

# Deep Learning (and Deep Thinking) for QCD

Jesse Thaler



QCD@LHC 2019, University at Buffalo — July 15, 2019

# Deep Learning

## Inpainting



Corrupted



Deep image prior

increased computational power and large data sets

[Ulyanov, Vedaldi, Lempitsky, [1711.10925](#)]

# Deep Learning (or Deep Thinking?)

## Inpainting



Corrupted



Deep image prior

Using randomly initialized neural network (!)

Progress made by understanding the structure of problems  
(not just increased computational power and large data sets)

[Ulyanov, Vedaldi, Lempitsky, [1711.10925](#)]

# Deep Learning for QCD?

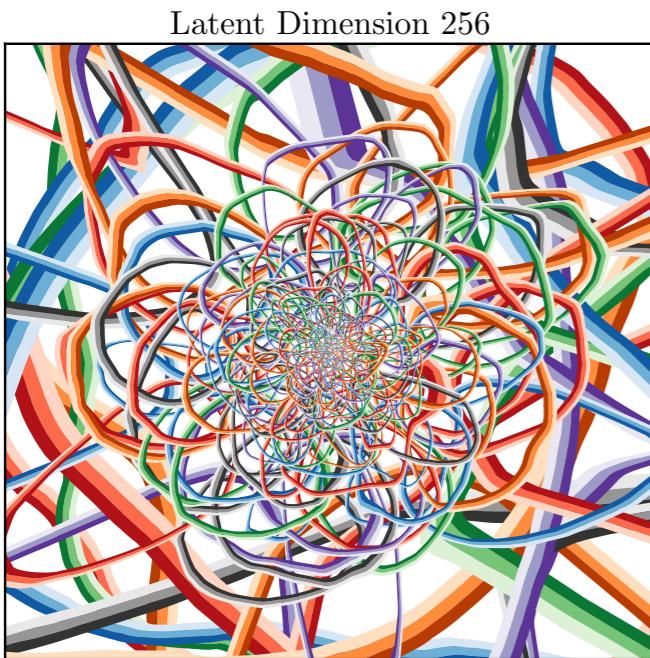
& other advanced data analysis strategies

New insights into structure of jets?  
Robust handles on hadronic final states?

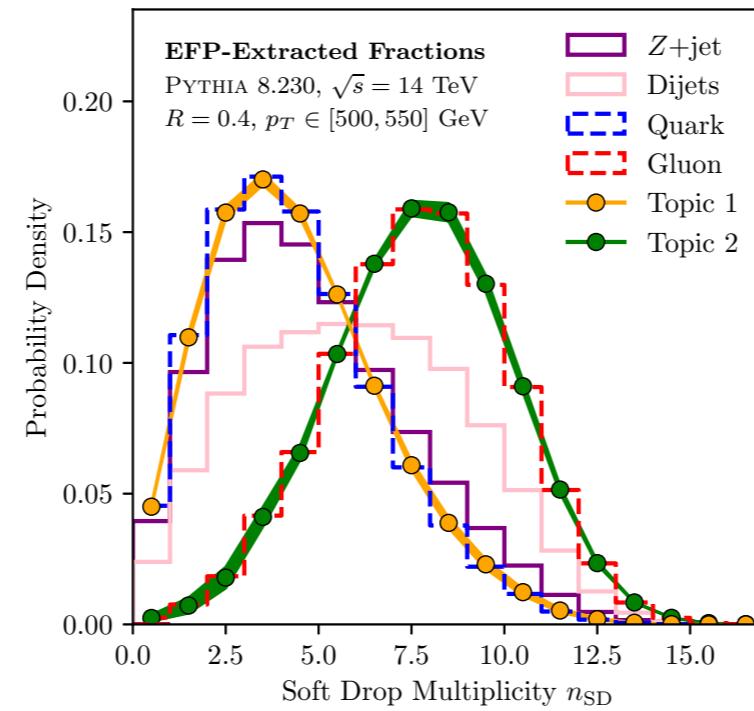
## Three case studies from my research group

See also broader [ML4Jets community](#)

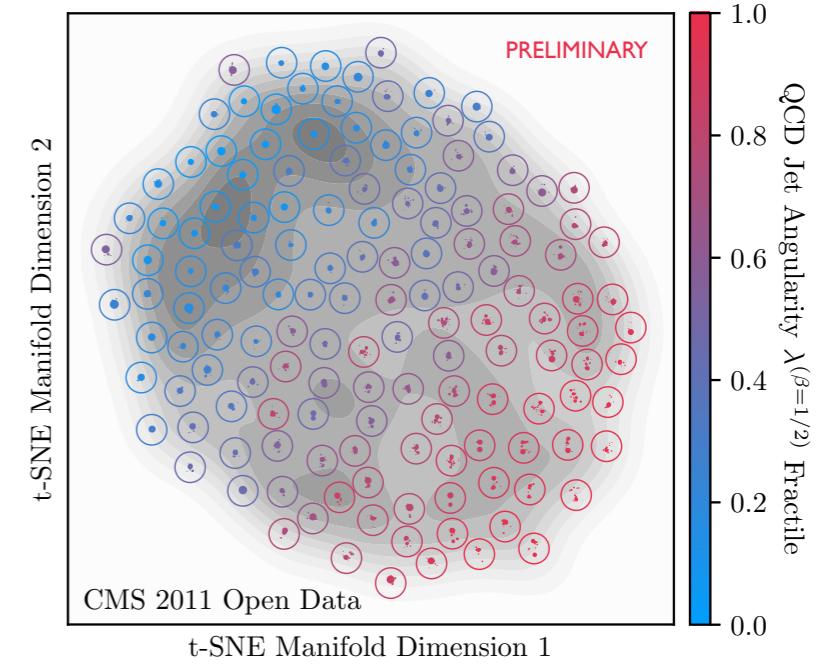
### Energy Flow Networks



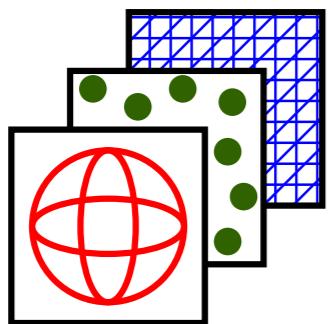
### Jet Topics



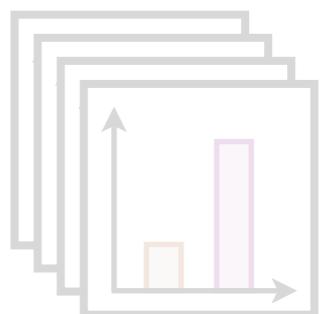
### (Energy Mover's Distance)



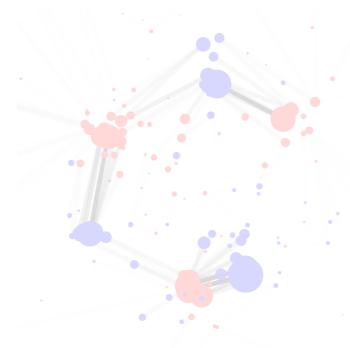
[Komiske, Metodiev, JDT, [I810.05165](#); Metodiev, JDT, [I802.00008](#); Komiske, Metodiev, JDT, [I809.01140](#);  
Komiske, Metodiev, JDT, [I902.02346](#); Komiske, Mastandrea, Metodiev, Naik, JDT, in preparation]



## Into the Network



## Data Ex Machina



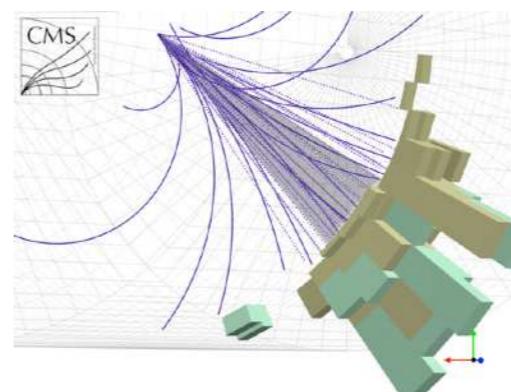
## (The Space of Jets)

# Cartoon of Machine Learning



E.g.: **Problem** = Minimize loss function  
**Solution** = Multi-layer neural network  
Strategy = Stochastic gradient descent

For most of this talk:  $\mathcal{J}$  = “jet”

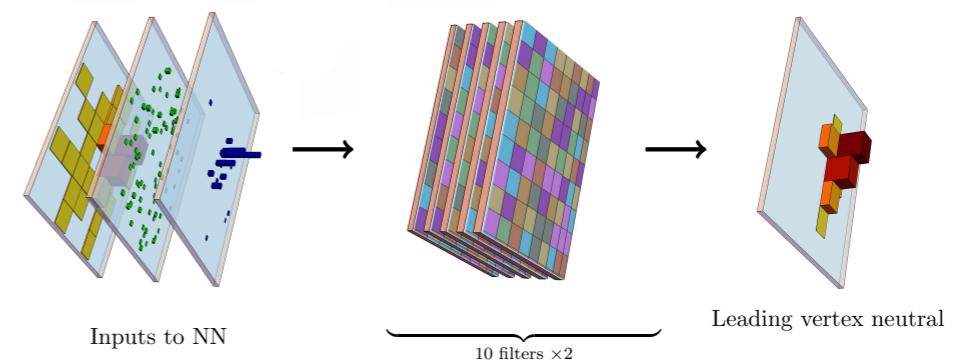


# Examples of Supervised Learning

## Regression

e.g. *PUMML for pileup mitigation*

[Komiske, Metodiev, Nachman, Schwartz, [1707.08600](#); see also Arjona Martínez, Cerri, Pierini, Spiropulu, Vlimant, [1810.07988](#)]

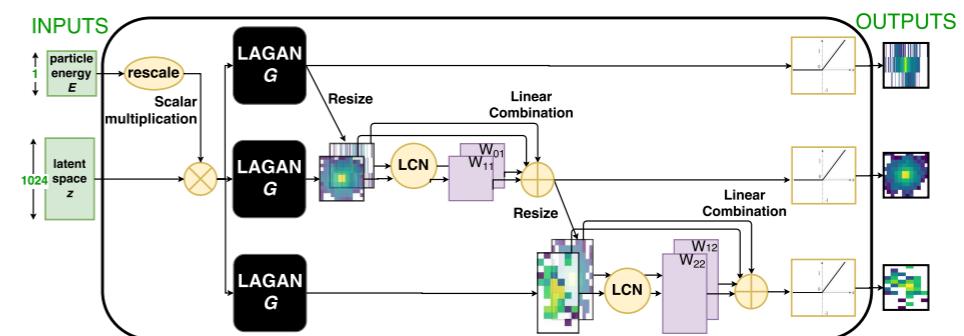


Labeled data: Objects J with property x  
Solution: Map from J to x

## Generation

e.g. *CaloGAN for fast detector simulation*

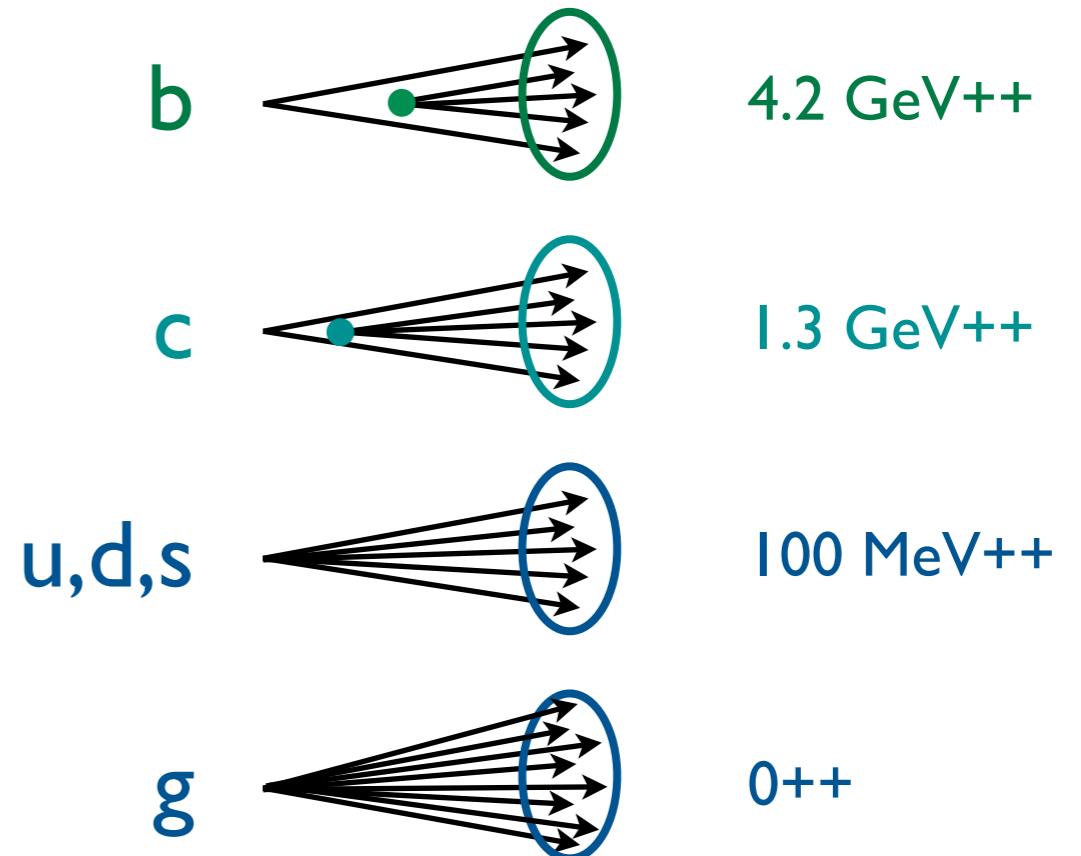
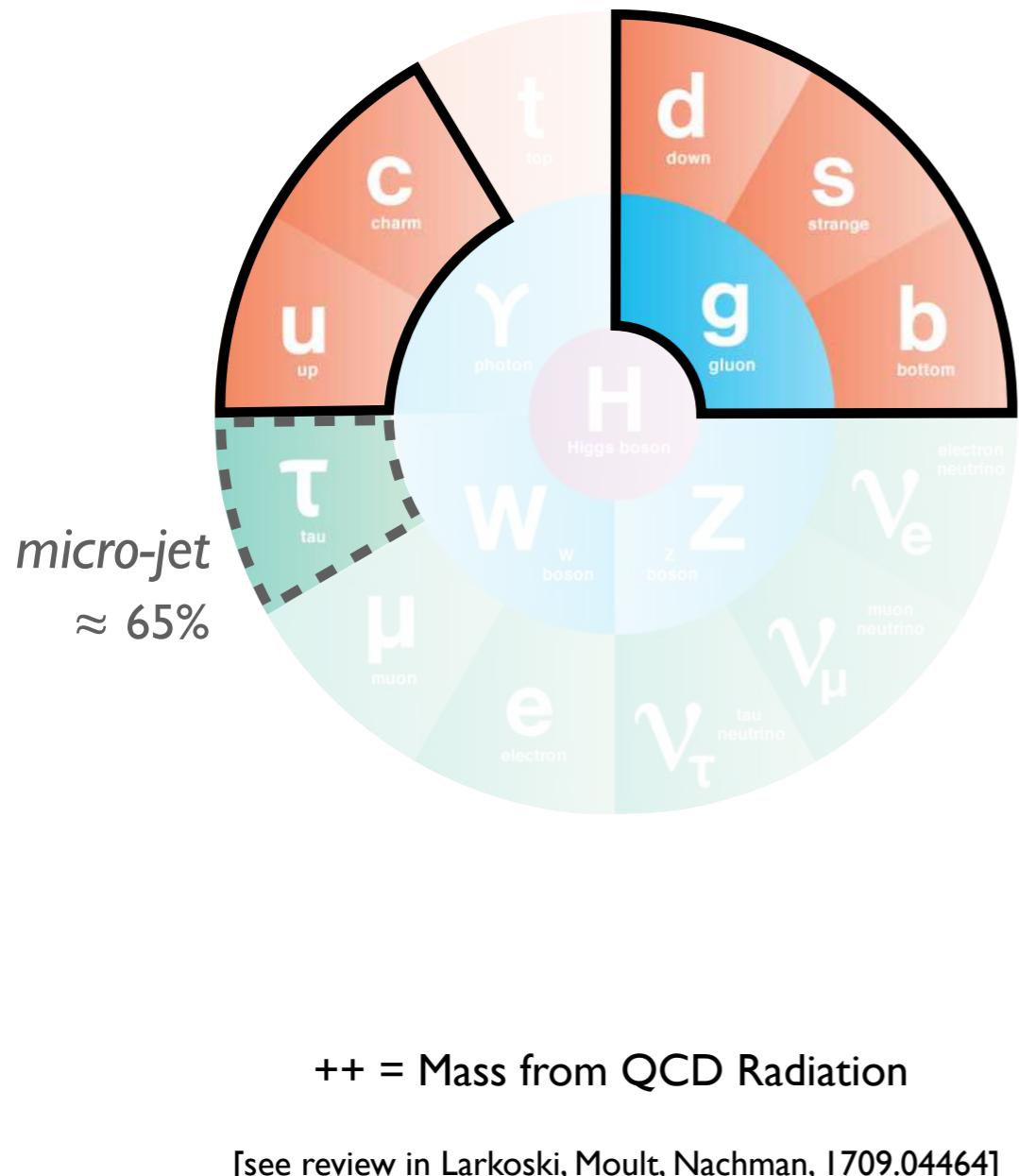
[Paganini, de Oliveira, Nachman, [1705.02355](#), [1712.10321](#); see also de Oliveira, Michela Paganini, Nachman, [1701.05927](#)]



Labeled data: Objects J with property x  
Solution: Map (conditioned on x)  
from noise to J

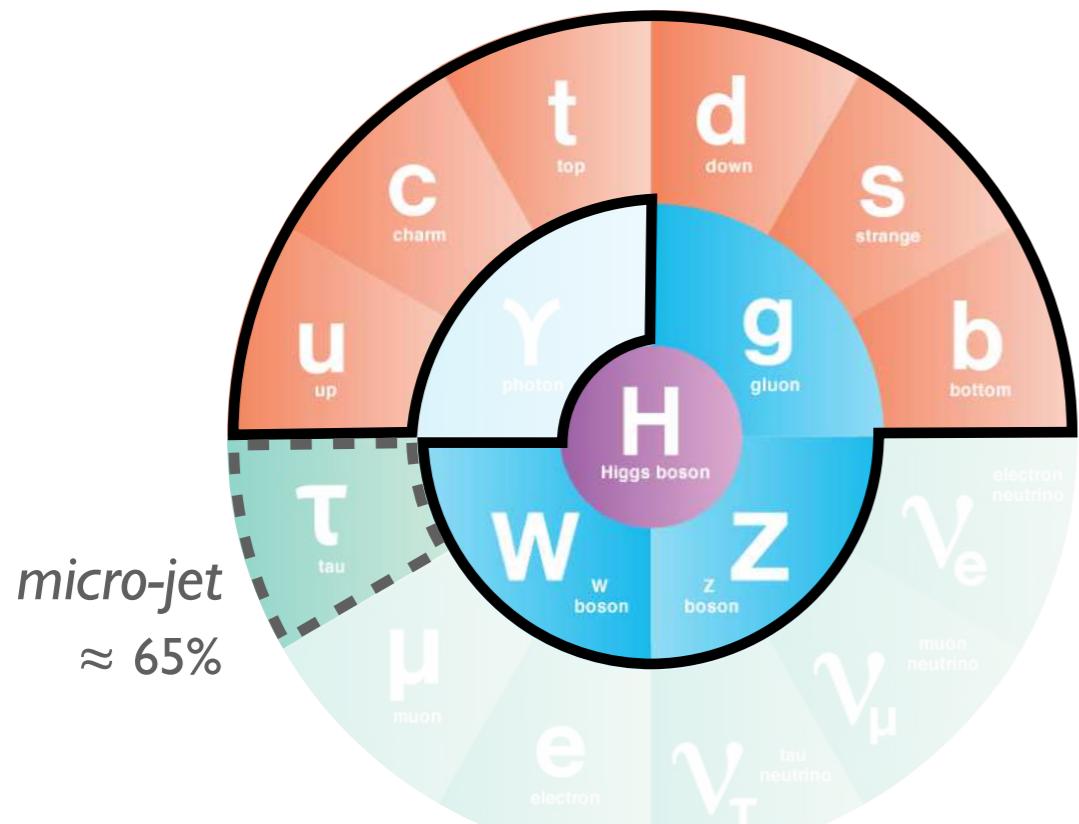
# Jet Classification

Key supervised learning task at LHC



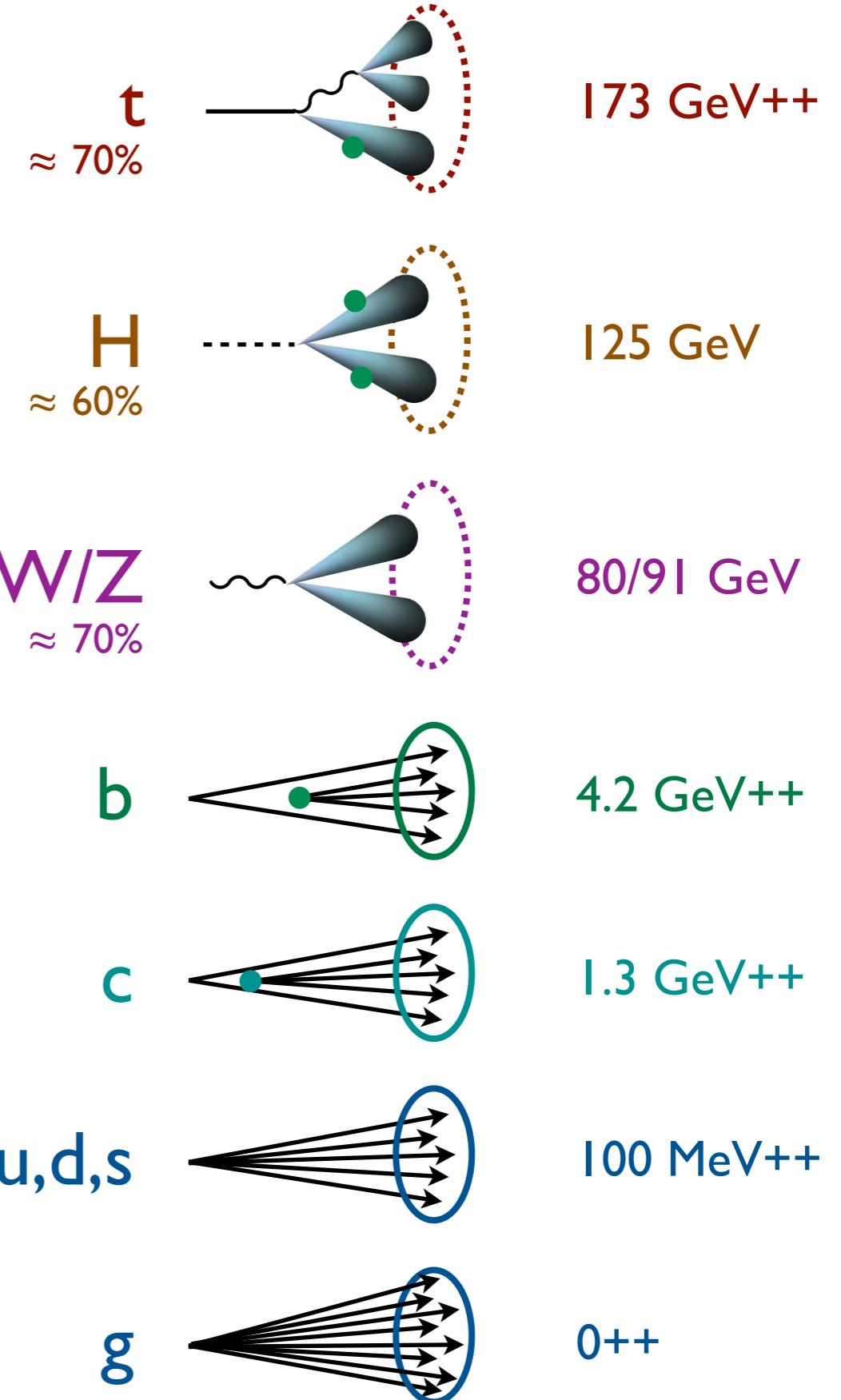
# Jet Classification

Key supervised learning task at LHC



$++$  = Mass from QCD Radiation

[see review in Larkoski, Moult, Nachman, [1709.04464](#)]



# BOSTON 2019

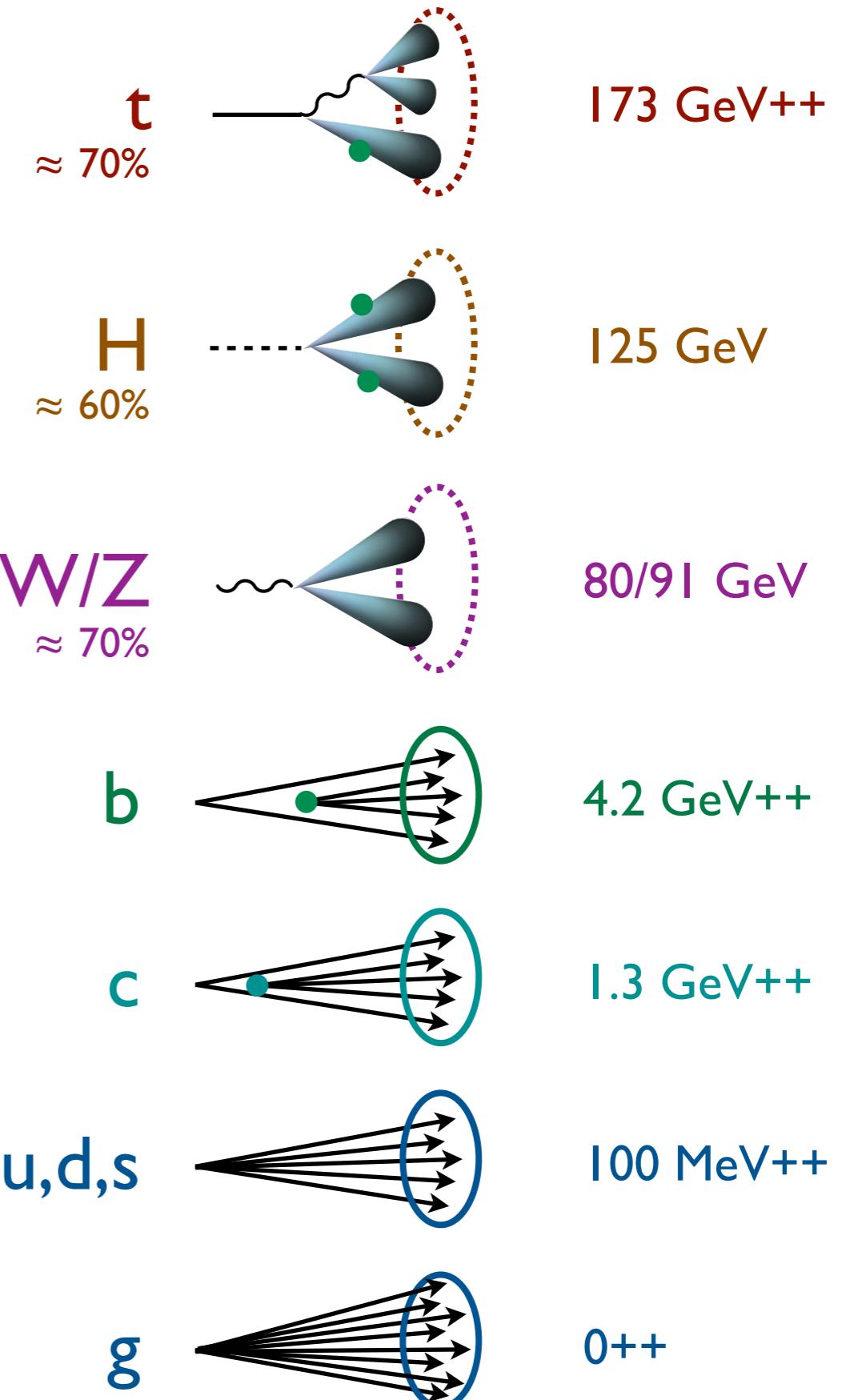
Phenomenology | Reconstruction | Searches | Algorithms | Measurements | Calculations  
 Modeling | Machine Learning | Pileup Mitigation | Heavy-Ion Collisions | Future Colliders

Local Organizing Committee:  
 Zeynep Demiragli (BU)  
 Philip Harris (MIT)  
 Yen-Jie Lee (MIT)  
 Matthew Schwartz (Harvard)  
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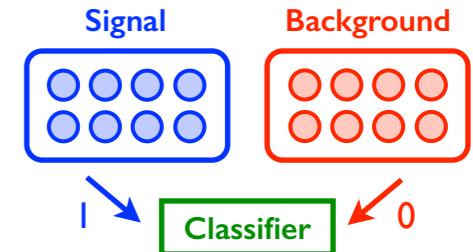
July 22-26, 2019  
 Stata Center, MIT

<https://indico.cern.ch/e/boost2019>

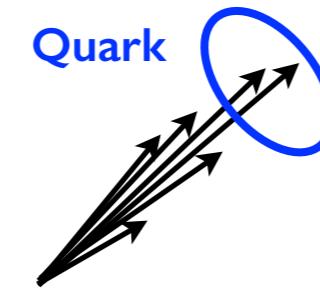


# Binary Classification

*Much more in backup*



e.g.



vs.



assuming trustable  
training data  
(more later...)

