

# Muon Anomalies and Their Future Investigations

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Fermilab

Muon Department Journal Club

Jason Bono, Fermilab

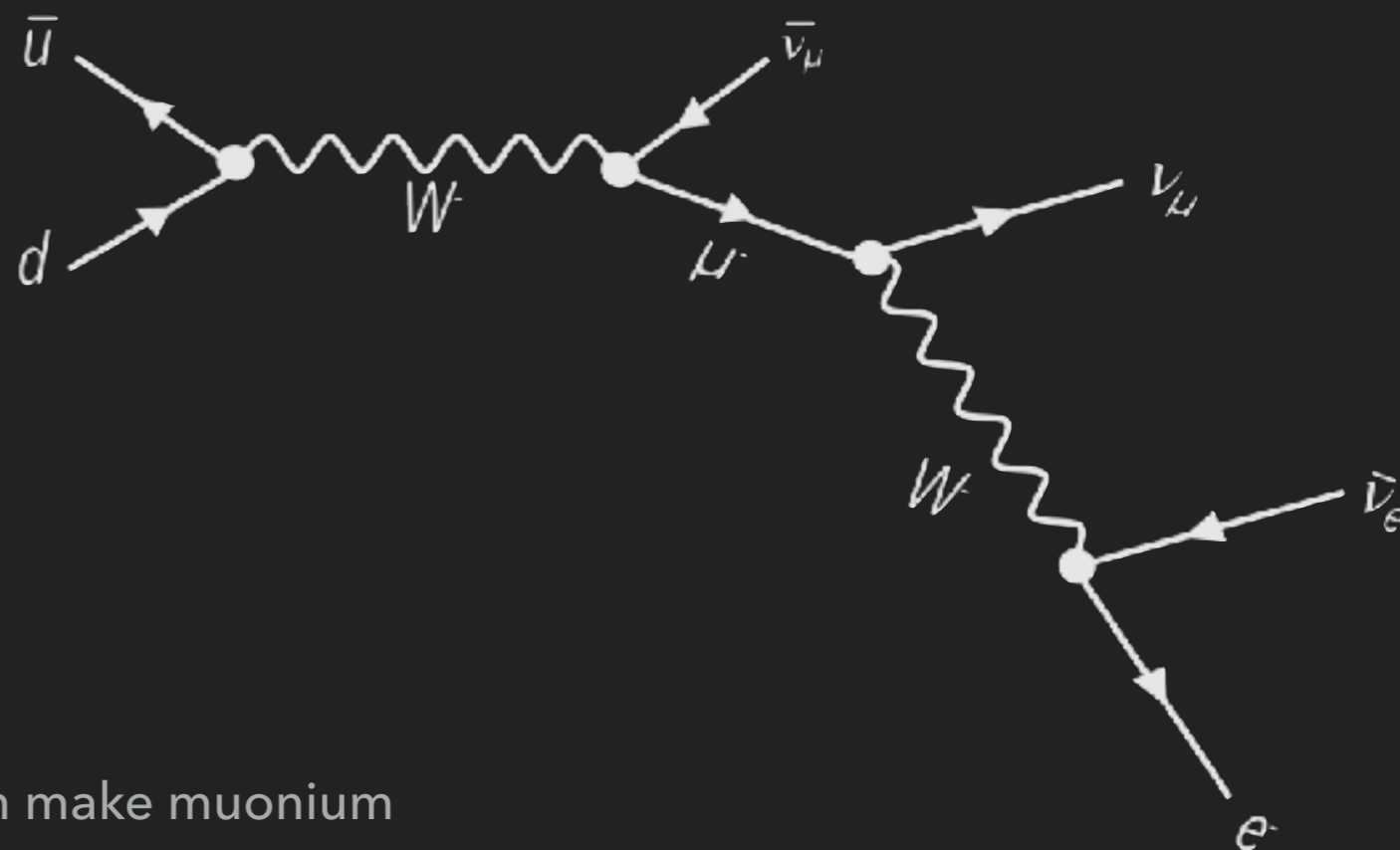
April 9, 2018

# Muons

- A few nice properties
- A historical perspective
- Anomalies and Future Investigations
  - ▶ The Proton Radius Puzzle
  - ▶ The Muon anomalous magnetic moment
  - ▶ Hints of Lepton Flavor Non-Universality in B decays
  - ▶ Searches for Charged Lepton Flavor Violation
  - ▶ Extra: Muons and The Great Pyramid of Giza

## Why We Like Muons

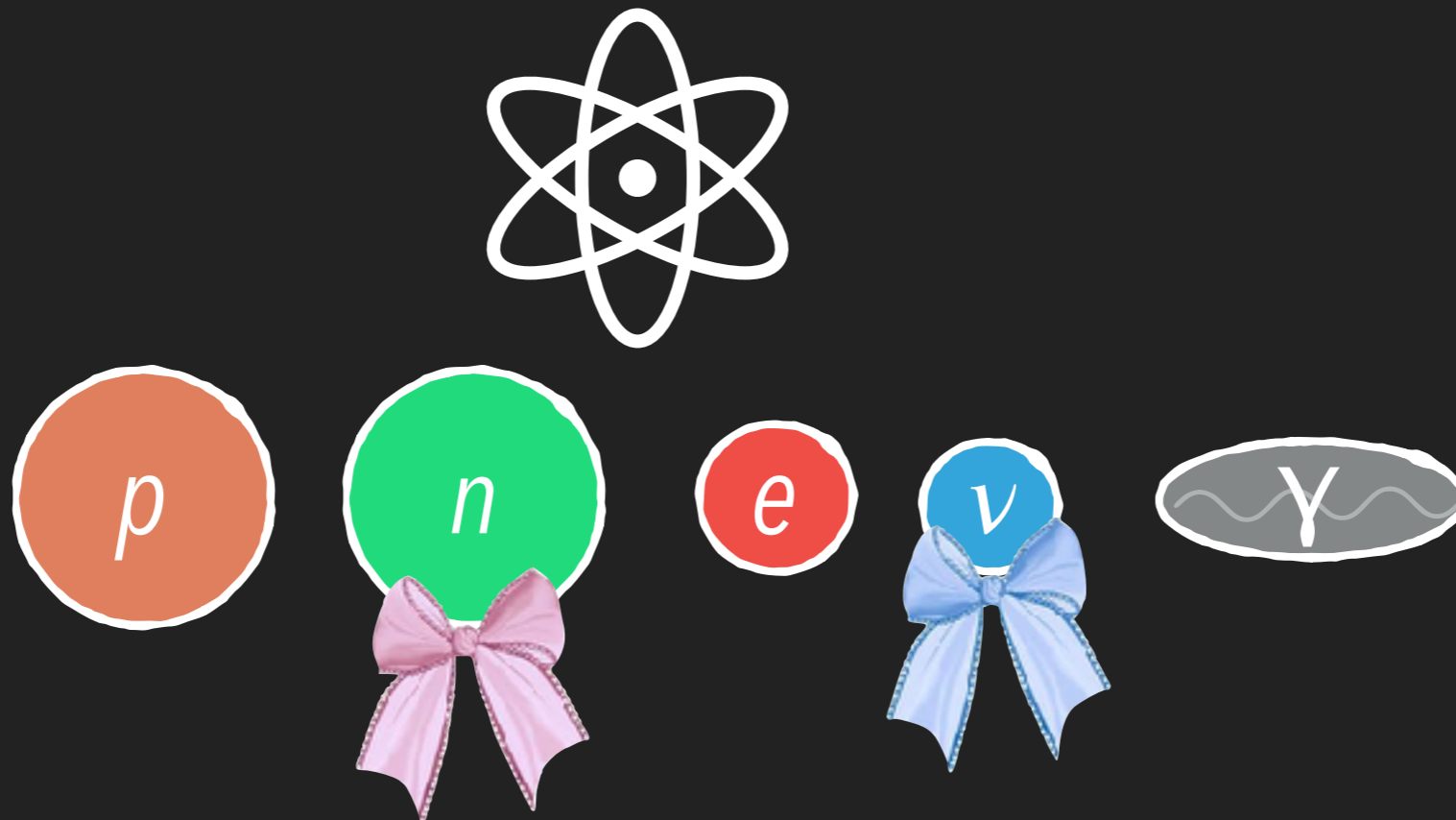
- They're easy to produce
  - ▶ Natural product of pion's weak decay
    - Helicity suppression of electrons
  - ▶ Come out 100% polarized
- They're charged
  - ▶ Can be contained with EM fields
  - ▶ Can be detected directly
  - ▶ Can  $\mu^-$  can make muonic atoms, and  $\mu^+$  can make muonium
- They're much heavier than the electron, but lighter than the pion
  - ▶ Access to virtual effects on high mass scales
  - ▶ No hadronic decay
  - ▶ Lifetime of 2.2  $\mu\text{s}$ : Long enough to study interaction, short enough to study decay
  - ▶ Penetrating: most abundant charged cosmic ray at sea level ( $\sim 10\text{K/s}\cdot\text{m}^2$ )
- They don't participate in the strong interaction
  - ▶ Interactions subject to precise theoretical predictions
  - ▶ Decay is "self analyzing" and contains an easily detectable electron



Muons offer a unique combination of theoretical "Cleanness," experimental sensitivity, and New Physics reach

# Nuclear Physics from 1930–1934

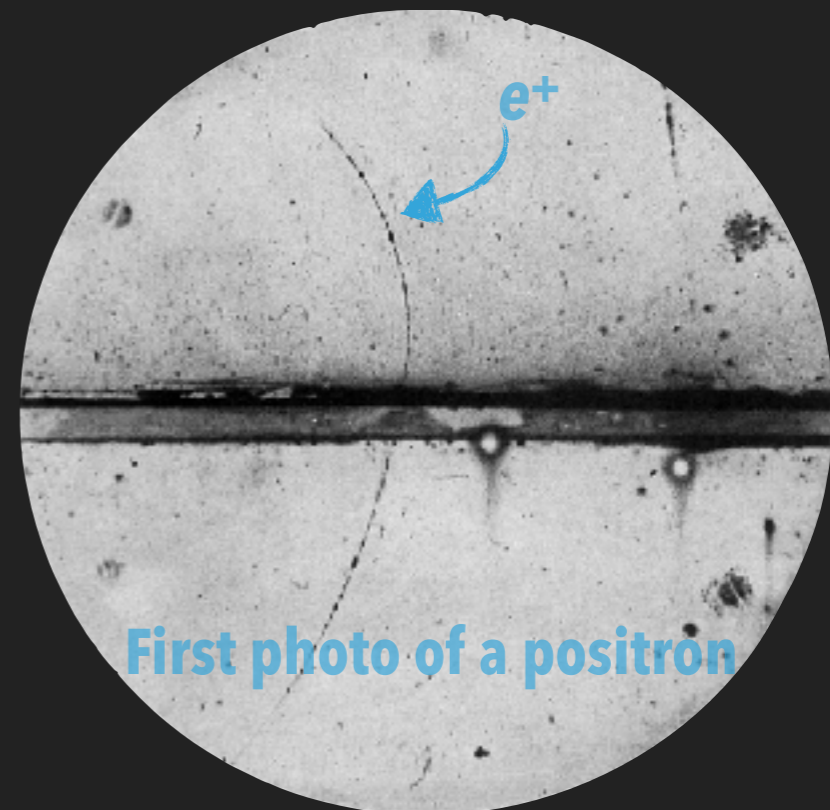
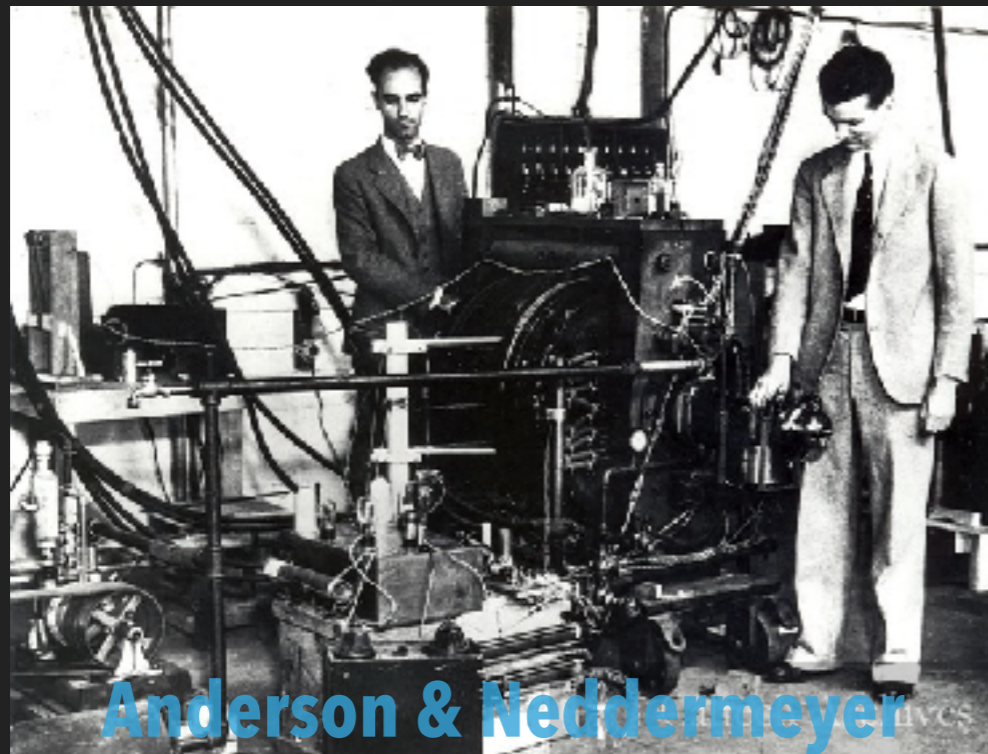
- Two new particles arrive on the scene!
  - ▶ A low/no mass neutrino is invoked by Pauli
    - to save the fundamental conservation laws in  $\beta$ -decay
  - ▶ The neutron is discovered
    - The proton-neutron model of nucleus arrives
    - Fermi proposed that nuclear  $\beta$ -decay is a result of  $n \rightarrow p e \nu$





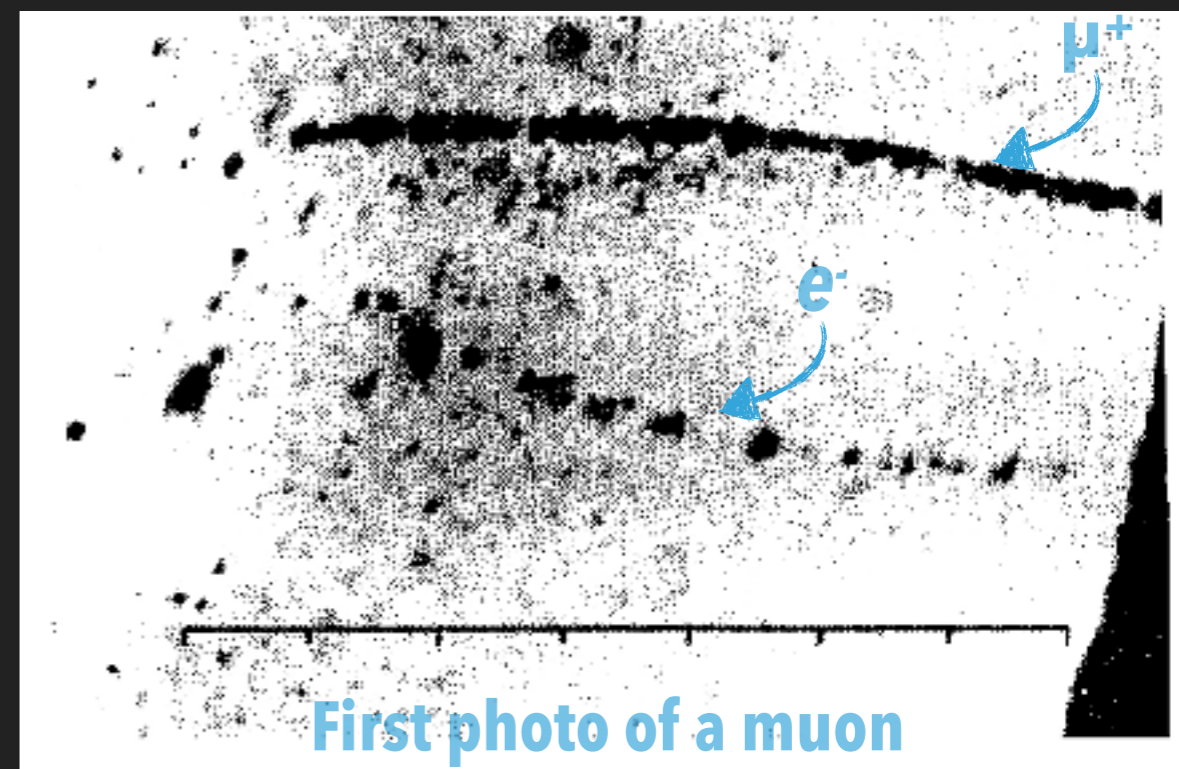
## More Success

- 1931: Dirac predicts the positron
  - ▶ A hole in the infinite sea of negative energy electrons
- 1932: Anderson and Neddermeyer discover the positron in cosmic rays
  - ▶ Using a cloud chamber in a strong magnetic field
  - ▶ Totally unaware of Dirac's prediction!



## A Particle “of uncertain nature” Appears

- 1933: Kunze publishes the first observation of a muon
  - ▶ “The nature of this particle is unknown; for a proton, it does not ionize enough, and for a positive electron, the ionization is too strong”



Next, cosmic rays get more interesting...

## The Mu-Meson

- 1934: To explain the cohesion of the nucleus, Yukawa predicts a “meson”
  - ▶ Conserved force carriers gives long distance forces;  $F(r) \sim 1/r^2$
  - ▶ Let the force carriers decay!  $N(r) = N_0 \exp(-(\alpha/v)r) \rightarrow F(r) \sim \exp(-\lambda r)/r^2$
  - ▶ Expect the meson to have  $m \sim 200 \cdot m_e$
- 1935: J.C. Street narrows in on Kunze’s bizarre particle
  - ▶ Identifies individual, highly penetrating, charged particles, at sea level
  - ▶ Are these electrons that somehow penetrate? “Red” and “green” electrons are spoken of
  - ▶ Or does quantum theory break down at higher energies?
- 1936: Three groups independently conclude that the penetrating particle is a new one, and of intermediate mass between the electron and proton.
  - ▶ The Caltech group published first, and are credited with the discovery of the the “mu-meson”
- 1937: Yukawa-meson = mu-meson
  - ▶ Whops... Idea not abandoned till a decade later!
    - Observed that the mu-meson doesn’t feel the nuclear force
    - Discovered the pi-meson: observed  $\pi \rightarrow \mu \nu$

A decade passes...



## A Heavy Electron?



Image by Roni Harnik

- When it became clear that the pion and muon were distinct, Rabi is said to have asked, about the latter, “Who ordered that?”
- 1948: The muon is not an excited electron
  - ▶  $\mu \rightarrow e\gamma$  excluded as a major decay mode
  - ▶ What is going on?
  - ▶ We still don't know, and we're still searching

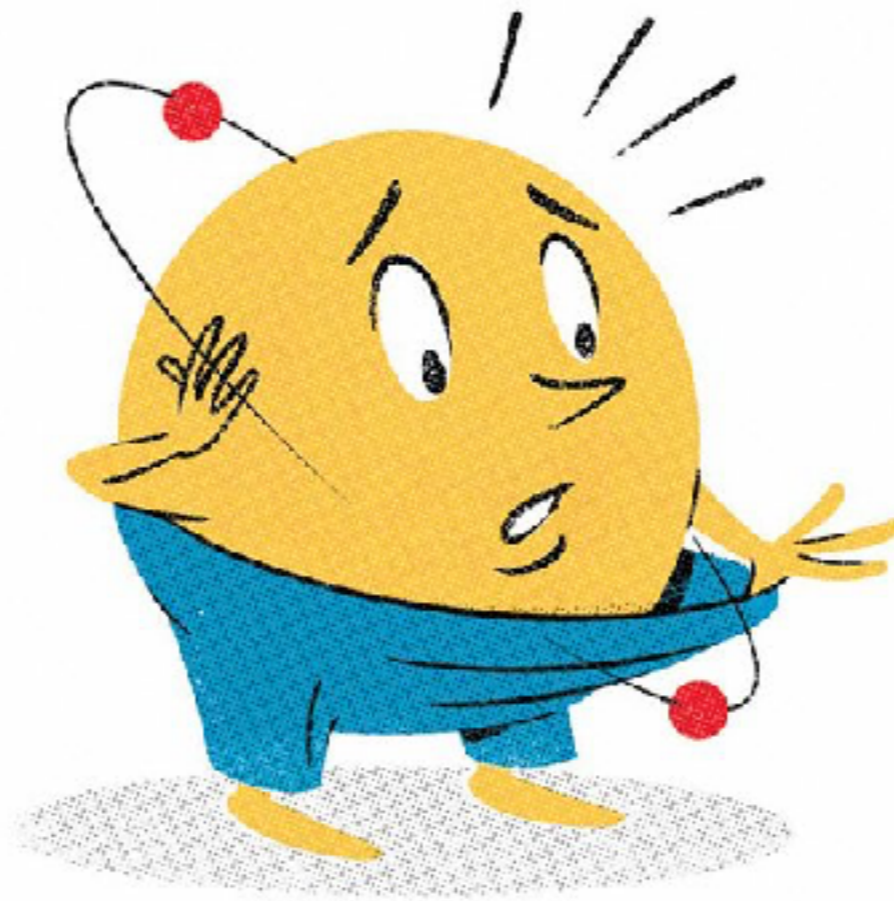
Soon after, nuclear physics splits, and a new field, HEP, appears

## The Muon Has Since Provided:

- The birth of HEP
- The first evidence for particle generations
- The decisive test of time dilation
- The best determination of the Fermi constant
  - ▶ Quantifying the universal strength of weak interactions
  - ▶ Through precision lifetime measurements
- First hint of weak universality
- The coupe de gras for universal parity conservation
  - ▶ Through anisotropies in muon decay
  - ▶ Preceded by the Theta-Tau Puzzle, and Lee and Yang's proposed solution, in which parity is violated in the weak interaction
- The conclusion that  $\nu_e \neq \nu_\mu$ 
  - ▶  $\text{BR}(\mu \rightarrow e\gamma) < 10^{-4} \rightarrow$  the electron does not absorb the neutrino emitted by the muon in  $\mu \rightarrow e\nu\nu$
- Precision tests of V-A theory
  - ▶ Through the muon's decay angle/energy distributions
- The most precise measurement of the proton radius
  - ▶ Through energy splitting in muonic hydrogen
  - ▶ Anomalous results! Stay tuned
- Arguably the best direct evidence for physics beyond the current SM

# Are Recent Muon Measurements Pointing to New Physics?

# The Proton Radius Puzzle



The New York Times

- The proton's charge radius,  $r_p$ , is defined as the RMS of its charge distribution
- Laser spectroscopy of Hydrogen has long been used to measure physical constants such as  $R_\infty$  and  $r_p$ 
  - ▶  $R_\infty$ , the Rydberg constant, is the wavenumber of the lowest energy photon capable of ionizing hydrogen

$$E(nS) \approx -\frac{R_\infty}{n^2} + \frac{L_{1S}}{n^3}$$

- The Lamb shift,  $L_{1S}$ , contains dependence on  $r_p$ 
  - ▶ It's the splitting between L=0 and L=1 orbital angular momentum states
  - ▶ L=0 has penetration to the nucleus, so its energy is raised due to finite nuclear size, more so than the L=1 state
- One can extract both terms with two transitions

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- Additionally, electron proton scattering has been used extensively to measure  $r_p$ 
  - ▶ Differential cross section  $\rightarrow$  electric (and magnetic) form factor
  - ▶ Typically extrapolate the slope of the electric form factor, from low  $Q^2$ , down to  $Q^2=0$

$$G_E(Q^2) = 1 + \sum_{n>0} \frac{(-1)^n}{(2n+1)!} \langle r^{2n} \rangle Q^{2n}$$

$$r_p \equiv \sqrt{\langle r^2 \rangle} = \left( -6 \frac{dG_E(Q^2)}{dQ^2} \Big|_{Q^2=0} \right)^{1/2}$$

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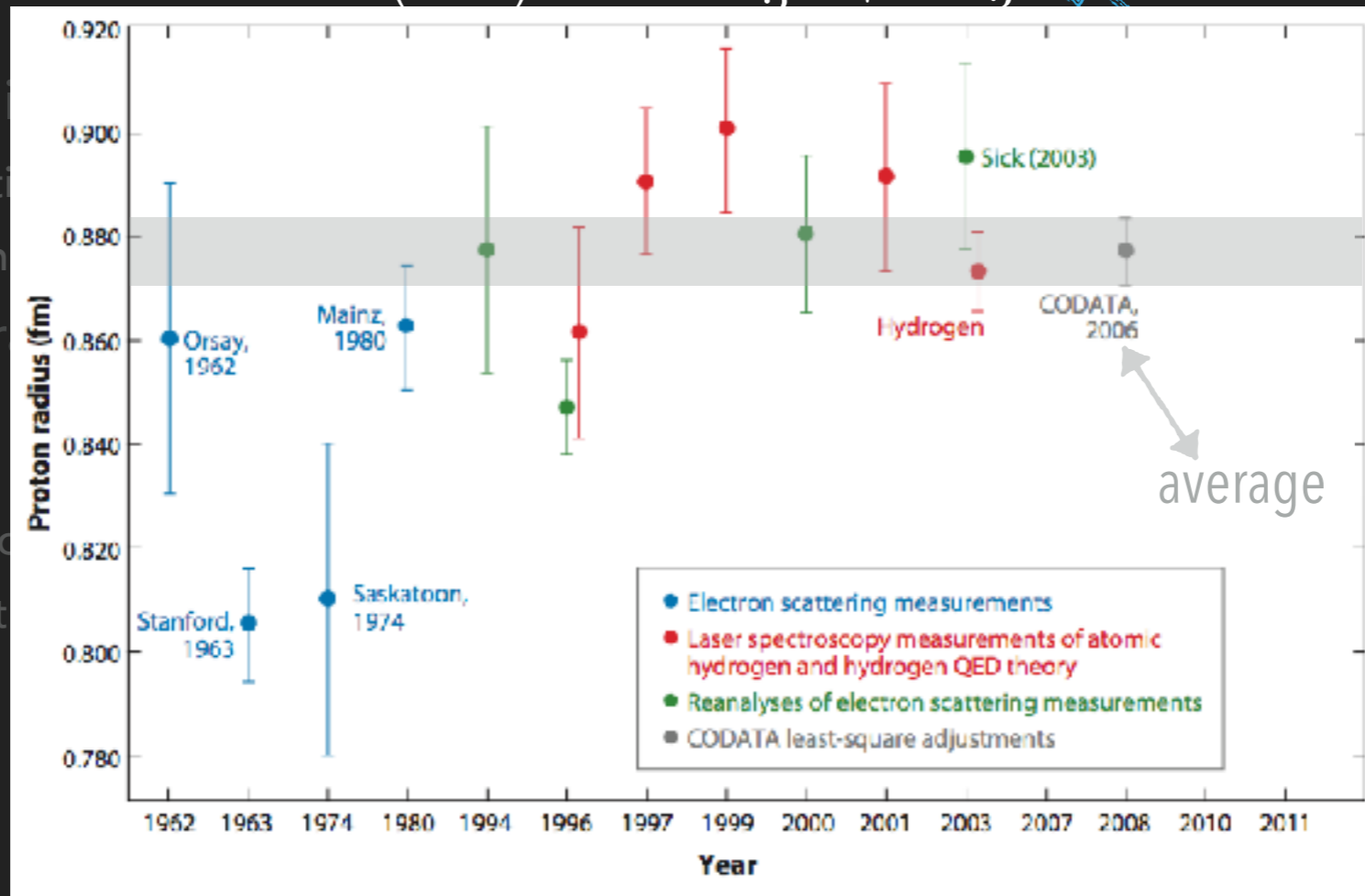
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## CREMA (Charge Radius Experiment With Muonic Atoms)

