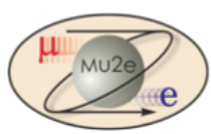


Mu2e → Mu2e-II
Recent Progress on Mu2e-II Proton Beamline
Studies

David Neuffer

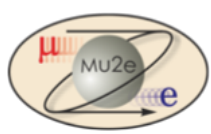
August 2018



Outline



- **PIP-II and mu2e-II**
 - Can PIP – II beam be injected into similar mu2e detector?
 - 8 GeV p \rightarrow 0.8 H⁻
 - ~ 8 kW \rightarrow ~100 kW
- **mu2e-II challenges**
 - lower energy p-beam injection
 - more beam power on target
- **H⁻ stripping**
 - foil heating
- **Transport into target through production solenoid**
 - requires changes from mu2e baseline
- **Extinction options**



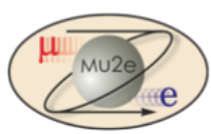
PIP-II Status and Goals



➤ **On trajectory toward construction –completion in 2026**

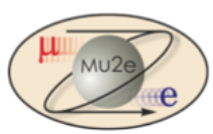
- **CD-1 → CD-2/3a in spring 201**
- **The Major Fermilab Accelerator Project**

Performance Parameter	Current	PIP-II	
Linac Beam Energy	400	800	MeV
Linac Beam Current	25	2	mA
Linac Bunch frequency	201.25	162.5	MHz
Linac Beam Power to Booster	4	17	kW
Linac Upgrade potential		1.6 MW CW	
Mu2e Upgrade Potential (800 MeV)		>100	kW
Booster Protons per Pulse	4.3×10^{12}	6.5×10^{12}	
Booster Pulse Repetition Rate	15	20	Hz
Booster Beam Power @ 8 GeV	80	166	kW
Beam Power to 8 GeV Program (max)	32	83	kW
Main Injector Protons per Pulse	4.9×10^{13}	7.5×10^{13}	
Main Injector Cycle Time @ 60-120 GeV	1.33*	0.7-1.2	sec
LBNF Beam Power @ 60-120 GeV	0.7*	1.0-1.2	MW
LBNF Upgrade Potential @ 60-120 GeV	NA	>2.0-2.4	MW



PIP-II and Mu2e-II

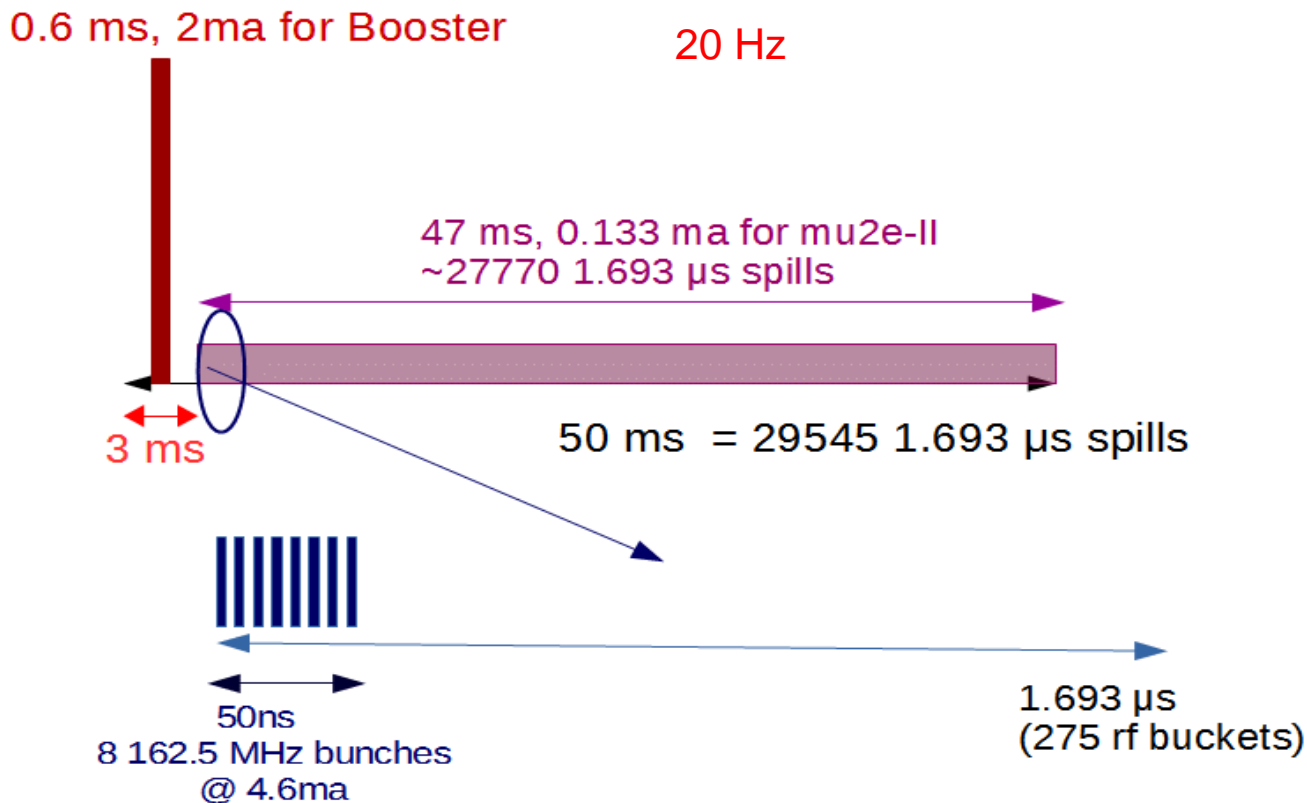
- PIP-II front end can produce arbitrary bunch structures with:
 - High beam quality !
 - $\epsilon_{T, N} \cong 0.3 \text{ mm-mr}$; $\epsilon_{L, N} \sim 1.1 \text{ keV-ns}$ ($0.004 \text{ ns} \times 0.275 \text{ MeV}$)
 - Peak current $\leq 5 \text{ mA}$
 - Can deliver **800-MeV protons** to a second generation Mu2e
 - while providing beam to Booster/MI/Dune
- **For Mu2e-II**
 - Use PIP-II (800 MeV) as beam source at up to $\sim 0.1 \text{ MW}$
 - similar beam pattern as used for Mu2e
 - $\sim 100\text{ns}$ beam on / $1.7\mu\text{s}$ cycle
 - Reuse as much as possible of the baseline Mu2e experiment
 - Follow similar experimental scenario
 - Improve **if possible**

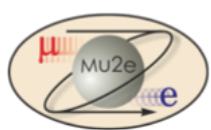


PIP-II and Mu2e-II beam



- Possible beam structure (matched to Mu2e)
 - 162.5 MHz chopped beam ($\sim 1.76 \times 10^8$ /bunch @ 4.6ma)
 - Beam pulse length: ~ 50 nsec (8 bunches) 1.4×10^9 pulse
 - Mu2e cycle: $1.693 \mu\text{sec}$
 - Three-year run achieves $> \sim$ single event sensitivity of 2×10^{-18}

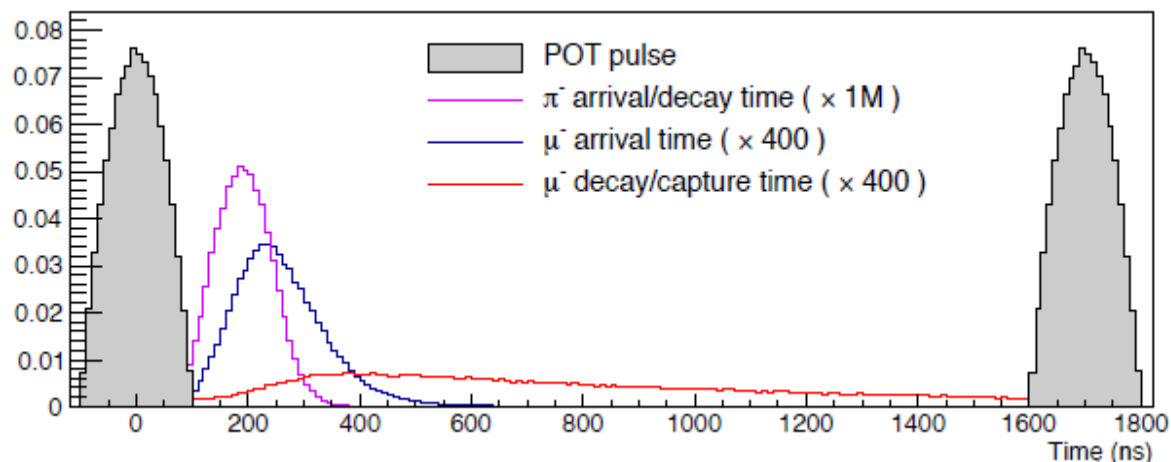




mu2e → mu2e-II



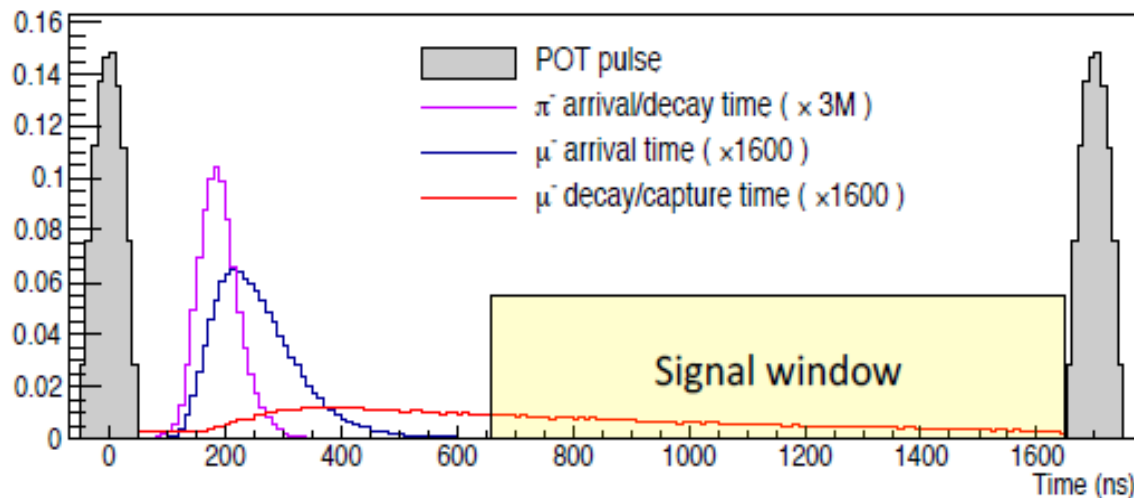
- mu2e → mu2e-II
 - shorter pulses
- timing comparison
 - K. Knoepfel et al.

