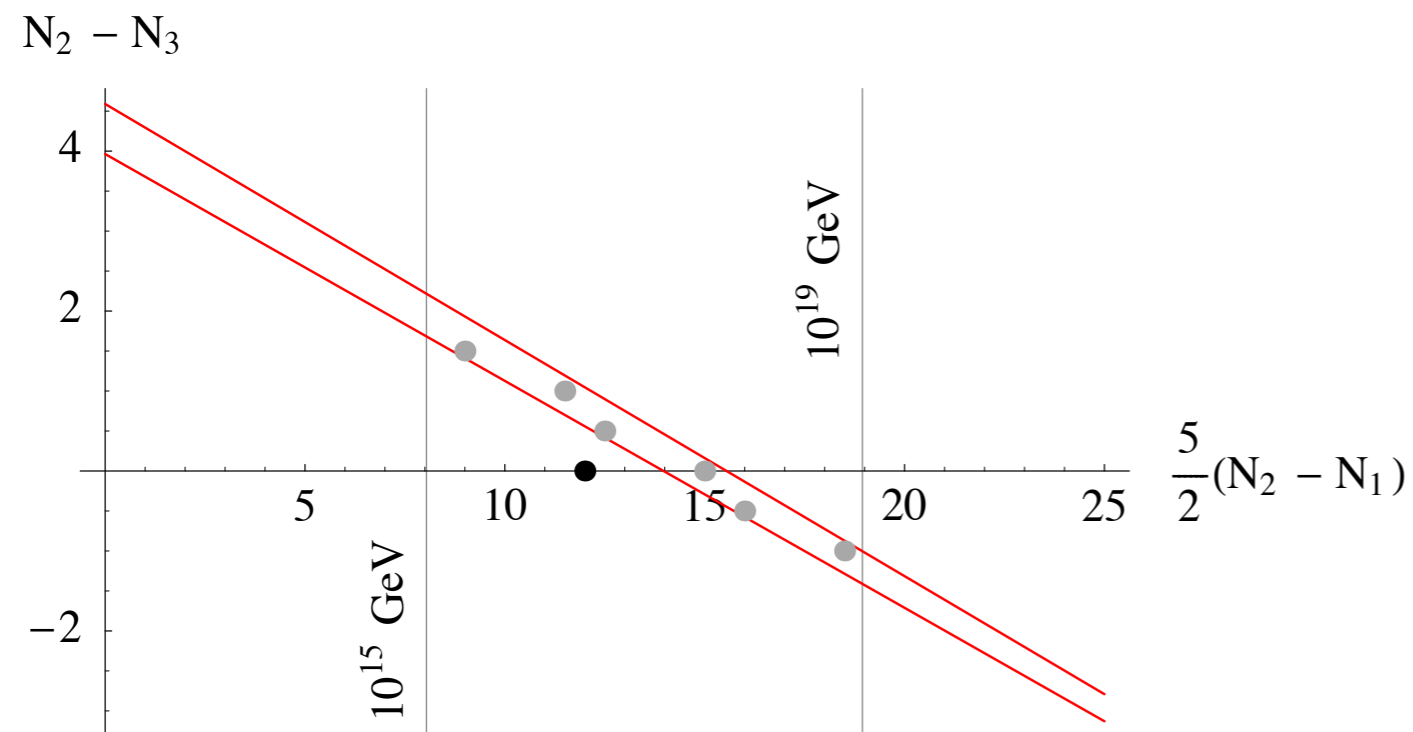
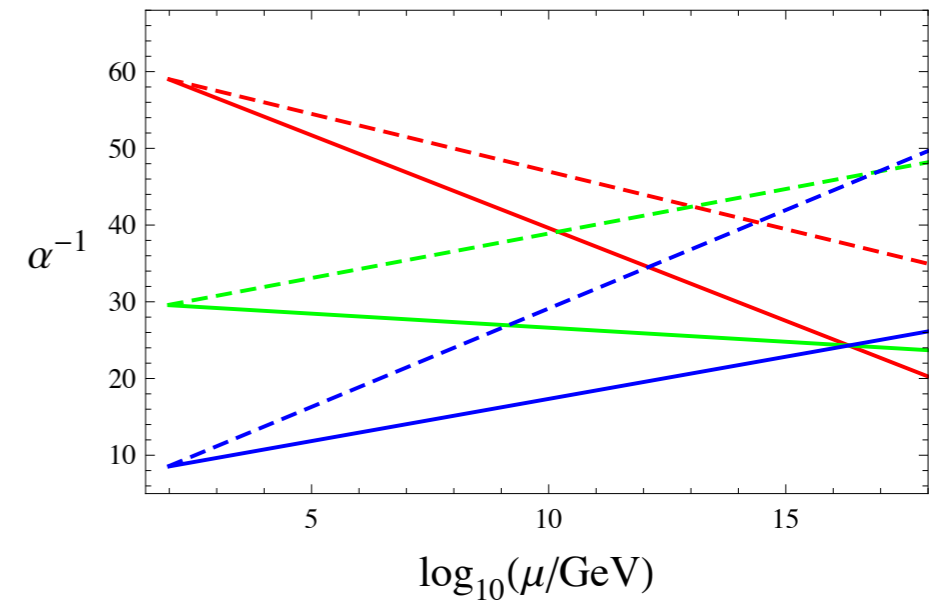
$$b = \frac{11}{3}N - \frac{2}{3} \sum_{fermions} C(r_f) - \frac{1}{3} \sum_{bosons} C(r_b)$$

Bugs and Features

Gauge coupling unification

Hint for what new physics?

Many possible combinations of weak scale states give good unification e.g. MSSM, NMSSM, 6 Higgs doublets,



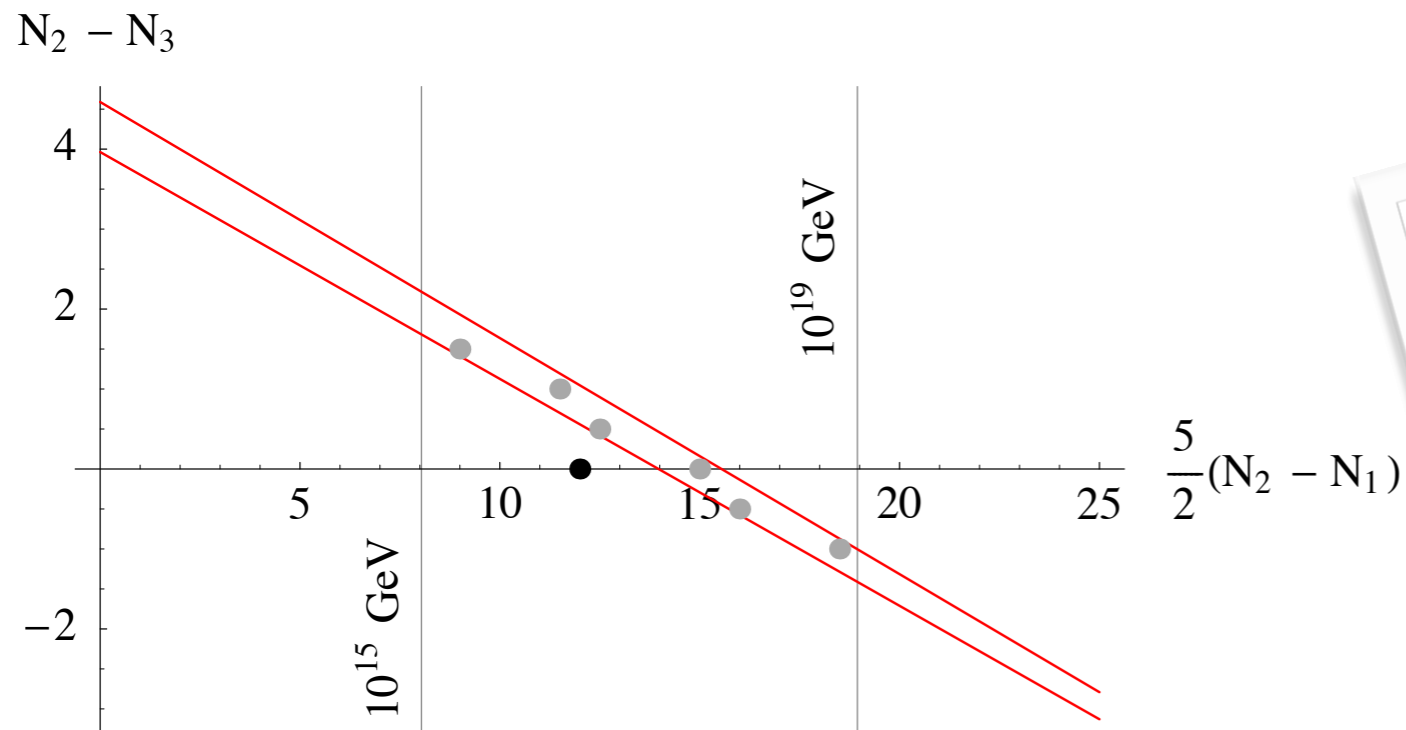
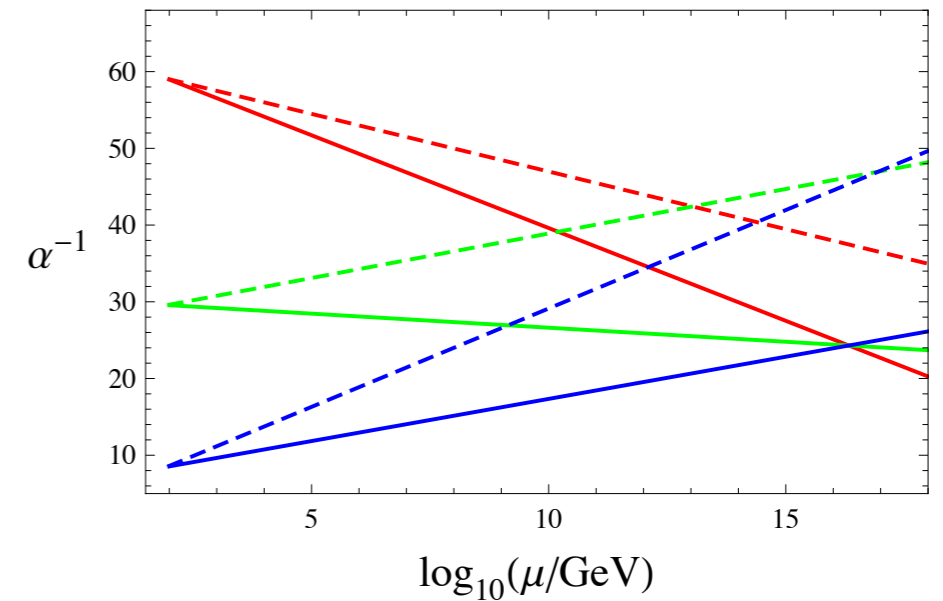
[Giudice, Romanino, ph/0406088]

Bugs and Features

Gauge coupling unification

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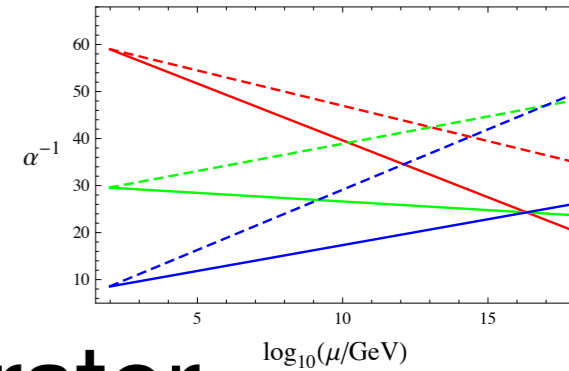
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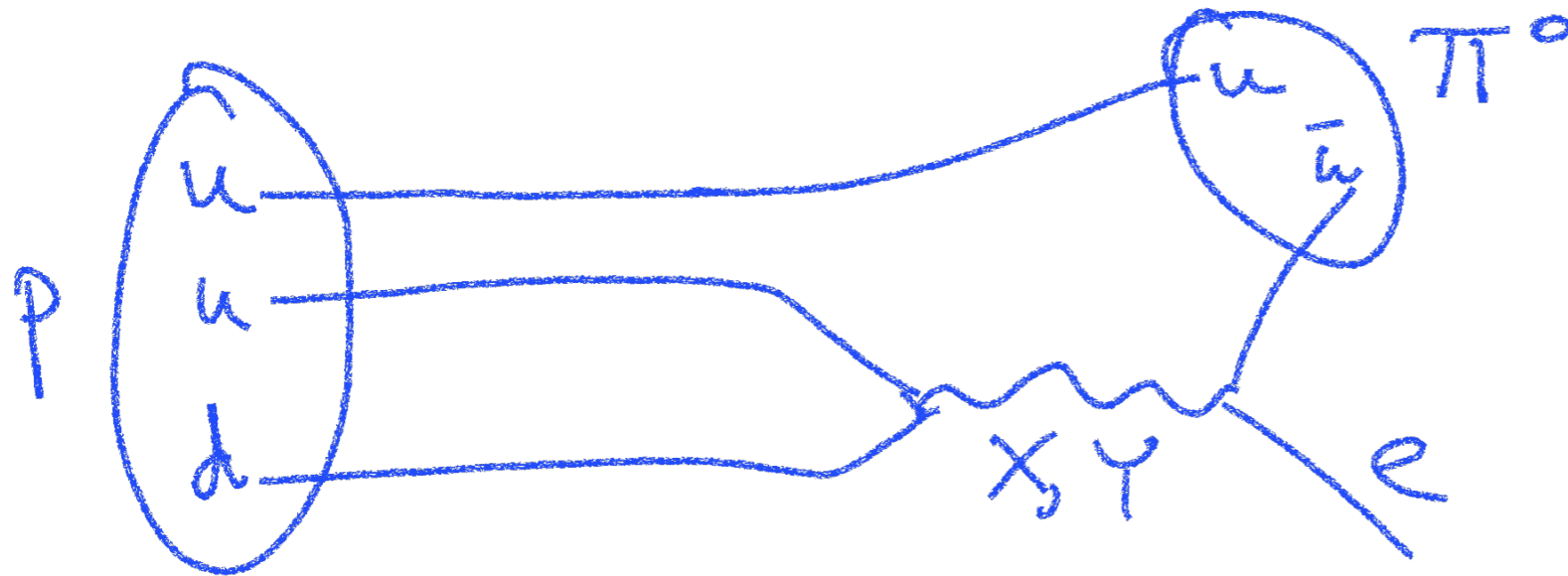
Predictions?
New states at weak scale with SM charge
New states at GUT scale
— proton decay!

