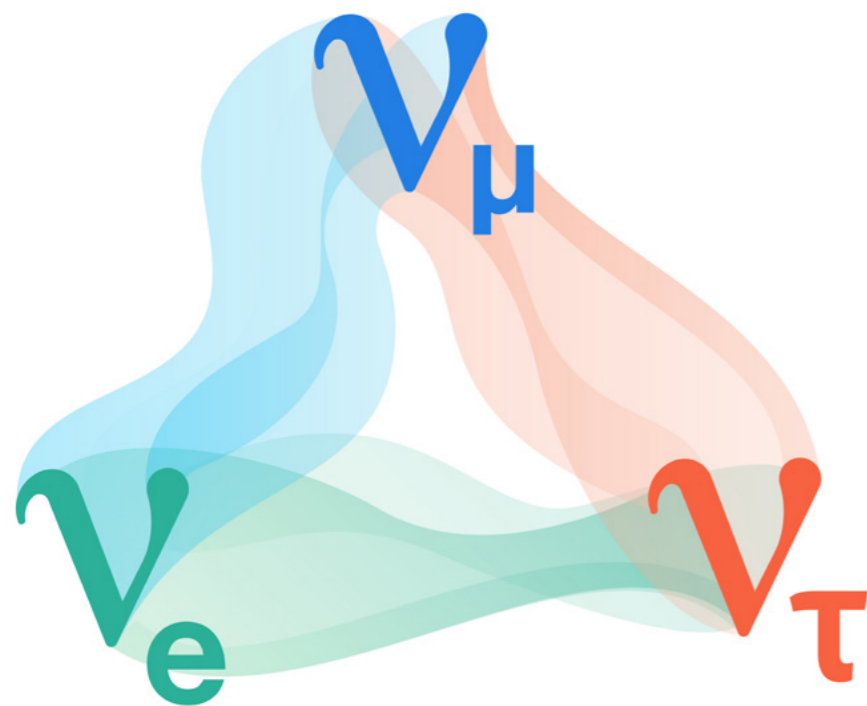




# Theoretical Aspects of the Quantum Neutrino circa 2025+

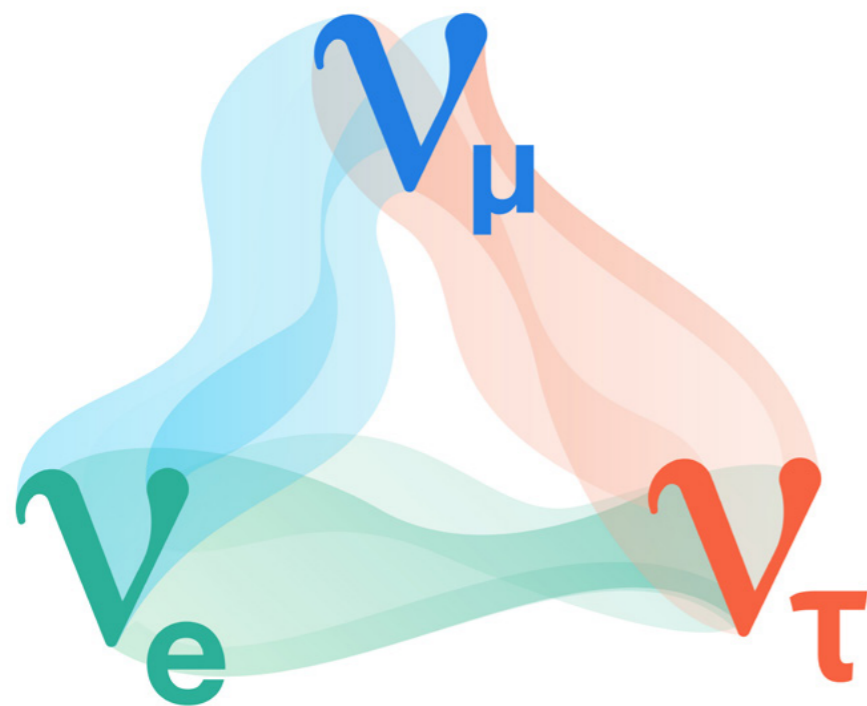


Stephen Parke  
Fermilab



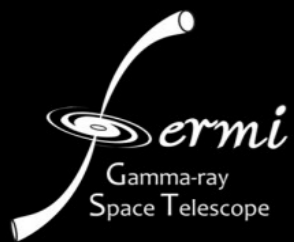
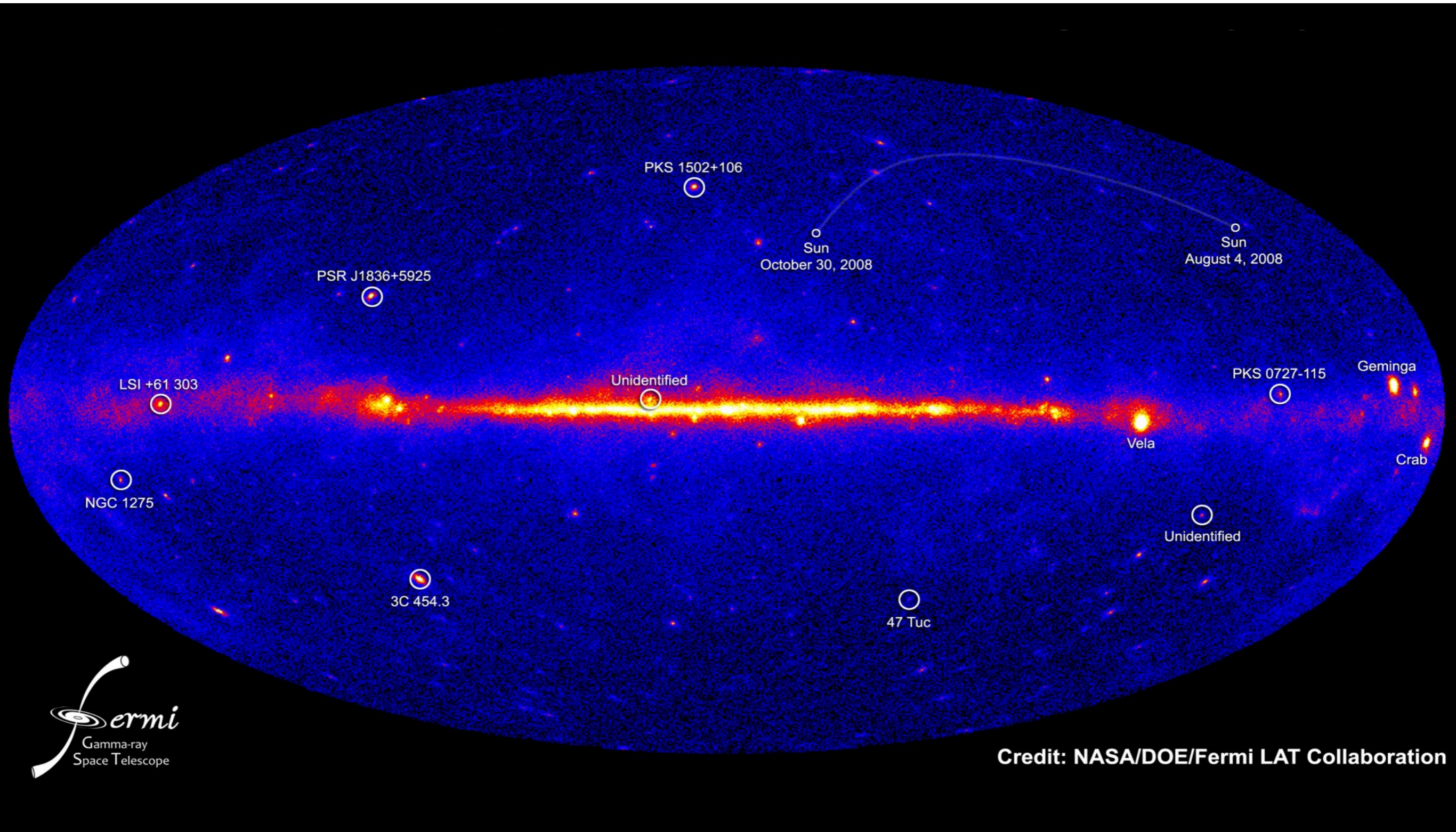


# Theoretical Aspects of the Quantum Neutrino circa 2025+



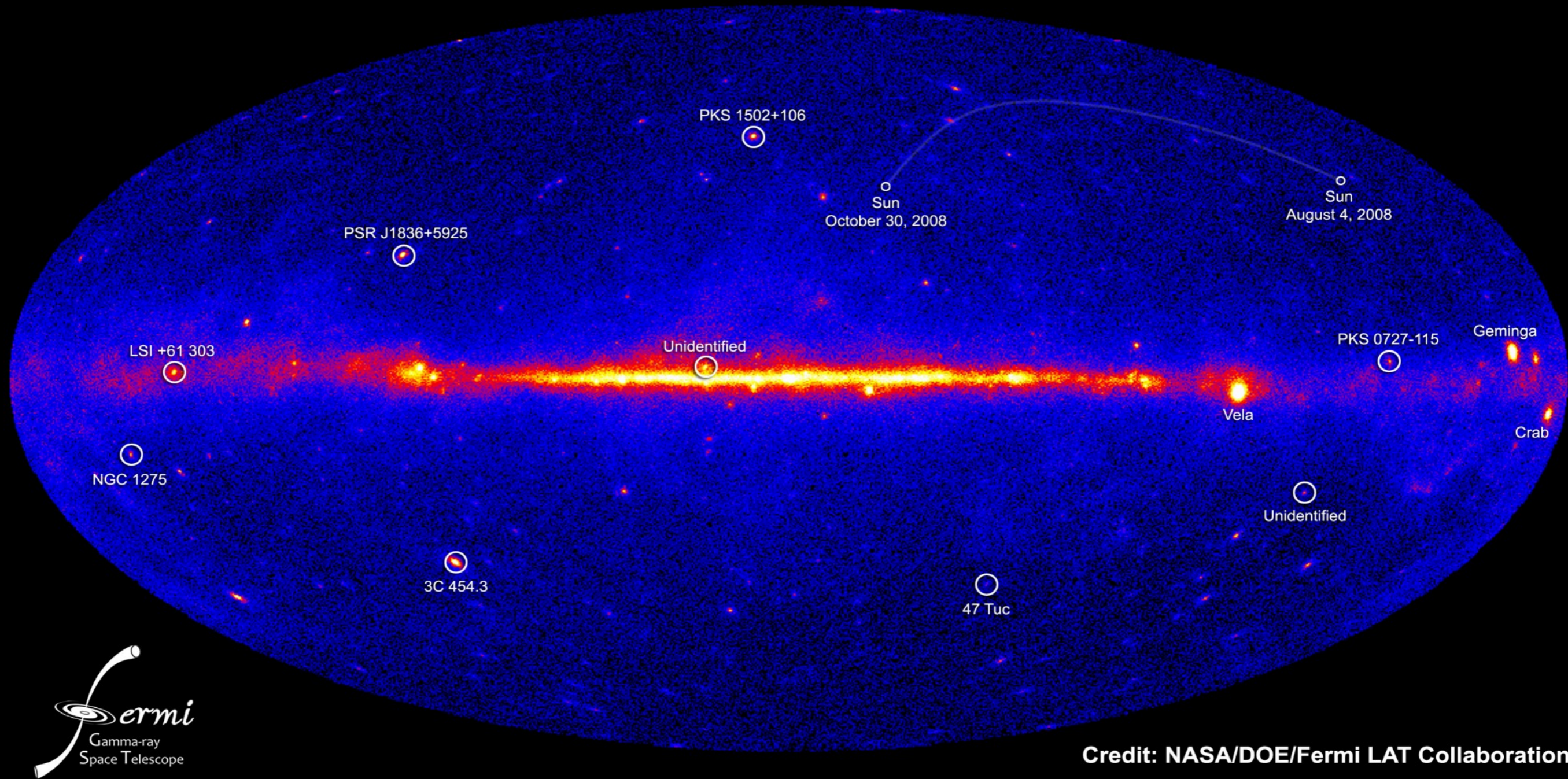
Stephen Parke  
Fermilab





Credit: NASA/DOE/Fermi LAT Collaboration

# Neutrinos are Everywhere !



# Neutrinos are Everywhere !



from Big Bang  $300 \text{ nus} / \text{cm}^3$   
2 or more  $v/c \ll 1$



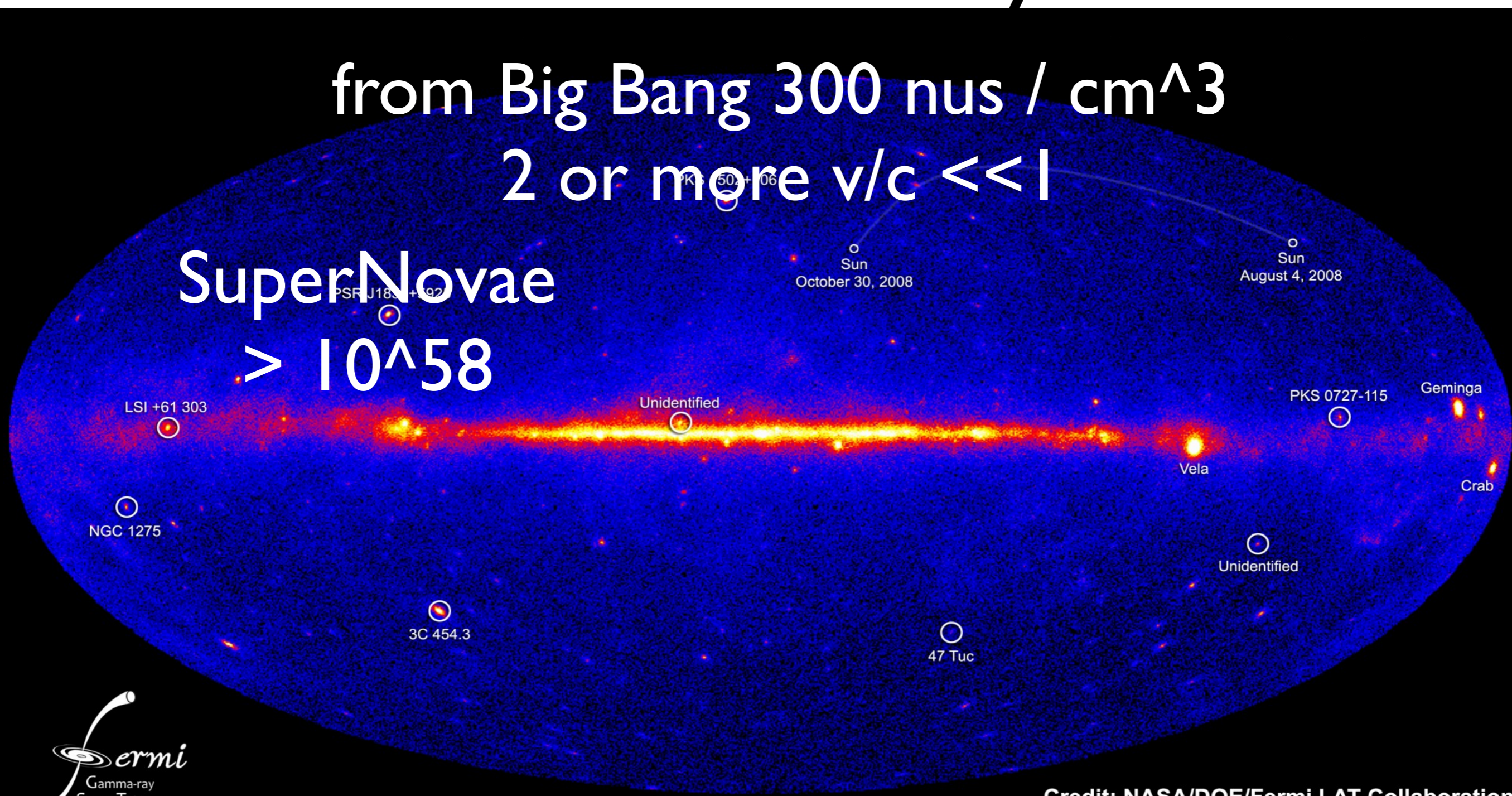
Credit: NASA/DOE/Fermi LAT Collaboration

# Neutrinos are Everywhere !



from Big Bang  $300 \text{ nus} / \text{cm}^3$   
2 or more  $v/c \ll 1$

SuperNovae  
 $> 10^{58}$



Credit: NASA/DOE/Fermi LAT Collaboration

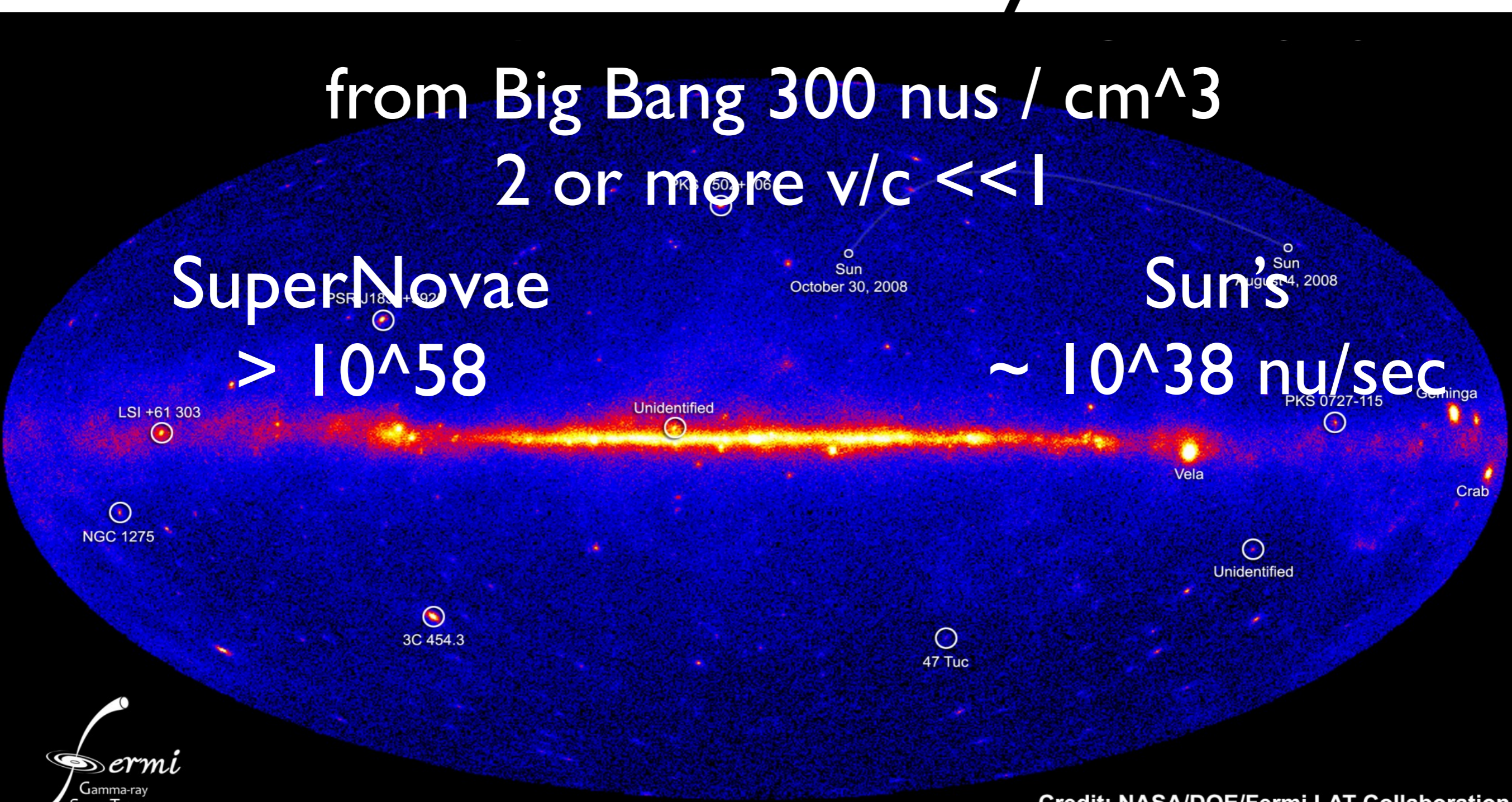
# Neutrinos are Everywhere !



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SuperNovae  
 $> 10^{58}$

Sun's  
 $\sim 10^{38} \text{ nu/sec}$



Credit: NASA/DOE/Fermi LAT Collaboration

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 $3 \times 10^{21} \text{ nu/sec}$



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$3 \times 10^{21} \text{ nu/sec}$

Neutrinos are Forever !!!

(except for the highest energy neutrino's)



Credit: NASA/DOE/Fermi LAT Collaboration

# Neutrinos are Everywhere !



from Big Bang  $300 \text{ nus} / \text{cm}^3$   
2 or more  $v/c \ll 1$

SuperNovae  
 $> 10^{58}$

Sun's  
 $\sim 10^{38} \text{ nu/sec}$

Daya Bay

$3 \times 10^{21} \text{ nu/sec}$

Neutrinos are Forever !!!

(except for the highest energy neutrino's)



therefore in the Universe:  $\frac{\partial N_\nu}{\partial t} > 0$

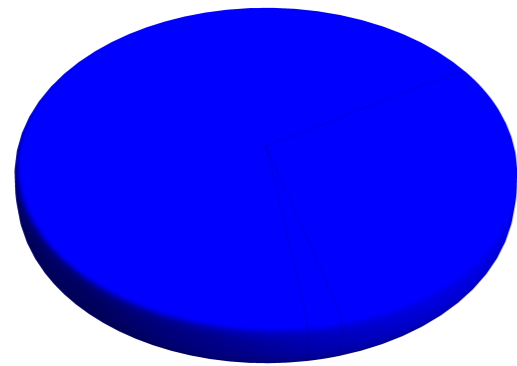


# Neutrino Flavor or Interaction States:

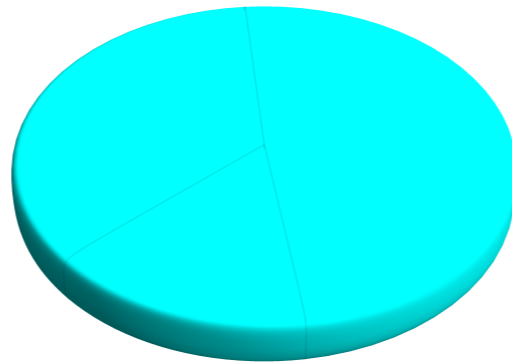
$$W^+ \rightarrow e^+ \nu_e$$

$$W^+ \rightarrow \mu^+ \nu_\mu$$

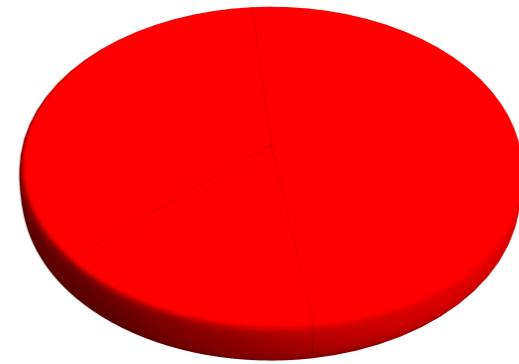
$$W^+ \rightarrow \tau^+ \nu_\tau$$



$\nu_e$



$\nu_\mu$



$\nu_\tau$

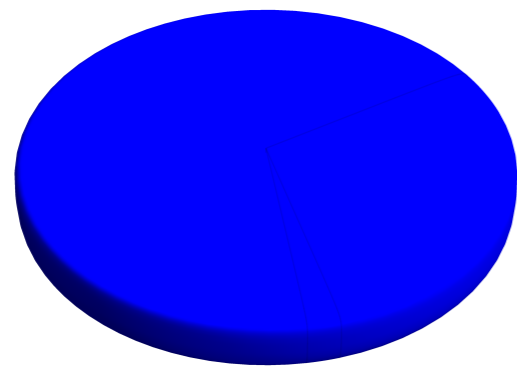


# Neutrino Flavor or Interaction States:

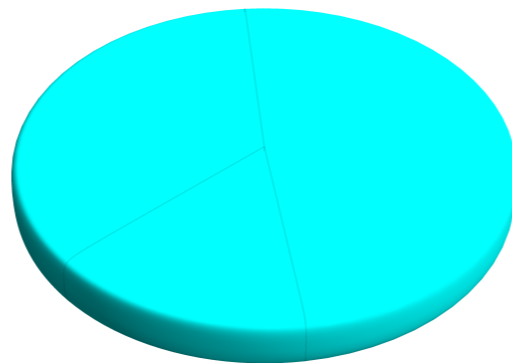
$$W^+ \rightarrow e^+ \nu_e$$

$$W^+ \rightarrow \mu^+ \nu_\mu$$

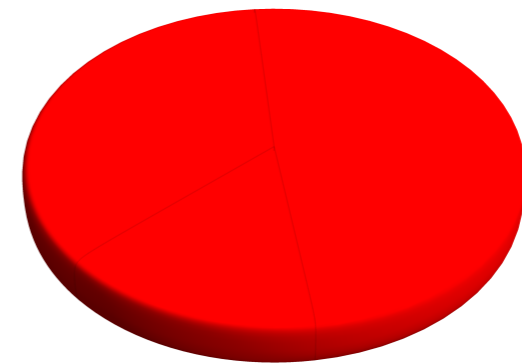
$$W^+ \rightarrow \tau^+ \nu_\tau$$



$\nu_e$



$\nu_\mu$



$\nu_\tau$

provided  $L/E \ll 0.5 \text{ km/MeV} = 500 \text{ km/GeV} !!!$

$\sim 1$  picosecond in Neutrino rest frame !!!

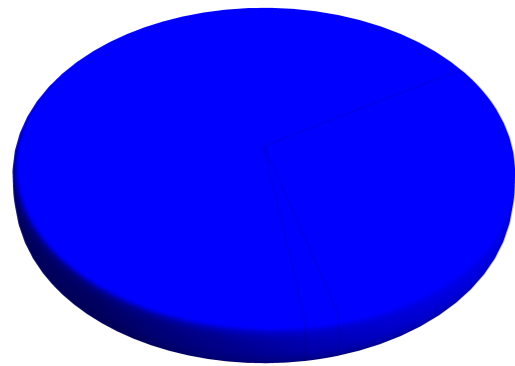


# Neutrino Flavor or Interaction States:

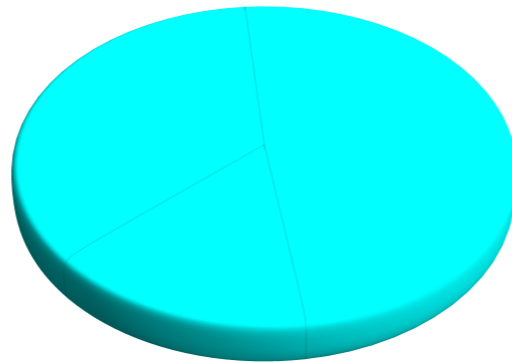
$$W^+ \rightarrow e^+ \nu_e$$

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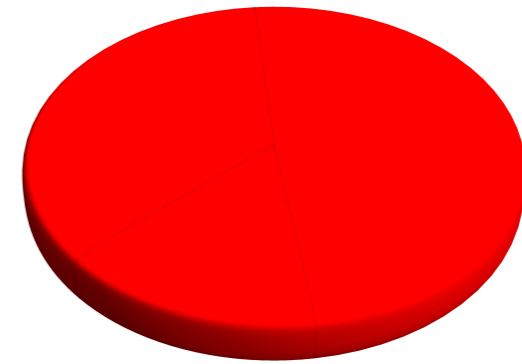
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$\nu_e$



$\nu_\mu$



$\nu_\tau$

provided  $L/E \ll 0.5 \text{ km/MeV} = 500 \text{ km/GeV} !!!$

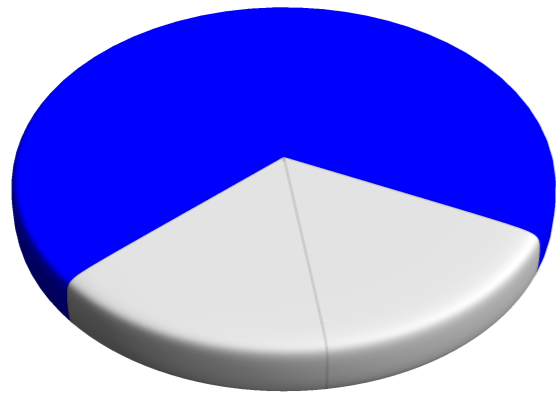
$\sim 1$  picosecond in Neutrino rest frame !!!