Find  $h\left(\begin{array}{c} \text{bundle of arrows} \\ \end{array}\right)$

such that

$$h(\text{Quark}) = 1$$

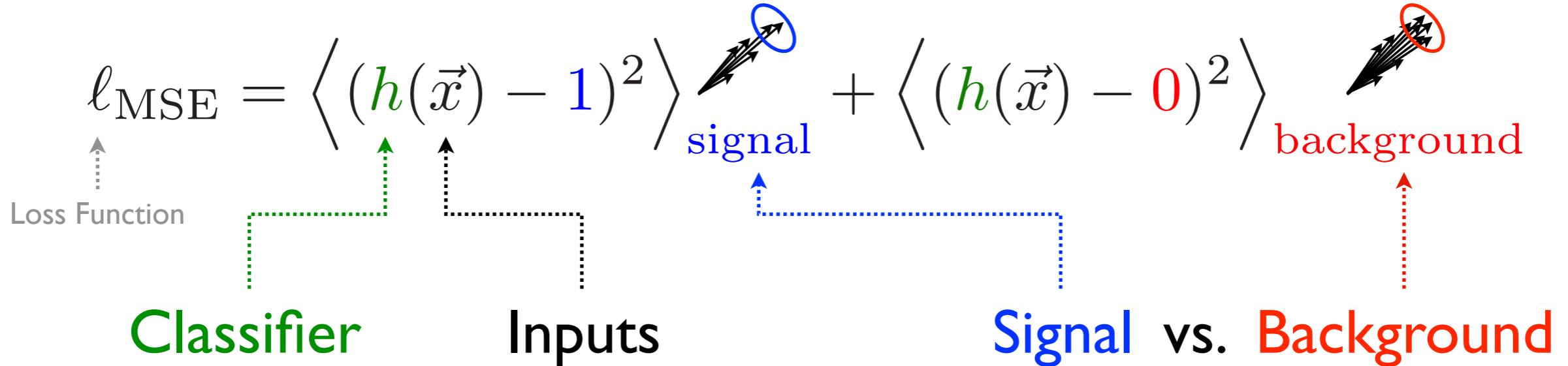
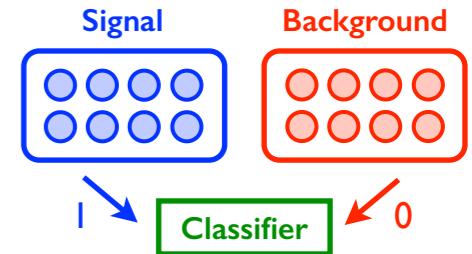
$$h(\text{Gluon}) = 0$$

Best you can do:  $h(\mathcal{J}) = \frac{p(\mathcal{J}|Q)}{p(\mathcal{J}|Q) + p(\mathcal{J}|G)}$

(Neyman-Pearson lemma)

# Jet Classification Studies

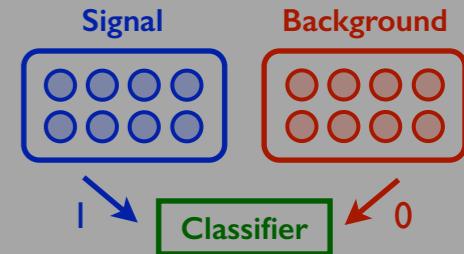
*Mix and match*



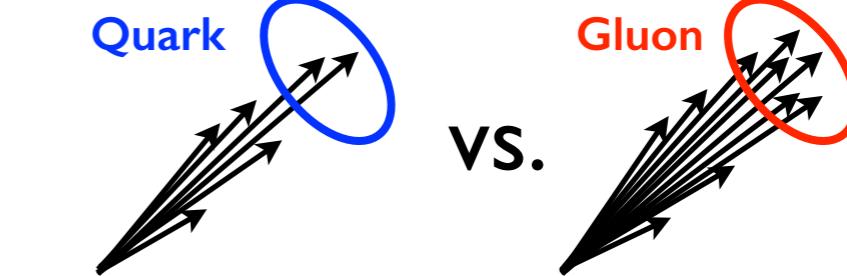
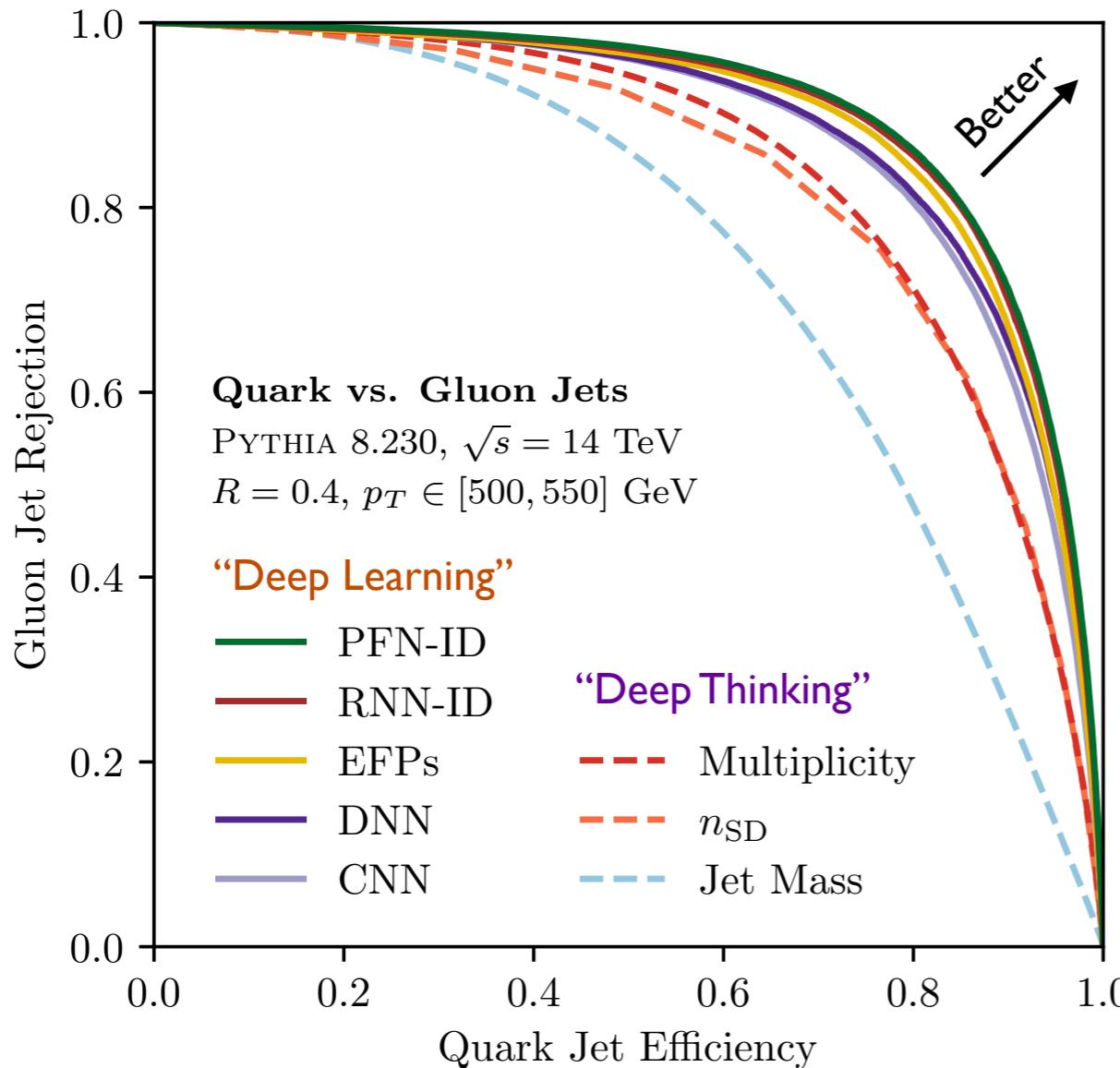
[Lönnblad, Peterson, Rögnvaldsson, [PRL 1990](#), ..., Cogan, Kagan, Strauss, Schwartzman, [1407.5675](#); Almeida, Backović, Cliche, Lee, Perelstein, [1501.05968](#); de Oliveira, Kagan, Mackey, Nachman, Schwartzman, [1511.05190](#); Baldi, Bauer, Eng, Sadowski, Whiteson, [1603.09349](#); Conway, Bhaskar, Erbacher, Pilot, [1606.06859](#); Guest, Collado, Baldi, Hsu, Urban, Whiteson, [1607.08633](#); Barnard, Dawe, Dolan, Rajcic, [1609.00607](#); Komiske, Metodiev, Schwartz, [1612.01551](#); Kasieczka, Plehn, Russell, Schell, [1701.08784](#); Louppe, Cho, Becot, Cranmer, [1702.00748](#); Pearkes, Fedorko, Lister, Gay, [1704.02124](#); Datta, Larkoski, [1704.08249](#), [1710.01305](#); Butter, Kasieczka, Plehn, Russell, [1707.08966](#); Fernández Madrazo, Heredia Cacha, Lloret Iglesias, Marco de Lucas, [1708.07034](#); Aguilar Saavedra, Collin, Mishra, [1709.01087](#); Cheng, [1711.02633](#); Luo, Luo, Wang, Xu, Zhu, [1712.03634](#); Komiske, Metodiev, JDT, [1712.07124](#); Macaluso, Shih, [1803.00107](#); Fraser, Schwartz, [1803.08066](#); Choi, Lee, Perelstein, [1806.01263](#); Lim, Nojiri, [1807.03312](#); Dreyer, Salam, Soyez, [1807.04758](#); Moore, Nordström, Varma, Fairbairn, [1807.04769](#); plus many ATLAS/CMS performance studies; plus my friends who will scold me for forgetting their paper (and not updating this after July 23, 2018)]

# Jet Classification Studies

Mix and match



## The “Hello, World!” of Jet Classification



*Substantial gains from deep learning... but why?*

[Komiske, Metodiev, JDT, 1810.05165]

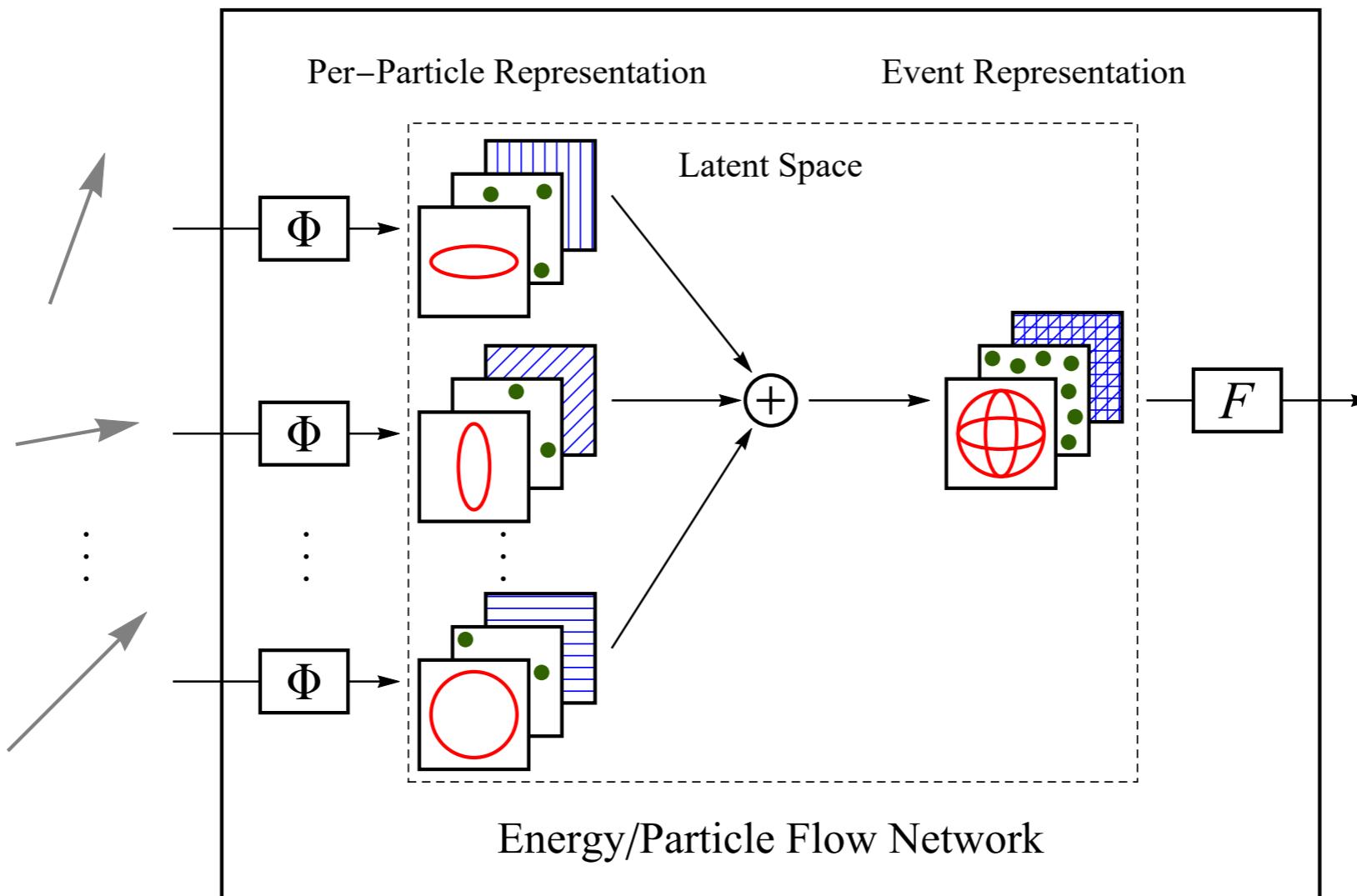
# Introducing Energy Flow Networks

(see backup for detailed architecture)

An architecture designed for *interpretability*

Particles

Observable

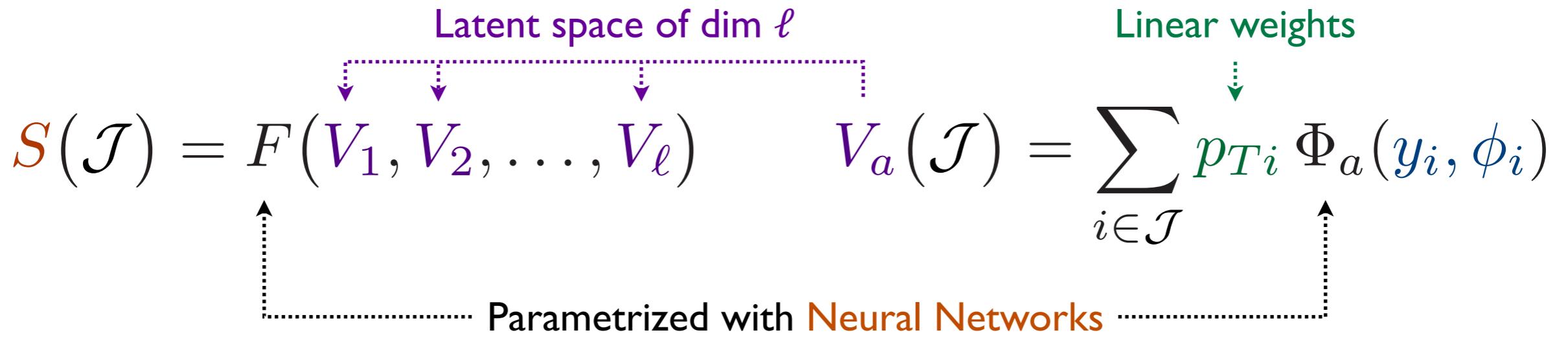


[Komiske, Metodiev, JDT, [1810.05165](#);  
special case of Zaheer, Kottur, Ravanbakhsh, Poczos, Salakhutdinov, Smola, [1703.06114](#)]

# Introducing Energy Flow Networks

An architecture designed for *interpretability*

(see backup for  
detailed architecture)



Flexible enough to describe any\* **IRC-safe** observable  
(assuming large enough  $\ell$ )

Generalization: Particle Flow Networks (aka “Deep Sets”)

[Komiske, Metodiev, JDT, [1810.05165](#);  
special case of Zaheer, Kottur, Ravanbakhsh, Poczos, Salakhutdinov, Smola, [1703.06114](#)]

# Introducing Energy Flow Networks

An architecture designed for *interpretability*

(see backup for  
detailed architecture)

## Visualization Strategy

$$S(\mathcal{J}) = F(V_1, V_2, \dots, V_\ell)$$

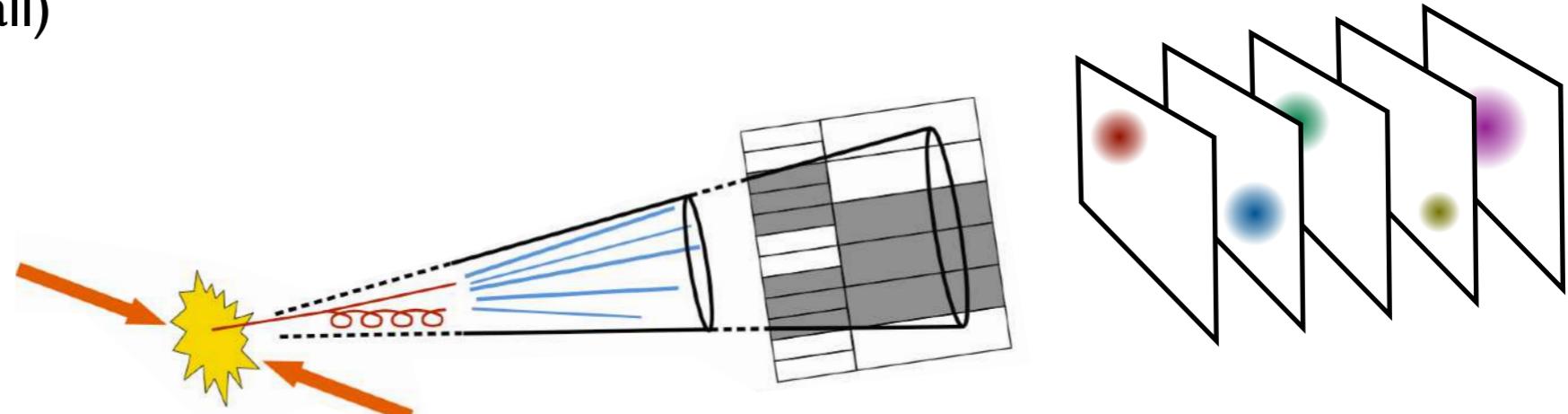


Difficult to visualize  
(unless  $\ell$  is small)

$$V_a(\mathcal{J}) = \sum_{i \in \mathcal{J}} p_{Ti} \Phi_a(y_i, \phi_i)$$



Easy to plot these!



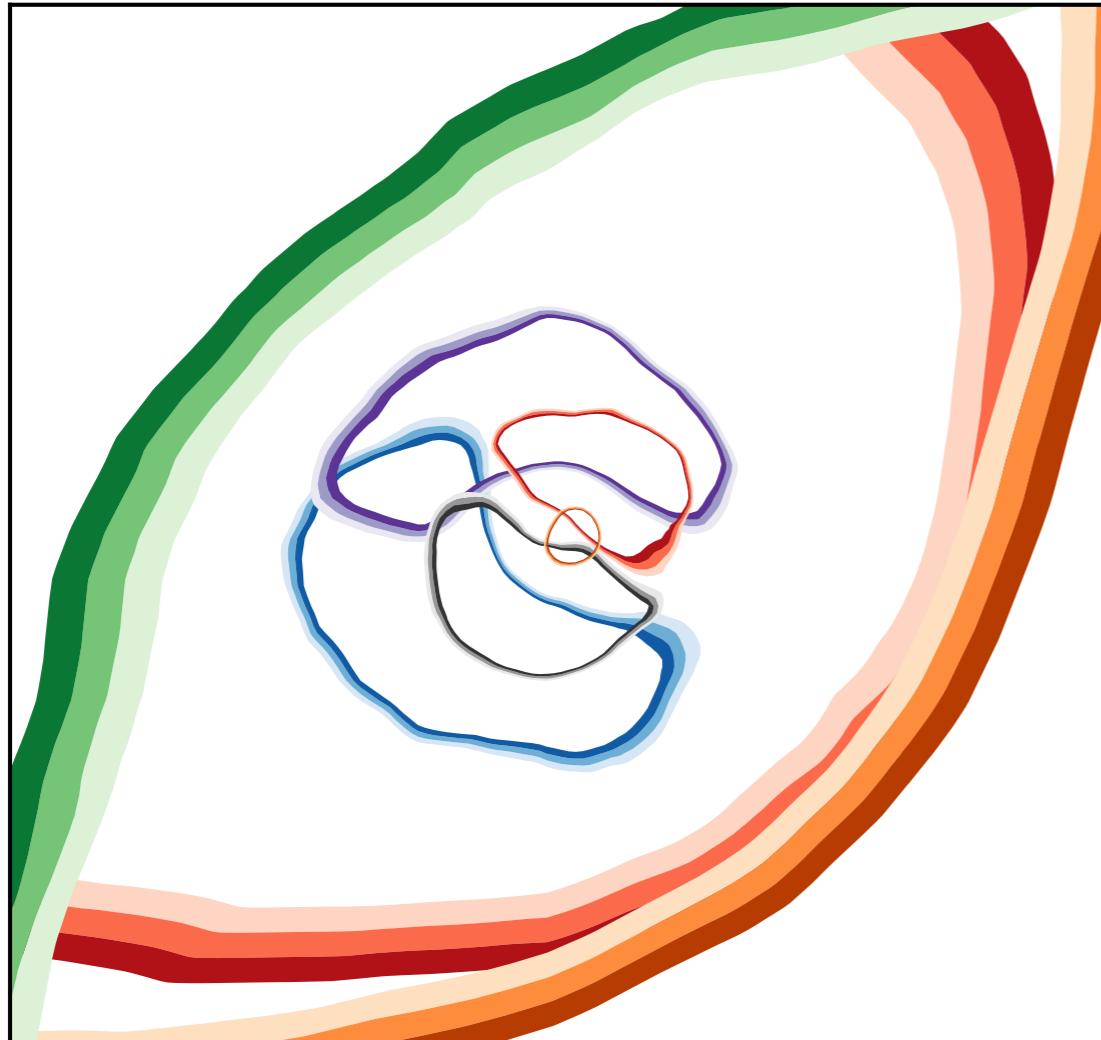
(similar to CNN  
filter activation)

[Komiske, Metodiev, JDT, 1810.05165;  
special case of Zaheer, Kottur, Ravanbakhsh, Poczos, Salakhutdinov, Smola, 1703.06114]

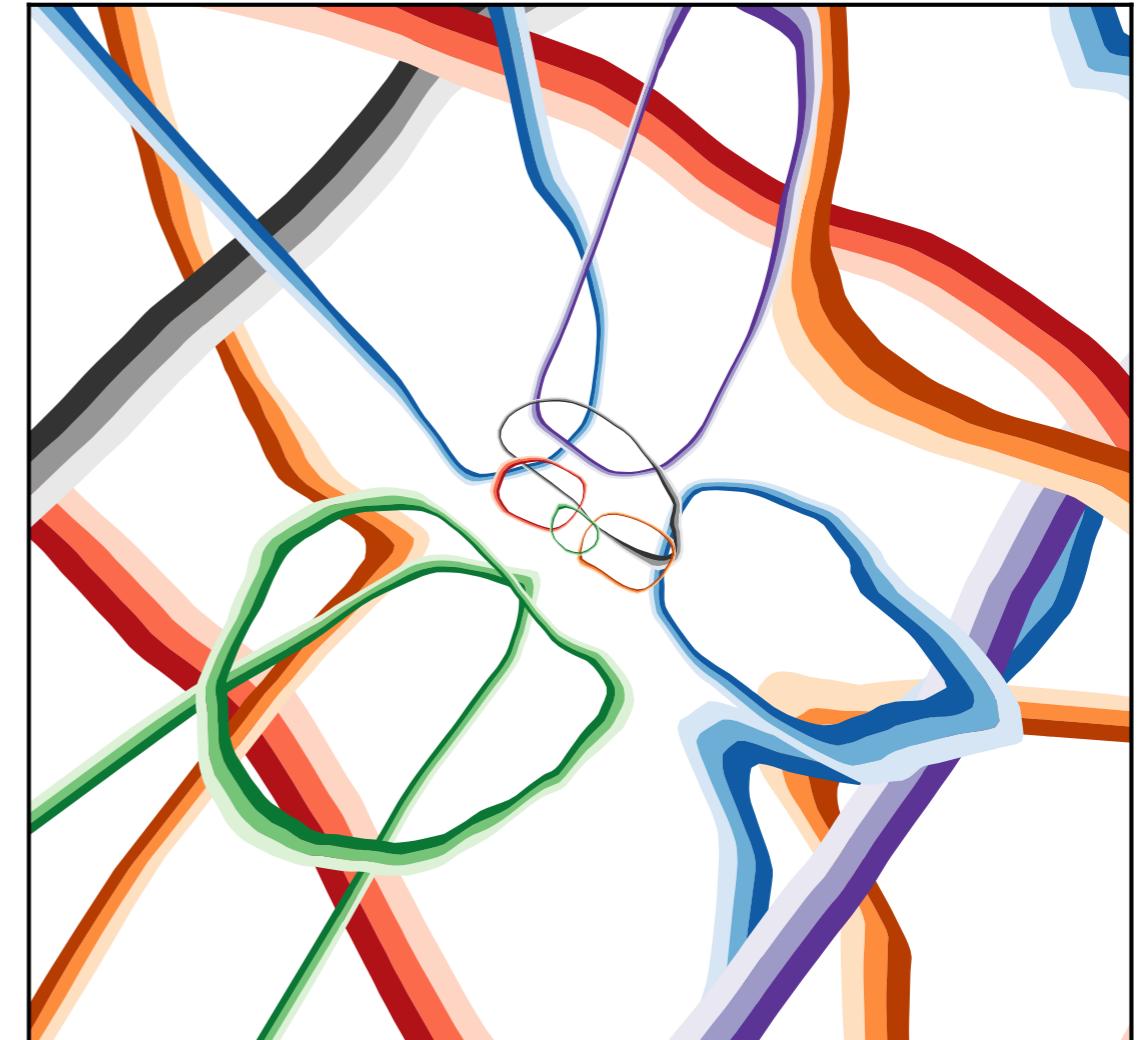
# Psychedelic Network Visualization

(see backup for  
how these are made)

Latent Dimension 8



Latent Dimension 16

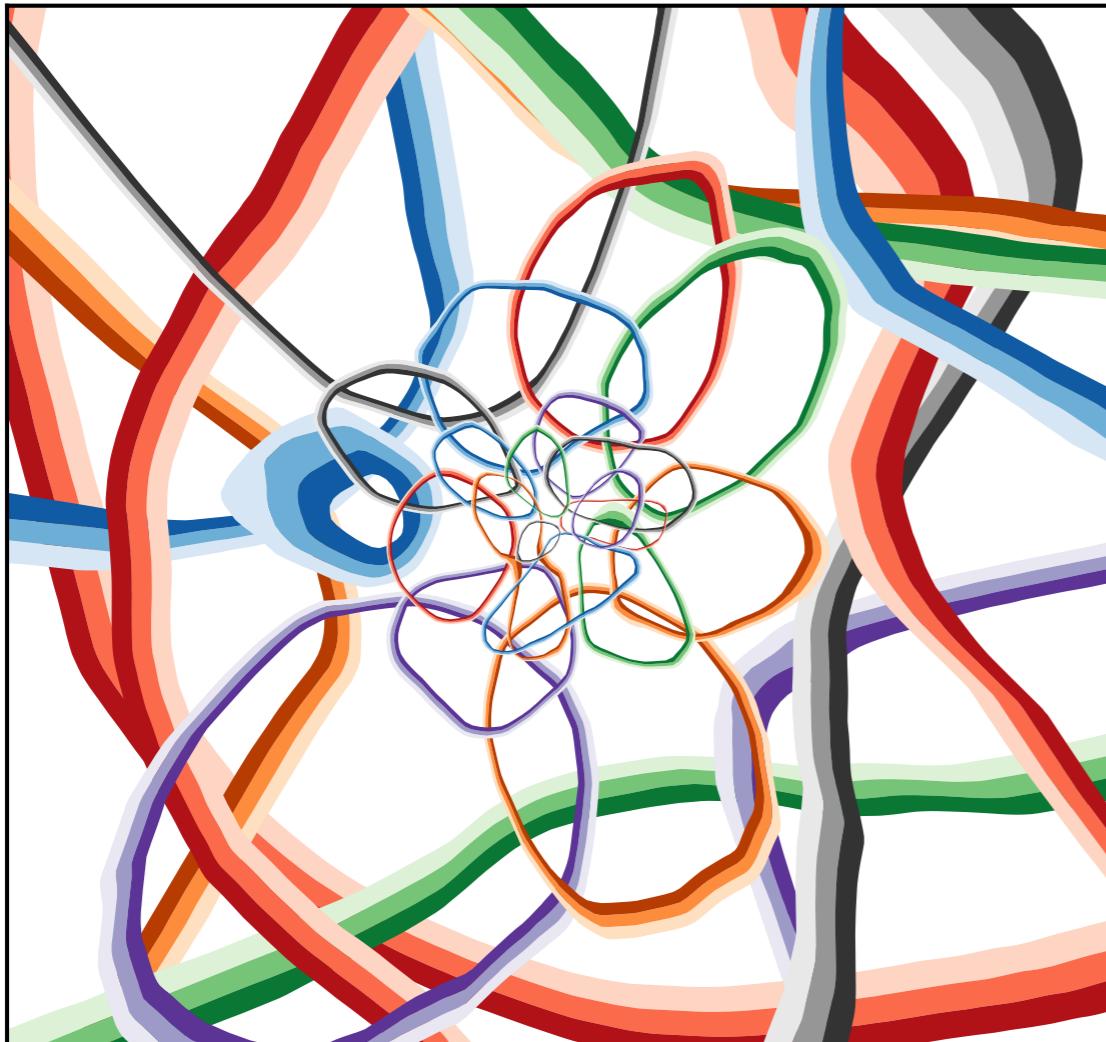


For the case of **quark** vs. **gluon** classification

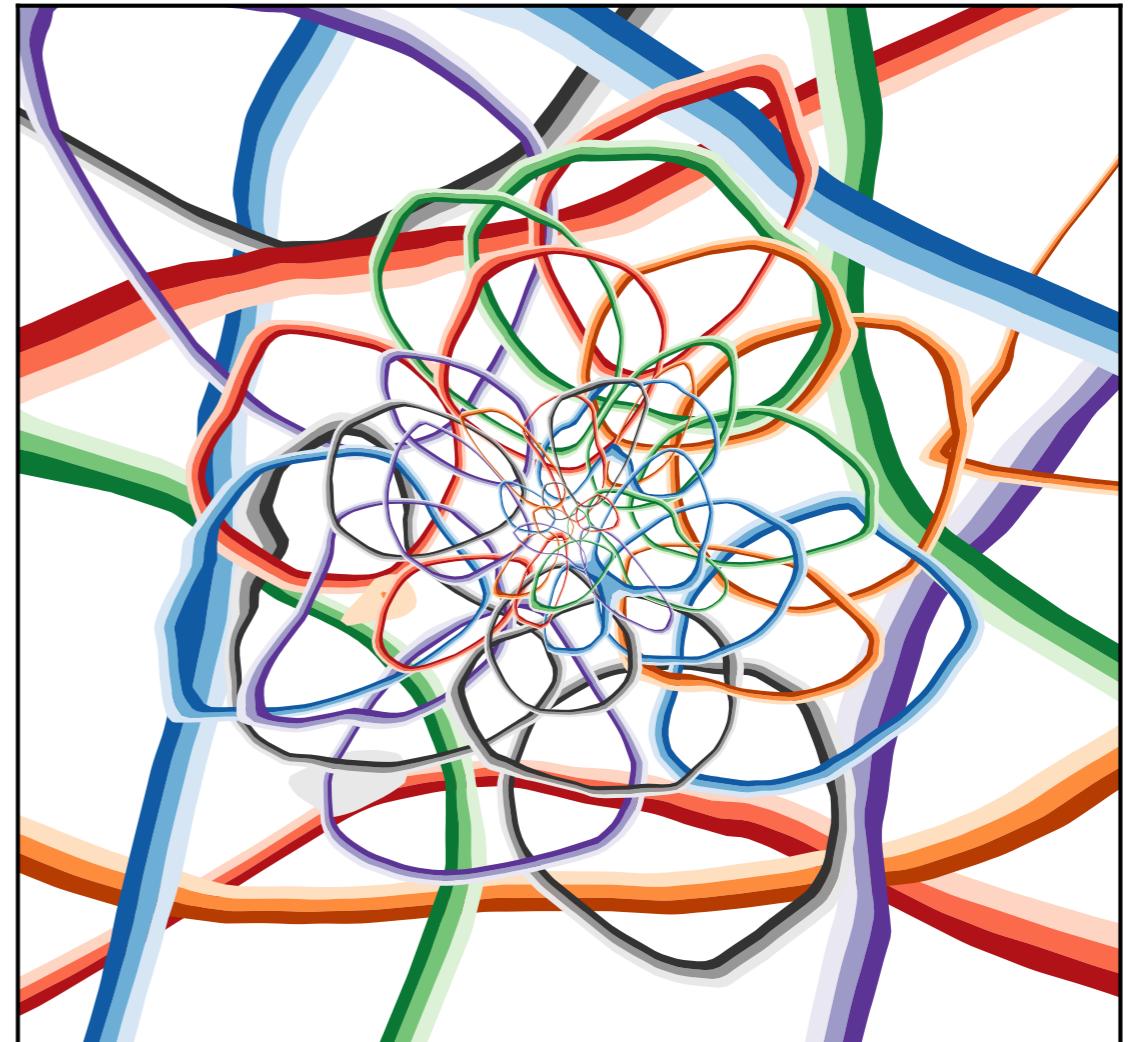
# Psychedelic Network Visualization

(see backup for  
how these are made)