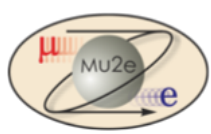


How the backgrounds change

Category	Source	Events	
		Current	PX (AI)
Intrinsic	μ decay in orbit	0.22	2.14
	Radiative μ capture	< 0.01	< 0.01
Late-arriving	Radiative π capture	0.03	0.04
	Beam electrons	< 0.01	< 0.01
	μ decay in flight	0.01	0.01
	π decay in flight	< 0.01	< 0.01
Miscellaneous	Antiproton	0.10	—
	Cosmic ray	0.05	0.16
	Pat. Recognition Errors	< 0.01	< 0.01
Total Background		0.41	2.36

Dominant background by far is DID for PX (AI)



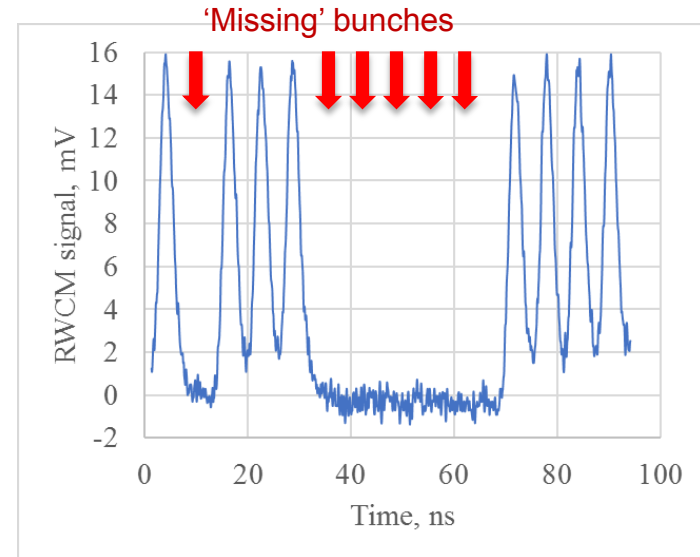


Bunch to Bunch extinction



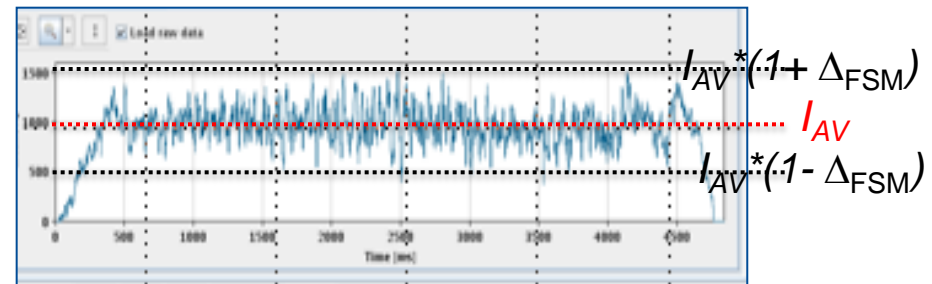
➤ Extinction

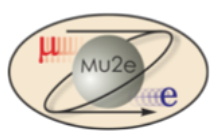
- kickers designed to deliver beam or no beam
- $> 10^{-4}$ extinction factor ..
- need $> 10^{-11}$ for mu2e-II
- need secondary extinction



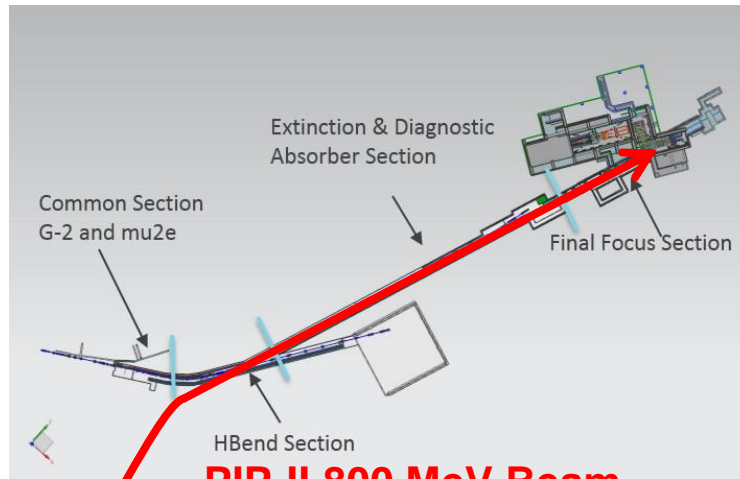
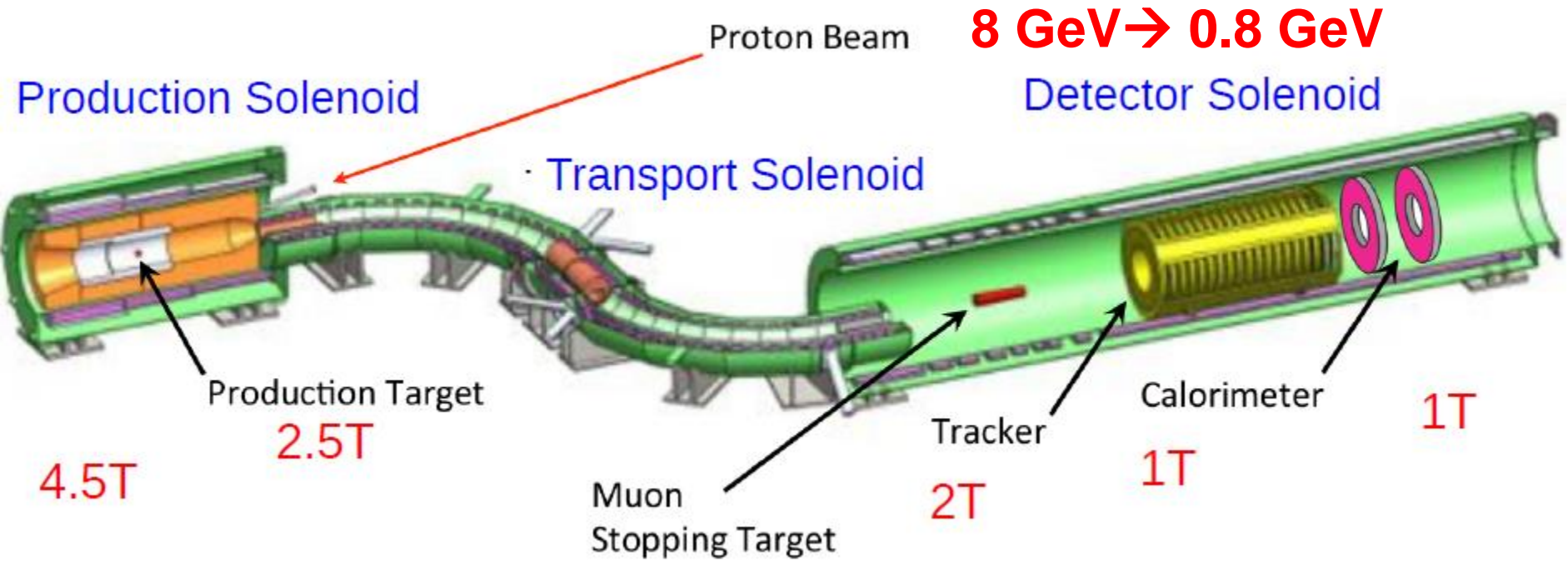
➤ spill uniformity

- linac pulse-to-pulse variation fairly small (few %)
- variation in mu2e slow extraction is intrinsically large
- “One should not be expecting beam intensity variations below $\pm 50\%$ in Mu2e” –Nagasleev .