[Giudice, Romanino, ph/0406088]

Gauge coupling unification



X, Y lead to proton decay, generate dim-6 operator

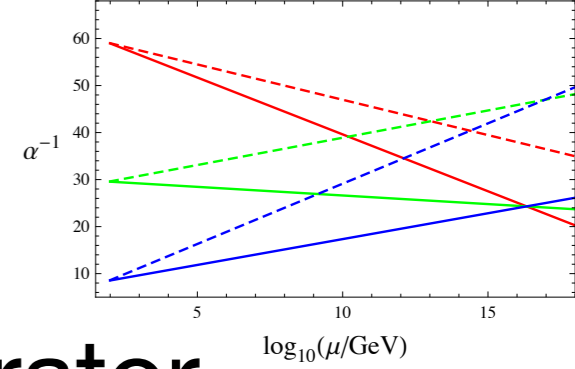


$$\frac{g_X^2}{M_X^2} (\bar{u}\gamma_\mu d) (\bar{e}\gamma^\mu u)$$

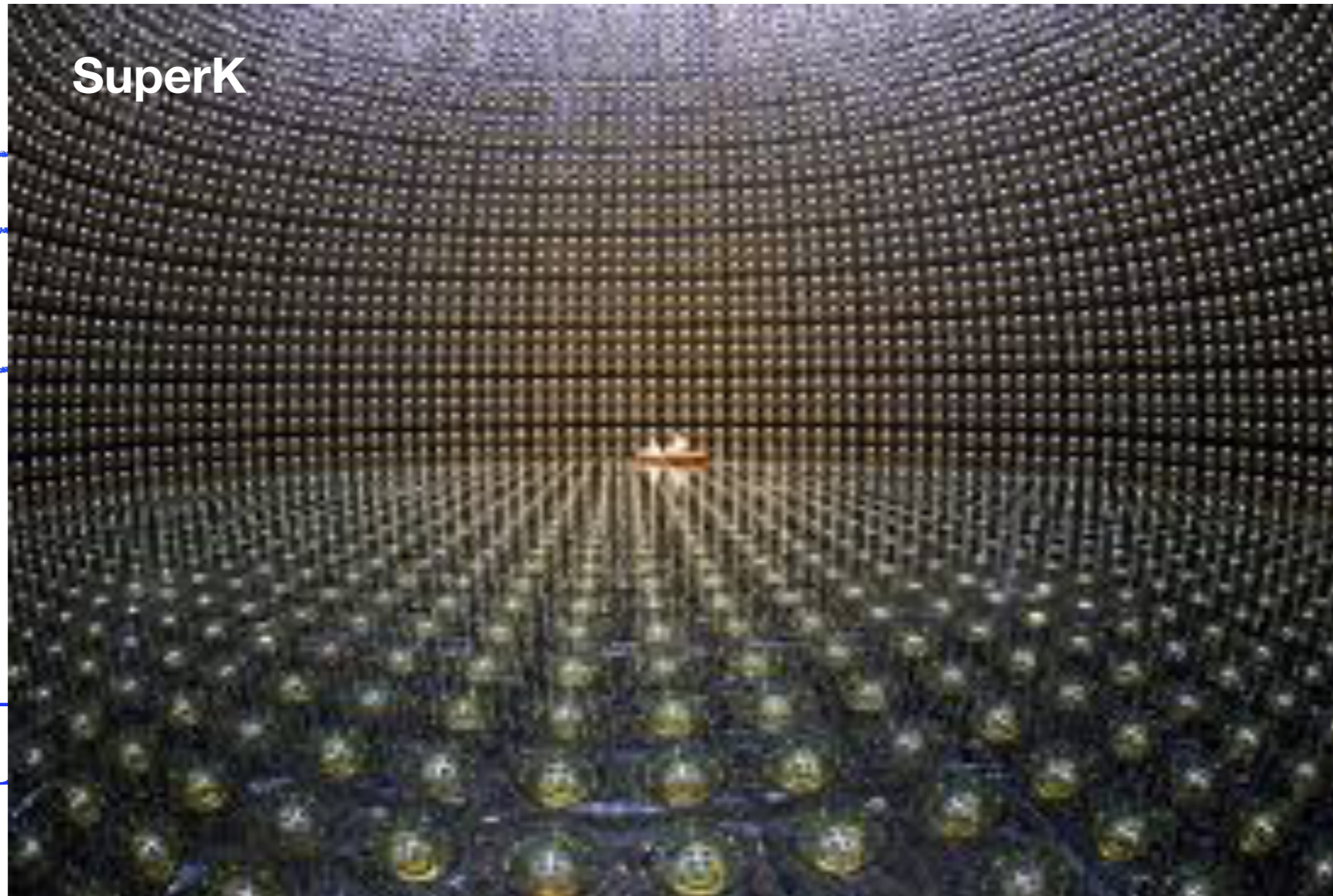
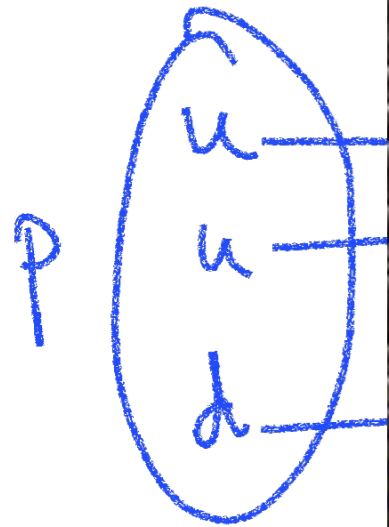
$$\Gamma \sim \left(\frac{g_X}{M_X^2} \right)^2 m_p^5 \times \text{NP} \quad \tau \sim 10^{32(24)} \text{ yr}$$

Use Avogadro's number to our advantage

Gauge coupling unification



X, Y lead to proton decay, generate dim-6 operator



$$d) (\bar{e}\gamma^\mu u)$$

$$\Gamma \sim \left(\dots \right) \text{yr}$$

Use Avogadro's number to our advantage

Bugs and Features

See Jure Zupan's lectures

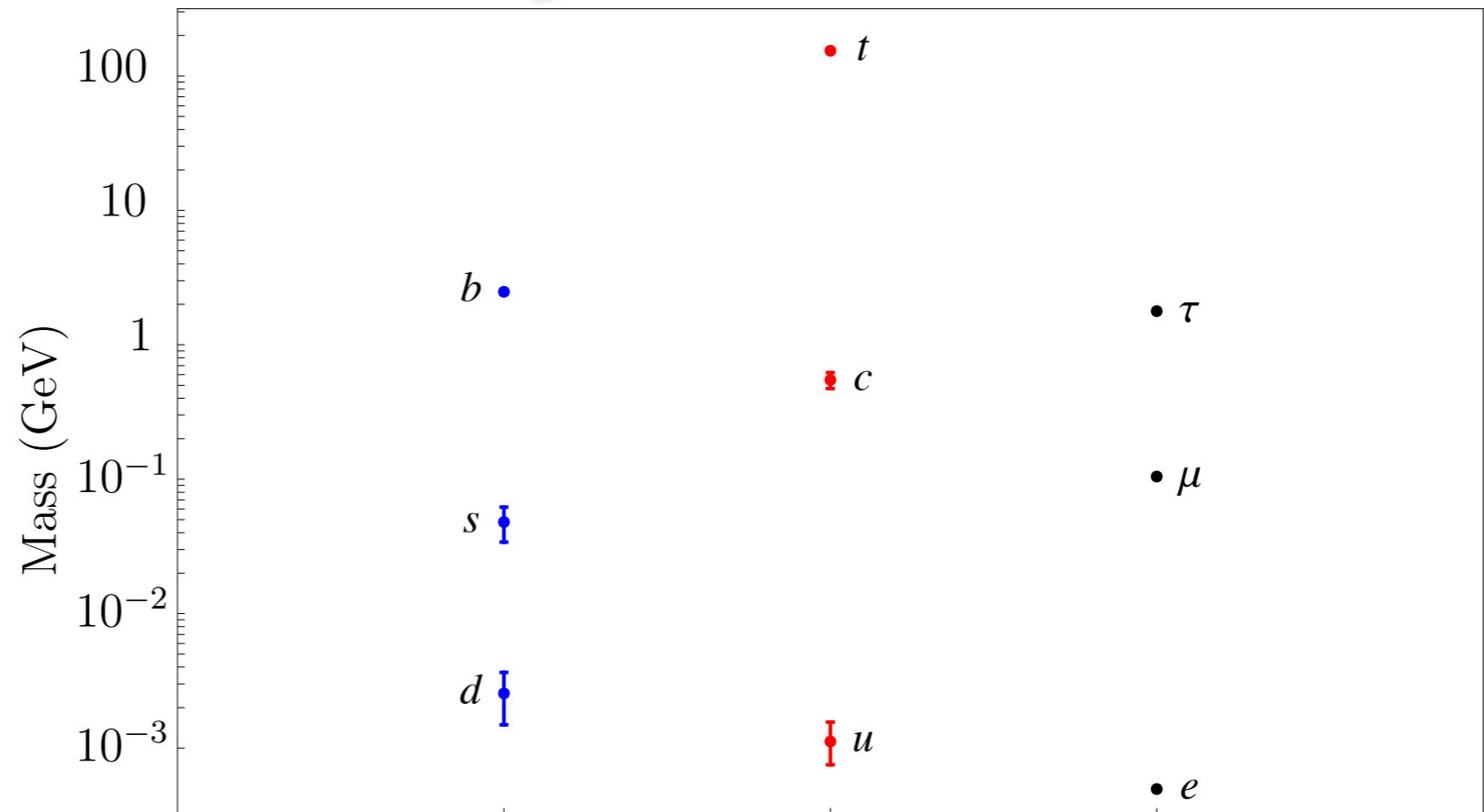
Fermion masses, and mixings

What explains this hierarchy?

Technically natural

$$\delta m_f \sim \frac{g^2}{16\pi^2} m_f \log\left(\frac{\Lambda}{m_f}\right)$$

chiral symmetry



SM has no tree-level FCNC's

BSM physics probed indirectly for FCNC searches

Bugs and Features

See Jure Zupan's lectures

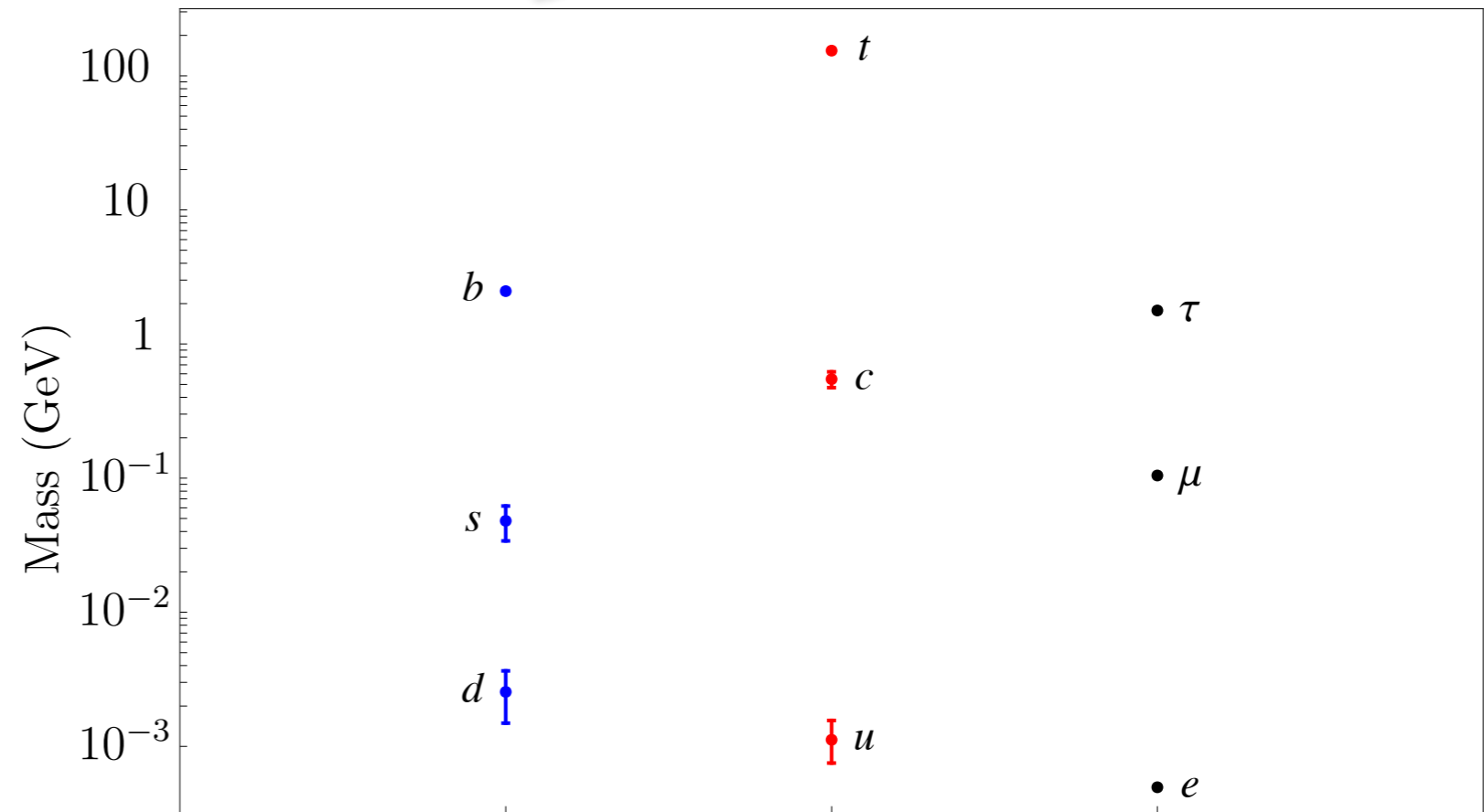
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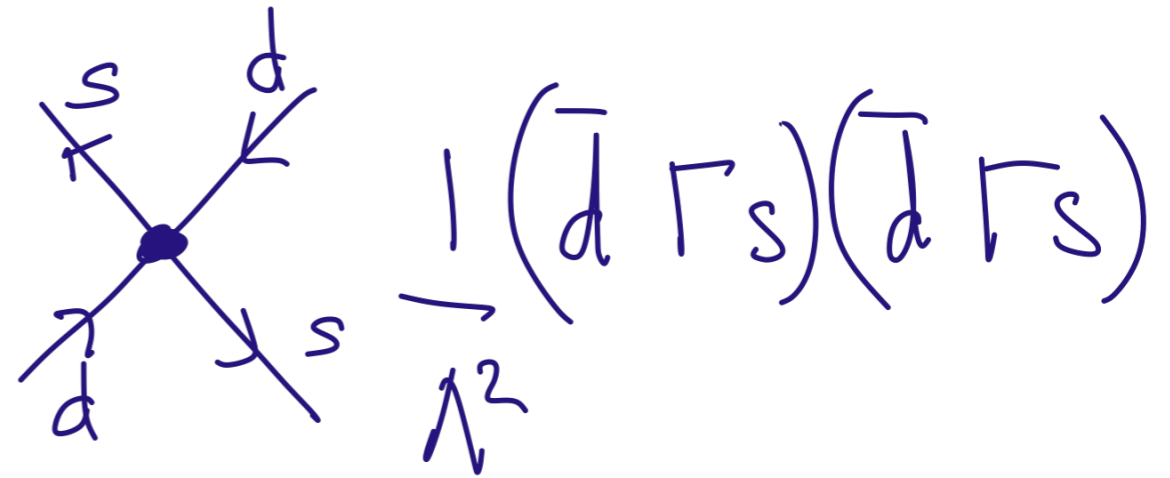
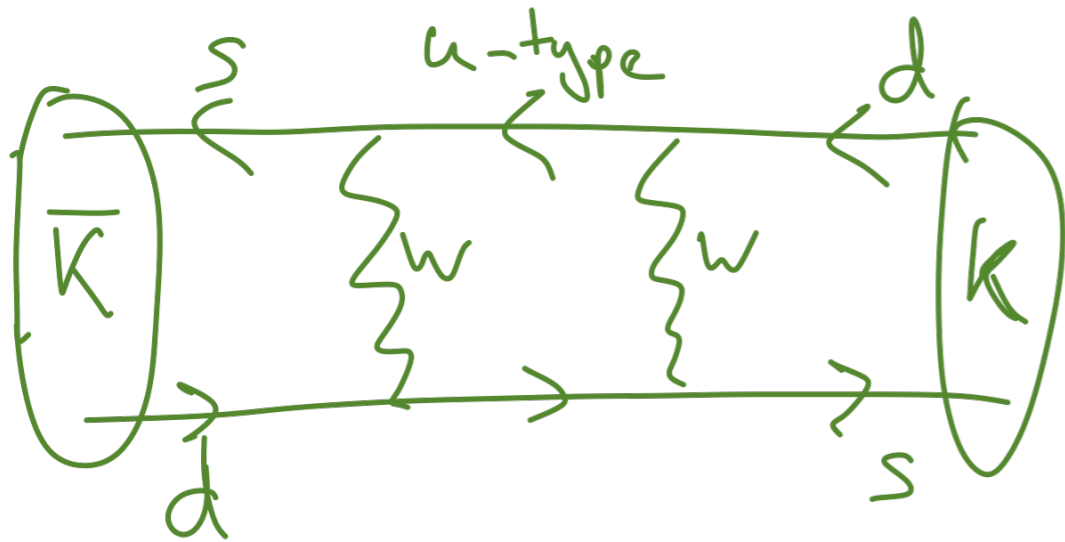