Latent Dimension 32



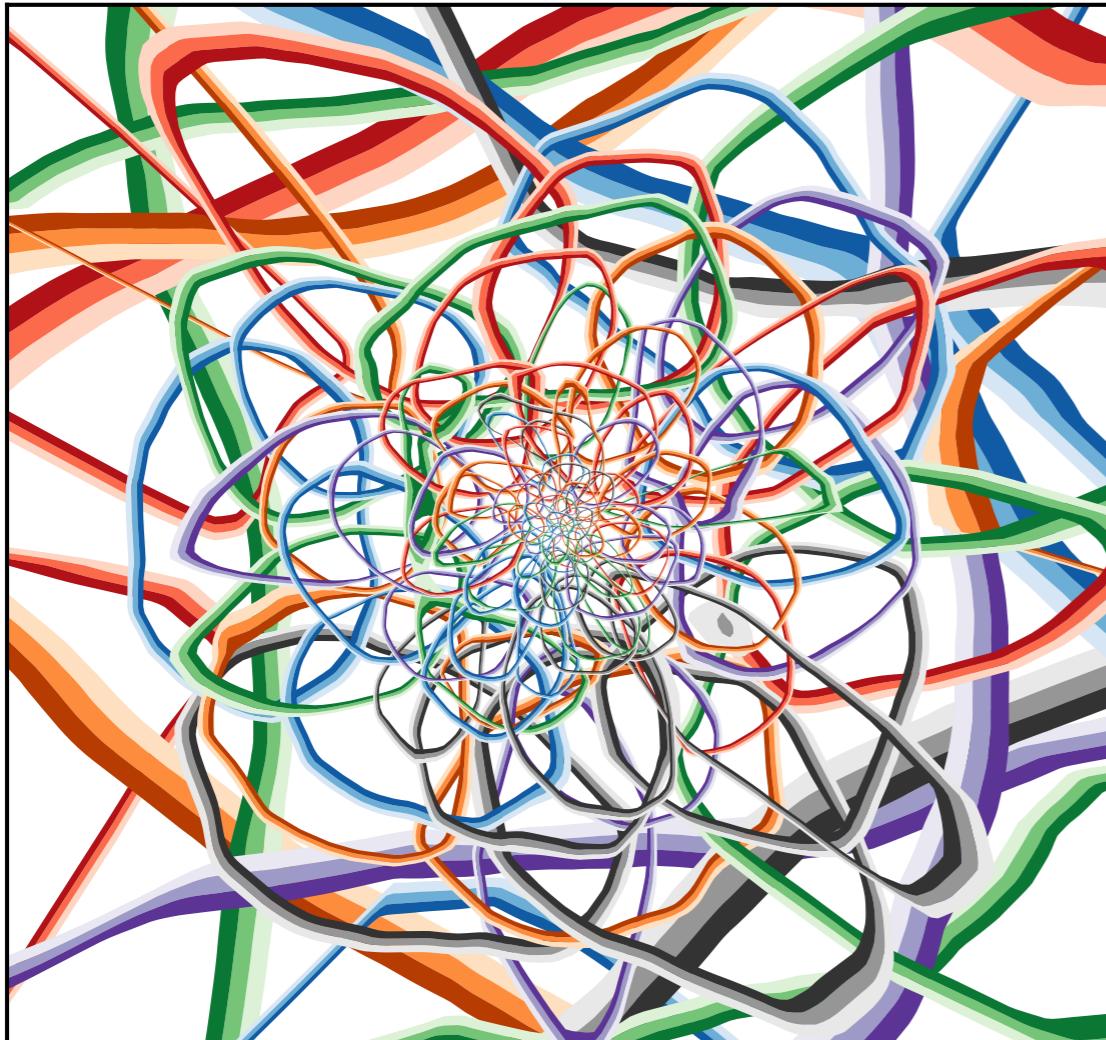
Latent Dimension 64



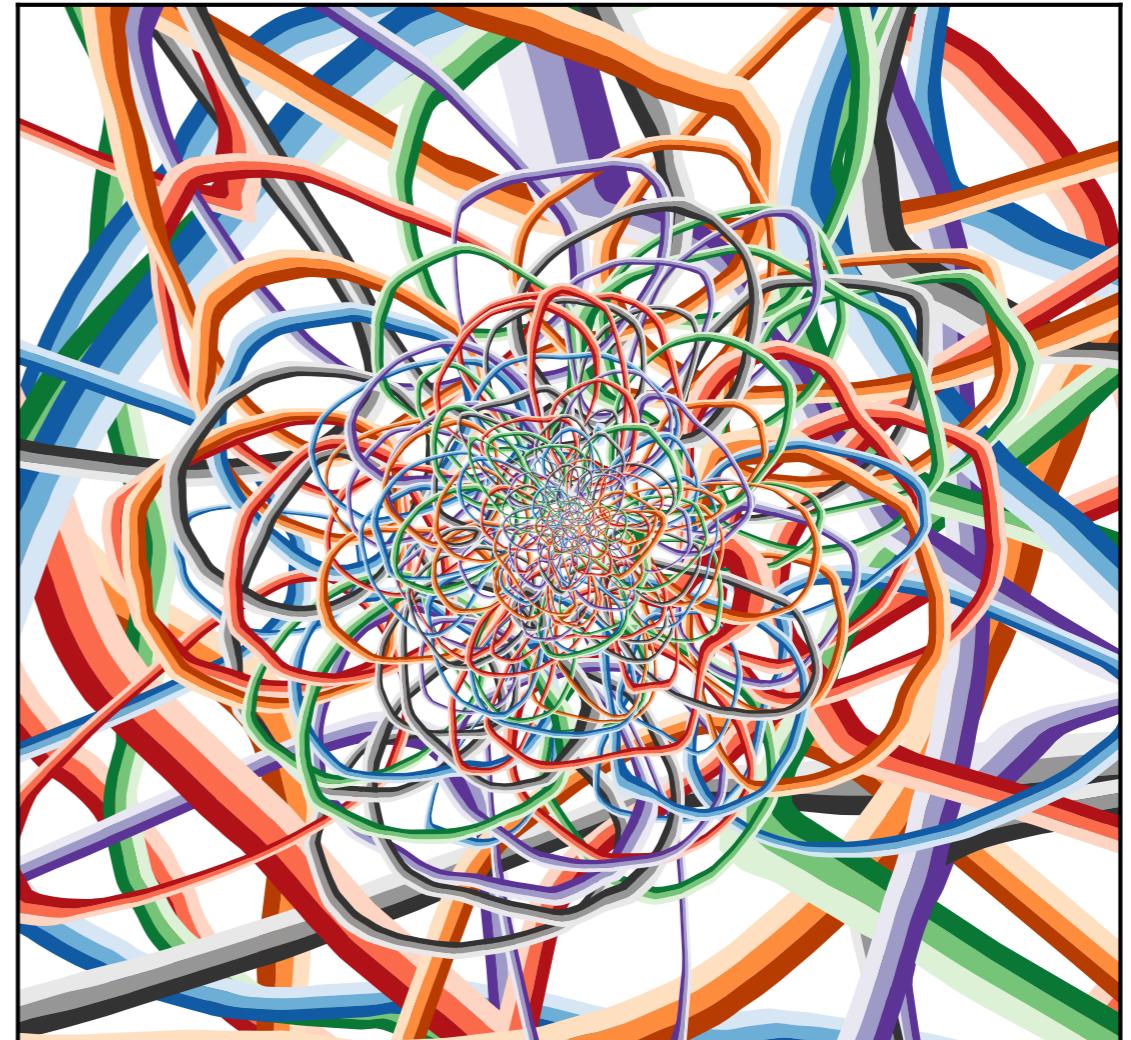
# Psychedelic Network Visualization

(see backup for  
how these are made)

Latent Dimension 128

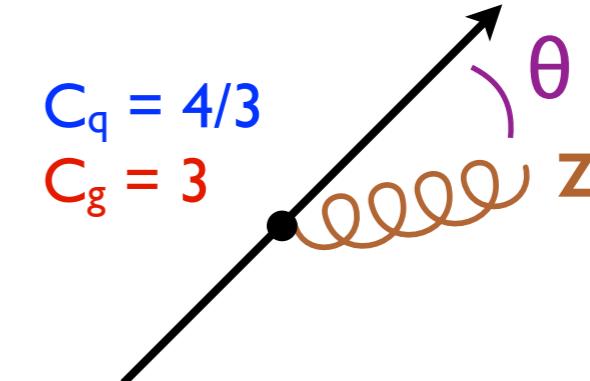
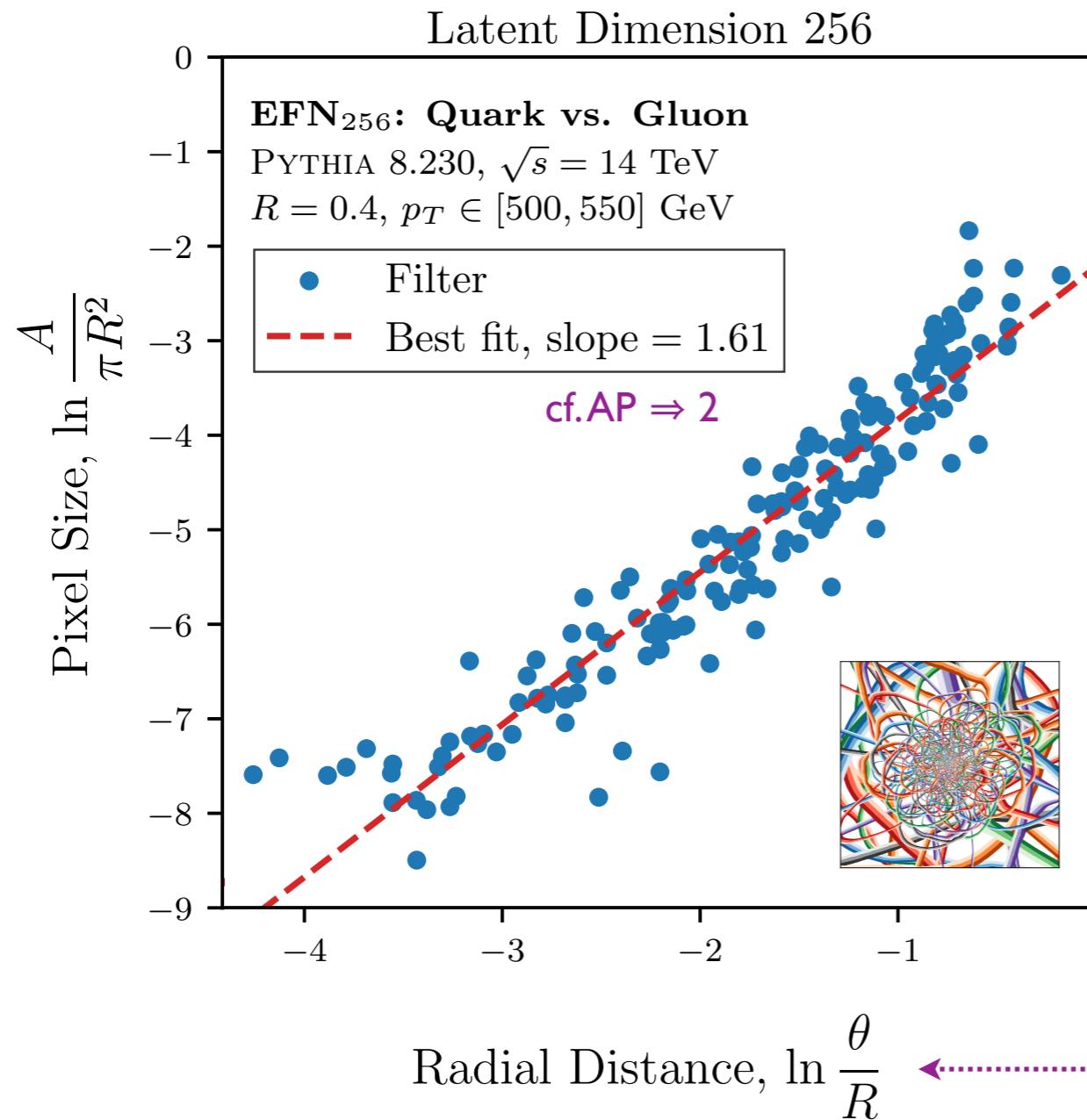
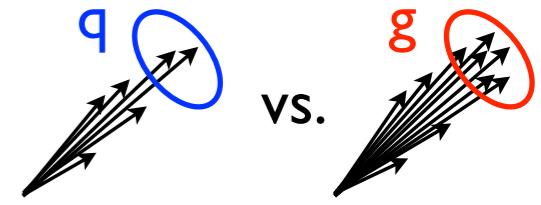


Latent Dimension 256



*Singularity structure of QCD!*

# Putting the AI in Altarelli-Parisi

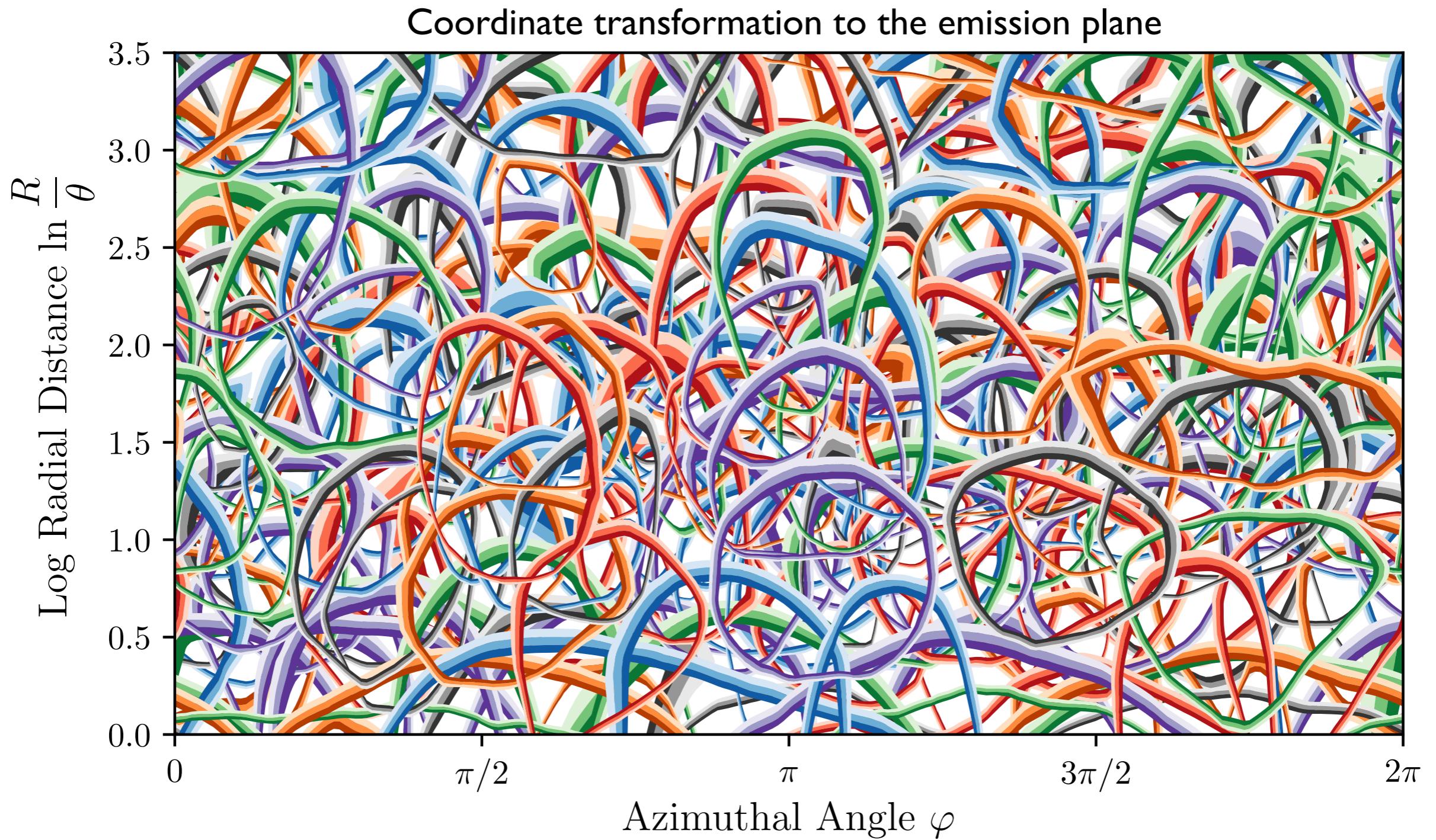


$$dP_{i \rightarrow ig} \simeq \frac{2\alpha_s}{\pi} C_i \frac{d\theta}{\theta} \frac{dz}{z}$$

Collinear Soft

[Komiske, Metodiev, JDT, 1810.05165]

# Suitable for Framing



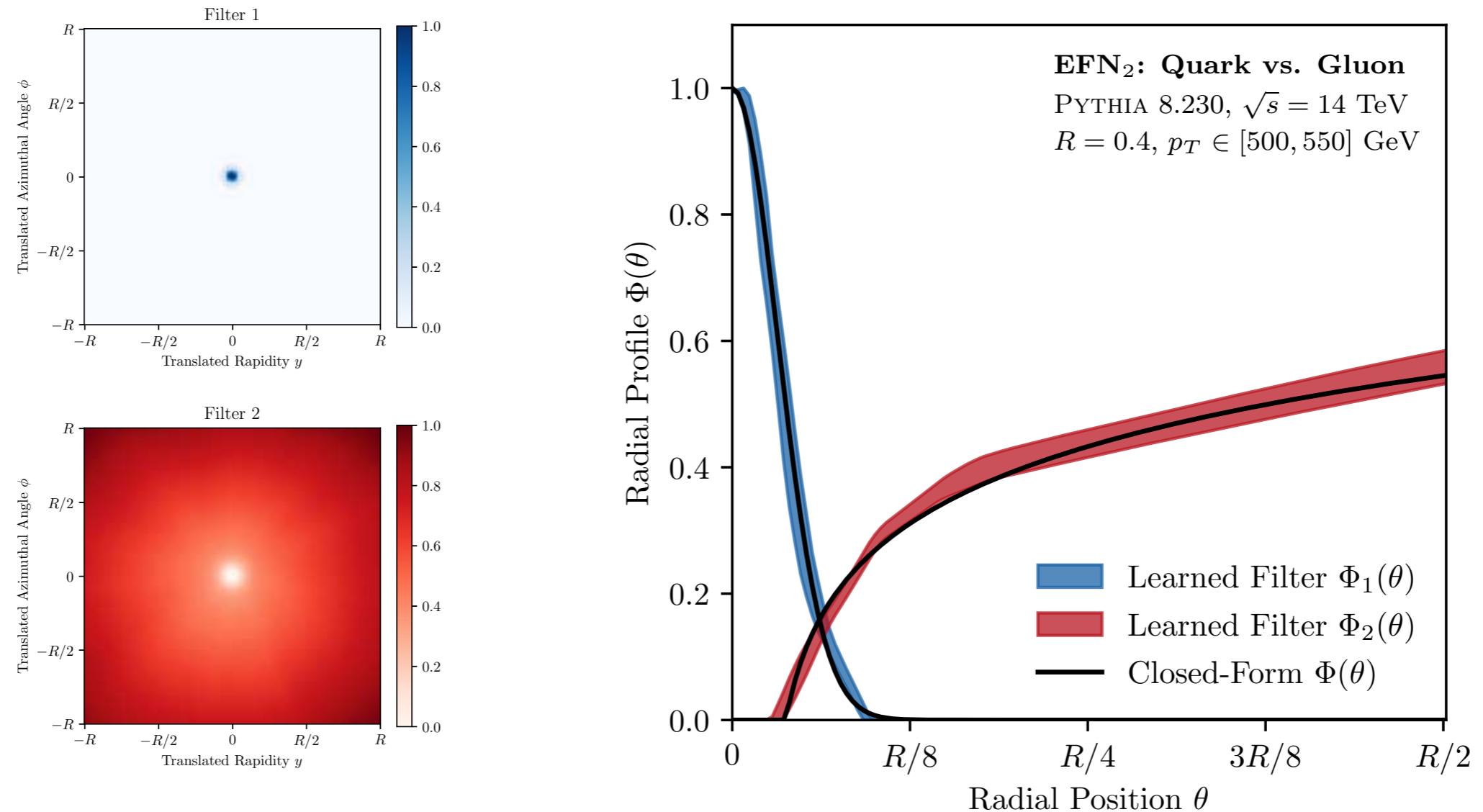
[Komiske, Metodiev, JDT, [1810.05165](#); see also Dreyer, Salam, Soyez, [1807.04758](#)]

*“Ok, but did you really learn something  
you didn’t already know?”*

# Learning from the Machine



For  $\ell = 2$  EFN, radial moments:  $\sum_{i \in \text{jet}} z_i f(\theta_i)$  cf. Angularities:  
 $f(\theta) = \theta^\beta$



[Komiske, Metodiev, JDT, [1810.05165](#);  
cf. Larkoski, JDT, Waalewijn, [JHEP08\(2018\)122](#); using Berger, Kucs, Sterman, [hep-ph/0303051](#); Ellis, Vermilion, Walsh, Hornig, Lee, [1001.0014](#)]

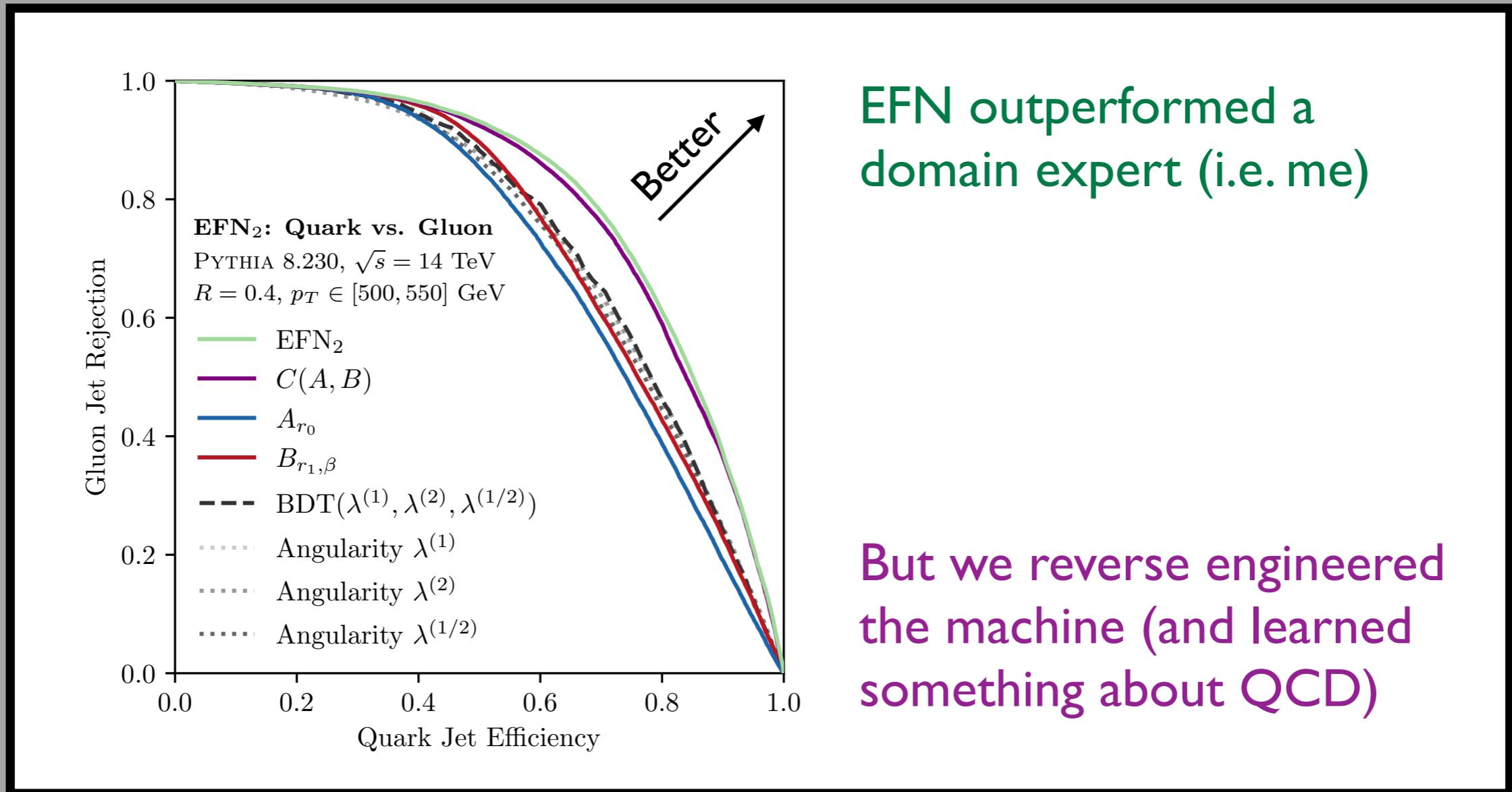
# Learning from the Machine



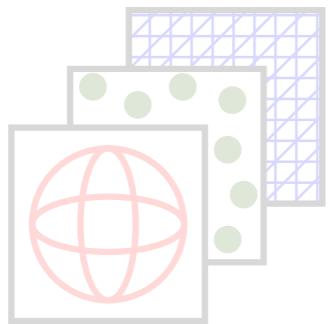
For  $\ell = 2$  EFN, radial moments:

$$\sum_{i \in \text{jet}} z_i f(\theta_i)$$

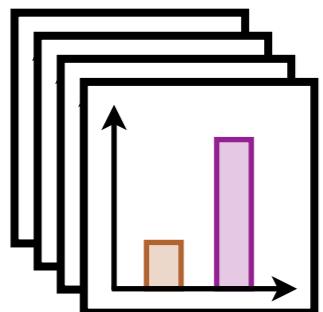
cf. Angularities:  
 $f(\theta) = \theta^\beta$



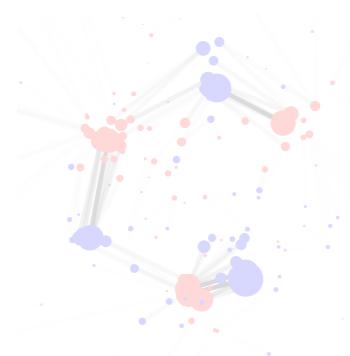
[Komiske, Metodiev, JDT, [1810.05165](#);  
cf. Larkoski, JDT, Waalewijn, [1408.3122](#); using Berger, Kucs, Sterman, [hep-ph/0303051](#); Ellis, Vermilion, Walsh, Hornig, Lee, [1001.0014](#)]



## Into the Network



## Data Ex Machina

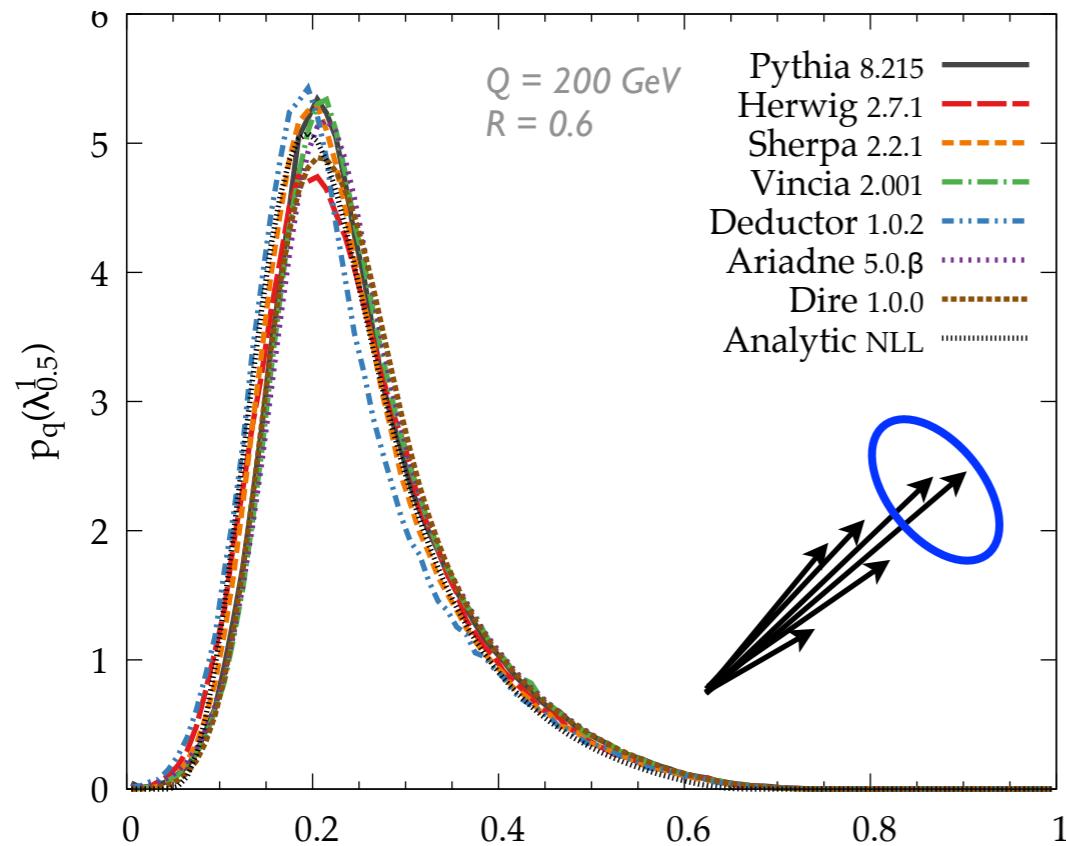


## (The Space of Jets)

*“Ok, but isn’t supervised learning only as reliable as your training samples?”*

# Uncertainties in Monte Carlo Samples?

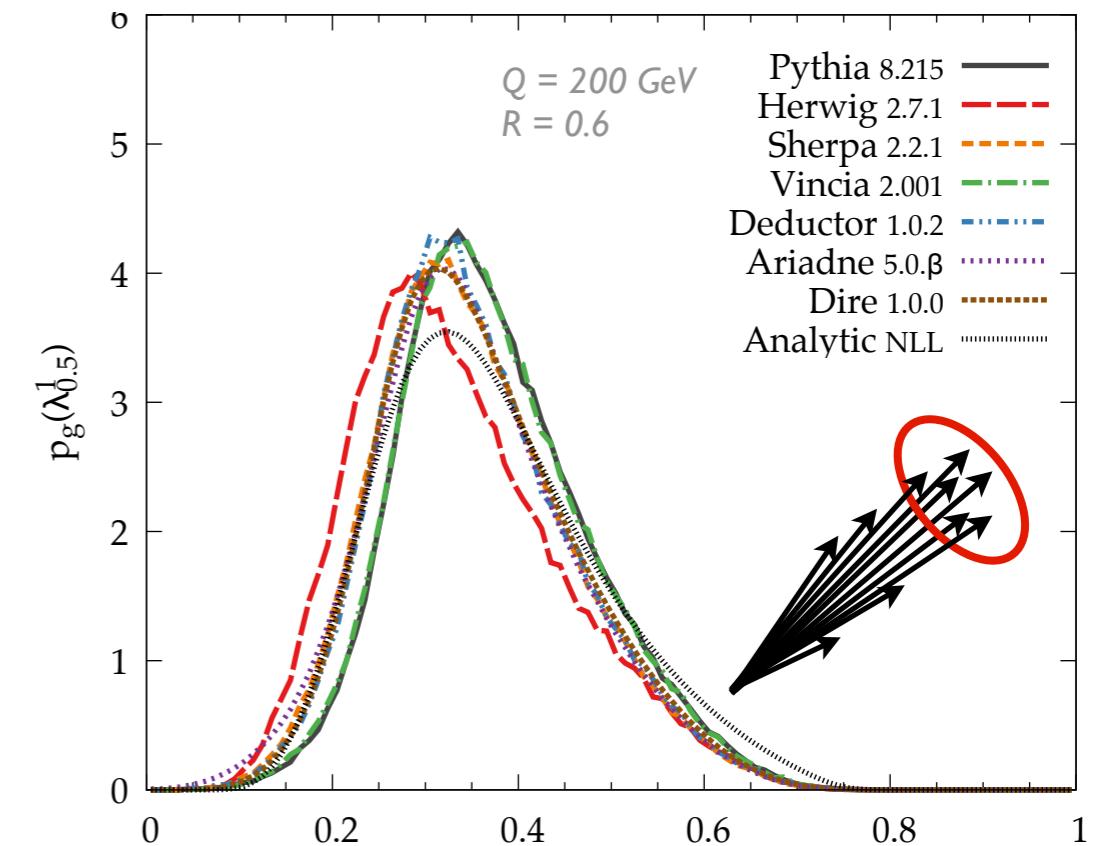
$e^+e^- \rightarrow \text{quarks } (C_F = 4/3)$



$$\text{LHA} = \sum_i z_i \sqrt{\theta_i}$$

VS.

