

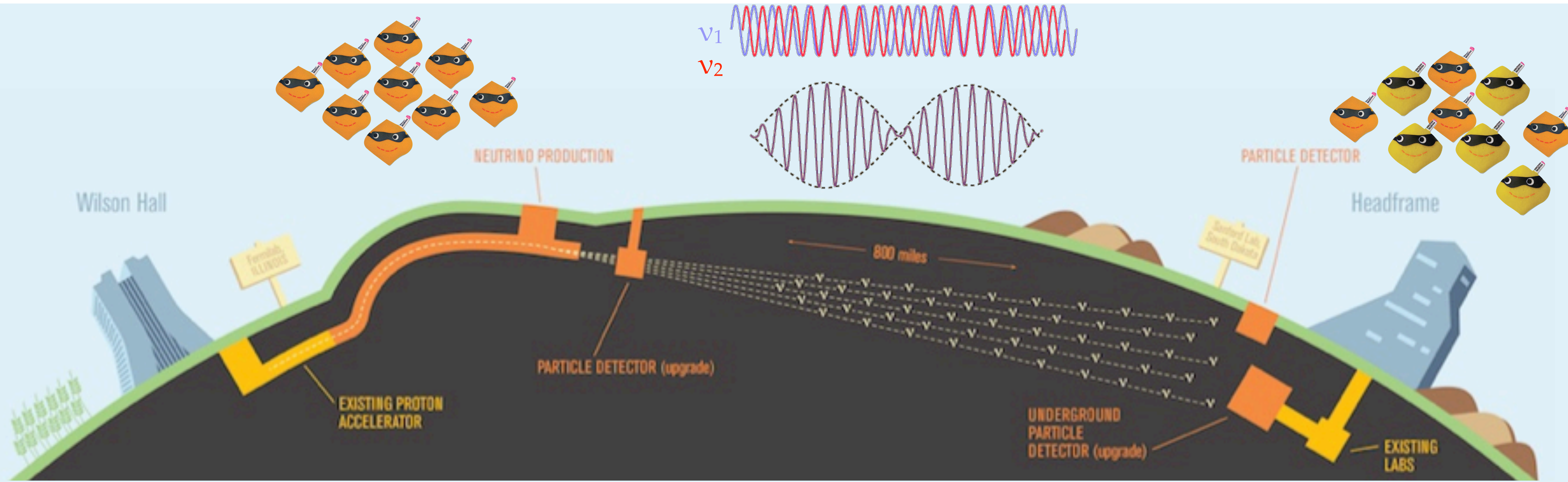


**UCL**

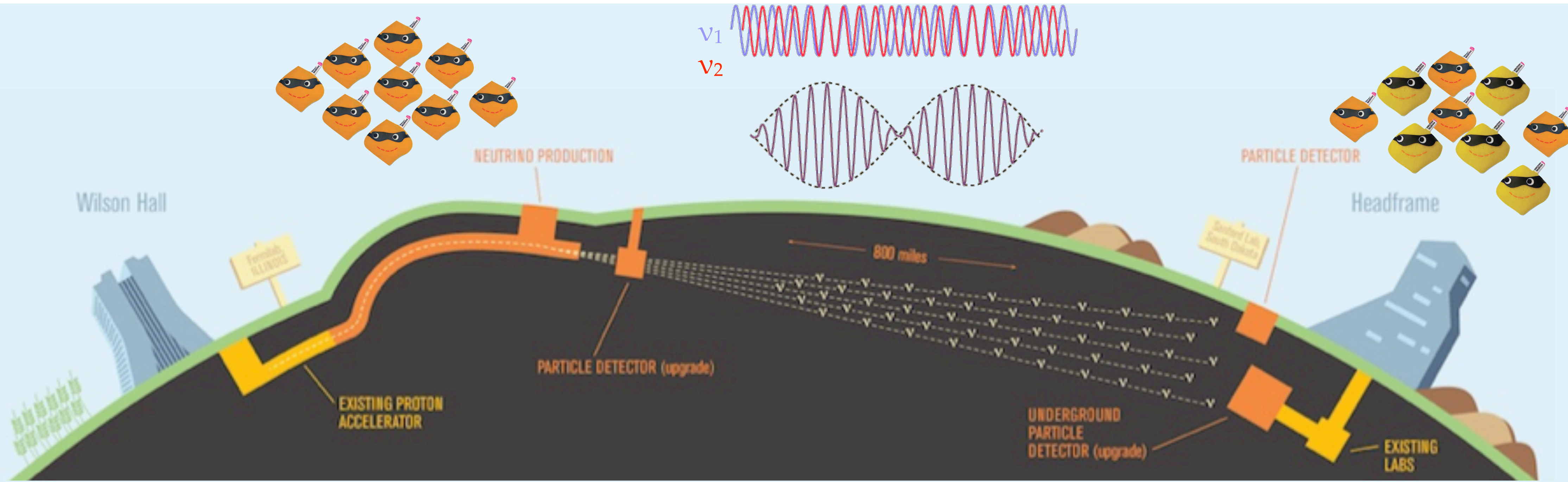
## Direct neutrino mass measurements

**Cheryl Patrick**, University College London  
International Neutrino Summer School 2019, Fermilab

# A nice, easy reminder of neutrino oscillations

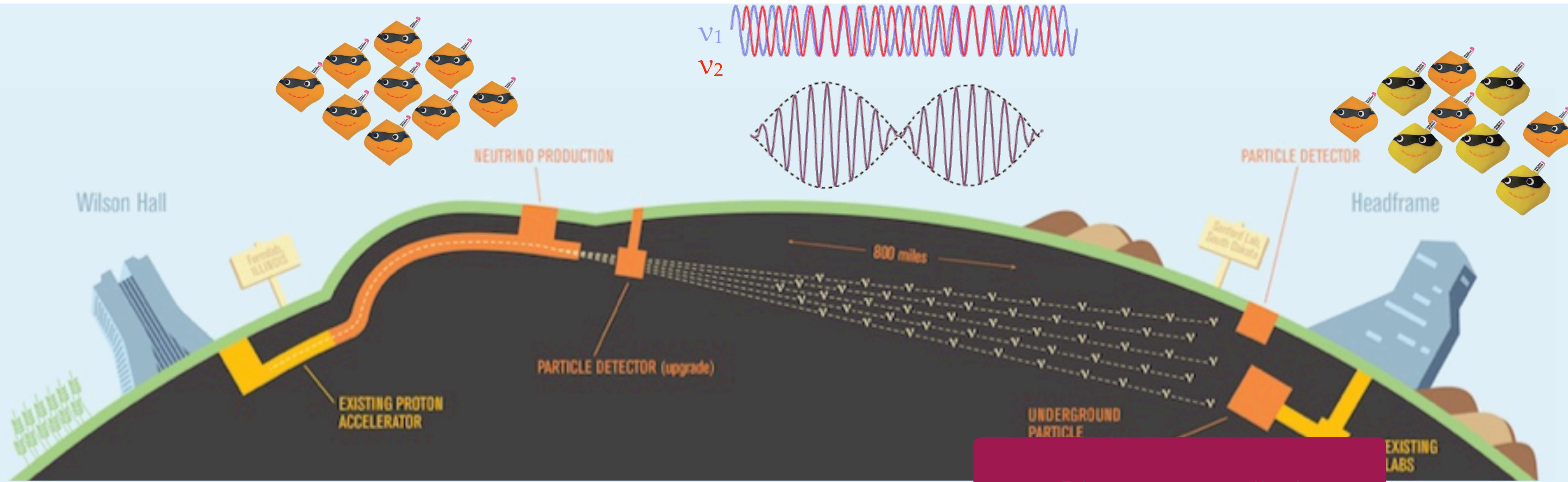


# A nice, easy reminder of neutrino oscillations



$$P(\nu_{l_\alpha} \rightarrow \nu_{l_\beta}, x) = \sin^2 2\theta \sin^2 \left( 1.27 \frac{\Delta M^2 (\text{eV}^2) x (\text{km})}{p_\nu (\text{GeV})} \right) \quad (\text{Two-flavour approximation})$$

# A nice, easy reminder of neutrino oscillations



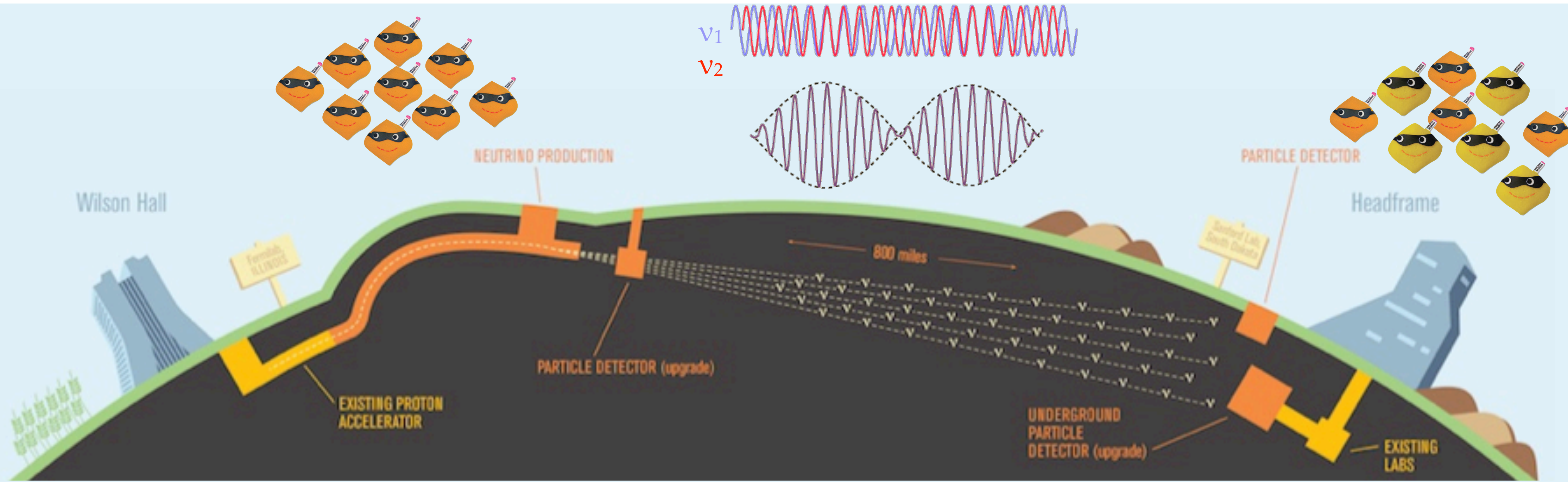
Distance travelled

$$P(\nu_{l_\alpha} \rightarrow \nu_{l_\beta}, x) = \sin^2 2\theta \sin^2 \left( 1.27 \frac{\Delta M^2 (\text{eV}^2) x (\text{km})}{p_\nu (\text{GeV})} \right) \quad (\text{Two-flavour approximation})$$

Oscillation probability

Momentum

# A nice, easy reminder of neutrino oscillations



$$P(\nu_{l_\alpha} \rightarrow \nu_{l_\beta}, x) = \sin^2 2\theta \sin^2 \left( 1.27 \frac{\Delta M^2 (\text{eV}^2) x (\text{km})}{p_\nu (\text{GeV})} \right) \quad (\text{Two-flavour approximation})$$

Mixing angle

Squared mass difference

$$P_{\alpha \rightarrow \beta} = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re} (U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2 \left( \frac{\Delta m_{ij}^2 L}{4E} \right) + 2 \sum_{i>j} \text{Im} (U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin \left( \frac{\Delta m_{ij}^2 L}{2E} \right)$$

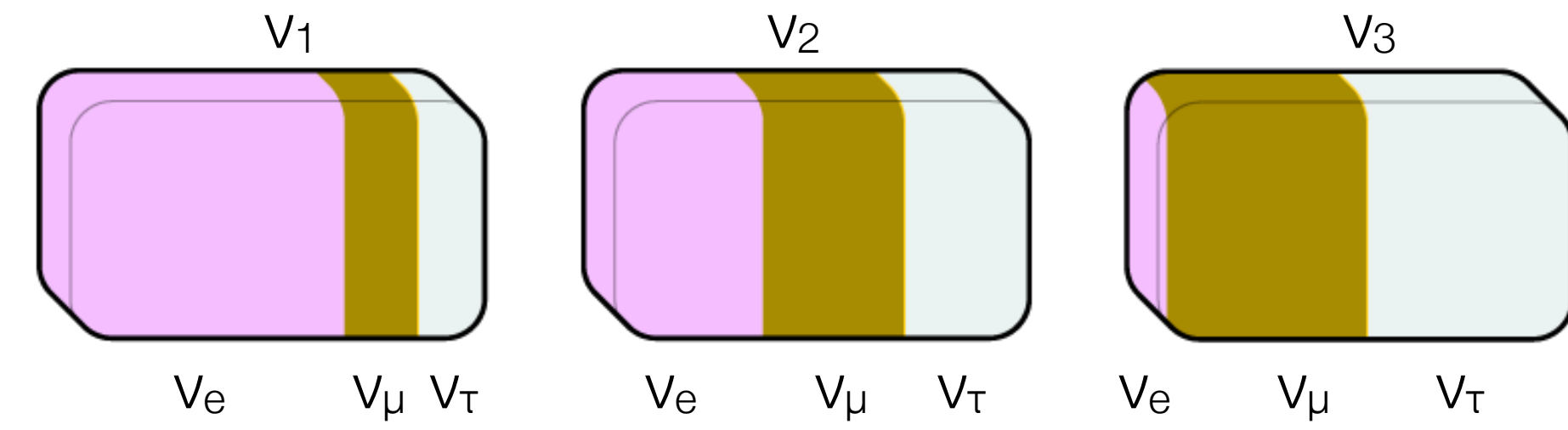
$$P_{\alpha \rightarrow \beta} = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re} \left( U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^* \right) \sin^2 \left( \frac{\Delta m_{ij}^2 L}{4E} \right) + 2 \sum_{i>j} \text{Im} \left( U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^* \right) \sin \left( \frac{\Delta m_{ij}^2 L}{2E} \right)$$

PMNS mixing matrix,  $U = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{bmatrix}$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha_1/2} & 0 \\ 0 & 0 & e^{i\alpha_2/2} \end{bmatrix}$$

# ... and a more complicated one

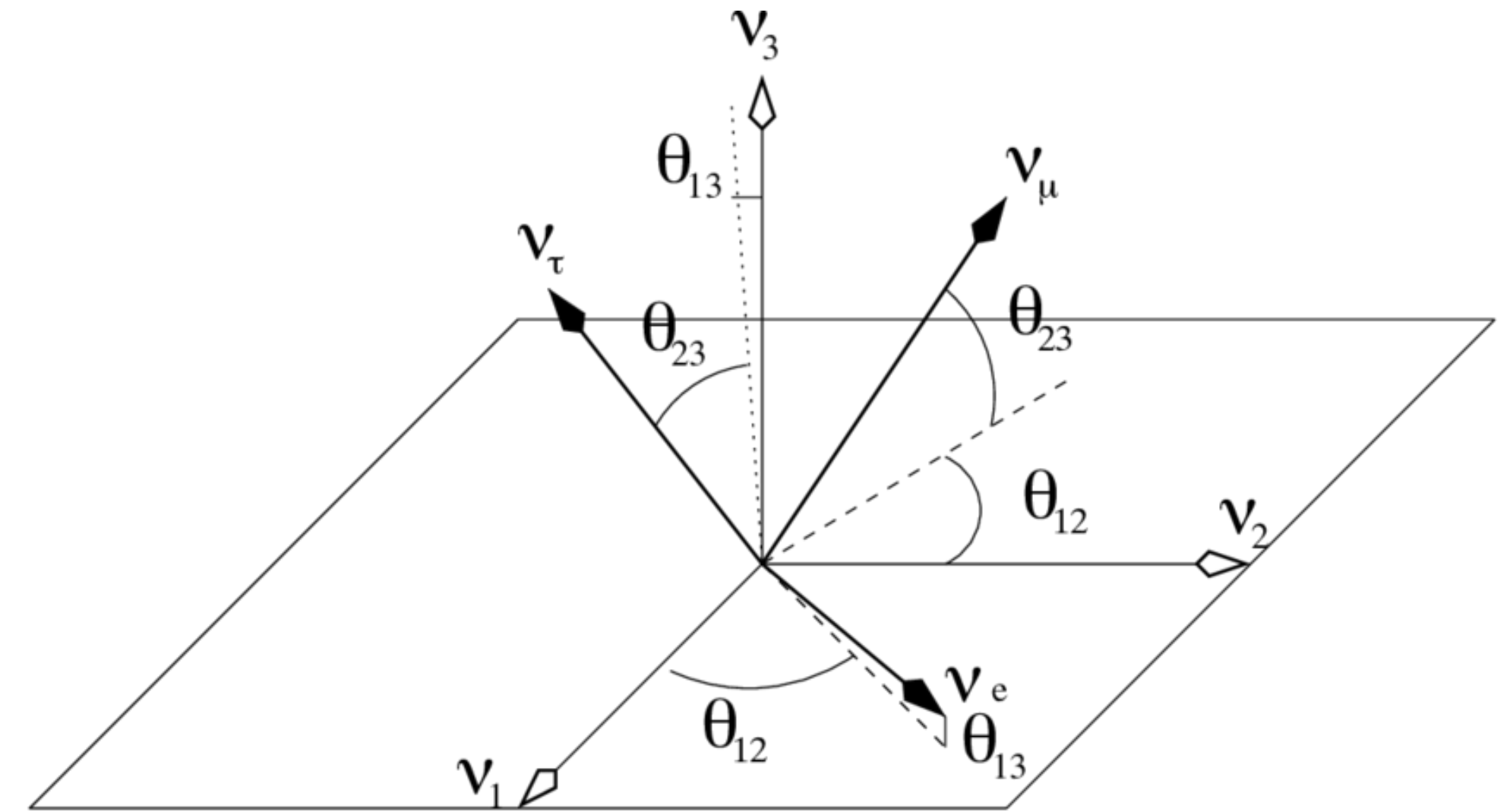
$$P_{\alpha \rightarrow \beta} = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re} \left( U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^* \right) \sin^2 \left( \frac{\Delta m_{ij}^2 L}{4E} \right) + 2 \sum_{i>j} \text{Im} \left( U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^* \right) \sin \left( \frac{\Delta m_{ij}^2 L}{2E} \right)$$



Sines and cosines of mixing angles

PMNS mixing matrix,  $U = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{bmatrix}$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha_1/2} & 0 \\ 0 & 0 & e^{i\alpha_2/2} \end{bmatrix}$$





$$P_{\alpha \rightarrow \beta} = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re} (U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2 \left( \frac{\Delta m_{ij}^2 L}{4E} \right) + 2 \sum_{i>j} \text{Im} (U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin \left( \frac{\Delta m_{ij}^2 L}{2E} \right)$$

PMNS mixing matrix,  $U = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{bmatrix}$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha_1/2} & 0 \\ 0 & 0 & e^{i\alpha_2/2} \end{bmatrix}$$

CP-violating phase changes sign for antineutrinos

$$P_{\alpha \rightarrow \beta} = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re} \left( U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^* \right) \sin^2 \left( \frac{\Delta m_{ij}^2 L}{4E} \right) + 2 \sum_{i>j} \text{Im} \left( U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^* \right) \sin \left( \frac{\Delta m_{ij}^2 L}{2E} \right)$$

PMNS mixing matrix,  $U = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{bmatrix}$

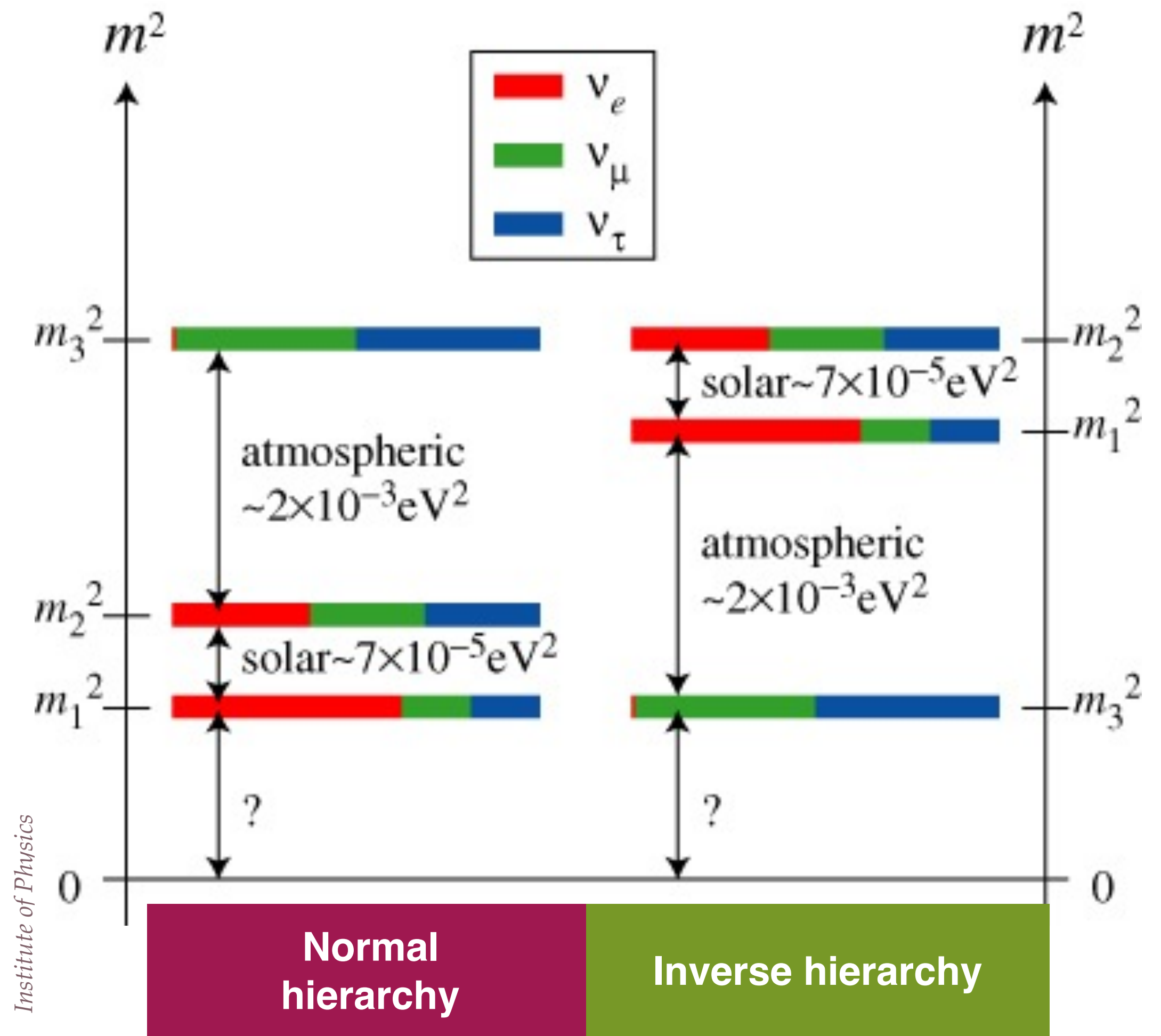
$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha_1/2} & 0 \\ 0 & 0 & e^{i\alpha_2/2} \end{bmatrix}$$

Majorana phases - more on these later!

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha_1/2} & 0 \\ 0 & 0 & e^{i\alpha_2/2} \end{bmatrix}$$

# ... and a more complicated one

$$P_{\alpha \rightarrow \beta} = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re} (U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2 \left( \frac{\Delta m_{ij}^2 L}{4E} \right) + 2 \sum_{i>j} \text{Im} (U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin \left( \frac{\Delta m_{ij}^2 L}{2E} \right)$$



Institute of Physics

## Indirectly



[cycling-challenge.com](http://cycling-challenge.com)

## Directly



Photo: Daniel Schwen

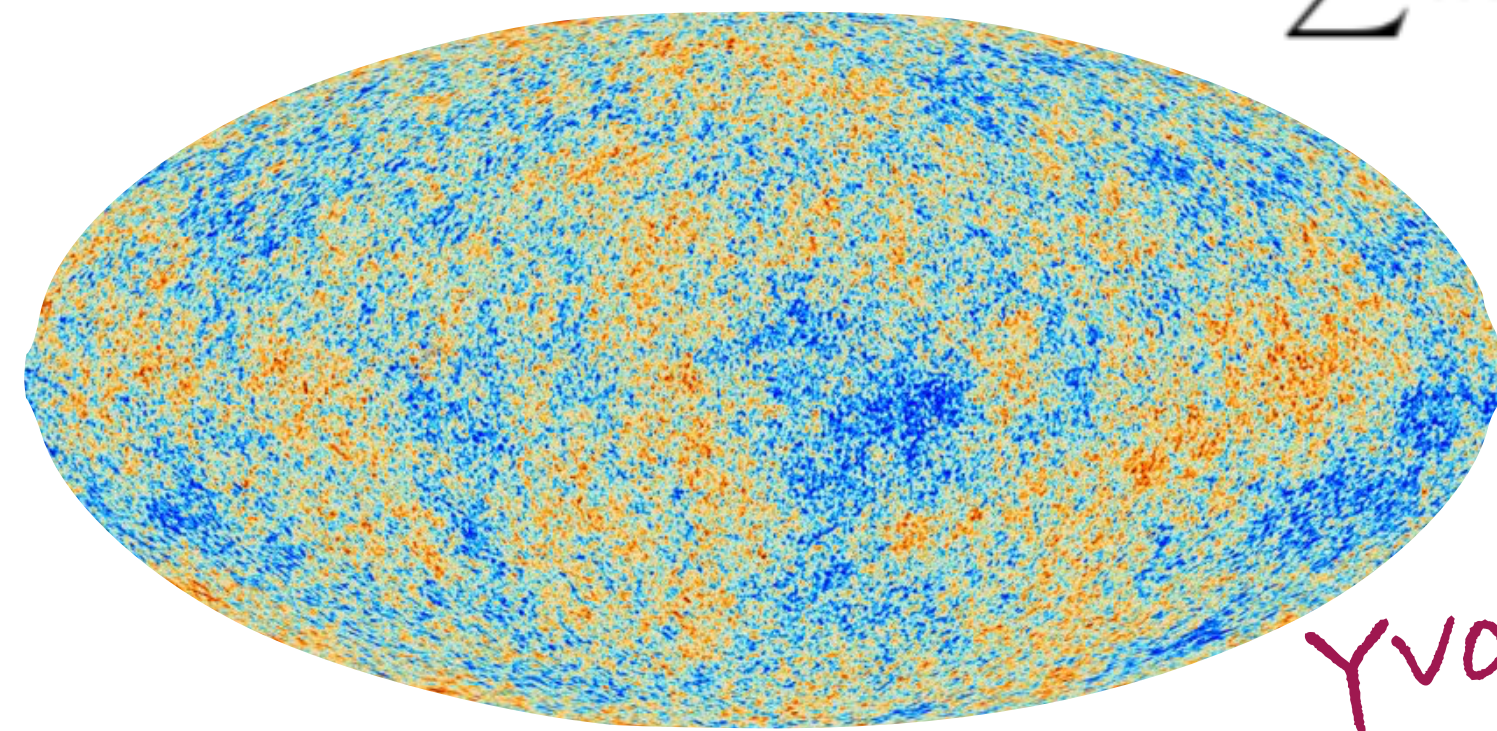
**Indirectly**

**Directly**

## Indirectly

## Directly

### Cosmology



$$\sum m_\nu$$

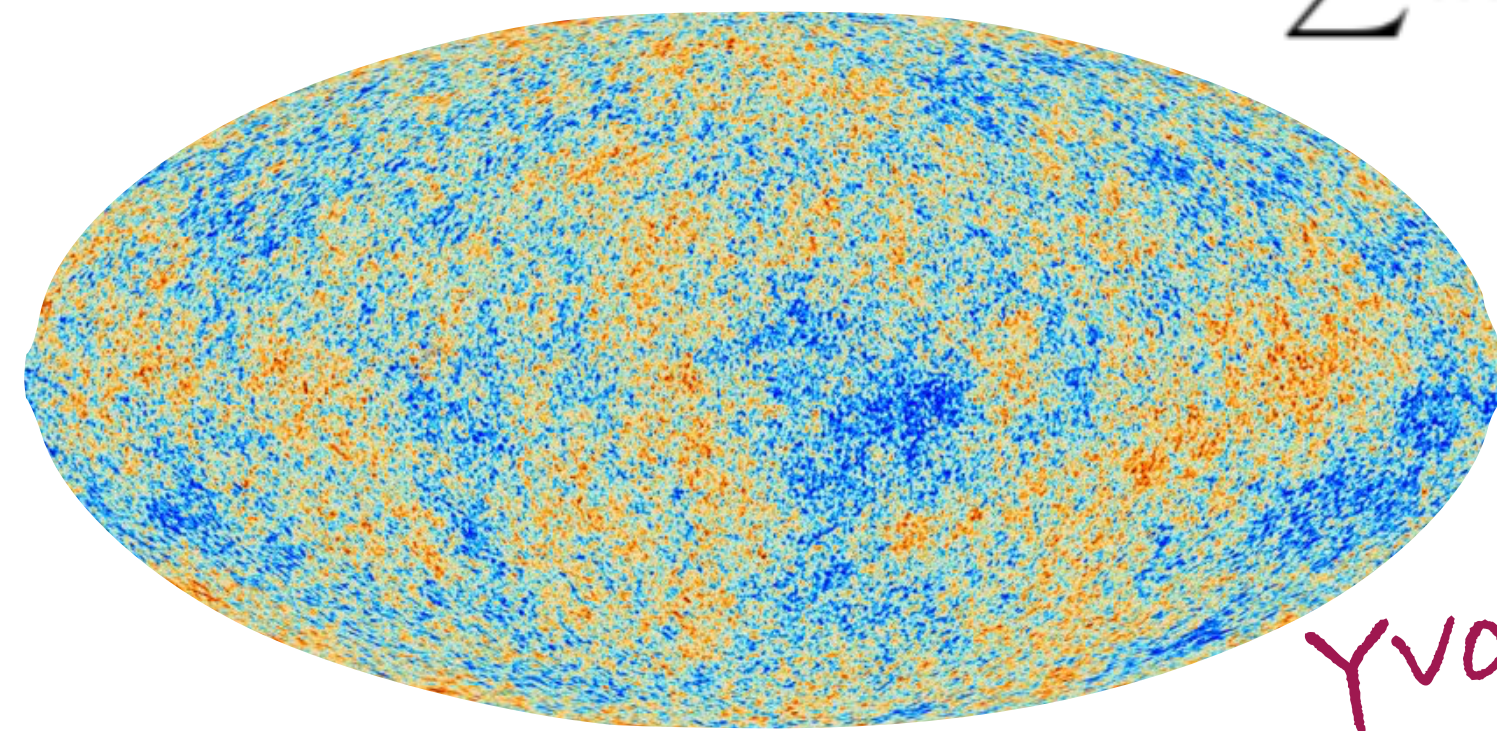
August 2019						
S	M	T	W	T	F	S
				1	2	3
4	5	6	7	8	9	10
11	12	13	14	15	16	17
18	19	20	21	22	23	24
25	26	27	28	29	30	31

Friday, Aug 16th 2019

*Yvonne Wong's talk*

## Indirectly

### Cosmology



$$\sum m_\nu$$

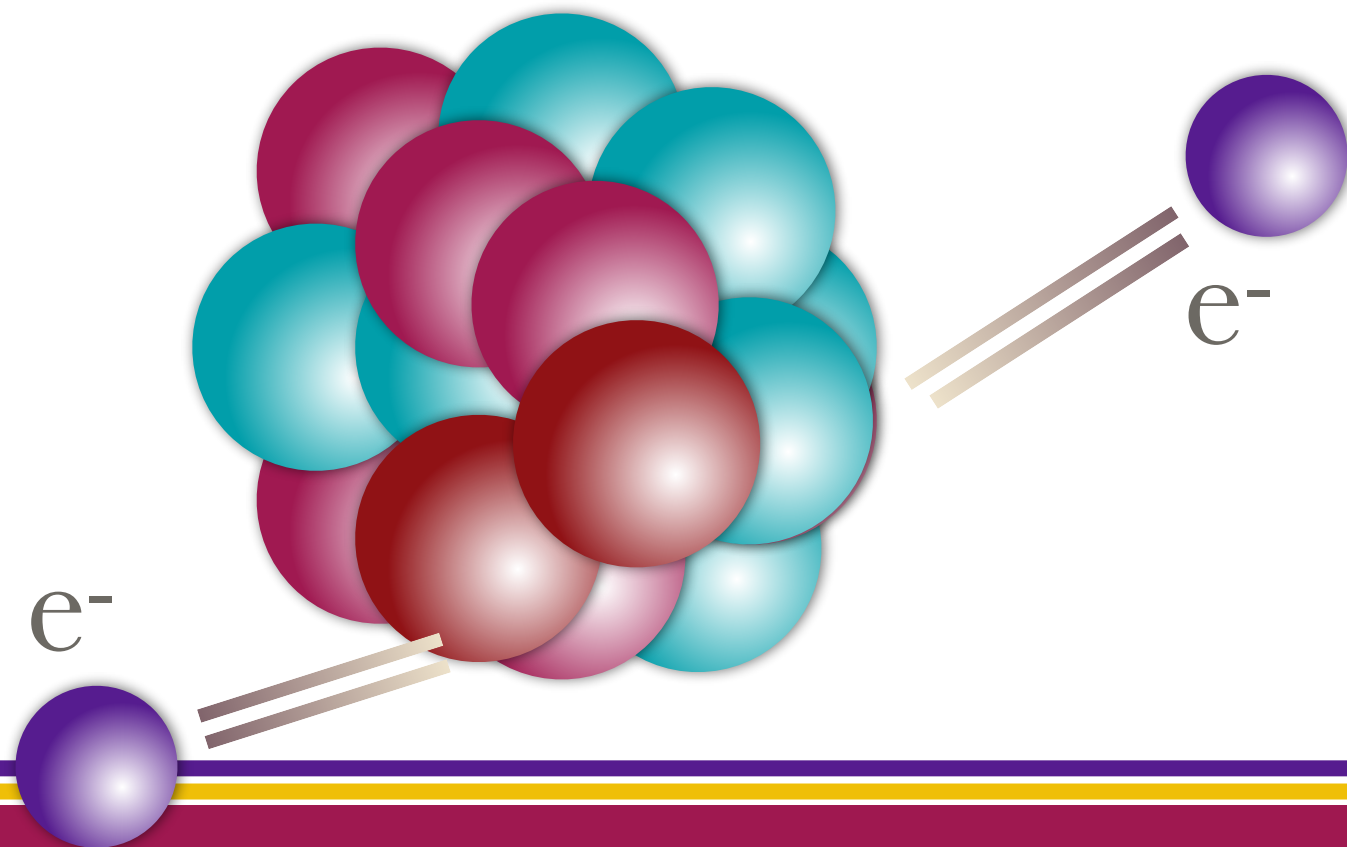
August 2019						
S	M	T	W	T	F	S
				1	2	3
4	5	6	7	8	9	10
11	12	13	14	15	16	17
18	19	20	21	22	23	24
25	26	27	28	29	30	31

Friday, Aug 16th 2019

*Yvonne Wong's talk*

### Neutrinoless double-beta decay

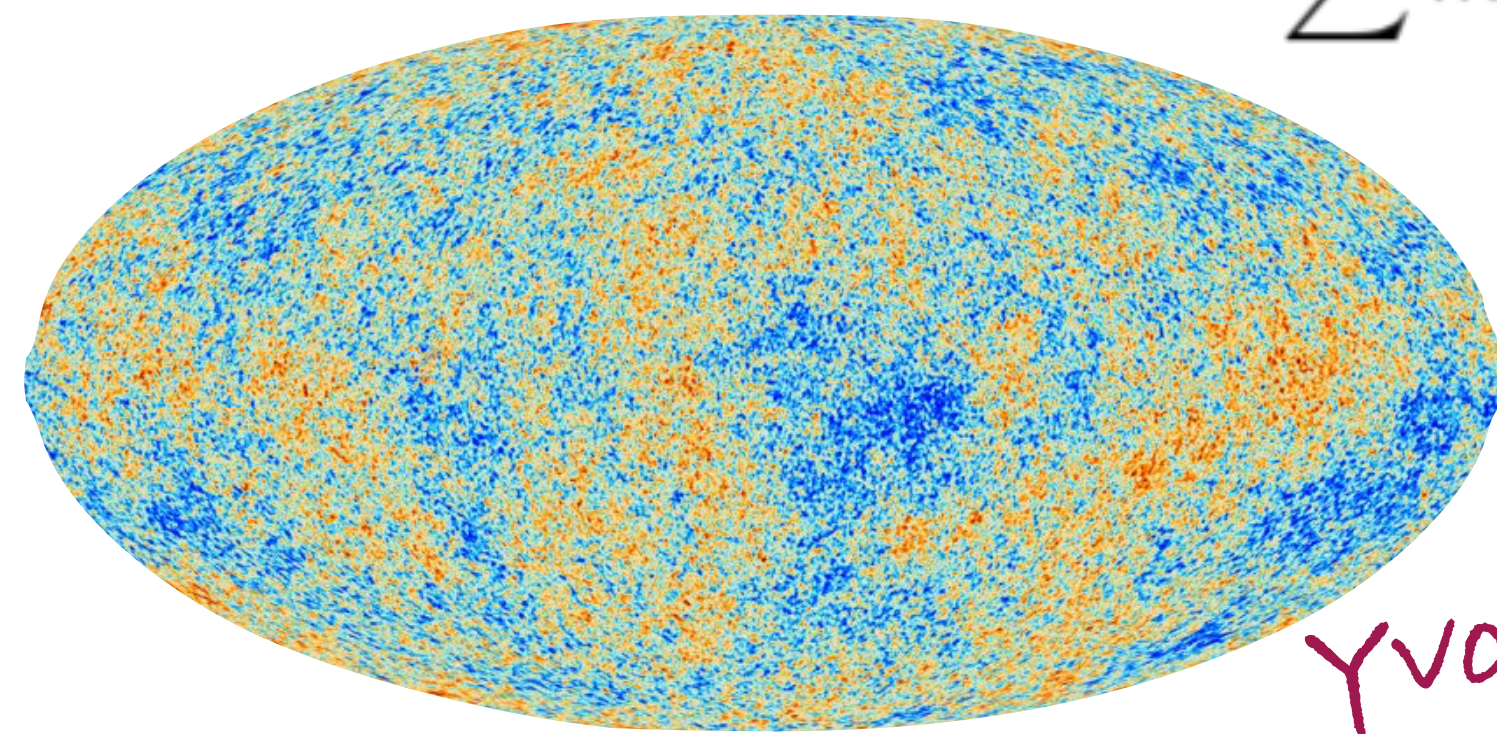
*After the break!*



## Directly

## Indirectly

### Cosmology



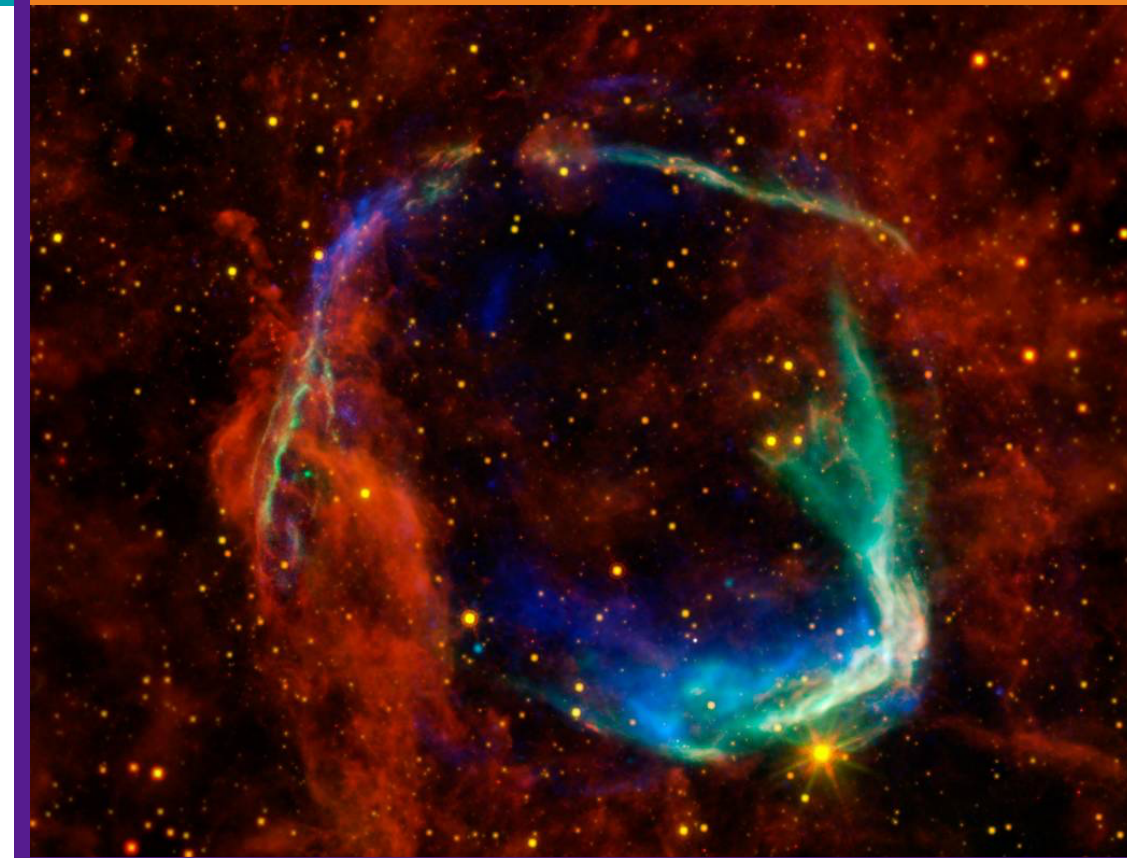
$$\sum m_\nu$$

August 2019						
S	M	T	W	T	F	S
				1	2	3
4	5	6	7	8	9	10
11	12	13	14	15	16	17
18	19	20	21	22	23	24
25	26	27	28	29	30	31

Friday, Aug 16th 2019

*Yvonne Wong's talk*

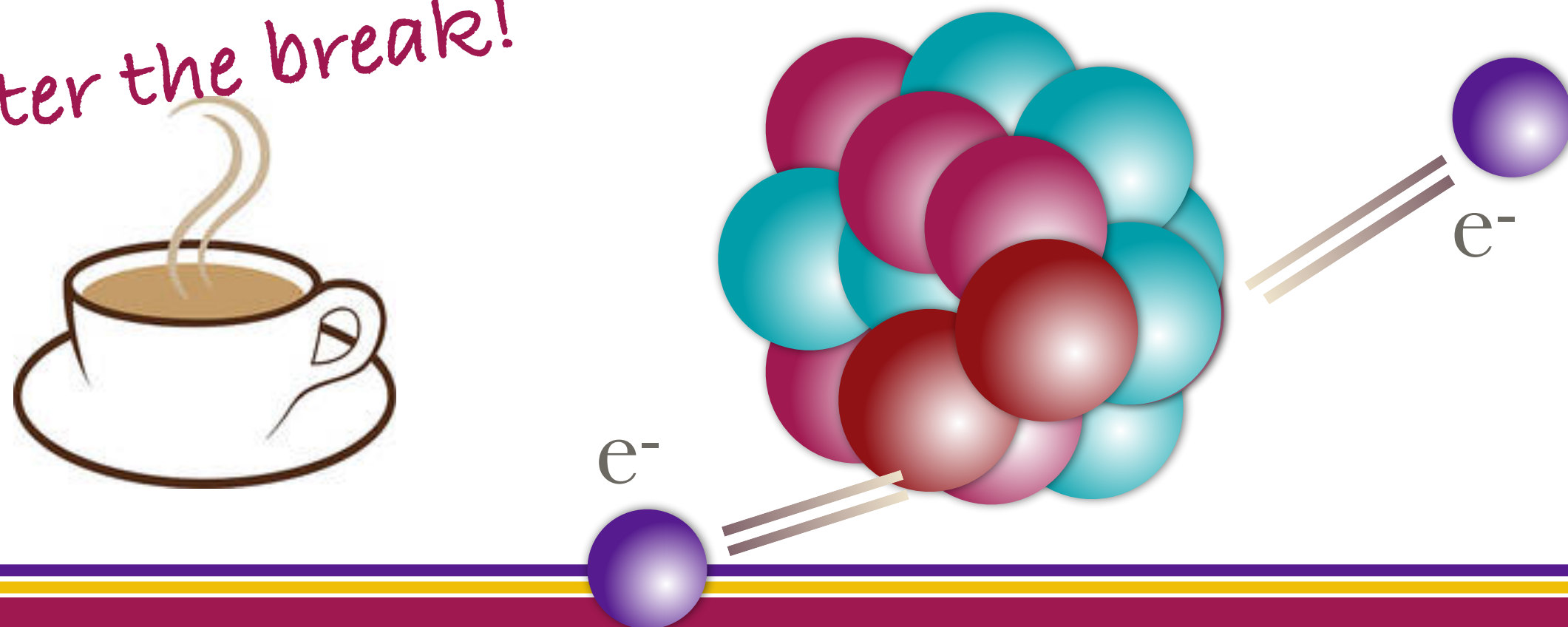
## Directly



### Supernova time-of-flight measurements

### Neutrinoless double-beta decay

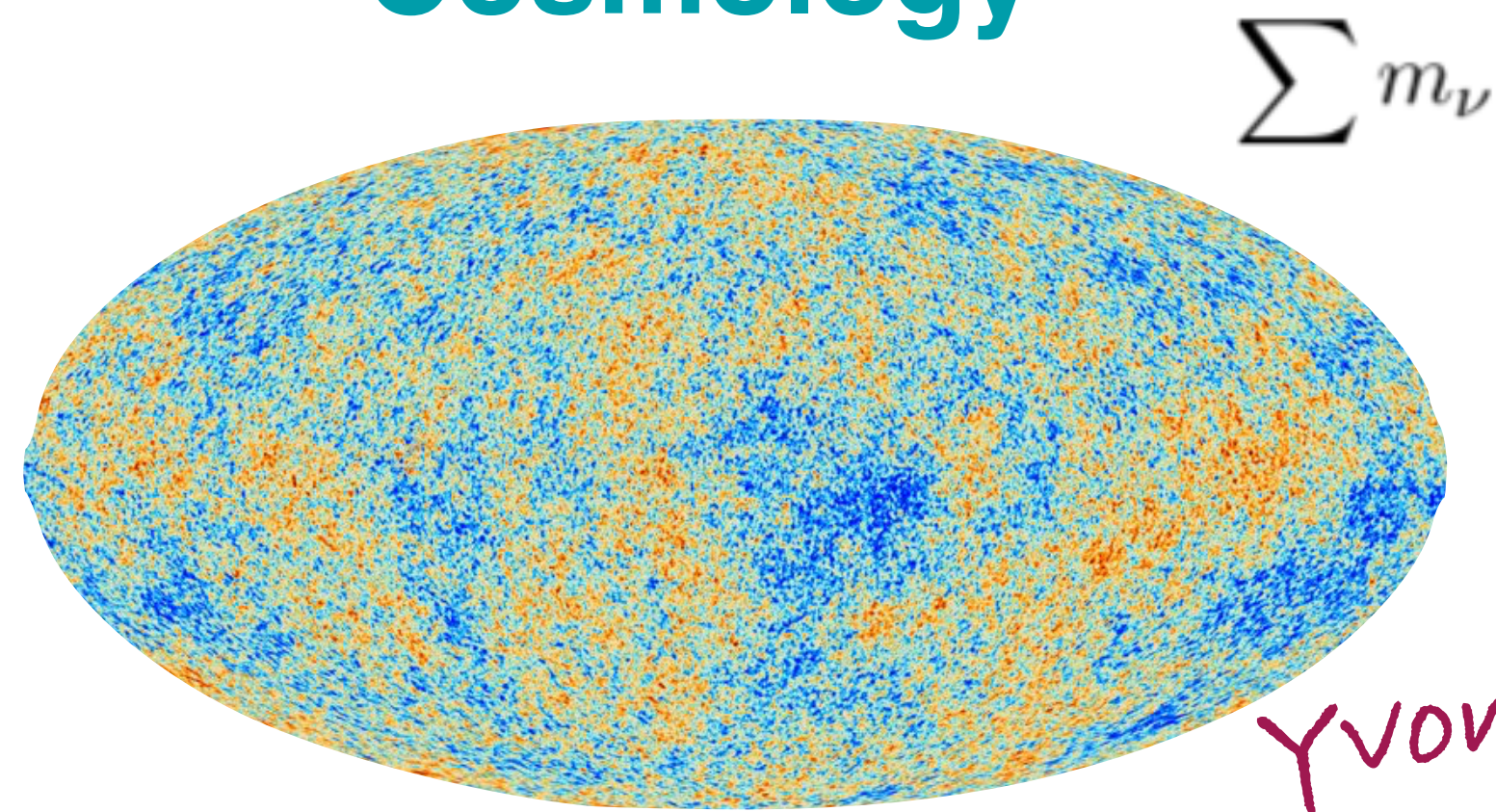
*After the break!*





## Indirectly

### Cosmology



$$\sum m_\nu$$

August 2019						
S	M	T	W	T	F	S
				1	2	3
4	5	6	7	8	9	10
11	12	13	14	15	16	17
18	19	20	21	22	23	24
25	26	27	28	29	30	31

Friday, Aug 16th 2019

*Yvonne Wong's talk*

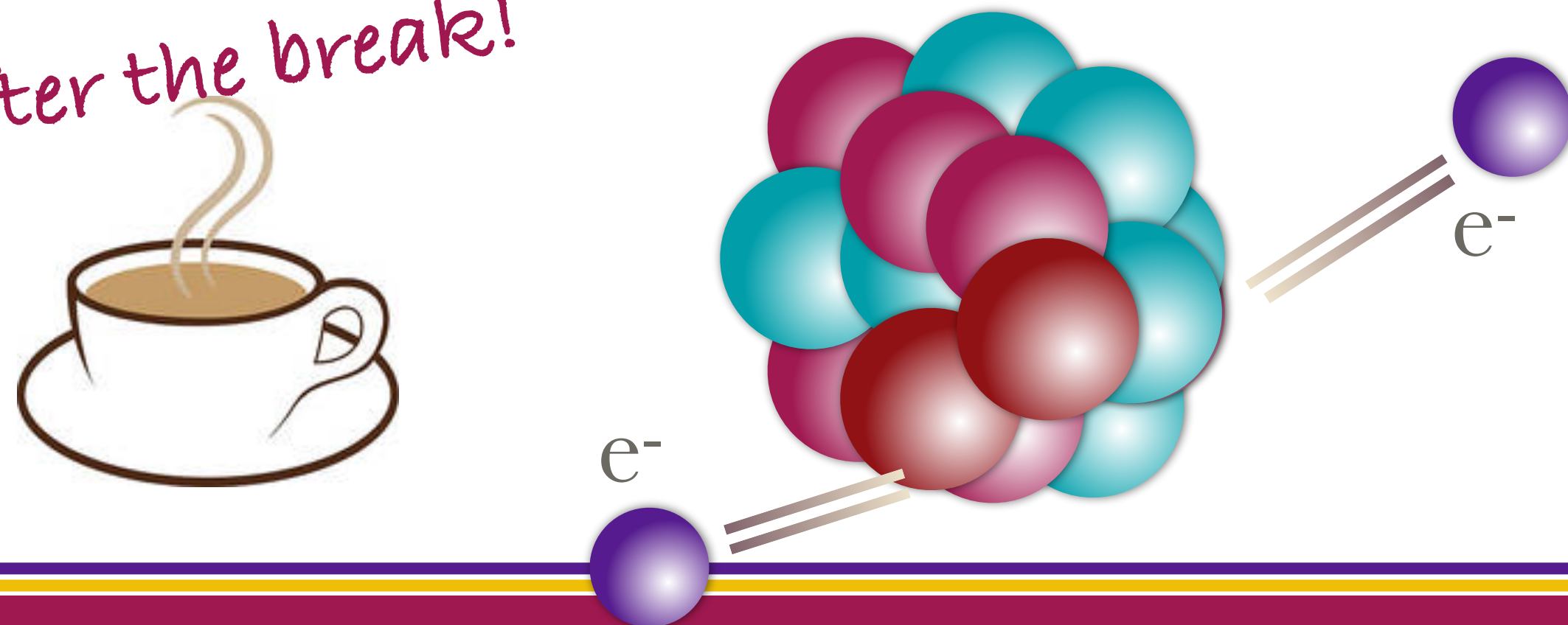
## Directly



Supernova time-of-flight measurements

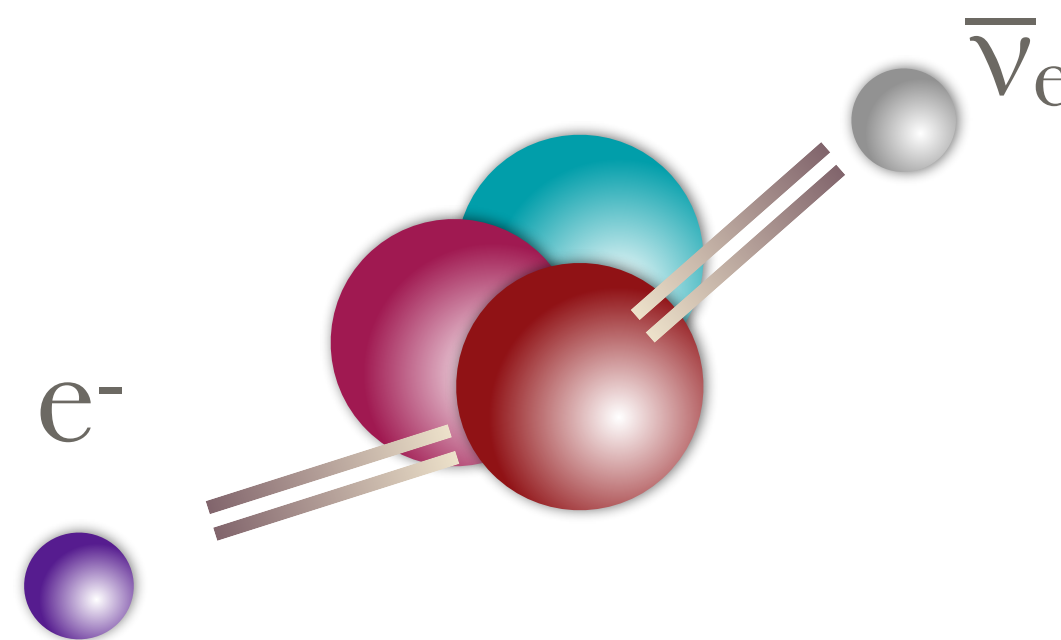
### Neutrinoless double-beta decay

*After the break!*

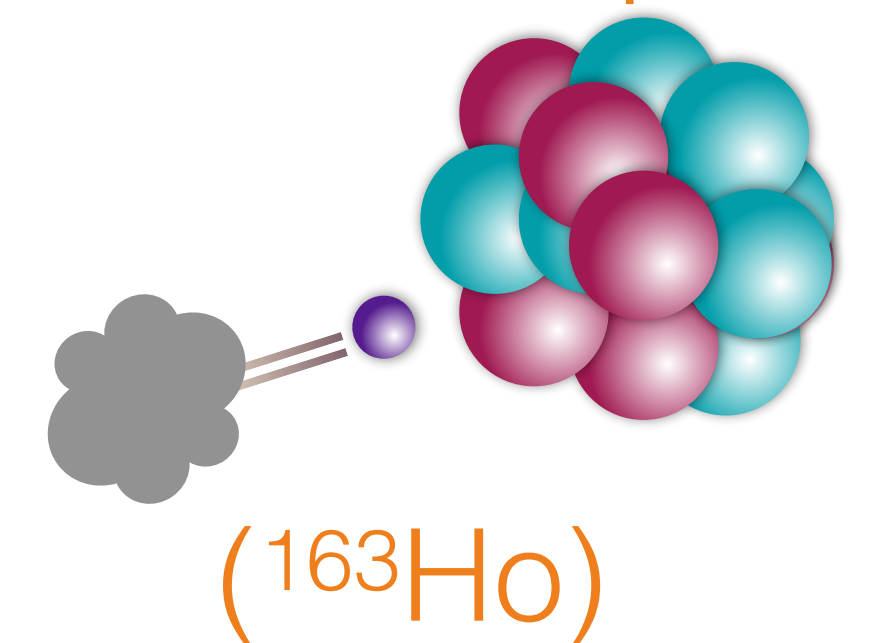


### Weak interaction kinematics

$\beta$  decay (tritium)



Electron capture





SN1987A - European Southern Observatory

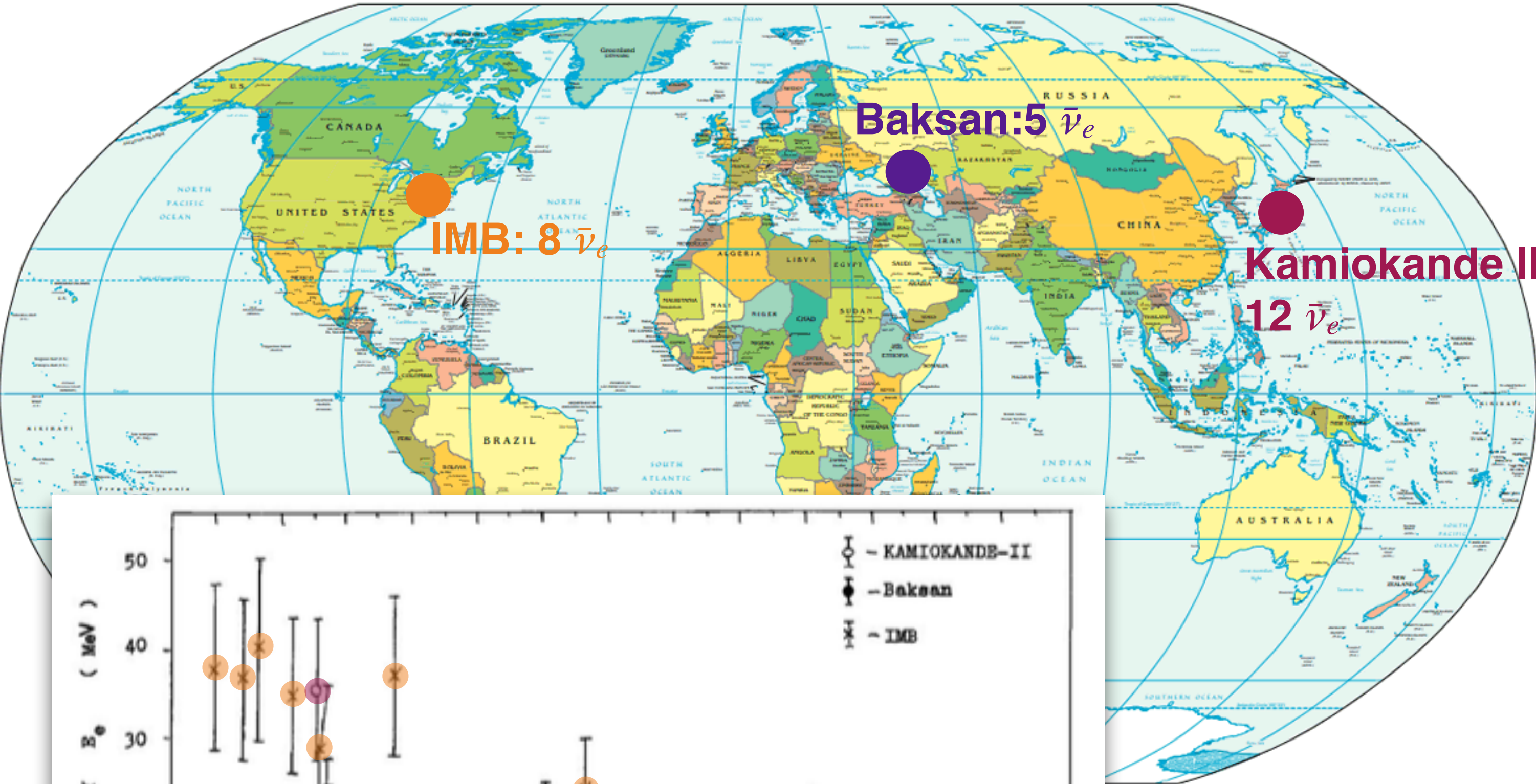
## February 1987

Sun	Mon	Tue	Wed	Thu	Fri	Sat
1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28



Spotted  
Supernova!

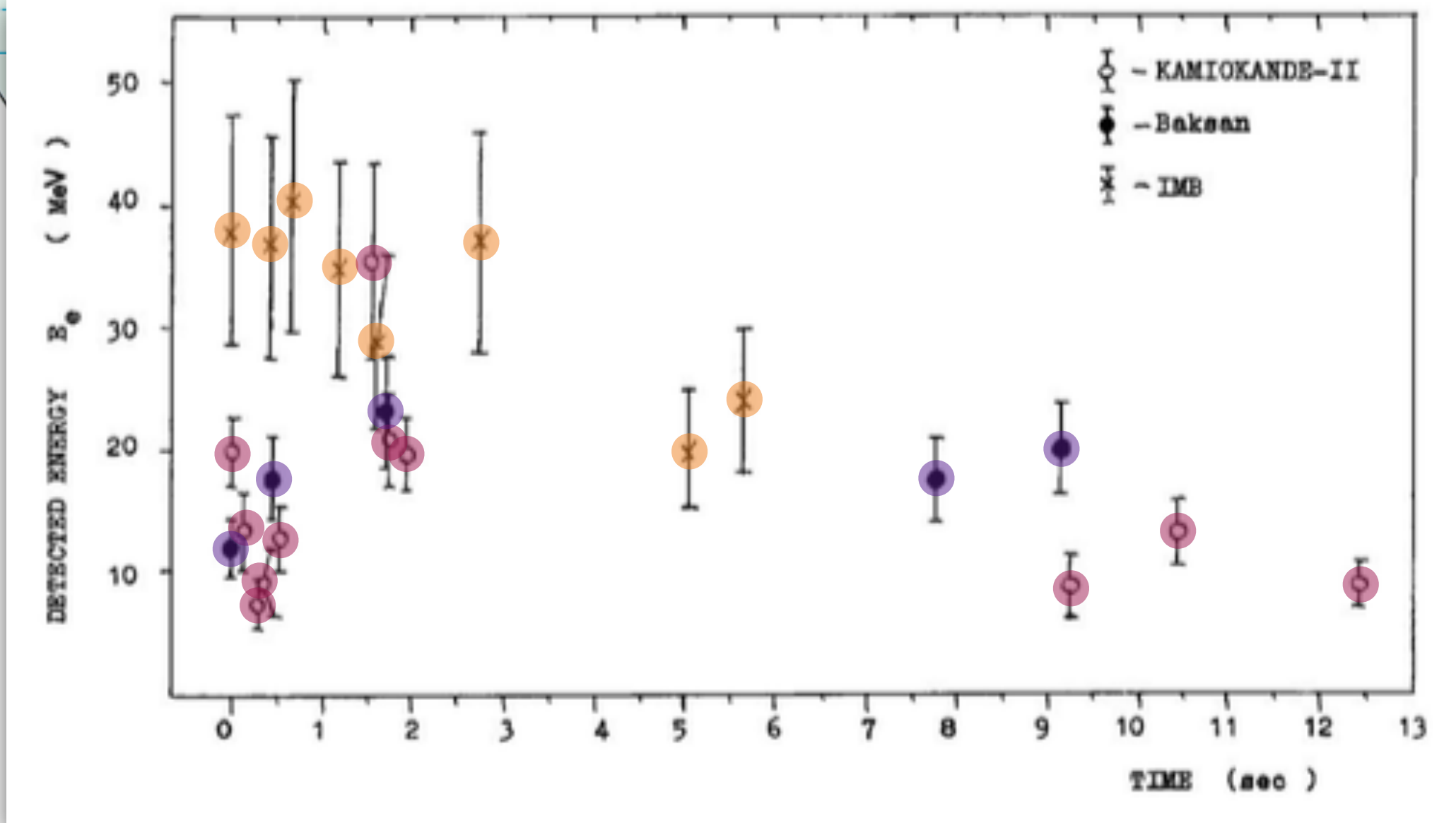
# Supernova time-of-flight measurements



## February 1987

Sun	Mon	Tue	Wed	Thu	Fri	Sat
1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28

**Neutrinos!**  
2-3 hours before the light



- **Neutrinos** emitted at **core collapse**; visible **light** only transmitted once shockwave reaches star's **surface**

# Modelling supernova time-of-flight measurements

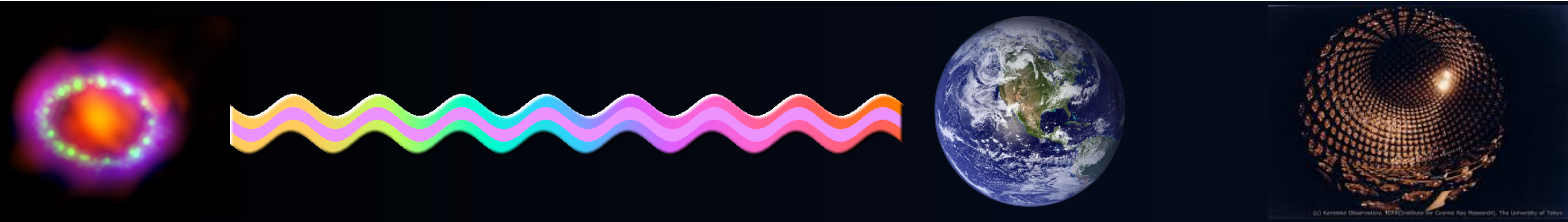
*T Laredo et al, Phys.Rev. D65 (2002) 063002*



## Neutrino emission

## Propagation to Earth

## Detection probability

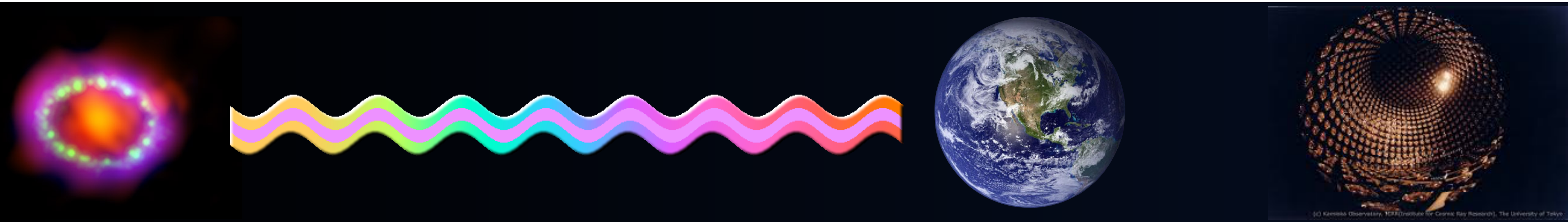


(C) Kamioka Observatory, ICRR(Institute for Cosmic Ray Research), The University of Tokyo

## Neutrino emission

## Propagation to Earth

## Detection probability

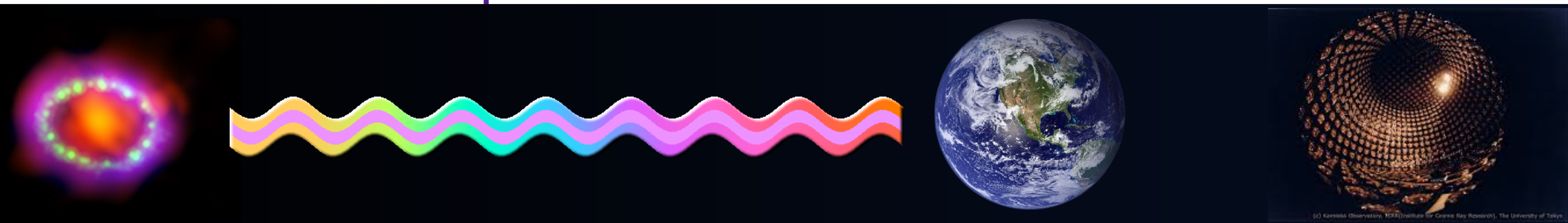


- Two sources:
  - **Cooling** of new neutron star in supernova core
  - Possible: hot, shocked **accreting** matter
- Paper compares 14 different emission models in Bayesian analysis

## Neutrino emission

## Propagation to Earth

## Detection probability



- Two sources:
  - **Cooling** of new neutron star in supernova core
  - Possible: hot, shocked **accreting** matter
- Paper compares 14 different emission models in Bayesian analysis

$$\Phi(E, t^{\text{det}}) = \frac{1}{4\pi D^2} \dot{N}(E, t^{\text{em}})$$

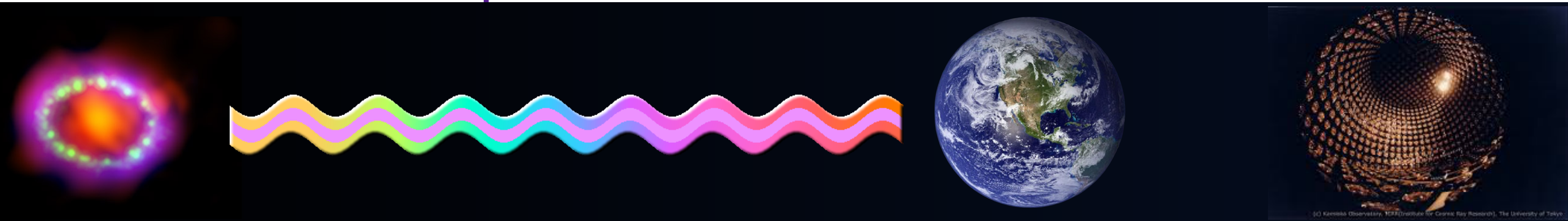
Flux spectrum as function of detected time

Emitted neutrino time and energy spectrum

## Neutrino emission

## Propagation to Earth

## Detection probability



- Two sources:
  - **Cooling** of new neutron star in supernova core
  - Possible: hot, shocked **accreting** matter
- Paper compares 14 different emission models in Bayesian analysis

$$\Phi(E, t^{\text{det}}) = \frac{1}{4\pi D^2} \dot{N}(E, t^{\text{em}})$$

$$t^{\text{det}} = t^{\text{em}} + \Delta t(m_\nu, E) - t^{\text{off}}$$

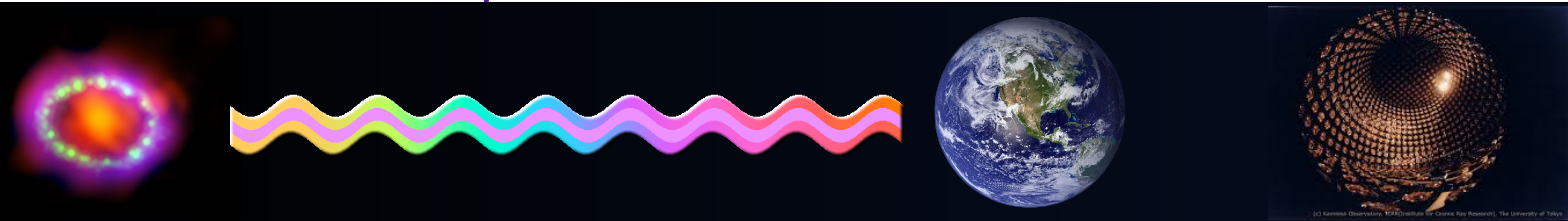
Propagation time depends on energy and  $\bar{\nu}_e$  mass

Clocks on experiments aren't aligned exactly

## Neutrino emission

## Propagation to Earth

## Detection probability



- Two sources:
  - **Cooling** of new neutron star in supernova core
  - Possible: hot, shocked **accreting** matter
- Paper compares 14 different emission models in Bayesian analysis

$$\Phi(E, t^{\text{det}}) = \frac{1}{4\pi D^2} \dot{N}(E, t^{\text{em}})$$

$$t^{\text{det}} = t^{\text{em}} + \Delta t(m_\nu, E) - t^{\text{off}}$$

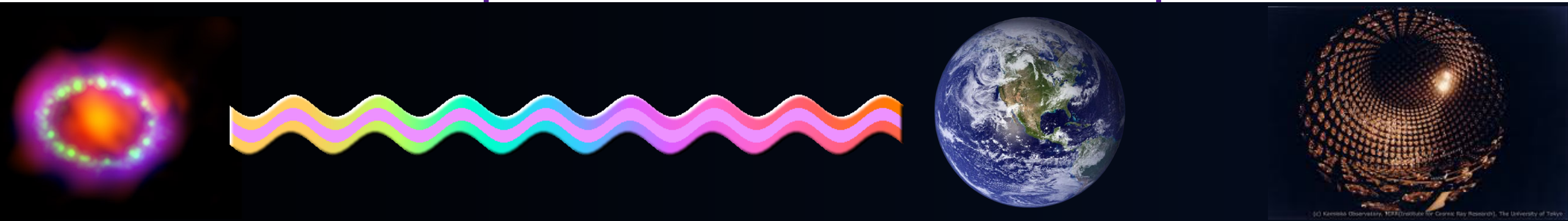
$$\Delta t(m_\nu, E) = 2.57 \left( \frac{m_\nu}{\text{eV}} \right)^2 \left( \frac{E}{\text{MeV}} \right)^{-2} \frac{D}{50 \text{ kpc}} \text{ s}$$



## Neutrino emission

## Propagation to Earth

## Detection probability



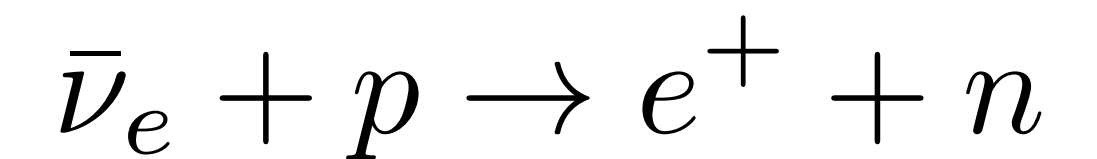
- Two sources:
  - **Cooling** of new neutron star in supernova core
  - Possible: hot, shocked **accreting** matter
- Paper compares 14 different emission models in Bayesian analysis

$$\Phi(E, t^{\text{det}}) = \frac{1}{4\pi D^2} \dot{N}(E, t^{\text{em}})$$

$$t^{\text{det}} = t^{\text{em}} + \Delta t(m_\nu, E) - t^{\text{off}}$$

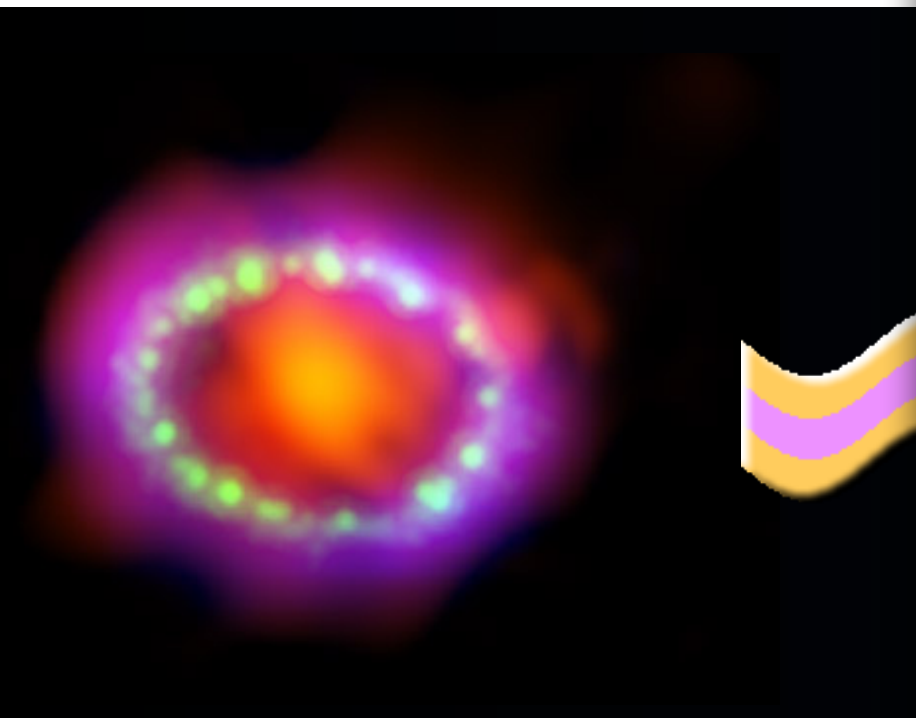
$$\Delta t(m_\nu, E) = 2.57 \left( \frac{m_\nu}{\text{eV}} \right)^2 \left( \frac{E}{\text{MeV}} \right)^{-2} \frac{D}{50 \text{ kpc}} \text{ s.}$$

- Main mechanism:



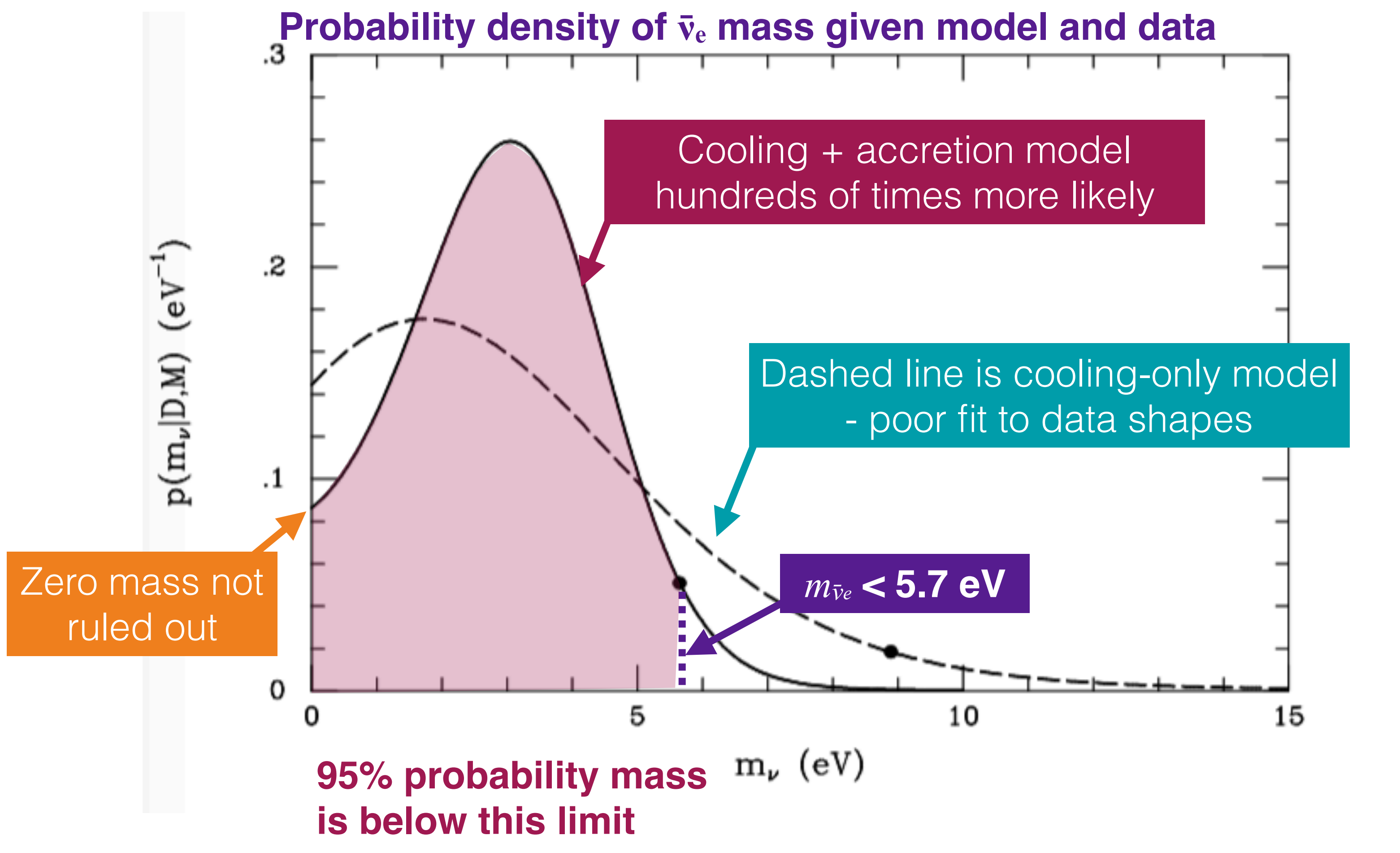
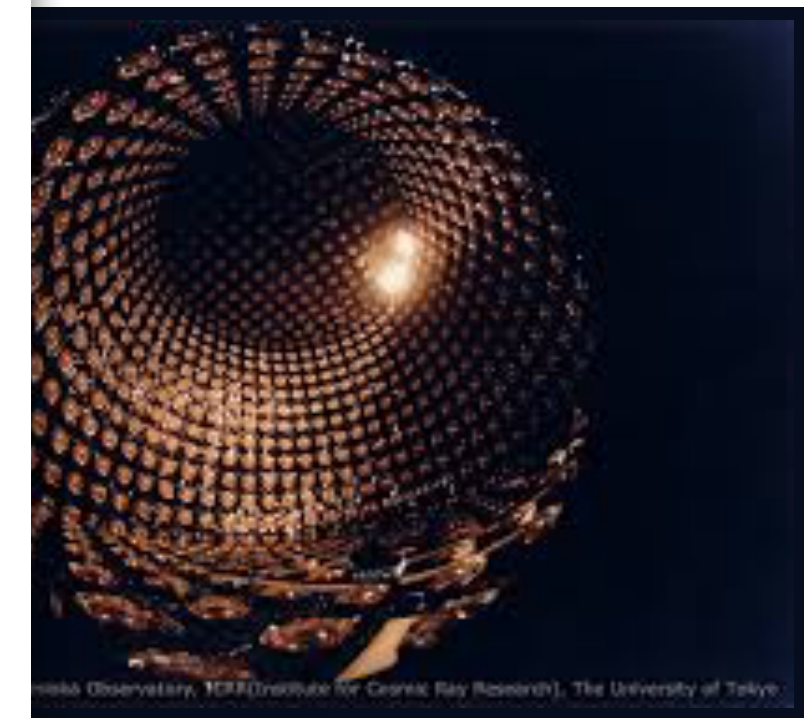
- Event rate depends on interaction **cross section** & **positron detection** efficiency
- Depends on energy & detector design

## Neutrino emission

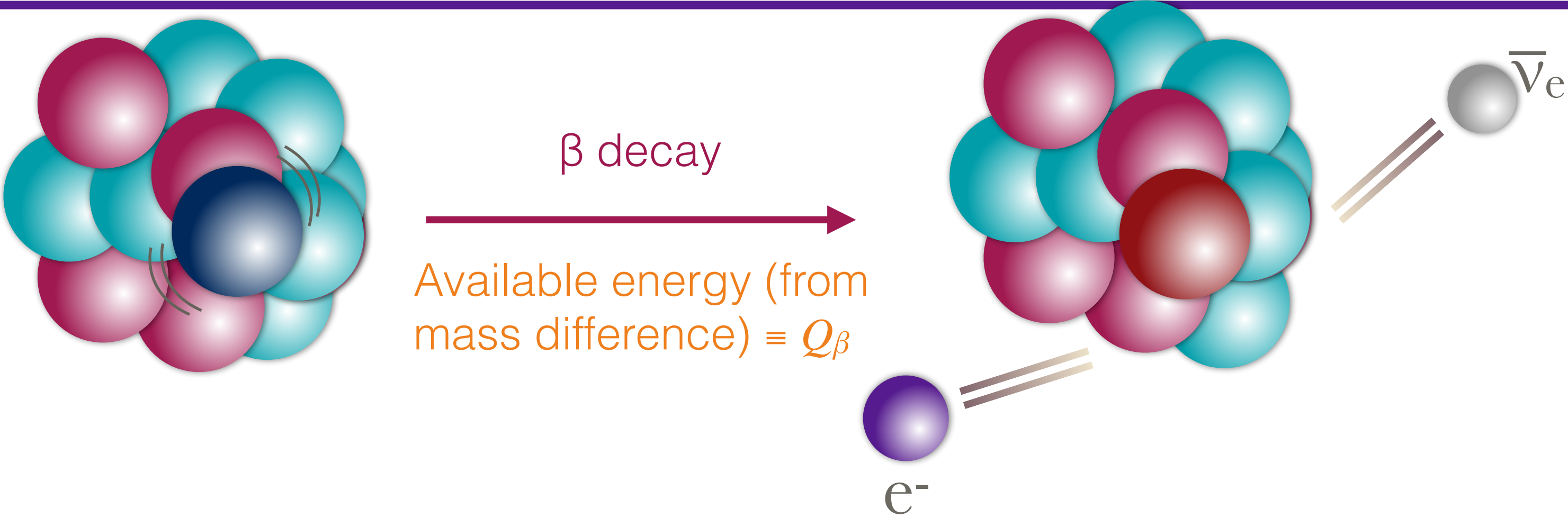


## Propagation to Earth

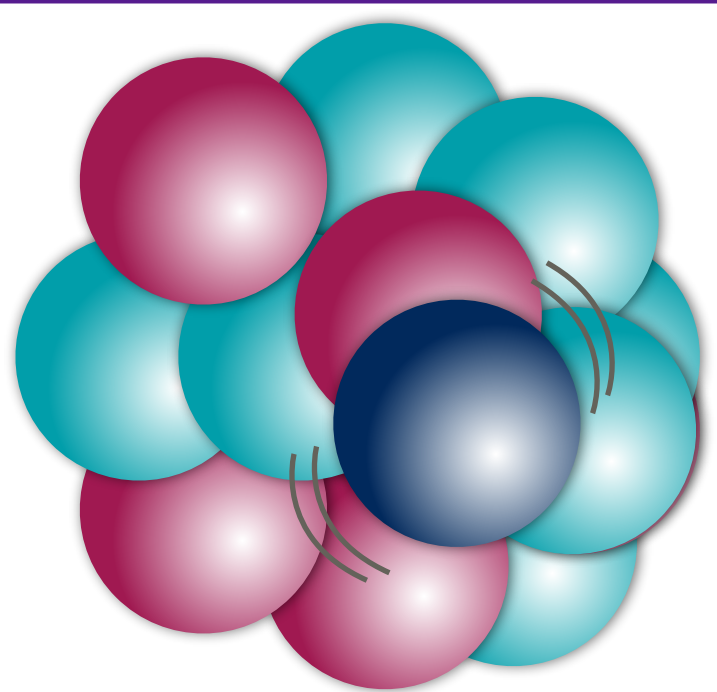
## Detection probability



# Back to basics - looking at beta decay

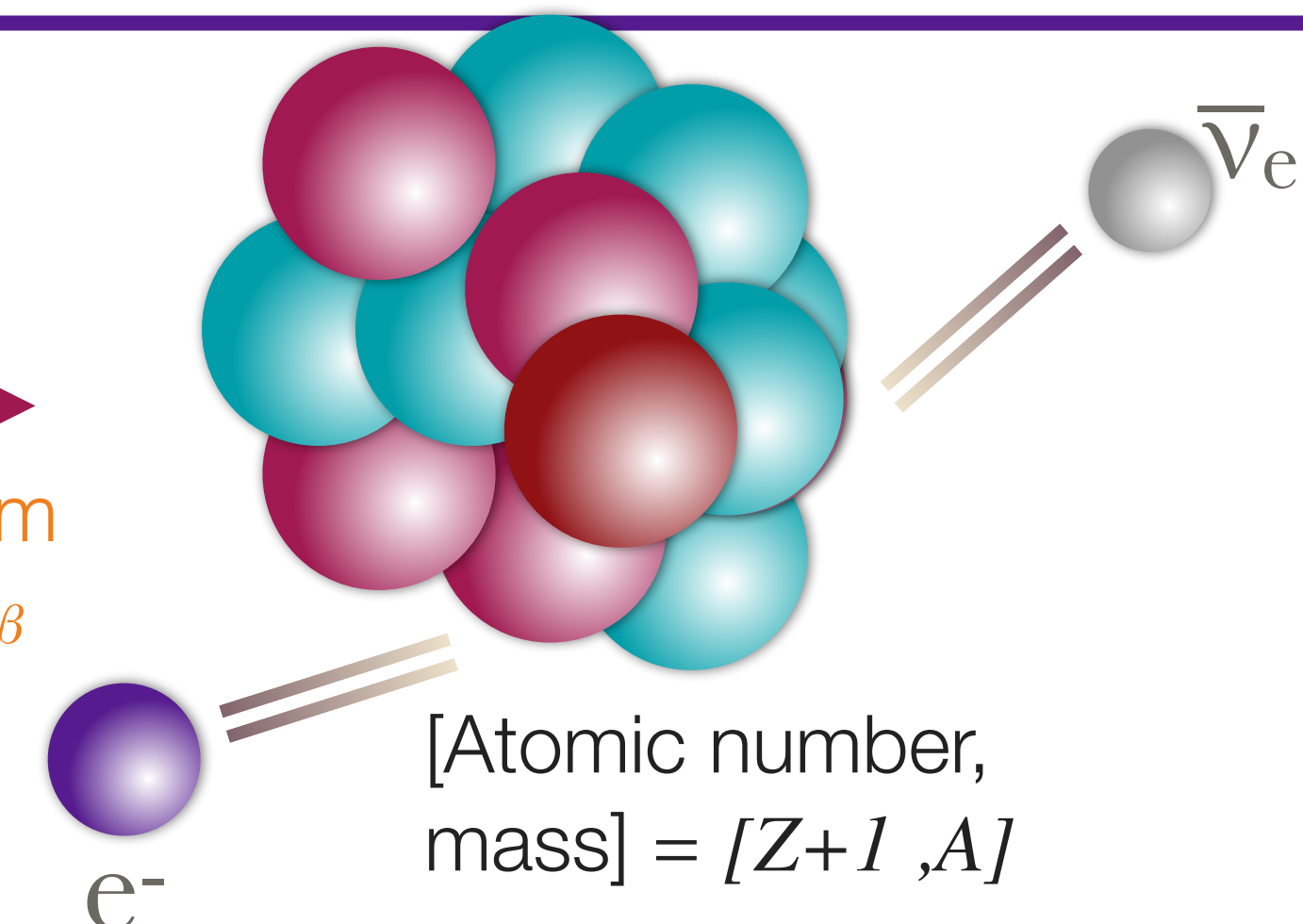


# Back to basics - looking at beta decay



[Atomic number, mass] = [Z, A]

$\beta$  decay  
 Available energy (from mass difference)  $\equiv Q_\beta$



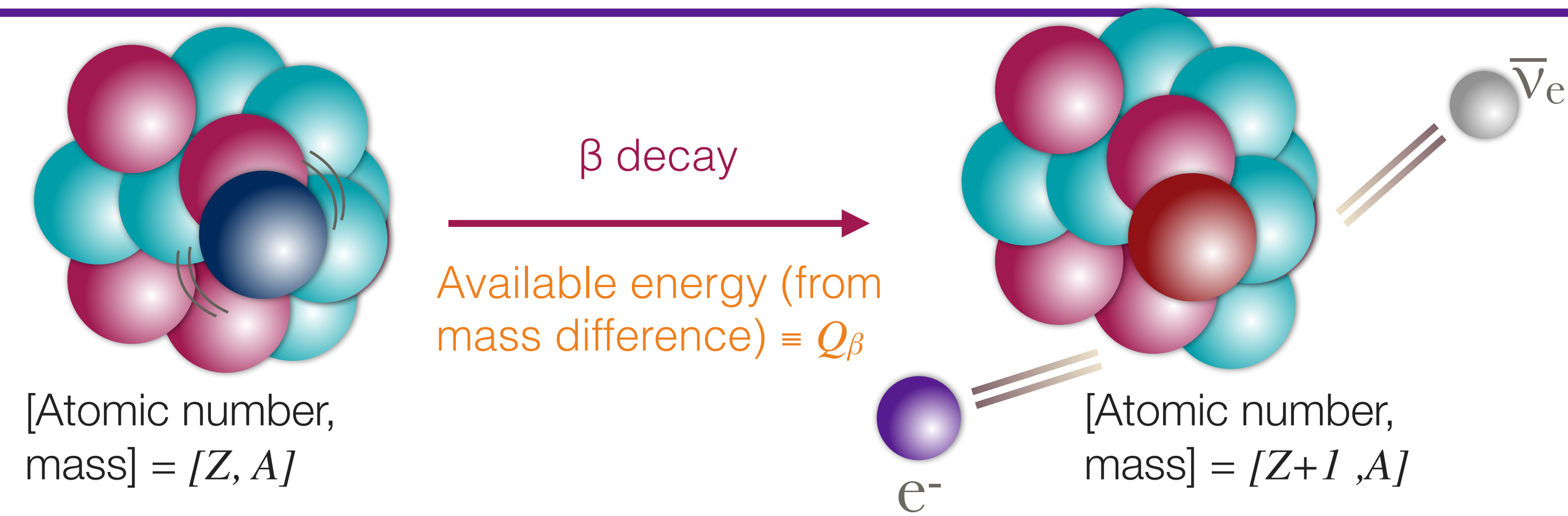
[Atomic number, mass] = [Z+1, A]

Mass of nucleus = mass of atom - mass of electrons

$$Q_\beta = (M [Z,A] - Z m_e) - (M [Z+1,A] - (Z+1) m_e) + m_e$$

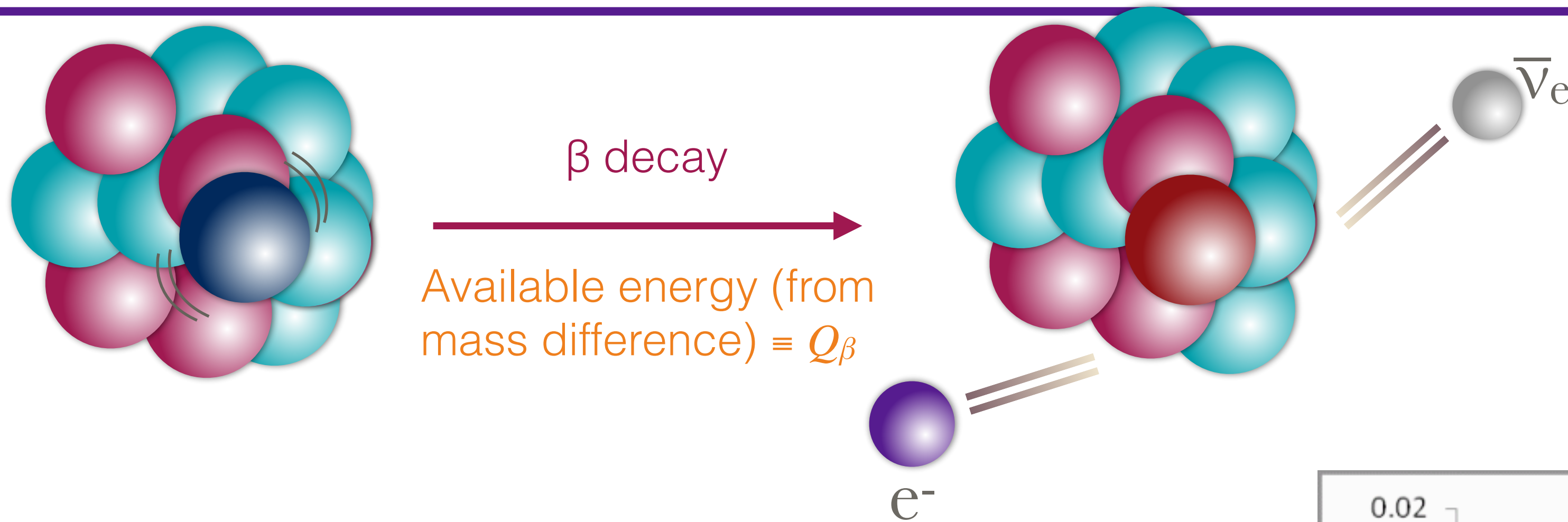
Daughter nucleus +  $\beta$  electron

# Back to basics - looking at beta decay



$$Q_\beta = ( M [Z,A] - Z m_e ) - ( M [Z+1,A] - (Z+1) m_e ) + m_e$$
$$= ( M [Z,A] - M [Z+1,A] )$$

# Back to basics - looking at beta decay



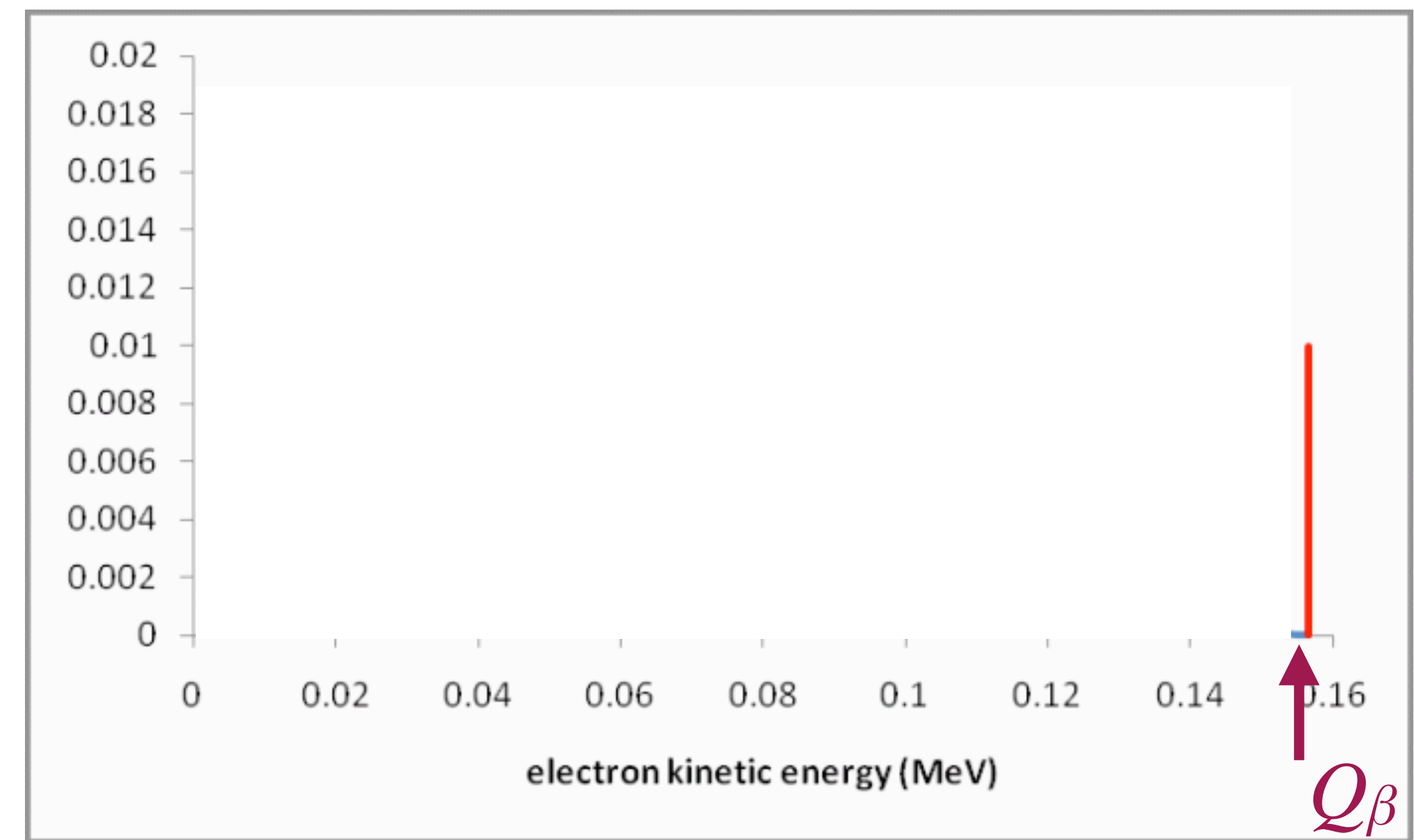
$$Q_\beta = ( M [Z,A] - Z m_e ) - ( M [Z+1,A] - (Z+1) m_e ) + m_e$$

$$= ( M [Z,A] - M [Z+1,A] )$$

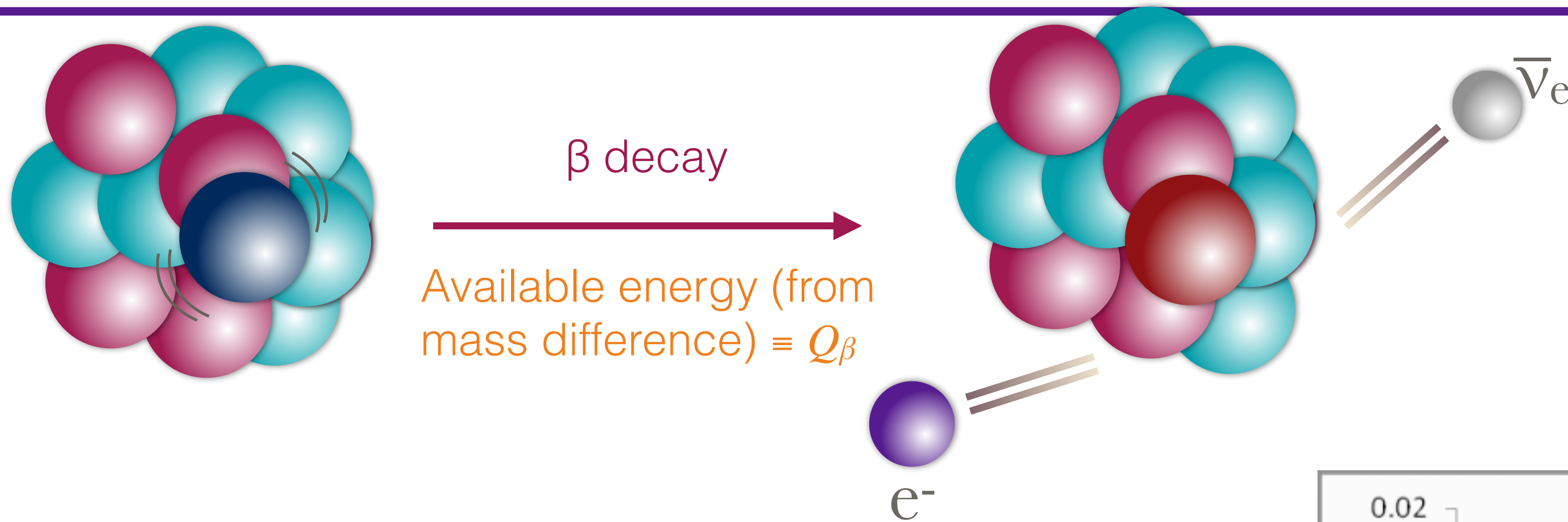


I have done a terrible thing, I have postulated a particle that cannot be detected.