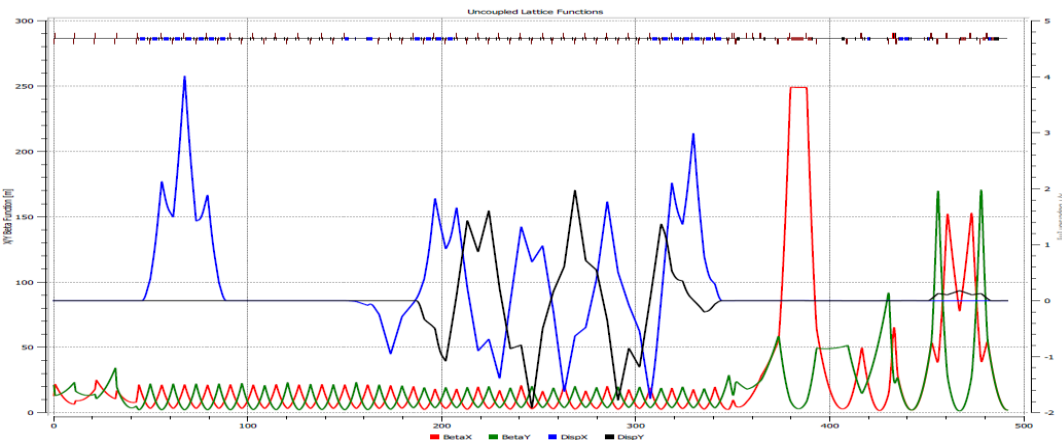
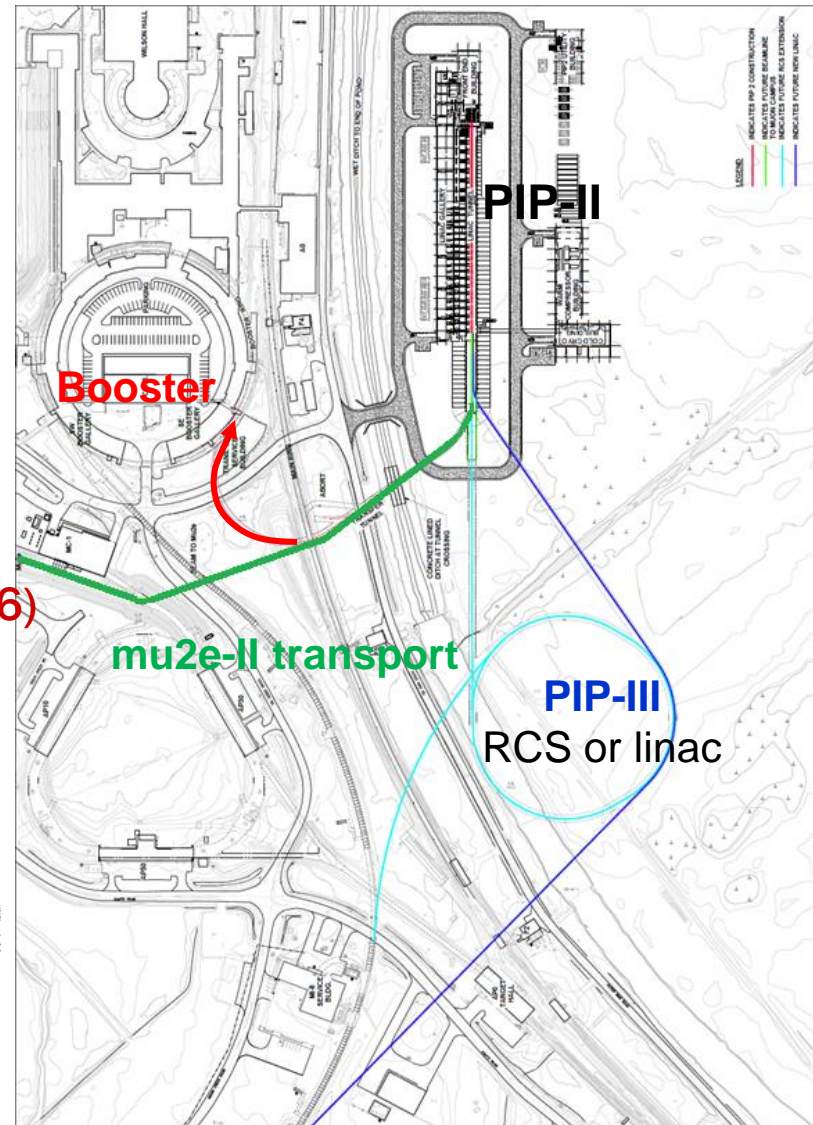


mu2e → mu2e-II



➤ 800 MeV beam line from PIP-II

- directly to production target
 - no Recycler, DR, slow extraction
 - 0.3 mm-mrad emittance H^-
- starts with transport to Booster
 - low-field ($B < 0.25$ T) for H^-
 - switchyard kicker splits (Booster / mu2e)
- mu2e line continues into M4 line
 - uses same magnets at lower strength (1/6)
 - could use mu2e extinction ...



➤ PIP-II Linac is H⁻

beam enters ~4T field

13° → 0.9 T transverse

H⁻ stripping time (W. Chou)

$$\tau = \frac{3.07 \cdot 10^{-14}}{3.2PB_t} \exp\left(\frac{44.14}{3.2PB_t}\right) s$$

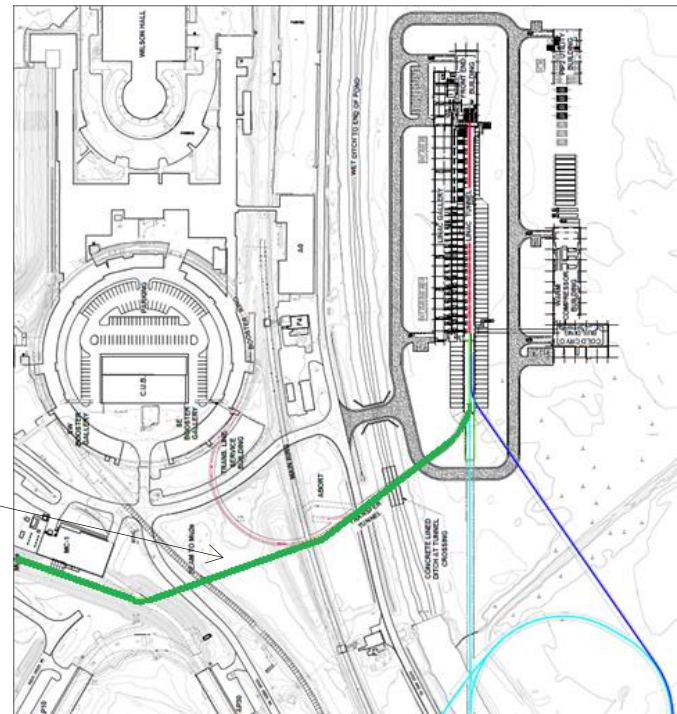
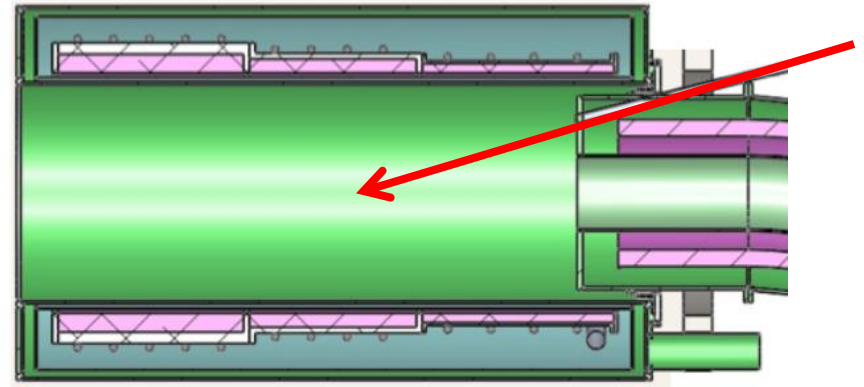
- P=1.463 GeV/c

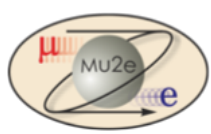
$c\tau = \sim 8 \text{ cm}$

(6km at $B_t/2$)

Beam should be stripped upstream

- orbit bump onto stripper foil could add to extinction (Roberts)





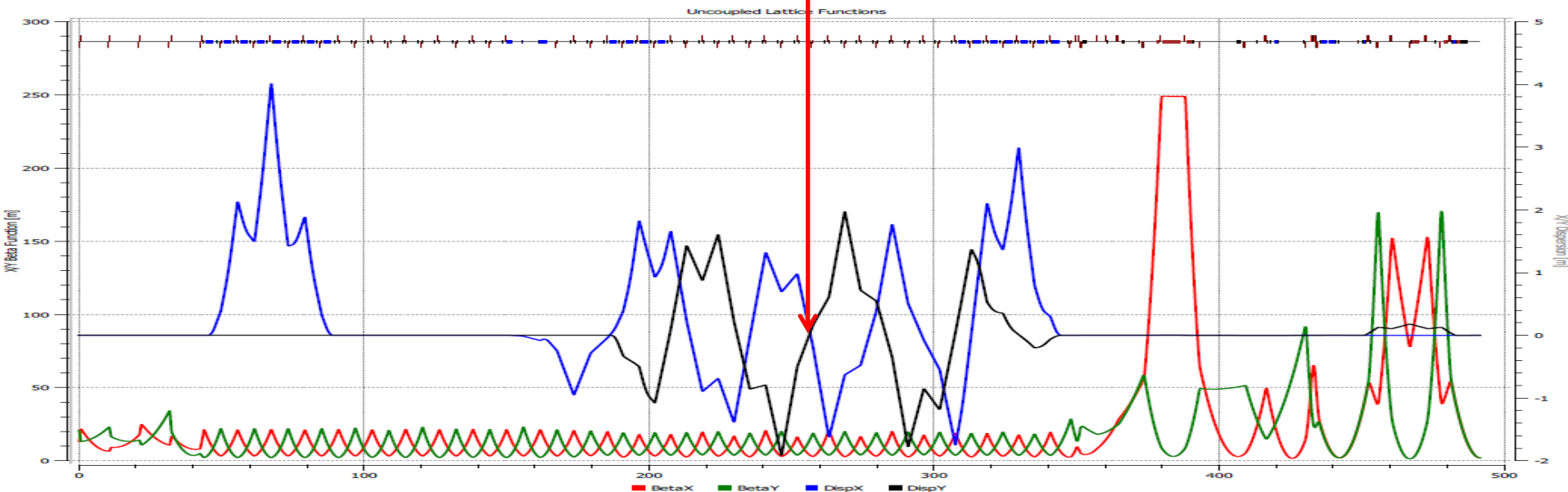
Location in Vivoli lattice

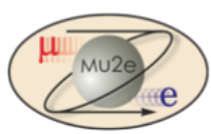


➤ Possible foil location is halfway through straight section (at $s = 257.5$)

- $\eta_x = 0$, $\eta_y = 0$, $\beta_x = 3.4\text{m}$, $\beta_y = 15.2\text{m}$
- Beam spot size is small (1.7×0.8 mm), however.
 - more intense spot heating of foil - ~ 5600 J/gm peak
- reoptimized lattice with larger beam spot (and collimation to localize foil-induced beam loss) is desirable