$e^+e^- \rightarrow \text{gluons } (C_A = 3)$



$$\text{LHA} = \sum_i z_i \sqrt{\theta_i}$$

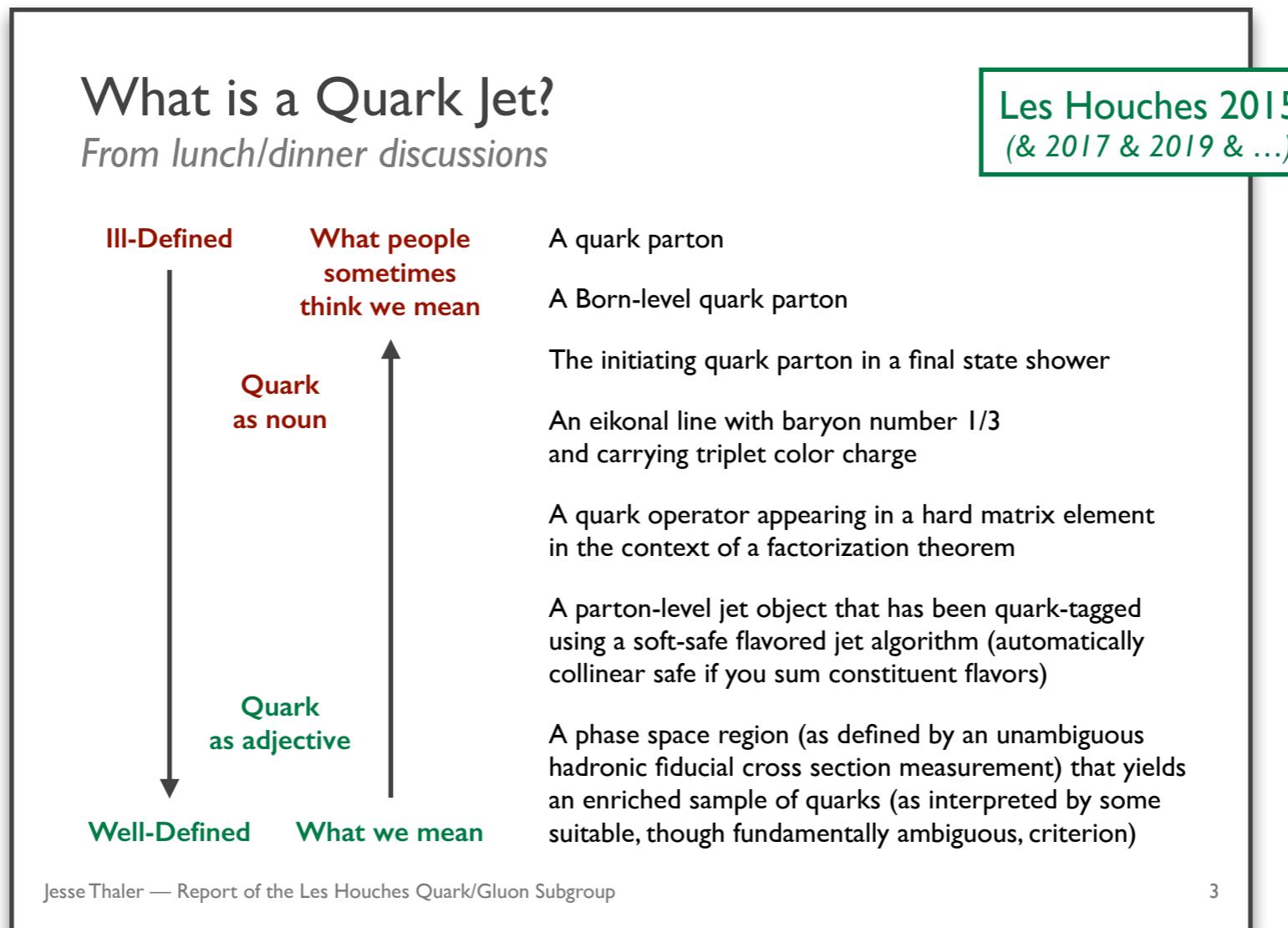
*Large shower variations (esp. gluon jets, hard to tune from LEP)*

[Gras, Hoeche, Kar, Larkoski, Lönnblad, Plätzer, Siódmok, Skands, Soyez, JDT, [J704.03878](#); see progress in Reichelt, Richardson, Siódmok, [J708.01491](#)]

# What are “Quarks” and “Gluons” anyways?

Color triplet vs. Color octet?

*But jet constituents are color-singlet hadrons!*



[Gras, Hoeche, Kar, Larkoski, Lönnblad, Plätzer, Siódtek, Skands, Soyez, JDT, [J704.03878](#); slide from Soyez, JDT, Freytsis, Gras, Kar, Lönnblad, Plätzer, Siódtek, Skands, Soper, [J1605.04692](#)]

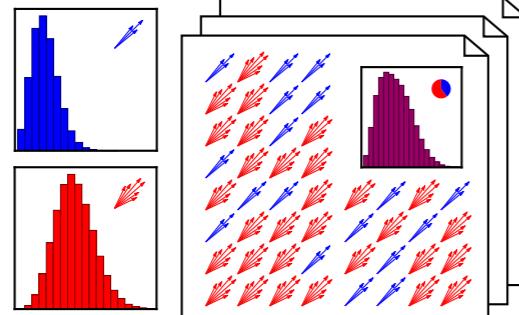
# Data ex Machina

*“A seemingly unsolvable problem is suddenly and abruptly resolved by an unexpected and seemingly unlikely occurrence, typically so much as to seem contrived”*

[slogan from Eric Metodiev; quote from Deus ex machina on Wikipedia]

# Enter Unsupervised Learning

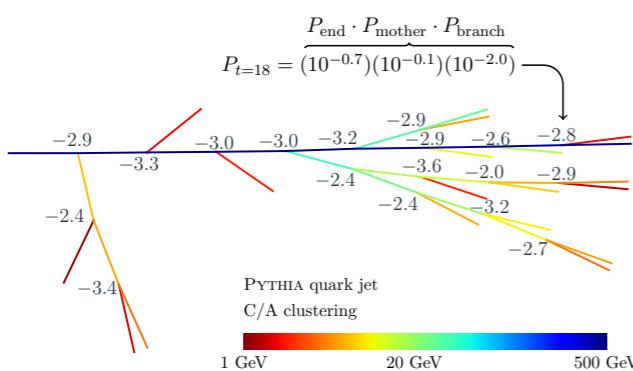
*Learning from *unlabeled* (or barely labeled) data*



## Jet Topics

*Blind Source Separation*

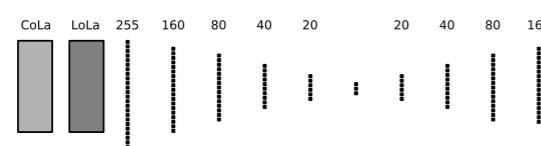
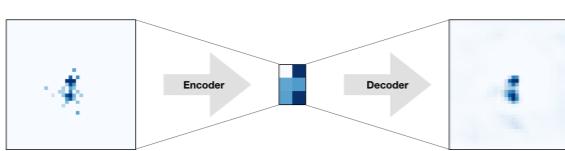
[Metodiev, JDT, [1802.00008](#); Komiske, Metodiev, JDT, [1809.01140](#);  
see also Metodiev, Nachman, JDT, [1708.02949](#); Dillon, Faroughy, Kamenik, [1904.04200](#)]



## JUNIPR

*Probability Modeling*

[Andreassen, Feige, Frye, Schwartz, [1804.09720](#), [1906.10137](#);  
see also Monk, [1807.03685](#)]



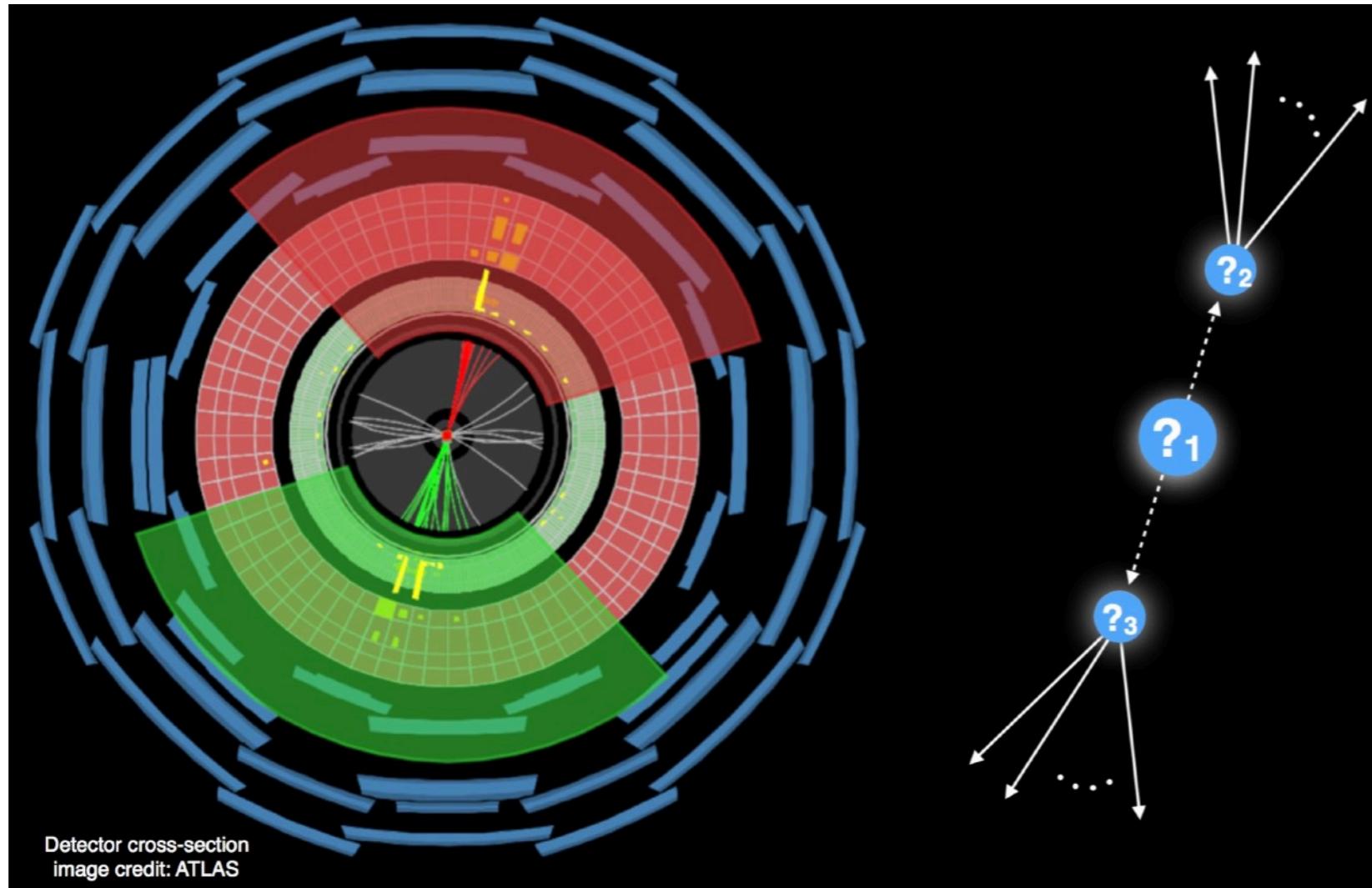
## Autoencoders

*Anomaly Detection*

[Hajer, Li, Liu, Wang, [1807.10261](#); Heimel, Kasieczka, Plehn, Thompson, [1808.08979](#);  
Farina, Nakai, Shih, [1808.08992](#); Cerri, Nguyen, Pierini, Spiropulu, Vlimant, [1811.10276](#);  
see also Collins, Howe, Nachman, [1805.02664](#), [1902.02634](#); De Simone, Jacques, [1807.06038](#)]

# LHC Olympics 2020

@ ML4Jets, NYU, January 15-17

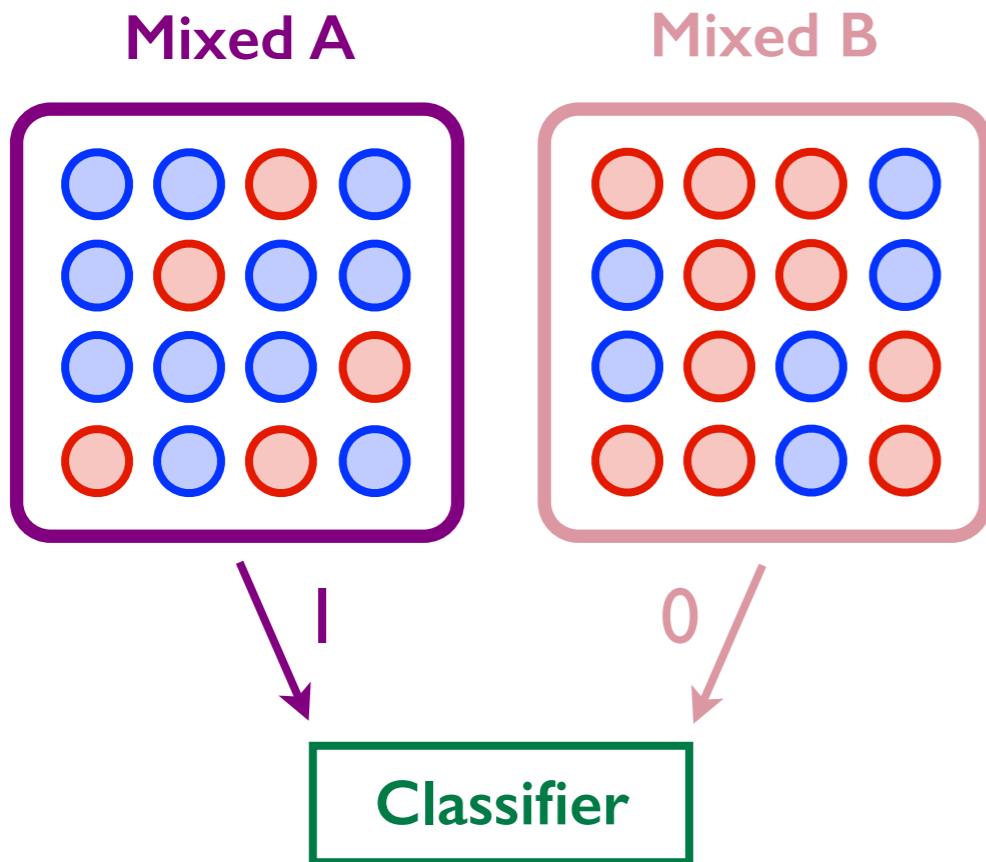


*An opportunity to stress test new **anomaly detection strategies***

# Biases from Training on Simulation?

*Train directly on mixed data!*

$$p_{\text{mixed}}(\vec{x}) = f_q \, p_{\text{quark}}(\vec{x}) + (1 - f_q) \, p_{\text{gluon}}(\vec{x})$$



$$\begin{aligned} h_{\text{mixed}}(\vec{x}) &= \frac{p_A(\vec{x})}{p_A(\vec{x}) + p_B(\vec{x})} \\ &\neq \\ h_{\text{pure}}(\vec{x}) &= \frac{p_q(\vec{x})}{p_q(\vec{x}) + p_g(\vec{x})} \end{aligned}$$

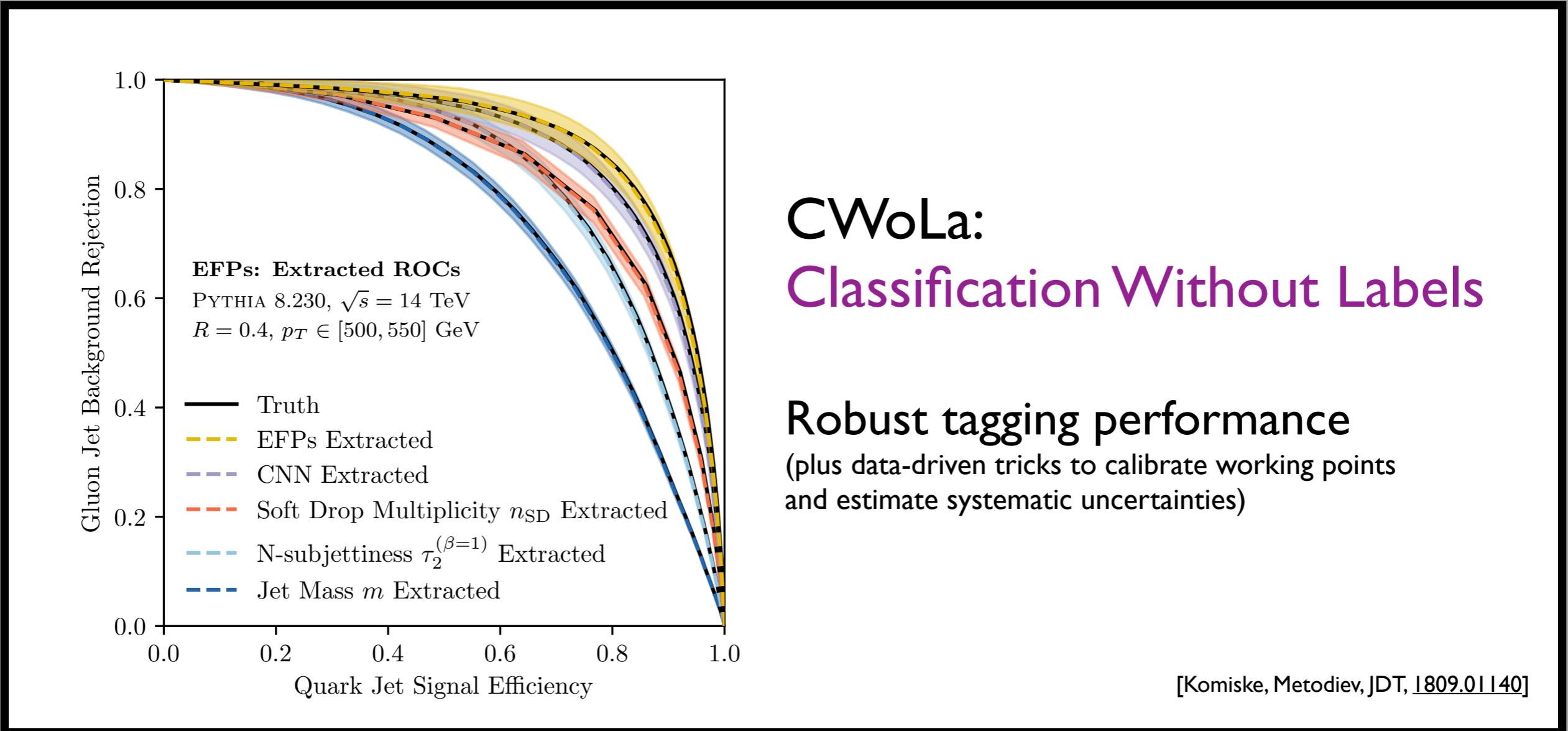
but...

$$\frac{\partial h_{\text{mixed}}(\vec{x})}{\partial h_{\text{pure}}(\vec{x})} > 0$$

[Metodiev, Nachman, JDT, [I708.02949](#);  
see also Blanchard, Flaska, Handy, Pozzi, Scott, [I303.I208](#); Cranmer, Pavez, Louppe, [I506.02169](#); Dery, Nachman, Rubbo, Schwartzman, [I702.00414](#);  
Cohen, Freytsis, Ostdiek, [I706.09451](#); Komiske, Metodiev, Nachman, Schwartz, [I801.10158](#); Collins, Howe, Nachman, [I805.02664](#), [I902.02634](#)]

# Biases from Training on Simulation?

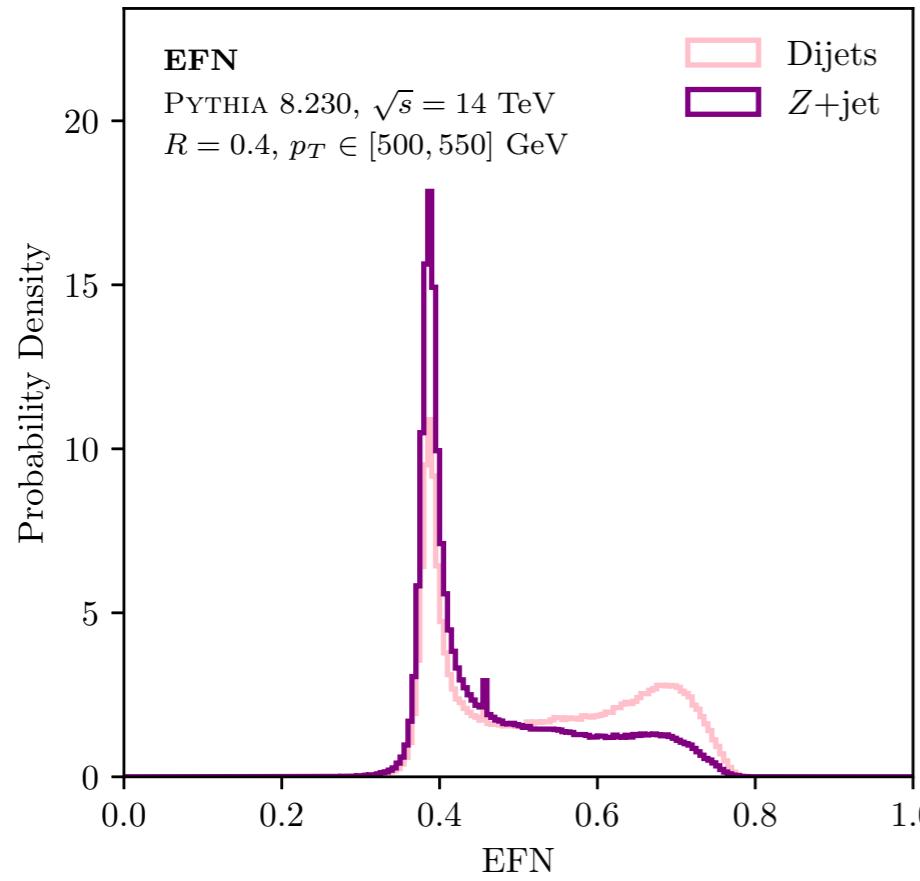
*Train directly on mixed data!*



[Metodiev, Nachman, JDT, [I708.02949](#);  
see also Blanchard, Flaska, Handy, Pozzi, Scott, [I303.I208](#); Cranmer, Pavez, Louppe, [I506.02169](#); Dery, Nachman, Rubbo, Schwartzman, [I702.00414](#);  
Cohen, Freytsis, Ostdiek, [I706.09451](#); Komiske, Metodiev, Nachman, Schwartz, [I801.10158](#); Collins, Howe, Nachman, [I805.02664](#), [I902.02634](#)]

# Ambiguous Definition of Jet Categories?

*Use classifiers to define categories!*



*Extract optimal jet categories from data,  
solely\* from assumption they exist (!)*

**Mutual Irreducibility**

“Anchor bins”:  
Pure representatives exist for  
each category (even if very rare)

**Sample Independence**

Mixed samples have  
different category fractions but  
same category properties



$$h_{\text{pure}} \in [0, 1]$$



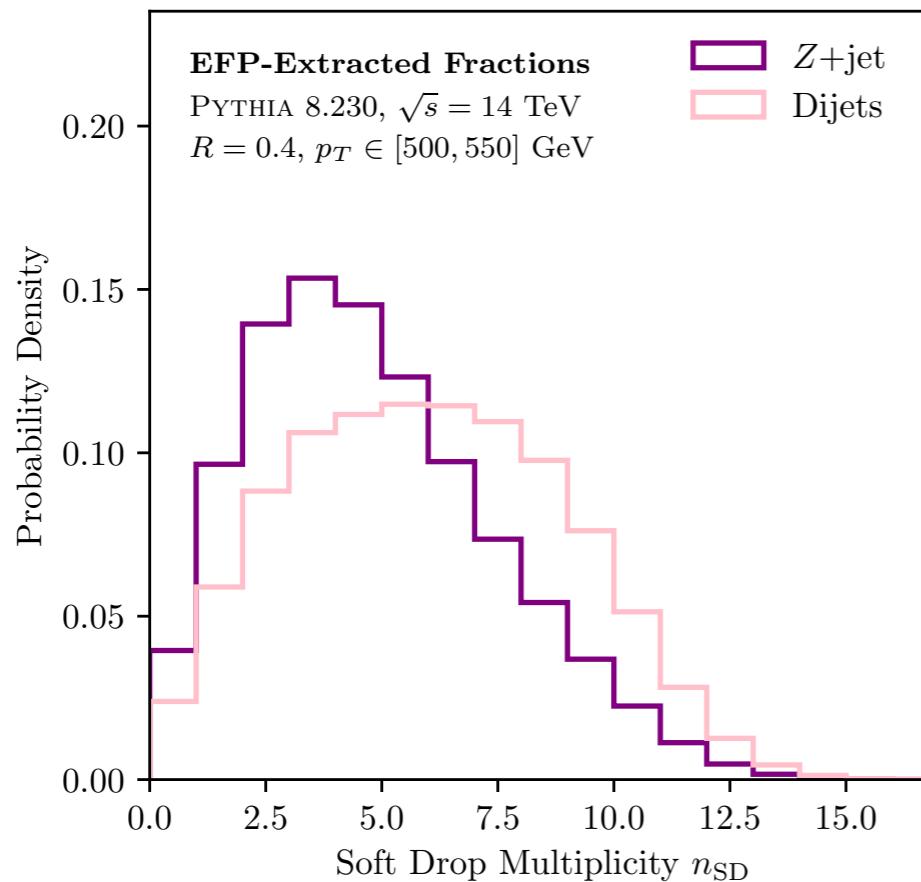
$$h_{\text{mixed}} \in \left[ \frac{f_g^A}{f_g^A + f_g^B}, \frac{f_q^A}{f_q^A + f_q^B} \right]$$

[Metodiev, JDT, [1802.00008](#); Komiske, Metodiev, JDT, [1809.01140](#); using Katz-Samuels, Blanchard, Scott, [1710.01167](#)]

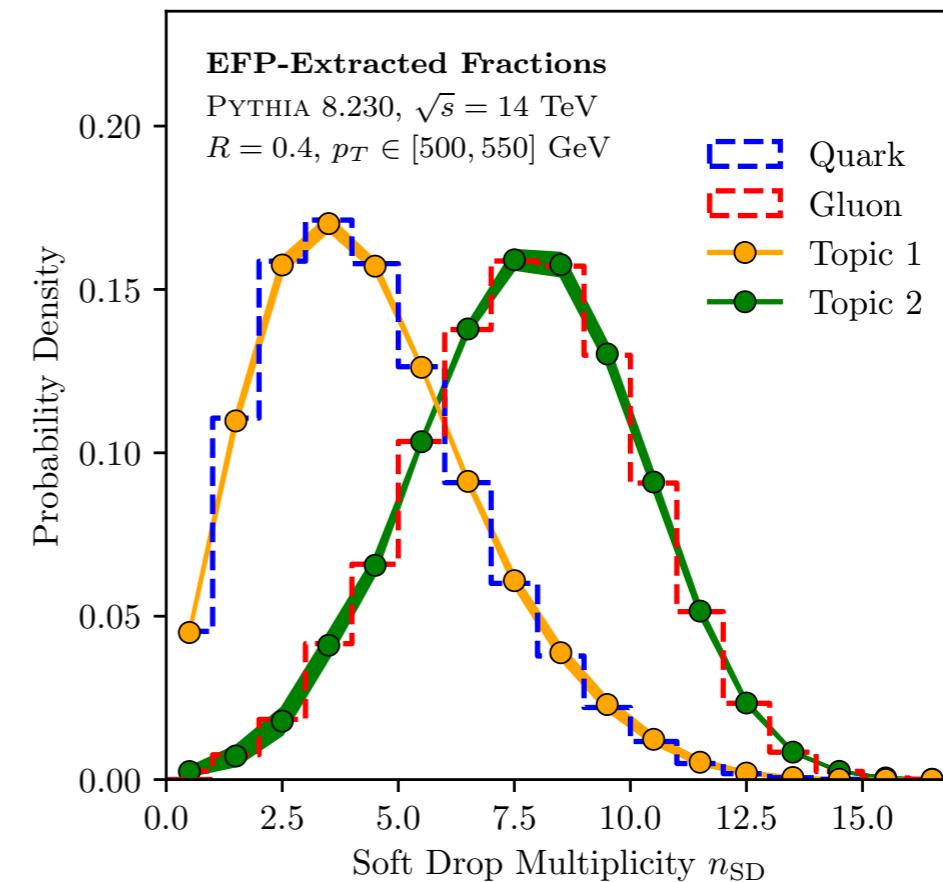
# Ambiguous Definition of Jet Categories?