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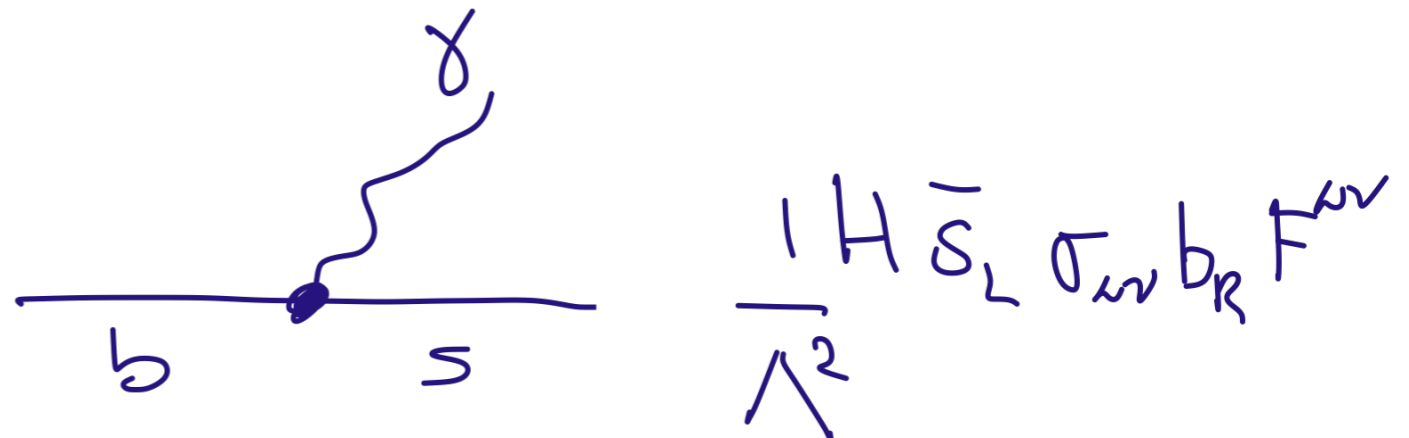
BSM physics probed indirectly for FCNC searches

Neutrinos?

Fermion masses, and mixings



$$\Lambda \geq 1000 - 10000 \text{ TeV}$$



$$\Lambda \geq 100 \text{ TeV}$$

BSM physics must have a carefully controlled flavour structure e.g. MFV

Bugs and Features

(see A. Shukraft lectures)

Neutrino masses-another window to high scales?

Not present in the SM, but observed in Nature

Dirac? $yLHN$ $y \sim 10^{-12}$ Lepton number ✓

Majorana? $\mathcal{L}_5 = \frac{1}{\Lambda} (LH) (LH)$ $\Lambda \sim 10^{14}$ GeV
Lepton number ✗

only dim-5 op...already observed?

Neutrino model building



Dial "N" for neutrino



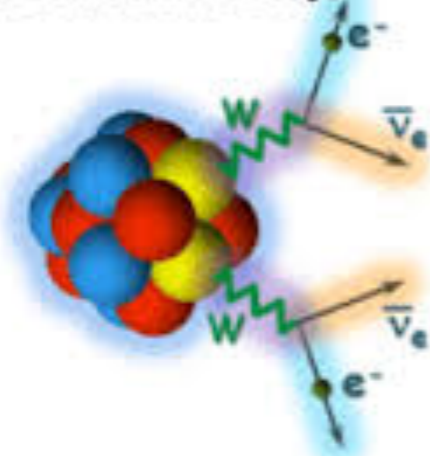
See-saw mechanism, new states at high scale
 Low energy observable

$$yLHN + MNN \rightarrow \frac{y^2}{M} (LH) (LH)$$

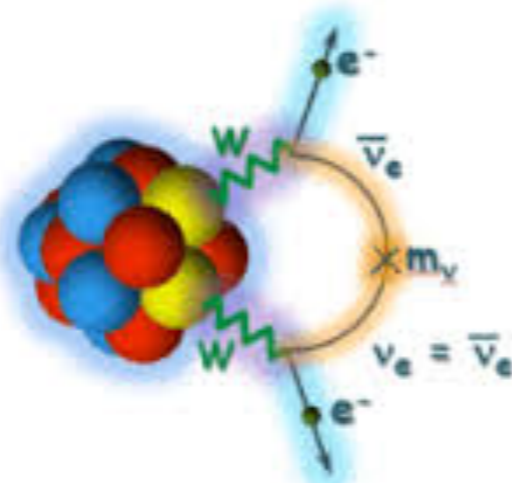


$0\nu\beta\beta$

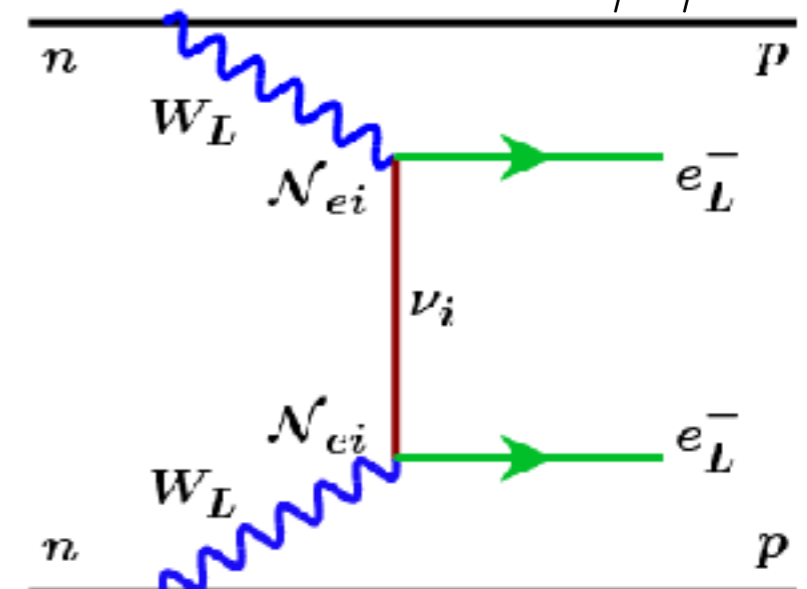
[Double beta decay]



Double beta decay which emits anti-neutrinos



Neutrinoless double beta decay



Dial "N" for neutrino

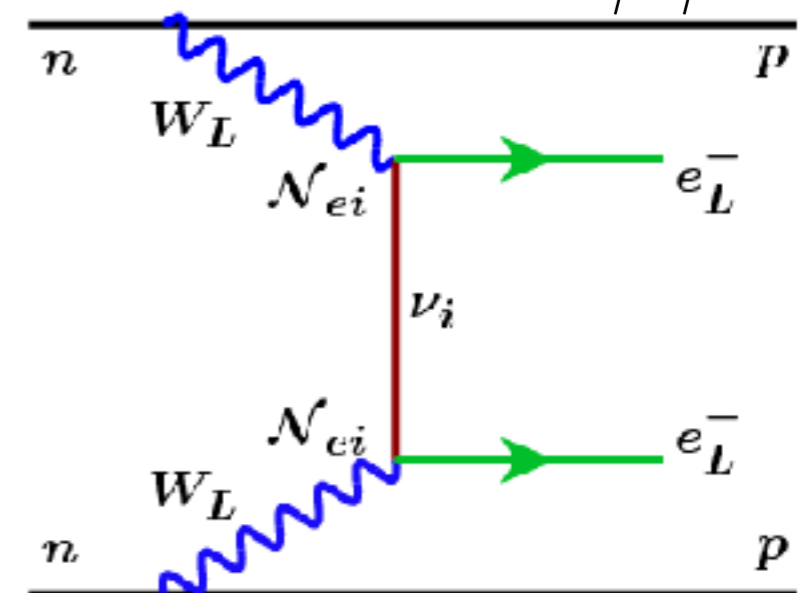
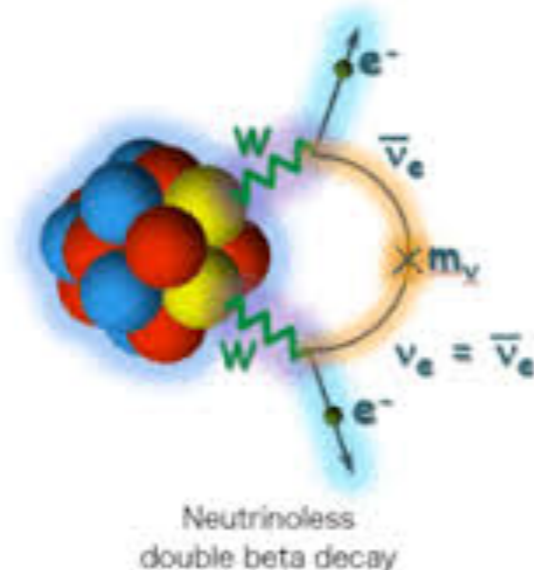
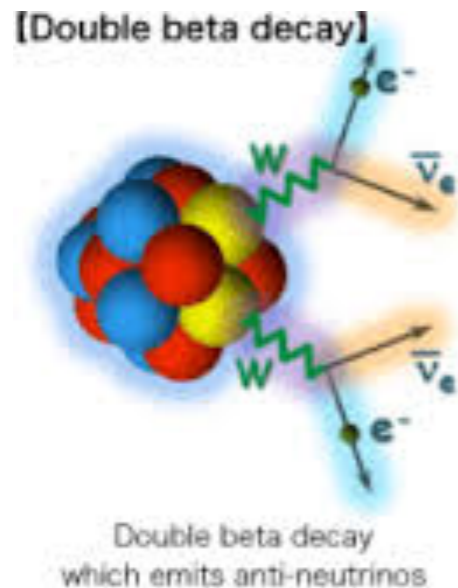


See-saw mechanism, new states at high scale
 Low energy observable

$$yLHN + \underbrace{MNN}_{\mathcal{L}_3} \rightarrow \frac{y^2}{M} \underbrace{(LH)(LH)}_{\mathcal{L}_5}$$



$0\nu\beta\beta$



Bugs and Features

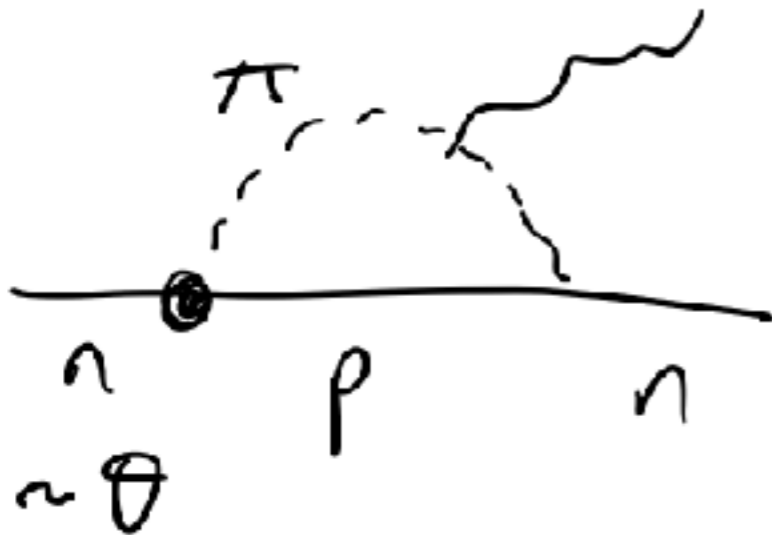
Strong CP problem

$$\mathcal{L}_4 \supset \theta_{QCD} G_{\mu\nu}^a G_{\alpha\beta}^a \epsilon^{\mu\nu\alpha\beta}$$