Possible Foil location





Stripper Foil calculations



➤ **Passing through foil, H^- beam strips, to H^0 , H^+**

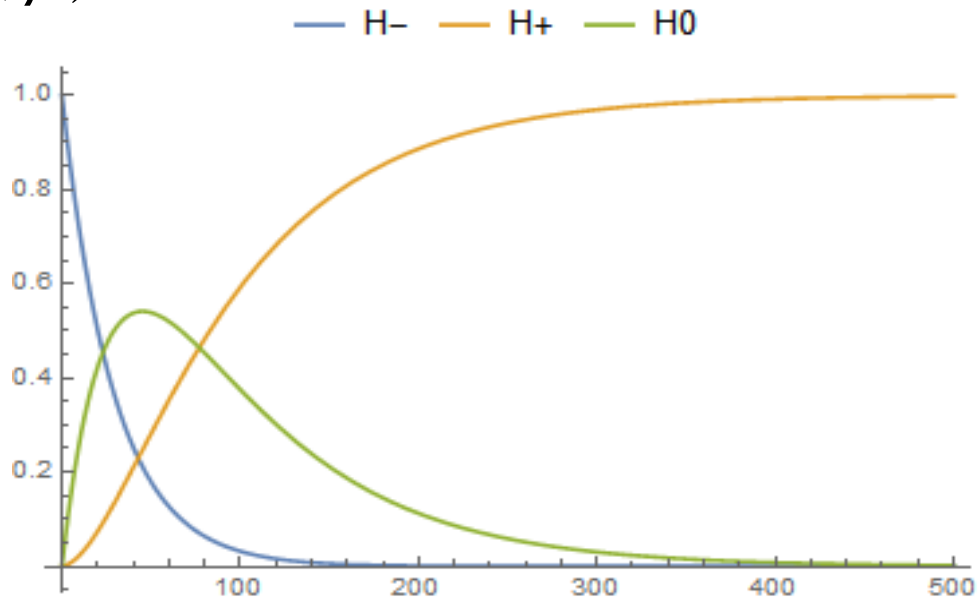
$$f_{H^-}(t, \beta) = \text{Exp}[-(0.479 + 0.0085) \cdot 0.05t / \beta^2]$$

$$f_{H^0}(t, \beta) = \frac{0.479}{(0.479 + 0.0085 - 0.187)} \left(\text{Exp}[-(0.187) \cdot 0.05t / \beta^2] - \text{Exp}[-(0.479) \cdot 0.05t / \beta^2] \right)$$

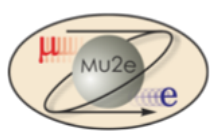
$$f_{H^+}(t, \beta) = 1 - f_{H^0}(t, \beta) - f_{H^-}(t, \beta)$$

Use $\sim 400 \mu\text{gm}/\text{cm}^2$

- **99.2% stripped to H^+**
- **requires $\sim 2\mu$ graphite or 1.2μ diamond**
- **$\sim 1\%$ beam loss from stripping**
 - **1 kW beam loss**



Stripper thickness in $\mu\text{gm}/\text{cm}^2$
For Graphite $0.1\text{mm} = 200 \mu\text{gm}/\text{cm}^2$



Stripper foil effects

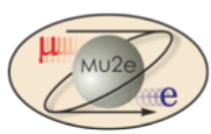


➤ Multiple Scattering and Energy loss effects are fairly small

- for $\beta_t=10\text{m}$, $\Delta\epsilon_N=0.011$ mm-mrad
 - $\epsilon_N \cong 0.3$ mm-mrad from linac
- The energy loss is ~ 1.0 keV ($\sim 10^{-6}$),
 - energy spread increase is less

- Optics should be almost unchanged, provided magnet polarities are all switched downstream of the foil.

$$\Delta \epsilon_N \cong \frac{\beta_T (13.6)^2 t}{2 \beta^2 P_{beam} m_{beam} X_0}$$



Stripper Foil heating



- **Energy loss of $H^- \rightarrow p$ heats foil:**

$$\rho V C_h \frac{dT}{dt} \cong \frac{dE_{H^- \rightarrow p}}{ds} t \frac{I}{e} - 2A\epsilon\sigma_B (T^4 - T_0^4)$$

- heating due to beam E loss, minus black body radiation
 - (Liaow et al.)

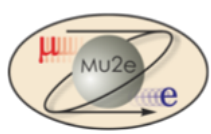
- **Equilibrium temperature is given by:**

$$(T_{eq}^4 - T_0^4) = \frac{dE_{H^- \rightarrow p}}{ds} t \frac{I}{\sigma_B 2\pi\epsilon\sigma_x\sigma_y e}$$

- for nominal focus, $T_{eq} \cong 760^\circ \text{ K}$
 - a slightly larger focus ($\beta^* = 30\text{m}$) would reduce this to 540° K

- **Heating is moderated by cw operation, and only one pass of beam through foil**

- foils in SNS, Booster peak at up to 1800° ($T_{eq} \sim 1000^\circ$)



Foil heating:



➤ Numerical solution of heating equation:

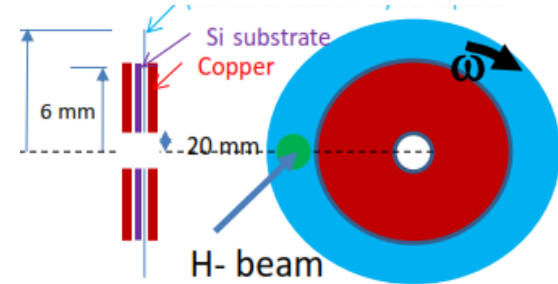
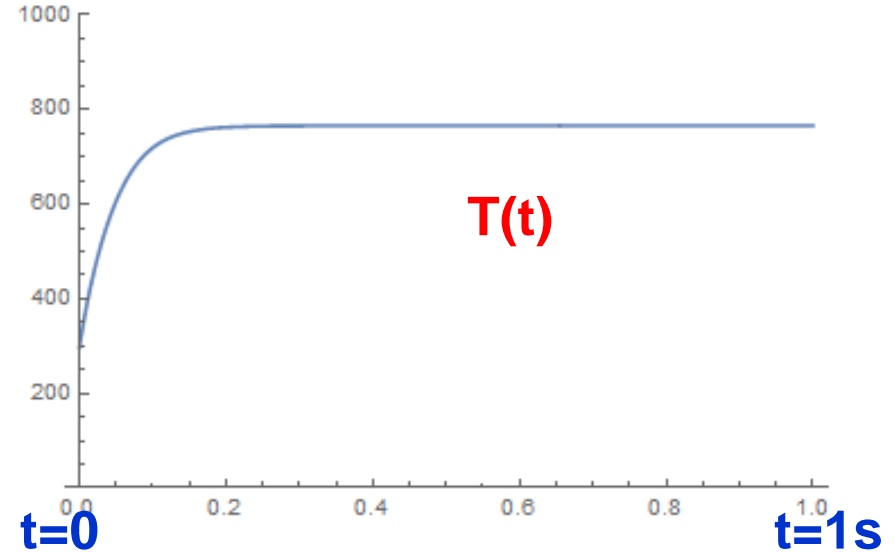
- $T_{eq} = 760^\circ \text{K}$ (0.8×1.7 mm)
 - larger spot:
 - $T_{eq} = 540^\circ \text{K}$ (2.5mm)

➤ Can spread out heating by moving beam across target

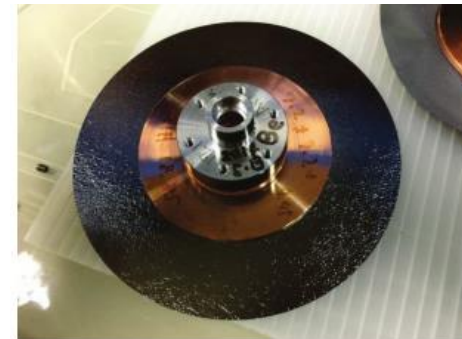
- or moving target – rotating

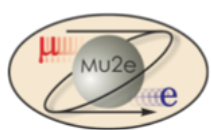
➤ Foil heating is relatively modest and manageable

- at 100kW
- but at 1MW
 - $T \rightarrow 1350^\circ \text{K} - 940^\circ \text{K}$



Johnson & Tang



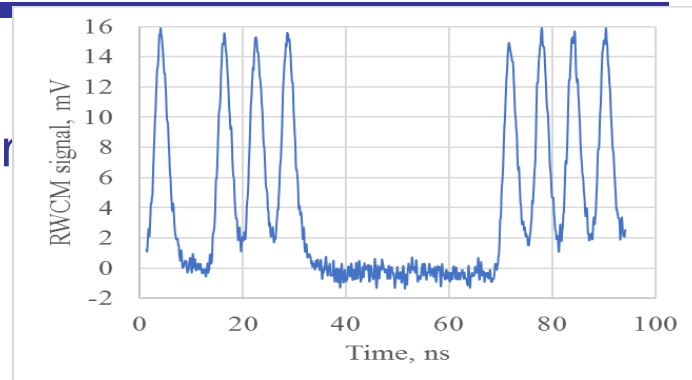


Extinction Considerations



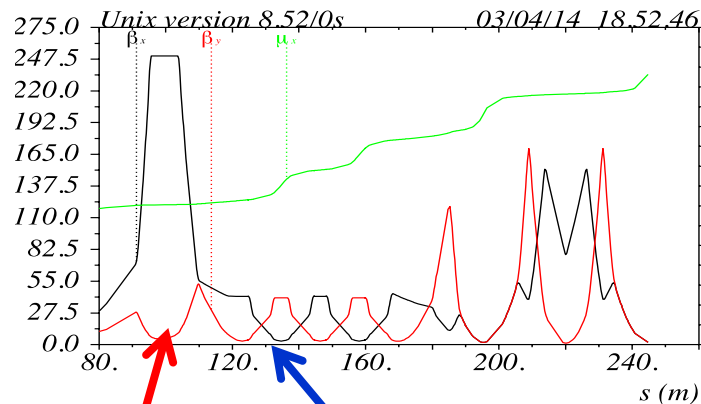
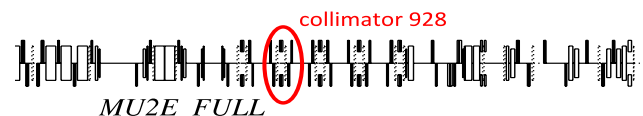
➤ Need $\sim 10^{-11}$ extinction

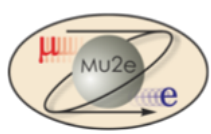
- Extinction from linac should be better than from Delivery Ring
 - $< 10^{-4}$
- measure in PIP2IT?