*Use classifiers to define categories!*

**Z+jet vs. dijet**



**Topic 1 vs. Topic 2**

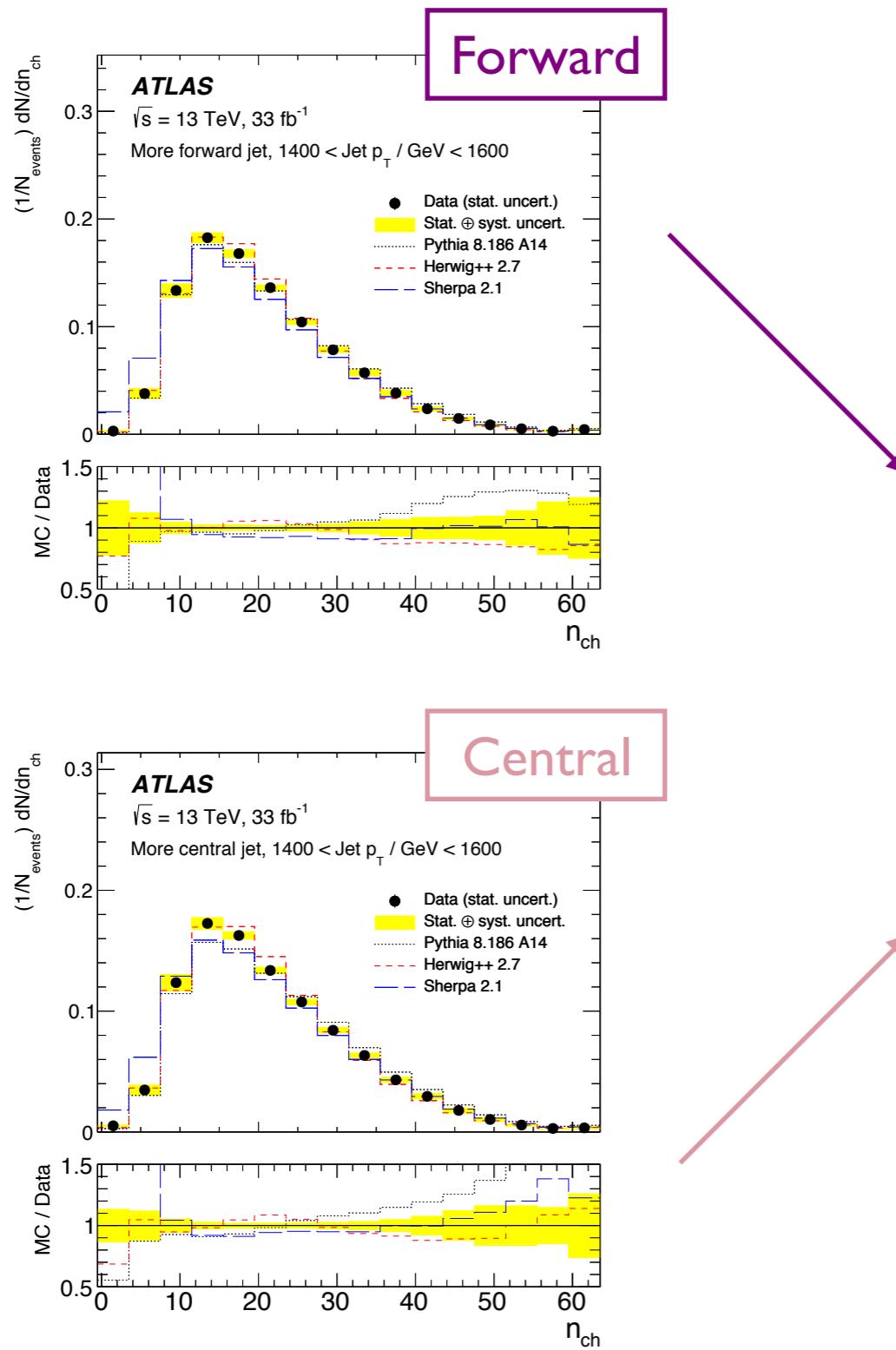


⇒ Operational Definition of “Quark” vs. “Gluon”

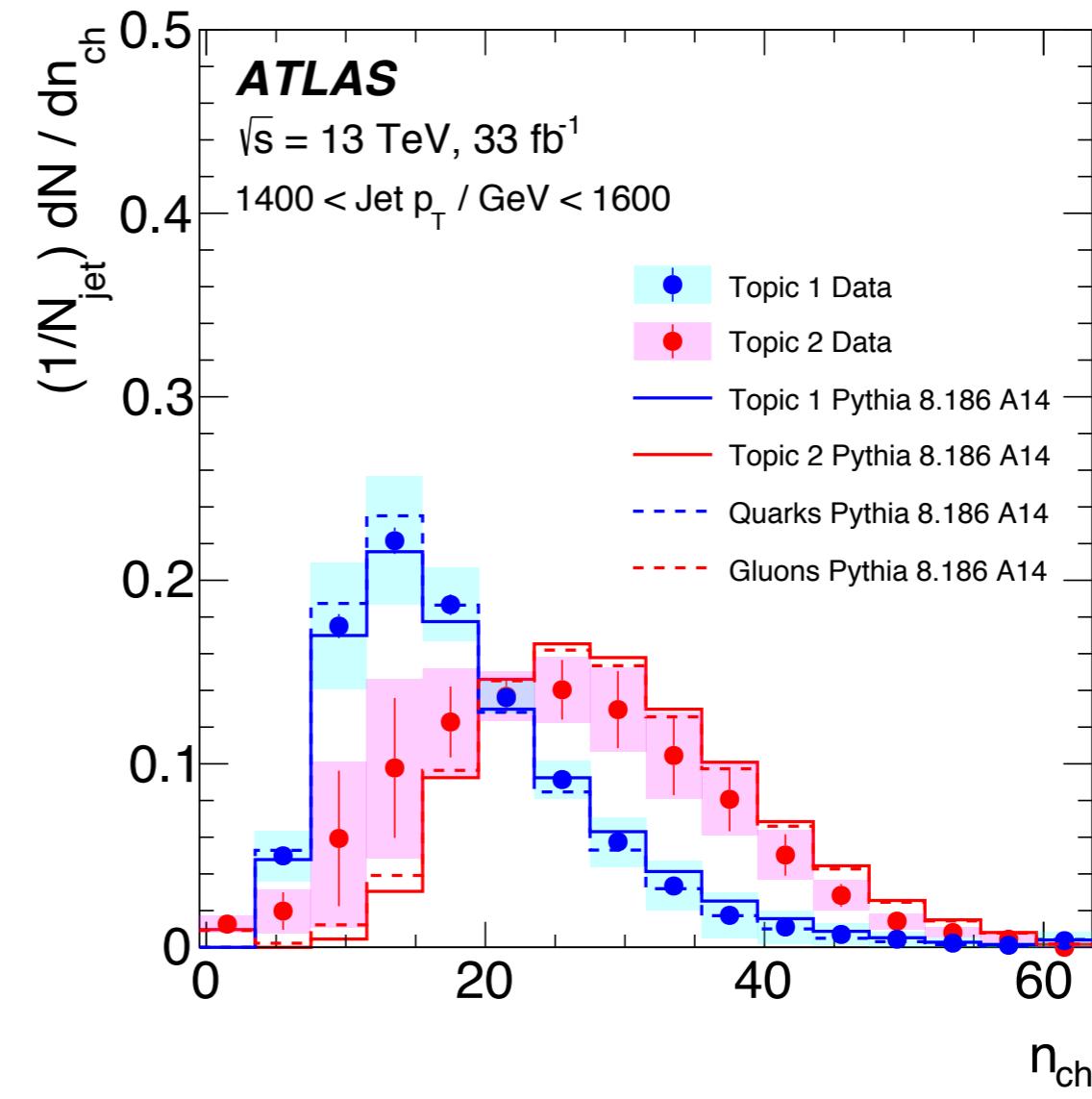
[Metodiev, JDT, [1802.00008](#); Komiske, Metodiev, JDT, [1809.01140](#); using Katz-Samuels, Blanchard, Scott, [1710.01167](#)]

*“Ok, but do you really think these techniques will ever be applied to real LHC data?”*

# First Jet Topics Result from ATLAS



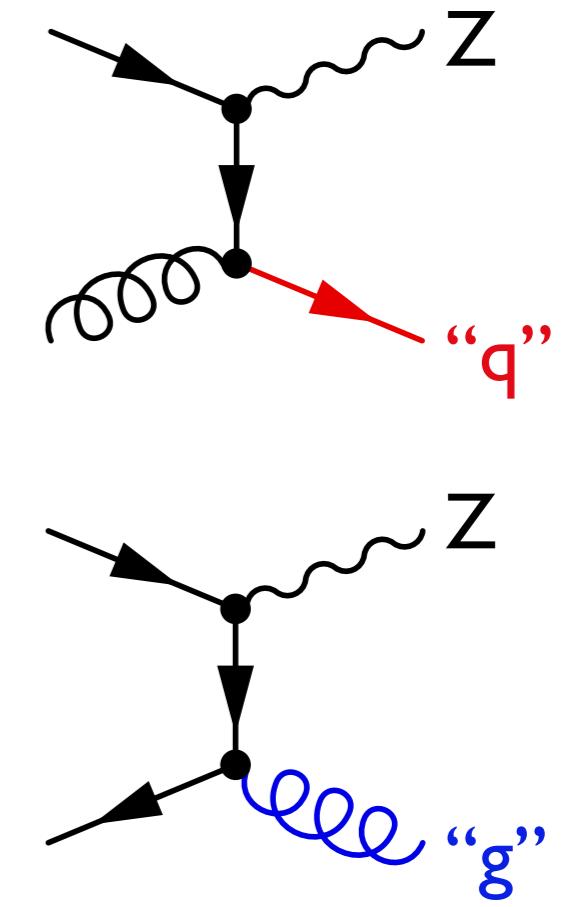
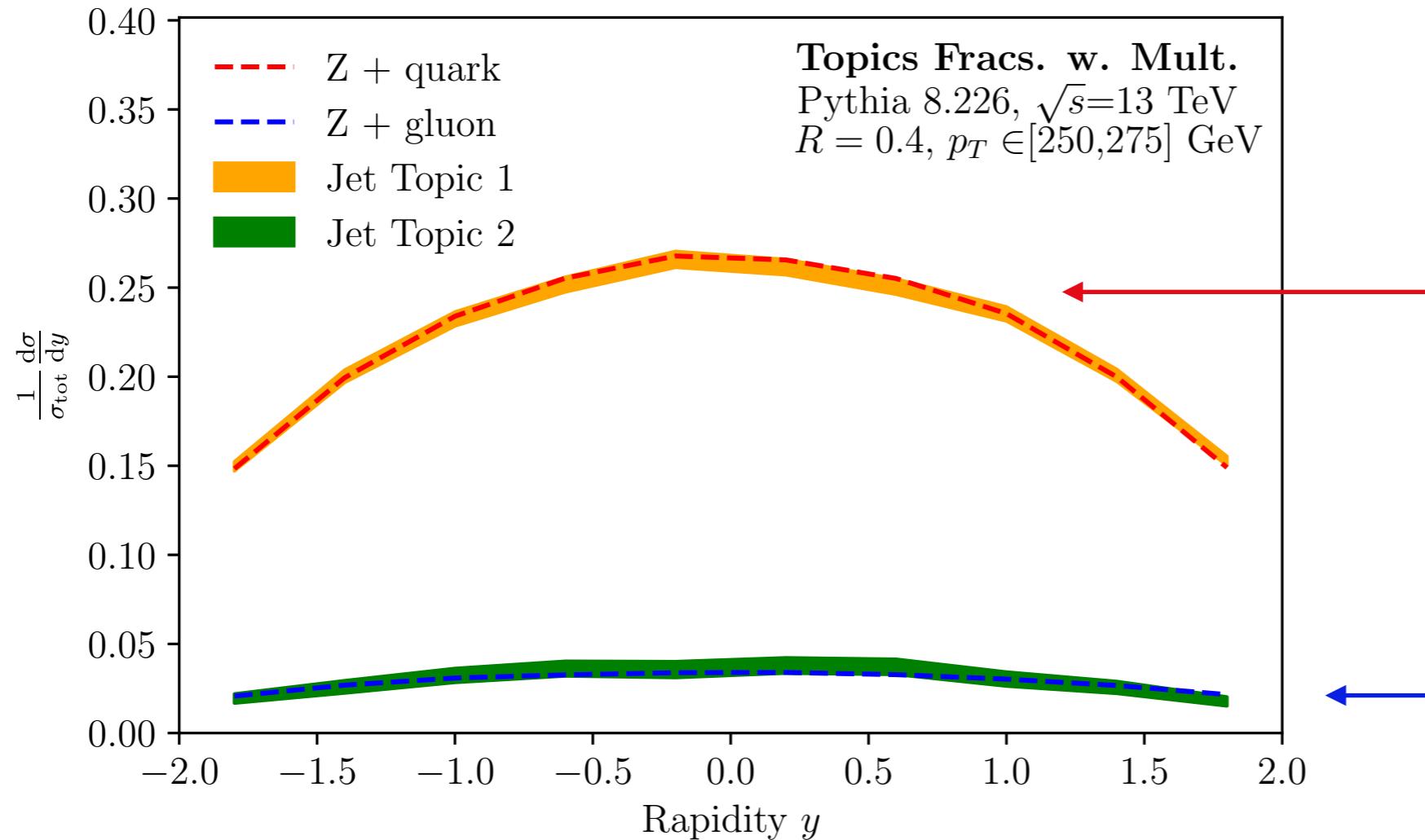
Track multiplicity for  
“Topic 1” and “Topic 2”



[ATLAS, [1906.09254](#)]

# “Parton”-Labeled Cross Sections?

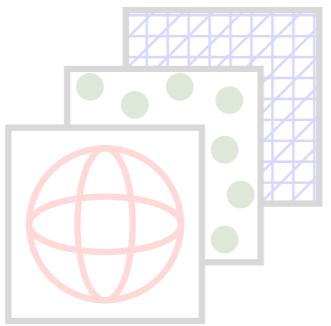
Potential boon for PDF extraction at colliders



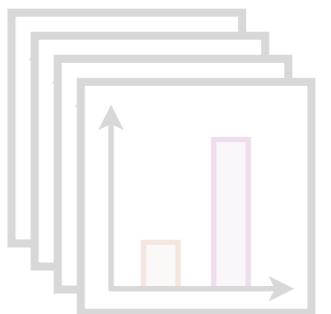
Key Challenges:

- Sample dependence from color coherence
- Limited statistics in anchor bin region
- Defining jet topics at fixed order

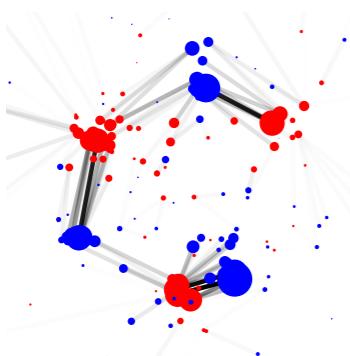
[Metodiev, JDT, 1802.00008]



## Into the Network



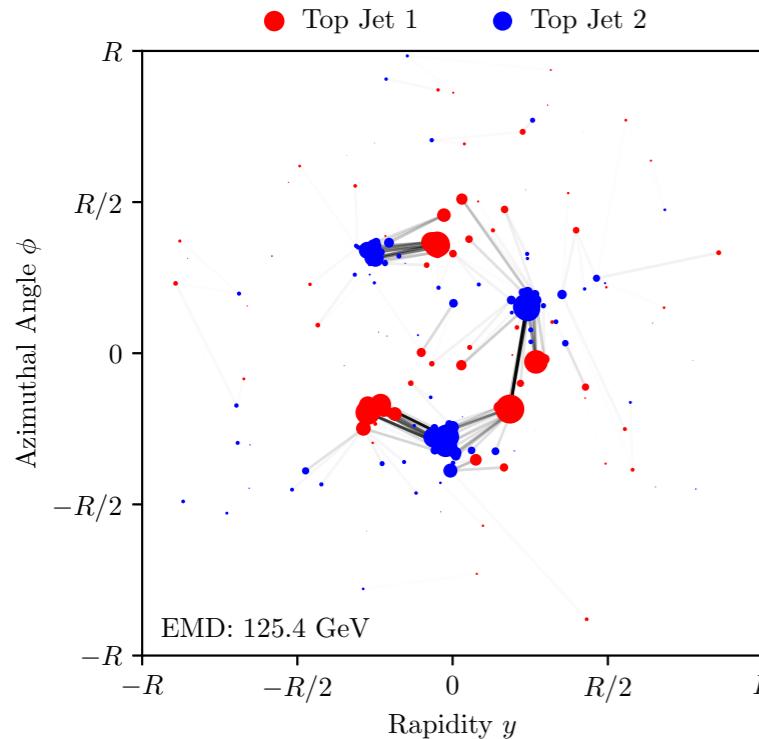
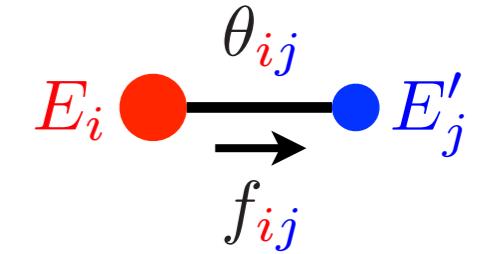
## Data Ex Machina



## (The Space of Jets)

# The Energy Mover's Distance

Closely related to  $\mathcal{I}$ -Wasserstein metric



Optimal transport between energy flows...

$$\text{EMD}(\mathcal{E}, \mathcal{E}') = \min_{\{f\}} \sum_i \sum_j f_{ij} \frac{\theta_{ij}}{R} + \left| \sum_i E_i - \sum_j E'_j \right|$$

↑  
in GeV

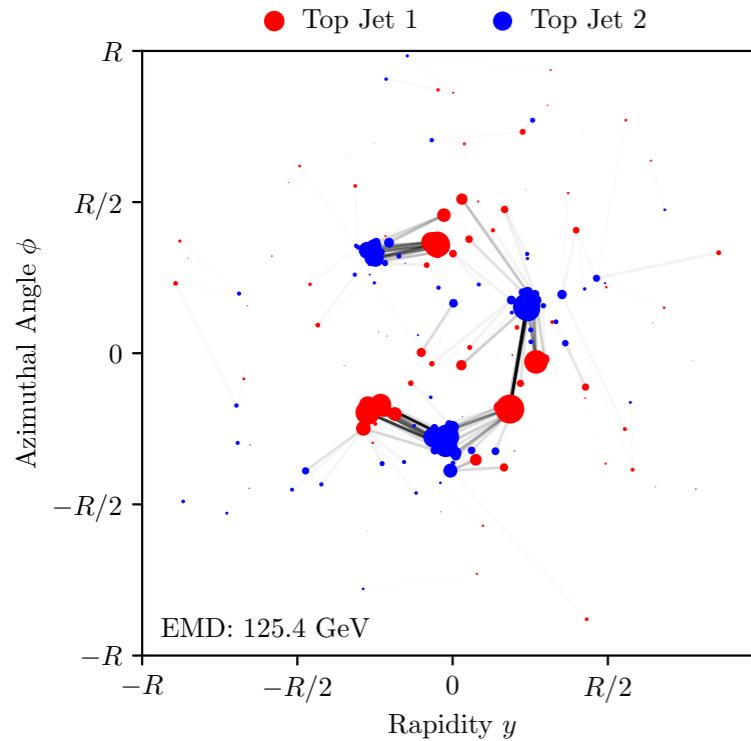
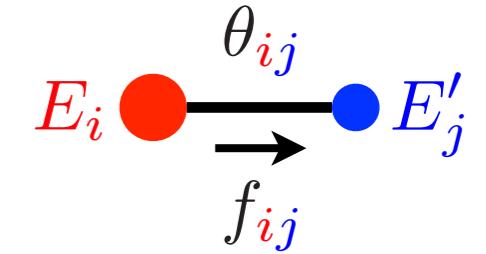
**Cost to move energy**

**Cost to create energy**

[Komiske, Metodiev, JDT, [1902.02346](#);  
see also Peleg, Werman, Rom, [IEEE 1989](#); Rubner, Tomasi, Guibas, [ICCV 1998](#), [ICJV 2000](#); Pele, Werman, [ECCV 2008](#); Pele Taskar, [GSI 2013](#)]

# The Energy Mover's Distance

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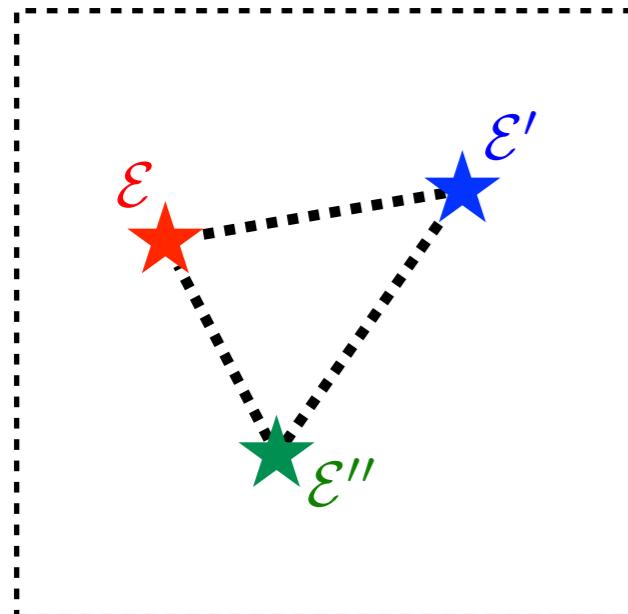


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↑  
in GeV

Cost to move energy      Cost to create energy



...defines a metric on the space of events

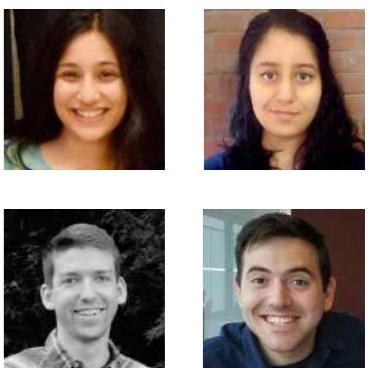
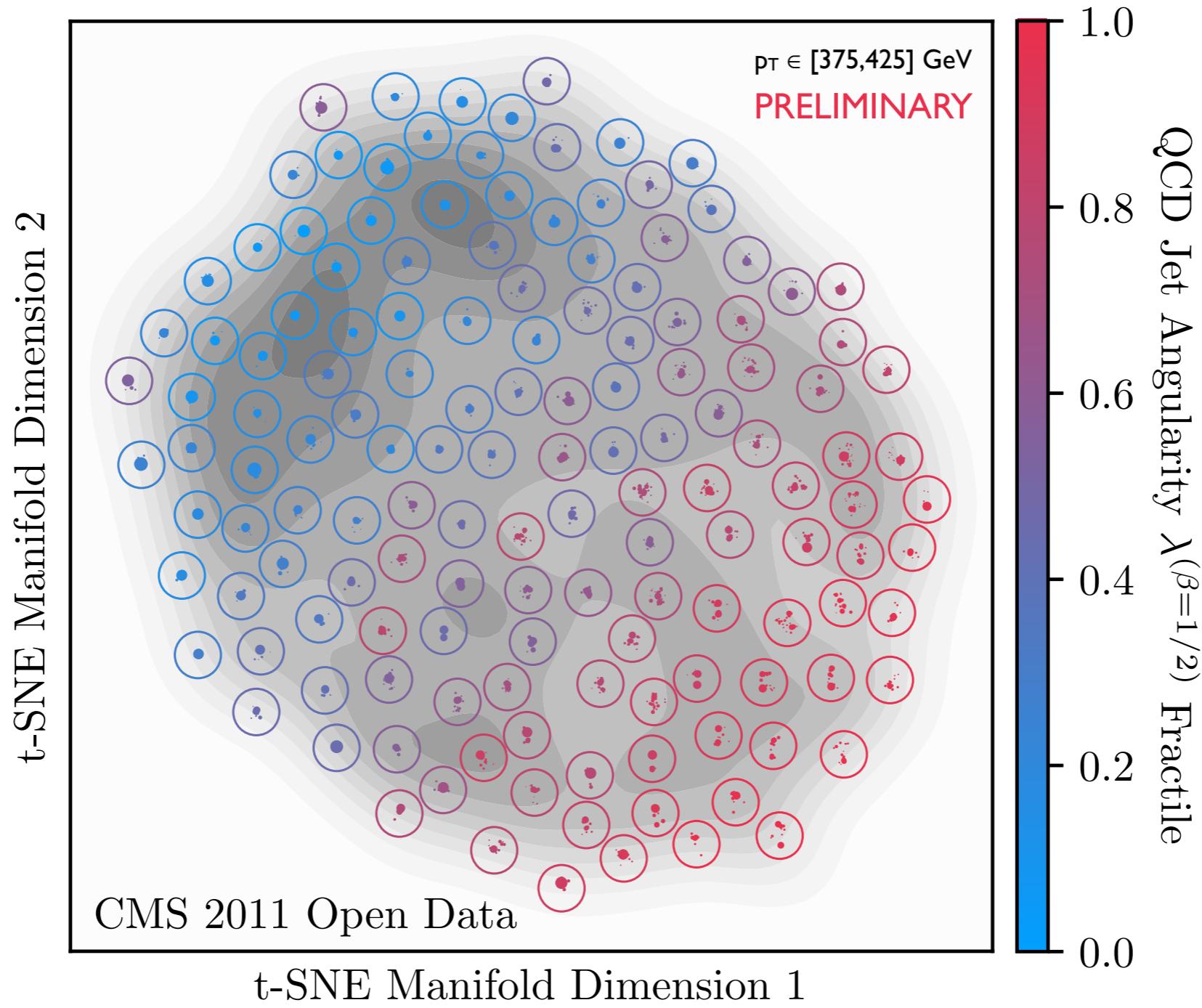
$$0 \leq \text{EMD}(\mathcal{E}, \mathcal{E}') \leq \text{EMD}(\mathcal{E}, \mathcal{E}'') + \text{EMD}(\mathcal{E}', \mathcal{E}'')$$

(assuming  $R \geq \theta_{\max}/2$ , i.e.  $R \geq$  jet radius for conical jets)

[Komiske, Metodiev, JDT, [1902.02346](#);

see also Peleg, Werman, Rom, [IEEE 1989](#); Rubner, Tomasi, Guibas, [ICCV 1998](#), [ICJV 2000](#); Pele, Werman, [ECCV 2008](#); Pele Taskar, [GSI 2013](#)]

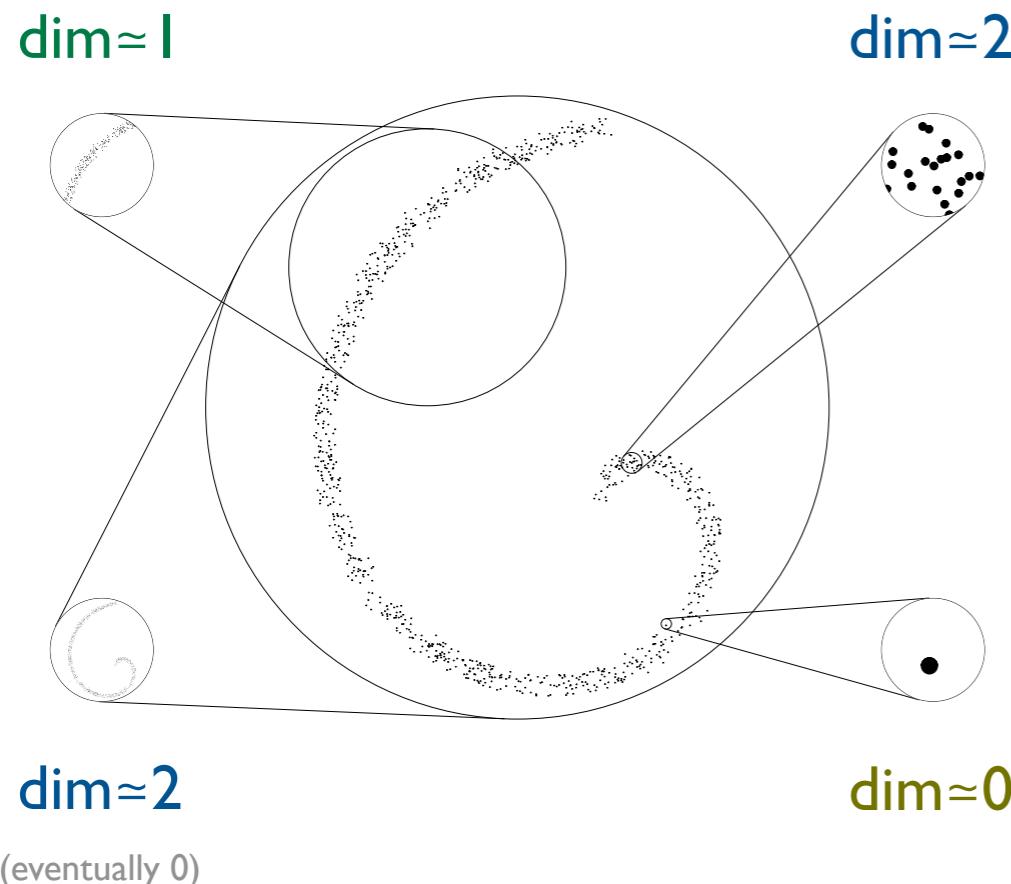
# The Space of Quark/Gluon Jets



[Komiske, Mastandrea, Metodiev, Naik, JDT, in preparation]

# Quantifying Dimensionality

**Correlation Dimension:**  $\dim(Q) = Q \frac{\partial}{\partial Q} \ln \sum_i \sum_j \Theta(\text{EMD}(\mathcal{E}_i, \mathcal{E}_j) < Q)$



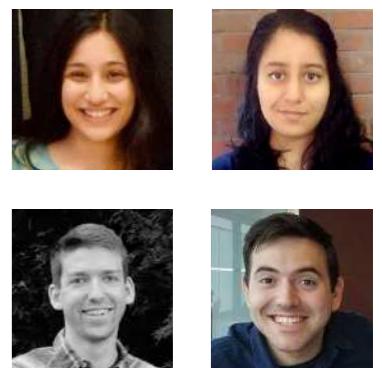
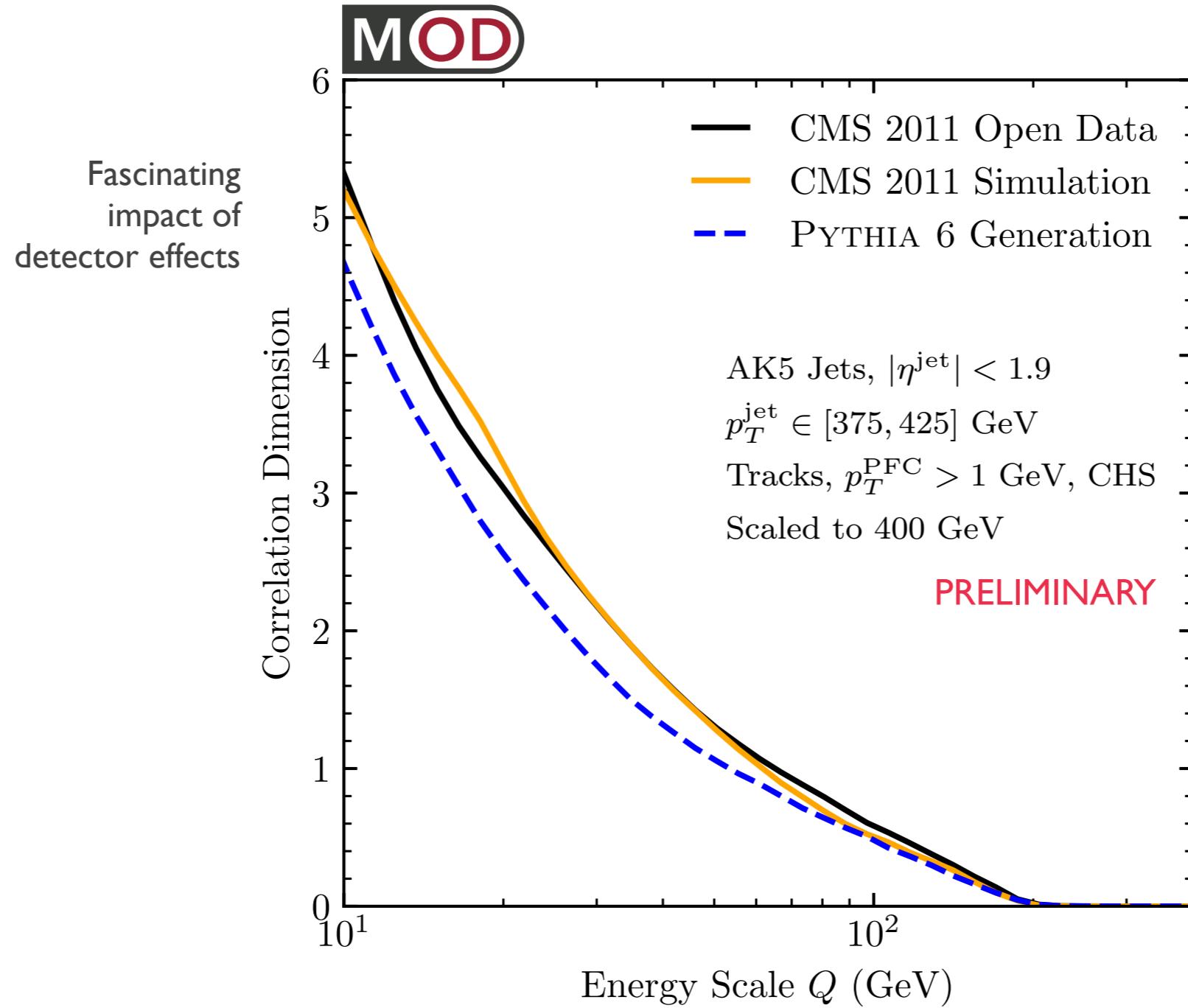
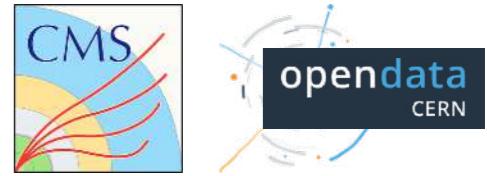
$$N_{\text{neighbors}}(r) \sim r^{\dim}$$



$$\dim(r) \sim r \frac{\partial}{\partial r} \ln N_{\text{neighbors}}(r)$$

[Grassberger, Procaccia, [PRL 1983](#); Kégl, [NIPS 2002](#)]