$\approx \text{Age of Universe} / 10^{26}$

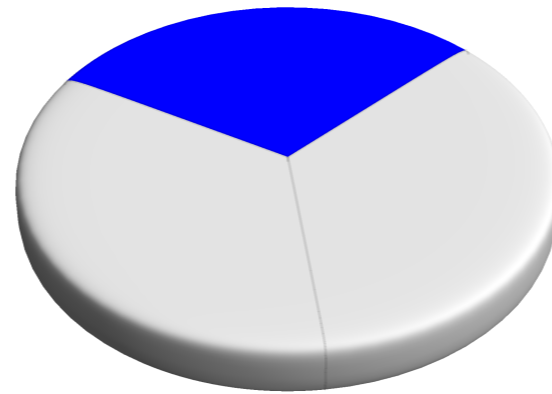
# Neutrino Mass EigenStates or Propagation States:



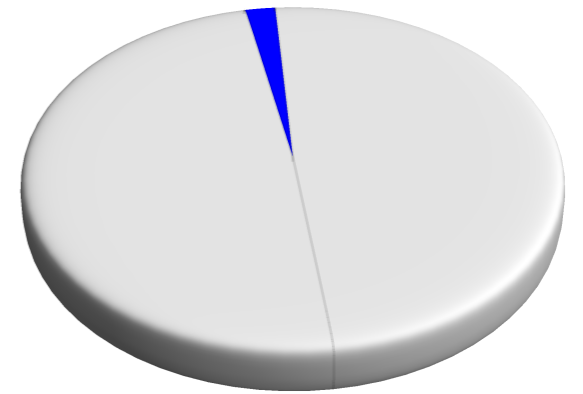
$$\text{Propagator } \nu_j \rightarrow \nu_k = \delta_{jk} e^{-i \left( \frac{m_j^2 L}{2E_\nu} \right)}$$



$\nu_1$



$\nu_2$



$\nu_3$

$$\nu_e = \text{blue circle}$$

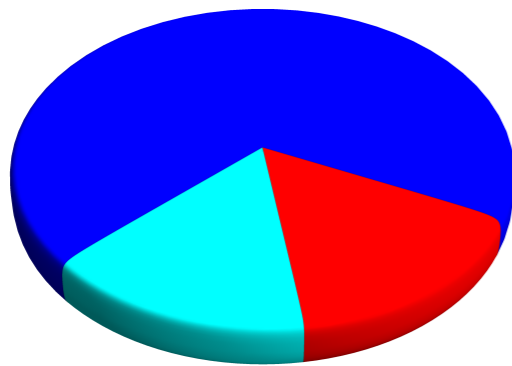
# Neutrino Mass EigenStates or Propagation States:



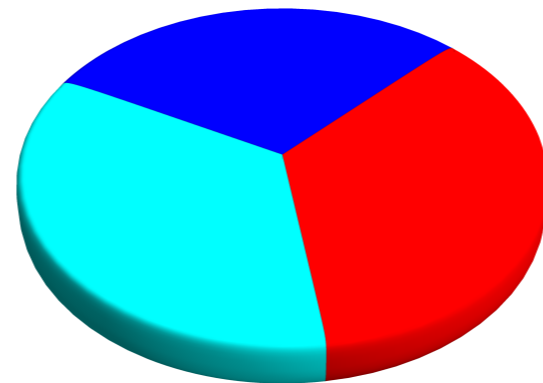
$$\text{Propagator } \nu_j \rightarrow \nu_k = \delta_{jk} e^{-i \left( \frac{m_j^2 L}{2E\nu} \right)}$$

$\nu_1$

most  $\nu_e$

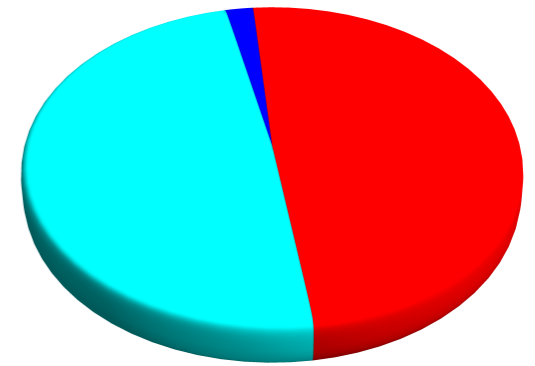


$\nu_2$

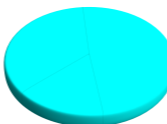



$\nu_3$

least  $\nu_e$



$\nu_e =$  

$\nu_\mu =$  

$\nu_\tau =$  

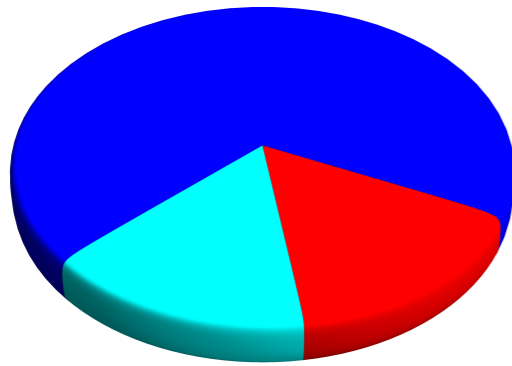
# Neutrino Mass EigenStates or Propagation States:



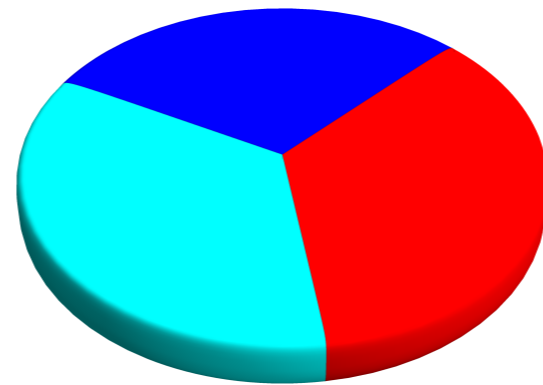
$$\text{Propagator } \nu_j \rightarrow \nu_k = \delta_{jk} e^{-i \left( \frac{m_j^2 L}{2E\nu} \right)}$$

$\nu_1$

most  $\nu_e$

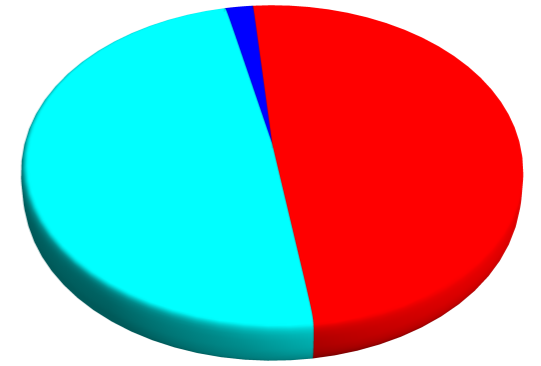


$\nu_2$



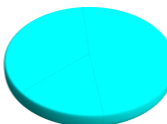
$\nu_3$


least  $\nu_e$



$\nu_e =$  

Solar Exp, SNO, SK,  
KamiLAND  
Daya Bay, RENO, ...

$\nu_\mu =$  

$\nu_\tau =$  



# Neutrino Mass EigenStates or Propagation

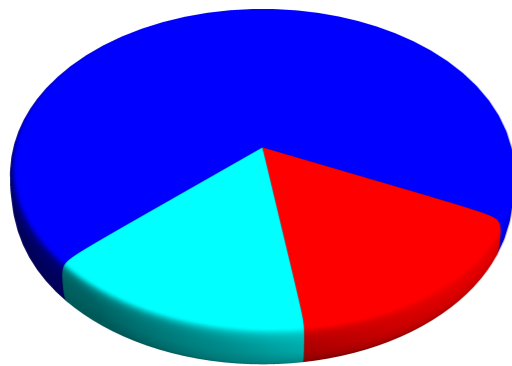


## States:

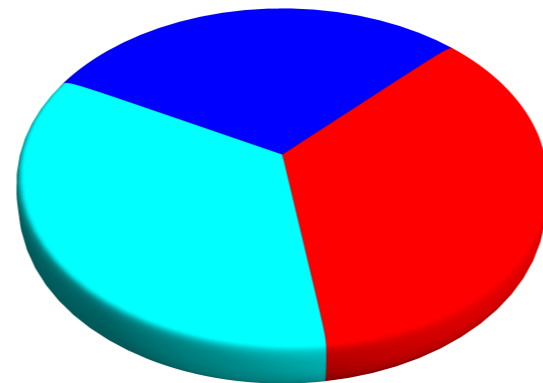
$$\text{Propagator } \nu_j \rightarrow \nu_k = \delta_{jk} e^{-i \left( \frac{m_j^2 L}{2E\nu} \right)}$$

$\nu_1$

most  $\nu_e$

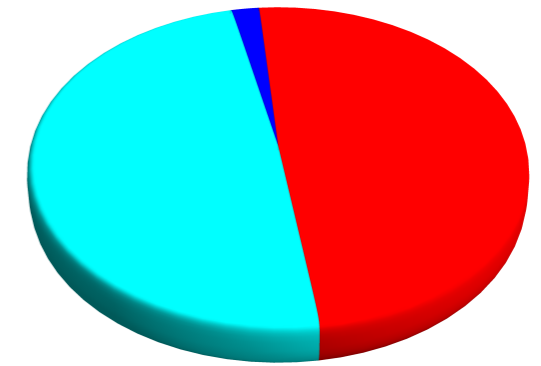


$\nu_2$



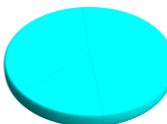
$\nu_3$

least  $\nu_e$



$\nu_e =$  

Solar Exp, SNO, SK,  
KamiLAND  
Daya Bay, RENO, ...

$\nu_\mu =$  

SuperK, K2K, T2K  
MINOS, NOvA  
ICECUBE

$\nu_\tau =$  

# Neutrino Mass EigenStates or Propagation

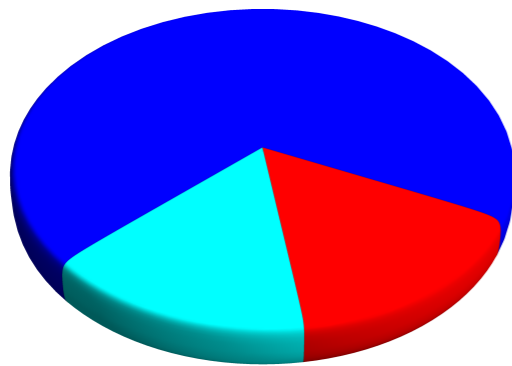


## States:

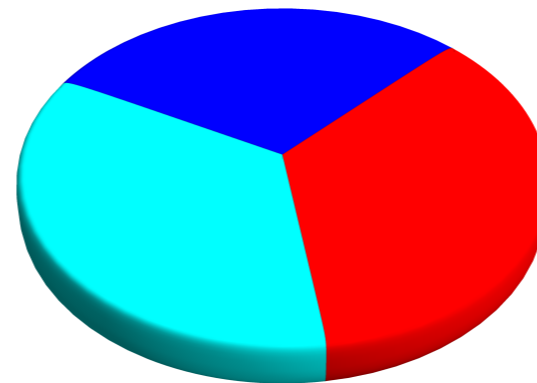
$$\text{Propagator } \nu_j \rightarrow \nu_k = \delta_{jk} e^{-i \left( \frac{m_j^2 L}{2E\nu} \right)}$$

$\nu_1$

most  $\nu_e$

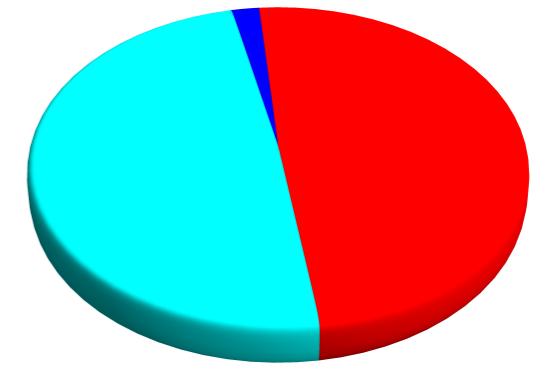


$\nu_2$



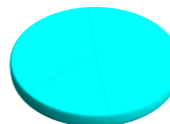
$\nu_3$

least  $\nu_e$



$\nu_e =$  

Solar Exp, SNO, SK,  
KamiLAND  
Daya Bay, RENO, ...

$\nu_\mu =$  

SuperK, K2K, T2K  
MINOS, NOvA  
ICECUBE

$\nu_\tau =$  

Unitarity  
SK, Opera  
ICECUBE ?

# Neutrino Mass EigenStates or Propagation

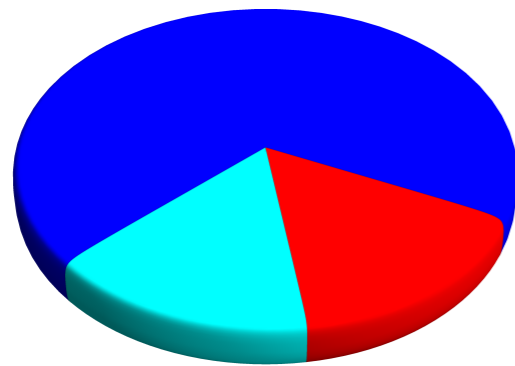


## States:

$$\text{Propagator } \nu_j \rightarrow \nu_k = \delta_{jk} e^{-i \left( \frac{m_j^2 L}{2E\nu} \right)}$$

$\nu_1$

most  $\nu_e$

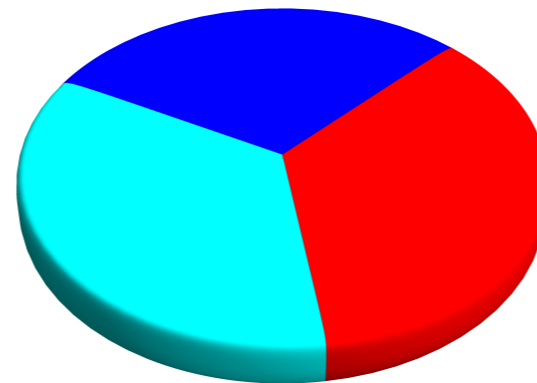


$\delta, \theta_{23}$

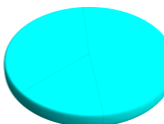
$\nu_e =$  

Solar Exp, SNO, SK,  
KamiLAND  
Daya Bay, RENO, ...

$\nu_2$



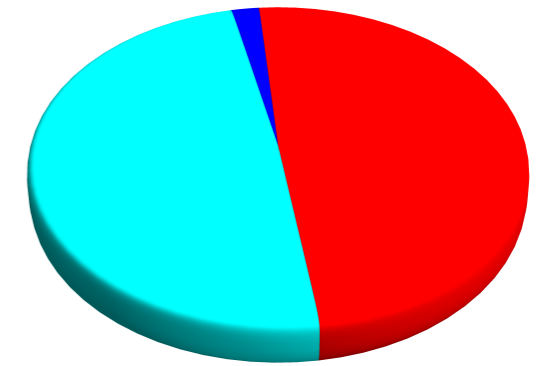
$\delta, \theta_{23}$

$\nu_\mu =$  

SuperK, K2K, T2K  
MINOS, NOvA  
ICECUBE

$\nu_3$

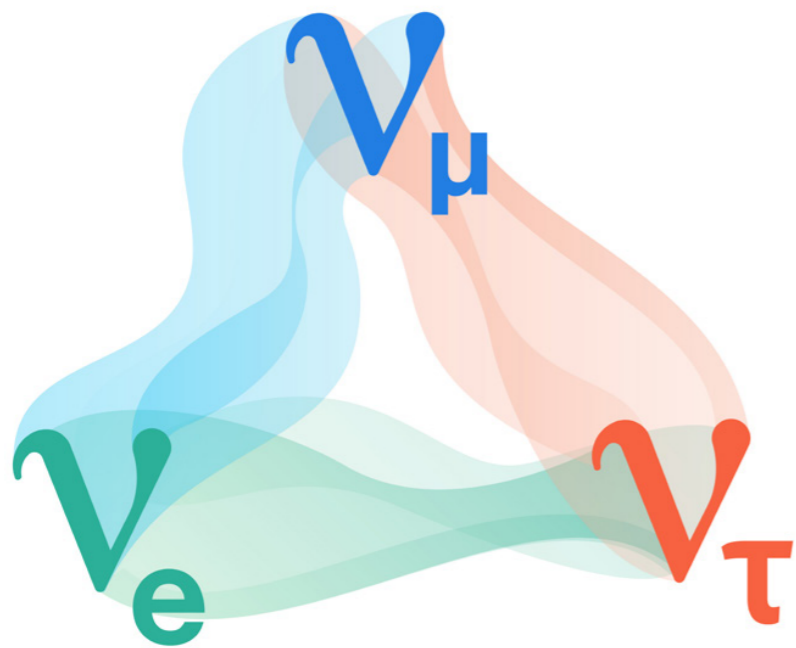
least  $\nu_e$

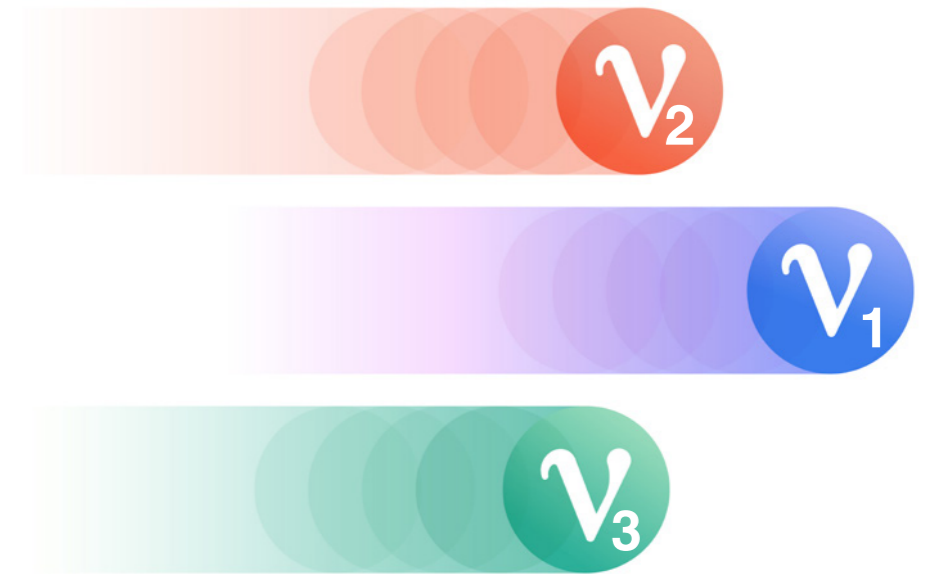
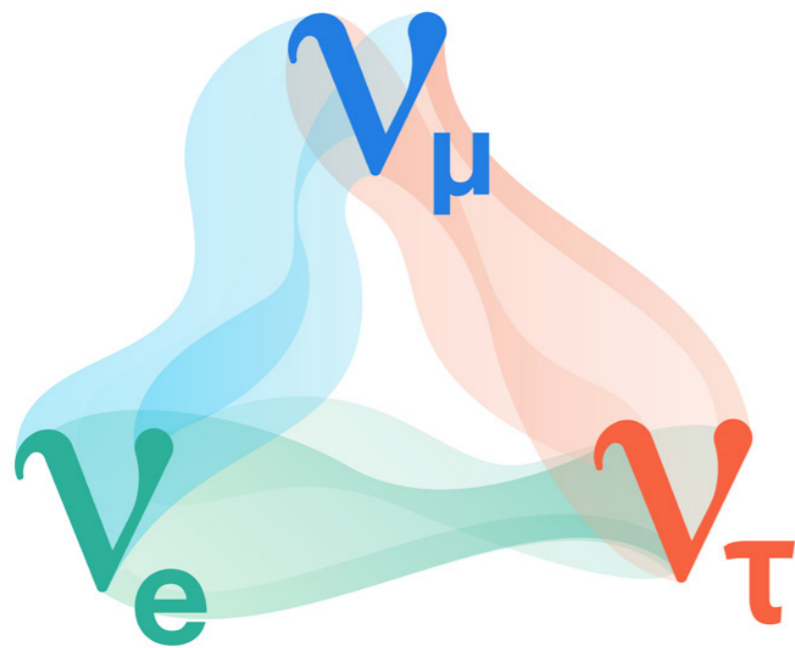


$\theta_{23}$

$\nu_\tau =$  

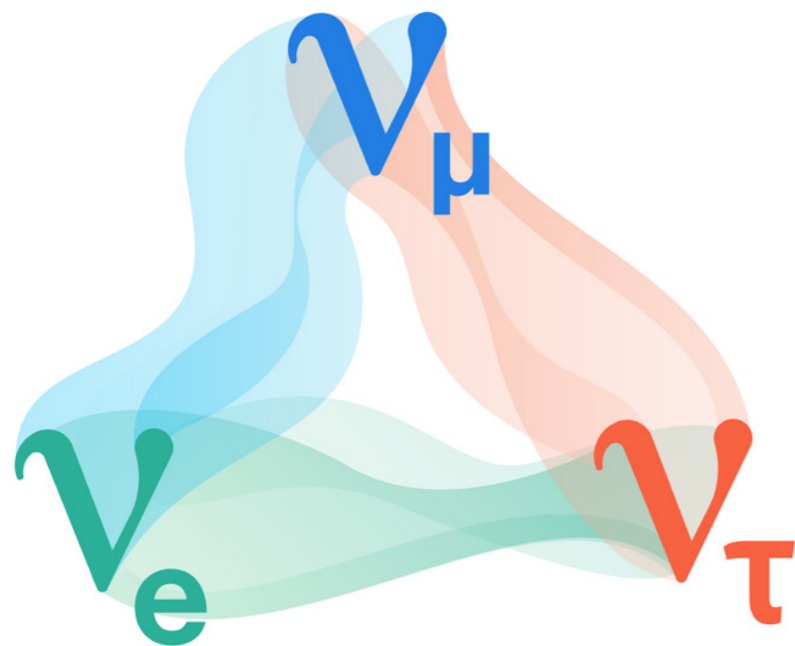
Unitarity  
SK, Opera  
ICECUBE ?