- 2010: Study muonic hydrogen to dramatically increase precision of  $r_p$ 
  - ▶ The Bohr radius is reduced by a factor of 200
  - ▶ The Lamb shift is exaggerated by  $\mathcal{O}(10^7)$
  - ▶ Finite nuclear size effects in energy transitions are enhanced by a factor of 100!
    - ~2% for of the total lamb shift for 2S-2P!
- Achieved, in one measurement, 10x better precision than the all of the world's electron data combined

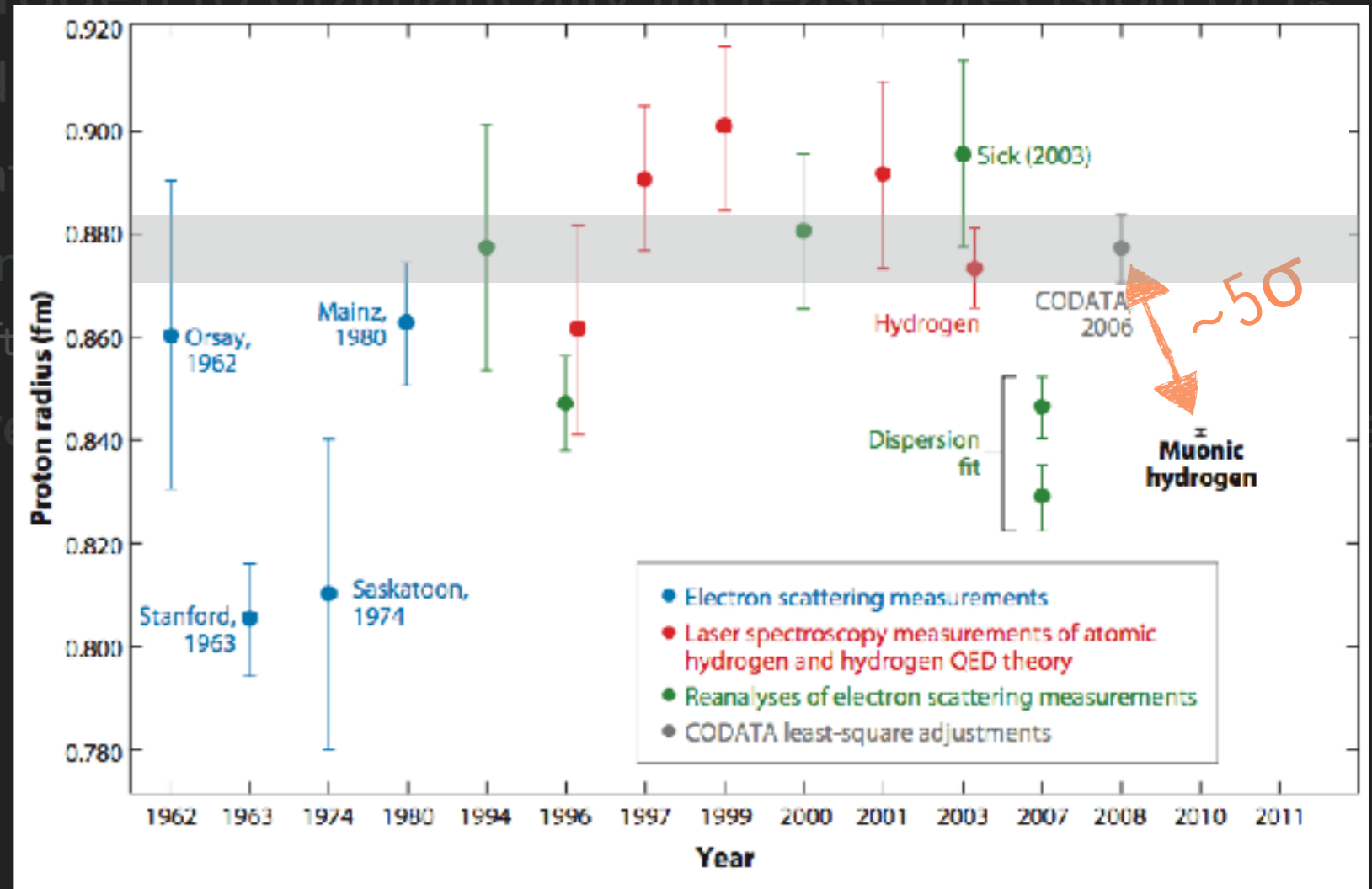
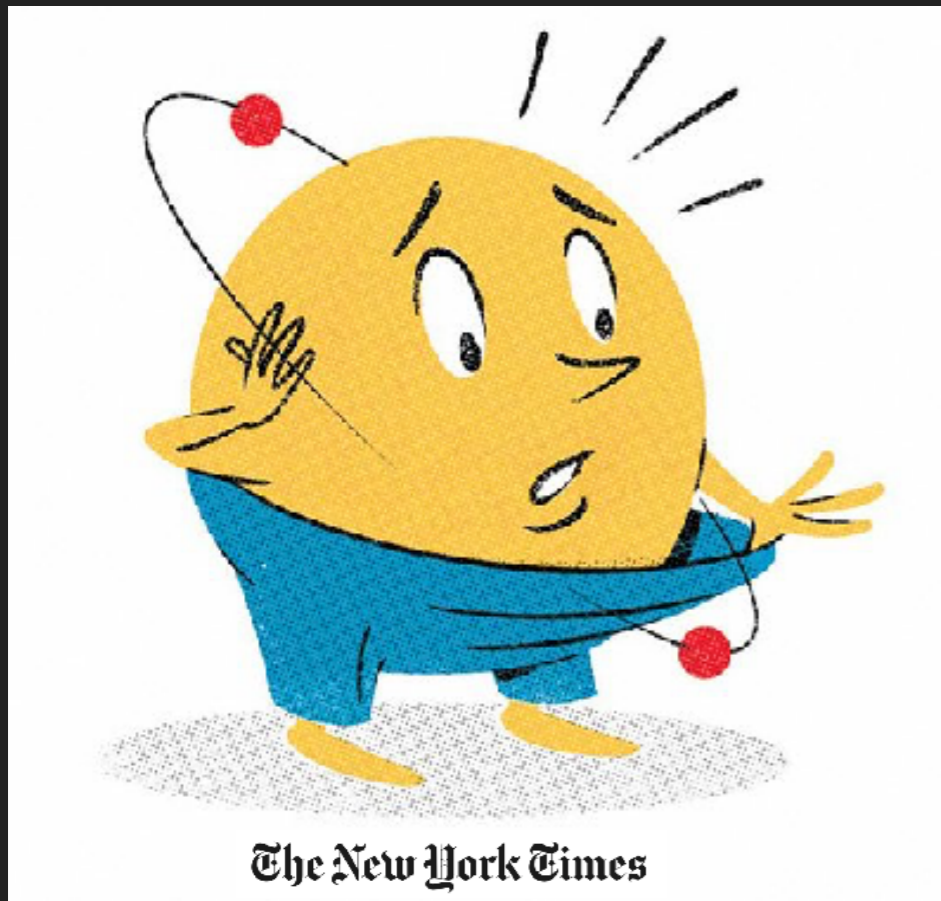


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© 2010: Study muonic hydrogen to dramatically increase precision of r



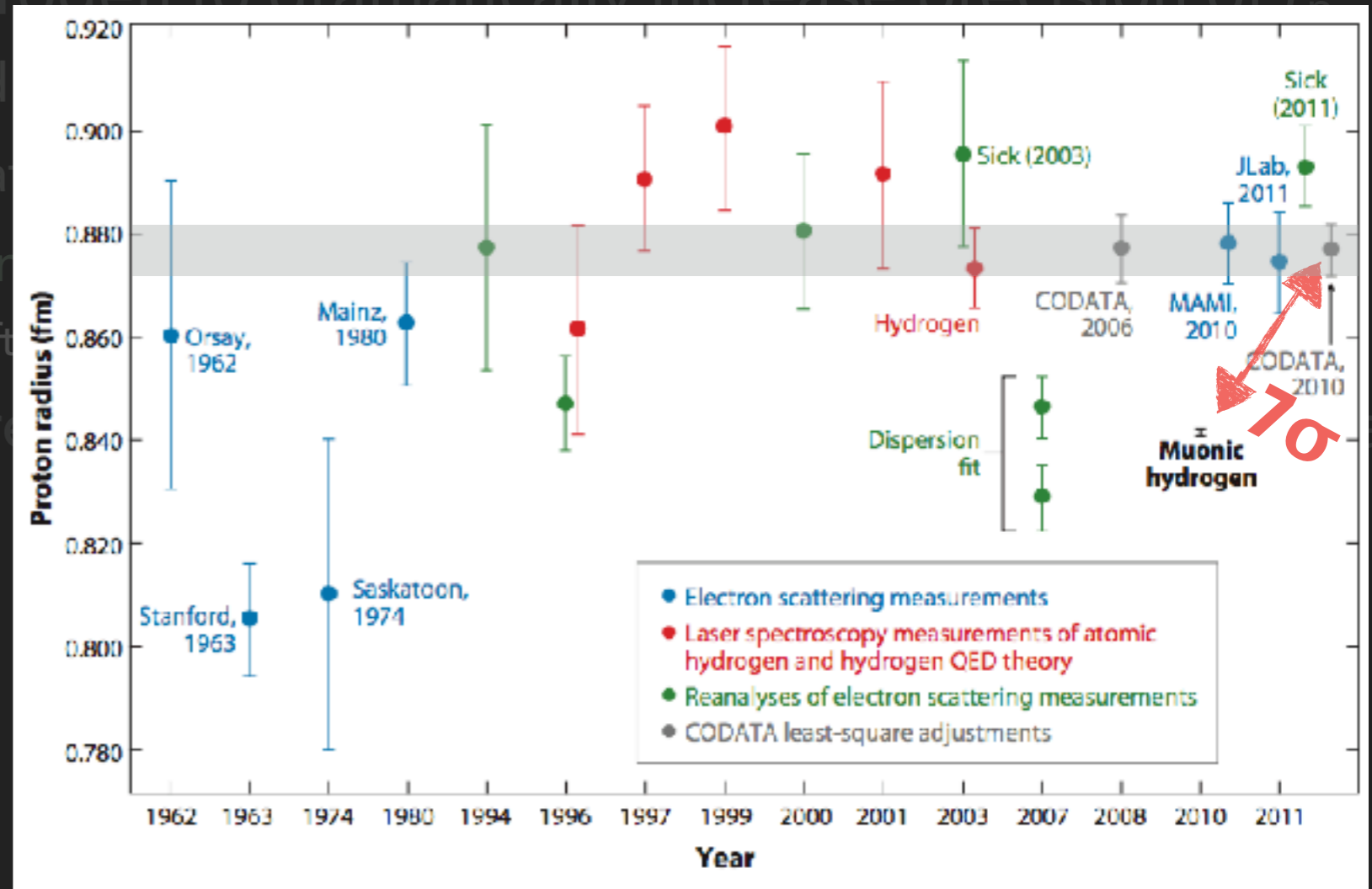
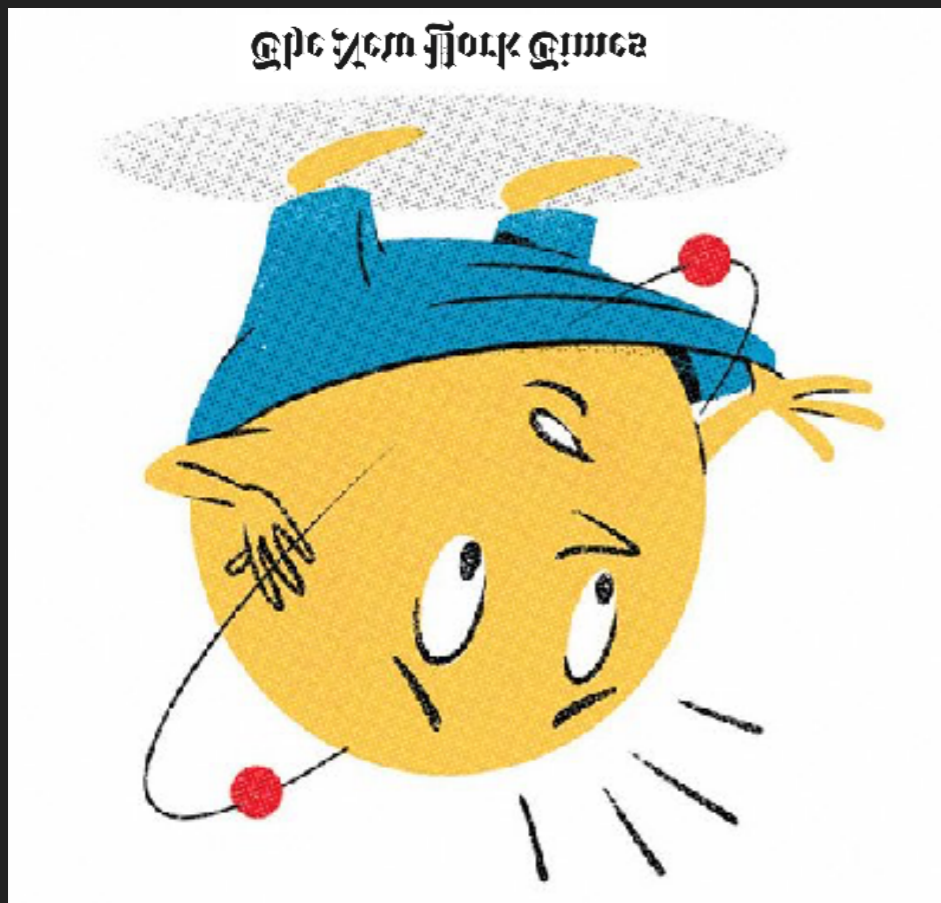
DOI: 10.1146/annurev-nucl-102212-170627

The experiment "shrunk" the proton radius by ~4%

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DOI: 10.1146/annurev-nucl-102212-170627

Subsequent electron measurements worsened the discrepancy

## Possible Explanations

- Lepton non universality?
  - ▶ Past experiments have compared e-p and  $\mu$ -p interactions, with no discrepancies
- Have the majority (or all) of laser spectroscopy and electron scattering experiments have much larger error bars than stated?
  - ▶ All relevant results have been triple checked by independent groups!
- Finite proton mass effect for muonic H?
  - ▶ This has recently been shown to be small
- Flaws with QCD calculations for atomic H?

Results from a few weeks ago may provide a clue

# Possible Explanations

- Lepton non universality
- Past experimental discrepancies
- Have the majority of experiments had independent groups?
- All relevant results are consistent
- Finite proton magnetic moment
- This has been shown to be consistent with QCD
- Flaws with QCD

Beyer et al., Science 358, 79–85 (2017) 6 October 2017

RESEARCH ARTICLE

ATOMIC PHYSICS

## The Rydberg constant and proton size from atomic hydrogen

And Beyer,<sup>1</sup> Lothar Maierbachner,<sup>1\*</sup> Arthur Matveev,<sup>1</sup> Rainer Földi,<sup>1</sup> Ksenia Khachatryan,<sup>2,3</sup> Alexey Gerasim,<sup>3</sup> Tobias Lamour,<sup>3</sup> Dylan G. Vogt,<sup>4</sup> Theodor W. Hänsch,<sup>1,5</sup> Nikolai Kolachevsky,<sup>6,7</sup> Thomas Udem<sup>1,5</sup>

At the core of the “proton radius puzzle” is a four-standard deviation discrepancy between the proton root-mean-square charge radii ( $r_p$ ) determined from the regular hydrogen (H) and the muonic hydrogen ( $\mu\text{p}$ ) atoms. Using a cryogenic beam of H atoms, we measured the 2S–4P transition frequency in H, yielding the values of the Rydberg constant  $R_\infty = 10973731.56816(16)$  per meter and  $r_p = 0.8335(16)$  femtometer. Our  $r_p$  value is 3.3 combined standard deviations smaller than the previous H world data, but in good agreement with the  $\mu\text{p}$  value. We motivate an asymmetric fit function, which eliminates line shifts from quantum interference of neighboring atomic resonances.

The study of the hydrogen atom (H) has been at the heart of the development of modern physics. Precision laser spectroscopy of H is used today to determine fundamental physical constants such as the Rydberg constant  $R_\infty$  and the proton charge radius  $r_p$ , defined as the root-mean-square (RMS) of the charge distribution. Owing to the simplicity of H, theoretical calculations can be carried out with astonishing accuracy, reaching precision up to the 12th decimal place. At the same time, high-resolution laser spectroscopy experiments deliver measurements with even higher accuracy, reaching up to the 10th decimal place in the case of the 2S–2S transition (1,2), the most precisely determined transition frequency in H.

The energy levels in H can be expressed as

$$E_{nl} = R_\infty \left( \frac{1}{n^2} + f_{nl} \left( \frac{r_p}{a_0} \right) + \dots \right) + \delta_{nl} \left( \frac{r_p}{a_0} \right)^2 \quad (1)$$

where  $n$ ,  $l$ , and  $f$  are the principal, orbital, and total angular momentum quantum numbers, respectively. The first term describes the gross structure of H as a function of  $n$  and was first derived in the visible H spectrum and explained empirically by Rydberg. Later, the Bohr model, in which the electron is orbiting a pointlike and, in simplest approximation, infinitely heavy proton, provided a deeper theoretical understanding.

The Rydberg constant  $R_\infty = \alpha^2 m_e c^2 / 2h$  links the natural energy scale of atomic systems and the SI unit system. It connects the mass of the electron  $m_e$ , the fine structure constant  $\alpha$ , Planck's constant  $h$ , and the speed of light in vacuum  $c$ . Precision spectroscopy of H has been used to determine  $R_\infty$  by means of Eq. 1 with a relative uncertainty of 6 parts in  $10^9$ , making it one of the most precisely determined constants of nature to date and a cornerstone in the global adjustment of fundamental constants (3).

The second term in Eq. 1,  $f_{nl}(r_p/a_0, \dots) = \chi_{nl} r_p^2 + \chi_{nl}^{(2)} r_p^3 + \chi_{nl}^{(3)} r_p^4 + \dots$ , accounts for relativistic corrections, contributions coming from the interactions of the bound-state system with the quantum electrodynamics (QED) vacuum fields, and other corrections calculated in the framework of QED (4). The electron-to-proton mass ratio enters the coefficients  $\chi_{nl}, \chi_{nl}^{(2)}, \dots$  through small corrections caused by the finite proton mass.

The last term in Eq. 1 with coefficient  $\delta_{nl}$  is the leading-order correction originating from the finite charge radius of the proton,  $r_p$  (5). It only affects atomic S states (with  $l = 0$ ) for which the electron's wave function is nonzero at the origin. Higher-order nuclear charge distribution contributions are included in  $f_{nl}(r_p/a_0, \dots)$ .

**The proton radius puzzle**

The proton charge radius  $r_p$  has been under debate for some time now because the very accurate value from laser spectroscopy of the exotic muonic hydrogen atom ( $\mu\text{p}$ ) (6,7) yielded a value that is 4% corresponding to 50% smaller than the CODATA 2010 value of  $r_p$  (8) [see (9–11) for reviews on this topic]. The CODATA value is obtained from a combination of 24 transition frequency measurements in H and deuterium and several results from elastic electron scattering (9–11). The accuracy of the  $\mu\text{p}$  result is enabled by the fact that the muon's orbit is  $\sim 200$  times smaller than the electron's.

In a recent review of magnitude of  $r_p$  on the energy levels.

Here we study the spectroscopic precision discrepancy, in particular the 4 $\sigma$  discrepancy between the  $\mu\text{p}$  value and the global average of all transitions measured in H (20) (H world data, Fig. 1). Recently, a similar discrepancy has arisen for the deuteron radius with a deviation from laser spectroscopy of muonic deuterium ( $\mu\text{d}$ ) (21).

Considering Eq. 1 and the fact that  $f_{nl}(r_p/a_0, \dots)$  is known with sufficiently high accuracy, one finds a very strong correlation between  $R_\infty$  and  $r_p$ . Equation 1 involves two parameters,  $R_\infty$  and  $r_p$ , which need to be determined simultaneously from a combination of at least two measurements in H. The 2S–2S transition frequency serves as a cornerstone in this procedure. Owing to its small natural line width of only 13 Hz, experimental determinations are one thousand times more accurate than the any other transition frequency in H, where typical line widths amount to 1 MHz or more.

Examining previous determinations of the value pair  $(R_\infty, r_p)$  from H (Fig. 1, bottom), one notes that many of the individual measurements are in fact not in disagreement with the  $\mu\text{p}$  value. The discrepancy of 4 $\sigma$  appears when averaging all H values (p versus l world data, Fig. 1, top).

**Principle of the measurement**

Here we report on a measurement of the 2S–4P transition in H (Fig. 2A), yielding  $(R_\infty, r_p)$  with an uncertainty comparable to the aggregate l-world data and significantly smaller than the proton radius discrepancy, which corresponds to 5.8 kHz in terms of the 2S–4P transition frequency. This uncertainty requires a determination of the resonance frequency to almost any part in 10,000 of the observed line width of 20 MHz (Fig. 2B).

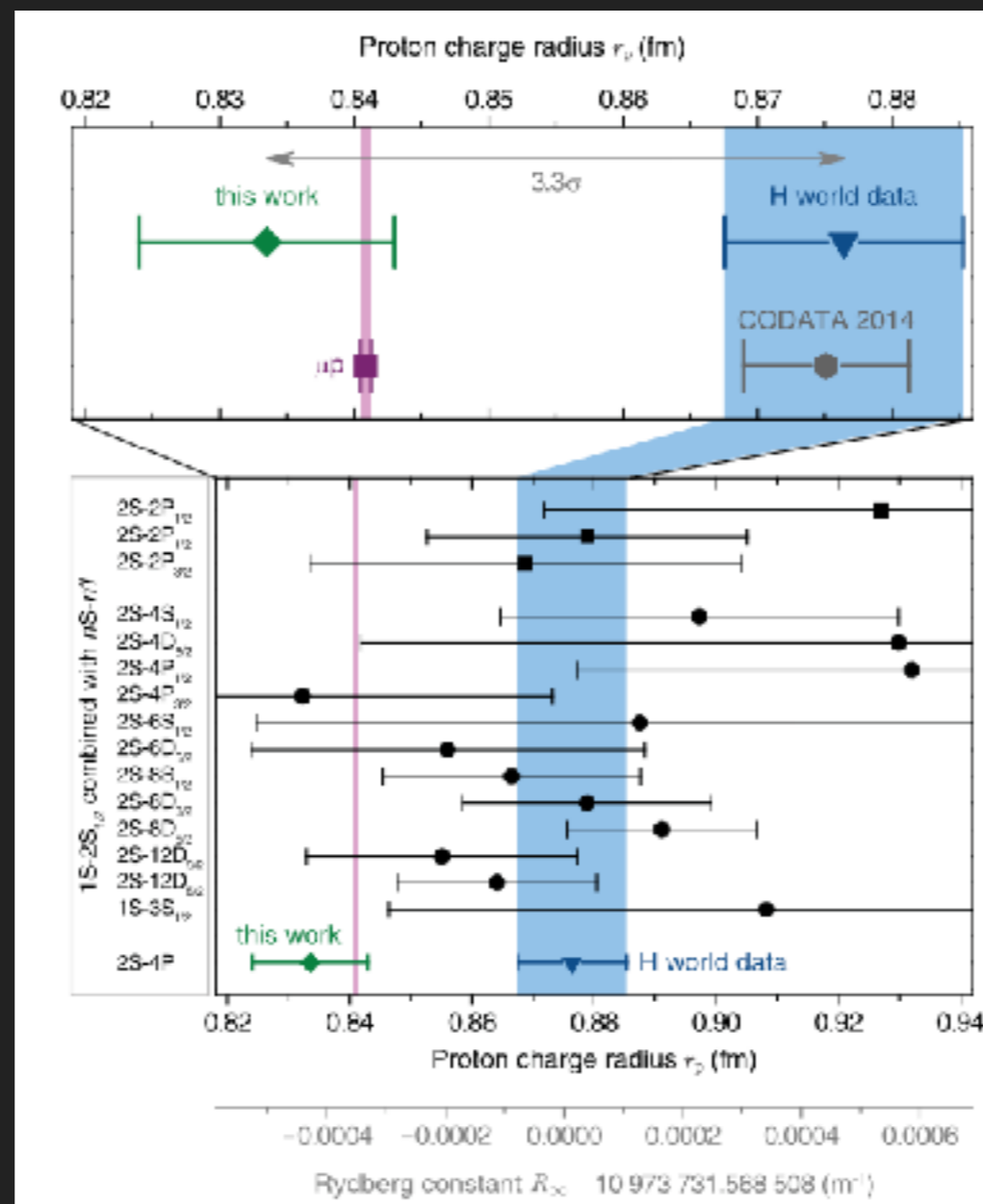
The previous most accurate measurements (see, e.g., (9–11) and references therein) were limited by the electron-impact excitation used to produce atoms in the metastable 2S state. This excitation results in hot atoms with mean thermal velocities of 3000 m/s or more and an uncontrolled mixture of population in the four 2S Zeeman sublevels. In turn, this typically leads to corrections on the order of tens of kilohertz because of effects such as the second-order Doppler and ac-Stark shifts or the excitation of multiple unresolved hyperfine components.