Wolfgang Pauli, 1930



# Back to basics - looking at beta decay



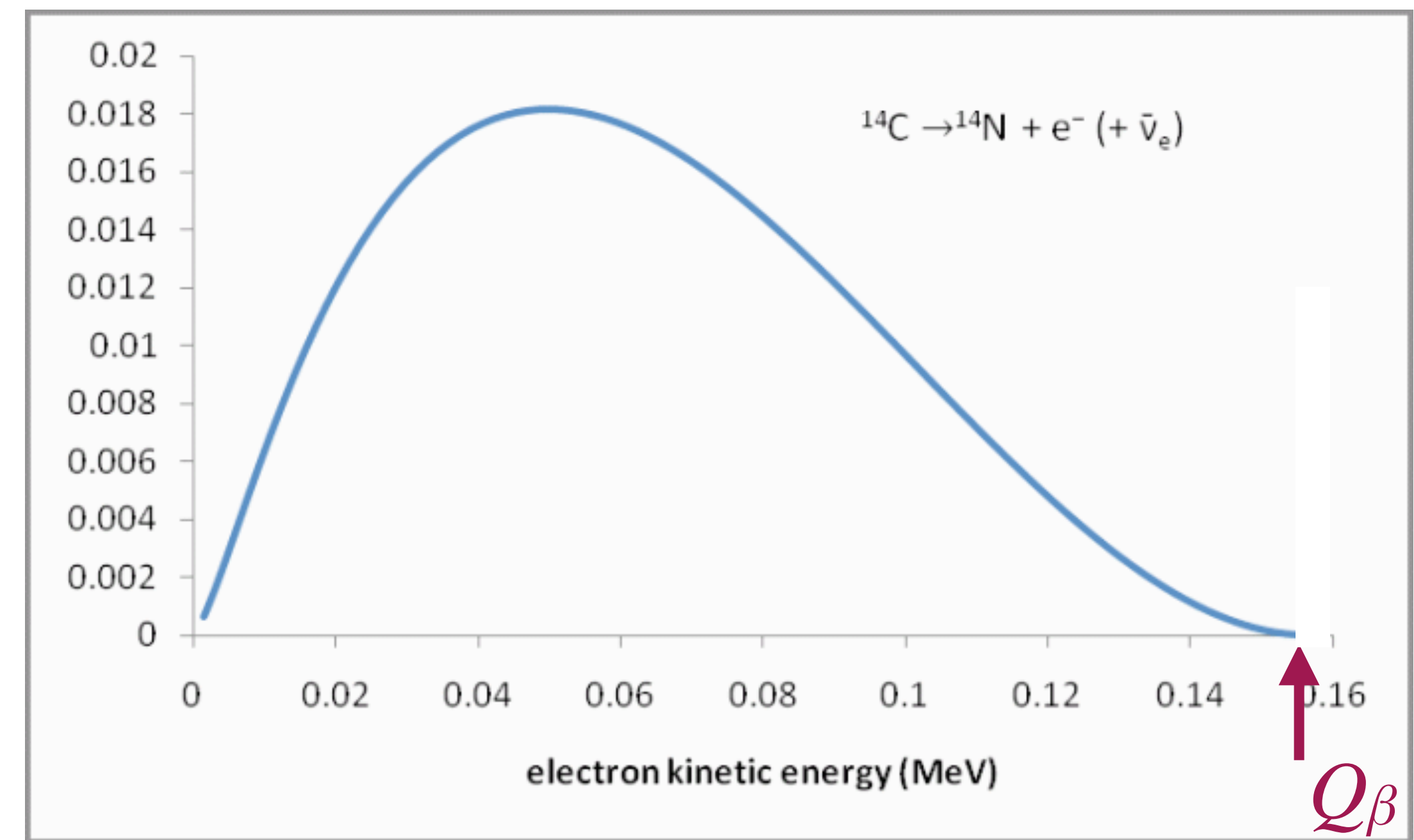
$$Q_\beta = ( M [Z,A] - Z m_e ) - ( M [Z+1,A] - (Z+1) m_e ) + m_e$$

$$= ( M [Z,A] - M [Z+1,A] )$$

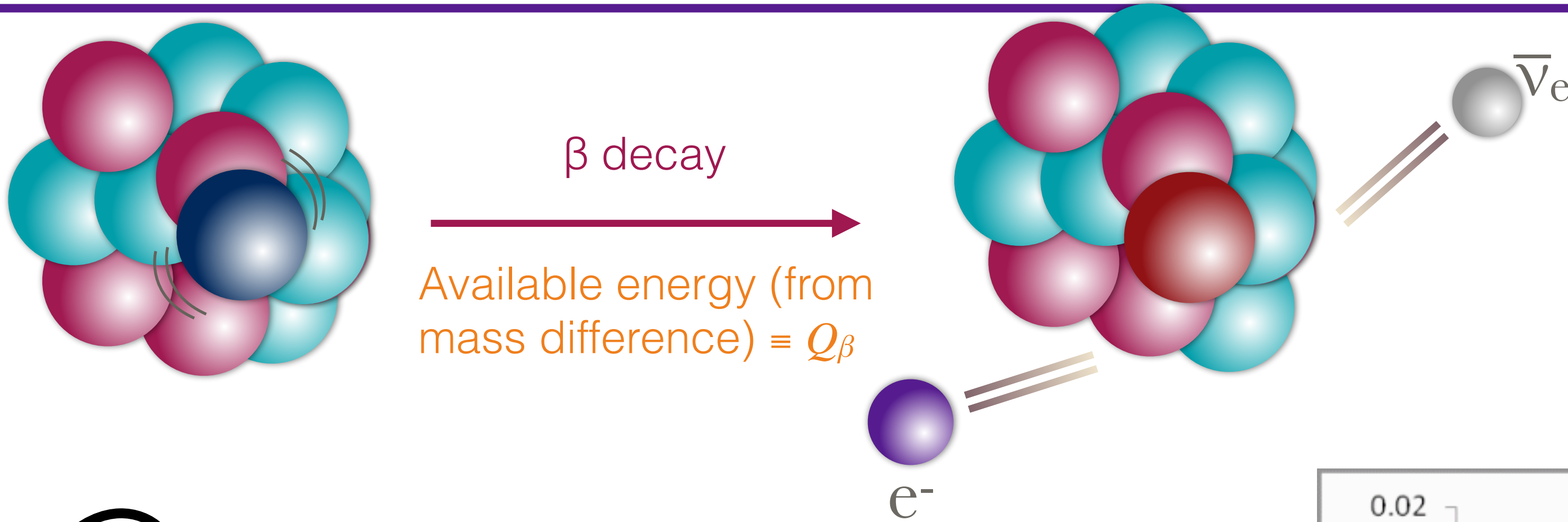


I have done a terrible thing, I have postulated a particle that cannot be detected.

Wolfgang Pauli, 1930

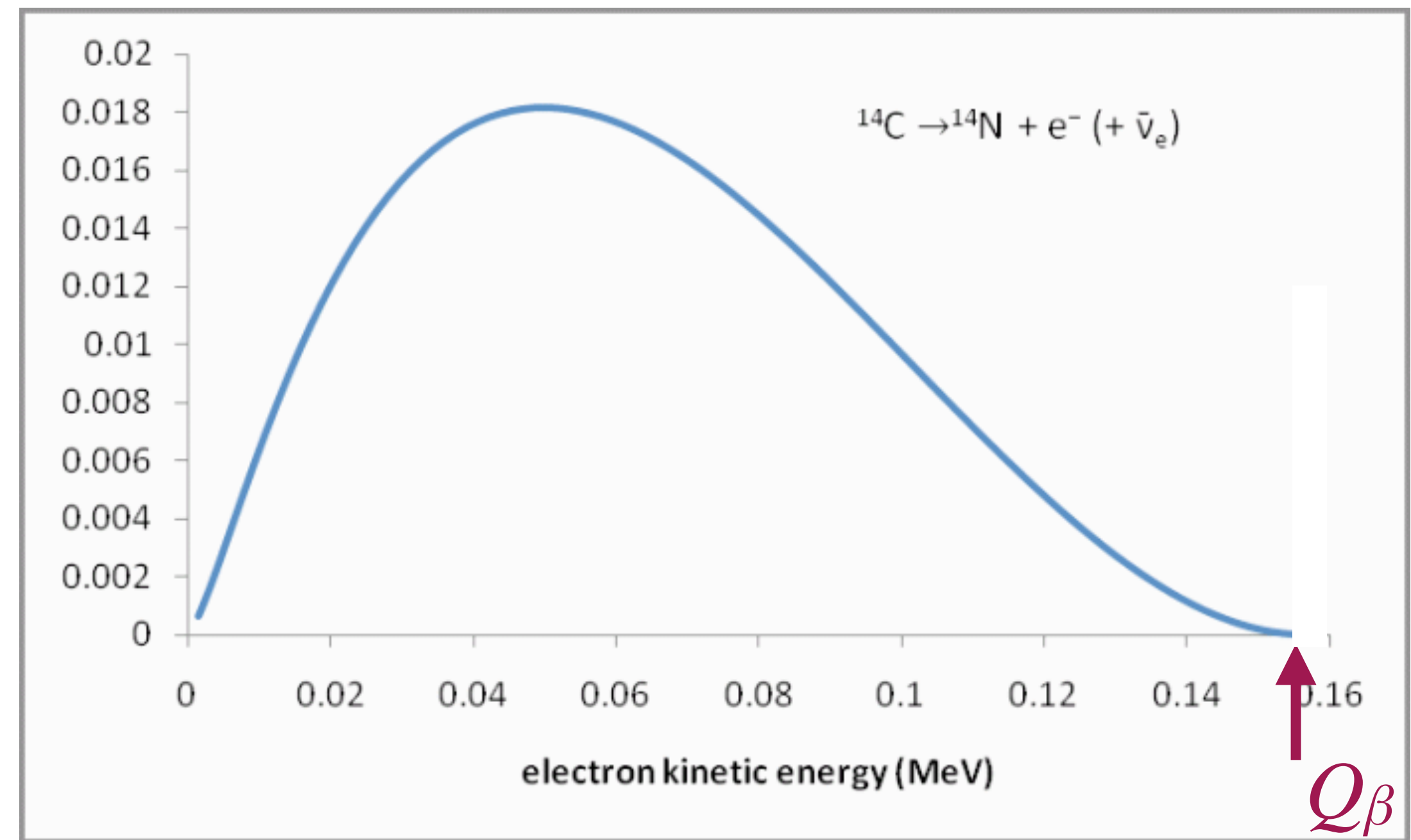
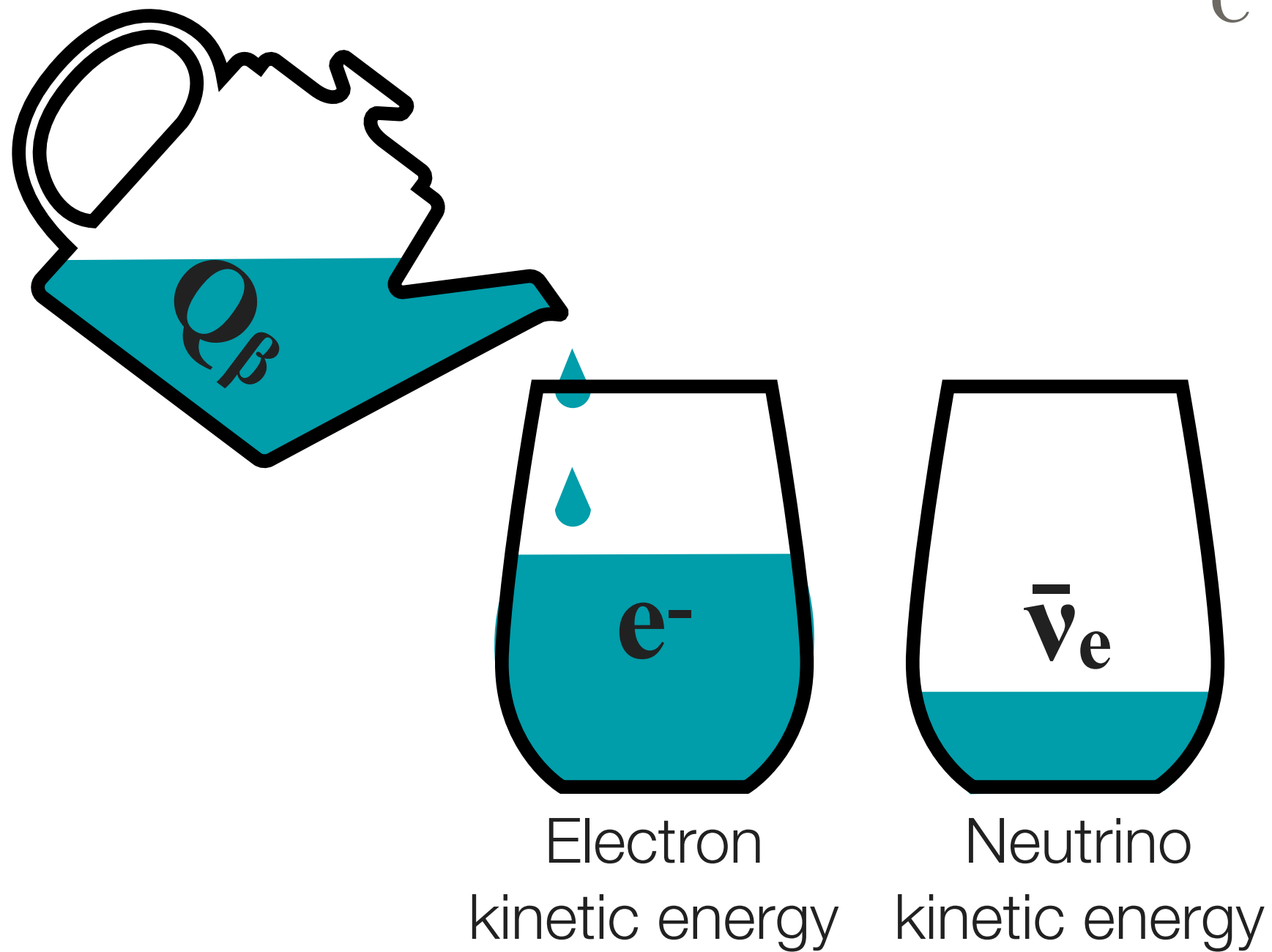


# Back to basics - looking at beta decay



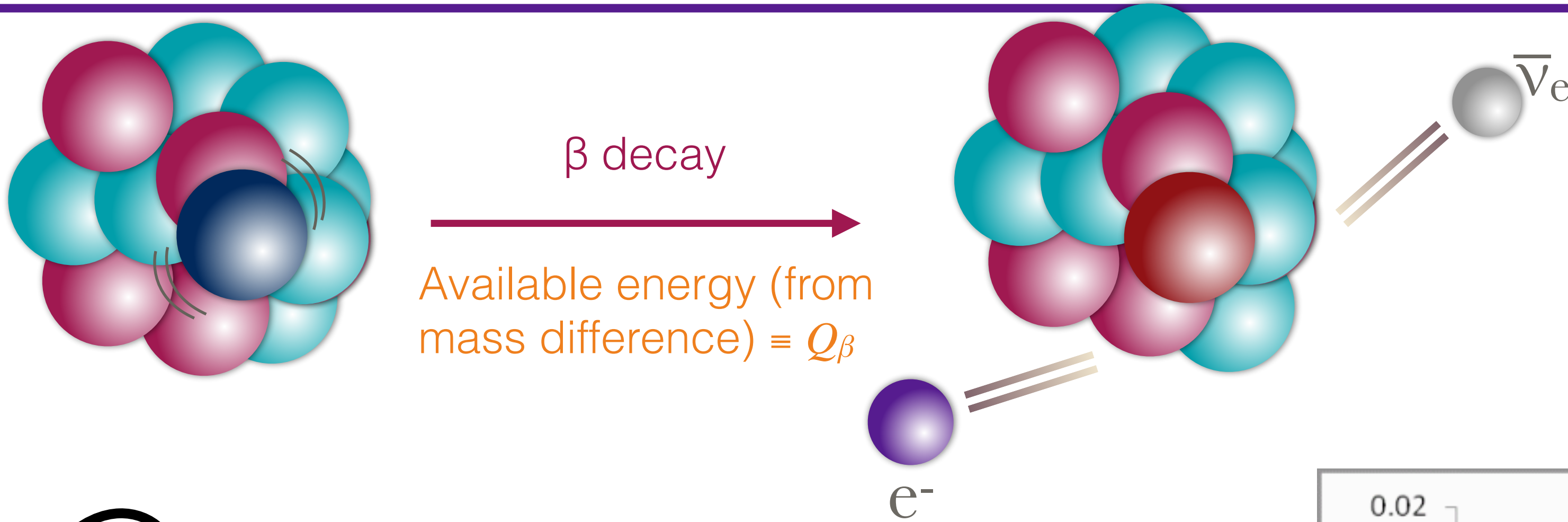
$$Q_\beta = ( M [Z,A] - Z m_e ) - ( M [Z+1,A] - (Z+1) m_e ) + m_e$$

$$= ( M [Z,A] - M [Z+1,A] )$$



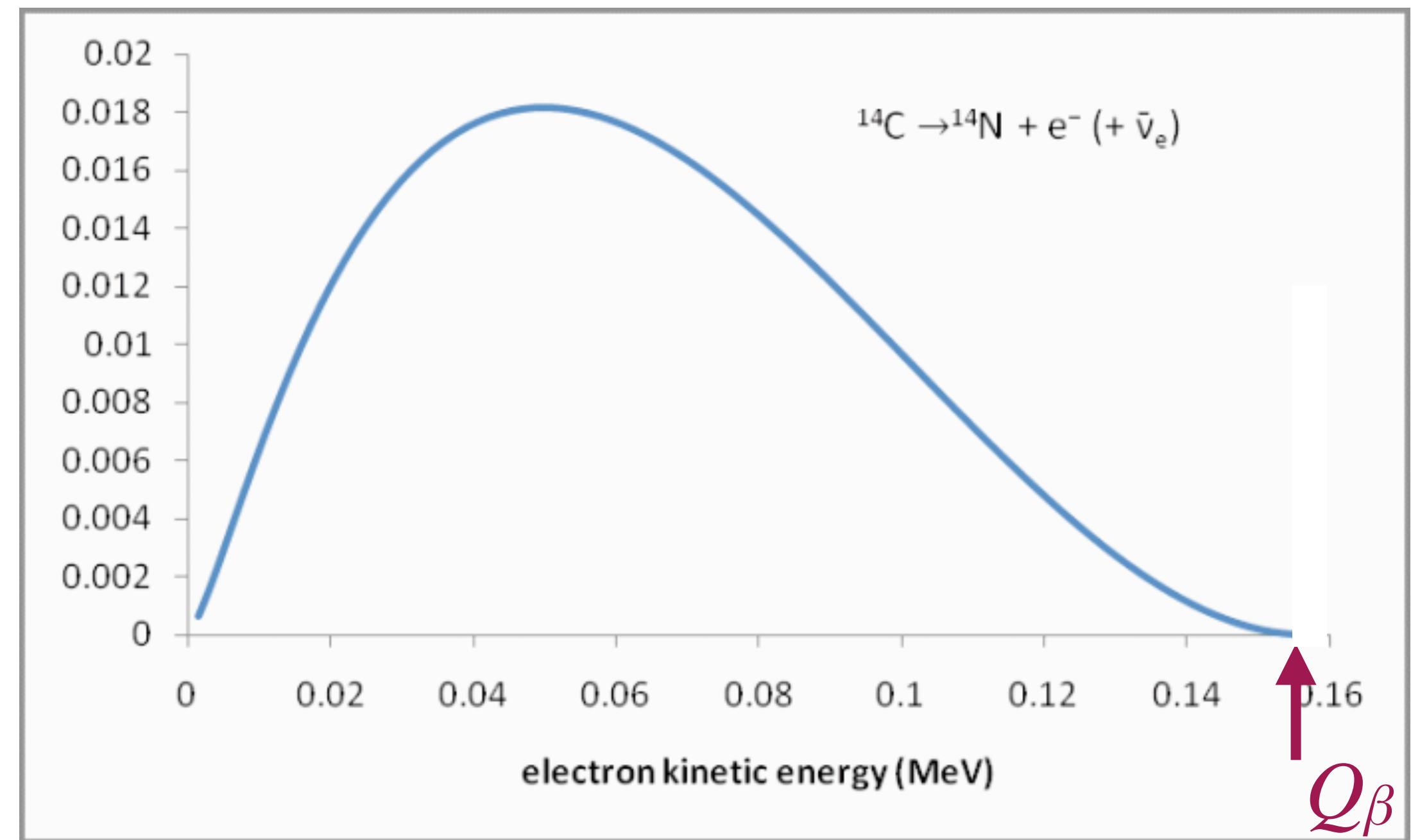
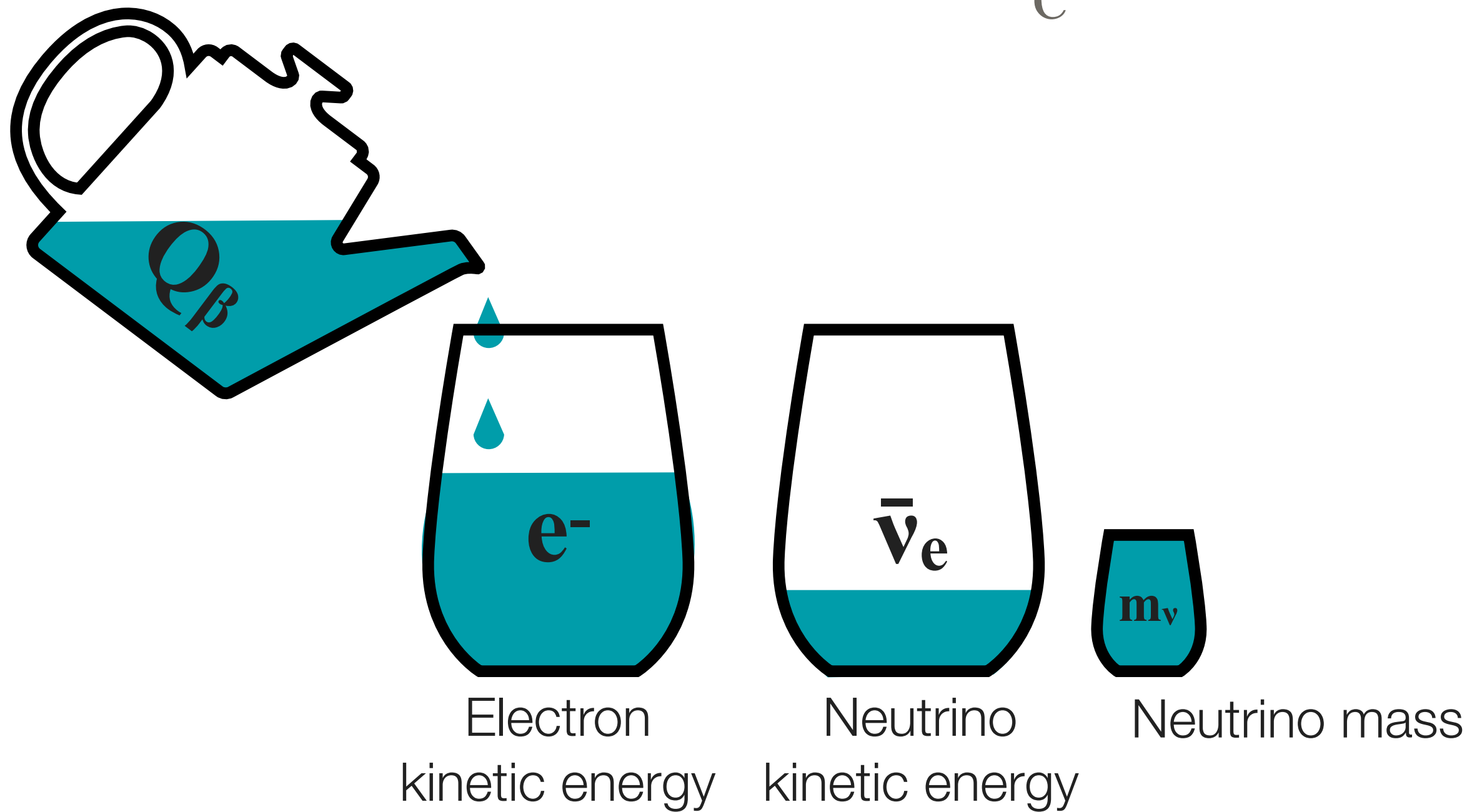


# Back to basics - looking at beta decay

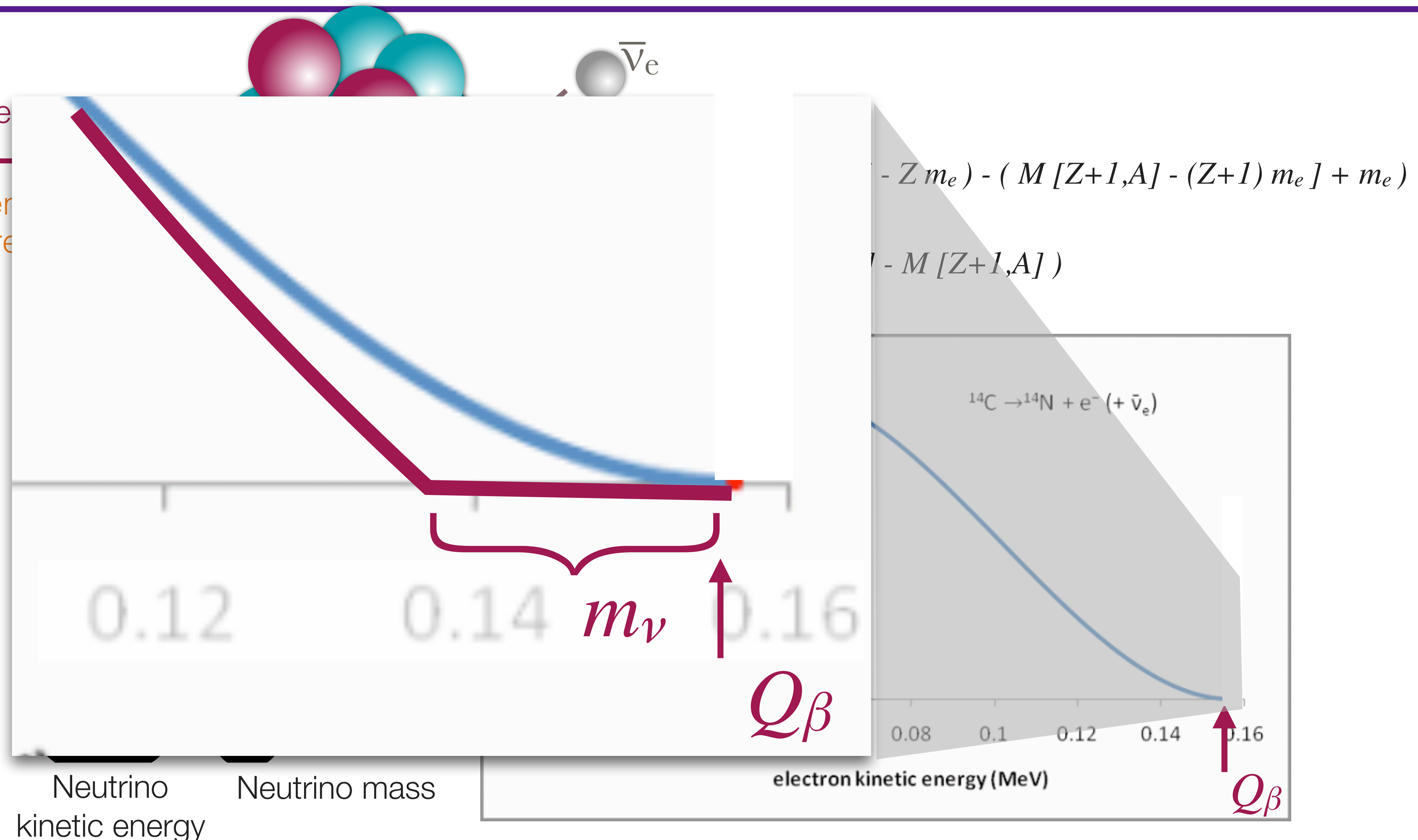


$$Q_\beta = ( M [Z,A] - Z m_e ) - ( M [Z+1,A] - (Z+1) m_e ) + m_e$$

$$= ( M [Z,A] - M [Z+1,A] )$$



# Back to basics - looking at beta decay



NATURE

August 21, 1948 Vol. 162

### Beta Spectrum of Tritium

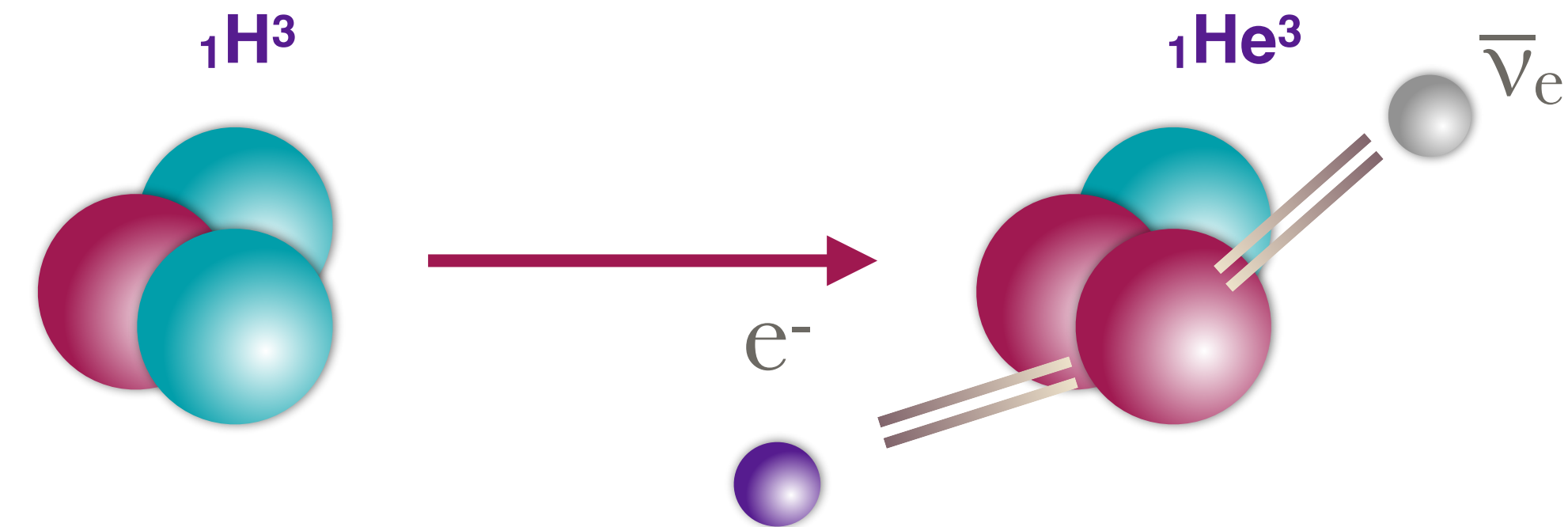
THE  $\beta$ -spectrum of tritium ( $^3_1\text{H}$ ) is of particular interest because: (1) the relatively simple structure of the  $^3_1\text{H}$  nucleus makes it well suited to a test of the Fermi theory of  $\beta$ -decay; (2) the unusually low energy of the  $\beta$ -particles means that the shape of the spectrum near the upper limit is an extremely sensitive function of the rest mass of the neutrino if the Fermi theory is confirmed; (3) a theoretical discrepancy<sup>1</sup> exists between the half-life<sup>2</sup> and the upper energy limit, as recently measured<sup>3</sup>; (4) the mass difference ( $^3_1\text{H} - ^3_2\text{He}$ ) can be accurately determined.

NATURE

August 21, 1948 Vol. 162

## Beta Spectrum of Tritium

THE  $\beta$ -spectrum of tritium ( ${}^3_1\text{H}$ ) is of particular interest because: (1) the relatively simple structure of the  ${}^3_1\text{H}$  nucleus makes it well suited to a test of the Fermi theory of  $\beta$ -decay; (2) the unusually low energy of the  $\beta$ -particles means that the shape of the spectrum near the upper limit is an extremely sensitive function of the rest mass of the neutrino if the Fermi theory is confirmed; (3) a theoretical discrepancy<sup>1</sup> exists between the half-life<sup>2</sup> and the upper energy limit, as recently measured<sup>3</sup>; (4) the mass difference ( ${}^3_1\text{H} - {}^3_2\text{He}$ ) can be accurately determined.



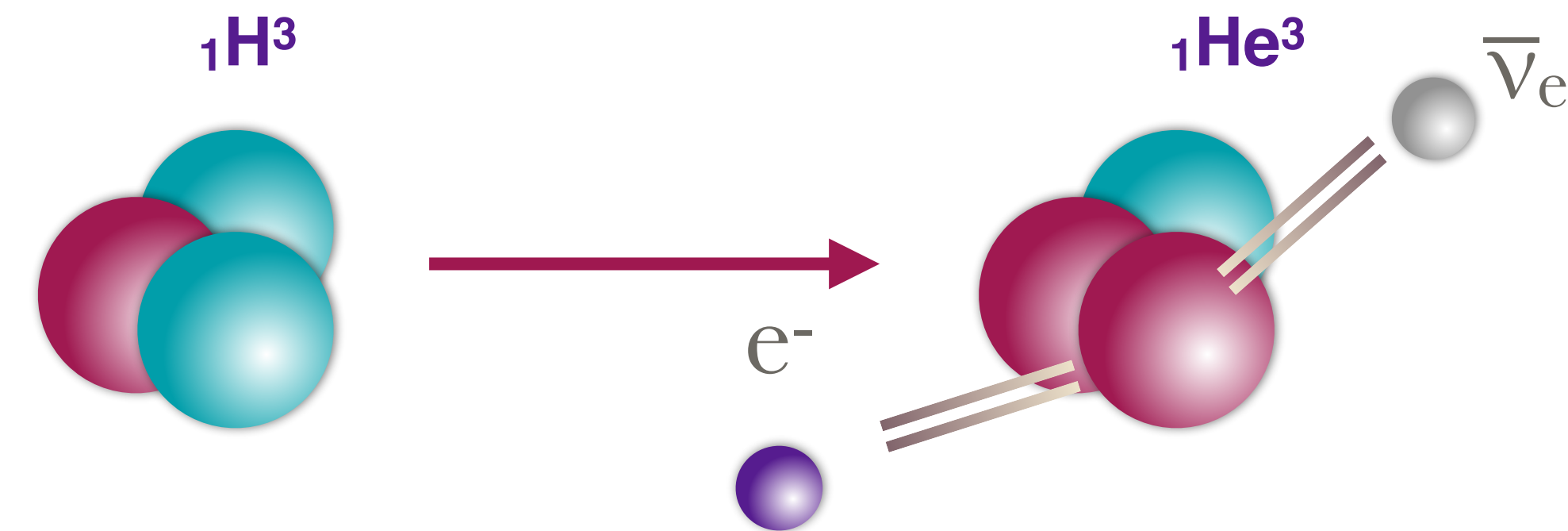
- **Simple structure** (1 proton, 2 neutrons) means **few nuclear effects**

NATURE

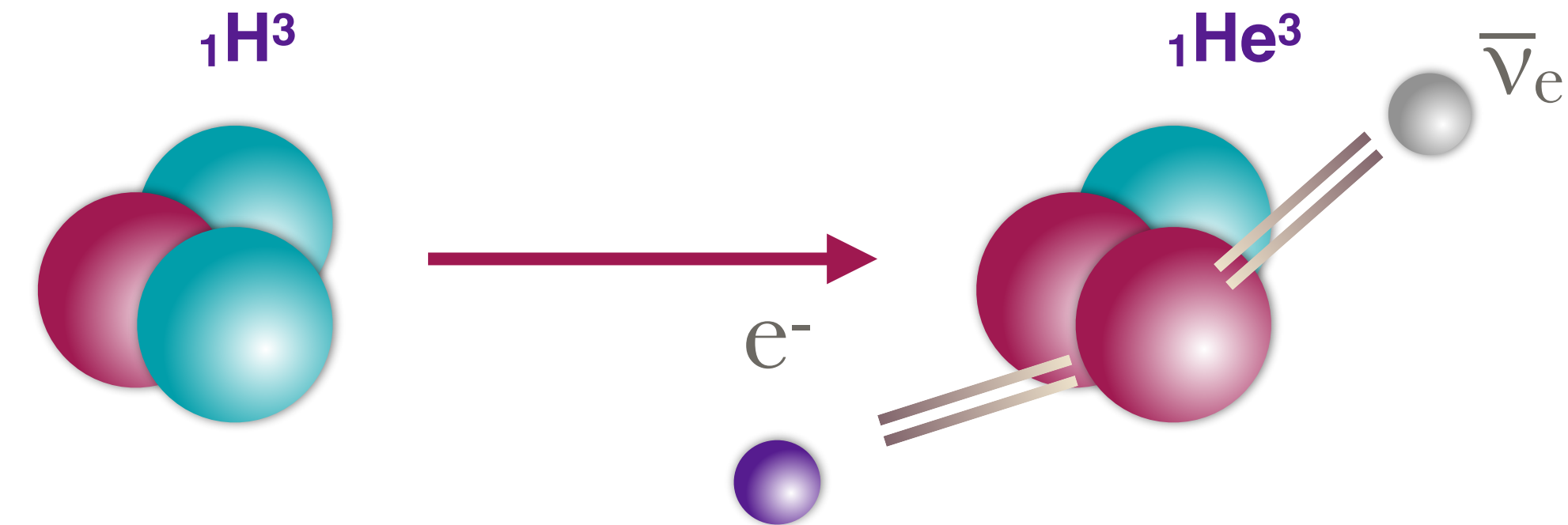
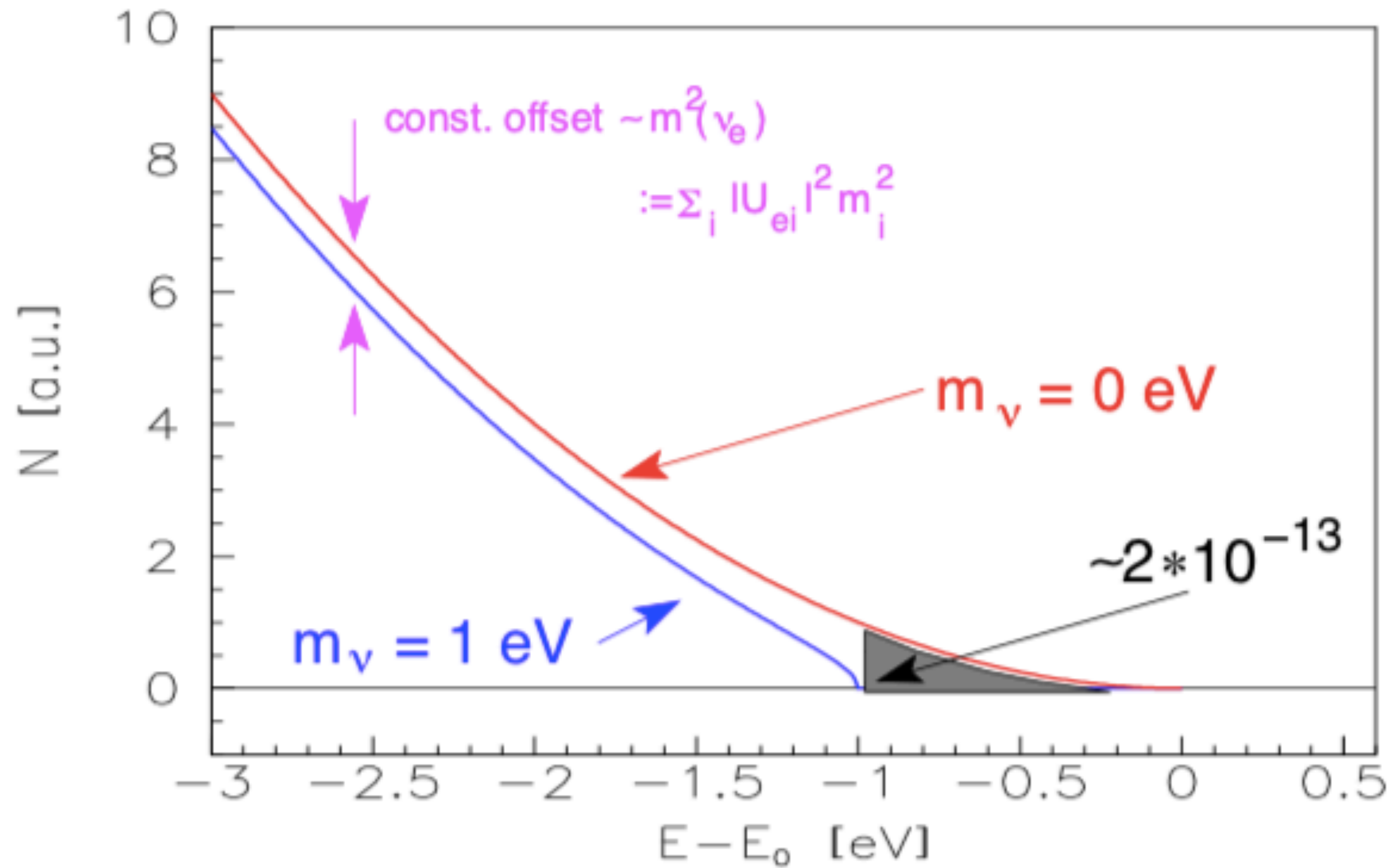
August 21, 1948 Vol. 162

## Beta Spectrum of Tritium

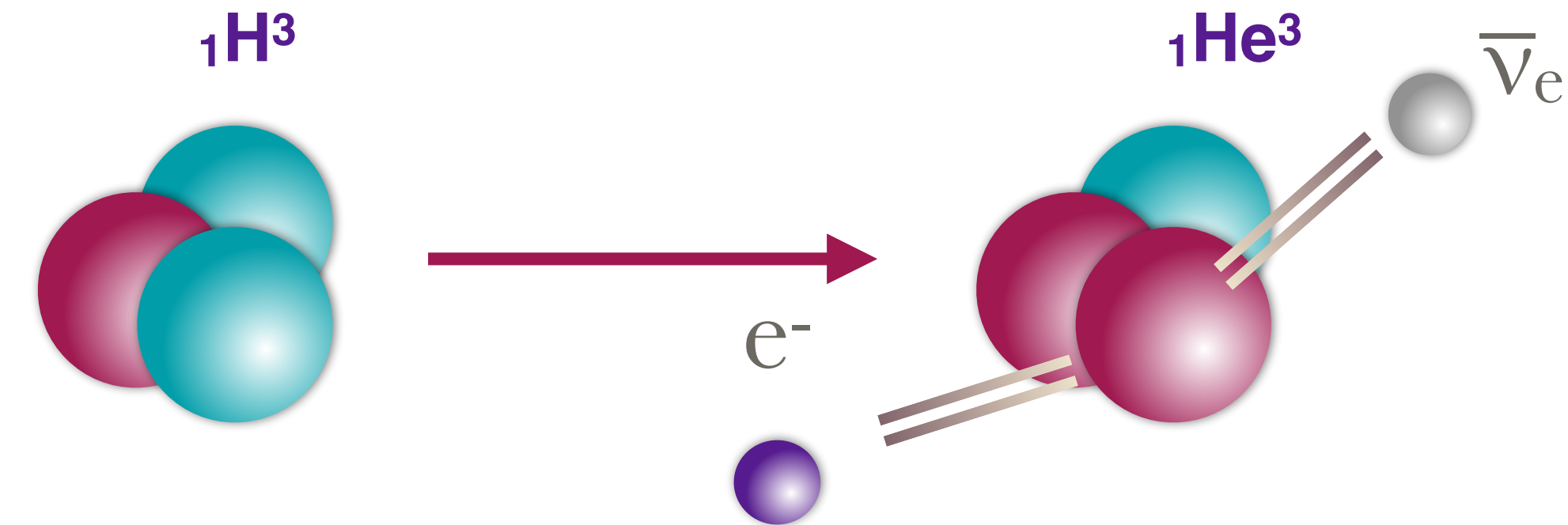
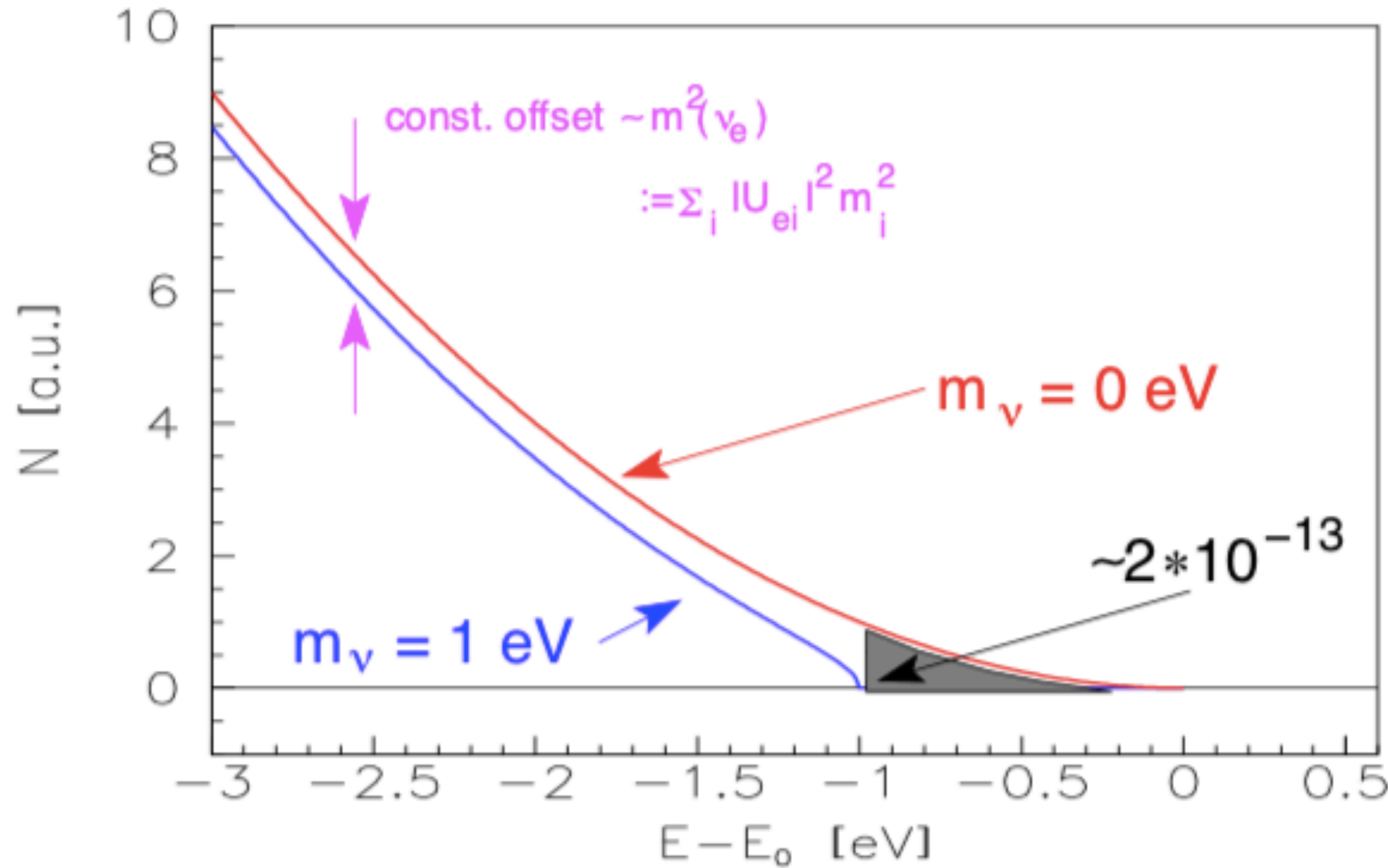
THE  $\beta$ -spectrum of tritium ( ${}^3_1\text{H}$ ) is of particular interest because: (1) the relatively simple structure of the  ${}^3_1\text{H}$  nucleus makes it well suited to a test of the Fermi theory of  $\beta$ -decay; (2) the unusually low energy of the  $\beta$ -particles means that the shape of the spectrum near the upper limit is an extremely sensitive function of the rest mass of the neutrino if the Fermi theory is confirmed; (3) a theoretical discrepancy<sup>1</sup> exists between the half-life<sup>2</sup> and the upper energy limit, as recently measured<sup>3</sup>; (4) the mass difference ( ${}^3_1\text{H} - {}^3_2\text{He}$ ) can be accurately determined.



- **Simple structure** (1 proton, 2 neutrons) means **few nuclear effects**
- **Super-allowed** decay = high activity:  
 **$T_{1/2} = 12.3$  years**



- **Simple structure** (1 proton, 2 neutrons) means **few nuclear effects**
- **Super-allowed** decay = high activity:  **$T_{1/2} = 12.3$  years**
- Low energy:  **$Q_\beta = 18.6$  keV** makes it sensitive to neutrino mass



- **Simple structure** (1 proton, 2 neutrons) means **few nuclear effects**
- **Super-allowed** decay = high activity:  **$T_{1/2} = 12.3 \text{ years}$**
- Low energy:  **$Q_\beta = 18.6 \text{ keV}$**  makes it sensitive to neutrino mass

Spectral distortion depends on an effective “**electron neutrino mass**” depending on PMNS matrix

$$m^2(\bar{\nu}_e) = \sum_{i=1}^3 |U_{ei}|^2 m_i^2$$

$$\begin{aligned} \frac{dN}{dE_e} = & \frac{G_F^2 m_e^5 \cos^2 \theta_C}{2\pi^3 \hbar^7} |M_{\text{nuc}}|^2 F(Z, E_e) p_e E_e \\ & \times (E_{\text{max}} - E_e) \sum_i |U_{ei}|^2 \sqrt{(E_{\text{max}} - E_e)^2 - m_{\nu_i}^2} \\ & \times \Theta(E_{\text{max}} - E_e - m_{\nu_i}) \end{aligned}$$

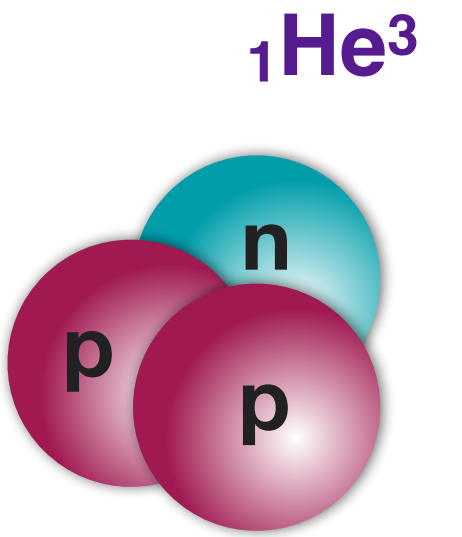
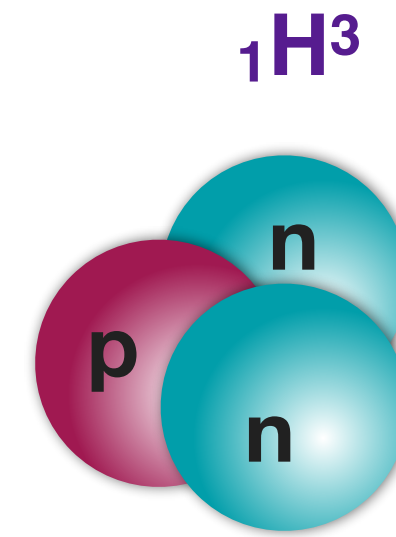


**Constant**  $G_F$  is Fermi constant  
 $\theta_c$  is Cabibbo angle

$$\frac{dN}{dE_e} = \frac{G_F^2 m_e^5 \cos^2 \theta_C}{2\pi^3 \hbar^7} |M_{\text{nuc}}|^2 F(Z, E_e) p_e E_e$$
$$\times (E_{\text{max}} - E_e) \sum_i |U_{ei}|^2 \sqrt{(E_{\text{max}} - E_e)^2 - m_{\nu_i}^2}$$
$$\times \Theta(E_{\text{max}} - E_e - m_{\nu_i})$$

# The tritium electron energy spectrum in more detail

Nuclear matrix element is maximal because  ${}^3\text{H}$  and  ${}^3\text{He}$  are mirror nuclei



$$\frac{dN}{dE_e} = \frac{G_F^2 m_e^5 \cos^2 \theta_C}{2\pi^3 \hbar^7} |M_{\text{nuc}}|^2 F(Z, E_e) p_e E_e$$

$$\times (E_{\text{max}} - E_e) \sum_i |U_{ei}|^2 \sqrt{(E_{\text{max}} - E_e)^2 - m_{\nu_i}^2}$$

$$\times \Theta(E_{\text{max}} - E_e - m_{\nu_i})$$

# The tritium electron energy spectrum in more detail

Fermi function corrects  
for electron-nucleus  
interaction

$$\frac{dN}{dE_e} = \frac{G_F^2 m_e^5 \cos^2 \theta_C}{2\pi^3 \hbar^7} |M_{\text{nuc}}|^2 F(Z, E_e) p_e E_e$$

$$\times (E_{\text{max}} - E_e) \sum_i |U_{ei}|^2 \sqrt{(E_{\text{max}} - E_e)^2 - m_{\nu_i}^2}$$

$$\times \Theta(E_{\text{max}} - E_e - m_{\nu_i})$$

$$\frac{dN}{dE_e} = \frac{G_F^2 m_e^5 \cos^2 \theta_C}{2\pi^3 \hbar^7} |M_{\text{nuc}}|^2 F(Z, E_e) p_e E_e$$

Electron momentum and energy

$$\times (E_{\text{max}} - E_e) \sum_i |U_{ei}|^2 \sqrt{(E_{\text{max}} - E_e)^2 - m_{\nu_i}^2}$$

$$\times \Theta(E_{\text{max}} - E_e - m_{\nu_i})$$

$$\frac{dN}{dE_e} = \frac{G_F^2 m_e^5 \cos^2 \theta_C}{2\pi^3 \hbar^7} |M_{\text{nuc}}|^2 F(Z, E_e) p_e E_e$$
$$\times (E_{\text{max}} - E_e) \sum_i |U_{ei}|^2 \sqrt{(E_{\text{max}} - E_e)^2 - m_{\nu_i}^2}$$
$$\times \Theta(E_{\text{max}} - E_e - m_{\nu_i})$$

**Energy conservation step function**

*Phys. Rev. C* **91**, 035505

$$\frac{dN}{dE_e} = \frac{G_F^2 m_e^5 \cos^2 \theta_C}{2\pi^3 \hbar^7} |M_{\text{nuc}}|^2 F(Z, E_e) p_e E_e$$

$$\times (E_{\text{max}} - E_e) \sum_i |U_{ei}|^2 \sqrt{(E_{\text{max}} - E_e)^2 - m_{\nu_i}^2}$$

**The neutrino bit!**

$$\times \Theta(E_{\text{max}} - E_e - m_{\nu_i})$$

$$\frac{dN}{dE_e} = \frac{G_F^2 m_e^5 \cos^2 \theta_C}{2\pi^3 \hbar^7} |M_{\text{nuc}}|^2 F(Z, E_e) p_e E_e$$


Neutrino energy  $\times (E_{\text{max}} - E_e) \sum_i |U_{ei}|^2 \sqrt{(E_{\text{max}} - E_e)^2 - m_{\nu_i}^2}$

$$\times \Theta(E_{\text{max}} - E_e - m_{\nu_i})$$

# The tritium electron energy spectrum in more detail

$$\frac{dN}{dE_e} = \frac{G_F^2 m_e^5 \cos^2 \theta_C}{2\pi^3 \hbar^7} |M_{\text{nuc}}|^2 F(Z, E_e) p_e E_e$$

Neutrino energy  $\times (E_{\text{max}} - E_e) \sum_i |U_{ei}|^2 \sqrt{(E_{\text{max}} - E_e)^2 - m_{\nu_i}^2}$



$\times \Theta(E_{\text{max}} - E_e - m_{\nu_i})$  **Neutrino momentum**

Phys. Rev. C **91**, 035505



$$\frac{dN}{dE_e} = \frac{G_F^2 m_e^5 \cos^2 \theta_C}{2\pi^3 \hbar^7} |M_{\text{nuc}}|^2 F(Z, E_e) p_e E_e$$

Sum over neutrino mass states  $i$

Neutrino energy  $\times (E_{\text{max}} - E_e) \sum_i |U_{ei}|^2 \sqrt{(E_{\text{max}} - E_e)^2 - m_{\nu_i}^2}$

$\times \Theta(E_{\text{max}} - E_e - m_{\nu_i})$  **Neutrino momentum**

Phys. Rev. C **91**, 035505

$$\frac{dN}{dE_e} = \frac{G_F^2 m_e^5 \cos^2 \theta_C}{2\pi^3 \hbar^7} |M_{\text{nuc}}|^2 F(Z, E_e) p_e E_e$$

Sum over neutrino mass states  $i$  **Electron component of PMNS matrix**

Neutrino energy  $\times (E_{\text{max}} - E_e) \sum_i |U_{ei}|^2 \sqrt{(E_{\text{max}} - E_e)^2 - m_{\nu_i}^2}$

$\times \Theta(E_{\text{max}} - E_e - m_{\nu_i})$  **Neutrino momentum**

Phys. Rev. C **91**, 035505

# The tritium electron energy spectrum in more detail


$$\frac{dN}{dE_e} = \frac{G_F^2 m_e^5 \cos^2 \theta_C}{2\pi^3 \hbar^7} |M_{\text{nuc}}|^2 F(Z, E_e) p_e E_e$$

Electron component of  
Sum over neutrino mass states  $i$  PMNS matrix Neutrino energy Neutrino mass

Neutrino energy  $\times (E_{\text{max}} - E_e) \sum_i |U_{ei}|^2 \sqrt{(E_{\text{max}} - E_e)^2 - m_{\nu_i}^2}$

$\times \Theta(E_{\text{max}} - E_e - m_{\nu_i})$  Neutrino momentum

Phys. Rev. C **91**, 035505



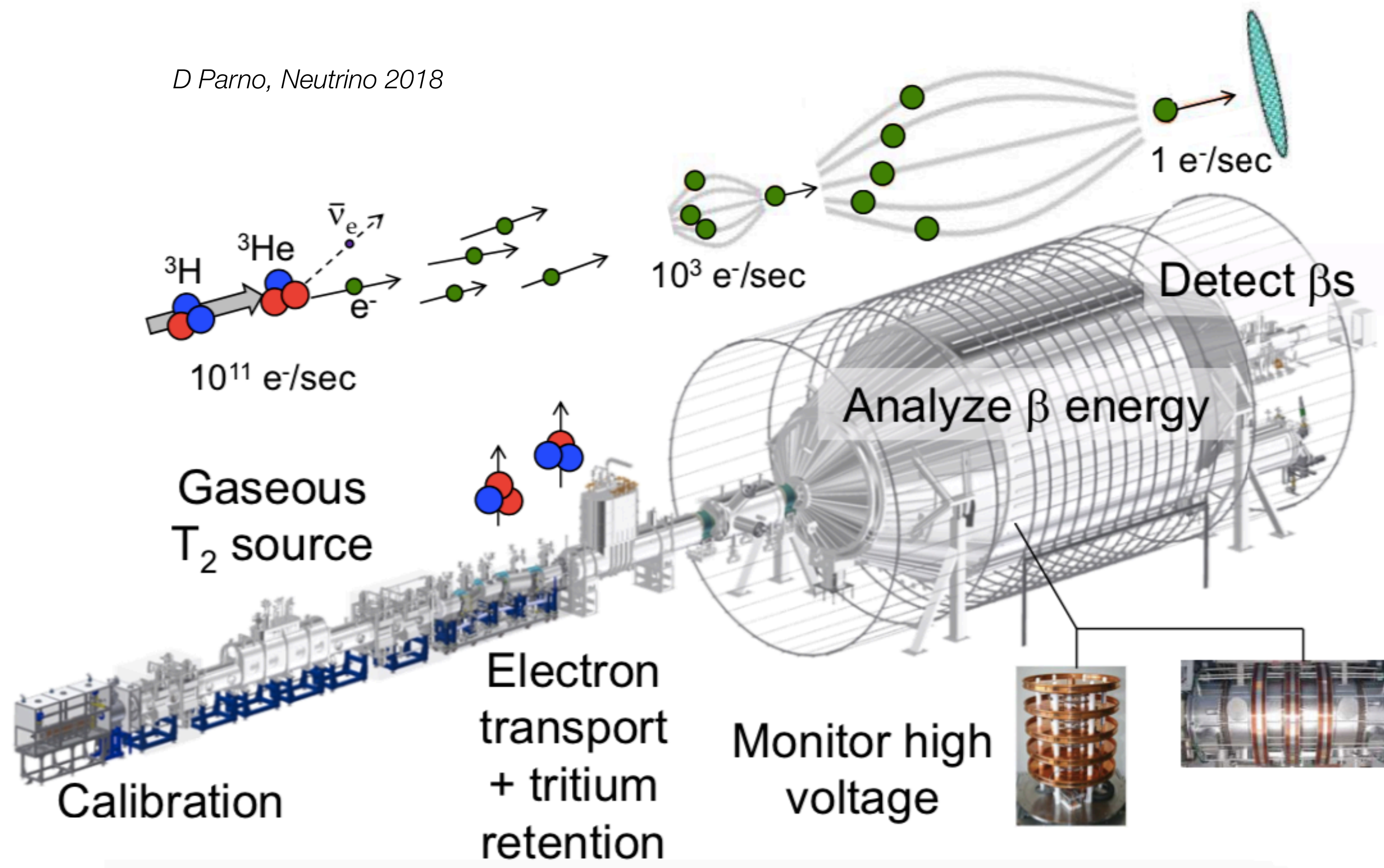
## TOP TRUMPS

$\beta$  emitter: Molecular tritium  
T<sub>2</sub>  
Located: Karlsruhe, Germany  
Status: Data taken; main run 2020–23  
Technology: High-resolution spectroscopy  
 $m_\nu$  sensitivity 200 meV  
Superpower: MAC-E filter

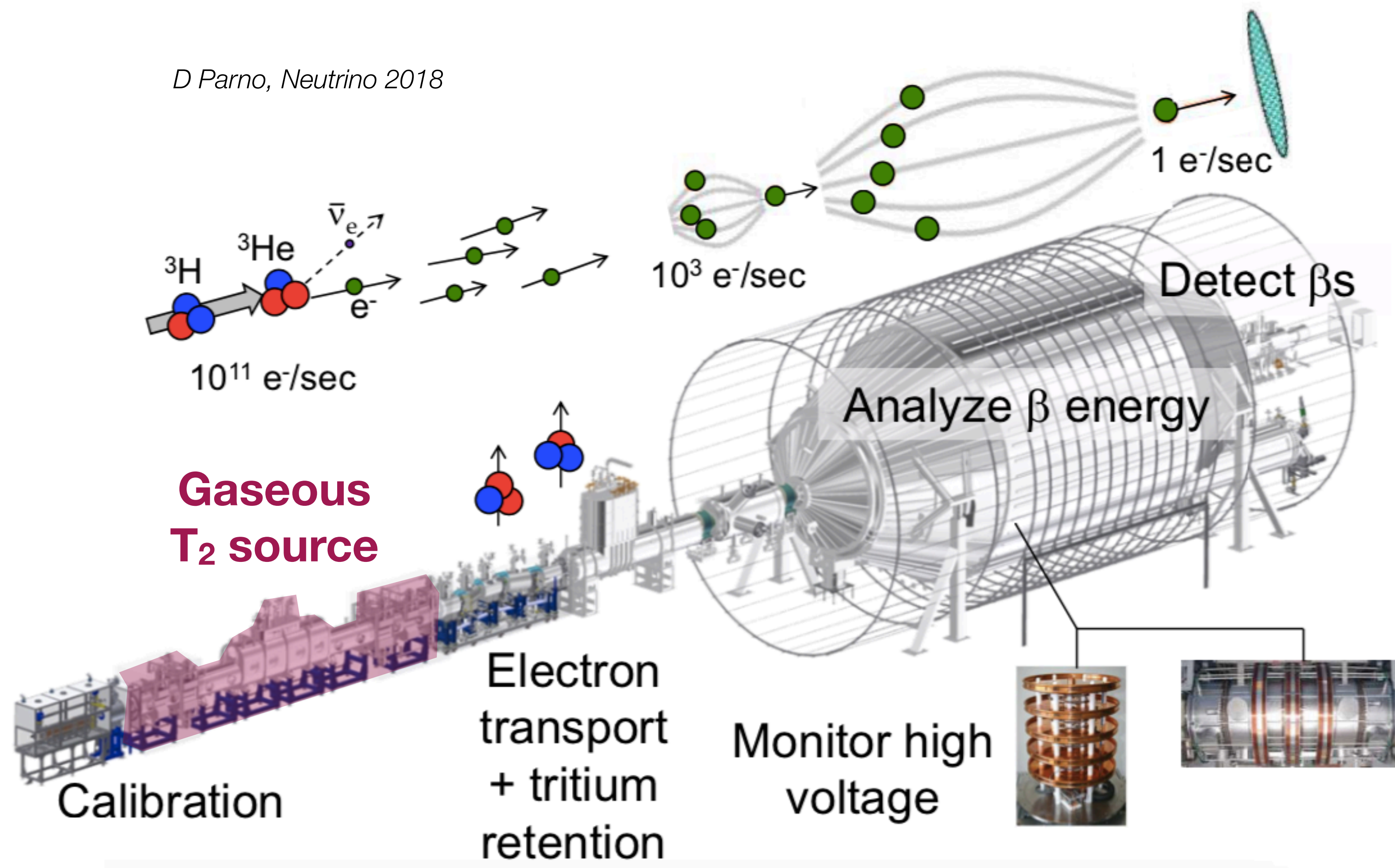
## PROJECT TOP TRUMPS

$\beta$  emitter: Atomic tritium  
Located: USA & Germany  
Status: First signals seen from T<sub>2</sub> data  
Technology: CRES  
 $m_\nu$  sensitivity 40 meV  
Superpower: Cyclotron radiation

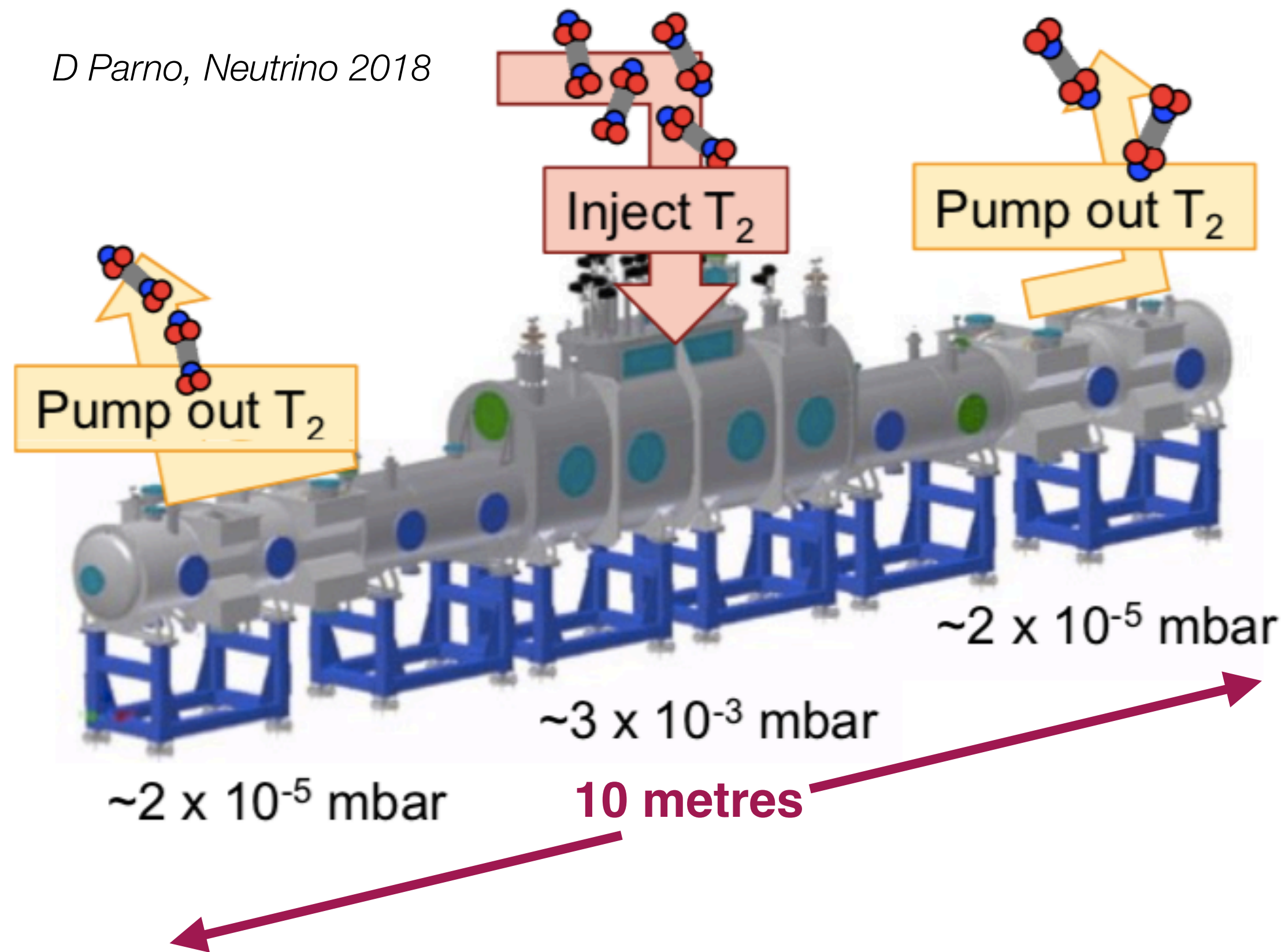
*D Parno, Neutrino 2018*



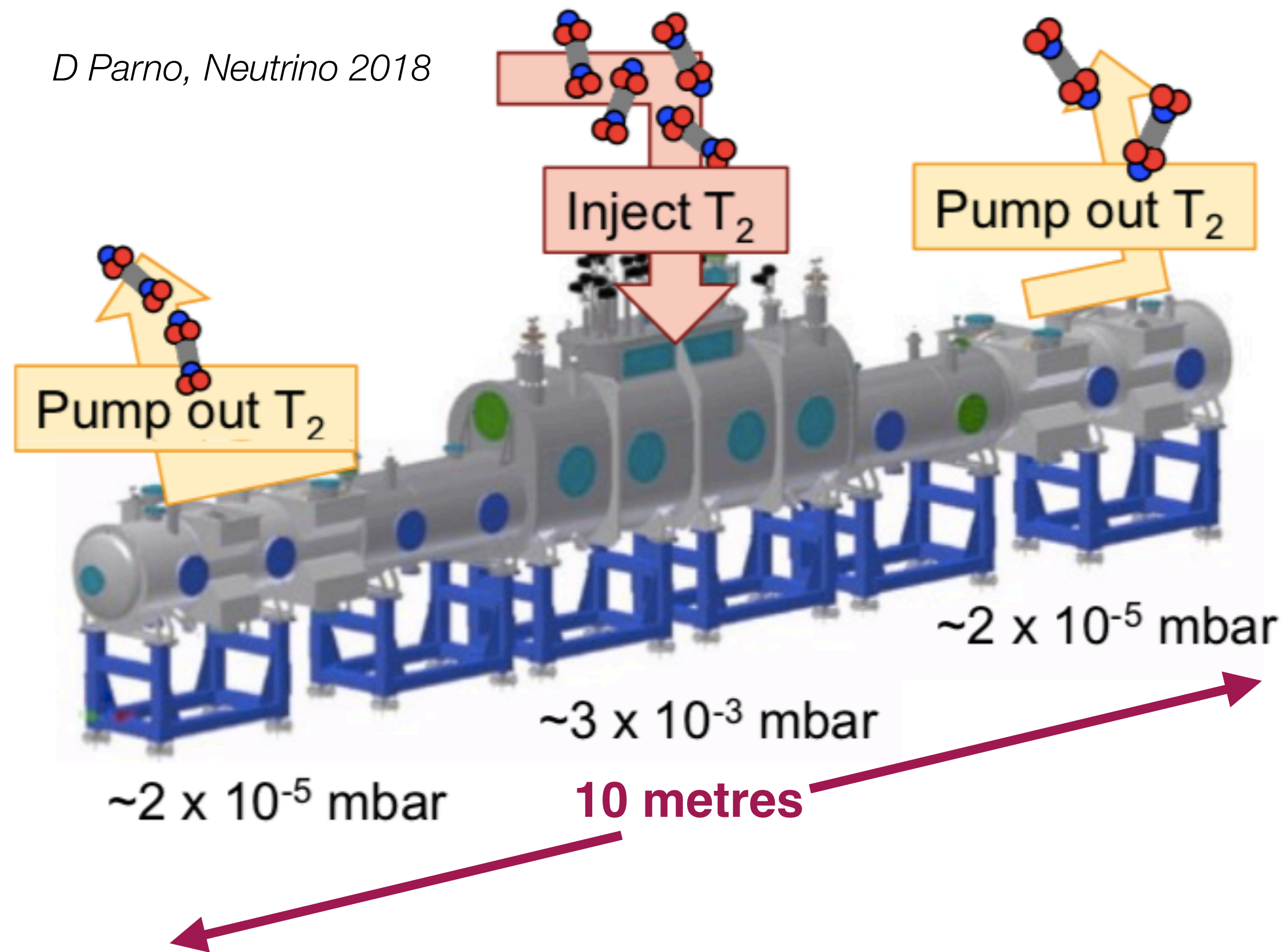
*D Parno, Neutrino 2018*



*D Parno, Neutrino 2018*

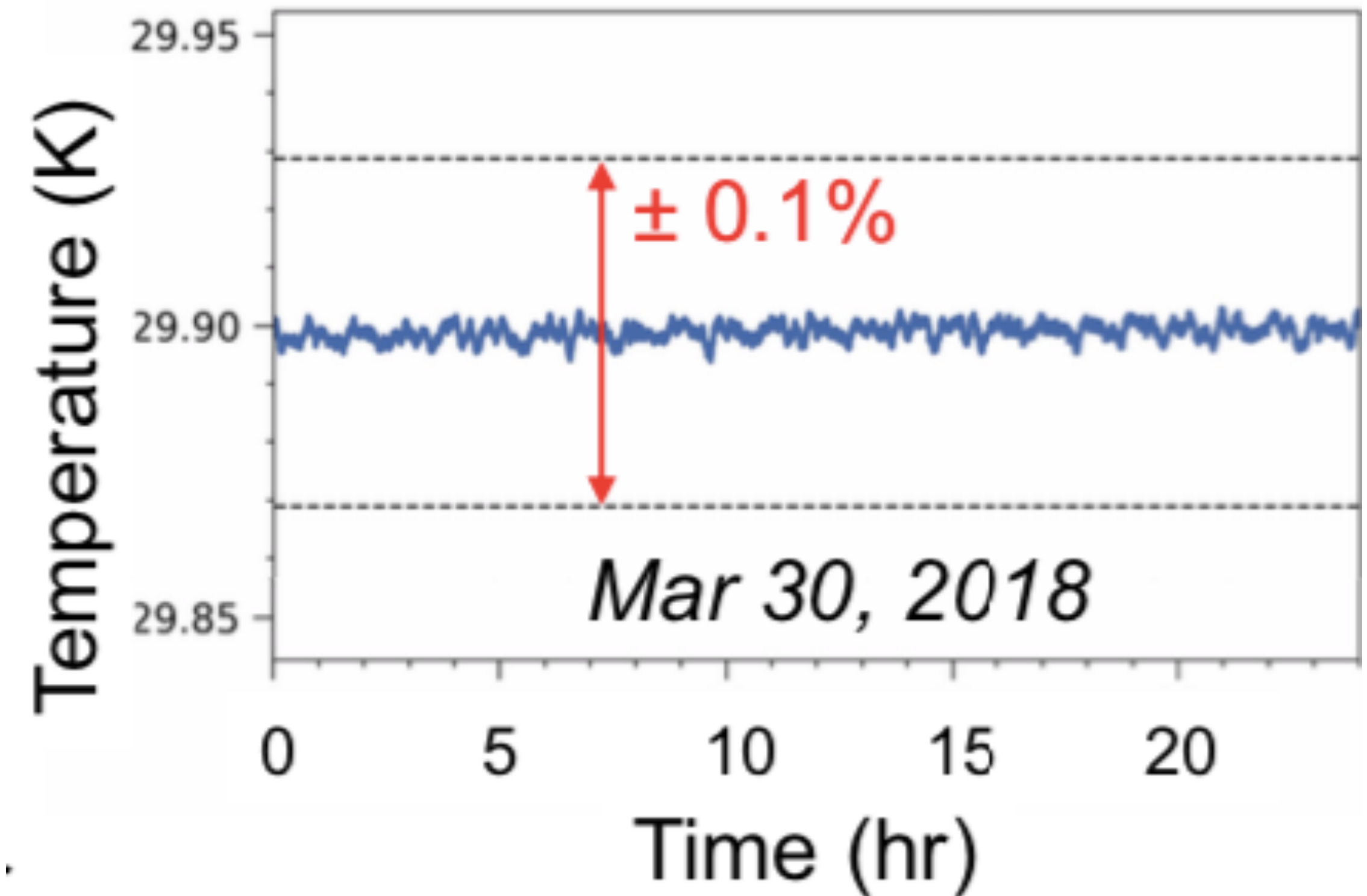


D Parno, Neutrino 2018



**Temperature:** 30 Kelvin

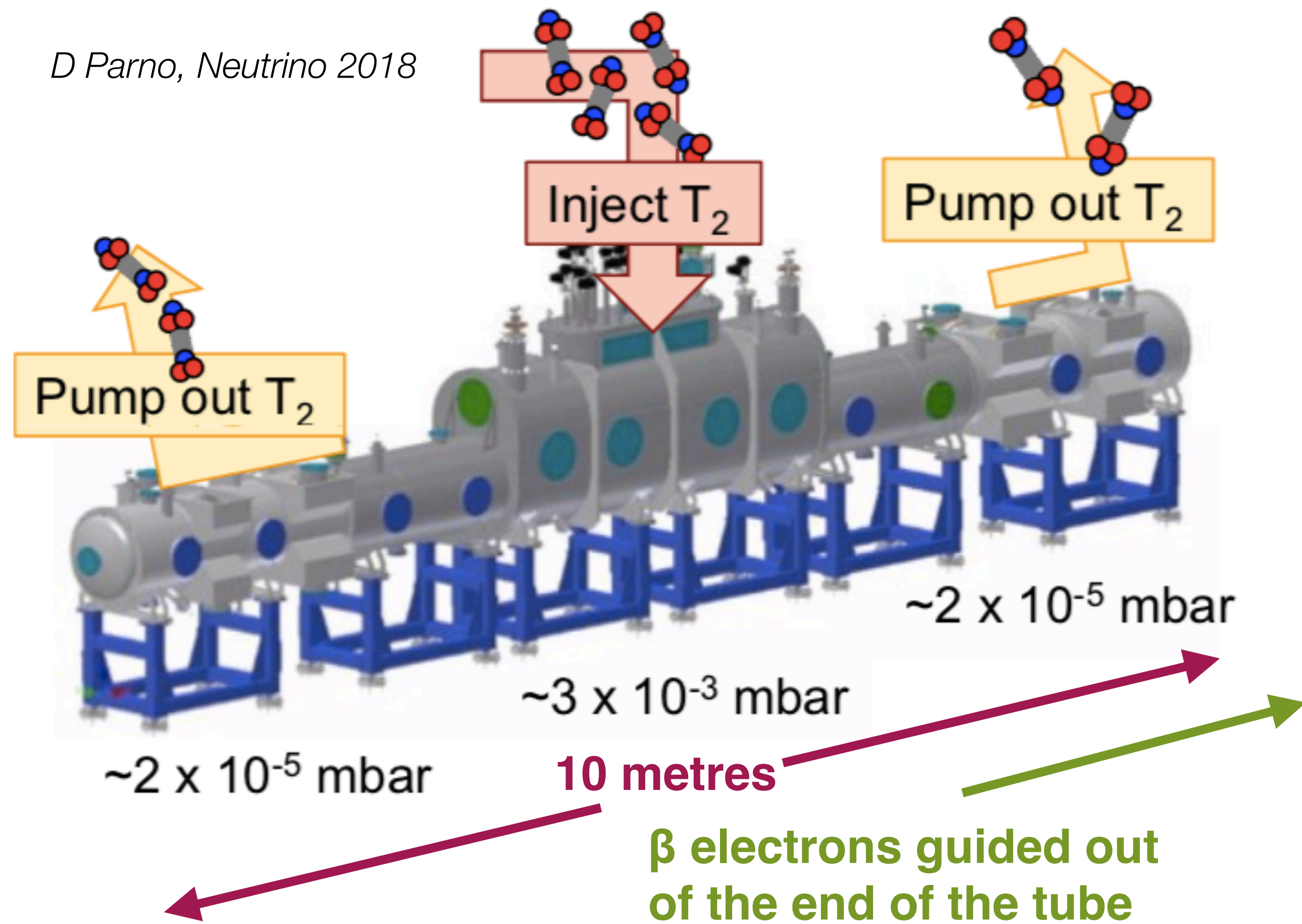
## Temperature stability @ 30 K



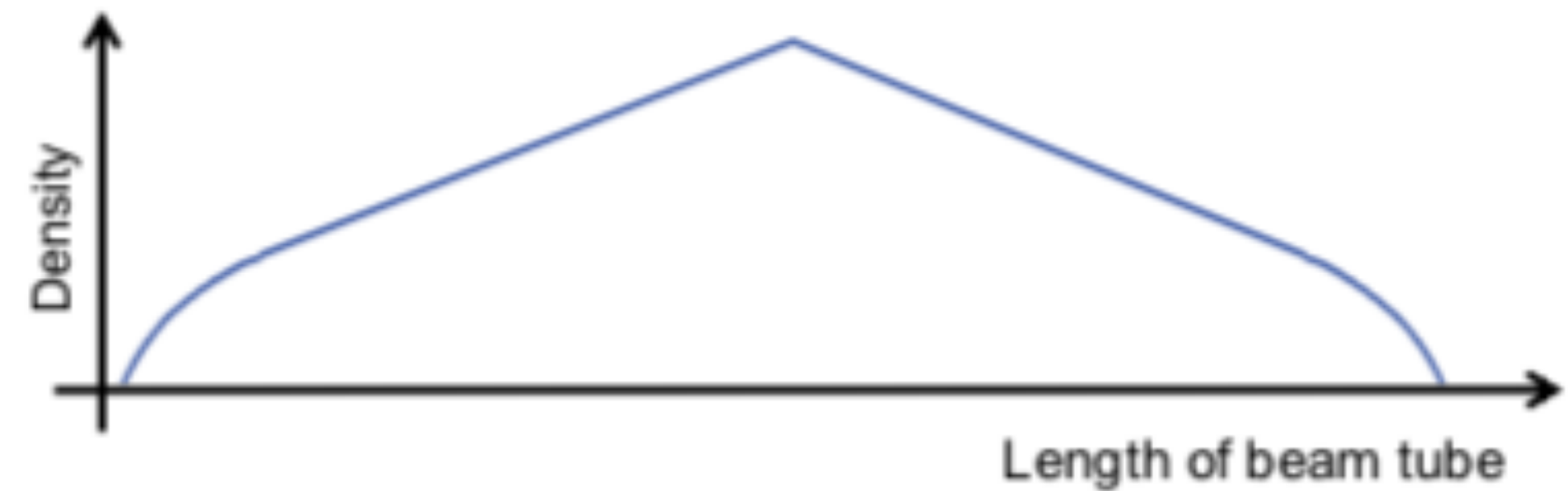
*Two-phase Ne cooling: Cryogenics 49 (2009) 413*



D Parno, Neutrino 2018

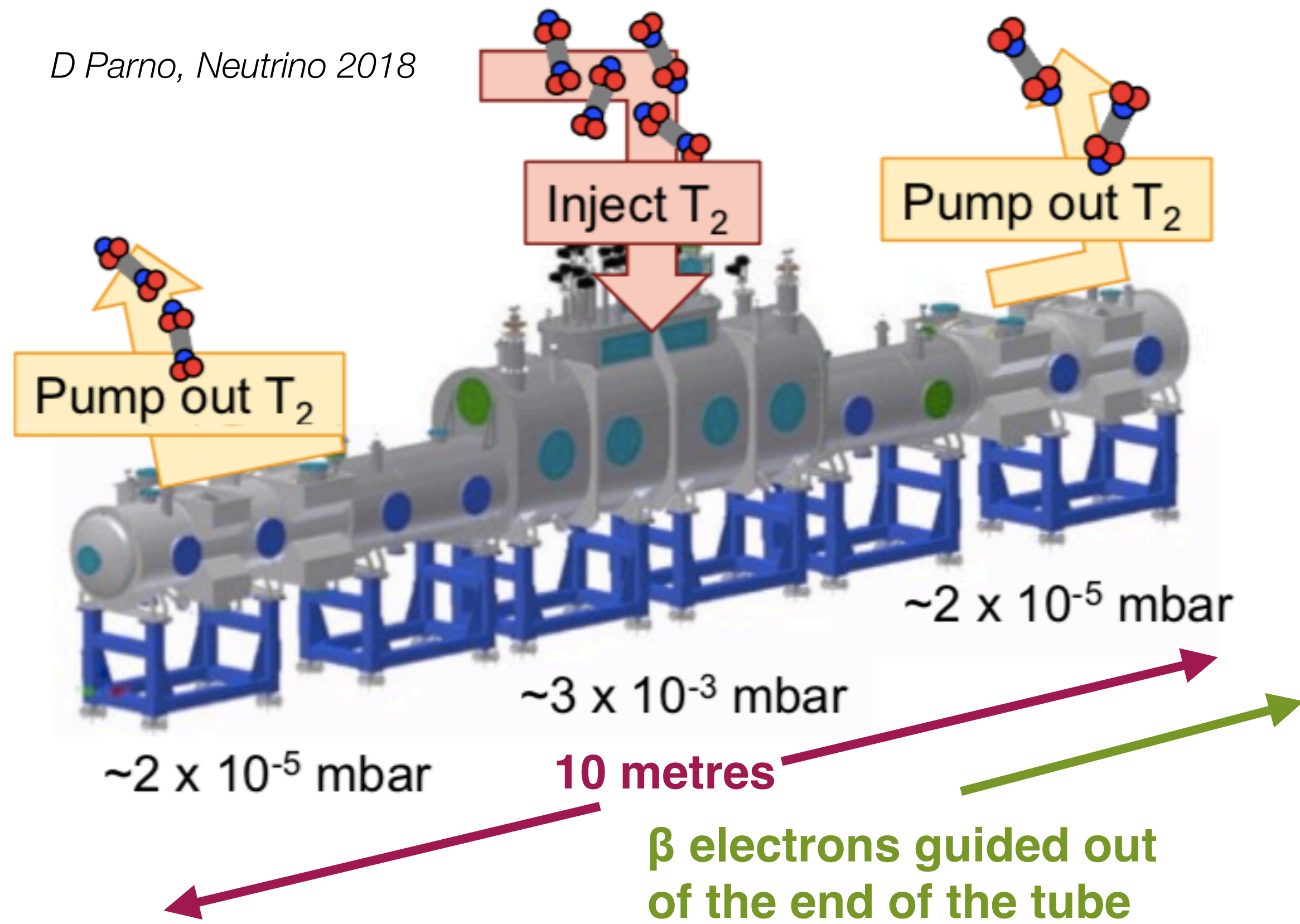


- Closed tritium cycle delivering **40g of T<sub>2</sub> per day**
- **9.9 X 10<sup>10</sup> decays** per second
- Electrons guided out of ends of tube by **3.6 T magnetic field**
- Reduced **gas density** along tube protects against scattering and energy loss

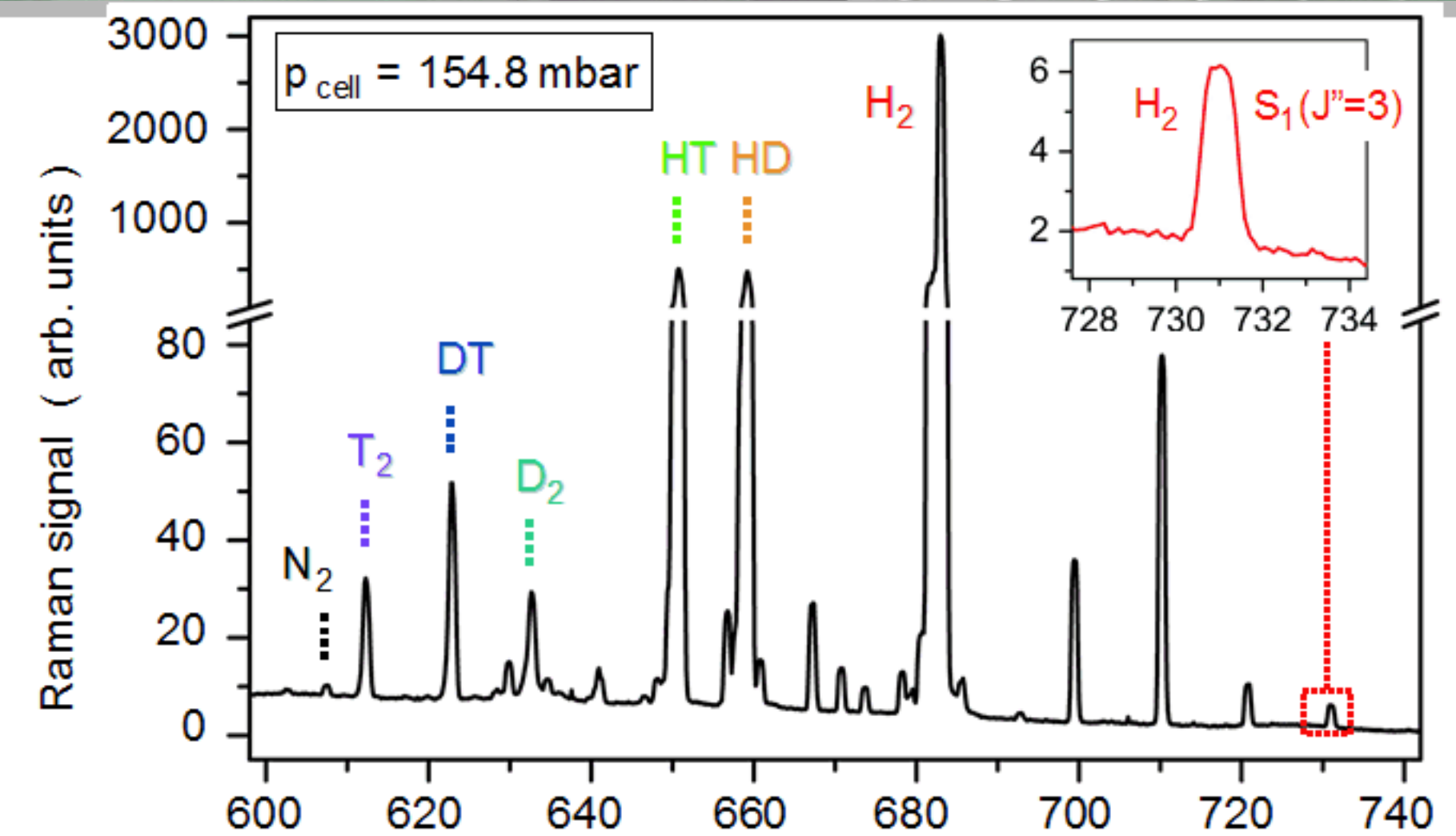
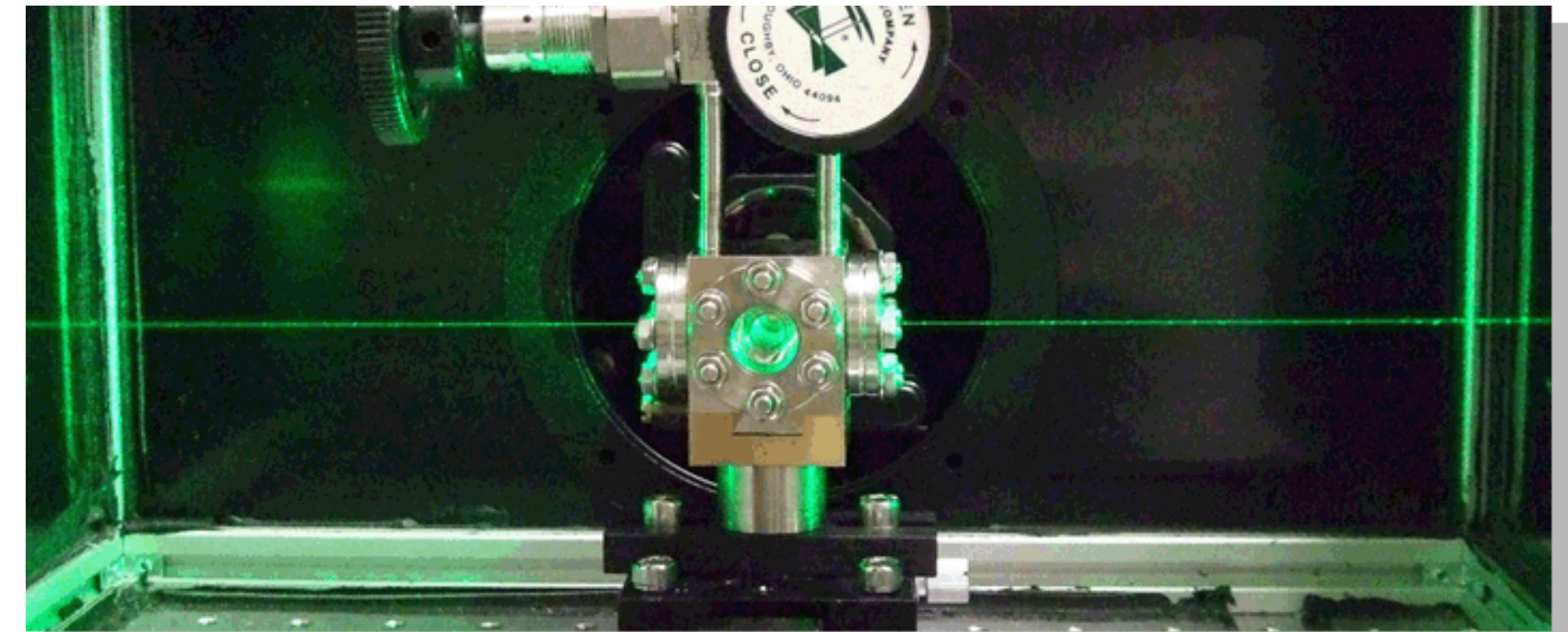


**Temperature:** 30 Kelvin  
**Activity:** 100 GBq

D Parno, Neutrino 2018



- Temperature:** 30 Kelvin
- Activity:** 100 GBq
- Isotopic Purity:** 95% molecular tritium



**Laser Raman Spectroscopy monitors isotopic content to 0.1% precision**

Remember this?

$$\frac{dN}{dE_e} = \frac{\text{Constant}}{2\pi^3 \hbar^7} |M_{\text{nuc}}|^2 F(Z, E_e) p_e E_e$$

Matrix element
Fermi function
Electron momentum and energy

$$\times (E_{\text{max}} - E_e) \sum_i |U_{ei}|^2 \sqrt{(E_{\text{max}} - E_e)^2 - m_{\nu_i}^2}$$

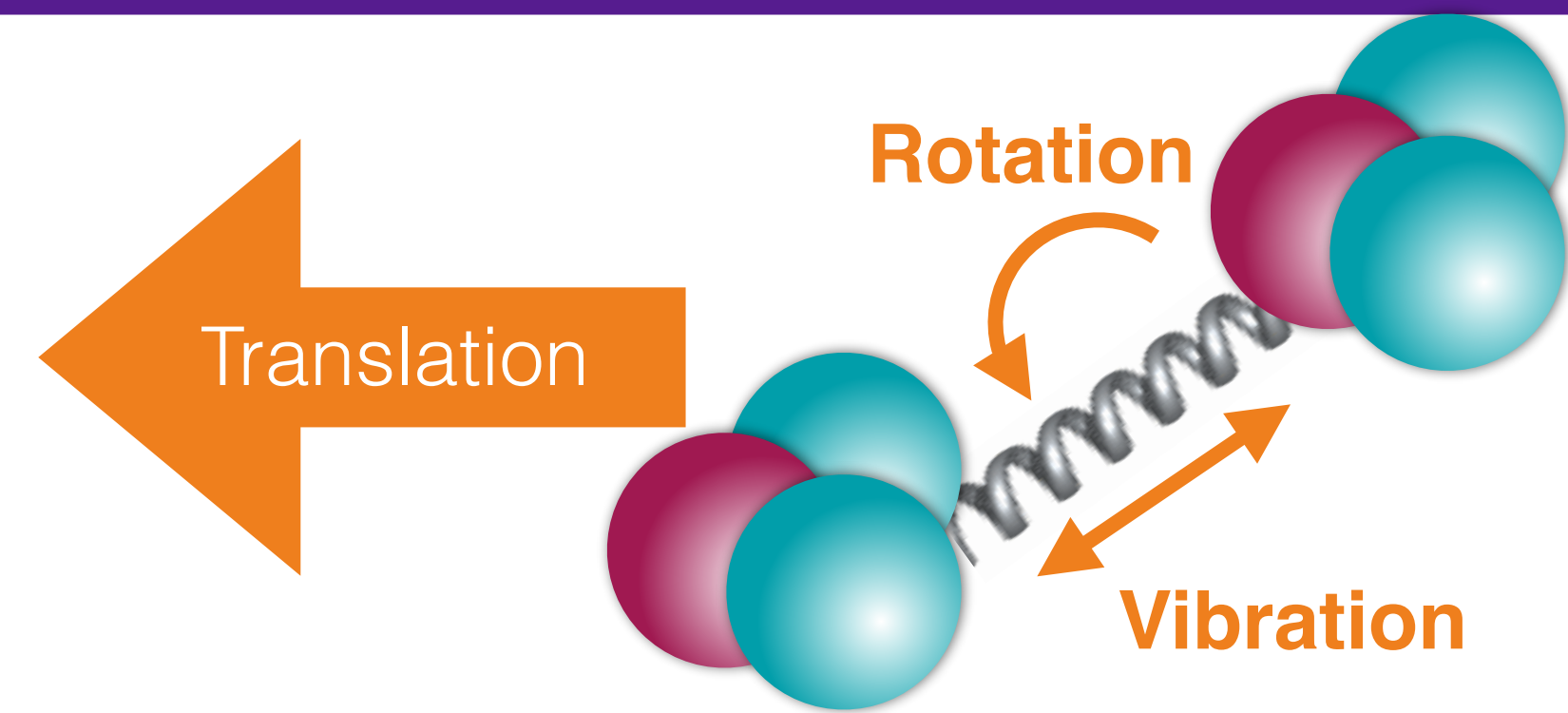
Neutrino energy and momentum

$$\times \Theta(E_{\text{max}} - E_e - m_{\nu_i})$$

Energy conservation step function

Remember this?

$$\frac{dN}{dE_e} = \frac{\text{Constant}}{2\pi^3 \hbar^7} \times \text{Matrix element}^2 \times \text{Fermi function} \times \text{Electron momentum and energy} +$$



$$\times (E_{\text{max}} - E_e) \sum_i |U_{ei}|^2 \sqrt{(E_{\text{max}} - E_e)^2 - m_{\nu_i}^2}$$

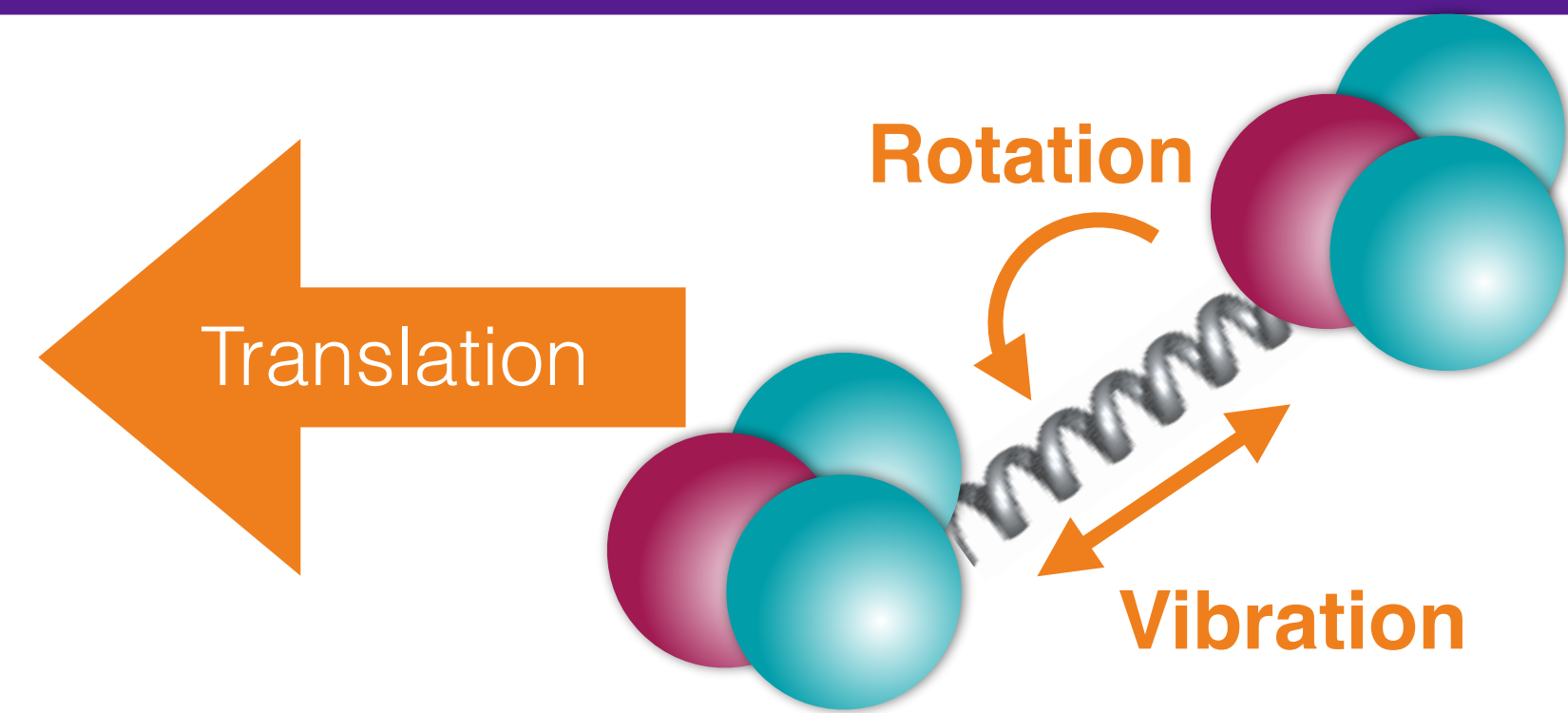
Neutrino energy and momentum

$$\times \Theta(E_{\text{max}} - E_e - m_{\nu_i})$$

Energy conservation step function

Remember this?

$$\frac{dN}{dE_e} = \frac{\text{Constant } G_F^2 m_e^5 \cos^2 \theta_C}{2\pi^3 \hbar^7} \times \text{Matrix element } |M_{\text{nuc}}|^2 \times \text{Fermi function } F(Z, E_e) \times \text{Electron momentum and energy } p_e E_e +$$



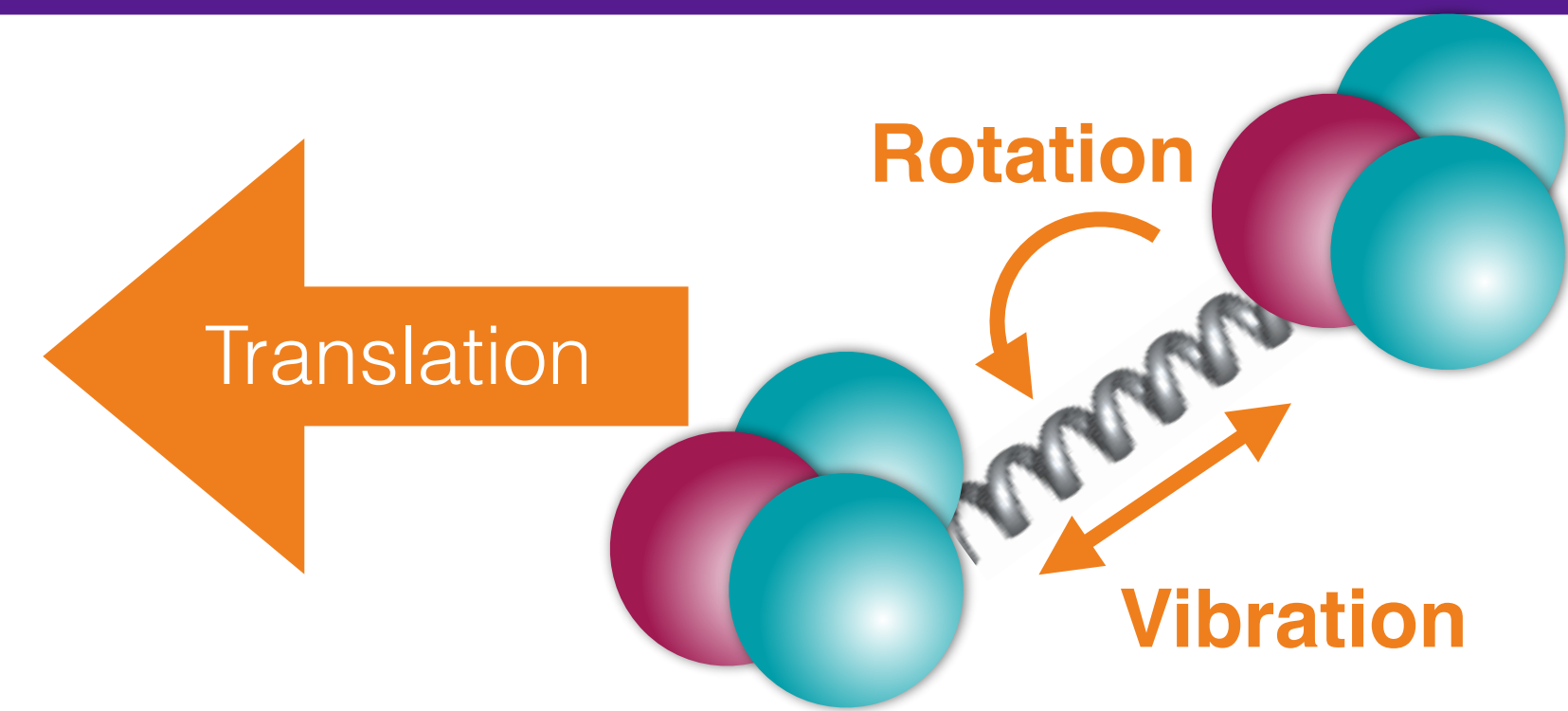
$$\times \sum_{ik} |U_{ei}|^2 P_k(E_{\text{max}} - E_e - V_k) \sqrt{(E_{\text{max}} - E_e - V_k)^2 - m_{\nu_i}^2}$$