# The Dimension of Quark/Gluon Jets



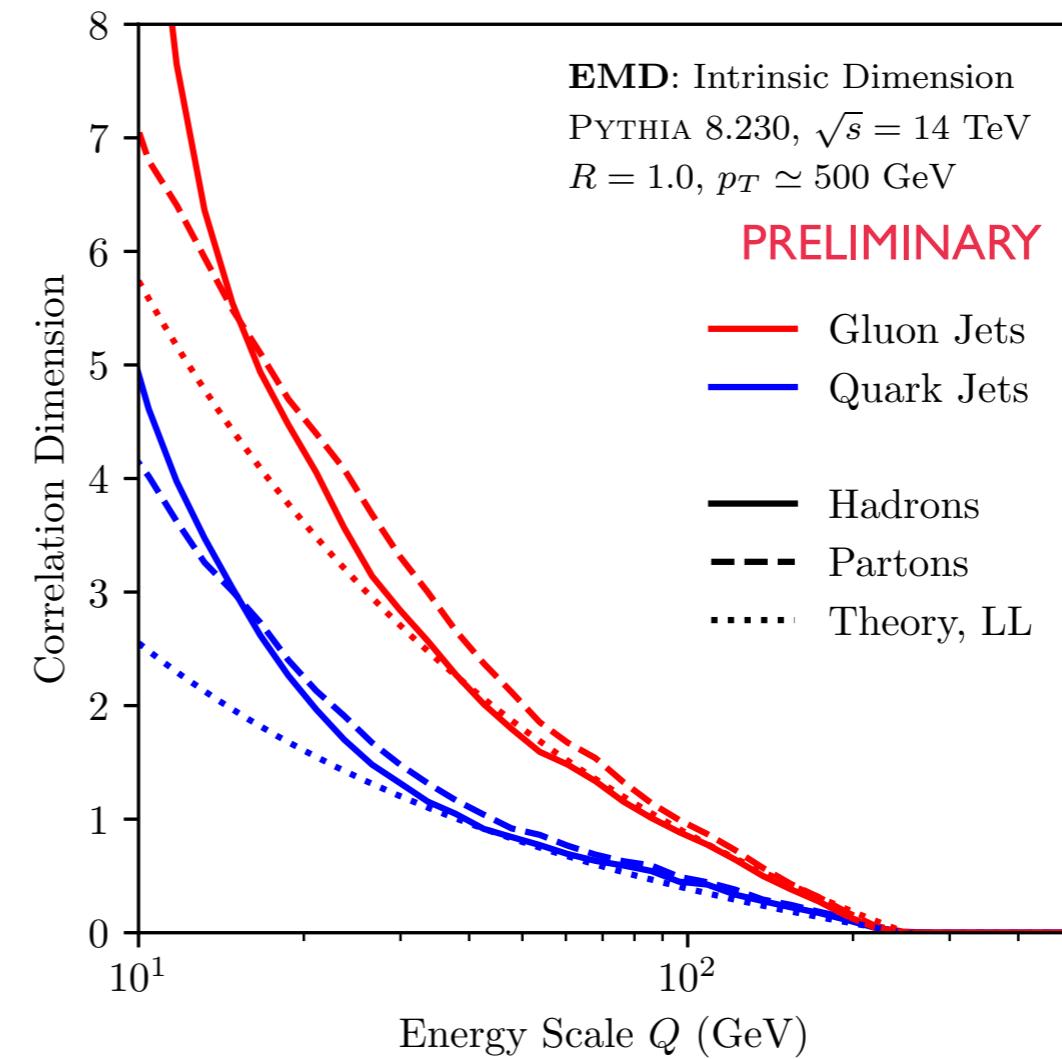
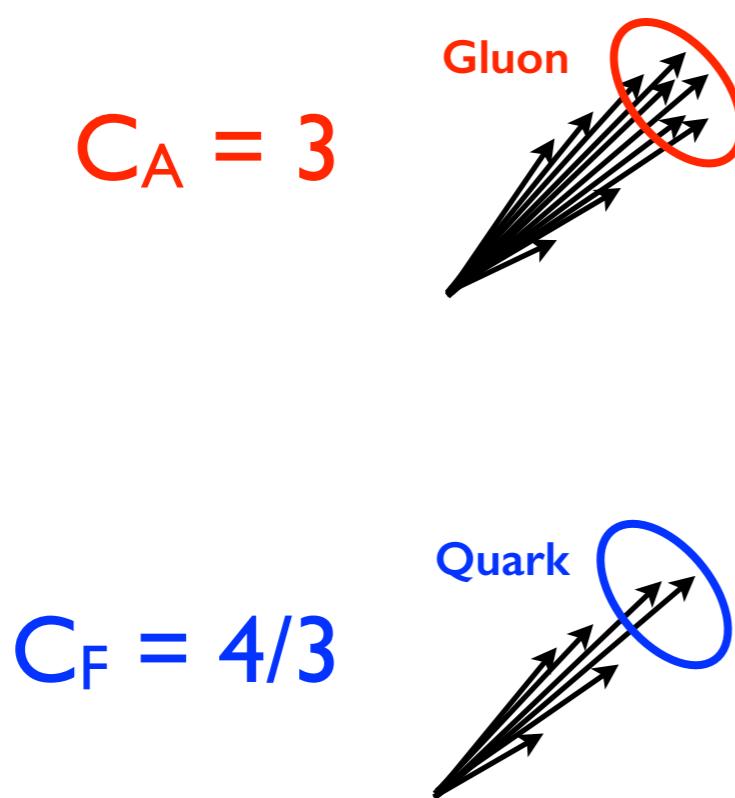
[Komiske, Mastandrea, Metodiev, Naik, JDT, in preparation]

# Preliminary Calculation

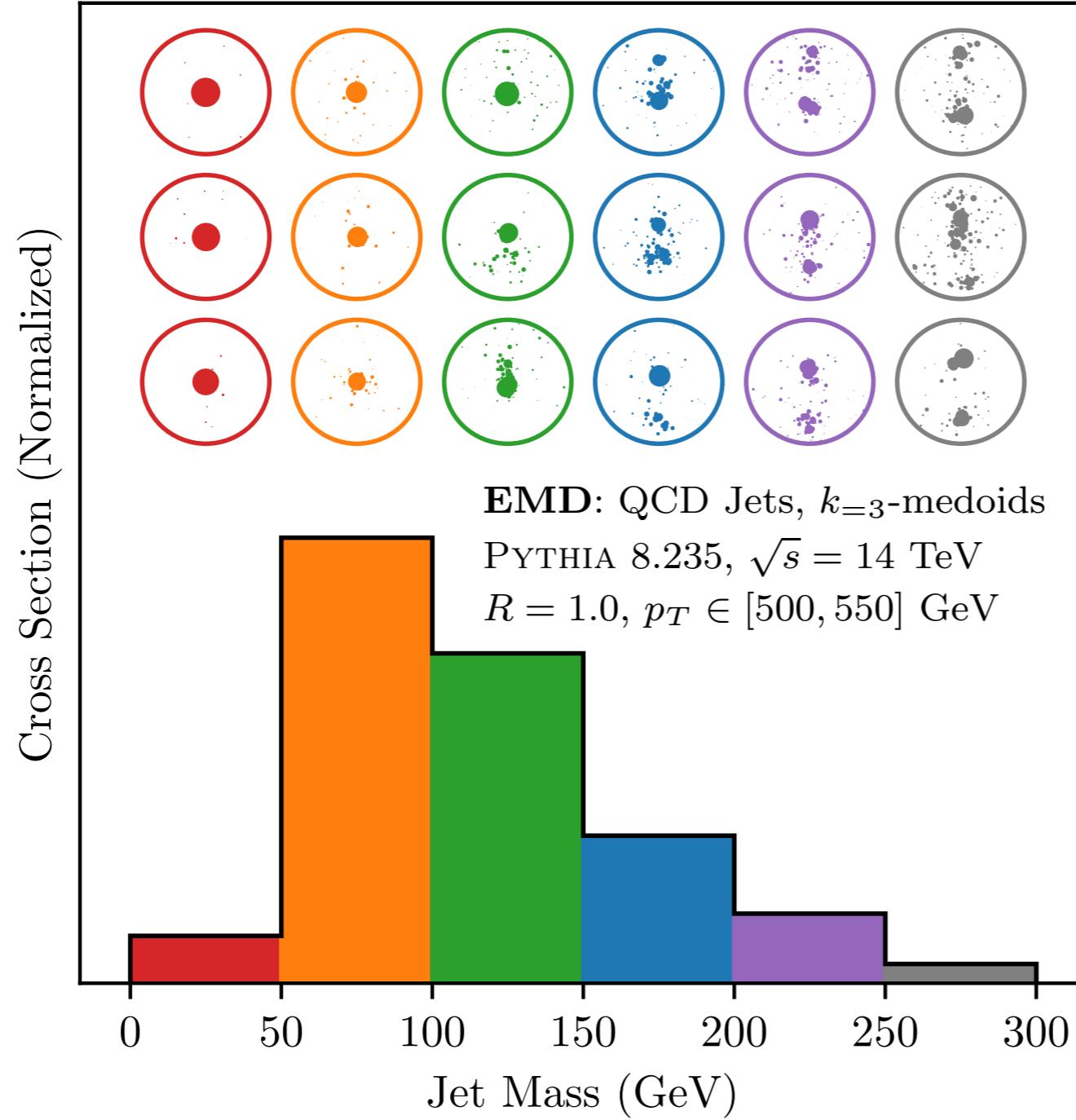
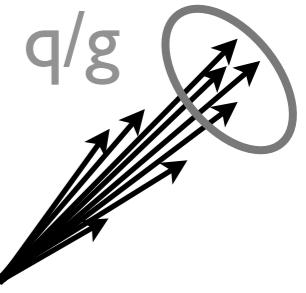
**Leading Log:**  
(single log, since dim has derivative)

$$\dim_i(Q) \simeq -\frac{8\alpha_s}{\pi} C_i \ln \frac{Q}{p_T}$$

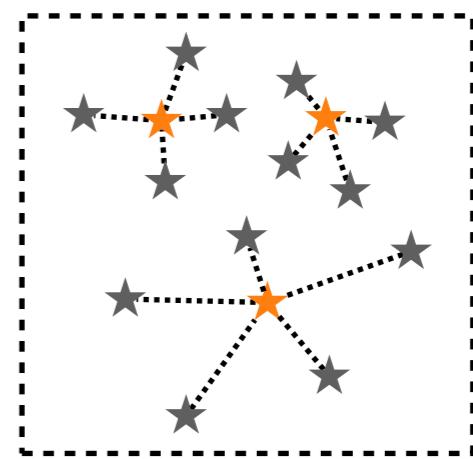
↑  
Color Factor



# Histograms meet Event Displays



**3-medoid:** Three most representative jets in each bin



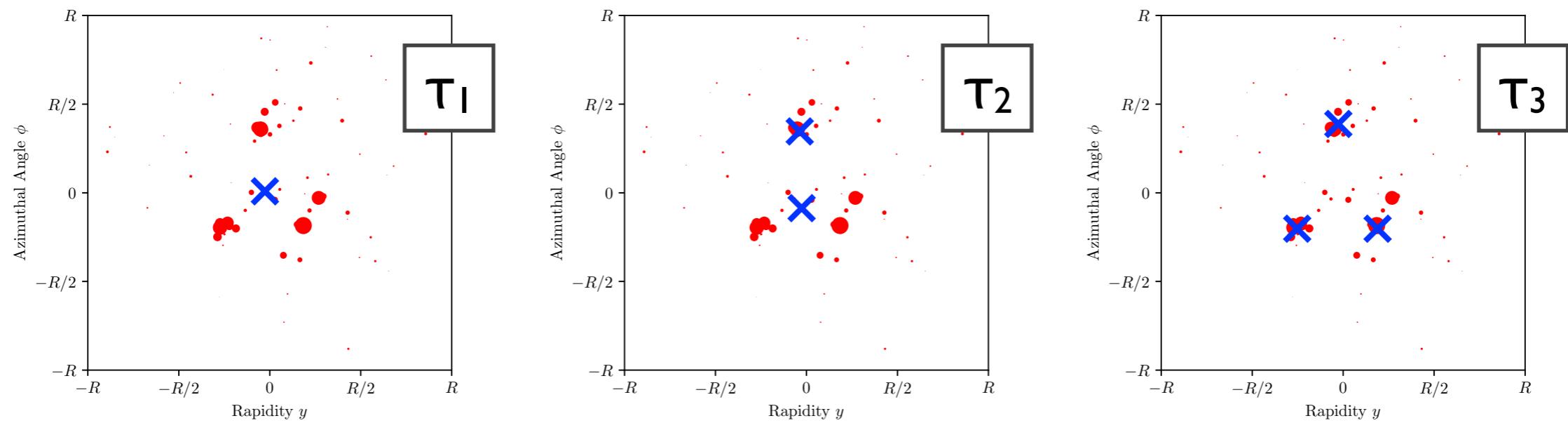
[Komiske, Metodiev, JDT, [1902.02346](#)]

# Insight into N-subjettiness

$$\tau_N^{(\beta)}(\mathcal{E}) = \min_{N \text{ axes}} \sum_i E_i \min \left\{ \theta_{1,i}^\beta, \theta_{2,i}^\beta, \dots, \theta_{N,i}^\beta \right\}$$

↑ kind of arbitrary

↑ IRC safe



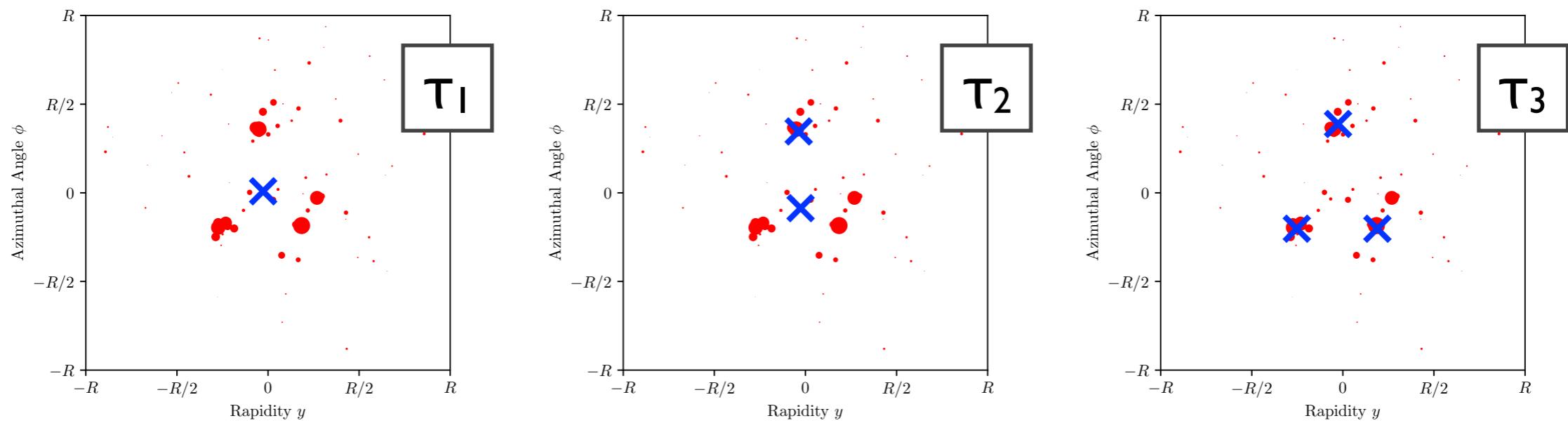
JDT, Van Tilburg, [1011.2268](#), [1108.2701](#);  
based on Brandt, Dahmen, [ZPC 1979](#); Stewart, Tackmann, Waalewijn, [1004.2489](#)

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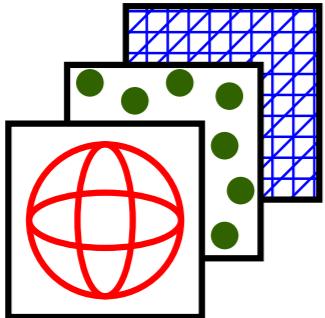
$$\tau_N(\mathcal{E}) = \min_{|\mathcal{E}'|=N} \text{EMD}(\mathcal{E}, \mathcal{E}') \quad \text{for } \beta = 1$$

↑ very satisfying

Related to p-Wasserstein metric for  $p = \beta > 1$

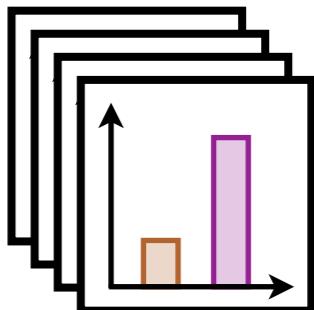
JDT, Van Tilburg, [1011.2268](#), [1108.2701](#);  
based on Brandt, Dahmen, [ZPC 1979](#); Stewart, Tackmann, Waalewijn, [1004.2489](#)

# Summary



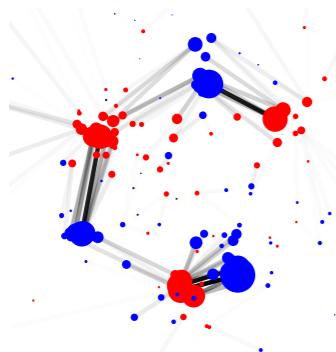
## Into the Network

*Designing architectures around symmetries and interpretability*



## Data Ex Machina

*Unsupervised learning to interpret hadronic final states*



## (The Space of Jets)

*Computational geometry as a new collider data analysis strategy*

(Theoretical)  
High Energy  
Physics



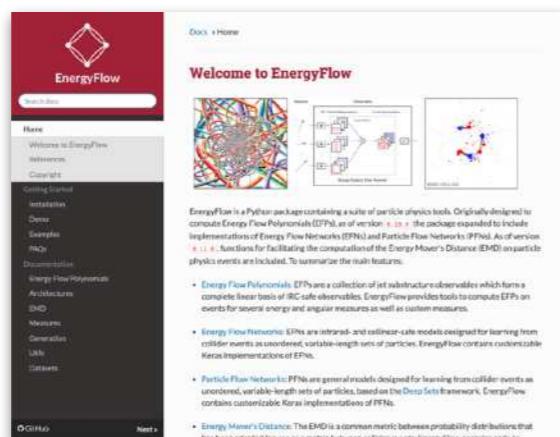
Patrick Komiske



Eric Metodiev



Mathematics,  
Statistics,  
Computer Science



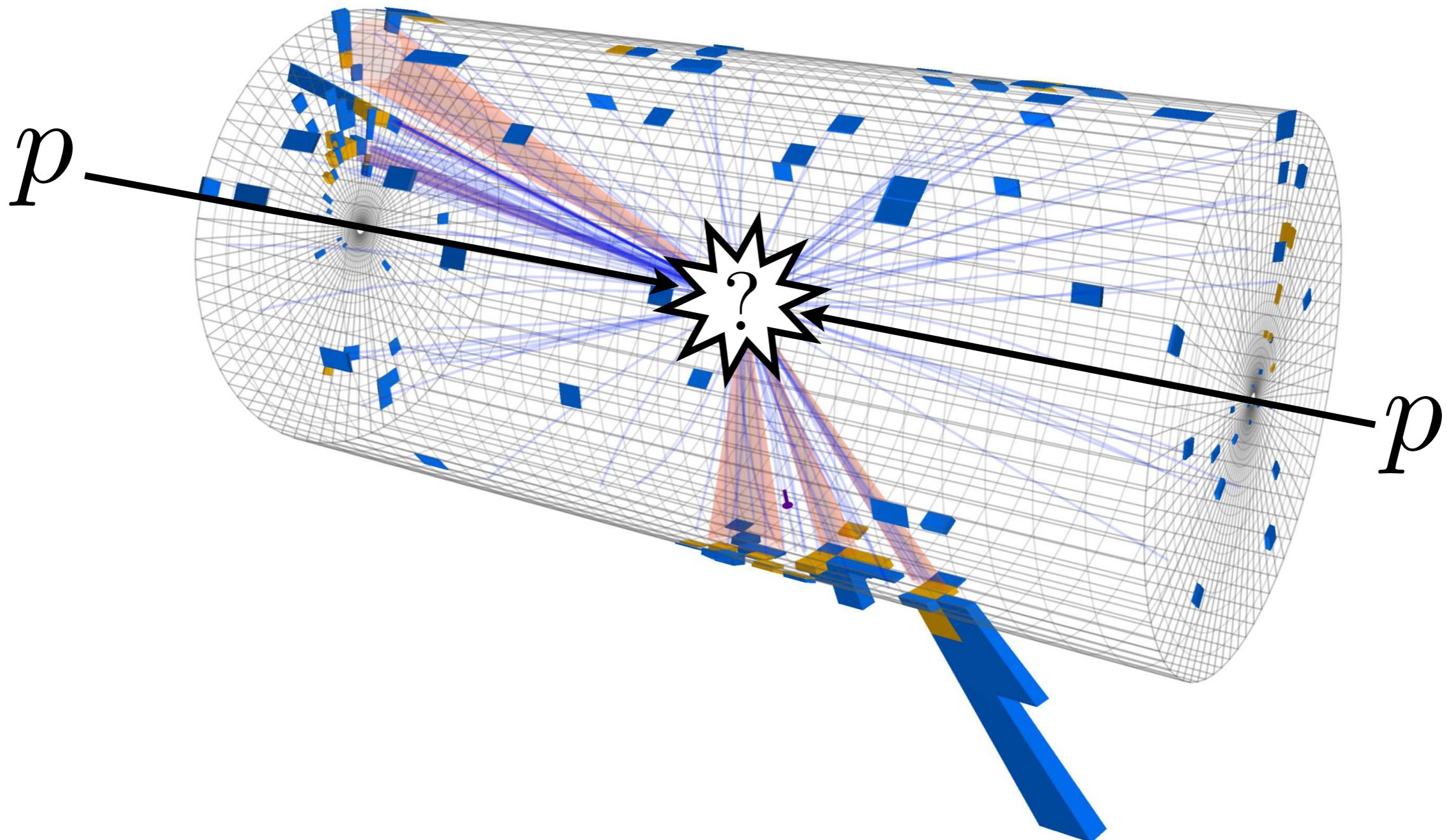
# Energy Flow Package

<https://energyflow.network/>

# *Backup Slides*

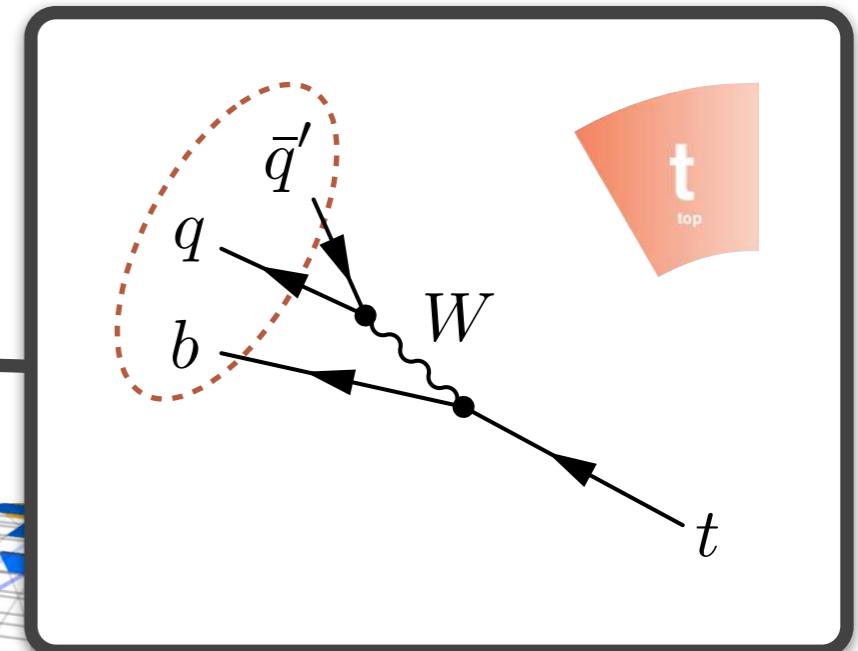
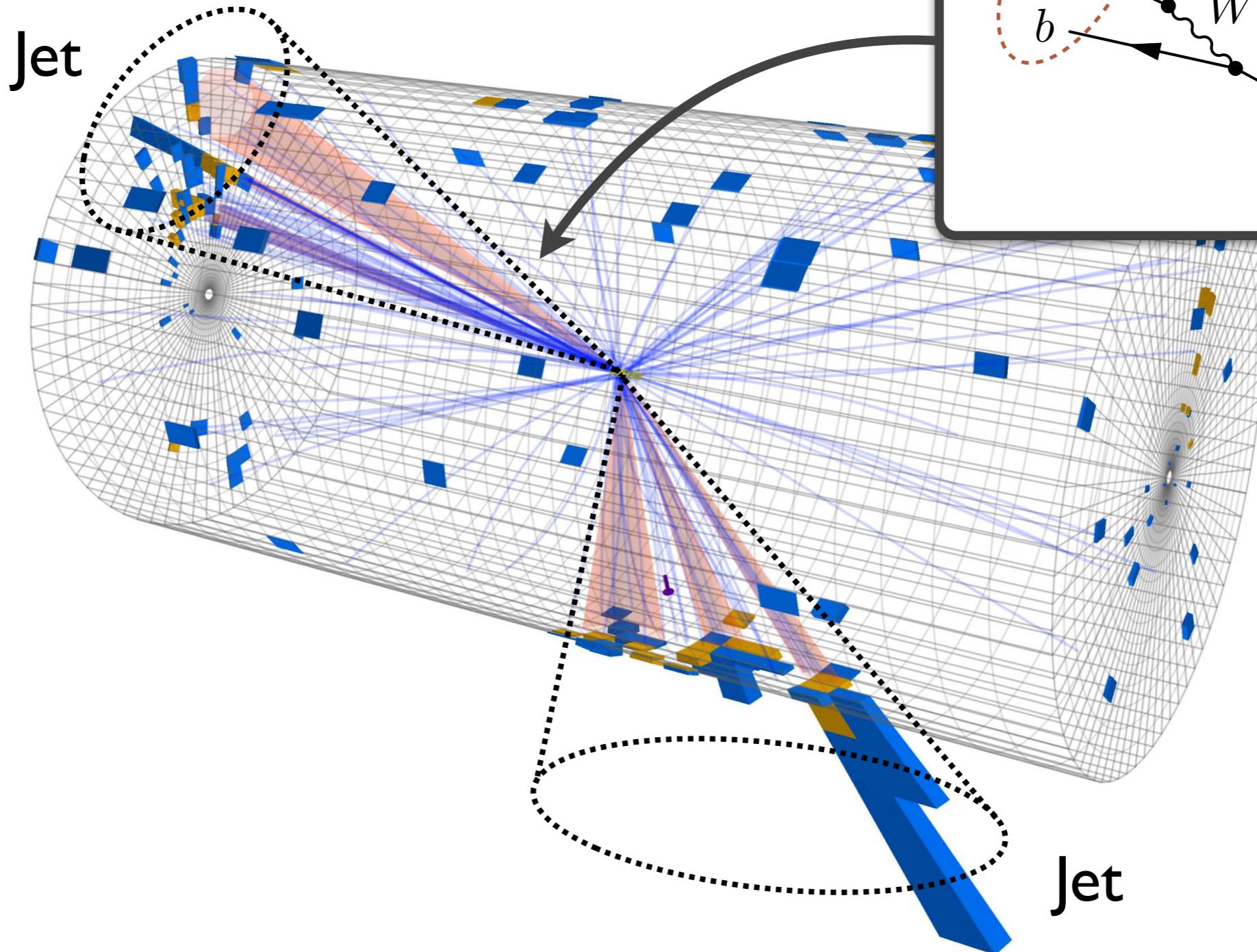


CMS Experiment at LHC, CERN  
Data recorded: Sun Jul 12 07:25:11 2015 CEST  
Run/Event: 251562 / 111132974  
Lumi section: 122  
Orbit/Crossing: 31722792 / 2253



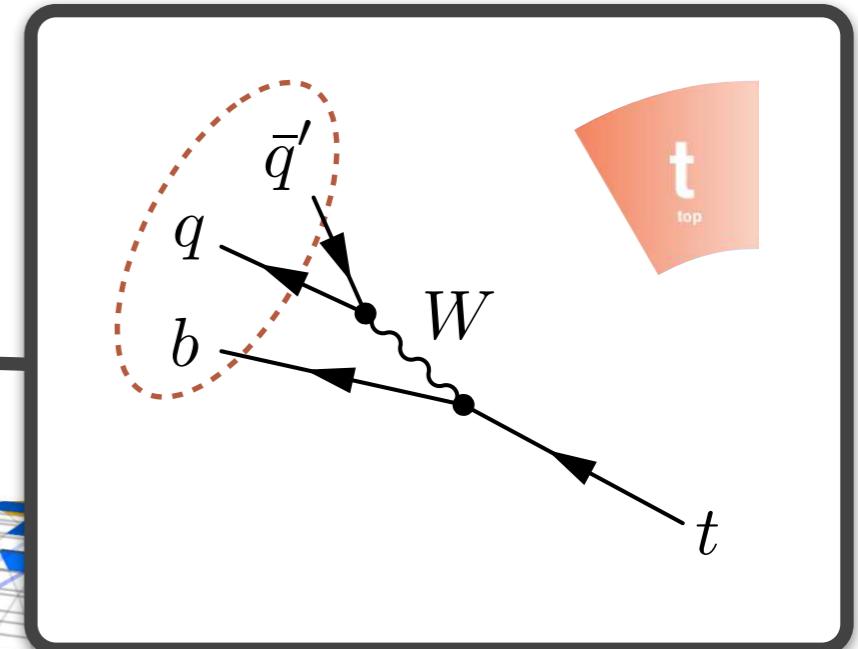
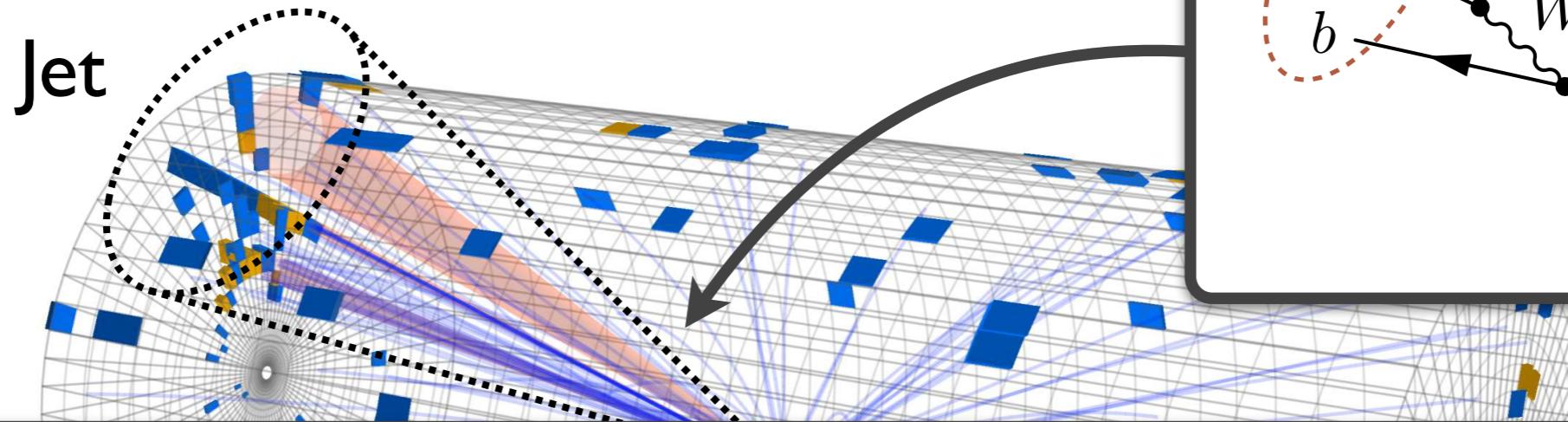


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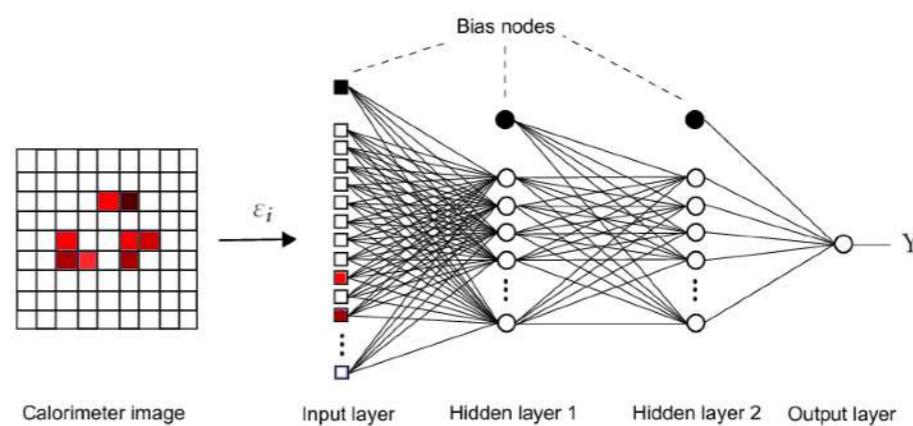
## “Deep Thinking”?

[e.g. JDT, Van Tilburg, [1011.2268](#), [1108.2701](#);  
 rephrased in language of Komiske, Metodiev, JDT, [1902.02346](#)]

$$\tau_N(\mathcal{J}) = \min_{|\mathcal{J}'|=N} \text{EMD}(\mathcal{J}, \mathcal{J}')$$

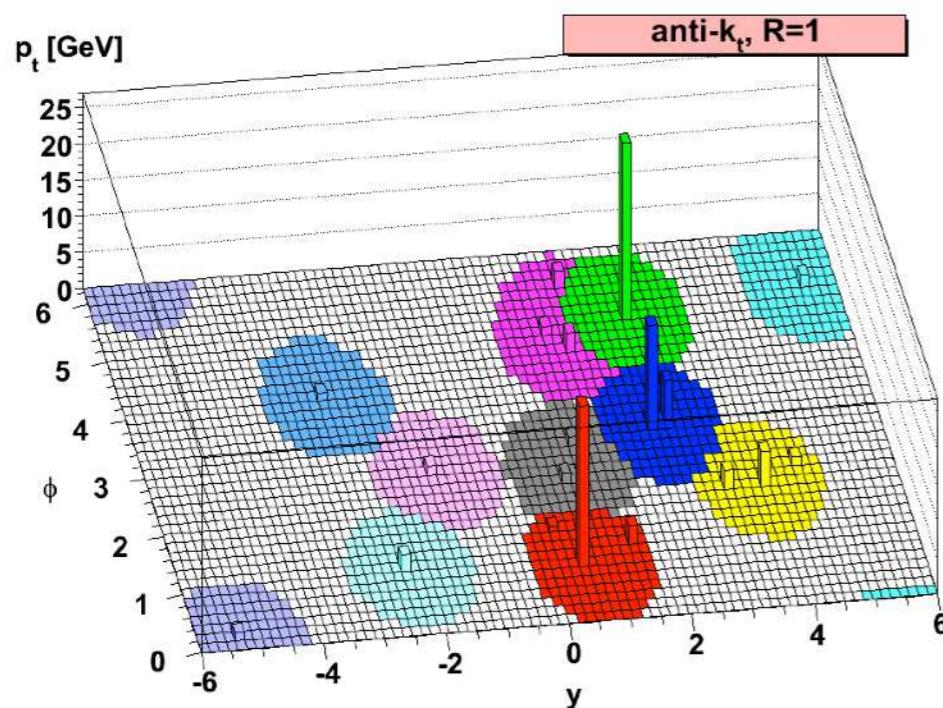
## “Deep Learning”?