Our measurement is essentially unaffected by these systematic effects (22) because we use the Garching IS 2S apparatus (4, 20) (Fig. 3) as a well-controlled cryogenic source of 2S- $l$  (2S) atoms. Here, Doppler-free two-photon excitation is used to address exclusively population the 2S( $^1$ ) Zeeman sublevel without imparting additional momentum on the atoms.

The remaining main systematic effects in our experiment are the first-order Doppler shift and apparent line shifts caused by quantum interference of neighboring atomic resonances, both of

Results from a few weeks ago may provide a clue

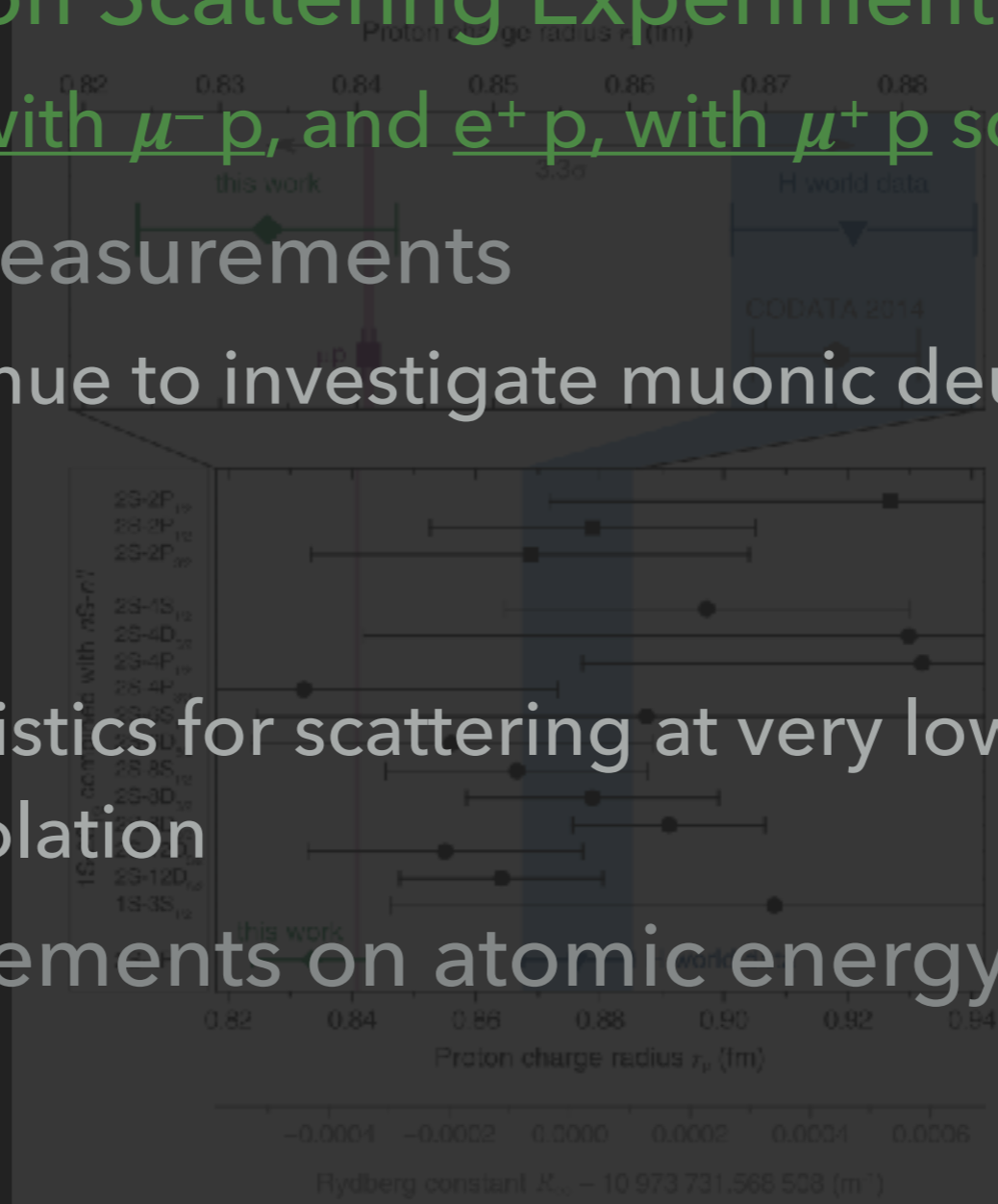
- New result using electrons
- Most precise spectroscopy measurement to date using atomic hydrogen
  - ▶ Agreement with the muonic hydrogen results



Plot of Rydberg constant is nearly identical, hence the double axes

## Looking Forward

- The Muon Proton Scattering Experiment (MUSE) @ PSI
  - ▶ Compare  $e^-p$  with  $\mu^-p$ , and  $e^+p$ , with  $\mu^+p$  scattering
- New CREMA measurements
  - ▶ Have/will continue to investigate muonic deuterium and muonic-ionic-helium
- PRad @ Jlab
  - ▶ Will collect statistics for scattering at very low scattering  $Q^2$  for reliable extrapolation
- Various improvements on atomic energy level splitting measurements



The muonic measurements have revealed something, but we don't know what, yet

# The Muon's Anomalous Magnetic Moment





## The g-factor

- A particle's magnetic moment is coupled to its spin by its gyromagnetic ratio:

$$\vec{\mu} = g \frac{e}{2mc} \vec{S}$$

- For a Dirac particle,

$$g = 2$$

- The anomalous component of the magnetic moment comes in internal structure, and from vacuum fluctuations from everything, known and unknown, that couples, either directly or indirectly, the the system in question

$$a = \frac{g - 2}{2}$$

Sensitive to a wide range of phenomena

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- E.g. the magnetic moments of nucleons:

$$g_p \approx 5.6 \neq 2$$

$$g_n \approx -3.8 \neq 0$$



Internal Structure

- E.g. the magnetic moment of the electron

$$g_e^{\text{exp}} / 2 = 1.00115965218073(28)$$

$$g_e^{\text{QED}} / 2 = 1.001159652181643(764)$$



Independent measurement of  $\alpha$   
QED corrections work!

Phys. Rev. Lett. 100, 120801 (2008)

## The g-factor

 $e$ 

- + Easy to produce and stable
  - measured to 0.28 parts per trillion!
- **Small mass**
  - Low sensitivity to new physics
  - Clean calculations

 $\mu$ 

- + Abundant from pion decays
- + 200 times the mass of the electron
  - ~40,000 times the sensitivity to new physics
- ± **Unstable**
  - Utilize the decay
- + long lifetime of 2.2 us
  - Sufficient time to interact with external magnetic field

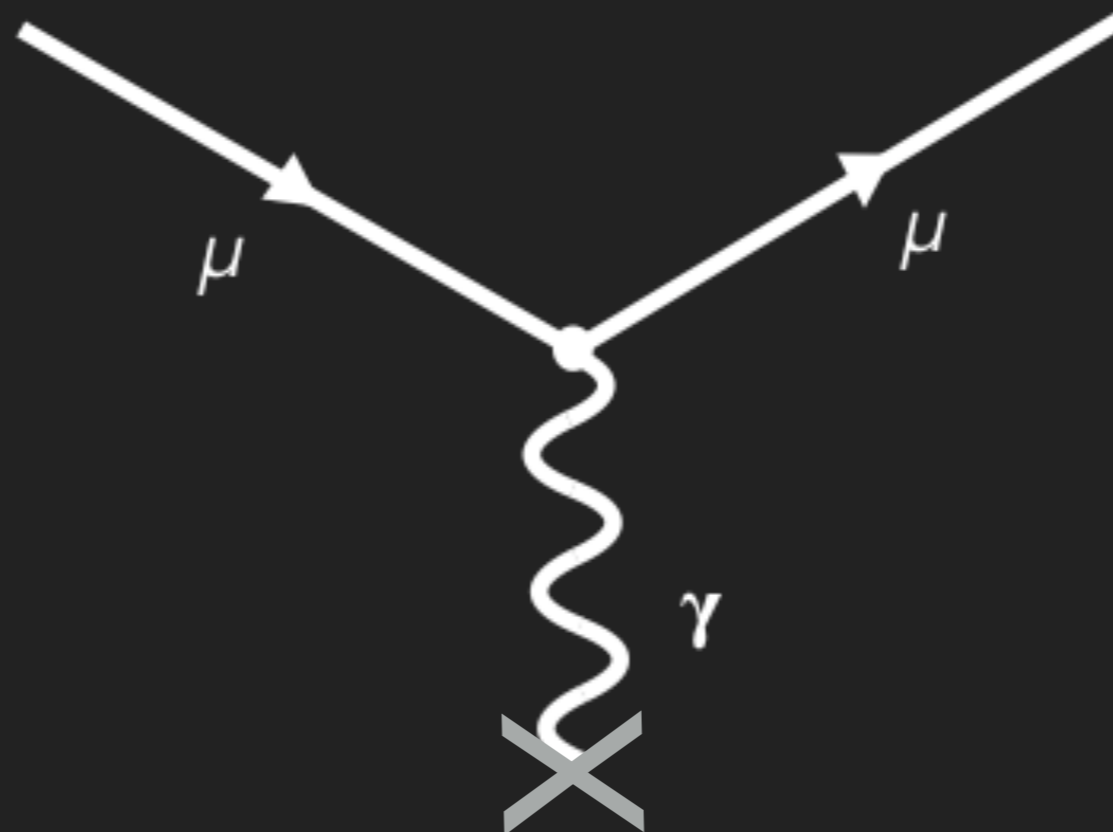
 $\tau$ 

- + 17 times the muon mass
  - More sensitivity!
- **Disproportionally difficult to produce**
- **Short lifetime, ~0.29 ps**

## The Muon's g-factor

$$\vec{\mu}_\mu = g_\mu \frac{e}{2m_\mu c} \vec{S}$$

Dirac:  $g_\mu = 2$



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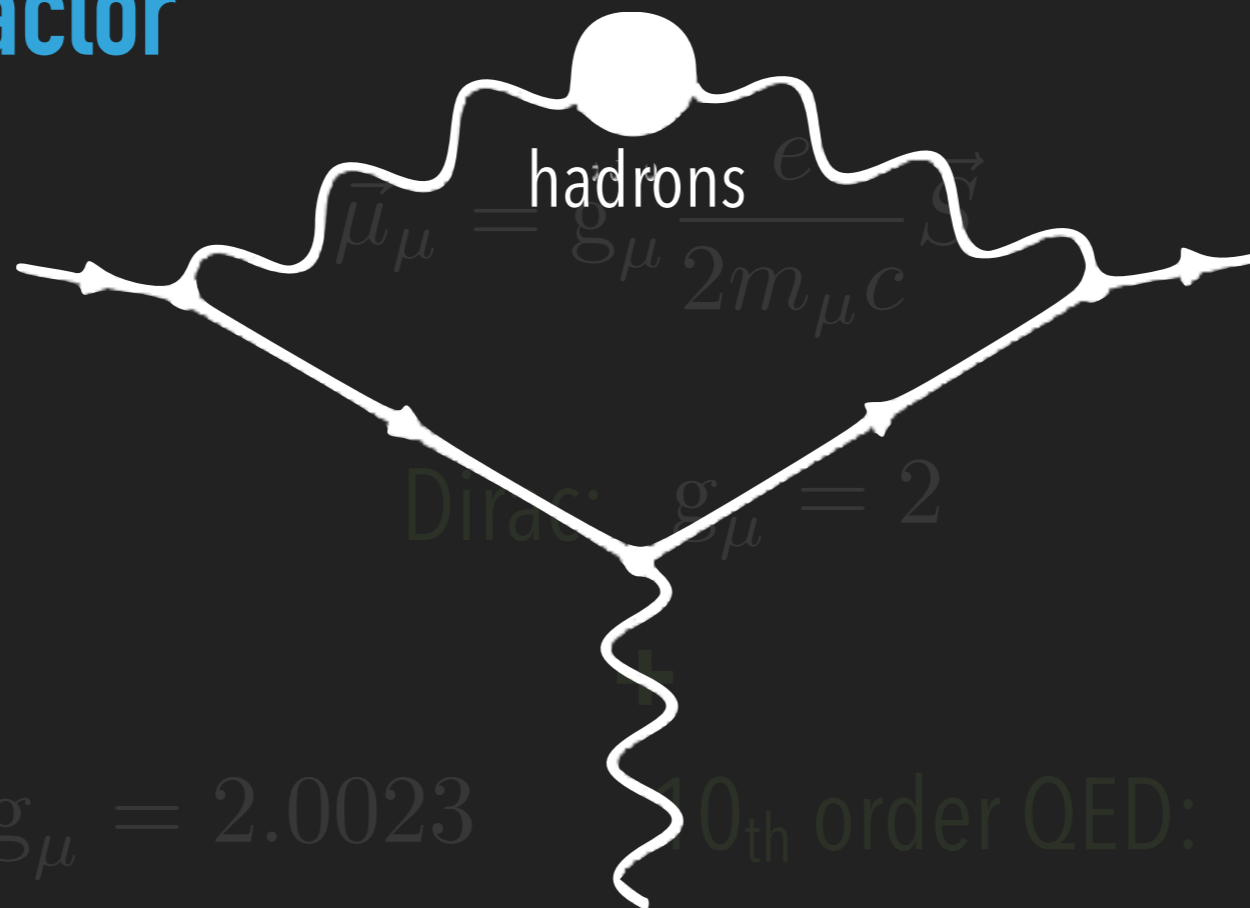
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1<sub>st</sub> order QED:  $g_\mu = 2.0023$

10<sub>th</sub> order QED:  $g_\mu = 2.002331$



# The Muon's g-factor



1<sup>st</sup> order QED:  $g_\mu = 2.0023$

10<sup>th</sup> order QED:  $g_\mu = 2.002331$

+

Hadronic Corrections:  $g_\mu = 2.00233184$

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10<sub>th</sub> order QED:  $g_\mu = 2.002331$

Hadronic Corrections:  $g_\mu = 2.00233184$

Electroweak Corrections:

$$g_\mu = 2.00233184178$$

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# The Muon's Anomalous Magnetic Moment

$$a_{\mu} = \frac{g_{\mu} - 2}{2}$$

Theory (420 ppb)

$$a_{\mu}^{\text{SM}} = a_{\mu}^{\text{QED}} + a_{\mu}^{\text{EW}} + a_{\mu}^{\text{Hadron}} = (11,659,182.8 \pm 4.9) \cdot 10^{-10}$$

Hagiwara *et al.* J. Phys. G38 085003 (2011)



Experiment (540 ppb)

$$a_{\mu}^{\text{EXP}} = 116,592,089(63) \cdot 10^{-11}$$

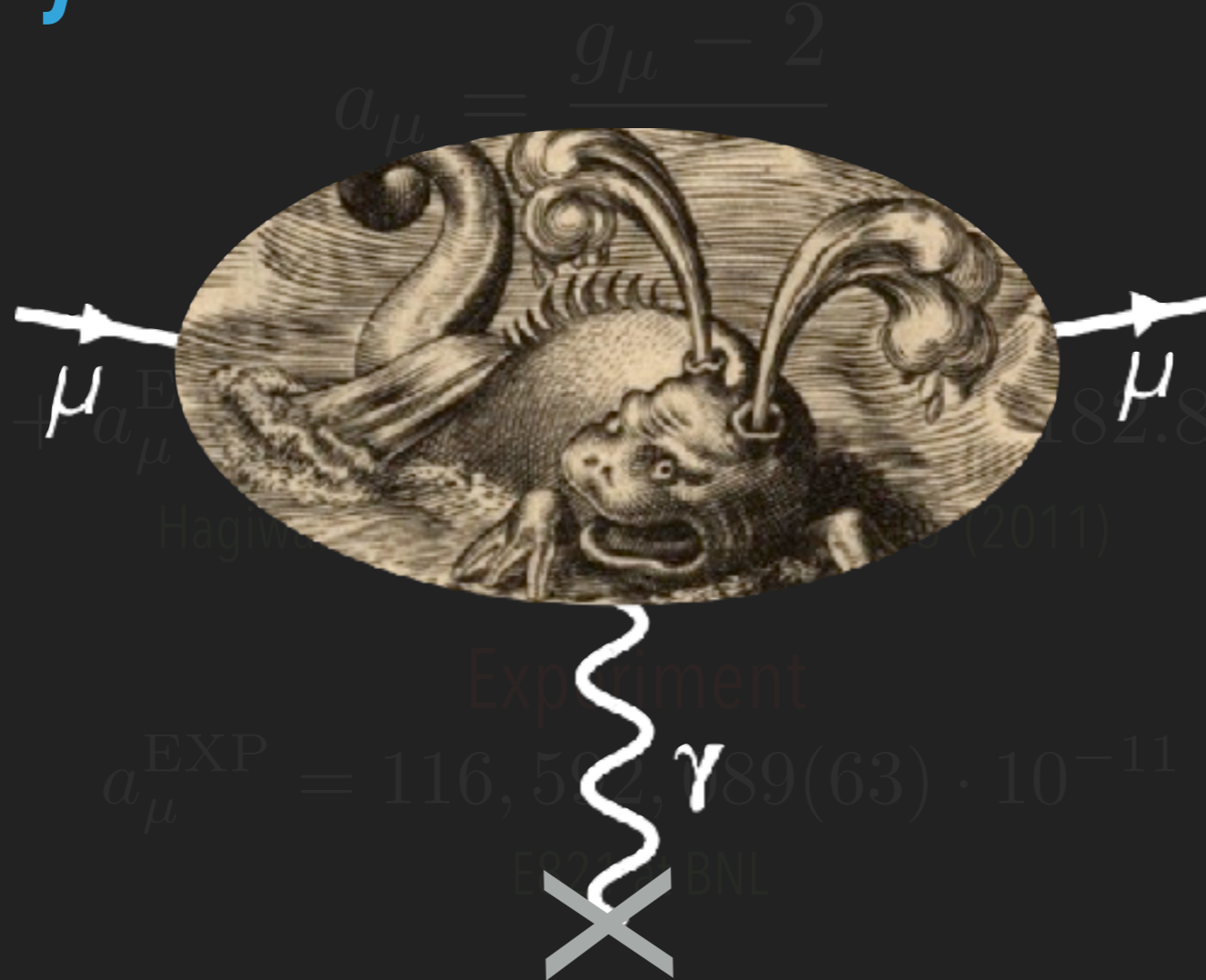
2004: E821 @ BNL



**3.3  $\sigma$  discrepancy**

$$a_{\mu}^{\text{EXP}} - a_{\mu}^{\text{SM}} = (26.1 \pm 8.0) \cdot 10^{-10}$$

**BLN's E821 was in uncharted territory.  
Did they see the effects of something new?**



**3.3  $\sigma$  discrepancy**

$$a_{\mu}^{\text{EXP}} - a_{\mu}^{\text{SM}} = (26.1 \pm 8.0) \cdot 10^{-10}$$

## Did BLN's E821 See Beyond the Standard Model?

$$a_{\mu}^{\text{SM}} = a_{\mu}^{\text{QED}} + a_{\mu}^{\text{EW}} + a_{\mu}^{\text{Hadron}} = (11,659,182.8 \pm 4.9) \cdot 10^{-10}$$

Hagiwara et al., Phys. 638 085003 (2011)

Higher precision needed

$$a_{\mu}^{\text{EXP}} = 116,592,789(63) \cdot 10^{-11}$$

E821 at BNL

**3.3  $\sigma$  discrepancy**

$$a_{\mu}^{\text{EXP}} - a_{\mu}^{\text{SM}} = (26.1 \pm 8.0) \cdot 10^{-10}$$

# Delivery of BNL's muon storage ring to Fermilab



# A vigorous global theory effort

## First Workshop of the Muon $g-2$ Theory Initiative

3-6 June 2017  
Q Center  
US/Central timezone

Sponsors

Committees

Timetable

Registration

↳ Registration Form

List of registrants

List of confirmed speakers

workshop photos

Accommodations

Wilson Hall

Visa Information

In the coming years, experiments at [Fermilab](#) and at [J-PARC](#) plan to reduce the uncertainties on the already very precisely measured anomalous magnetic moment of the muon by a factor of four. The goal is to resolve the current tantalizing tension between theory and experiment of three to four standard deviations. On the theory side the hadronic corrections to the anomalous magnetic moment are the dominant sources of uncertainty. They must be determined with better precision in order to unambiguously discover whether or not new physics effects contribute to this quantity.

There are a number of complementary theoretical efforts underway to better understand and quantify the hadronic corrections, including dispersive methods, lattice QCD, effective field theories, and QCD models. We have formed a [new theory initiative](#) to facilitate interactions between the different groups through organizing a series of workshops. The goal of this first workshop is to bring together theorists from the different communities to discuss, assess, and compare the status of the various efforts, and to map out strategies for obtaining the best theoretical predictions for these hadronic corrections in advance of the experimental results.

All sessions in this workshop will be plenary, featuring a mix of talks and discussions.



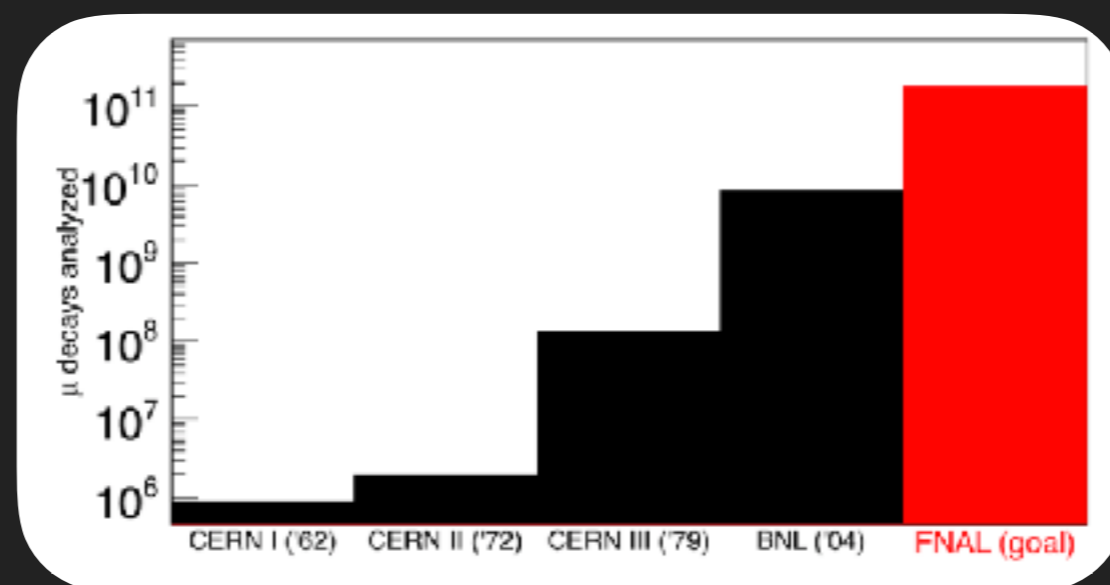
Starts Jun 3, 2017 08:00  
Ends Jun 6, 2017 18:00  
US/Central

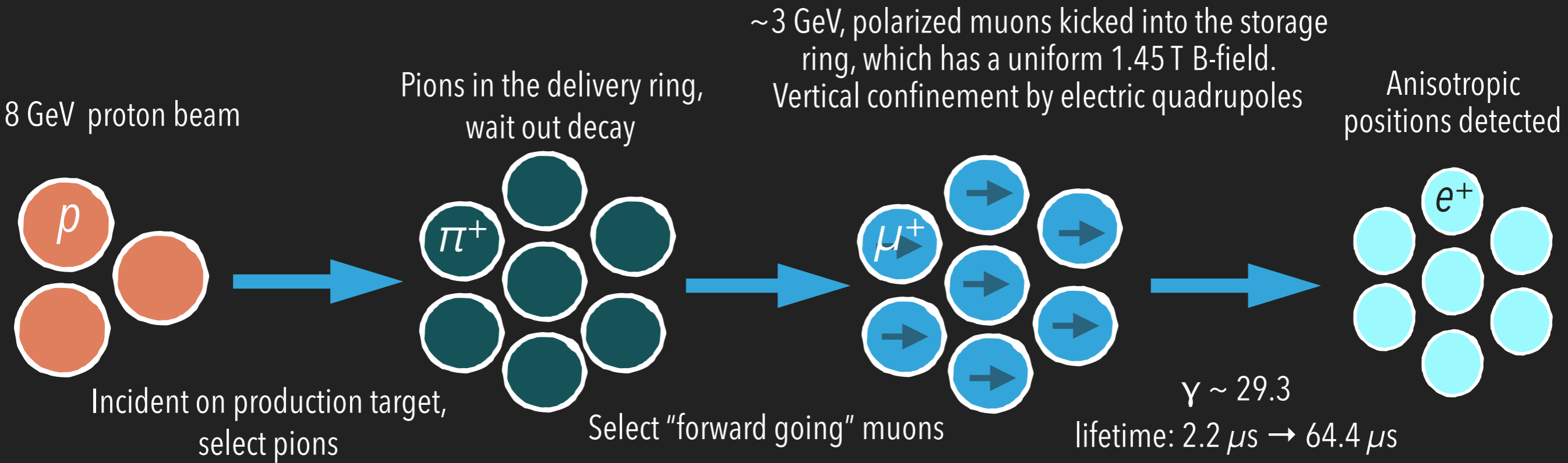


Q Center  
D L1 69 (The L1 denotes that the meeting room is on the Lower Level 1 floor)

## Higher Precision on the Way

- A new muon beamline at FNAL will deliver 21x the statistics as in E821
  - ▶ As well as reduced 3x systematic uncertainty from B field uniformity
  - ▶ Overall 4 fold improvement: 540 ppb @ BNL → 140 ppb @ FNAL
- First physics run to begin this month!
  - ▶ Should be the highest statistics dataset in a few months
- Theory expected to improved by a factor of 2 on experiments timescale
  - ▶ If central values remain the same:
    - ~ $5\sigma$  discrepancy if theory does not improve
    - ~ $7-8\sigma$  discrepancy if theory improves as expected







## The Extraction of $a_\mu$

If  $\vec{B} \cdot \vec{P}_\mu = 0$  then the cyclotron frequency is  $\vec{\omega}_c = -\frac{q\vec{B}}{m\gamma}$

The spin precession frequency is  $\vec{\omega}_s = -\frac{gq\vec{B}}{2m} - (1 - \gamma)\frac{q\vec{B}}{\gamma m}$

And if  $g = 2 \rightarrow \vec{\omega}_s = \vec{\omega}_c$

So, one may define  $\vec{\omega}_a \equiv \vec{\omega}_s - \vec{\omega}_c = -\frac{g-2}{2} \frac{q\vec{B}}{m} = -a_\mu \frac{q\vec{B}}{m}$

spin, relative to momentum, precession
anomalous magnetic moment

However, because of the quadrupoles,  $\vec{\omega}_a = -\frac{q}{m} \left[ a_\mu \vec{B} - \left( a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$

But at the "magic momentum" ( $\gamma \sim 29.3$ ), the 2nd term vanishes  $\overset{=0}{\curvearrowright}$

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Need to measure this, too.  
Won't be covered here!