Dim-4 term violates CP (like E.B)

Leads to neutron electric dipole moment

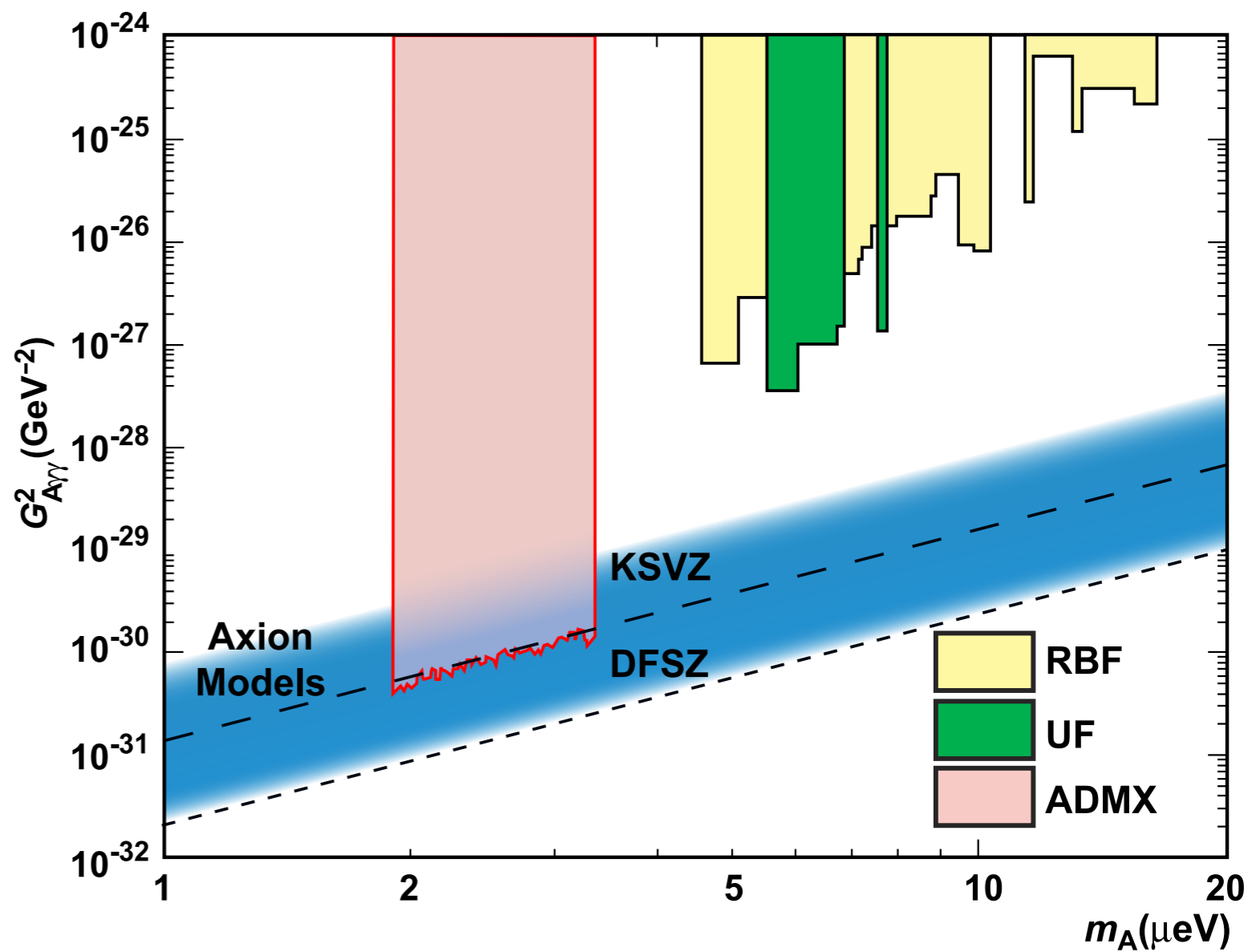
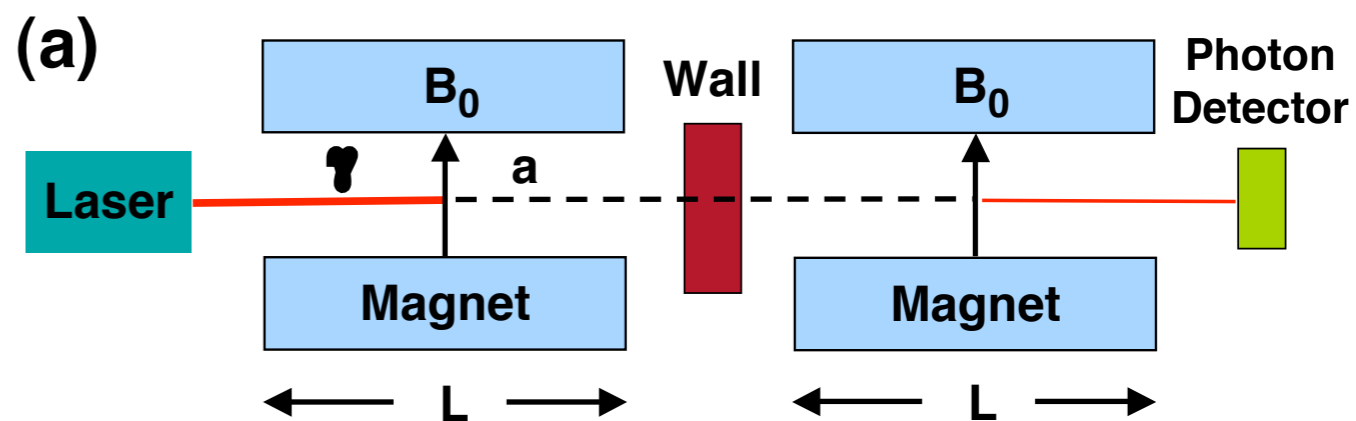
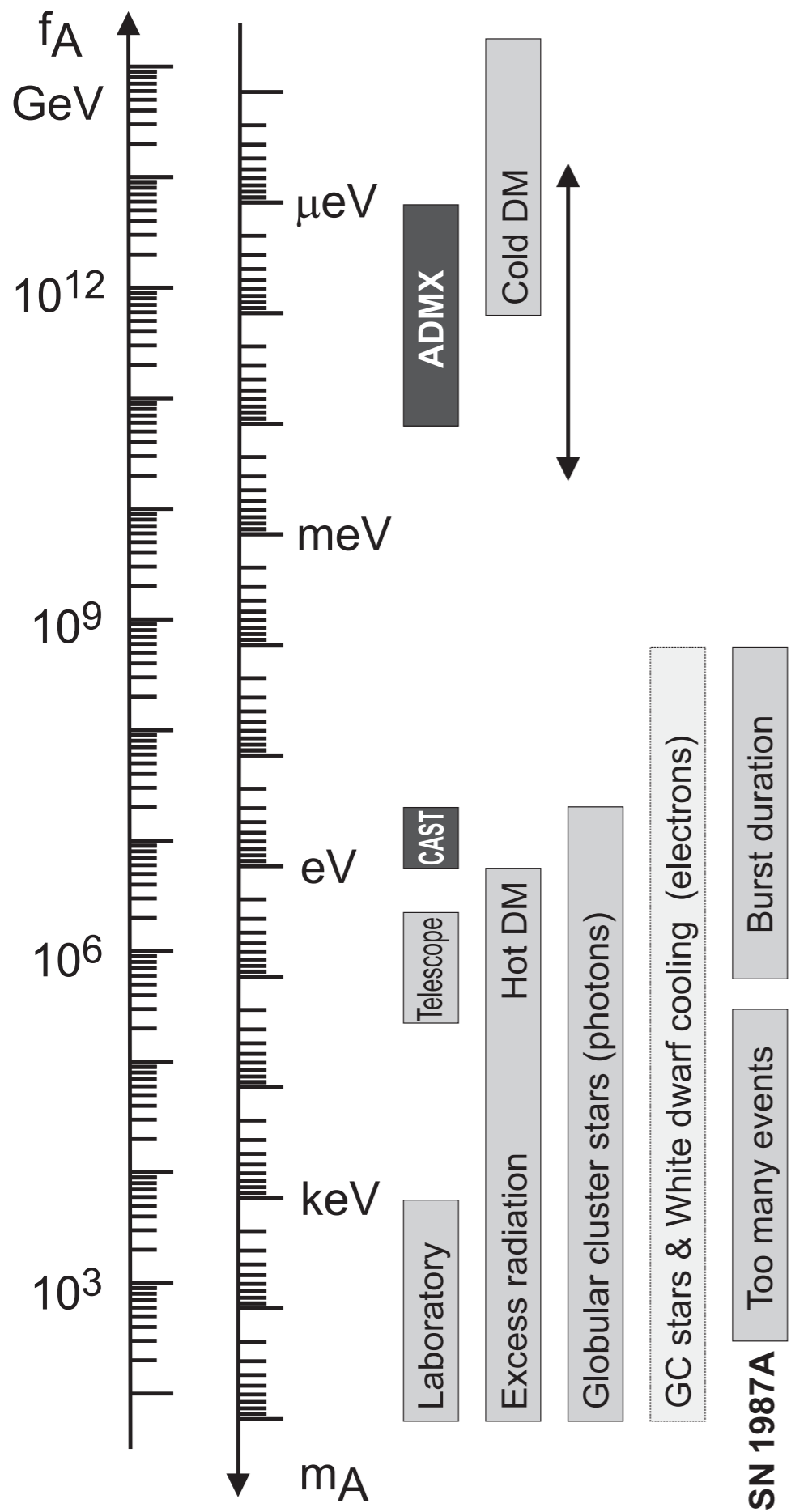
$$d_n \leq 10^{-26} e \text{ cm}$$



$$d_n \sim \theta \frac{eg_A}{(4\pi f_\pi)^2} \frac{m_u m_d}{m_u + m_d} \log \frac{m_n^2}{m_\pi^2}$$
$$\sim \theta \times 10^{-16} e \text{ cm}$$

Massless up quark? (probably not)

Symmetry protection? e.g. Peccei-Quinn, Nelson-Barr



Bugs and Features

Hierarchy (Naturalness) problem

$$\mathcal{L}_2 = \pm \mu^2 |H|^2$$

Why is μ so much smaller than M_{GUT}, M_{Pl} ?

Unlike fermions (and gauge bosons) no symmetry protects scalar mass parameter

1. Nature is fine-tuned (anthropics?)
2. The SM has no high scales (gravity?, unification?)
3. New dynamics/symmetries keeps mass scale low



Bugs and Features

Hierarchy (Naturalness) problem

$$\mathcal{L}_2 = \pm \mu^2 |H|^2$$

Why is μ so small?

There is something fascinating about science. One gets such wholesale returns of conjecture out of such a trifling investment of fact.

—Mark Twain

Unlike fermions (and gauge bosons) no symmetry protects scalar mass parameter

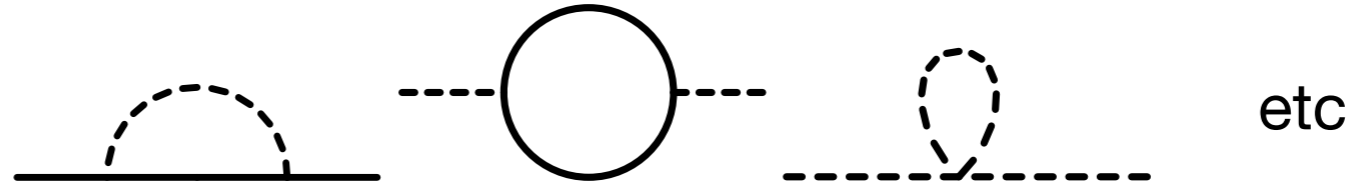
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Hierarchy (Naturalness) problem



$$\mathcal{L} = |\partial_\mu \phi|^2 + \bar{\psi} i \not{\partial} \psi - m_f \bar{\psi} \psi - y \phi \bar{\psi} \psi - \mu^2 |\phi|^2 - \lambda |\phi|^4$$



$$\Delta m_f \sim -\frac{y^2}{16\pi^2} m_f \log \left(\frac{\Lambda}{m_f} \right)$$

$$\Delta \mu^2 \sim \frac{\lambda - y^2}{16\pi^2} \Lambda^2 - \frac{y^2}{16\pi^2} m_f^2 \log \frac{\Lambda}{m_f}$$

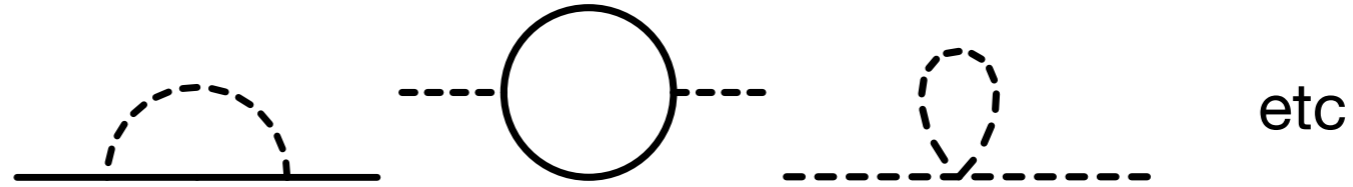
Scalars are sensitive to the highest scale in the theory!

Expect new physics (Λ) at $\frac{4\pi}{g} m_h$

Hierarchy (Naturalness) problem



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*Possible
solution?*

Scalars are sensitive to the highest scale in the theory!

Expect new physics (Λ) at $\frac{4\pi}{g} m_h$

Hierarchy (Naturalness) problem

SM Higgs sensitivity (how low ~~can you~~ go)



$$\delta m_h^2 = \alpha_t \Lambda_t^2 + \alpha_g \Lambda_g^2 + \alpha_h \Lambda_h^2$$

$$\alpha_t = \frac{3m_t^2}{4\pi^2 v^2}, \quad \alpha_g = -\frac{6m_W^2 + 3m_Z^2}{16\pi^2 v^2}, \quad \alpha_h = -\frac{3m_h^2}{16\pi^2 v^2}$$

(One) Measure of fine tuning: $D_i(m_h) \equiv \left| \frac{\partial \log m_h^2}{\partial \log \Lambda_i^2} \right| = \frac{|\alpha_i| \Lambda_i^2}{m_h^2}$

No guaranteed discovery, unlike Higgs mechanism

Should not stop us looking!!