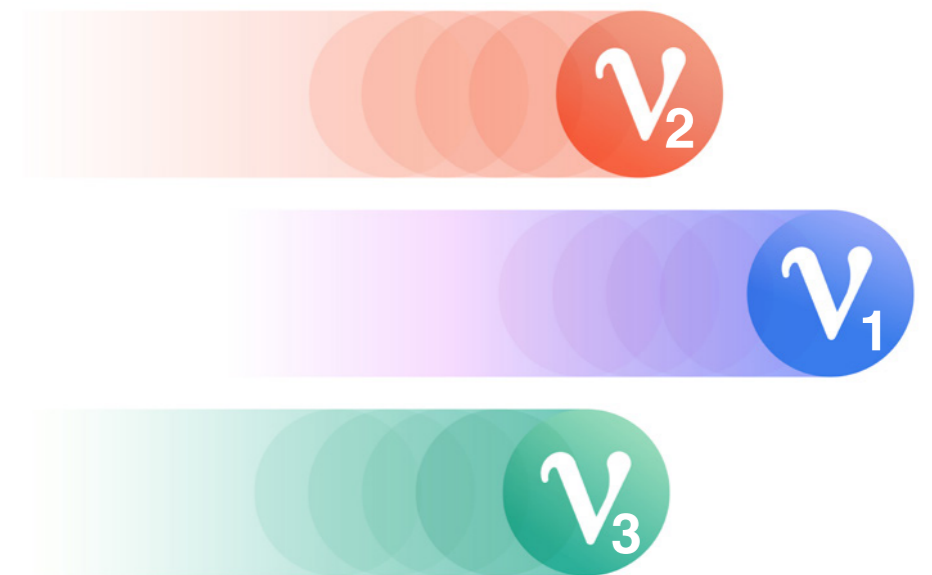


# Interactions:

simple

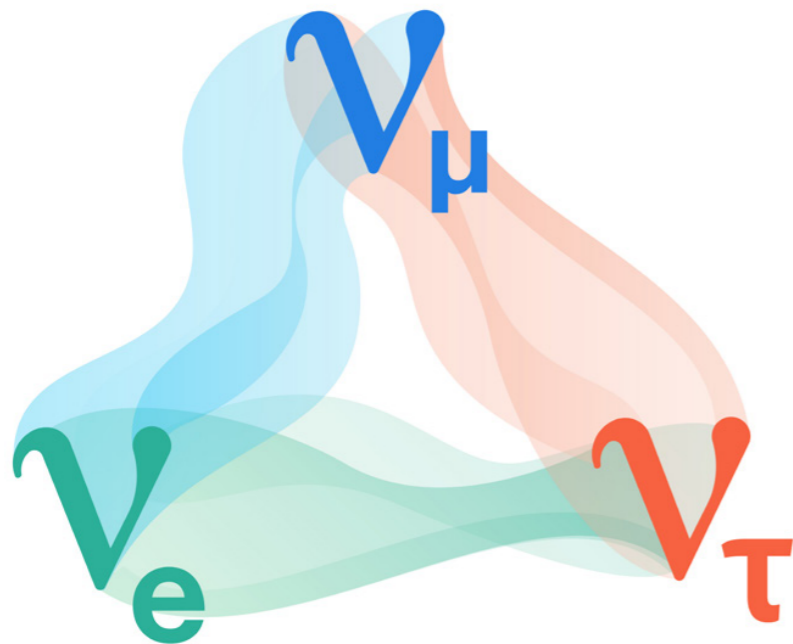


complicated



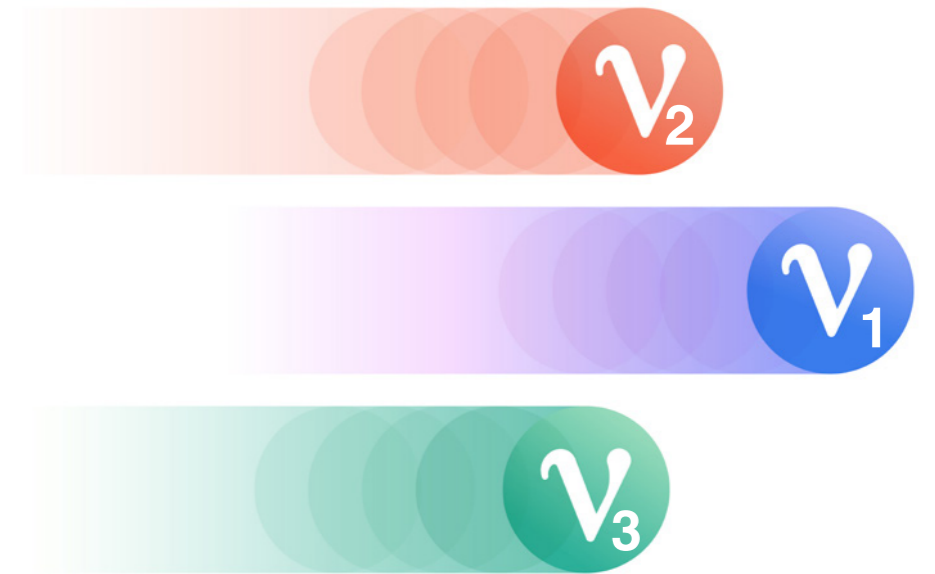
# Interactions:

simple



complicated

complicated



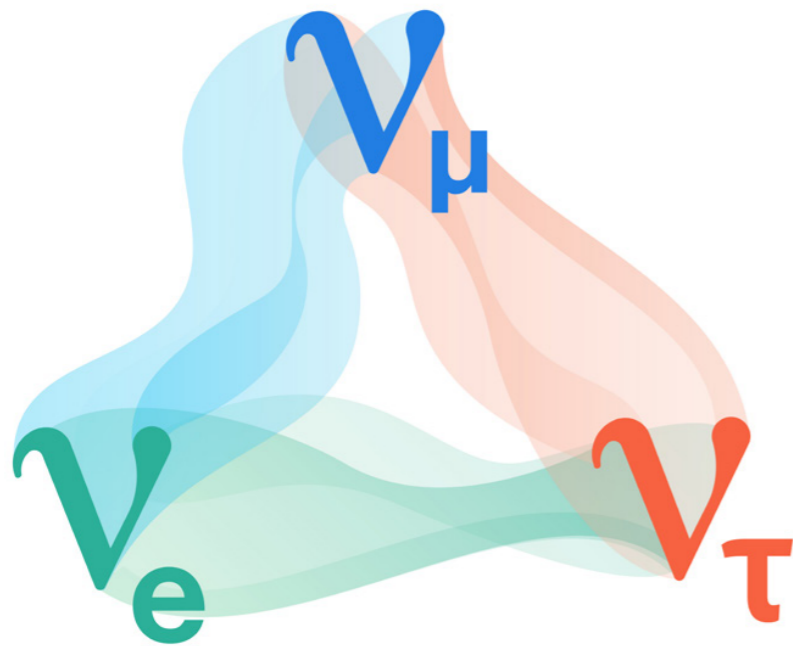
simple

# Propagation:

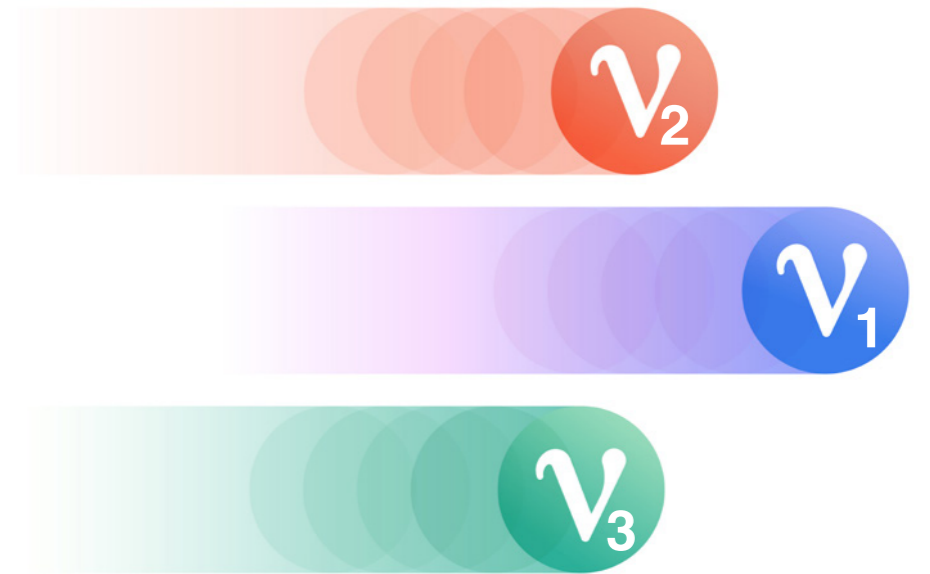
# Interactions:

simple

complicated



$$= U$$



complicated

simple

# Propagation:

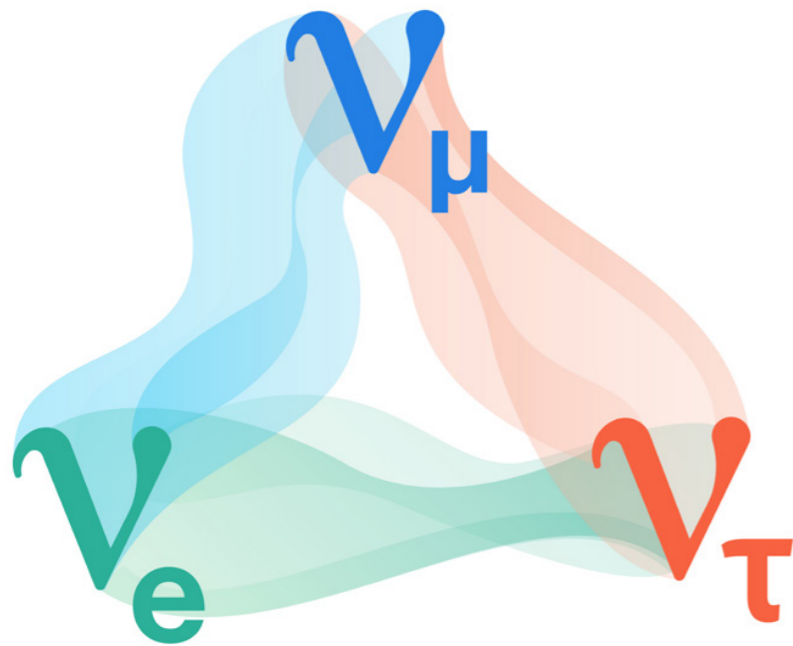




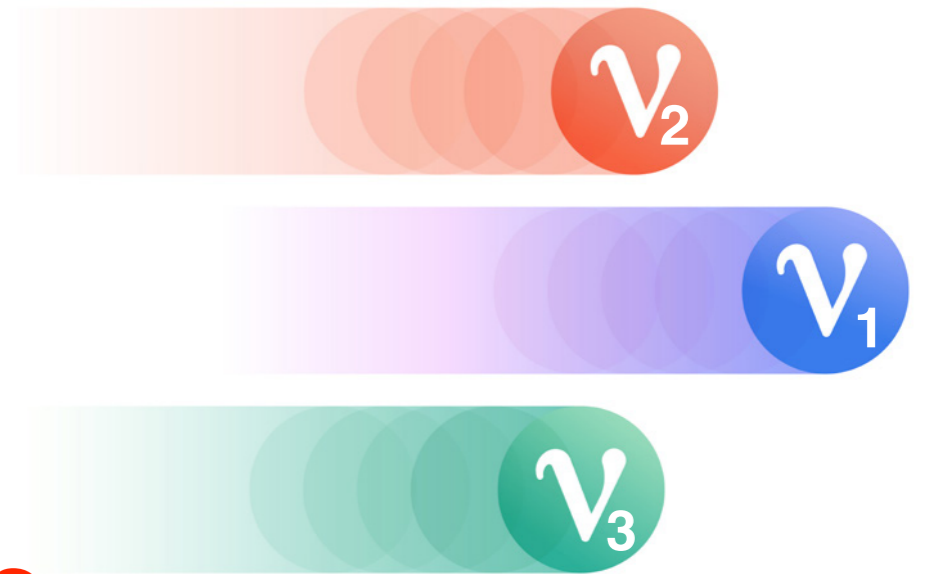
# Interactions:

simple

complicated



$$= U$$



**unitary matrix ?**

complicated

simple

**masses ?**

# Propagation:



unitary matrix

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

by defn  $|U_{e1}|^2 > |U_{e2}|^2 > |U_{e3}|^2$



unitary matrix

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

by defn  $|U_{e1}|^2 > |U_{e2}|^2 > |U_{e3}|^2$

$$U_{PMNS} = U_{23}(\theta_{23}, 0) U_{13}(\theta_{13}, \delta) U_{12}(\theta_{12}, 0) \quad \text{Why this order ???}$$

$$= \begin{pmatrix} 1 & & \\ & c_{23} & s_{23} \\ & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} & c_{13} & s_{13}e^{-i\delta} \\ & & 1 \\ -s_{13}e^{+i\delta} & & c_{13} \end{pmatrix} \begin{pmatrix} & c_{12} & s_{12} \\ -s_{12} & c_{12} & \\ & & 1 \end{pmatrix}$$

$$s_{ij} = \sin \theta_{ij}, \quad c_{ij} = \cos \theta_{ij} \quad \times \text{diag}(1, e^{i\frac{\alpha_{21}}{2}}, e^{i\frac{\alpha_{31}}{2}})$$



unitary matrix

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

by defn  $|U_{e1}|^2 > |U_{e2}|^2 > |U_{e3}|^2$

$$U_{PMNS} = U_{23}(\theta_{23}, 0) U_{13}(\theta_{13}, \delta) U_{12}(\theta_{12}, 0) \quad \text{Why this order ???}$$

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$$s_{ij} = \sin \theta_{ij}, c_{ij} = \cos \theta_{ij} \quad \times \text{diag}(1, e^{i\frac{\alpha_{21}}{2}}, e^{i\frac{\alpha_{31}}{2}})$$

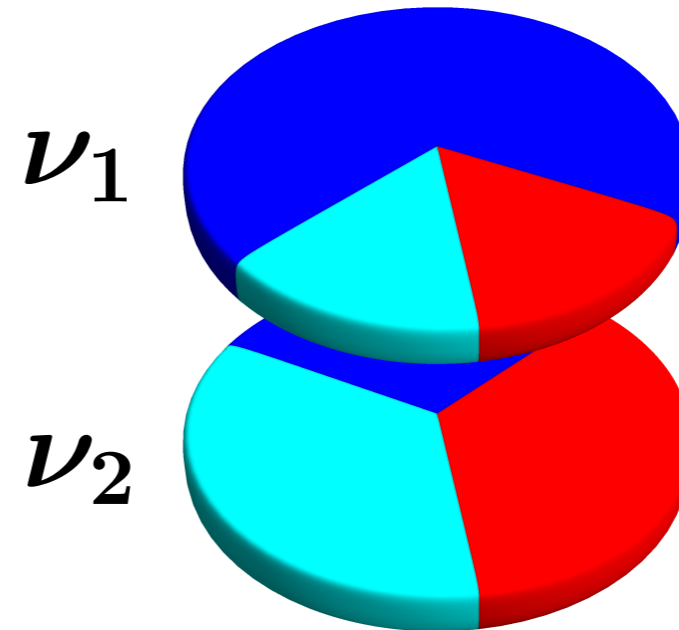
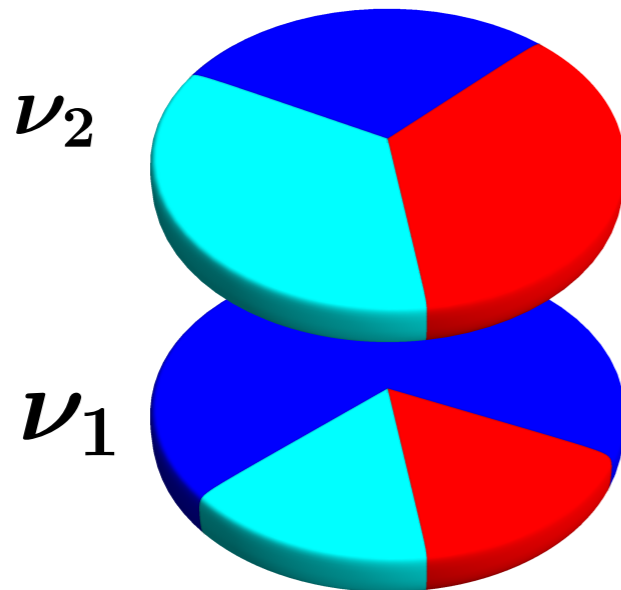
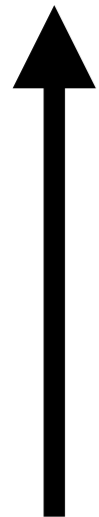
$$\begin{pmatrix} c_{13}c_{12} & c_{13}s_{12} & s_{13}e^{-i\delta} \\ -c_{23}s_{12} - s_{13}s_{23}c_{12}e^{i\delta} & c_{23}c_{12} - s_{13}s_{23}s_{12}e^{i\delta} & c_{13}s_{23} \\ s_{23}s_{12} - s_{13}c_{23}c_{12}e^{i\delta} & -s_{23}c_{12} - s_{13}c_{23}s_{12}e^{i\delta} & c_{13}c_{23} \end{pmatrix}$$



# $\nu_1, \nu_2$ Mass Ordering:

–solar mass ordering

mass



$$|\Delta m_{21}^2| = |m_2^2 - m_1^2| = 7.5 \times 10^{-5} \text{ eV}^2$$

$$L/E = 15 \text{ km/MeV} = 15,000 \text{ km/GeV}$$

# SNO

$$m_2 > m_1$$

$\nu_e =$  

$\nu_\mu =$  

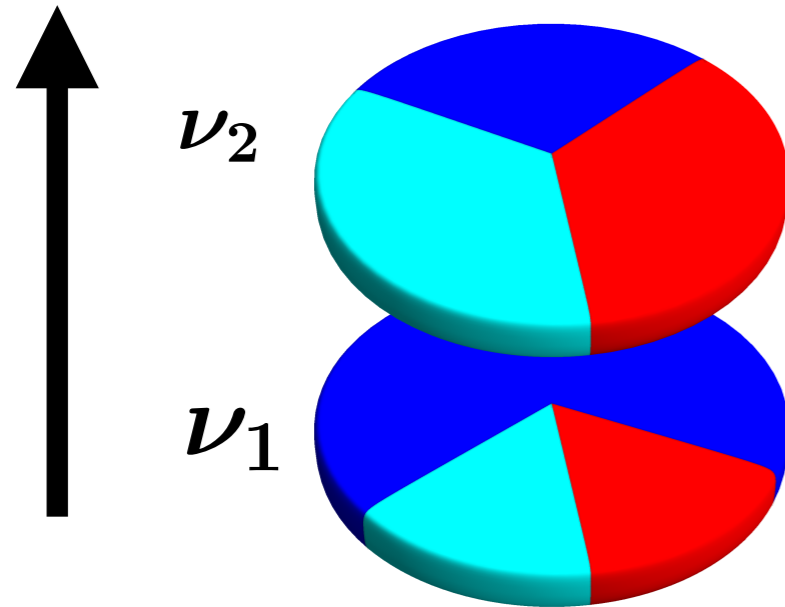
$\nu_\tau =$  



# $\nu_1, \nu_2$ Mass Ordering:

–solar mass ordering

mass



$$|\Delta m_{21}^2| = |m_2^2 - m_1^2| = 7.5 \times 10^{-5} \text{ eV}^2$$

$$L/E = 15 \text{ km/MeV} = 15,000 \text{ km/GeV}$$

# SNO

$$m_2 > m_1$$

$$\nu_e = \text{blue circle}$$

$$\nu_\mu = \text{cyan circle}$$

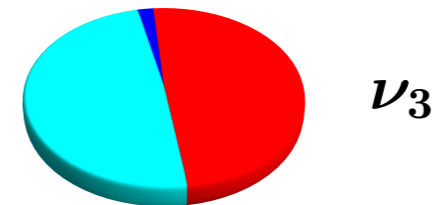
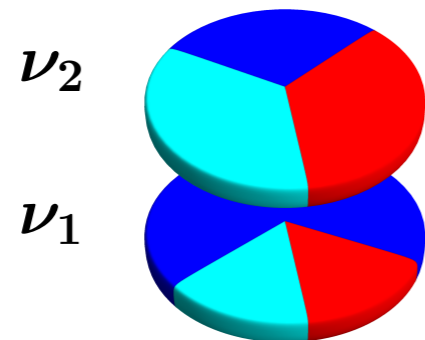
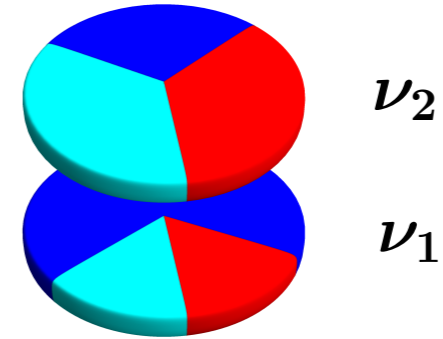
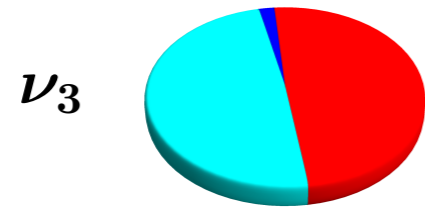
$$\nu_\tau = \text{red circle}$$



# $\nu_3, \nu_1/\nu_2$ Mass Ordering:

–atmospheric mass ordering

mass



$$|\Delta m_{31}^2| = |m_3^2 - m_1^2| = 2.5 \times 10^{-3} \text{ eV}^2$$

$$L/E = 0.5 \text{ km/MeV} = 500 \text{ km/GeV}$$

$\nu_e =$  

$\nu_\mu =$  

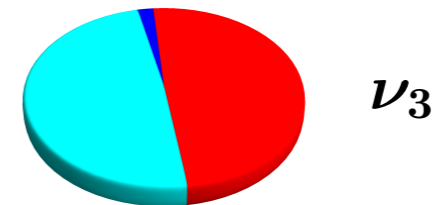
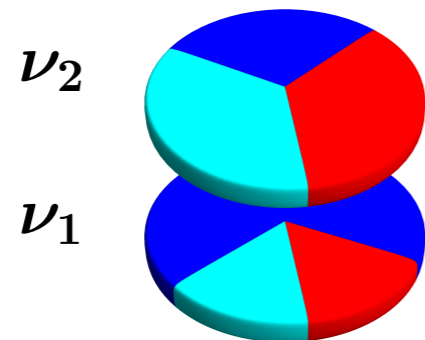
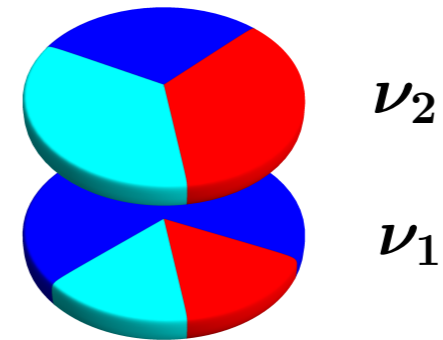
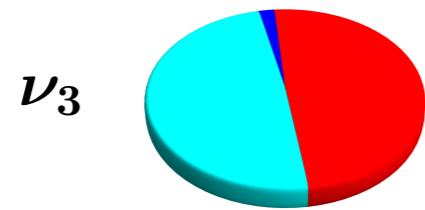
$\nu_\tau =$  



# $\nu_3, \nu_1/\nu_2$ Mass Ordering:

–atmospheric mass ordering

mass



$$|\Delta m_{31}^2| = |m_3^2 - m_1^2| = 2.5 \times 10^{-3} \text{ eV}^2$$

$$L/E = 0.5 \text{ km/MeV} = 500 \text{ km/GeV}$$

Unknown: NO $\nu$ A, JUNO, ICECUBE, DUNE, T2HKK....

$\nu_e =$  

$\nu_\mu =$  

$\nu_\tau =$  





# Summary:

## Octant of $\theta_{23}$

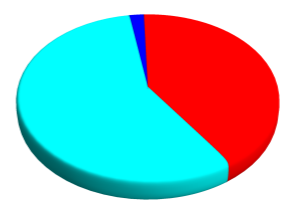
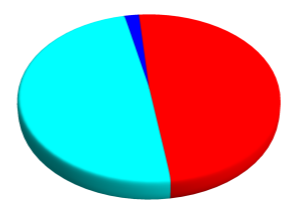
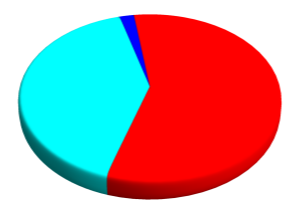
$\sin^2 \theta_{23}$

0.40

0.50

0.60


$\nu_3$




0

$\delta$

$\pm \pi/2$

$\nu_e =$  

$\nu_\mu =$  

$\nu_\tau =$  

$\pi$



# Summary:

## Octant of $\theta_{23}$

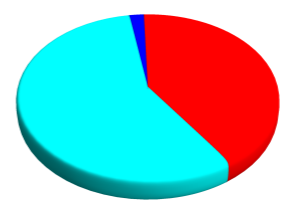
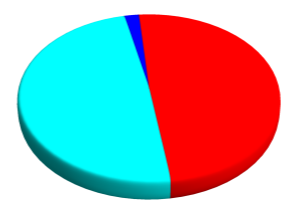
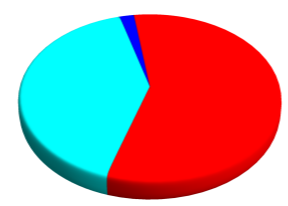
$\sin^2 \theta_{23}$

0.40

0.50

0.60

$\nu_3$



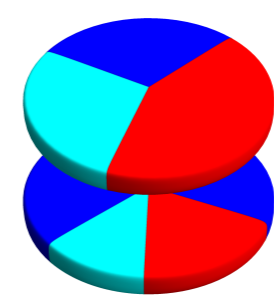
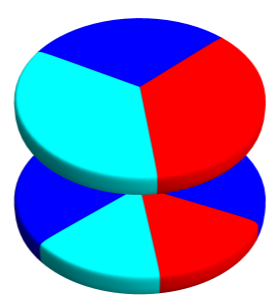
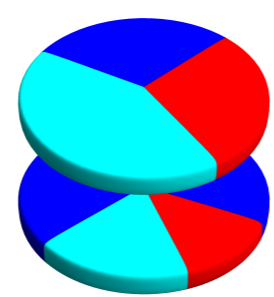
0