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**A non-zero electric dipole moment would also affect the spin**

But at the "magic momentum" ( $\gamma \sim 29.3$ ) the 2nd term vanishes

**precession, but we're not going in to that!**

## The Extraction of $\omega_a$

- $\omega_a$  is the difference between the ensemble averaged muon spin precession and cyclotron frequencies
- In the CM frame, muon spin direction is correlated with positron angle
- In the lab frame (as well as the CM frame), the positron energy is correlated with its angle relative to the muon spin

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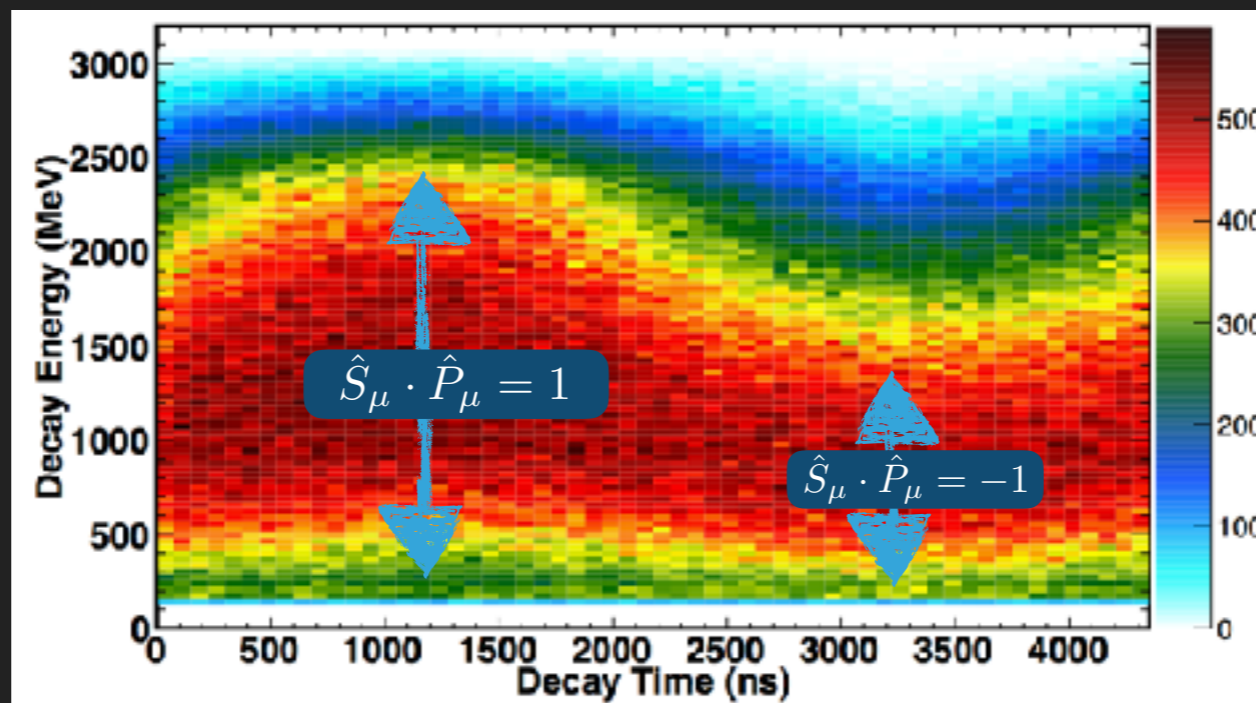
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  - ▶ Maximal energy when positron momentum and muon spin are parallel

$$E_{e,\text{lab}} = \gamma(E_{e,\text{CM}} + \beta P_{e,\text{CM}} \cos \theta_{\text{CM}}) \approx \gamma E_{e,\text{CM}} (1 + \cos \theta_{\text{CM}})$$

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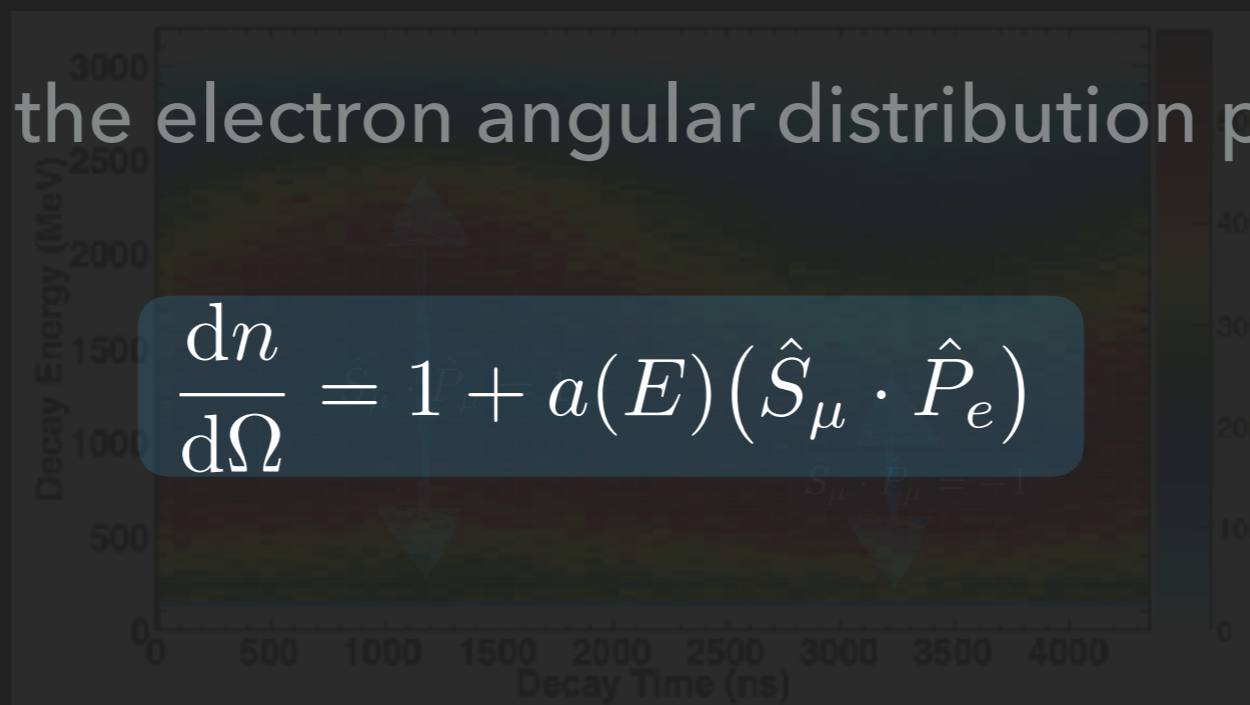
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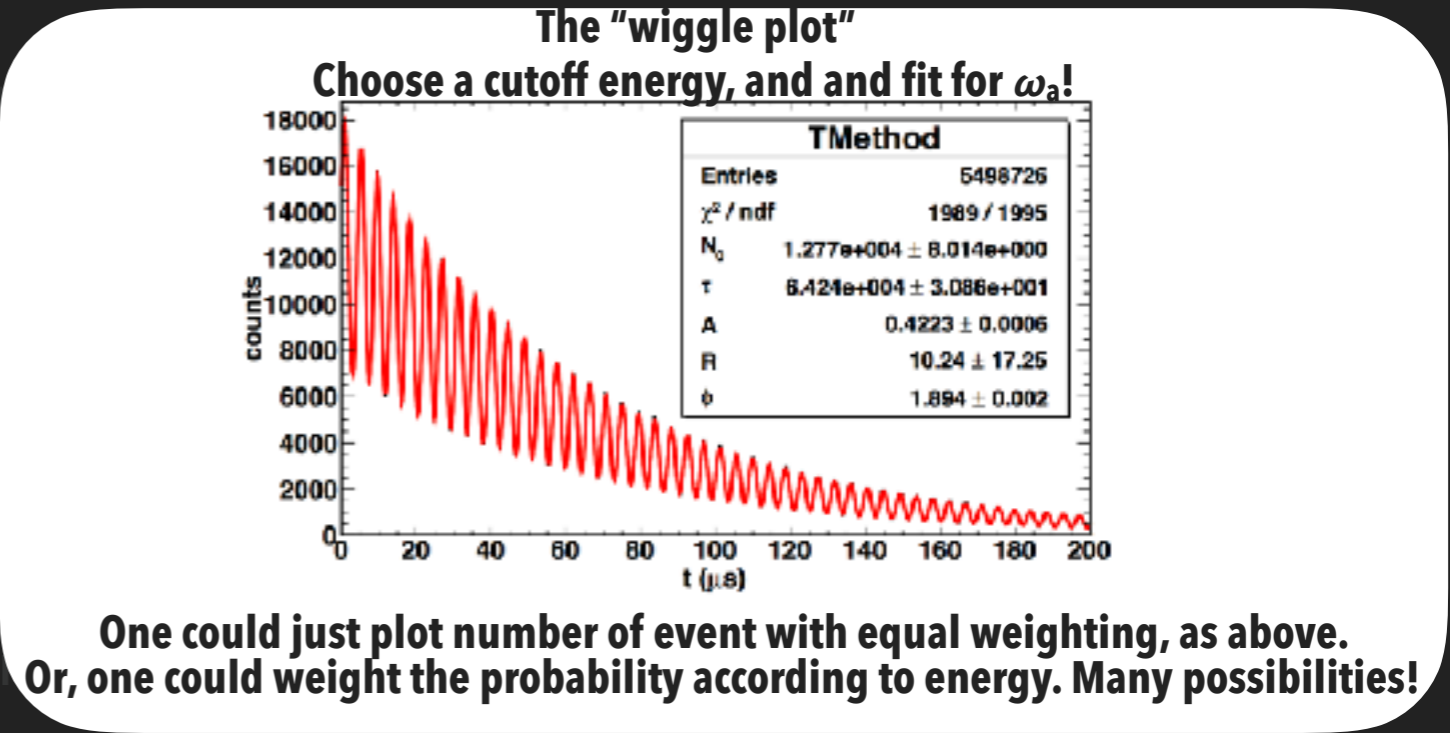
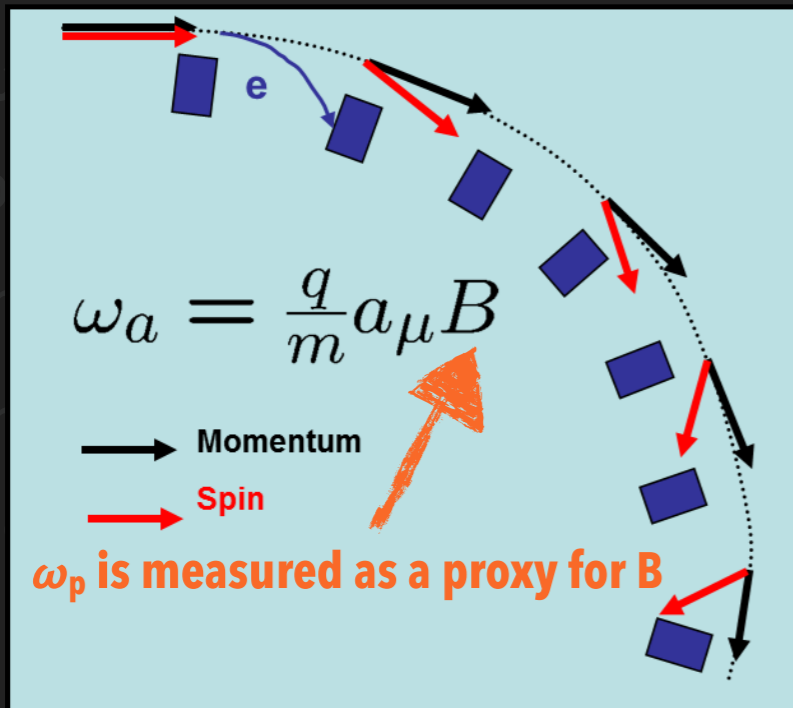
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- Also note that the electron angular distribution peaks for parallel alignment:

$$\frac{dn}{d\Omega} = 1 + a(E) (\hat{S}_\mu \cdot \hat{P}_e)$$



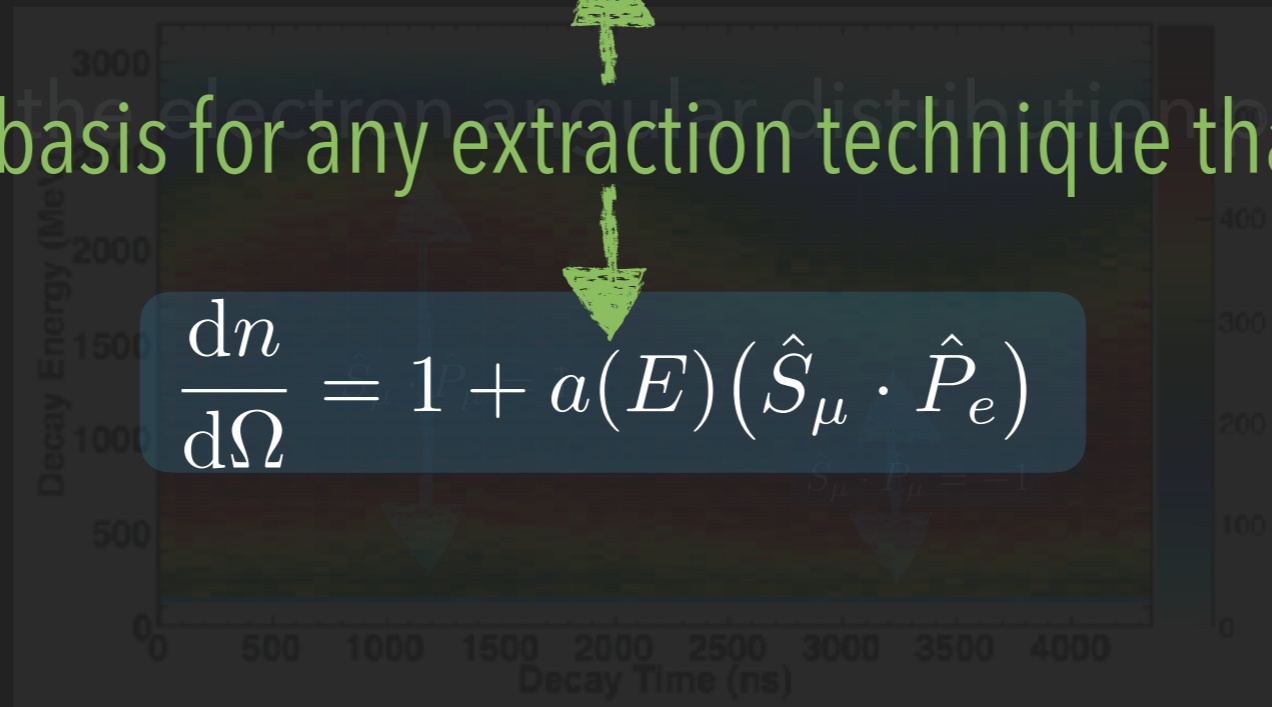
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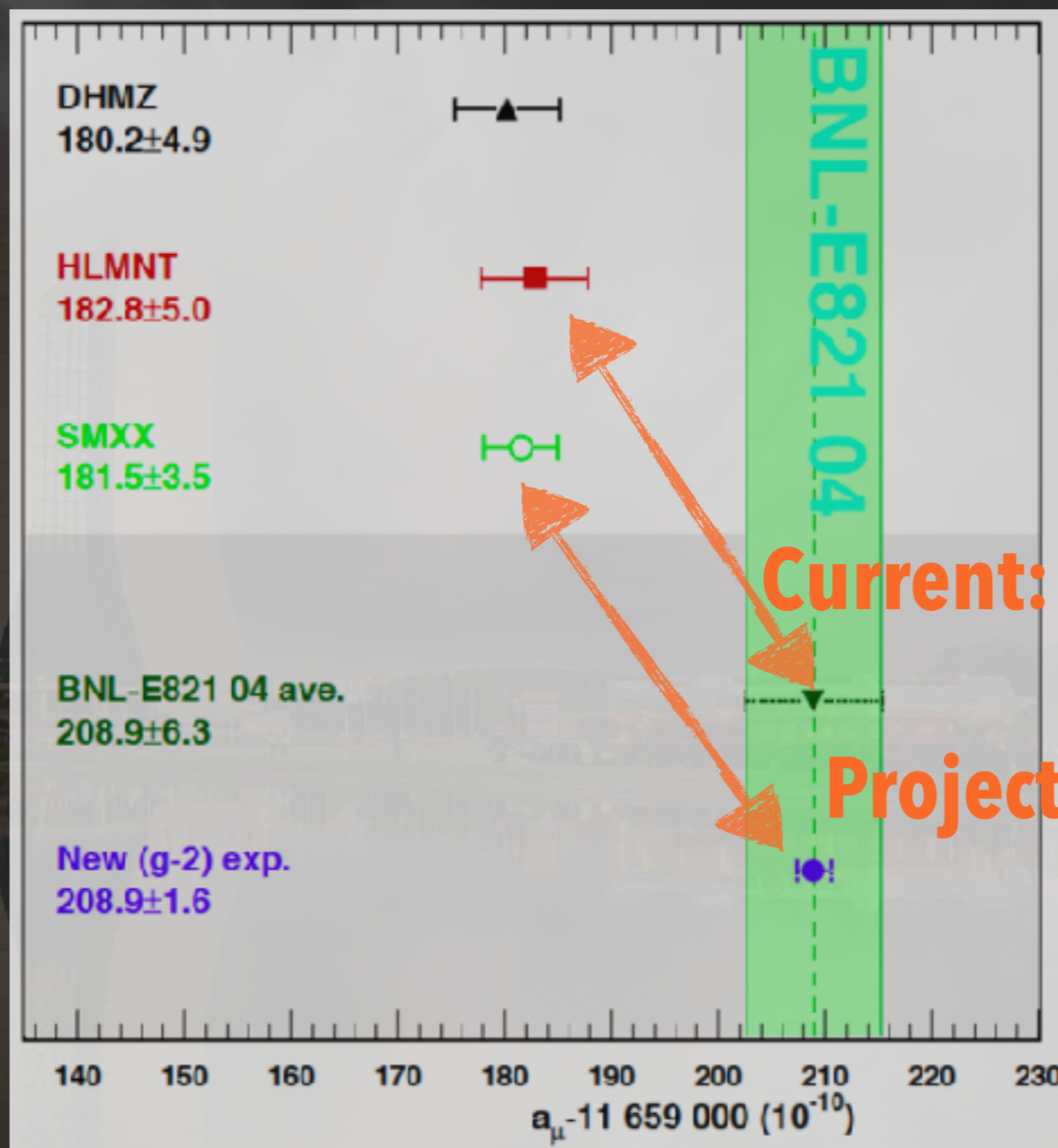
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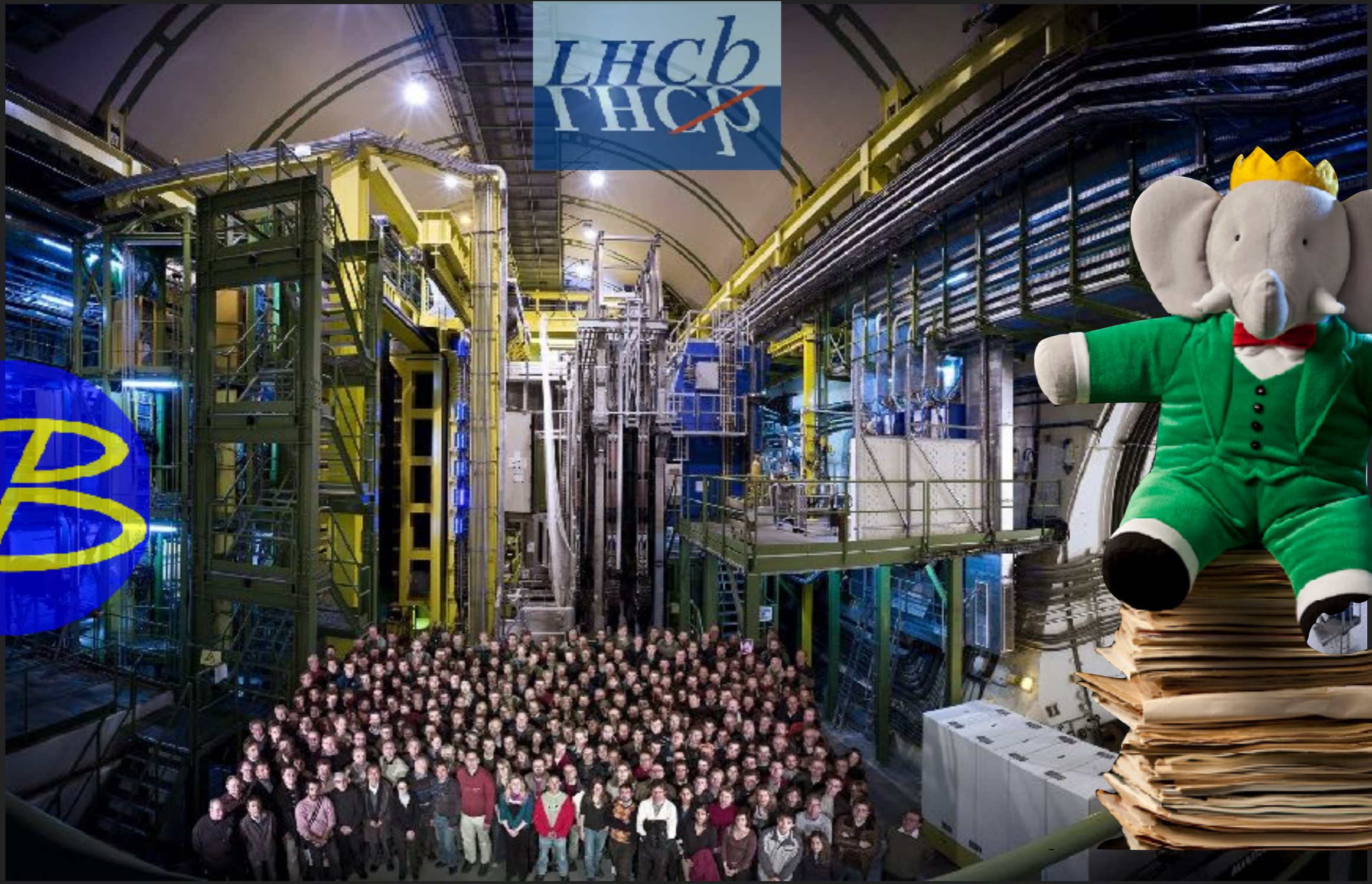






Stay tuned in the coming months for preliminary results!