Hierarchy (Naturalness) problem

SM Higgs sensitivity (how low *does Nature go*)



$$\delta m_h^2 = \alpha_t \Lambda_t^2 + \alpha_g \Lambda_g^2 + \alpha_h \Lambda_h^2$$

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Supersymmetry...a BSM case study



(more than) Doubling of the spectrum

SM Field	SU(3)	SU(2)	U(1)	MSSM partner	Superfield
q_i (LH quarks)	3	2	$\frac{1}{6}$	\tilde{q}_i (LH squarks)	Q_i
u_i^c (RH top, charm, up)	$\bar{3}$	1	$-\frac{2}{3}$	\tilde{u}_i^c (RH stop, scharm, sup)	U_i^c
d_i^c (RH bottom, strange, down)	$\bar{3}$	1	$\frac{1}{3}$	\tilde{d}_i^c (RH sbottom, sstrange, sdown)	D_i^c
ℓ_i (LH leptons)	1	2	$-\frac{1}{2}$	$\tilde{\ell}_i$ (LH sleptons)	L_i
e_i^c (RH tau, muon, electron)	1	1	1	\tilde{e}_i^c (RH stau, smuon, selectron)	E_i^c
h_u (h_d) (up-type (down-type) Higgs)	1	2	$\frac{1}{2}$ ($-\frac{1}{2}$)	\tilde{h}_u (\tilde{h}_d) (up-type (down-type) higgsino)	H_u (H_d)
gluino	8	1	0	gluino	
W/Z	1	3	0	Wino/Zino	
B/photon	1	1	0	bino/photino	

Superpartners have the same couplings as SM partners

If SUSY (softly) broken they have different masses

Many new interactions...>100 new parameters!

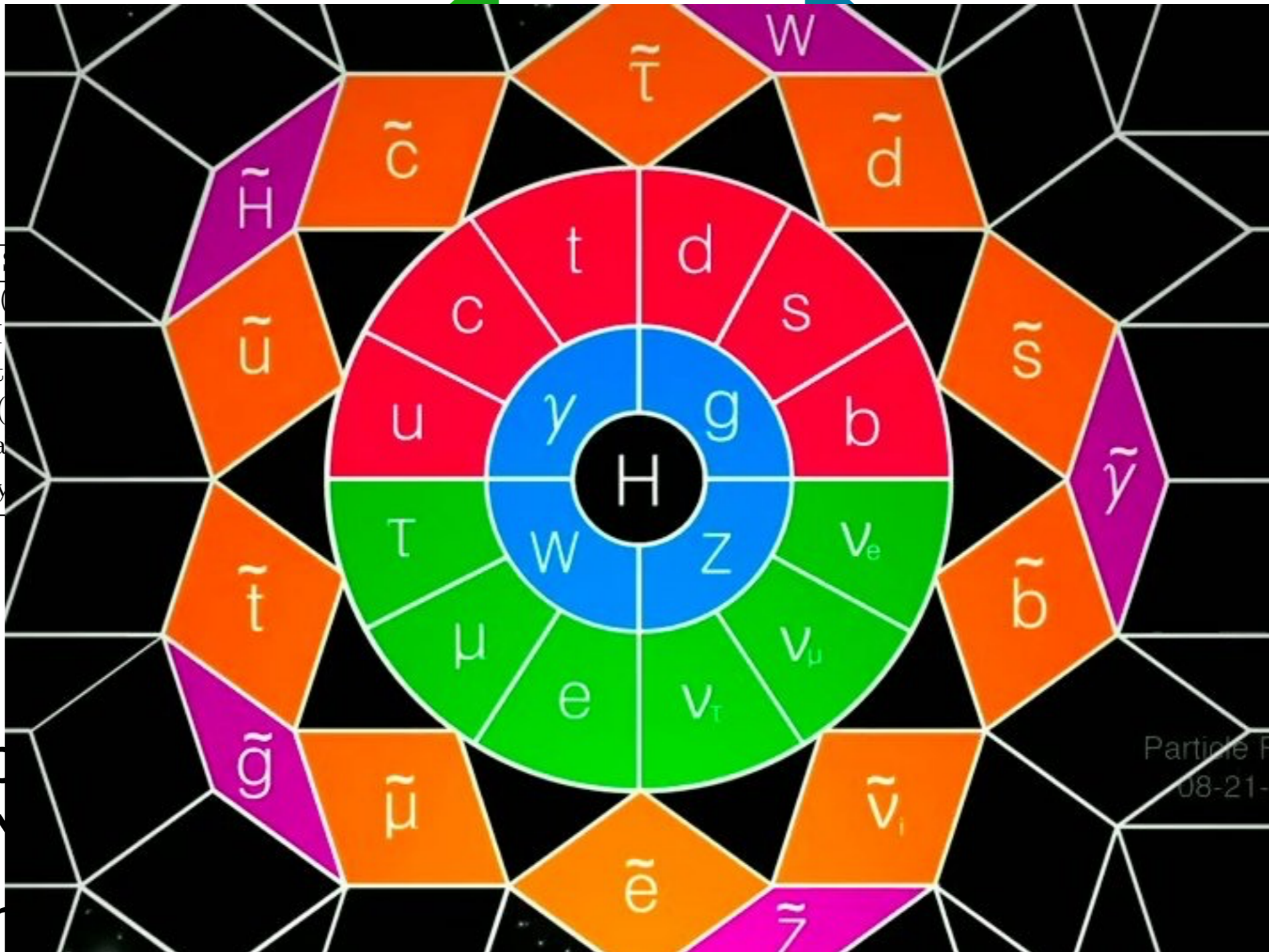
Many constrained by flavour, CP-violation

SUSY breaking models (GMSB, AMSB, ...) predict relations

Supersymmetry...a BSM case study



q_i (LH)
u_i^c (RH)
d_i^c (RH bot)
l_i (LH)
e_i^c (RH ta)
h_u (h_d) (up-ty)



Superfield
Q_i
U_i^c
D_i^c
L_i
E_i^c
H_u (H_d)

Superp
If SUSY
Many r

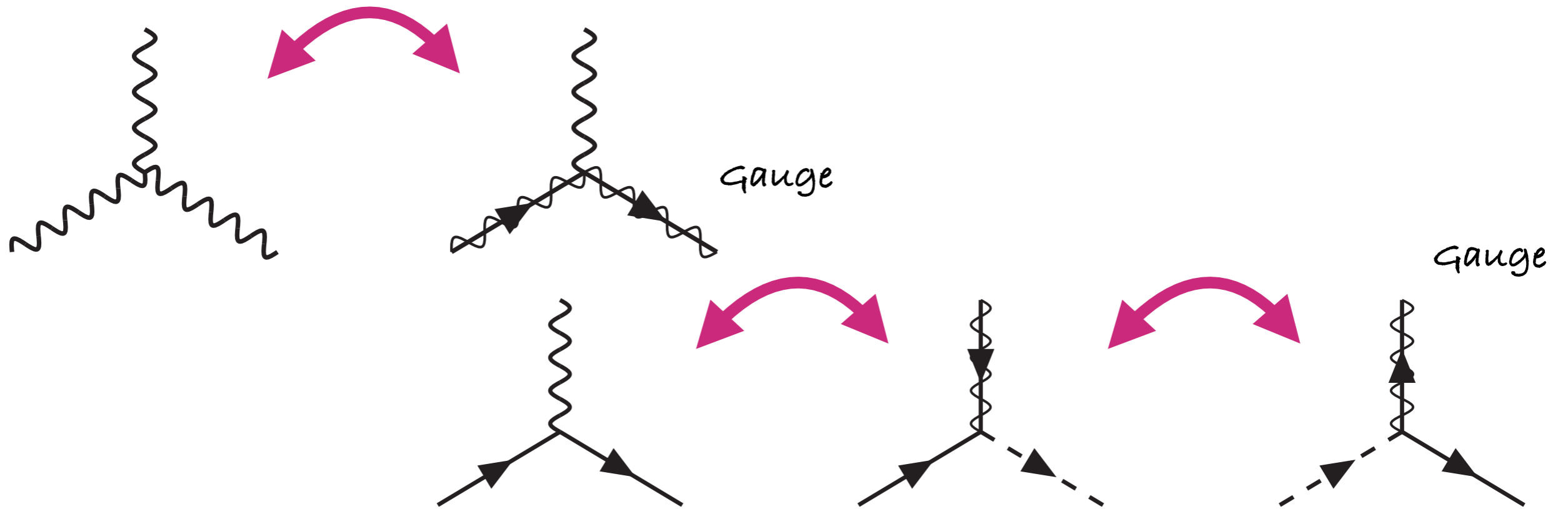
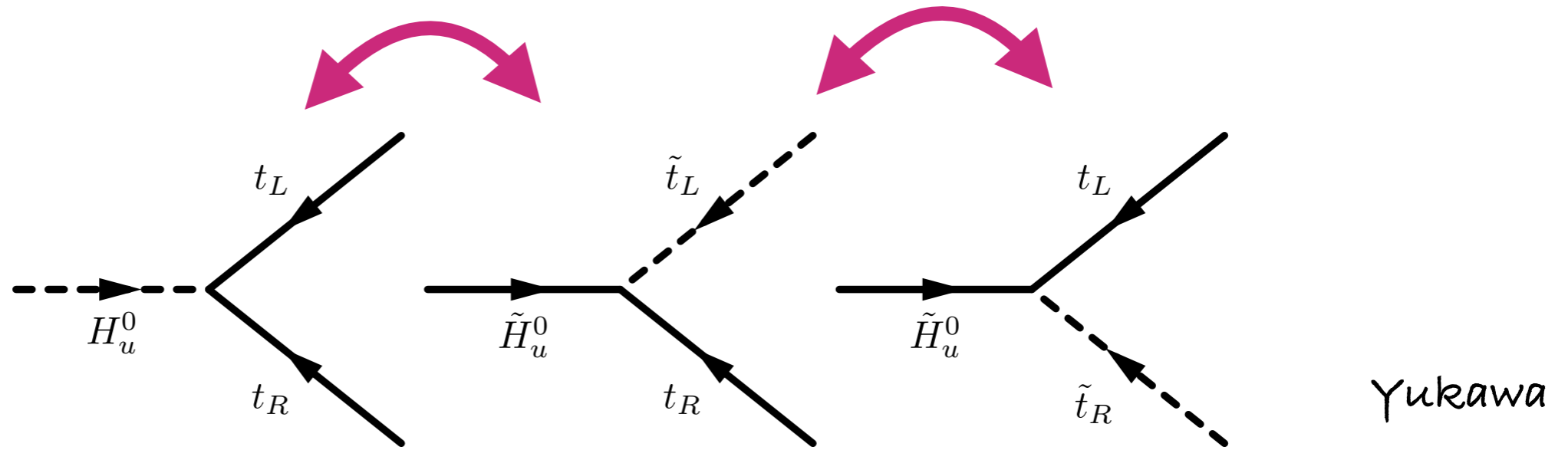
Partners
S

Many constrained by flavour, CP-violation
SUSY breaking models (GMSB, AMSB, ...) predict relations