$\delta$

$\pm \pi/2$

$\nu_2$

$\nu_1$



$\nu_e =$

$\nu_\mu =$

$\nu_\tau =$

$\pi$

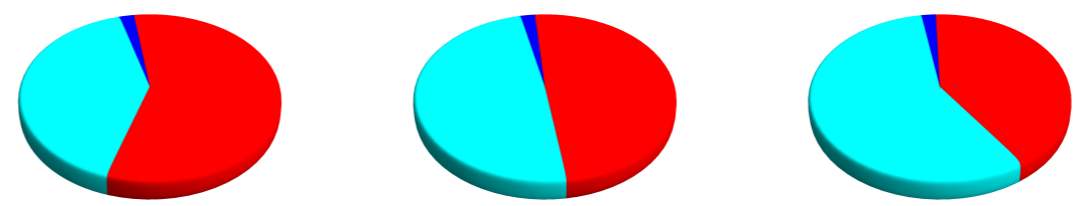


# Summary:

## Octant of $\theta_{23}$

$\sin^2 \theta_{23}$       **0.40**      **0.50**      **0.60**

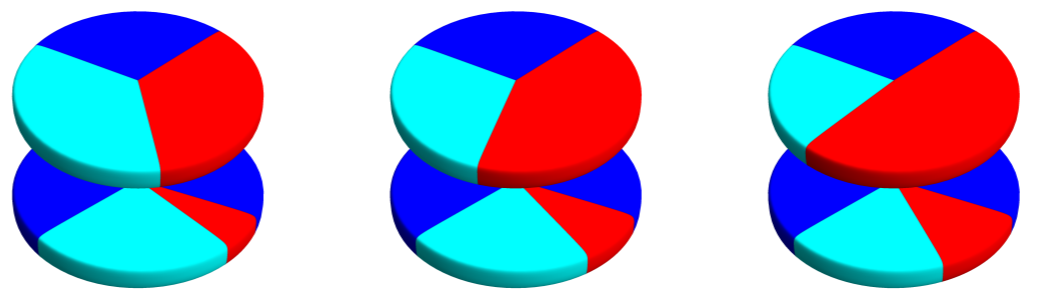
$\nu_3$



0

$\nu_2$

$\nu_1$

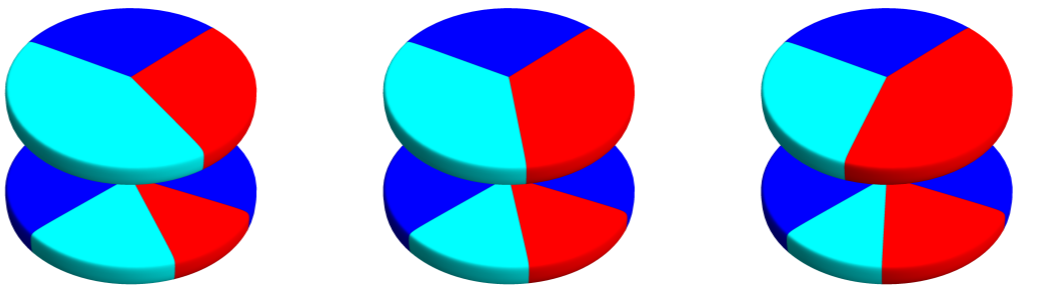


$\delta$

$\pm \pi/2$

$\nu_2$

$\nu_1$



$\nu_e =$

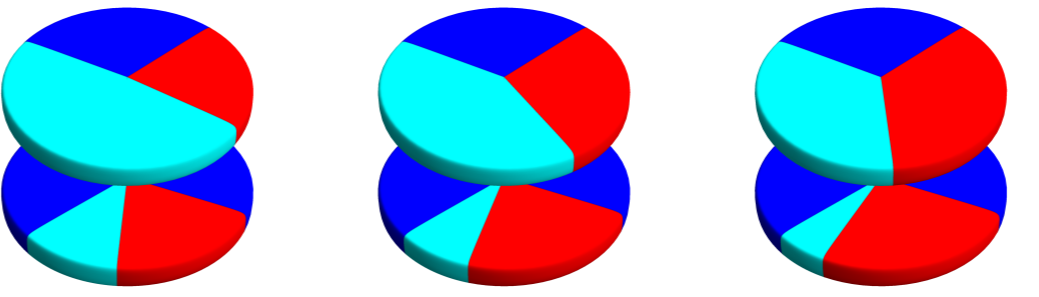
$\nu_\mu =$

$\nu_\tau =$

$\pi$

$\nu_2$

$\nu_1$



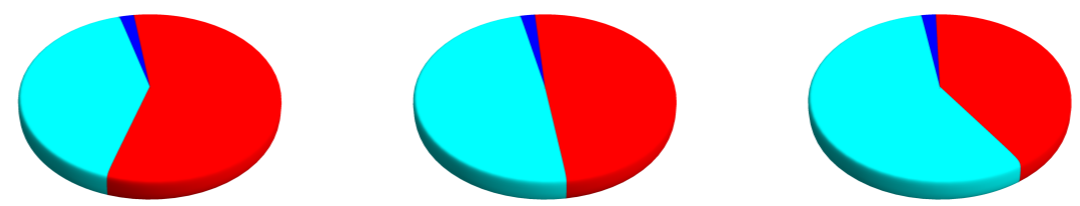


# Summary:

## Octant of $\theta_{23}$

$\sin^2 \theta_{23}$       **0.40**      **0.50**      **0.60**

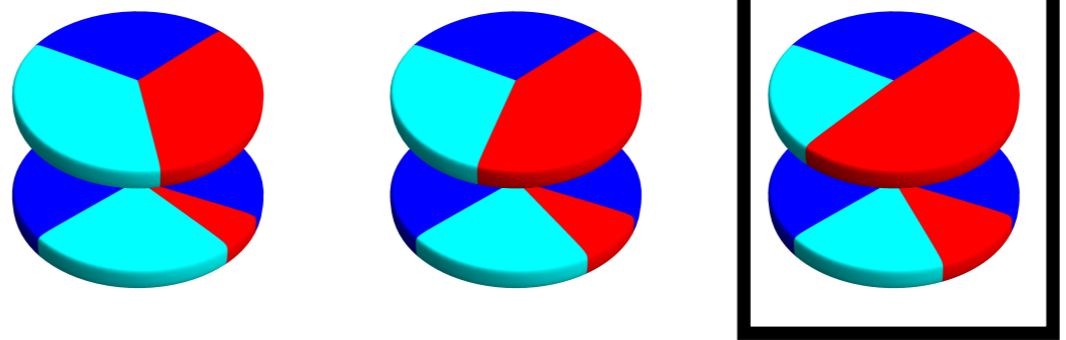
$\nu_3$



0

$\nu_2$

$\nu_1$



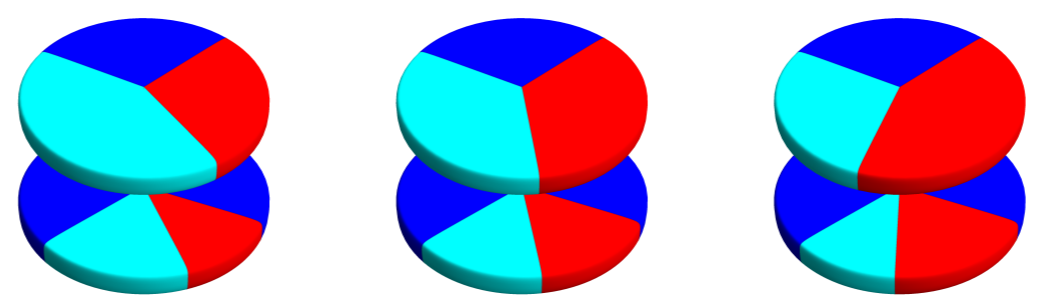
$\nu_2$  variation

$\delta$

$\pm \pi/2$

$\nu_2$

$\nu_1$

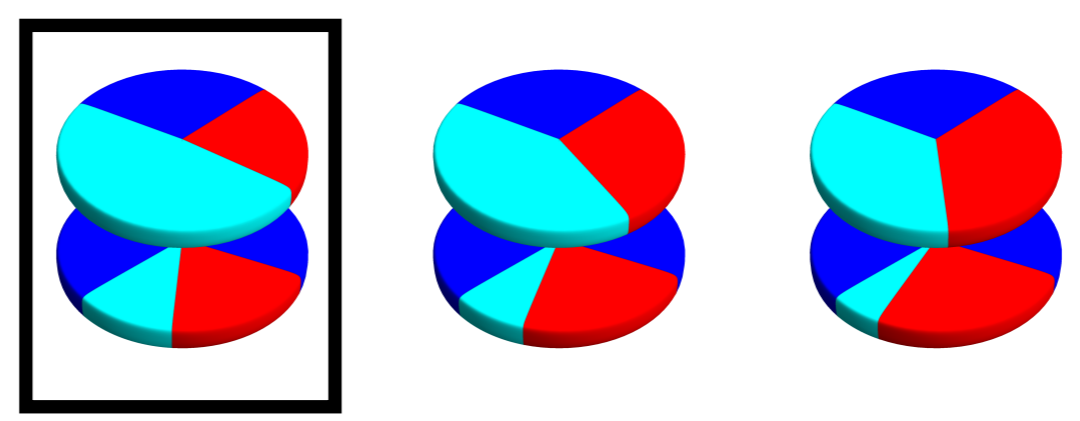


- $\nu_e =$  ●
- $\nu_\mu =$  ●
- $\nu_\tau =$  ●

$\pi$

$\nu_2$

$\nu_1$



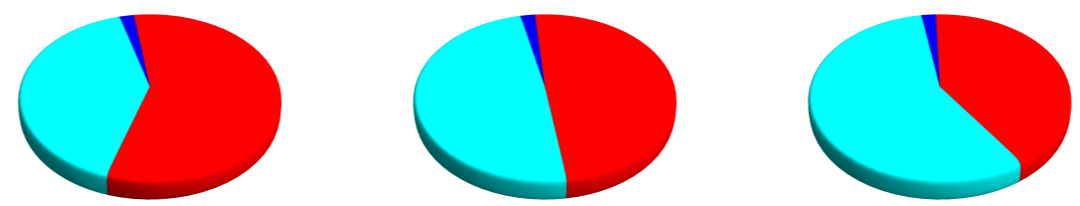


# Summary:

## Octant of $\theta_{23}$

$\sin^2 \theta_{23}$       **0.40**      **0.50**      **0.60**

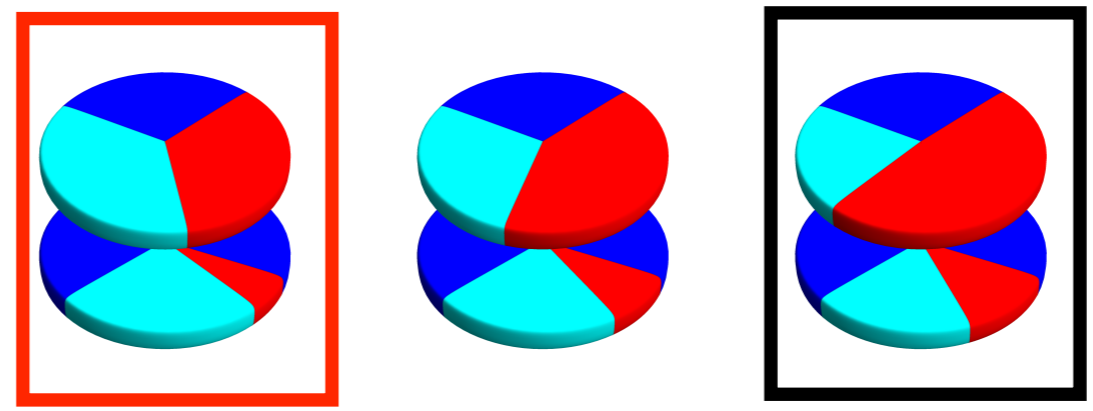
$\nu_3$



0

$\nu_2$

$\nu_1$



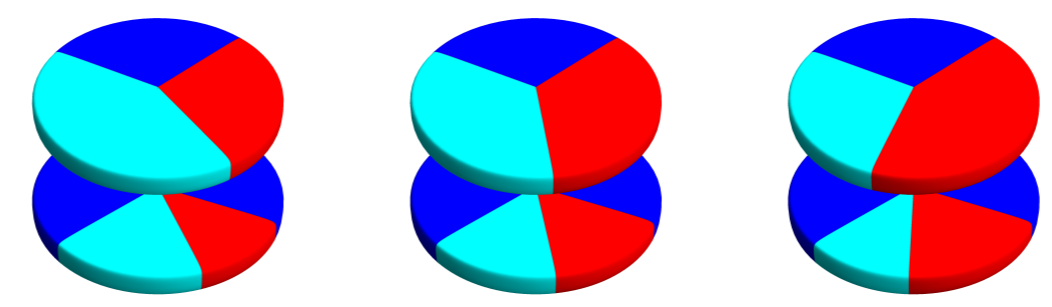
$\nu_2$  variation

$\delta$

$\pm \pi/2$

$\nu_2$

$\nu_1$

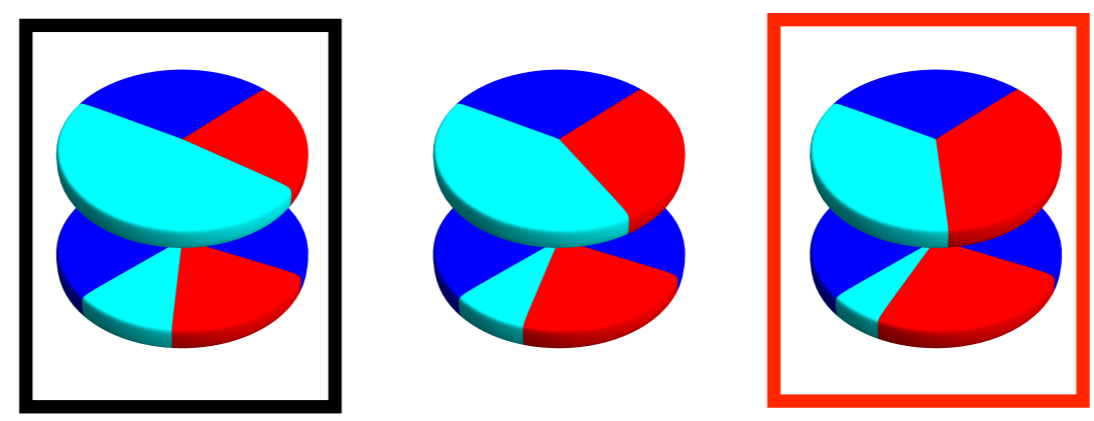


- $\nu_e =$
- $\nu_\mu =$
- $\nu_\tau =$

$\pi$

$\nu_2$

$\nu_1$



$\nu_1$  variation

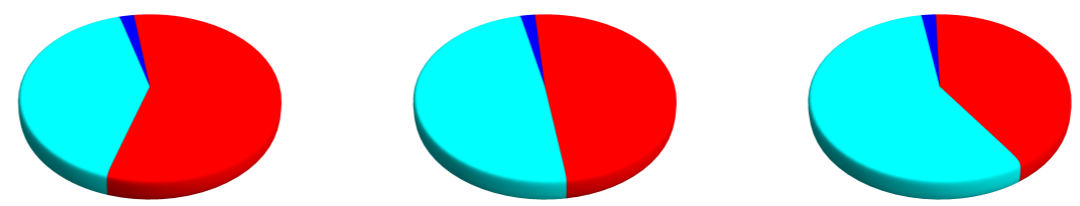


# Summary:

## Octant of $\theta_{23}$

$\sin^2 \theta_{23}$       0.40      0.50      0.60

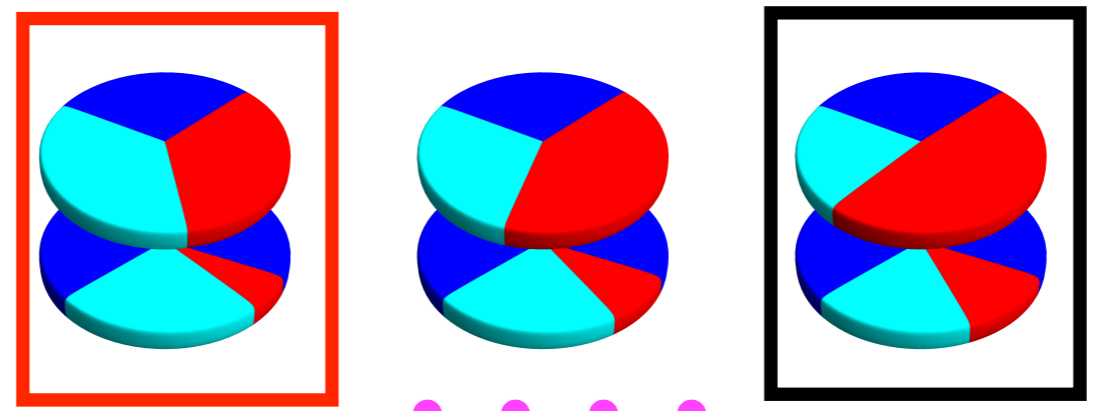
$\nu_3$



0

$\nu_2$

$\nu_1$



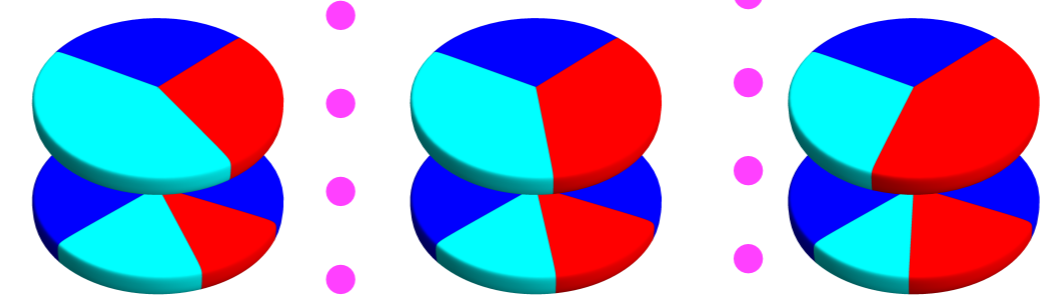
$\nu_2$  variation

$\delta$

$\pm \pi/2$

$\nu_2$

$\nu_1$

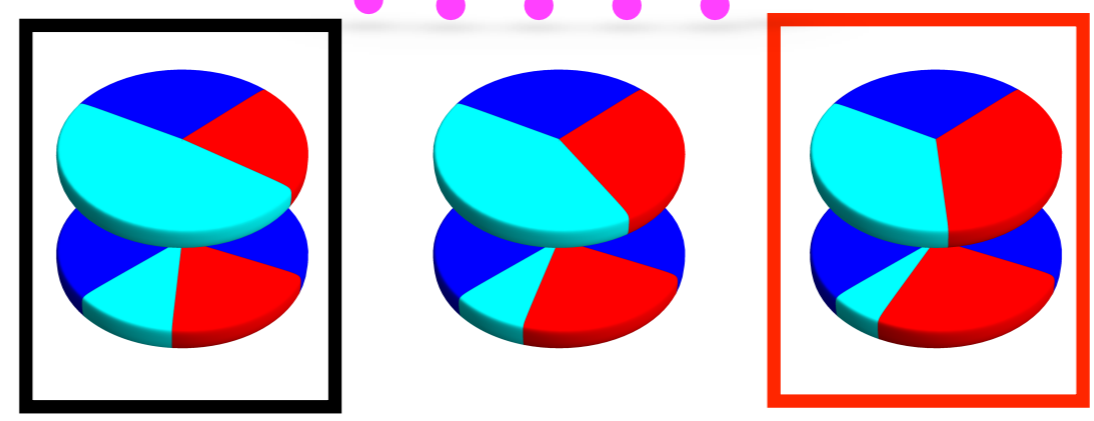


- $\nu_e =$
- $\nu_\mu =$
- $\nu_\tau =$

$\pi$

$\nu_2$

$\nu_1$



$\nu_1$  variation



# WHY?

**Precision  
Neutrino  
Measurements:**



# WHY?

**Precision  
Neutrino  
Measurements:**

**To discover neutrino BSM,  
one needs precision predictions for nuSM**



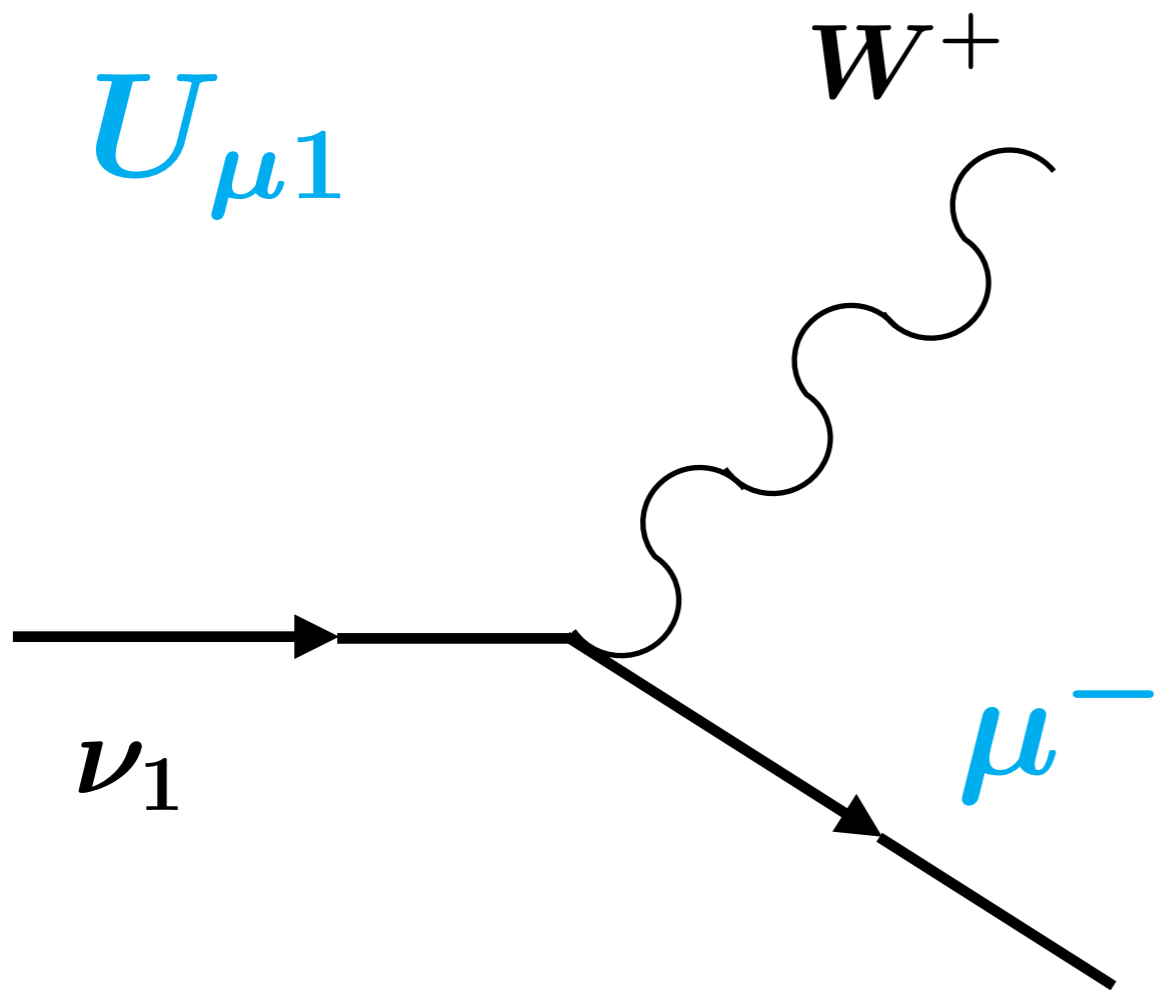


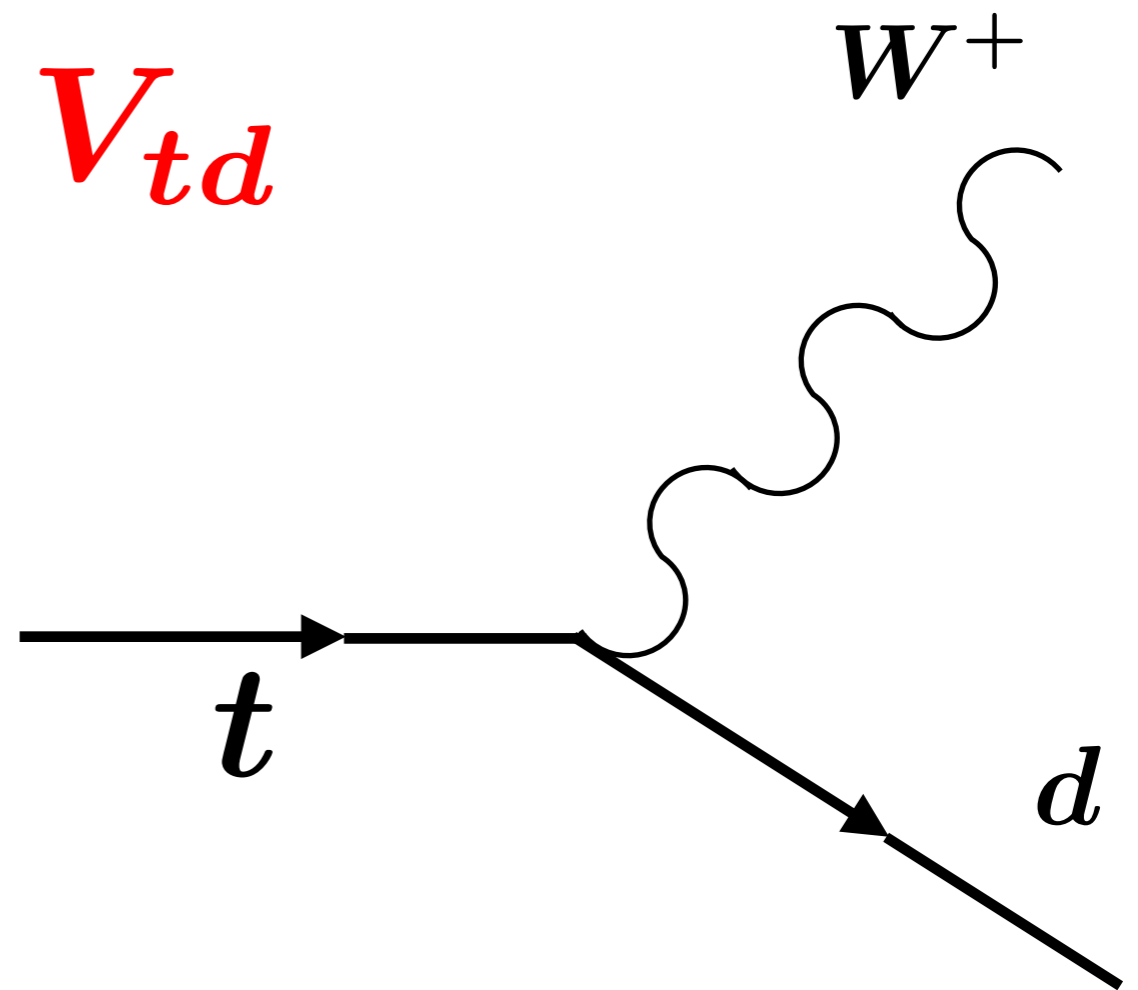
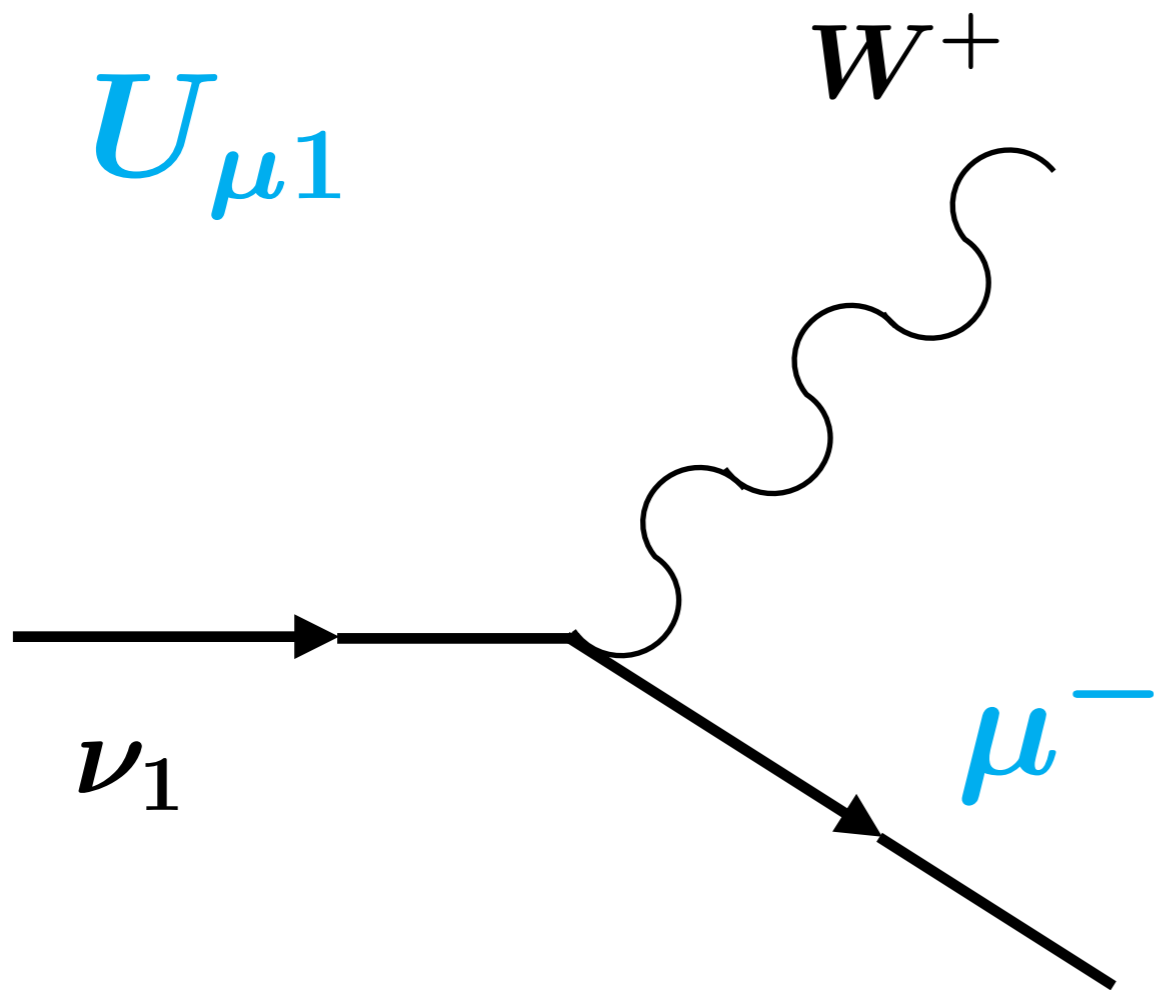
**Determine flavor  
fractions of neutrino  
mass states**