➤ Need additional extinction

- can use Mu2e AC dipole extinction
 - Kick $\sim \text{Sin}(\pi x/t_0) - f \text{Sin}(\pi h x/t_0)$
- Geometric emittances of PIP-II and mu2e P-beam are similar
- $\epsilon_{N,RMS}$: 2.5 (8 GeV) \rightarrow 0.3 (0.8 GeV) mm-mr
- $\epsilon_{geo,RMS}$: **0.26** (8 GeV) \rightarrow **0.19** (0.8 GeV) mm-mr
- ~same apertures in same lattice
 - $B\rho$: 29.84 \rightarrow 4.91 T-m
- Use magnets and fields at 1/6 strength





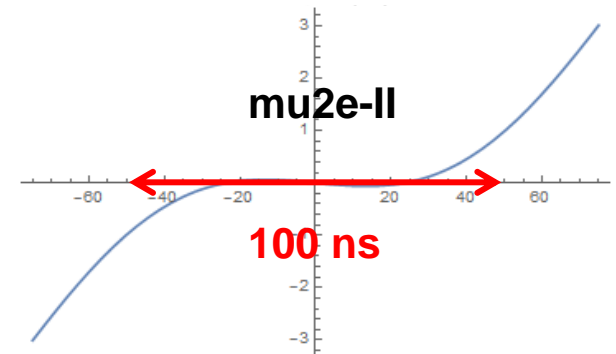
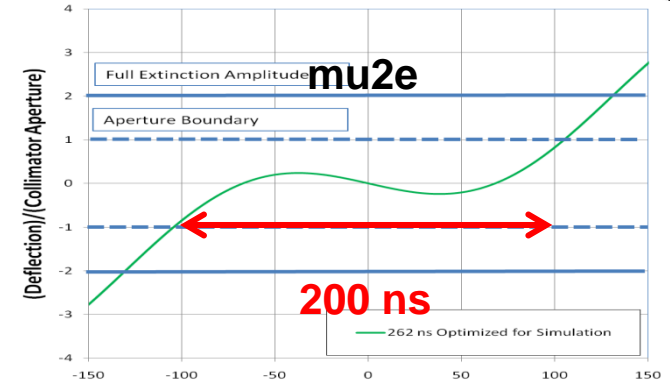
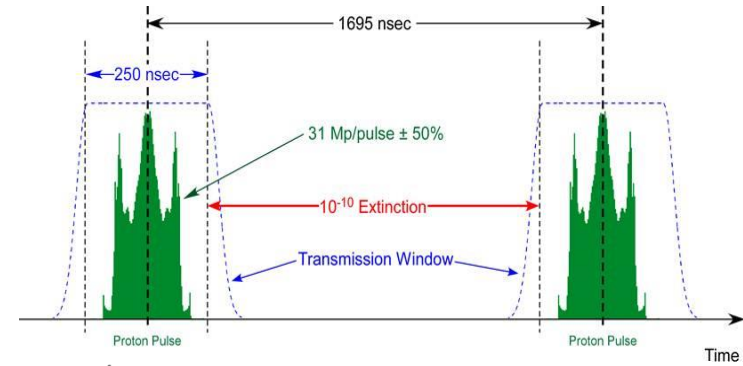
Extinction comments

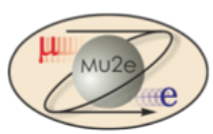


- **Mu2e extinction is designed to accept $\pm 125\text{ns}$**
 - Kick $\sim \text{Sin}(\pi x/t_0) - f \text{Sin}(\pi h x/t_0)$
 - h – harmonic (15), $f = 0.084$

- **Mu2e-II bunch length could be $\sim 2\times$ shorter.**
 - can reduce window a factor of 2 by changing h , f , and Kick strength
 - $K=2.5$, $h=21$, $f=0.055$

- **should work at least as well as for Mu2e**





Primary Beam Transport through the Solenoid:

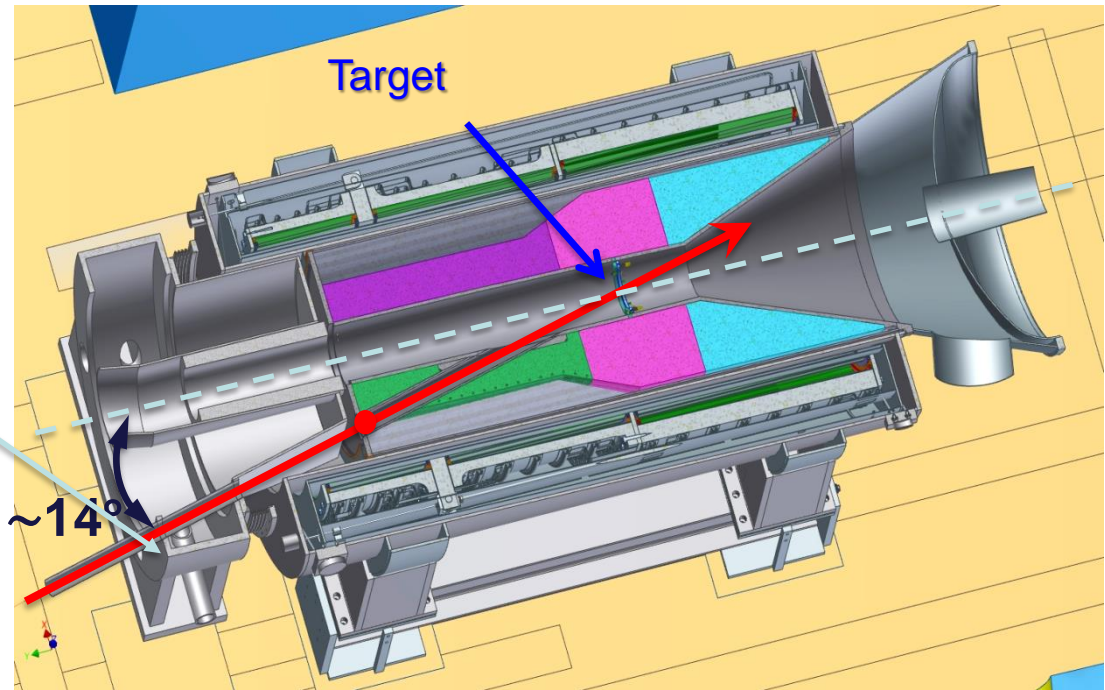


8 GeV proton beam enters PS:

- 0.6 m off-axis
- vertical pitch = $\sim -3^\circ$
- horizontal bearing = $\sim 13.6^\circ$
- For 8 GeV beam, the proton trajectory is well approximated by a straight line.

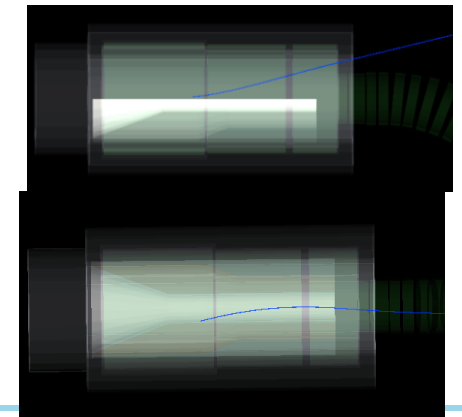
This is not the case at 800 MeV

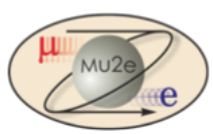
- S. Werkema



800 MeV p would not follow 8 GeV path

- miss target and hit shielding
- T. Roberts
- Can we modify motion to \sim fit mu2e ?





8GeV beam \rightarrow 0.8 GeV



➤ Unlike 8 GeV beam, 800 MeV beam is significantly deflected by B-field

- $8.89 \rightarrow 1.46 \text{ GeV}/c$

➤ If sent along same direction, would miss target by $\sim 30\text{cm}$

- hit HRS shielding

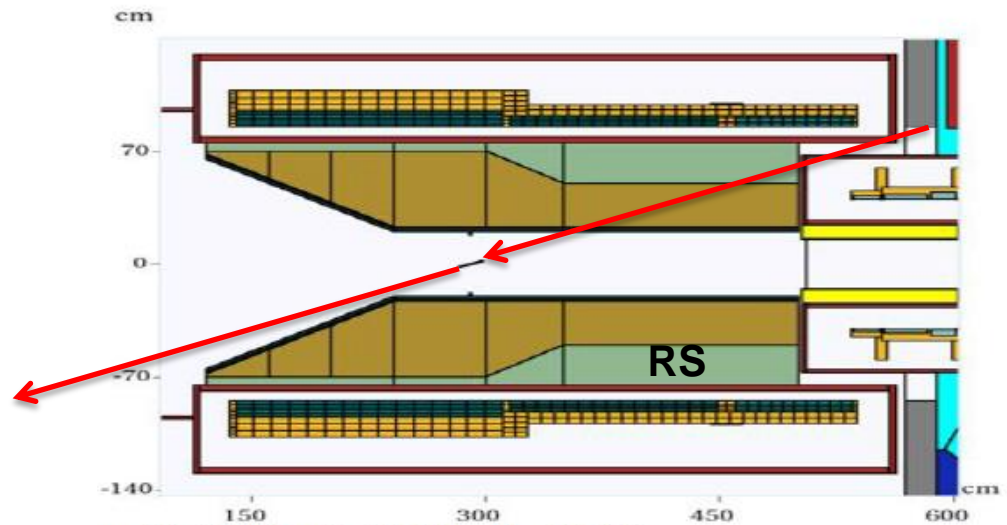
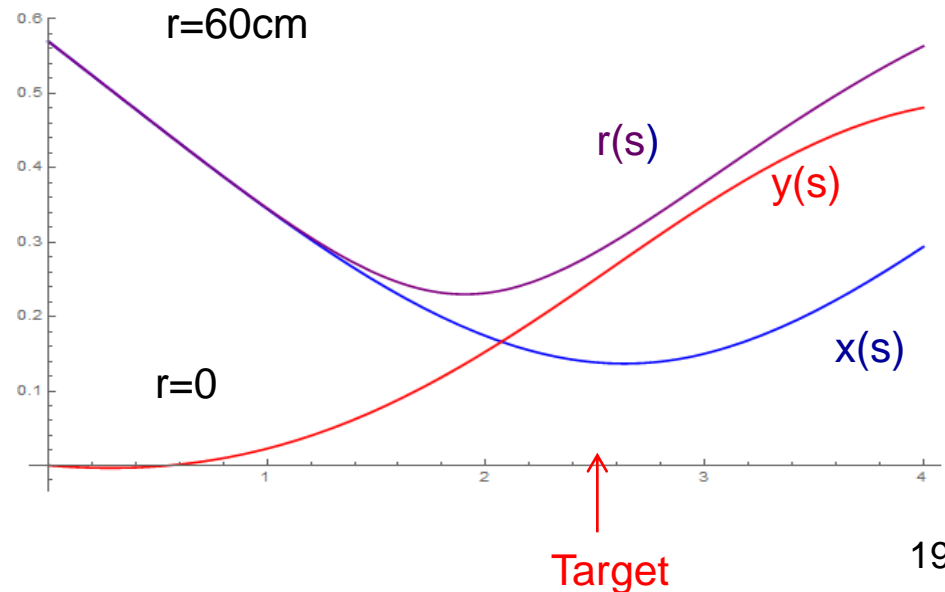
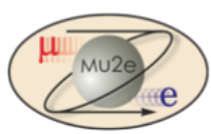


Figure 6.26. MARS15 model of the PS magnet and the HRS.