[e.g. Almeida, Backović, Cliche, Lee, Perelstein, [1501.05968](#);  
 review in Kasieczka, Plehn, et al., [1902.09914](#)]

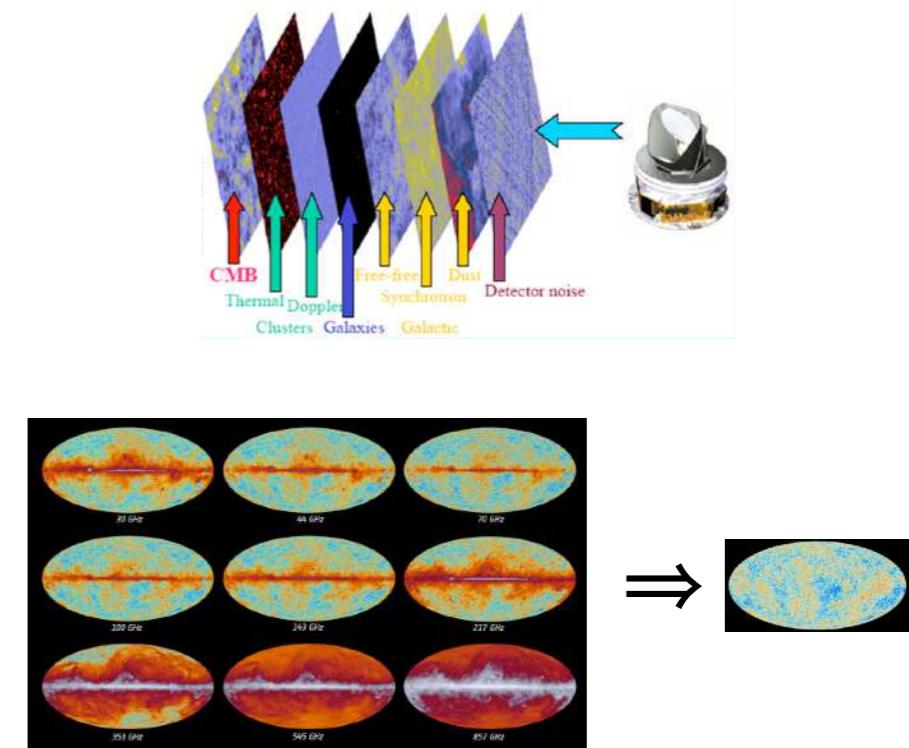


# Examples of Unsupervised Learning

## Clustering



## Topic Modeling

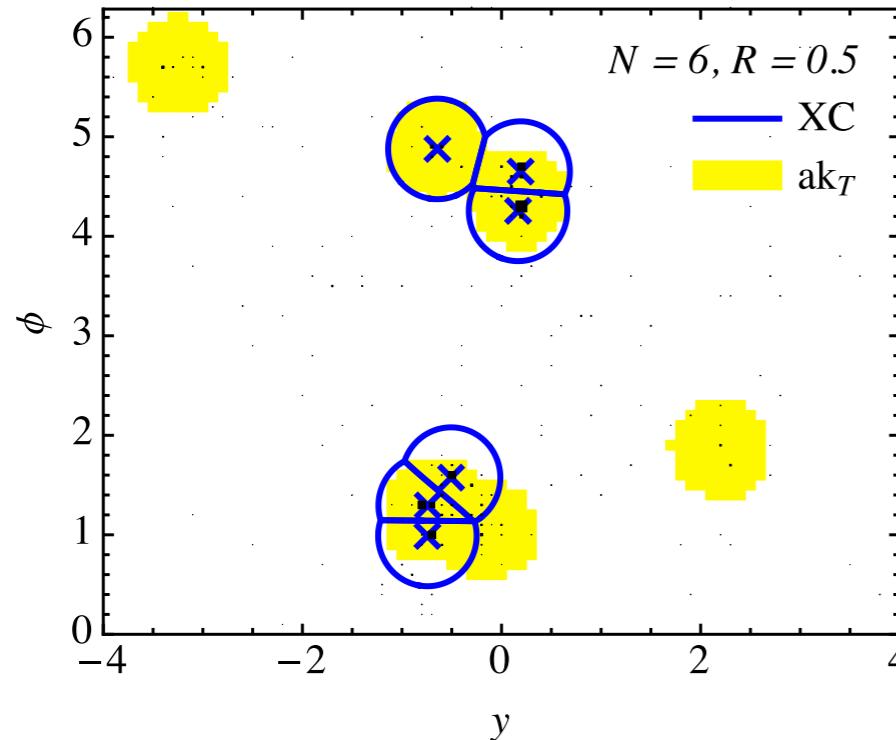


(Approximate) *solutions* to properly specified problems

[figures from Cacciari, Salam, Soyez, [0802.1189](#); [Planck Outreach](#)]

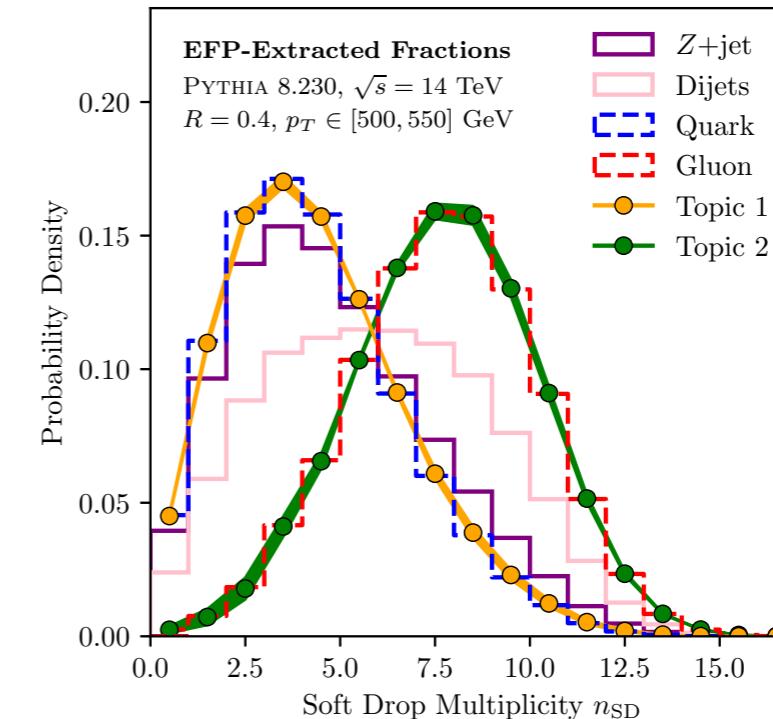
# Examples of Unsupervised Learning

## XCone Jet Finding



“Find  $N$  axes that minimize  $N$ -jettiness”

## Jet Topics



“Find two mutually irreducible distributions”

[Stewart, Tackmann, JDT, Vermilion, Wilkason, [1508.01516](#); based on Stewart, Tackmann, Waalewijn, [1004.2489](#)]  
[Metodiev, JDT, [1802.00008](#); Komiske, Metodiev, JDT, [1809.01140](#); see also Dillon, Faroughy, Kamenik, [1904.04200](#)]

(Approximate) solutions to properly specified problems

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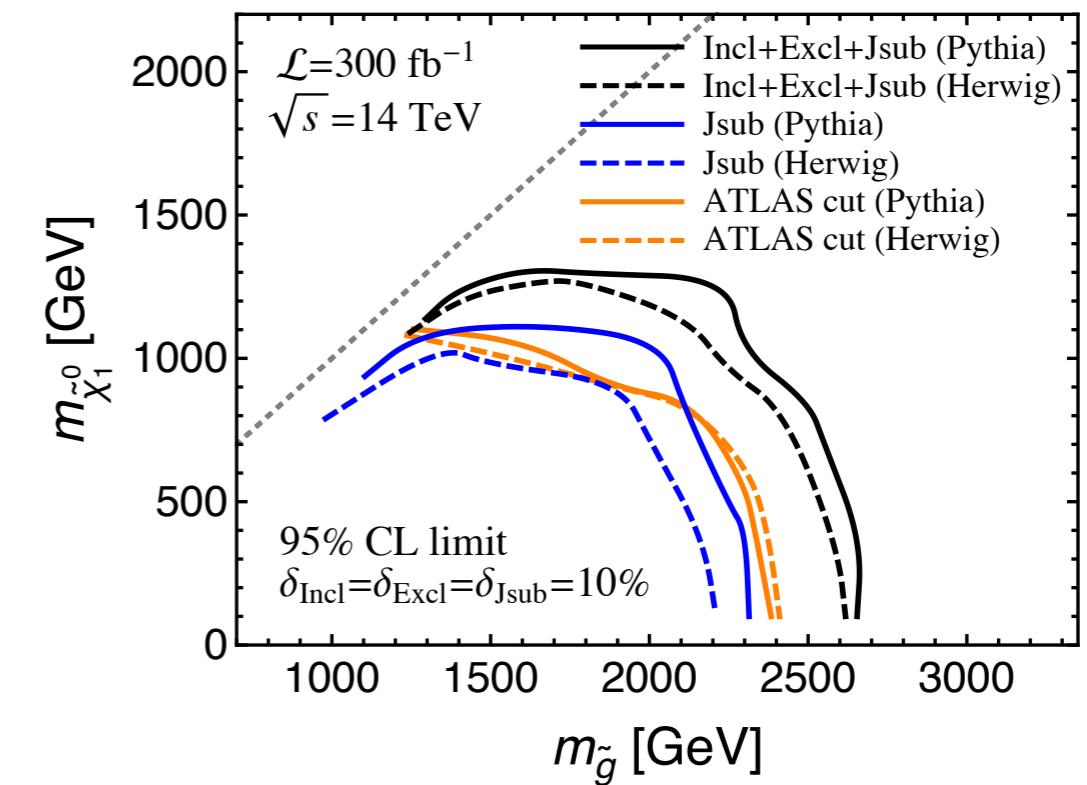
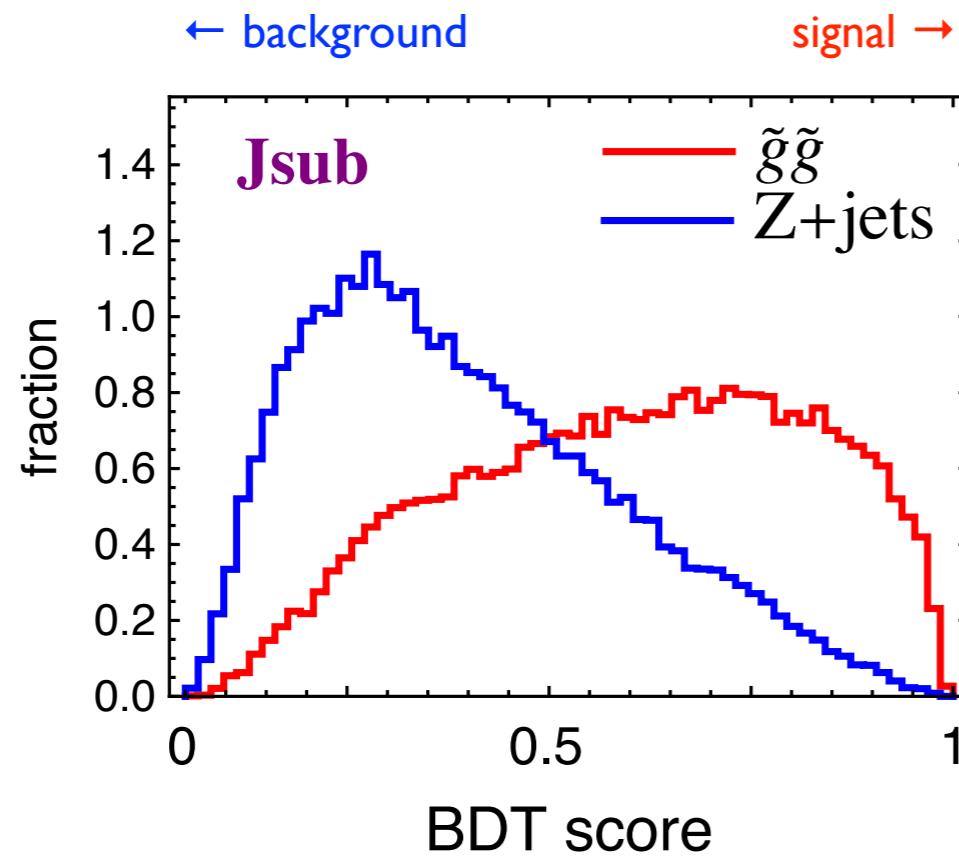
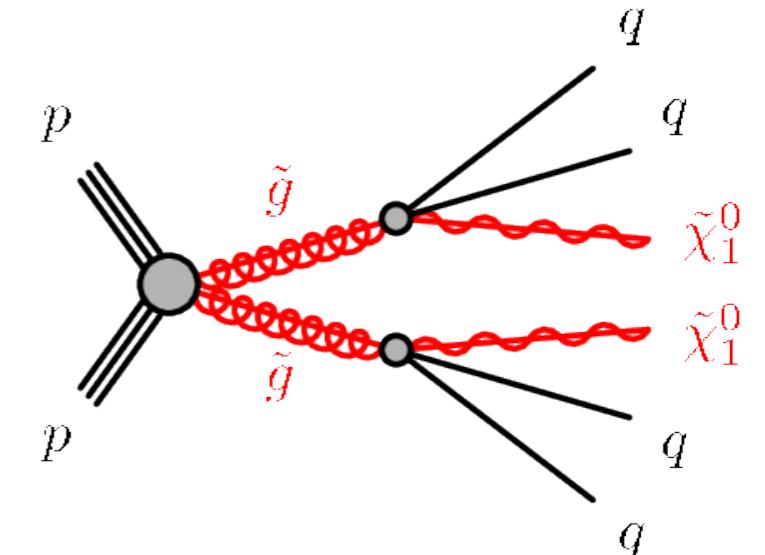
# E.g. SUSY Search for Gluino Pairs

Classifier: Boosted decision tree (for each of 4 jets)

Inputs: Jet mass, width, track multiplicity

Signal: Quark enriched ( $C_F = 4/3$ )

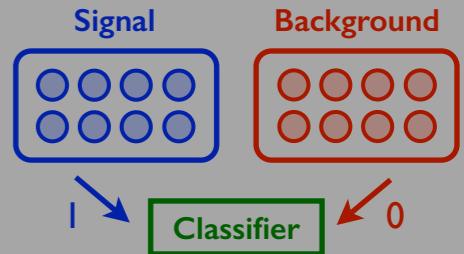
Background: Gluon enriched ( $C_A = 3$ )



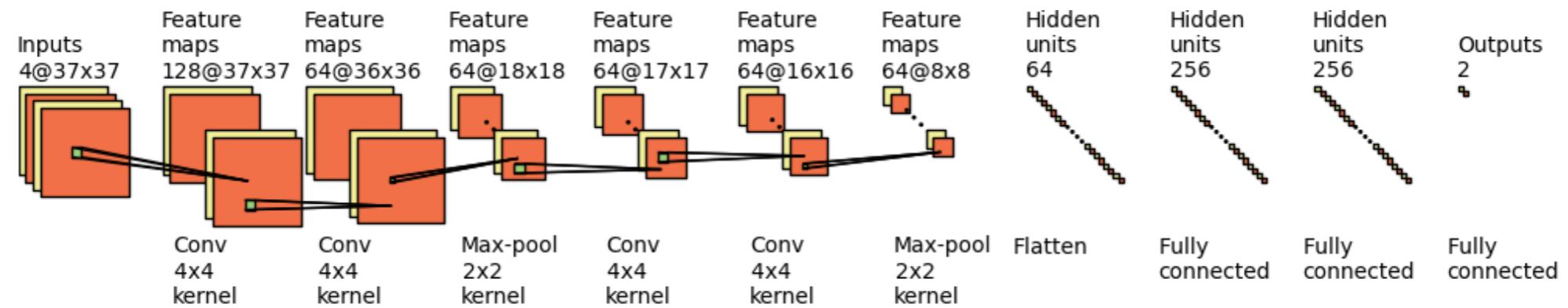
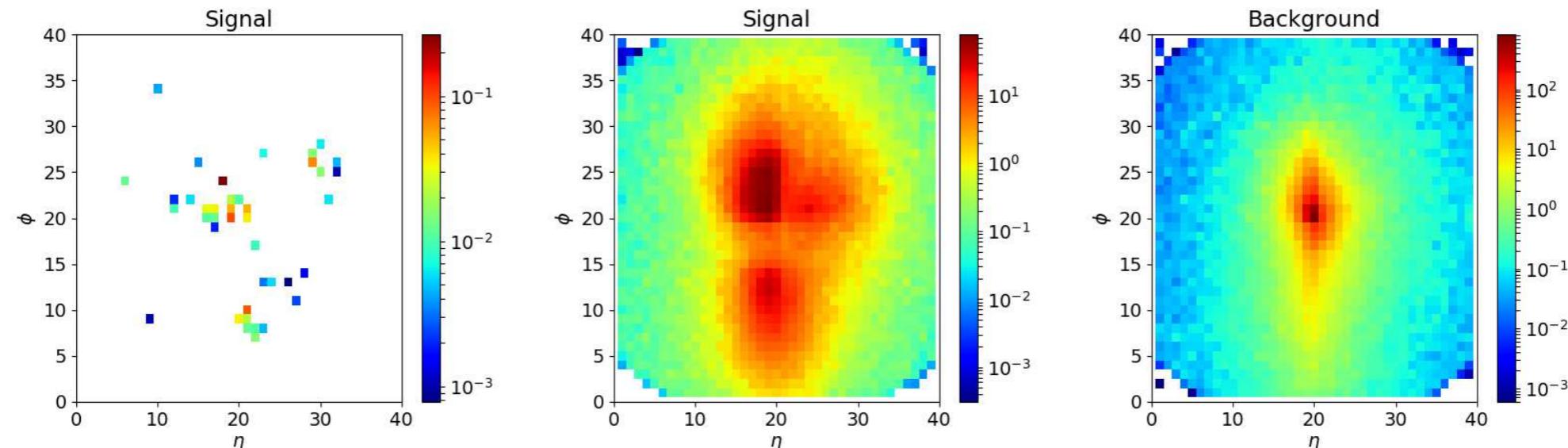
[Bhattacherjee, Mukhopadhyay, Nojiri, Sakakie, Webber, [1609.08781](#)]

# Jet Classification Studies

*Mix and match*

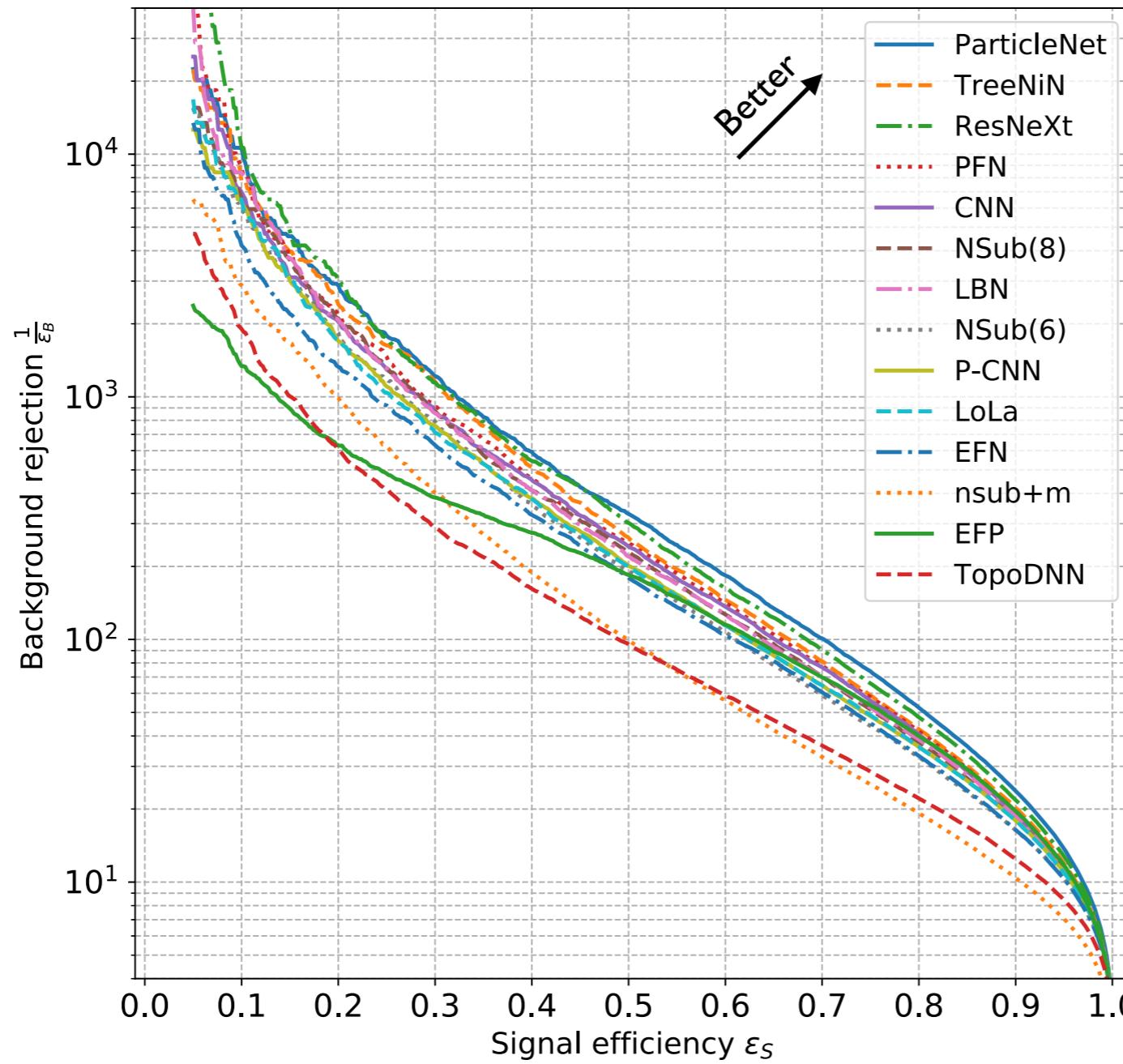
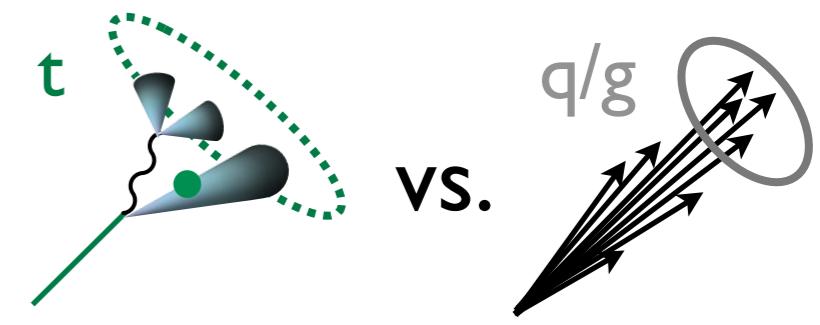


## Deep Learning: Jet Image Strategy with CNNs



[Macaluso, Shih [1803.00107](#); building off Kasieczka, Plehn, Russell, Schell, [1701.08784](#); based on Cogan, Kagan, Strauss, Schwartzman, [1407.5675](#); de Oliveira, Kagan, Mackey, Nachman, Schwartzman, [1511.05190](#)]

# Throwing Down the Gauntlet

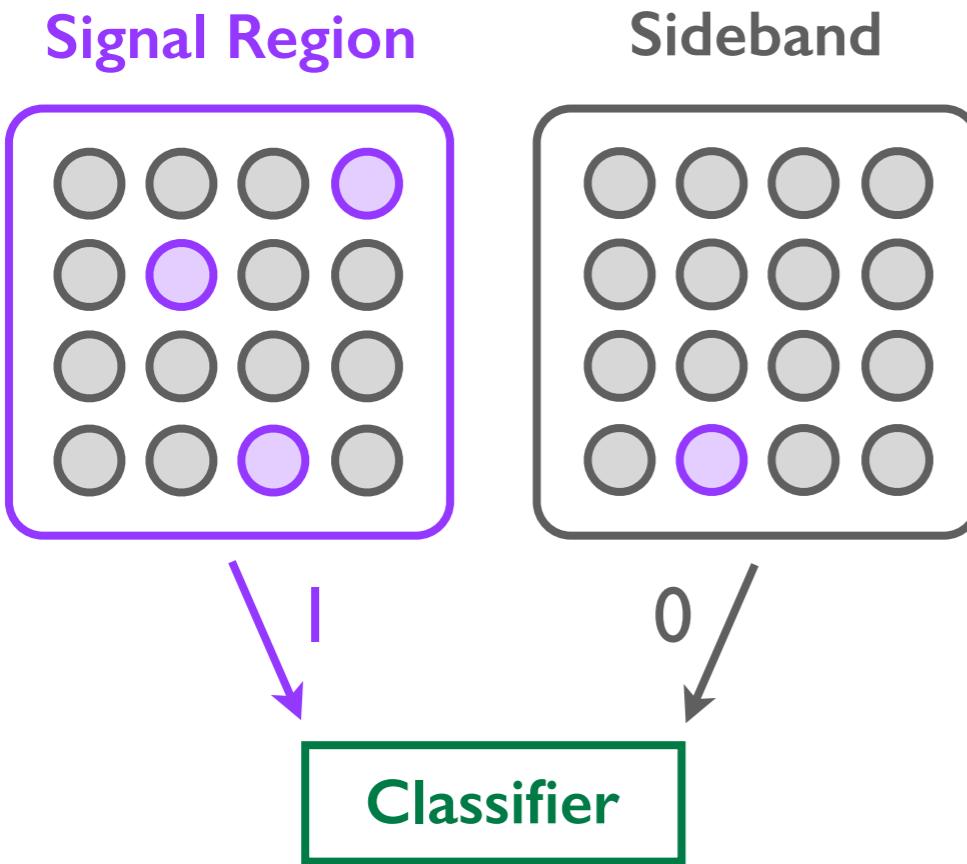


← “Deep Pockets”  
 ← Previous slide  
 Deep Sets  
 ← “Deep Thinking”

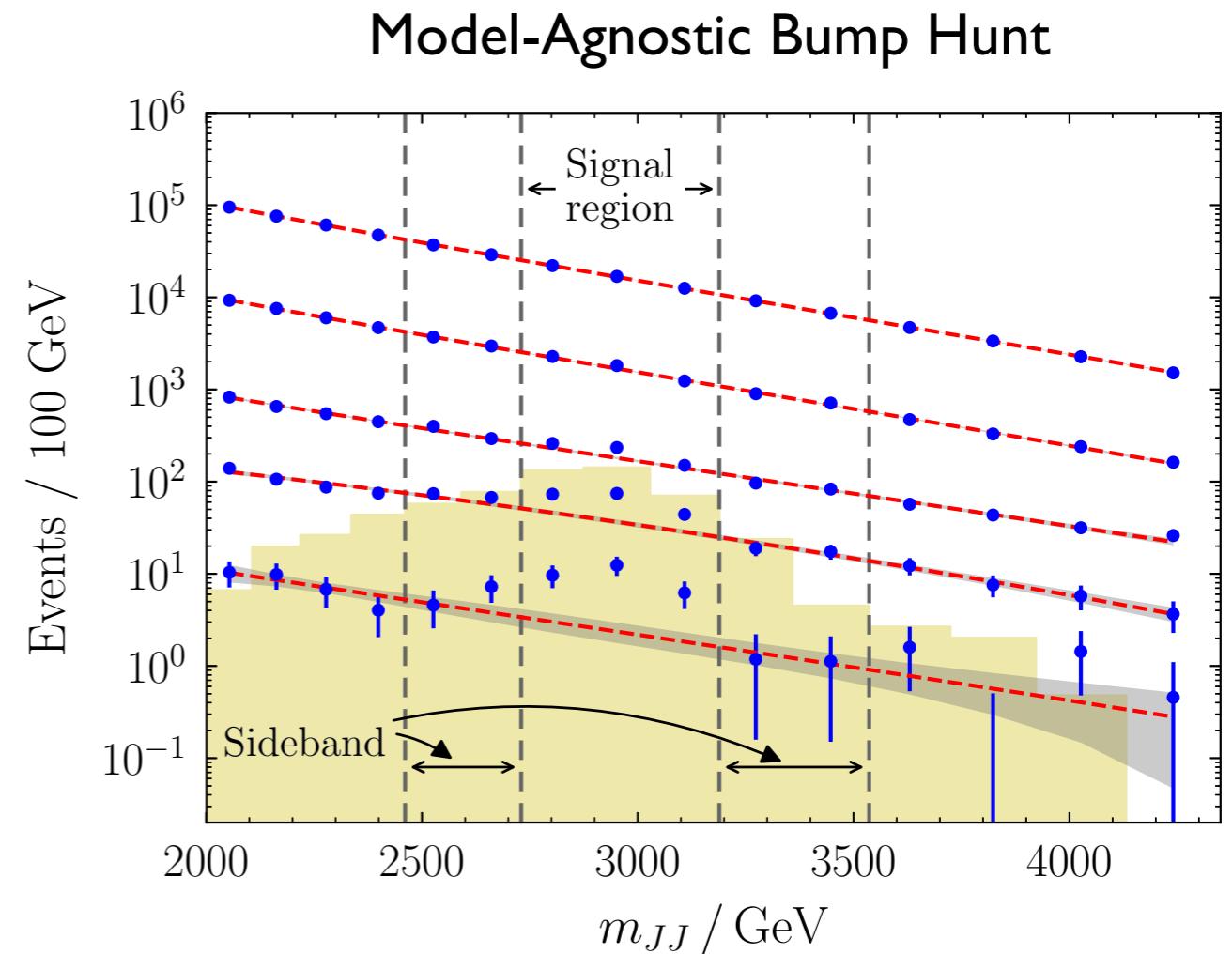
[Kasieczka, Plehn, et al., [1902.09914](#);  
 comparison of JDT, Van Tilburg, [1011.2268](#), [1108.2701](#); Xie, Girshick, Dollár, Tu, He, [1611.05431](#); CMS-DP-2017-049; Pearkes, Fedorko, Lister, Gay, [1704.02124](#);  
 Butter, Kasieczka, Plehn, Russell, [1707.08966](#); Komiske, Metodiev, JDT, [1712.07124](#); Macaluso, Shih [1803.00107](#); Moore, Nordström, Varma, Fairbairn [1807.04769](#);  
 Komiske, Metodiev, JDT, [1810.05165](#); Erdmann, Geiser, Rath, Rieger, [1812.09722](#); Qu, Gouskos, [1902.08570](#); Macaluso, Cranmer, to appear]

# CWoLa Hunting

## Using “Classification Without Labels”

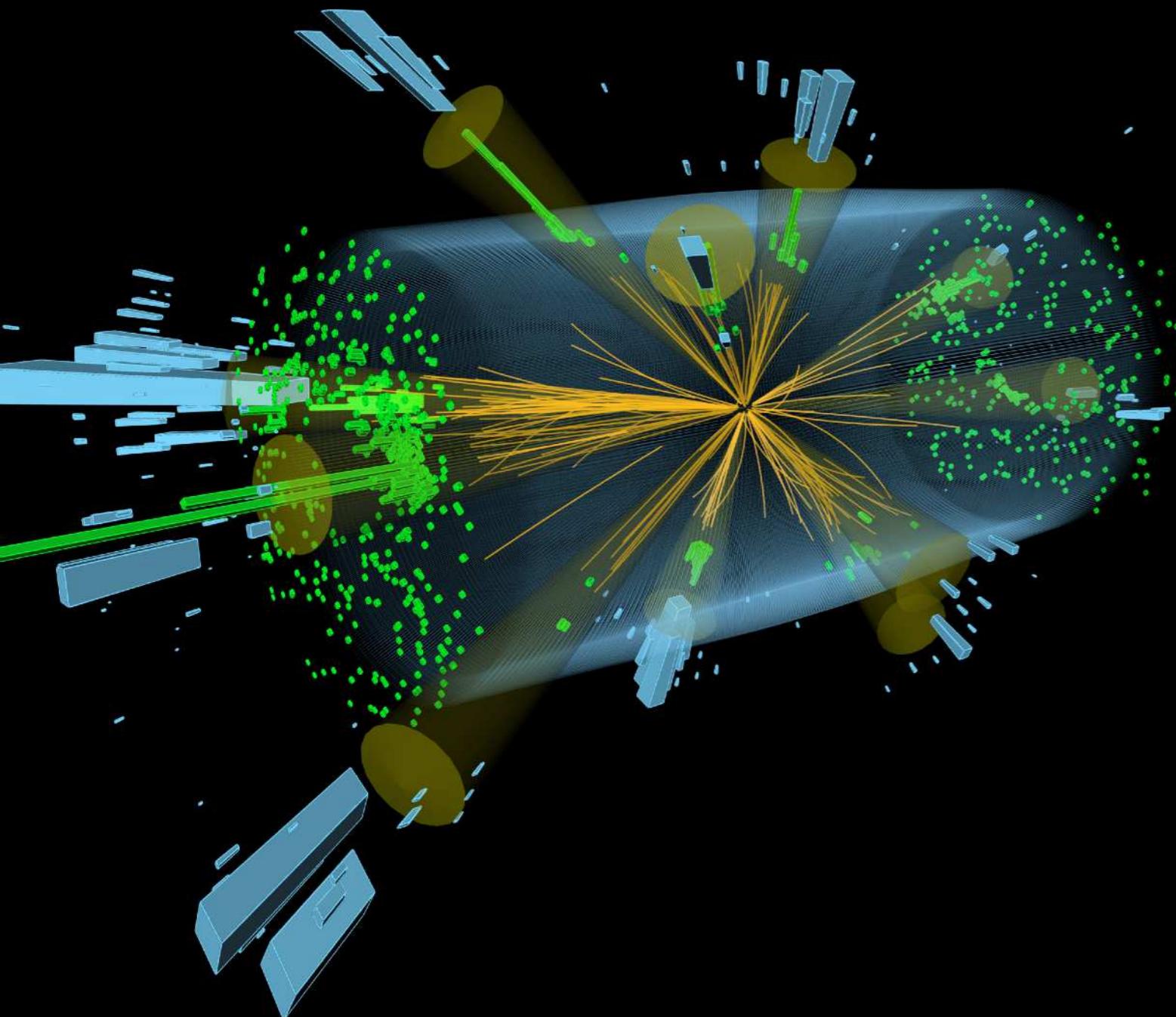


With enough data, monotonic  
w.r.t. optimal classifier (!)



