

$$\mathcal{L}_{\phi a} \hat{\phi} = - \vec{\nabla} \times \vec{M}_a = \frac{\partial P_{\phi a}}{\partial t} \hat{\phi}$$