# Hints of Lepton Flavor Non-Universality in B decays



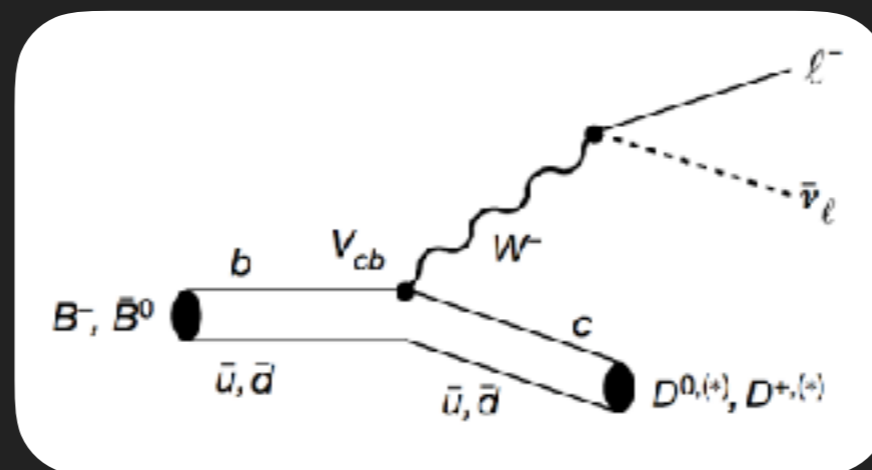
LHCb  
~~LHCb~~



## Semi-Leptonic B-Meson Decays

- Lepton Universality:  $e$ ,  $\mu$ , and  $\tau$  differ only by their masses
  - Identical coupling constants
- In semi-leptonic decays of B mesons, both  $e$  and  $\mu$  can be treated as massless [1]
  - Therefore expect identical rates and kinematics of the decay for either lepton in the final state
- The mass of the  $\tau$  must be accounted for [1]
  - $m_\tau \sim 1777 \text{ MeV} \sim 17 \times m_\mu$
  - hadronic effects
- These decays are well understood in the SM, and so can be used to probe for new phenomena

$$\mathcal{B}(\bar{B} \rightarrow D l^- \bar{\nu}_l)$$



[1] Z. Phys. C - Particles and Fields 46, 93-109 (1990)

## Semi-Leptonic B-Meson Decays

- SM predictions for the semi-leptonic B branching ratios:
  - ▶ Small suppression for  $\tau$  in the final state

$$\mathcal{R}_{D^*}^{SM} = \frac{\mathcal{B}(\bar{B} \rightarrow D^* \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^* e^- \bar{\nu}_e)} = \frac{\mathcal{B}(\bar{B} \rightarrow D^* \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^* \mu^- \bar{\nu}_\mu)} = 0.252 \pm 0.003$$

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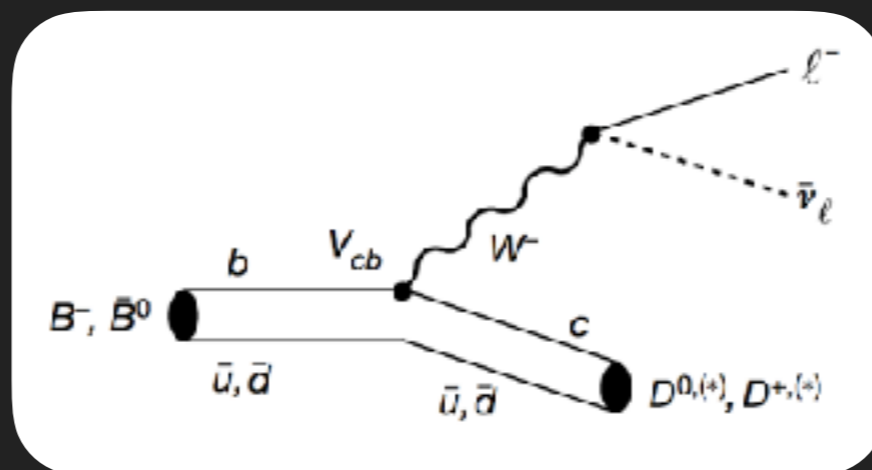
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- These ratios have been measured in  $p\bar{p}$  and  $e^+e^-$  production
  - BaBar & Belle:  $\sim 10$  GeV lepton collider data collected from 1999 to  $\sim 2010$
  - LHCb: 7-8 TeV hadron collider data collected from 2008 to 2012

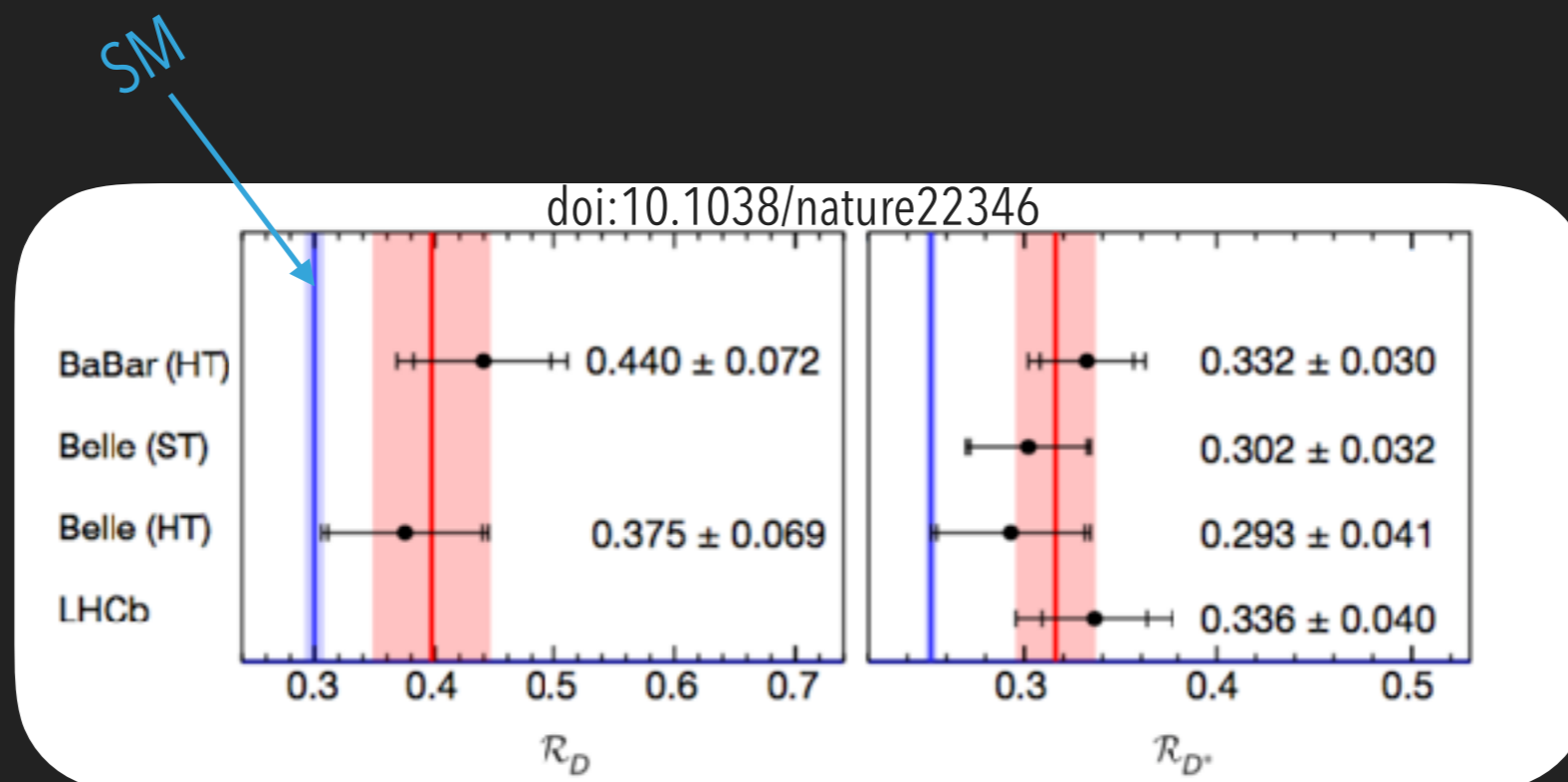
## B-Meson Measurements

- All analyses fit to  $m_{\text{miss}}^2$ ,  $E_{\ell}$ , and  $q^2$ 
  - ▶ The invariant mass squared of all undetected particles, lepton energy in the B rest frame, and invariant mass squared of the  $\ell\nu$  system
- BaBar and Belle require  $B_{\text{tag}}$ ,  $D^{(*)}$  and  $\ell$  in the final state
  - ▶ Hadronic B tagging algorithm
  - ▶ Semileptonic B tagging algorithm
- Similarly for LHCb

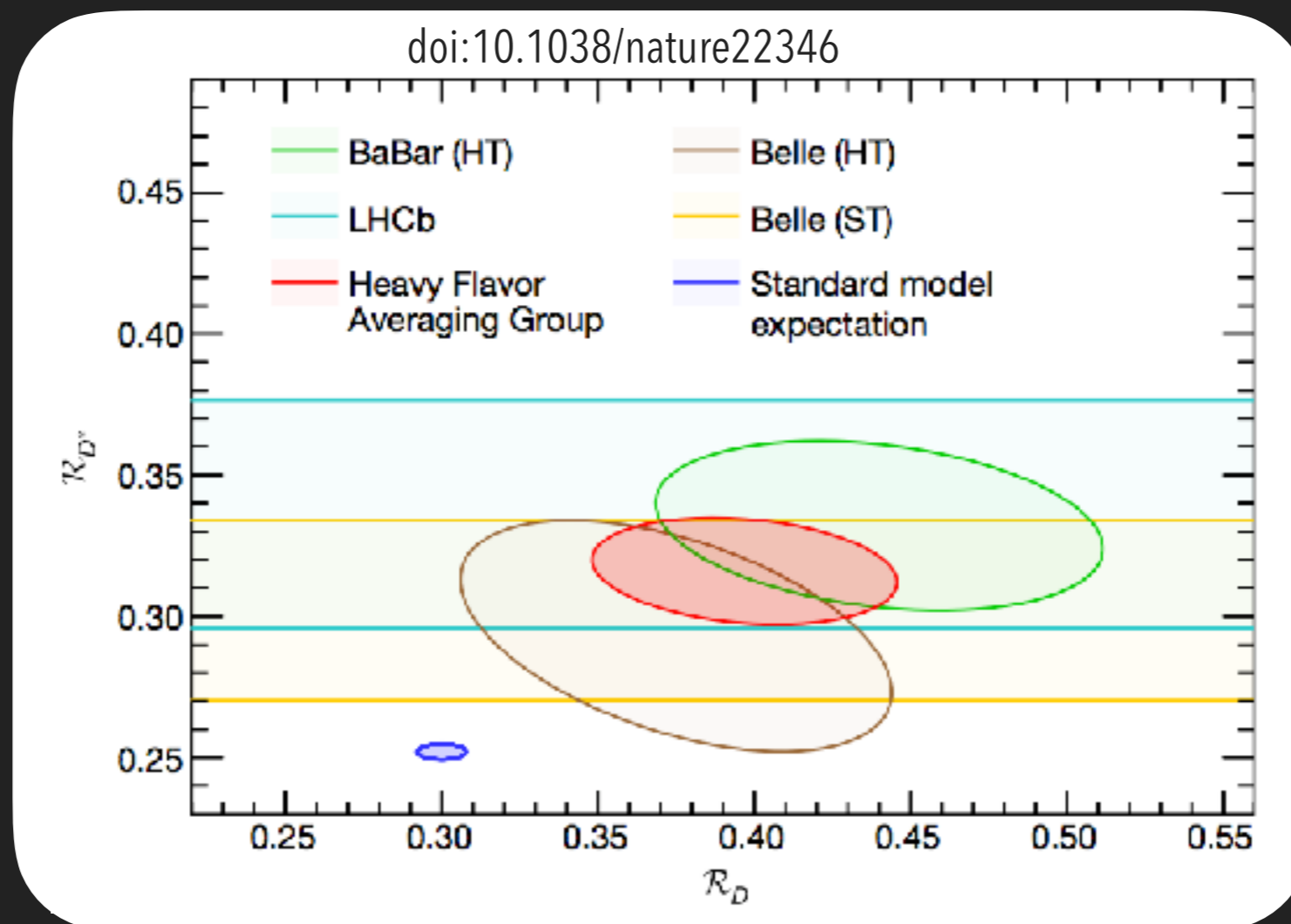


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  - HT: Hadronic B tagging algorithm
  - ST: Semileptonic B tagging algorithm
- Similarly for LHCb



# B-Meson Measurements



Accounting for correlations, the combined discrepancies from  $R_D$  and  $R_{D^*}$  gives  $\sim 4\sigma$



## B-Meson Measurements

- Similarly, can test lepton universality with a kaon in the final state

$$\mathcal{R}_K^{SM} = \frac{\mathcal{B}(\bar{B} \rightarrow K^+ \mu^- \bar{\nu}_\mu)}{\mathcal{B}(\bar{B} \rightarrow K^+ e^- \bar{\nu}_e)} \approx 1$$

- These ratios have been measured in  $p\bar{p}$  and  $e^+e^-$  production
  - ▶ BaBar, Belle & CDF had large error bars, results consistent with the SM
  - ▶ LHCb produced a better measurement: Phys. Rev. Lett. 113, 151601 (2014)

## B-Meson Measurements

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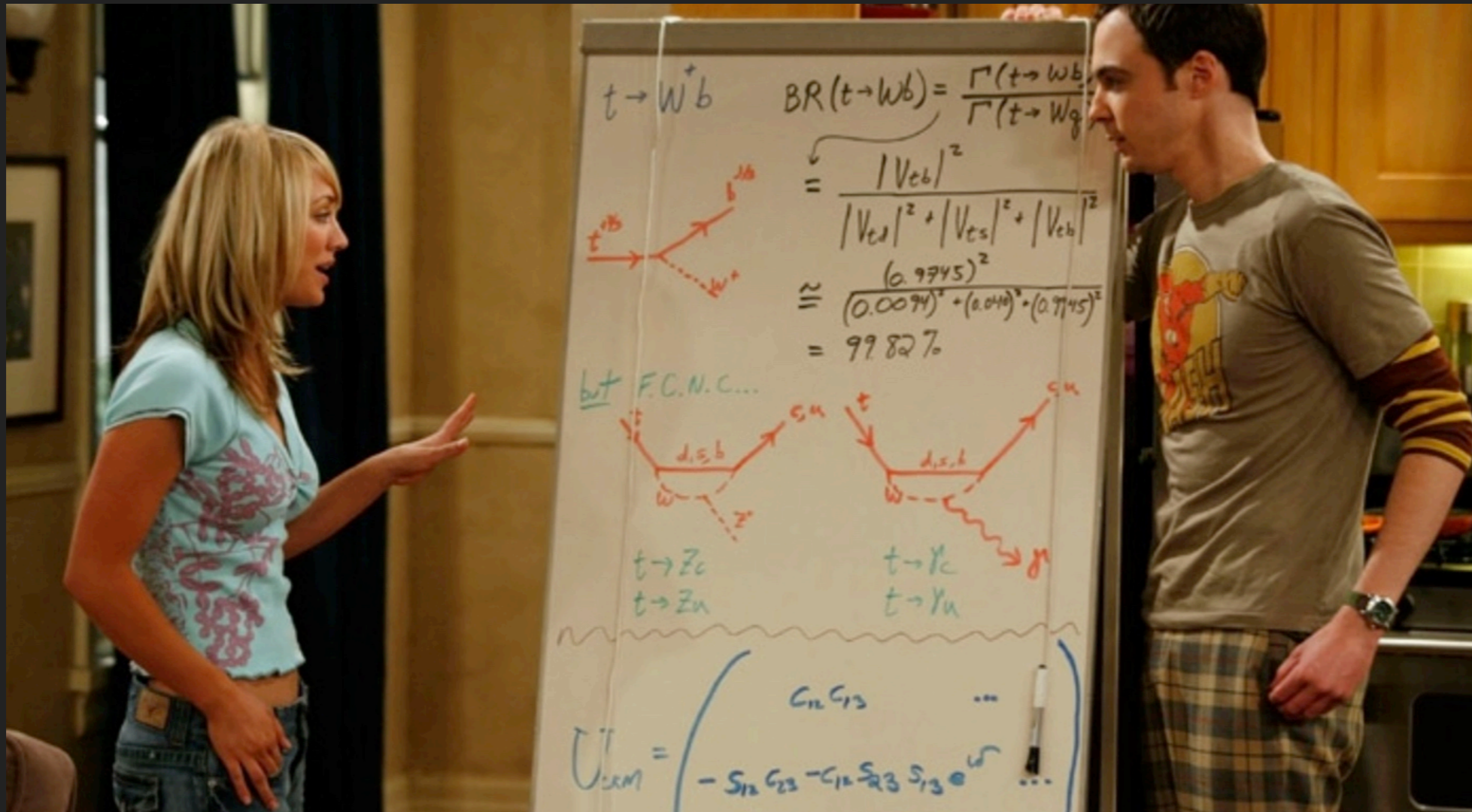
$$\mathcal{R}_K^{\text{LHCb}} = 0.745 \pm_{0.074}^{0.090} \pm 0.036$$

A  $2.6\sigma$  departure from unity

## B-Meson Measurements

- SM discrepancies in  $R_{D^{(*)}}$  from three independent experiments
  - ▶ Adds up to  $4\sigma$  departure
- SM discrepancy in  $R_K$  from LHCb
  - ▶  $2.6\sigma$  departure
- Could be seeing the effects of a new interaction that breaks lepton flavor universality
  - ▶ A new vector boson,  $W'^-$ , with different couplings for different quarks and leptons?
  - ▶ A scalar, i.e. charged Higgs,  $H^-$  ?
  - ▶ Leptoquarks?
- No conclusion yet
  - ▶ Underestimated experimental uncertainties?
  - ▶ SM predictions lacking some ordinary ingredient?
  - ▶ Awaiting Belle II and the LHCb upgrade

# Searches for Charged Lepton Flavor Violation



## Charged Lepton Flavor Violation

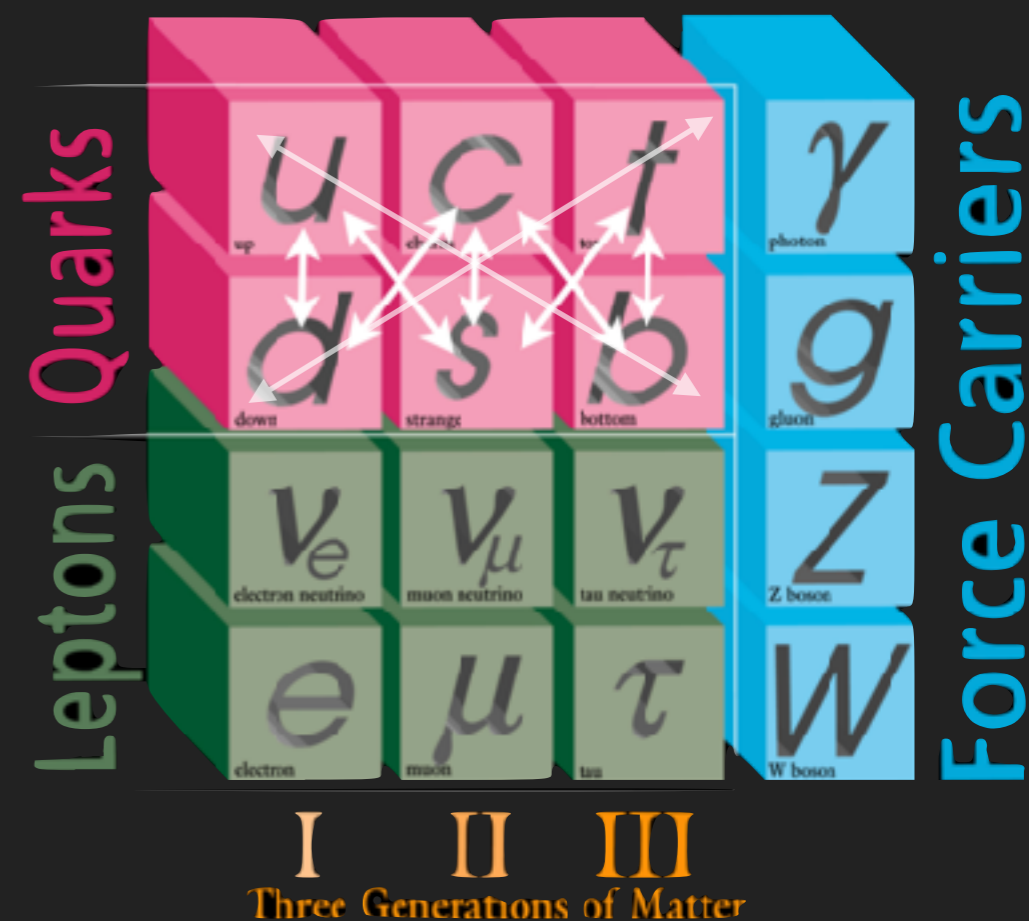
- The recent anomalies in the lepton sector certainly add to the excitement of looking for Charged Lepton Flavor Violation (CLFV)
- But these searches have always been interesting!
  - ▶ Recall the role that the early muon experiments had in piecing together the SM



# Flavor Violation in the SM

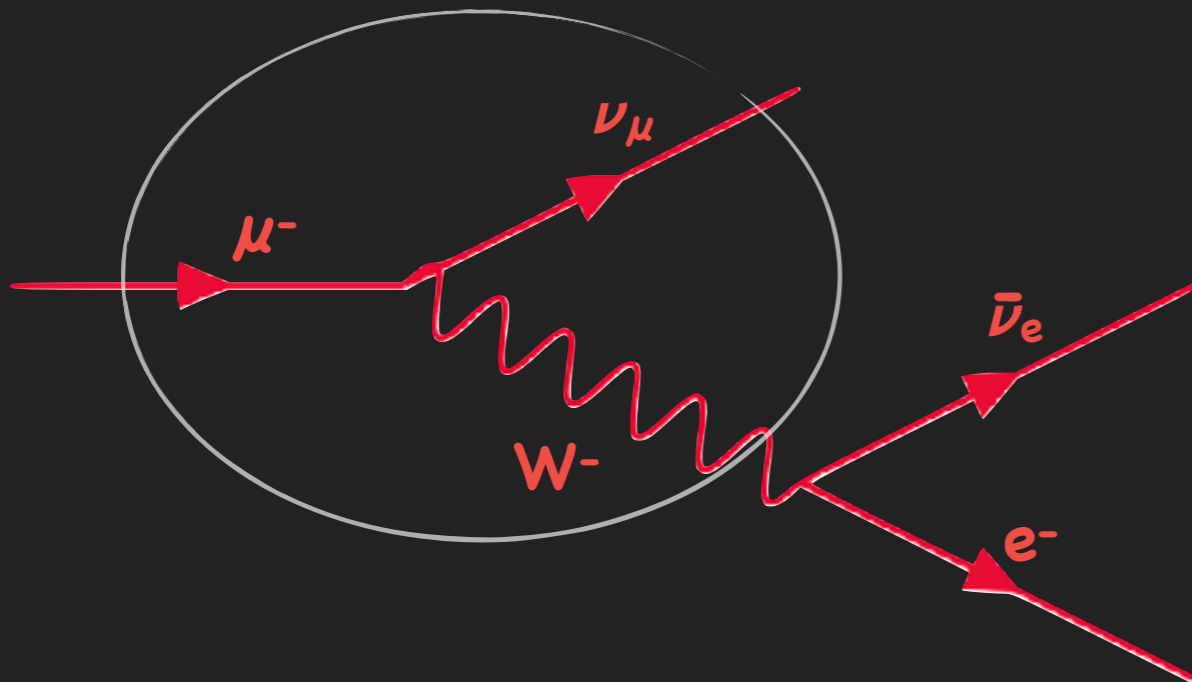
- The quarks commit Flavor Violation
  - ▶ They mix via the  $W$

## ELEMENTARY PARTICLES

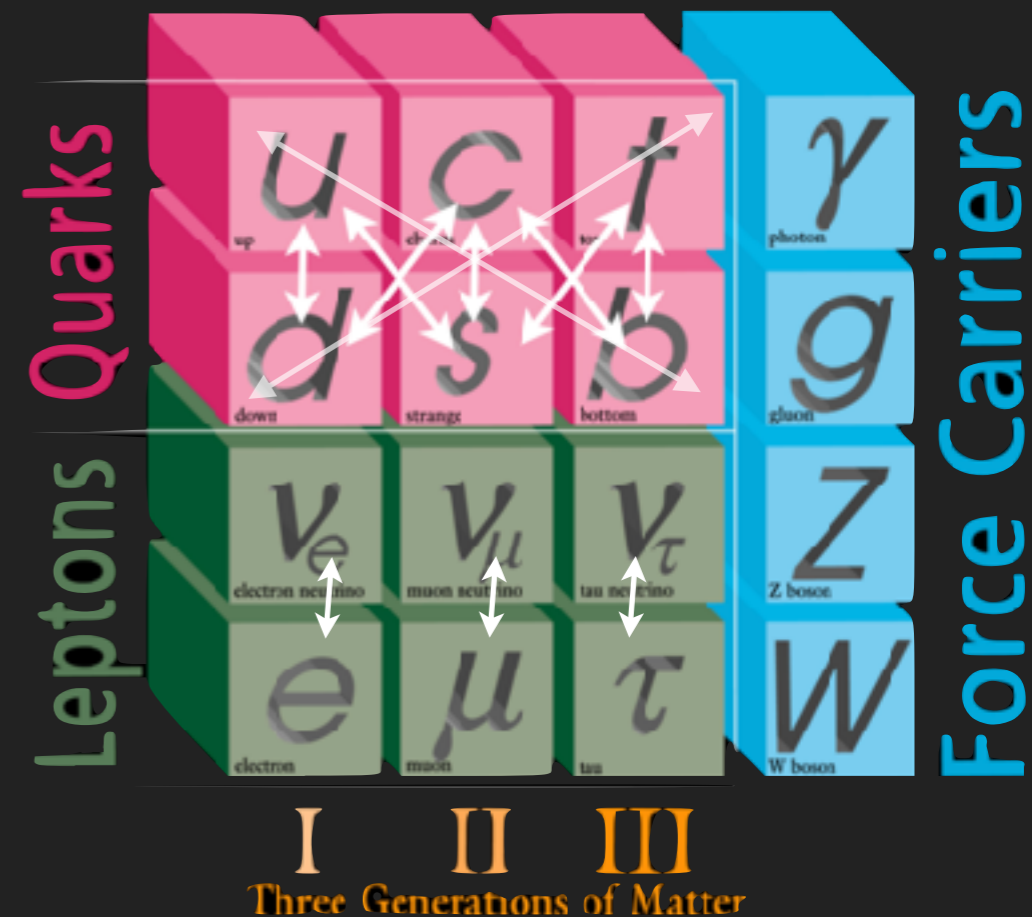


# Flavor Violation in the SM

- The quarks commit Flavor Violation
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- The neutrinos can change into their partners (and vice versa)



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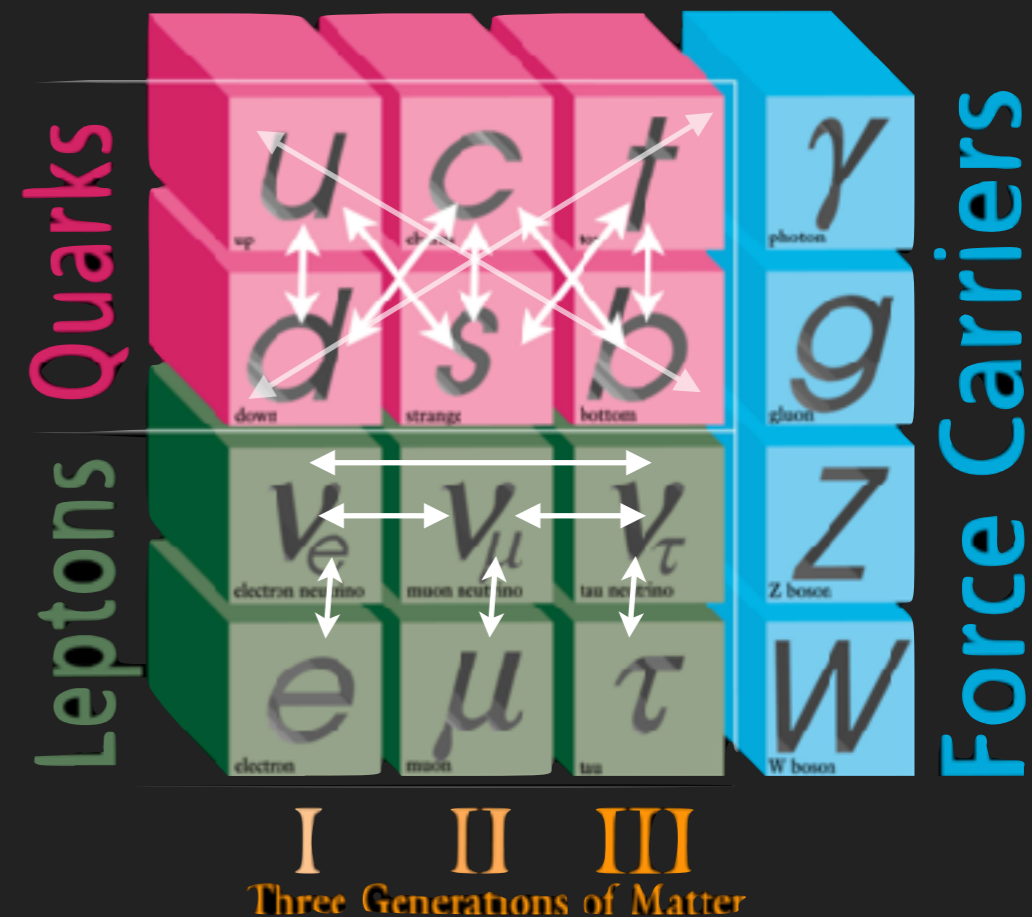


# Flavor Violation in the SM

- The quarks commit Flavor Violation
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- The neutrinos can change into their partners (and vice versa)
- And the neutrinos also mix!