Supersymmetry

$$W_{MSSM} = Y_U U^c Q H_u - Y_D D^c Q H_d - Y_E E^c L H_d + \mu H_u H_d$$

Flip two

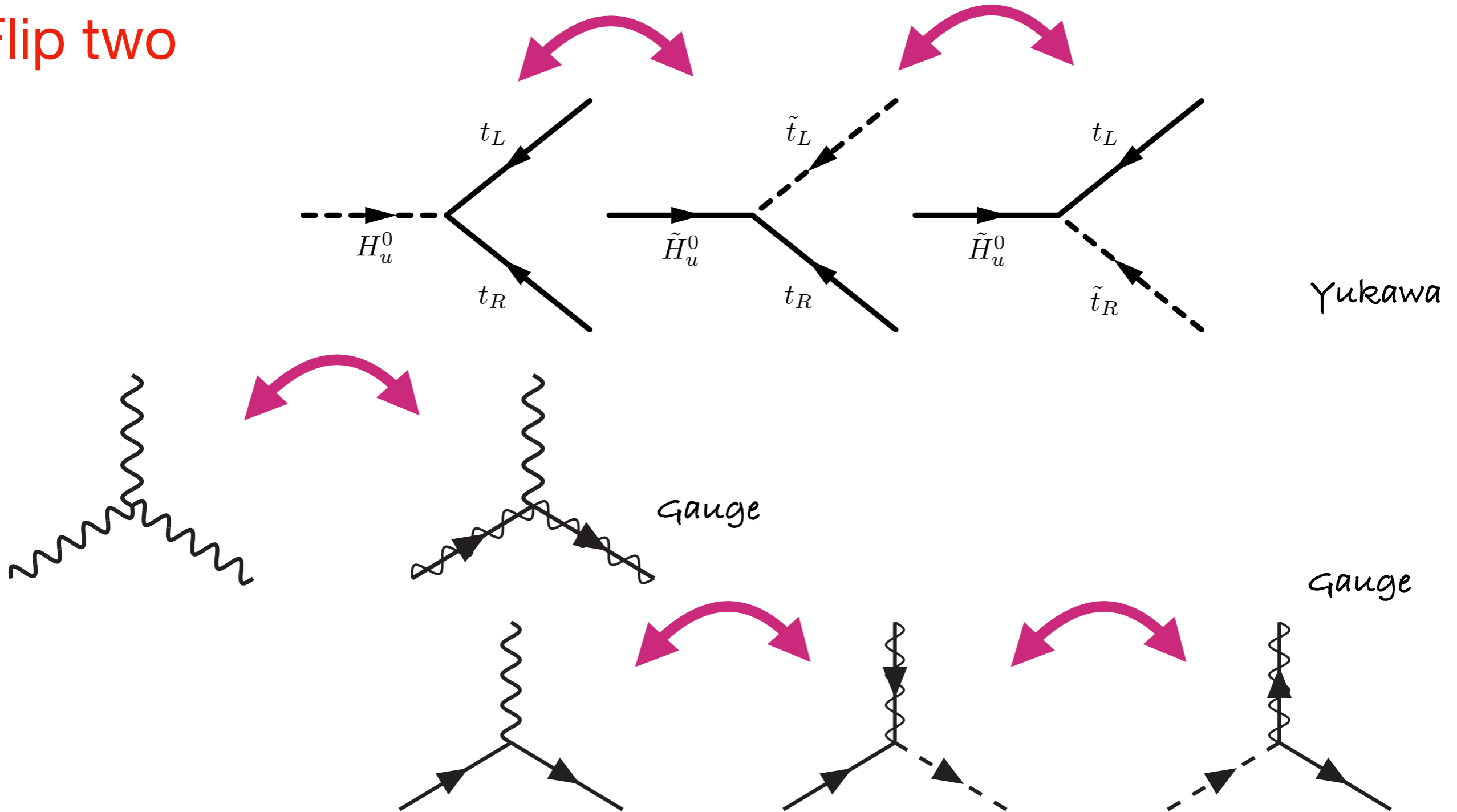


Supersymmetry

Extended Higgs sector Higgs modifications

$$W_{MSSM} = Y_U U^c Q H_u - Y_D D^c Q H_d - Y_E E^c L H_d + \mu H_u H_d$$

Flip two

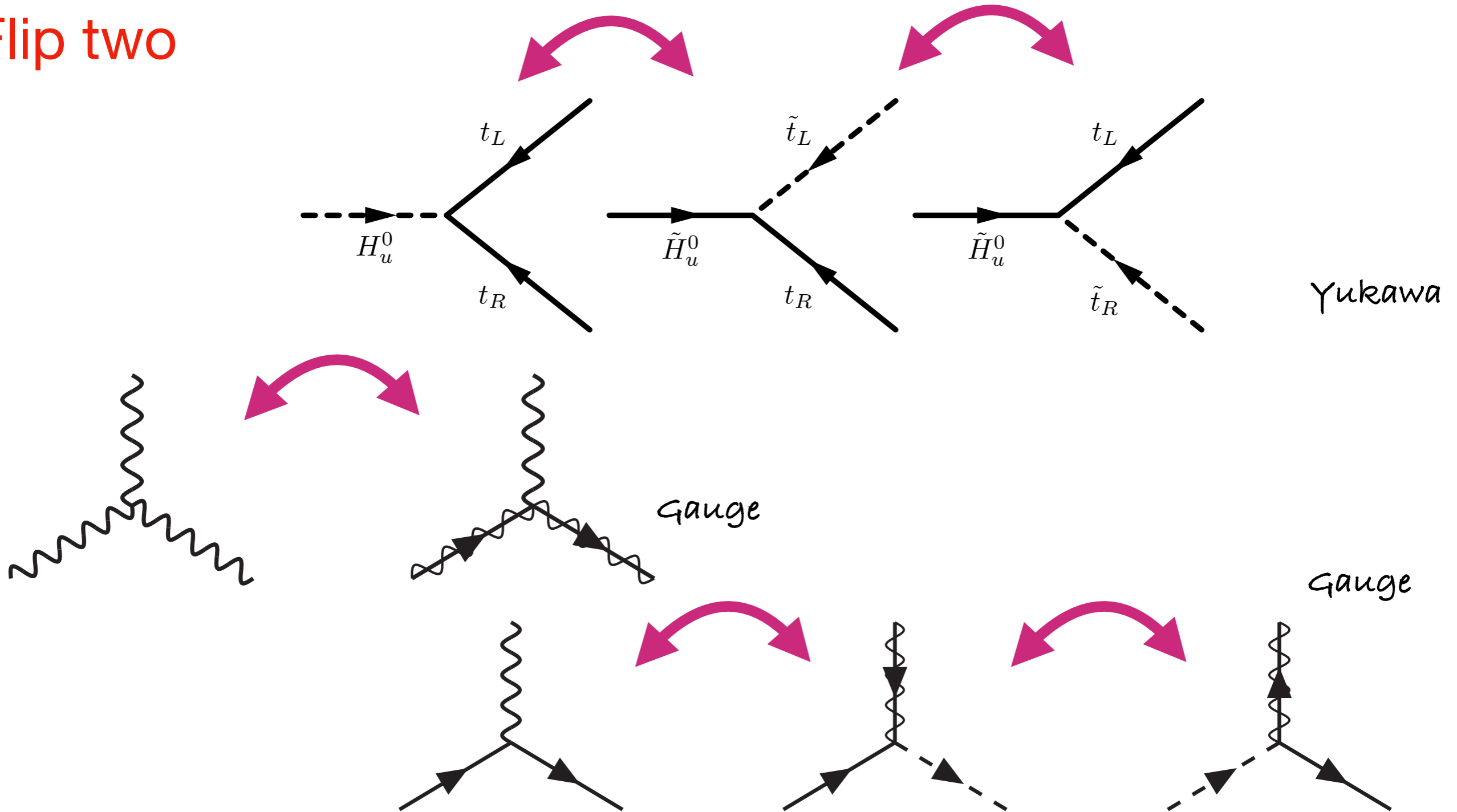


Supersymmetry

Extended Higgs sector
Higgs modifications

$$W_{MSSM} = Y_U U^c Q H_u - Y_D D^c Q H_d - Y_E E^c L H_d + \mu H_u H_d$$

Flip two



Supersymmetry

New fields allow for new interactions (EFT philosophy)

$$W_{\Delta B, L} = \cancel{\kappa_1^{ijk} Q_i L_j D_k^c}^{\Delta L = 1} + \cancel{\kappa_2^{ijk} L_i L_j E_k^c}^{\Delta L = 1} + \cancel{\kappa_3^i L^i H_u}^{\Delta L = 1} + \cancel{\kappa_4^{ijk} D_i^c D_j^c U_k^c}^{\Delta B = 1}$$

Proton lifetime: $\Gamma \sim \frac{\kappa_1 \kappa_4}{16\pi} \frac{m_p^5}{m_{\tilde{q}}^4} \quad \kappa < 10^{-12}!$

Forbid these (RPV) operators with a parity (R-parity)

$$SM \rightarrow SM$$

$$BSM \rightarrow -BSM$$

LPOP

1. SM and partners don't mix
2. SUSY states pair produced
3. Lightest parity odd particle stable (DM?)



Supersymmetry

New fields allow for new interactions (EFT philosophy)

$$W_{\Delta B, L} = \cancel{\kappa_1^{ijk} Q_i L_j D_k^c}^{\Delta L = 1} + \cancel{\kappa_2^{ijk} L_i L_j E_k^c}^{\Delta L = 1} + \cancel{\kappa_3^i L^i H_u}^{\Delta L = 1} + \cancel{\kappa_4^{ijk} D_i^c D_j^c U_k^c}^{\Delta B = 1}$$

Proton lifetime: $\Gamma \sim \frac{\kappa_1 \kappa_4}{16\pi} \frac{m_p^5}{m_{\tilde{q}}^4} \quad \kappa < 10^{-12}!$

Forbid these (RPV) operators with a parity (R-parity)

$$SM \rightarrow SM$$

$$BSM \rightarrow -BSM$$

LPOP

1. SM and partners don't mix
2. SUSY states pair produced
3. Lightest parity odd particle stable (DM?)

More later....

Supersymmetry

Complicated spectrum, details depend on model

GMSB, Effective/Natural SUSY, Dirac gauginos....

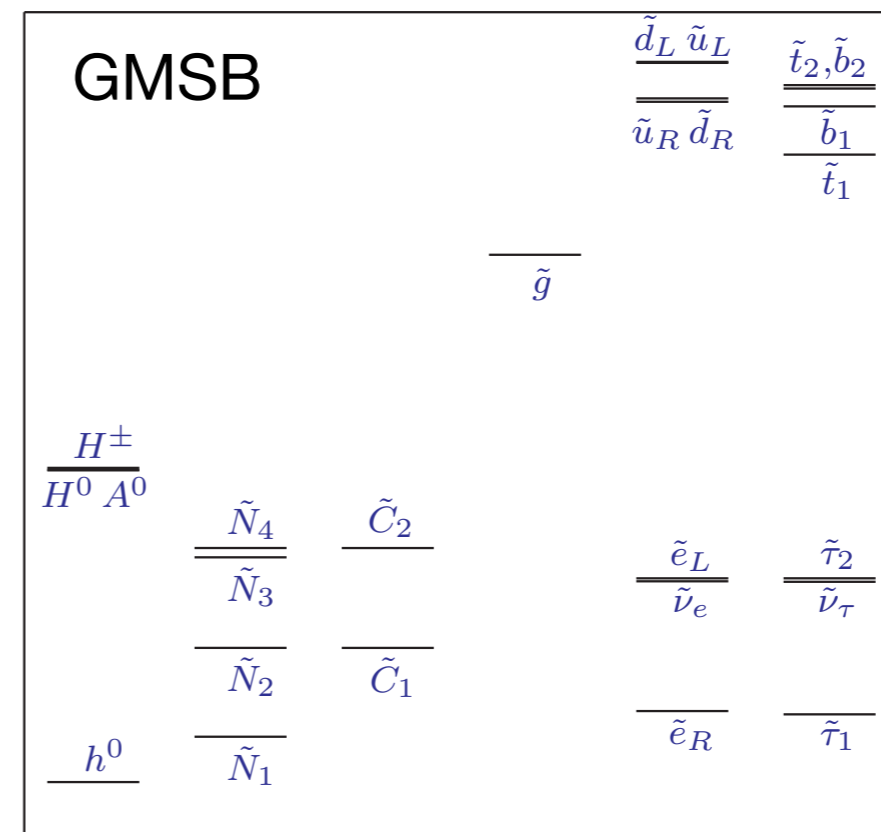
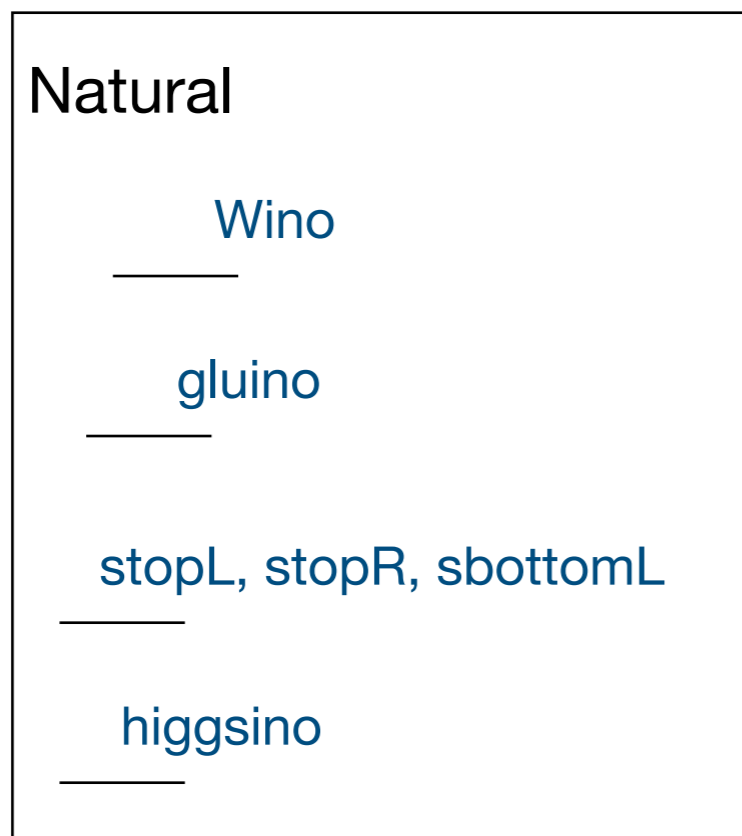
Many, many interesting collider signatures

Lightest coloured states made first, decays involve MET

Compressed/Stealth spectra can hide SUSY (a little)

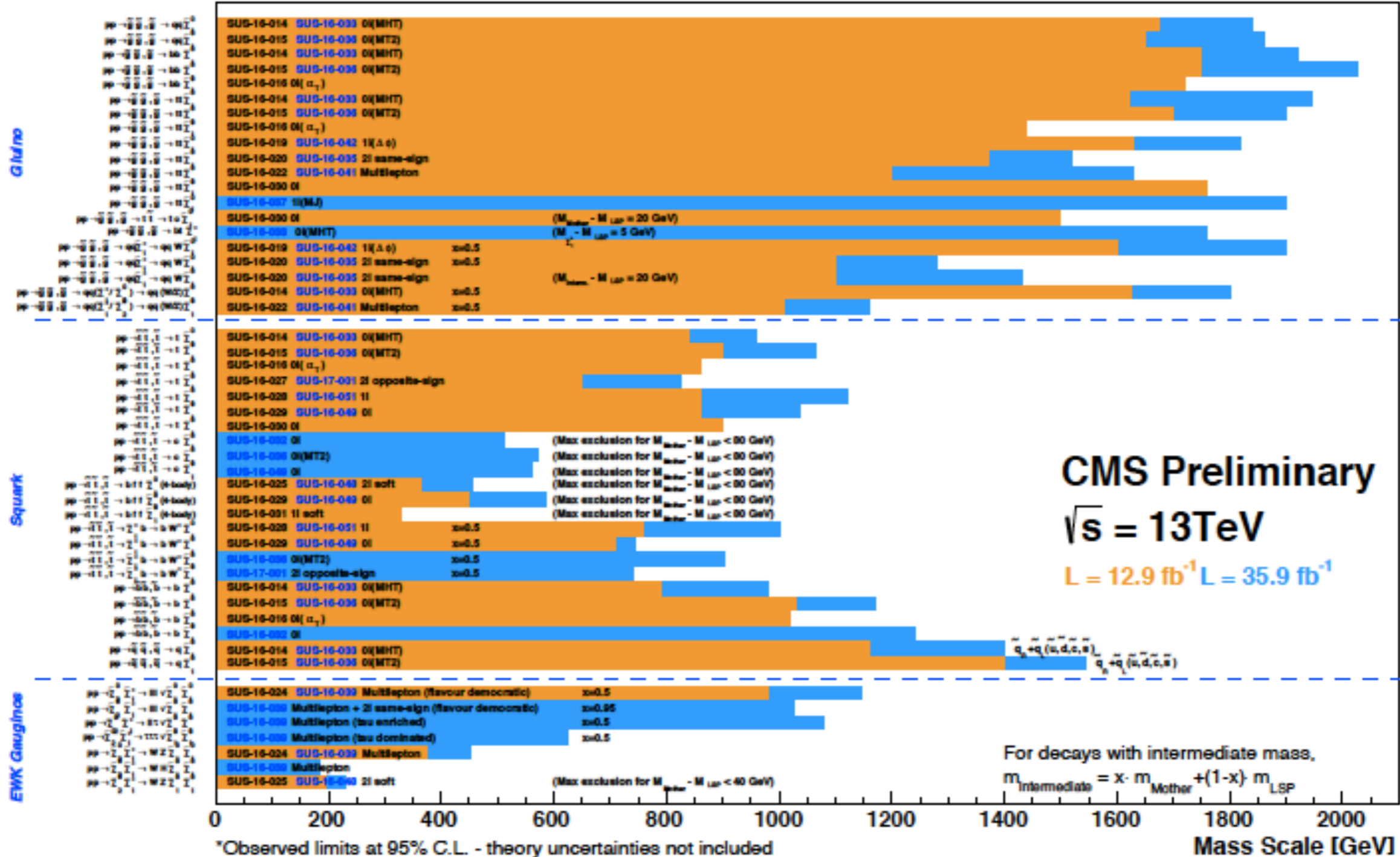
Electroweakino sector starting to be probed (DM)