Injection beam dynamics



➤ Variation for mu2e-II

- Require beam to go through entry point and target (G4BL Mu2e modell)
 - (x=0.6, y=, at z=0) and (x=y=0 at z=2.5m)
- Use linearized magnetic field

$$x'' = \frac{B}{B\rho} y' + \frac{B'}{2B\rho} y$$

$$y'' = -\frac{B}{B\rho} x' - \frac{B'}{2B\rho} x$$

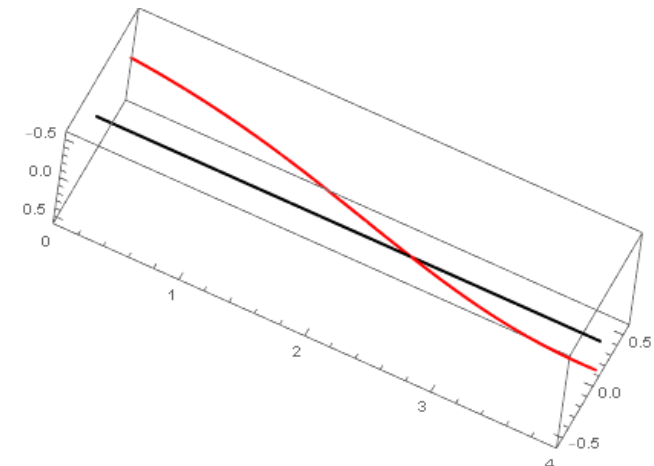
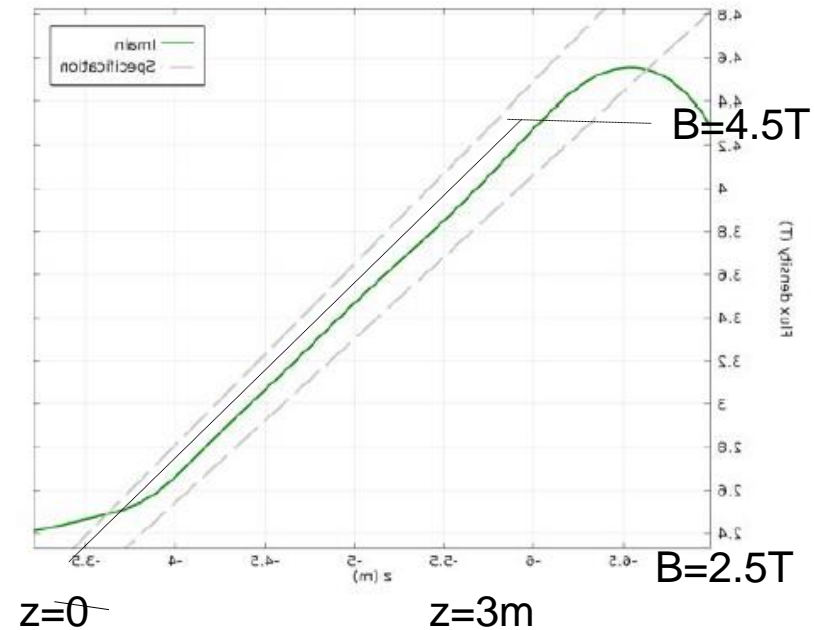
- Solve using mathematica

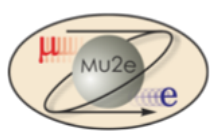
- for 800 MeV, 8 GeV

- Third order terms:

$$x'' = +Sy' + \frac{1}{2} S'y + \frac{1}{4} (2x'^2 y'S + x'^2 yS' + 2y'^3 S + y y'^2 S')$$

$$y'' = -Sx' - \frac{1}{2} S'x - \frac{1}{4} (2x'y'^2 S + x y'^2 S' + 2x'^3 S + x x'^2 S')$$

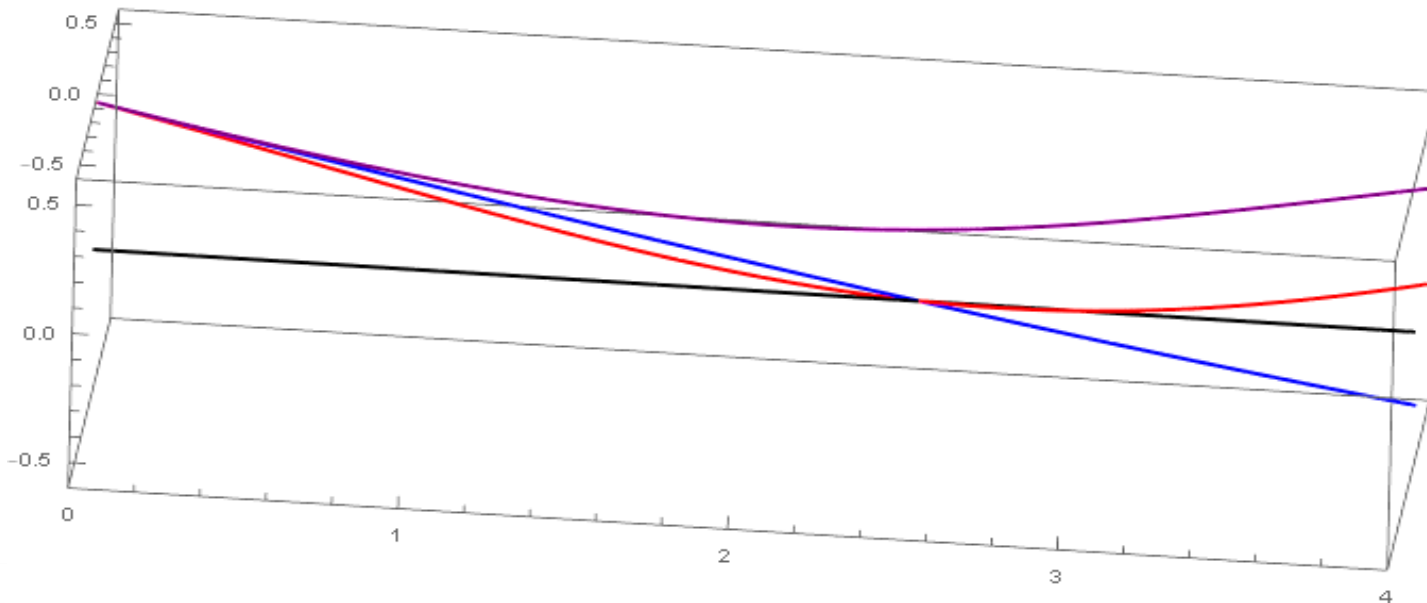


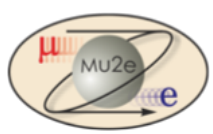


Solution exists!



- Requires change in direction of injection
- A path compatible with the Production solenoid is possible
 - need initial vertical angle ($\sim 10.5^\circ$), and reduced horizontal angle ($\sim 10^\circ$)
 - beam wobbles away from straight line (by $\sim 10\text{cm}$ before target)
 - (Mu2e entry beam pipe is too narrow)
 - emerges after target in different location and angle
 - (horizontal \rightarrow vertical)



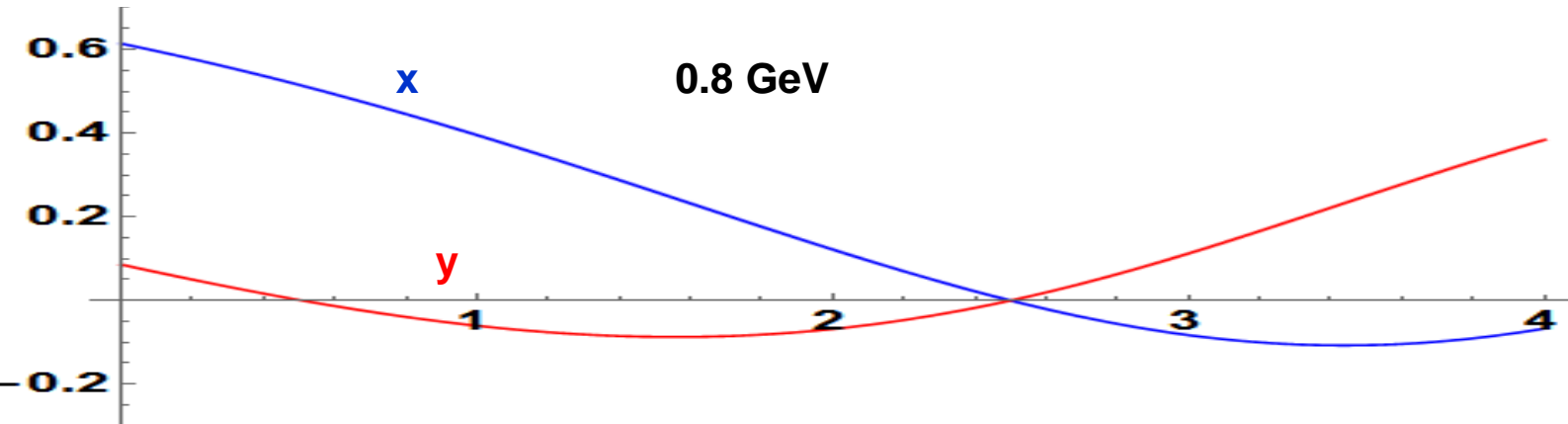
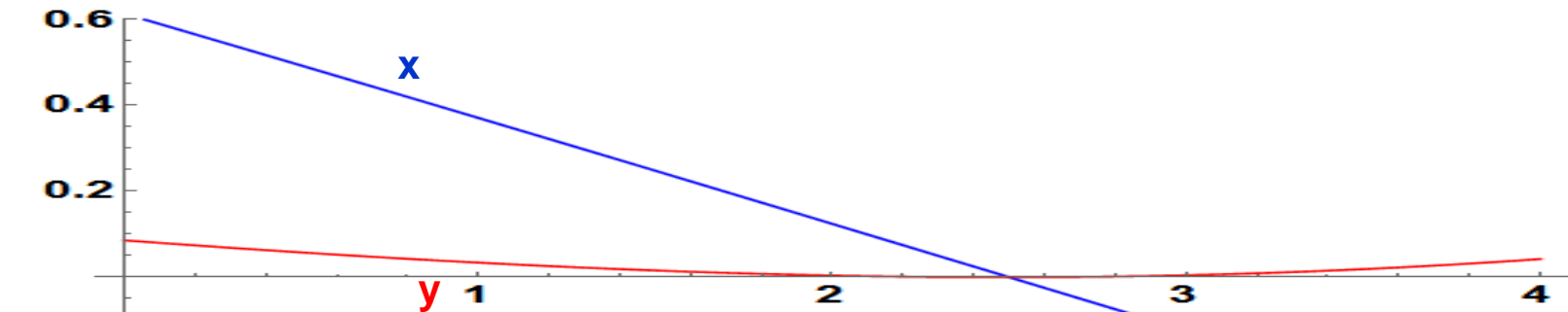