## ELEMENTARY PARTICLES

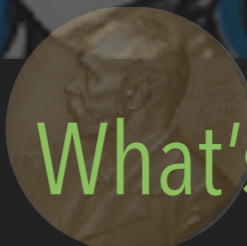
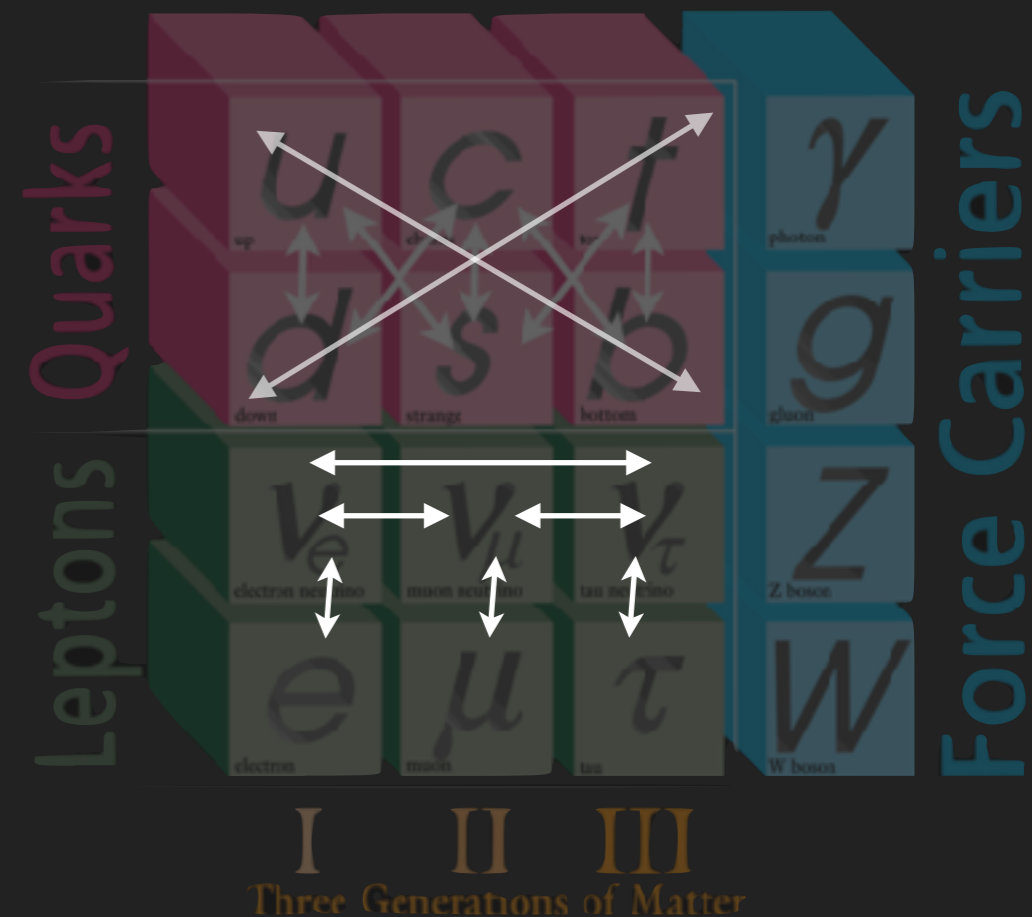




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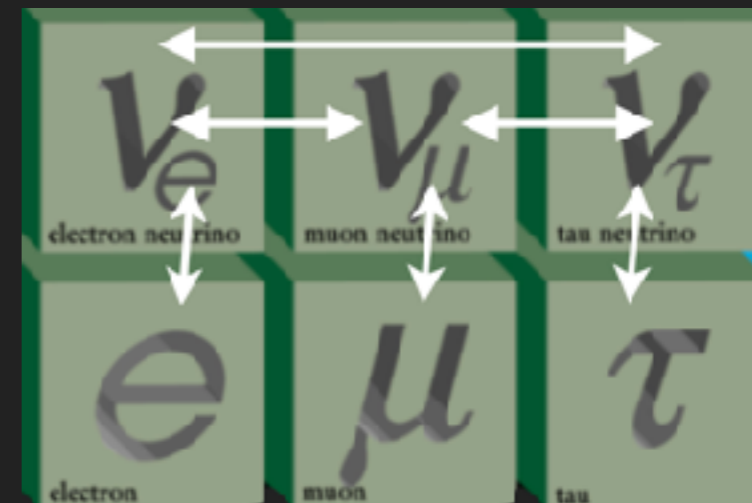
## ELEMENTARY PARTICLES



What's going on with the charged leptons?

## CLFV in the Standard Model

- All CLFV processes are dynamically suppressed in the SM
  - ▶ it's impossible to proceed through SM interactions without violating deeper conservation laws



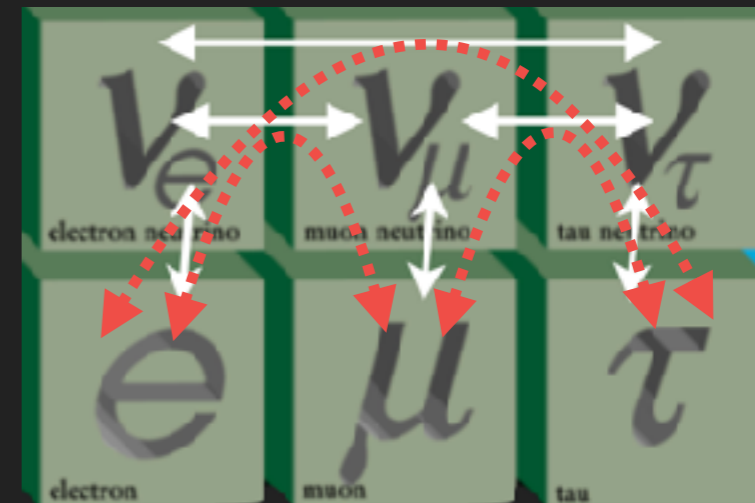
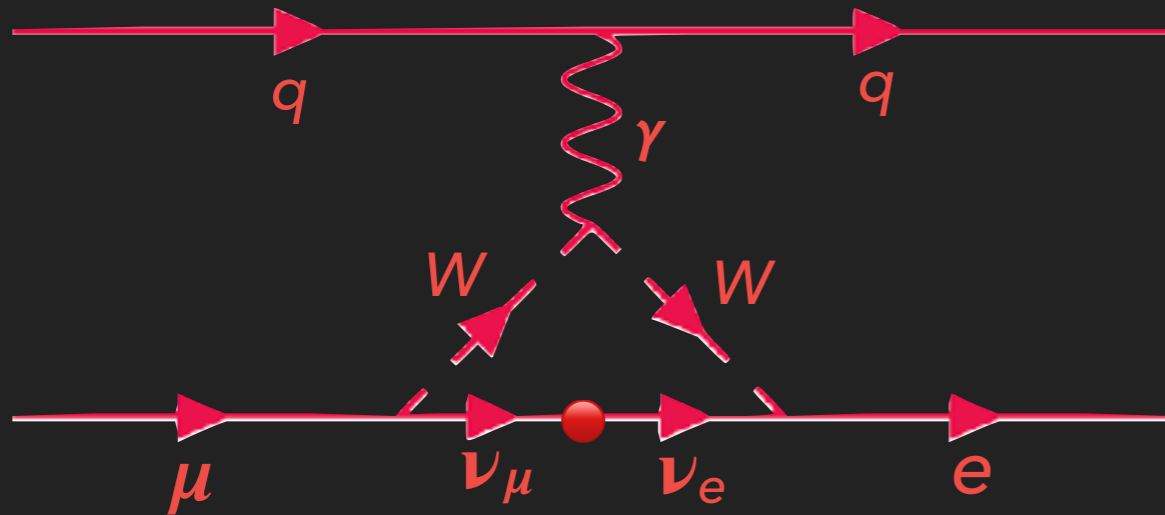
But neutrino mixing implies an encouraging fact...

# CLVF Must Occur

- Neutrino oscillations *require* CLFV on some level

$$\text{e.g. } \mathcal{B}(\mu \rightarrow e\gamma) = \frac{3\alpha}{32\pi} \left| \sum_{i=2,3} U_{\mu i}^* U_{ei} \frac{\Delta m_{il}^2}{M_W^2} \right|^2 10^{-54}$$

- But that level is tiny, because all SM CLFV processes involve loops with  $W$  and  $\nu$



Charged lepton flavor is not an exact symmetry in our universe, so there's no formal reason for new phenomena to feature it.

Furthermore, if CLFV is observed, it's physics beyond the standard model, unequivocally

## CLFV Searches

Process	Current Limit
$\tau \rightarrow \mu\eta$	BR < 6.5 E-8
$\tau \rightarrow \mu\gamma$	BR < 6.8 E-8
$\tau \rightarrow \mu\mu\mu$	BR < 3.2 E-8
$\tau \rightarrow eee$	BR < 3.6 E-8
$K_L \rightarrow e\mu$	BR < 4.7 E-12
$K^+ \rightarrow \pi^+e^-\mu^+$	BR < 1.3 E-11
$B^0 \rightarrow e\mu$	BR < 7.8 E-8
$B^+ \rightarrow K^+e\mu$	BR < 9.1 E-8
$\mu^+ \rightarrow e^+\gamma$	BR < 4.2 E-13
$\mu^+ \rightarrow e^+e^+e^-$	BR < 1.0 E-12
$\mu N \rightarrow eN$	$R_{\mu e} < 7.0 E-13$

## CLFV Searches

Process	Current Limit	Next Generation exp
$\tau \rightarrow \mu\eta$	BR < 6.5 E-8	10 <sup>-9</sup> - 10 <sup>-10</sup> (Belle II)
$\tau \rightarrow \mu\gamma$	BR < 6.8 E-8	
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$\mu^+ \rightarrow e^+\gamma$	BR < 4.2 E-13	10 <sup>-14</sup> (MEG)
$\mu^+ \rightarrow e^+e^+e^-$	BR < 1.0 E-12	10 <sup>-16</sup> (PSI)
$\mu N \rightarrow eN$	$R_{\mu e} < 7.0 E-13$	10 <sup>-17</sup> (Mu2e, COMET)

Next generation experiments will bring us a ~1-4 orders of magnitude increase in sensitivity

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Muons, with their relative ease of production, long lifetime, large mass, and simple decay, offer the best combination of access to new physics and experimental sensitivity

## Many Muon Searches Planned

$$\mu \rightarrow e\gamma$$

The oldest search

$$\mu N \rightarrow eN$$

$\mu$ -e conversion. Extremely sensitive searches to come!

$$\mu \rightarrow eee$$

Excellent complimentary to above

$$\mu^- N \rightarrow e^+ N (Z - 2)$$

*Lepton number violation* can also be searched for by the  $\mu$ -e conversion experiments!

$$\mu^- e^- \rightarrow e^- e^-$$

Likely won't be searched for until CLFV is observed  
Limits come from  $\mu \rightarrow eee$

$$\mu^+ e^- \rightarrow \mu^- e^+$$

Muonium-antimuonium conversion. Best limit is from the 90s. Nothing new planned yet! (to my knowledge)

## A Long History of CLFV Searches With Muons

- Despite nearly eight decades of searching, it's never been observed

Why continue to search?

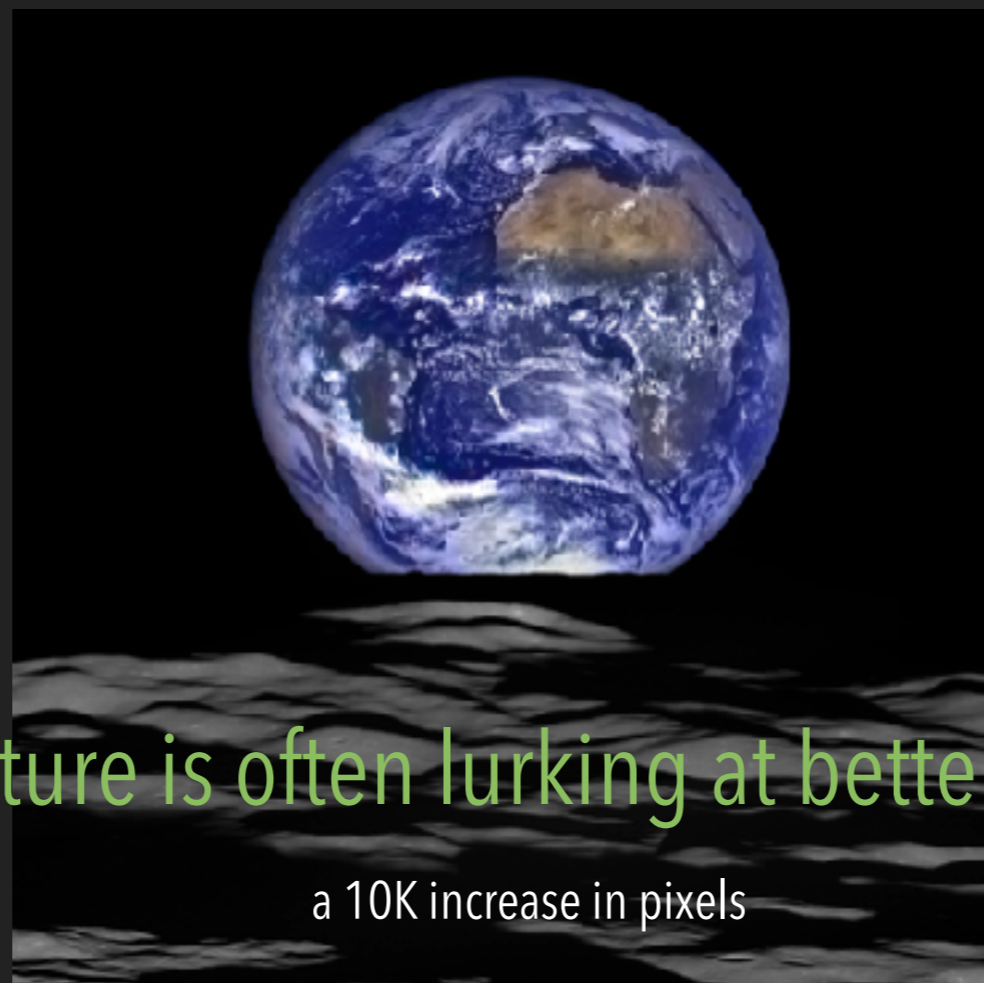


Thanks to Nina Hazen, NYC



## A 10 to 10000 Fold Leap In Sensitivity

- Leading New Physics models predict CLFV rates to be within reach
- The next generation of rare muon decay searches, with their revolutionary sensitivity, will ultimately help guide future experimental and theoretical developments in HEP



Hidden structure is often lurking at better "resolution"

a 10K increase in pixels

## A 10 to 10000 Fold Leap In Sensitivity

- Leading New Physics models predict CLFV rates to be within reach

- The next generation of rare muon decay searches, with their revolutionary sensitivity, will ultimately help guide future experimental and theoretical developments in HF

### The Adventure of Silver Blaze

From Wikipedia, the free encyclopedia

For the 1937 film, see *Silver Blaze (1937 film)*. For the 1977 film, see *Silver Blaze (1977 film)*.

"**Silver Blaze**", one of the 56 **Sherlock Holmes** short stories written by British author Sir **Arthur Conan Doyle**, is ranked "Silver Blaze" 13th in a list of his 19 favourite Sherlock Holmes stories.<sup>[1]</sup>

One of the most popular Sherlock Holmes short stories, "Silver Blaze" focuses on the disappearance of the epor on the apparent murder of its trainer. The tale is distinguished by its atmospheric **Dartmoor** setting and late-Vict plotting, hinging on the "curious incident of the dog in the night-time:"

Gregory (**Scotland Yard** detective): "Is there any other point to which you would wish to draw my attention?"

Holmes: "To the curious incident of the dog in the night-time."

Gregory: "The dog did nothing in the night-time."

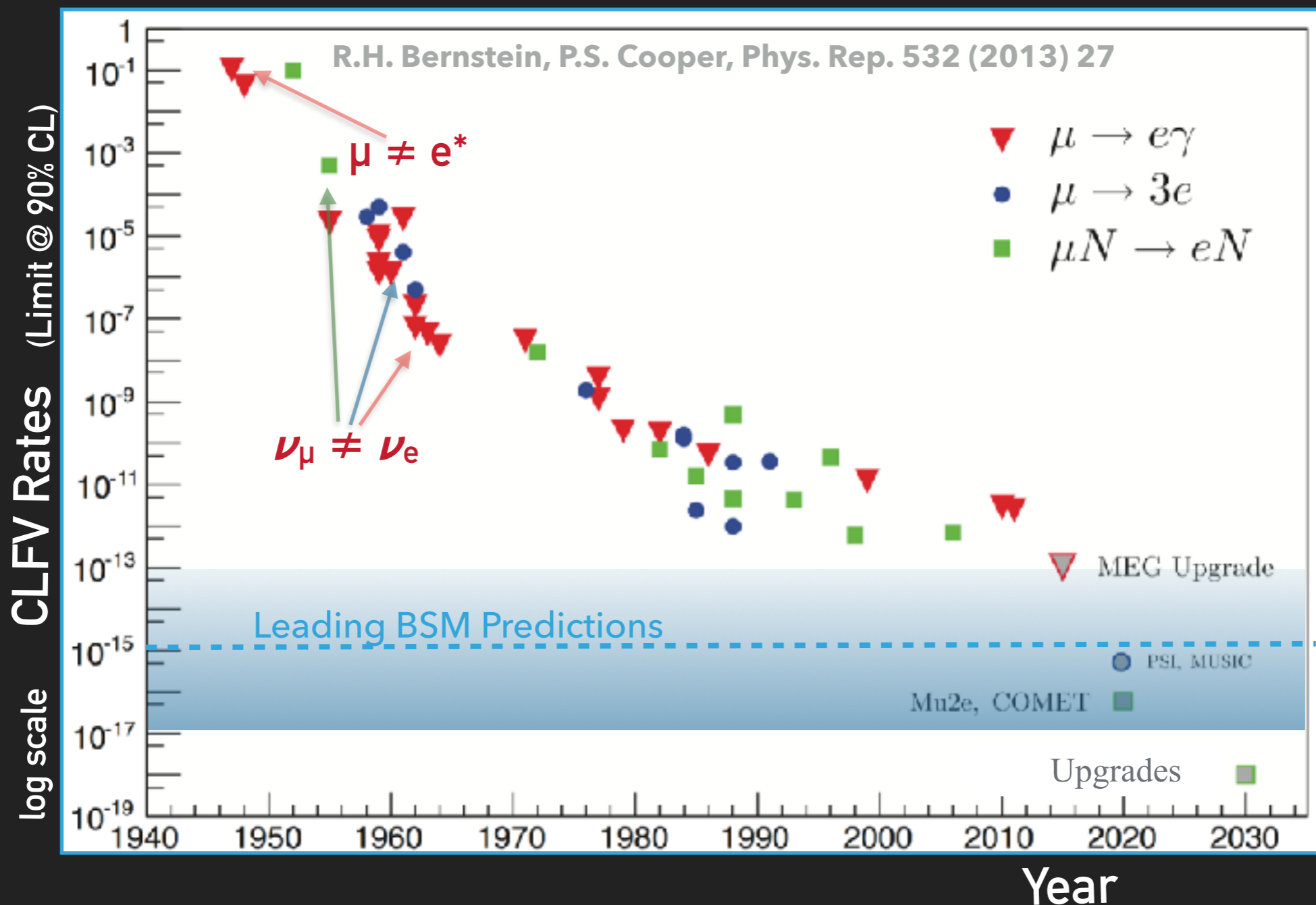
Holmes: "That was the curious incident."<sup>[2]</sup>



Hidden structure is often lurking at better "resolution"

And if it isn't, that's also interesting!

# A History of Searches for CLFV Muon Decays

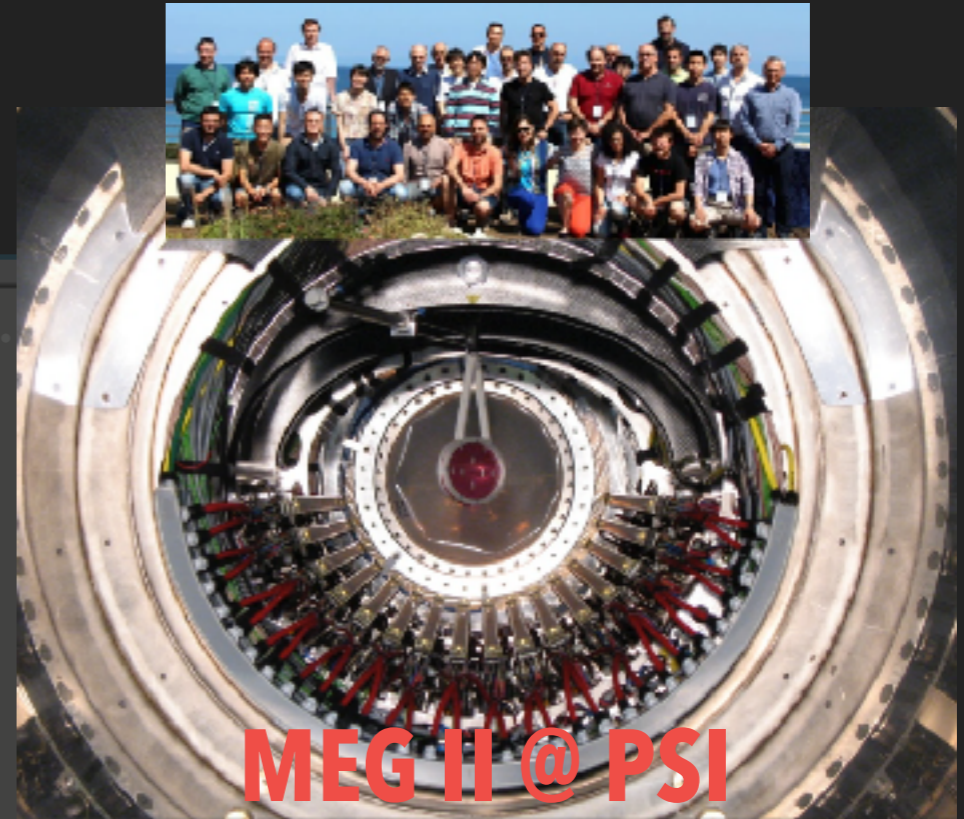


Breaking Through the Plateau... And Beyond the SM?

# The Future of Muon CLFV Searches



**Mu3e @ PSI**



**MEG II @ PSI**



**Mu2e @ FNAL**



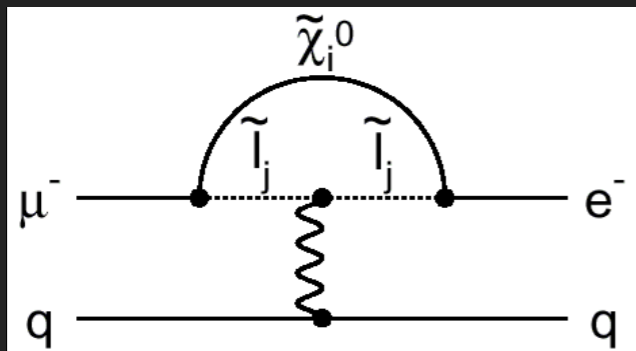
**COMET @ KEK**

Breaking Through the Plateau... And Beyond the SM?