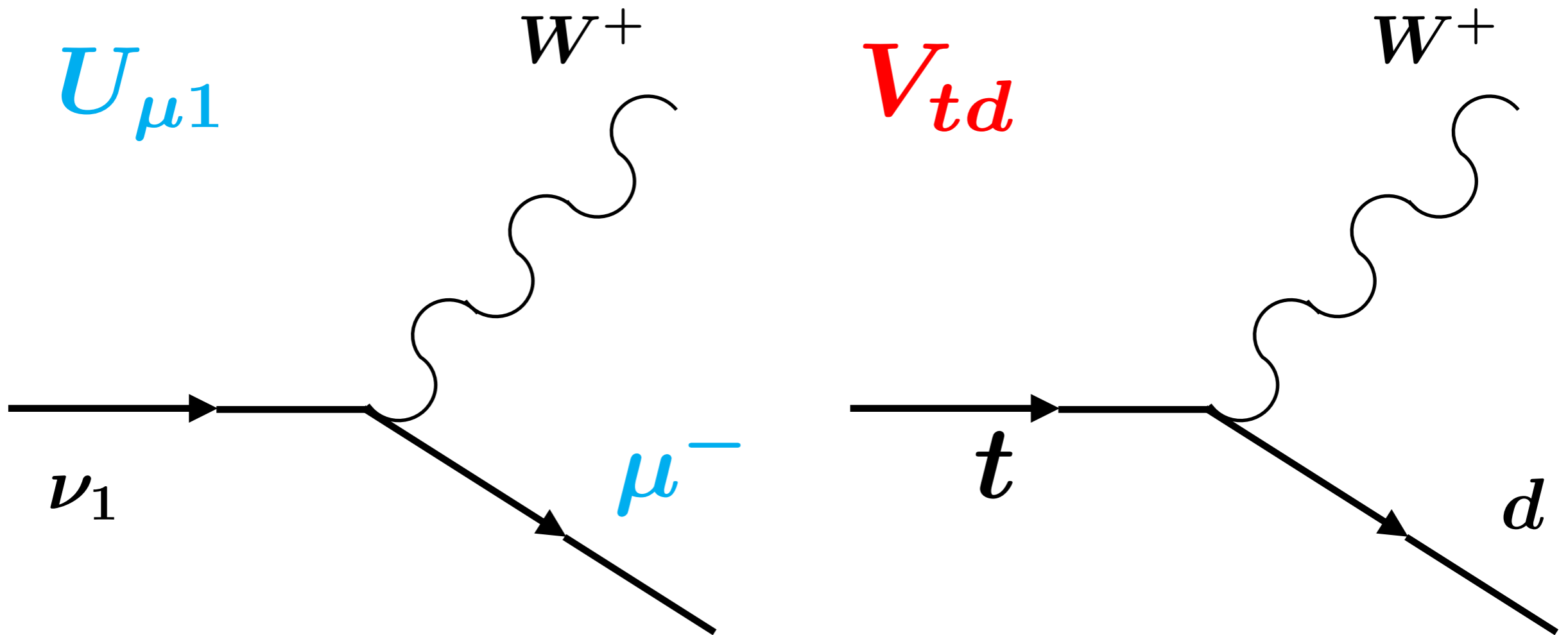
**WHY?**

**Precision  
Neutrino  
Measurements:**

**To discover neutrino BSM,  
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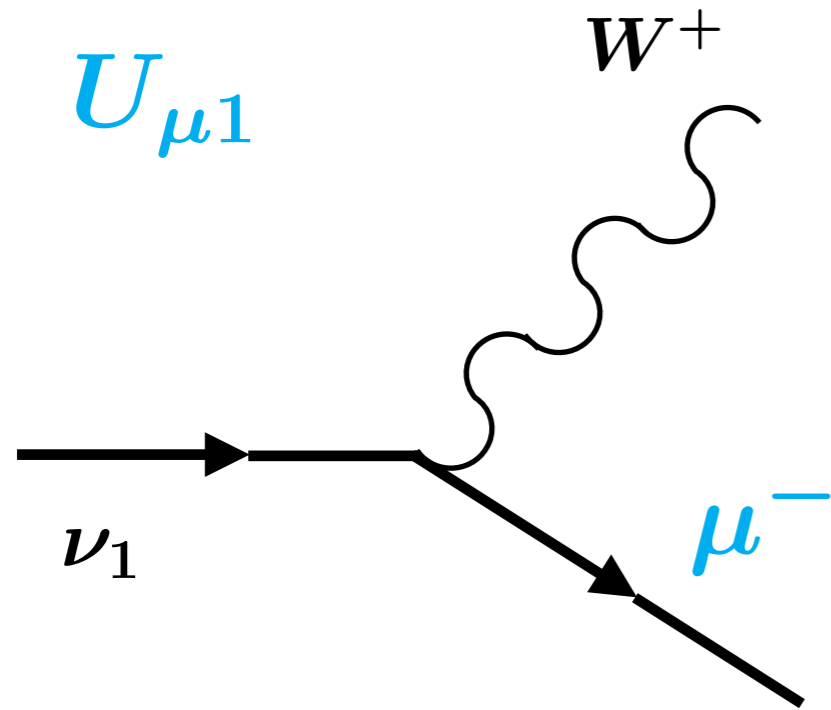




Rates:  $|U_{\mu 1}|^2$  &  $|V_{td}|^2$



# Leptons:

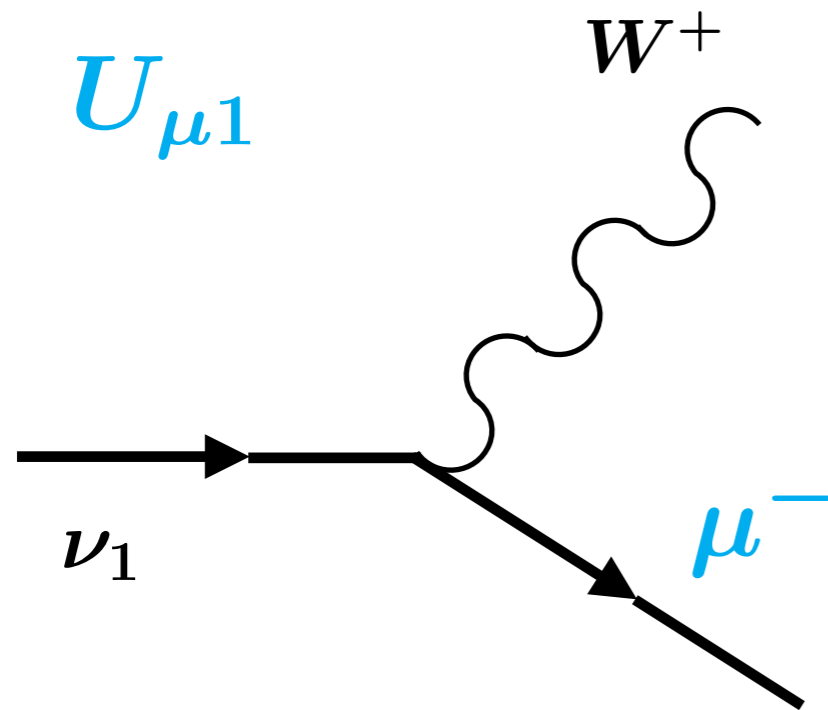


$$0.08 < |U_{\mu 1}|^2 < 0.24$$

variation in  $\delta$  only !



# Leptons:



$0.08 < |U_{\mu 1}|^2 < 0.24$   
variation in  $\delta$  only !

**factor of 3 diff.**

$$|U_{\mu 3}|^2 = 0.4 - 0.6$$

$$|U_{\mu 2}|^2 = 0.26 - 0.41$$

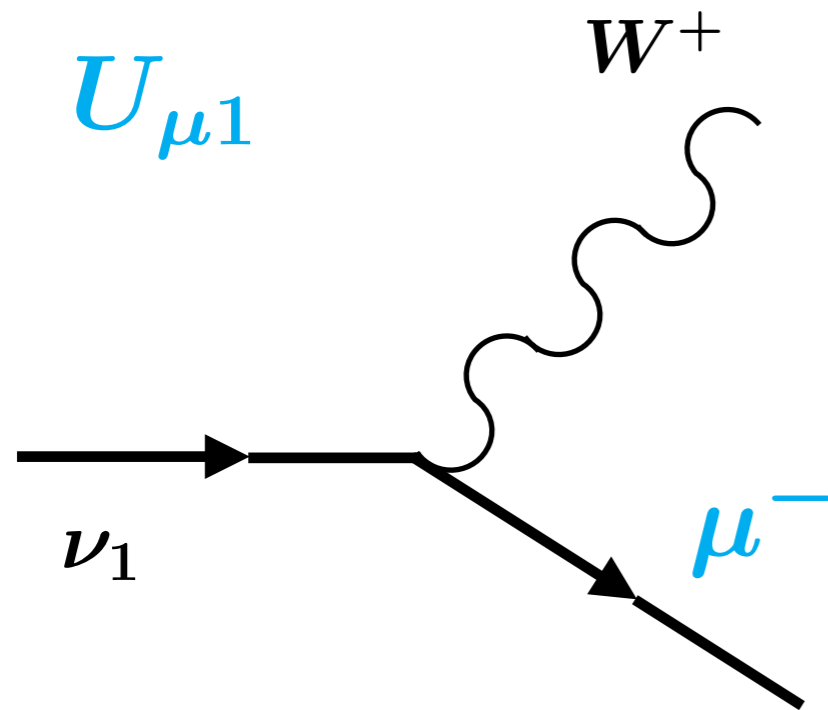
$$|U_{\mu 1}|^2 = 0.08 - 0.24$$



# Leptons:

# Quarks:

$|V_{ij}|^2$  essentially independent of  $\delta_q$  !



$0.08 < |U_{\mu 1}|^2 < 0.24$   
variation in  $\delta$  only !

**factor of 3 diff.**

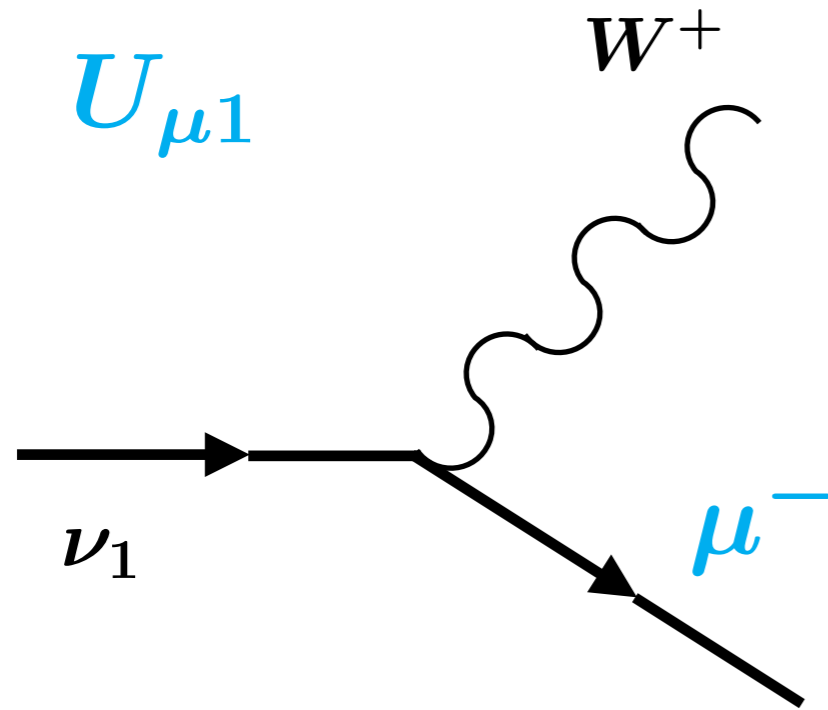
$$|U_{\mu 3}|^2 = 0.4 - 0.6$$

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$$|U_{\mu 1}|^2 = 0.08 - 0.24$$



# Leptons:



$0.08 < |U_{\mu 1}|^2 < 0.24$   
variation in  $\delta$  only !

**factor of 3 diff.**

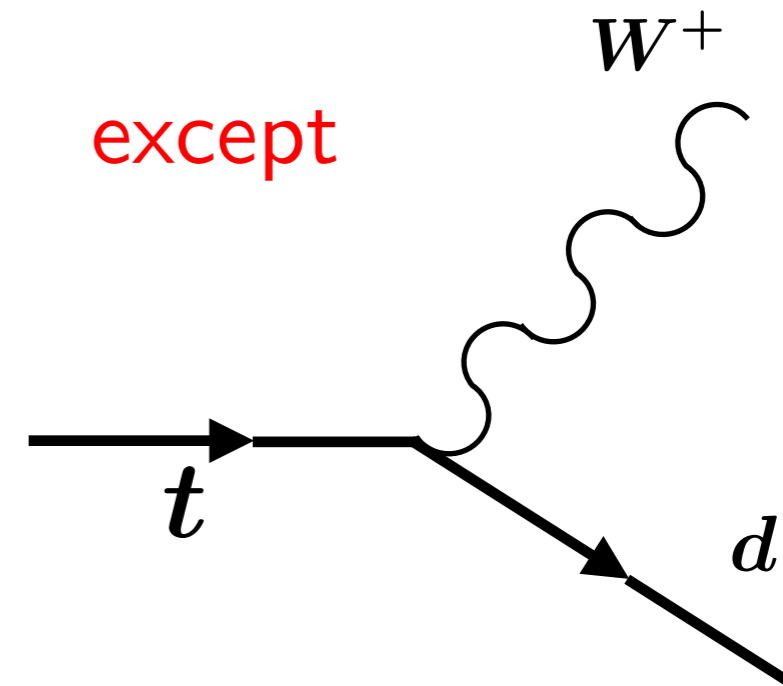
$$|U_{\mu 3}|^2 = 0.4 - 0.6$$

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$$|U_{\mu 1}|^2 = 0.08 - 0.24$$

# Quarks:

$|V_{ij}|^2$  essentially independent of  $\delta_q$  !



except

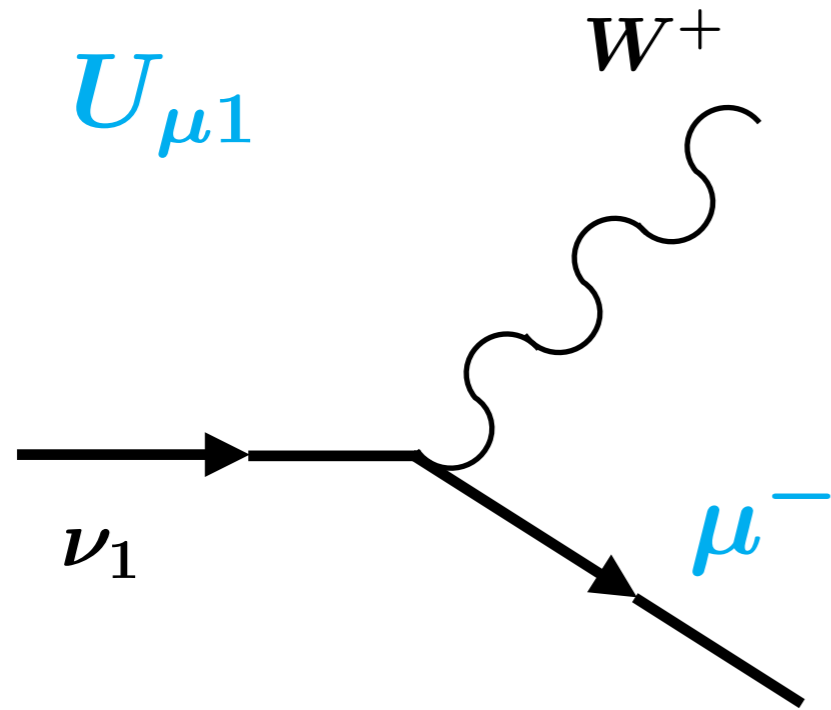
$$V_{td} \approx A\lambda^3(1 - 0.37e^{i\delta_q})$$

$$|V_{td}|^2 \approx 10^{-4}$$





# Leptons:



$0.08 < |U_{\mu 1}|^2 < 0.24$   
variation in  $\delta$  only !

**factor of 3 diff.**

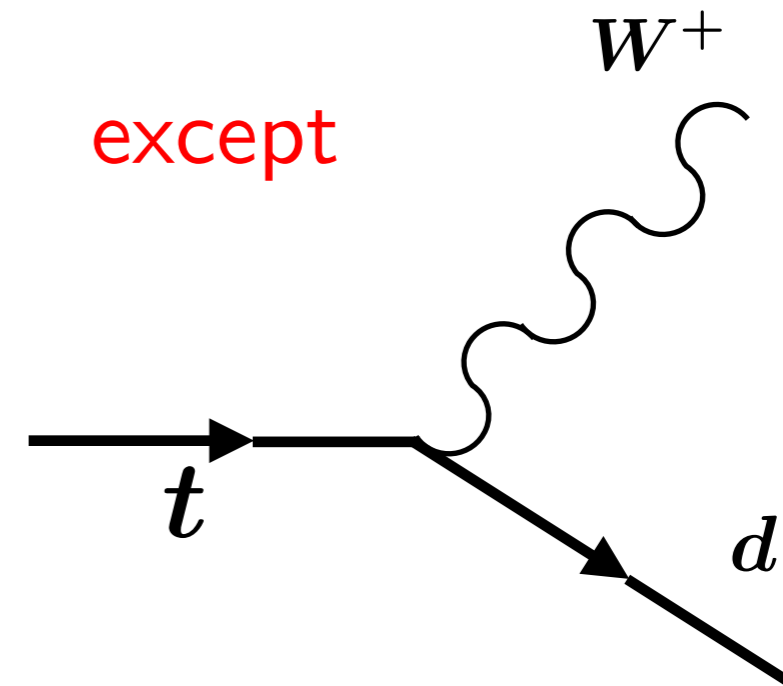
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# Quarks:

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except

$$V_{td} \approx A\lambda^3(1 - 0.37e^{i\delta_q})$$

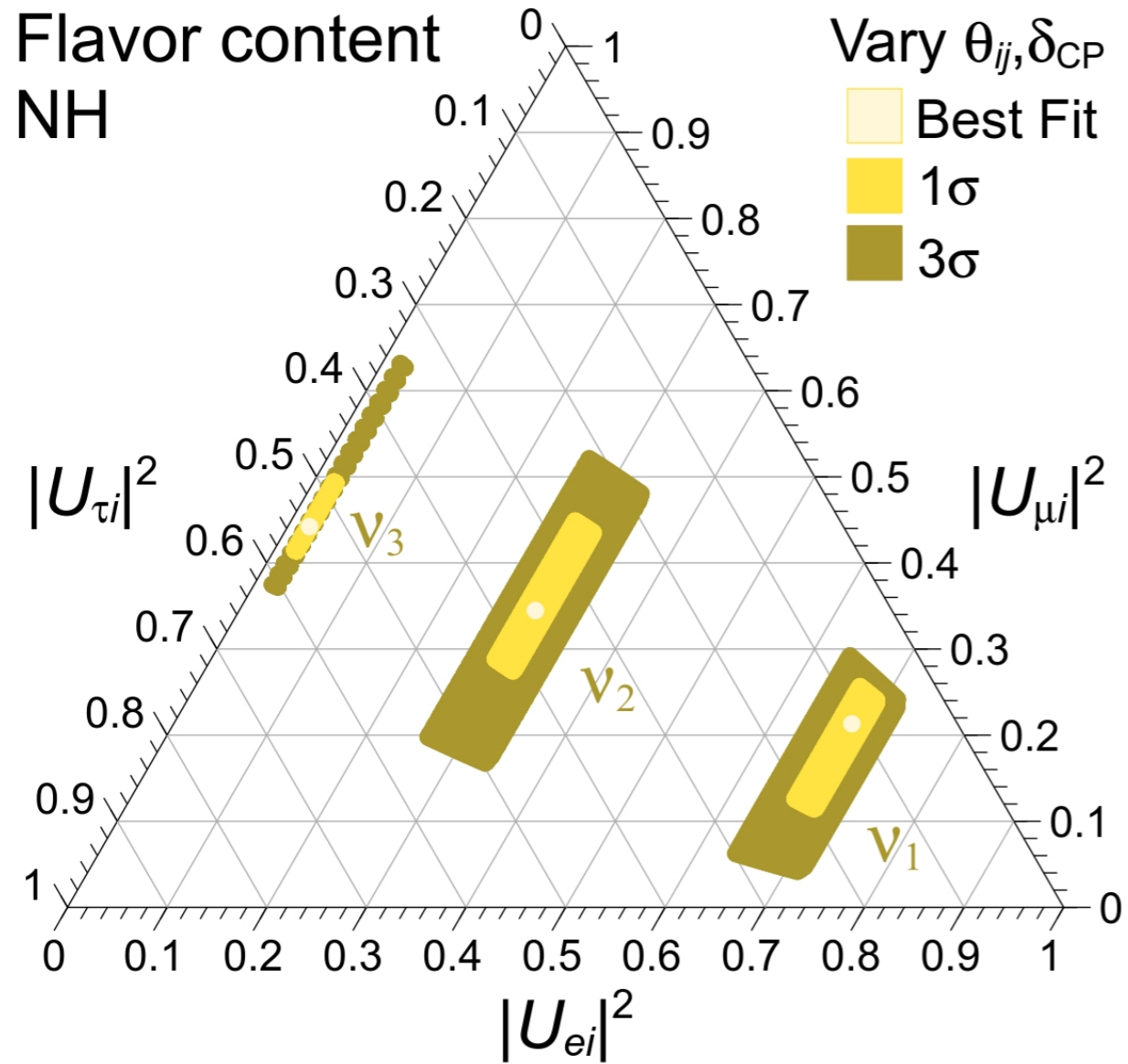
$$|V_{td}|^2 \approx 10^{-4}$$



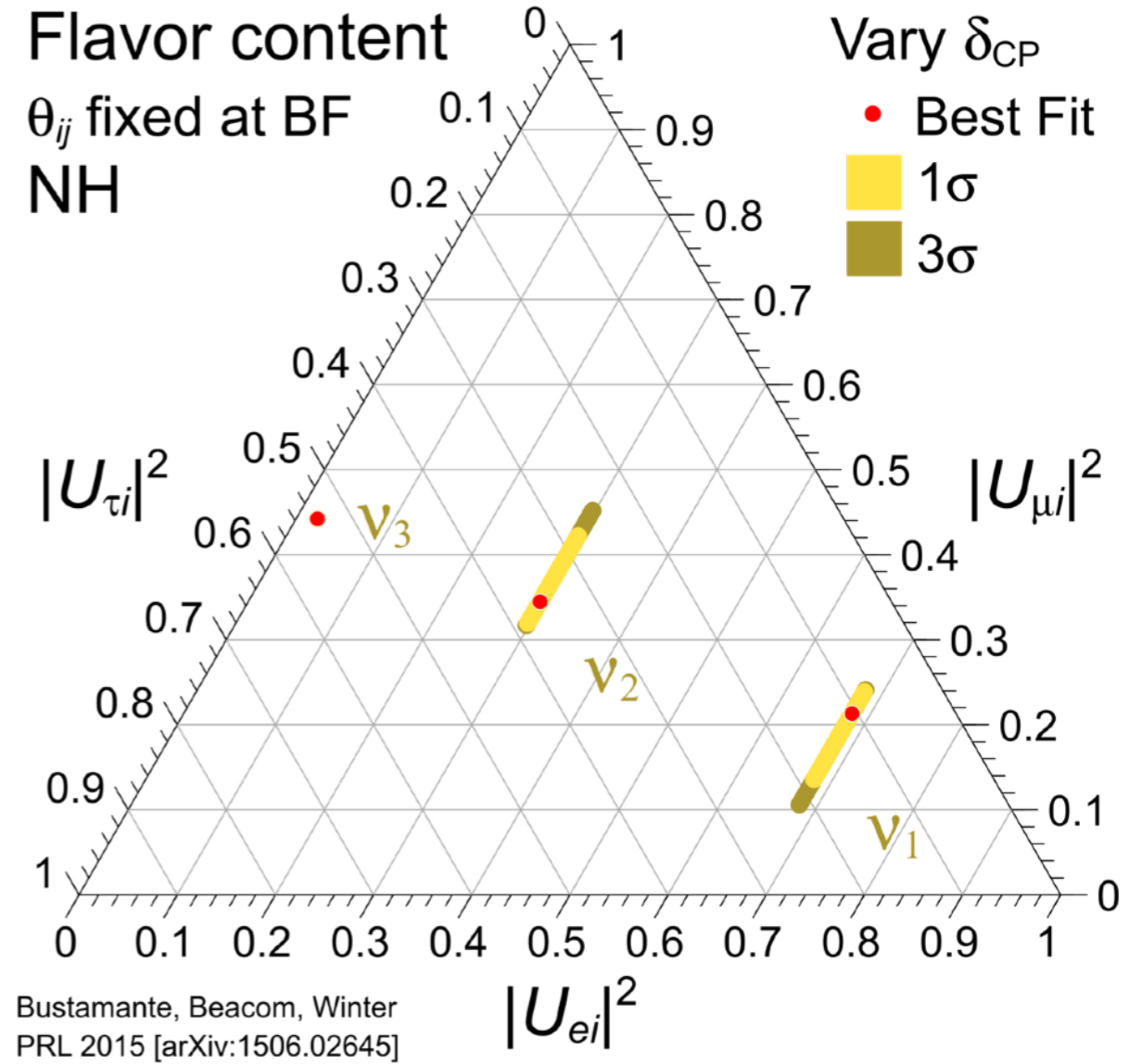
$$|V_{tb}|^2 \approx 1$$

$$|V_{ts}|^2 \sim \lambda^4 \approx 2 \times 10^{-3}$$

$$|V_{td}|^2 \sim \lambda^6 \approx 8 \times 10^{-5}$$



$\delta$  &  $\theta_{23}$  uncertainty

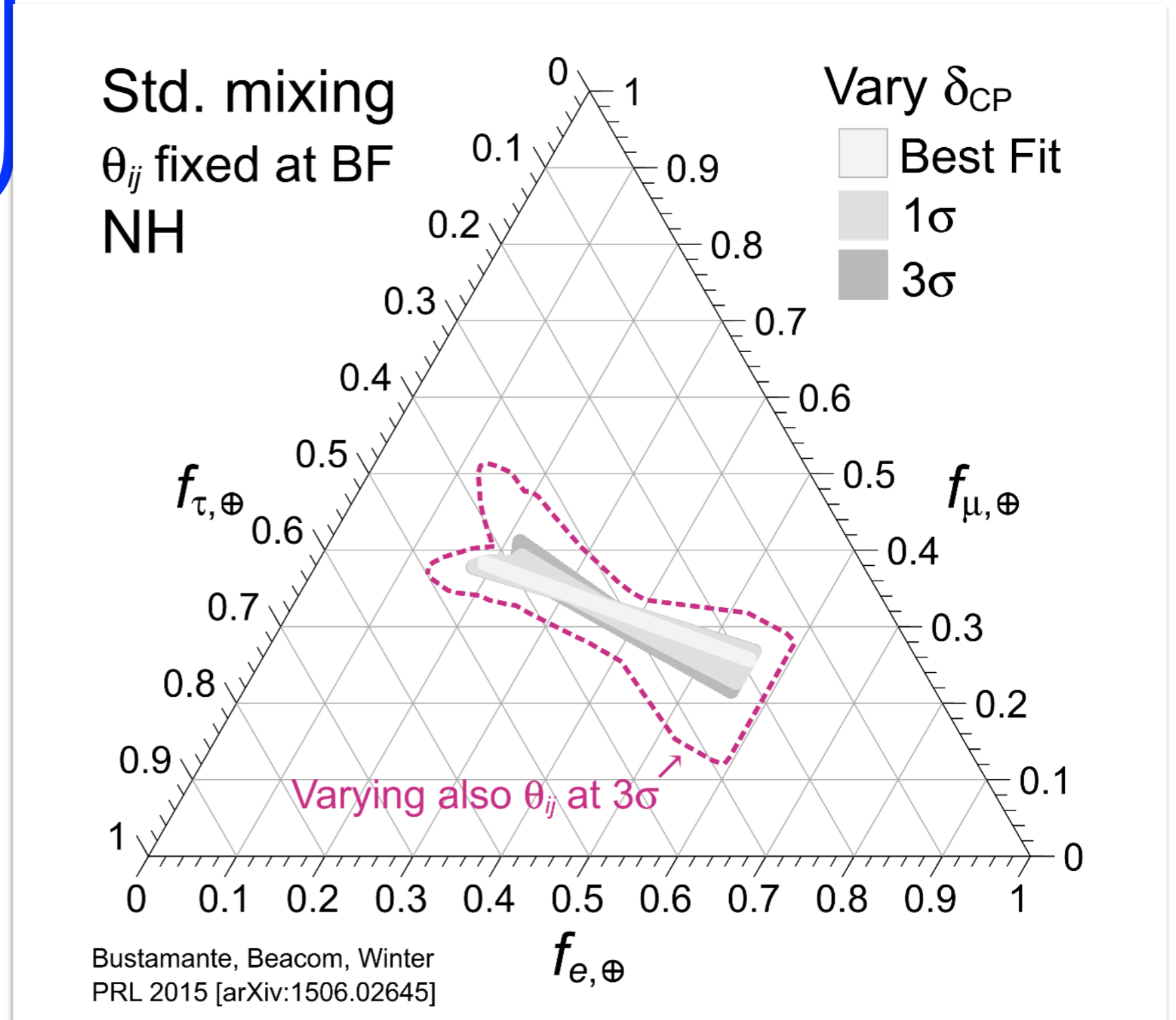


no  $\theta_{23}$  uncertainty



Determine flavor fractions of neutrino mass states

Precision Predictions for flavor ratios at ICECUBE.