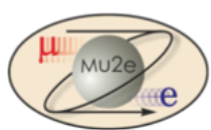
Compare x, y for 8, 0.8 GeV



	x, y (8)	x', y' (8)	x, y (0.8)	x', y' (0.8)
0	0.614, 0.086	$-13.5^\circ, -3.4^\circ$	0.614, 0.086	$-9.9^\circ, -10.5^\circ$
2.5	0, 0	$-14.0^\circ, 0^\circ$	0, 0	$-12.0^\circ, 10.5^\circ$
4	-0.37, 0.042	$-13.6^\circ, 3.2^\circ$	-0.067, 0.384	$7.95^\circ, 13.75^\circ$

8 GeV

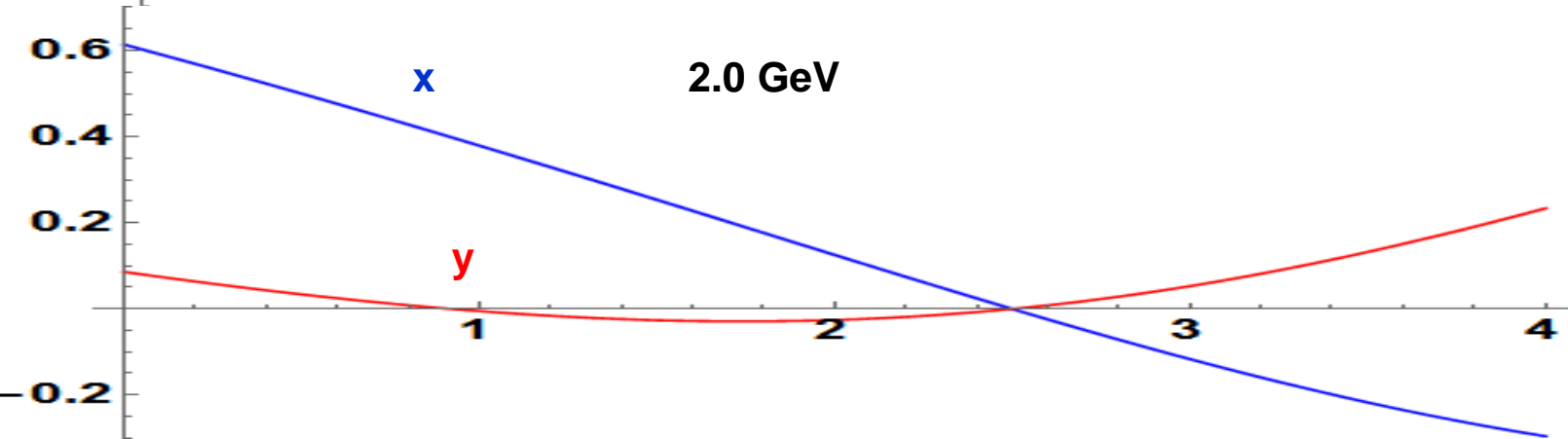
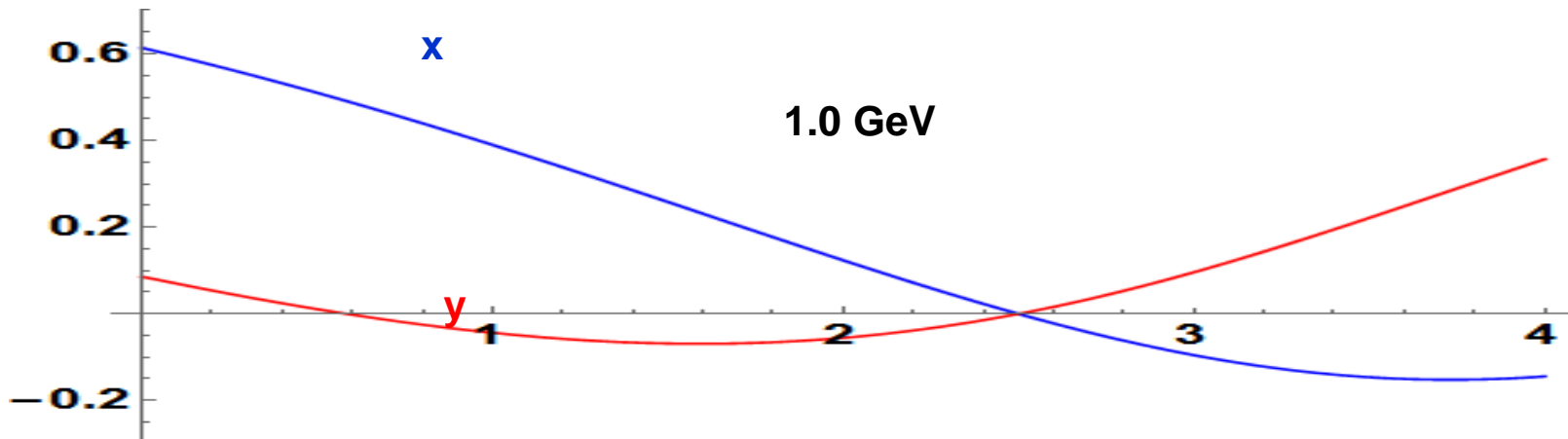


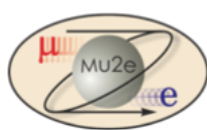


Compare x, y for 1, 2 GeV



	x, y (1)	x', y' (1)	x, y (2.0)	x', y' (2.0)
0	0.614, 0.086	$-10.8^\circ, -9.4^\circ$	0.614, 0.086	$-12.78^\circ, -5.86^\circ$
2.5	0, 0	$-12.7^\circ, 8.7^\circ$	0, 0	$-13.87^\circ, 3.435^\circ$
4	-0.144, 0.357	$3.29^\circ, 14.9^\circ$	-0.321, 0.194	$-9.56, 10.78^\circ$

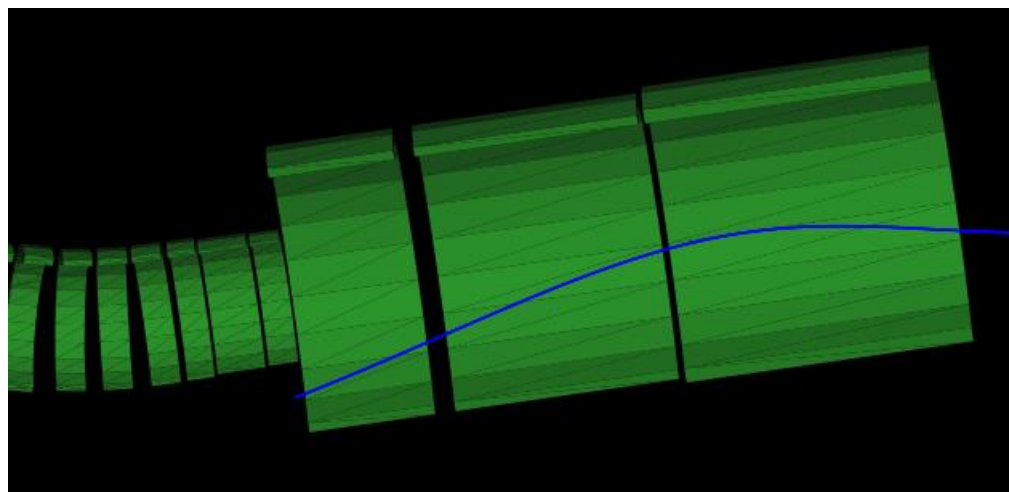




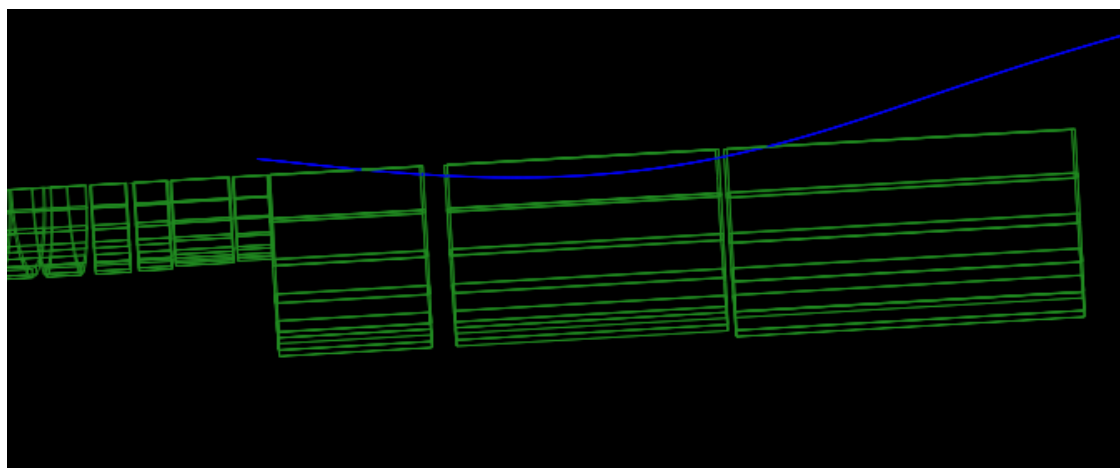
Verified in G4Beamline Mu2e Model



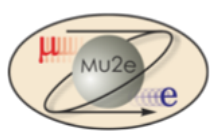
- **Direct copy misses target by 1-2cm**
 - tweak initial momentum to match
- **Requires minor tweaks from Mathematica model**
 - $P_y \rightarrow (260 \rightarrow 230 \text{ MeV}/c)$
 - $\sim 1^\circ$ correction



x projection



y projection



3-D projection of trajectories..