Neutrino energy and momentum

$$\times \Theta(E_{\text{max}} - E_e - V_k - m_{\nu_i})$$

Energy conservation step function

$$\frac{dN}{dE_e} = \frac{G_F^2 m_e^5 \cos^2 \theta_C}{2\pi^3 \hbar^7} |M_{\text{nuc}}|^2 F(Z, E_e) p_e E_e +$$



Probability of excited daughter state

$$\times \sum_{ik} |U_{ei}|^2 P_k (E_{\text{max}} - E_e - V_k) \sqrt{(E_{\text{max}} - E_e - V_k)^2 - m_{\nu_i}^2}$$

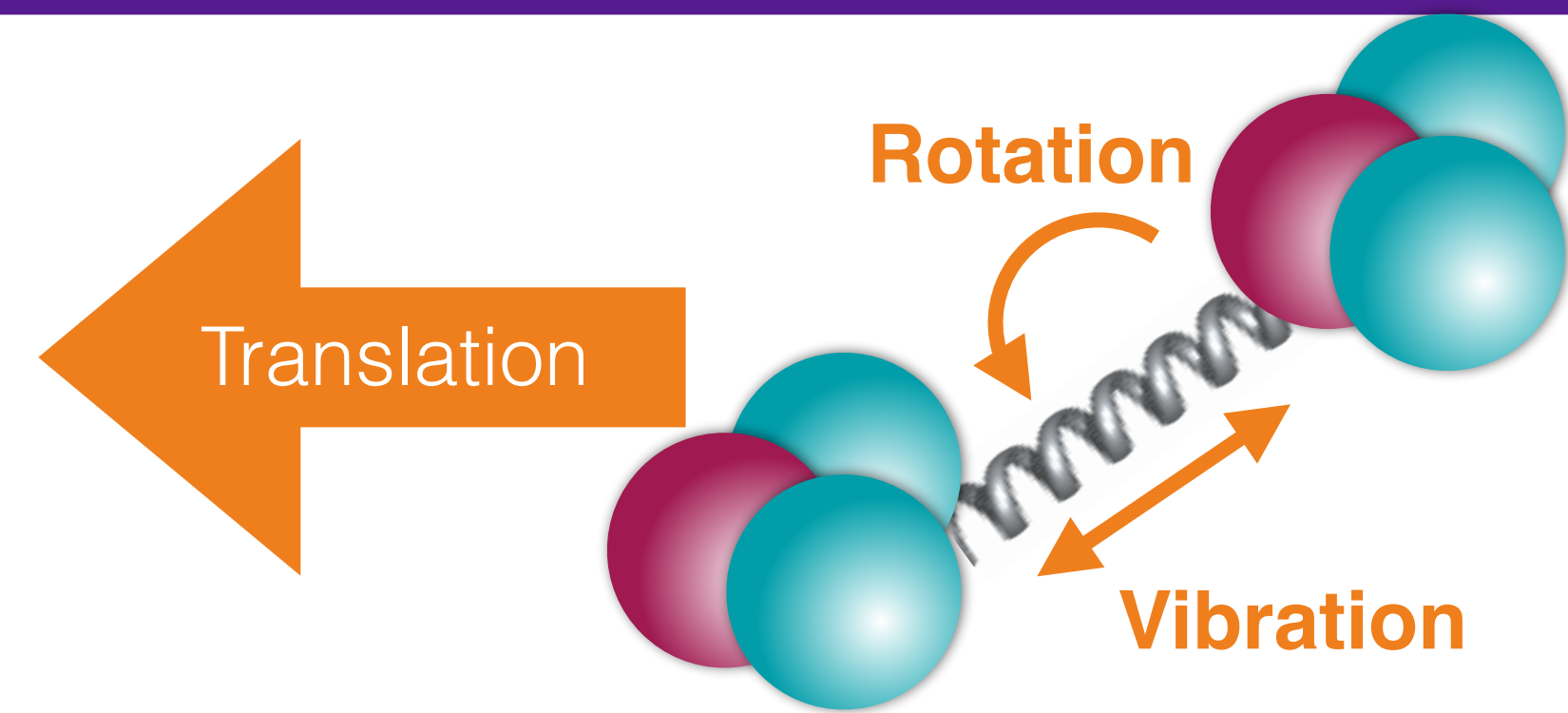
Sum over neutrino mass states  $i$  and excited states of daughter  $k$

Energy of daughter state

$$\times \Theta(E_{\text{max}} - E_e - V_k - m_{\nu_i})$$

$$\frac{dN}{dE_e} = \frac{G_F^2 m_e^5 \cos^2 \theta_C}{2\pi^3 \hbar^7} |M_{\text{nuc}}|^2 F(Z, E_e) p_e E_e$$

+



Probability of excited daughter state

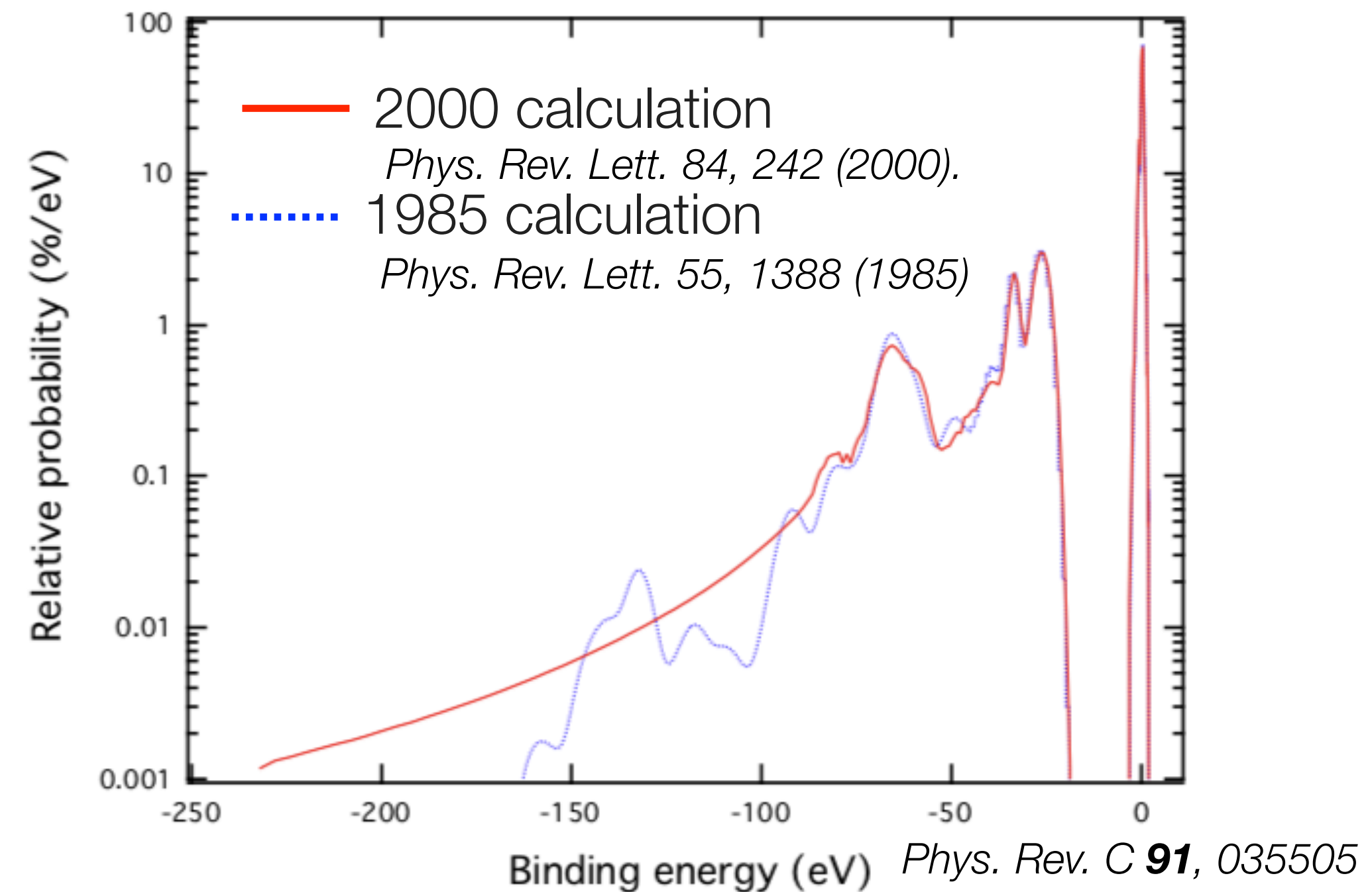
$$\times \sum_{ik} |U_{ei}|^2 P_k (E_{\text{max}} - E_e - V_k) \sqrt{(E_{\text{max}} - E_e - V_k)^2 - m_{\nu_i}^2}$$

Sum over neutrino mass states  $i$  and excited states of daughter  $k$

Energy of daughter state

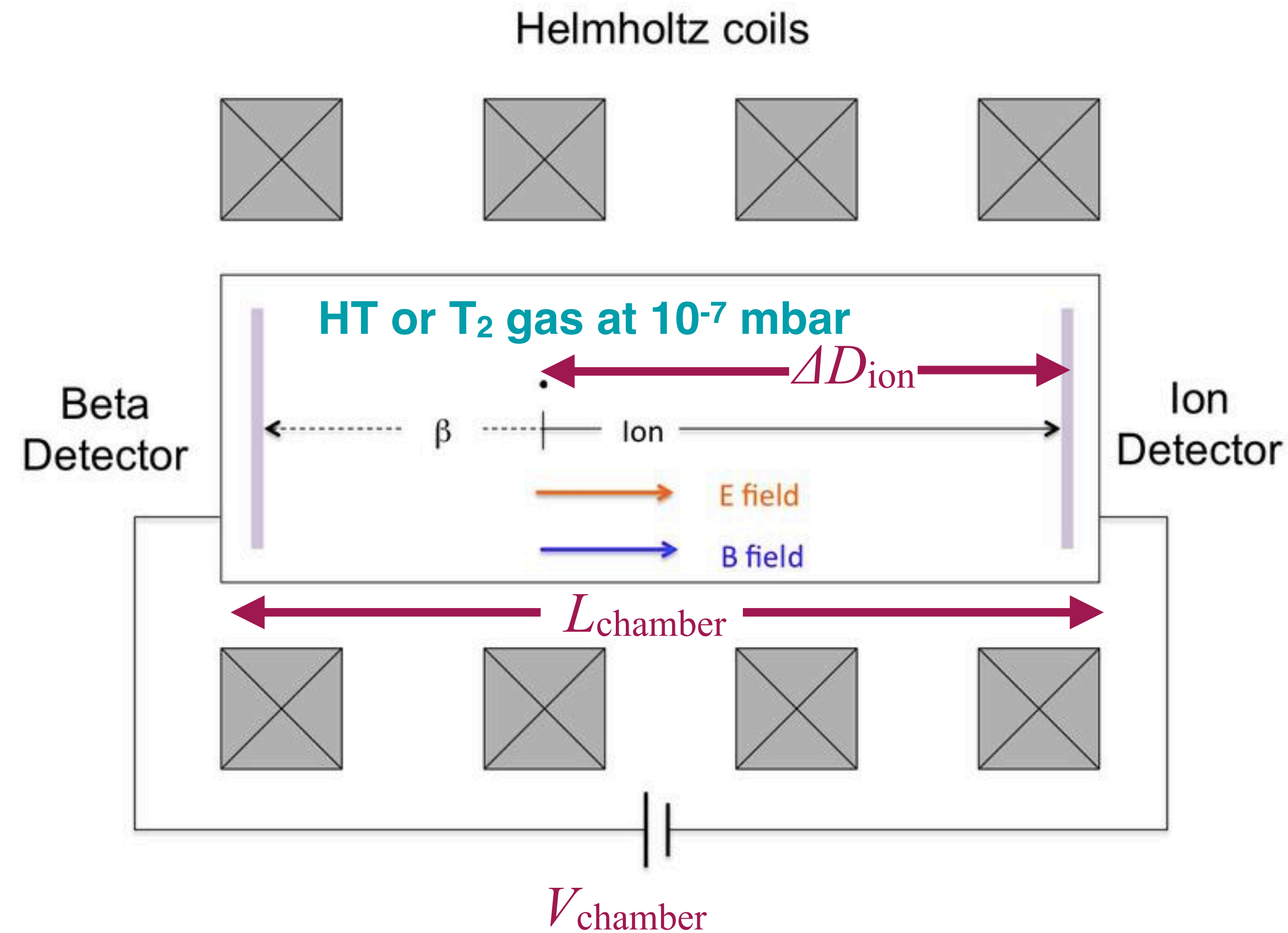
$$\times \Theta(E_{\text{max}} - E_e - V_k - m_{\nu_i})$$

Calculated final-state molecular spectrum

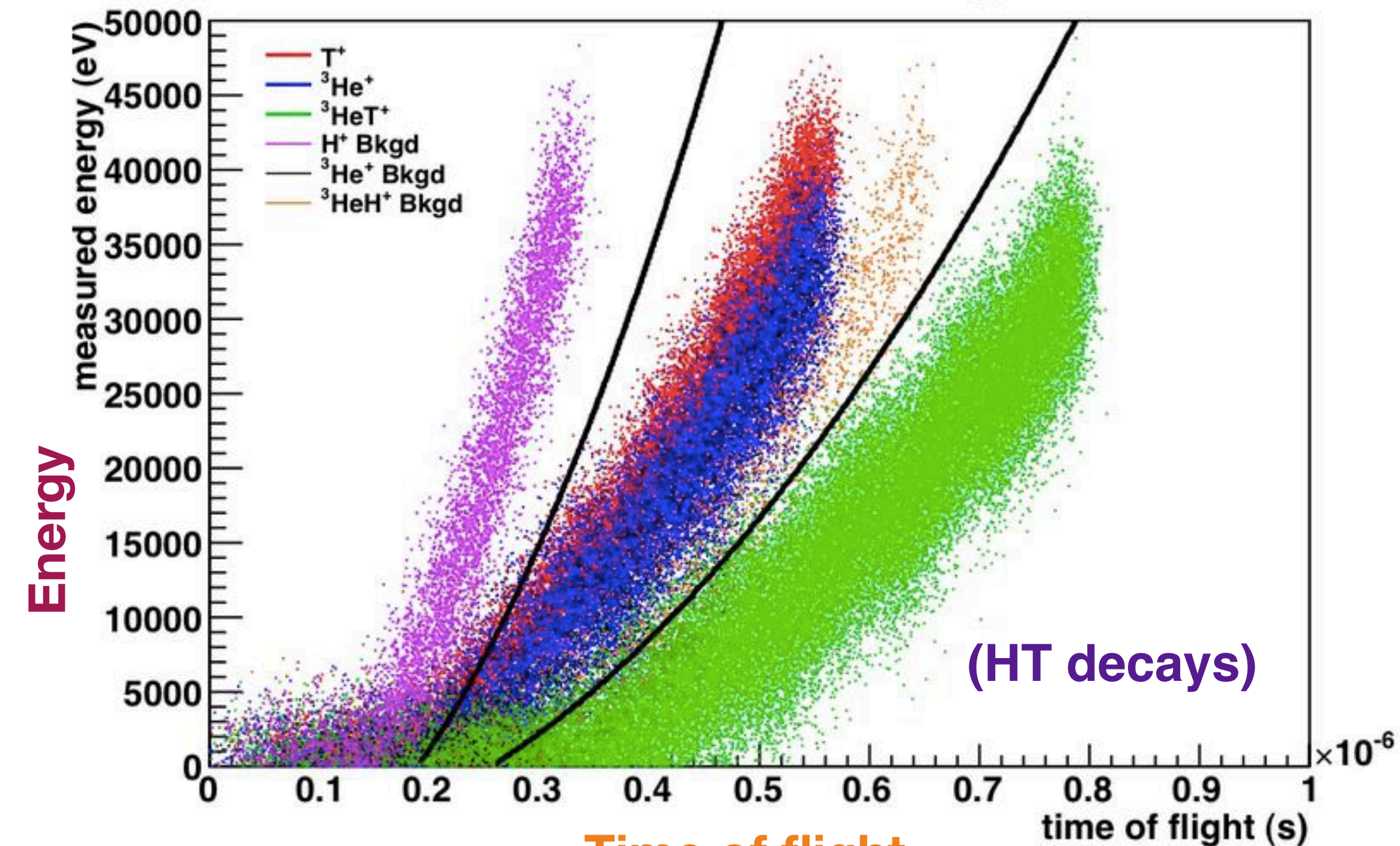


# TRIMS

<https://www.npl.washington.edu/TRIMS>



TRIMS Sim: Ion Measured Energy vs TOF



Time of flight

$$E_{\text{ion}} \sim \frac{qV_{\text{chamber}}\Delta D_{\text{ion}}}{L_{\text{chamber}}}$$

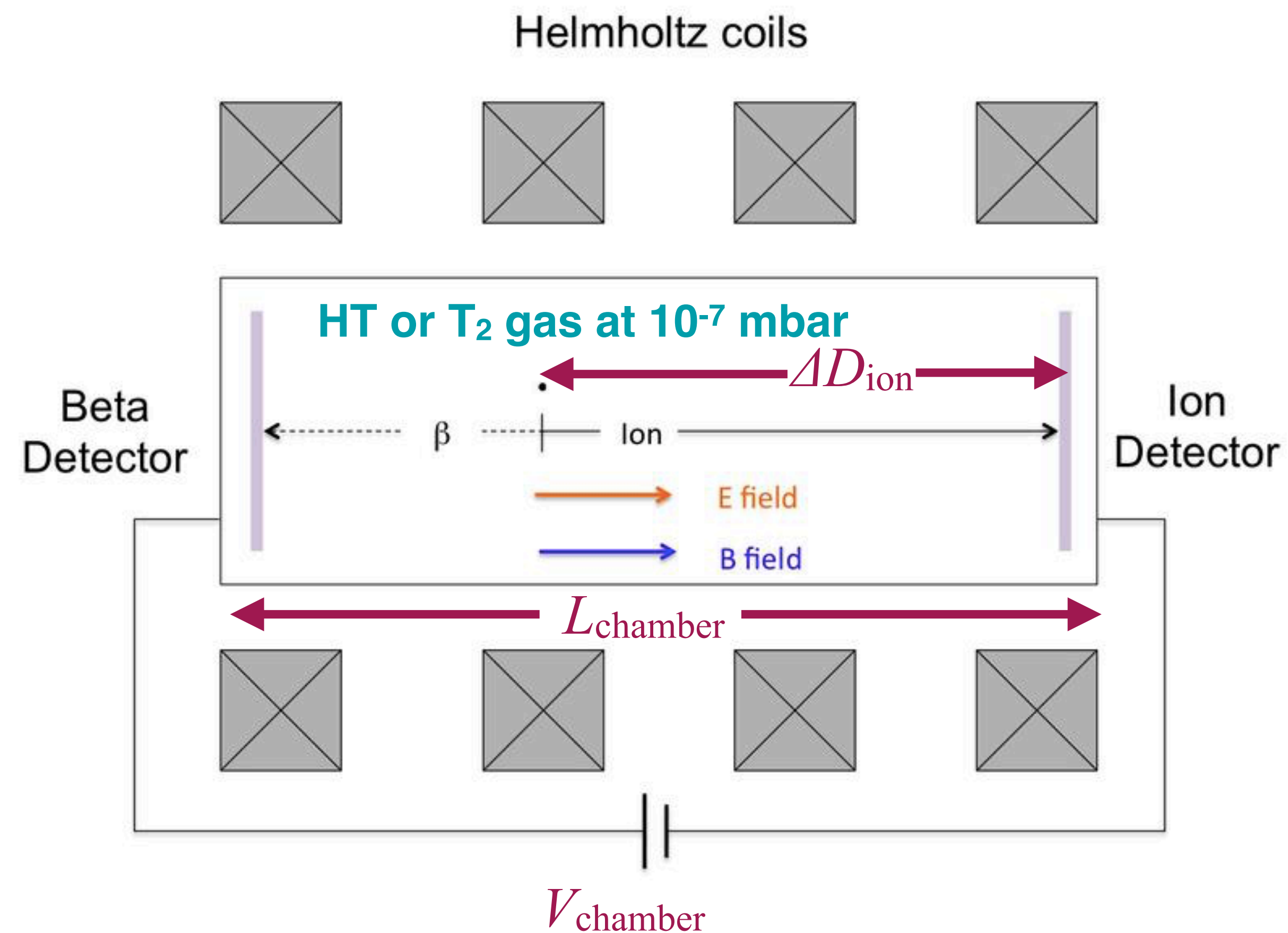
$$t_{\text{drift}} \sim \sqrt{\frac{2mL_{\text{chamber}}\Delta D_{\text{ion}}}{qV_{\text{chamber}}}}$$

Energy and time of flight separate final states so **branching ratio** can be calculated



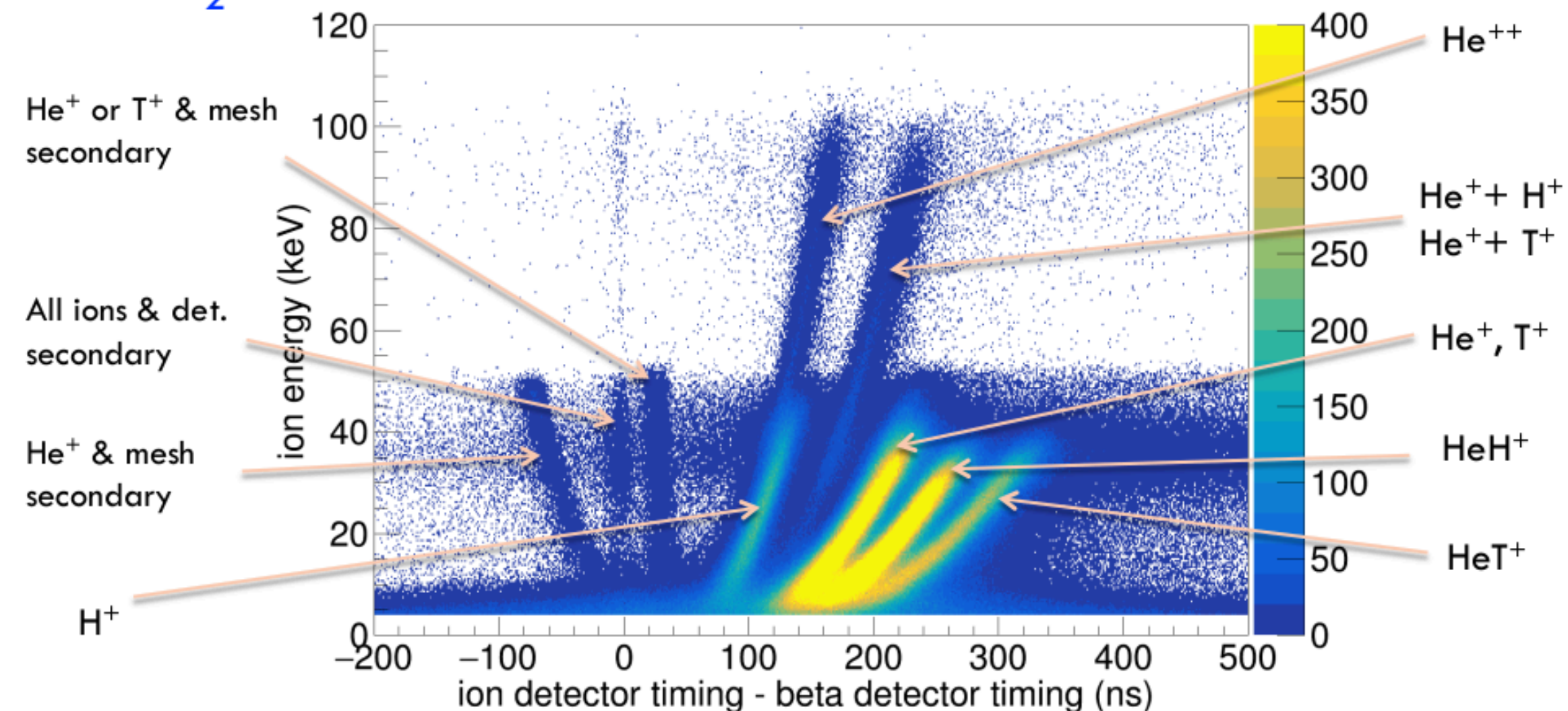
# TRIMS

<https://www.npl.washington.edu/TRIMS>



HT + T<sub>2</sub>

Run 2084-3404, Ion Spectrum

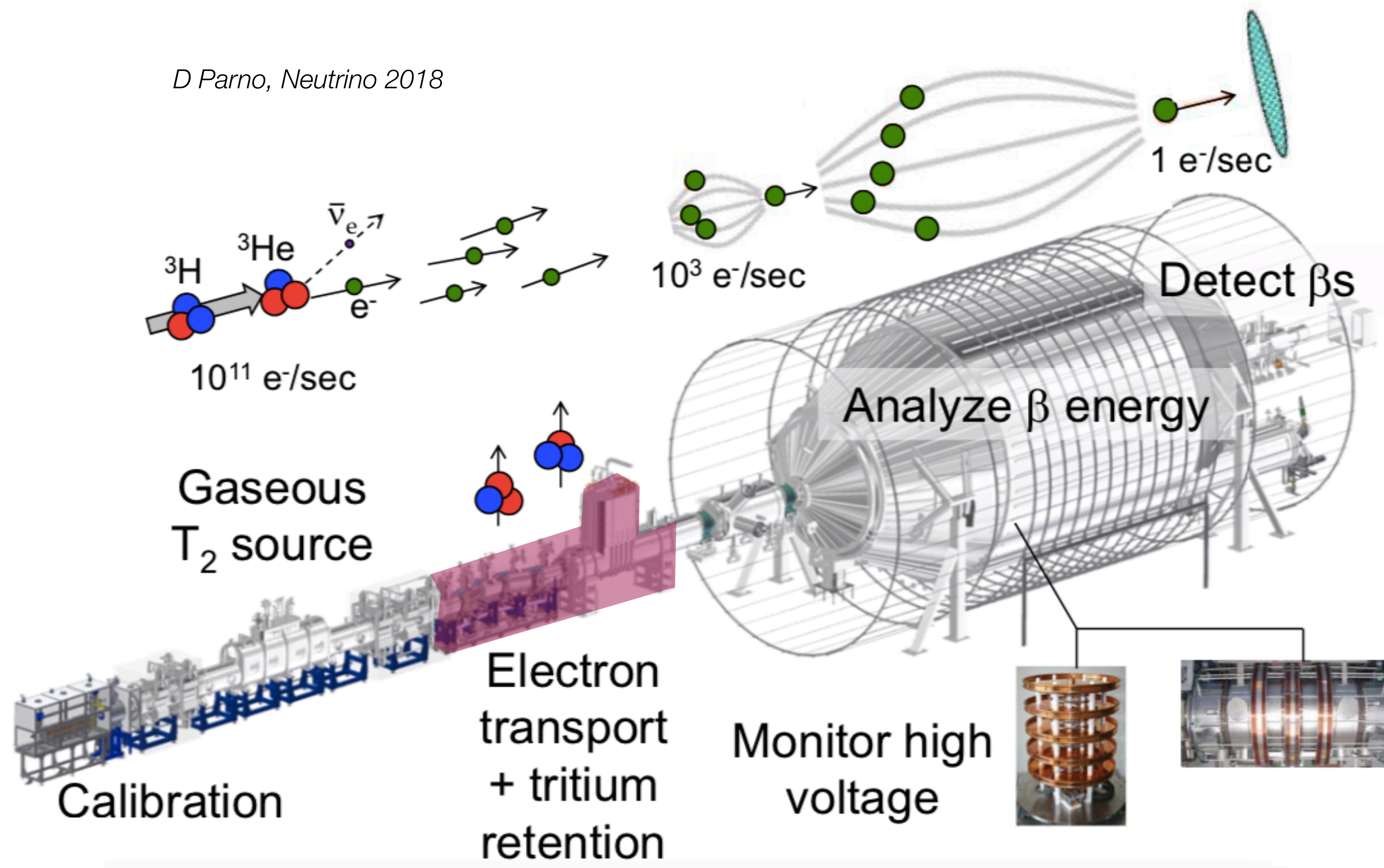


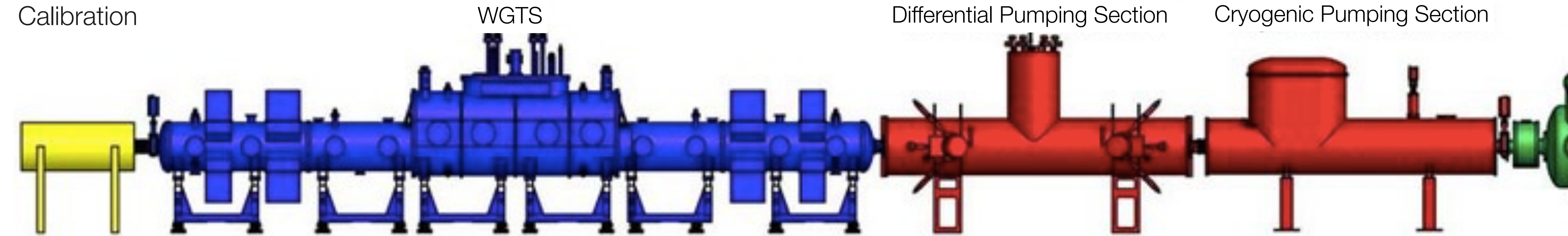
$$E_{\text{ion}} \sim \frac{qV_{\text{chamber}} \Delta D_{\text{ion}}}{L_{\text{chamber}}}$$

$$t_{\text{drift}} \sim \sqrt{\frac{2mL_{\text{chamber}} \Delta D_{\text{ion}}}{qV_{\text{chamber}}}}$$

**Energy** and **time of flight** separate final states so **branching ratio** can be calculated

*D Parno, Neutrino 2018*



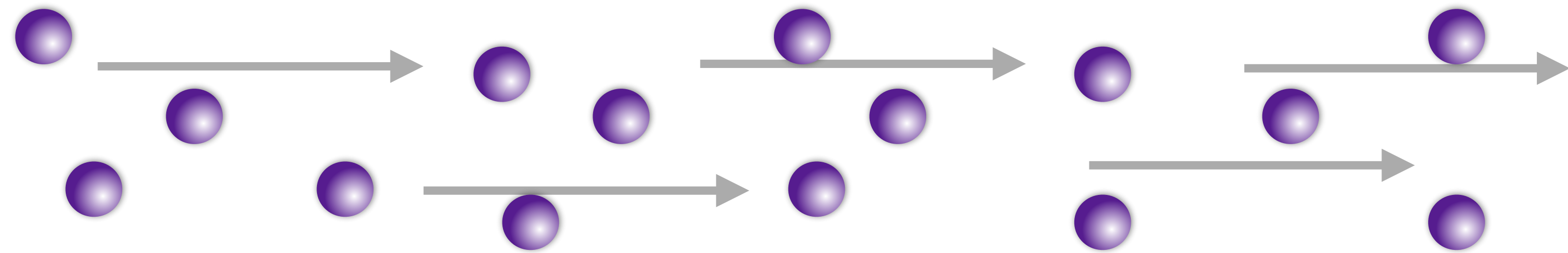
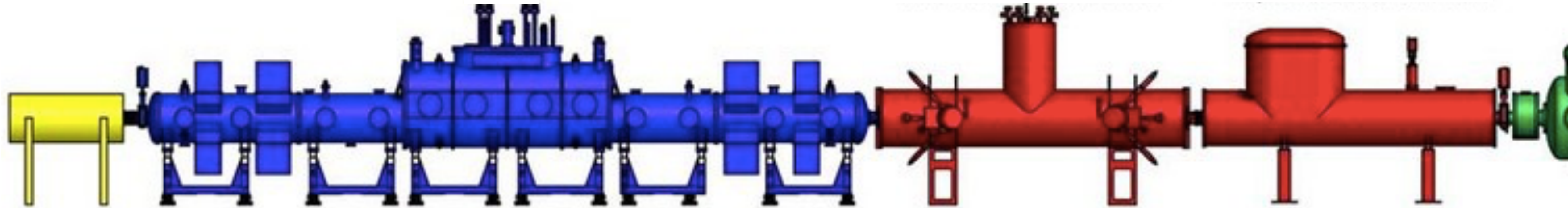


Calibration

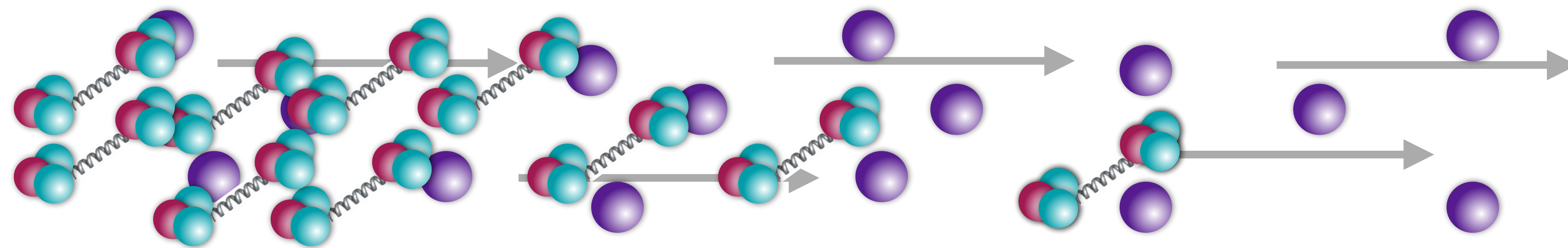
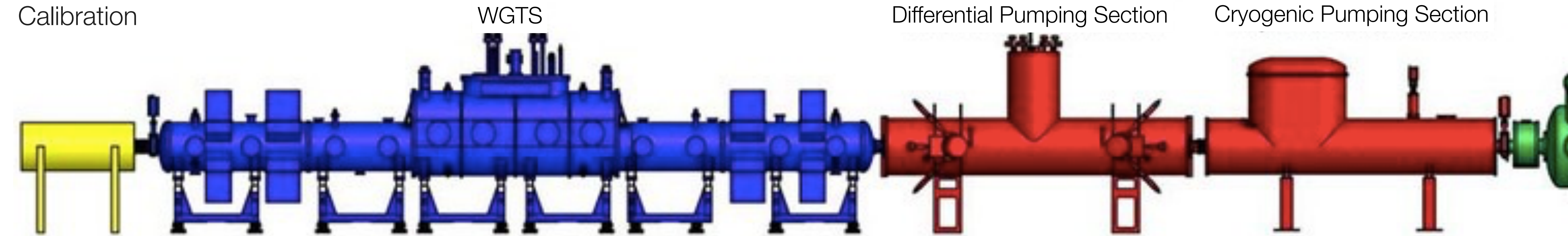
WGTS

Differential Pumping Section

Cryogenic Pumping Section

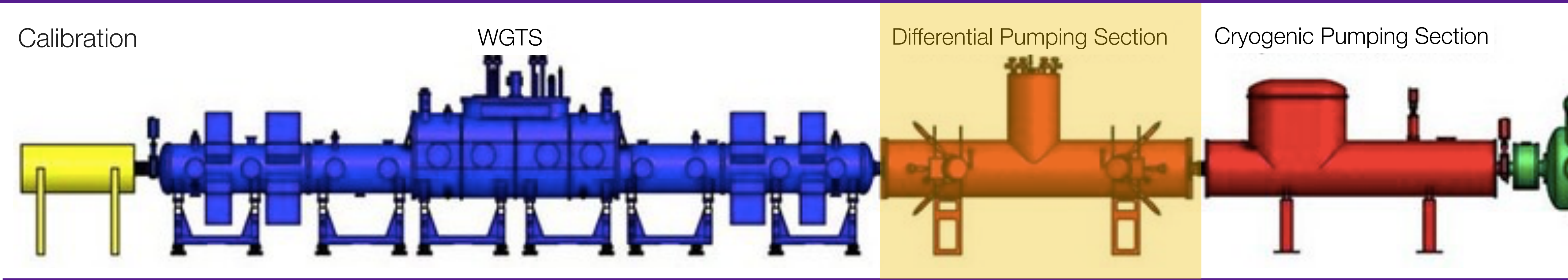


Electrons are guided adiabatically towards the spectrometers...

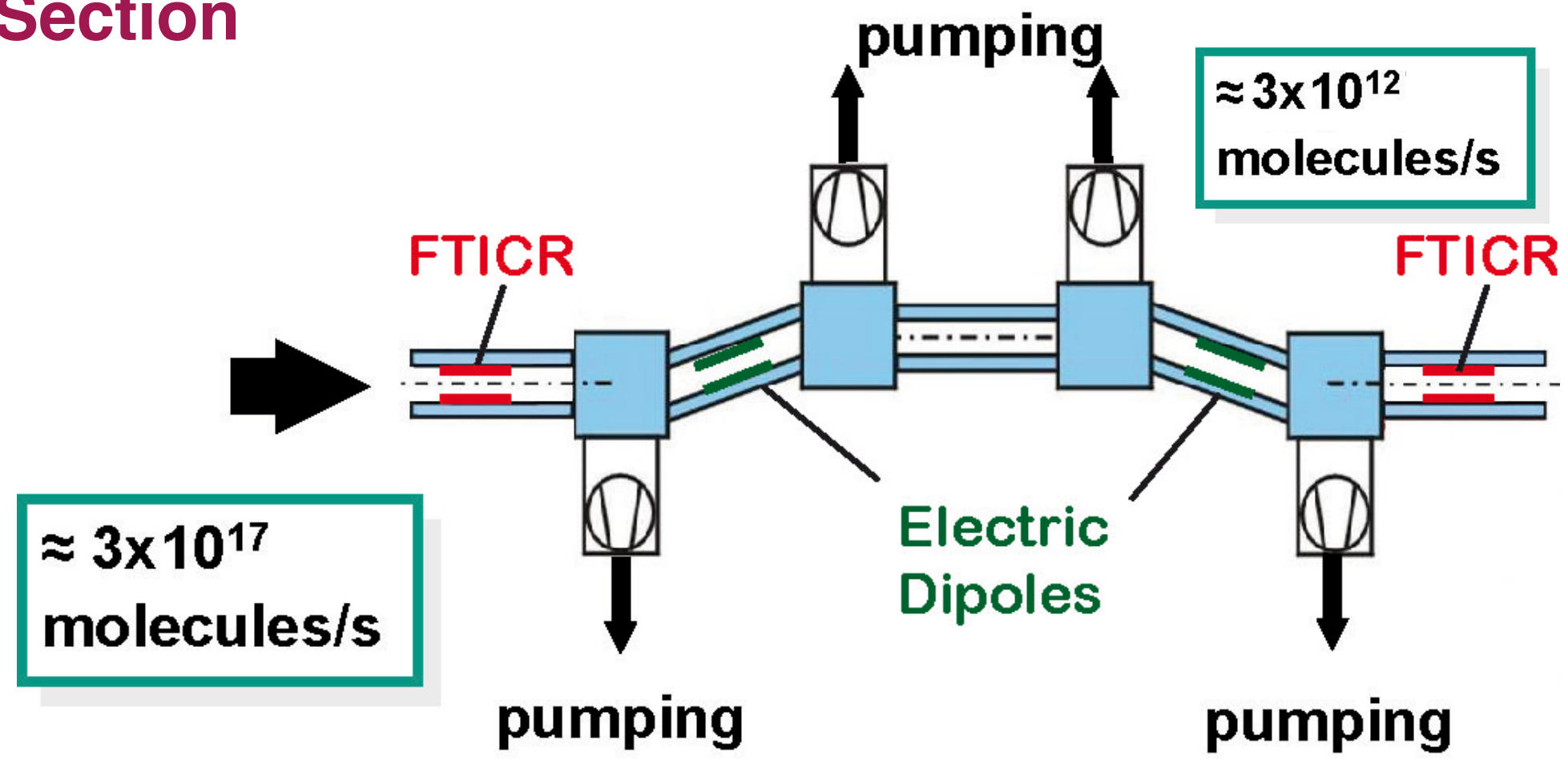


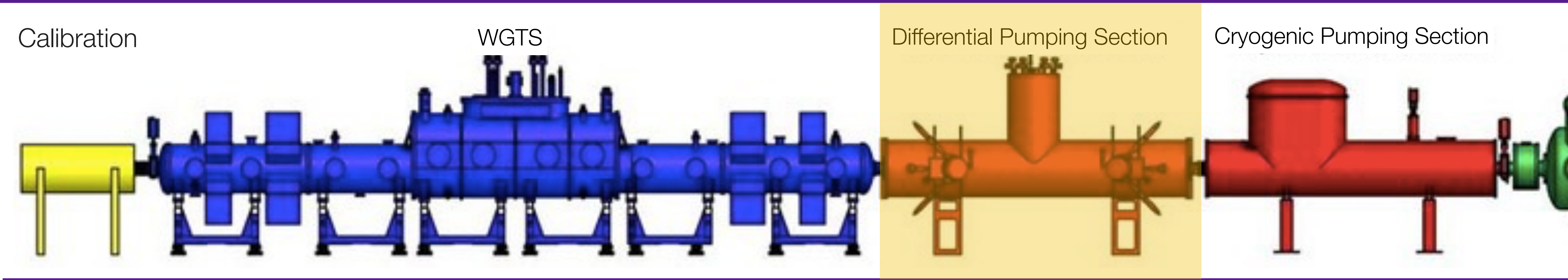
Electrons are guided adiabatically towards the spectrometers...

... while any remaining tritium is suppressed by a factor of  $10^9$

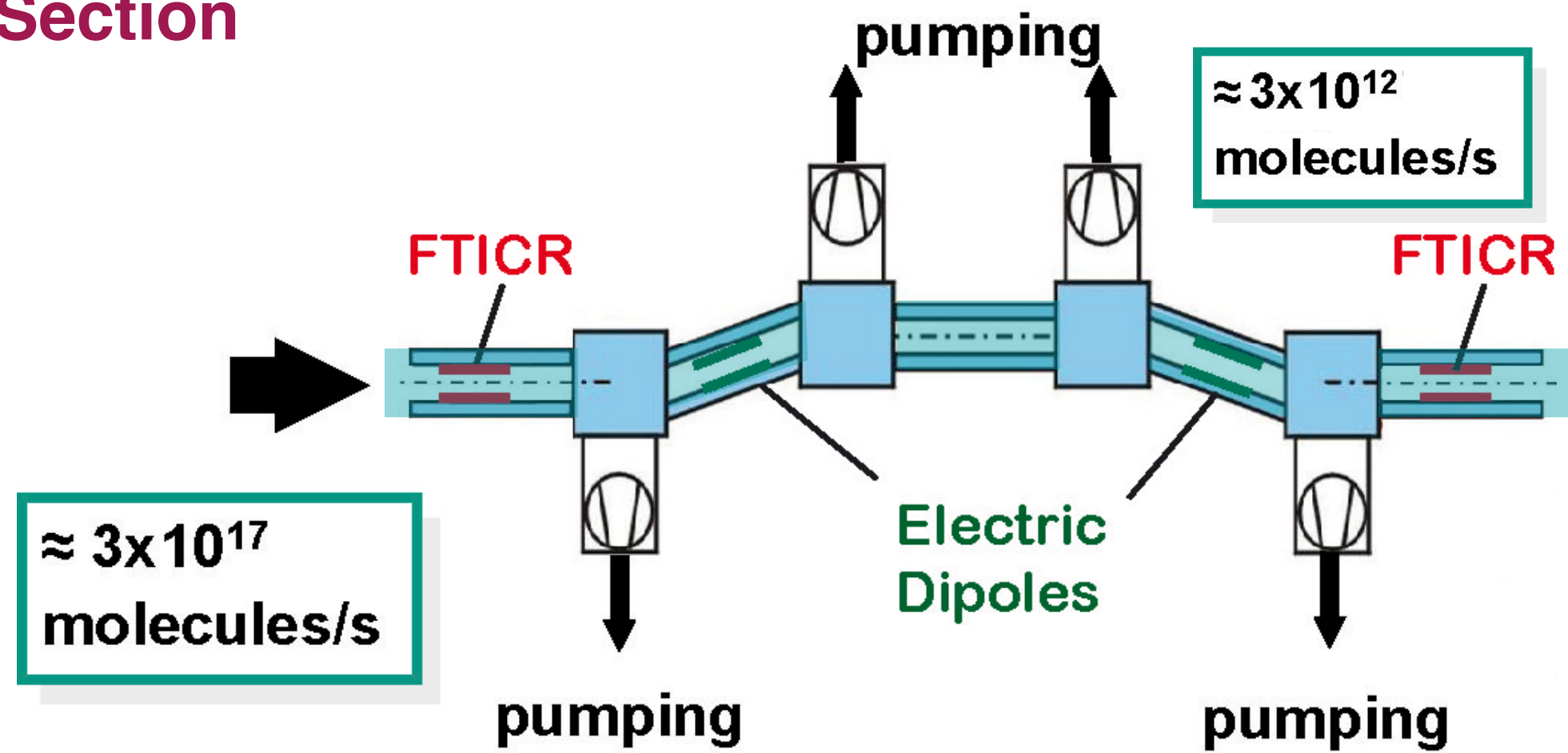


## Differential Pumping Section

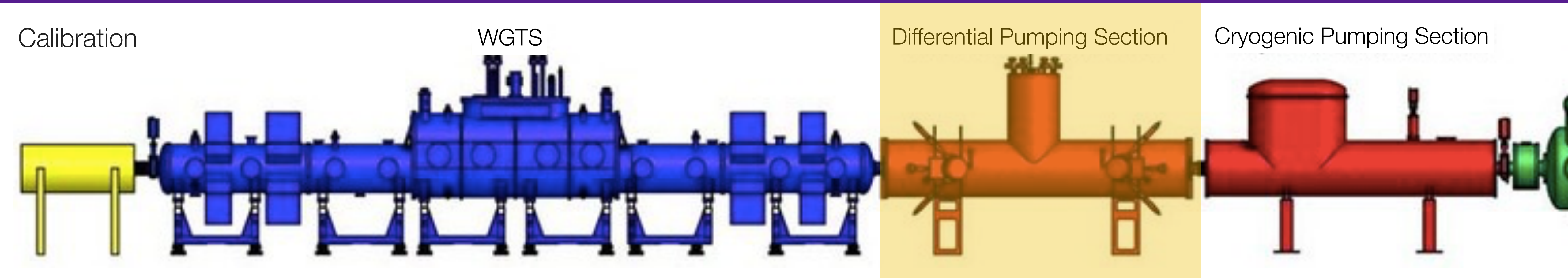




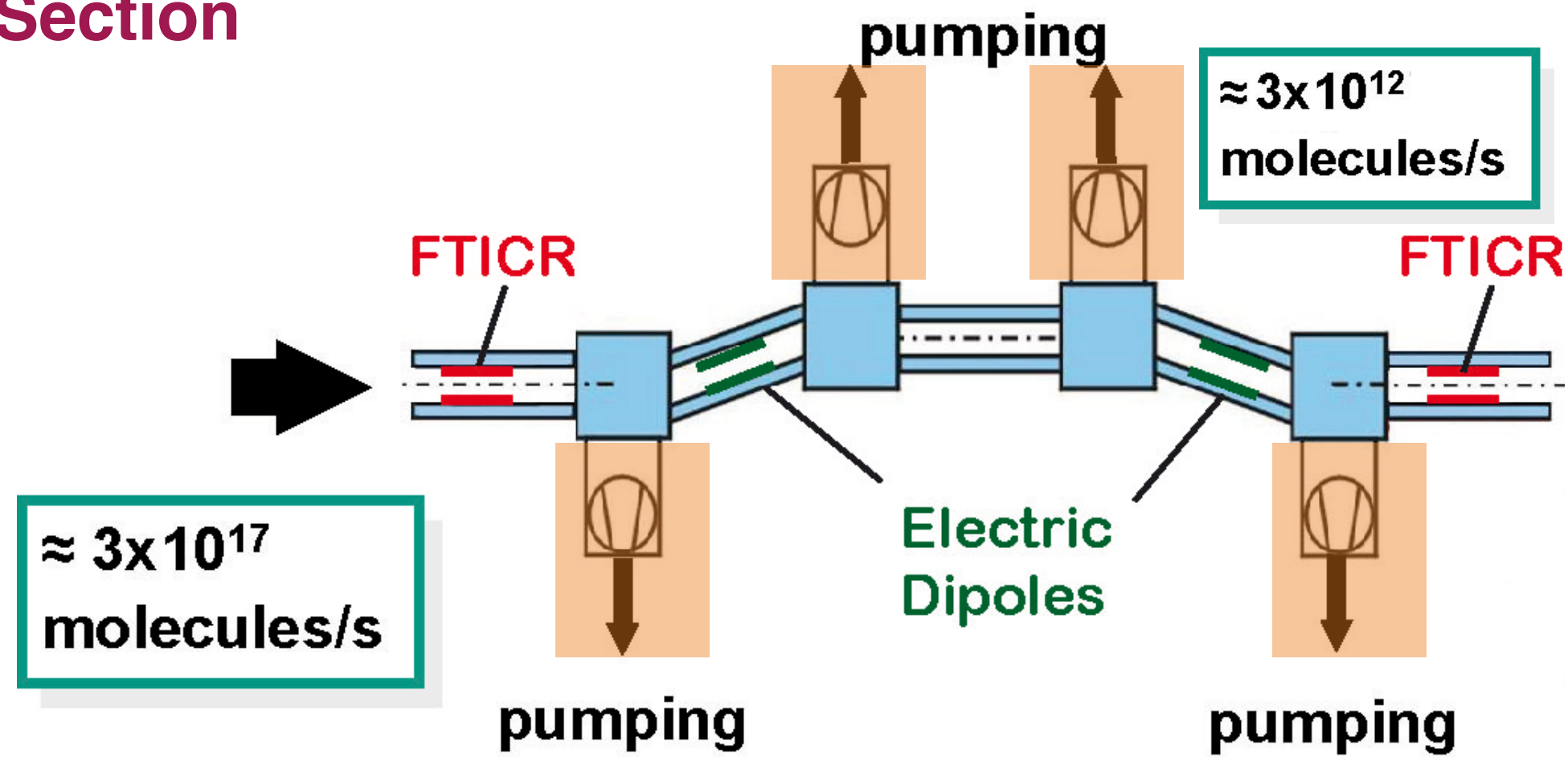
## Differential Pumping Section



- Five 1-metre tubes with 20 degree tilt to block line of sight for **neutral molecules**

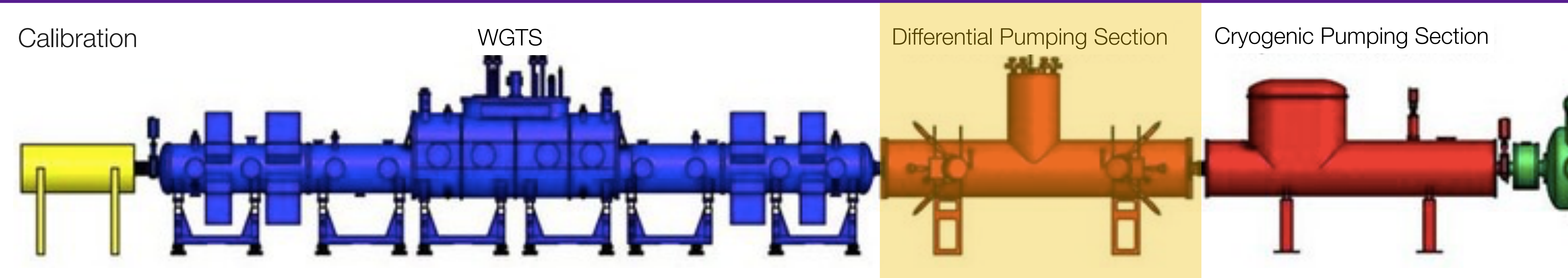


## Differential Pumping Section

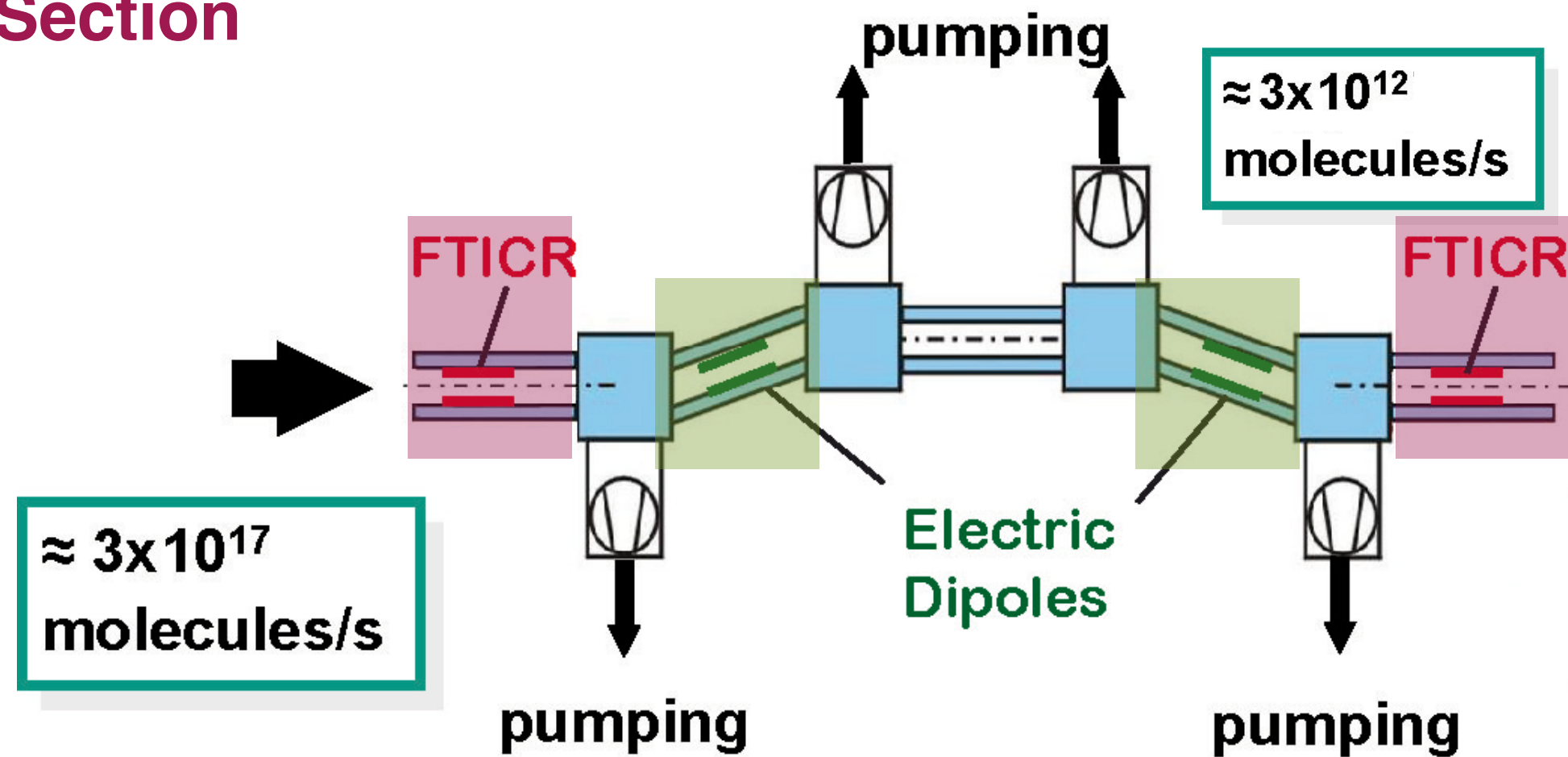


- Five 1-metre tubes with 20 degree tilt to block line of sight for **neutral molecules**
- **Turbo-molecular pumps** reduce tritium flow by  $2.5 \times 10^4$

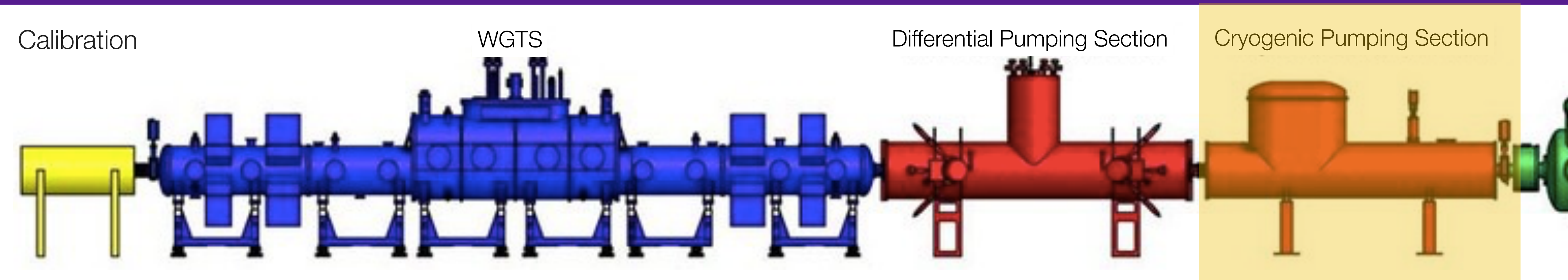




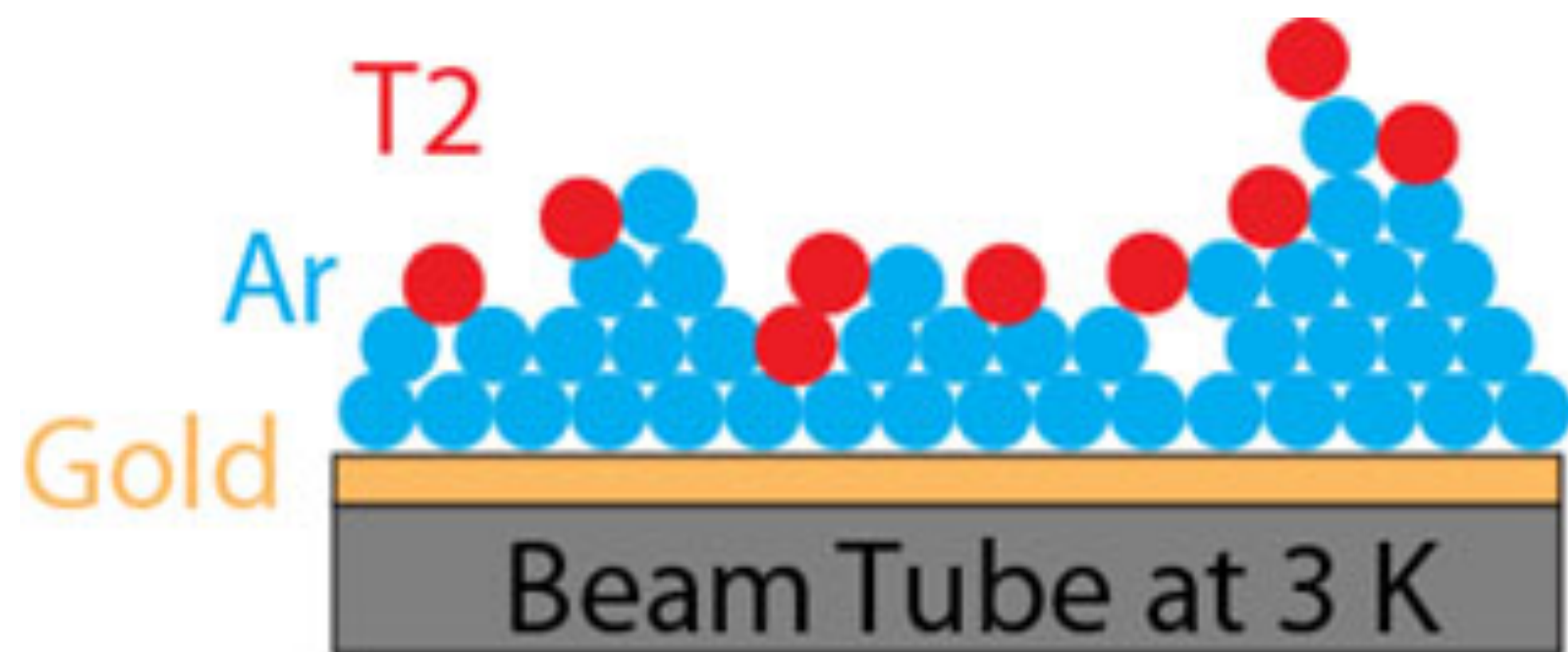
## Differential Pumping Section



- Five 1-metre tubes with 20 degree tilt to block line of sight for **neutral molecules**
- **Turbo-molecular pumps** reduce tritium flow by  $2.5 \times 10^4$
- **Dipole electrodes** and **Fourier-transform ion cyclotron resonators** remove positive ions

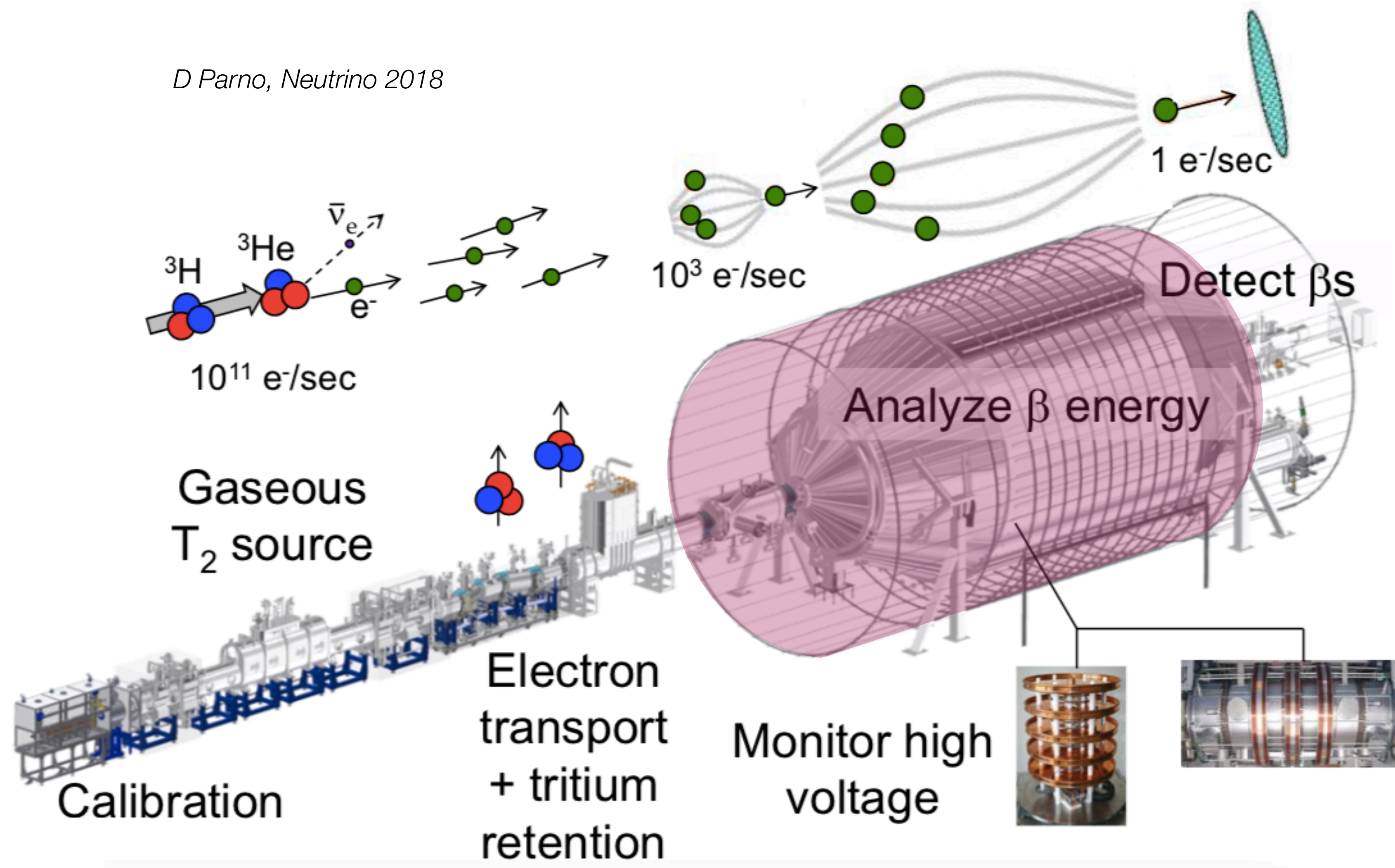


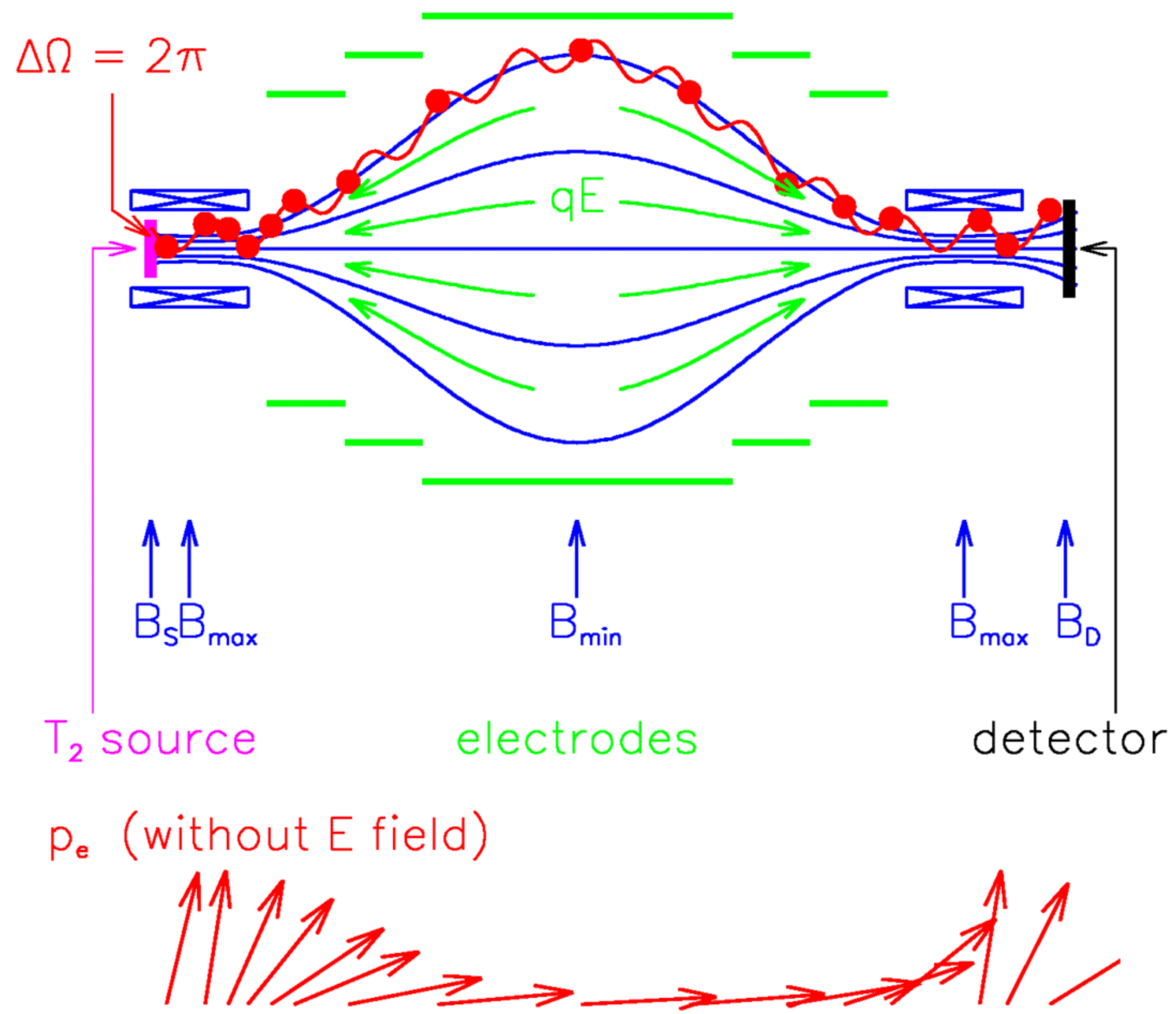
## Cryogenic pumping section



- Beam pipe coated with **argon frost**
- Remaining **tritium** is trapped by **cryo-sorption**
- After 60 days, surface is **saturated** - **heat** to 100 K to release tritium and **pump** it away
- Tritium suppressed by **12 orders of magnitude** relative to source inlet

*D Parno, Neutrino 2018*

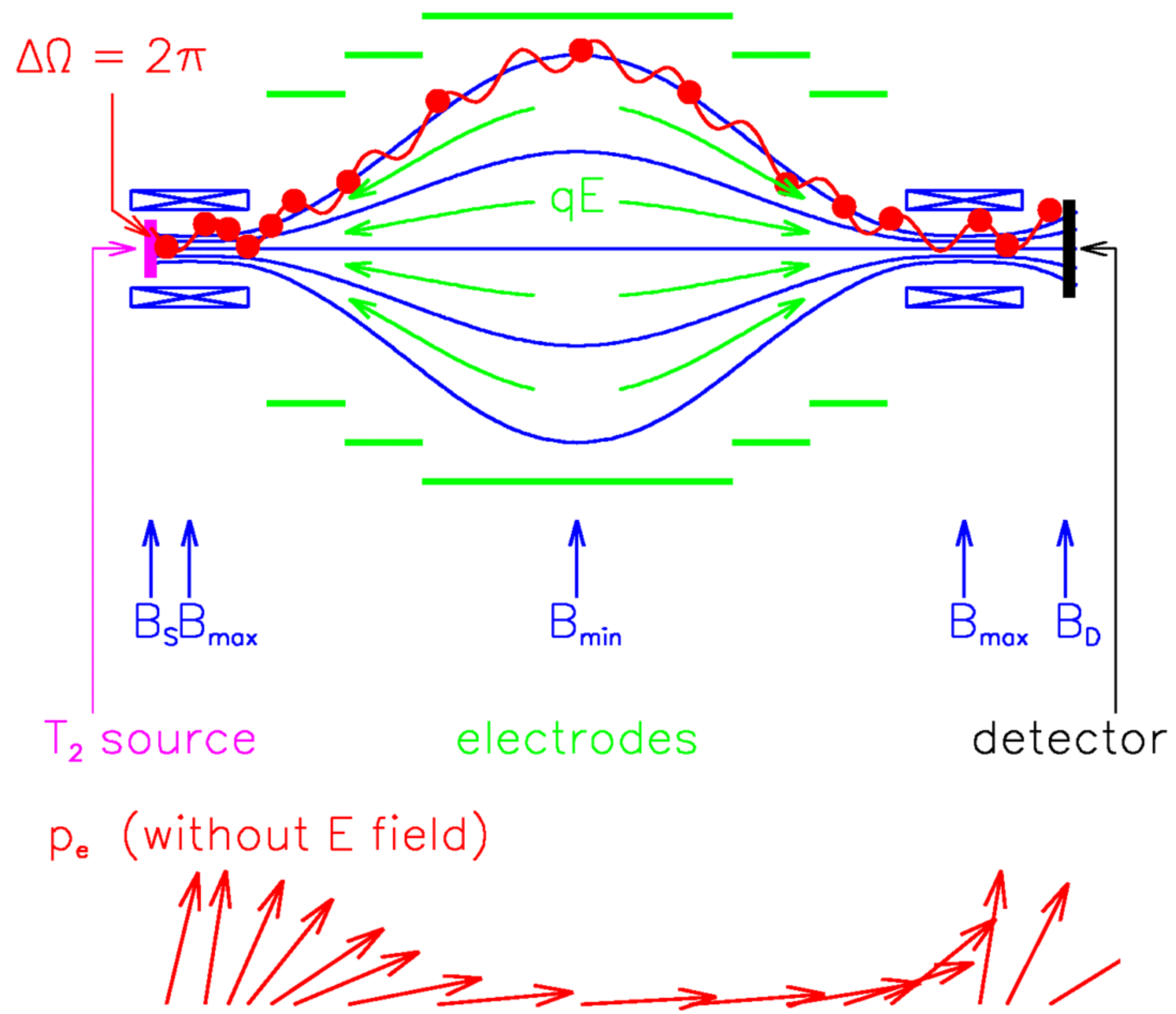




<https://www.katrin.kit.edu/>

Kleesiek et al., arXiv:1806.00369

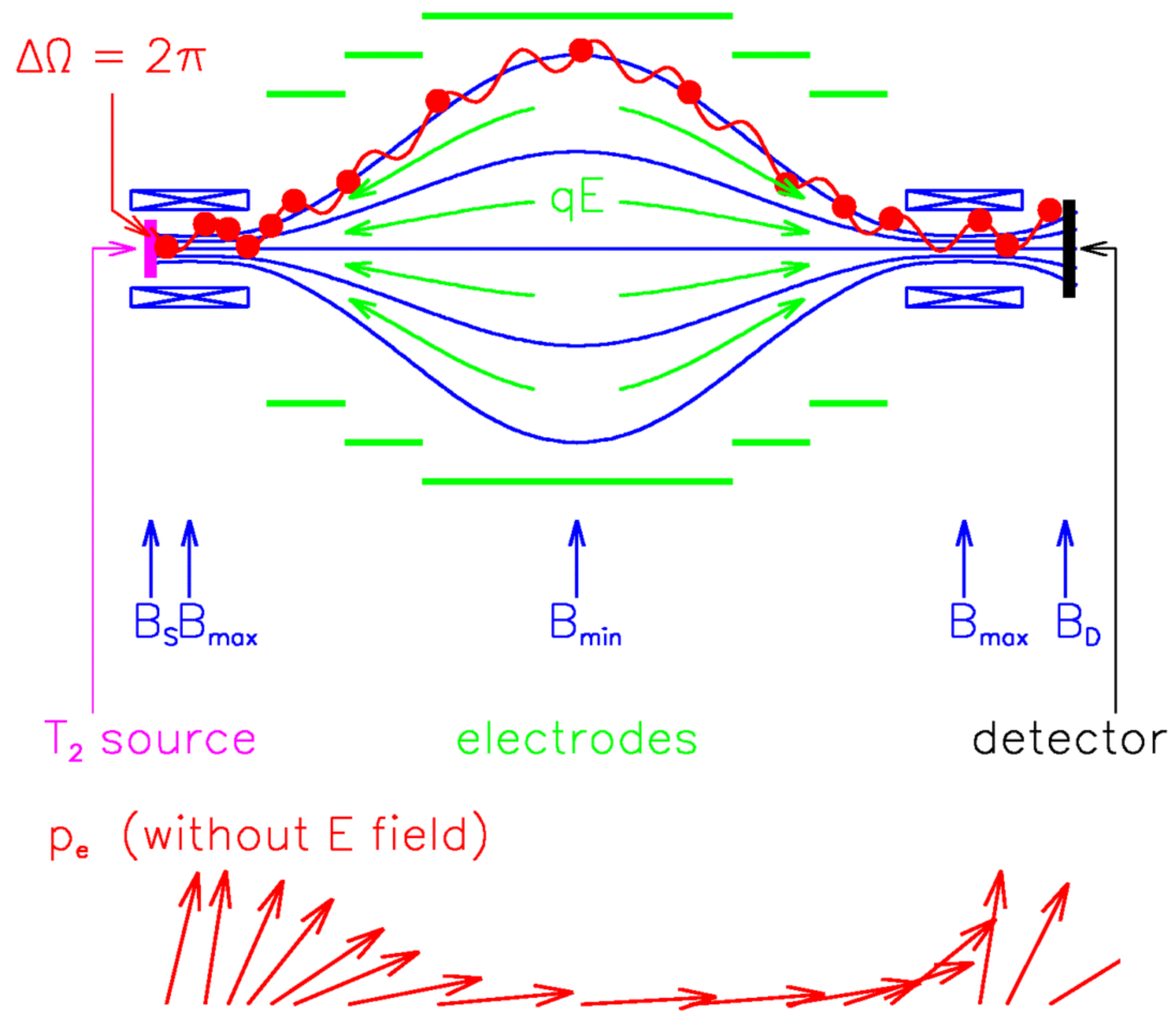
## Magnetic



<https://www.katrin.kit.edu/>

Kleesiek et al., arXiv:1806.00369

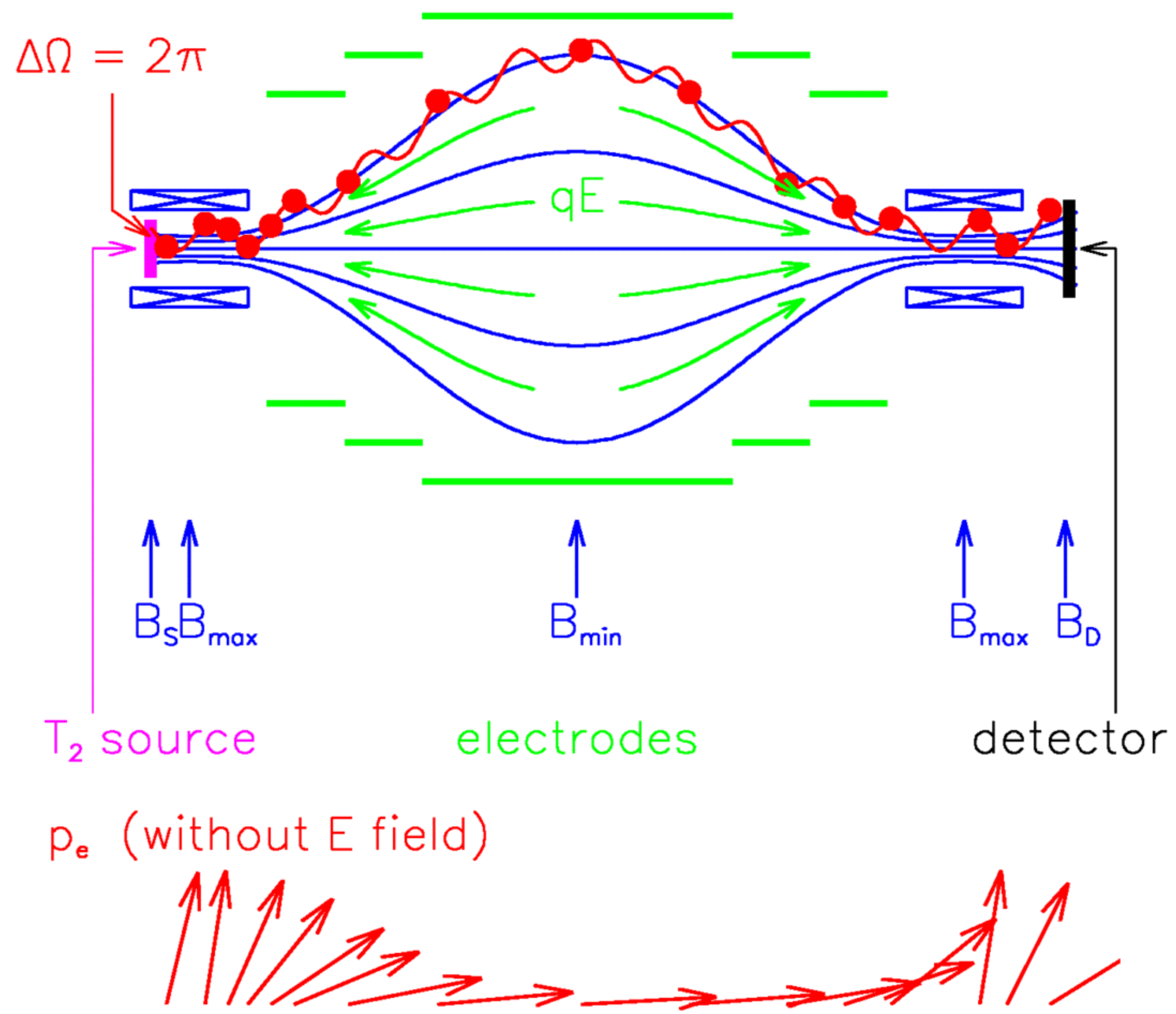
Magnetic **A**diabatic



<https://www.katrin.kit.edu/>

Kleesiek et al., arXiv:1806.00369

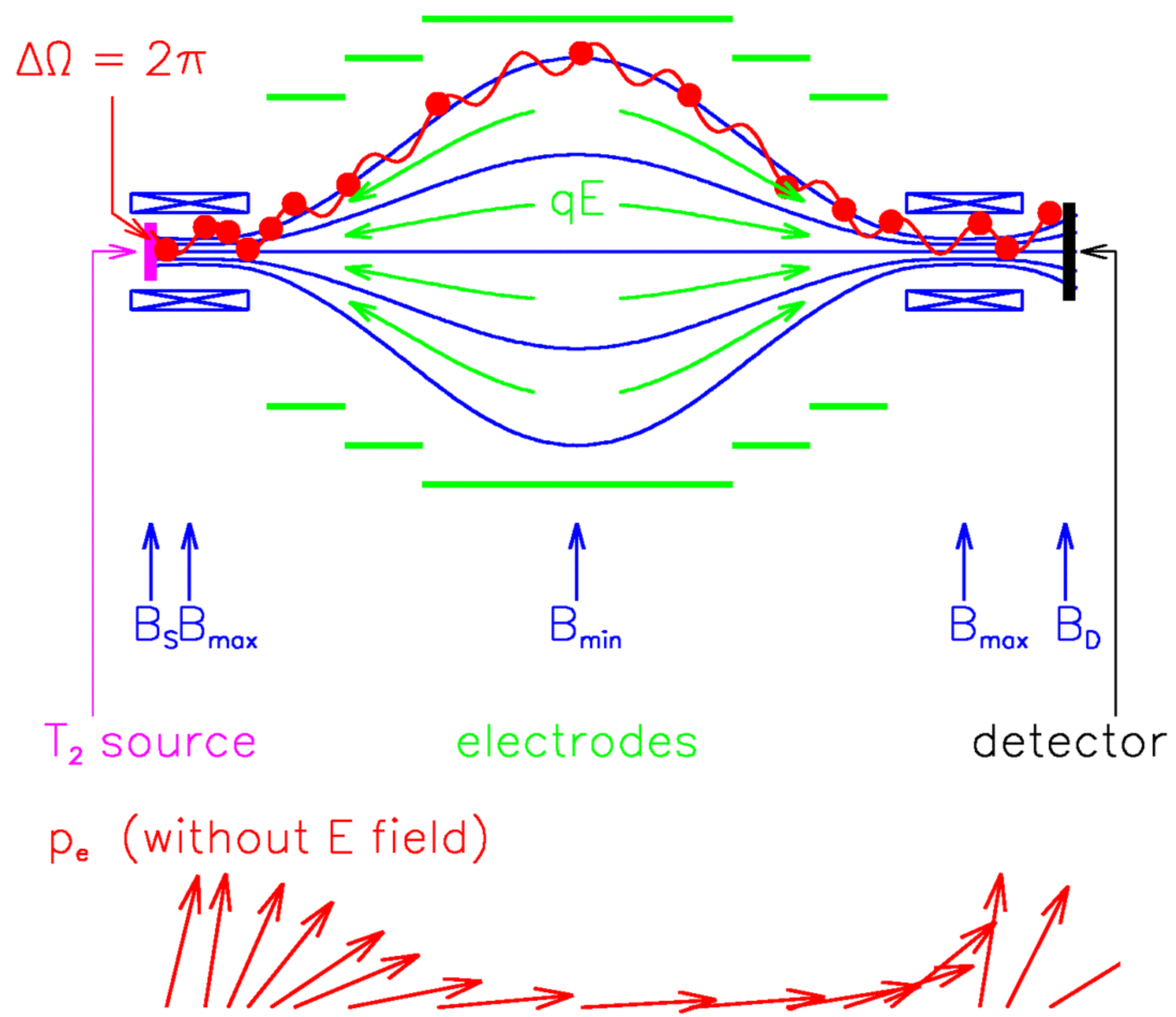
Magnetic Adiabatic Collimation with an



<https://www.katrin.kit.edu/>

Kleesiek et al., arXiv:1806.00369

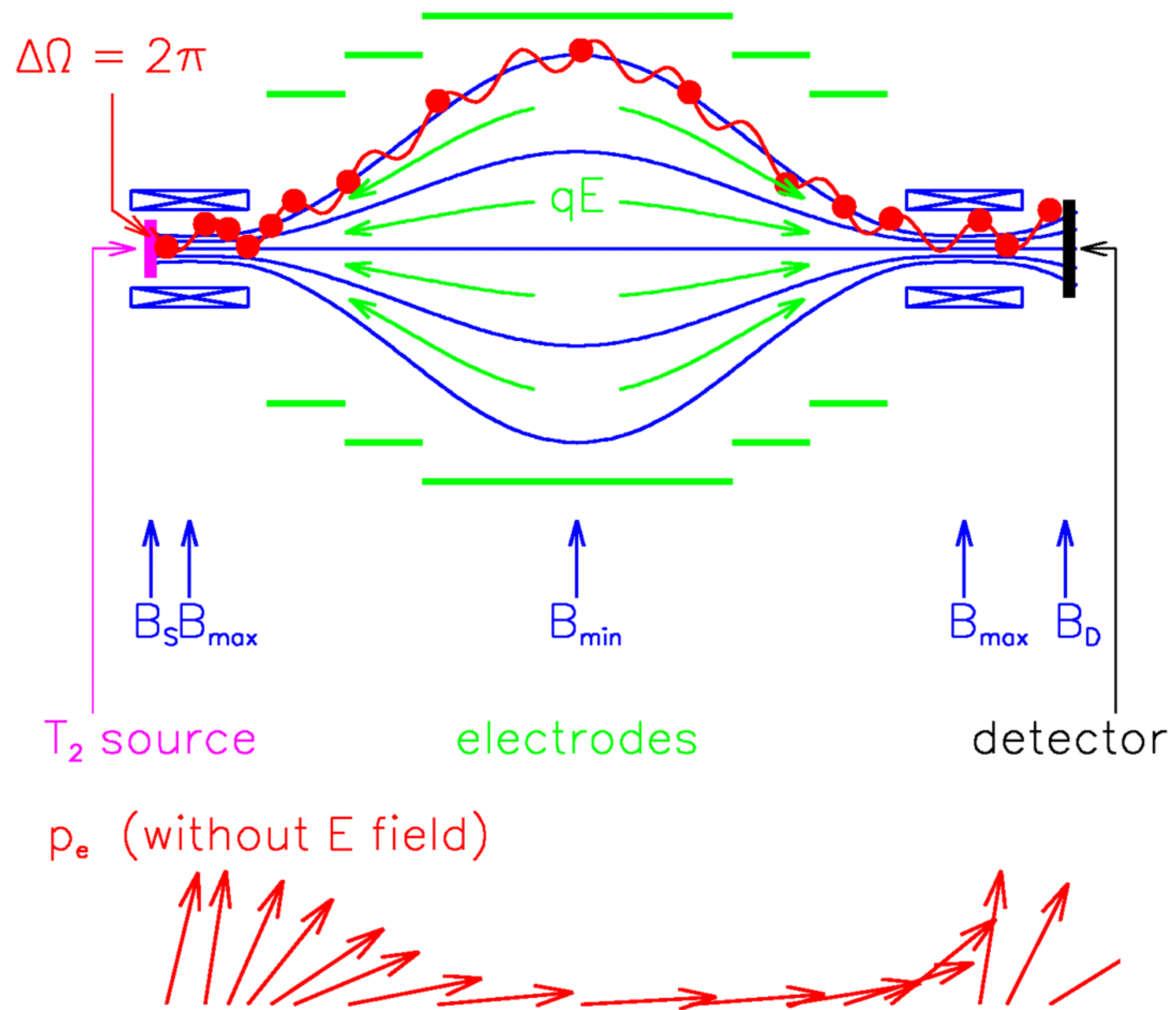
## Magnetic Adiabatic Collimation with an Electrostatic Filter



<https://www.katrin.kit.edu/>

Kleesiek et al., arXiv:1806.00369



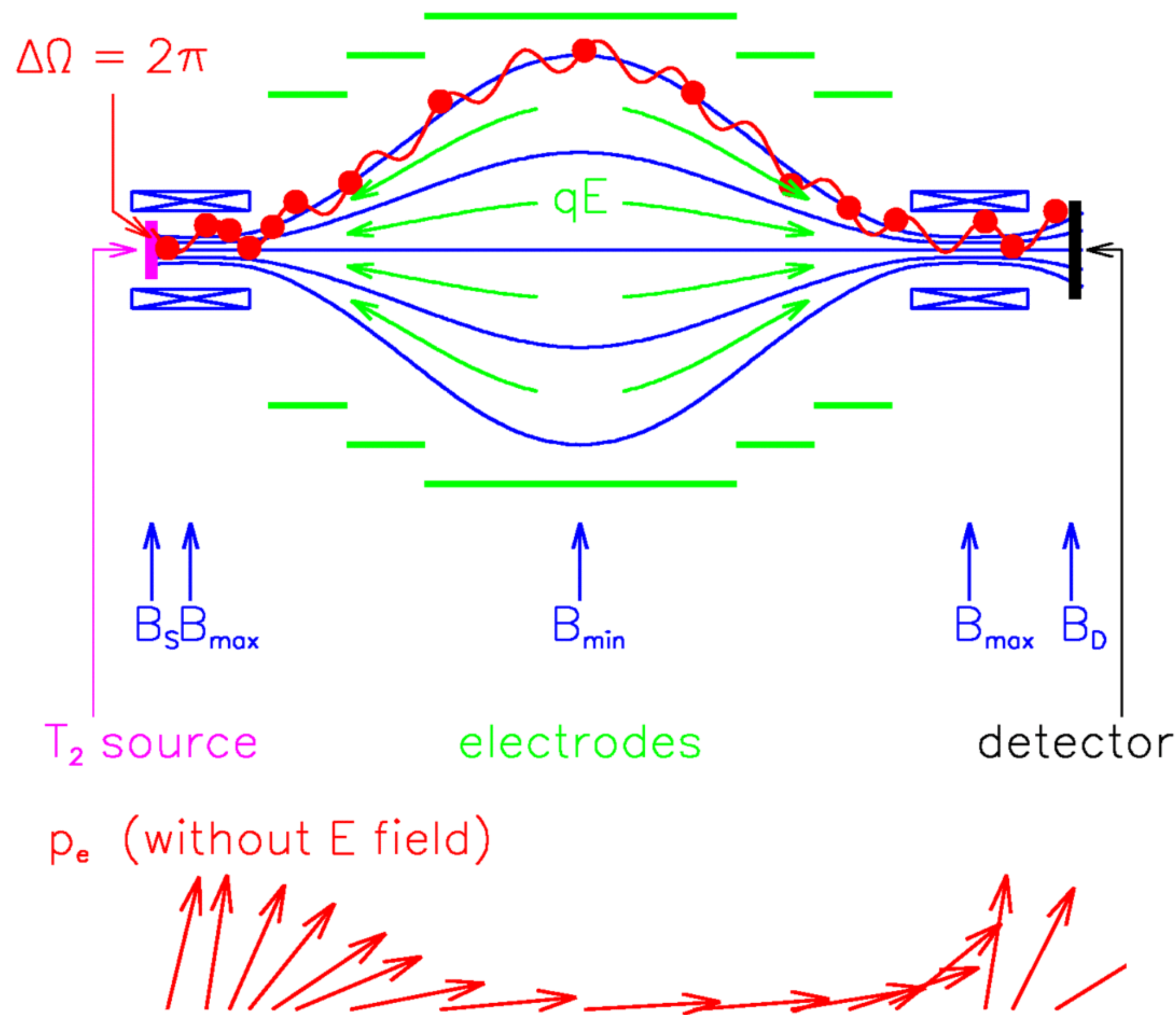


<https://www.katrin.kit.edu/>

## Magnetic Adiabatic Collimation with an Electrostatic Filter

- Two **superconducting solenoids** produce a guiding field **B**.
- Any forward-going  **$\beta$  electrons** from the **tritium source** are guided in **cyclotron motion** along the **B-field lines**, towards the **detector**, giving angular acceptance  $\sim 2\pi$ .

Kleesiek et al., arXiv:1806.00369



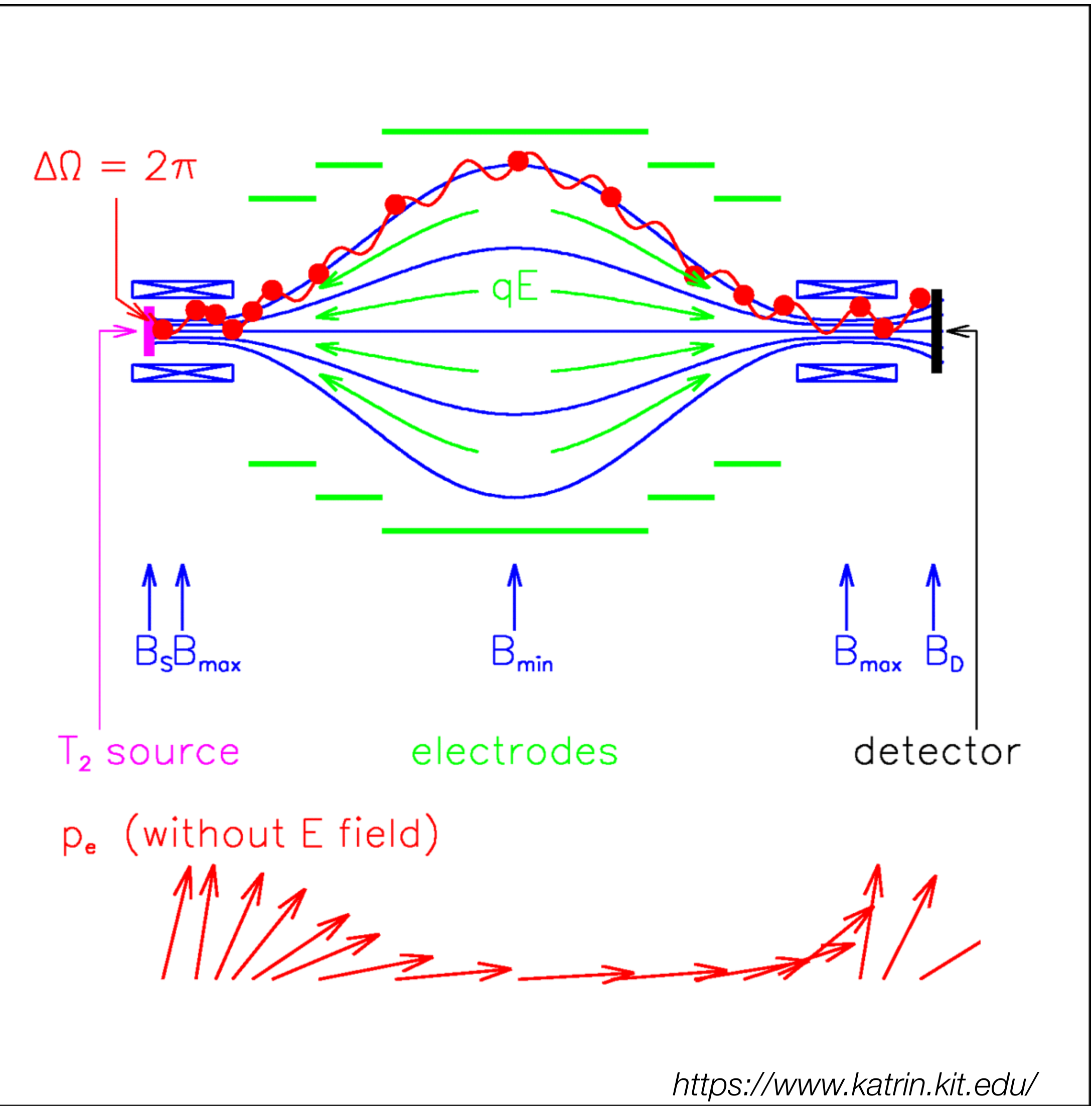
<https://www.katrin.kit.edu/>

## Magnetic Adiabatic Collimation with an Electrostatic Filter

- The **magnetic field** varies through the spectrometer - strongest at the solenoids near source and detector, orders of magnitude weaker in the middle.
- Cyclotron motion is transformed to longitudinal motion in the middle of the spectrometer : isotropic  $\beta$  electrons become **parallel electron beam**
- The slow variation of field means transformation is **adiabatic**: constant magnetic moment

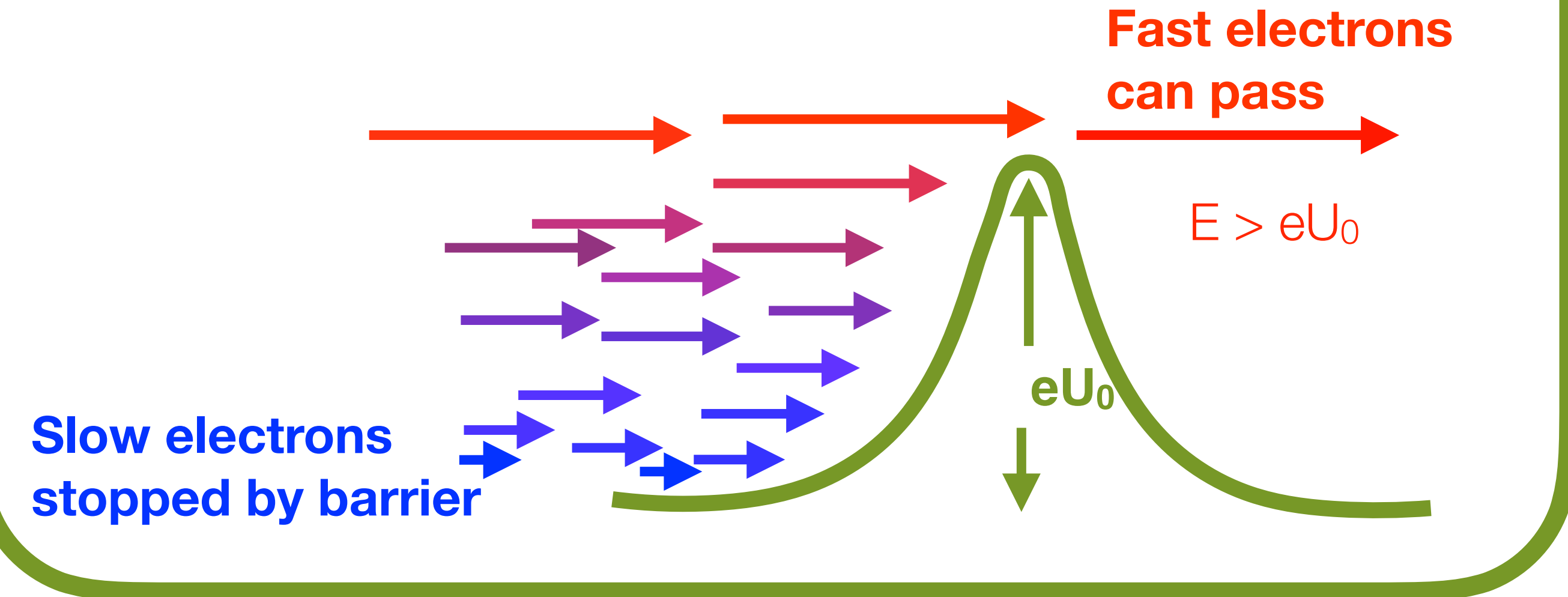
$$\mu = \frac{E_{\perp}}{B} = \text{const}$$

Kleesiek et al., arXiv:1806.00369



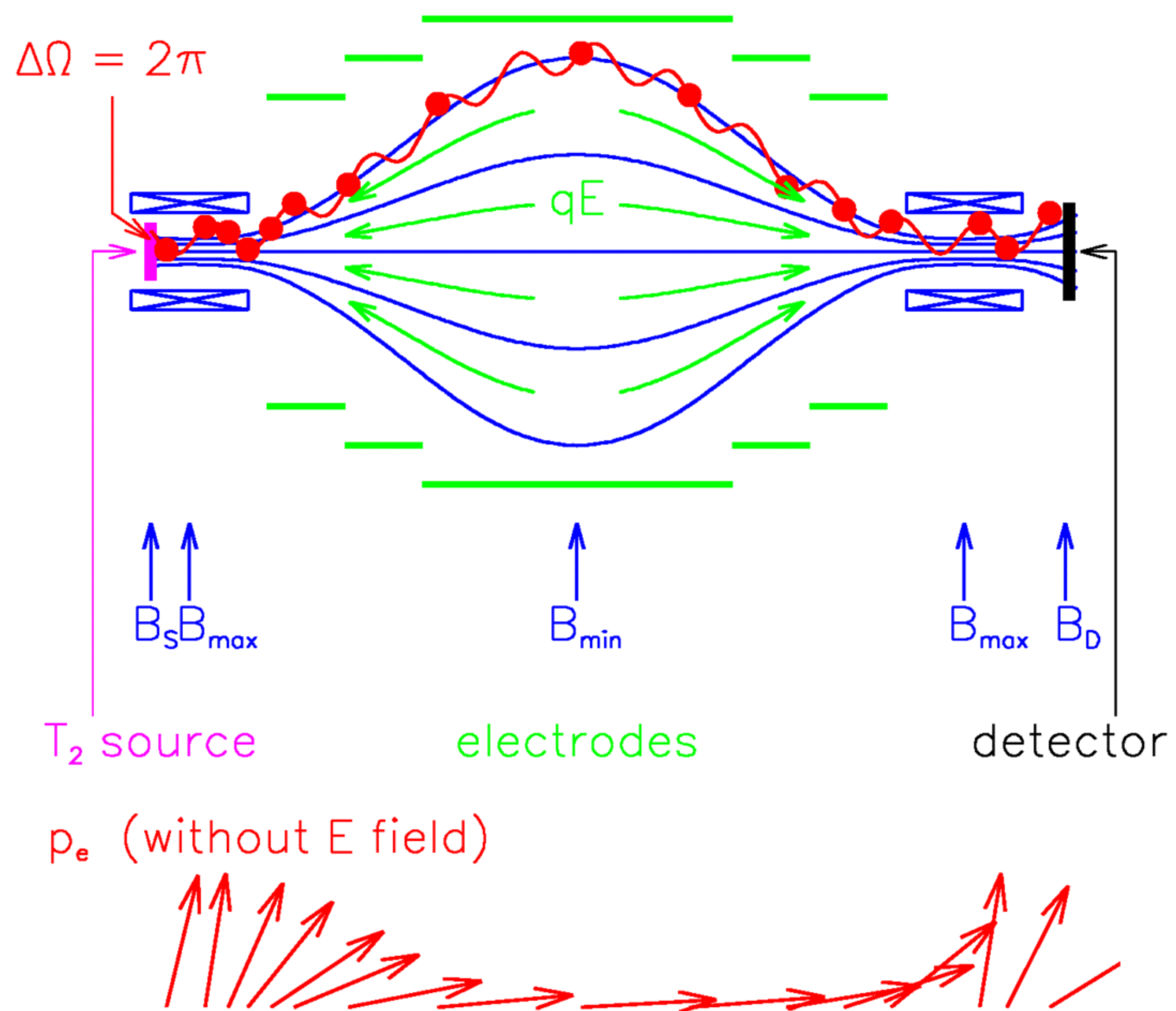
## Magnetic Adiabatic Collimation with an Electrostatic Filter

- Cylindrical **electrodes** create an electrostatic potential
- This acts in the opposite direction from the **electron beam**
- Only the **highest energy electrons** can pass through the **electrostatic barrier**



Kleesiek et al., arXiv:1806.00369

## Magnetic Adiabatic Collimation with an Electrostatic Filter

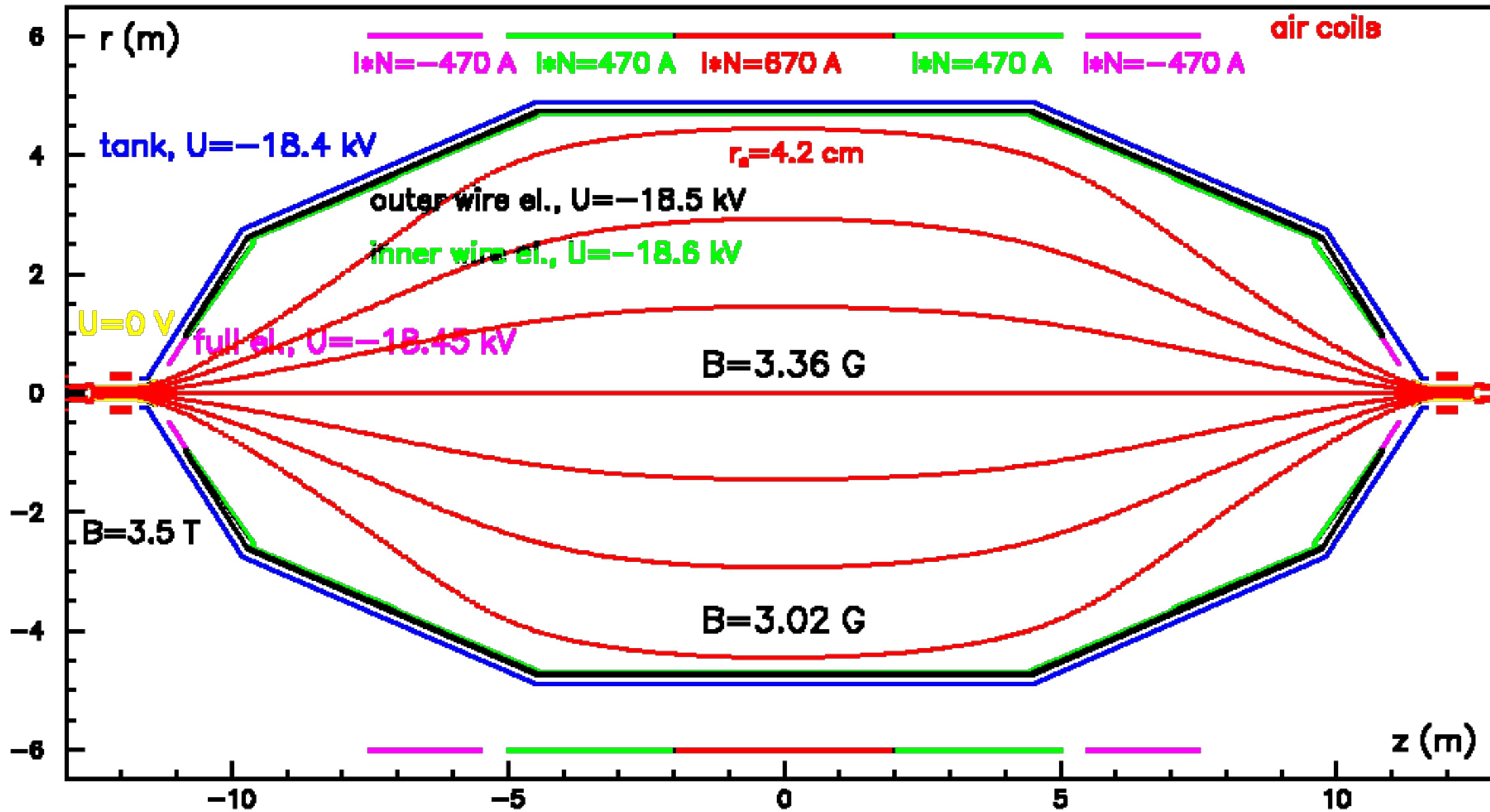


<https://www.katrin.kit.edu/>

- Surviving electrons are re-accelerated and **collimated** on the **detector**
- By measuring the count that make it through the high-pass energy filter at different **electrostatic potentials**, we can measure an **integrated electron energy spectrum**.
- Sharpness of filter given by

$$\frac{\Delta E}{E} = \frac{B_{min}}{B_{max}}$$

Kleesiek et al., arXiv:1806.00369



(1 Tesla =  $10^4$  Gauss)



Photos from symmetry magazine



**Karlsruhe**

**Deggendorf**

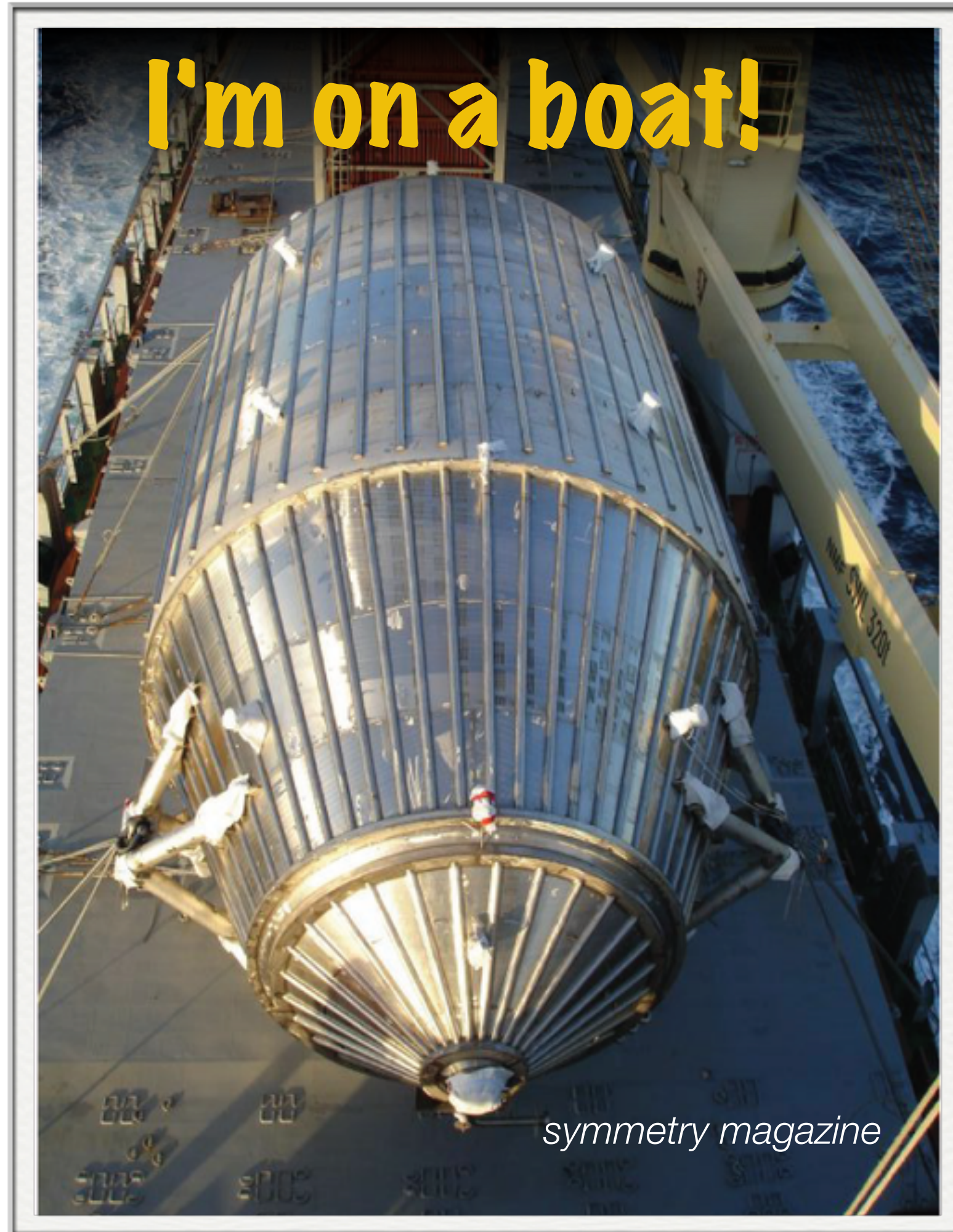


- 10 metres wide, 200 tons
- Half a mile of specialist welding at **Deggendorf**
- Destination: **Karlsruhe**



- 10 metres wide, 200 tons
- Half a mile of specialist welding at **Deggendorf**
- Destination: **Karlsruhe**

*Photos from symmetry magazine*



Photos from symmetry magazine



- 10 metres wide, 200 tons
- Half a mile of specialist welding at **Deggendorf**
- Destination: **Karlsruhe**





- 10 metres wide, 200 tons
- Half a mile of specialist welding at **Deggendorf**
- Destination: **Karlsruhe**

Photos from symmetry magazine



## Getting picked up at the docks



10 metres wide, 200 tons

- Half a mile of specialist welding at **Deggendorf**
- Destination: **Karlsruhe**

Photos from symmetry magazine



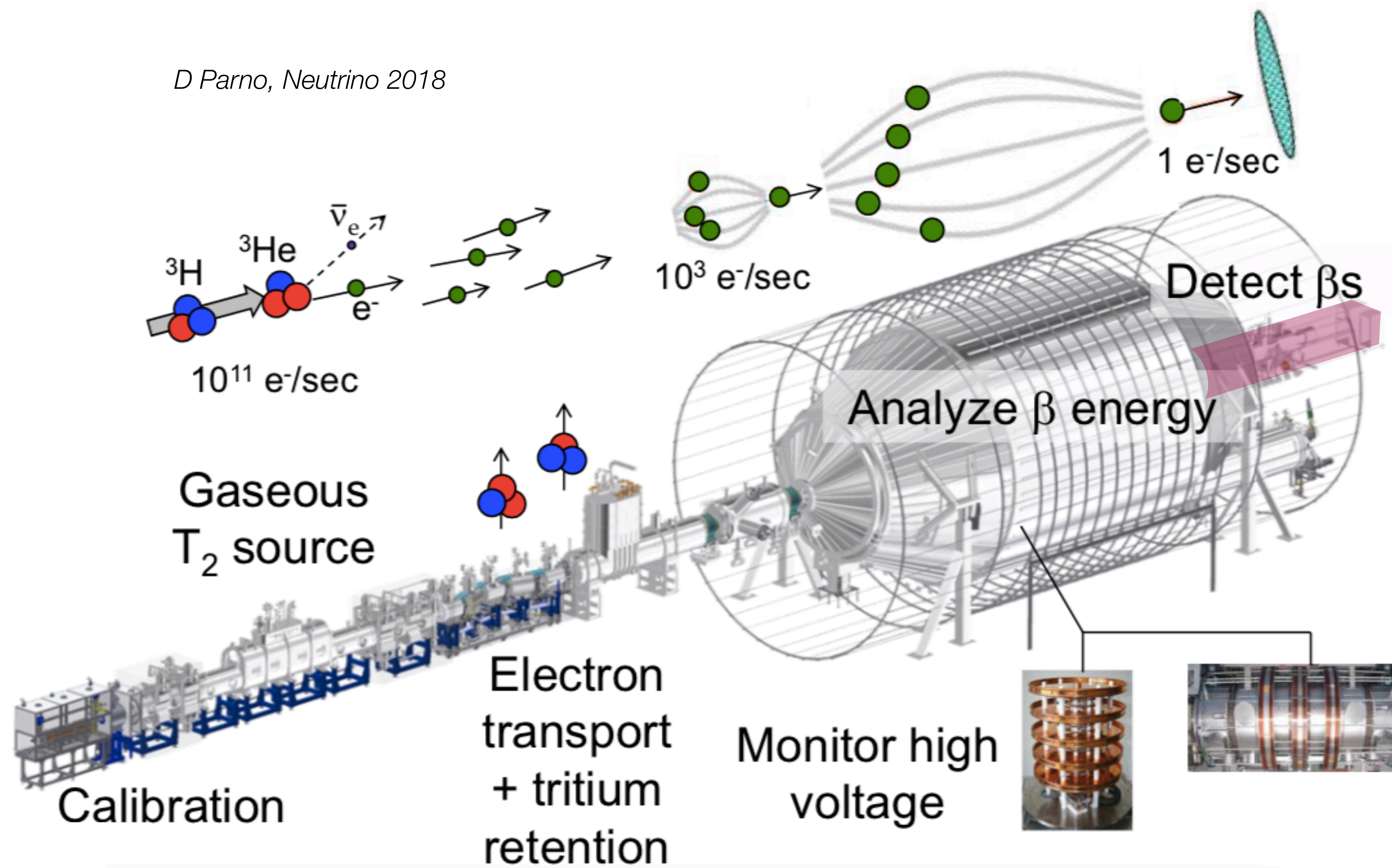
Leopoldshafen, are you ready?