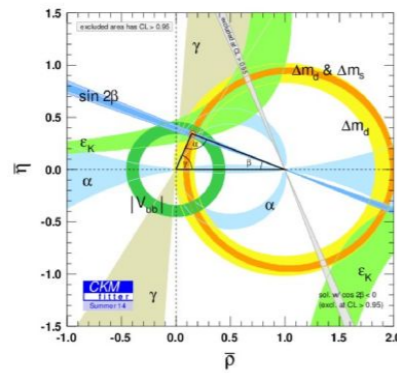
# WHY?

**Determine flavor  
fractions of neutrino  
mass states**

**Stress Test  
Neutrino paradigm  
search for new physics**

**Precision  
Neutrino  
Measurements:**

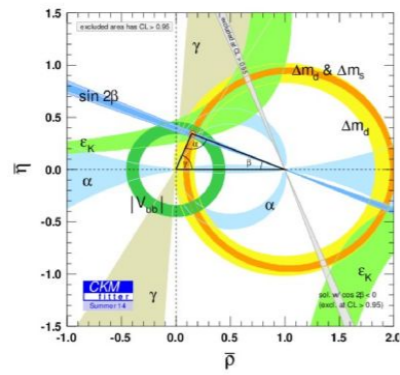
# Quark



**Stress Test**  
**Neutrino paradigm**  
**search for new physics**



# Quark

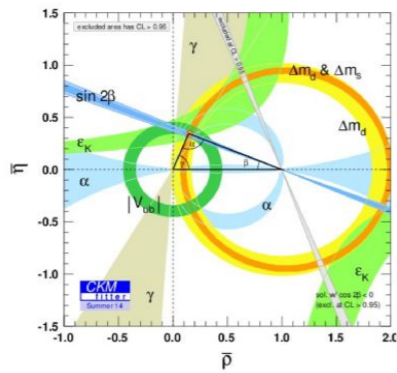


$$A\lambda^3$$

**Stress Test**  
**Neutrino paradigm**  
**search for new physics**

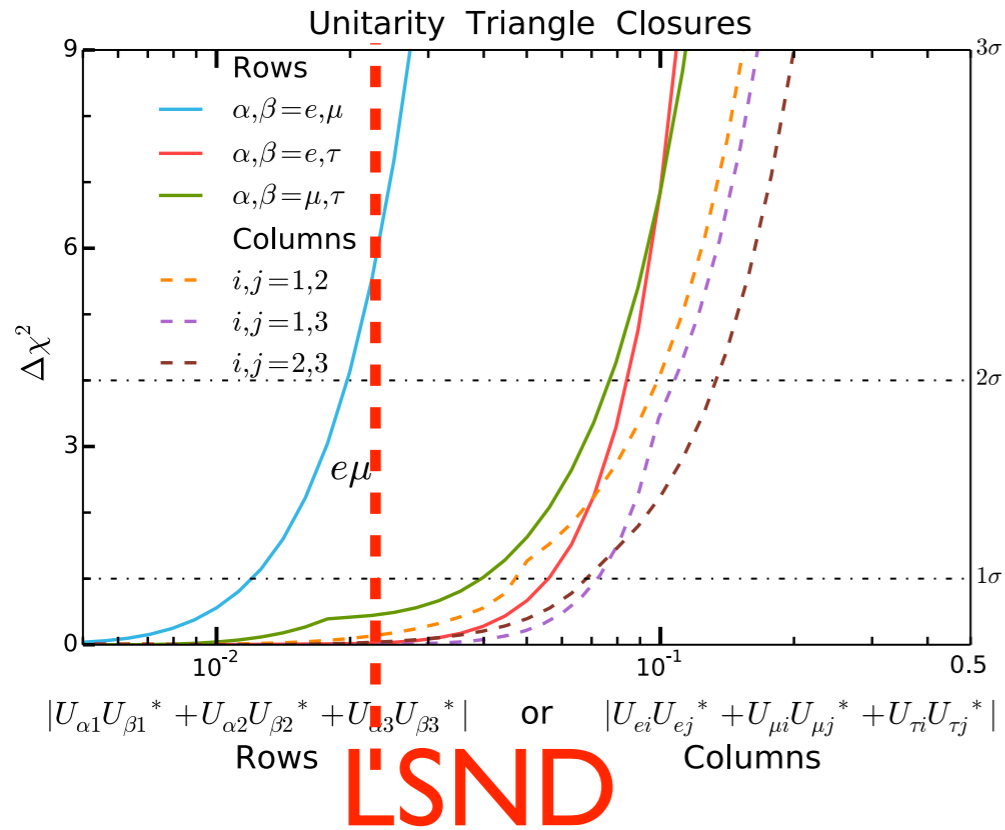


# Quark



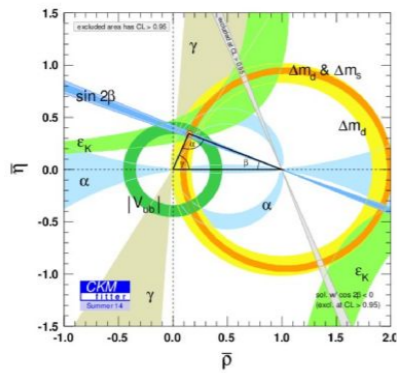
$A\lambda^3$

Stress Test  
Neutrino paradigm  
search for new physics



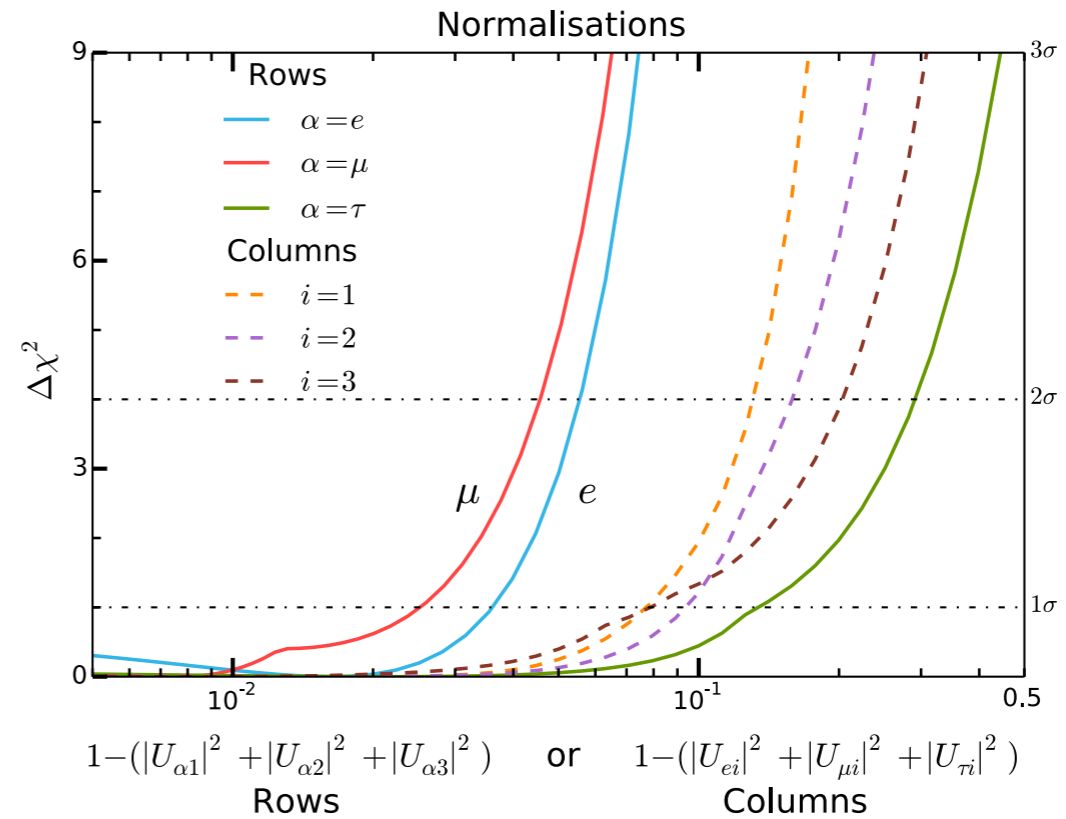
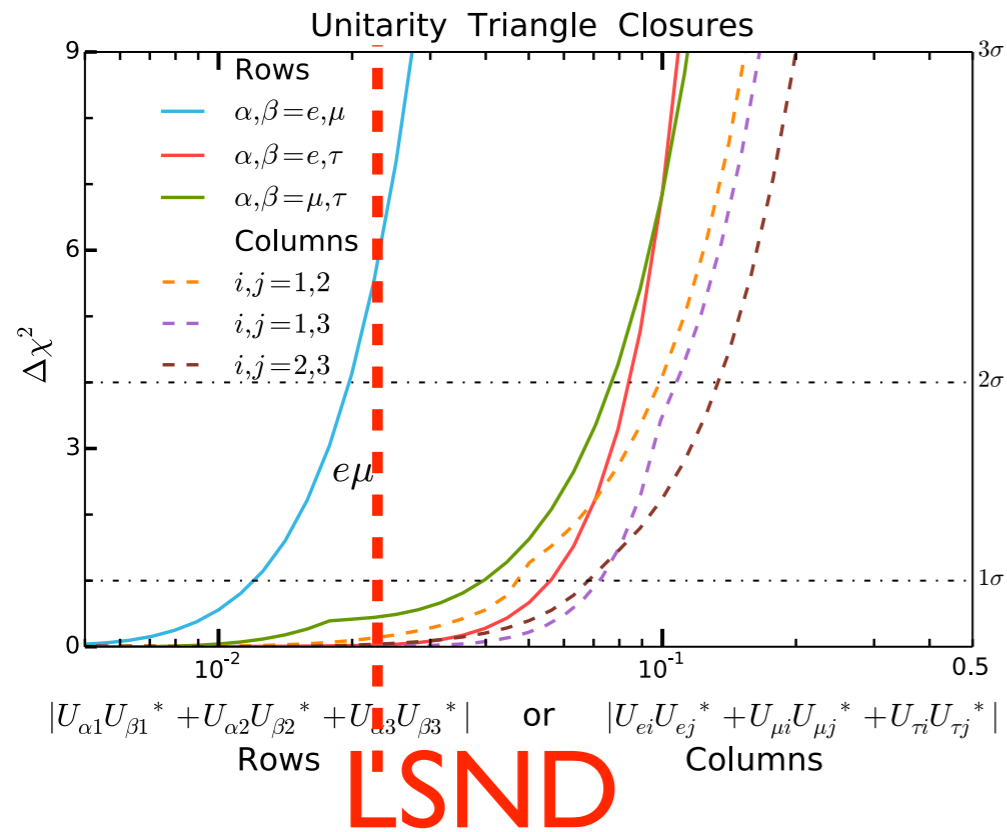
M. Ross-Lonergan + SP  
arXiv:1508.05095

# Quark



$A\lambda^3$

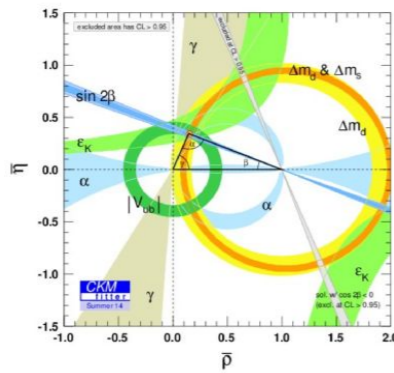
Stress Test  
Neutrino paradigm  
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arXiv:1508.05095

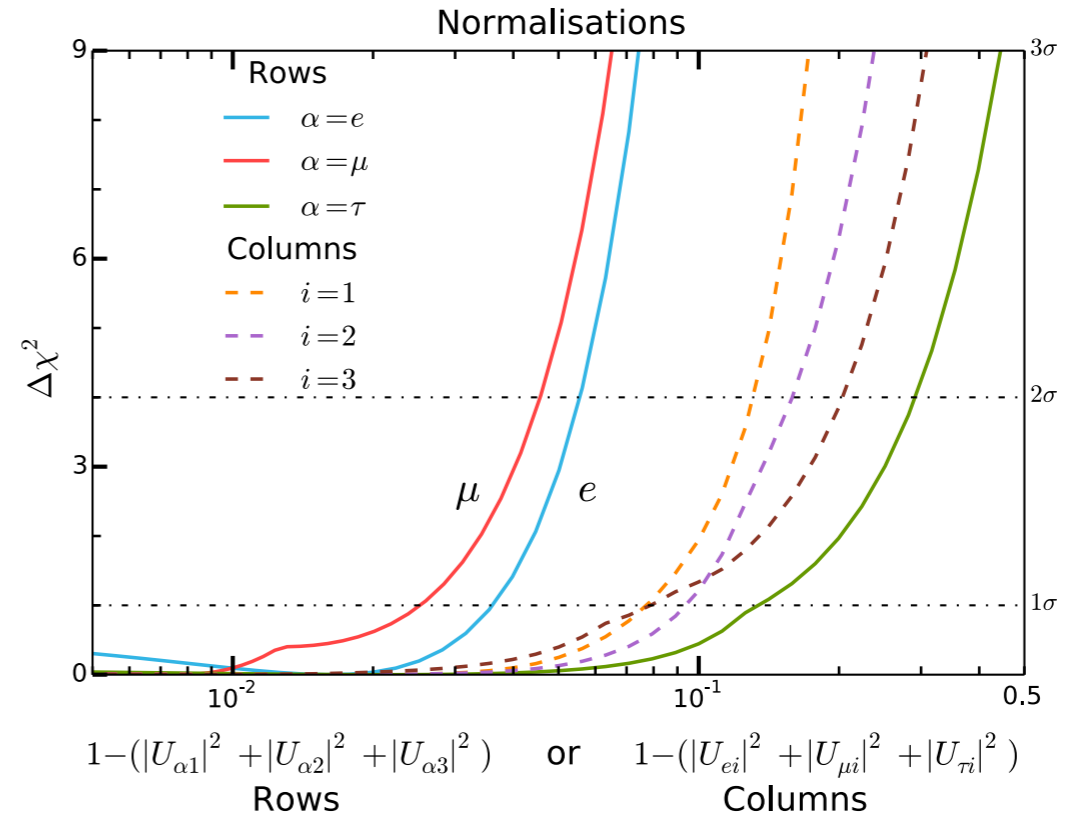
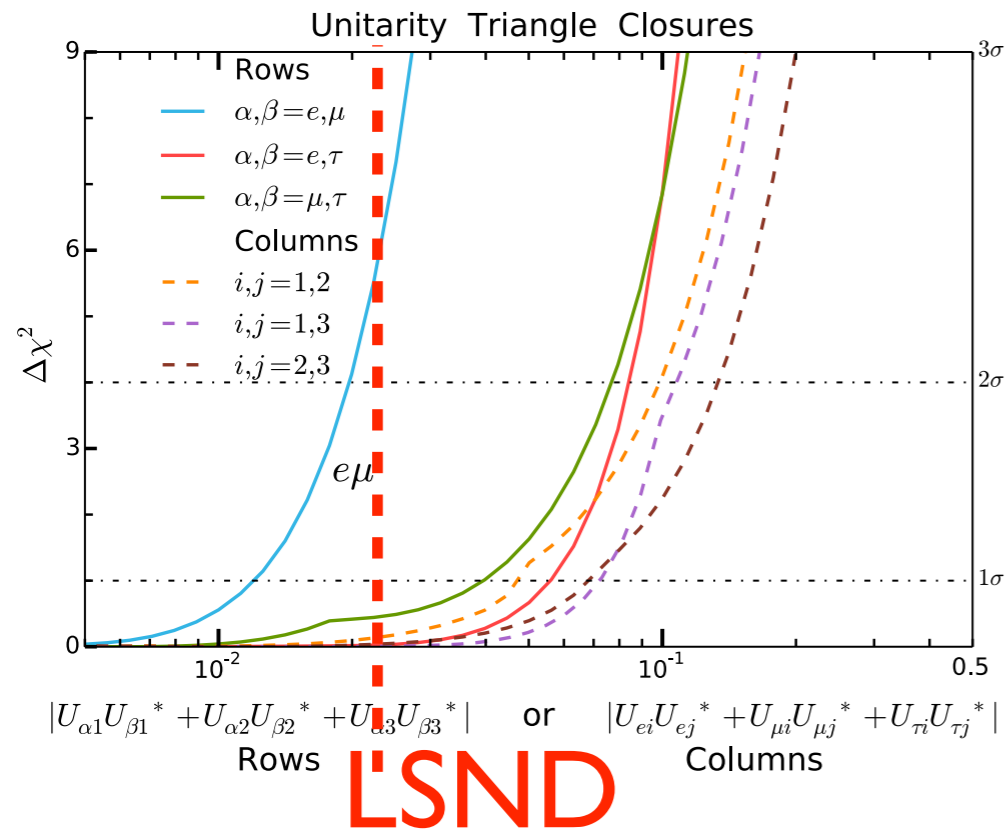


# Quark



$A\lambda^3$

Stress Test  
Neutrino paradigm  
search for new physics

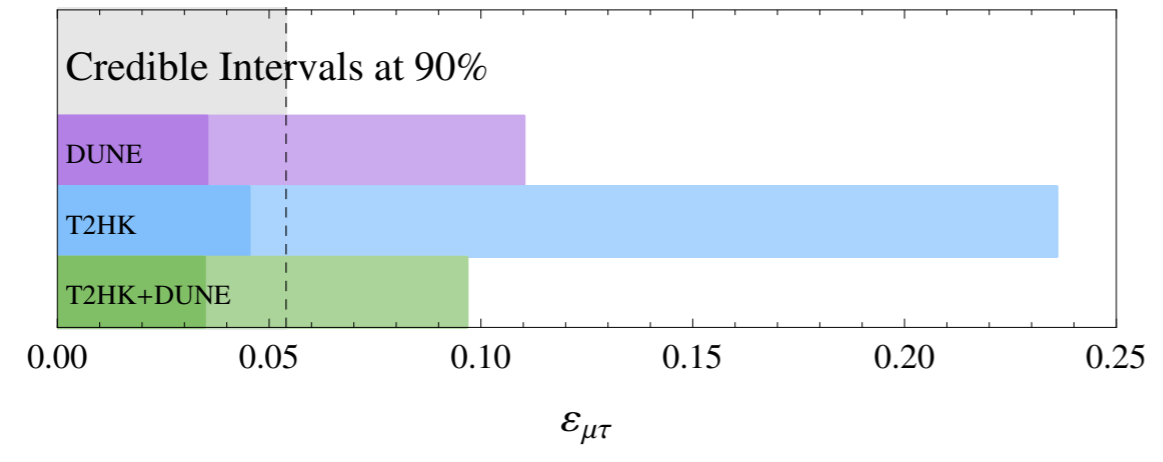
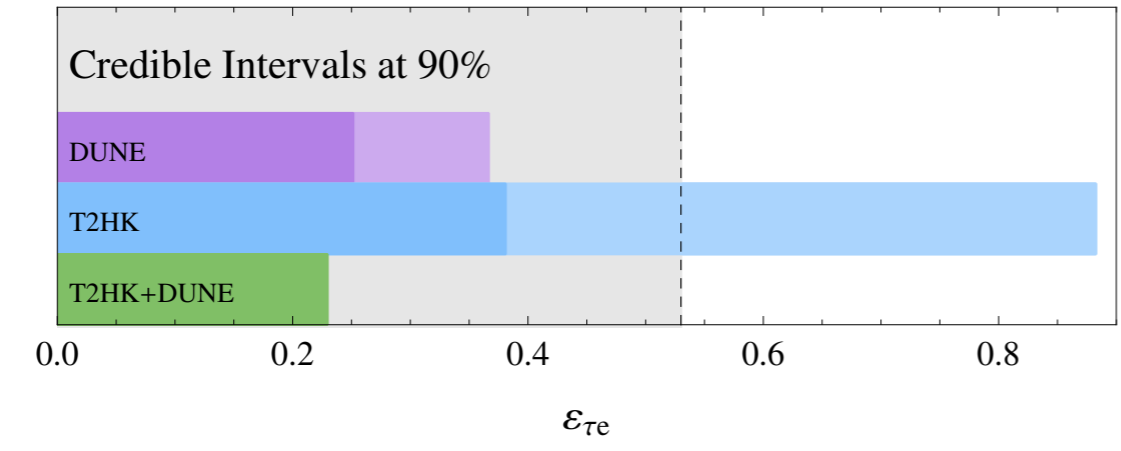
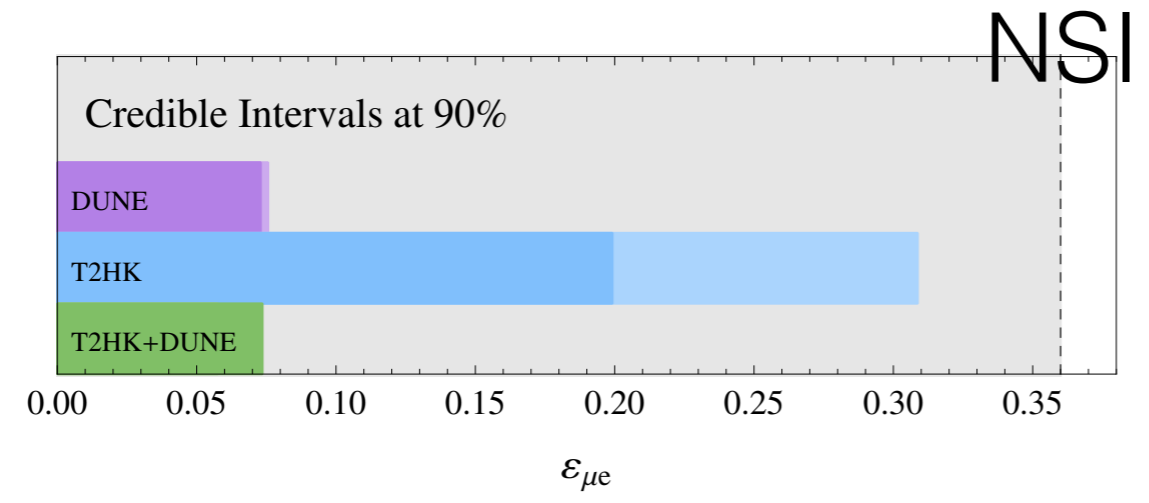


M. Ross-Lonergan + SP  
arXiv:1508.05095

9 out of 12 involve nu\_tau !!!



**Stress Test  
Neutrino paradigm  
search for new physics**



**P.Coloma  
arXiv:1511.06357**



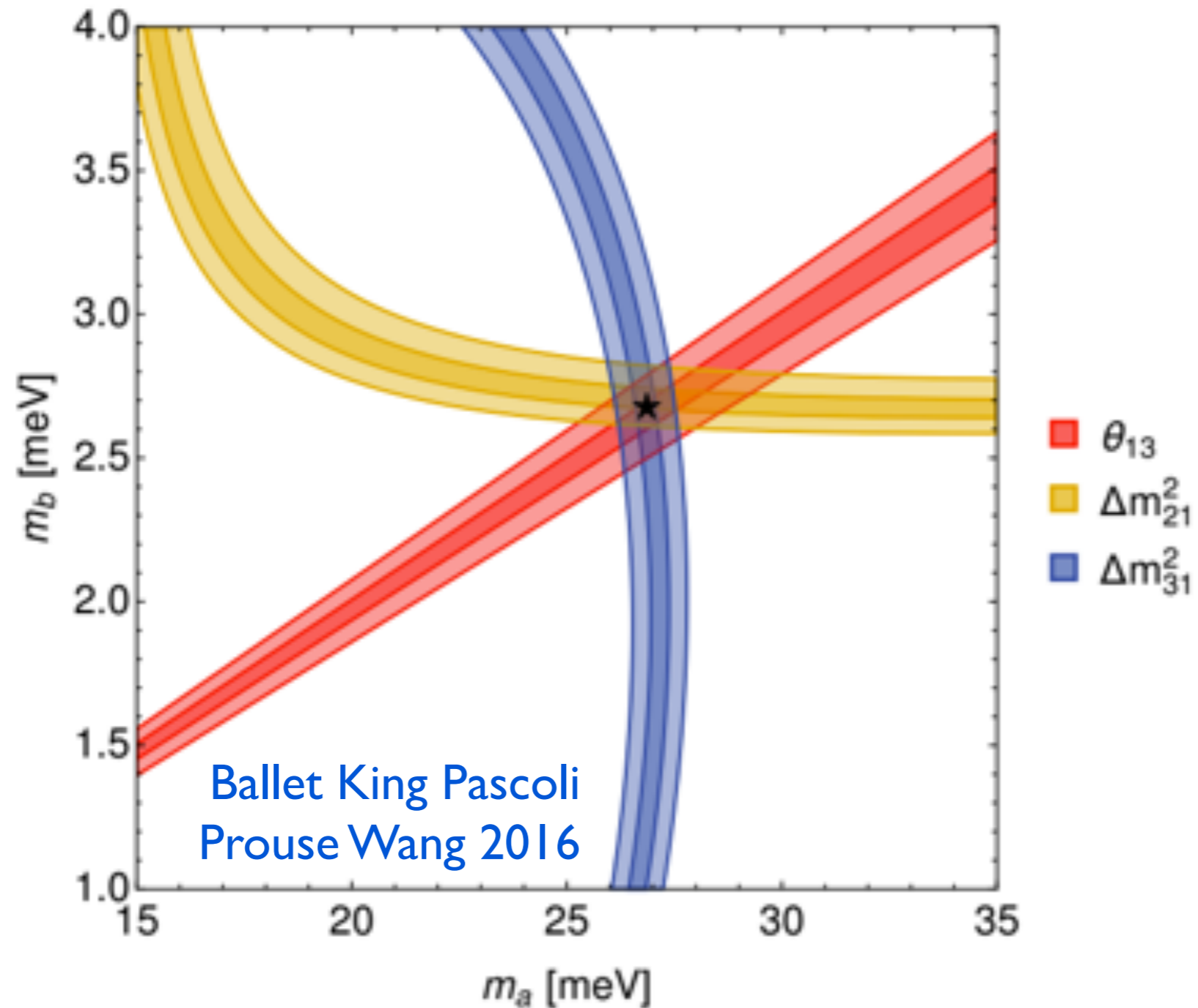
# WHY?