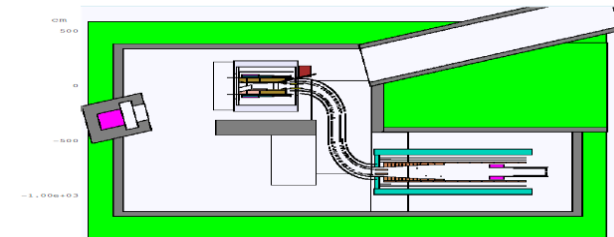
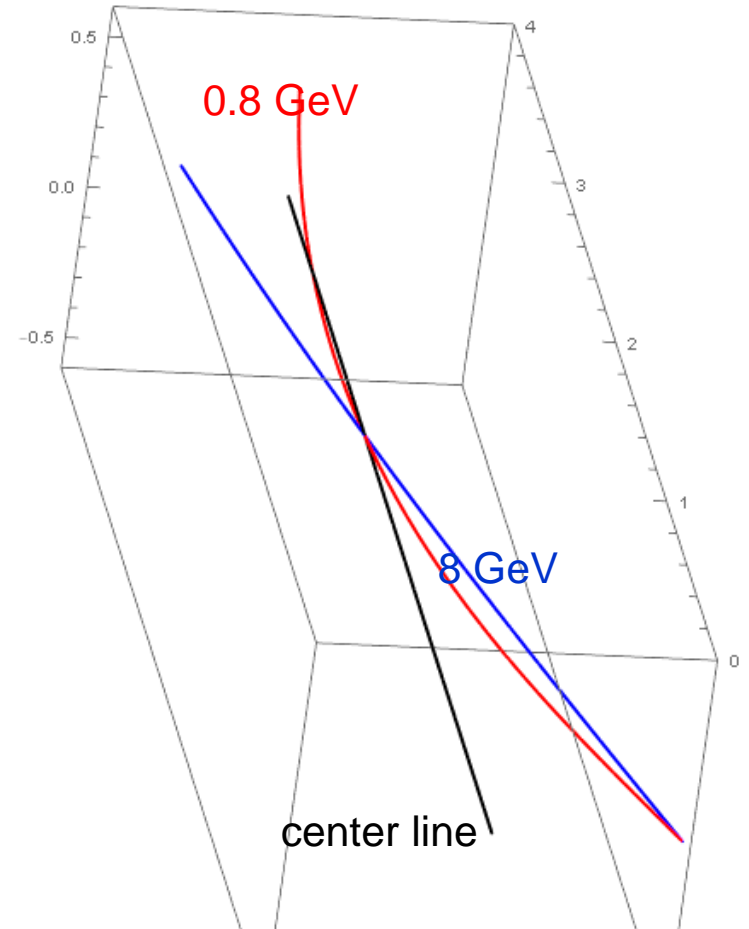
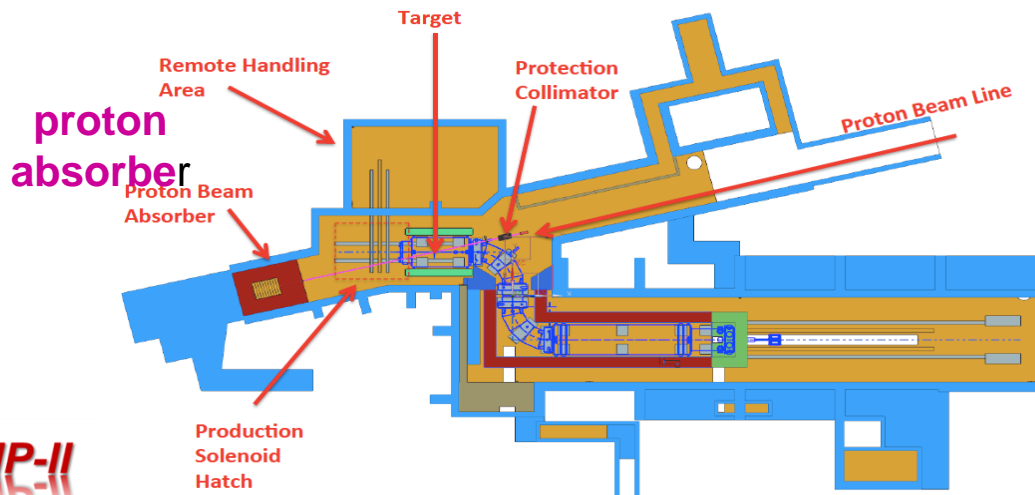


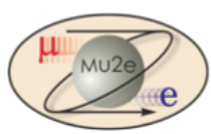
➤ 0.8 GeV beam would not meet proton absorber

- unless steered toward it ...
 - ~0.3 T-m bend ..
- Or inject ~vertically
 - exiting beam would be horizontal

➤ proton absorber changes?

- multiple scattering in target is six times larger angle ($\theta_0 \rightarrow 3.6^\circ$ at 16cm W)





Target considerations



➤ Mu2e

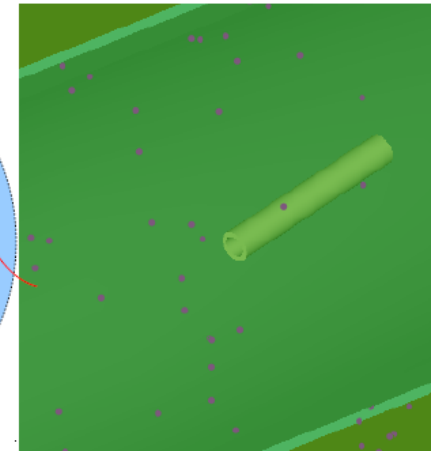
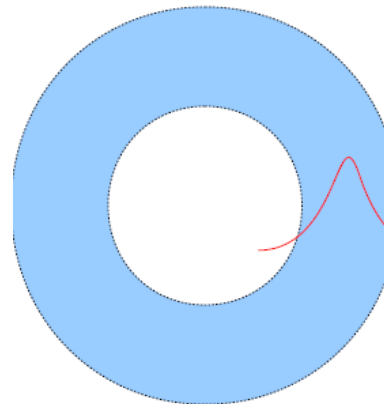
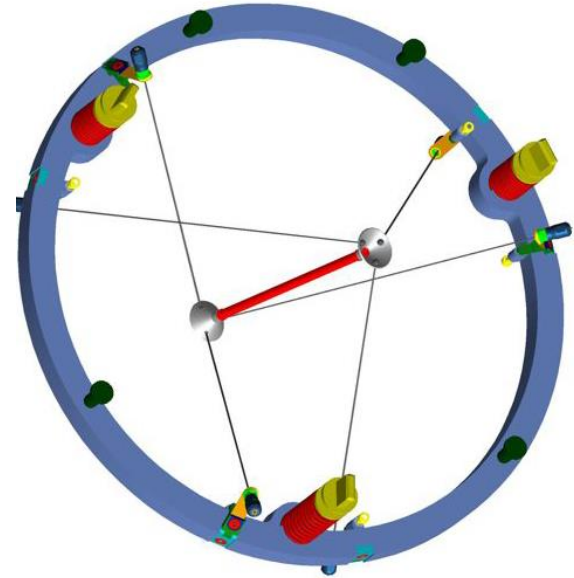
- 8 GeV, 8 kW (0.7 kW in target)
- passively cooled freestanding W target
- 3mm radius, 16cm long

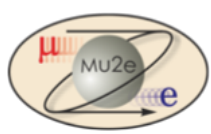
➤ Mu2e-II

- 800 MeV, 100kW (22.5 kW in target)
- Target DPA $\gg 1 \rightarrow$ (rad damage)

➤ Update requires

- active cooling (?)
- rastering on target
- could lose $\sim 1/3$ of μ 's from target reabsorption



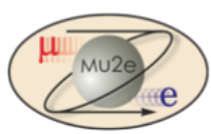


Summary



- **A Mu2e-II scenario using PIP-II 800 MeV H⁻ beam could follow the mu2e baseline**
- **Minimal changes needed:**
 - PIP-II to mu2e beam transport
 - need H⁻ → p stripping
 - beam must enter production solenoid at different angle
 - and possibly location?
 - production solenoid shielding modified ...
 - Proton Absorber (after target) must be changed
 - ~10× more irradiation in production solenoid/target vault
 - target for 10× power (and 800 MeV)

 - could reuse AC Dipole extinction system



Comments



- **More extensive variations from mu2e should be considered and compared by mu2e-II task force**
 - Higher power ?
 - 100 kW → MW
 - changes in timing pattern 1.69 μs → ?
 - Ti or Au target
 - change collimation
 - no p-bar, K, etc.
 - Change extinction
 - use stripping foil
 - Include other experiments using PIP-II beam
 - $\mu \rightarrow e \gamma$ using ~cw PIP-II source ??
 - Use forward muons ?