- 10 metres wide, 200 tons
- Half a mile of specialist welding at **Deggendorf**
- Destination: **Karlsruhe**

Photos from symmetry magazine

*D Parno, Neutrino 2018*





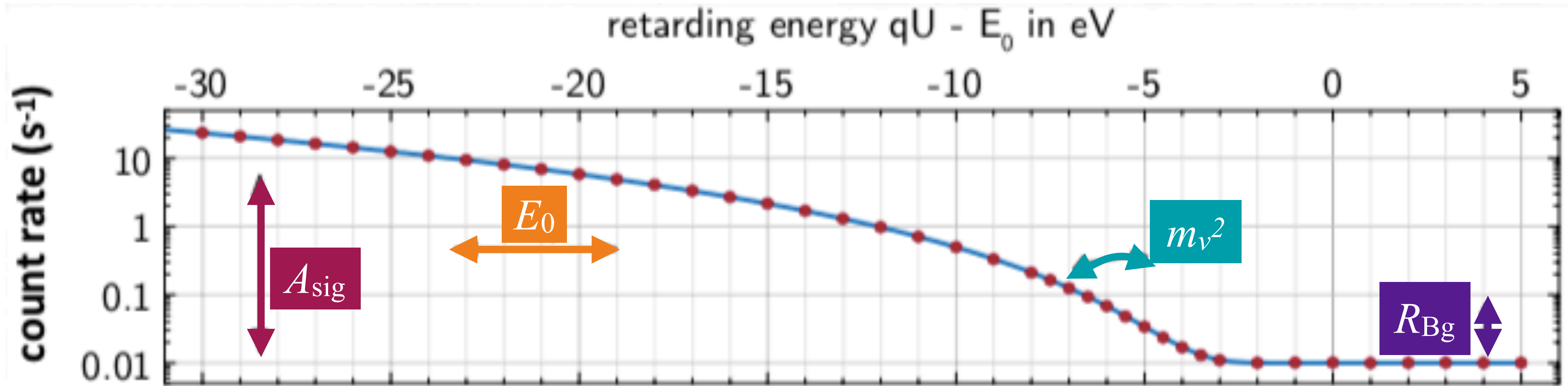
Multi-pixel **silicon** PIN diode array with high **energy resolution** and thin entrance window, in second of two superconducting **magnets**



**Radial position** is affected by the shape of the electrostatic potential - use this to calibrate

Use position data to map source **shape**

**Backgrounds** can also be position-dependent e.g. cosmics (but **energy** is key discriminator)



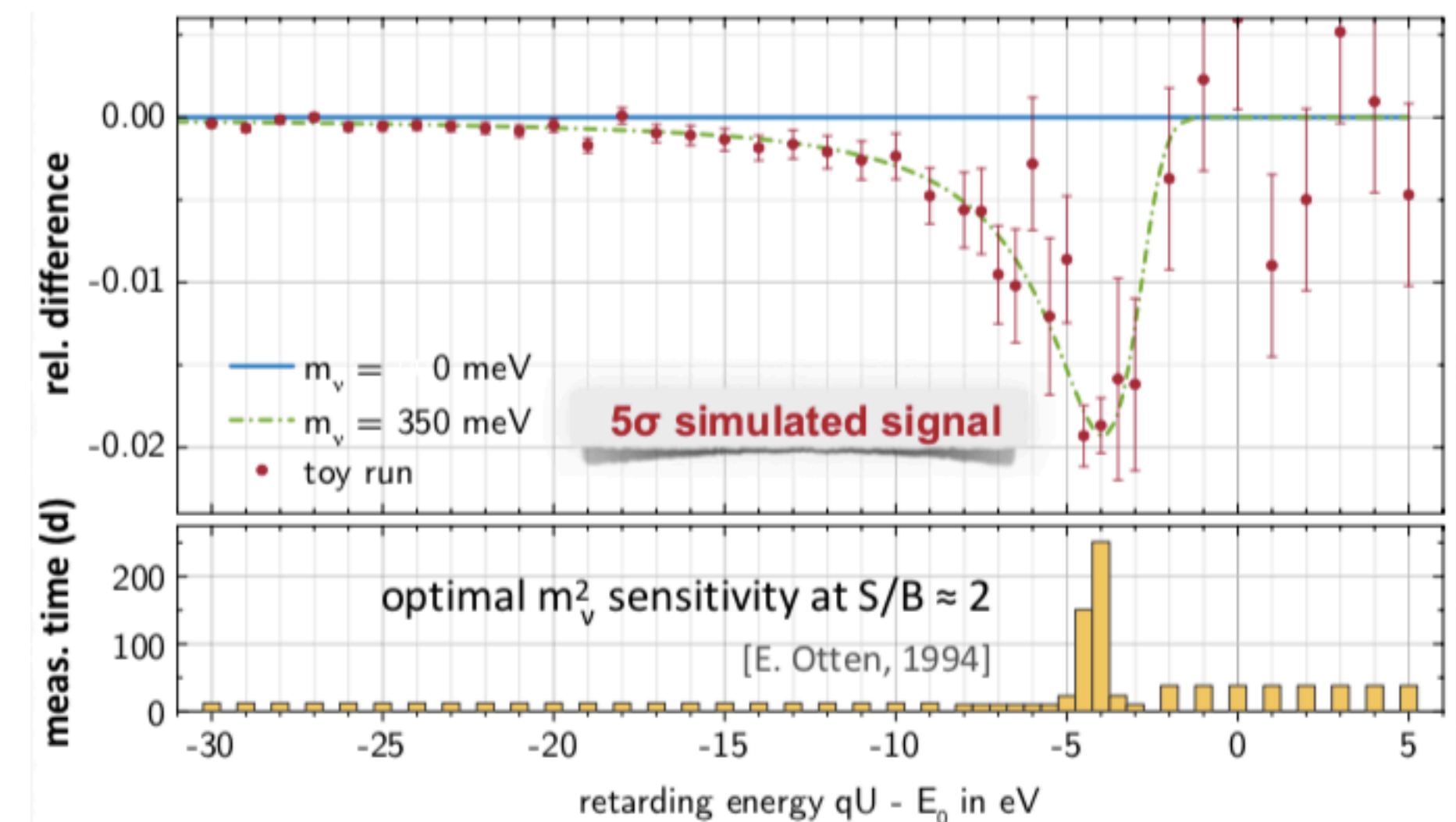
Simultaneous fit of **integrated** spectrum for 4 parameters:

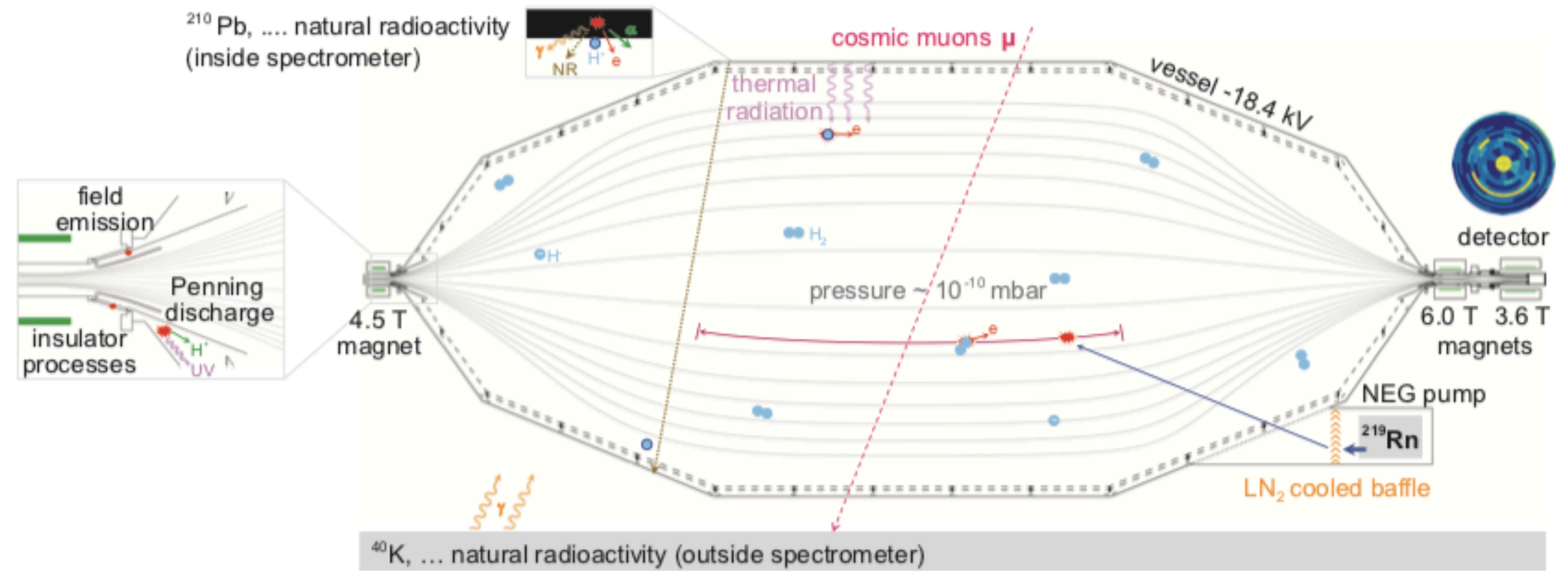
**Spectrum amplitude**  $A_{sig}$

**Endpoint energy**  $E_0$

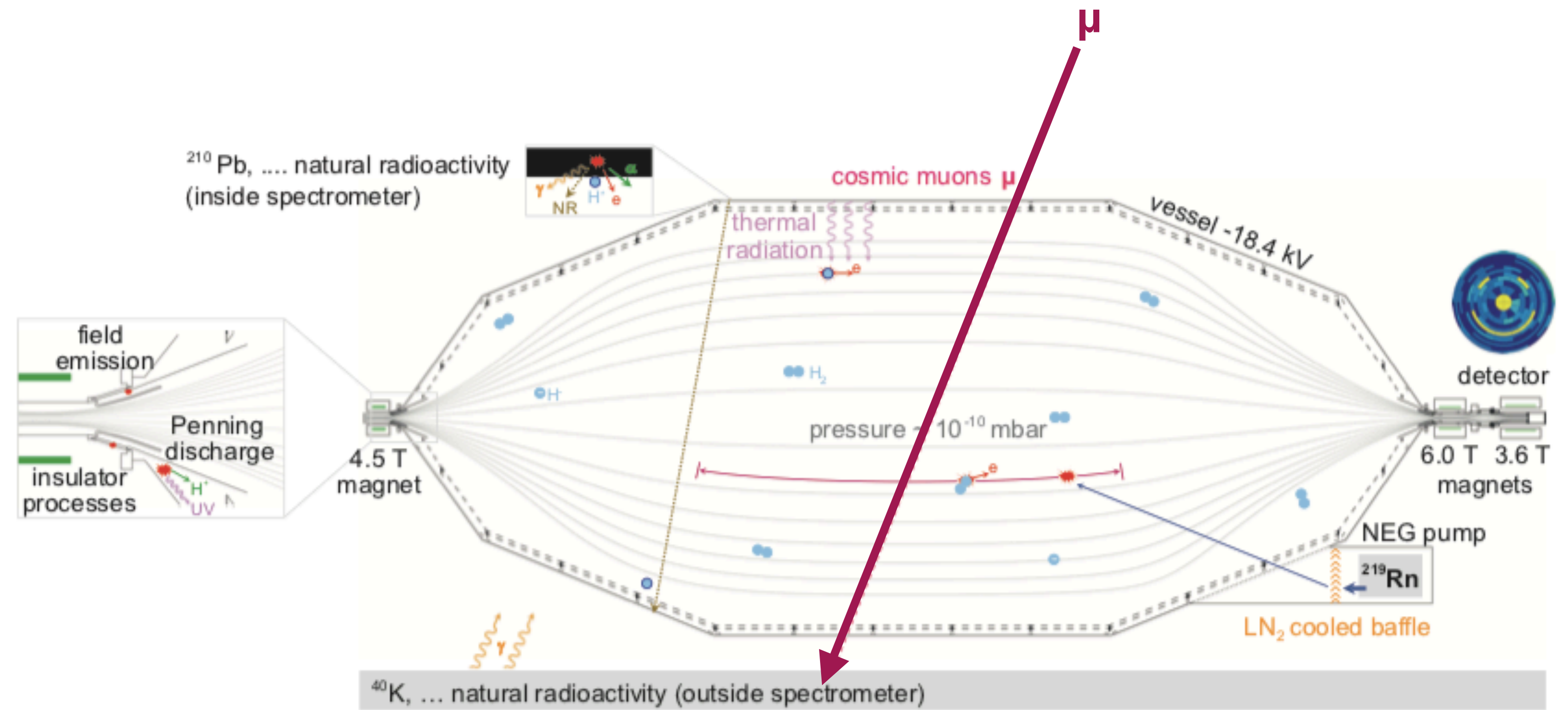
**Background rate**  $R_{Bg}$  should be independent of retarding potential

**Squared neutrino mass**  $m_{\nu}^2$  affects the shape





## Cosmic muons



Problem

Can produce secondary electrons

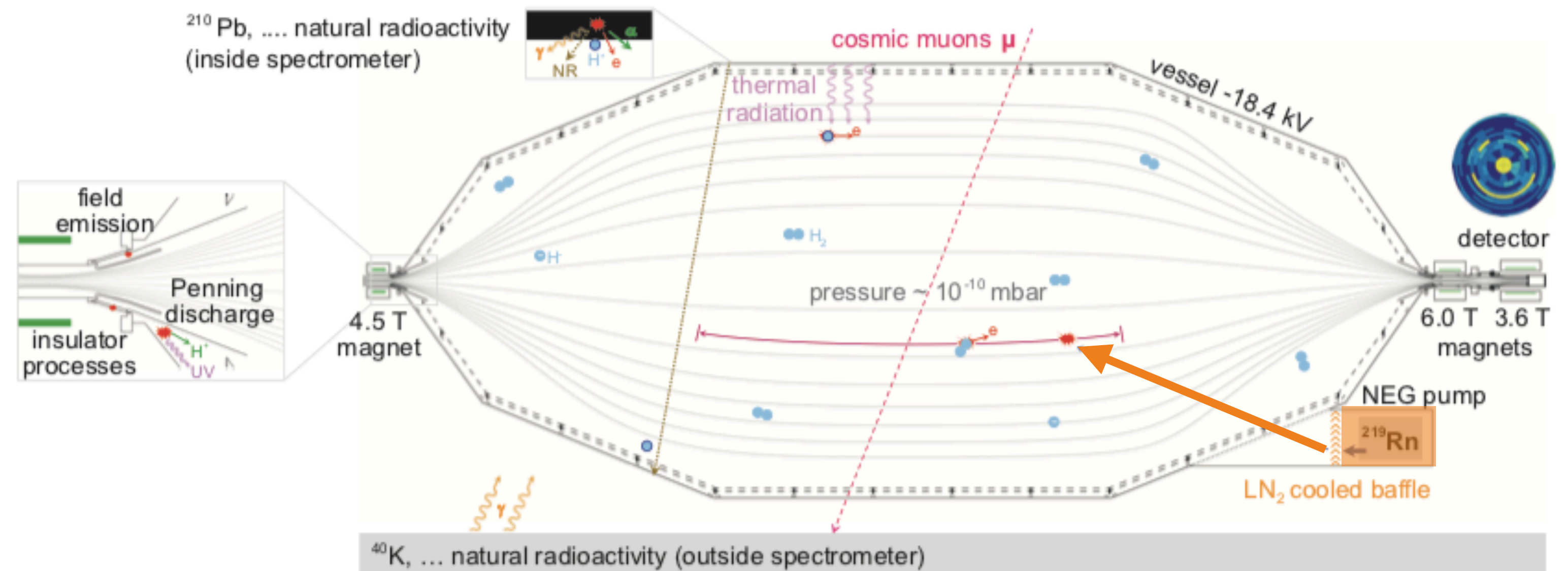
Fixed by

Magnetic shielding by electron-guiding field



## Cosmic muons

## Radon in components



Problem

Electrons from decay chain get trapped in spectrometer & generate secondaries

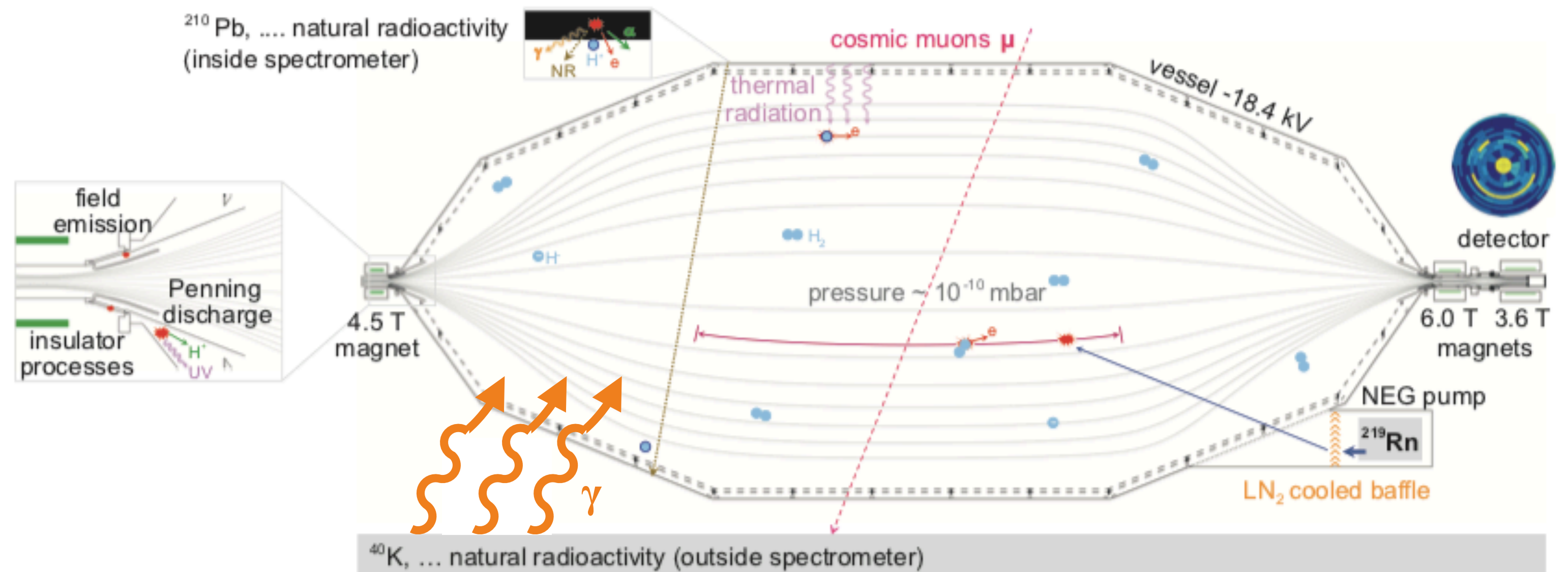
Fixed by

Baffle to clean radon from main source ("NEG" pump)

## Cosmic muons

## Radon in components

## External radioactivity



Problem

Gammas from  $^{40}\text{K}$  outside spectrometer

Fixed by

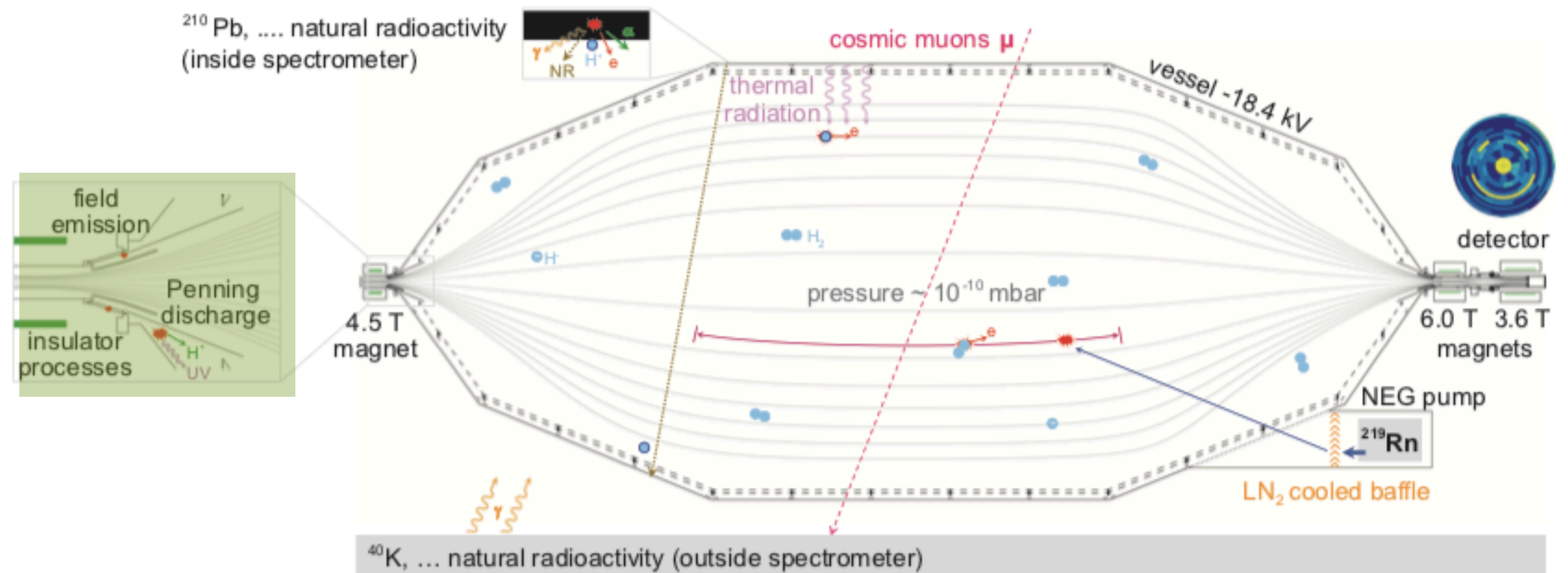
Spectrometer shielding

## Cosmic muons

## Radon in components

## External radioactivity

## Penning discharge



Problem

Ionization at entrance to spectrometer where fields are strong

Fixed by

Careful electrode design

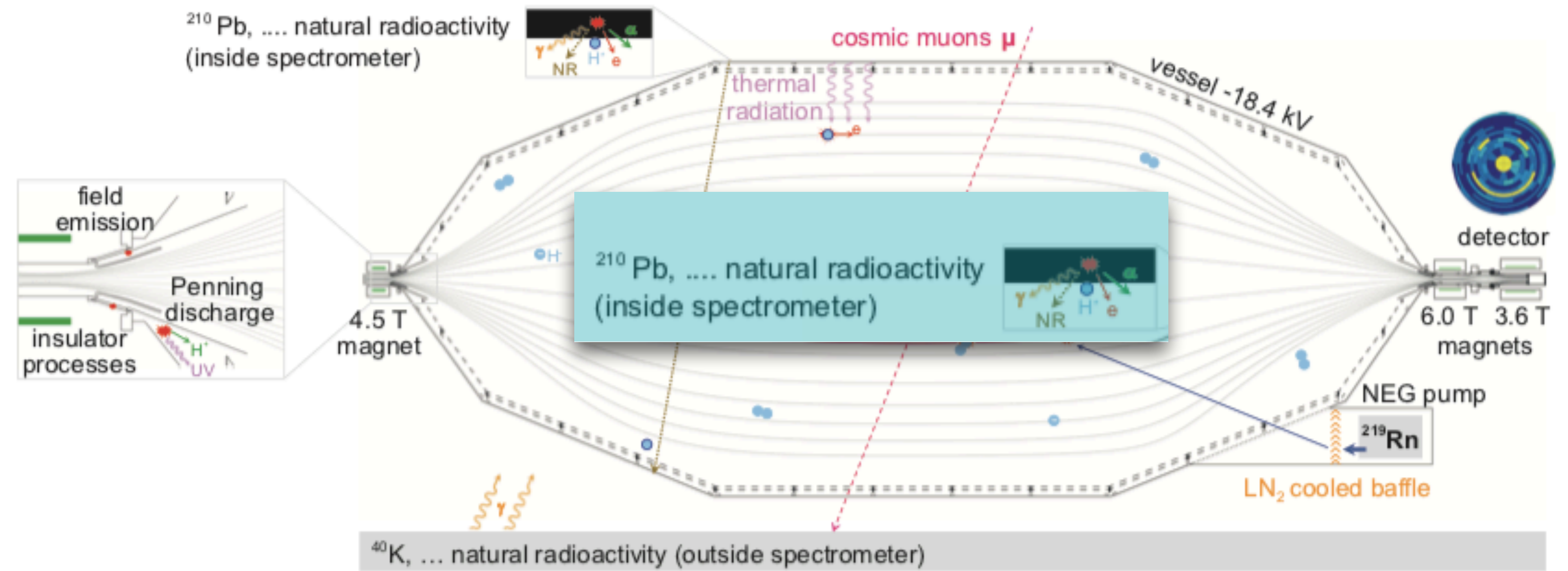
## Cosmic muons

## Radon in components

## External radioactivity

## Penning discharge

## Internal $^{210}\text{Pb}$ decays



### Problem

Decay products include Rydberg atoms, which are ionised by thermal radiation

### Fixed by

Biggest background - not affected by shielding

## Cosmic muons

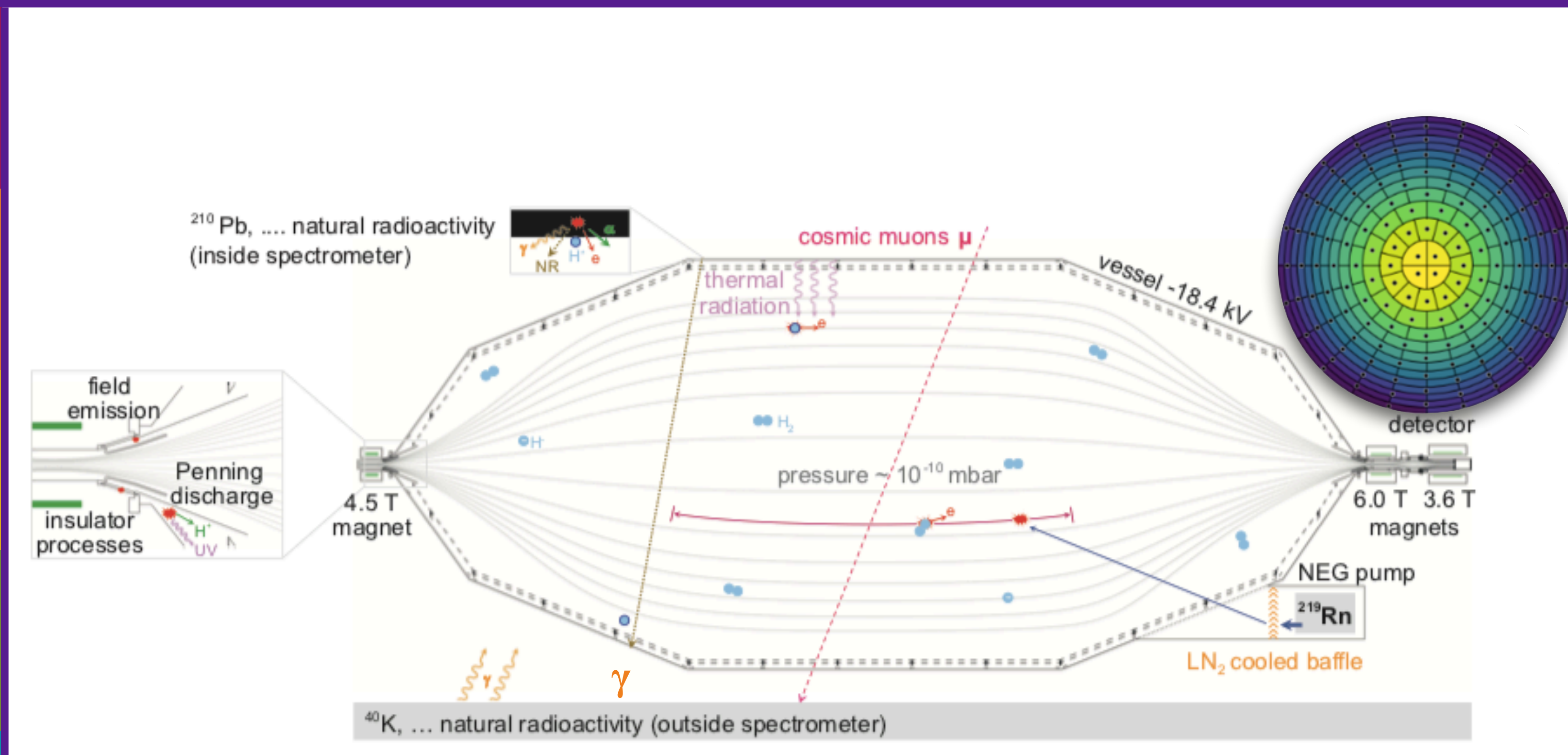
## Radon in components

## External radioactivity

## Penning discharge

## Internal $^{210}\text{Pb}$ decays

## Detector backgrounds

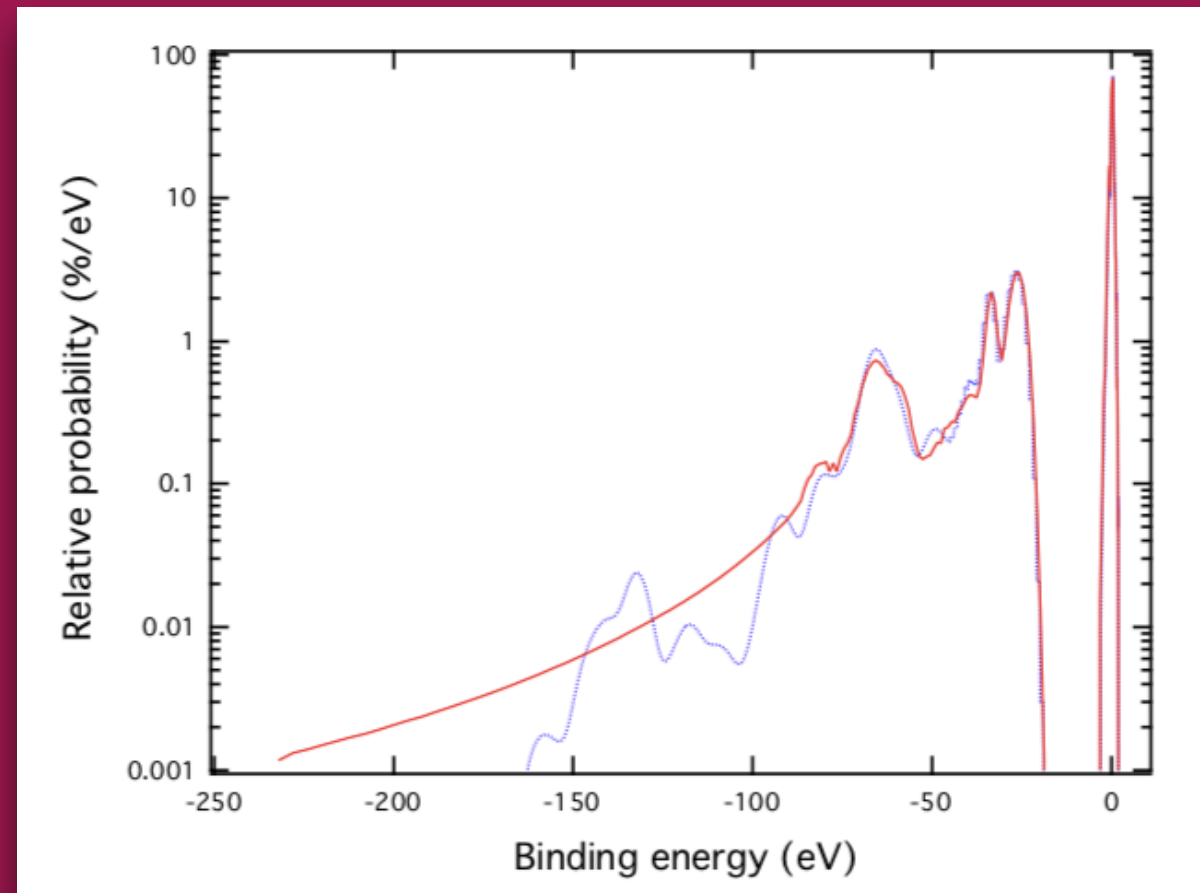


Problem

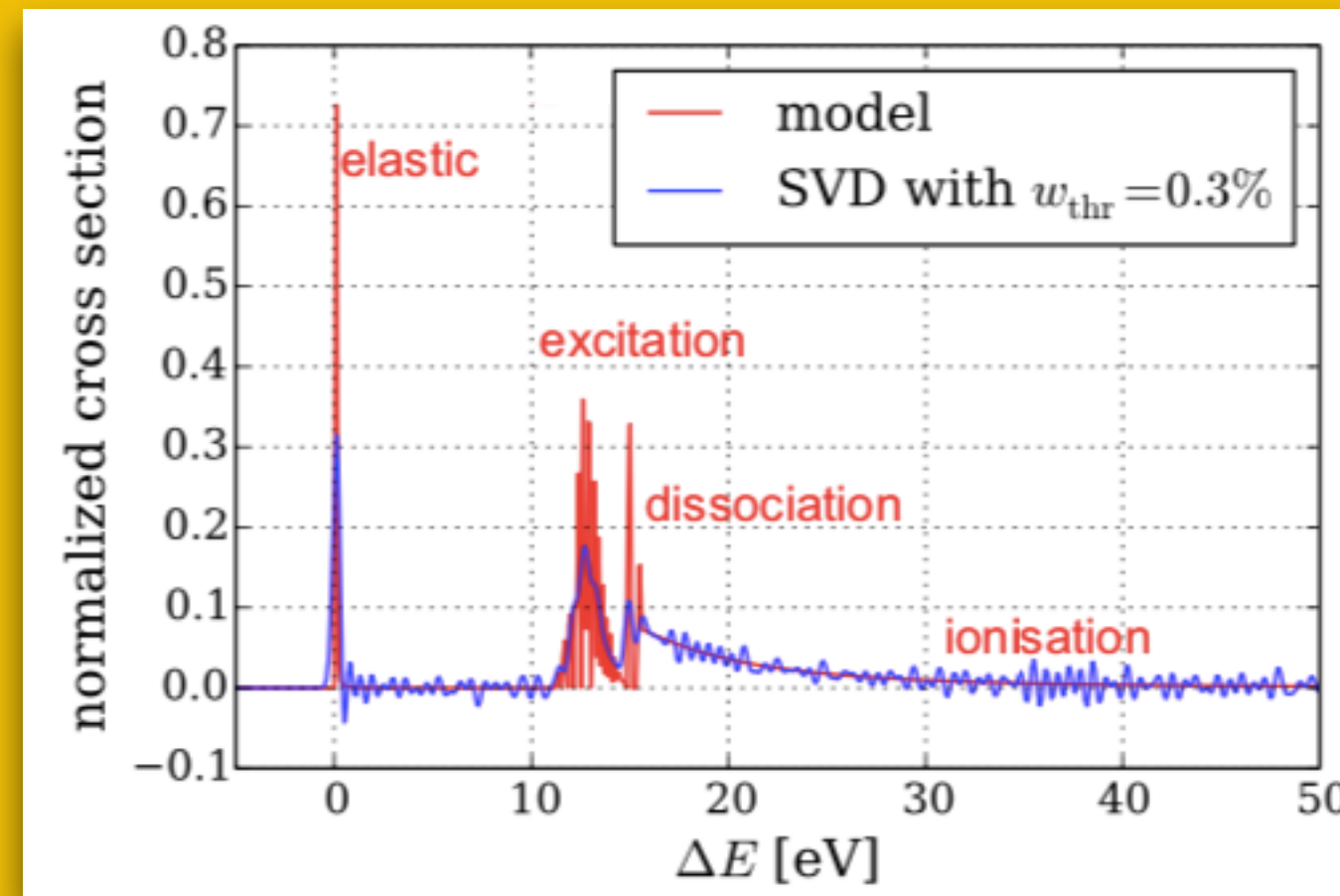
Electrons from sources other than the spectrometer

Fixed by

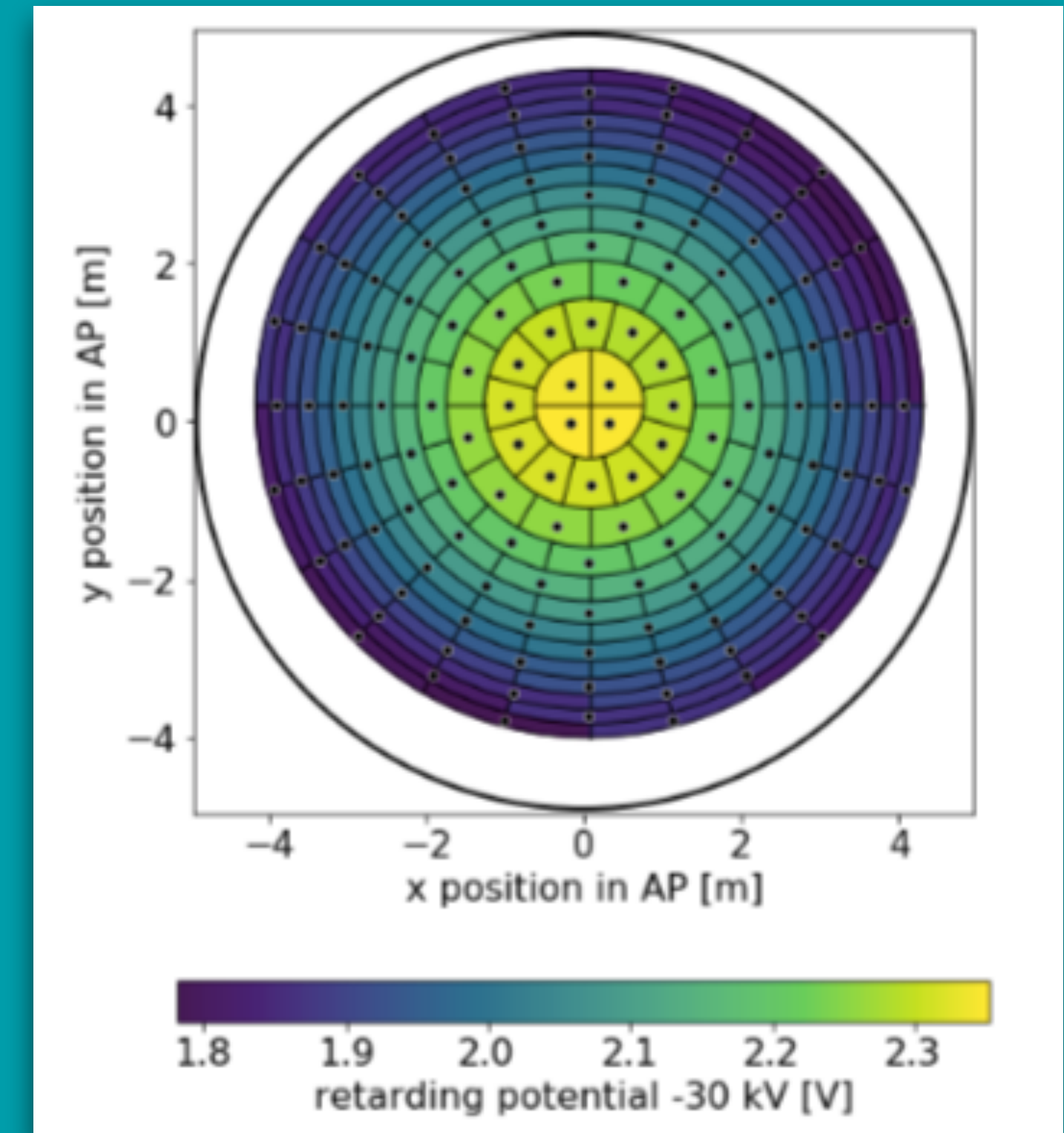
Lead and copper shielding; scintillator veto for cosmics



$\beta$  decay model and final state ion distributions

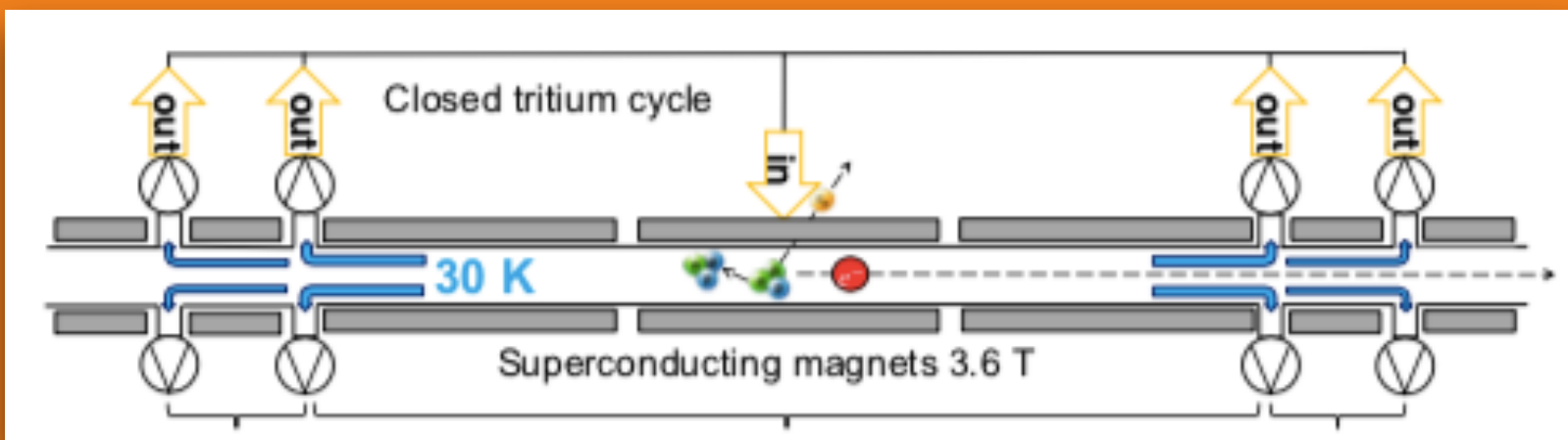


$\beta$ -electron scattering and energy loss

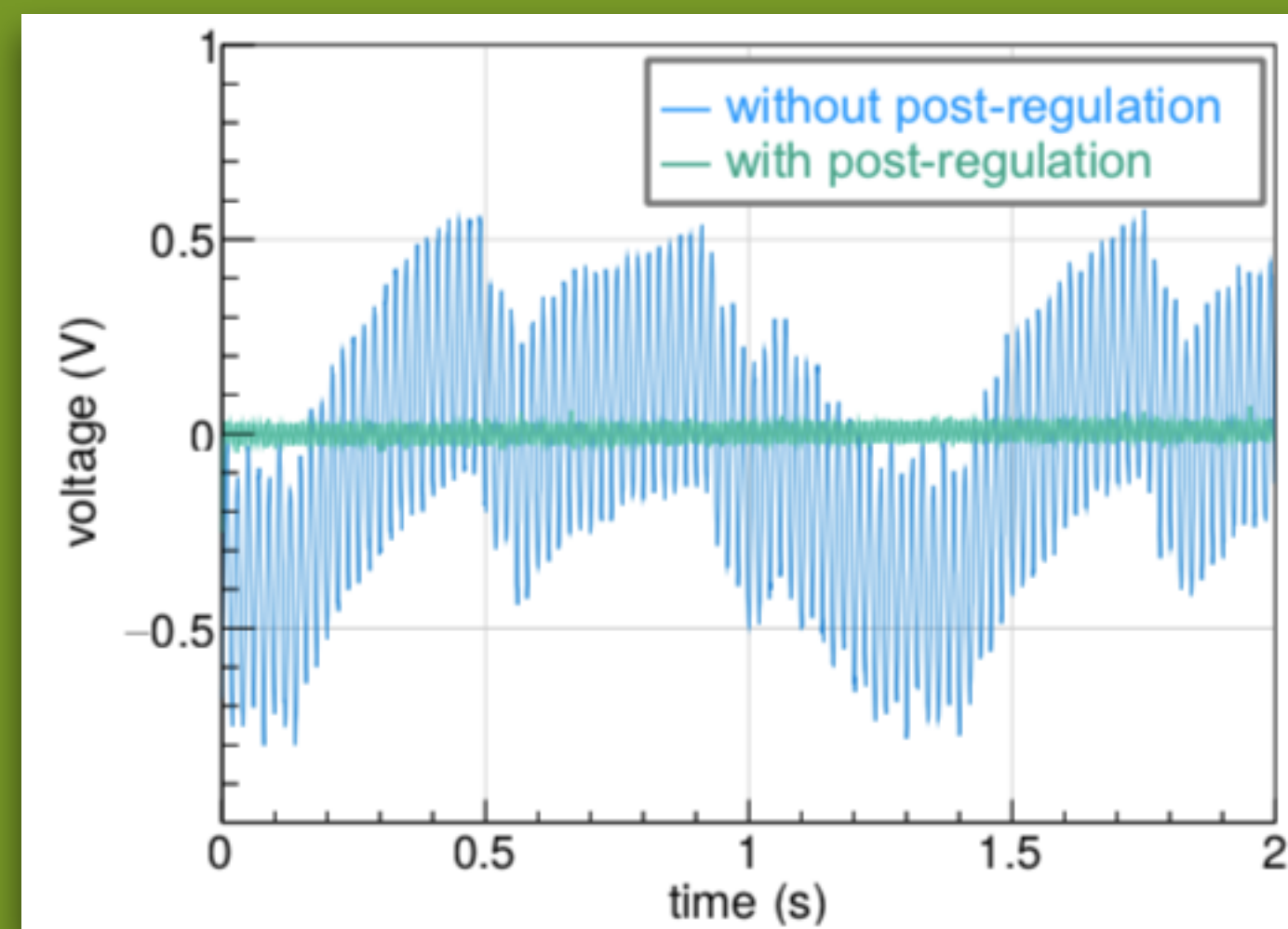


Field homogeneity in the analyzing plane

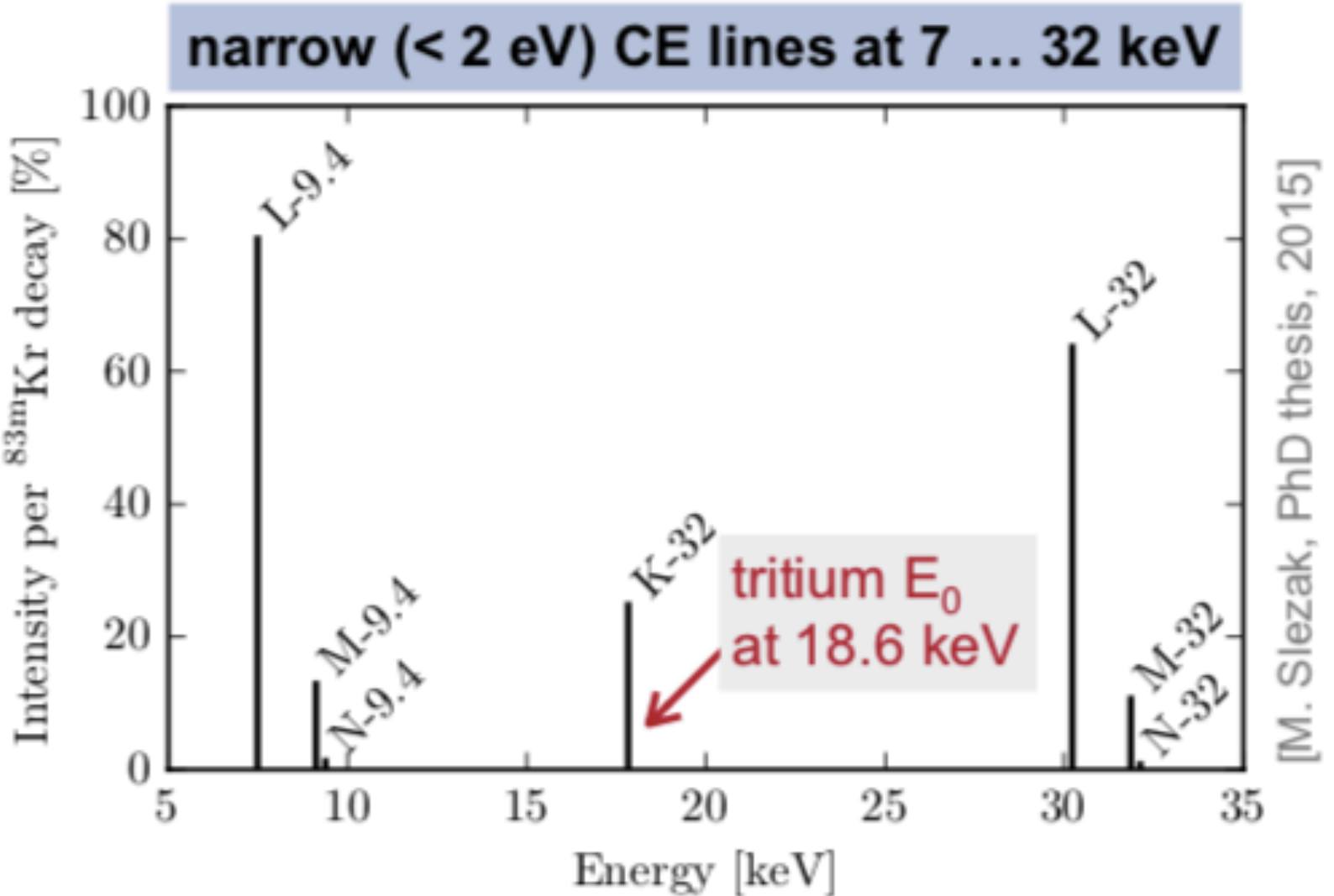
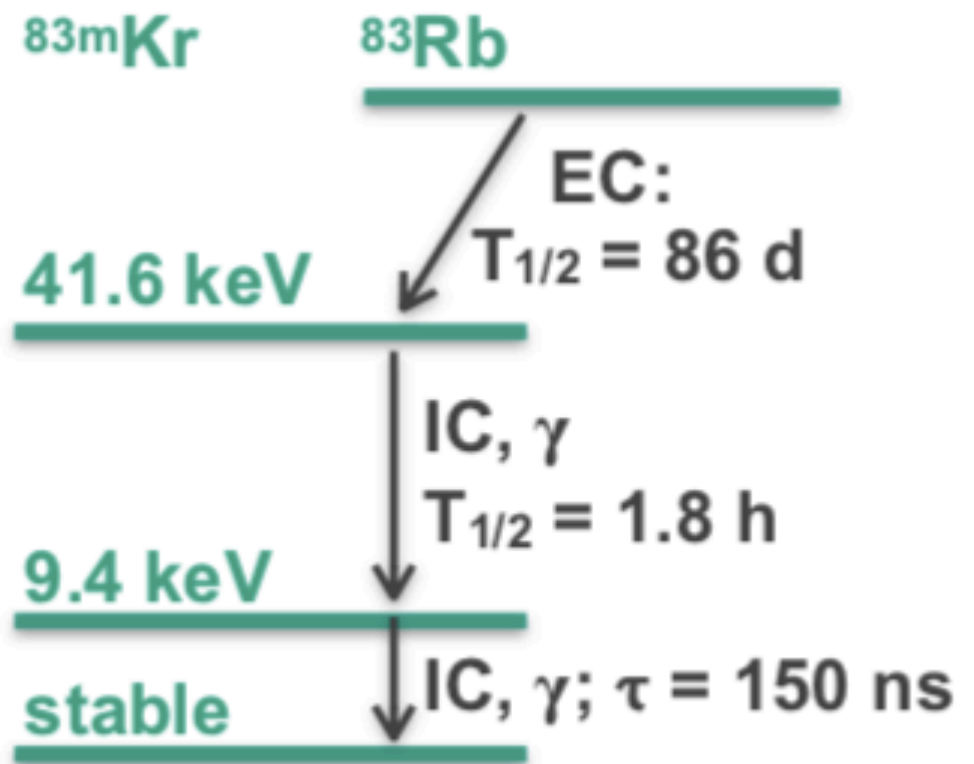
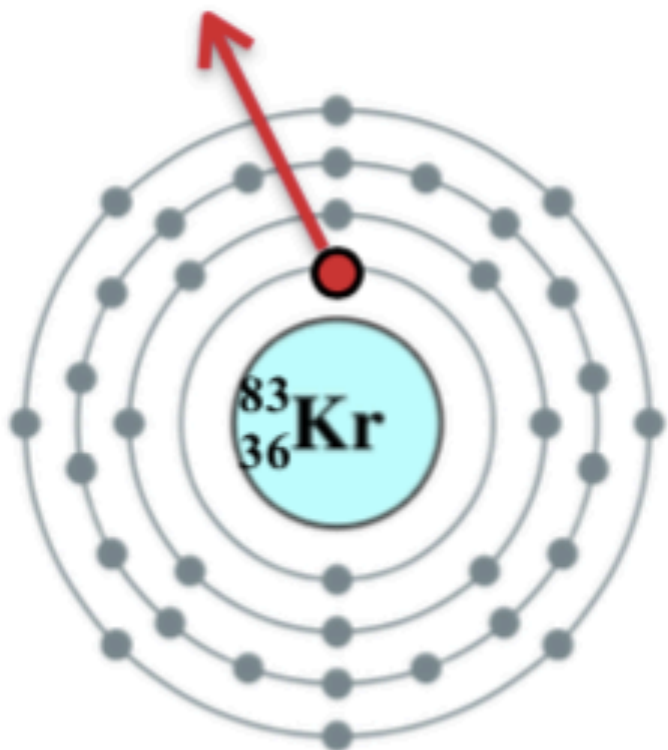
Systematic uncertainties > statistical uncertainties after 3 beam years (5 calendar years)

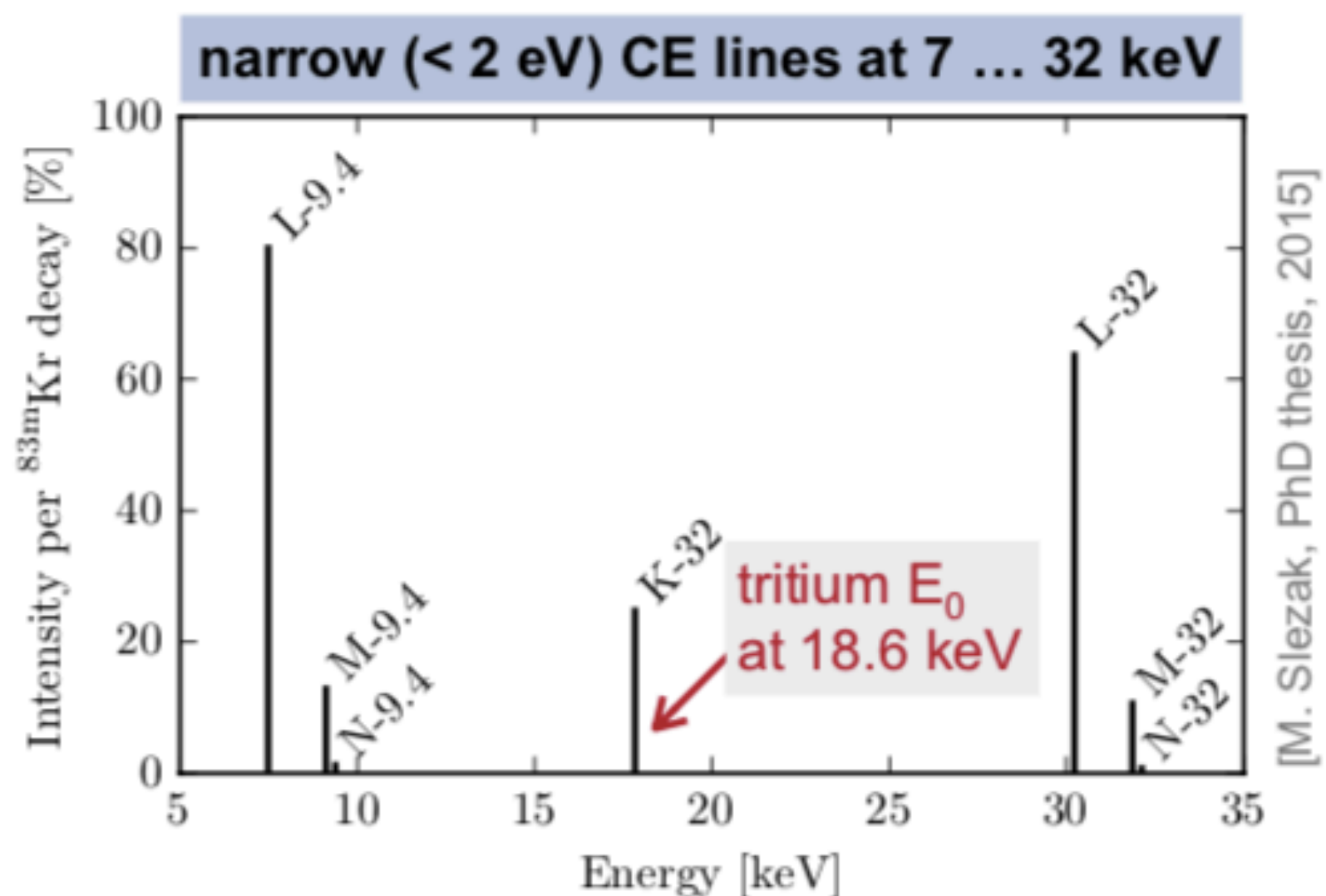
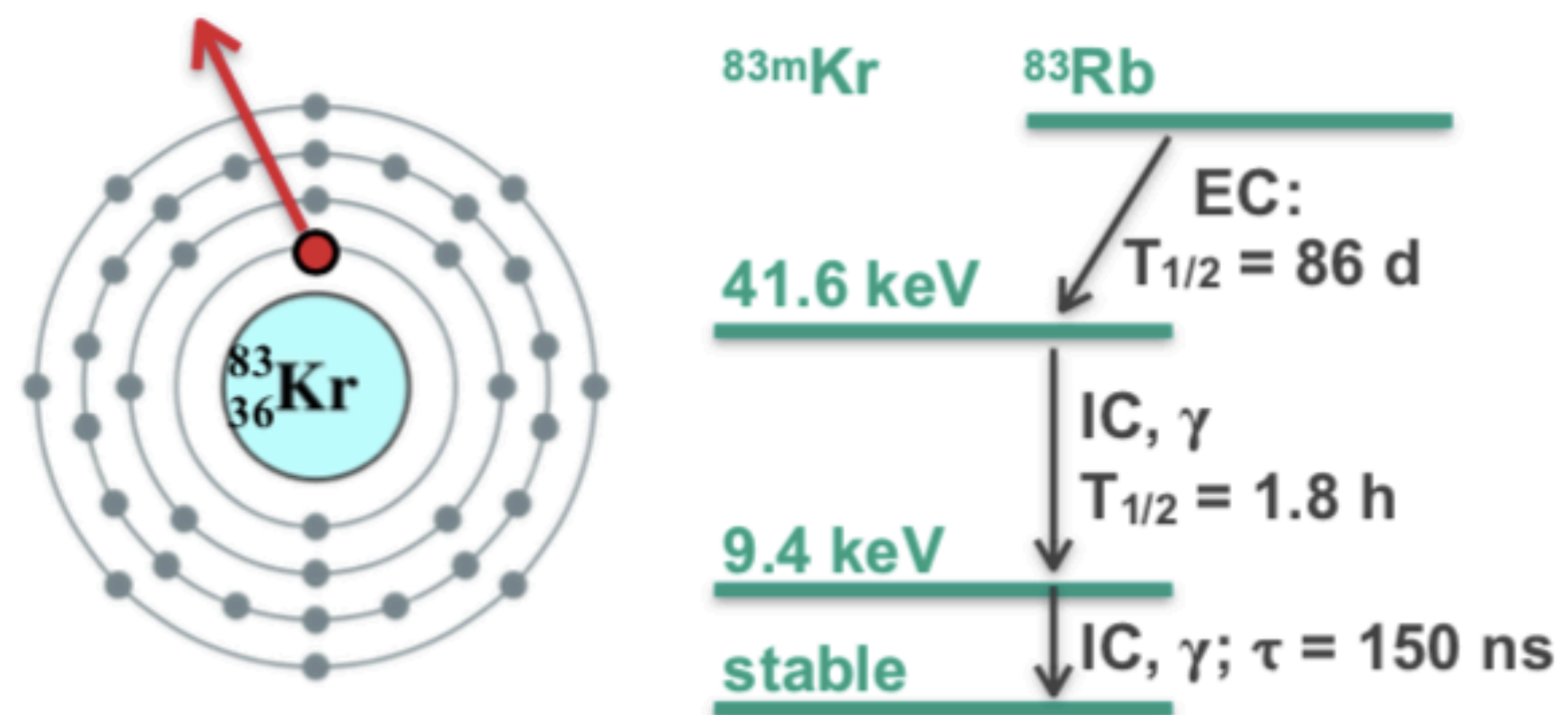


Source gas dynamics



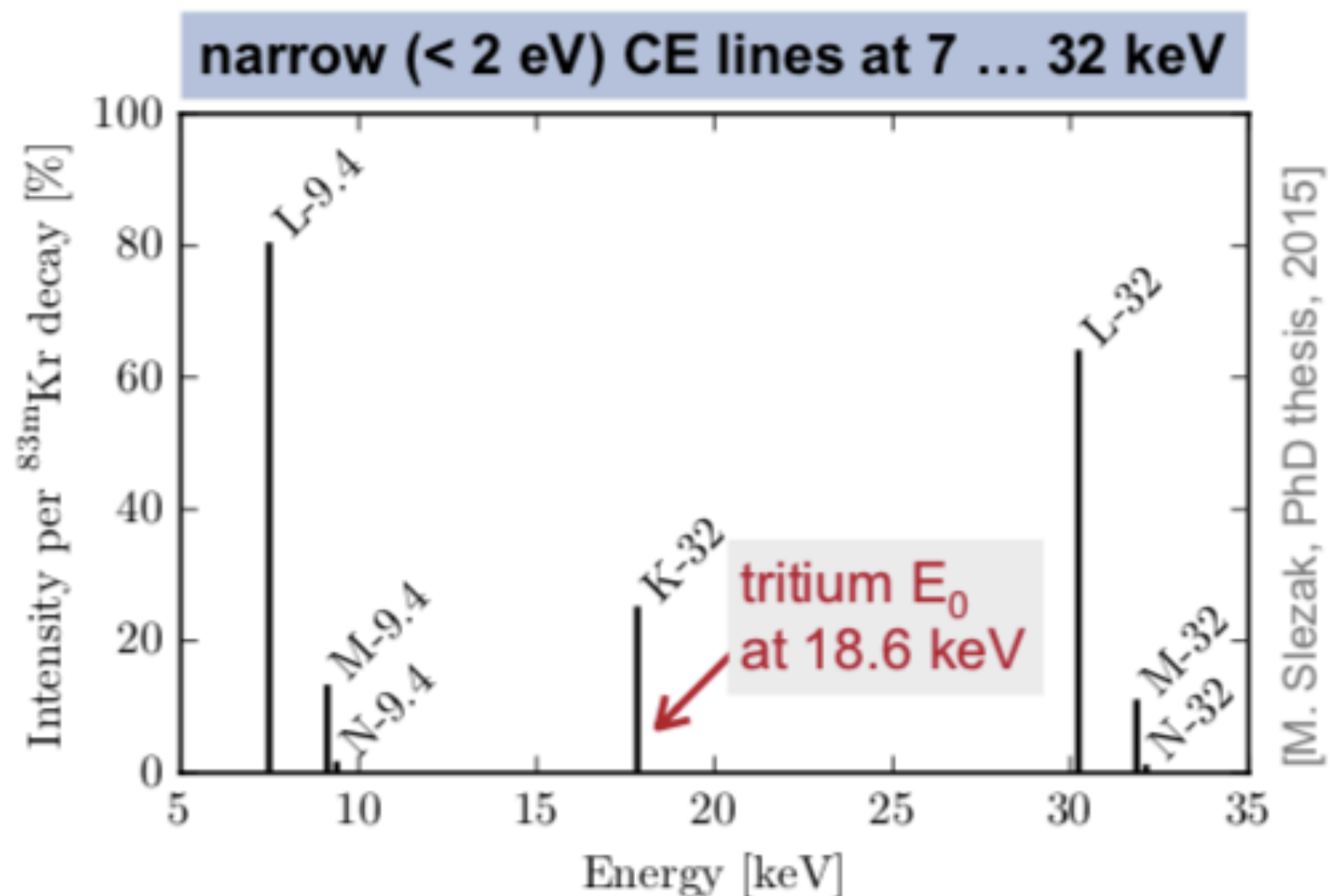
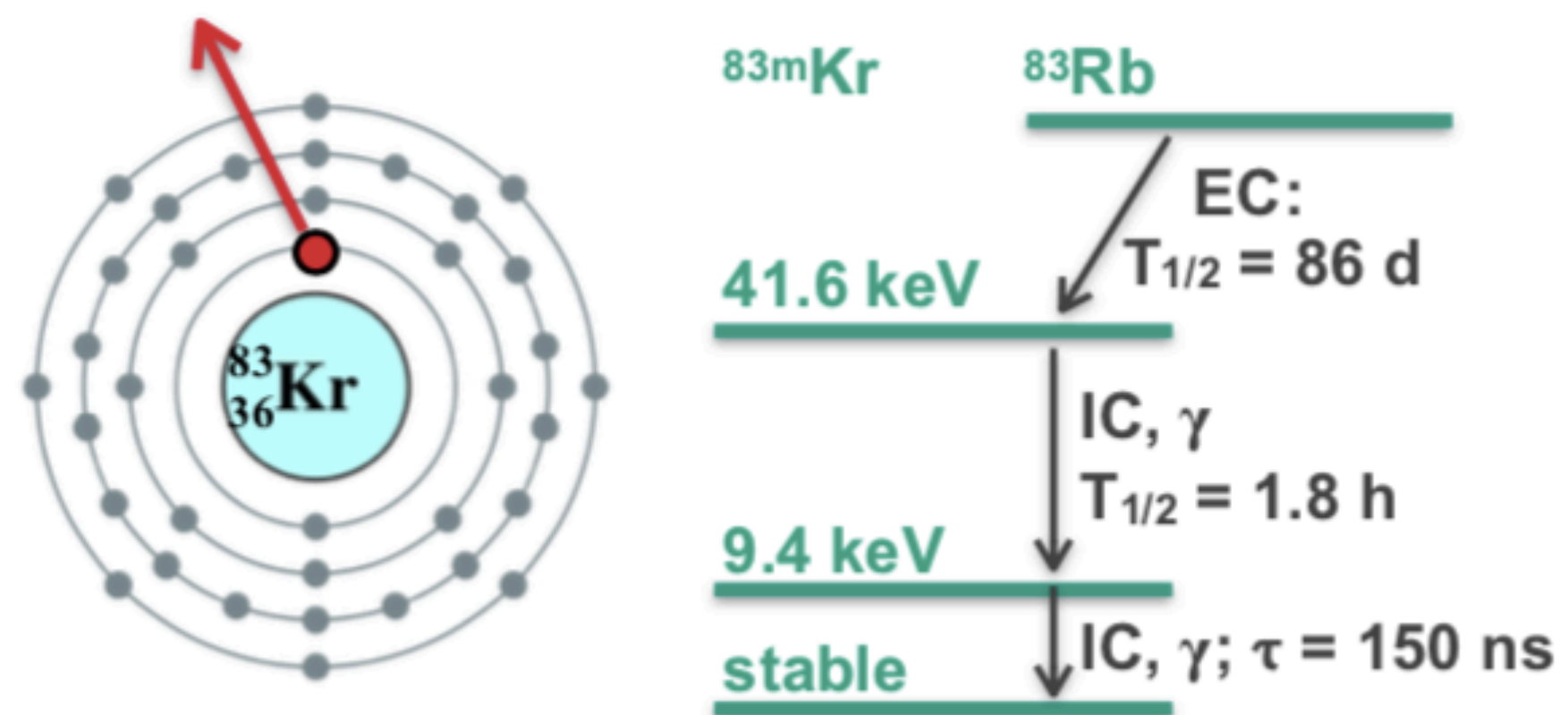
High voltage stability and calibration



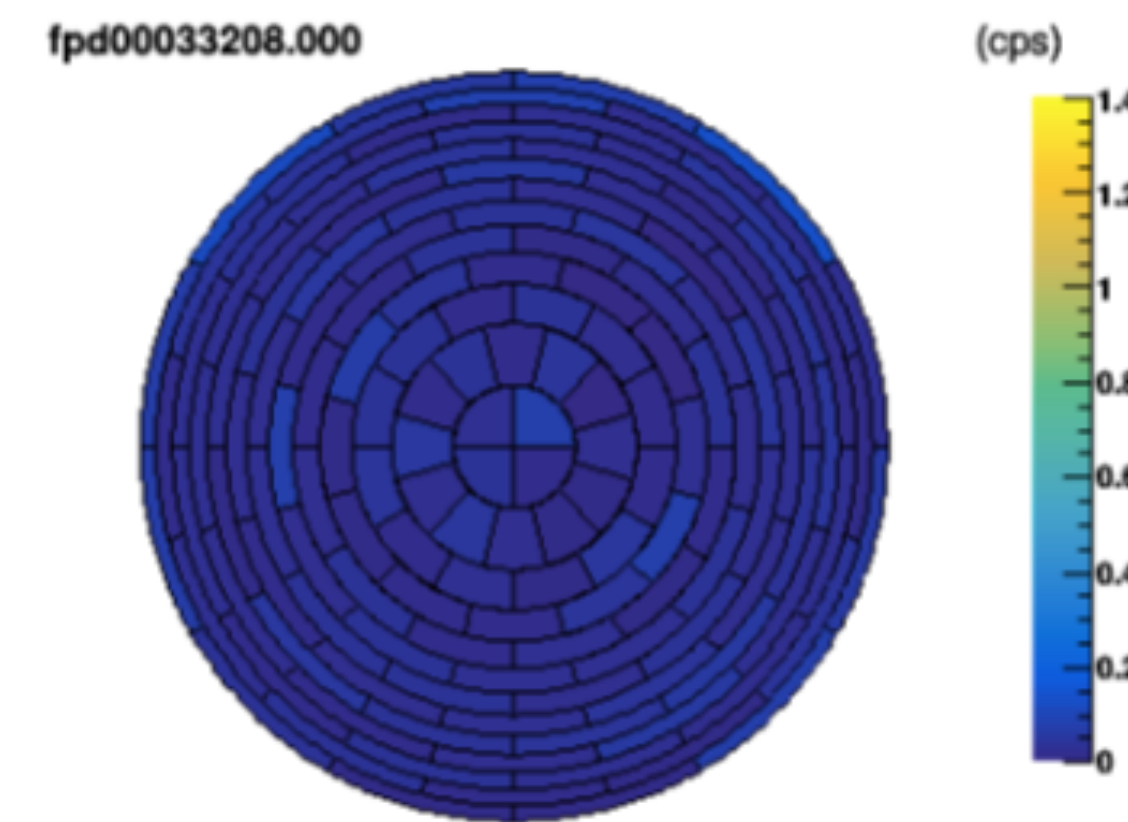
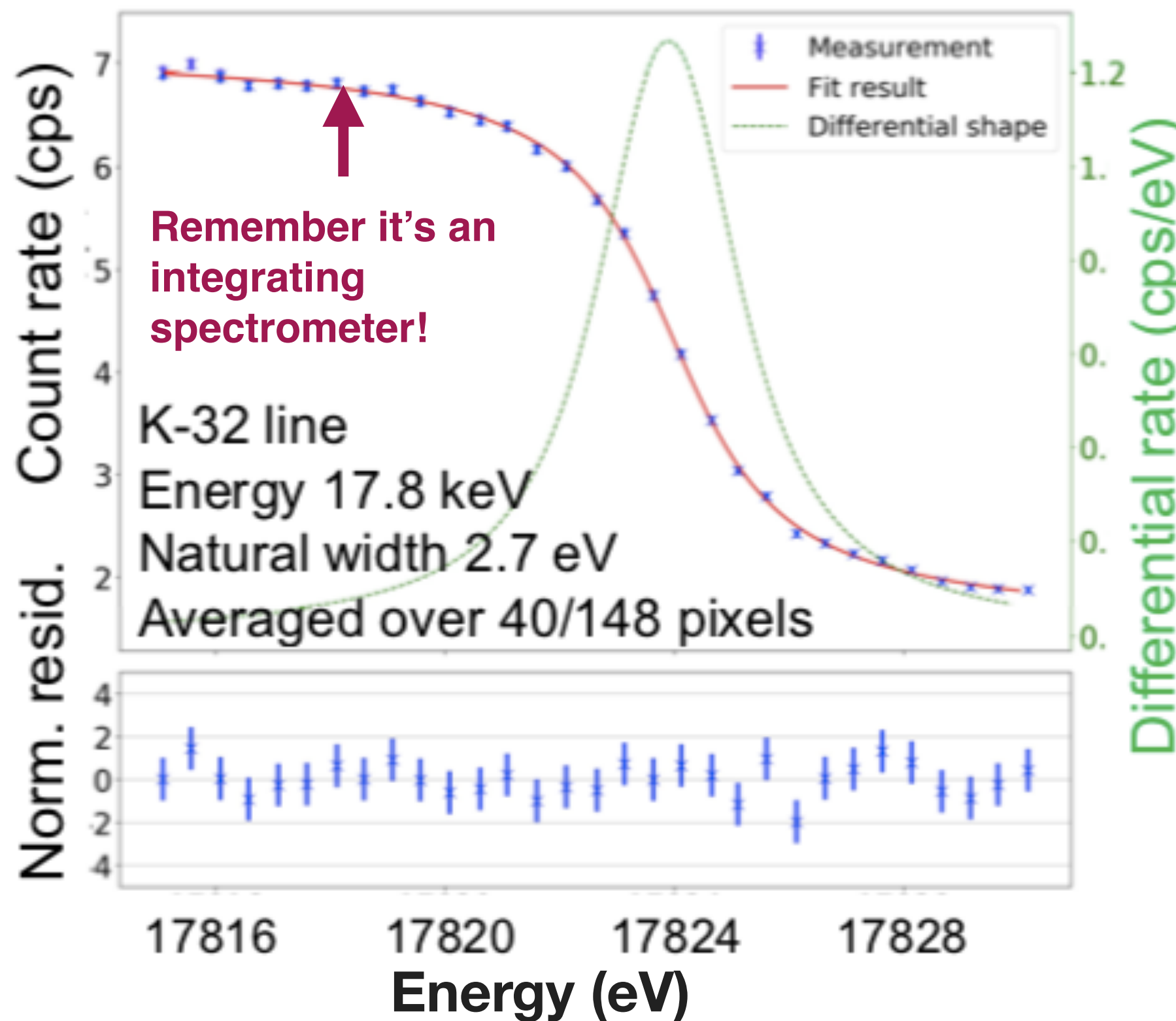


- Energy scans
- Hardware testing/commissioning
- Test of data acquisition/analysis pipeline
- System characterization (e.g. confirm sub-eV resolution)
- Calibration





- **Energy scans**
- **Hardware** testing/commissioning
- Test of **data acquisition/analysis** pipeline
- System **characterization** (e.g. confirm sub-eV resolution)
- Calibration

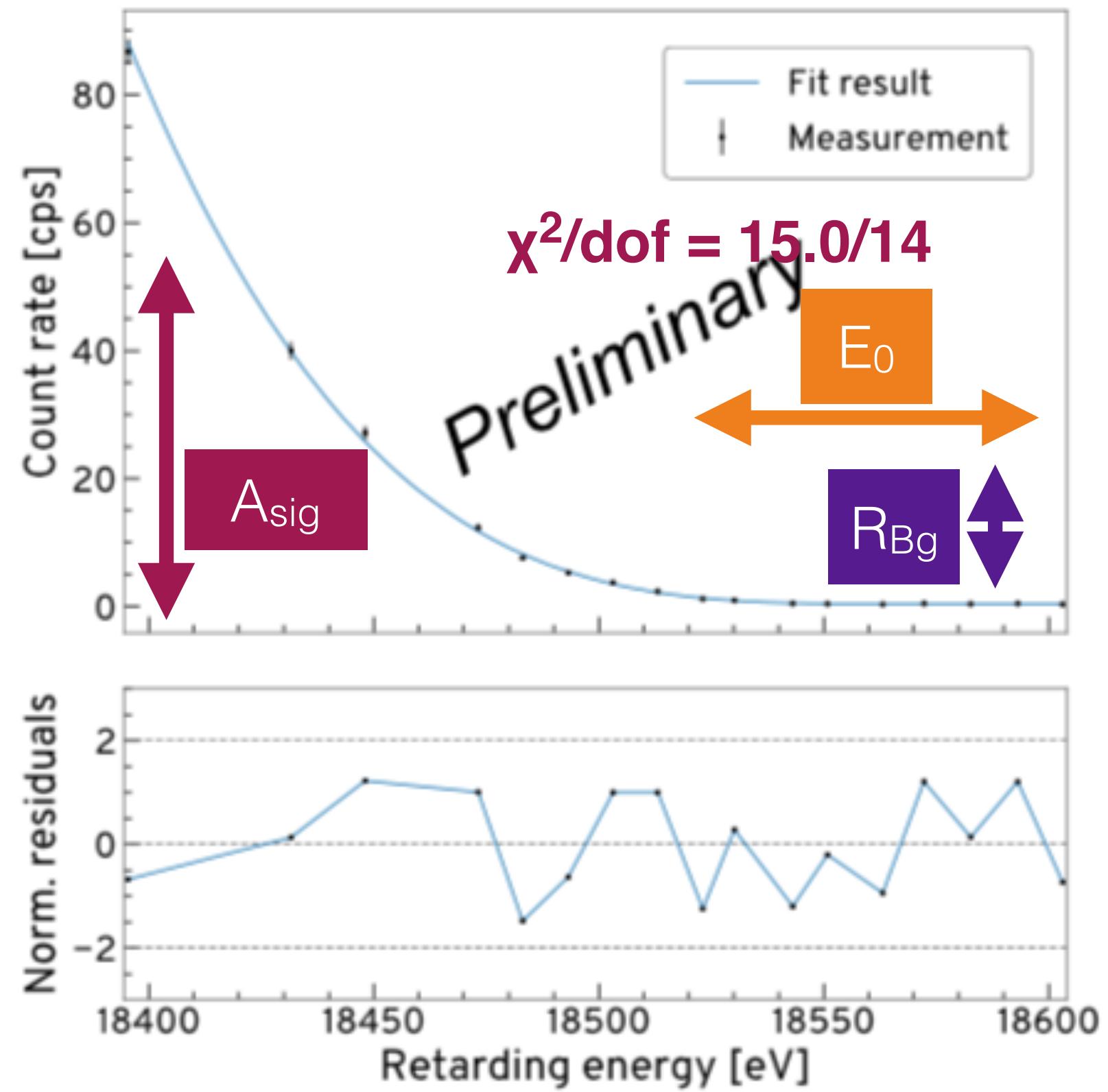


Real data from KATRIN!

EPJ C 78 368 (2018)  
JINST 13 P04020 (2018)

Test with D<sub>2</sub> at 90% nominal density, with 0.5% T atoms

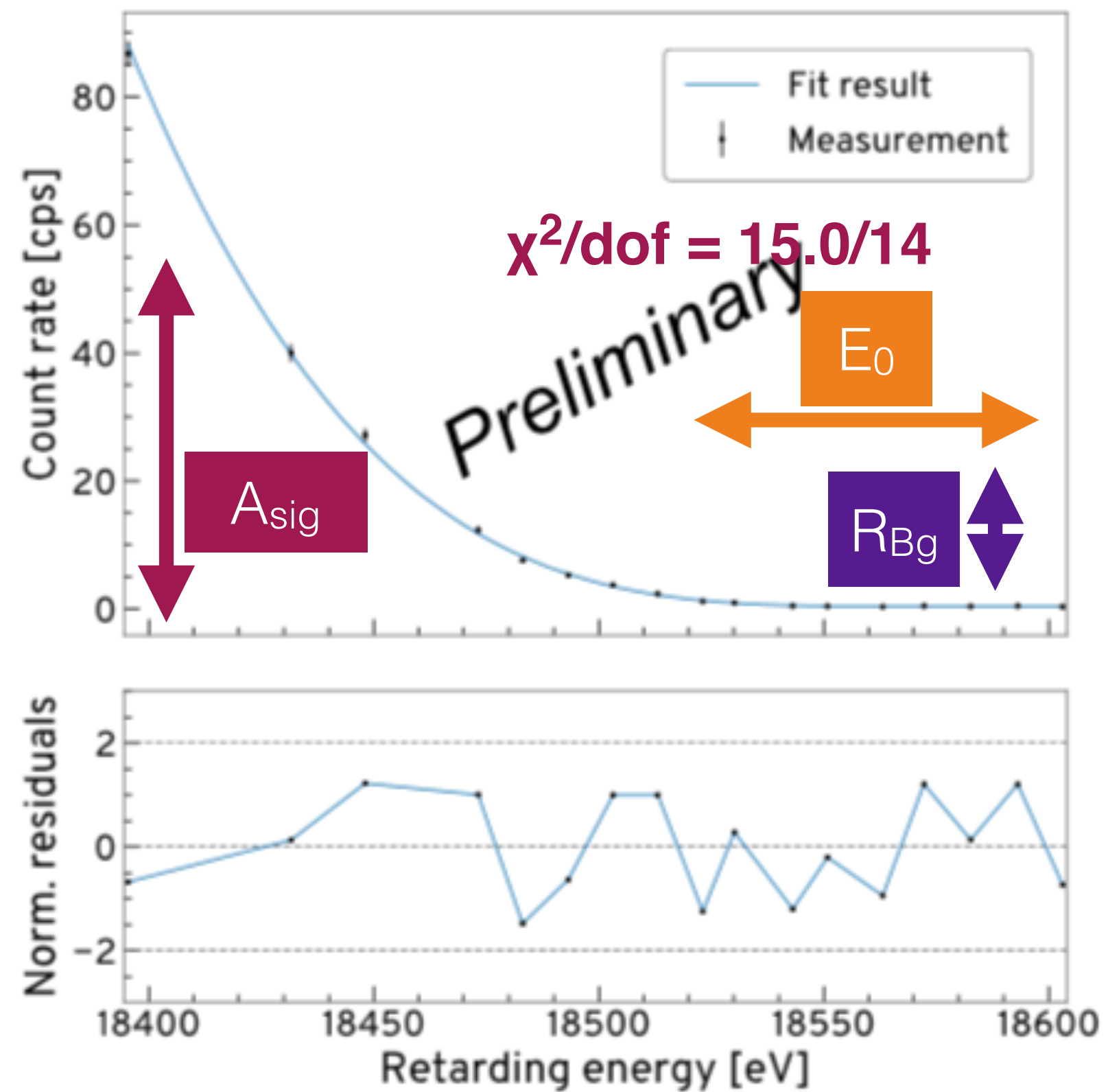
## First measurement of tritium spectrum



Fitted for  
**Activity  $A_{\text{sig}}$**       **Endpoint energy  $E_0$**   
**Background rate  $R_{\text{Bg}}$**

Test with D<sub>2</sub> at 90% nominal density, with 0.5% T atoms

## First measurement of tritium spectrum



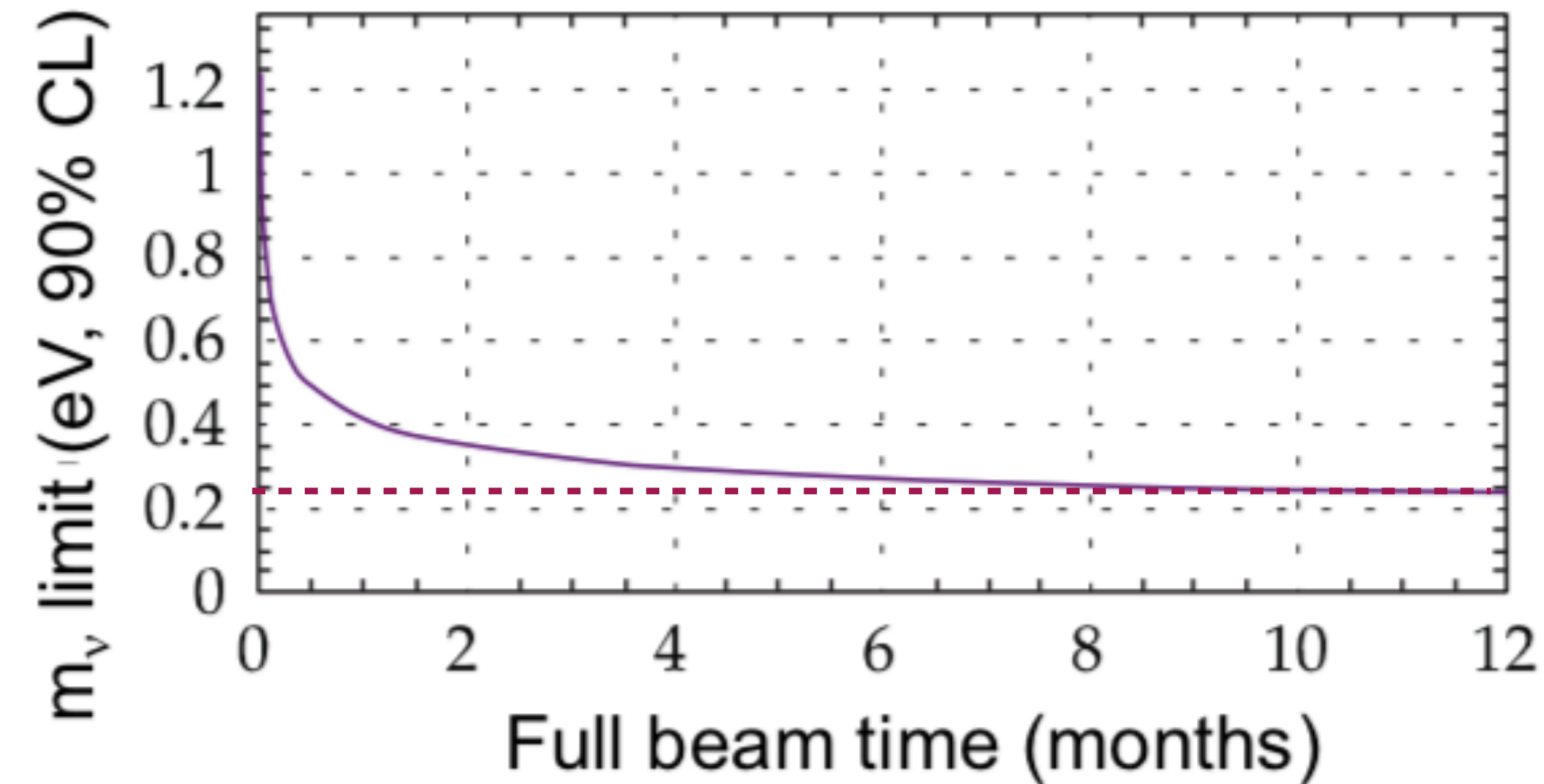
Fitted for  
**Activity  $A_{sig}$**       **Endpoint energy  $E_0$**   
**Background rate  $R_{Bg}$**

## KATRIN Timeline

<b>June 5th–18th, 2018</b>	First Tritium run: 81 hours of data
<b>March-May 2019</b>	“KNM1” with higher tritium concentration. First data usable for neutrino mass measurement
<b>2020</b>	Plan to start 3-year run at nominal settings
<b>2025</b>	Analysis becomes systematics limited. Should reach design sensitivity 0.2eV.

arXiv:1906.10168

**Sensitivity** - if KATRIN measures zero mass

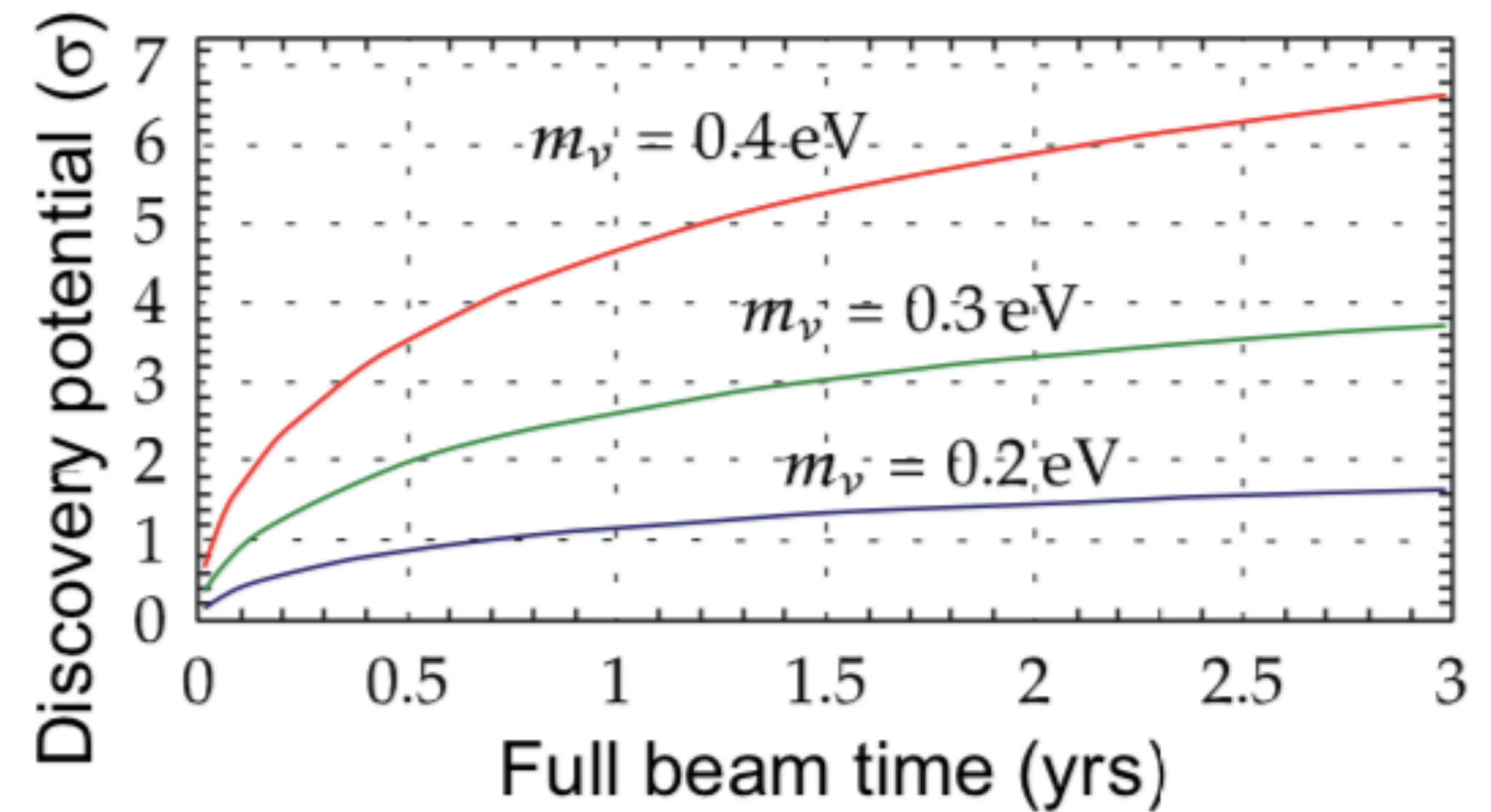


$m_\nu < 0.24$  eV at 90% confidence

Jargon: **sensitivity**

The upper limit on the measured value (neutrino mass) if the mass is measured to be zero. Typically quoted with 90% confidence.