**Determine flavor  
fractions of neutrino  
mass states**

**Stress Test  
Neutrino paradigm  
search for new physics**

**Precision  
Neutrino  
Measurements:**

**Connection to  
Leptogenesis  
Understanding Universe**



Connection to  
Leptogenesis  
Understanding Universe



# WHY?

**Determine flavor  
fractions of neutrino  
mass states**

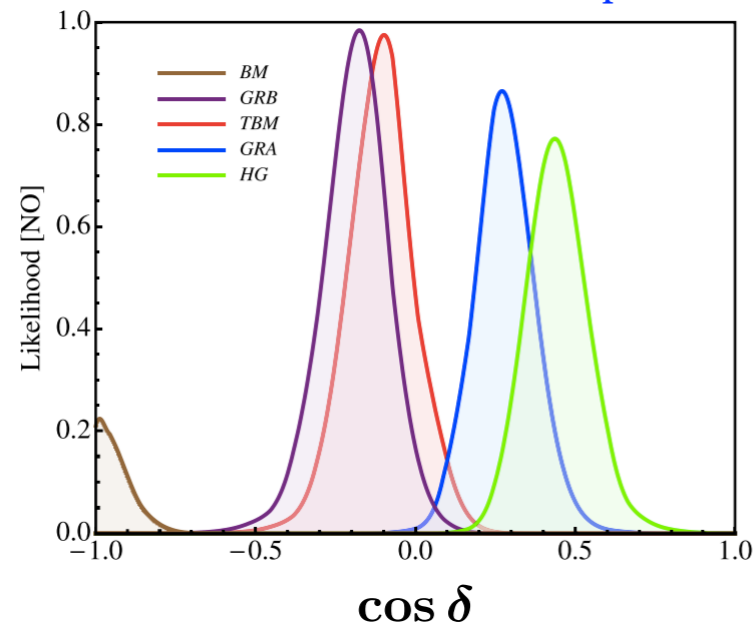
**Stress Test  
Neutrino paradigm  
search for new physics**

**Precision  
Neutrino  
Measurements:**

**Test Theoretical  
Neutrino Models**

**Connection to  
Leptogenesis  
Understanding Universe**

Predictions from flavor symmetry forms  
with current measurement precision



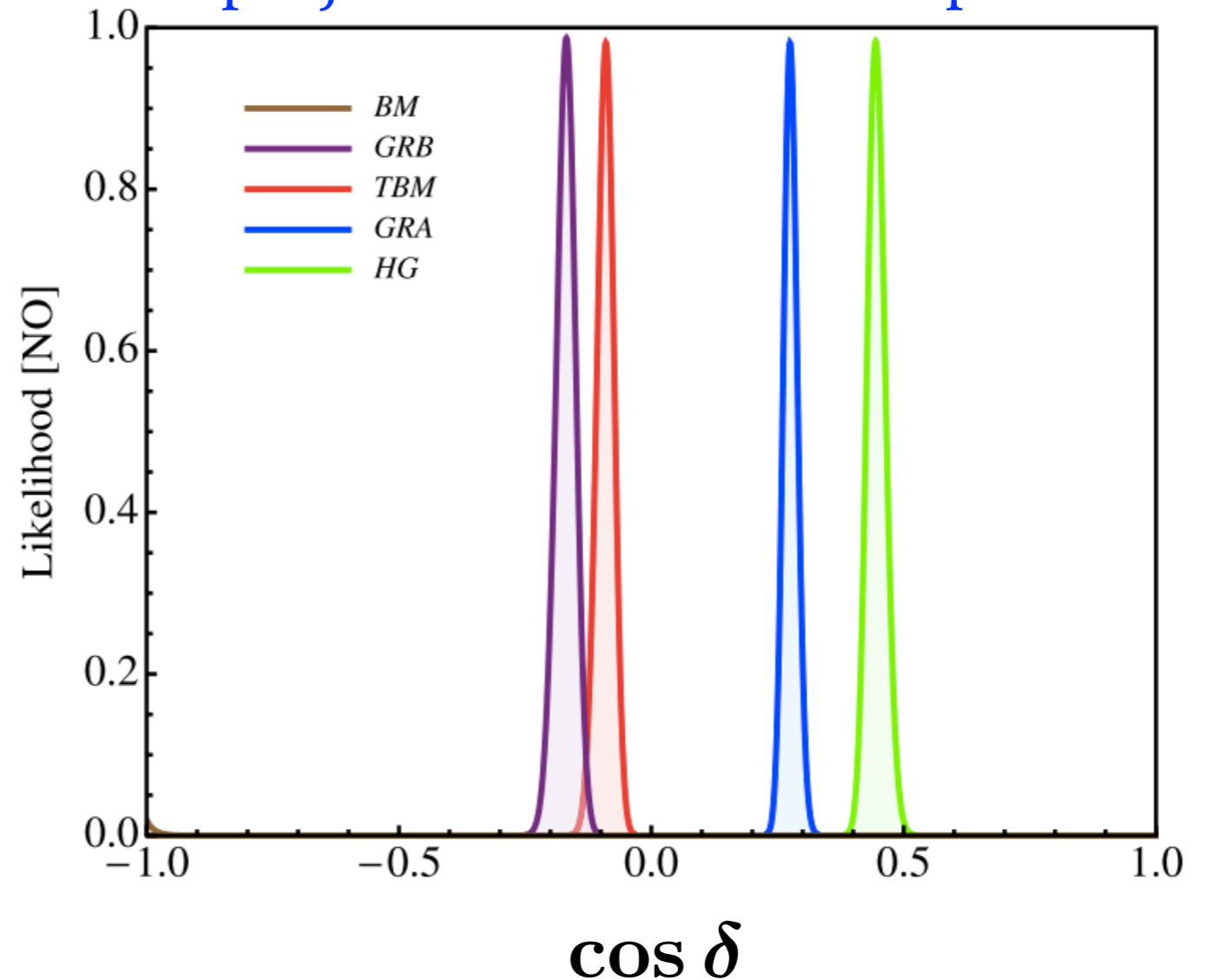
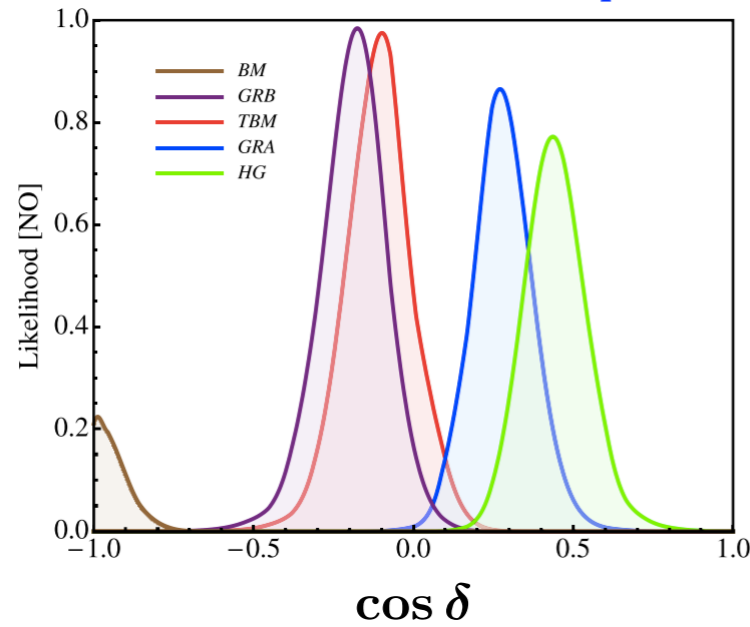
**Test Theoretical  
Neutrino Models**

Girardi, Petcov, Titov, arXiv:1410.8056  
*Nucl. Phys. B, Vol. 894, 733-768 (2015)*



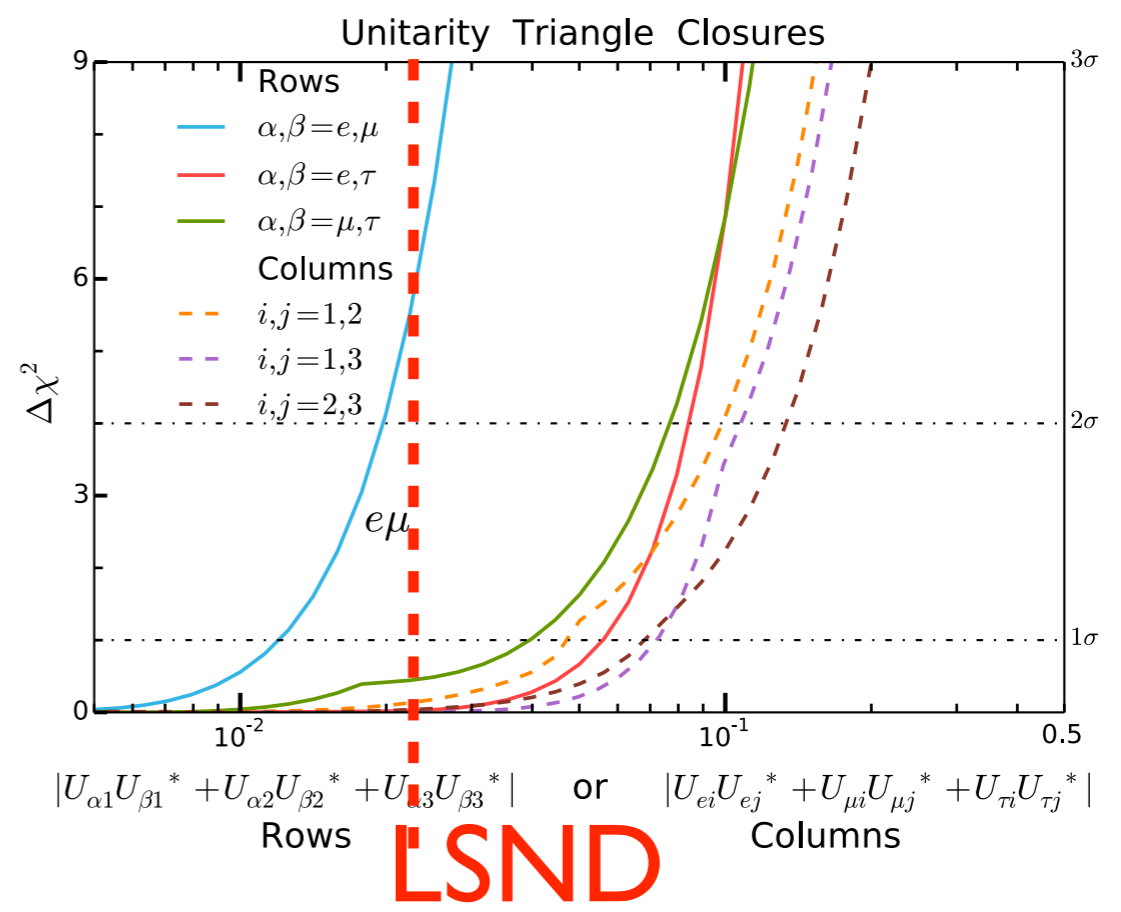
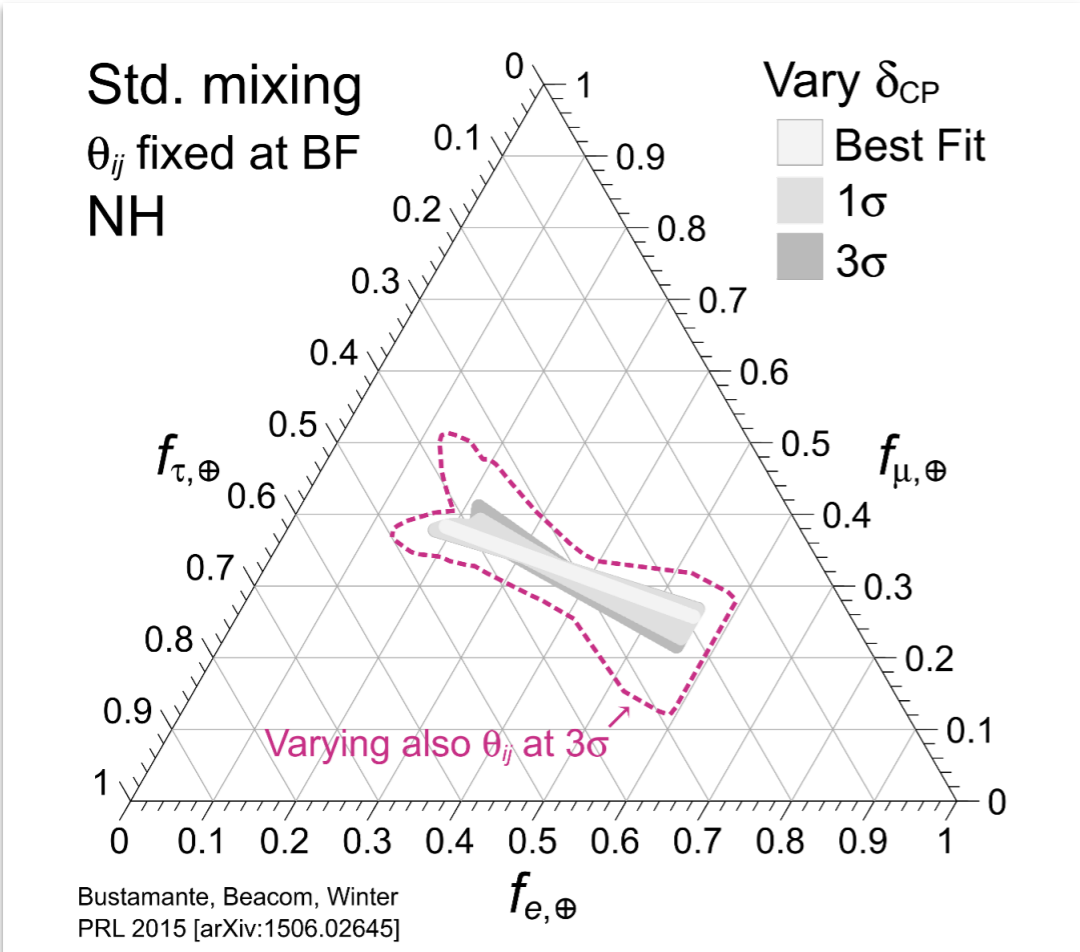
# Predictions of flavor symmetry forms with projected measurement precision

Predictions from flavor symmetry forms with current measurement precision

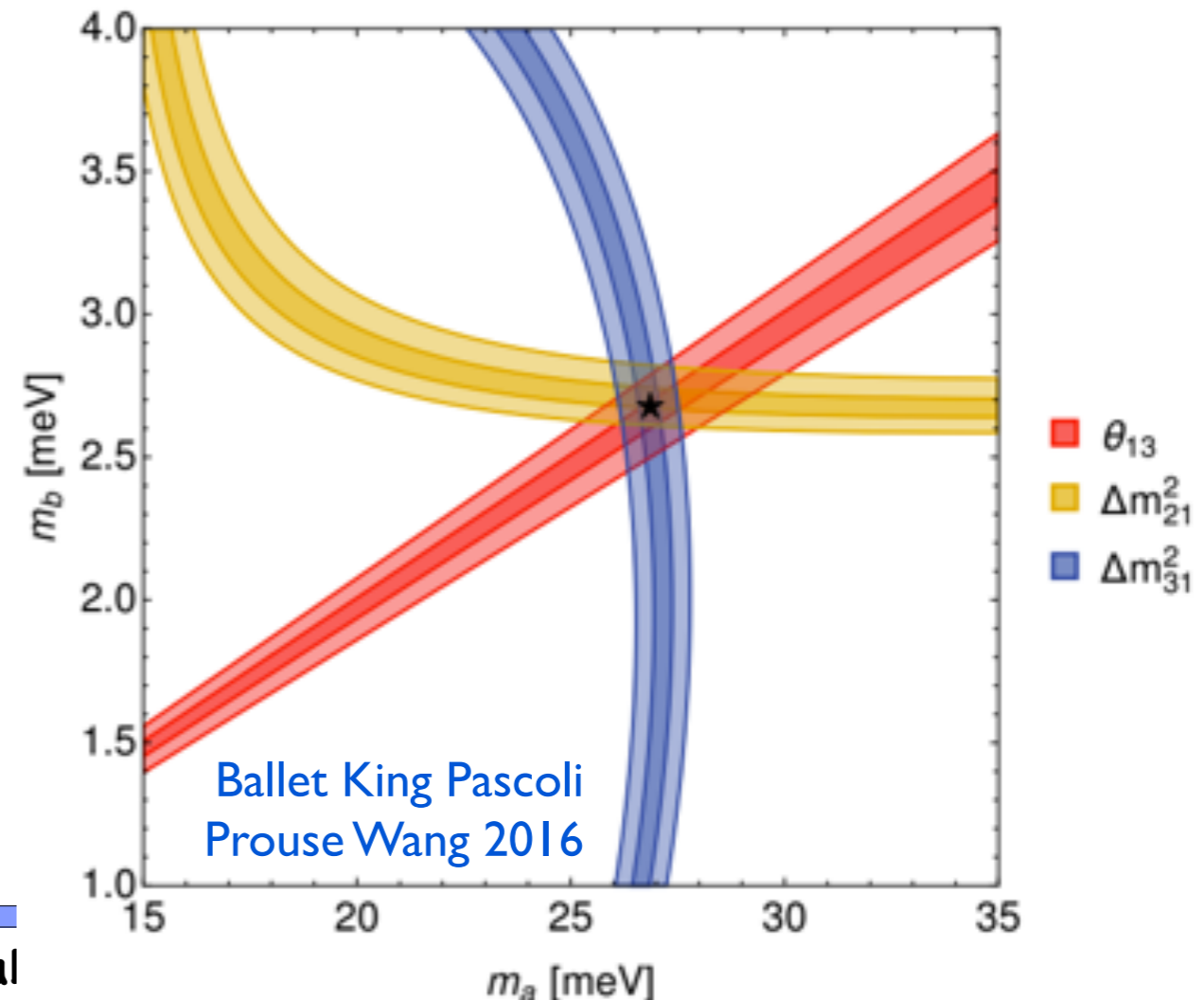
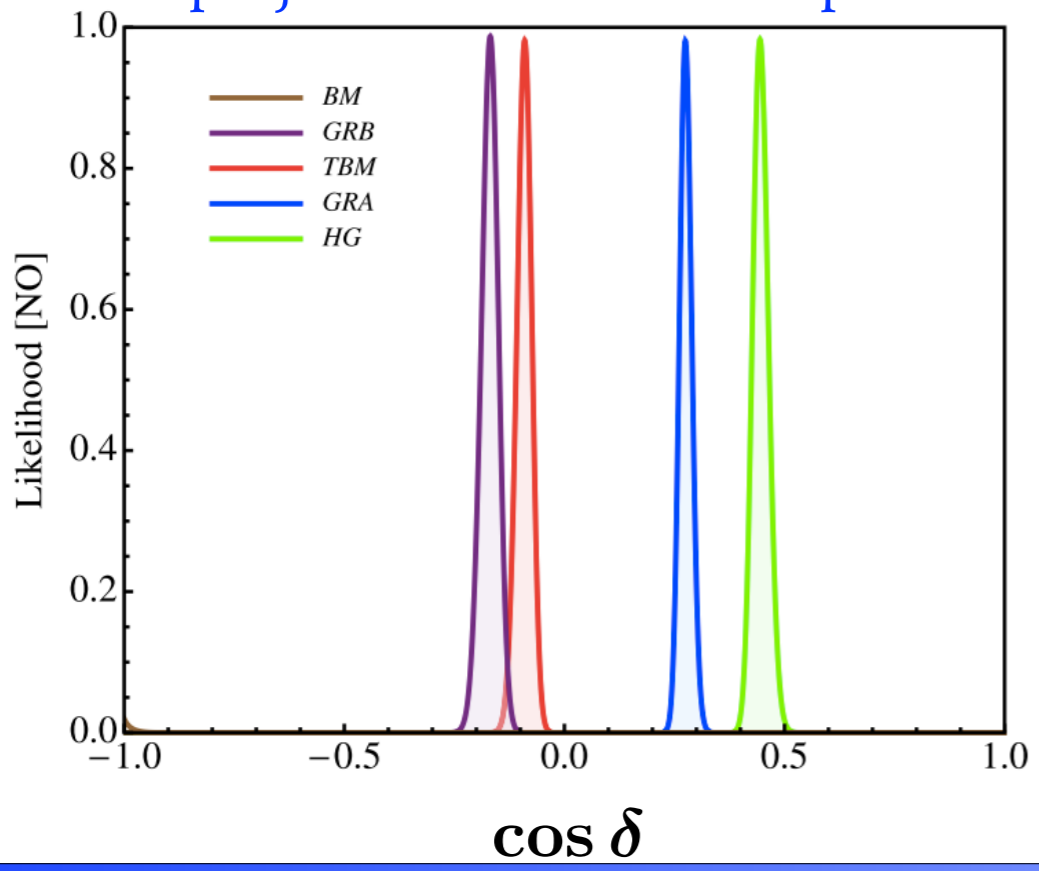


**Test Theoretical  
Neutrino Models**

Girardi, Petcov, Titov, arXiv:1410.8056  
*Nucl. Phys. B, Vol. 894, 733-768 (2015)*



Predictions of flavor symmetry forms with projected measurement precision







# ARE THERE LIGHT STERILE

$$U_{\text{PMNS}}^{\text{Extended}} = \left( \begin{array}{ccc|ccc} \overbrace{\left( \begin{array}{ccc} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{array} \right)}^{U_{\text{PMNS}}^{3 \times 3}} & \cdots & U_{en} \\ \vdots & \ddots & \vdots \\ U_{s_n1} & U_{s_n2} & U_{s_n3} & \cdots & U_{s_nn} \end{array} \right)$$



# ARE THERE LIGHT STERILE

$$U_{\text{PMNS}}^{\text{Extended}} = \begin{pmatrix} \overbrace{\begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix}}^{U_{\text{PMNS}}^{3 \times 3}} & \cdots & U_{en} \\ \vdots & \ddots & \vdots \\ U_{s_n1} & U_{s_n2} & U_{s_n3} & \cdots & U_{s_nn} \end{pmatrix}$$

Cauchy-Schwartz

$$\left| \sum_{i=1}^3 U_{ei} U_{\mu i}^* \right|^2 \leq \left( 1 - \sum_{i=1}^3 |U_{ei}|^2 \right) \left( 1 - \sum_{i=1}^3 |U_{\mu i}|^2 \right)$$

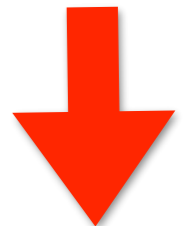


# ARE THERE LIGHT STERILE

$$U_{\text{PMNS}}^{\text{Extended}} = \begin{pmatrix} \overbrace{\begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix}}^{U_{\text{PMNS}}^{3 \times 3}} & \cdots & U_{en} \\ \vdots & \ddots & \vdots \\ U_{s_n1} & U_{s_n2} & U_{s_n3} & \cdots & U_{s_nn} \end{pmatrix}$$

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- $\nu_{\mu}$  Disappearance

- $\nu_{\mu}$  Disappearance

MINOS+, NOvA, T2K, atmospheric neutrinos (SK and ICECUBE)



# ARE THERE LIGHT STERILE

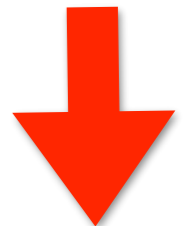
$$U_{\text{PMNS}}^{\text{Extended}} = \begin{pmatrix} \overbrace{\begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix}}^{U_{\text{PMNS}}^{3 \times 3}} & \cdots & \begin{pmatrix} U_{en} \\ U_{\mu n} \\ U_{\tau n} \\ \vdots \\ U_{s_n n} \end{pmatrix} \end{pmatrix}$$

## Cauchy-Schwartz

$$\left| \sum_{i=1}^3 U_{ei} U_{\mu i}^* \right|^2 \leq \left( 1 - \sum_{i=1}^3 |U_{ei}|^2 \right) \left( 1 - \sum_{i=1}^3 |U_{\mu i}|^2 \right)$$



•  $\nu_e$  Disappearance



•  $\nu_\mu$  Disappearance

•  $\nu_\mu$  Disappearance

MINOS+, NOvA, T2K, atmospheric neutrinos (SK and ICECUBE)

•  $\nu_e$  Disappearance

Daya Bay, RENO, many  $\sim 10\text{m}$  Reactor experiments & source experiments.



# ARE THERE LIGHT STERILE

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•  $\nu_{\mu} \rightarrow \nu_e$  Appearance

•  $\nu_e$  Disappearance

•  $\nu_{\mu}$  Disappearance

•  $\nu_{\mu}$  Disappearance

MINOS+, NOvA, T2K, atmospheric neutrinos (SK and ICECUBE)

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Daya Bay, RENO, many  $\sim 10\text{m}$  Reactor experiments & source experiments.

