

$$\vec{M}_{\phi a} = g_{a\gamma\gamma} \sqrt{\frac{\epsilon_0}{\mu_0}} \frac{r}{2} B_0 \frac{\partial a}{\partial t} \hat{\phi} = -\frac{1}{\mu_0 \mu_r} \vec{B}_a \text{eff}$$