SUSY is a great signal generator



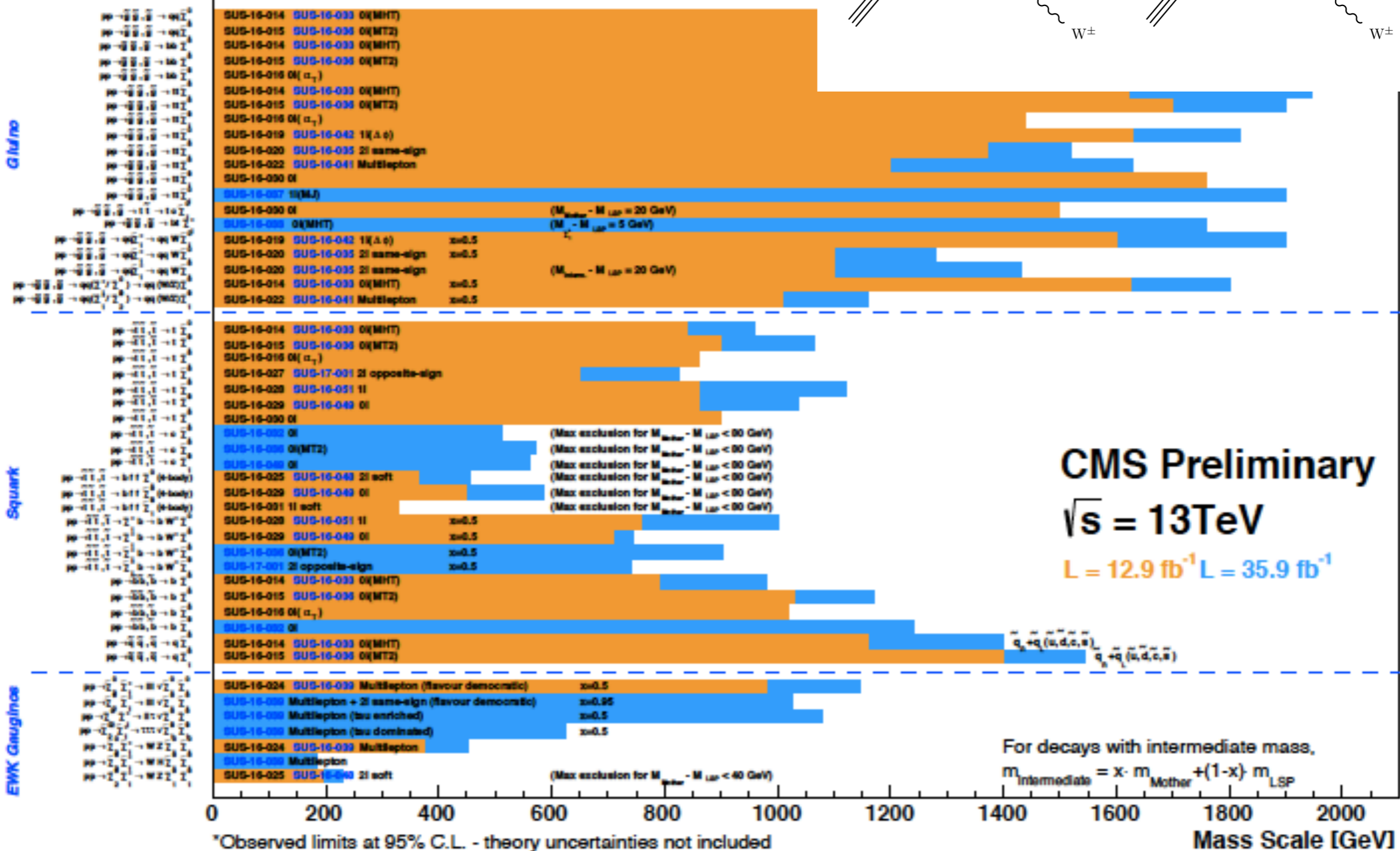
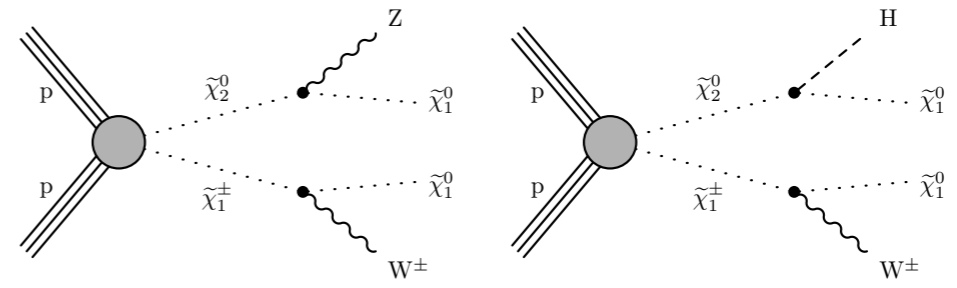
Selected CMS SUSY Results* - SMS Interpretation

ICHEP '16 - Moriond '17



*Observed limits at 95% C.L. - theory uncertainties not included
 Only a selection of available mass limits. Probe "up to" the quoted mass limit for $m_{\text{LSP}} = 0 \text{ GeV}$ unless stated otherwise

Selected CMS SUSY Results* - SMS Interpretation



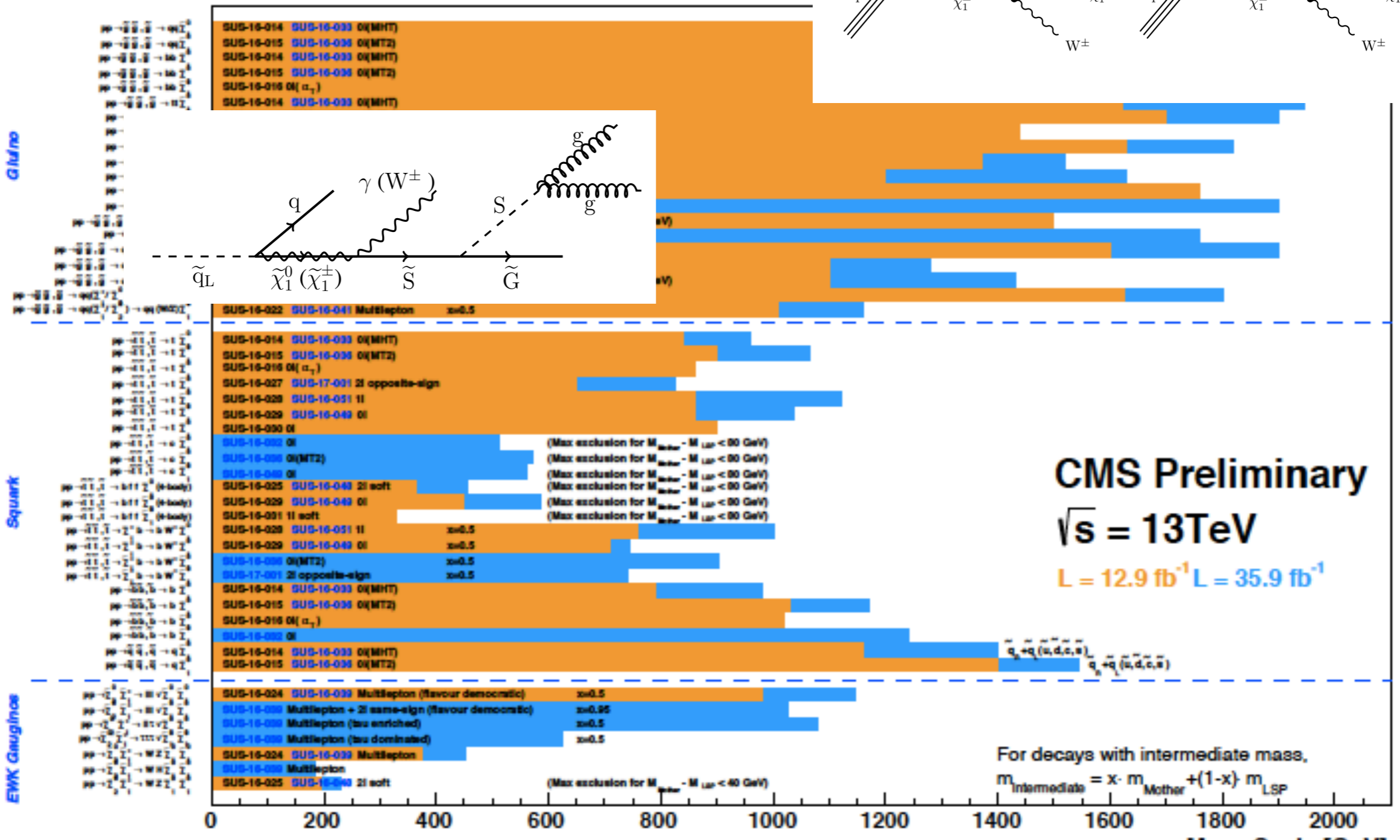
CMS Preliminary
 $\sqrt{s} = 13\text{TeV}$
 $L = 12.9 \text{ fb}^{-1}$ $L = 35.9 \text{ fb}^{-1}$

For decays with intermediate mass,

$$m_{\text{intermediate}} = x \cdot m_{\text{Mother}} + (1-x) \cdot m_{\text{LSP}}$$

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Selected CMS SUSY Results* - SMS Interpretation



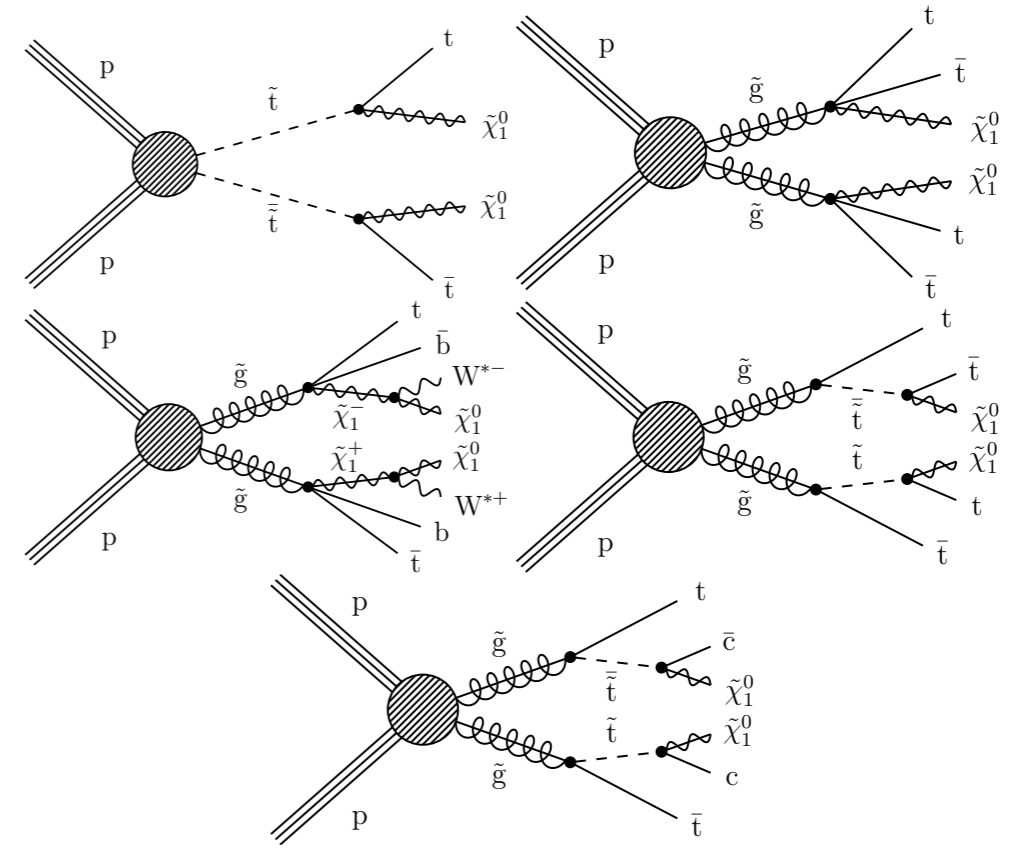
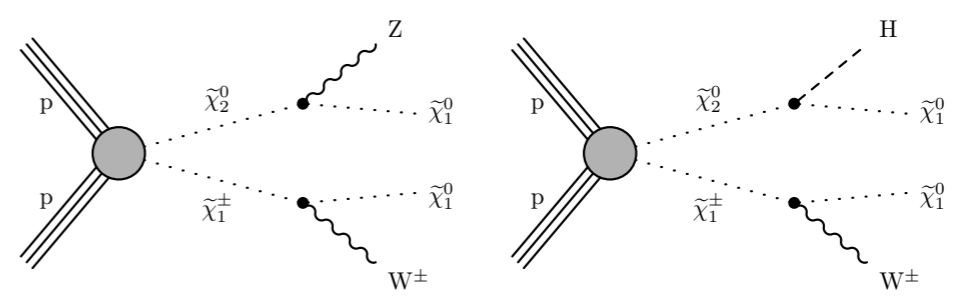
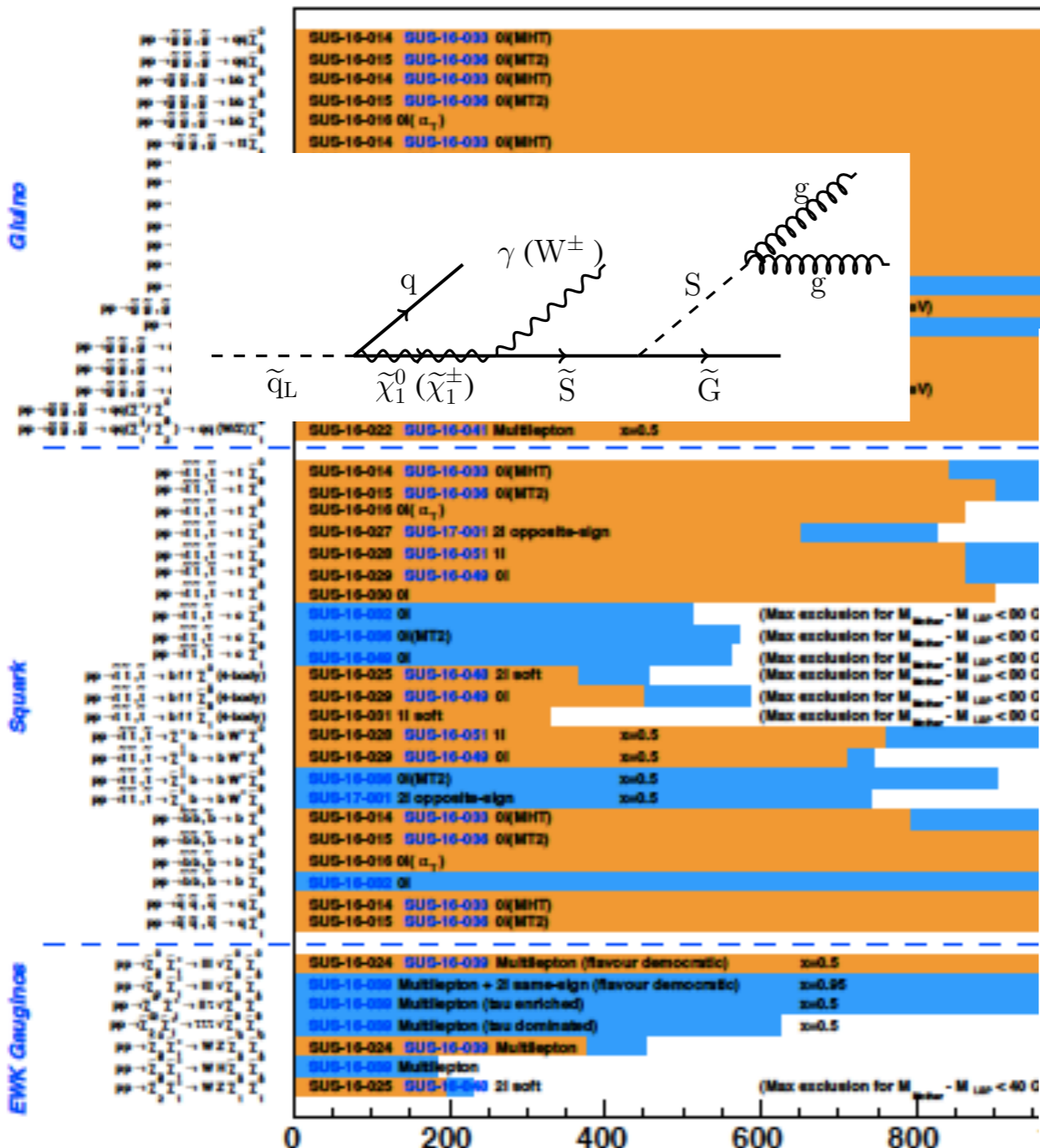
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For decays with intermediate mass, $m_{intermediate} = x \cdot m_{Mother} + (1-x) \cdot m_{LSP}$