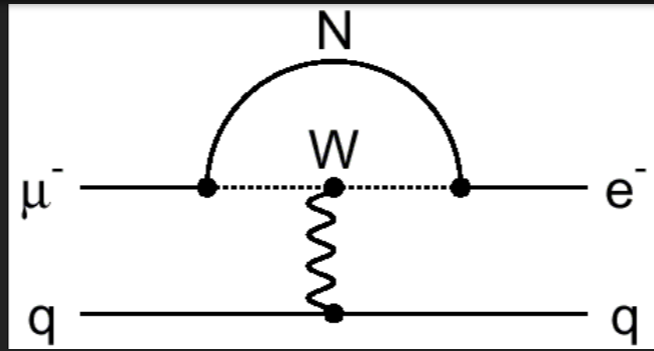
Effective CLFV Lagrangian: de Gouvea, A., and P. Vogel (2013)

$$\mathbf{L} = \frac{m_\mu}{(\kappa+1)\Lambda^2} \bar{\mu}_R \sigma_{\mu\nu} e_L F^{\mu\nu} + \frac{\kappa}{(\kappa+1)\Lambda^2} \bar{\mu}_L \gamma_\mu e_L \sum_{q=u,d} \bar{q}_L \gamma_\mu q_L$$

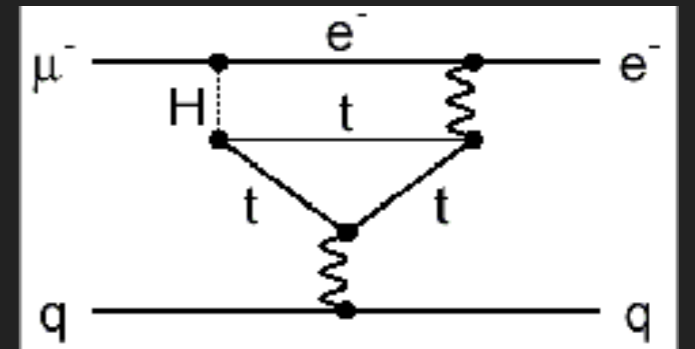
Magnetic moment type operator



Supersymmetry

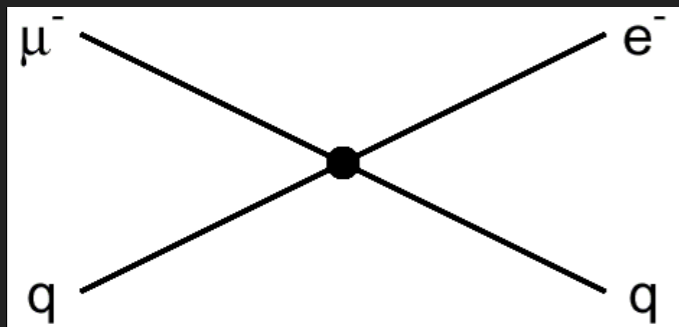


Heavy neutrinos

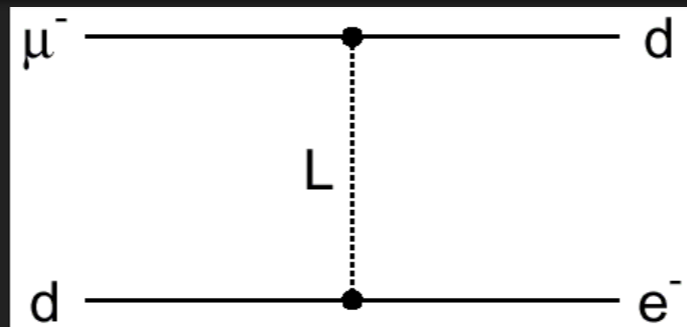


Two Higgs doublets

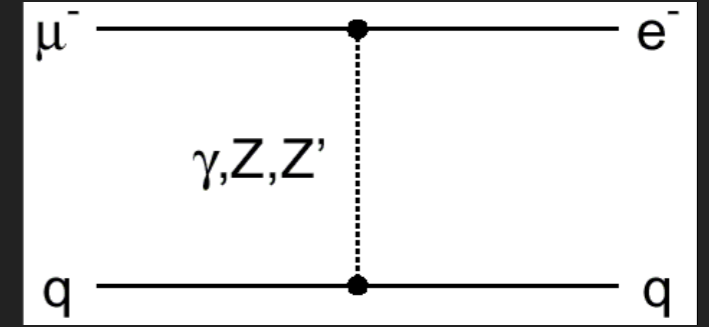
Contact term operator



Compositeness



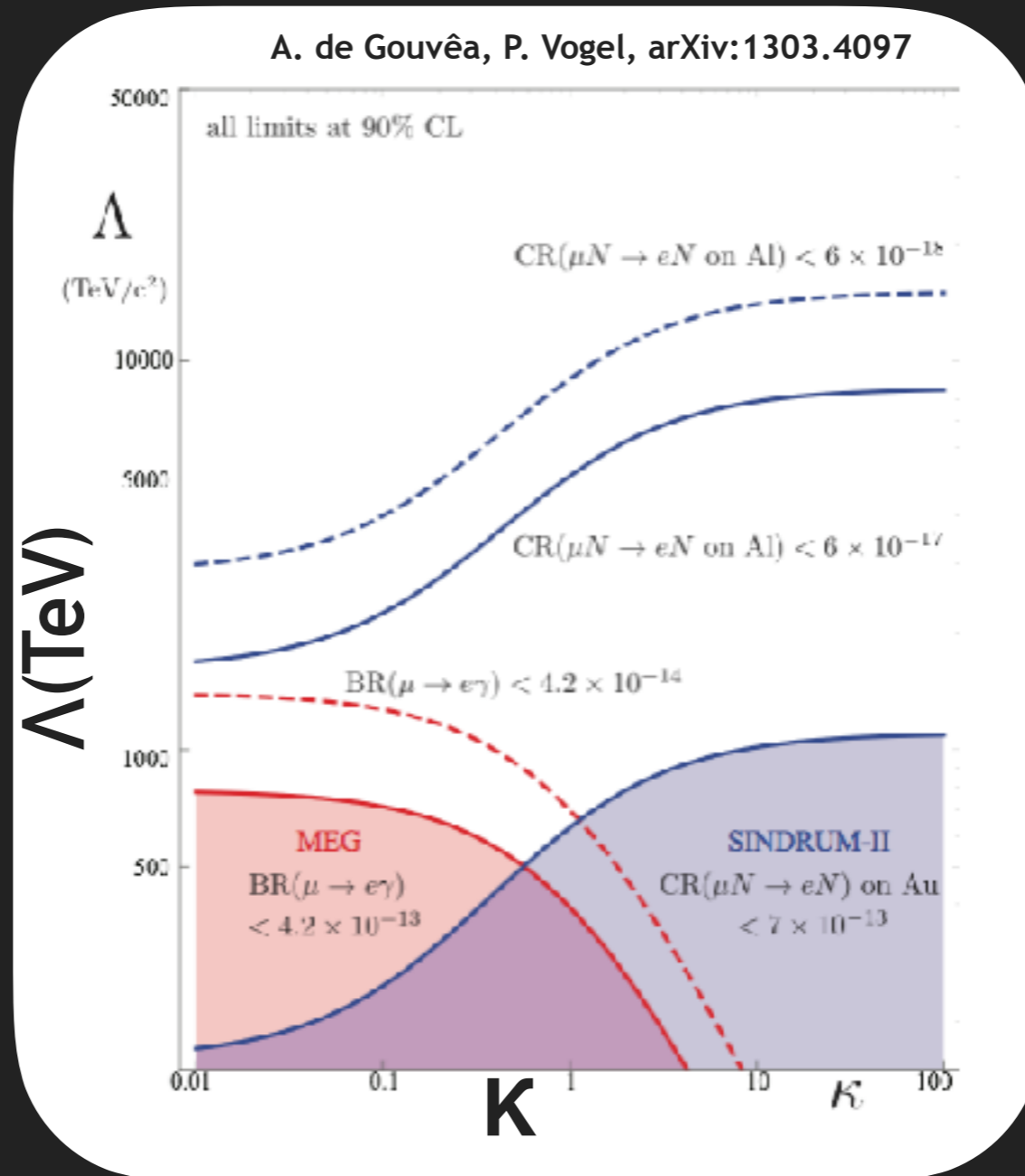
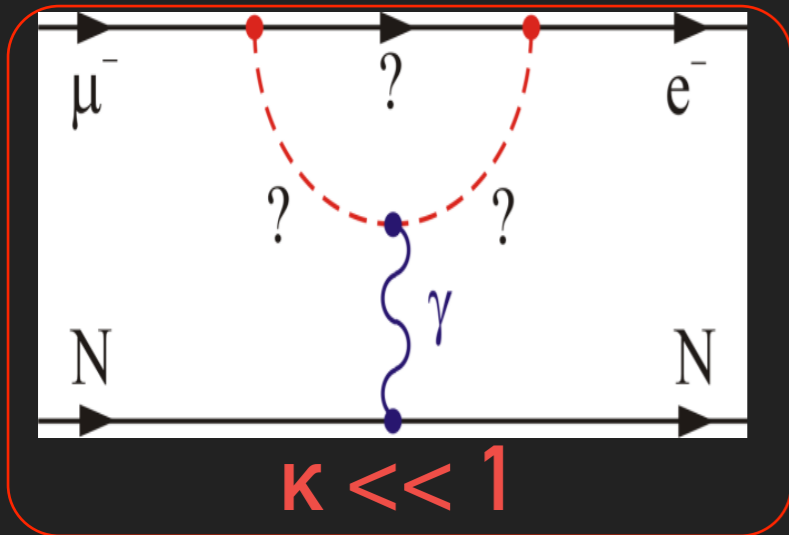
Leptoquarks



New heavy bosons / anomalous coupling

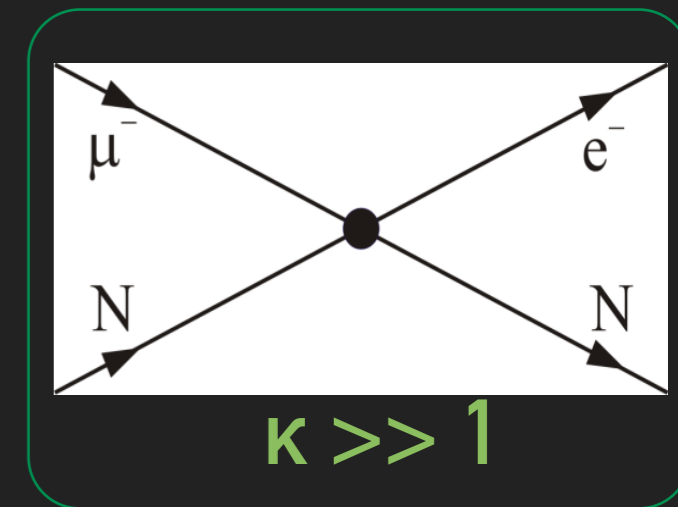
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Loop dominated

Contact dominated



# Observables and a Handful of New Physics Models

★ Vanishingly small effects

★★ Moderate, but visible effects

★★★ Large effects

GLOSSARY	
AC [10]	RH currents & U(1) flavor symmetry
RVV2 [11]	SU(3)-flavored MSSM
AKM [12]	RH currents & SU(3) family symmetry
δLL [13]	CKM-like currents
FBMSSM [14]	Flavor-blind MSSM
LHT [15]	Little Higgs with T Parity
RS [16]	Warped Extra Dimensions

	AC	RVV2	AKM	δLL	FBMSSM	LHT	RS
$D^0 - \bar{D}^0$	★★★	★	★	★	★	★★★	?
$\epsilon_K$	★	★★★	★★★	★	★	★★	★★★
$S_{\psi\psi}$	★★★	★★★	★★★	★	★	★★★	★★★
$S_{\Delta K_S}$	★★★	★★	★	★★★	★★★	★	?
$\Lambda_{CP}(B \rightarrow X_s \gamma)$	★	★	★	★★★	★★★	★	?
$A_{7,8}(B \rightarrow K^* \mu^+ \mu^-)$	★	★	★	★★★	★★★	★★	?
$\Lambda_0(B \rightarrow K^* \mu^+ \mu^-)$	★	★	★	★	★	★	?
$B \rightarrow K^{(*)} \nu \bar{\nu}$	★	★	★	★	★	★	★
$B_s \rightarrow \mu^+ \mu^-$	★★★	★★★	★★★	★★★	★★★	★	★
$K^+ \rightarrow \pi^+ \nu \bar{\nu}$	★	★	★	★	★	★★★	★★★
$K_L \rightarrow \pi^0 \nu \bar{\nu}$	★	★	★	★	★	★★★	★★★
$\mu \rightarrow e \gamma$	★★★	★★★	★★★	★★★	★★★	★★★	★★★
$\tau \rightarrow \mu \gamma$	★★★	★★★	★	★★★	★★★	★★★	★★★
$\mu + N \rightarrow e + N$	★★★	★★★	★★★	★★★	★★★	★★★	★★★
$d_n$	★★★	★★★	★★★	★★	★★★	★	★★★
$d_e$	★★★	★★★	★★	★	★★★	★	★★★
$(g-2)_\mu$	★★★	★★★	★★	★★★	★★★	★	?

Altmannshofer, Buras, et al, **Nucl.Phys.B830:17-94, 2010**

# Observables and a Handful of New Physics Models

★ Vanishingly small effects

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	AC	RVV2	AKM	δLL	FBMSSM	LHT	RS
$D^0 - \bar{D}^0$	★★★				★	★★★	?
$\epsilon_K$					★	★★	★★★
$S_{\psi\psi}$					★	★★★	★★★
$S_{e\mu}$					★	★	?
$S_{\tau\mu}$						★	?
$S_{\tau e}$						★★	?
$S_{\tau\tau}$					★	★	?
$S_{\mu\mu}$					★	★	★
$S_{\mu e}$			★	★★★	★★★	★	★
$S_{\mu\tau}$			★	★★★	★	★★★	★★★
$S_{e\tau}$	★★★	★★★	★★★	★★★	★★★	★★★	★★★
$S_{ee}$	★★★	★★★	★	★★★	★★★	★★★	★★★
$\mu \rightarrow e + N$	★★★	★★★	★★★	★★★	★★★	★★★	★★★
$d_n$	★★★	★★★	★★★	★★	★★★	★	★★★
$d_e$	★★★	★★★	★★	★	★★★	★	★★★
$(g-2)_\mu$	★★★	★★★	★★	★★★	★★★	★	?

**Check out the theory reviews:**  
 Y. Kuno, Y. Okada, 2001  
 M. Raidal et al., 2008  
 A. de Gouvêa, P. Vogel, 2013

GLOSSARY

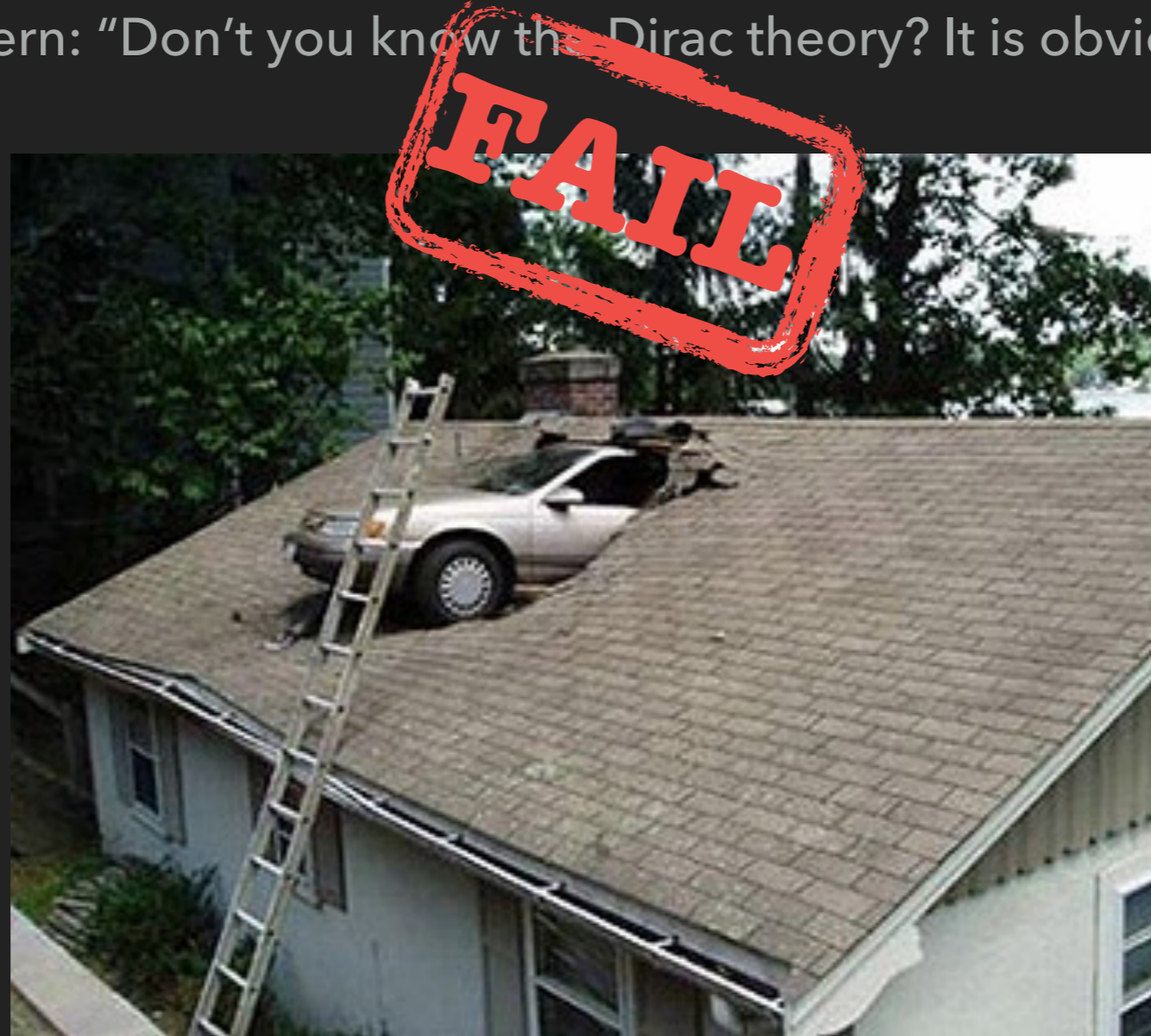
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Altmannshofer, Buras, et al. *Nucl.Phys.B830:17-94, 2010*



- Precision searches and measurements needn't be theoretically motivated
  - ▶ Recall the discovery of the muon!
  - ▶ Or, Pauli to Stern: "Don't you know the Dirac theory? It is obvious that  $g_p=2$ ."

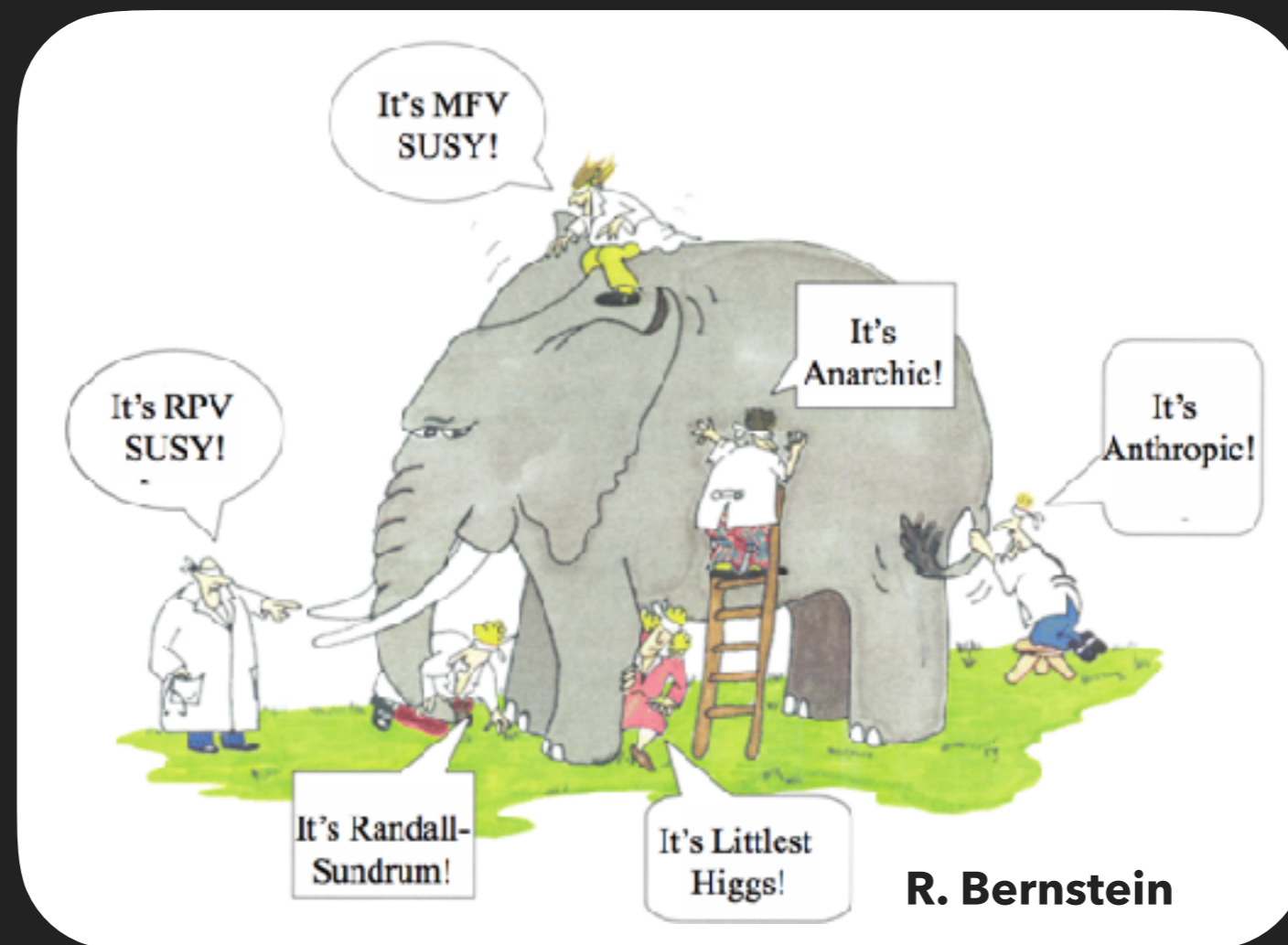
- Precision searches and measurements needn't be theoretically motivated
  - ▶ Recall the discovery of the muon!
  - ▶ Or, Pauli to Stern: "Don't you know the Dirac theory? It is obvious that  $g_p = 2$ ."



Luckily for Stern, he didn't listen

# Complementarity

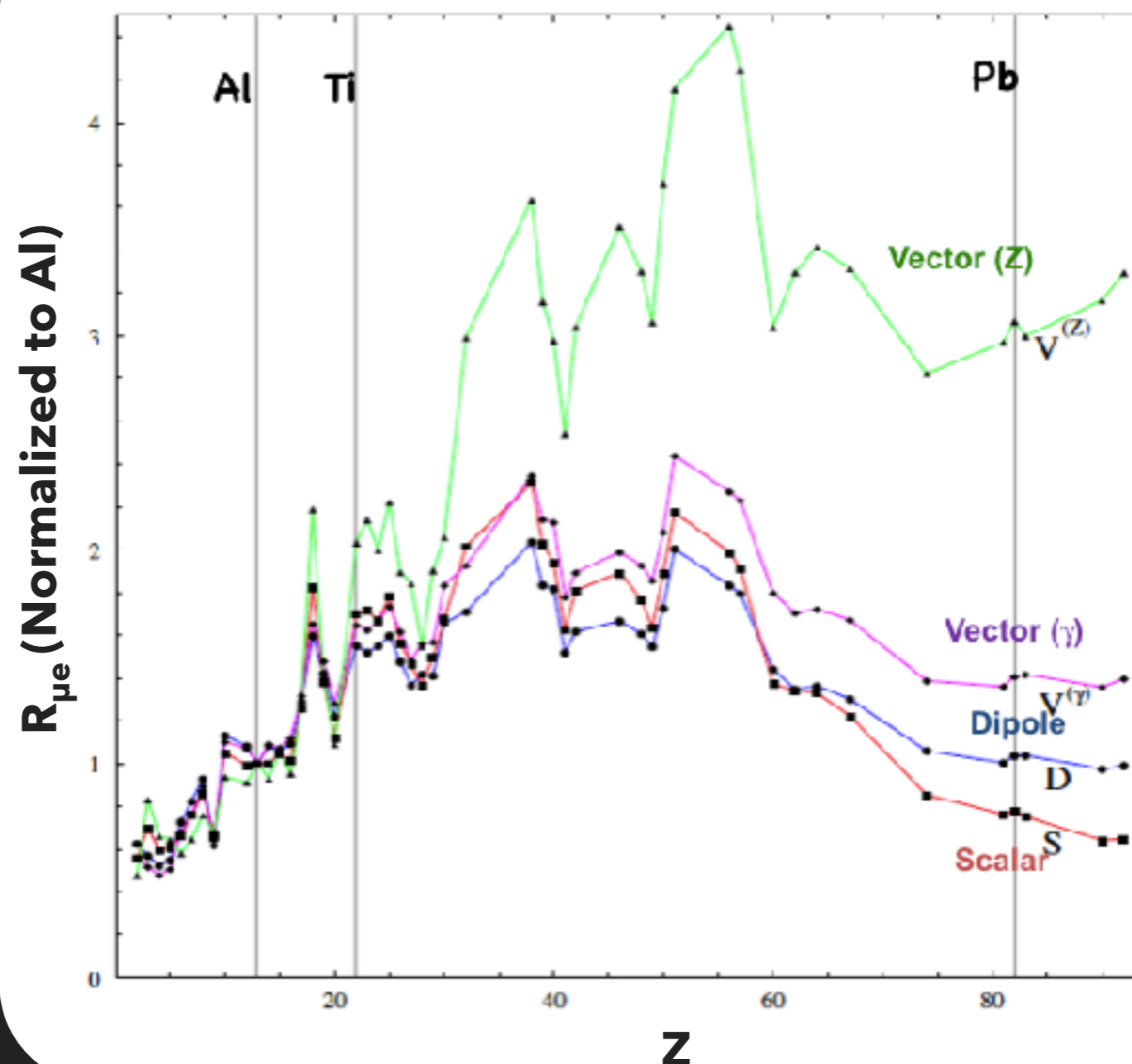
- If BSM physics is seen in CLFV searches or elsewhere, the complementarity between measurements will be crucial for discerning its nature



# Conversion Experiments With Various Nuclei

- Can begin to distinguish models by changing target material

Cirigliano, V., R. Kitano, Y. Okada, and P. Tuzon (2009), Phys. Rev. D 80, 013002, arXiv:0904.0957 [hep-ph]



Results in the years to come!



# Muons and The Great Pyramid of Giza



# Muons and The Great Pyramid of Giza

published two weeks ago:



“We have been very surprised to discover something so big—a big anomaly”

Not quite the type of anomaly that we've been talking about, but that's ok!