**Discovery potential** - if KATRIN measures a non-zero mass



$m_\nu = 0.35$  eV at 5 $\sigma$  significance

$m_\nu = 0.3$  eV at 3 $\sigma$  significance

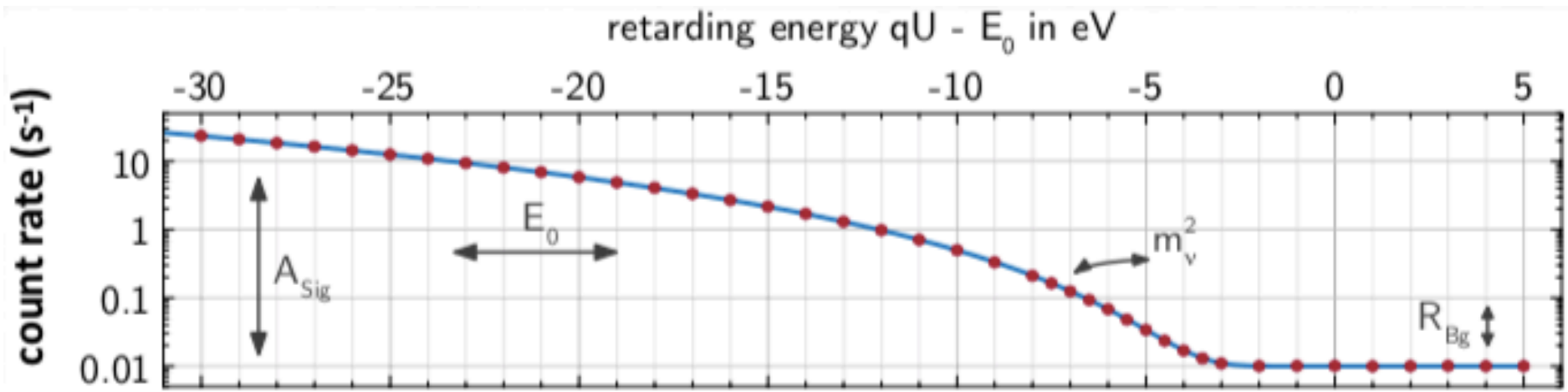


**Systematic uncertainties > statistical uncertainties after 3 years (5 calendar years)**

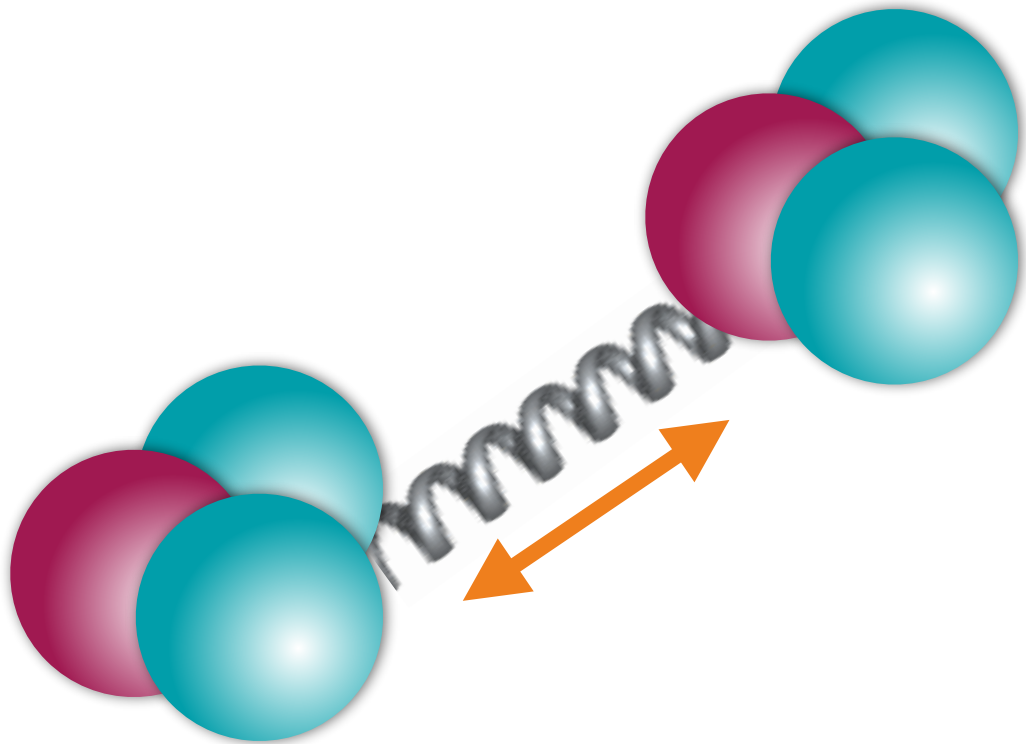
# Challenges for future MAC-E experiments



Spectrometer already as big as is practical - can't improve resolution



Integrated  $\beta$  spectrum means throwing away spectrum information

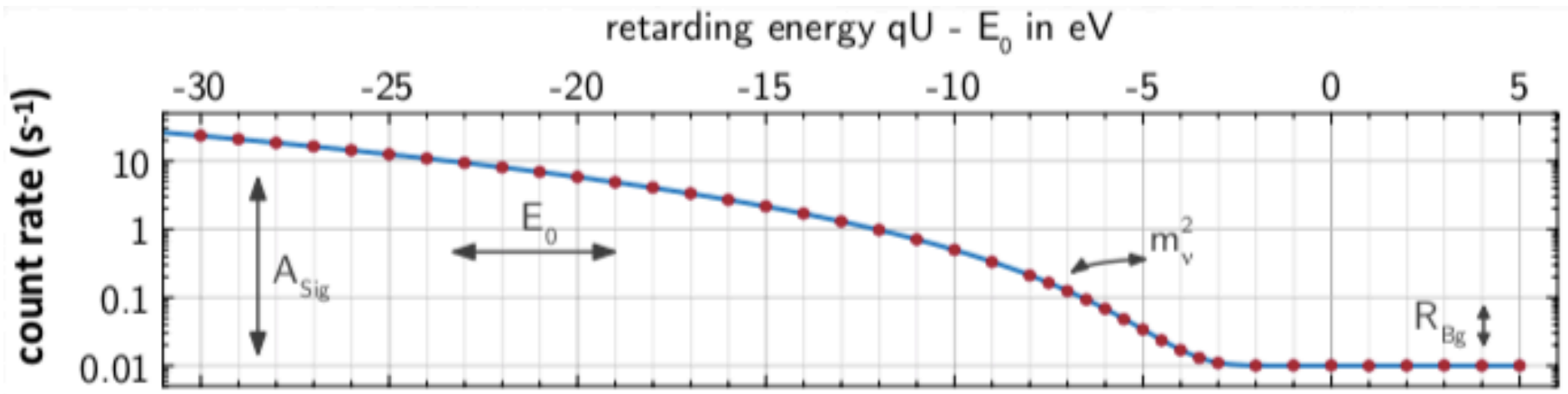


Molecular final state excitations / vibrations set ultimate  $T_2$  limit

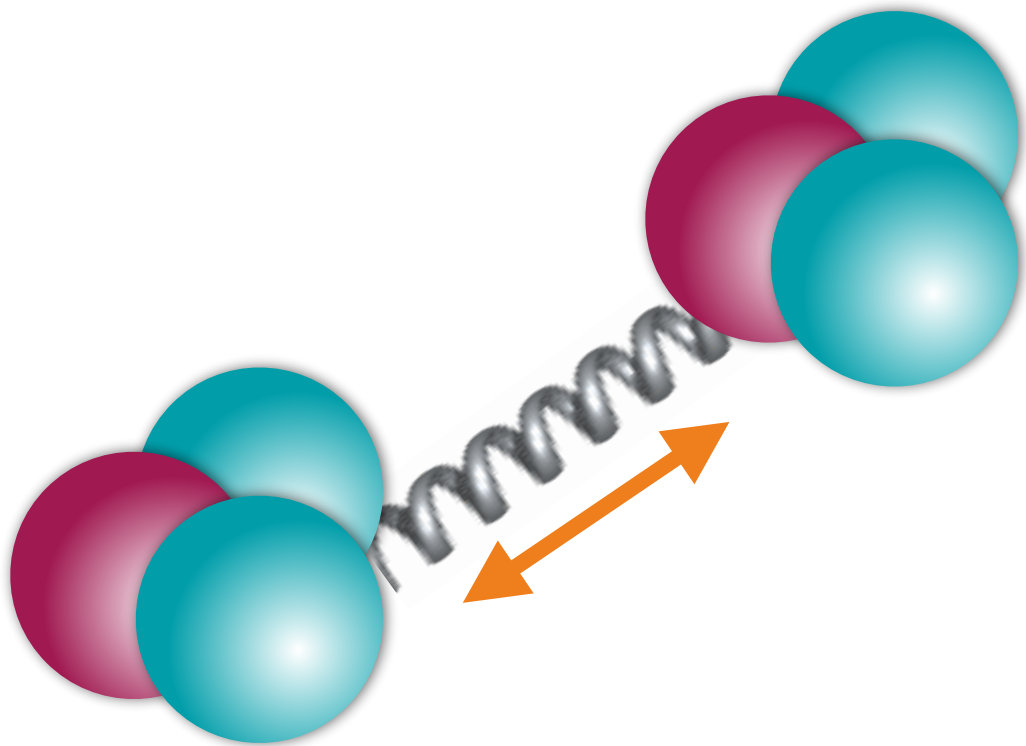
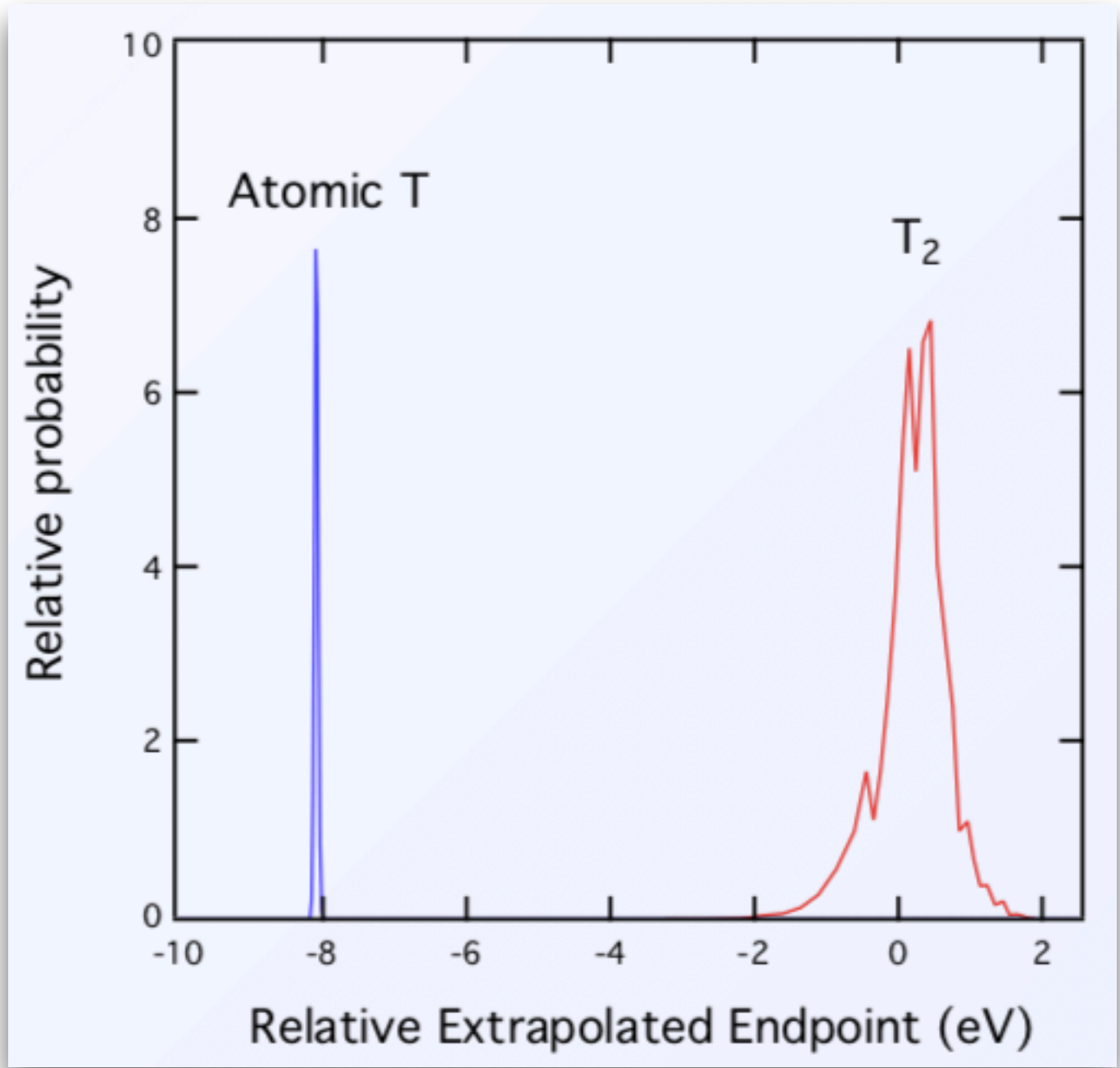
# Challenges for future MAC-E experiments



Spectrometer already as big as is practical - can't improve resolution



Integrated  $\beta$  spectrum means throwing away spectrum information

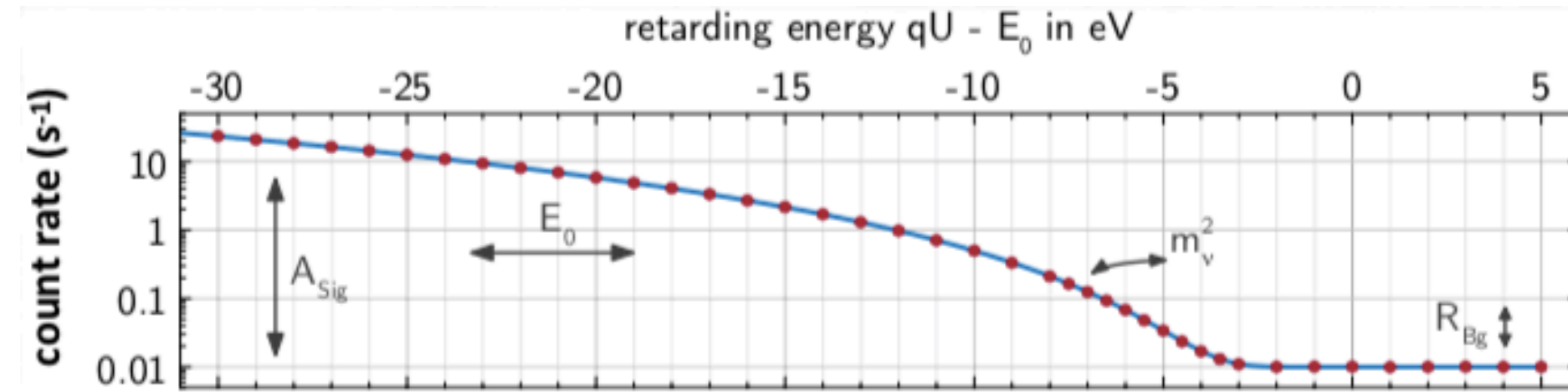


Molecular final state excitations / vibrations set ultimate  $T_2$  limit

# Challenges for future MAC-E experiments

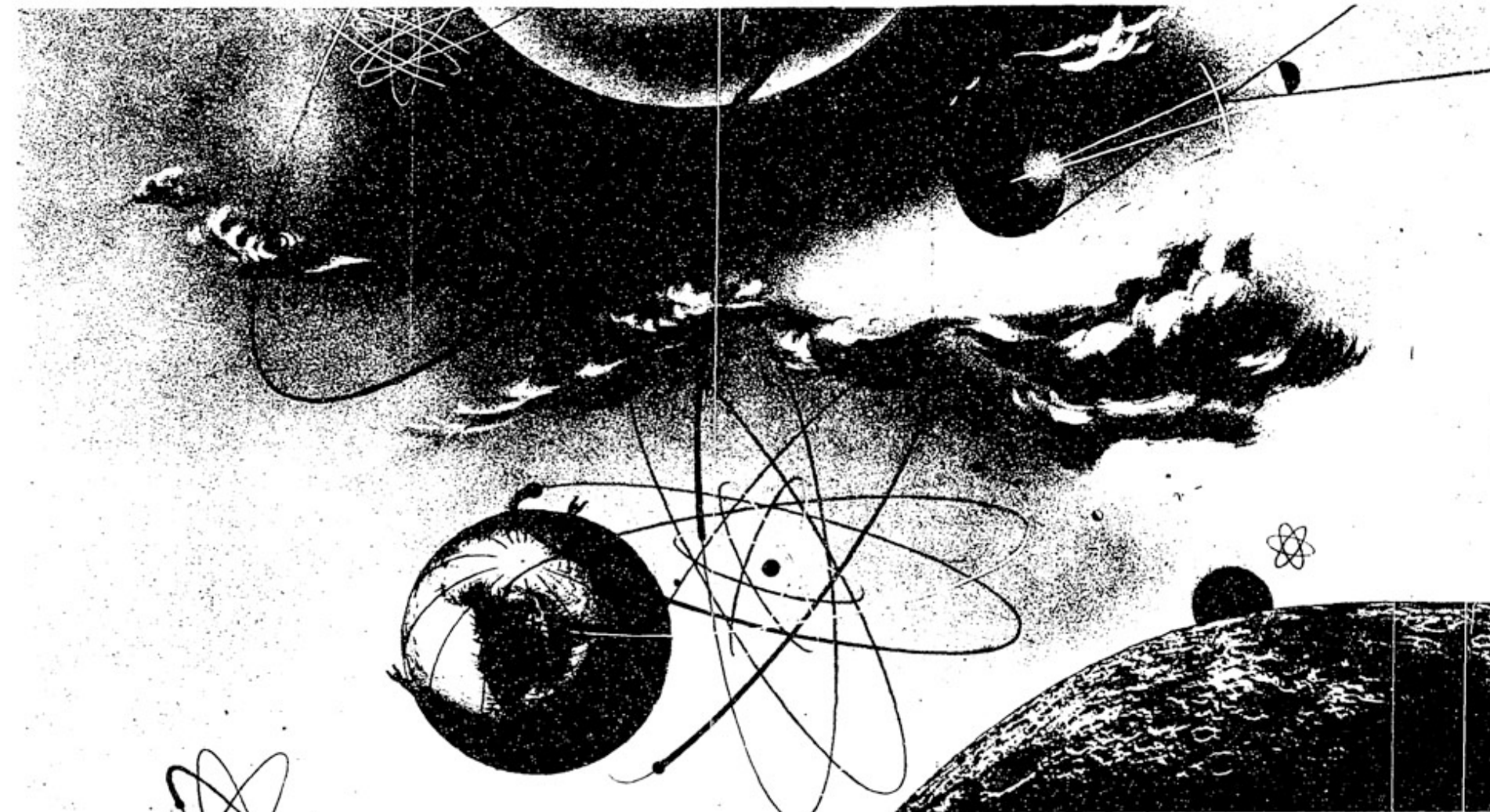


Spectrometer already as big as is practical - can't improve resolution



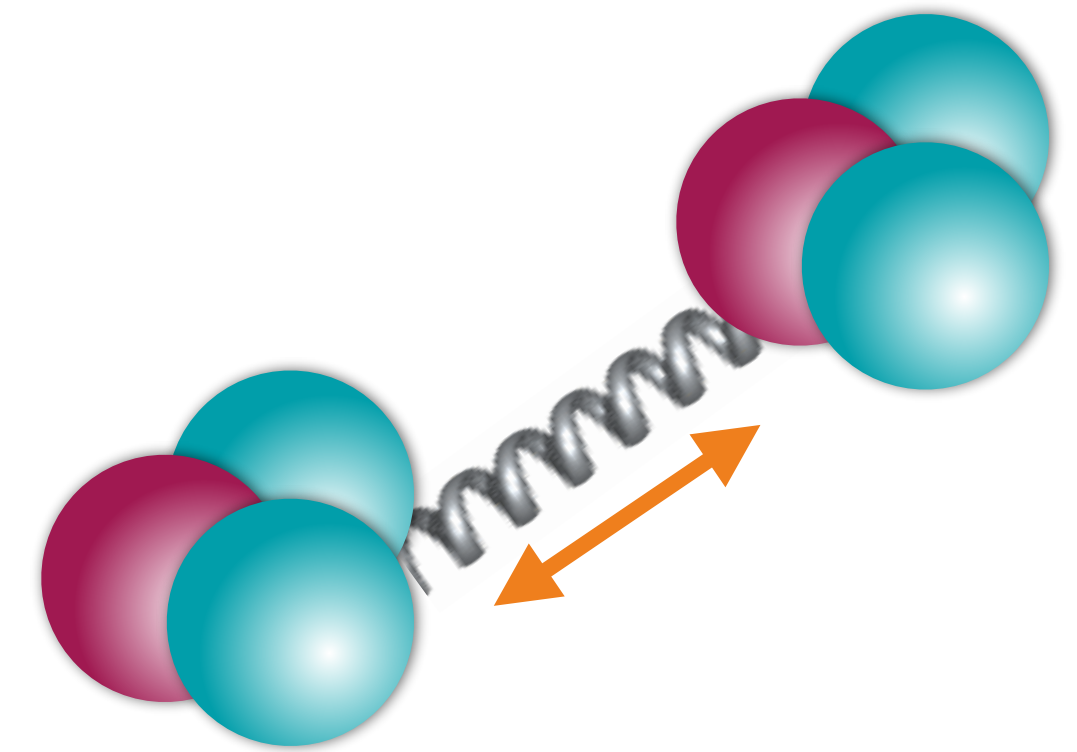
Integrated  $\beta$  spectrum means throwing away spectrum information

The New York Times Magazine



"In the world around us, atomic energy is working on a tremendous scale." Drawing by Herbert Bayer. © General Electric Co.

We Enter a New Era—the Atomic Age

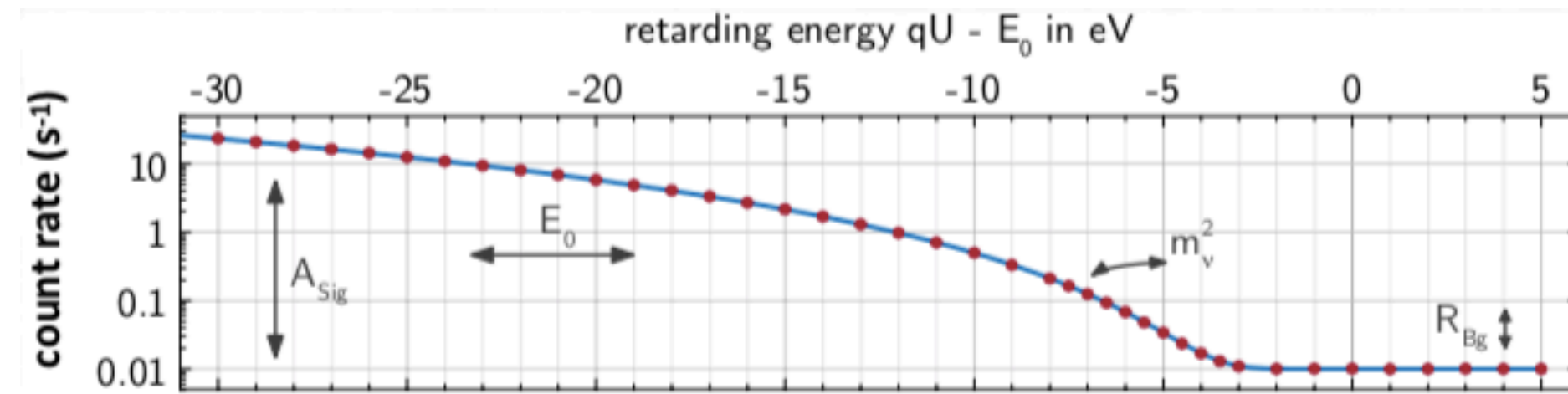


Molecular final state excitations / vibrations set ultimate  $T_2$  limit

# Challenges for future MAC-E experiments



Spectrometer already as big as is practical - can't improve resolution



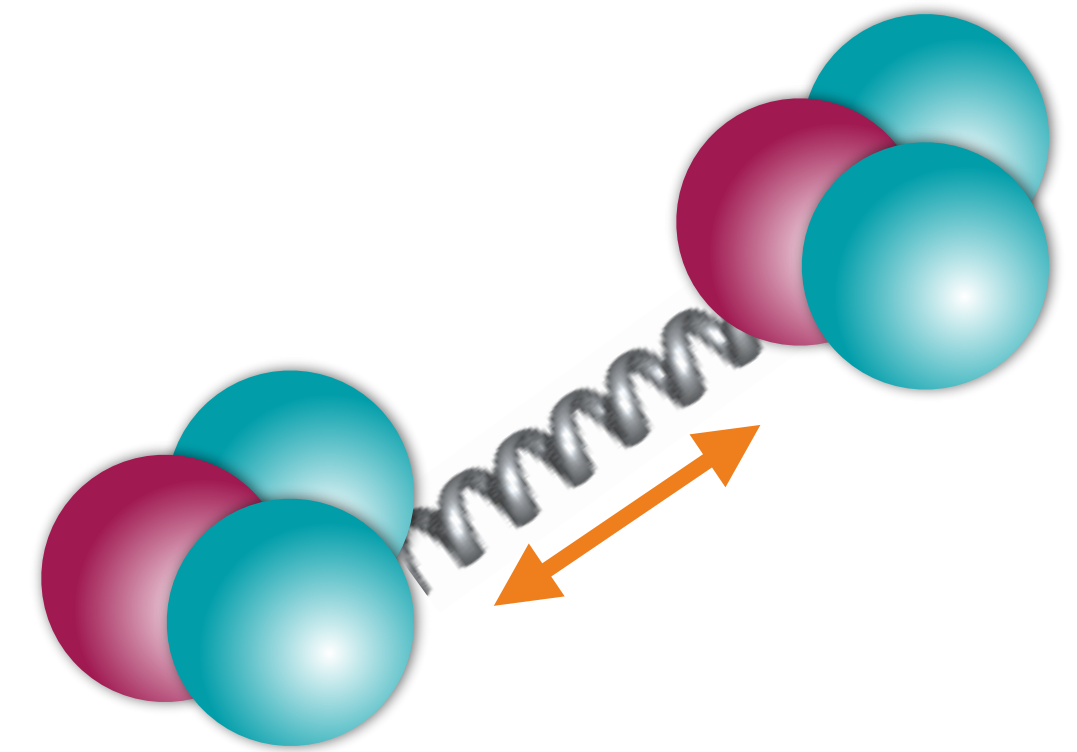
Integrated  $\beta$  spectrum means throwing away spectrum information

The New York Times Magazine



**PROJECT 8**

We Enter a New Era—the Atomic Age



Molecular final state excitations / vibrations set ultimate  $T_2$  limit

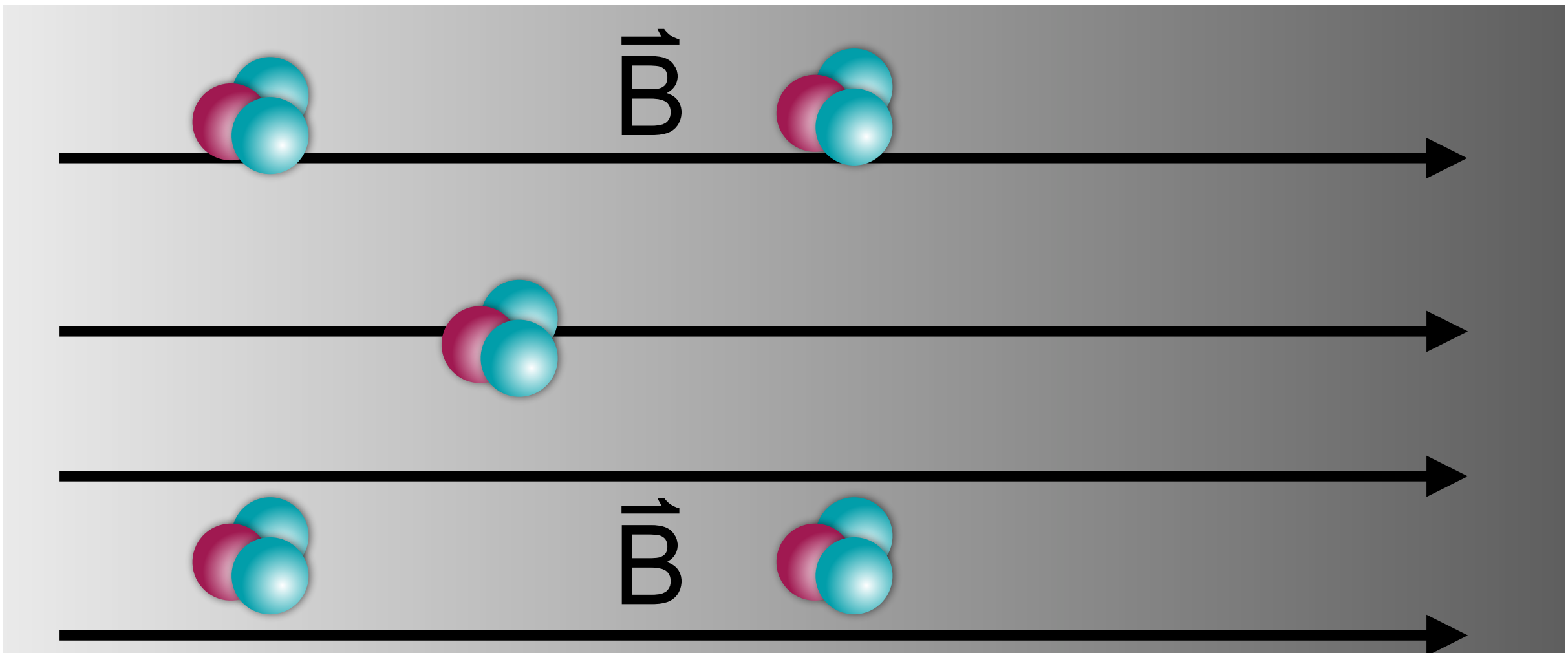




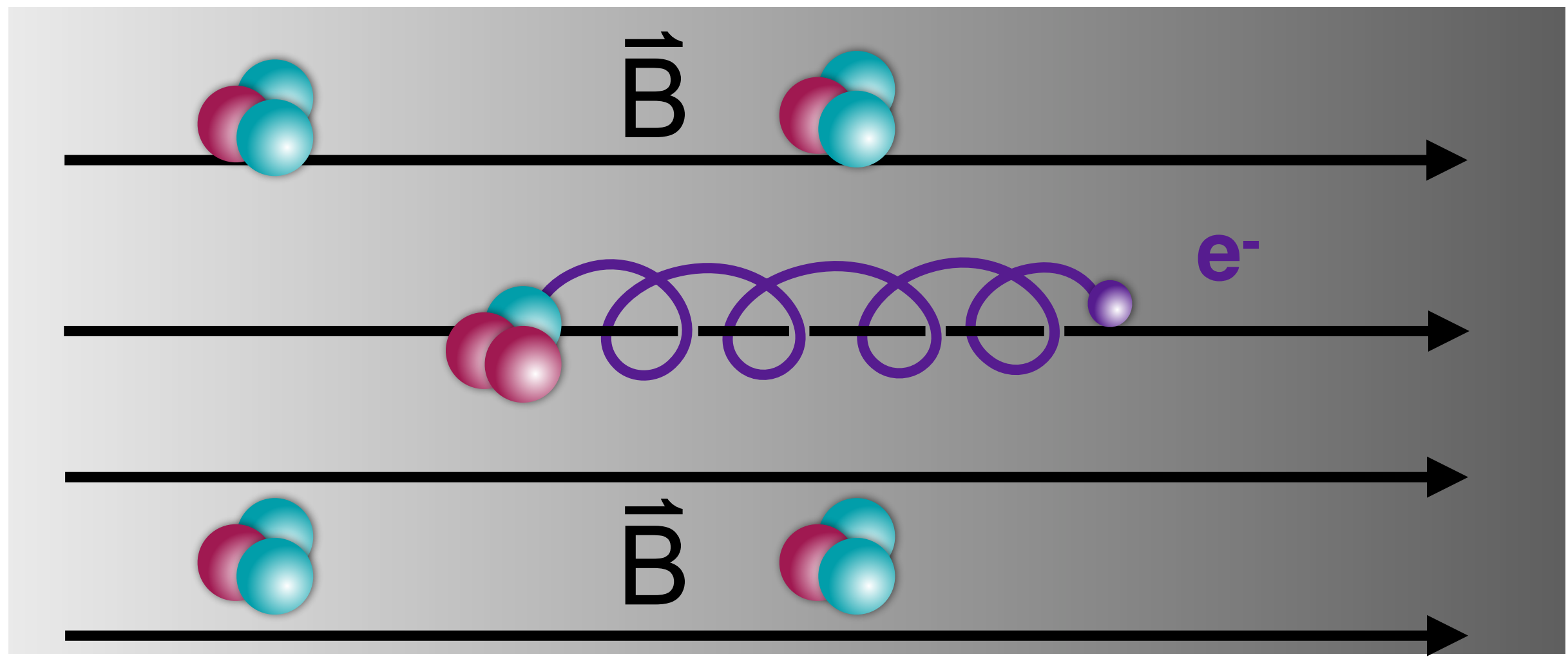
**Arthur Schawlow**

“Never measure anything  
but frequency!”

Trapped low-temperature **tritium atoms** in uniform magnetic field

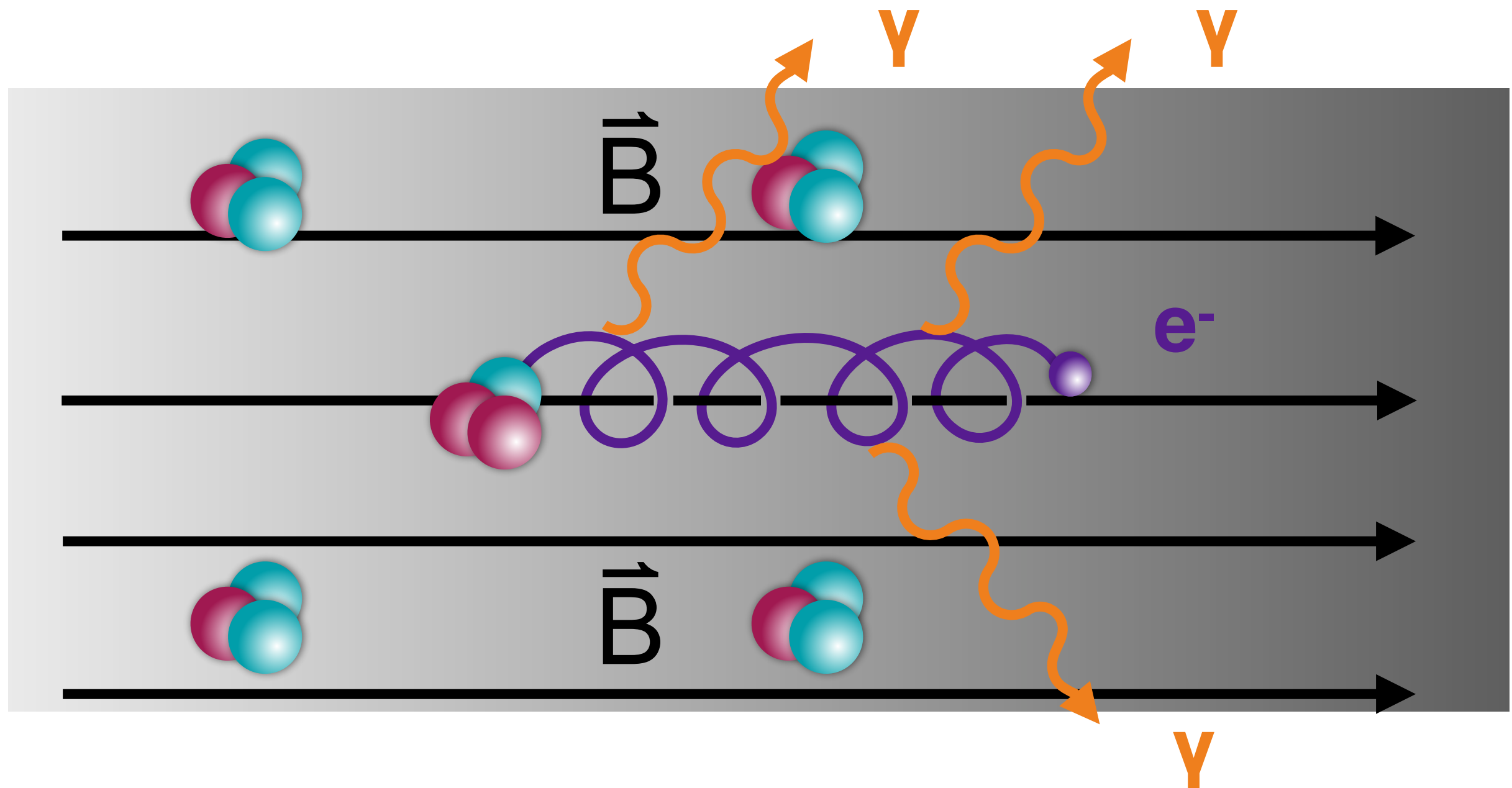


*J. Formaggio and B. Monreal, Phys. Rev D 80:051301 (2009)*



Trapped low-temperature **tritium atoms** in uniform magnetic field  
 $\beta$ -decay electrons exhibit **cyclotron motion** around the field

*J. Formaggio and B. Monreal, Phys. Rev D 80:051301 (2009)*



Trapped low-temperature **tritium atoms** in uniform magnetic field

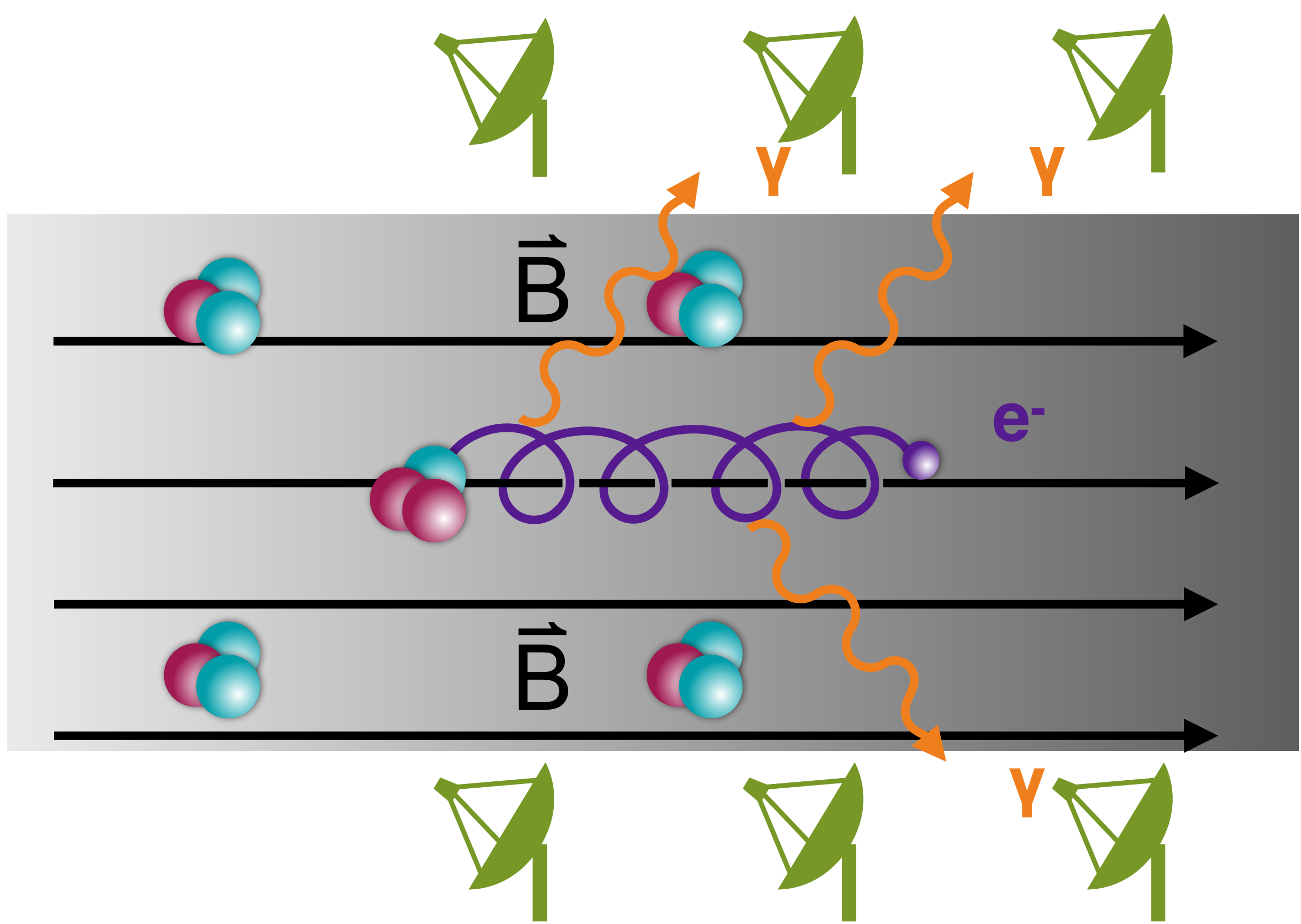
$\beta$ -decay electrons exhibit **cyclotron motion** around the field

The spiralling electrons emit **cyclotron radiation**

$$f_\gamma \equiv \frac{\omega_c}{2\pi\gamma} = \frac{1}{2\pi} \frac{eB}{m_e + K_e/c^2}$$

↑ Cyclotron frequency      ↑ Electron kinetic energy

*J. Formaggio and B. Monreal, Phys. Rev D 80:051301 (2009)*



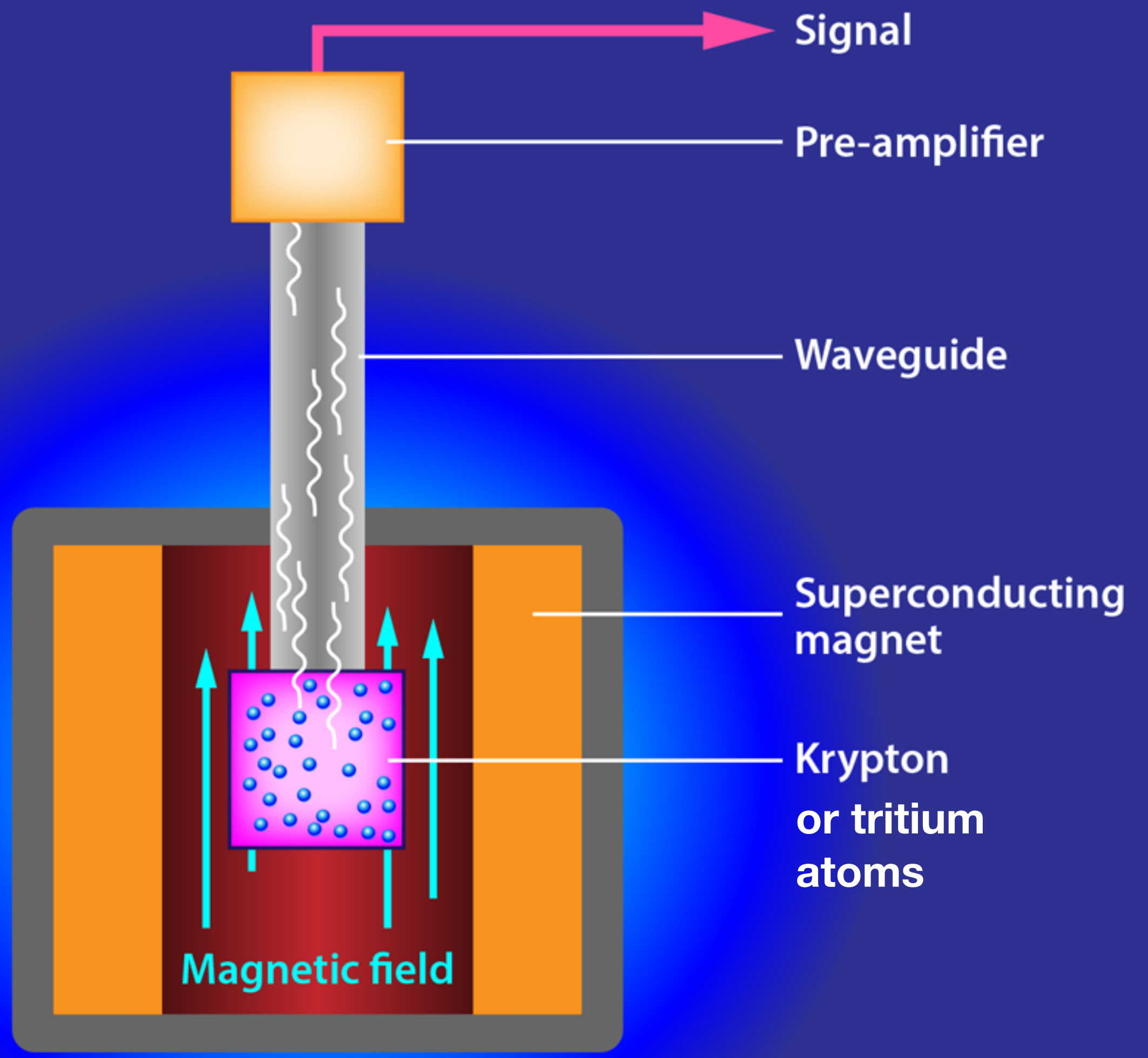
Trapped low-temperature **tritium atoms** in uniform magnetic field

$\beta$ -decay electrons exhibit **cyclotron motion** around the field

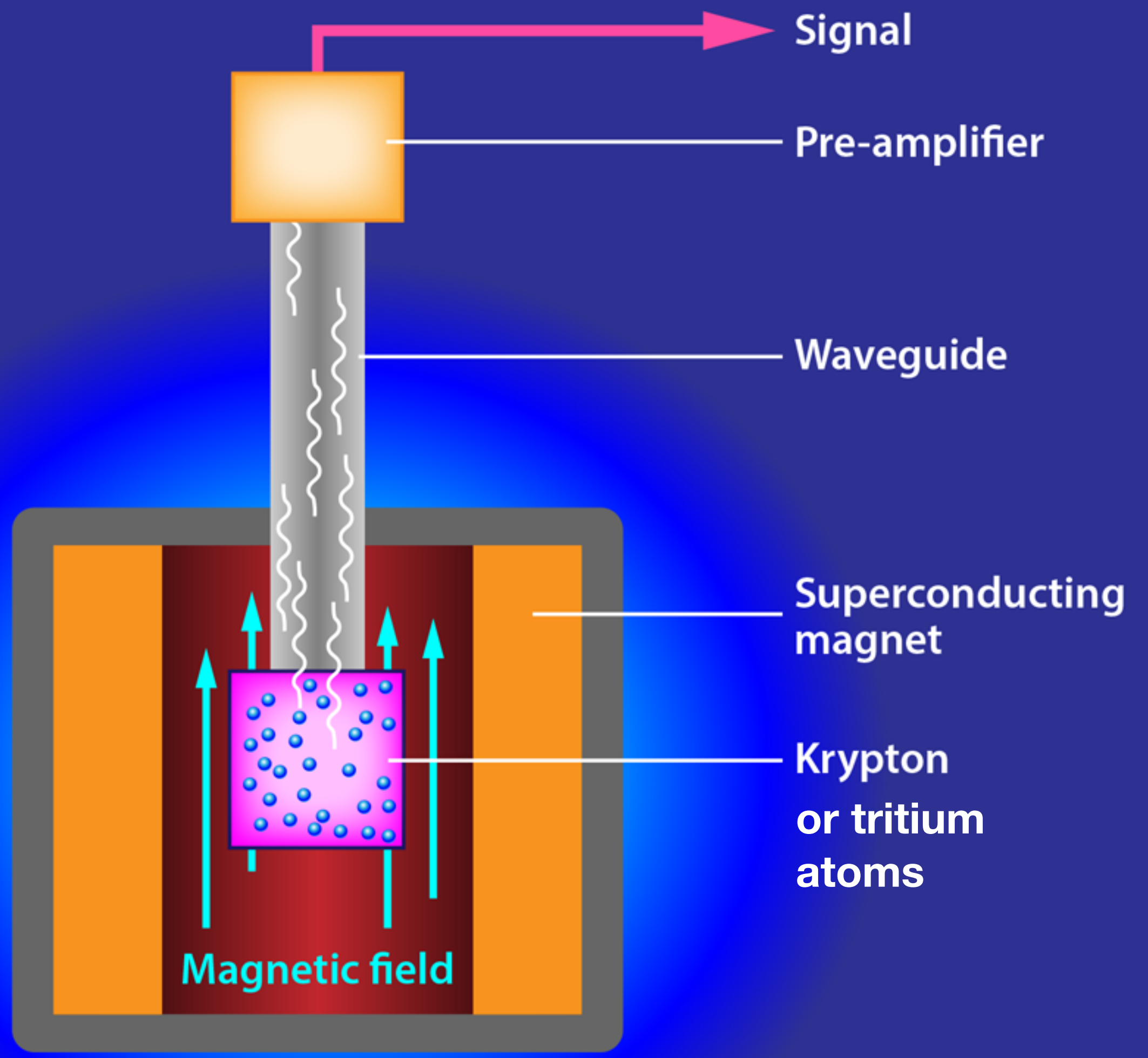
The spiralling electrons emit **cyclotron radiation**

**Measure gamma frequency** to reconstruct **electron energy**

*J. Formaggio and B. Monreal, Phys. Rev D 80:051301 (2009)*



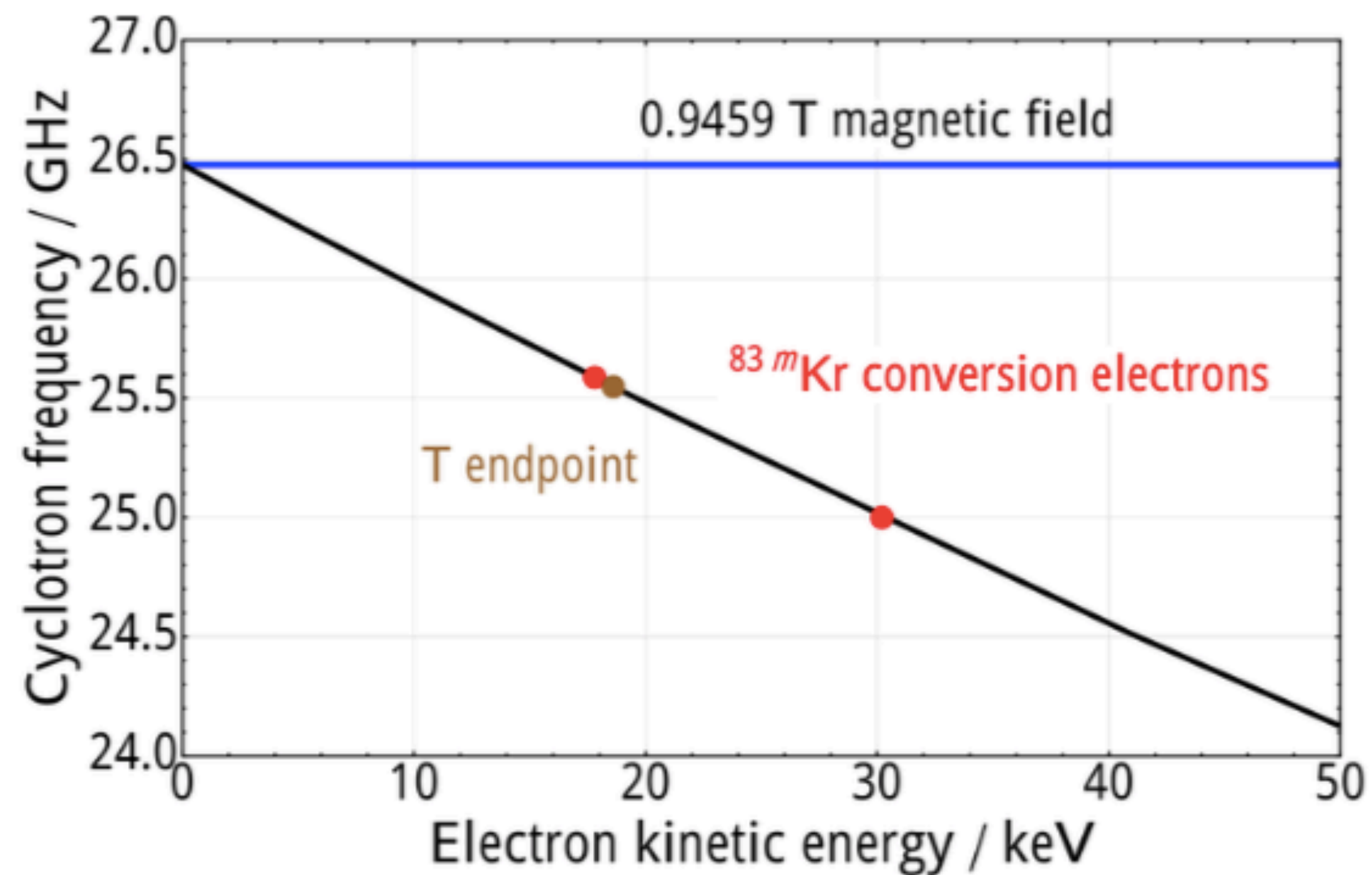
**Magnetic field: ~ 1 Tesla**



**Magnetic field: ~ 1 Tesla**

**Cyclotron frequency range 25-26.5 GHz  
(microwave)**

**Tritium endpoint 18.6 keV  
(0 - 30keV for  $^{83m}\text{Kr}$  spectrum)**





**Magnetic field: ~ 1 Tesla**

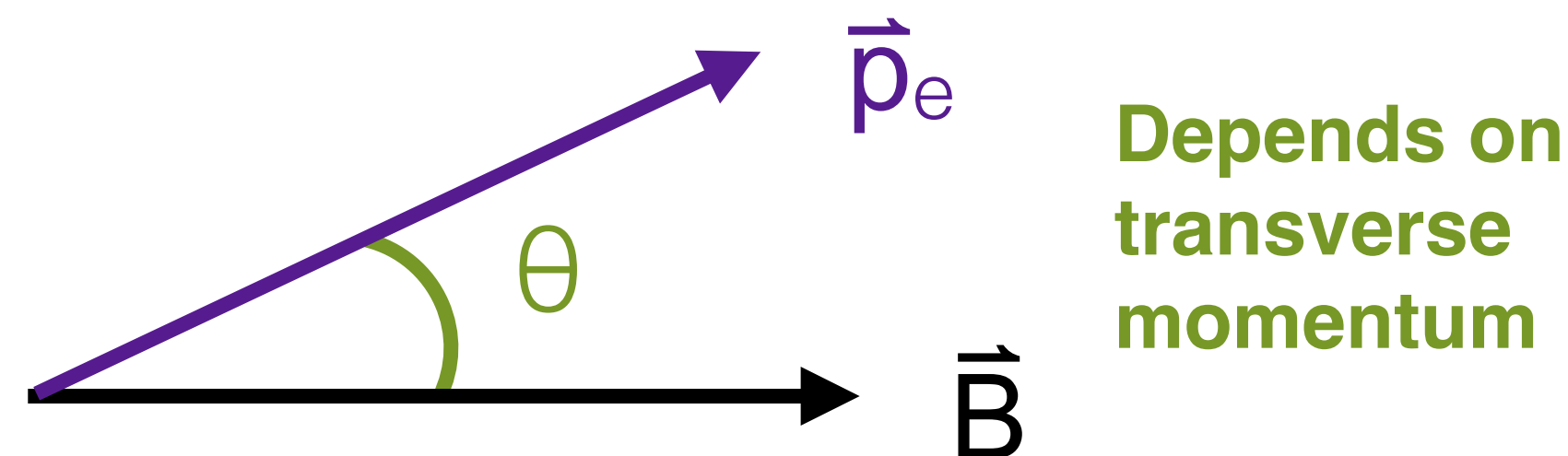
**Cyclotron frequency range 25-26.5 GHz  
(microwave)**

**Tritium endpoint 18.6 keV  
(0 - 30keV for <sup>83m</sup>Kr spectrum)**

**Power in femtowatt range**

**Larmor formula**

$$P(\gamma, \theta) = \frac{1}{4\pi\epsilon_0} \frac{2}{3} \frac{e^4}{m_e^2} B^2 (\gamma^2 - 1) \sin^2 \theta$$



$$P(K_e, m_e, \theta) = \frac{1}{4\pi\epsilon_0} \frac{2}{3} \frac{e^4}{m_e^2} B^2 (K_e^2 + 2K_e m_e c^2) \sin^2 \theta$$

$$P(18.6 \text{ keV}, 1 \text{ T}, 90^\circ) = 1 \text{ fW}$$

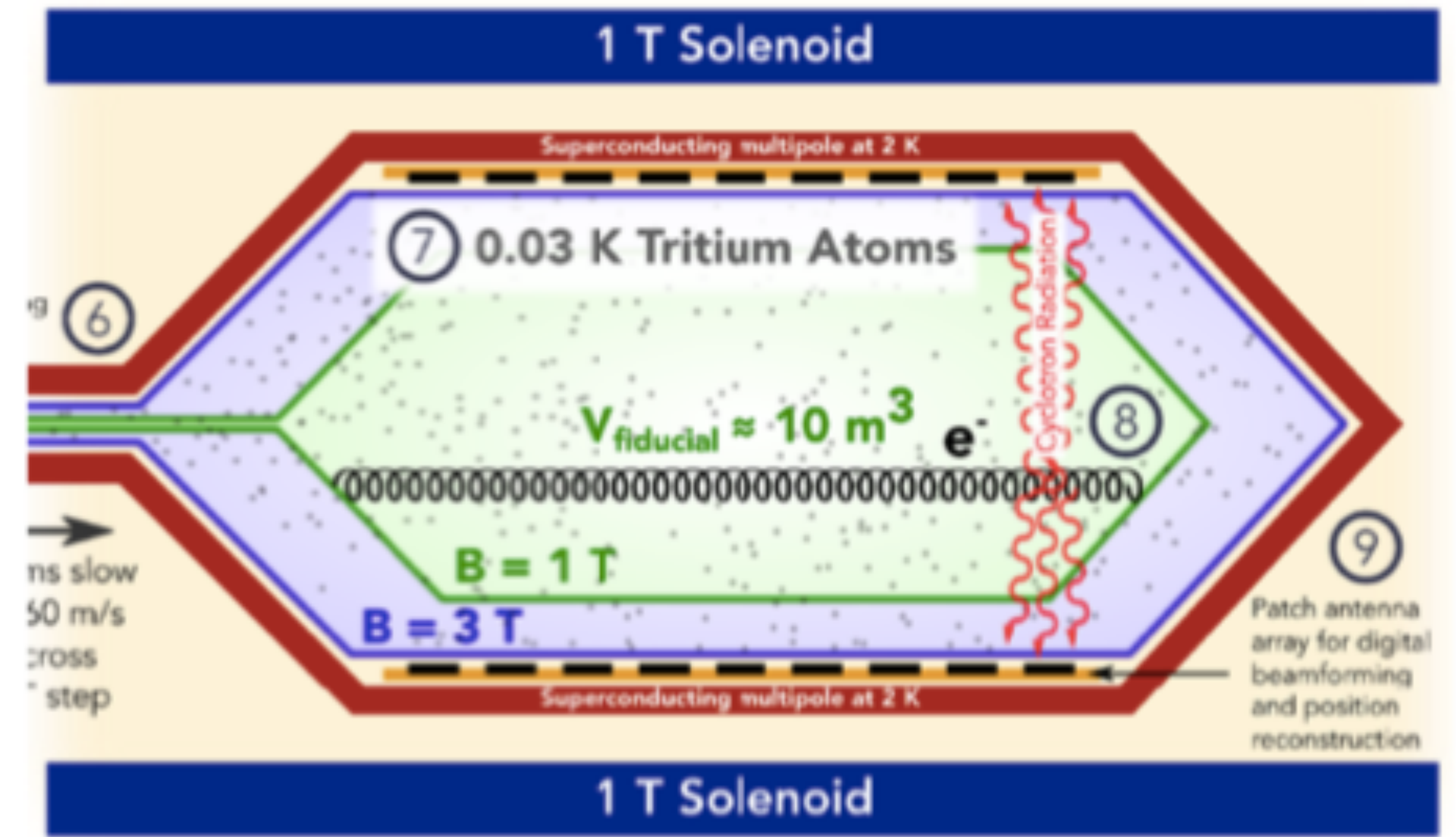
**Magnetic field: ~ 1 Tesla**

**Cyclotron frequency range 25-26.5 GHz  
(microwave)**

**Tritium endpoint 18.6 keV  
(0 - 30keV for <sup>83m</sup>Kr spectrum)**

**Power in femtowatt range**

**Gas volume 10m<sup>3</sup> (final phase)**



**Magnetic field: ~ 1 Tesla**

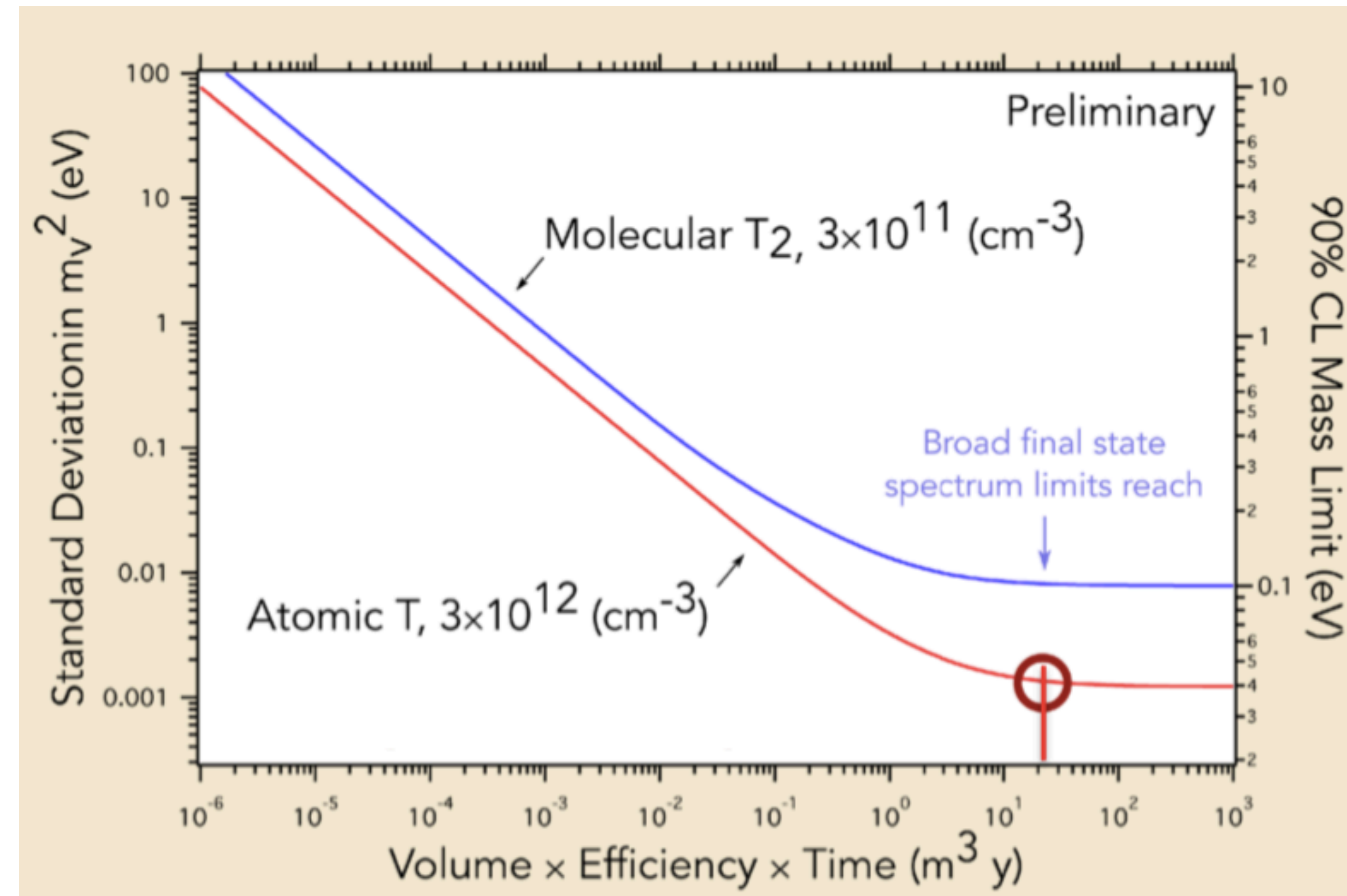
**Cyclotron frequency range 25-26.5 GHz  
(microwave)**

**Tritium endpoint 18.6 keV  
(0 - 30keV for  $^{83m}\text{Kr}$  spectrum)**

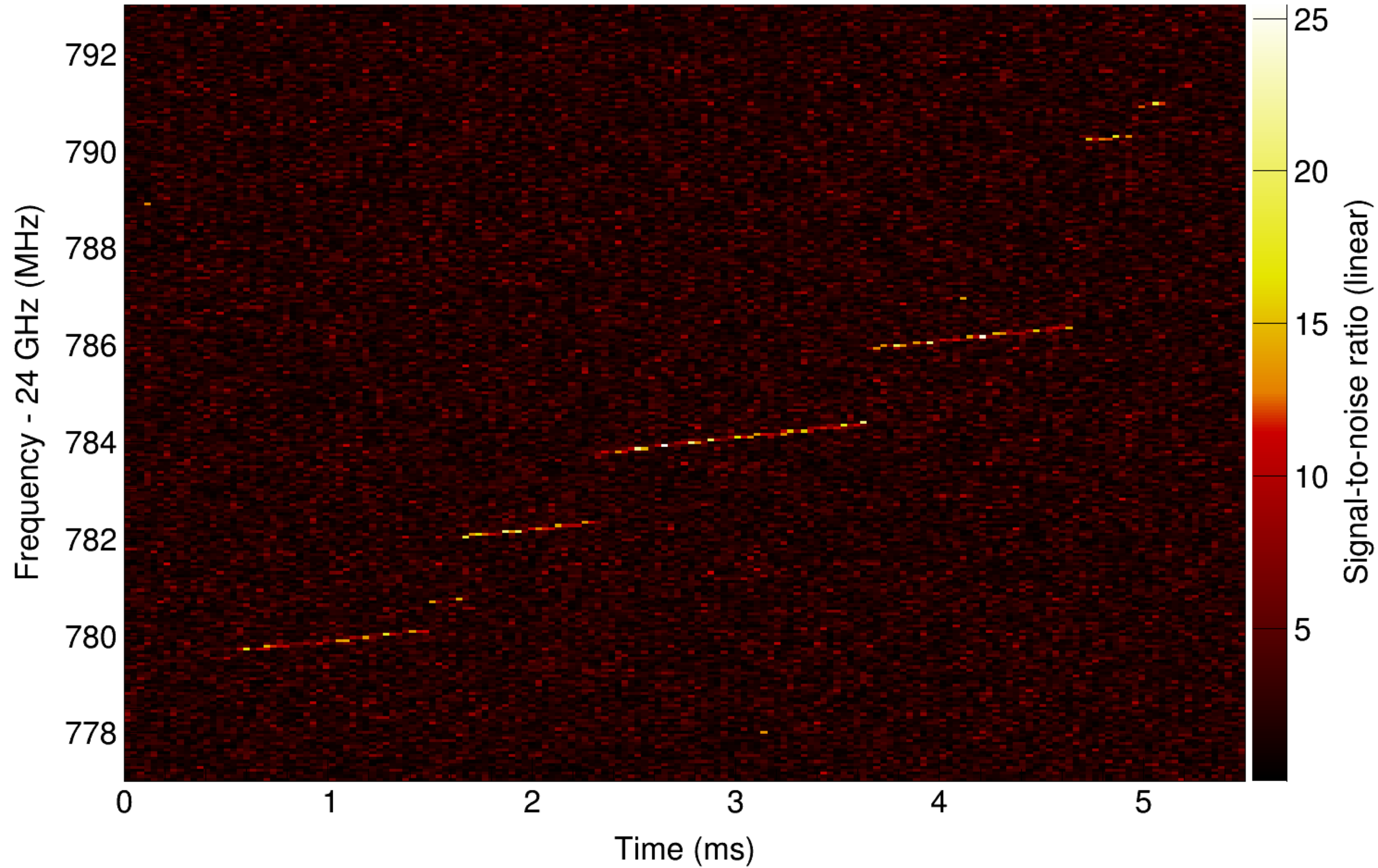
**Power in femtowatt range**

**Gas volume 10m<sup>3</sup> (final phase)**

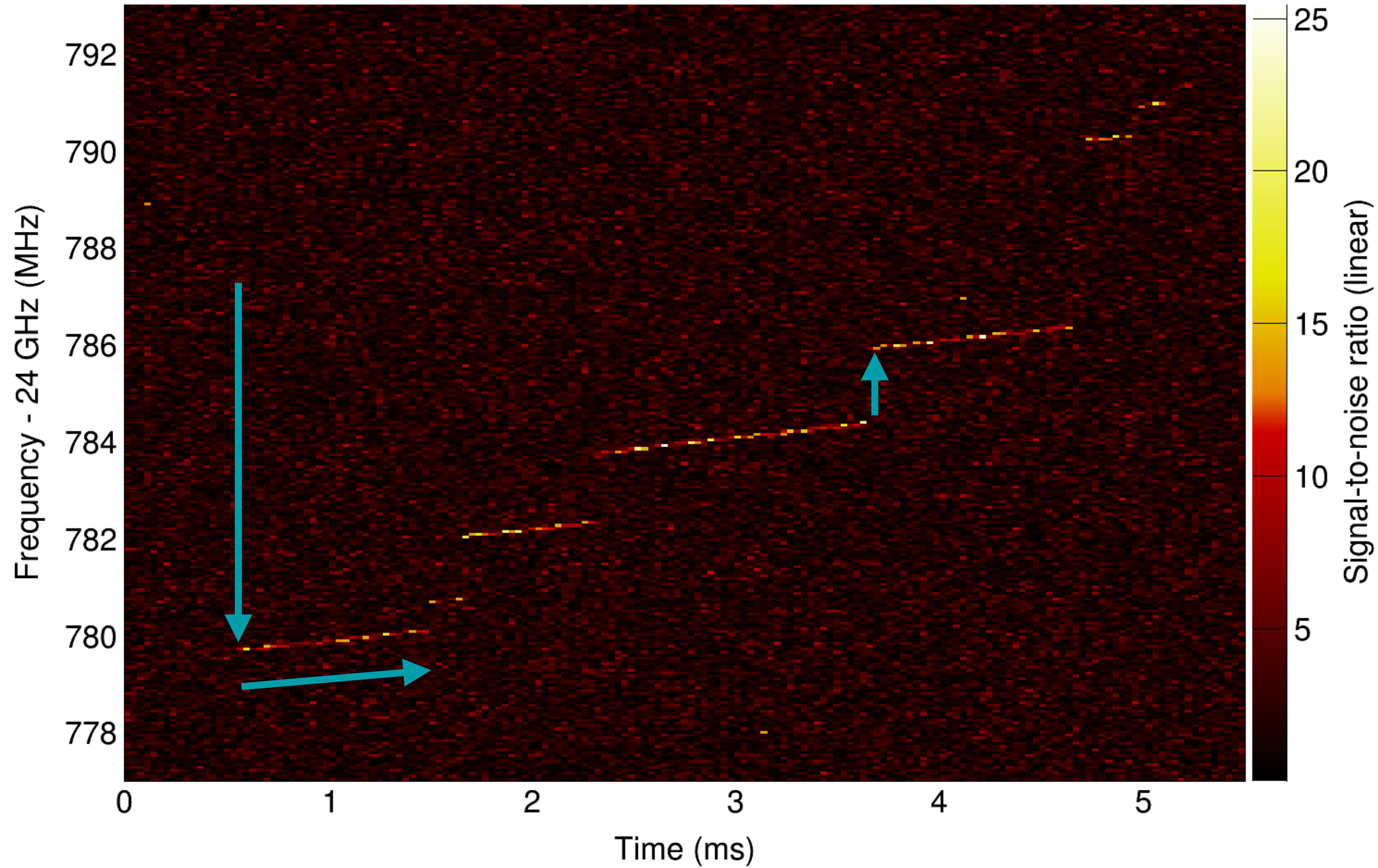
**Projected  $m_\nu$  sensitivity 40 meV**



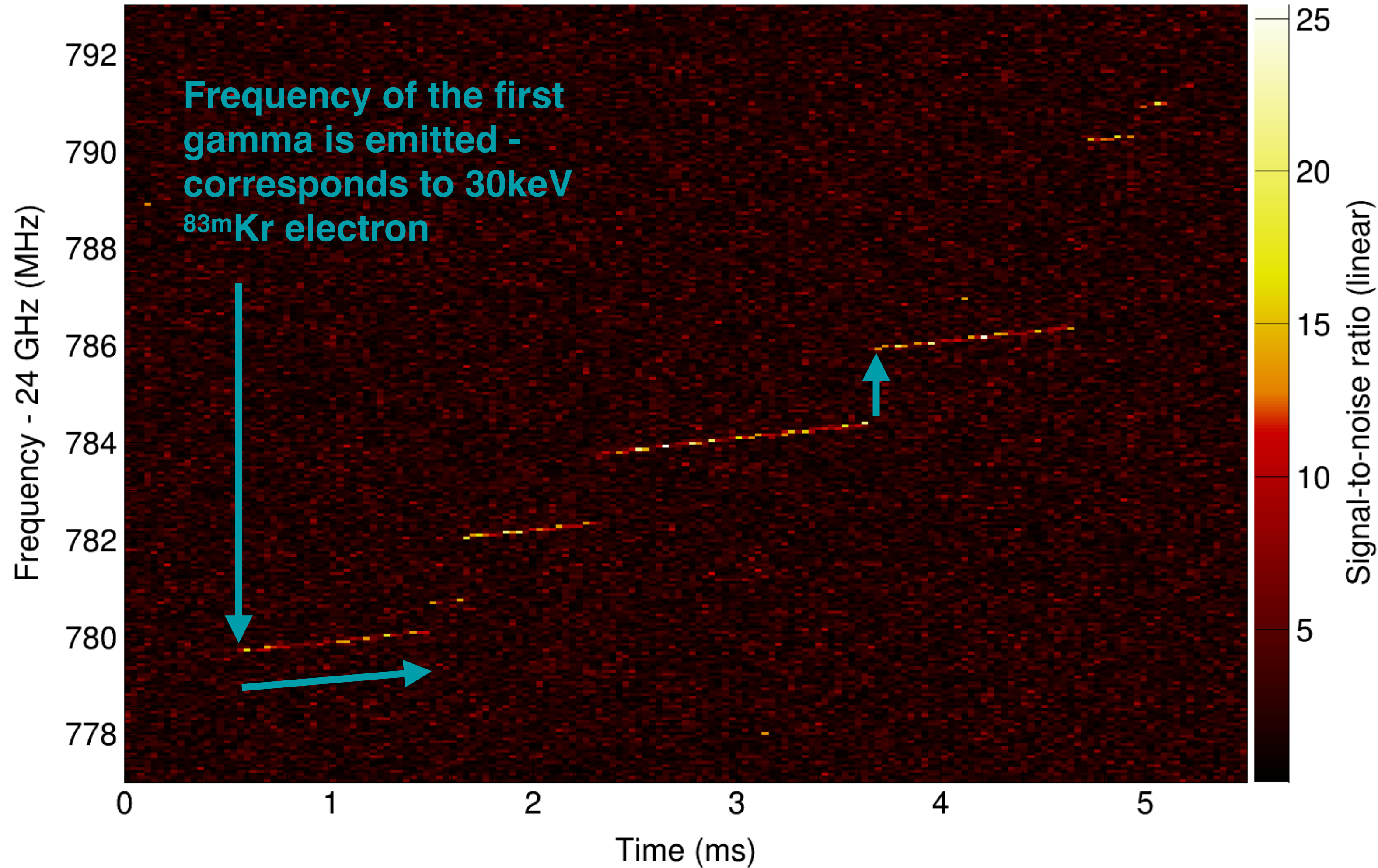
*Phys. Rev. Lett. 114, 162501 (2015)*



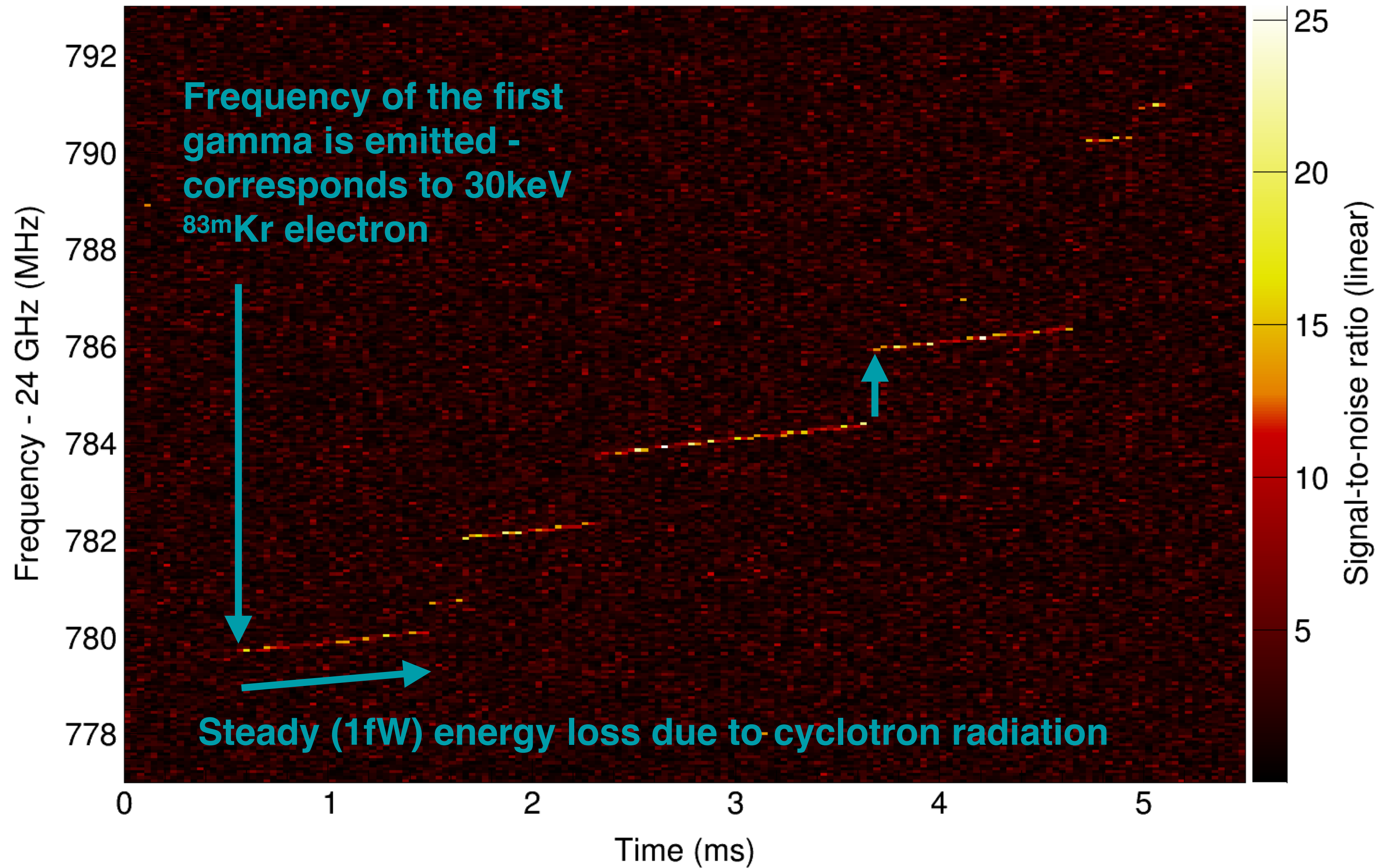
*Phys. Rev. Lett.* 114, 162501 (2015)



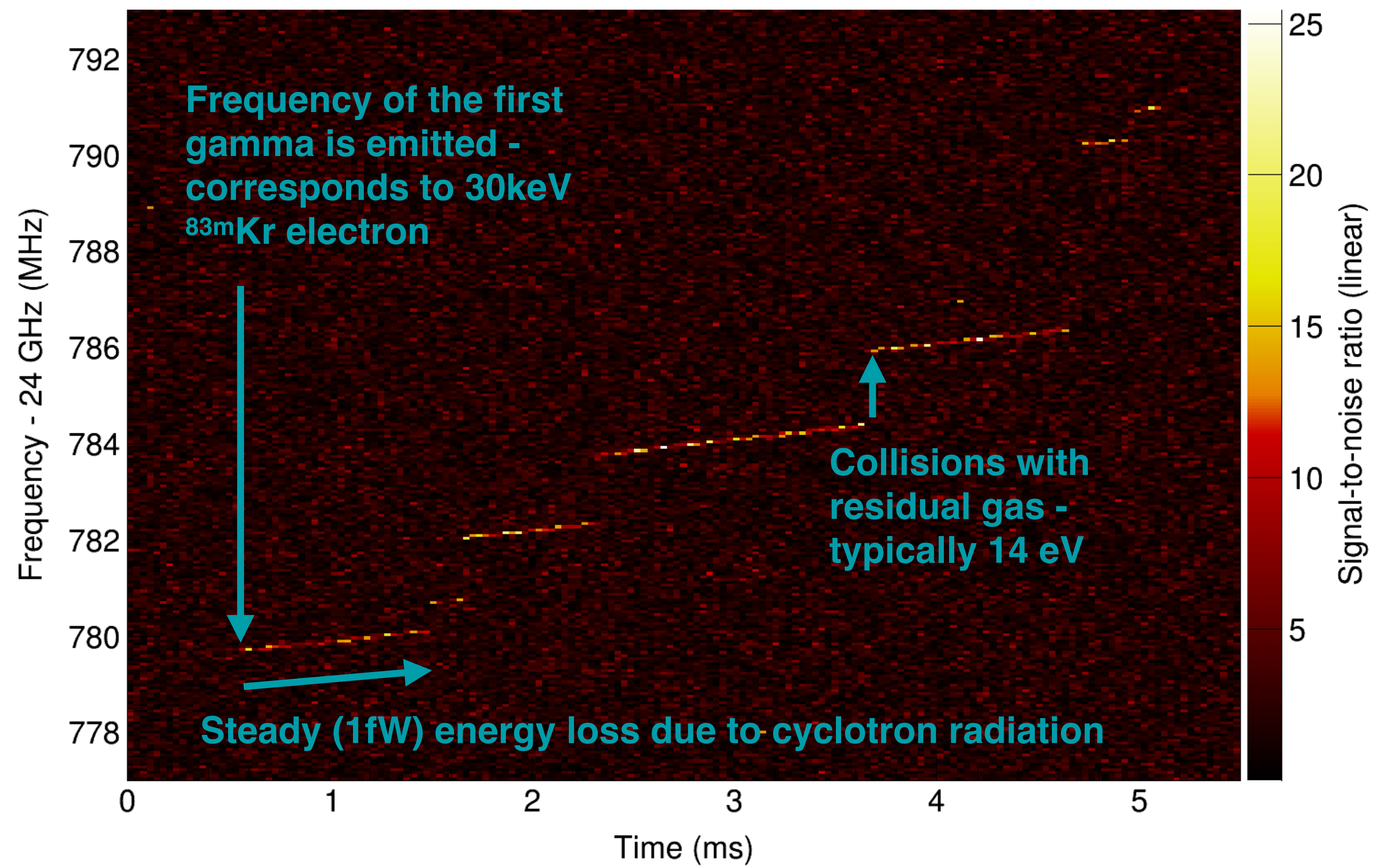
*Phys. Rev. Lett.* 114, 162501 (2015)



*Phys. Rev. Lett.* 114, 162501 (2015)

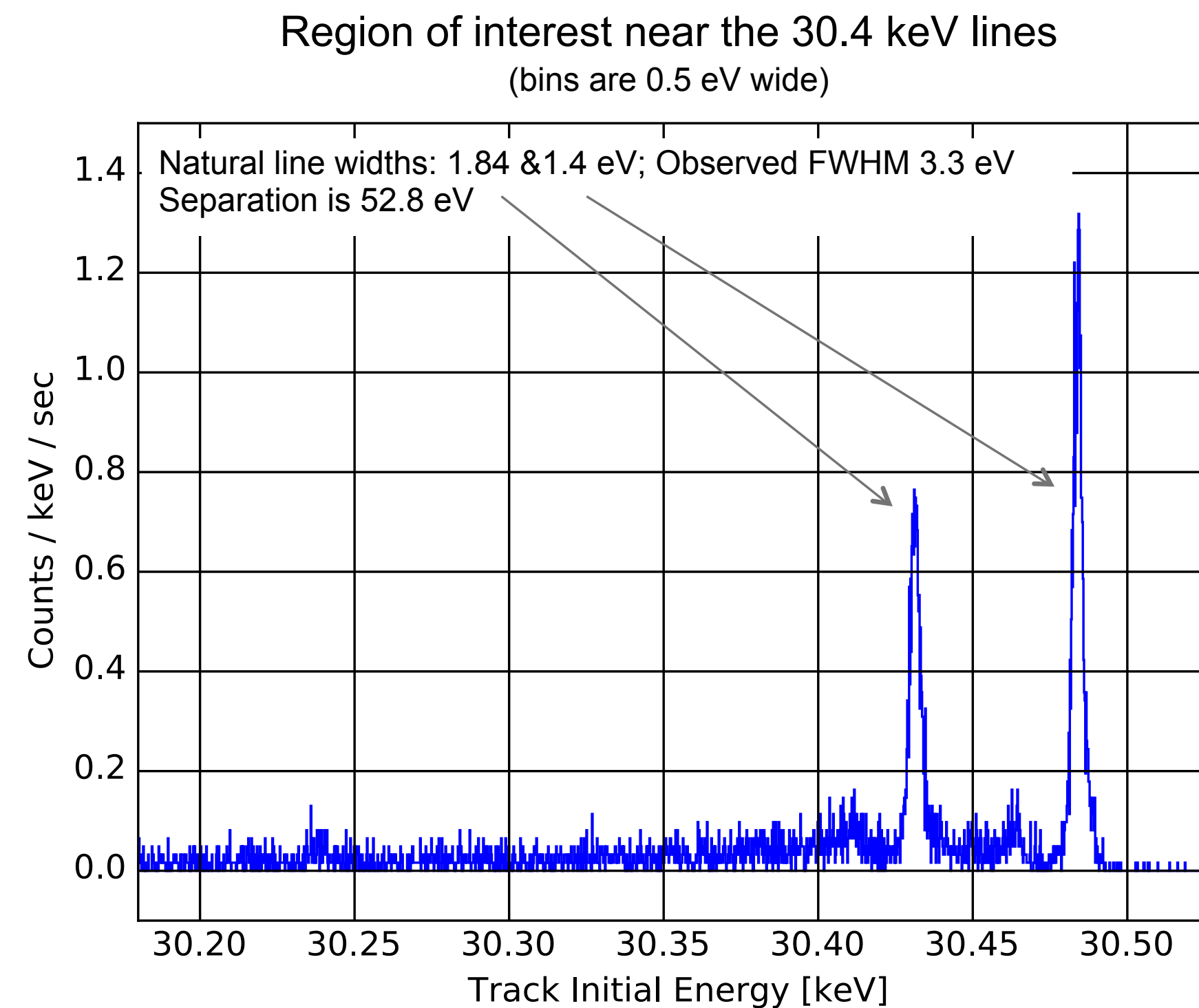
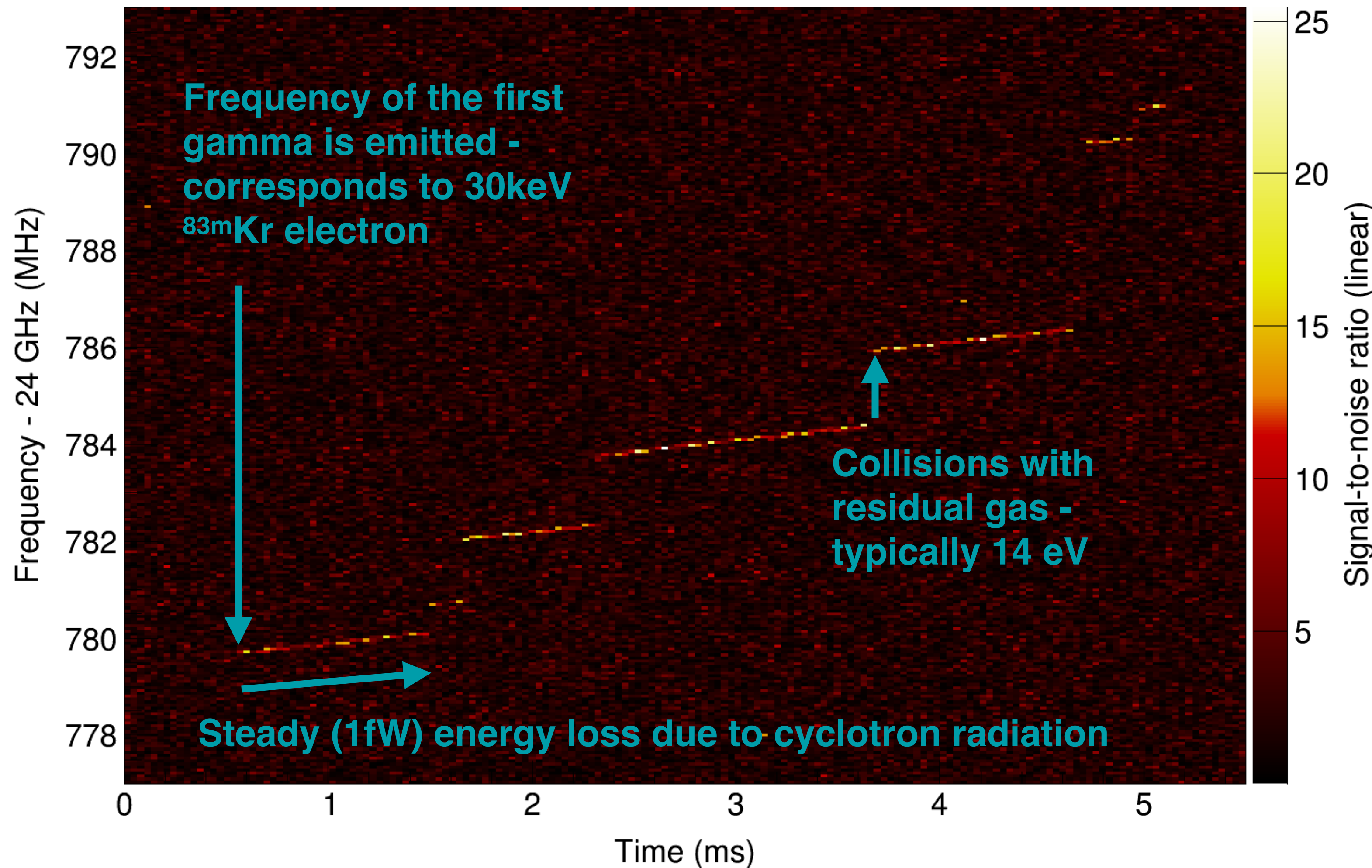


*Phys. Rev. Lett. 114, 162501 (2015)*



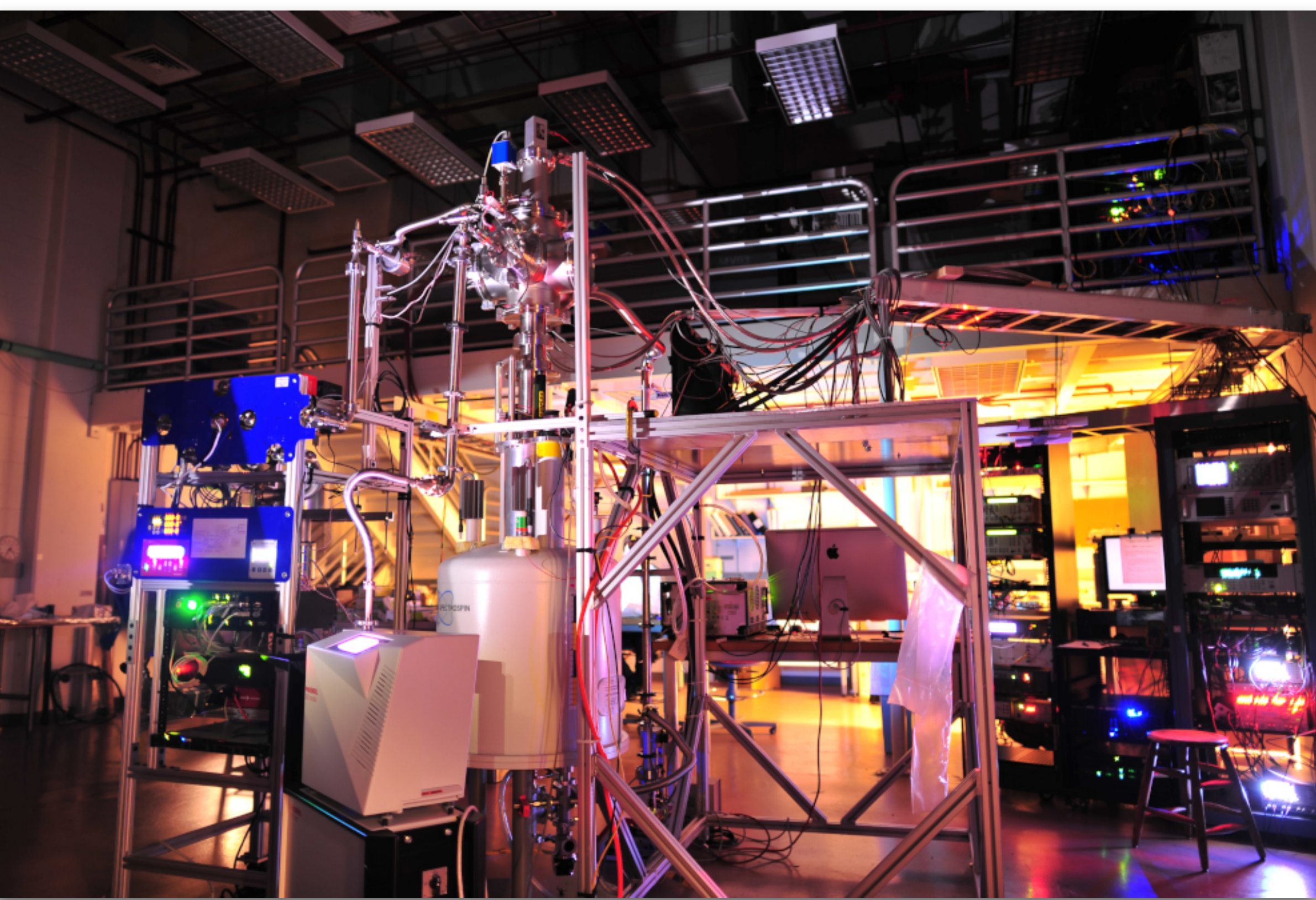


Phys. Rev. Lett. 114, 162501 (2015)



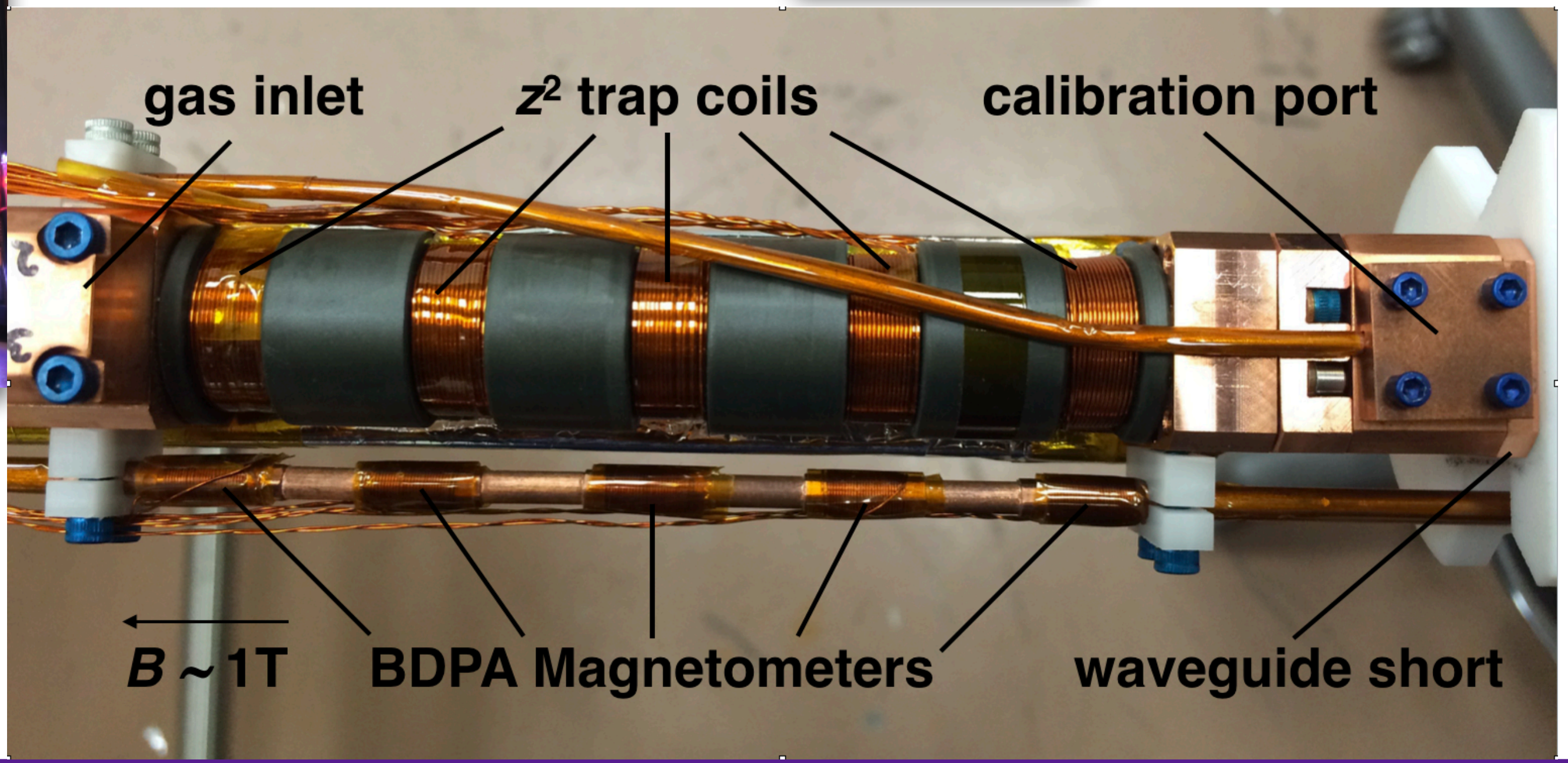
**30.4 keV  $^{83m}\text{Kr}$  lines resolved with FWHM 3.3 eV (actual widths 1.84 & 1.4 eV)**

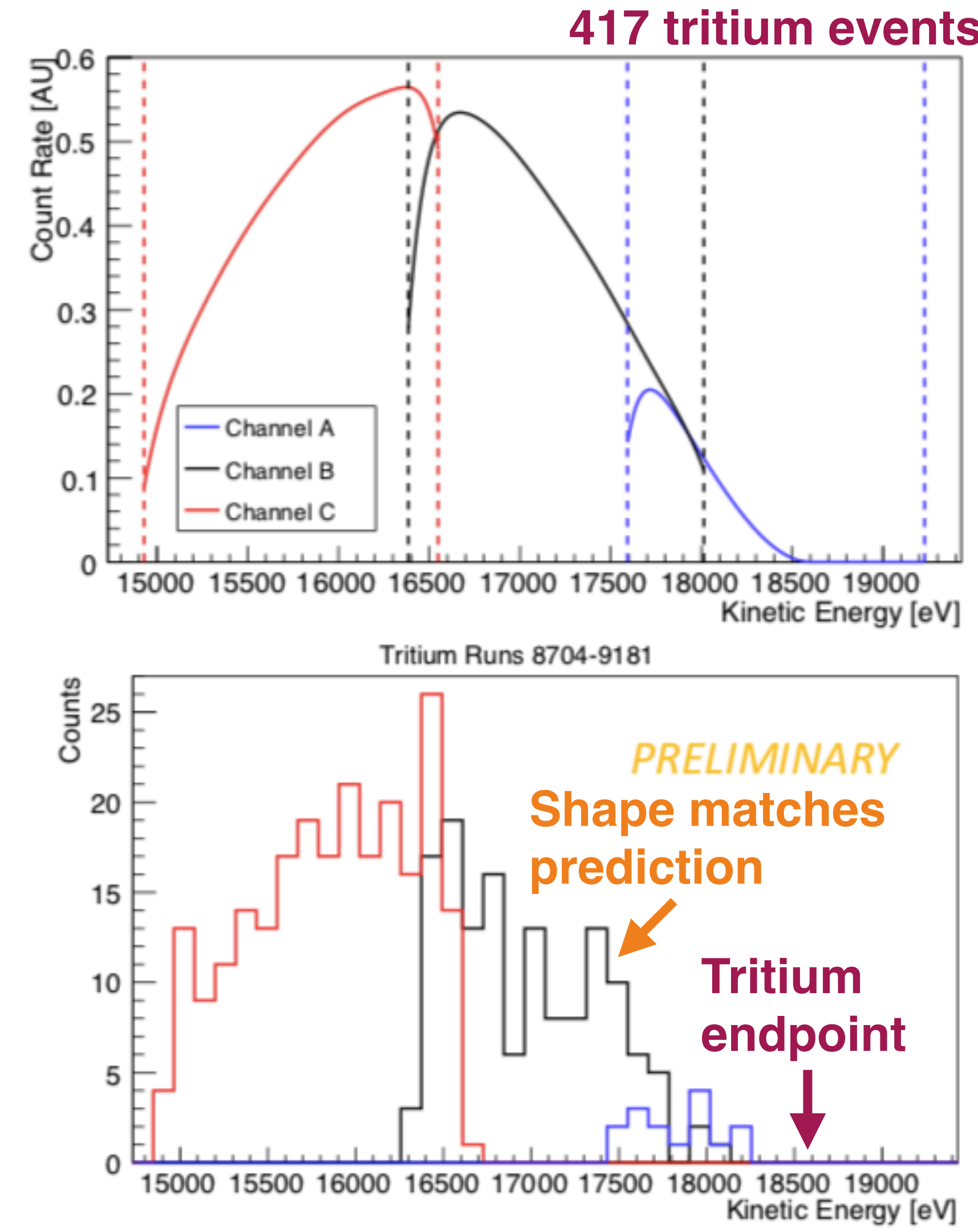
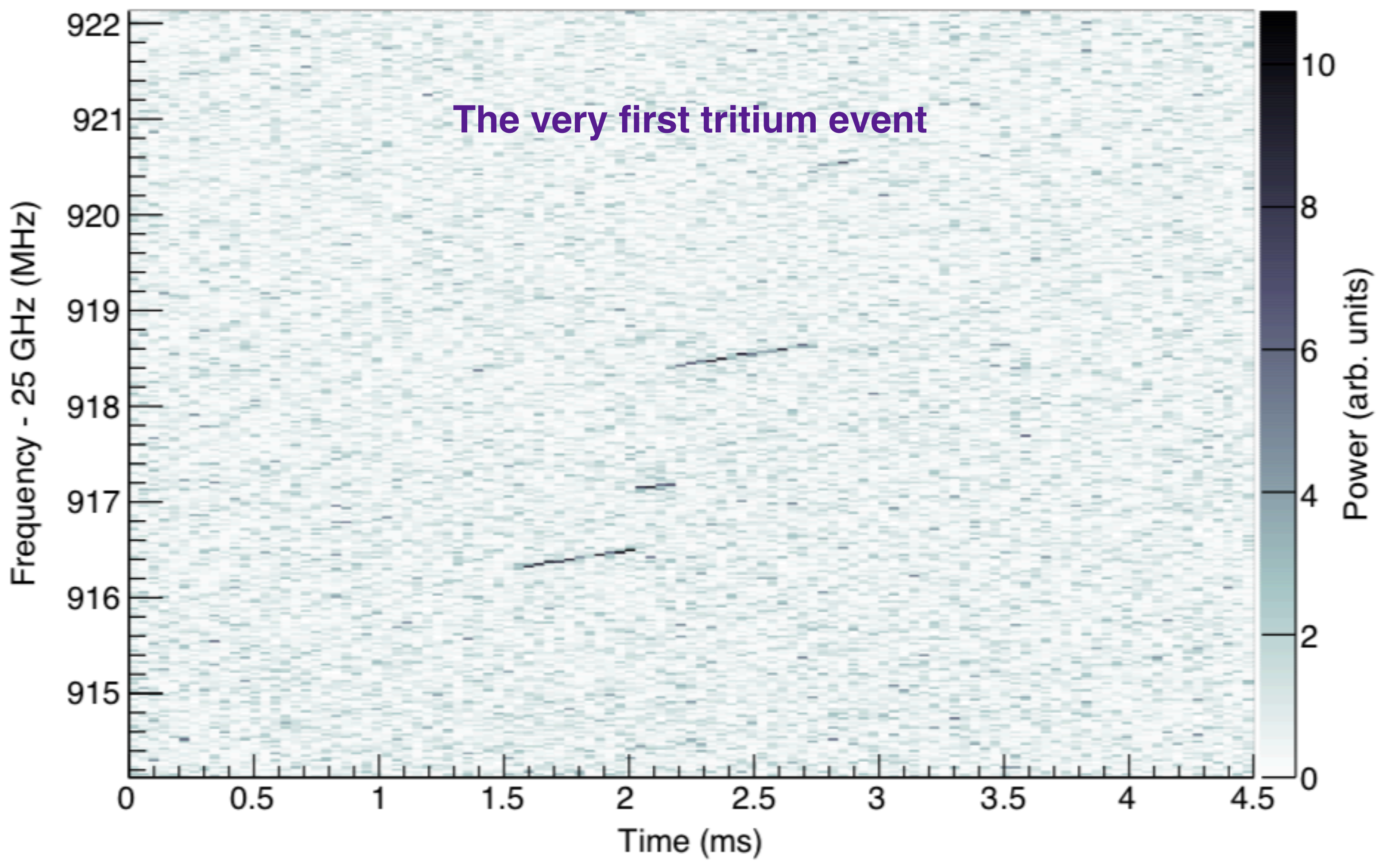
*JPhysG 44 (2017) 5*