•  $\nu_{\mu} \rightarrow \nu_e$  Appearance

Fermilab SBN Program, T2K and NOvA: DUNE & HyperK

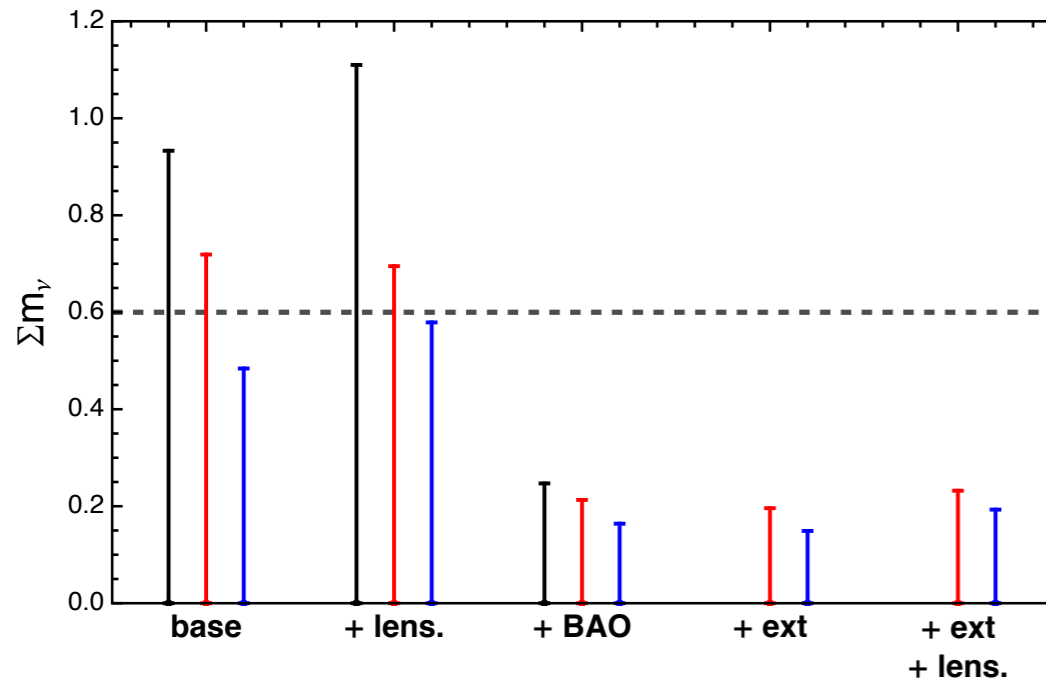


CP violation ???

What about  $\text{Nu}_\tau$  ???



# Cosmology & Neutrinos



**Figure 1.** Comparison between constraints on  $\sum m_\nu$  from *Planck* 2013 (black) and *Planck* 2015 without (red) and with (blue) small-scale polarization. The baseline always includes the full TT spectrum and the low-ell polarization (taken from WMAP in 2013). The dashed line represents KATRIN sensitivity to the effective electron neutrino mass, translated in terms of  $\sum m_\nu$ .

$$N_{\text{eff}} = 3.13 \pm 0.32 \quad \textit{PlanckTT} + \text{lowP}, \quad (1a)$$

$$N_{\text{eff}} = 3.15 \pm 0.23 \quad \textit{PlanckTT} + \text{lowP} + \text{BAO}, \quad (1b)$$

$$N_{\text{eff}} = 2.99 \pm 0.20 \quad \textit{PlanckTT, TE, EE} + \text{lowP}, \quad (1c)$$

$$N_{\text{eff}} = 3.04 \pm 0.18 \quad \textit{PlanckTT, TE, EE} + \text{lowP} + \text{BAO}. \quad (1d)$$

*Planck* is consistent with the standard value of  $N_{\text{eff}}$ , and excludes  $N_{\text{eff}} = 4$  (*i.e.*, a fully-thermalized fourth neutrino state) at a level between  $2.7$  and  $5.3\sigma$ ; however, sizeable amounts

# Reactor:



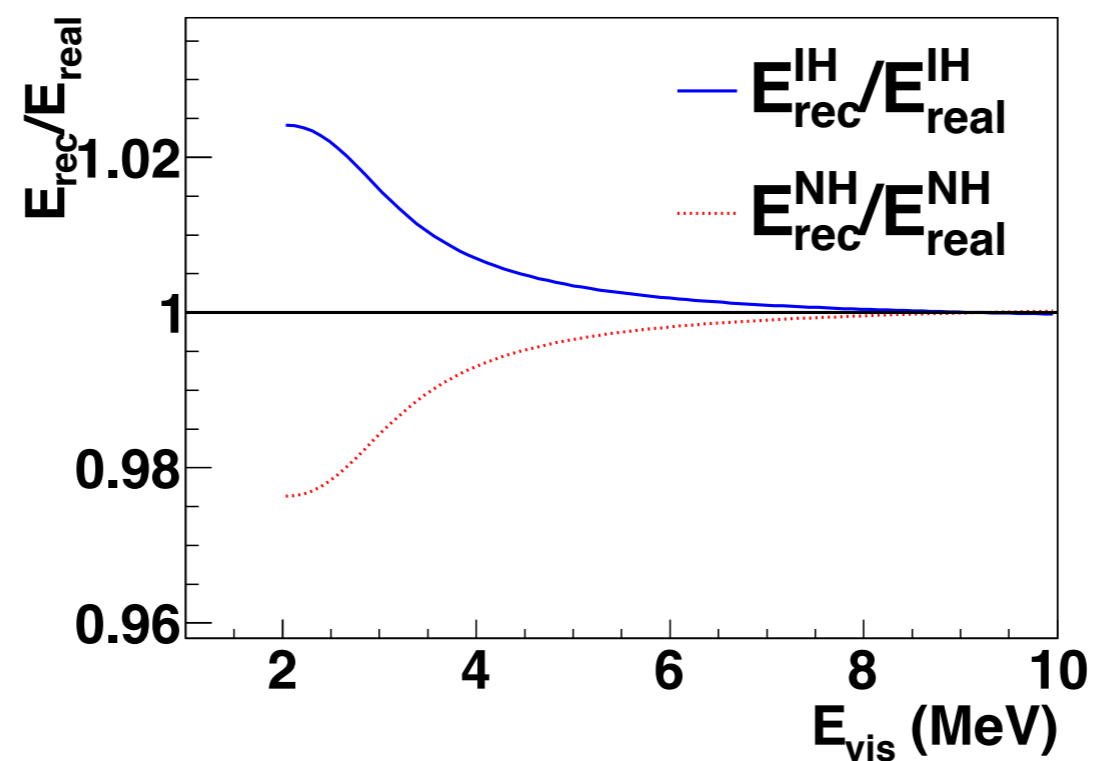
	Nominal	+ B2B (1%)	+ BG	+ EL (1%)	+ NL (1%)
$\sin^2 \theta_{12}$	0.54%	0.60%	0.62%	0.64%	0.67%
$\Delta m_{21}^2$	0.24%	0.27%	0.29%	0.44%	0.59%
$ \Delta m_{ee}^2 $	0.27%	0.31%	0.31%	0.35%	0.44%



# Reactor:

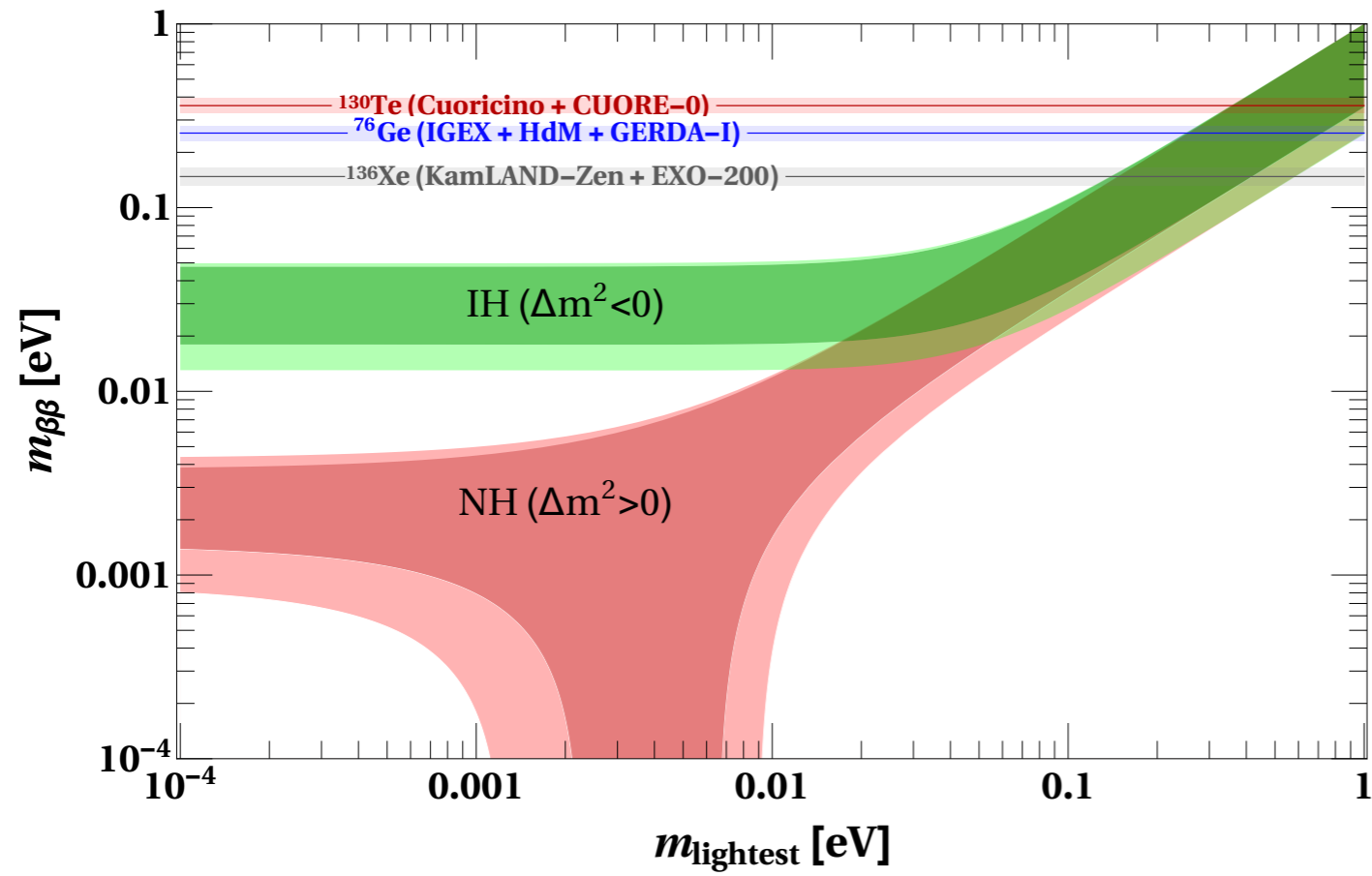


	Nominal	+ B2B (1%)	+ BG	+ EL (1%)	+ NL (1%)
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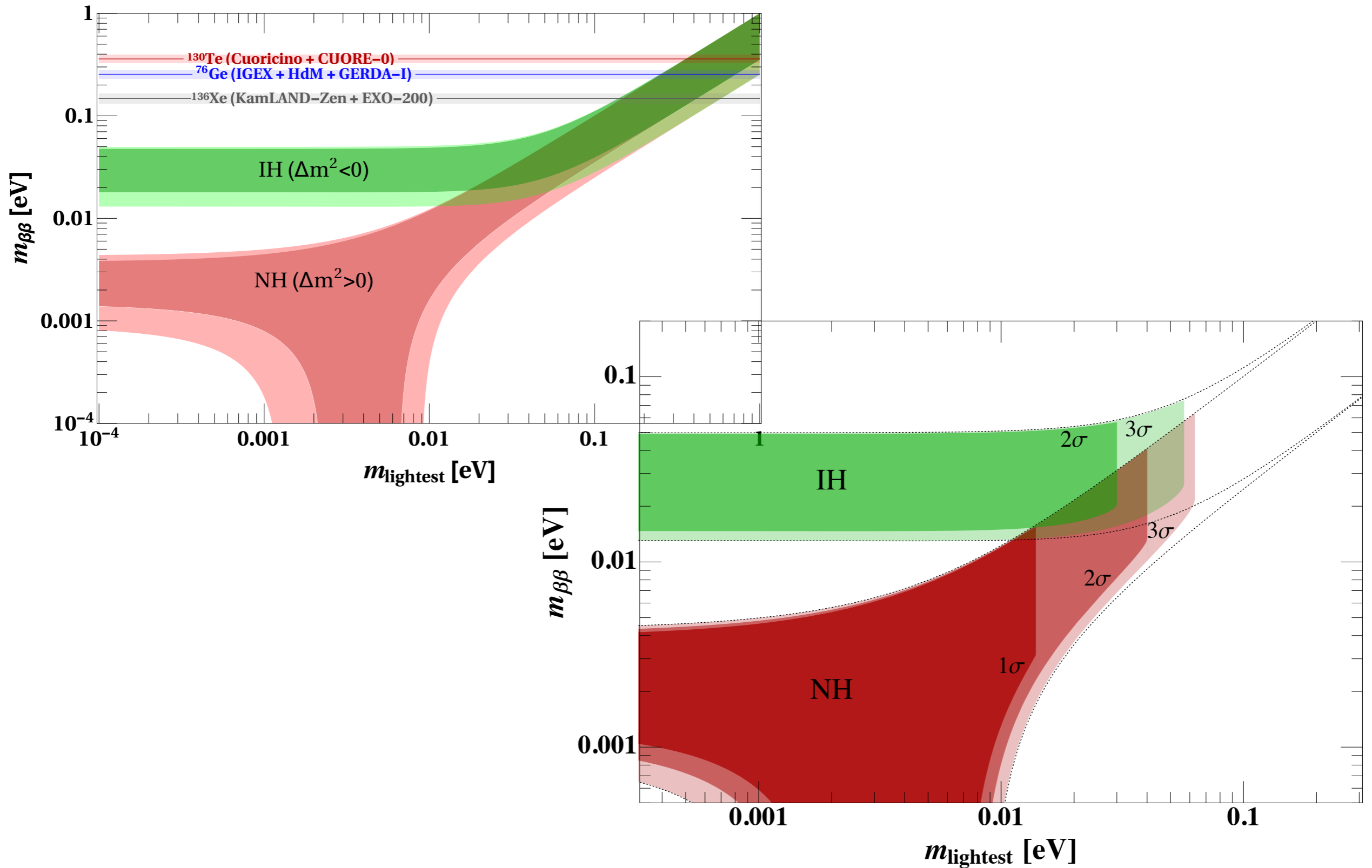


# Neutrinoless Double Beta decay





# Neutrinoless Double Beta decay





# QCD & Nuclear Physics:

- Reactor Flux and Spectrum
- Matrix elements for neutrinoless double beta decay
- Cross Sections for neutrino nucleon AND nucleus scattering
- .....



# Recent highlights from neutrino theory

Pedro A. N. Machado

Fermilab *soon to be at LBNL as junior staff member*

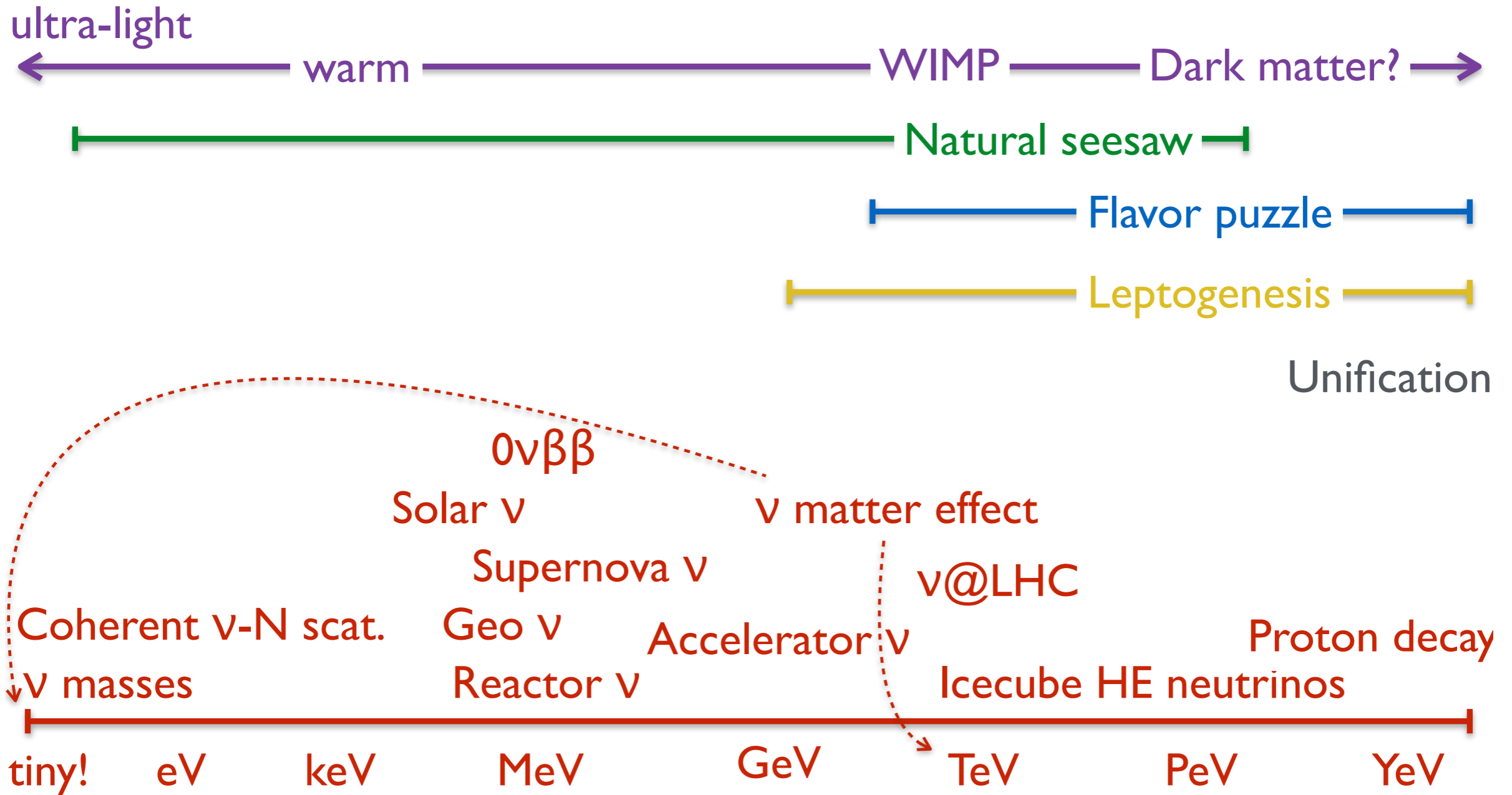


Aug/2017

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# Neutrinos as a portal to new Physics





# Many many many other fronts!

Neutrino cross sections  
(NuSTEC effort)



Neutrinos in cosmology  
Early universe - BBN

Abazajian, Barbieri, Cirelli, Chizov, Di Bari, Dodelson, Dolgov, Foot, Holanda, Iocco, Kirilova, Kusenko, Mangano, Lesgourges, Pastor, Smirnov, Steigman, Volkas

Secret neutrino interactions

Dasgupta Kopp 2013, Chu Dasgupta Kopp 2015, Lundkvist Archidiacono Hannestad Tram 2016, Ghalsasi McKeen Nelson 2016, Archidiacono Gariazzo Giunti Hannestad Hansen Laveder Tram 2016, Forastieri Lattanzi Mangano Mirizzi Natoli Saviano 2017

Supernova evolution: non-linear effects from collective oscillations



Friedland 2010, Cherry Carlson Friedland Fuller Vlaesenko 2012, Chakraborty Hansen Izaguirre Raffelt 2016, Capozzi Basudeb Dasgupta 2016, Izaguirre Raffelt Tamborra 2016, Capozzi Dasgupta Lisi Marrone Mirizzi 2017

Chen Ratz Trautner 2015

Cosmic neutrino background: ideas to measure it?  
Non-thermal component?

Type II, type III and radiative seesaw

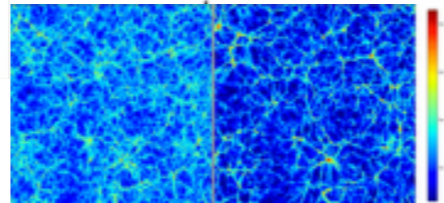
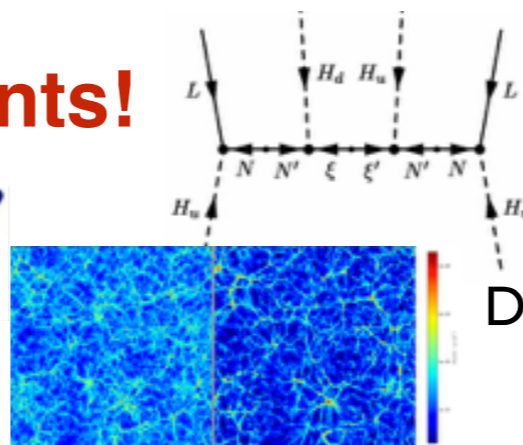
Akhmedov, Bonnet, Babu, Barbieri, Barger, Berezhiani, Ellis, Gaillard, Glashow, Hirsch, Keung, Ma, Mohapatra, Ota, Pakvasa, Schechter, Senjanovic, Valle, Yanagida, Winter, Wolfenstein, Zee, and many others

Flat extra dimensions: light sterile neutrinos

Antoniadis, Arkani-Hamed, Barbieri, Berryman, Davoudiasl, Dimopoulos, Dvali, de Gouvea, Langacker, Machado, Mohapatra, Nandi, Nunokawa, Perelstein, Peres, Perez-Lorenzana, Smirnov, Strumia, Tabrizi, Zukanovich-Funchal, ...

Leptogenesis

Barenboim, Davidson, Di Bari, Dolgov, Fukugita, Kuzmin, Rubakov, Servant, Shaposhnikov, Yanagida, Zeldovich, ...



Sterile neutrino in long baseline oscillation experiments

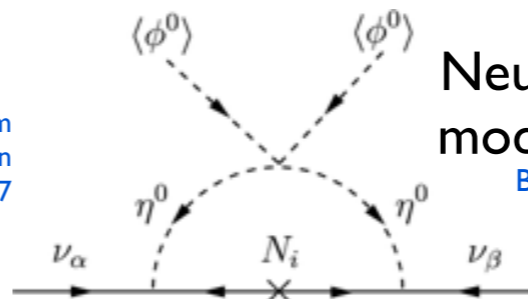
Agarwalla, Bhattacharya, Chatterjee, Dasgupta, Dighe, Donini, Fuki, Klop, Lopez-Pavon, Meloni, Migliozzi, Palazzo, Ray, Tang, Terranova, Thalappilil, Wagner, Yasuda, Winter, ...

Dark matter in neutrino detectors: light DM and light mediators

Ballett, Batell, Chen, Coloma, deNiverville, Dobrescu, Frugieue, Harnik, McKeen, Pascoli, Pospelov, Ritz, Ross-Lonergan

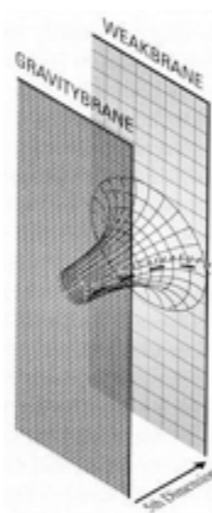
Neutrinos and the standard solar model: CNO cycle and metallicity

Bailey, Busoni, Christensen-Dalsgaard, Krief, Simone, Serenelli, Scott, Vincent, Vilante, Vissani, Vynioli, ...



Neutrino magnetic moment

see e.g. Salam 1957, Barbieri Fiorentini 1988, Barbieri Mohapatra 1989, Babu Chang Keung Phillips 1992, Tarazona Diaz Morales Castillo 2015, Cañas Miranda Parada Tortola Valle 2015, Barranco Delepine Napsuciale Yebra 2017, Coloma Machado Martinez-Soler Shoemaker 2017



Discrete symmetries with non-zero  $\theta_{13}$

Feruglio Hagedorn Toroop 2011, Lam 2012, Lam 2013, Holthausen Lim Lindner 2012, Neder King Stuart 2013, Hagedorn Meroni Vitale 2013, King Neder 2014, Ishimori King Okada Tanimoto 2014, Yao Ding 2015, ...

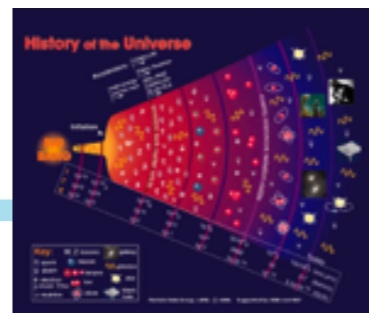
Effective operator approach to neutrino masses and collider/low scale pheno

de Gouvea Jenkins 2007, Boucenna Morisi Valle 2014, Nath Syed 2015, Geng Tsai Wang 2015, Chiang Huo 2015, Bhattacharya Wudka 2015, Geng Huang 2016, Quintero 2016, Mohapatra 2016, Kobach 2016

New physics in neutrinoless double beta decay, lepton number violation at the LHC, left-right models, RS models and neutrino masses, neutrinos as dark matter, and much more!



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# Circa 2025+



- from Nu1998 to now, tremendous exp. progress on Neutrino SM: more at Nu2018 and much more before 2025 ! -  $\nu_3$  mass ordering and dominant flavor, size CP violation phase.
- Unitarity ? 12 constraints, only 3 will be tested with reasonable precision !!! All with  $\nu$ -tau poorly constrained except thru Cauchy-Schwartz.
- LSND Sterile Nu's neither confirmed or ruled out at acceptable CL: - CP violation ? and role of  $\nu$ \_tau ?
- Neutrinoless Double beta decay will be probing below 10 scale.



# Circa 2025+



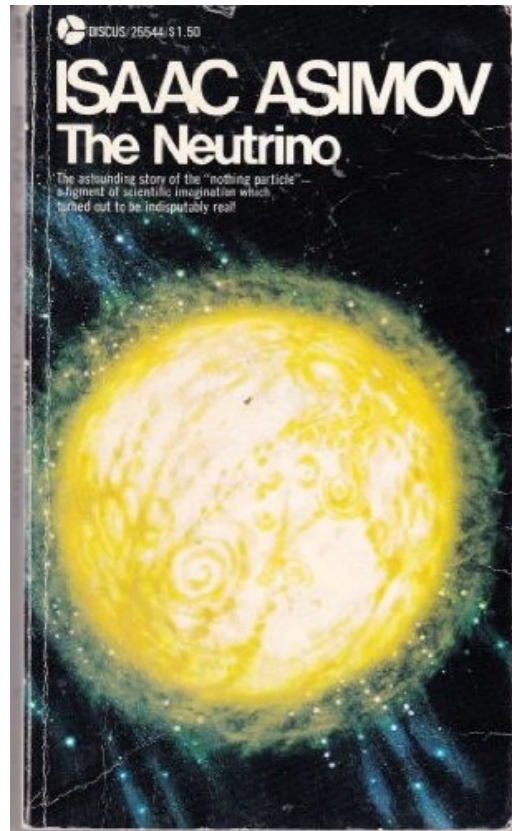
- Great Theoretical progress on understand many aspects of Quantum Neutrino Physics: – Oscillations, Decoherence, Osc. Probabilities in Matter, Leptogenesis, ....
- Convincing model of Neutrino masses and mixings: with testable and confirmed predictions !
- Connections to other sectors

# Circa 2025+



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- Convincing model of Neutrino masses and mixings: with testable and confirmed predictions !
- Connections to other sectors

● Surprises !!!



***“And yet the nothing-particle  
is not a nothing at all.”***

***– Isaac Asimov 1966***