# The Great Pyramid of Giza

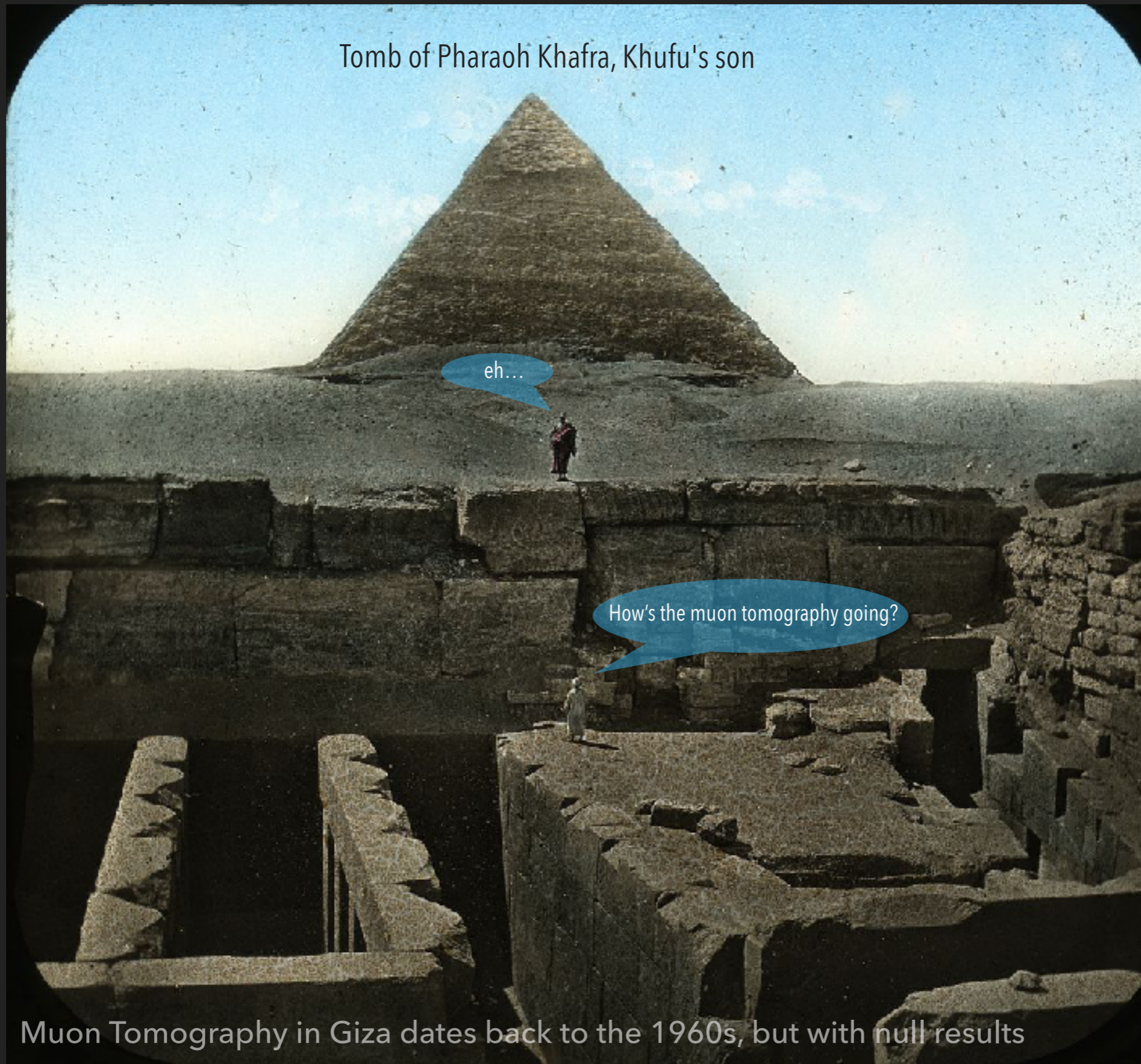
- The oldest of the six “pyramids of Giza”
  - ▶ Built more than 4.5 millennia ago, as a Mausoleum for the fourth dynasty Egyptian Pharaoh Khufu
- The oldest and only standing of the Seven Wonders of the Ancient World
- Was the world’s tallest man-made structure for nearly four millennia (135x230 m)
  - ▶ The finishing of the pyramid marked the end of an “period of experimentation”
  - ▶ Subsequently, conventions of visual art became fixed, and architecture simplified
- Has a comparatively complex internal architecture
  - ▶ But the most complete account of construction is from Herodotus, two millennia later!





## The Technique: Cosmic Ray Muon Tomography

- 10K cosmic muons per square meter per minute, at sea level
  - ▶ About 1% of pass through the Great Pyramid
  - ▶ Weeks or months of data collection
- Get muon flux and momentum angular distribution:
  - ▶ Three independent muon detection methods:
    - Nuclear emulsion films, argon based detectors, scintillating hodoscopes
- Obtain angular mass distribution from absorption and deflection
  - ▶ Radial component requires multiple detection locations
- Because it's passive, it's gaining use in a variety of applications
  - ▶ **Volcanos** -> imaging interior -> **predict eruptions**
  - ▶ **Fukushima** -> image the reactor core mass distribution -> **safe dismantling**
  - ▶ **Non proliferation** -> no artificial radiation dose on humans, nuclear warheads, or other sensitive materials -> easy to enforce -> **slow the spread of nuclear weapons**
  - ▶ And, of course, pyramids
    - Use in Giza dates back to the 1960s (*Science* **167** (3919), 832-839)



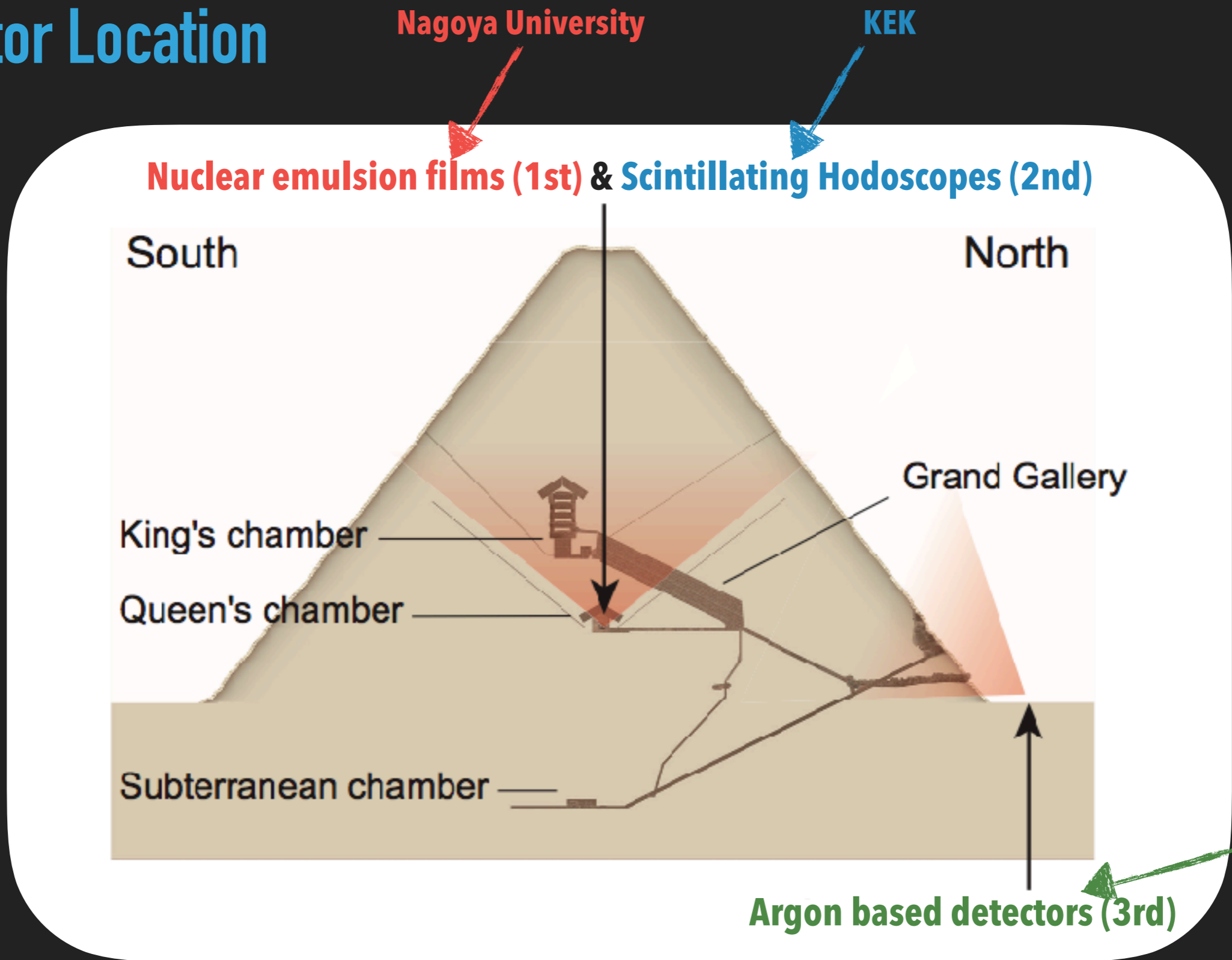
Tomb of Pharaoh Khafra, Khufu's son

eh...

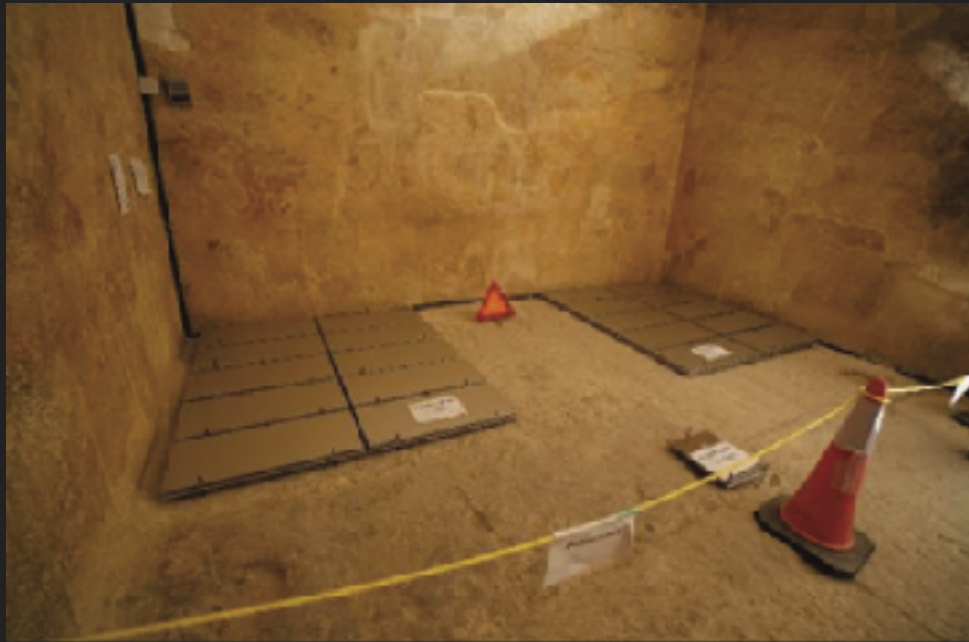
How's the muon tomography going?

Muon Tomography in Giza dates back to the 1960s, but with null results

# Detector Location



## Nagoya University Nuclear emulsion films in the Queen's chamber



- 8 m<sup>2</sup> of double sided 70 μm film
- 3D tracks: ~1 μm & 1.8 mrad
- 2 sets, 10 m separated horizontally for stereo imaging of detected structures

## KEK

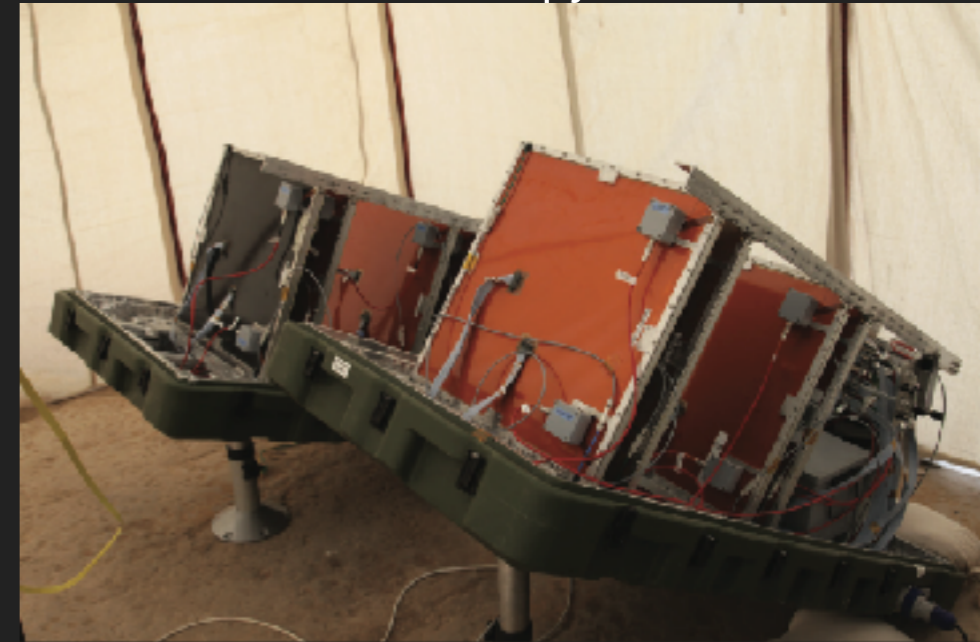
### Scintillating hodoscopes in the Queen's chamber



- 4 scintillating layers in 2 orthogonal sets
- 120, 1 cm<sup>2</sup> bars in a layer
- 2 units separated vertically by 1 m
  - ▶ trade off between angular acceptance and angular resolution

## CEA

### Argon based detectors outside the pyramid



- 4, 50x50 cm micro-pattern gas detectors
- require coincidence in 3 out of 4
- Gets solid angles of tracks
  - ▶ No mention of track resolution in paper
- No stereo imaging of structures

Nagoya University  
Nuclear emulsion films in the  
Queen's chamber



KEK  
Scintillating hodoscopes in the  
Queen's chamber



CEA  
Argon based detectors  
outside the pyramid



Subtract Monte Carlo simulations, using the pyramid's known internal structure (~1 cm resolution), from data collected since 2015

Nagoya University  
Nuclear emulsion films in the  
Queen's chamber



KEK  
Scintillating hodoscopes in the  
Queen's chamber



CEA  
Argon based detectors  
outside the pyramid



Found an excess coming from above  
the grand gallery

~8 m high × 30 m long × 1-2 m wide

Nagoya University  
Nuclear emulsion films in the  
Queen's chamber



KEK  
Scintillating hodoscopes in the  
Queen's chamber



CEA  
Argon based detectors  
outside the pyramid



Found an excess coming from above  
the grand gallery

~8 m high × 30 m long × 1-2 m wide

Saw a similar excess

KEK

Scintillating hodoscopes in the Queen's chamber

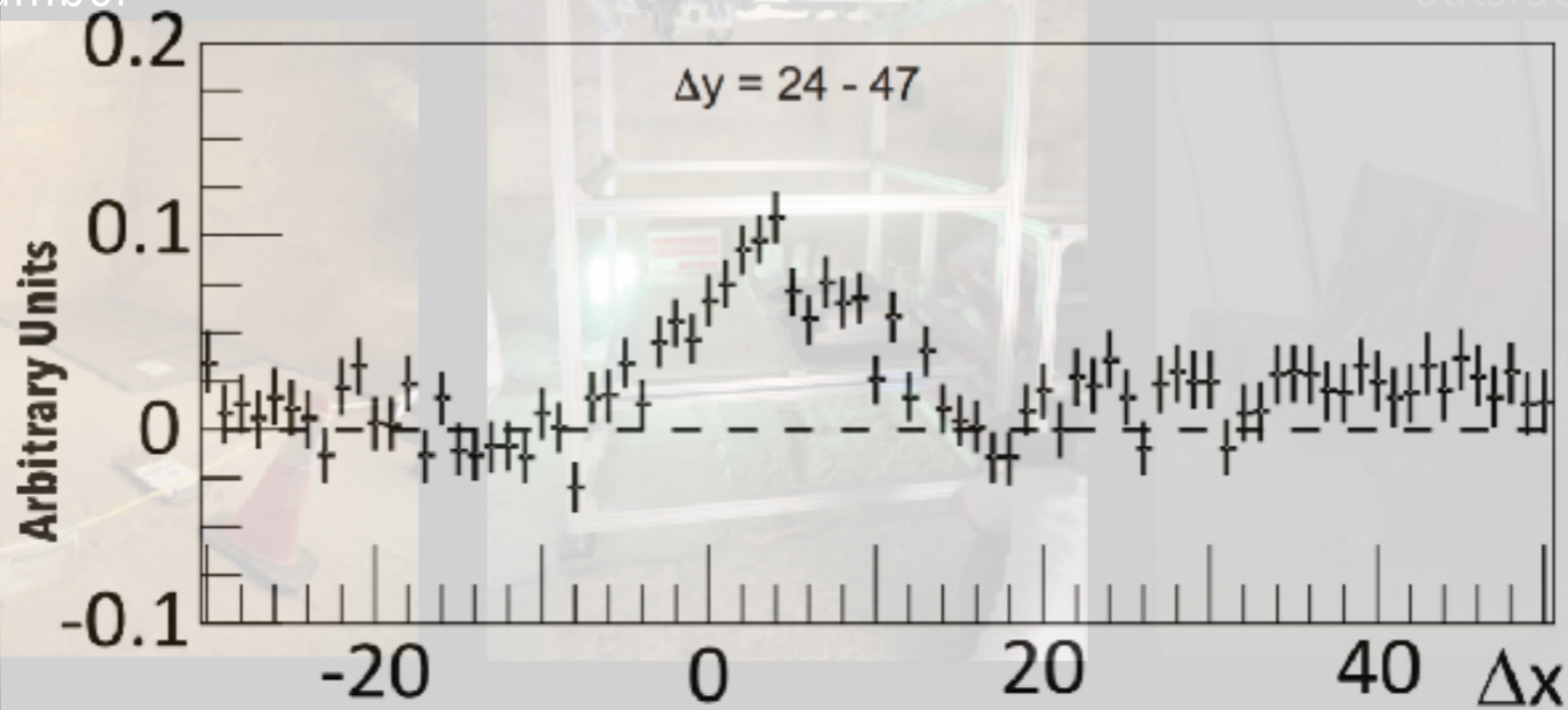
Nagoya University

Nuclear emulsion films in the Queen's chamber

CEA

Argon based detectors outside the pyramid

Muon Excess From Scintillator



$\Delta x$  is the difference between x position in top layer and bottom layer hits (separation = 1 m), in cm  
 $\theta = \arctan(100/\Delta x)$

Found an excess coming from above the grand gallery

~8 m high x 30 m long x 1-2 m wide

Saw a similar excess



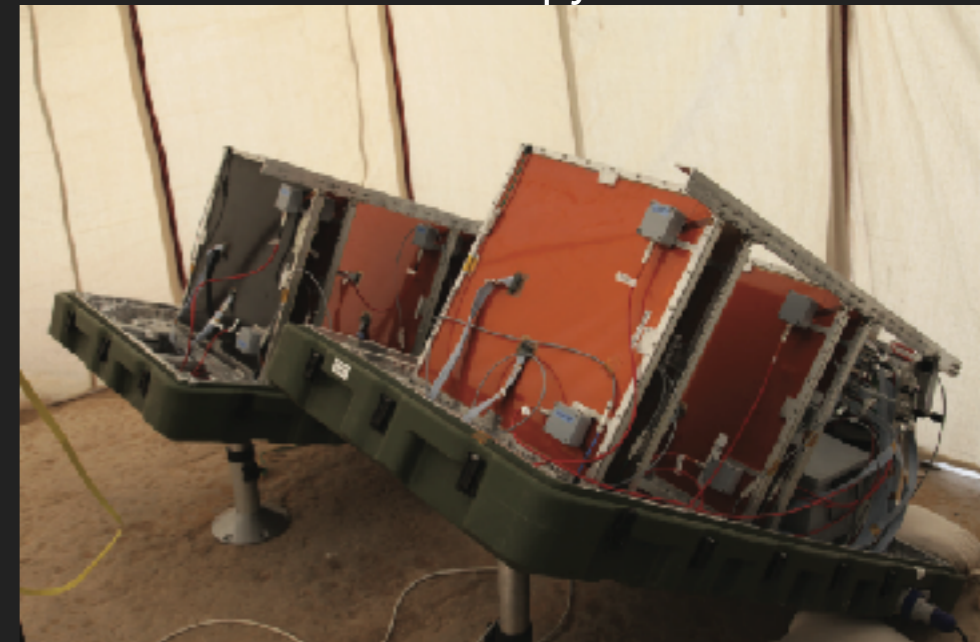
Nagoya University  
Nuclear emulsion films in the  
Queen's chamber



KEK  
Scintillating hodoscopes in the  
Queen's chamber



CEA  
Argon based detectors  
outside the pyramid



Found an excess coming from above  
the grand gallery

Saw the same excess, projected  
onto a different plane

Saw a similar excess

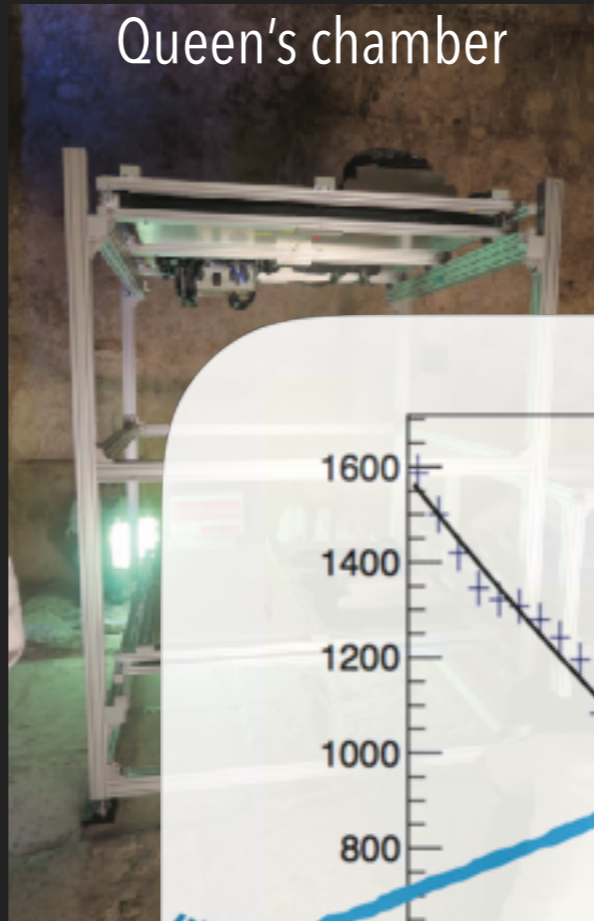
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KEK

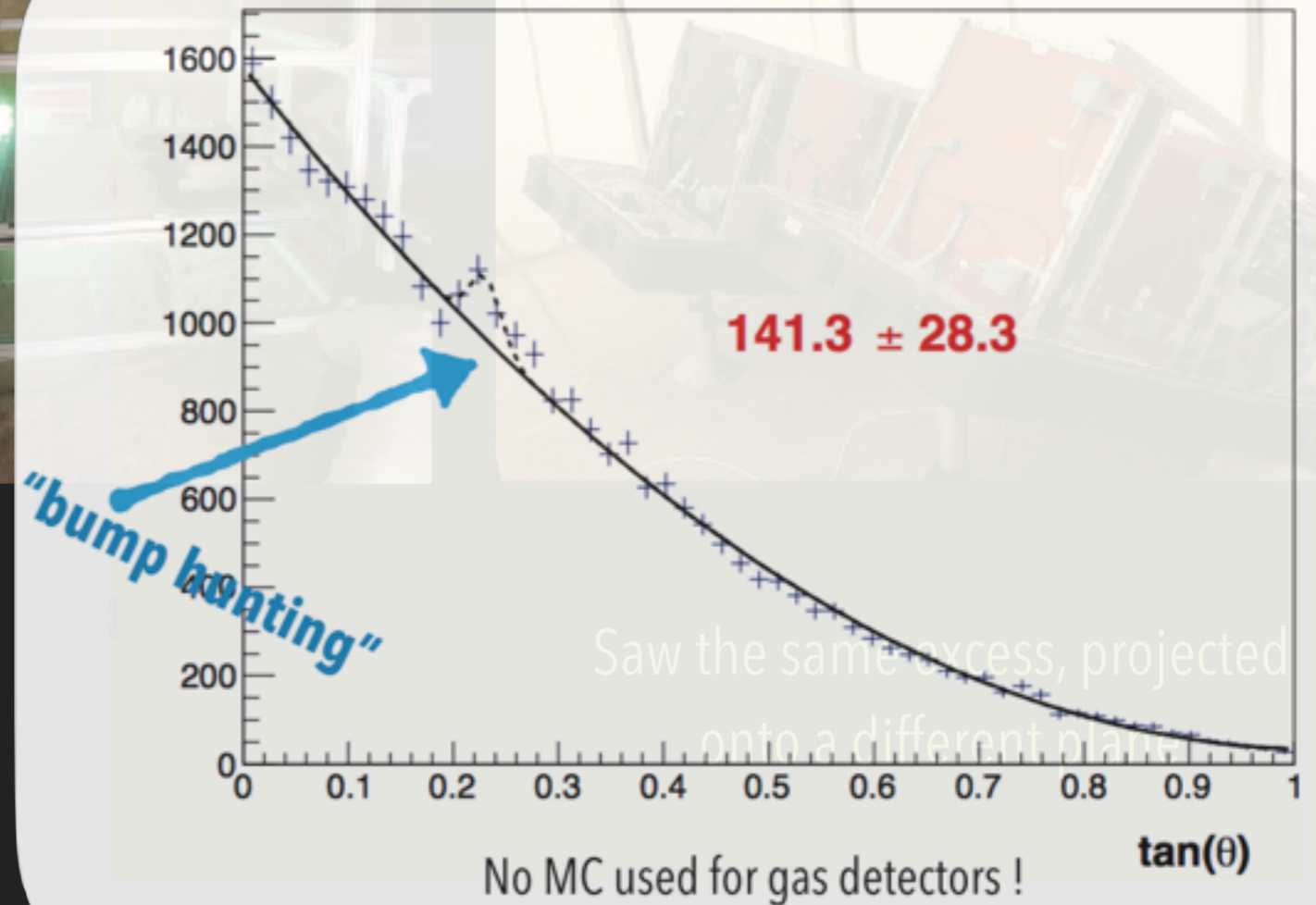
Scintillating hodoscopes in the  
Queen's chamber



CEA

Argon based detectors  
outside the pyramid

Muons Gas Detectors



Saw a similar excess

Nagoya University  
Nuclear emulsion films in the  
Queen's chamber

KEK  
Scintillating hodoscopes in the  
Queen's chamber

CEA  
Argon based detectors  
outside the pyramid

Together, a  $10\sigma$  signal for a previously unknown  
"void"  $\sim 8$  m high  $\times$  30 m long  $\times$  1-2 m wide

Found an excess coming from above  
the grand gallery

Saw a similar excess, projected  
onto a different plane

Saw a similar excess



# The Archeological Significance

- We've known about "voids" in the design of the pyramids for two decades
  - ▶ Thought to relieve pressure on chambers below
- However, the newly discovered void is particularly large and mimics the Grand Gallery
  - ▶ It could be another steeply slanted passage
    - ▶ If the great gallery ever contained anything, before being plundered, this could too!
  - ▶ Or, it could just have an engineering purpose
    - ▶ Could shed light on construction details
- There is debate among egyptologists regarding the significance of the find
  - ▶ Co-director of ScanPyramids: "We are sure there is a void, now let us continue our research"
    - ▶ It's too early to conclude anything!
- Next step might be to get drones in to explore the cavity

# Muons

- ~~A few nice properties~~
- ~~A historical perspective~~
- ~~Anomalies and Future Investigations~~
  - ▶ ~~The Proton Radius Puzzle~~
  - ▶ ~~The Muon anomalous magnetic moment~~
  - ▶ ~~Hints of Lepton Flavor Non-Universality in B decays~~
  - ▶ ~~Searches for Charged Lepton Flavor Violation~~
  - ▶ ~~Extra: Muons and The Great Pyramid of Giza~~

**Thank you!**