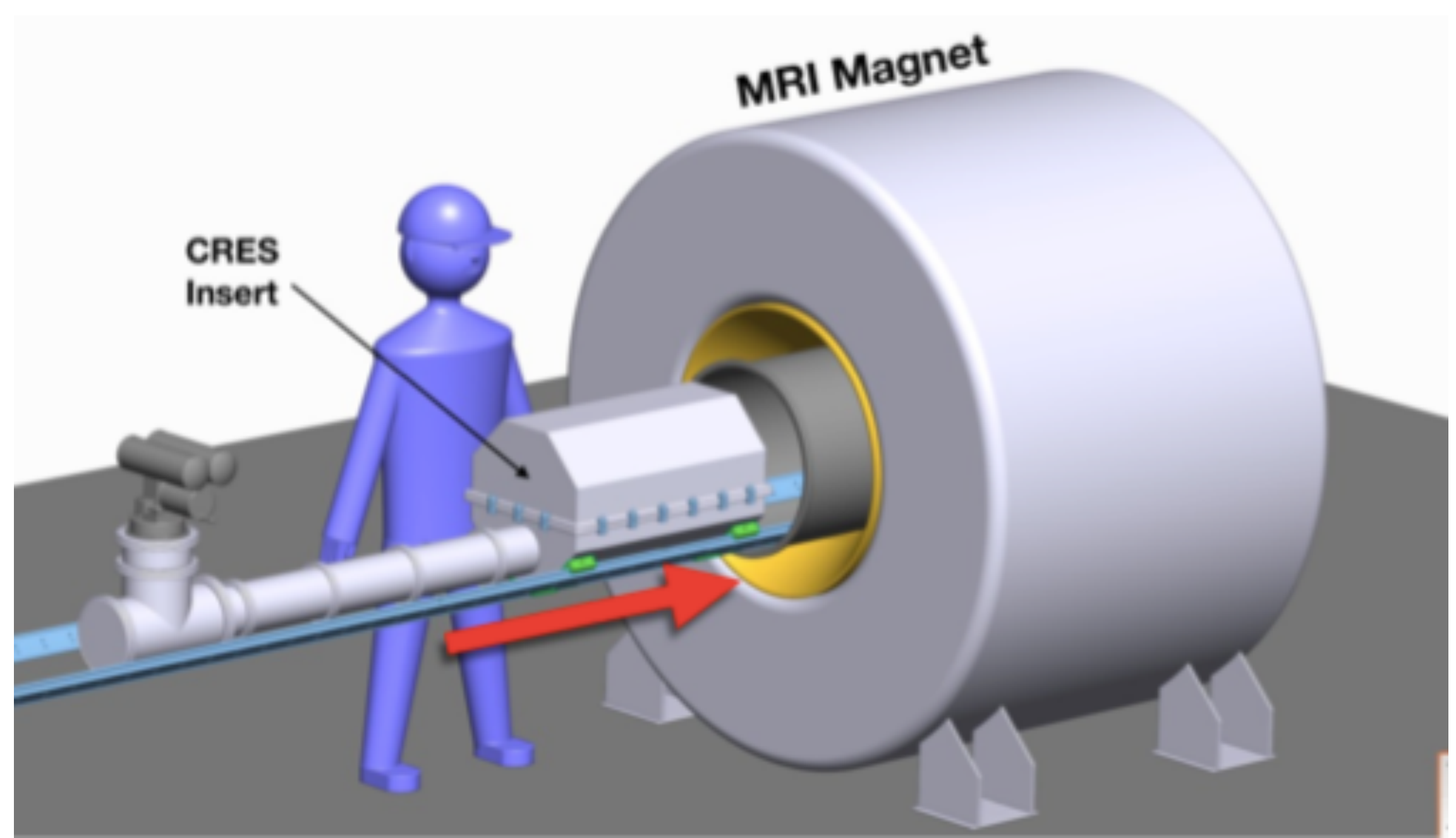
**Project 8, phase II**

**Tritium!**



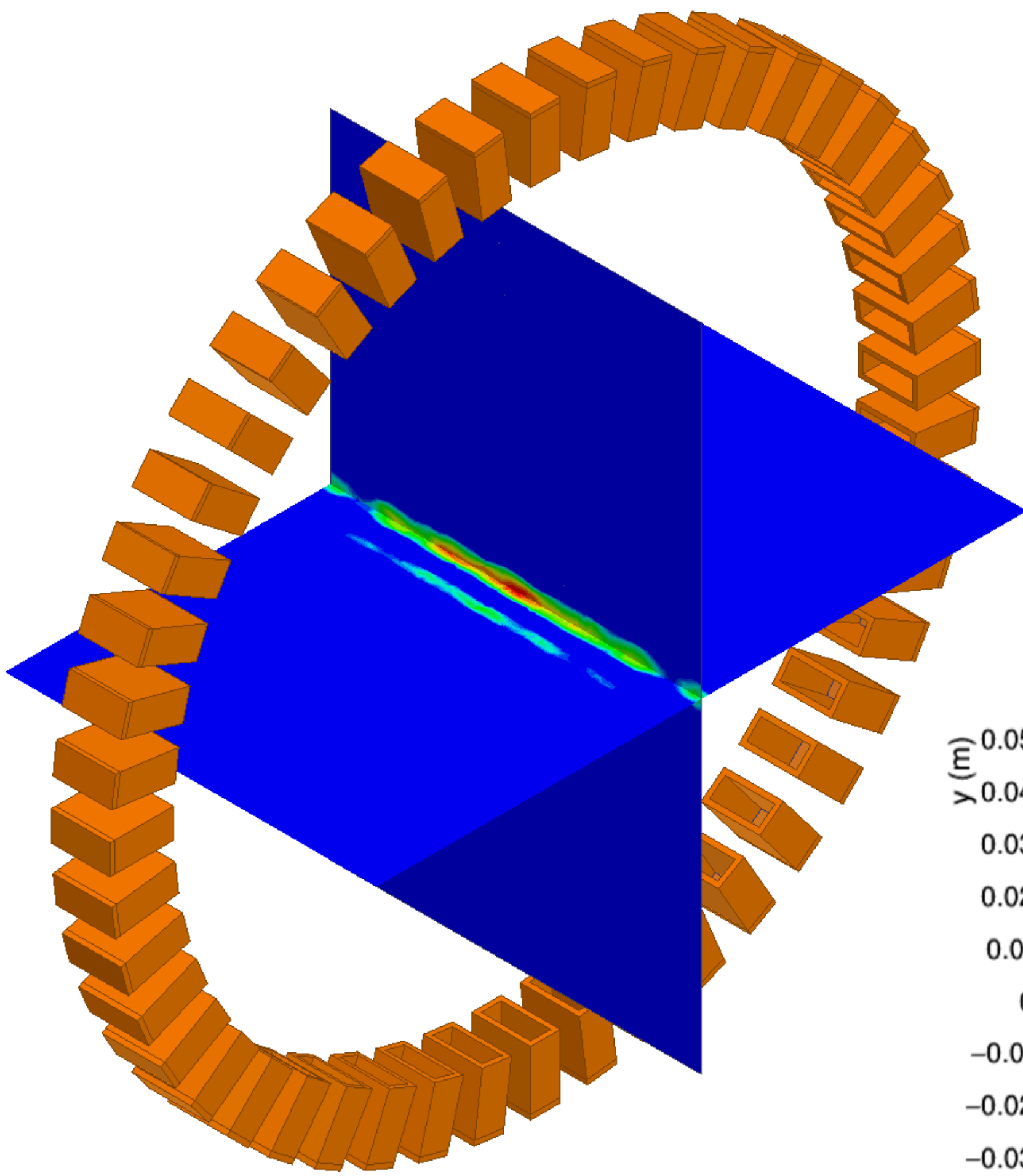


W Pettus, APS/JPS 2018, Waikoloa, HI

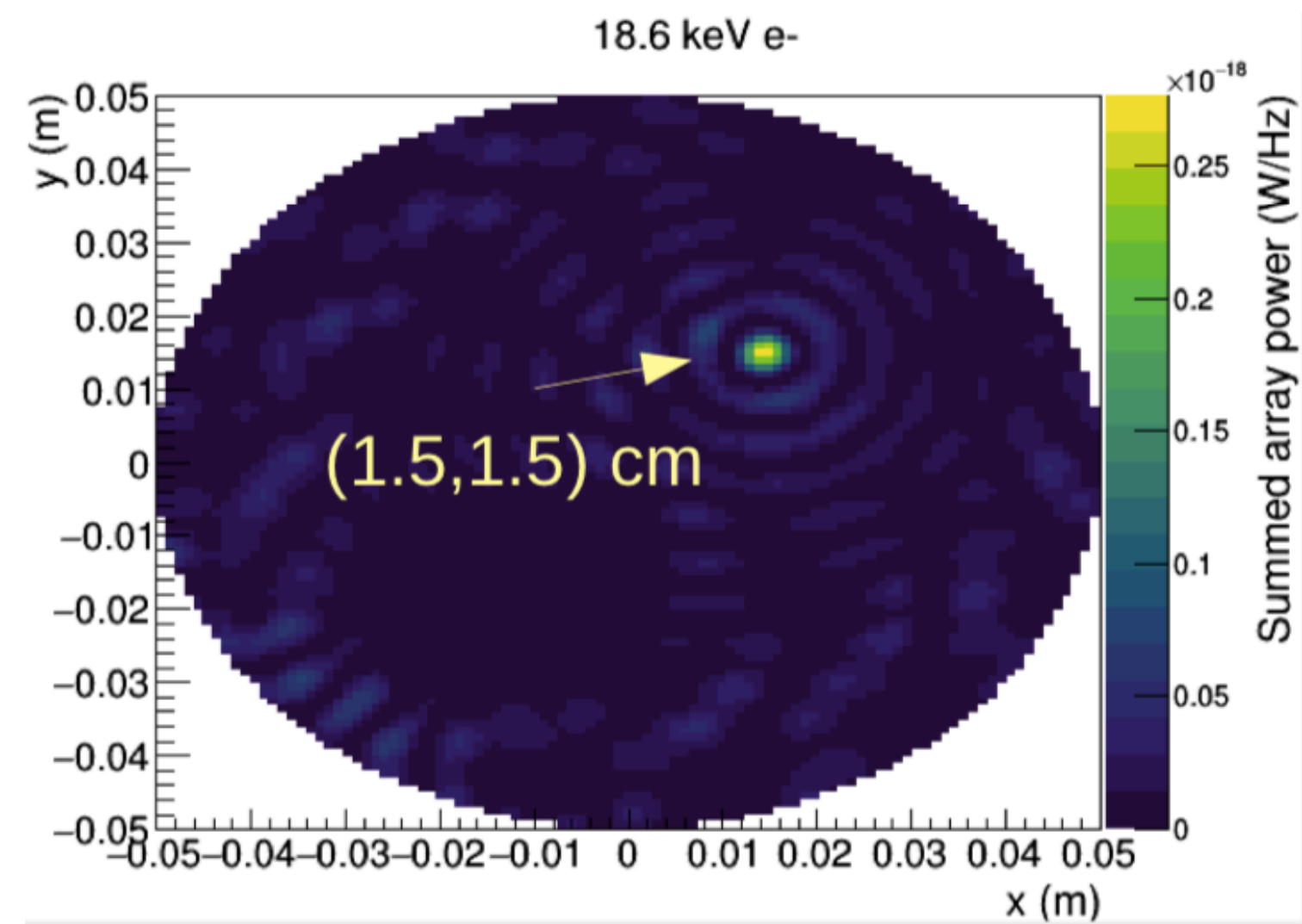


- **1 T** CRES field (MRI magnet)

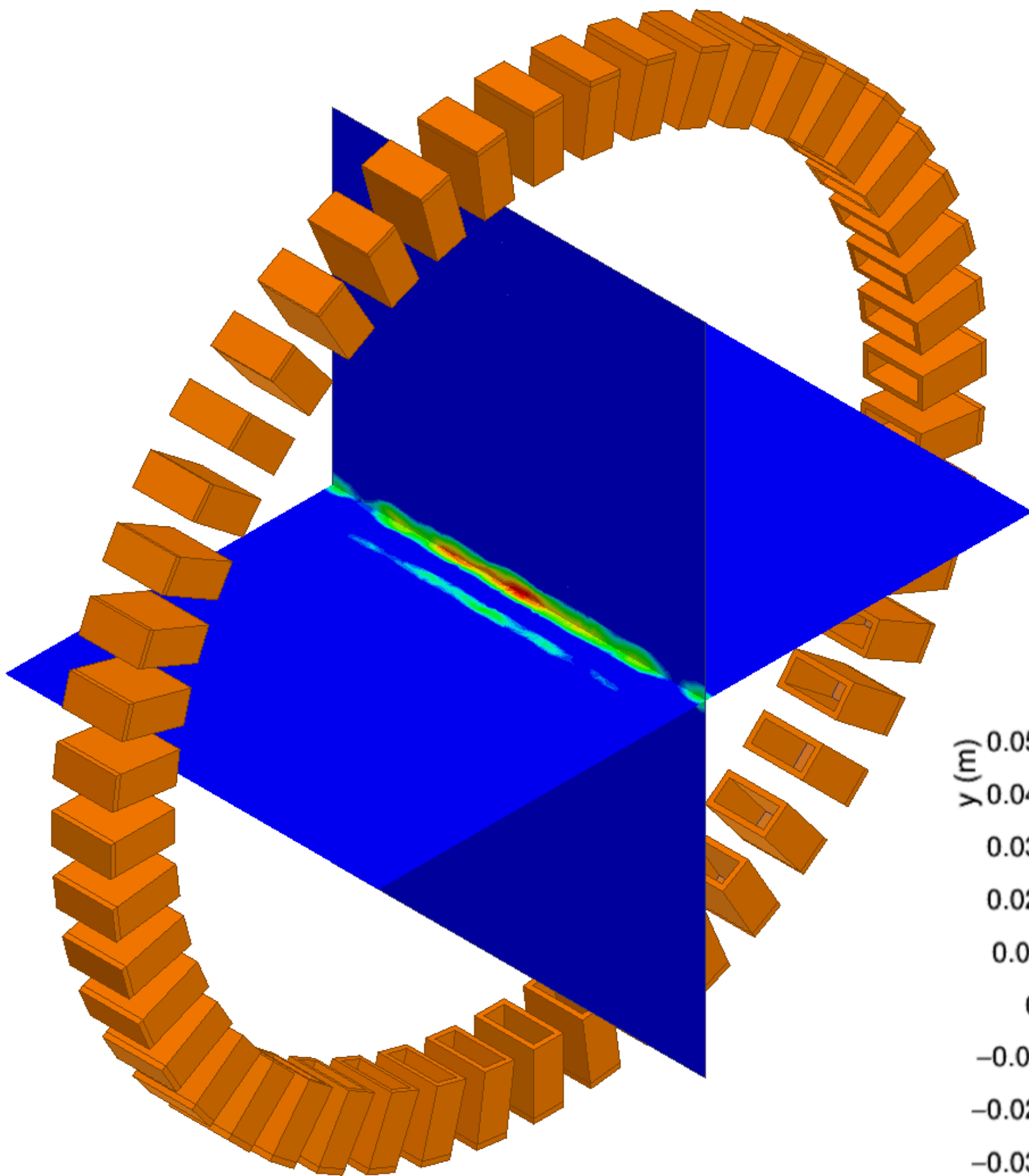
*P Slocum, APS/JPS 2018, Waikoloa, HI*



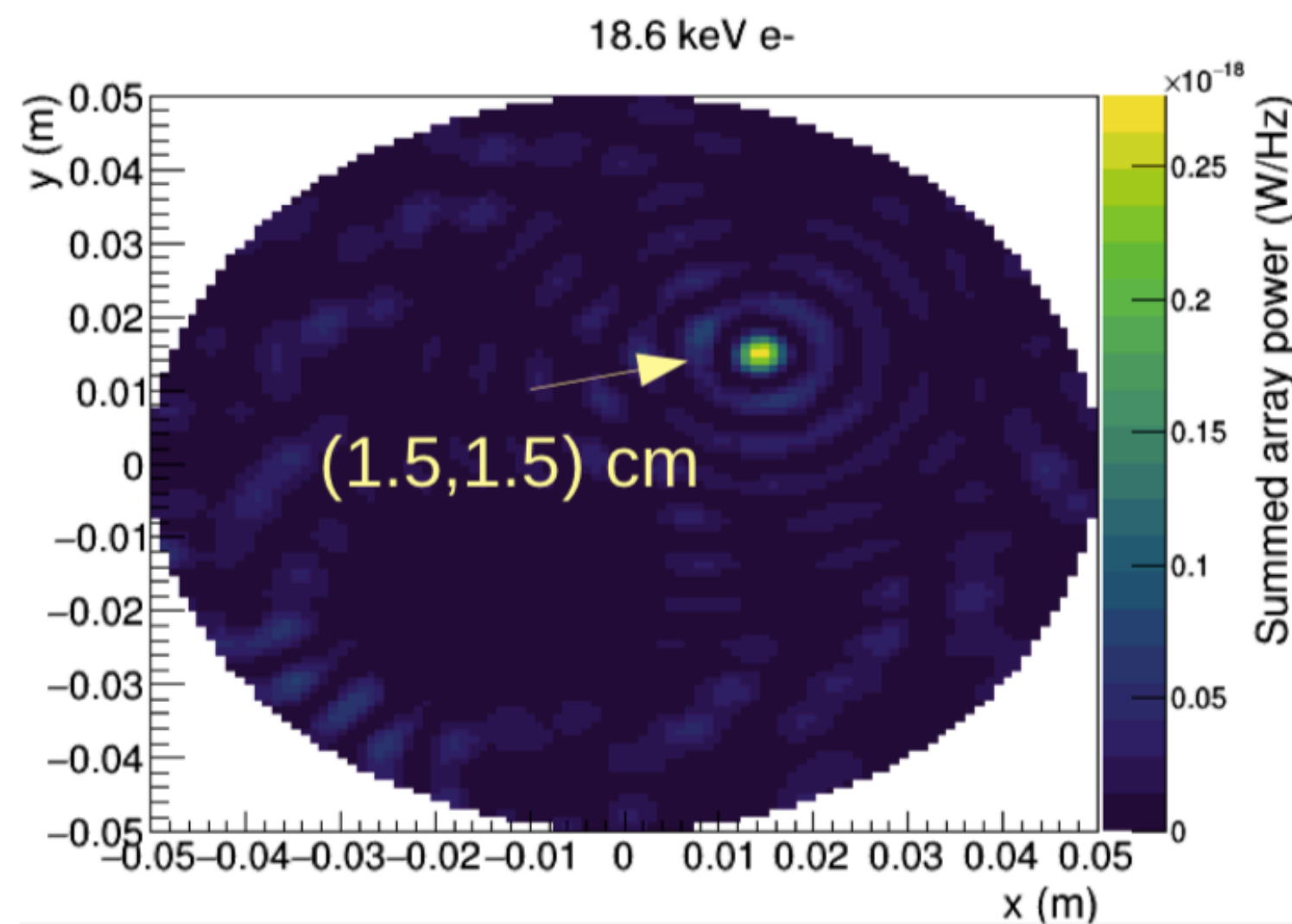
*P Slocum, APS/JPS 2018, Waikoloa, HI*



- **1 T** CRES field (MRI magnet)
- **200cm<sup>3</sup>** gas volume
  - No waveguide
  - Electrons radiate into free space
  - Phased array of waveguide antenna elements

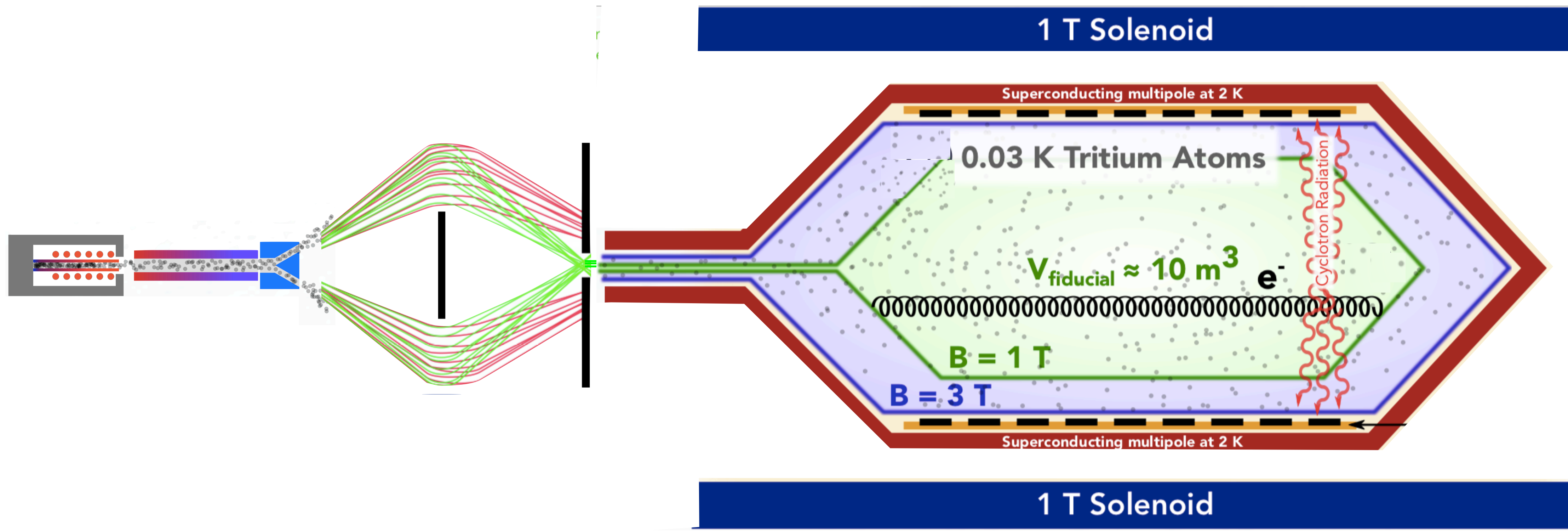


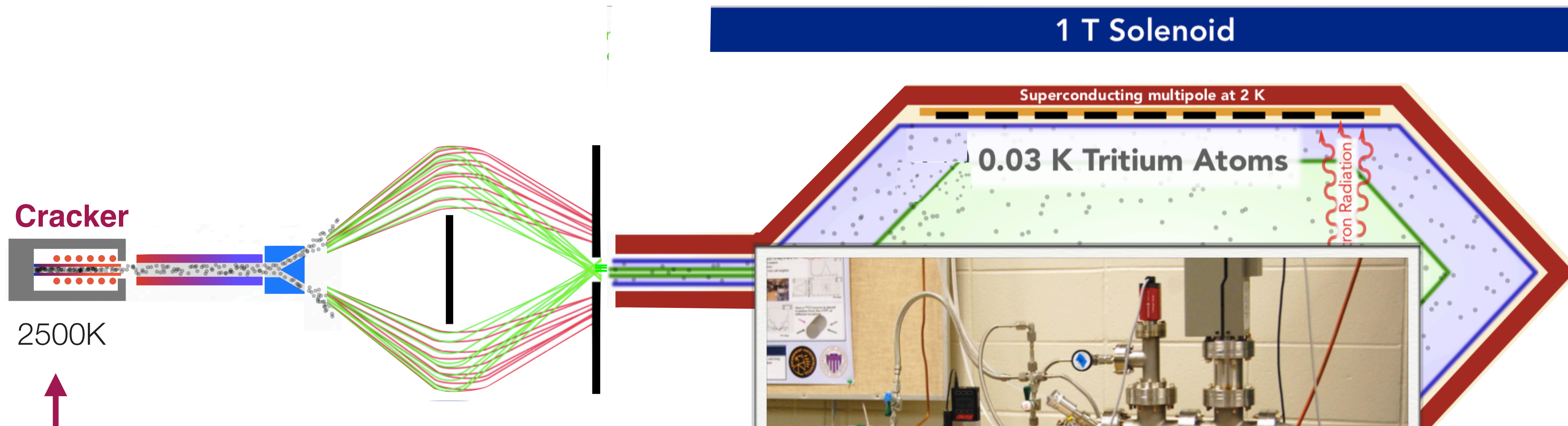
P Slocum, APS/JPS 2018, Waikoloa, HI



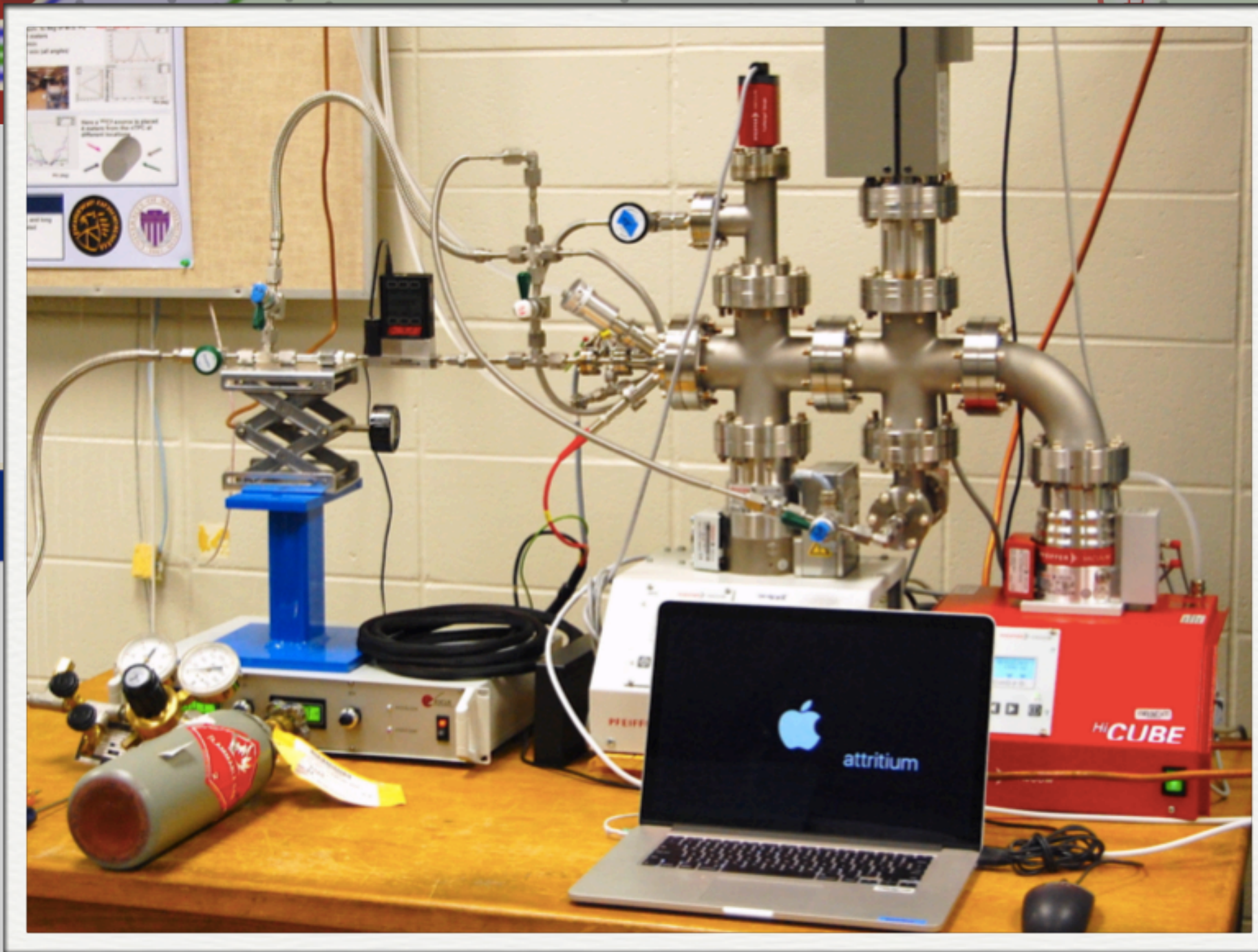
- **1 T** CRES field (MRI magnet)
- **200cm<sup>3</sup>** gas volume
  - No waveguide
  - Electrons radiate into free space
  - Phased array of waveguide antenna elements

- Electron energy resolution **1eV**
- Sensitivity  $m_\nu < 2 \text{ eV}$
- Efficiency **10%**



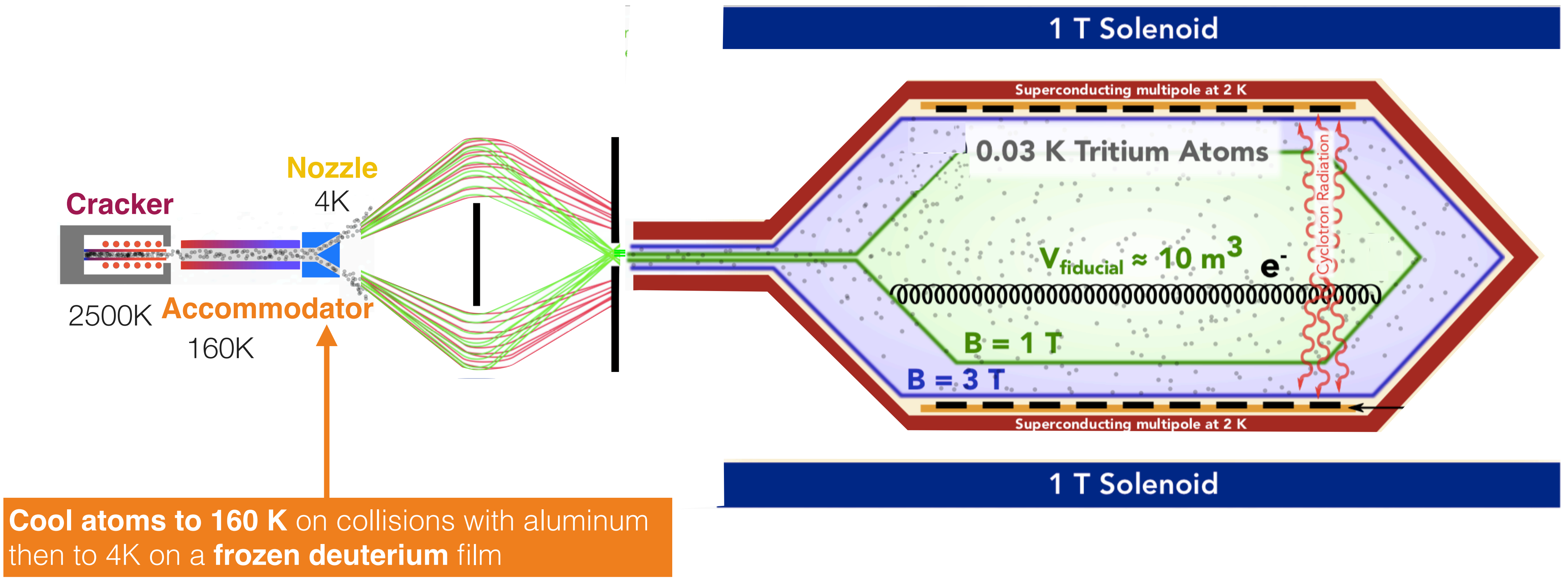


- **Disassociate** tritium gas into **atoms** in tungsten tube
- $10^{17}$  atoms / second
- Atomic fraction > 90%

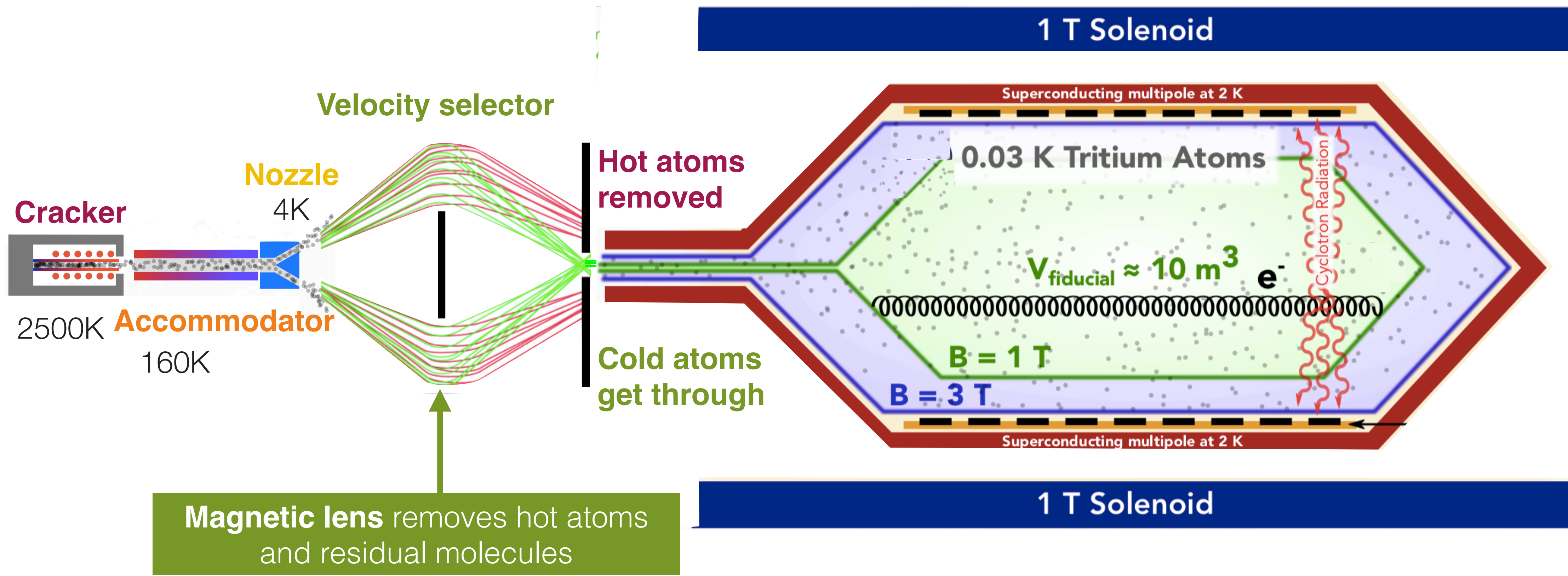


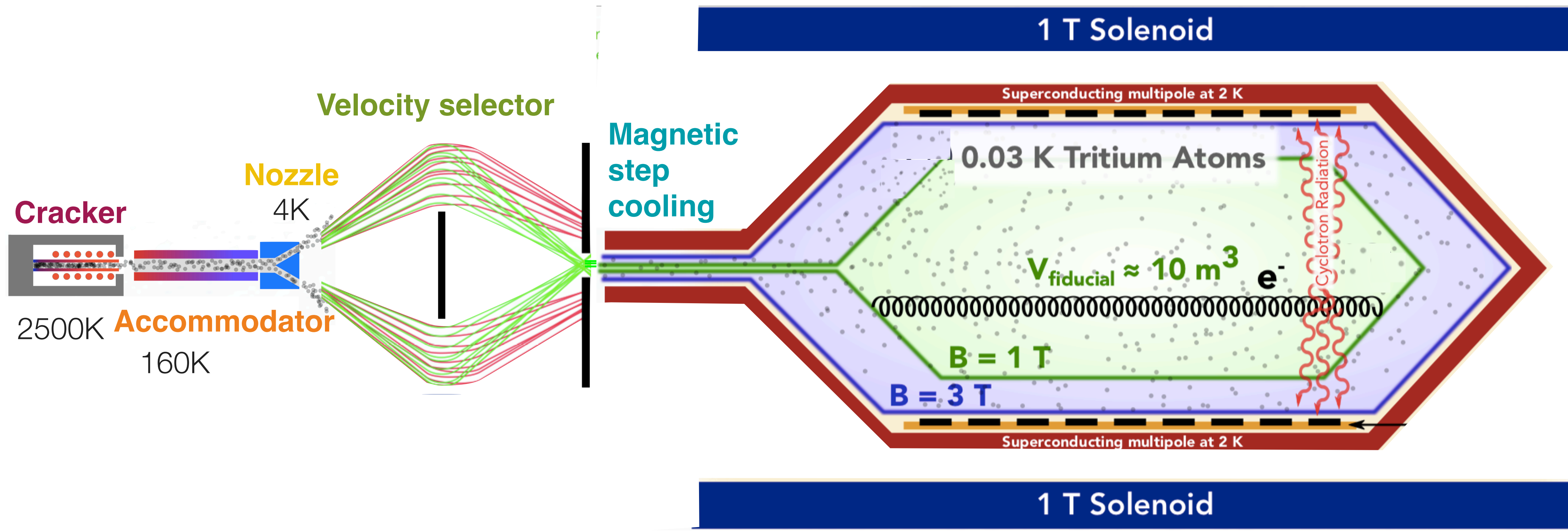
**Deuterium Cracker test stand**

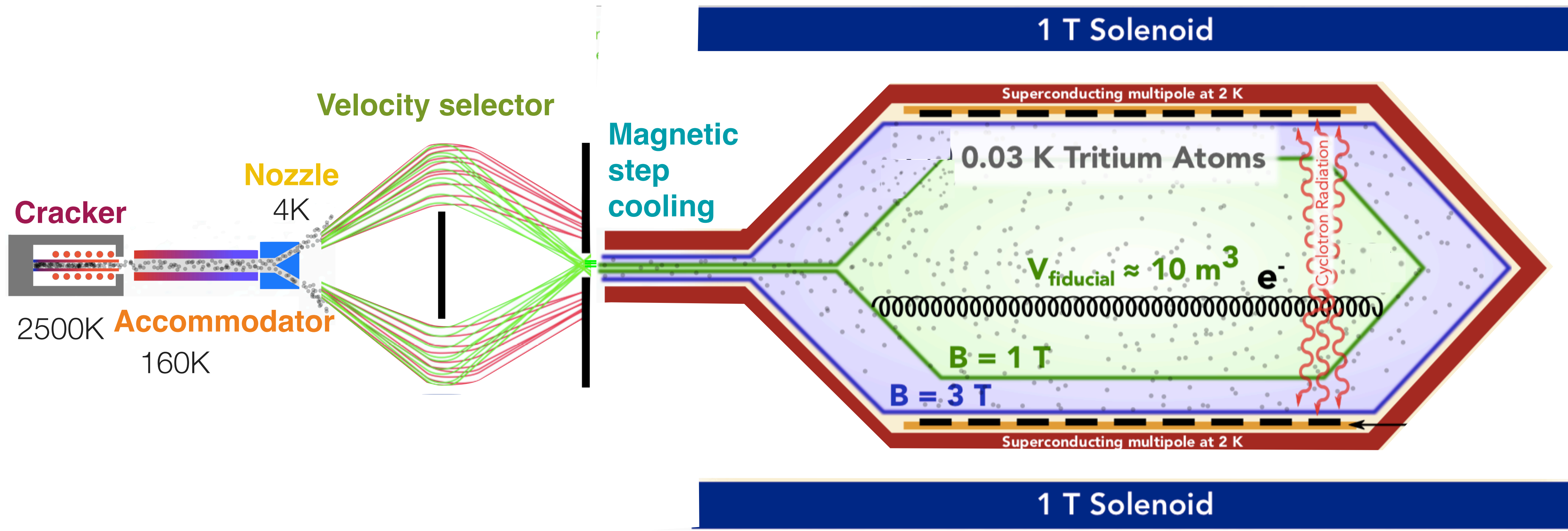




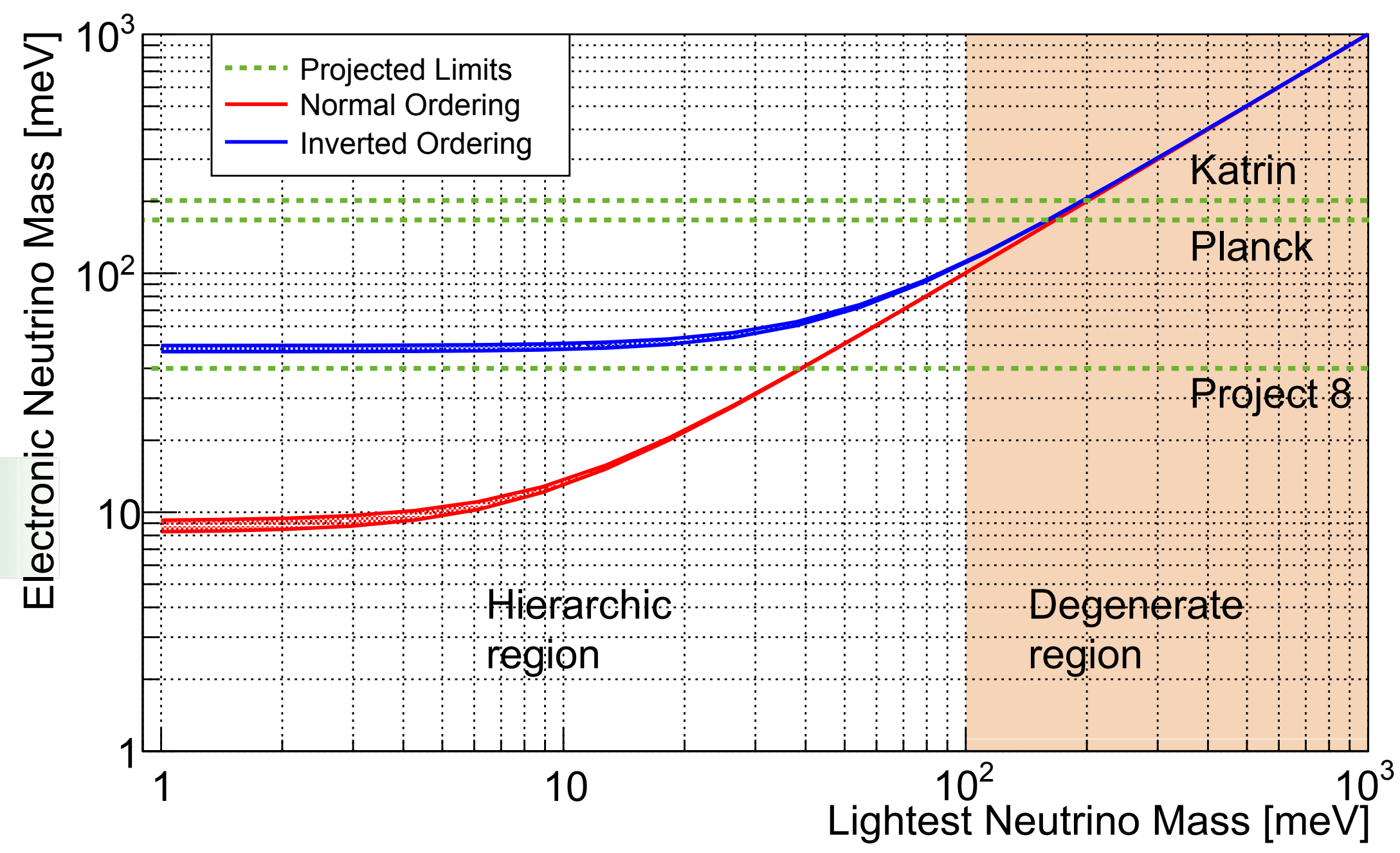
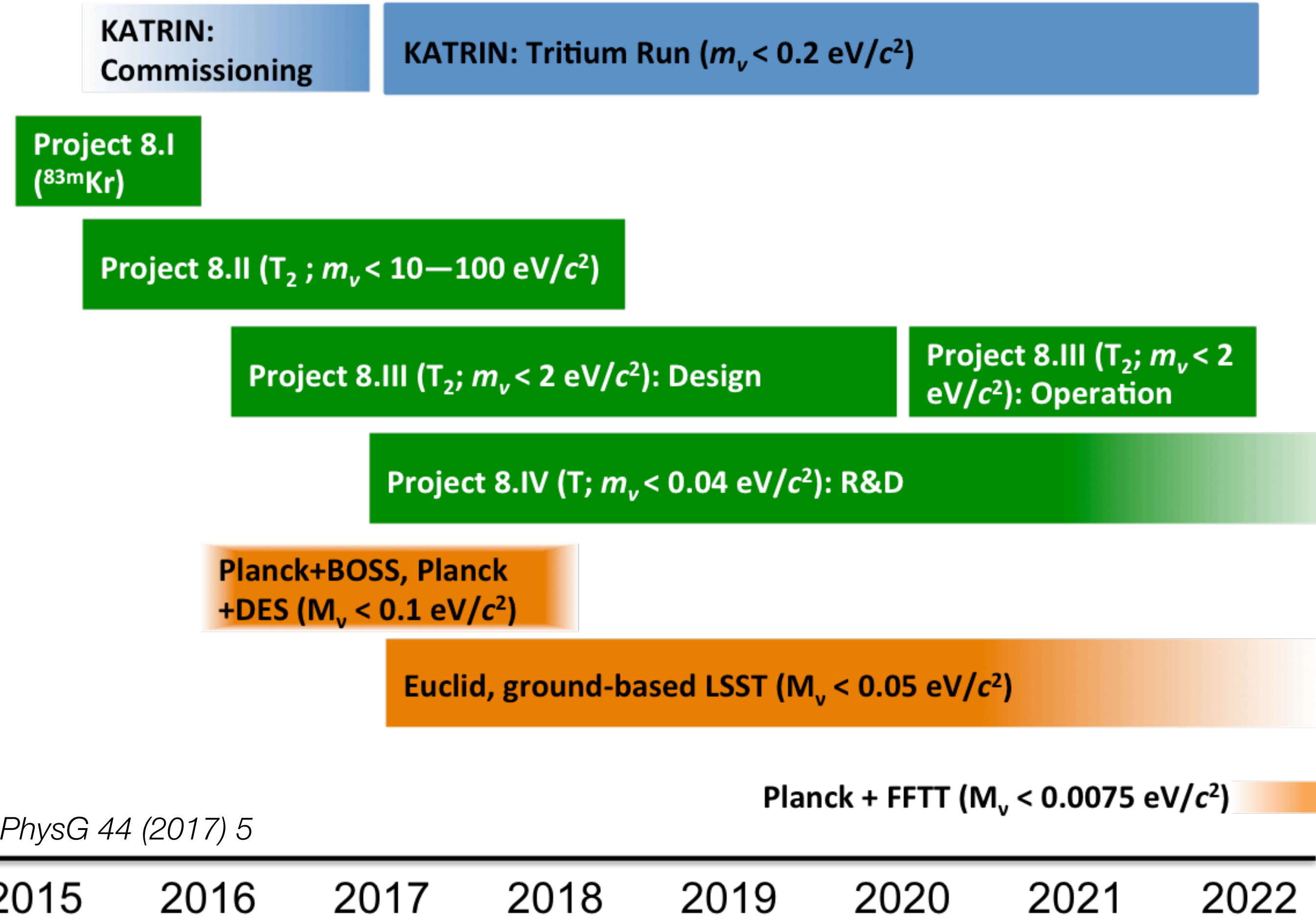
**Deuterium Cracker test stand**



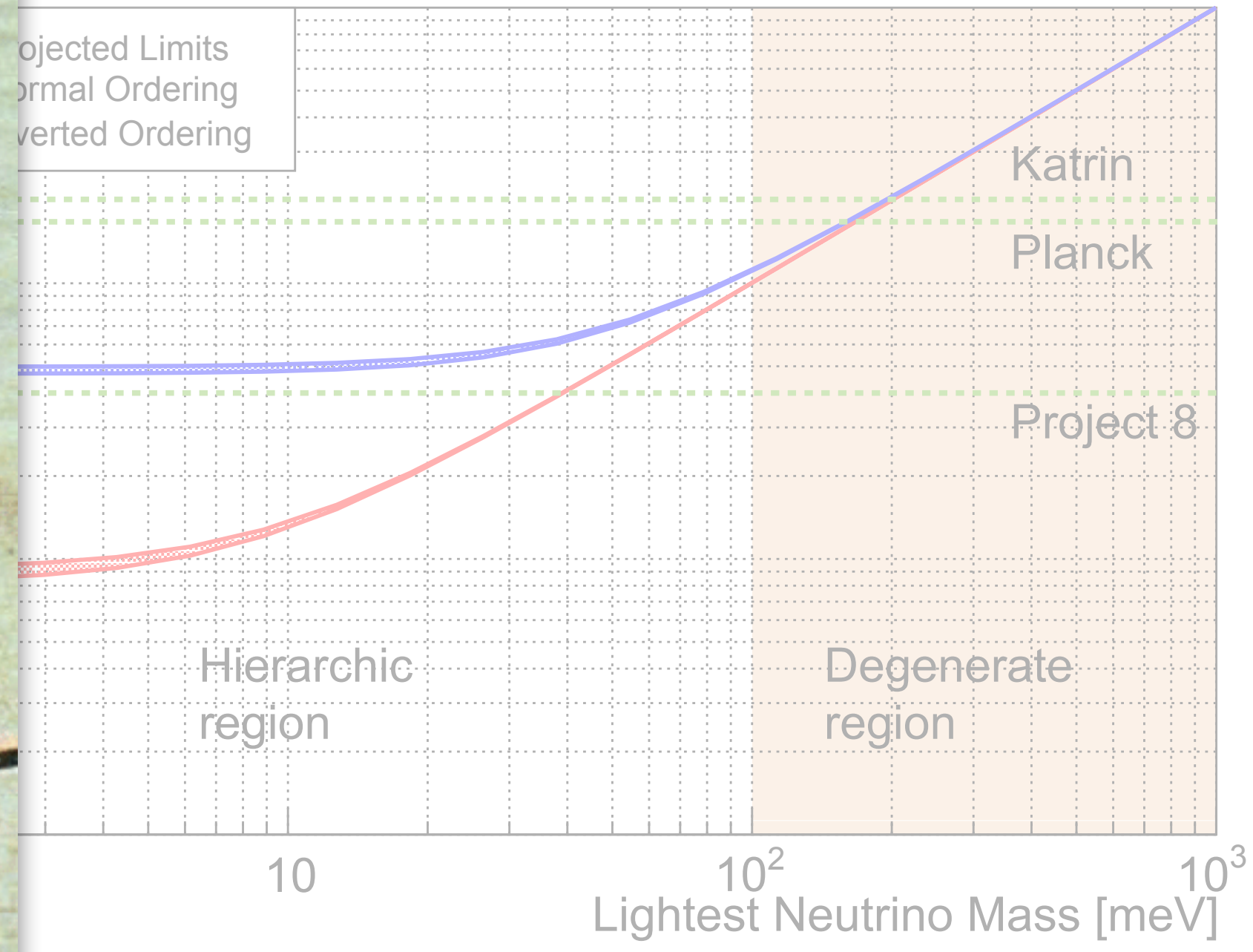
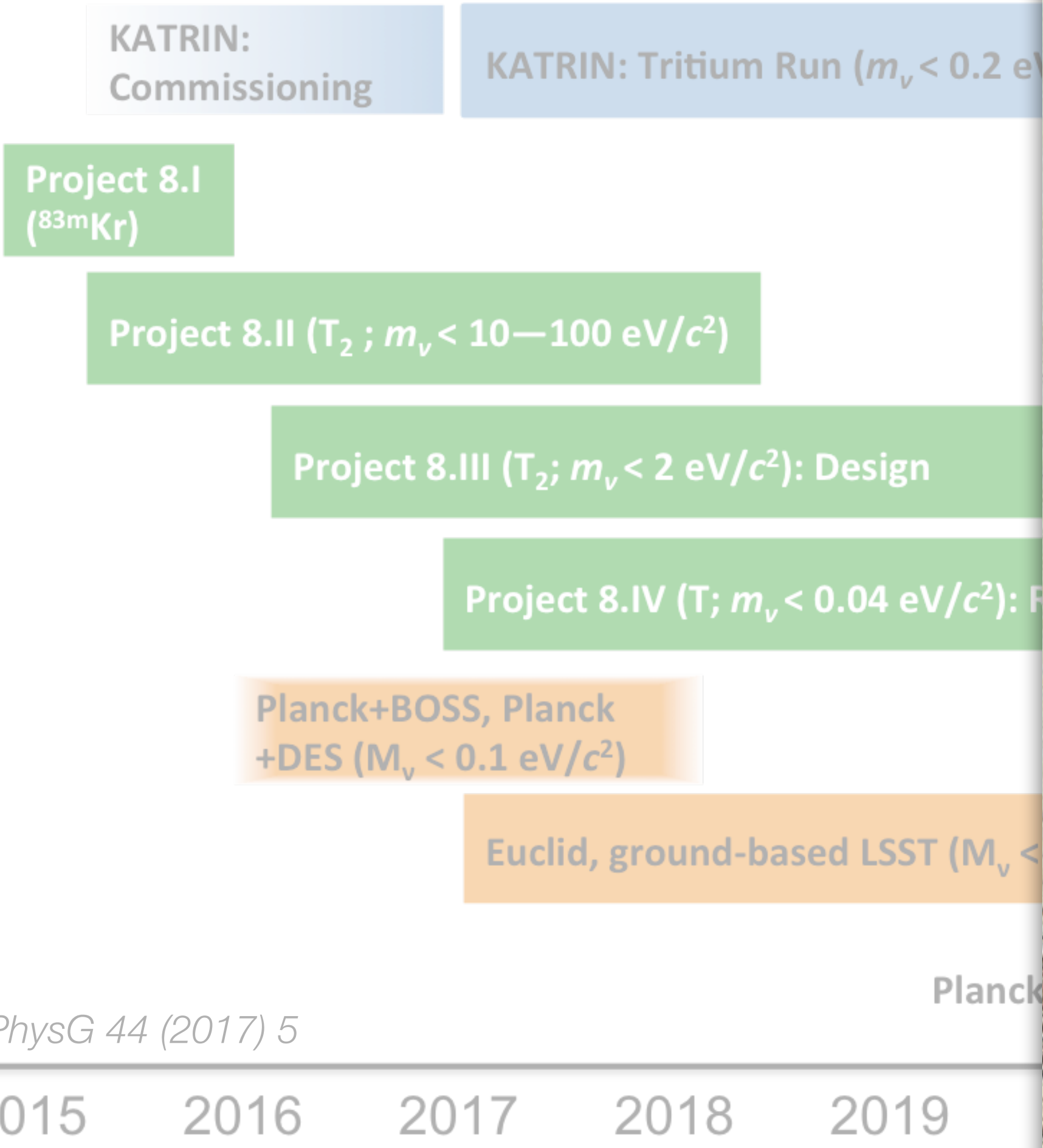
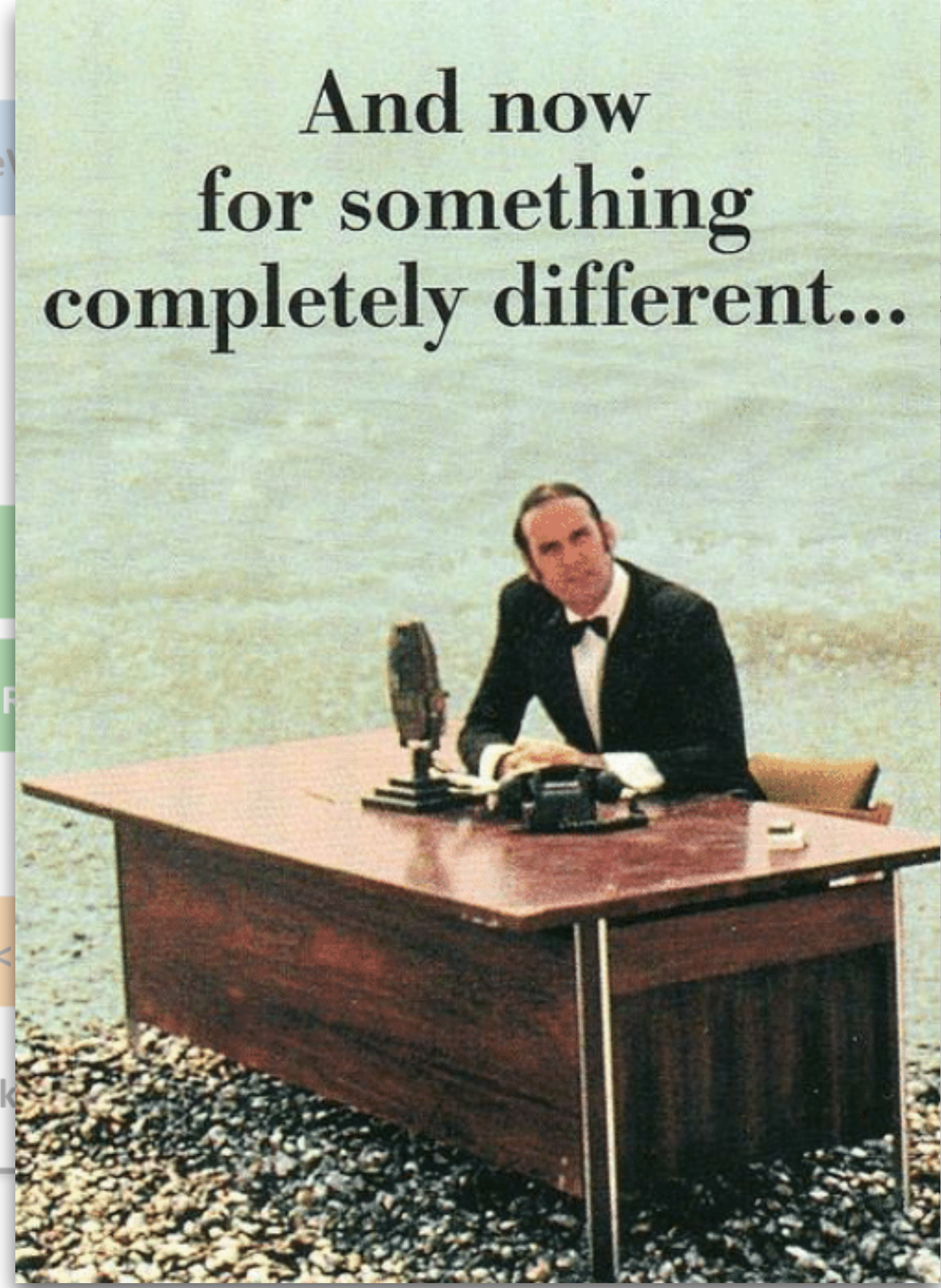




T atoms trapped in potential well (Ioffe trap) due to magnetic moment  
T<sub>2</sub> molecules freeze to walls



*JPhysG 44 (2017) 5*



*JPhysG 44 (2017) 5*

2015 2016 2017 2018 2019

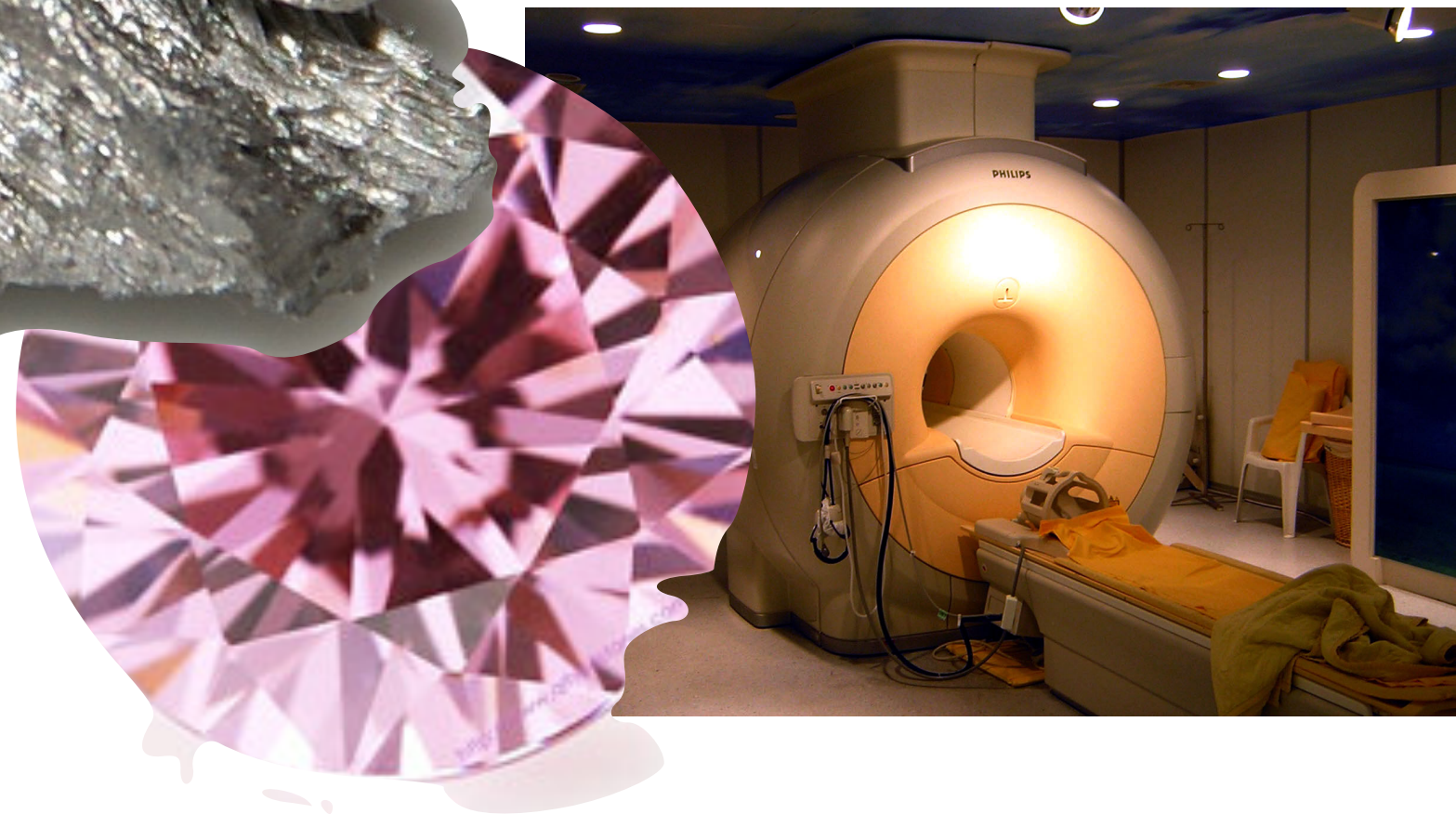


## What on Earth is holmium?



## What on Earth is holmium?

- Rare earth metal, with highest magnetic moment of all elements
- Named for the city Stockholm
- Used to colour cubic zirconia, in lasers, as a neutron absorber in nuclear reactors, and in MRI machines
- Only one natural, stable isotope,  $^{165}\text{Ho}$



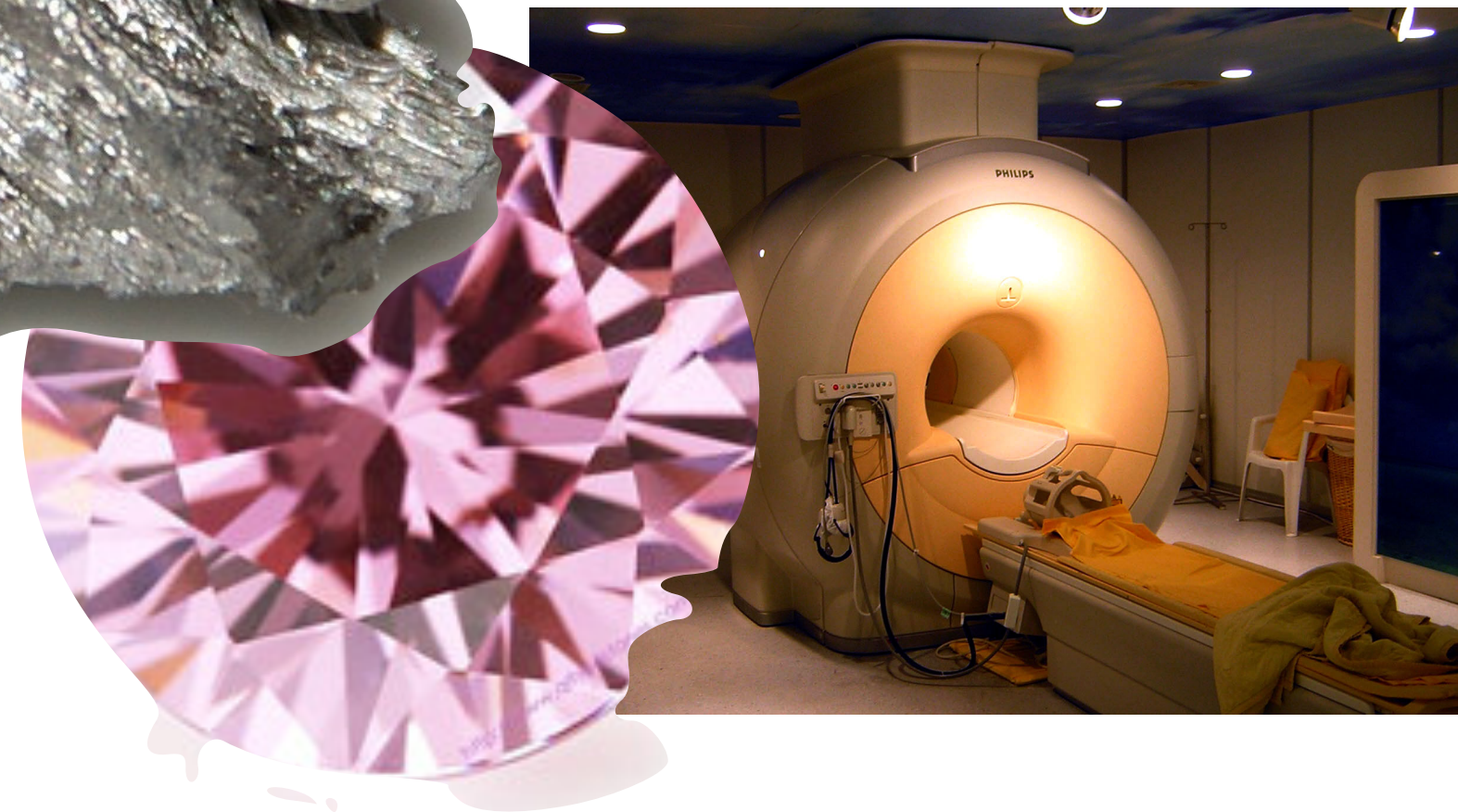
*Per Teodor Cleve discovered holmium*

1 H 1.008																	2 He 4.0026
3 Li 6.94	4 Be 9.0122											5 B 10.81	6 C 12.011	7 N 14.007	8 O 15.999	9 F 18.998	10 Ne 20.180
11 Na 22.990	12 Mg 24.305	13 Al 26.982	14 Si 28.085	15 P 30.974	16 S 32.06	17 Cl 35.45	18 Ar 39.948										
19 K 39.098	20 Ca 40.078	21 Sc 44.956	22 Ti 47.867	23 V 50.942	24 Cr 51.996	25 Mn 54.938	26 Fe 55.845	27 Co 58.933	28 Ni 58.693	29 Cu 63.546	30 Zn 65.38	31 Ga 69.723	32 Ge 72.630	33 As 74.922	34 Se 78.97	35 Br 79.904	36 Kr 83.798
37 Rb 85.468	38 Sr 87.62	39 Y 88.906	40 Zr 91.224	41 Nb 92.906	42 Mo 95.95	43 Tc (98)	44 Ru 101.07	45 Rh 102.91	46 Pd 106.42	47 Ag 107.87	48 Cd 112.41	49 In 114.82	50 Sn 118.71	51 Sb 121.76	52 Te 127.60	53 I 126.90	54 Xe 131.29
55 Cs 132.91	56 Ba 137.33	57-71 * #	72 Hf 178.49	73 Ta 180.95	74 W 183.84	75 Re 186.21	76 Os 190.23	77 Ir 192.22	78 Pt 195.08	79 Au 196.97	80 Hg 200.59	81 Tl 204.38	82 Pb 207.2	83 Bi 208.98	84 Po (209)	85 At (210)	86 Rn (222)
87 Fr (223)	88 Ra (226)	89-103 #	104 Rf (261)	105 Db (268)	106 Sg (271)	107 Bh (270)	108 Hs (277)	109 Mt (276)	110 Ds (281)	111 Rg (280)	112 Cn (285)	113 Nh (286)	114 Fl (289)	115 Mc (289)	116 Lv (293)	117 Ts (294)	118 Og (294)
* Lanthanide series			57 La 138.91	58 Ce 140.12	59 Pr 140.91	60 Nd 144.24	61 Pm (145)	62 Sm 150.36	63 Eu 151.96	64 Gd 157.25	65 Tb 158.93	66 Dy 162.50	67 Ho 164.93	68 Er 167.26	69 Tm 168.93	70 Yb 173.05	71 Lu 174.967
# Actinide series			89 Ac (227)	90 Th 232.04	91 Pa 231.04	92 U 238.03	93 Np (237)	94 Pu (244)	95 Am (243)	96 Cm (247)	97 Bk (247)	98 Cf (251)	99 Es (252)	100 Fm (257)	101 Md (258)	102 No (259)	103 Lr (262)

67  
**Ho**  
164.93

## What on Earth is holmium?

- Rare earth metal, with highest magnetic moment of all elements
- Named for the city Stockholm
- Used to colour cubic zirconia, in lasers, as a neutron absorber in nuclear reactors, and in MRI machines
- Only one natural, stable isotope,  $^{165}\text{Ho}$



*Per Teodor Cleve discovered holmium*

1 H 1.008																	2 He 4.0026
3 Li 6.94	4 Be 9.0122											5 B 10.81	6 C 12.011	7 N 14.007	8 O 15.999	9 F 18.998	10 Ne 20.180
11 Na 22.990	12 Mg 24.305	3	4	5	6	7	8	9	10	11	12	13 Al 26.982	14 Si 28.085	15 P 30.974	16 S 32.06	17 Cl 35.45	18 Ar 39.948
19 K 39.098	20 Ca 40.078	21 Sc 44.956	22 Ti 47.867	23 V 50.942	24 Cr 51.996	25 Mn 54.938	26 Fe 55.845	27 Co 58.933	28 Ni 58.693	29 Cu 63.546	30 Zn 65.38	31 Ga 69.723	32 Ge 72.630	33 As 74.922	34 Se 78.97	35 Br 79.904	36 Kr 83.798
37 Rb 85.468	38 Sr 87.62	39 Y 88.906	40 Zr 91.224	41 Nb 92.906	42 Mo 95.95	43 Tc (98)	44 Ru 101.07	45 Rh 102.91	46 Pd 106.42	47 Ag 107.87	48 Cd 112.41	49 In 114.82	50 Sn 118.71	51 Sb 121.76	52 Te 127.60	53 I 126.90	54 Xe 131.29
55 Cs 132.91	56 Ba 137.33	57-71 * #	72 Hf 178.49	73 Ta 180.95	74 W 183.84	75 Re 186.21	76 Os 190.23	77 Ir 192.22	78 Pt 195.08	79 Au 196.97	80 Hg 200.59	81 Tl 204.38	82 Pb 207.2	83 Bi 208.98	84 Po (209)	85 At (210)	86 Rn (222)
87 Fr (223)	88 Ra (226)	89-103 #	104 Rf (261)	105 Db (268)	106 Sg (271)	107 Bh (270)	108 Hs (277)	109 Mt (276)	110 Ds (281)	111 Rg (280)	112 Cn (285)	113 Nh (286)	114 Fl (289)	115 Mc (289)	116 Lv (293)	117 Ts (294)	118 Og (294)
* Lanthanide series			57 La 138.91	58 Ce 140.12	59 Pr 140.91	60 Nd 144.24	61 Pm (145)	62 Sm 150.36	63 Eu 151.96	64 Gd 157.25	65 Tb 158.93	66 Dy 162.50	67 Ho 164.93	68 Er 167.26	69 Tm 168.93	70 Yb 173.05	71 Lu 174.967
# Actinide series			89 Ac (227)	90 Th 232.04	91 Pa 231.04	92 U 238.03	93 Np (237)	94 Pu (244)	95 Am (243)	96 Cm (247)	97 Bk (247)	98 Cf (251)	99 Es (252)	100 Fm (257)	101 Md (258)	102 No (259)	103 Lr (262)

67  
Ho  
164.93

$^{163}\text{Ho}$  decays via electron capture to  $^{163}\text{Dy}$  with half-life 4570 years



**Álvaro de Rújula**

“The relation between experimentalists and theorists is often one of healthy competition for truth and less healthy competition for fame.”

“Science is what we do when we don't know what we're doing.”



Álvaro de Rújula

**The proximity of the spectral endpoint to an atomic resonance makes the fraction of events that are sensitive to a non-zero neutrino mass superior in**

**$^{163}\text{Ho}$  decay than in tritium decay.** *Physics Letters B Volume 118, Issues 4–6, 9 December 1982, Pages 429-434*

“The relation between experimentalists and theorists is often one of healthy competition for truth and less healthy competition for fame.”

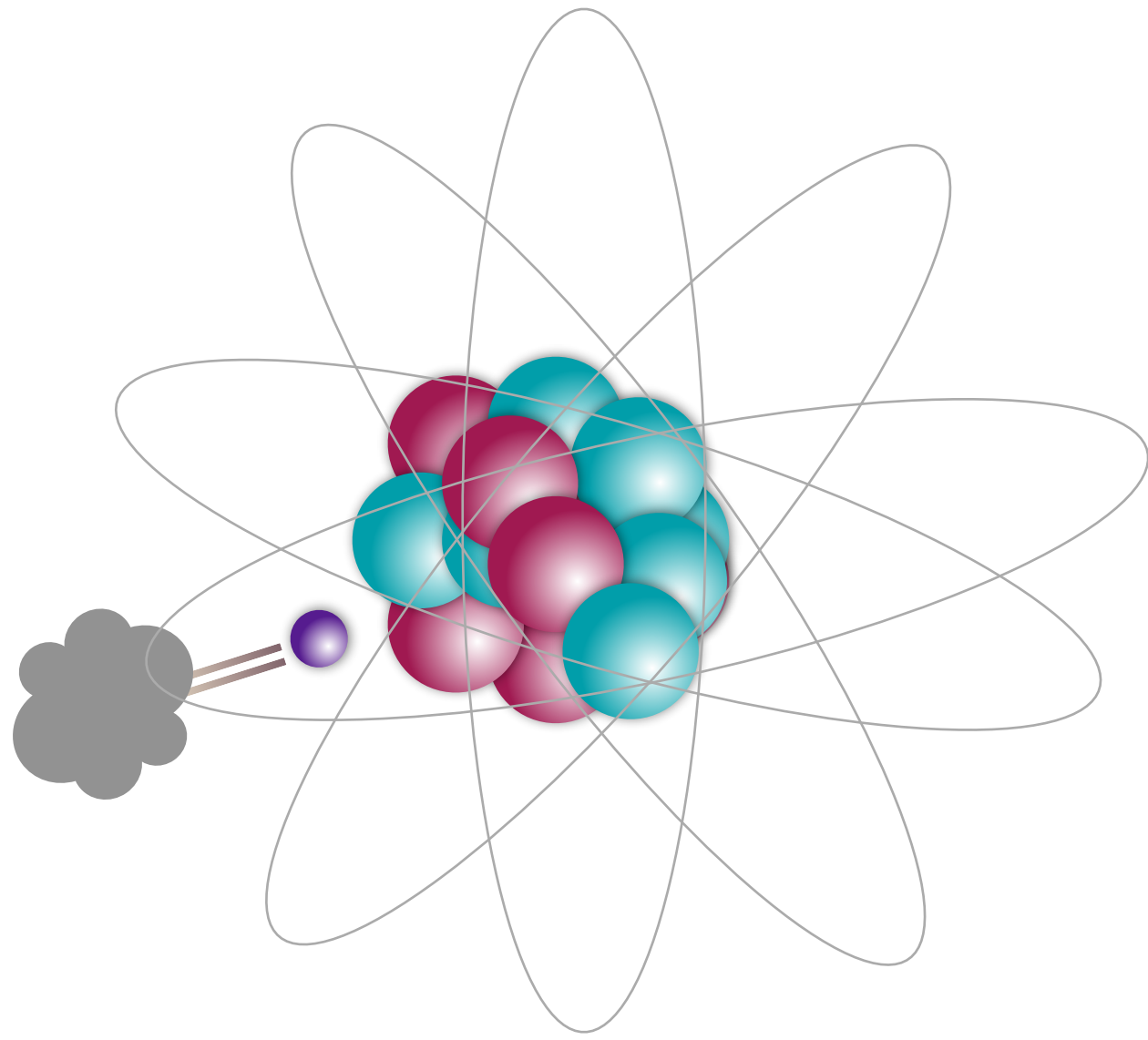
“Science is what we do when we don't know what we're doing.”

The proximity of the spectral endpoint to an atomic resonance makes the fraction of events that are sensitive to a non-zero neutrino mass superior in

$^{163}\text{Ho}$  decay than in tritium decay. *Physics Letters B Volume 118, Issues 4–6, 9 December 1982, Pages 429-434*



**Lowest known Q-value  
(c.f. tritium 18.6 keV)**

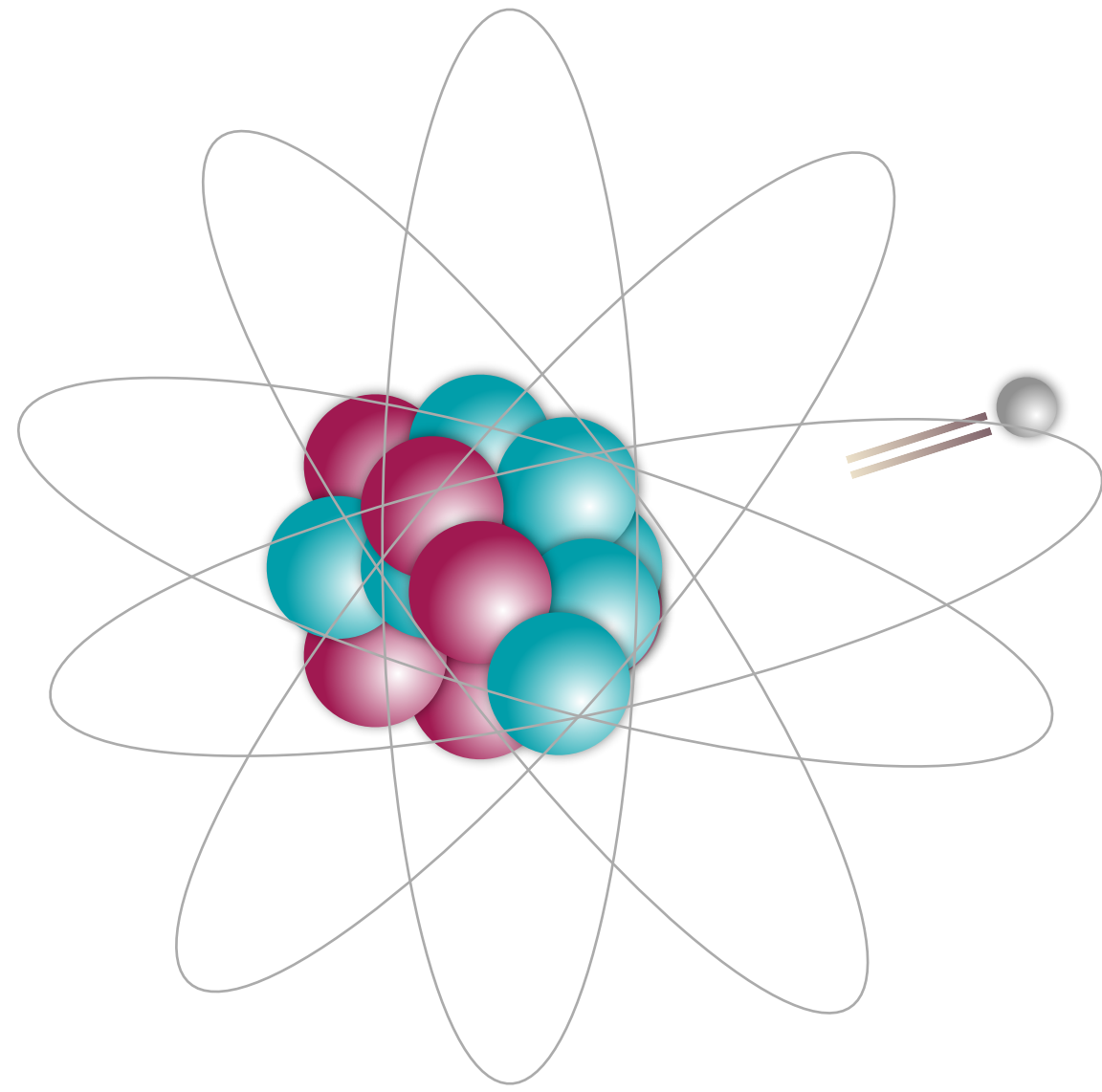


The proximity of the spectral endpoint to an atomic resonance makes the fraction of events that are sensitive to a non-zero neutrino mass superior in

$^{163}\text{Ho}$  decay than in tritium decay. *Physics Letters B* Volume 118, Issues 4–6, 9 December 1982, Pages 429-434



**Lowest known Q-value  
(c.f. tritium 18.6 keV)**

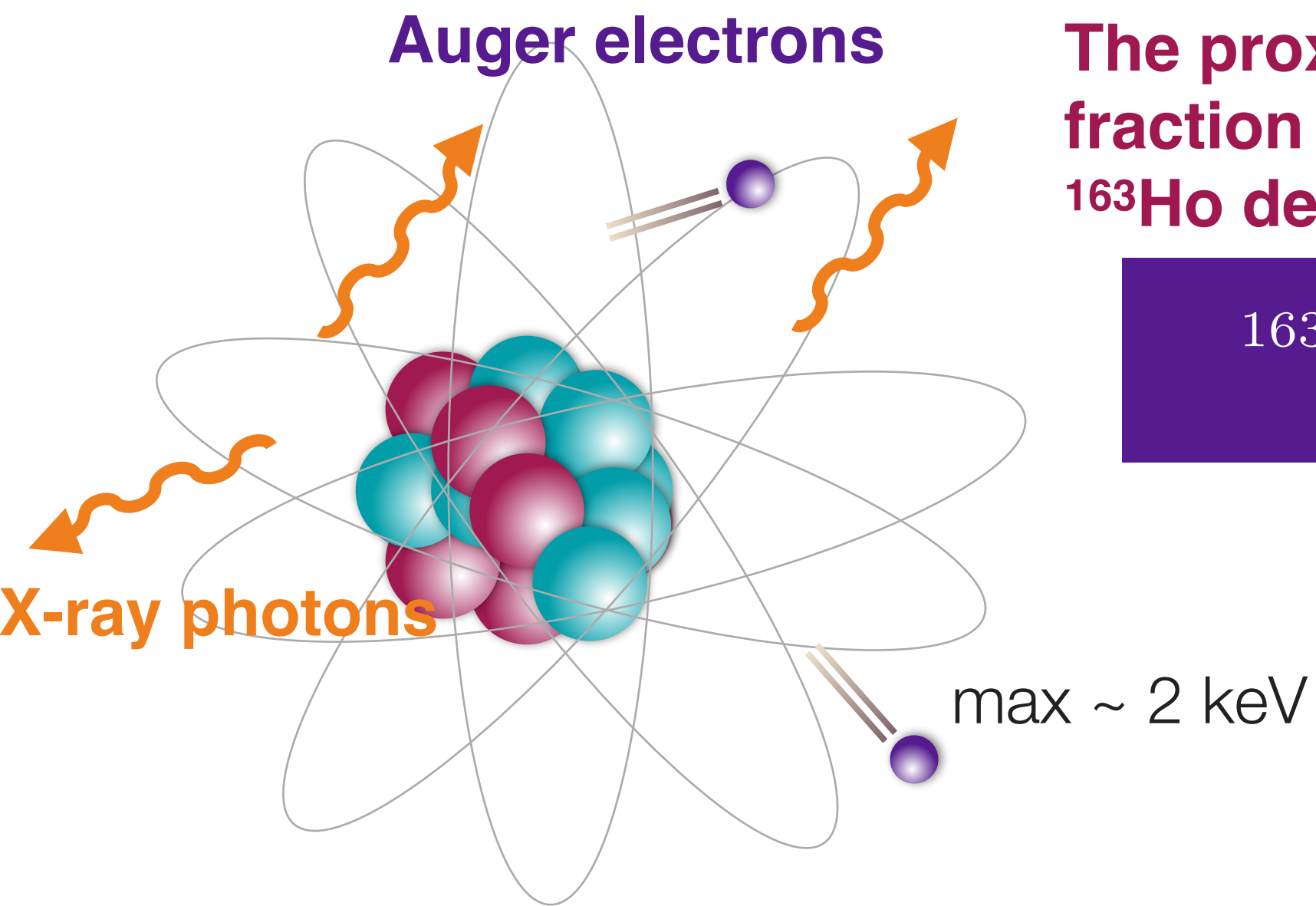


The proximity of the spectral endpoint to an atomic resonance makes the fraction of events that are sensitive to a non-zero neutrino mass superior in

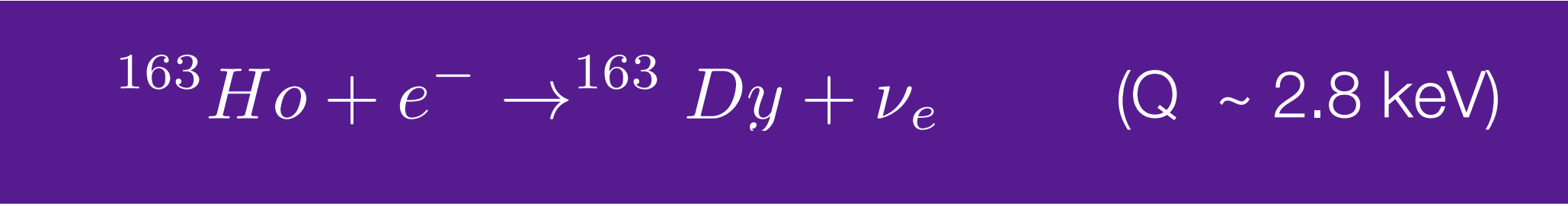
**$^{163}\text{Ho}$  decay than in tritium decay.** *Physics Letters B Volume 118, Issues 4–6, 9 December 1982, Pages 429-434*



**Lowest known Q-value  
(c.f. tritium 18.6 keV)**

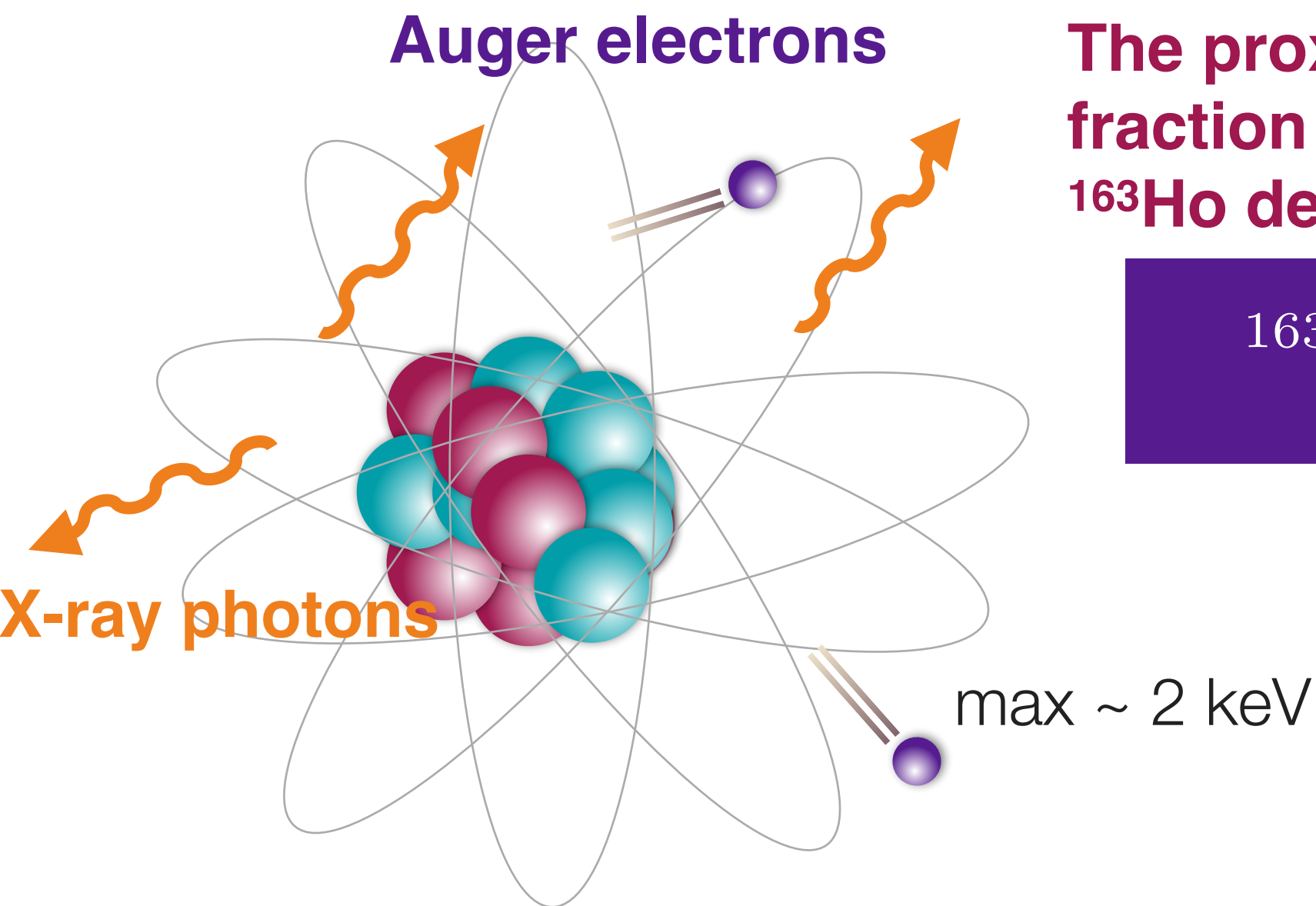


The proximity of the spectral endpoint to an atomic resonance makes the fraction of events that are sensitive to a non-zero neutrino mass superior in  $^{163}\text{Ho}$  decay than in tritium decay. *Physics Letters B Volume 118, Issues 4–6, 9 December 1982, Pages 429-434*

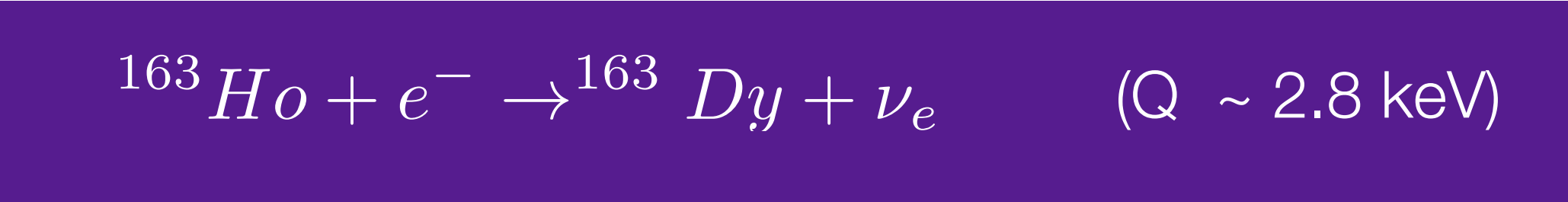


Lowest known Q-value  
(c.f. tritium 18.6 keV)





The proximity of the spectral endpoint to an atomic resonance makes the fraction of events that are sensitive to a non-zero neutrino mass superior in  $^{163}\text{Ho}$  decay than in tritium decay. *Physics Letters B* Volume 118, Issues 4–6, 9 December 1982, Pages 429-434



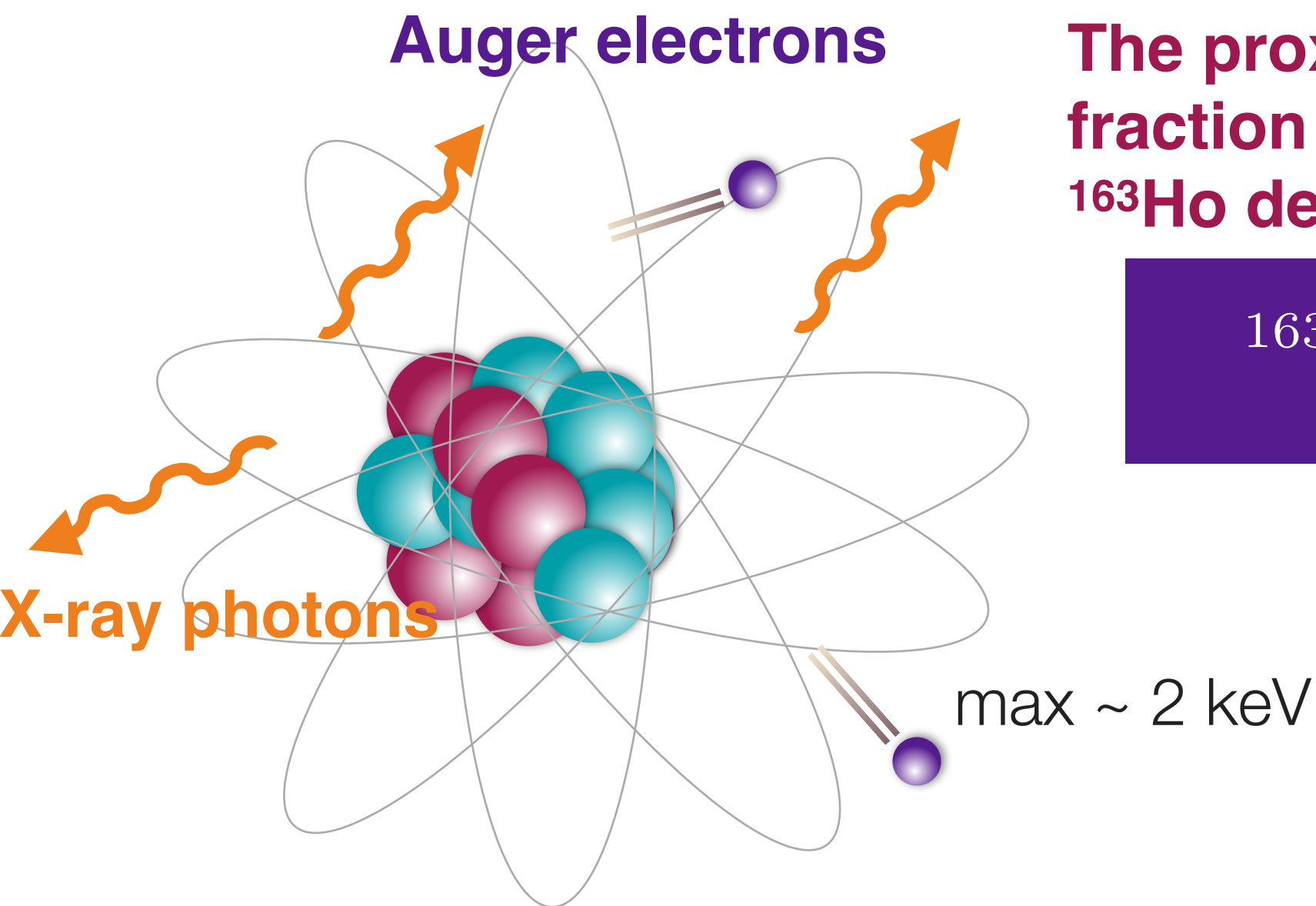
Lowest known Q-value  
(c.f. tritium 18.6 keV)

Total calorimetric energy

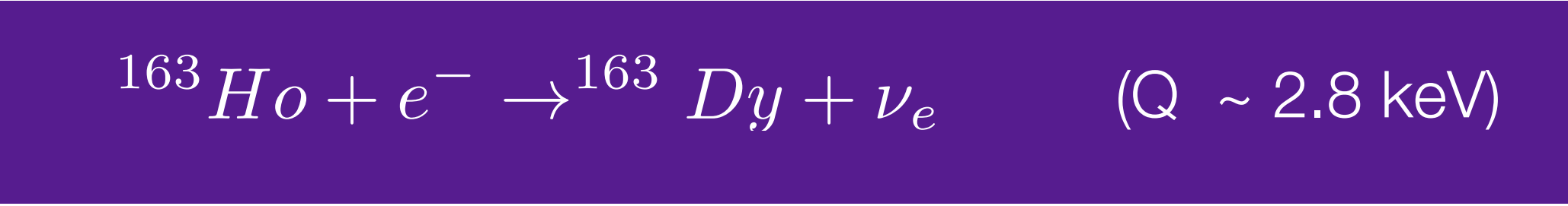
Energy spectrum  $\frac{d\lambda_{EC}}{dE_c} = \frac{G_\beta^2}{4\pi^2} (Q - E_c) \sqrt{(Q - E_c)^2 - m_\nu^2}$

$$\times \sum_i n_i C_i \beta_i^2 B_i \frac{\Gamma_i}{2\pi} \frac{1}{(E_c - E_i)^2 + \Gamma_i^2/4}$$

*Eur Phys J C Part Fields.* 2015; 75(3): 112



The proximity of the spectral endpoint to an atomic resonance makes the fraction of events that are sensitive to a non-zero neutrino mass superior in  $^{163}\text{Ho}$  decay than in tritium decay. *Physics Letters B Volume 118, Issues 4–6, 9 December 1982, Pages 429-434*

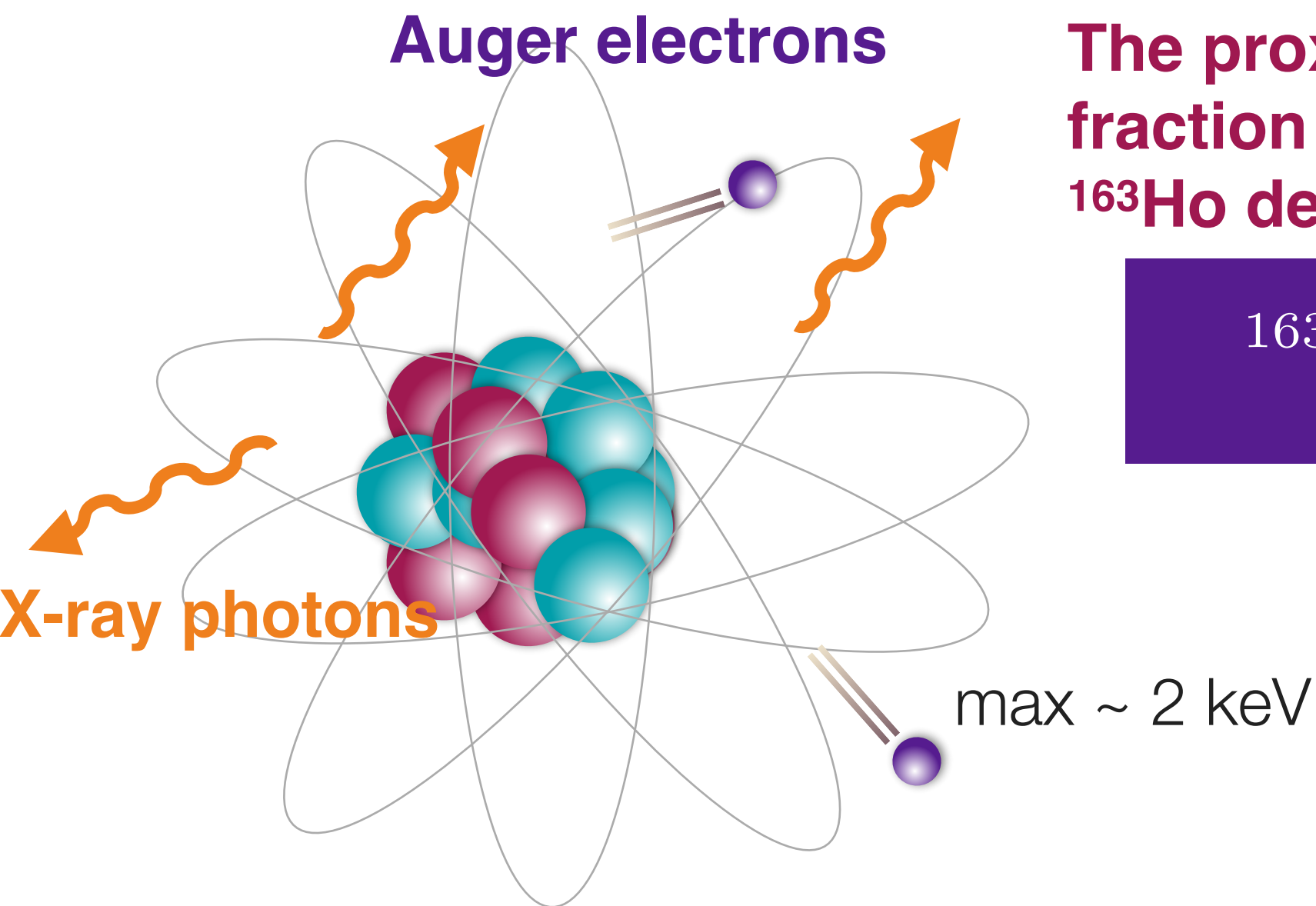


Lowest known Q-value  
(c.f. tritium 18.6 keV)

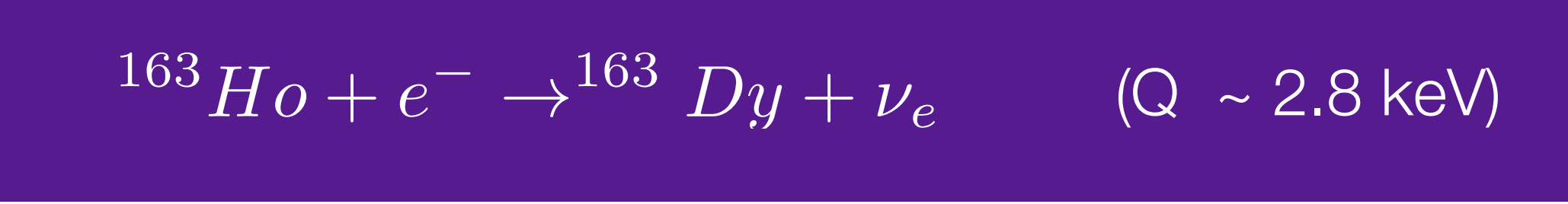
Neutrino energy    Neutrino momentum

$$\frac{d\lambda_{EC}}{dE_c} = \frac{G_\beta^2}{4\pi^2} (Q - E_c) \sqrt{(Q - E_c)^2 - m_\nu^2} \times \sum_i n_i C_i \beta_i^2 B_i \frac{\Gamma_i}{2\pi} \frac{1}{(E_c - E_i)^2 + \Gamma_i^2/4}$$

*Eur Phys J C Part Fields. 2015; 75(3): 112*



The proximity of the spectral endpoint to an atomic resonance makes the fraction of events that are sensitive to a non-zero neutrino mass superior in  $^{163}\text{Ho}$  decay than in tritium decay. *Physics Letters B* Volume 118, Issues 4–6, 9 December 1982, Pages 429-434



Lowest known Q-value  
(c.f. tritium 18.6 keV)

$$\frac{d\lambda_{EC}}{dE_c} = \frac{G_\beta^2}{4\pi^2} (Q - E_c) \sqrt{(Q - E_c)^2 - m_\nu^2} \times \sum_i n_i C_i \beta_i^2 B_i \frac{\Gamma_i}{2\pi} \frac{1}{(E_c - E_i)^2 + \Gamma_i^2/4}$$

Parameters of ionization spectral lines

*Eur Phys J C Part Fields*. 2015; 75(3): 112

The proximity of the spectral endpoint to an atomic resonance makes the fraction of events that are sensitive to a non-zero neutrino mass superior in

$^{163}\text{Ho}$  decay than in tritium decay. *Physics Letters B* Volume 118, Issues 4–6, 9 December 1982, Pages 429-434



Lowest known Q-value  
(c.f. tritium 18.6 keV)

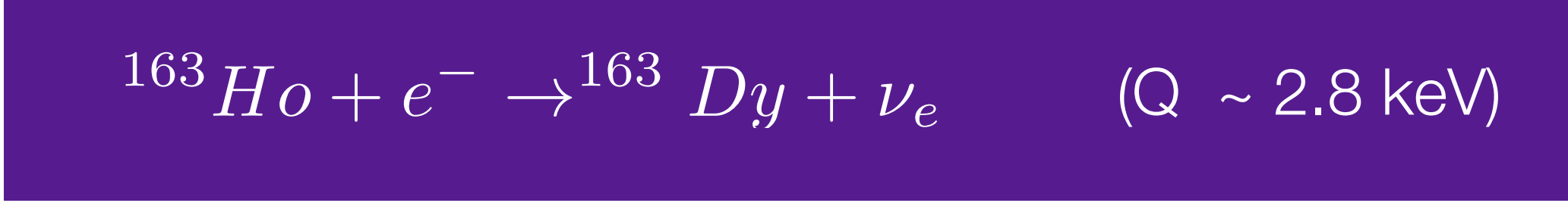
$$\frac{d\lambda_{EC}}{dE_c} = \frac{G_\beta^2}{4\pi^2} (Q - E_c) \sqrt{(Q - E_c)^2 - m_\nu^2} \times \sum_i n_i C_i \beta_i^2 B_i \frac{\Gamma_i}{2\pi} \frac{1}{(E_c - E_i)^2 + \Gamma_i^2/4}$$