Mass Scale [GeV]

Selected CMS SUSY Results* - SMS Interpretation



*Observed limits at 95% C.L. - theory uncertainties not included

Only a selection of available mass limits. Probe "up to" the quoted mass limit for $m_{LSP} = 0$ GeV unless stated otherwise

Mass Scale [GeV]

General BSM lessons

Top partners (fermions/bosons)

Higgs sector modifications

LPOPs, parity, DM, MET

Extra matter in fundamental and adjoint reps.

New gauge groups?

Lighter, more weakly coupled particles?

Resonances?



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Little Higgs



Twin Higgs

[Chacko, Goh, Harnik]

$$SM_A \times SM_B \times \mathbb{Z}_2$$

$$\mathcal{L} \supset y Q_A H_A U_A^c + y Q_B H_B U_B^c$$

Higgs is a PNGB, and Higgs potential is $O(8)$ symmetric

$$V = -m^2 H^\dagger H + \lambda (H^\dagger H)^2$$

$O(8) \rightarrow O(7)$: 7 Goldstone bosons, 3 eaten by B gauge bosons

$$H = \begin{pmatrix} H_A \\ H_B \end{pmatrix} = e^{ih^a t^a / f} \begin{pmatrix} 0 \\ 0 \\ 0 \\ f \end{pmatrix}$$

Twin Higgs

[Chacko, Goh, Harnik]

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Twin Higgs

Gauge and Yukawa interactions explicitly break the $O(8)$

Mass for Higgs?

$$\frac{3}{8\pi^2} \Lambda^2 \left(y_A^2 H_A^\dagger H_A + y_B^2 H_B^\dagger H_B \right)$$


$$Z_2 \Rightarrow y_A = y_B$$

$$\frac{3}{8\pi^2} \Lambda^2 y^2 H^\dagger H$$

Loop corrections to mass is $O(8)$ symmetric, does not lead to *quadratically divergent* Higgs mass

EFT aside

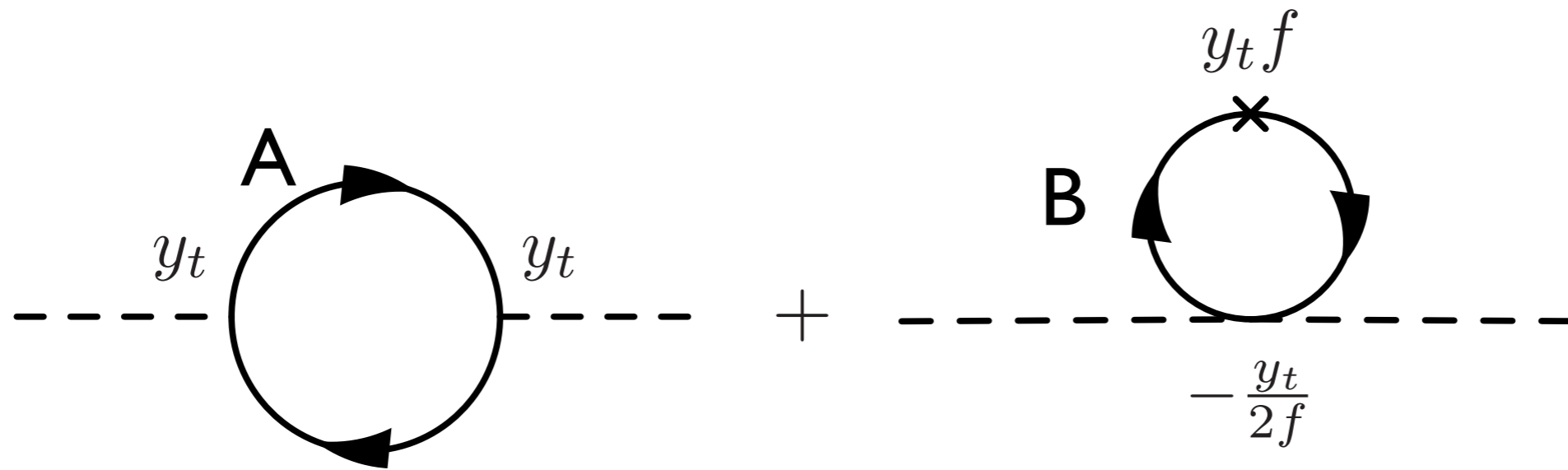
Low energy degrees of freedom, non-linearly realized symm.

$$H = \begin{pmatrix} H_A \\ H_B \\ \vdots \end{pmatrix} = e^{i\mathbf{h}^a t^a / f} \begin{pmatrix} 0 \\ 0 \\ 0 \\ f \end{pmatrix}$$

$$H = \begin{pmatrix} \mathbf{h} \frac{if}{\sqrt{\mathbf{h}^\dagger \mathbf{h}}} \sin \frac{\sqrt{\mathbf{h}^\dagger \mathbf{h}}}{f} \\ 0 \\ f \cos \frac{\sqrt{\mathbf{h}^\dagger \mathbf{h}}}{f} \end{pmatrix} = \begin{pmatrix} i\mathbf{h} \\ 0 \\ f - \frac{1}{2f} \sqrt{\mathbf{h}^\dagger \mathbf{h}} \end{pmatrix} + \dots$$

Top sector

$$\mathcal{L} \sim y Q_A H U_A^c + y Q_B \left(f - \frac{|H|^2}{2f^2} \right) U_B^c$$

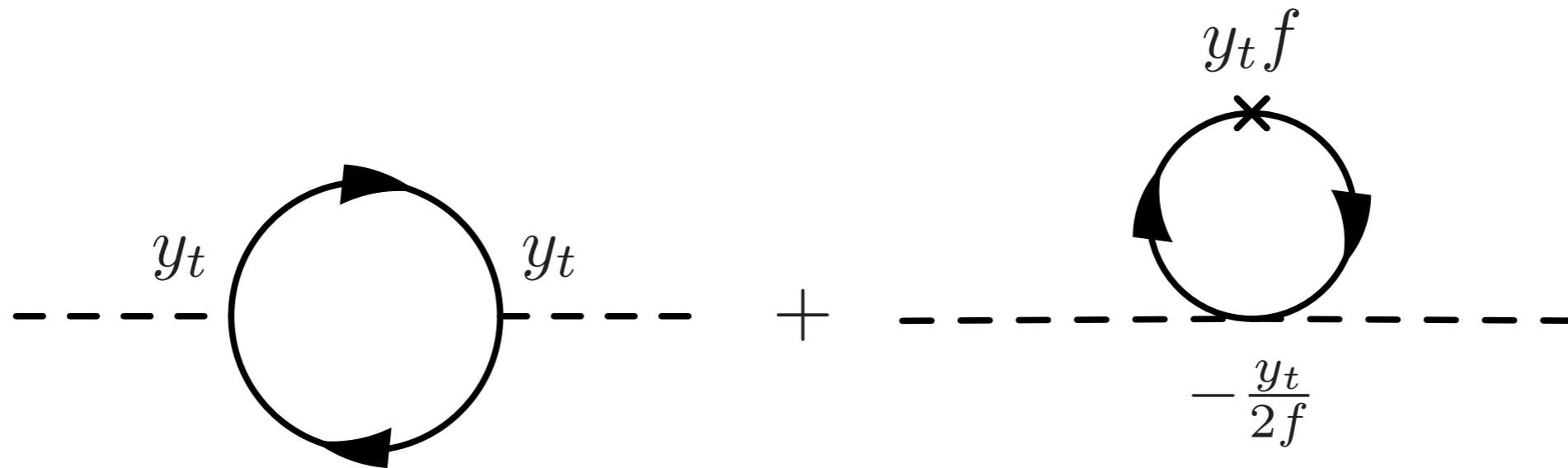


Quadratic divergences cancel, states running in loop have no SM charge, same spin (3 is just a number)

**Cancelling states not coloured:
small production x-sec at LHC**

To separate v and f and make the SM Higgs lie mostly in A
 introduce soft breaking $\mu_A^2 |H_A|^2$

$$\langle H_A \rangle = v_{SM} \ll \langle H_B \rangle = f \sim 1 \text{ TeV}$$



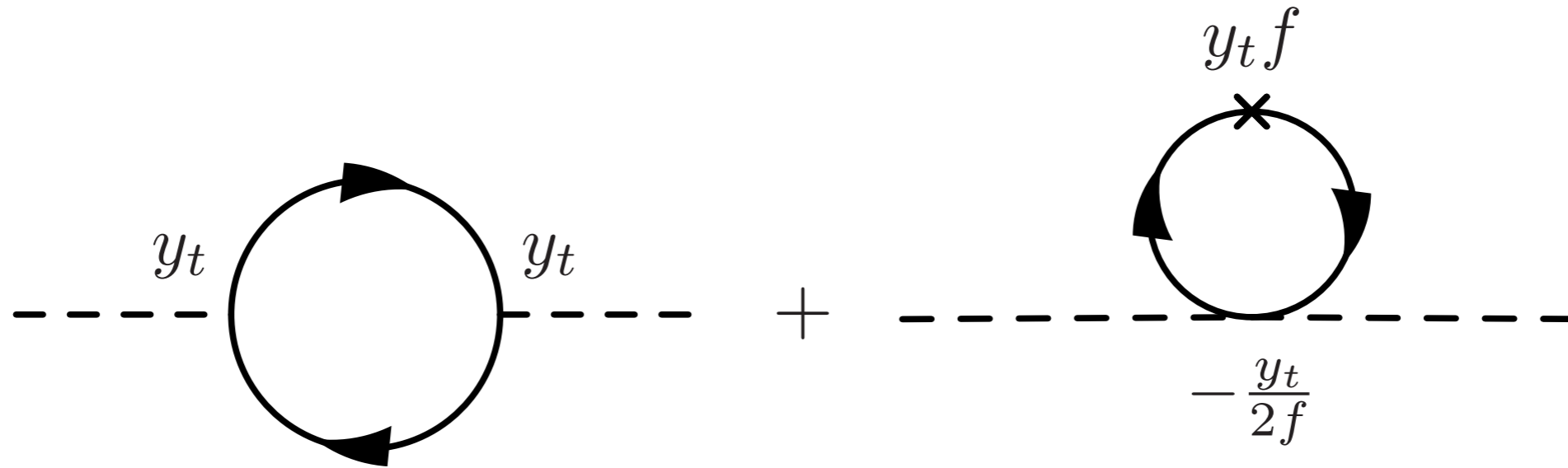
Tuning grows with f/v

$$\delta m_h^2 \sim \frac{3y_t m_t^2}{4\pi^2} \left(\frac{f}{v} \right)^2 \log \frac{\Lambda v}{m_t f}$$

$$\Delta = \left| \frac{2\delta m_h^2}{m_h^2} \right|^{-1}$$

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$f/v \sim 3-5$

$$V = -m^2 \left(H_A^\dagger H_A + H_B^\dagger H_B \right) + \lambda \left(H_A^\dagger H_A + H_B^\dagger H_B \right)^2$$

Higgs portal between A and B sectors

- Higgs mixing and corrections to Higgs pheno at $\frac{v^2}{f^2}$
- Higgs invisible decay width, to light B sector stuff