*Eur Phys J C Part Fields.* 2015; 75(3): 112

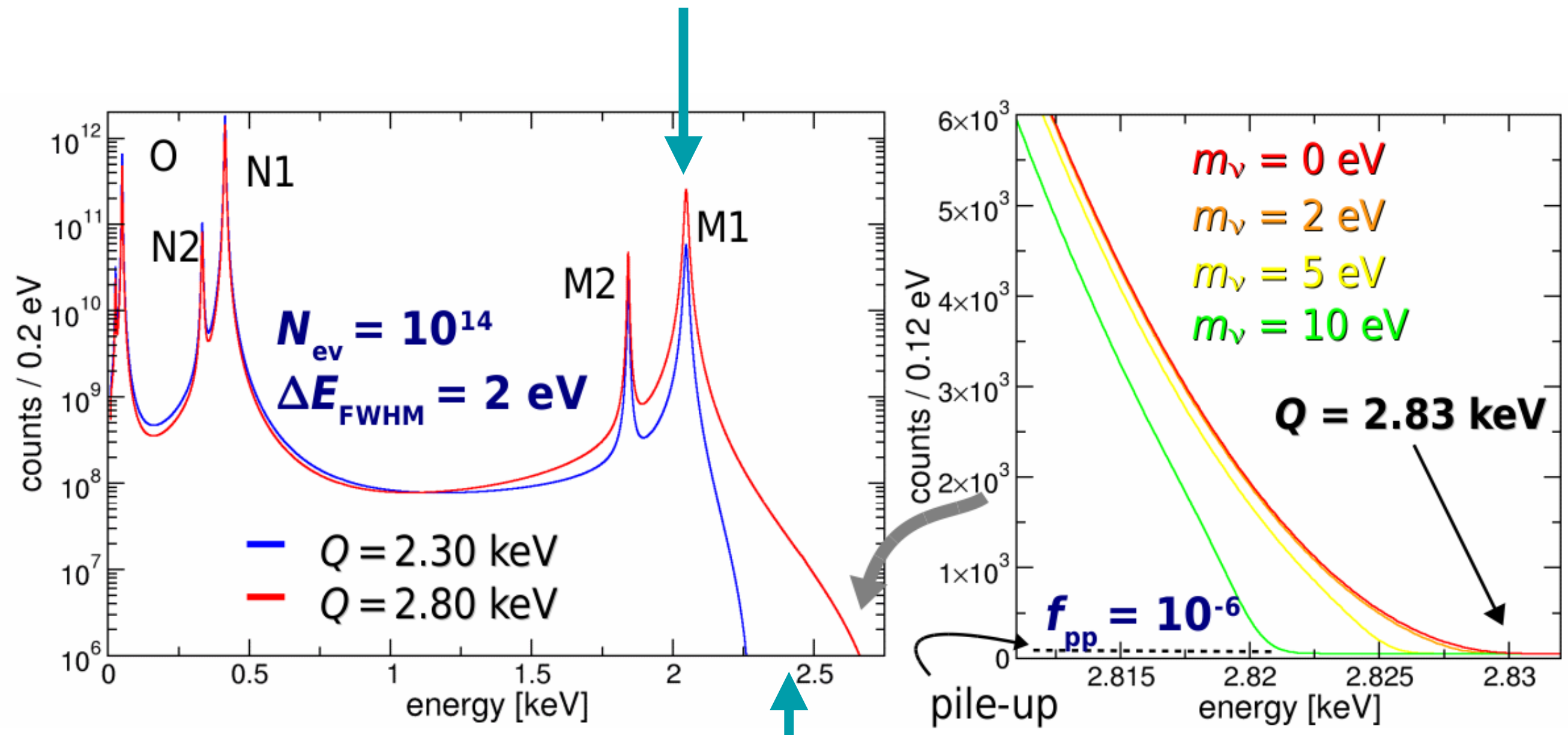
The proximity of the spectral endpoint to an atomic resonance makes the fraction of events that are sensitive to a non-zero neutrino mass superior in

$^{163}\text{Ho}$  decay than in tritium decay. *Physics Letters B Volume 118, Issues 4–6, 9 December 1982, Pages 429-434*

Enhancement near endpoint = even better chance of seeing neutrino mass effects



Lowest known Q-value (c.f. tritium 18.6 keV)



Low  $Q$  value increases neutrino mass effects (end point rate  $\sim 1/Q^3$ )

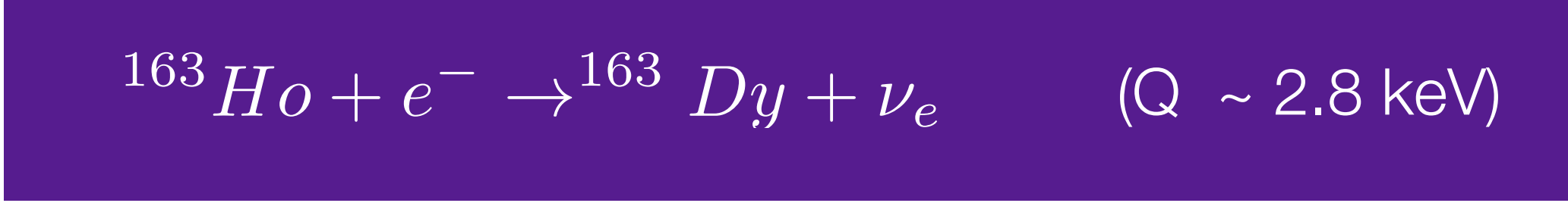
$$\frac{d\lambda_{EC}}{dE_c} = \frac{G_\beta^2}{4\pi^2} (Q - E_c) \sqrt{(Q - E_c)^2 - m_\nu^2} \times \sum_i n_i C_i \beta_i^2 B_i \frac{\Gamma_i}{2\pi} \frac{1}{(E_c - E_i)^2 + \Gamma_i^2/4}$$

<https://holmes0.mib.infn.it/holmes/>

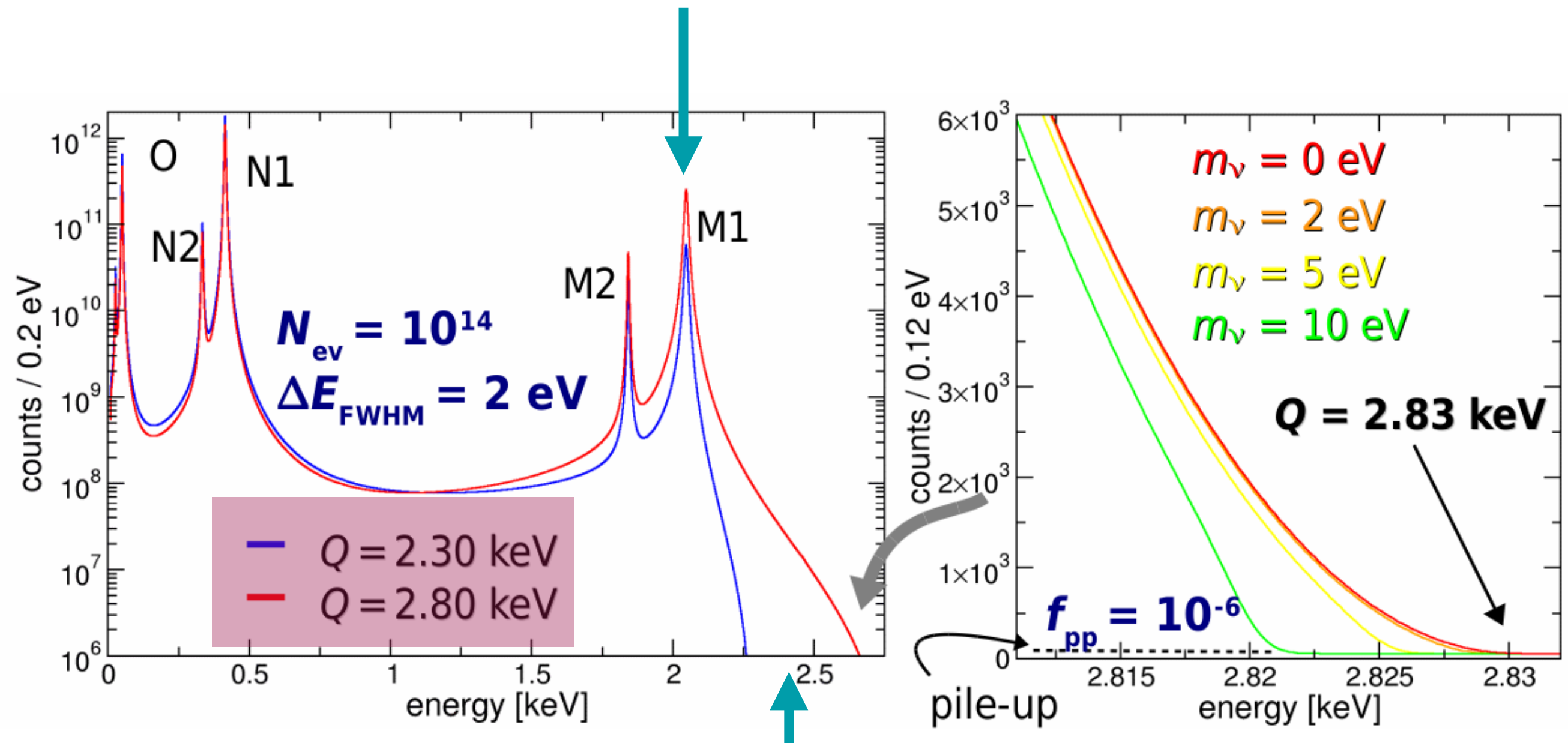
*Eur Phys J C Part Fields. 2015; 75(3): 112*

The proximity of the spectral endpoint to an atomic resonance makes the fraction of events that are sensitive to a non-zero neutrino mass superior in  $^{163}\text{Ho}$  decay than in tritium decay. *Physics Letters B Volume 118, Issues 4–6, 9 December 1982, Pages 429-434*

Enhancement near endpoint = even better chance of seeing neutrino mass effects



Lowest known Q-value (c.f. tritium 18.6 keV)



Low  $Q$  value increases neutrino mass effects (end point rate  $\sim 1/Q^3$ )

$$\frac{d\lambda_{EC}}{dE_c} = \frac{G_\beta^2}{4\pi^2} (Q - E_c) \sqrt{(Q - E_c)^2 - m_\nu^2} \times \sum_i n_i C_i \beta_i^2 B_i \frac{\Gamma_i}{2\pi} \frac{1}{(E_c - E_i)^2 + \Gamma_i^2/4}$$

<https://holmes0.mib.infn.it/holmes/>

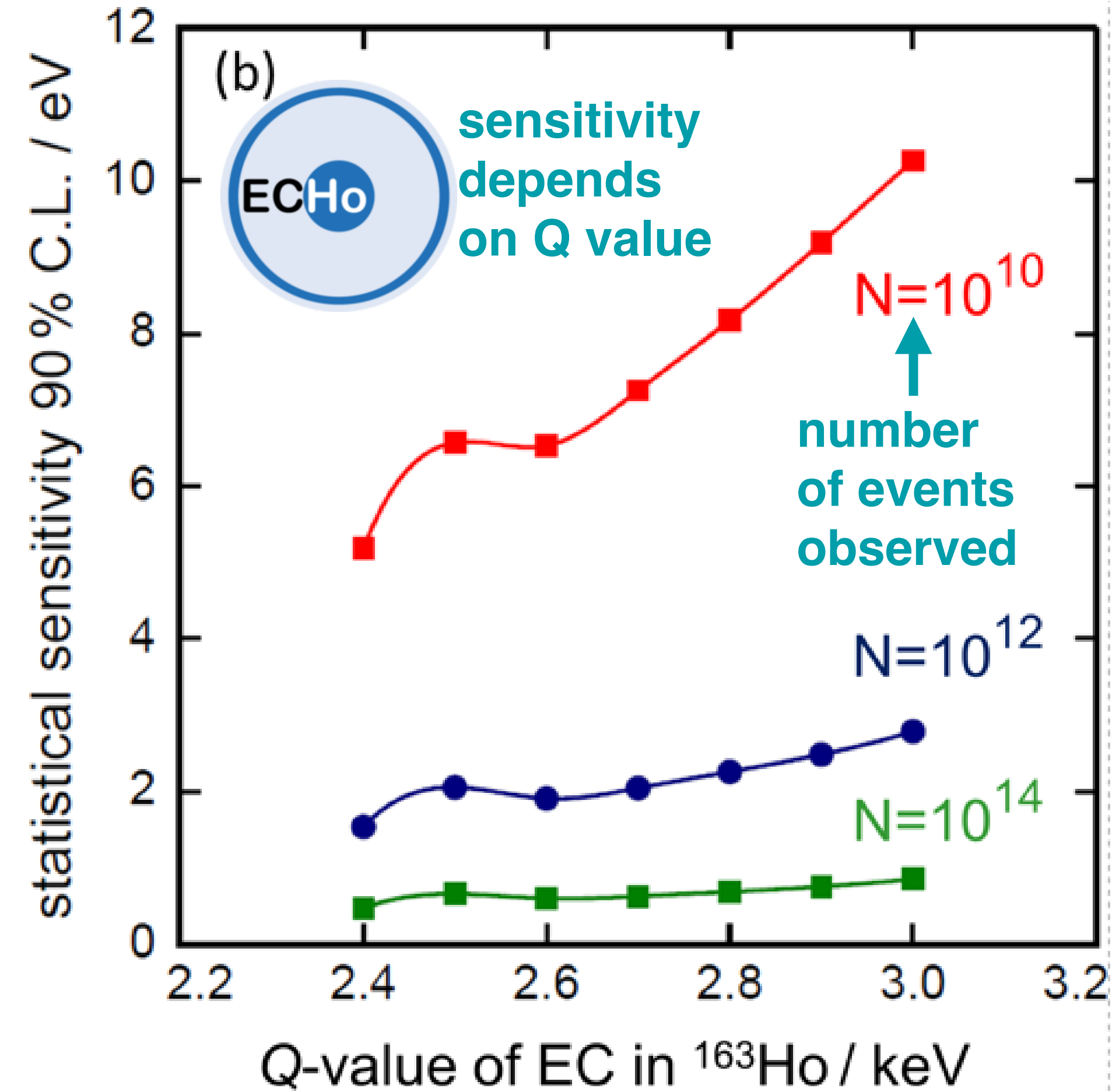
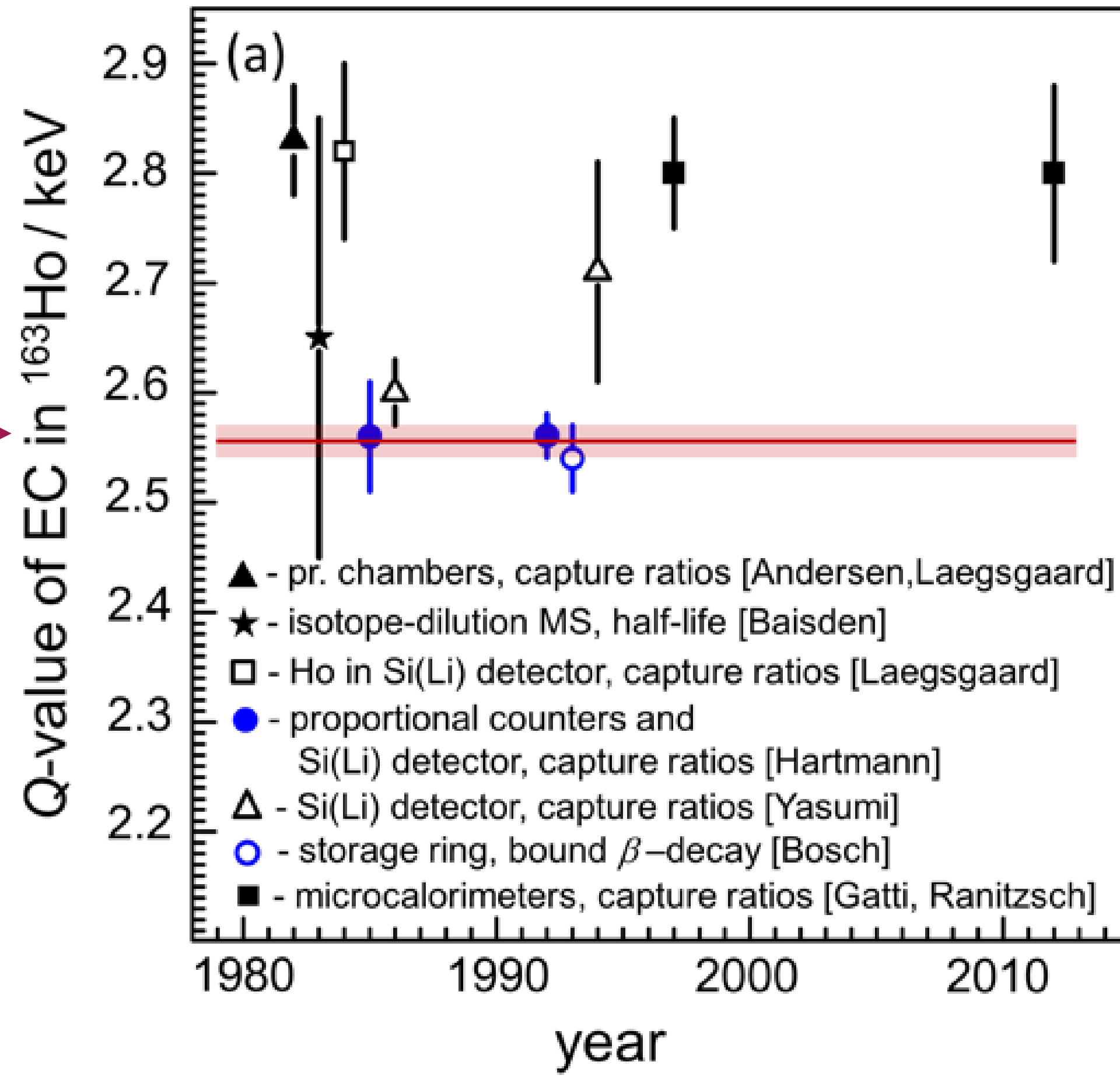
*Eur Phys J C Part Fields. 2015; 75(3): 112*

# The question of Q

Electron capture spectrum results disagree with accepted value

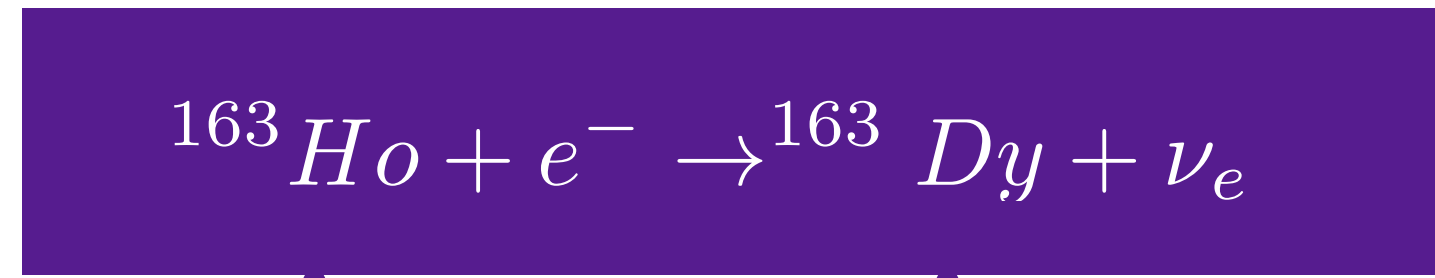
Accepted Q-value

Proportional counter and storage ring measurements averaged to give accepted value



PRL115,062501 (2015)

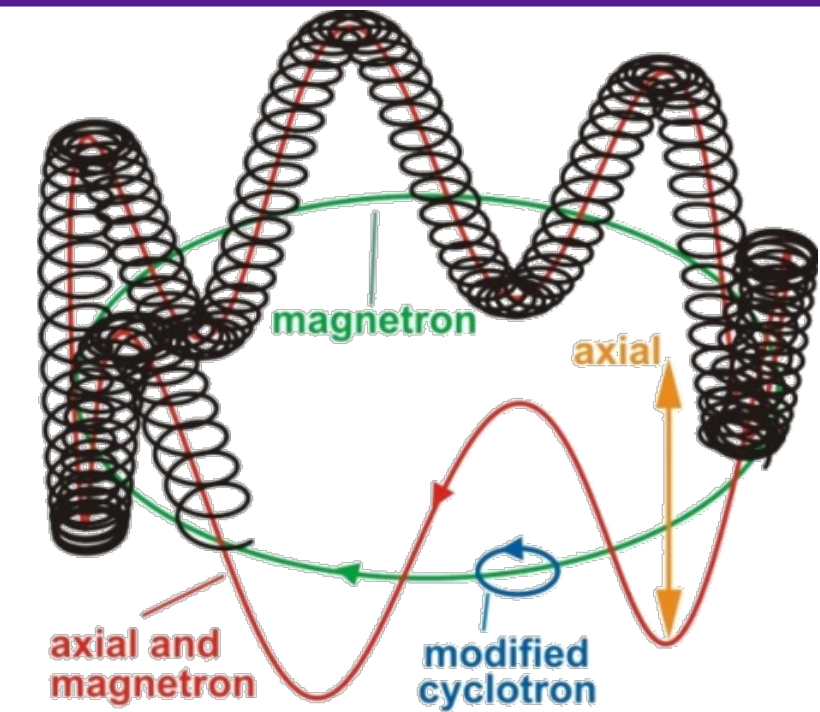
# Enter SHIPTRAP - Penning ion trapping facility



Look for mass difference by measuring the cyclotron-frequency ratio of  $^{163}\text{Ho}$  and  $^{163}\text{Dy}$  ions

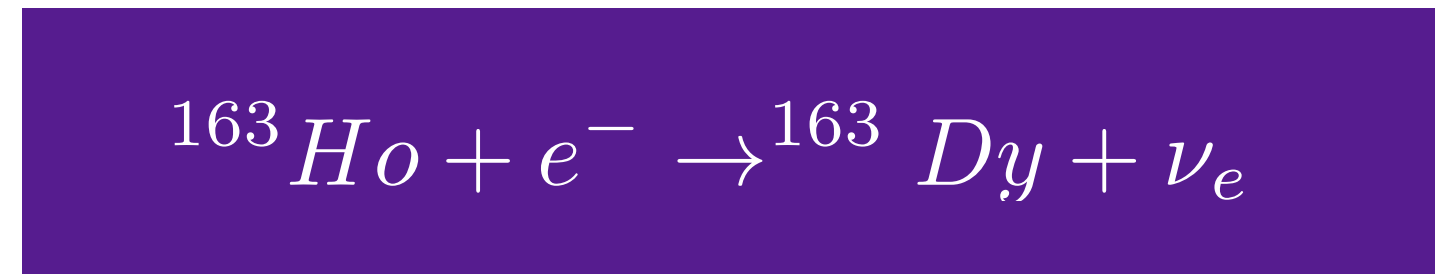
$$\nu_c = \frac{qB}{2\pi m} = \nu_- + \nu_+$$

magnetron frequency  
ion mass  
modified cyclotron frequency





# Enter SHIPTRAP - Penning ion trapping facility

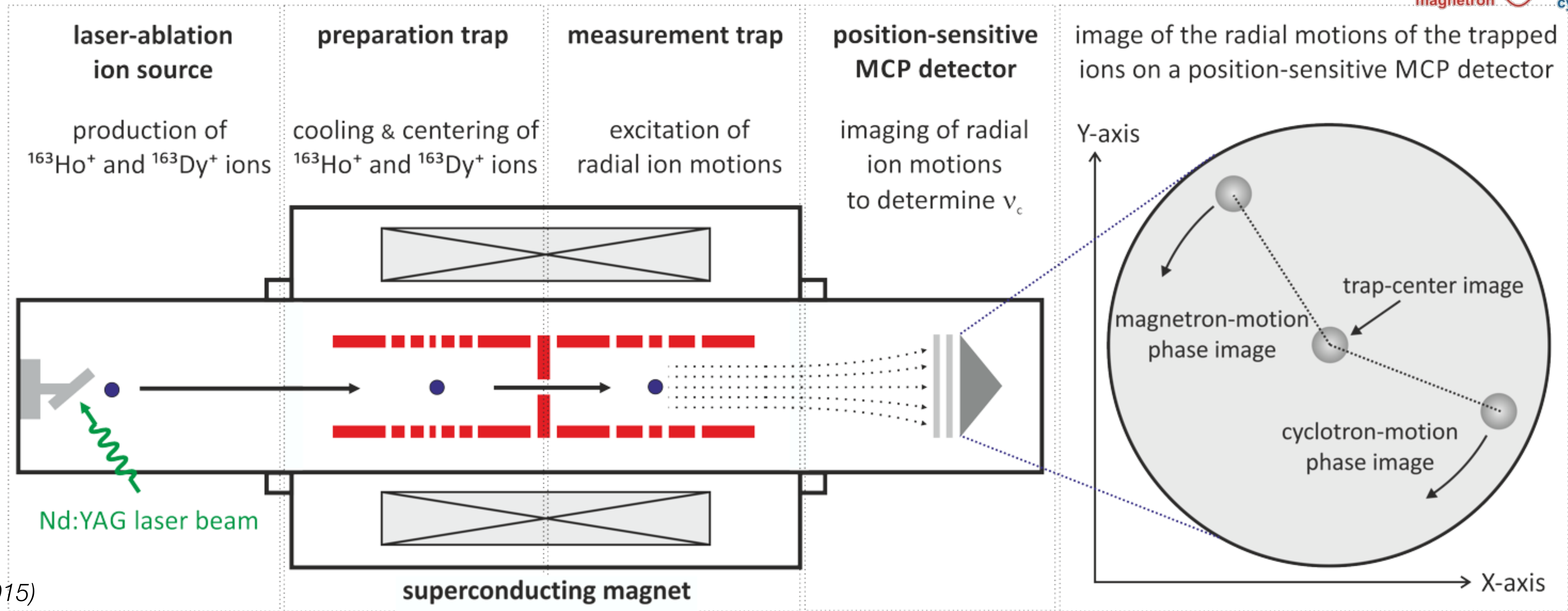
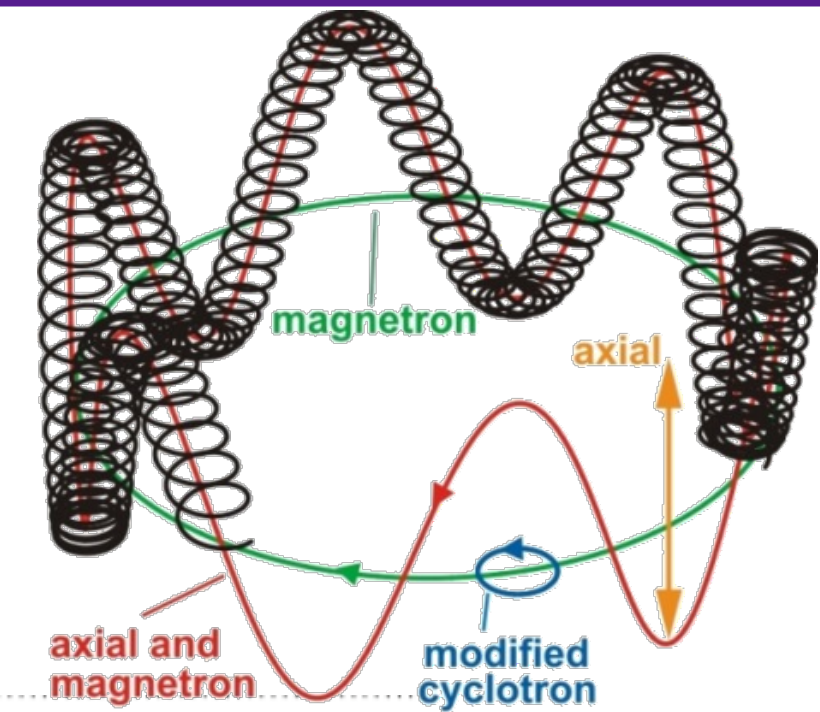


Look for mass difference by measuring the cyclotron-frequency ratio of  $^{163}\text{Ho}$  and  $^{163}\text{Dy}$  ions

$$\nu_c = \frac{qB}{2\pi m} = \nu_- + \nu_+$$

ion mass

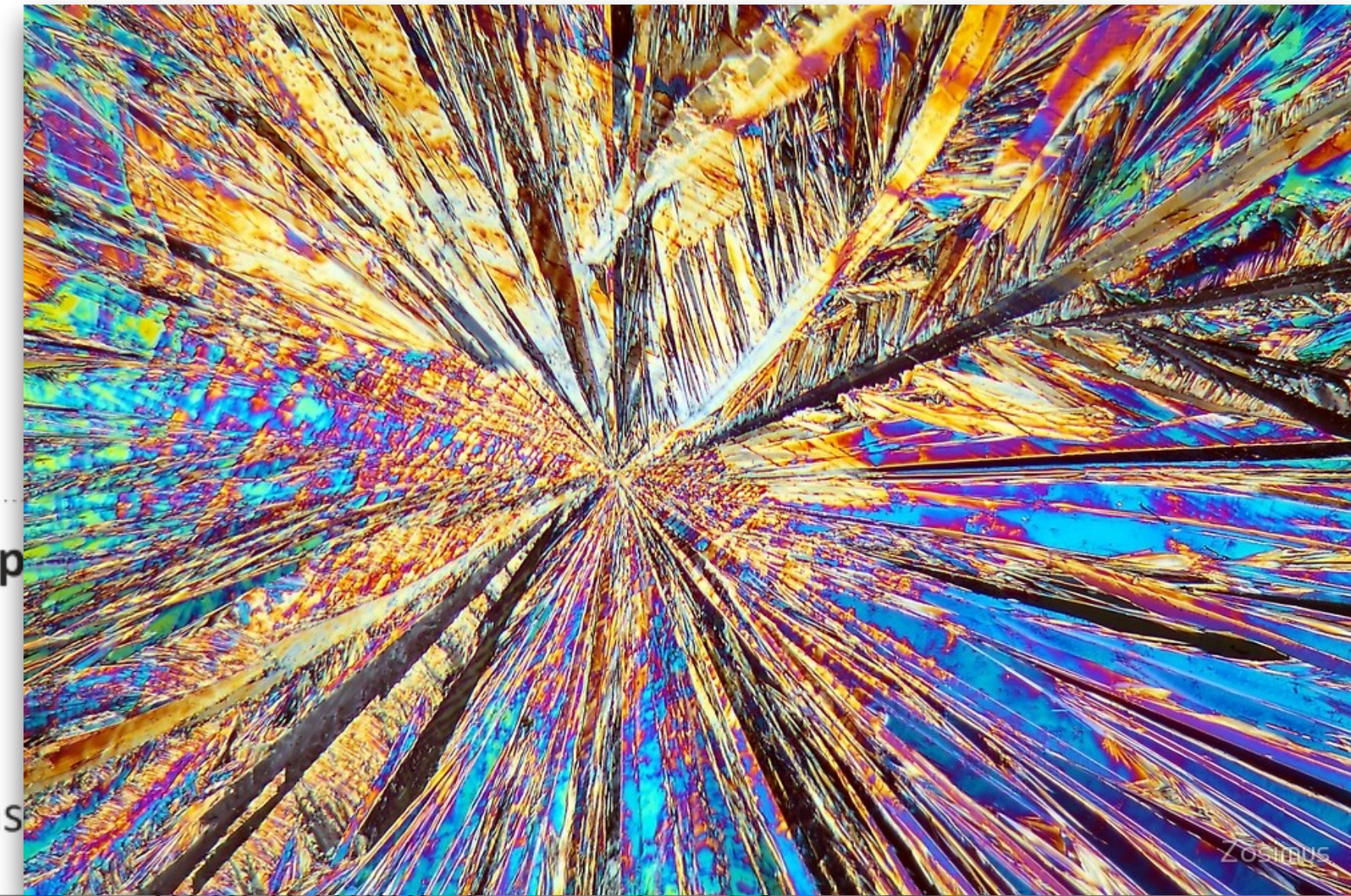
magnetron frequency  
modified cyclotron frequency



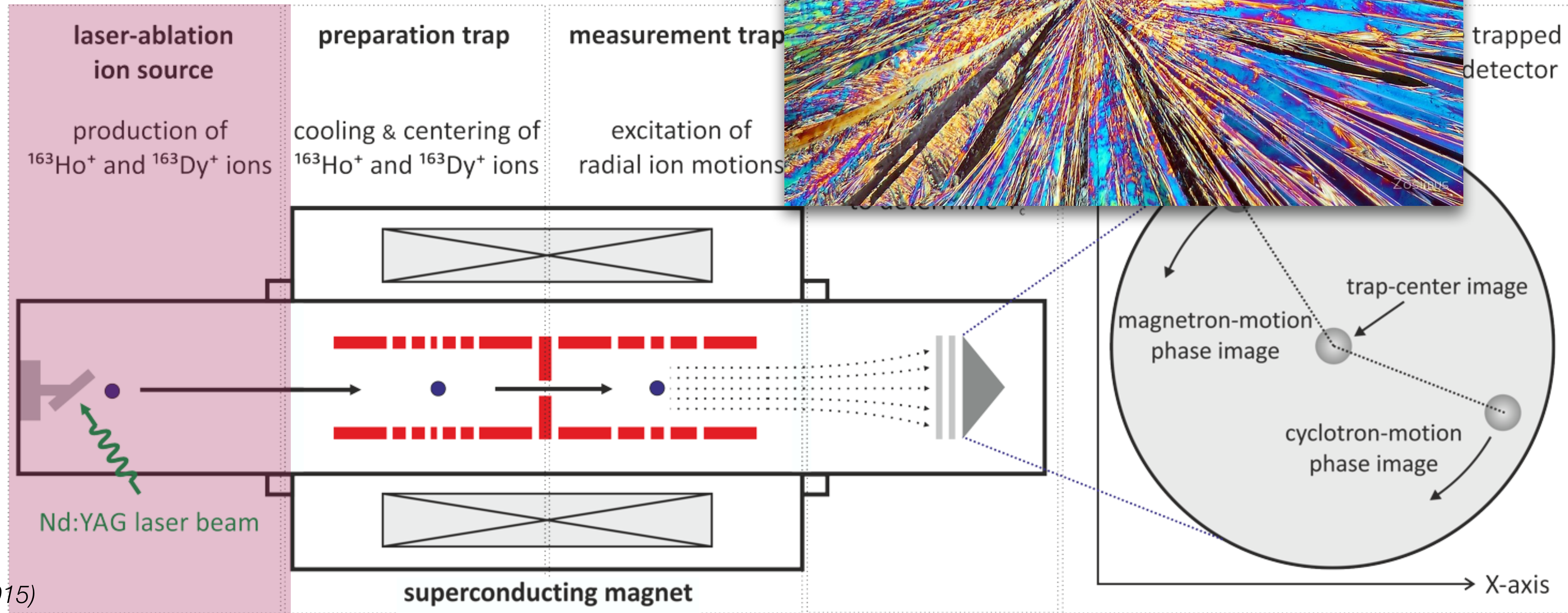
PRL115,062501 (2015)

# Enter SHIPTRAP - Penning ion trapping facility

- $^{163}\text{Ho}$  nitrate on a titanium base ( **$10^{16}$   $^{163}\text{Ho}$  atoms**)
- Nd:YAG **laser** produces  $^{163}\text{Ho}^+$  ions
- Repeat with natural Dy



*Holmium nitrate, Redbubble*



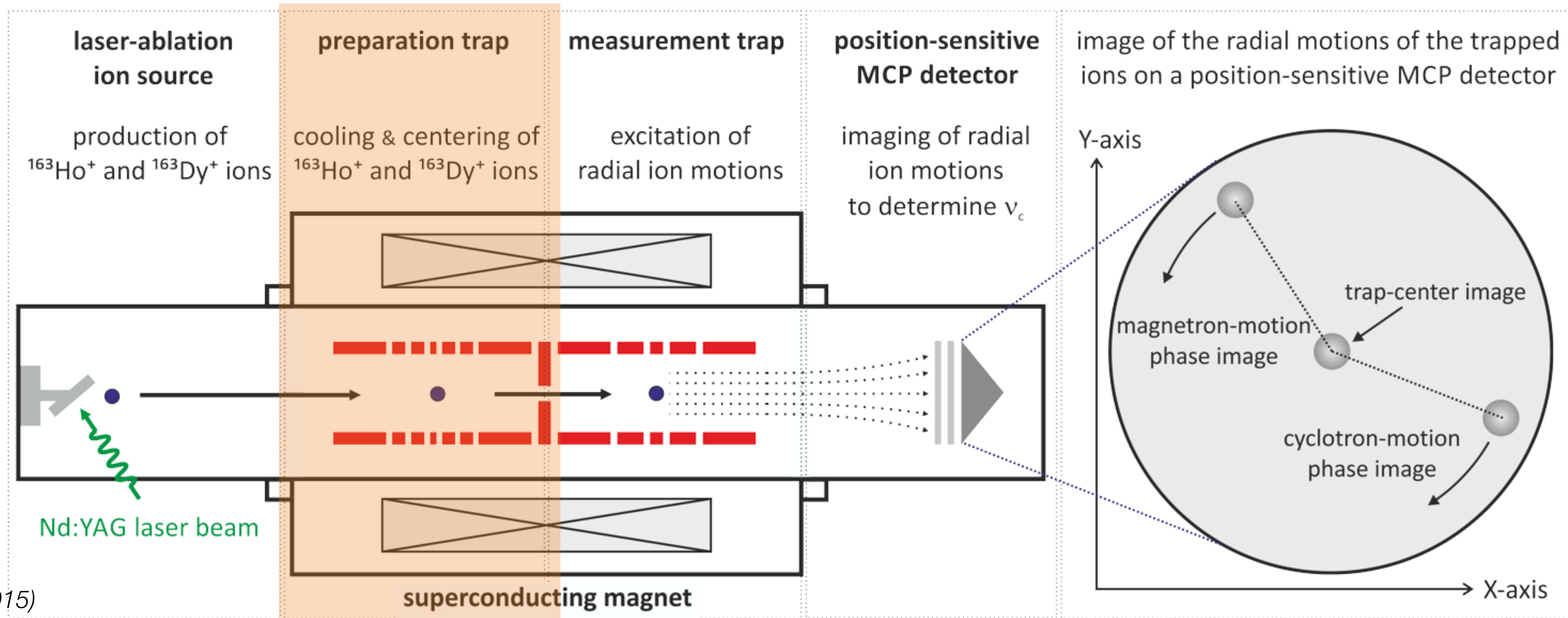
PRL115,062501 (2015)

# Enter SHIPTRAP - Penning ion trapping facility

- **Cool** and **centre** ions
- Remove **impurities**
- Increase **cyclotron radius** to **0.5mm**



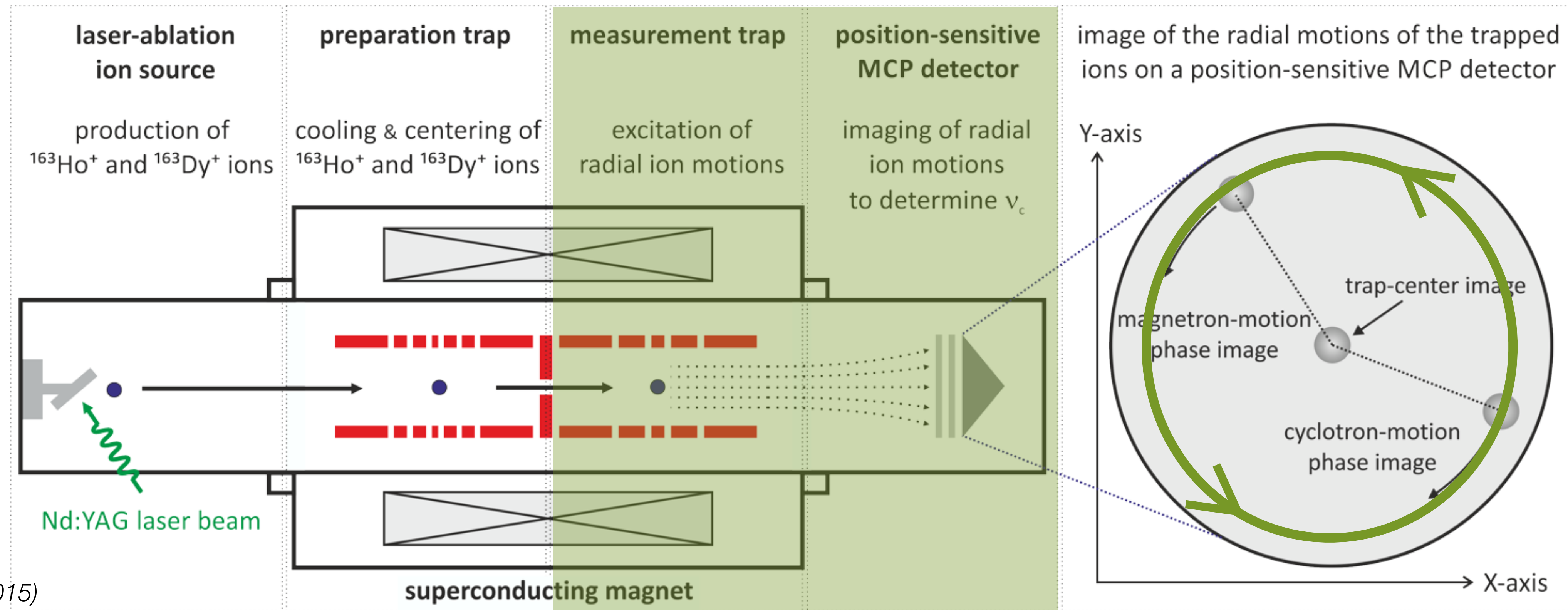
gsi.de



PRL115,062501 (2015)

# Enter SHIPTRAP - Penning ion trapping facility

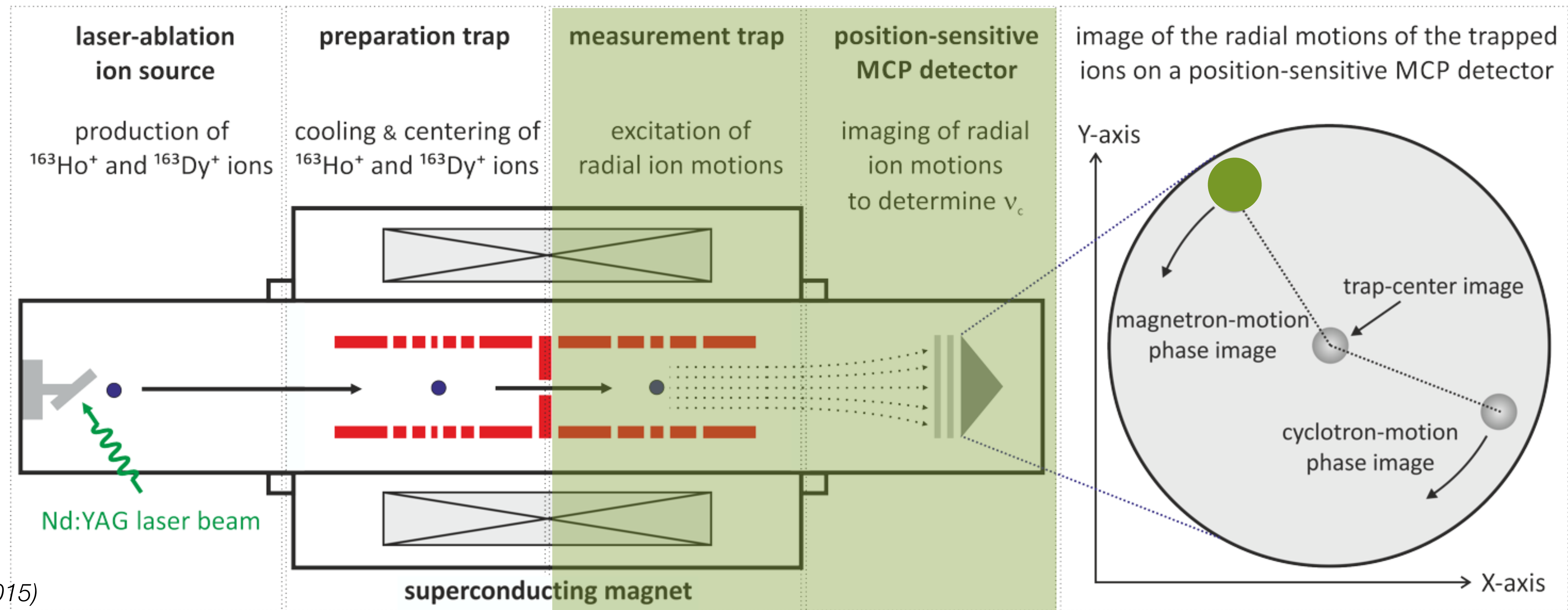
- Use RF dipole pulses to **excite ions** to a given radius
- A quadrupole pulse converts **cyclotron to magnetron** motion,



PRL115,062501 (2015)

# Enter SHIPTRAP - Penning ion trapping facility

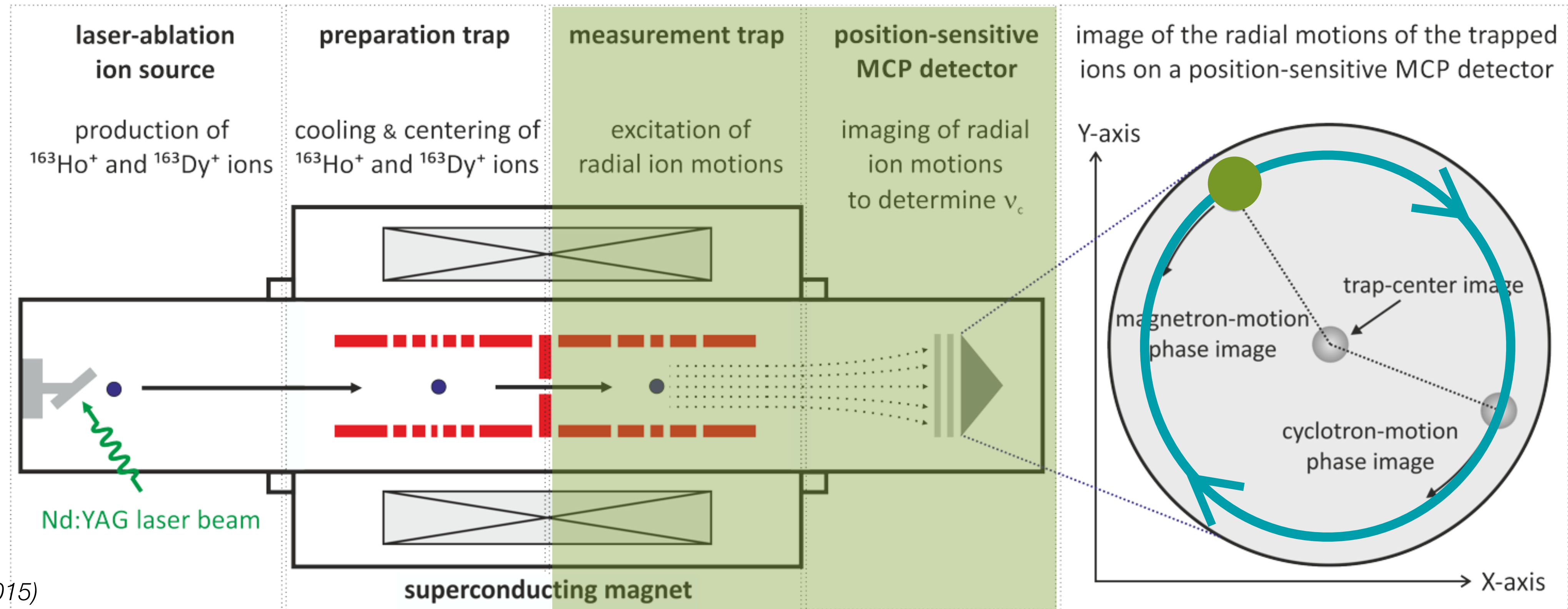
- Use RF dipole pulses to **excite ions** to a given radius
- A quadrupole pulse converts **cyclotron to magnetron** motion,
- After 600ms, a **phase shift**, related to the magnetron frequency, is measured by letting ions hit the detector



PRL115,062501 (2015)

# Enter SHIPTRAP - Penning ion trapping facility

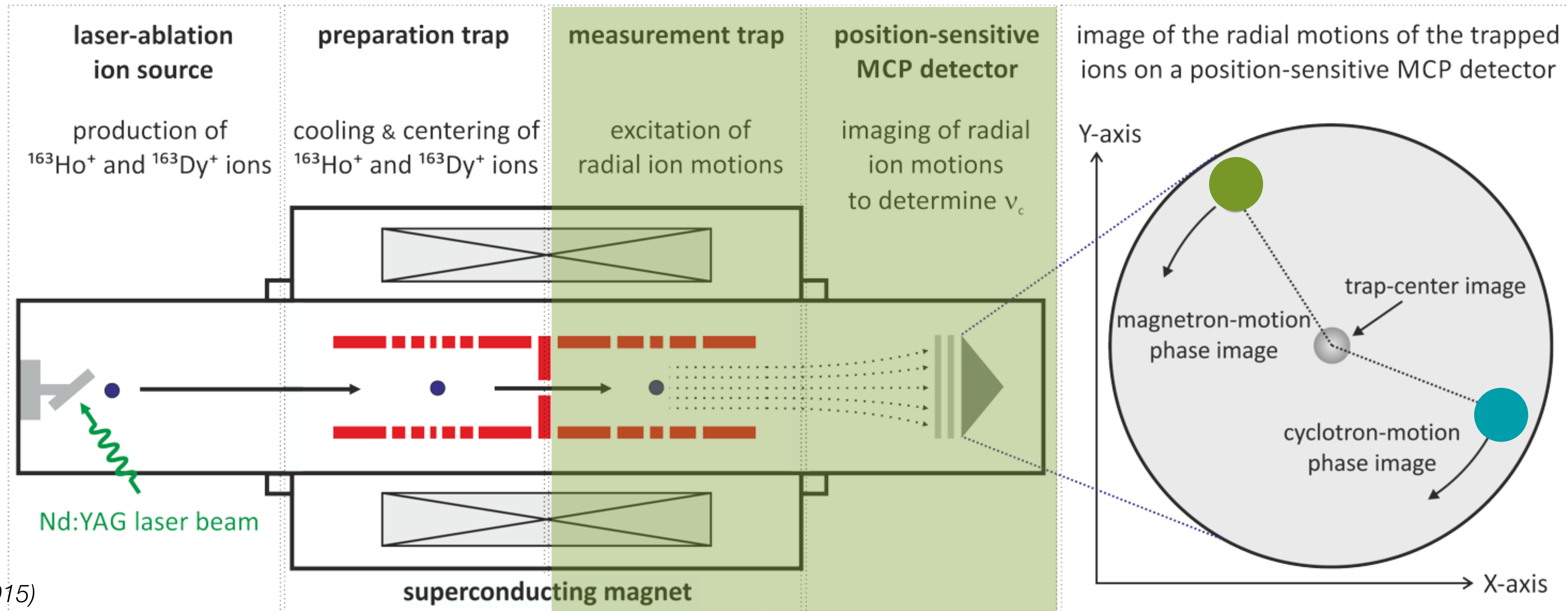
- Use RF dipole pulses to **excite ions** to a given radius
- A quadrupole pulse converts **cyclotron to magnetron** motion,
- After 600ms, a **phase shift**, related to the magnetron frequency, is measured by letting ions hit the detector
- In phase 2, excite to radius that allows **cyclotron motion**



PRL115,062501 (2015)

# Enter SHIPTRAP - Penning ion trapping facility

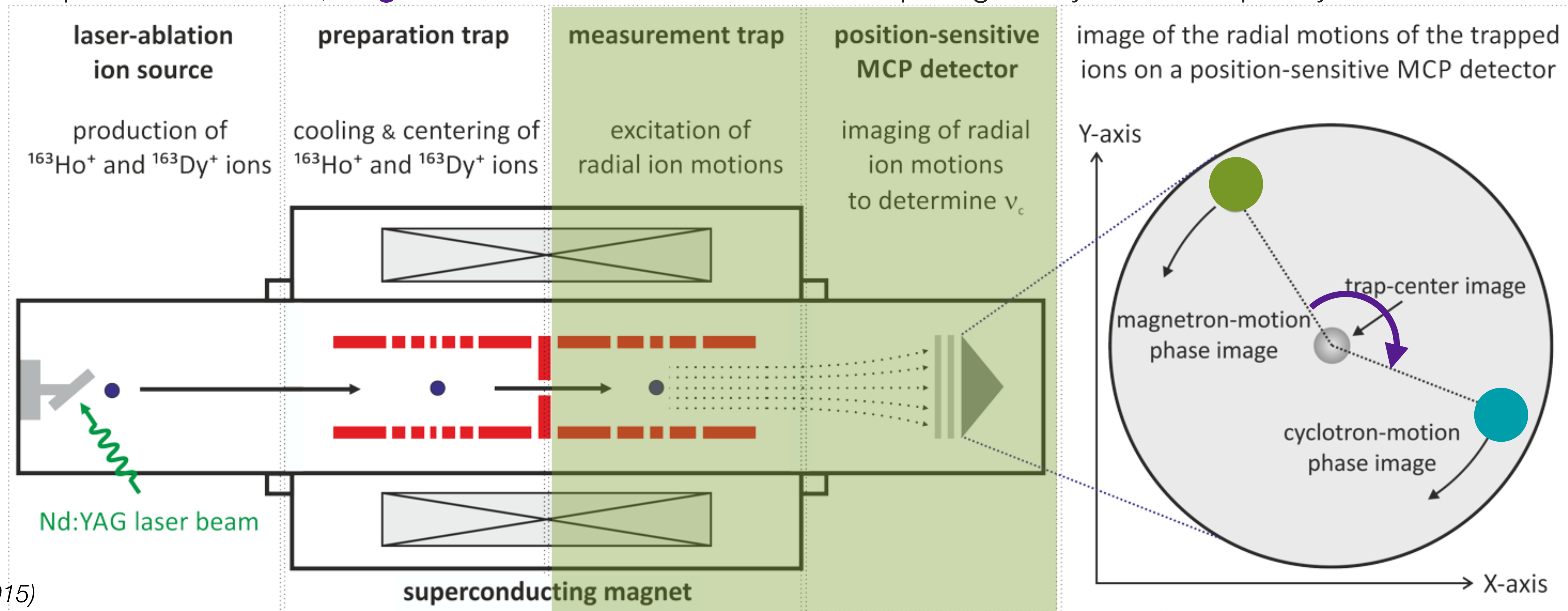
- Use RF dipole pulses to **excite ions** to a given radius
- A quadrupole pulse converts **cyclotron to magnetron** motion,
- After 600ms, a **phase shift**, related to the magnetron frequency, is measured by letting ions hit the detector
- In phase 2, excite to radius that allows **cyclotron motion**
- When converted, the phase shows the **modified cyclotron frequency**



PRL115,062501 (2015)

# Enter SHIPTRAP - Penning ion trapping facility

- Use RF dipole pulses to **excite ions** to a given radius
- A quadrupole pulse converts **cyclotron to magnetron** motion,
- After 600ms, a **phase shift**, related to the magnetron frequency, is measured by letting ions hit the detector
- In phase 2, excite to radius that allows **cyclotron motion**
- When converted, the phase shows the **modified cyclotron frequency**
- Repeat for 5 minutes, **angle** between accumulated detector spots gives cyclotron frequency



PRL115,062501 (2015)

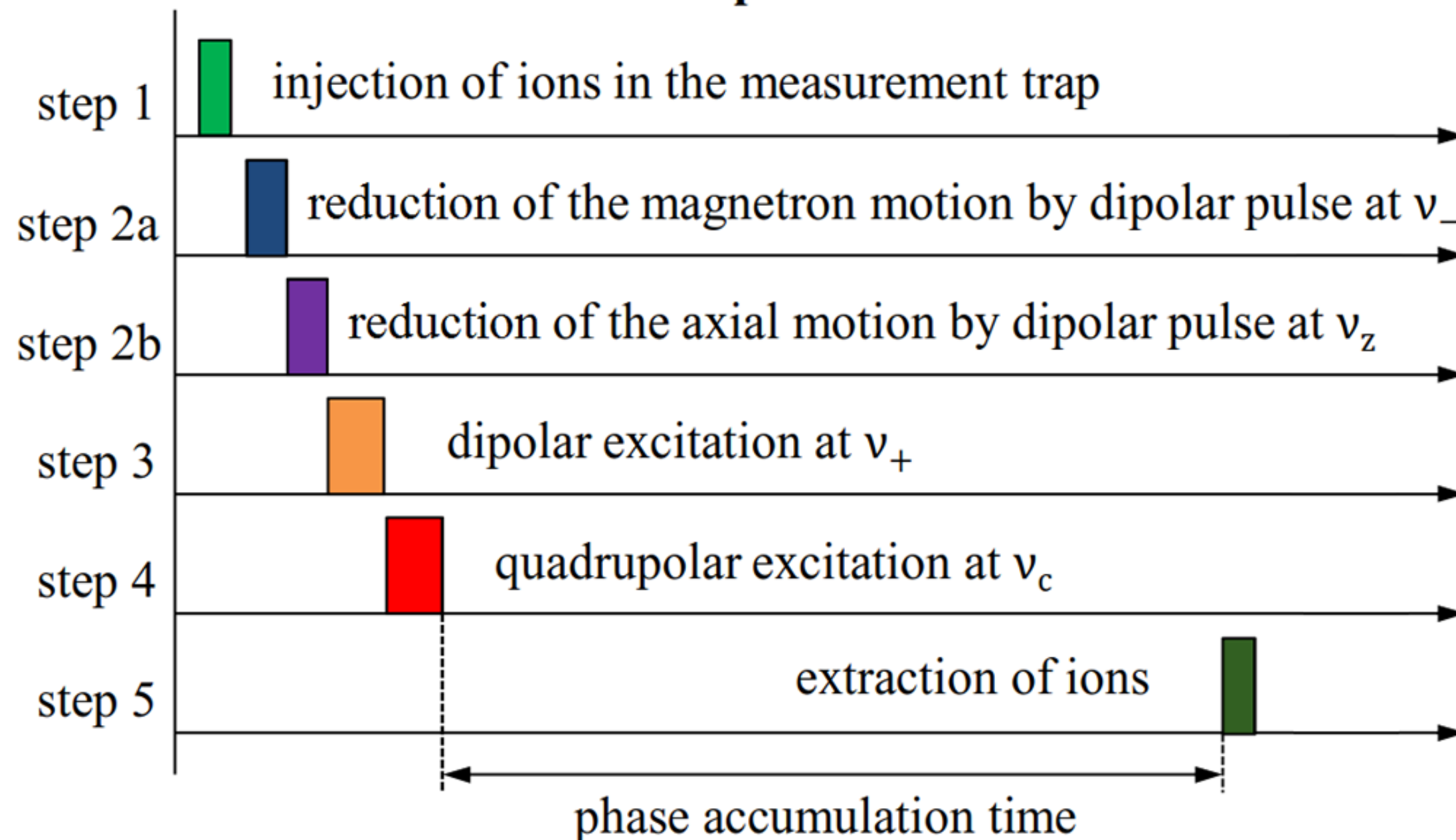


- Use RF dipole pulses to **excite ions** to a given radius
- A quadrupole pulse converts **cyclotron to magnetron** motion,
- After 600ms, a **phase shift**, related to the magnetron frequency, is measured by letting ions hit the detector
- In phase 2, excite to radius that allows **cyclotron motion**
- When converted, the phase shows the **modified cyclotron frequency**
- Repeat for 5 minutes, **angle** between accumulated detector spots gives cyclotron frequency

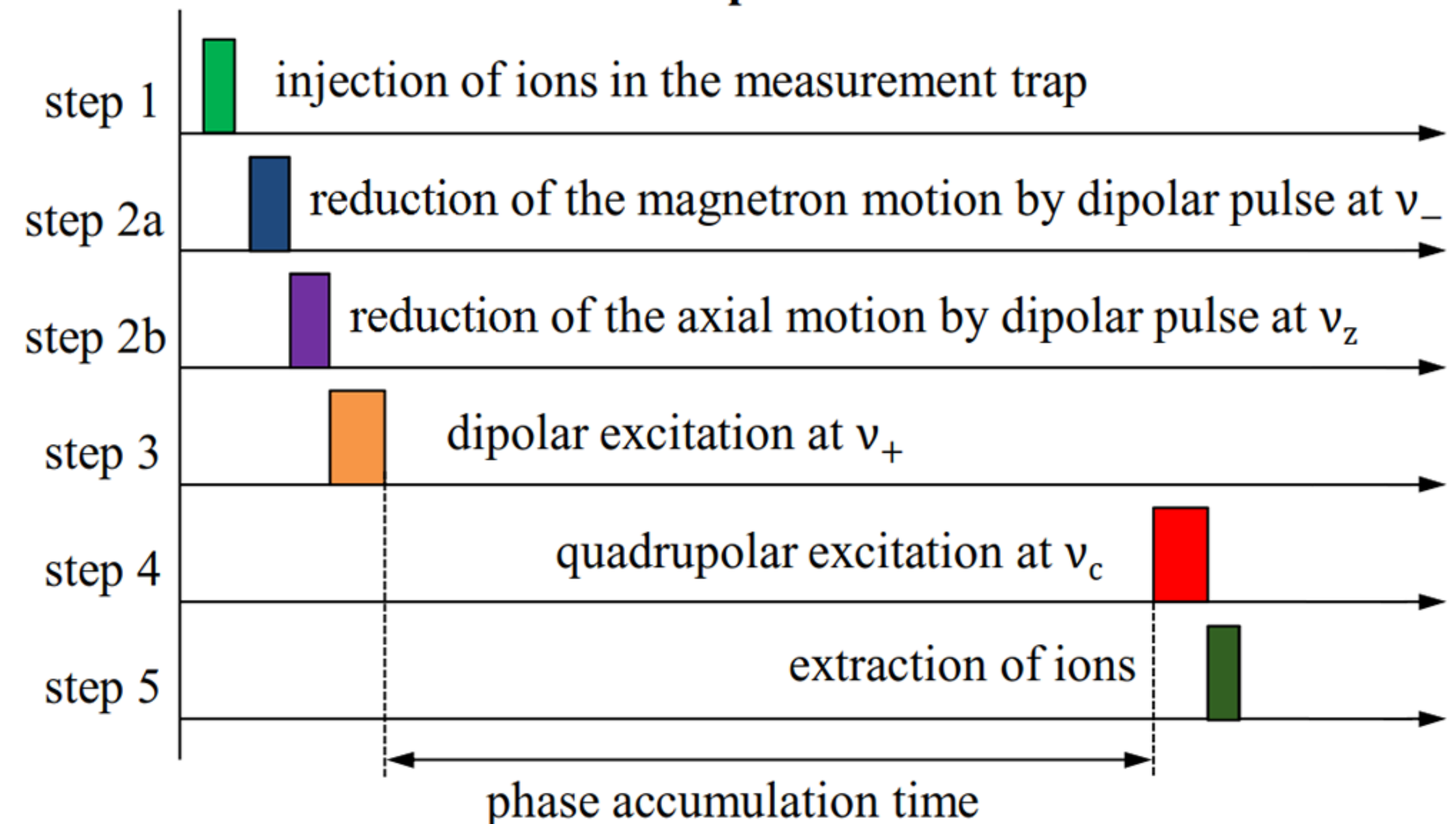
## Phase-Imaging Ion-Cyclotron-Resonance technique

*Eur. Phys. J. A (2018)54: 154*

**pattern 1**

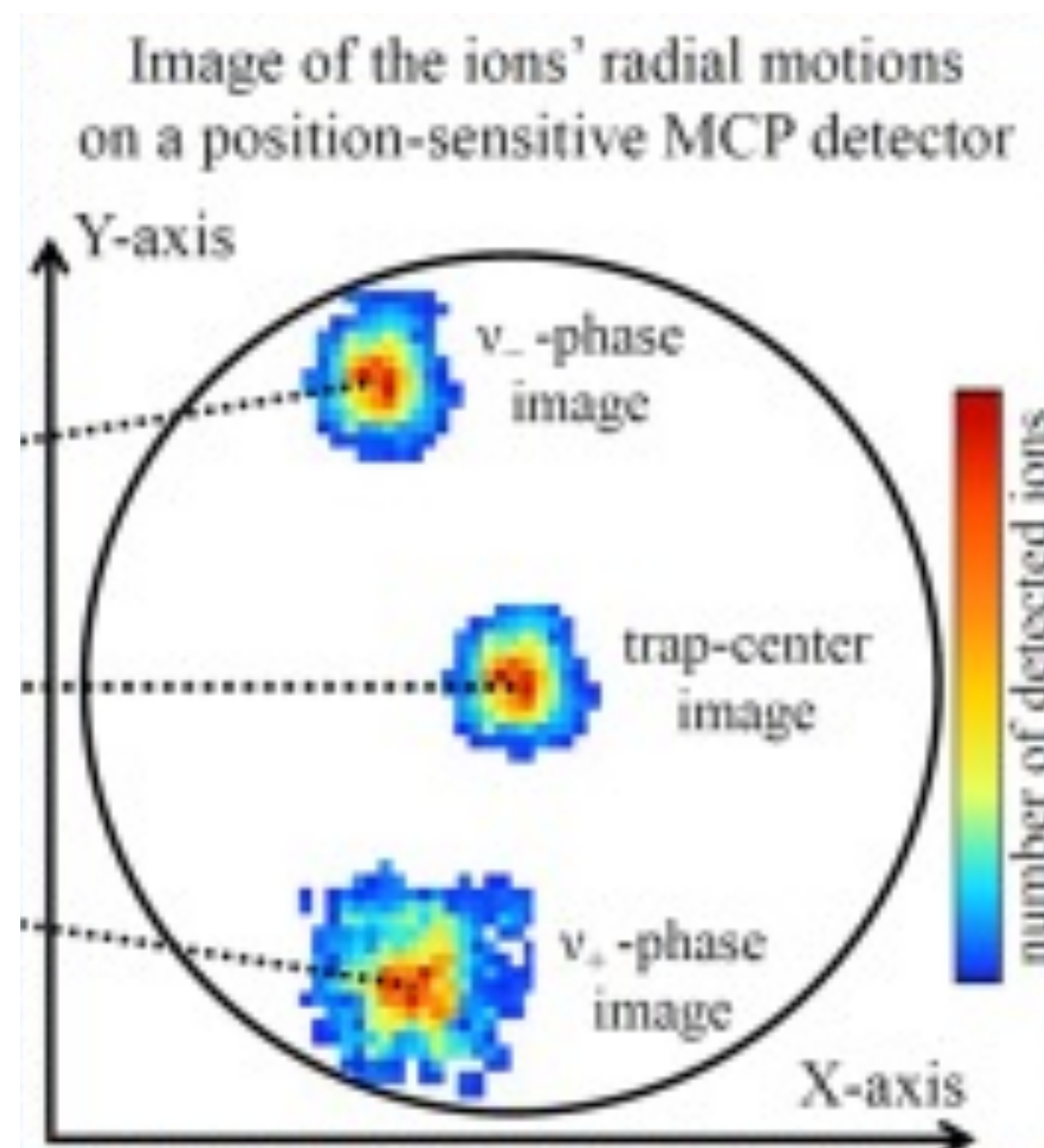


**pattern 2**



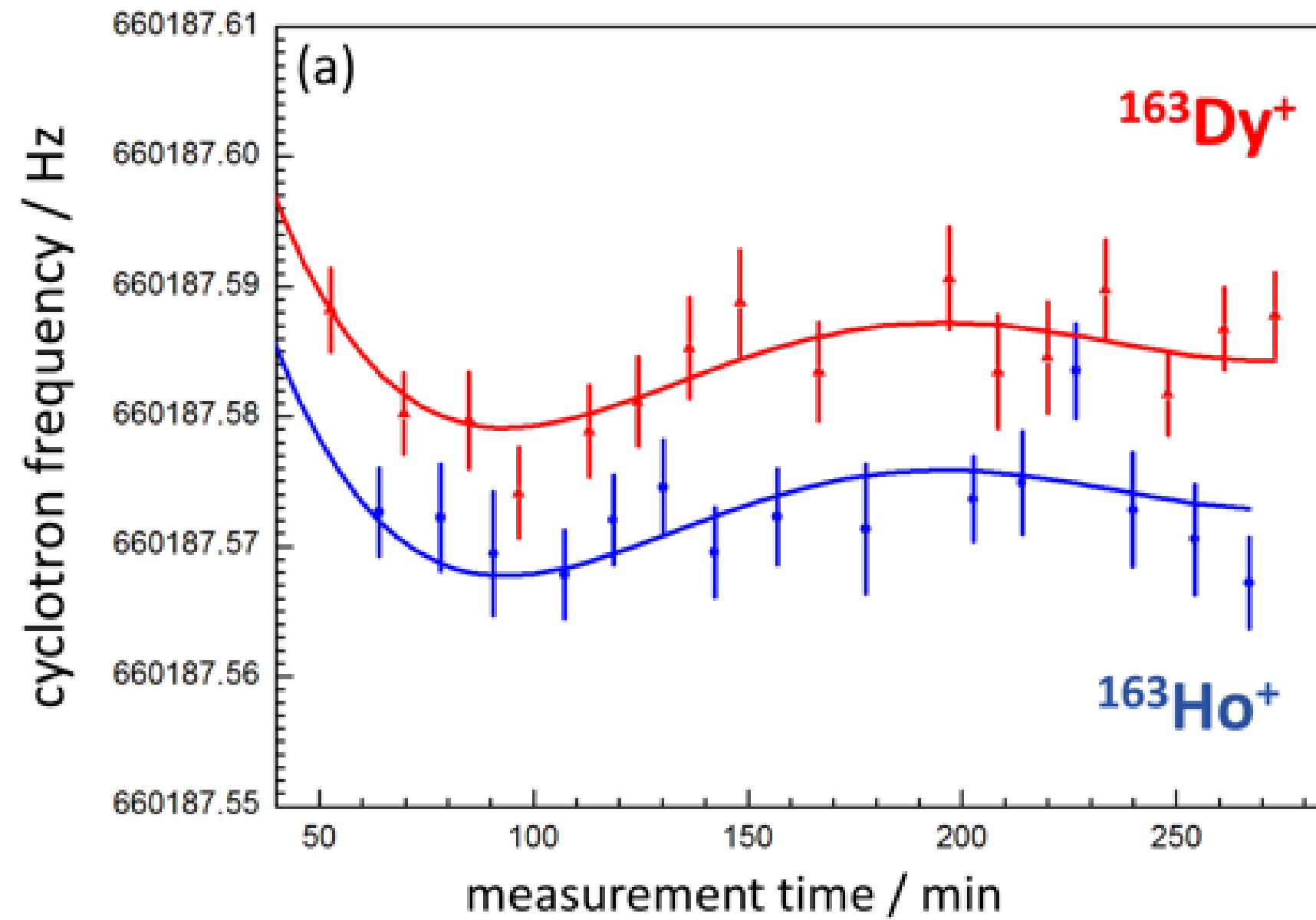
PRL115, ...

- Use RF dipole pulses to **excite ions** to a given radius
- A quadrupole pulse converts **cyclotron to magnetron** motion,
- After 600ms, a **phase shift**, related to the magnetron frequency, is measured by letting ions hit the detector
- In phase 2, excite to radius that allows **cyclotron motion**
- When converted, the phase shows the **modified cyclotron frequency**
- Repeat for 5 minutes, **angle** between accumulated detector spots gives cyclotron frequency



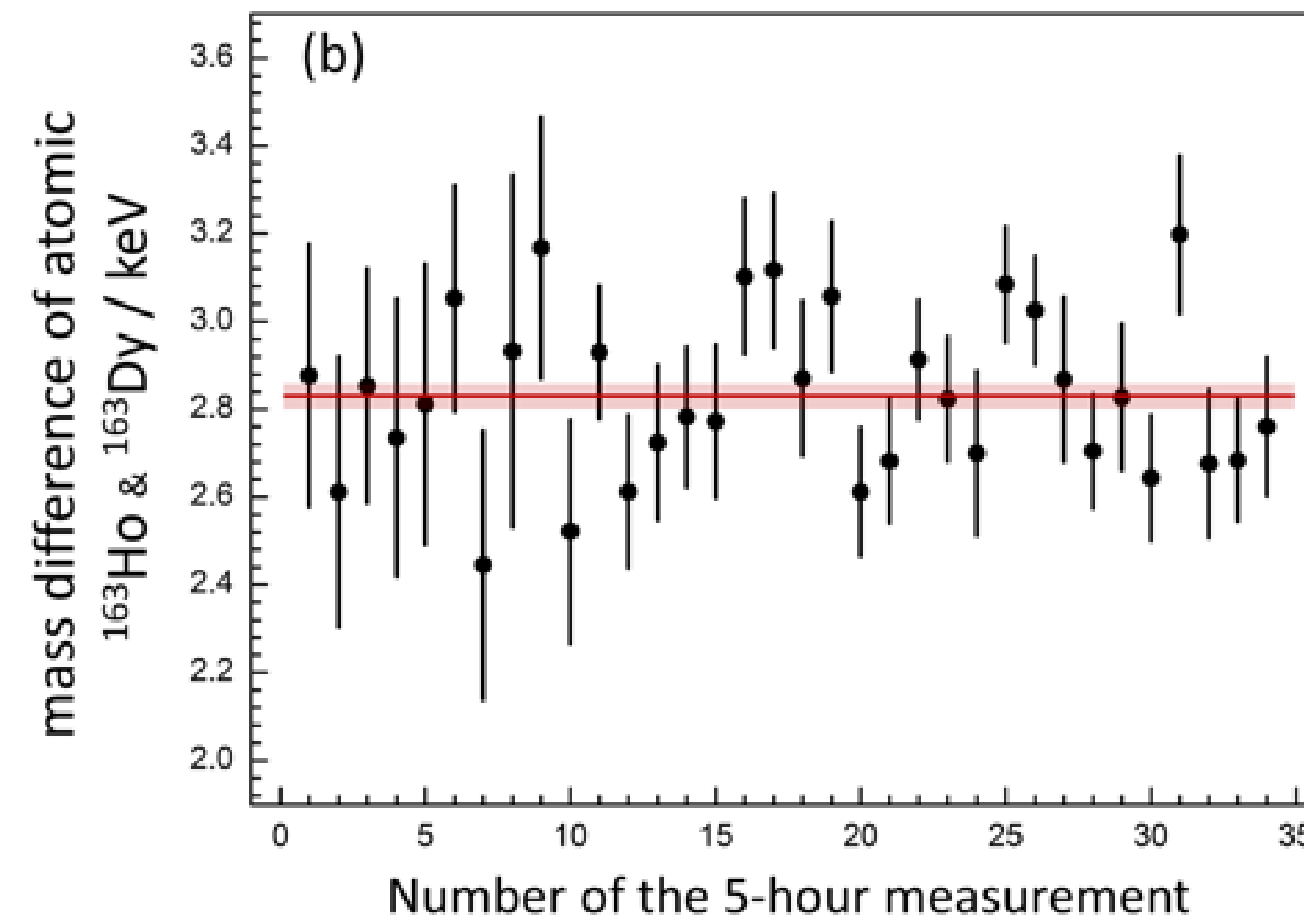
$^{123}\text{Te}$   
SHIPTRAP  
image

*Physics Letters B*  
758(C) (2016)



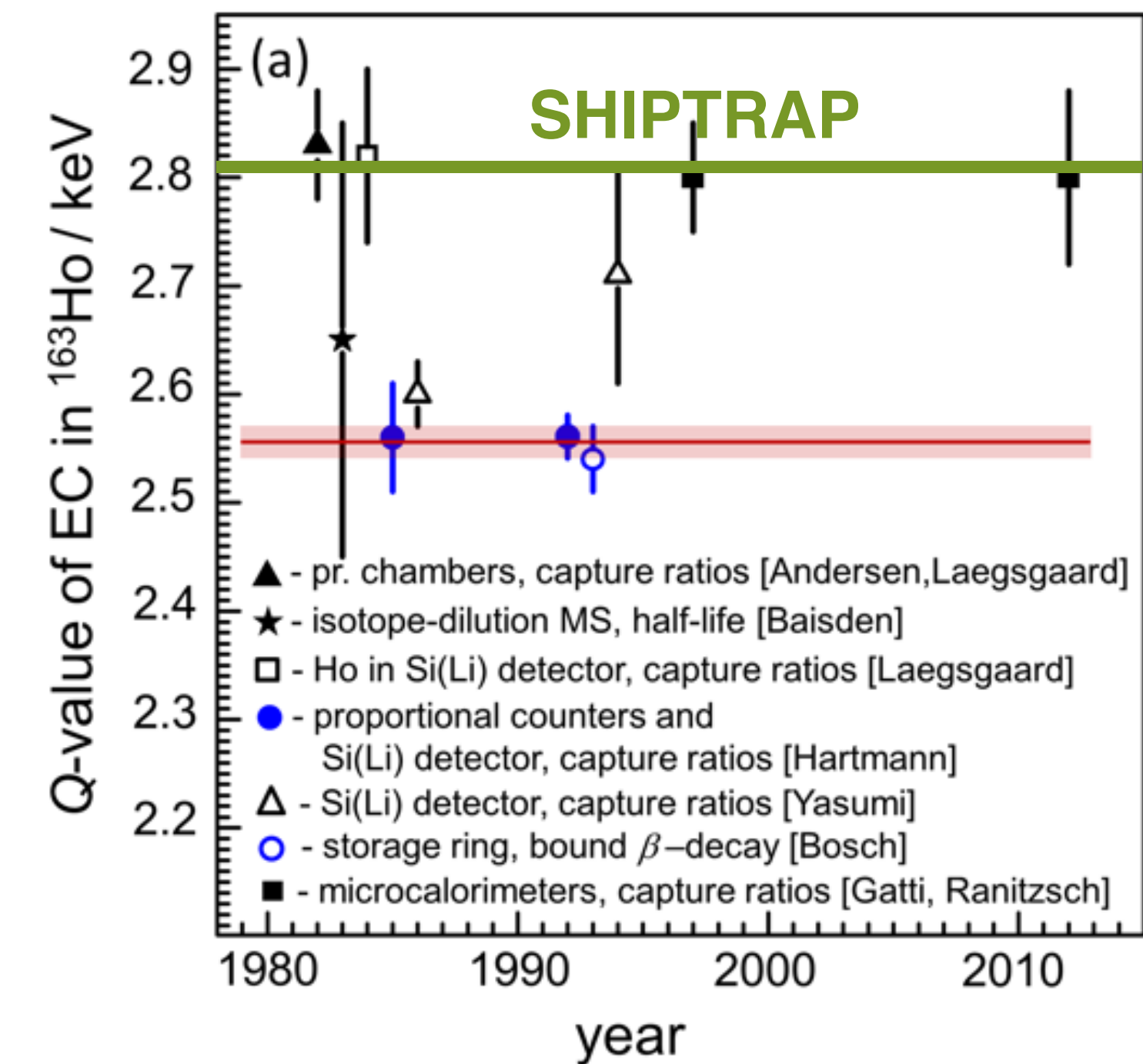
PPB measurement of frequency ratio

$$R = \frac{M_{163\text{Ho}}}{M_{163\text{Dy}}} = 1.00000001867(20_{\text{stat}})(10_{\text{sys}})$$

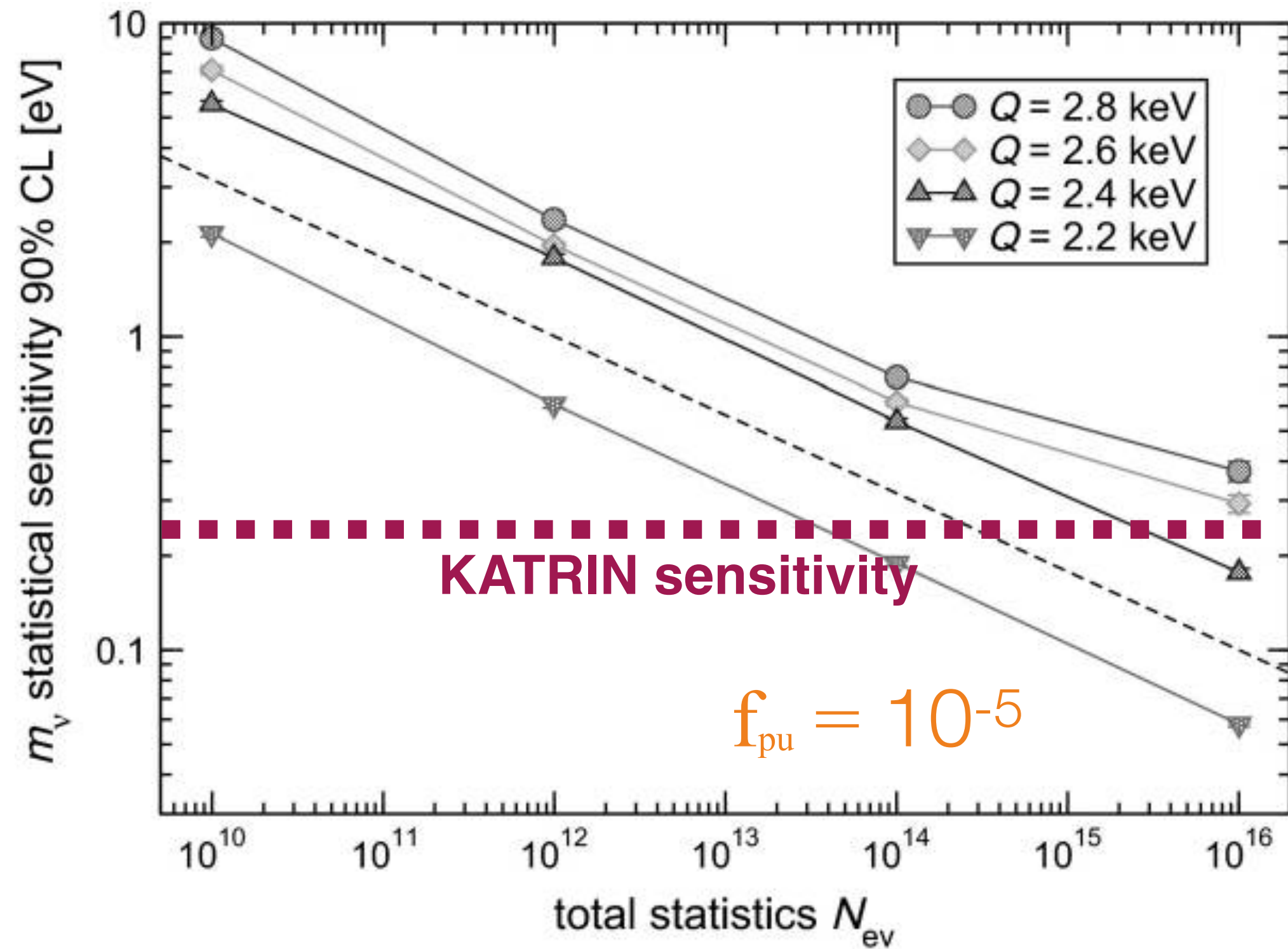


Mass difference agrees with micro calorimeter experiments

$$\Delta M = Q_{\text{EC}} = 2833(30_{\text{stat}})(15_{\text{sys}})\text{eV}/c^2$$

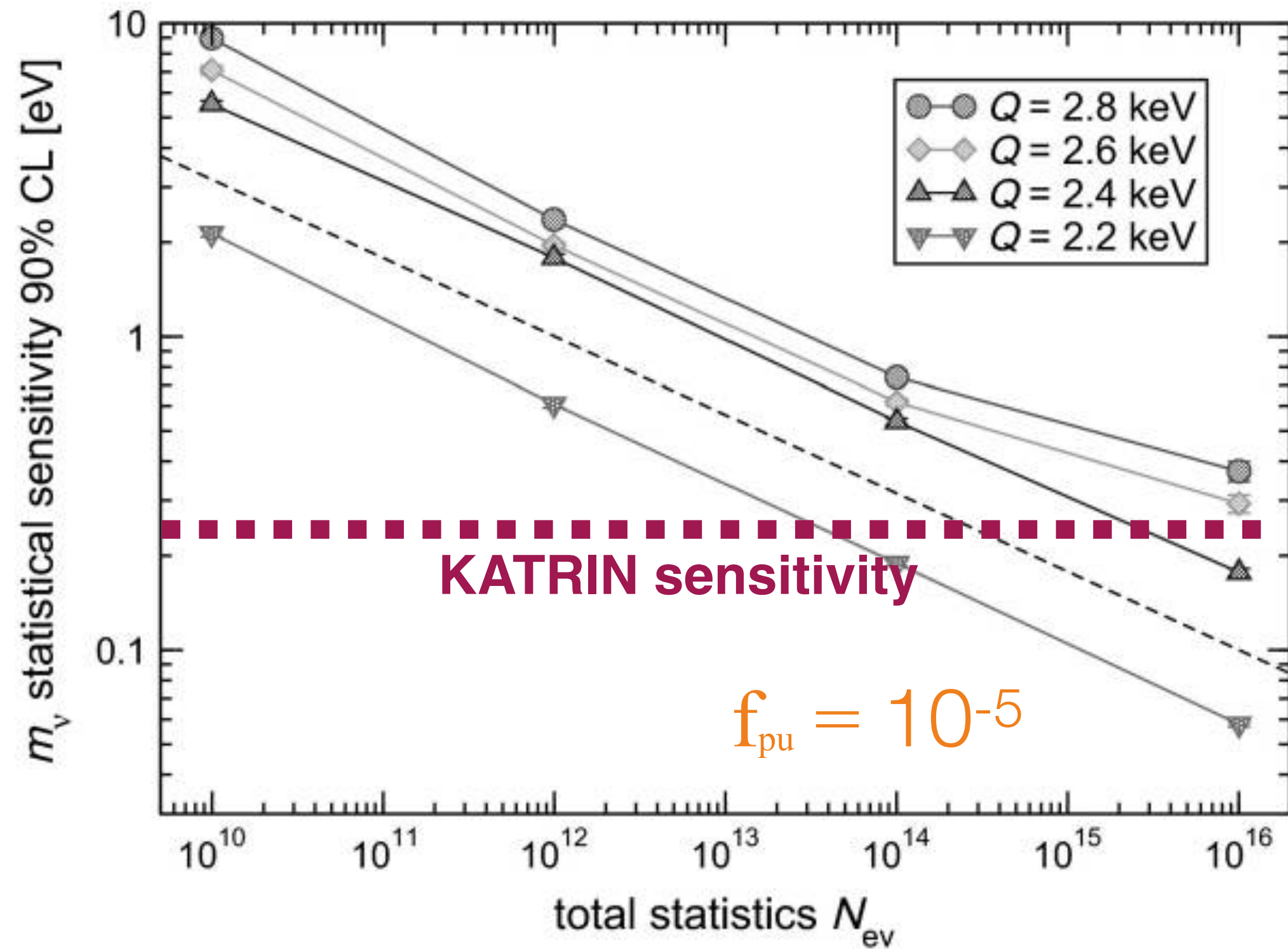


# How much $^{163}\text{Ho}$ do we need?



*Eur Phys J C Part Fields. 2015; 75(3): 112.*

# How much $^{163}\text{Ho}$ do we need?

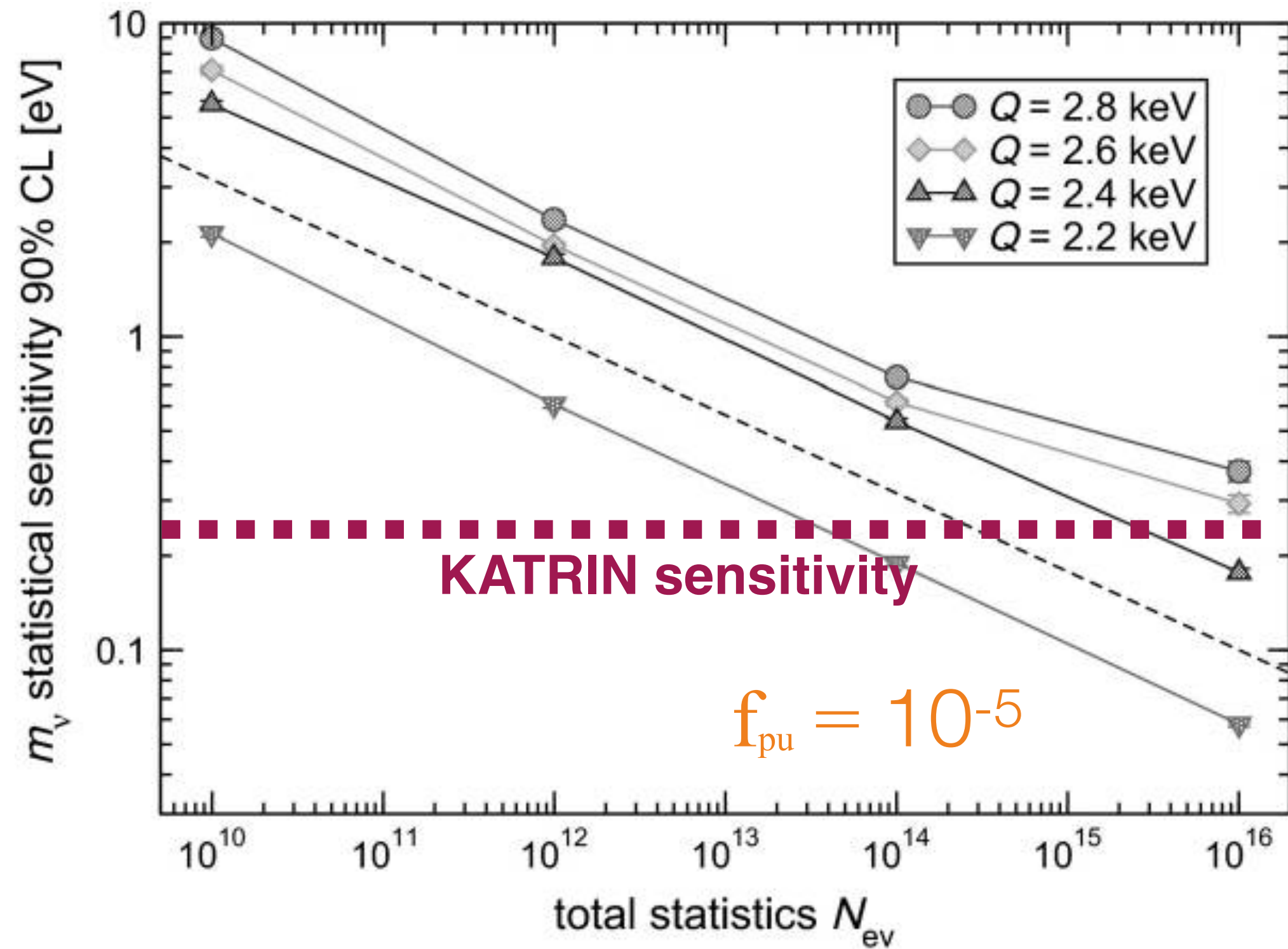


- For competitive  $m_\nu$  sensitivity, we need  $\sim 10^{14}$  decays
  - $\sim$  MBq activity for few-year run-times
  - $2 \times 10^{11}$  atoms = 1Bq; we need  $\sim 10^{17}$  atoms

$$f_{pu} = A_{EC} \tau_R$$

↑ 2-event pile-up probability     
 ↑ activity in the detector     
 ← time resolution

# How much $^{163}\text{Ho}$ do we need?



- For competitive  $m_\nu$  sensitivity, we need  $\sim 10^{14}$  decays
  - $\sim$  MBq activity for few-year run-times
  - $2 \times 10^{11}$  atoms = 1Bq; we need  $\sim 10^{17}$  atoms

$$f_{pu} = A_{EC} \tau_R$$

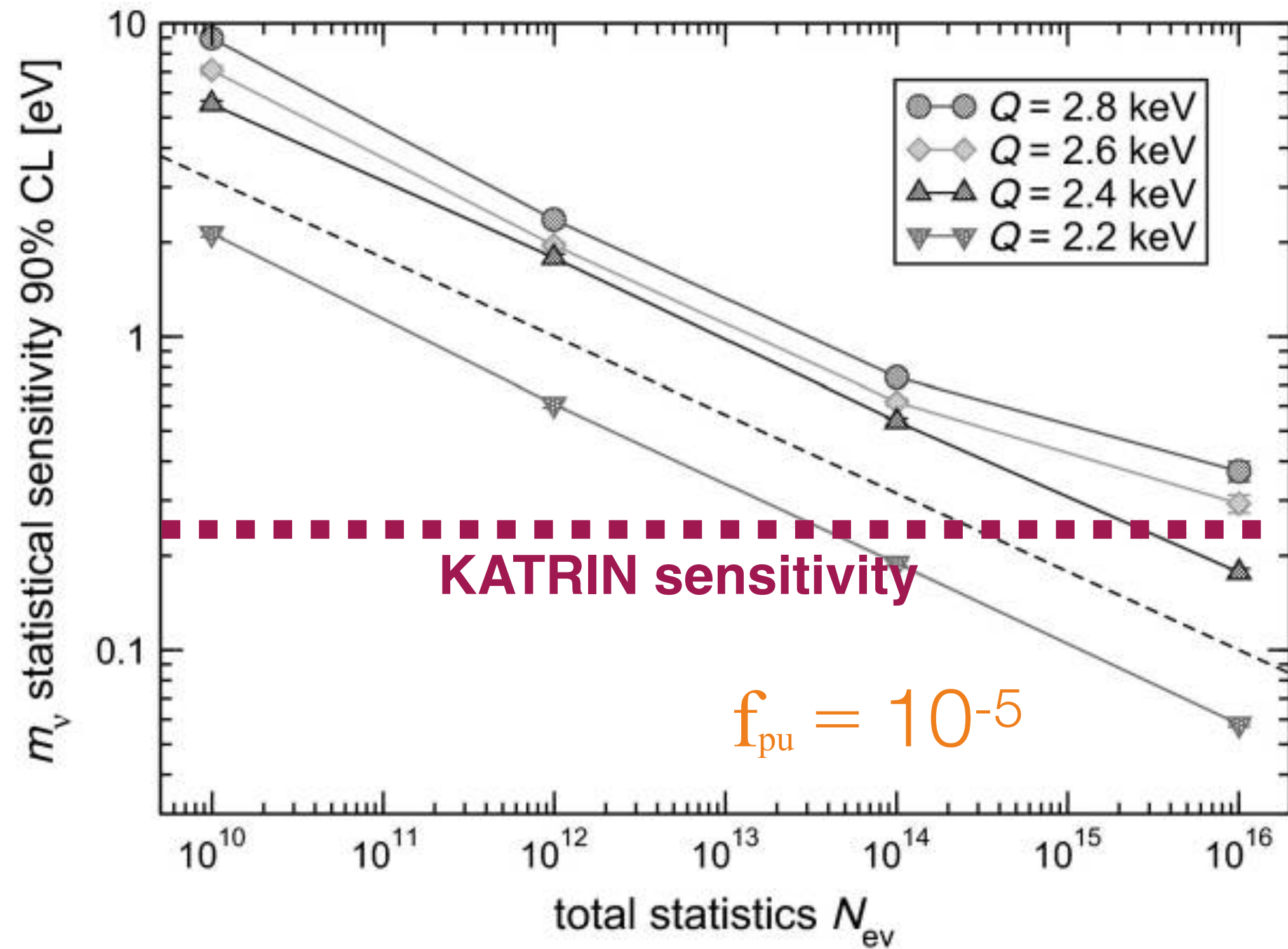
↑ 2-event pile-up probability    
 ↑ activity in the detector    
 ← time resolution

We need  $f_{pu} < 10^{-5}$

Typical  $\tau_R \sim \mu\text{s}$

Do we have a problem?

# How much $^{163}\text{Ho}$ do we need?



- For competitive  $m_\nu$  sensitivity, we need  $\sim 10^{14}$  decays
  - $\sim$  MBq activity for few-year run-times
  - $2 \times 10^{11}$  atoms = 1Bq; we need  $\sim 10^{17}$  atoms
- **Pile-up** can be a limiting factor

$$f_{pu} = A_{EC} \tau_R$$

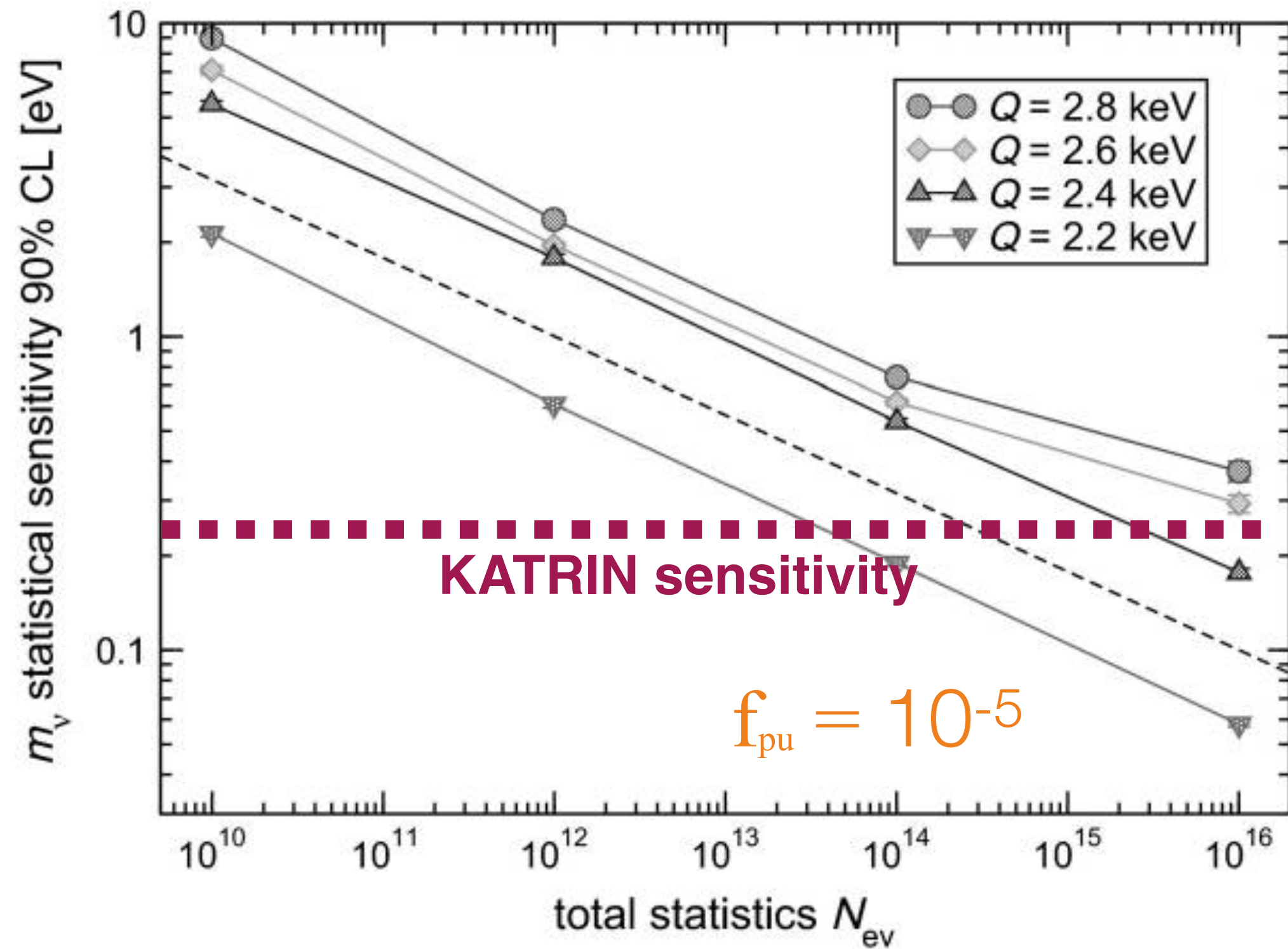
↑ 2-event pile-up probability    
 ↑ activity in the detector    
 ← time resolution

We need  $f_{pu} < 10^{-5}$

Typical  $\tau_R \sim \mu\text{s}$

Do we have a problem?

# How much $^{163}\text{Ho}$ do we need?

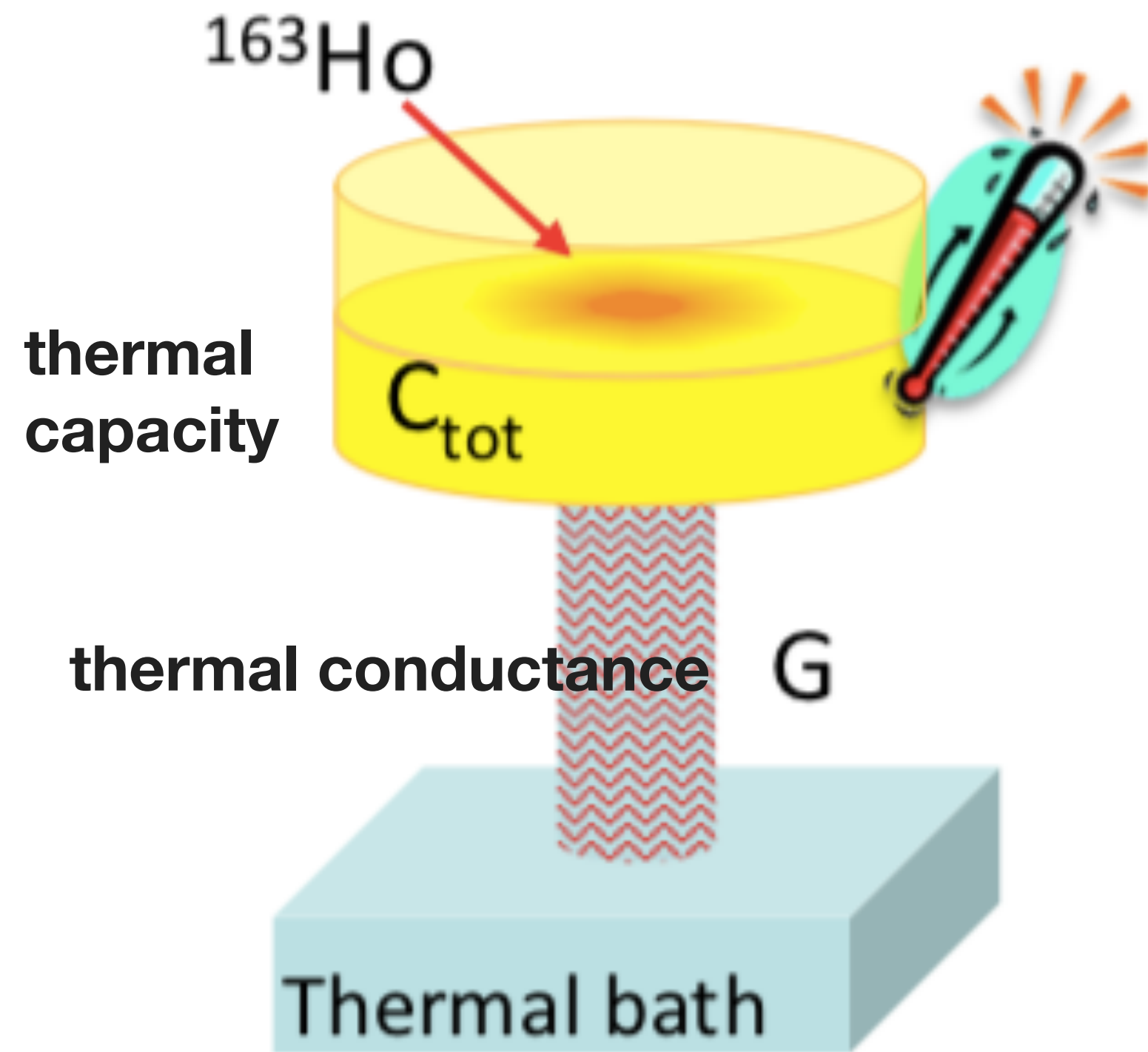


- For competitive  $m_\nu$  sensitivity, we need  $\sim 10^{14}$  decays
  - $\sim$  MBq activity for few-year run-times
  - $2 \times 10^{11}$  atoms = 1Bq; we need  $\sim 10^{17}$  atoms
- **Pile-up** can be a limiting factor
  - Separate detector into **micro-calorimeter pixels**
- Energy resolution  $\Delta E < 3$  eV
- **Backgrounds**  $< 10^{-5}$  events/eV/detector/day

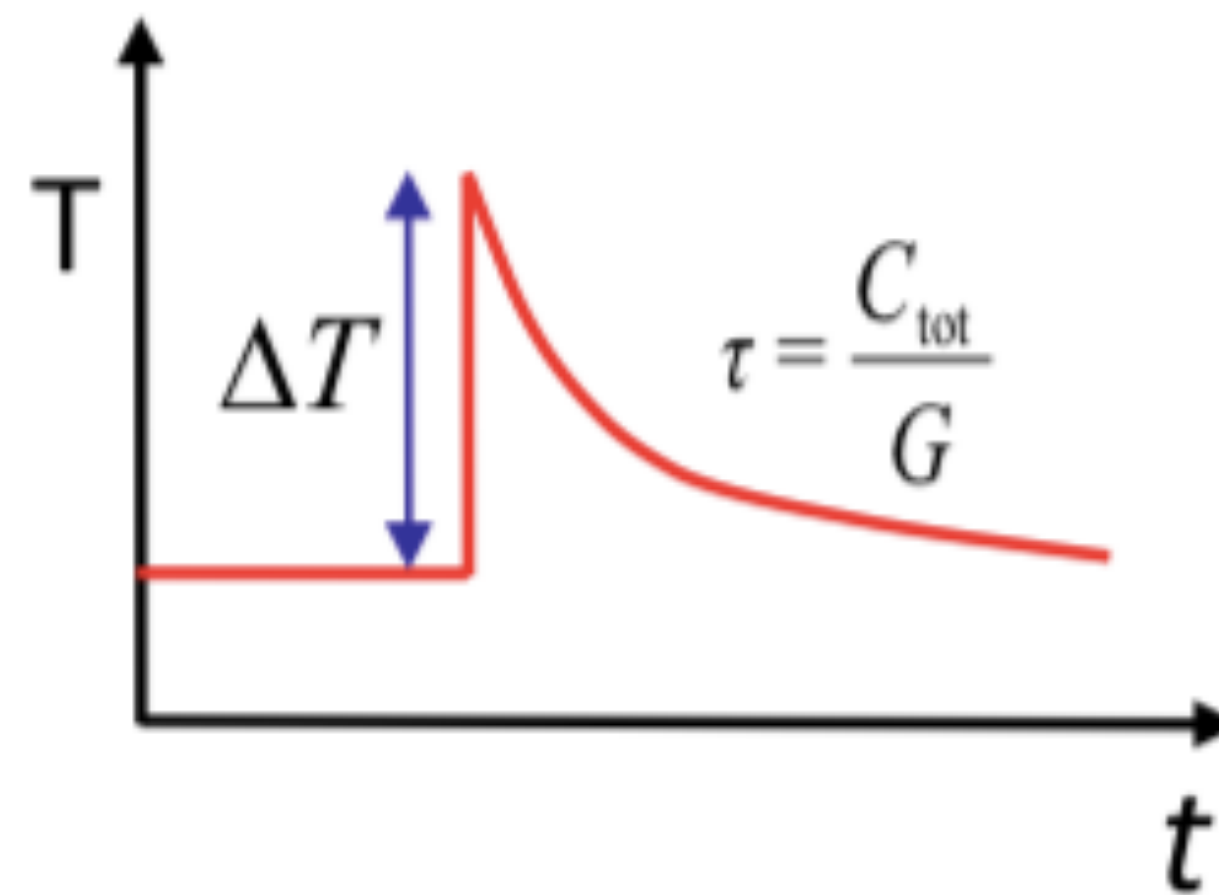


Eur Phys J C Part Fields. 2015; 75(3): 112.





$$\Delta T \cong \frac{E}{C_{\text{tot}}}$$



- $\mathcal{O}(10^3 \text{ to } 10^6)$  individual detectors
- $\mathcal{O}(10^{14})$   $^{163}\text{Ho}$  atoms per detector
- **Very small volume**
- **Working temperature < 100 mK**
  - Low specific heat
  - Reduce thermal noise
- **Very sensitive temperature sensor**



L Gastaldo, Neutrino 2018  
doi: 10.5281/zenodo/1286949



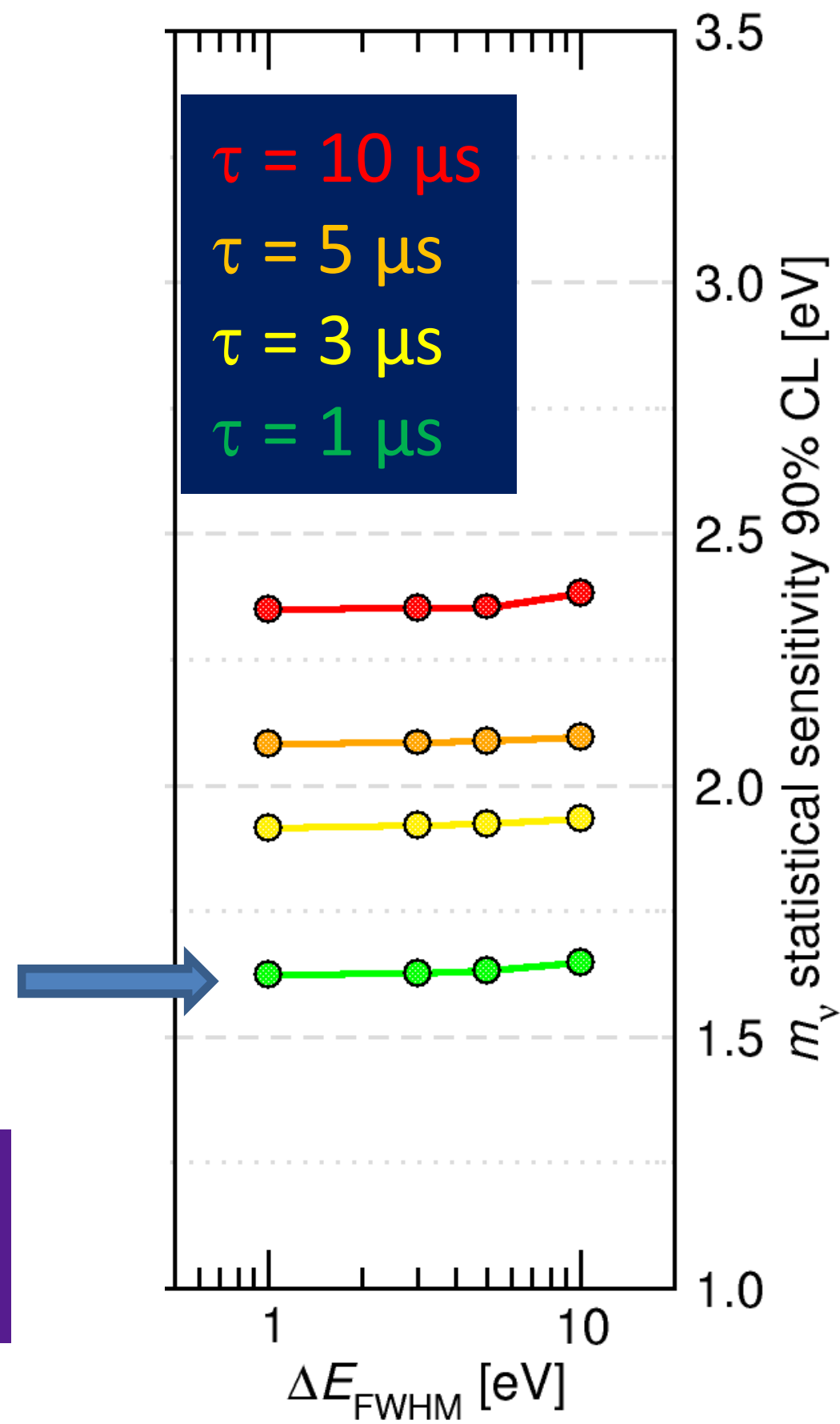
1024 detectors (16 arrays)

$6.5 \times 10^{16}$   $^{163}\text{Ho}$  nuclei (18  $\mu\text{g}$ )

$3 \times 10^{13}$  events

$3 \times 10^{13}$  events (300Bq / pixel)

$\Delta E_{\text{FWHM}} \sim 3\text{-}5\text{eV}$ ;  $\Delta t \sim 10 \mu\text{s}$





1024 detectors (16 arrays)

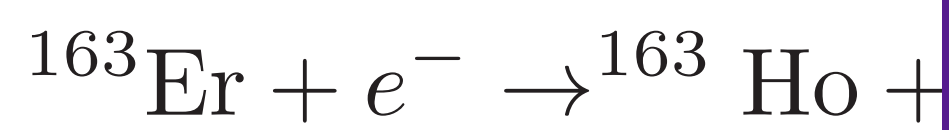


$6.5 \times 10^{16}$   $^{163}\text{Ho}$  nuclei (18  $\mu\text{g}$ )

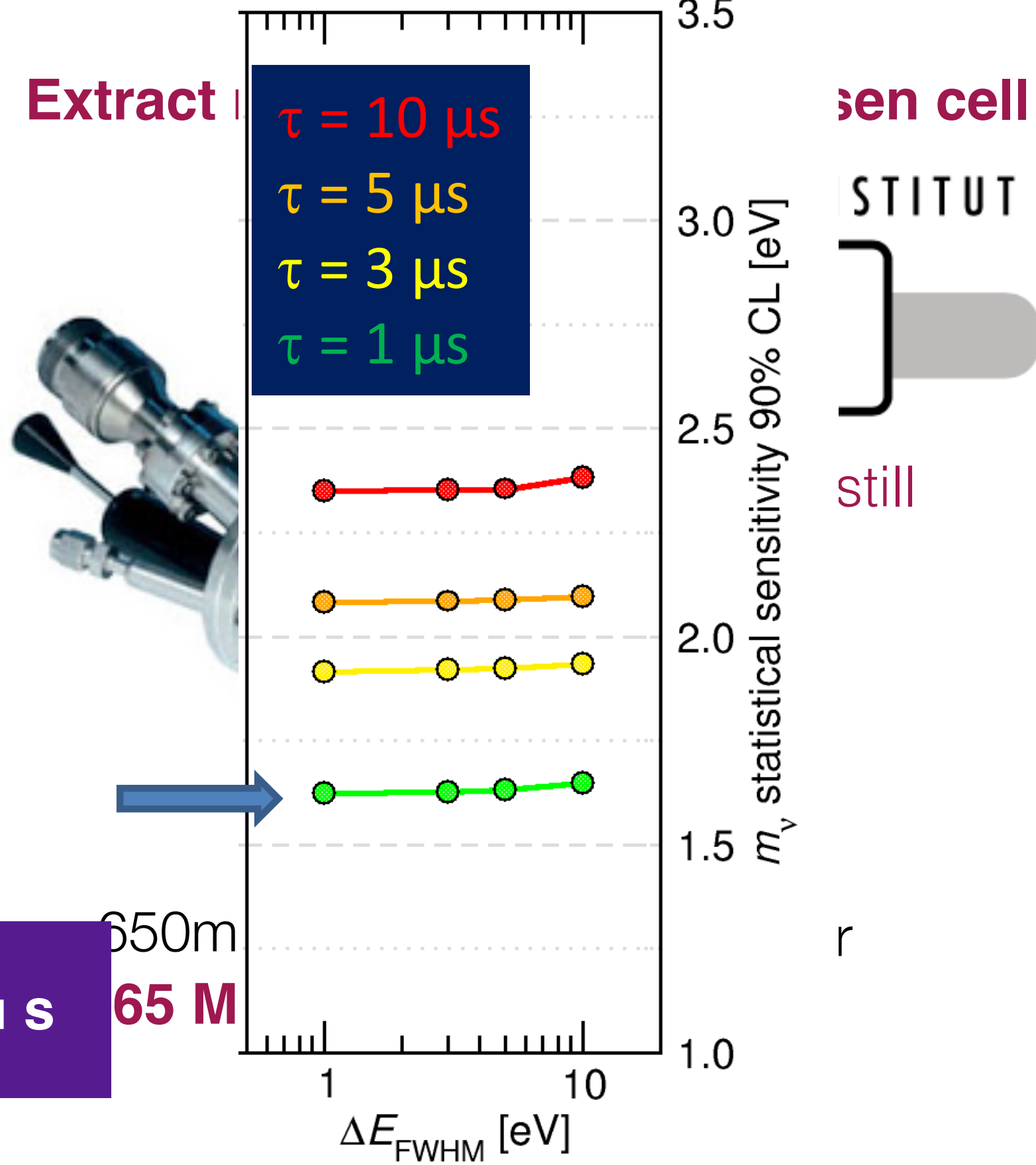
$3 \times 10^{13}$  events

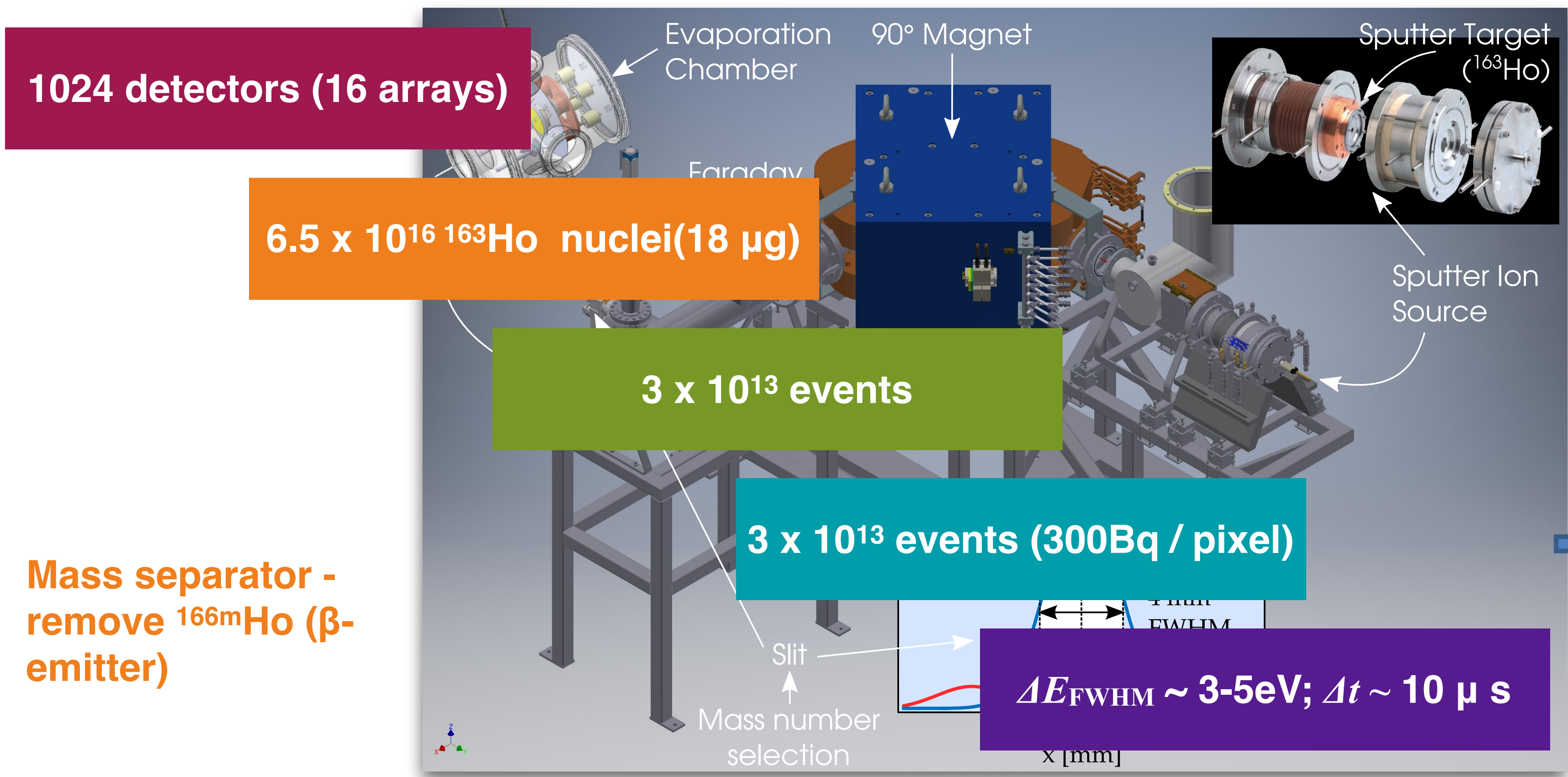
$3 \times 10^{13}$  events (300Bq / pixel)

Enriched erbium(III) oxide



$\Delta E_{\text{FWHM}} \sim 3\text{-}5\text{eV}; \Delta t \sim 10 \mu\text{s}$





1024 detectors (16 arrays)

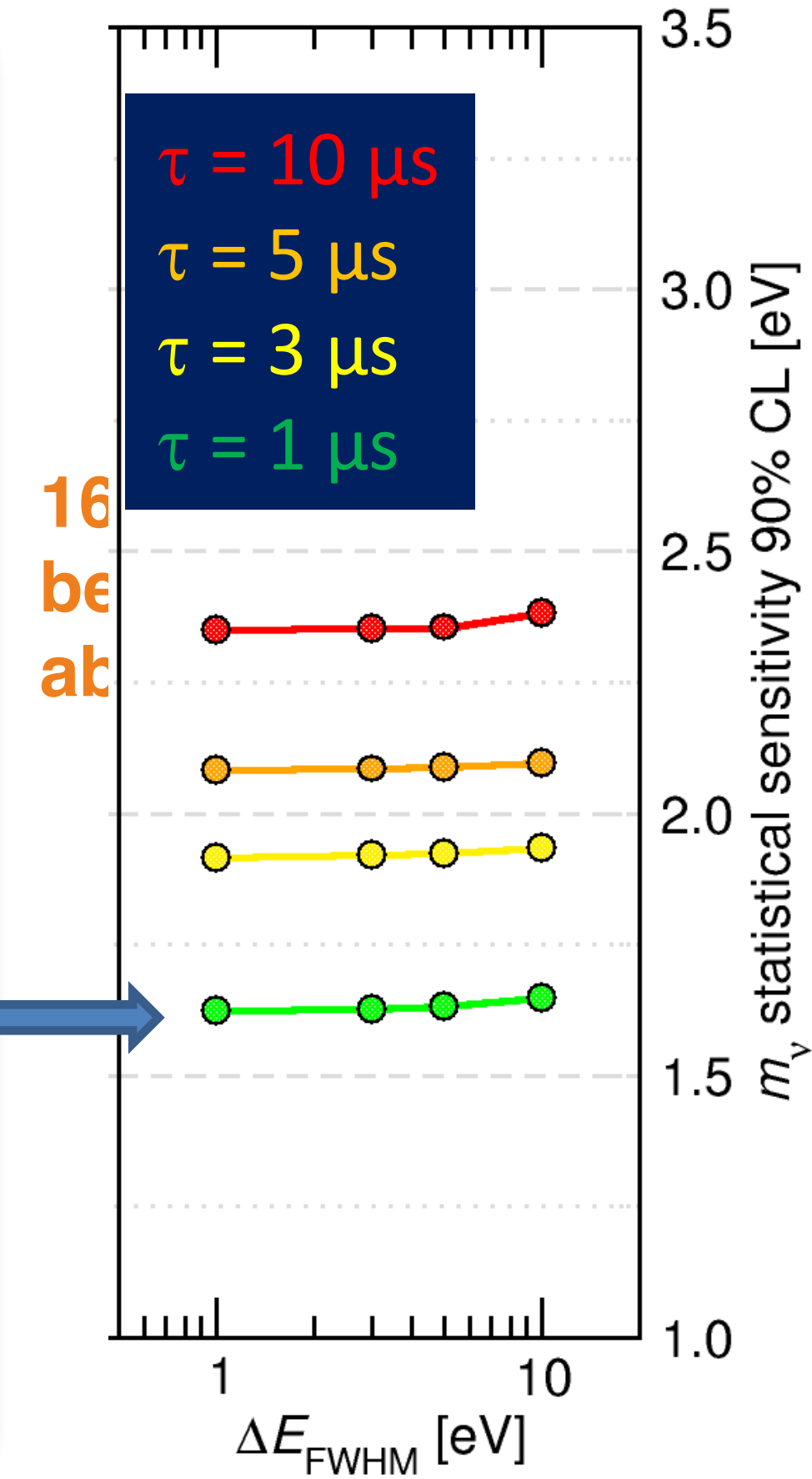
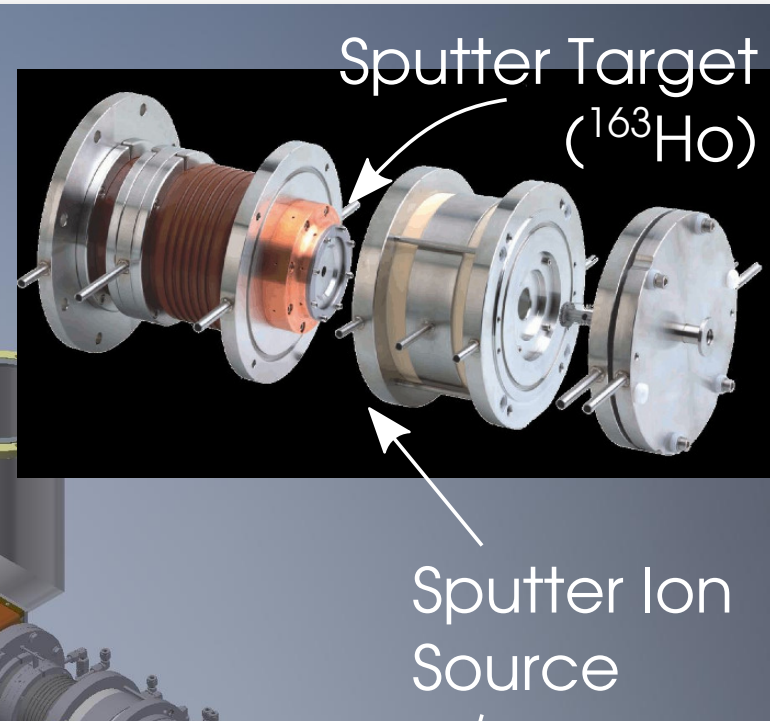
$6.5 \times 10^{16}$   $^{163}\text{Ho}$  nuclei (18  $\mu\text{g}$ )

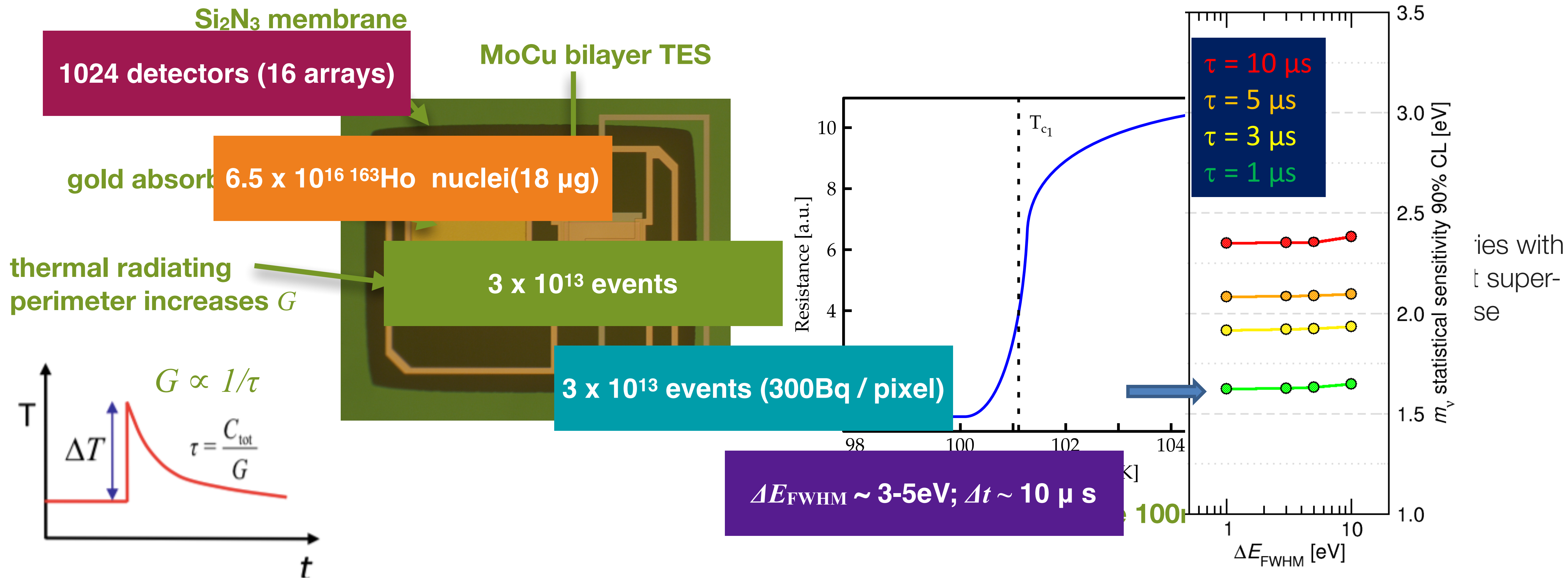
$3 \times 10^{13}$  events

$3 \times 10^{13}$  events (300Bq / pixel)

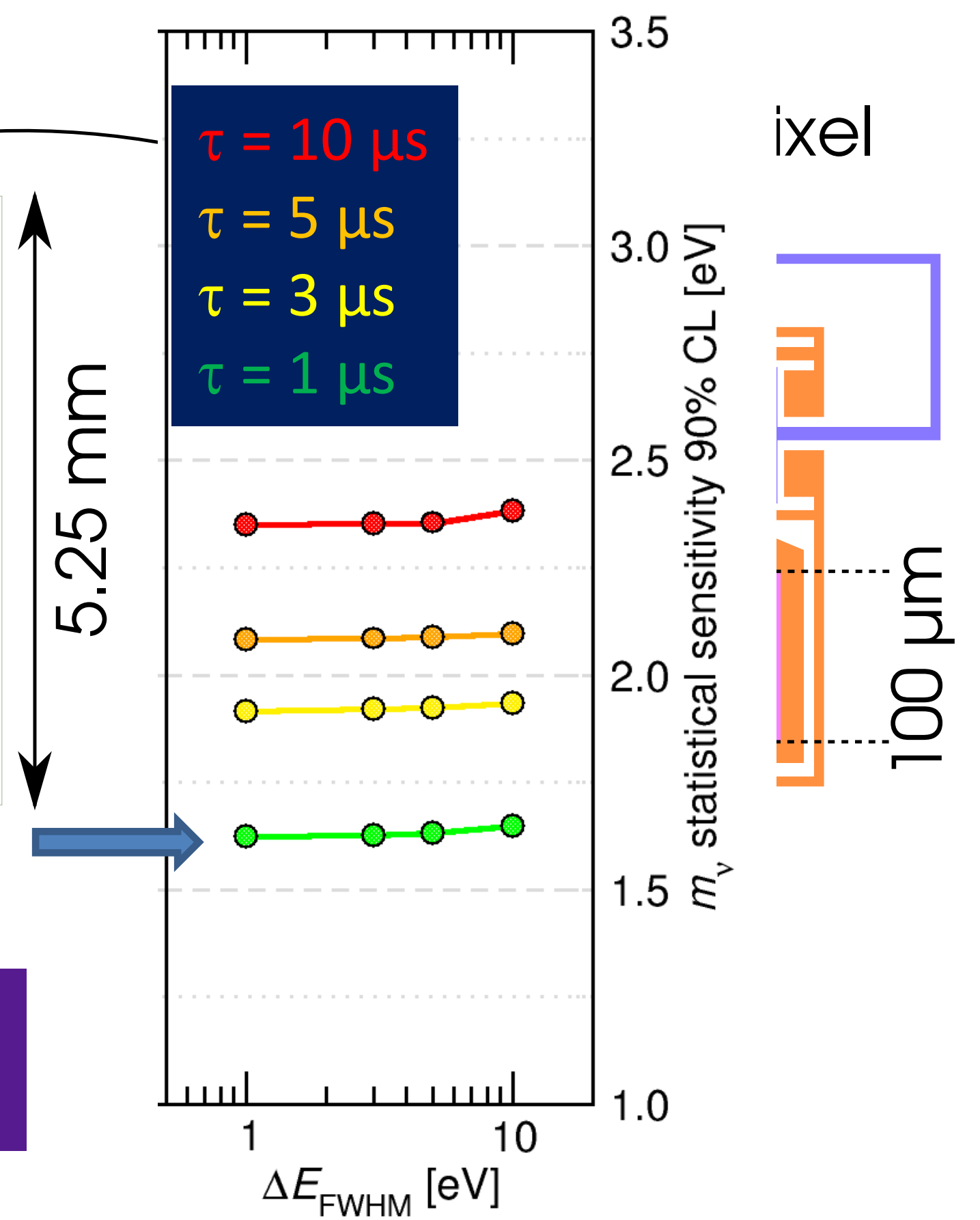
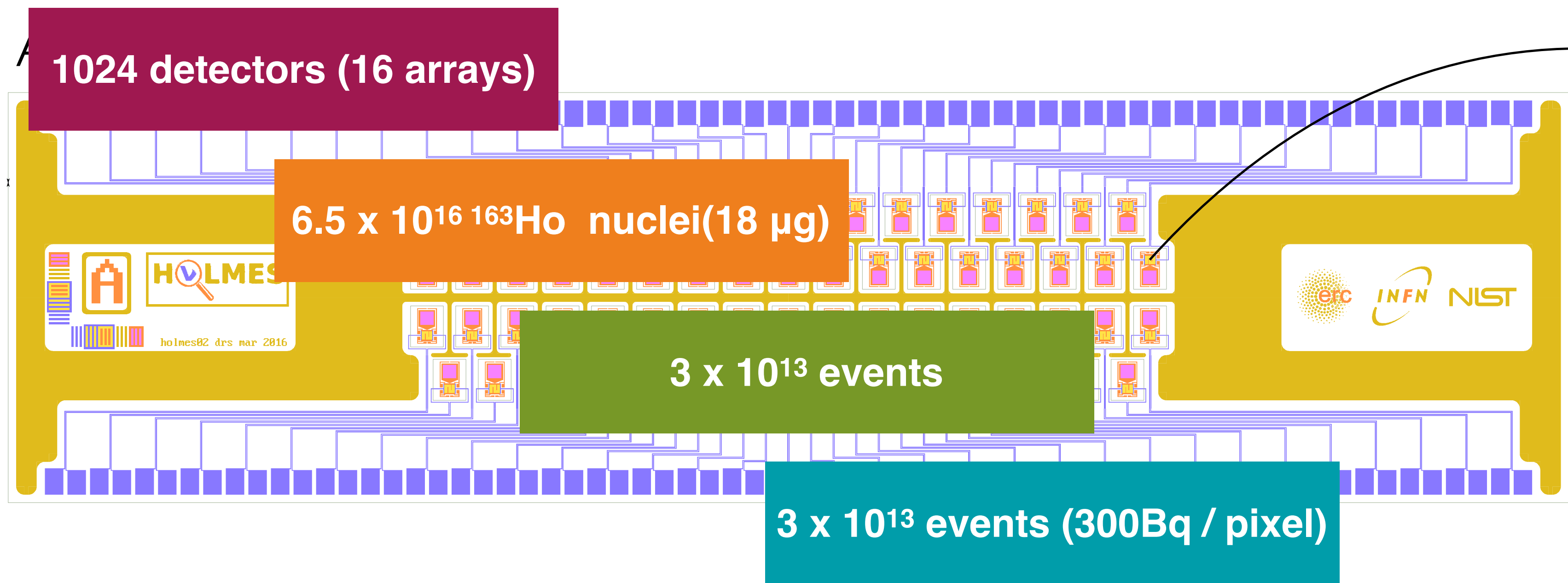
Mass separator - remove  $^{166\text{m}}\text{Ho}$  ( $\beta$ -emitter)

$\Delta E_{\text{FWHM}} \sim 3\text{-}5\text{eV}; \Delta t \sim 10 \mu\text{s}$





ies with  
t super-  
se



- TES current converted and modulated using rf SQUID
  - Each channel at different frequency
  - **4x16 detector** prototype
- $\Delta E_{\text{FWHM}} \sim 3\text{-}5\text{eV}; \Delta t \sim 10 \mu\text{s}$



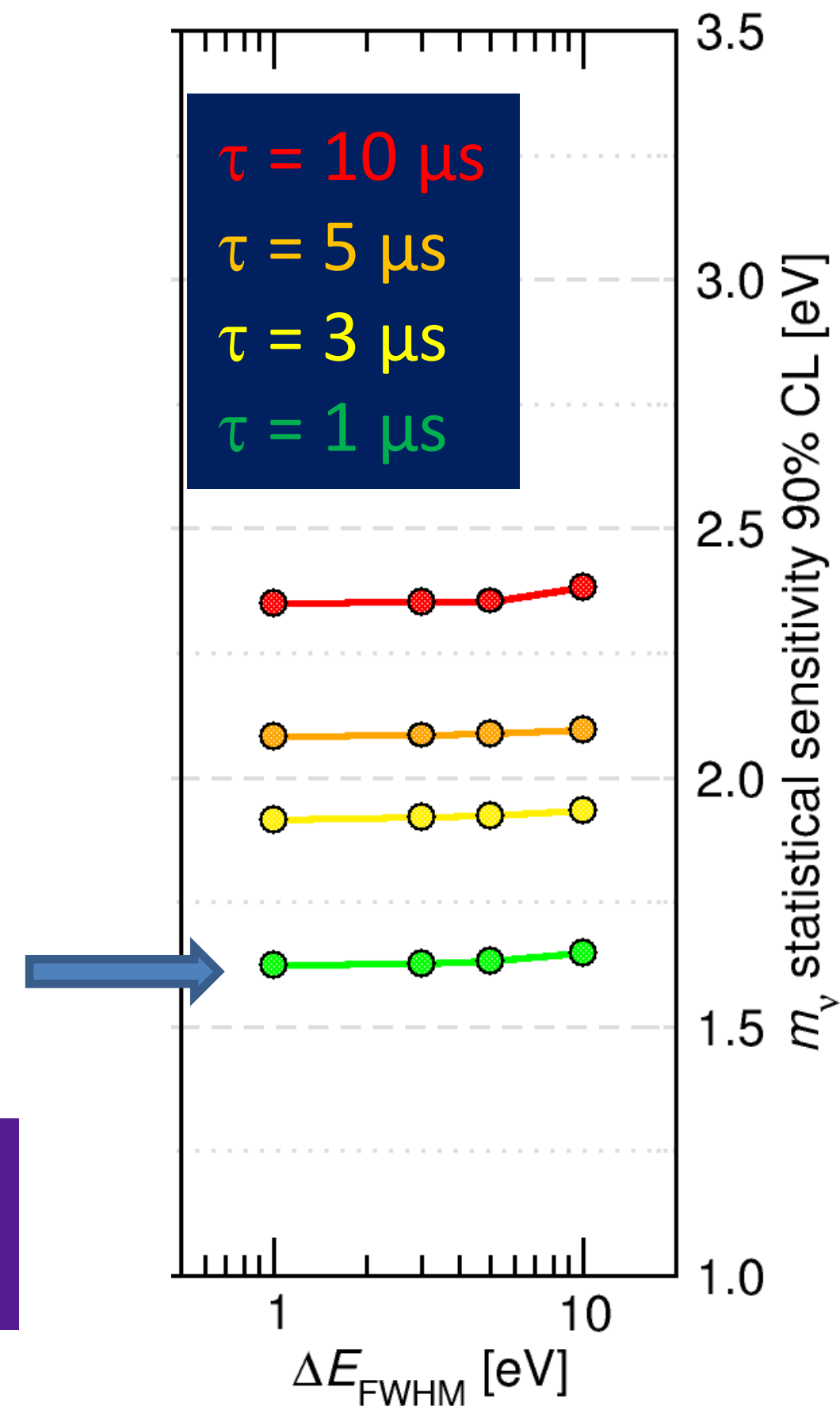
1024 detectors (16 arrays)

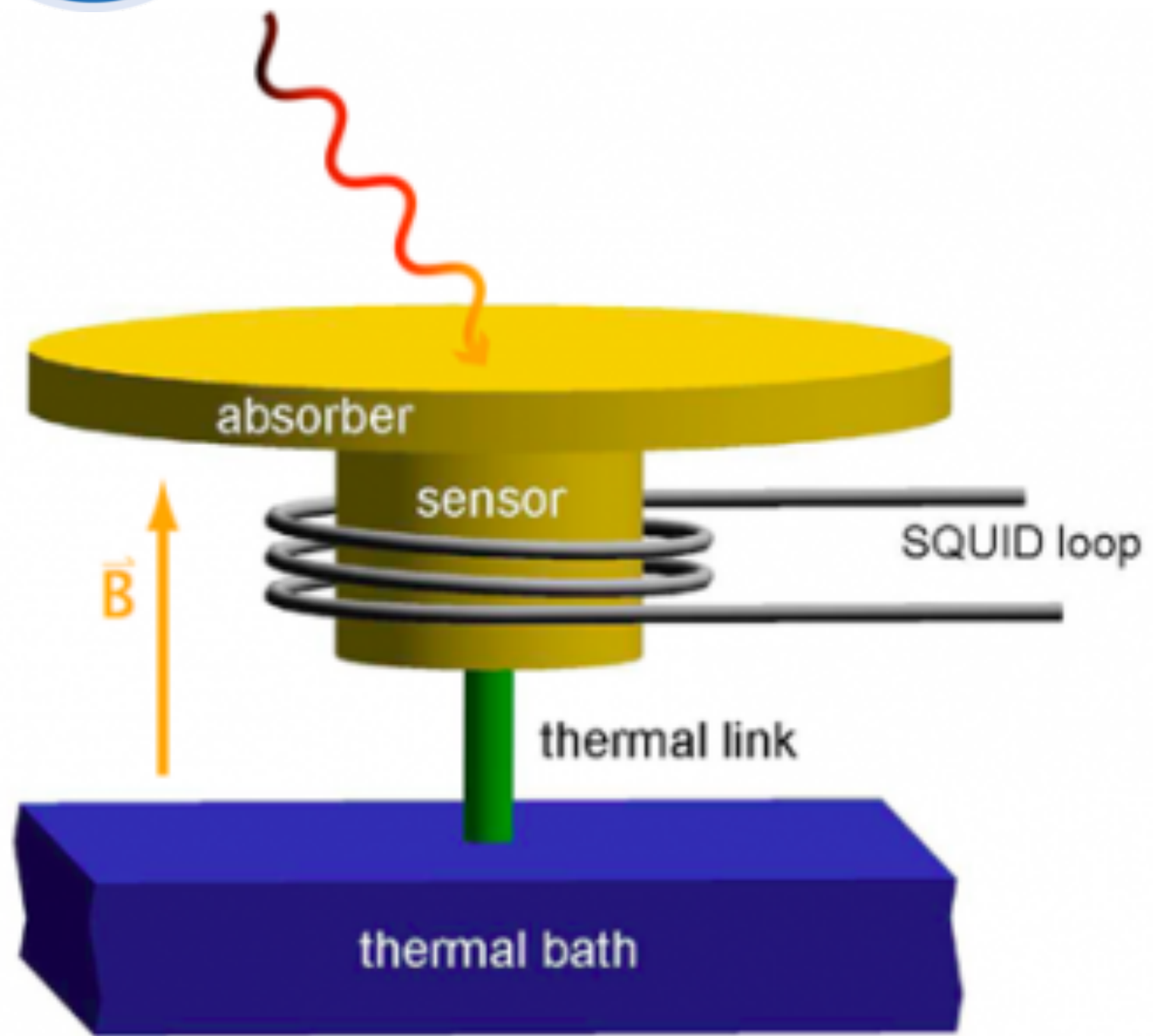
$6.5 \times 10^{16}$   $^{163}\text{Ho}$  nuclei (18  $\mu\text{g}$ )

$3 \times 10^{13}$  events

$3 \times 10^{13}$  events (300Bq / pixel)

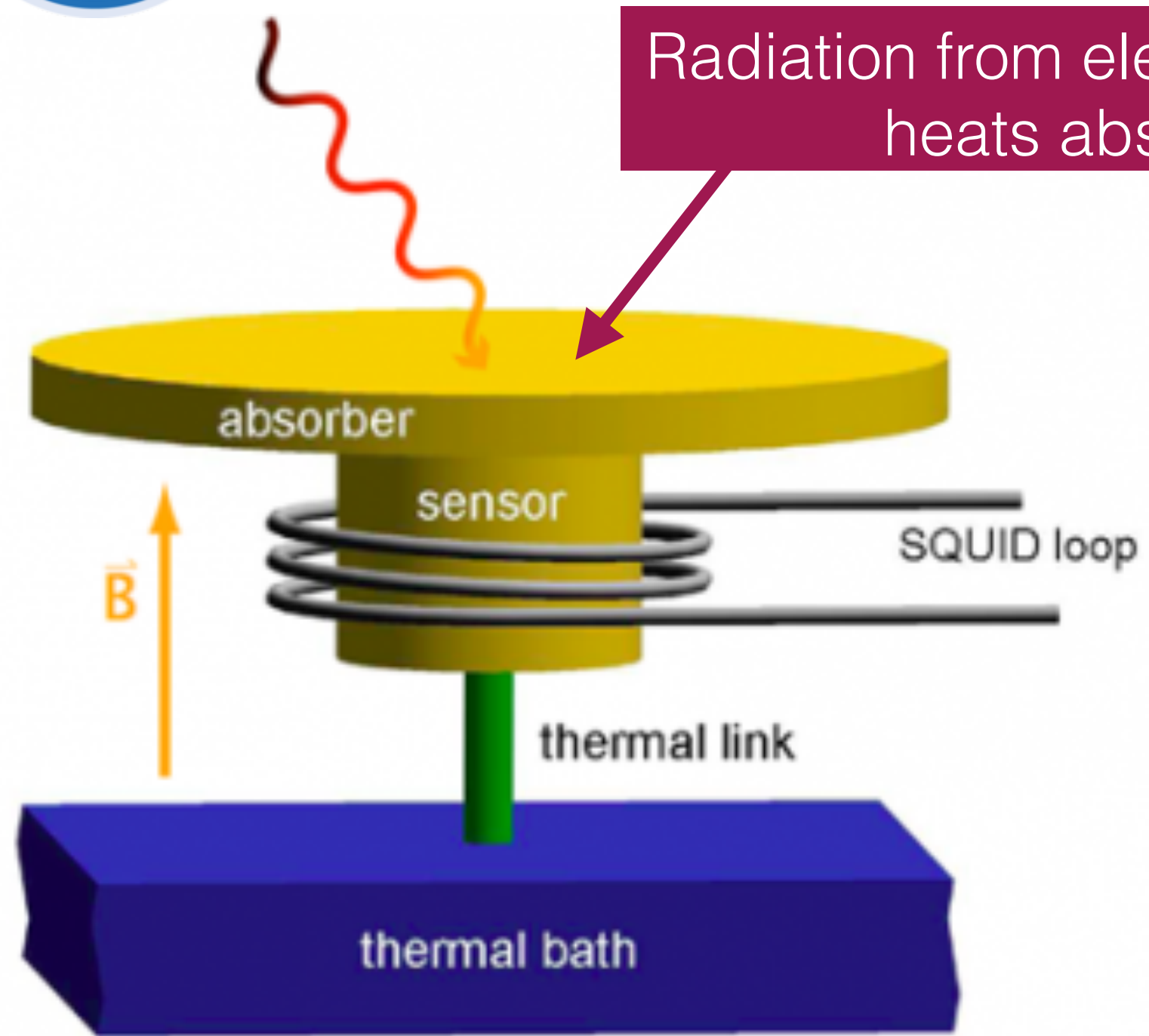
$\Delta E_{\text{FWHM}} \sim 3\text{-}5\text{eV}$ ;  $\Delta t \sim 10 \mu\text{s}$



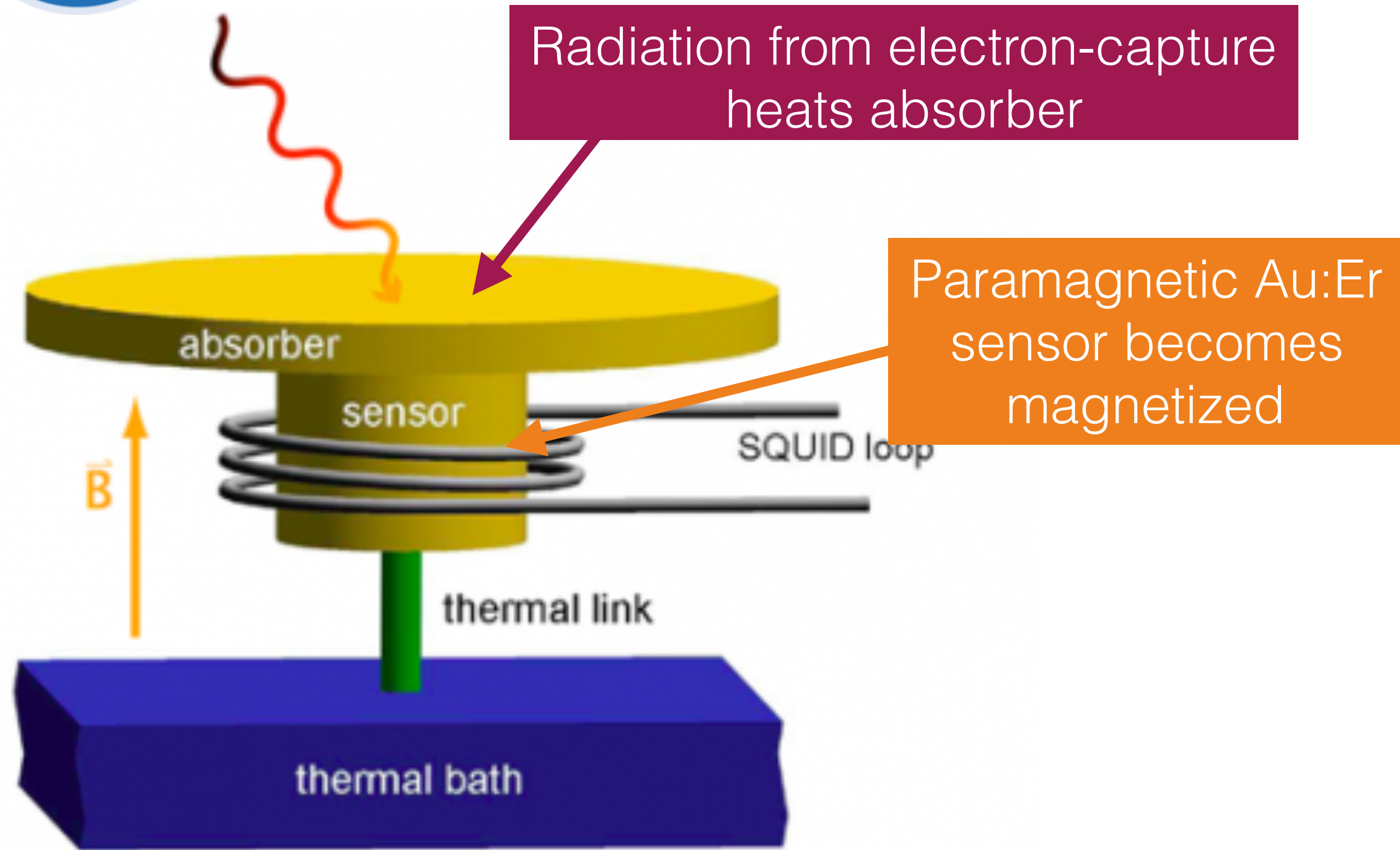


*AIP Conf. Proc. 1185, 571, (2009)*

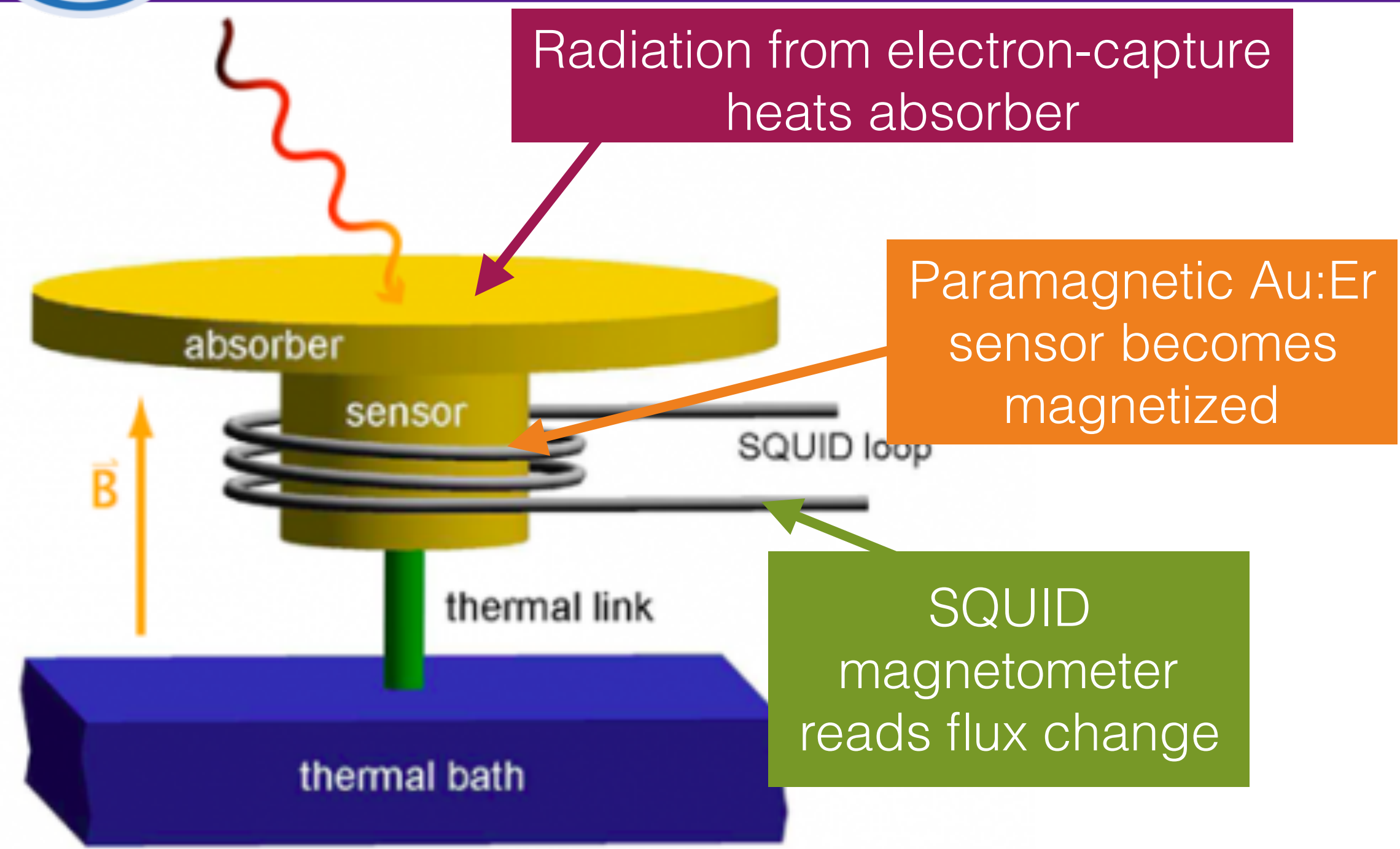




*AIP Conf. Proc. 1185, 571, (2009)*

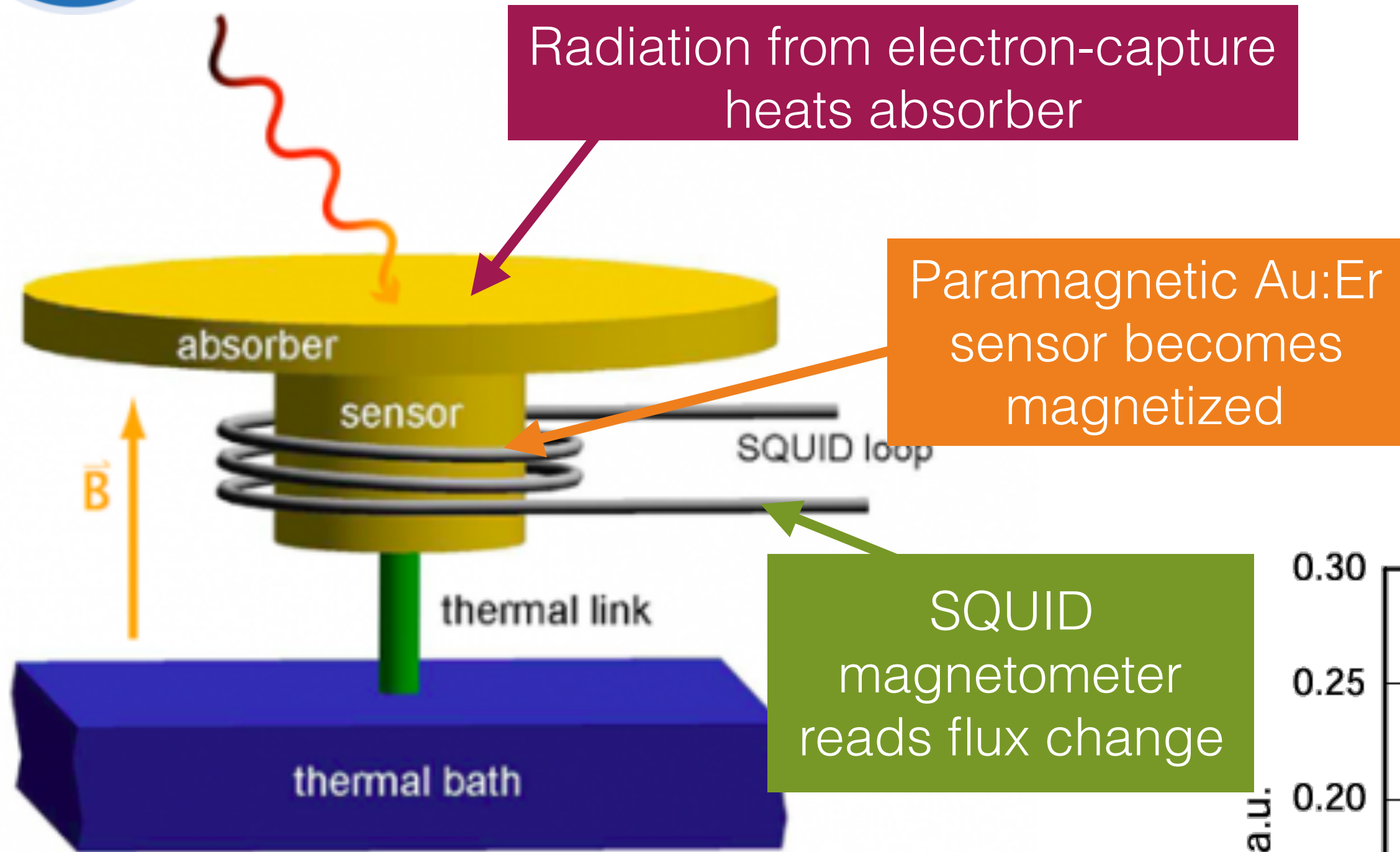


*AIP Conf. Proc. 1185, 571, (2009)*



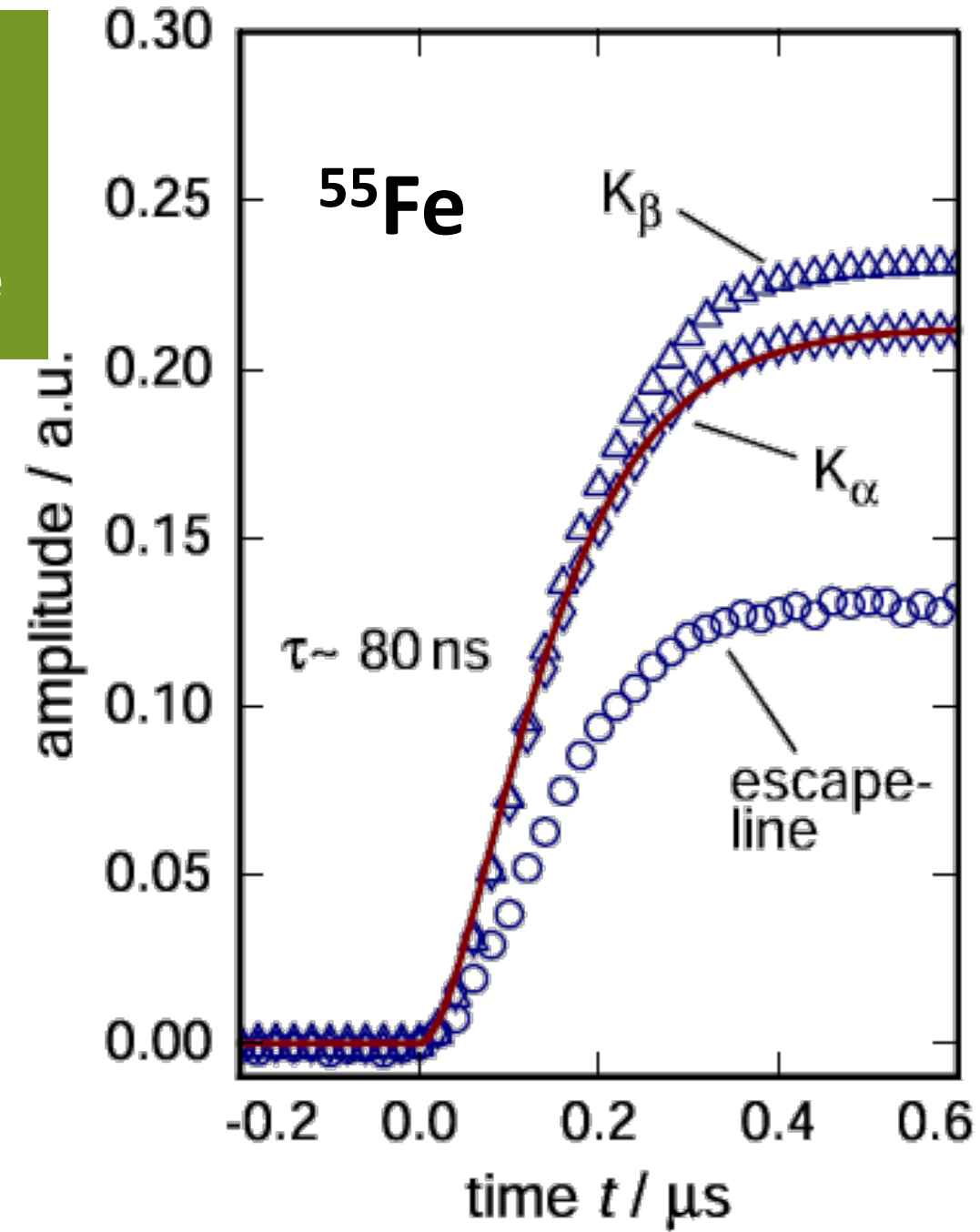
$$\Delta\Phi_s \propto \frac{\partial M}{\partial T} \Delta T \rightarrow \Delta\Phi_s \propto \frac{\partial M}{\partial T} \frac{E}{C_{\text{sens}} + C_{\text{abs}}}$$

*AIP Conf. Proc. 1185, 571, (2009)*

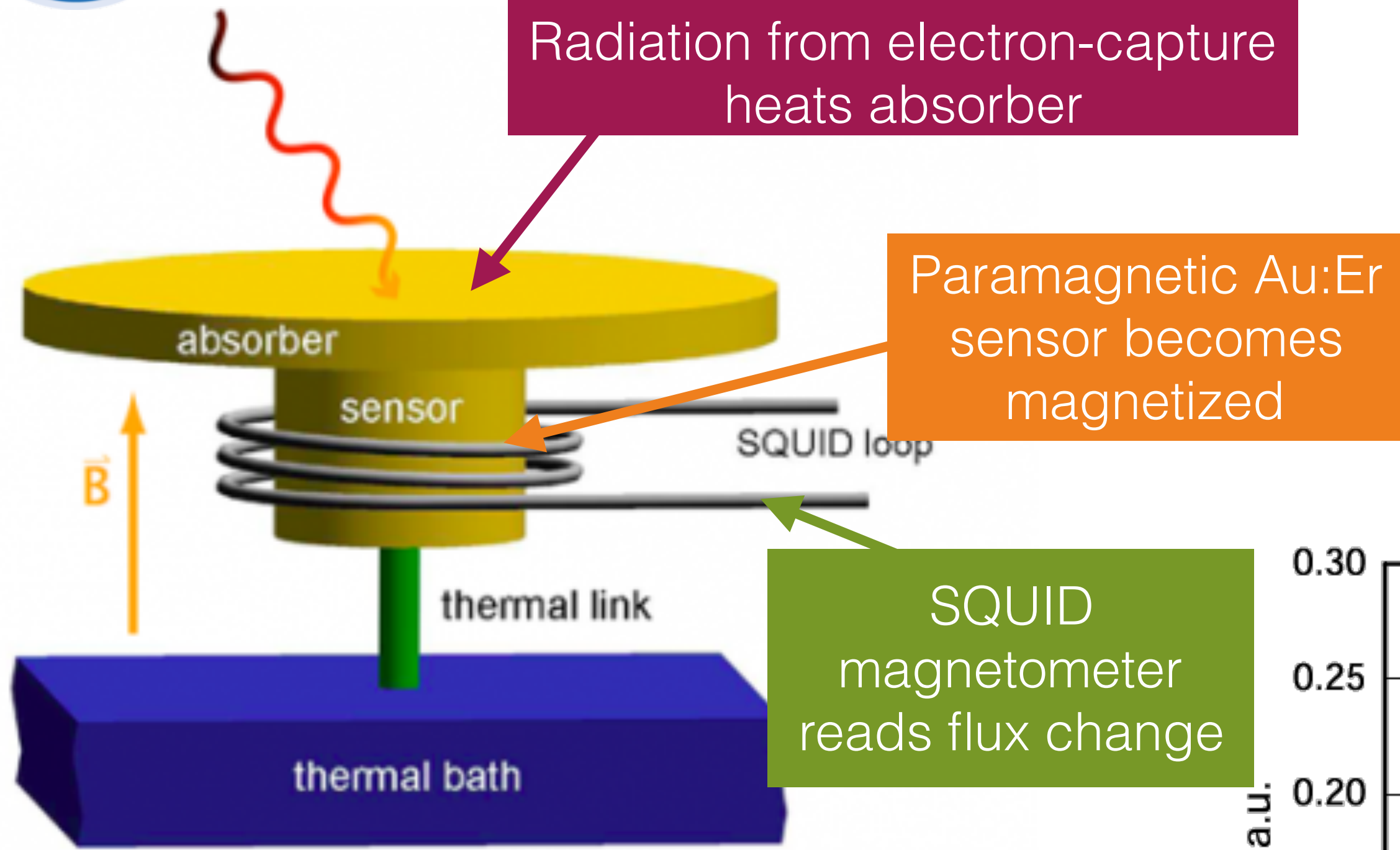


$$\Delta\Phi_s \propto \frac{\partial M}{\partial T} \Delta T \rightarrow \Delta\Phi_s \propto \frac{\partial M}{\partial T} \frac{E}{C_{\text{sens}} + C_{\text{abs}}}$$

Fast rise time reduces pile-up

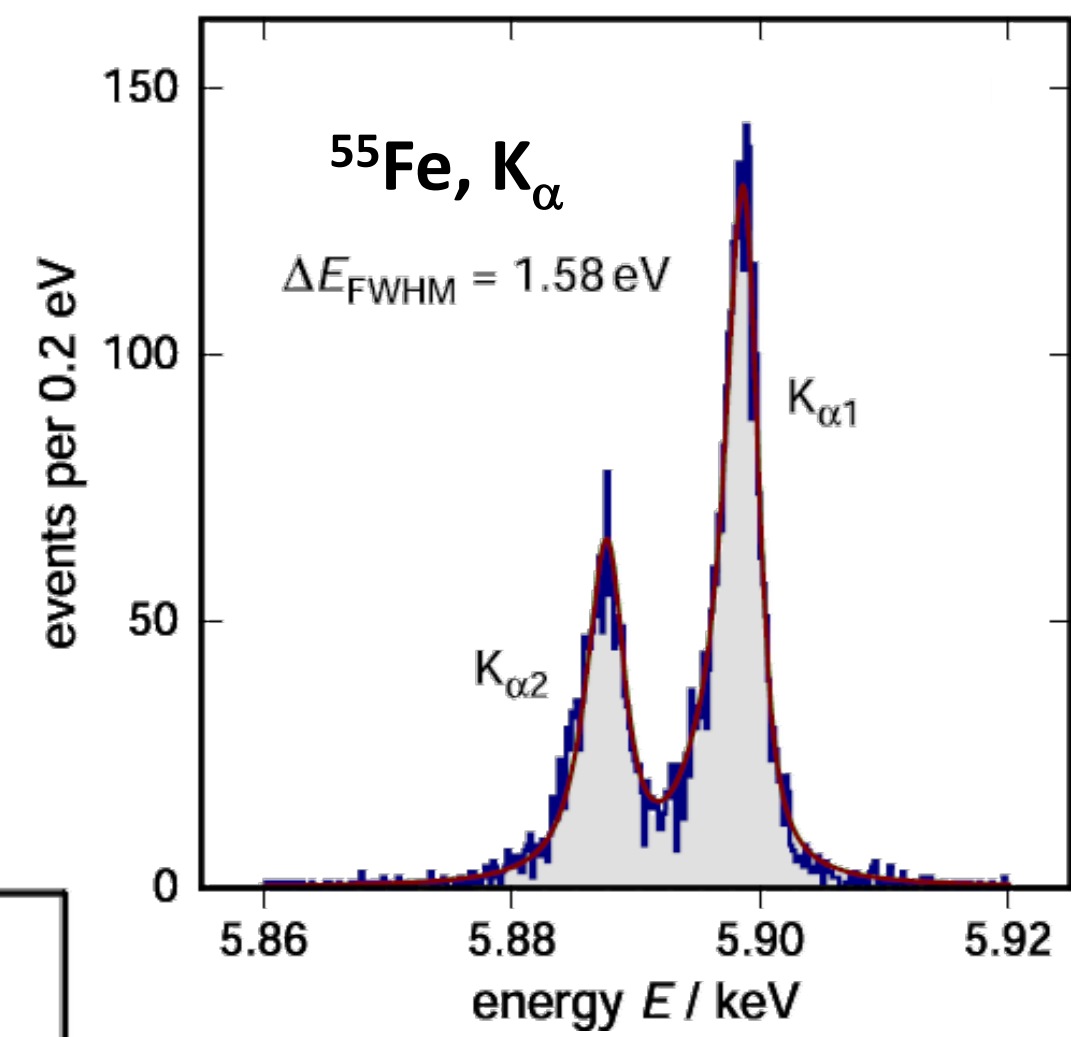
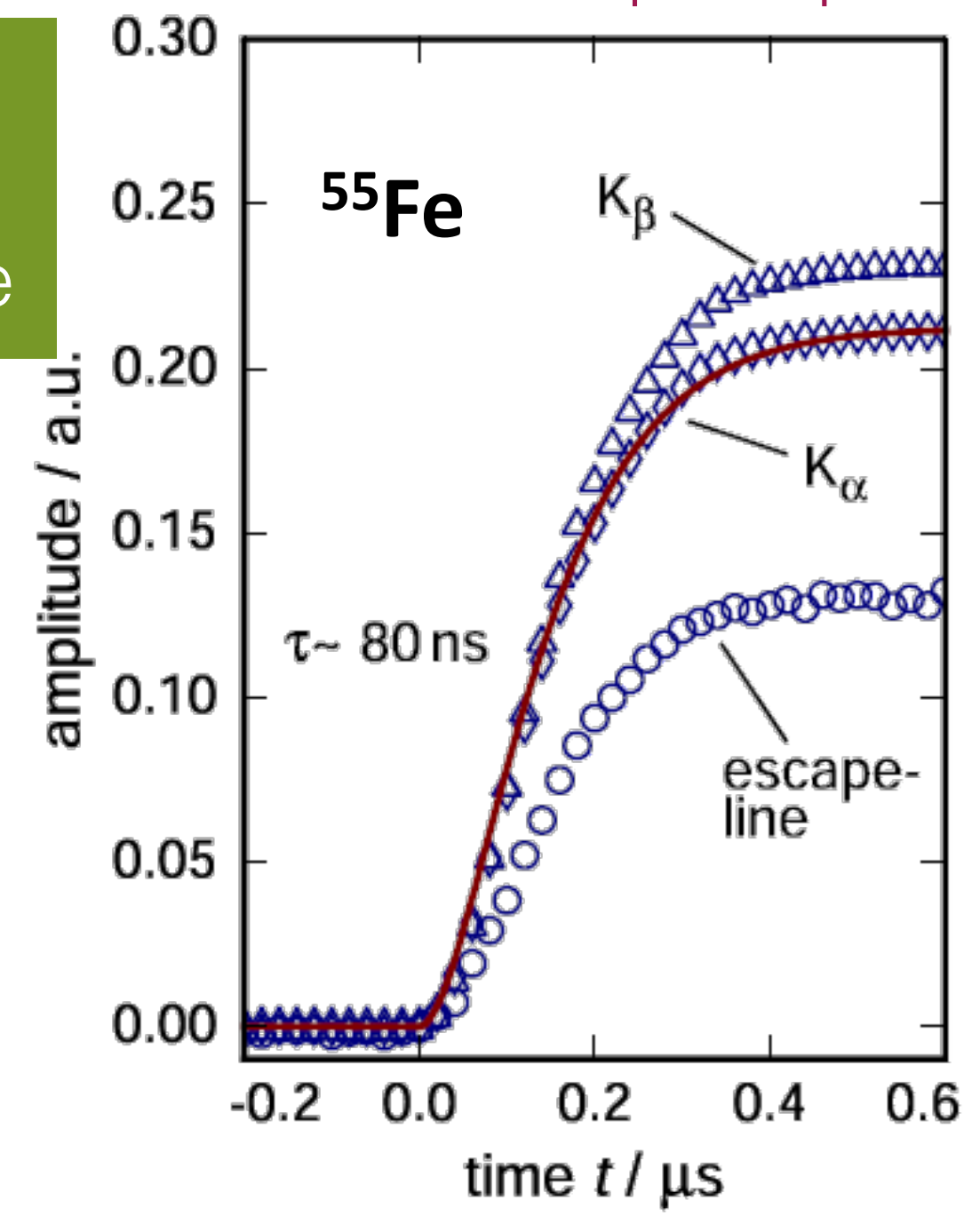


AIP Conf. Proc. 1185, 571, (2009)



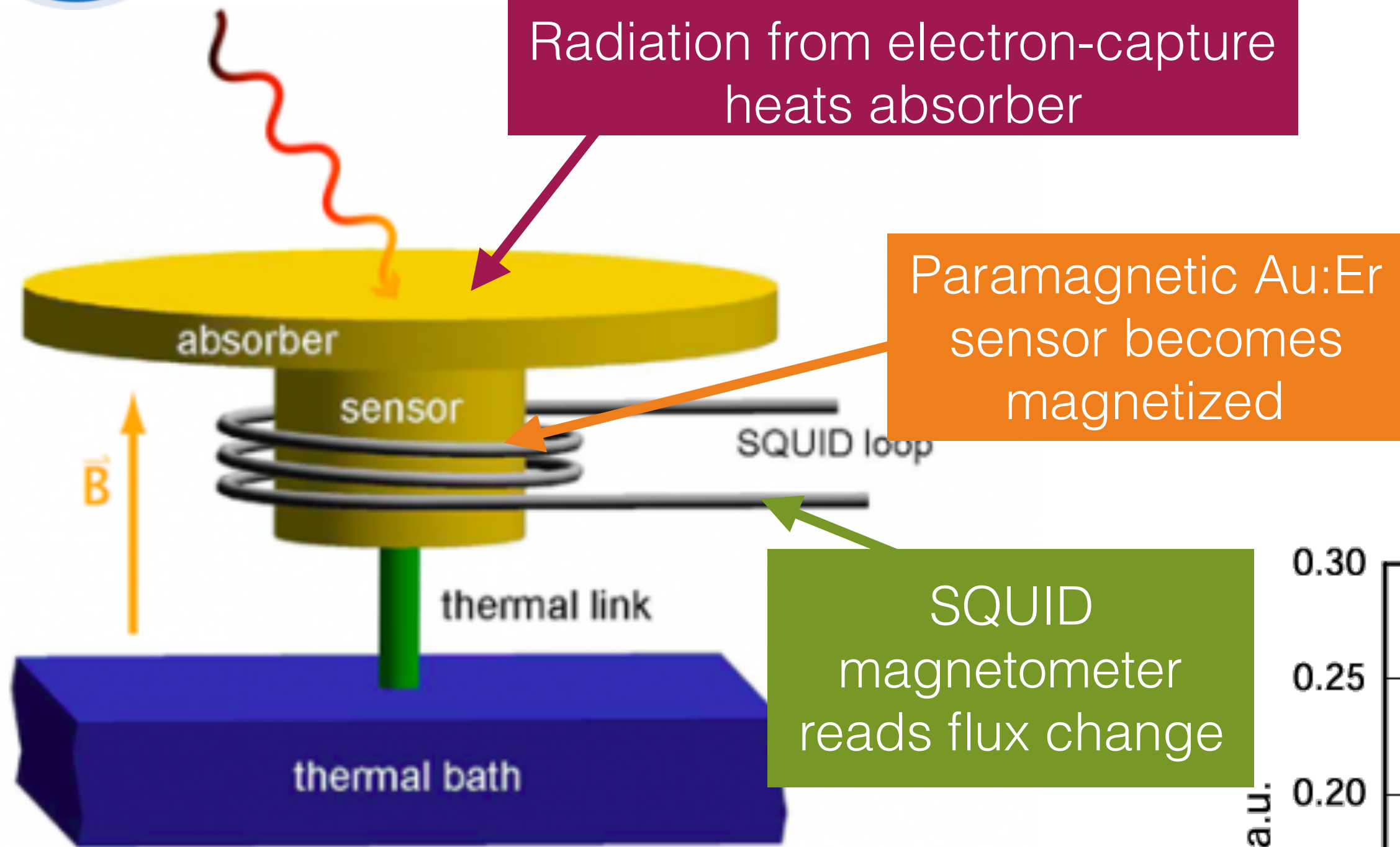
$$\Delta\Phi_s \propto \frac{\partial M}{\partial T} \Delta T \rightarrow \Delta\Phi_s \propto \frac{\partial M}{\partial T} \frac{E}{C_{\text{sens}} + C_{\text{abs}}}$$

Fast rise time reduces pile-up



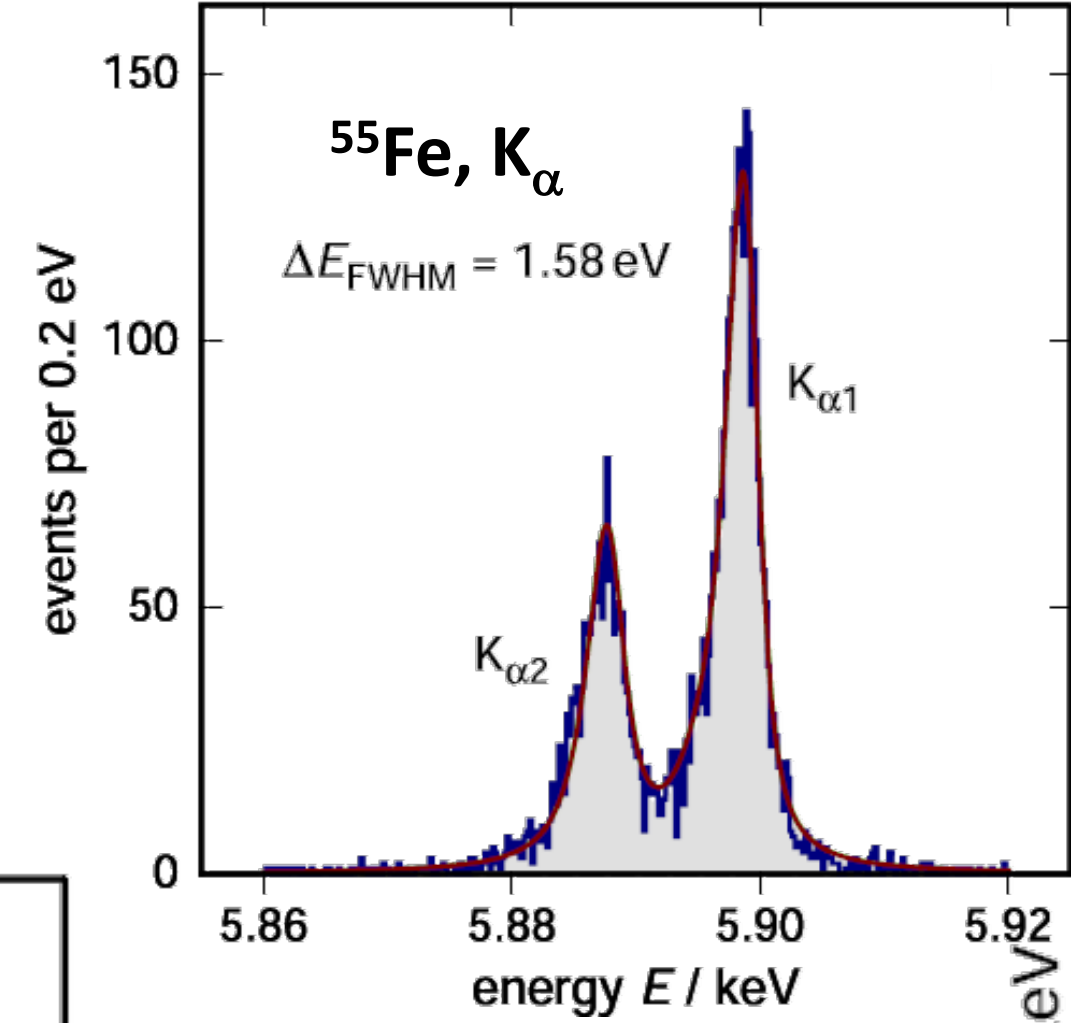
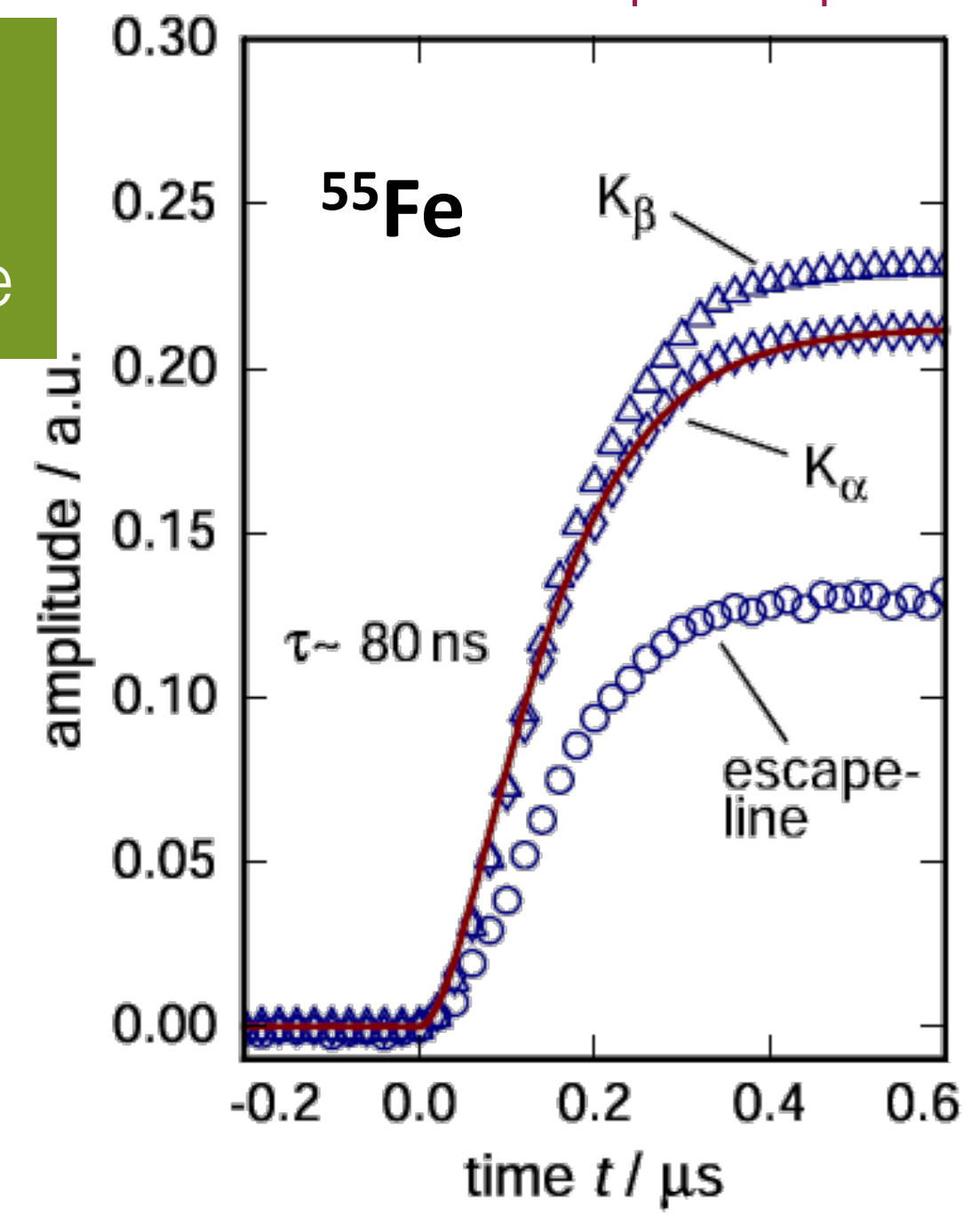
Excellent energy resolution  
 $\Delta E_{\text{FWHM}} \sim 1.6 \text{ eV}$

AIP Conf. Proc. 1185, 571, (2009)



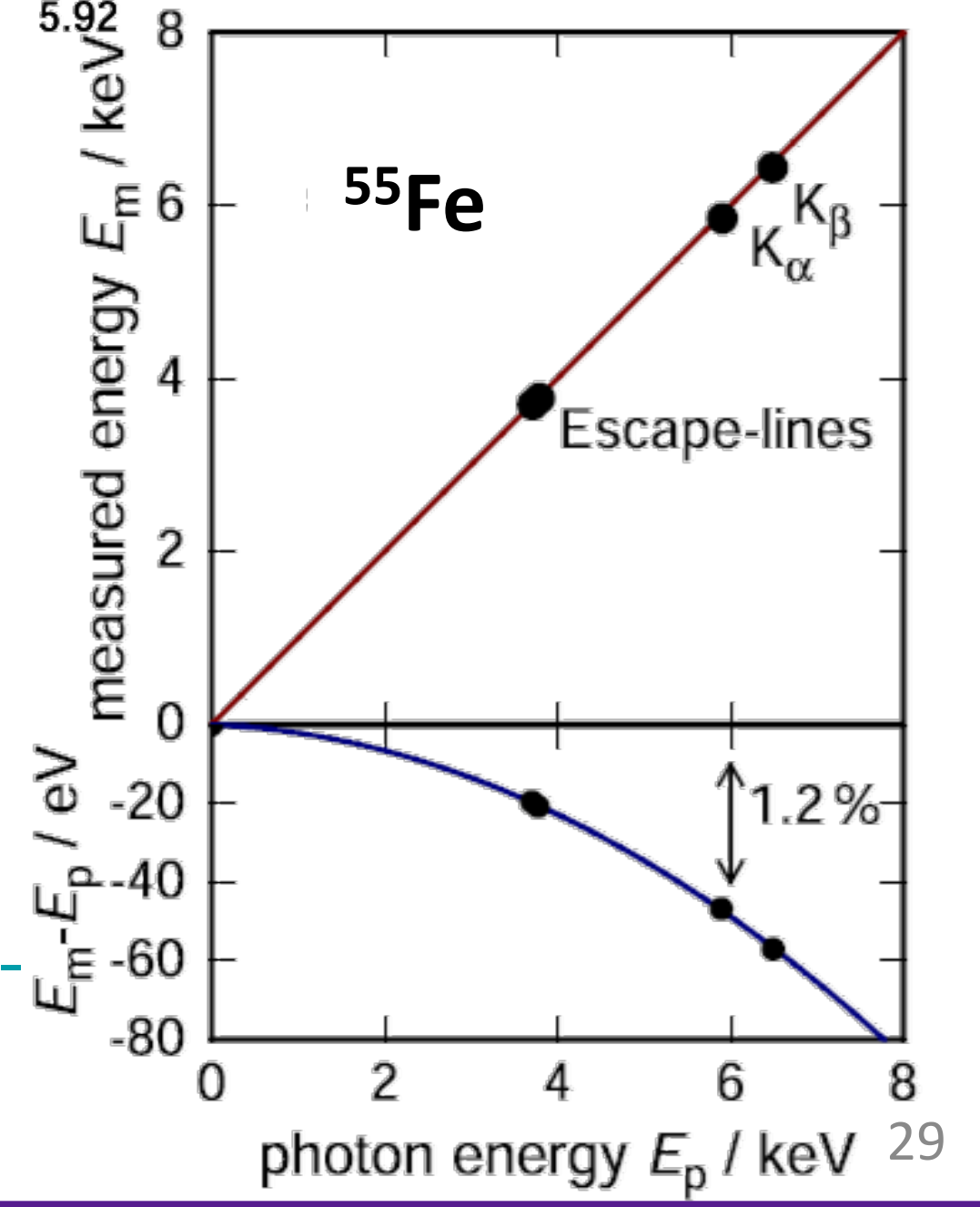
$$\Delta\Phi_s \propto \frac{\partial M}{\partial T} \Delta T \rightarrow \Delta\Phi_s \propto \frac{\partial M}{\partial T} \frac{E}{C_{\text{sens}} + C_{\text{abs}}}$$

Fast rise time reduces pile-up

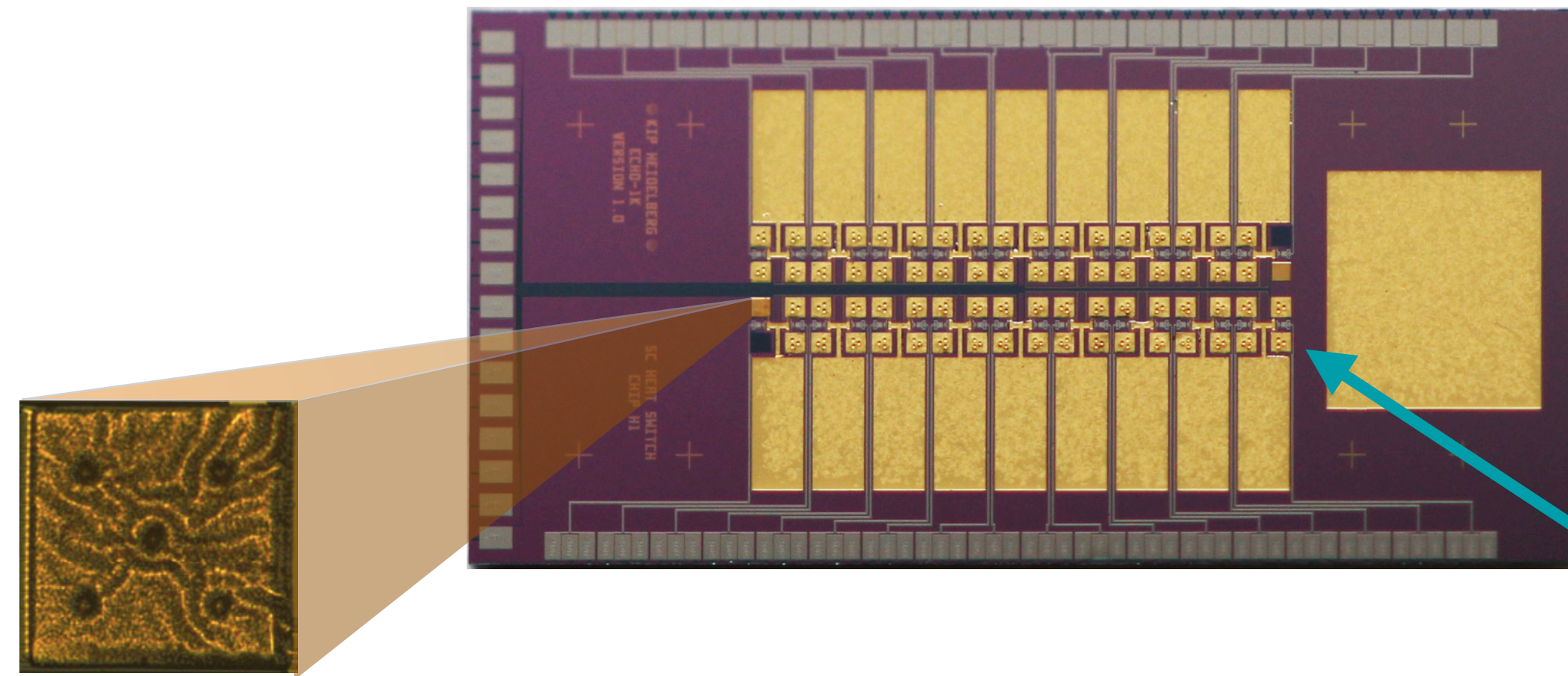


Excellent energy resolution  
 $\Delta E_{\text{FWHM}} \sim 1.6 \text{ eV}$

Linear response  
 Energy scale well-understood



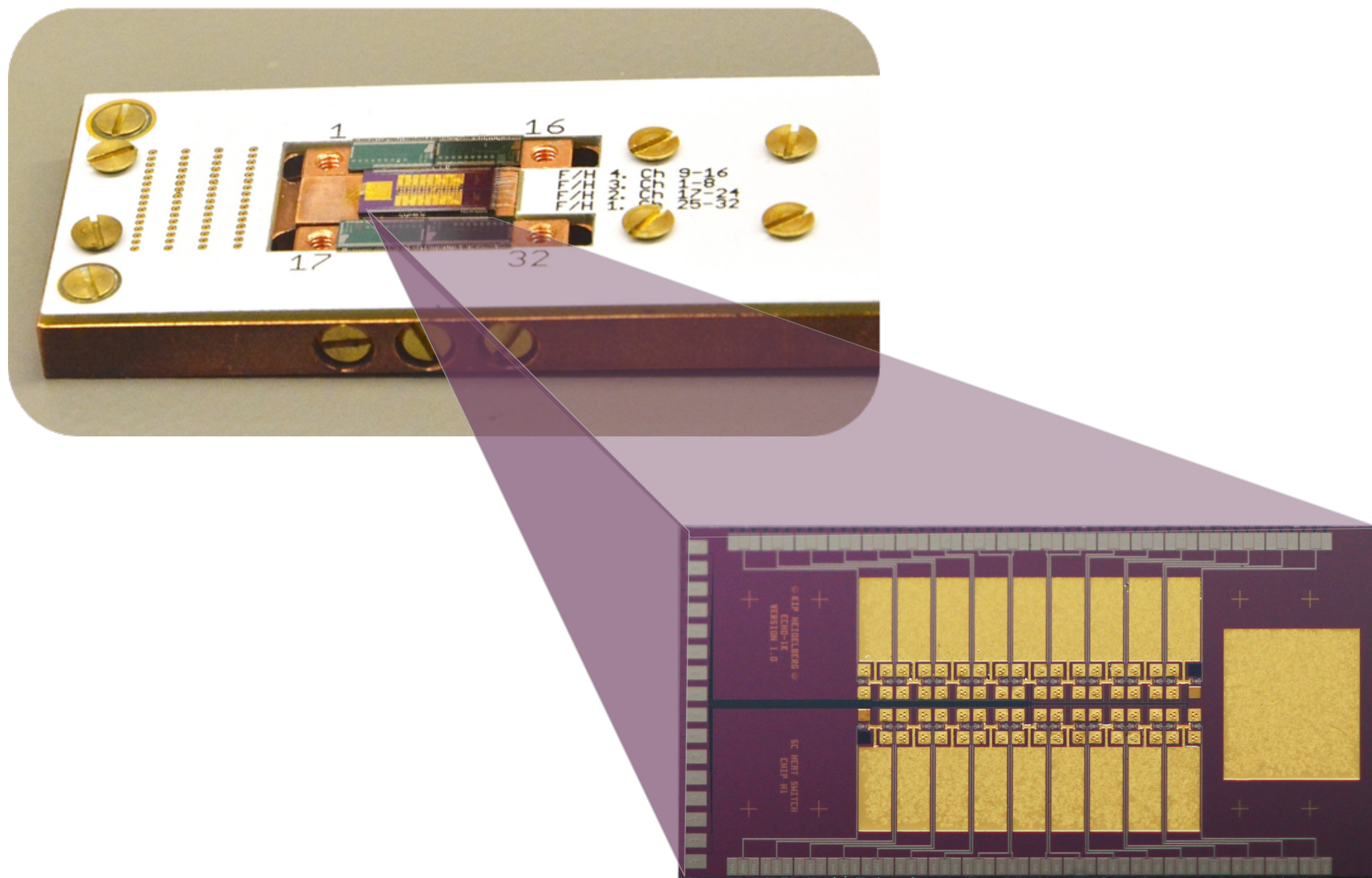
AIP Conf. Proc. 1185, 571, (2009)



**60 pixels with  $^{163}\text{Ho}$  sandwiched between (+4 for diagnostics)**

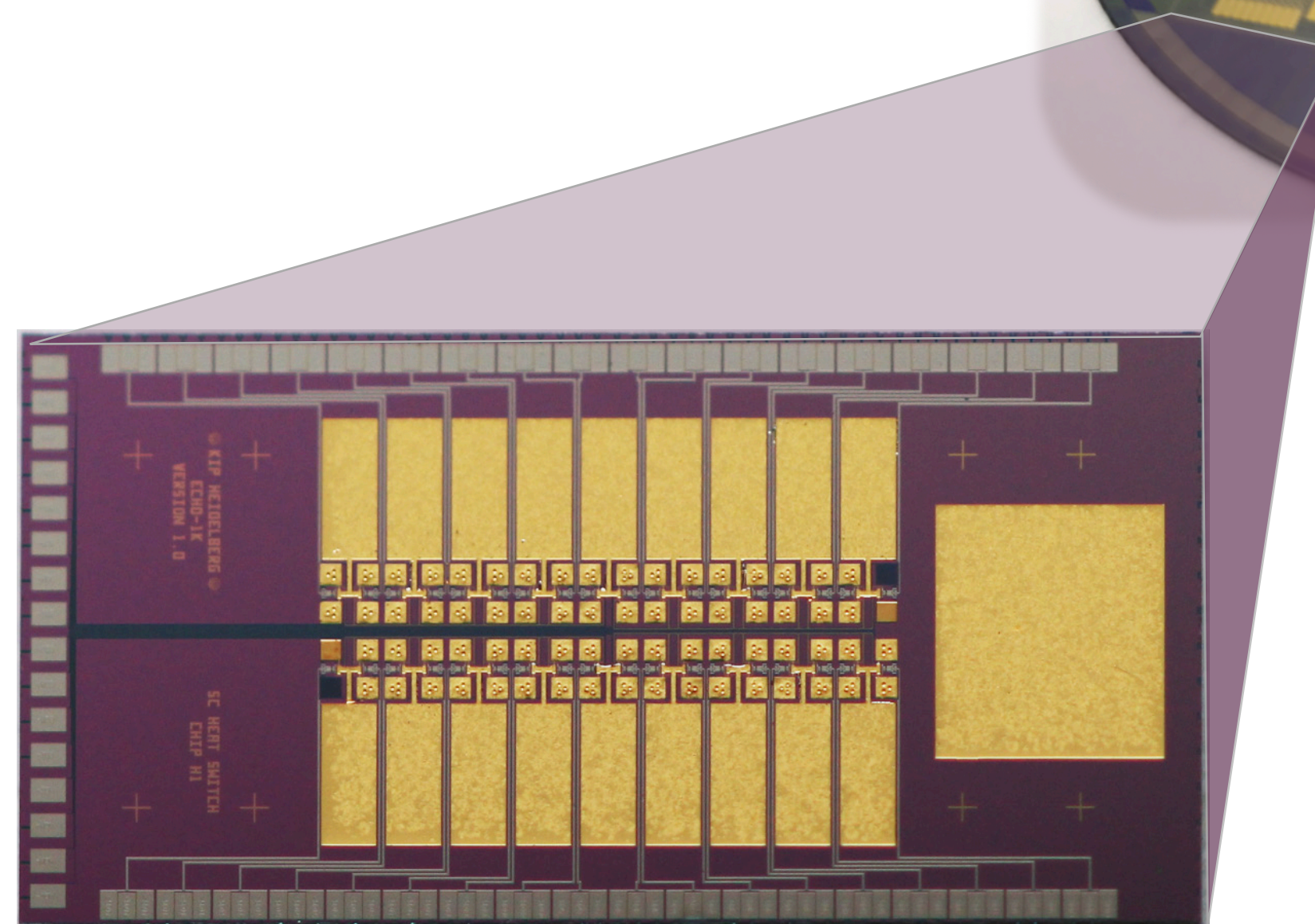
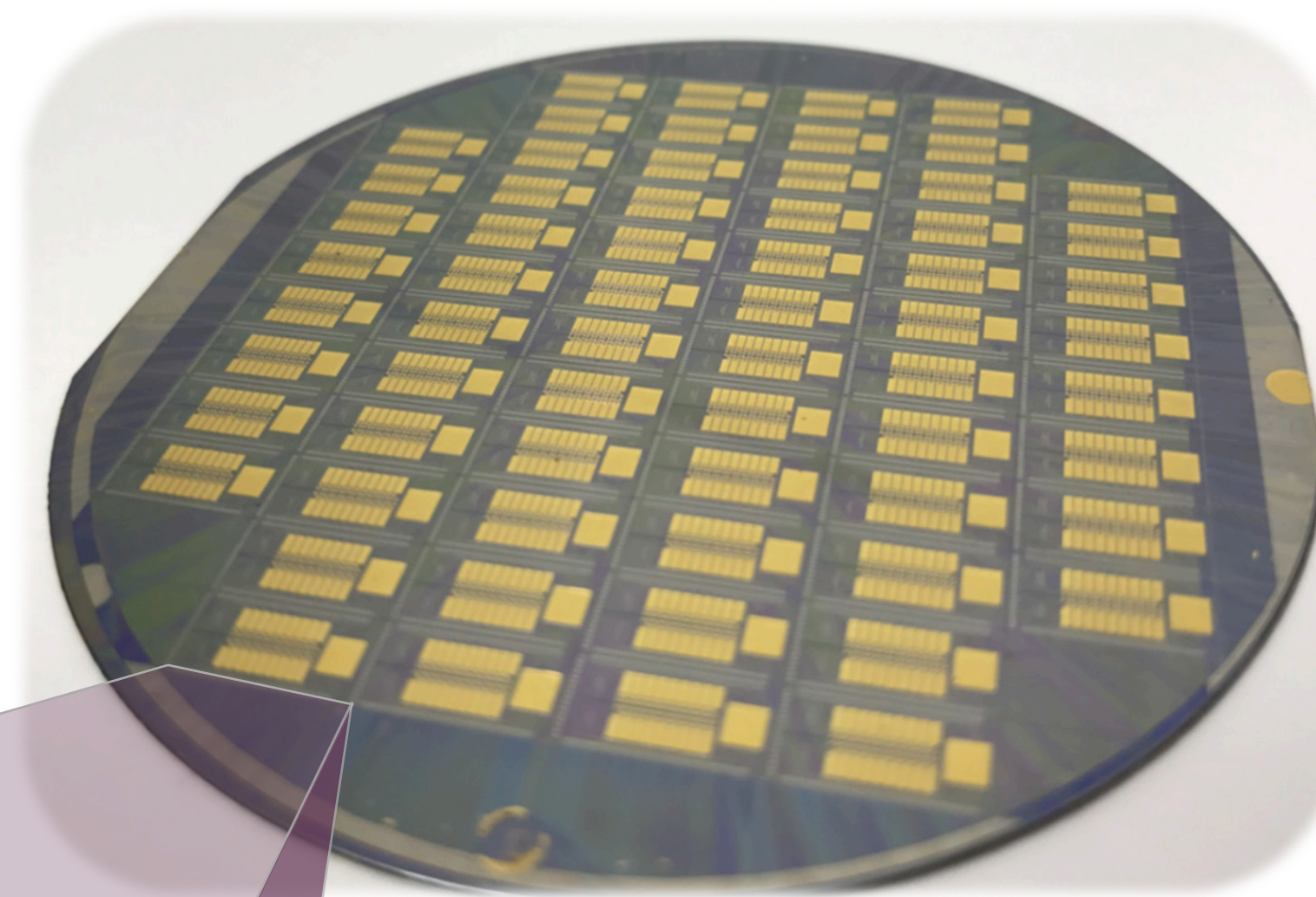
*L Gastaldo, Neutrino 2018*  
doi: 10.5281/zenodo/1286949

## 100Bq 64-pixel prototype at RISIKO (Mainz)



L Gastaldo, Neutrino 2018  
doi: 10.5281/zenodo/1286949





**ECHO-1k : 3" wafer with 64 chips**

$\Delta E_{FWHM} \sim 3\text{eV}$

Readout time 90ns (single-channel)

300ns (multiplexed)

## Scale up

- Total activity **1MBq**
- Neutrino mass sensitivity **< 1eV**
- Approximately **50 wafers of ~1000 detectors** each

## Holmium production

- Chemical separation for **bigger Er samples**
- Improved  $^{162}\text{Er}$  **enrichment**
- Study  $^{163}\text{Ho}(n,\gamma)$  reaction to optimise **irradiation time**

## Optimise design with ECHO-1k

- Optimal activity per pixel (target  $f_{pu} < 10^{-6}$ )
- Study different **absorber** materials
- **Signal processing** algorithms for more detectors
- Improve **background** model ( $10^{-6}$  counts/eV/det/day )

*Eur. Phys. J. Special Topics 226, 1623–1694 (2017)*

# $^{163}\text{Ho}$ demonstrators

Advances in High Energy Physics  
2016 (9)

L Gastaldo (Neutrino 2018)



ECHO-1k



Proof of concept



# $^{163}\text{Ho}$ demonstrators

Advances in High Energy Physics  
2016 (9)

L Gastaldo (Neutrino 2018)



**ECHO-100k**



**Full design**

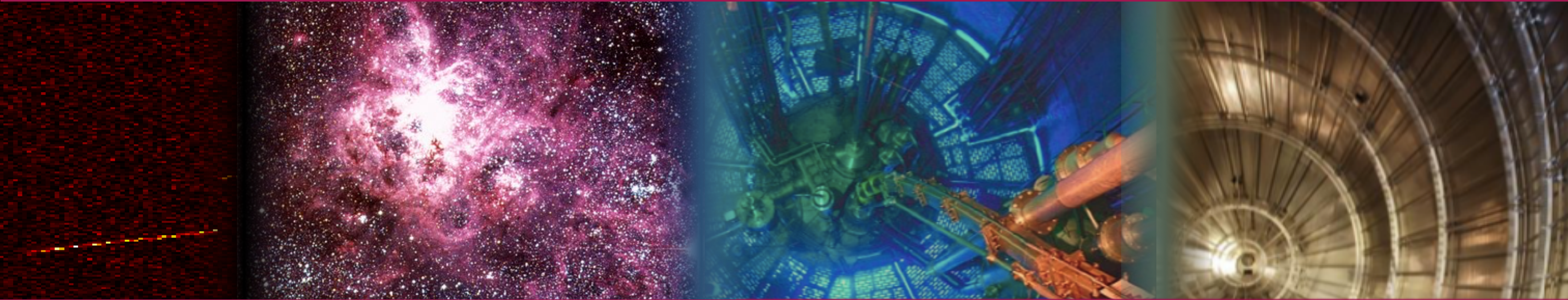


**NuMECS**





**Did you spot the pictures?**



Project 8 event  
display

**Did you spot the pictures?**



Project 8 event  
display

Supernova 1987A

**Did you spot the pictures?**



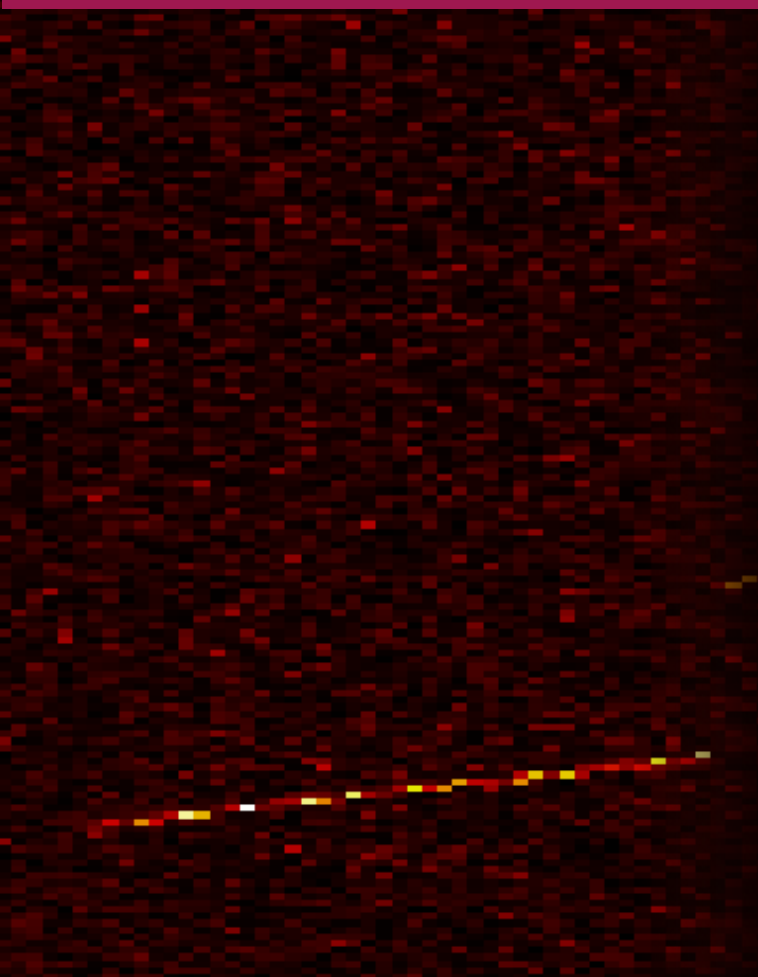
Project 8 event  
display

Supernova 1987A

ILL reactor making  
 $^{163}\text{Ho}$  for ECHO

Did you spot the pictures?





Project 8 event display



Supernova 1987A



ILL reactor making  $^{163}\text{Ho}$  for ECHO



KATRIN spectrometer

**Did you spot the pictures?**