[Collins, Howe, Nachman, [1805.02664](#), [1902.02634](#); using Metodiev, Nachman, JDT, [1708.02949](#);  
see also Blanchard, Flaska, Handy, Pozzi, Scott, [1303.1208](#); Cranmer, Pavez, Louppe, [1506.02169](#)]

# What is a Collision Event?



T E H M

 $\gamma$ 

photon

 $e^+$ 

electron

 $\mu^+$ 

muon

 $\pi^+$ 

pion

 $K^+$ 

kaon

 $K_L^0$ 

K-long

 $p/\bar{p}$ 

proton

 $n/\bar{n}$ 

neutron

elementary

composite

# Point Cloud

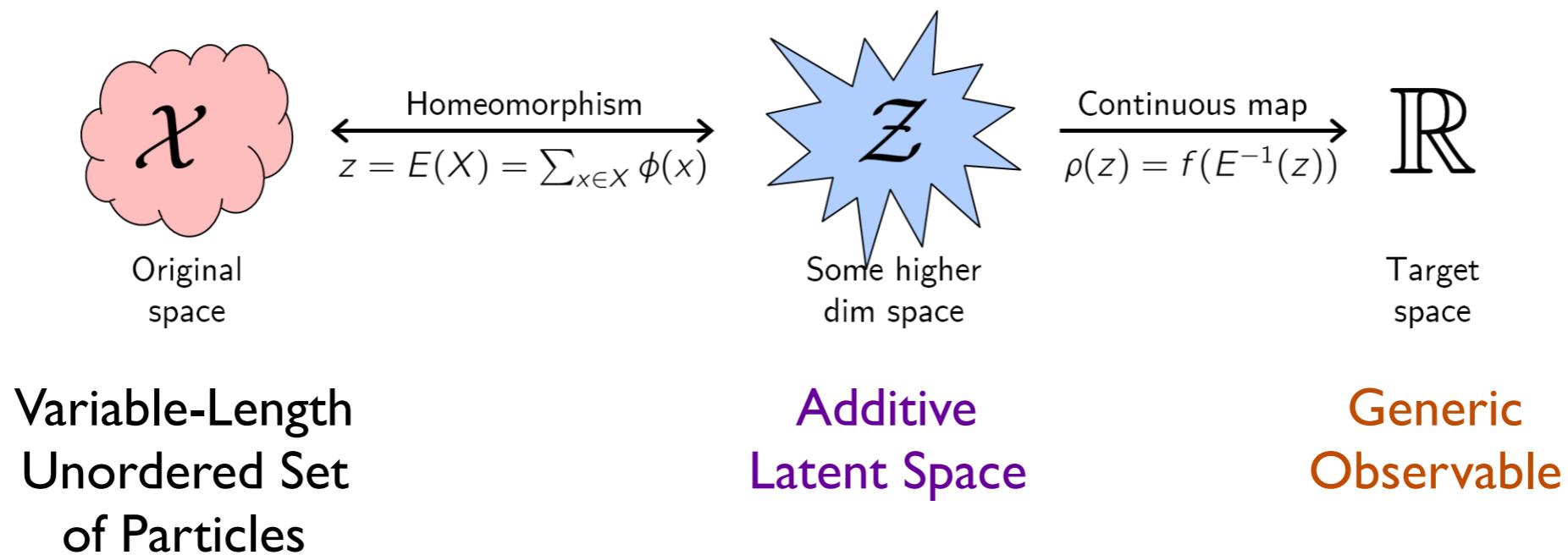


[Popular Science, 2013]

# Meanwhile in ML-Land: Deep Sets

**Theorem 2** A function  $f(X)$  operating on a set  $X$  having elements from a countable universe, is a valid set function, i.e., **invariant** to the permutation of instances in  $X$ , iff it can be decomposed in the form  $\rho \left( \sum_{x \in X} \phi(x) \right)$ , for suitable transformations  $\phi$  and  $\rho$ .

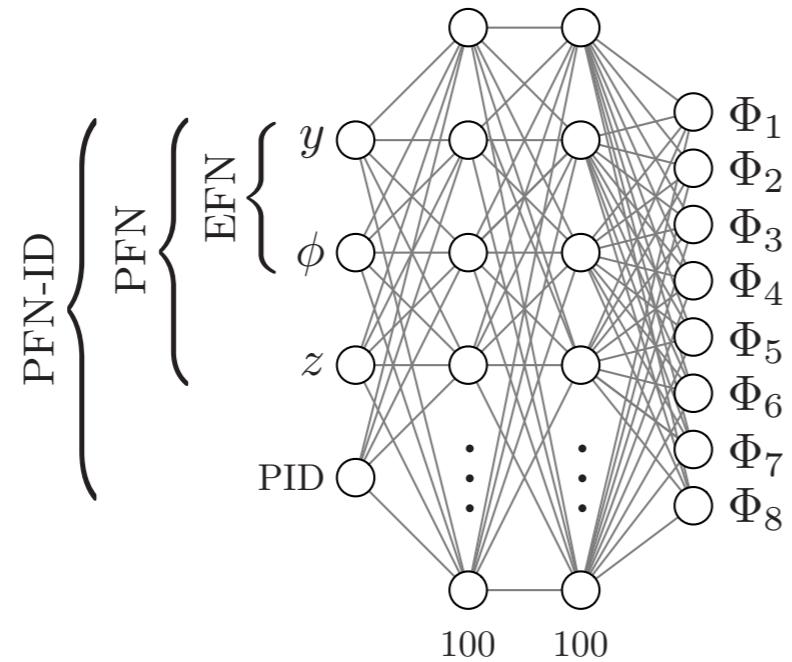
↑  
(!)



[Zaheer, Kottur, Ravanbakhsh, Poczos, Salakhutdinov, Smola, [1703.06114](#); see also Vinyals, Bengio, Kudlur, [1511.06391](#); Qi, Su, Mo, Guibas, [1612.00593](#)]

# Technical Implementation

## Per-Particle Network: $\Phi$

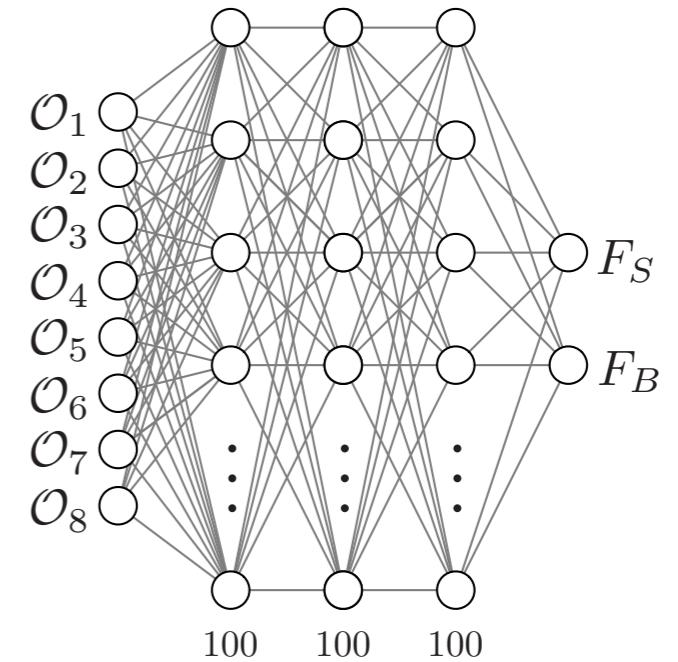


## Per-Jet (Latent Space):

$$\text{EFN: } \mathcal{O}_a = \sum_{i \in \text{jet}} z_i \Phi_a(y_i, \phi_i) \quad z_i = \frac{p_{Ti}}{\sum_j p_{Tj}}$$

$$\text{PFN: } \mathcal{O}_a = \sum_{i \in \text{jet}} \Phi_a(y_i, \phi_i, z_i, \text{PID}_i)$$

## Latent Combiner: $F$



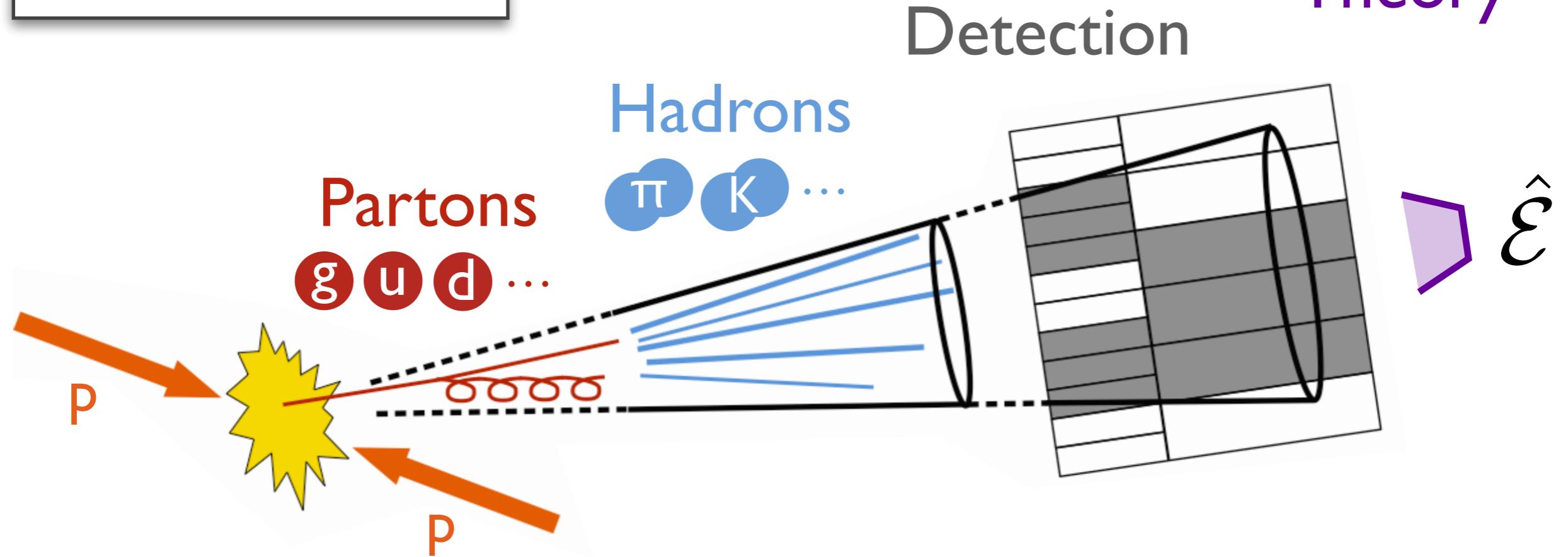
## Final Discriminant:

$$\text{softmax}(F_S, F_B)$$

[Komiske, Metodiev, JDT, 1810.05165]

# Focus on Energy Flow

$$\hat{\mathcal{E}} \simeq \lim_{t \rightarrow \infty} \hat{n}_i T^{0i}(t, vt\hat{n})$$



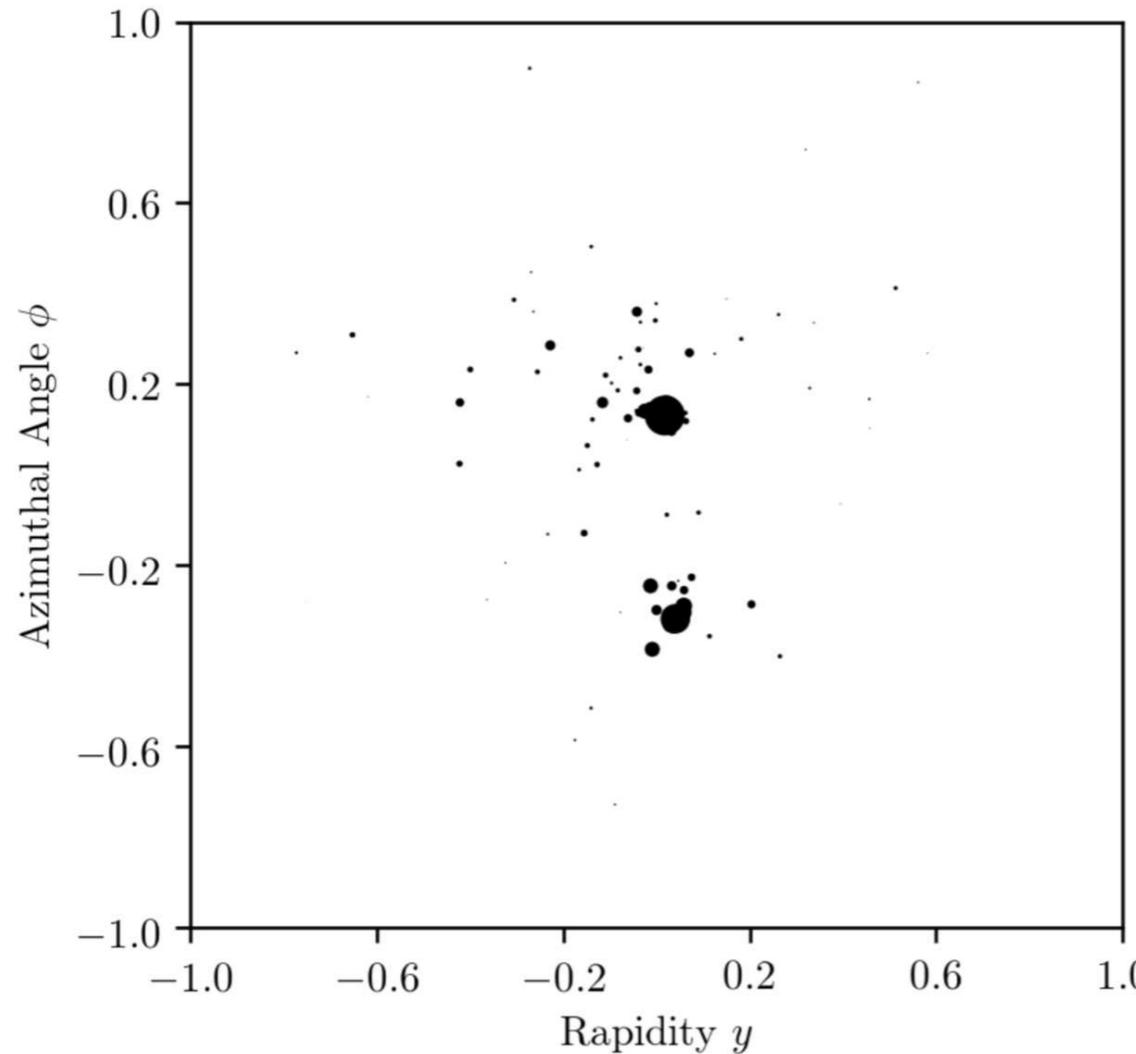
Detection

Theory

*Stress-energy flow: Measure of event/jet structure  
robust to non-perturbative and detector effects (i.e. **IRC safe**)*

[Sveshnikov, Tkachov, [hep-ph/9512370](#); Hofman, Maldacena, [0803.1467](#); Mateu, Stewart, JDT, [I209.3781](#); Komiske, Metodiev, JDT, [I712.07124](#), [I810.05165](#)]

# Focus on Energy Flow



Represent jet as:

$$\rho(\hat{p}) = \sum_{i \in \text{jet}} E_i \delta(\hat{p} - \hat{p}_i)$$

↑  
Energy ( $p_T$ )      ↑  
Direction ( $y, \varphi$ )

Safe to infrared & collinear splittings  
No flavor/charge information  
No pixelation needed

*Stress-energy flow: Measure of event/jet structure  
robust to non-perturbative and detector effects (i.e. **IRC safe**)*

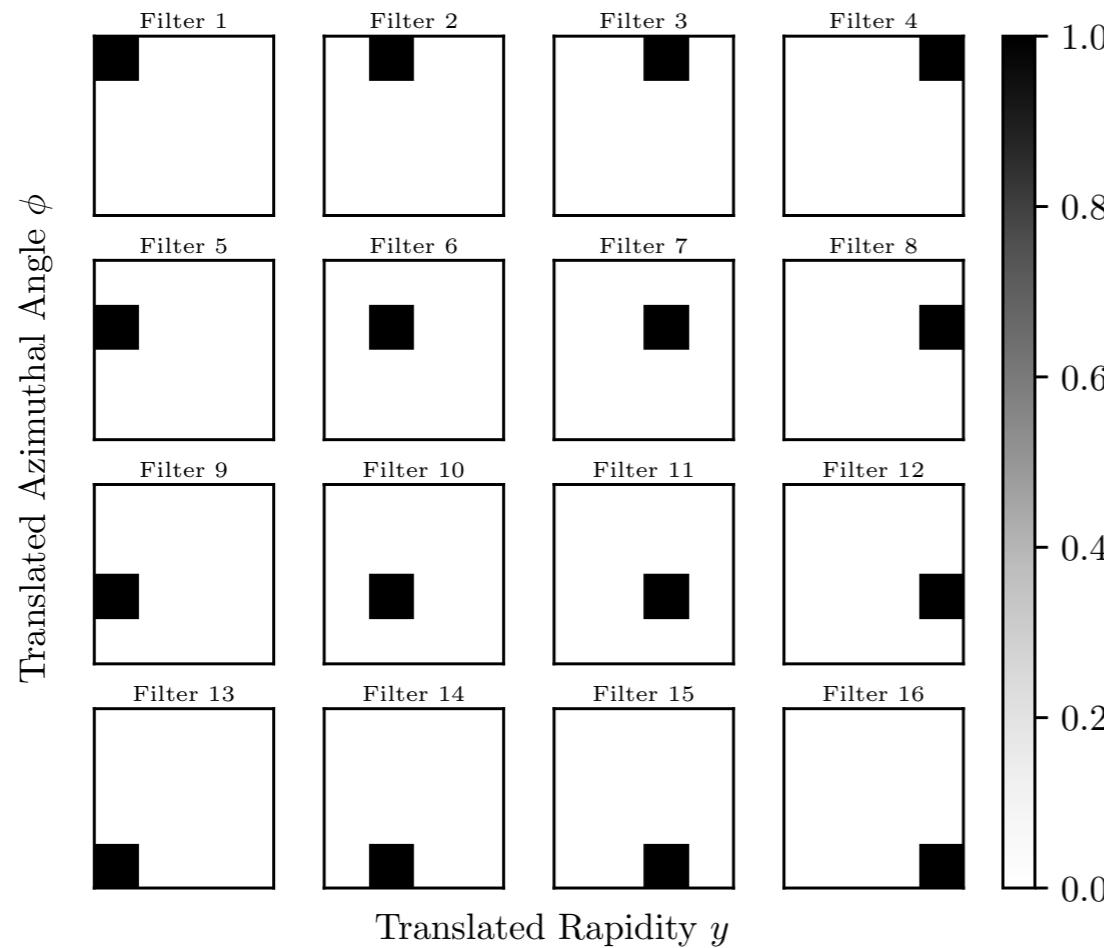
[Sveshnikov, Tkachov, [hep-ph/9512370](#); Hofman, Maldacena, [0803.1467](#); Mateu, Stewart, JDT, [I209.3781](#); Komiske, Metodiev, JDT, [I712.07124](#), [I810.05165](#)]

# Latent Space Visualization

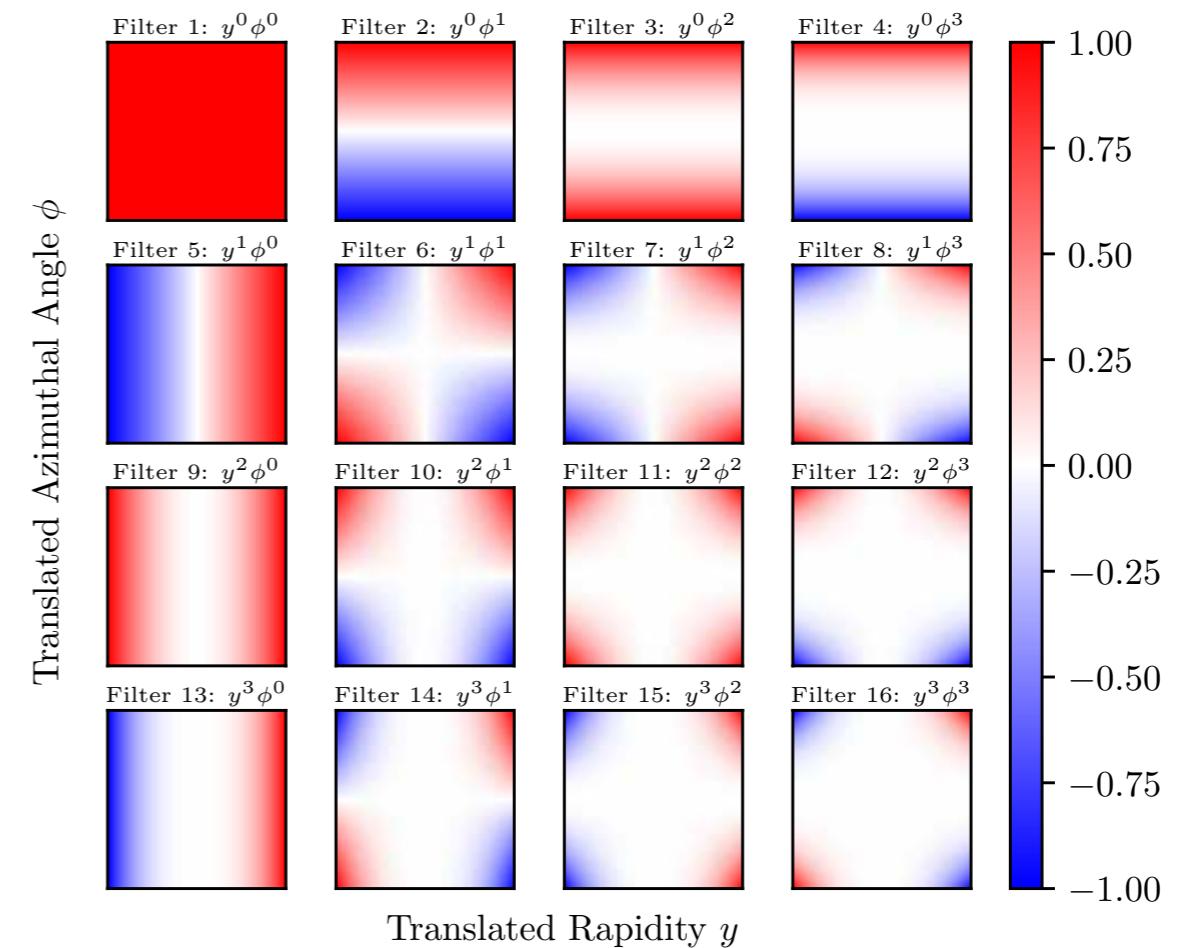
$$\mathcal{O}(\{p_i^\mu\}) = F(\mathcal{O}_1, \mathcal{O}_2, \dots, \mathcal{O}_\ell)$$

**IRC-safe:**  $\mathcal{O}_a = \sum_{i \in \text{jet}} E_i \Phi_a(\hat{p}_i)$

## Calorimeter Pixels



## Radiation Moments

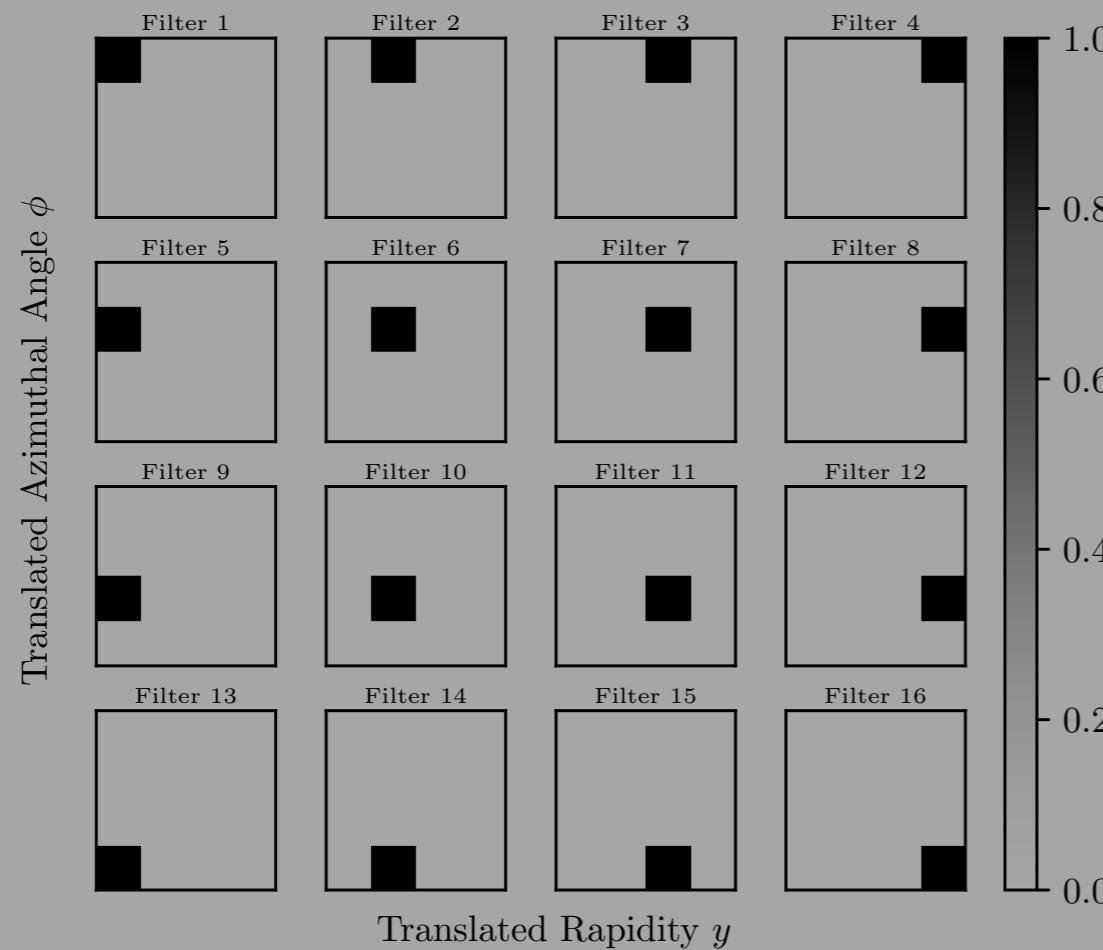


# Latent Space Visualization

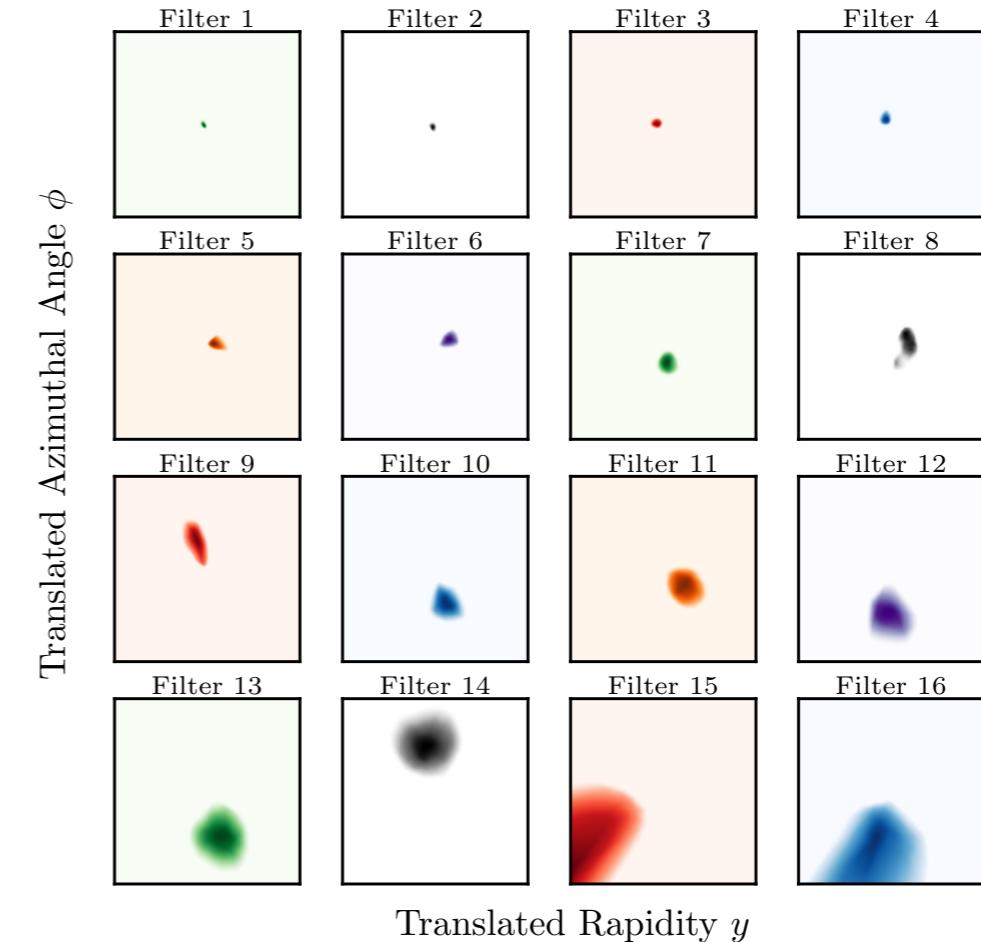
$$\mathcal{O}(\{p_i^\mu\}) = F(\mathcal{O}_1, \mathcal{O}_2, \dots, \mathcal{O}_\ell)$$

**IRC-safe:**  $\mathcal{O}_a = \sum_{i \in \text{jet}} E_i \Phi_a(\hat{p}_i)$

## Calorimeter Pixels

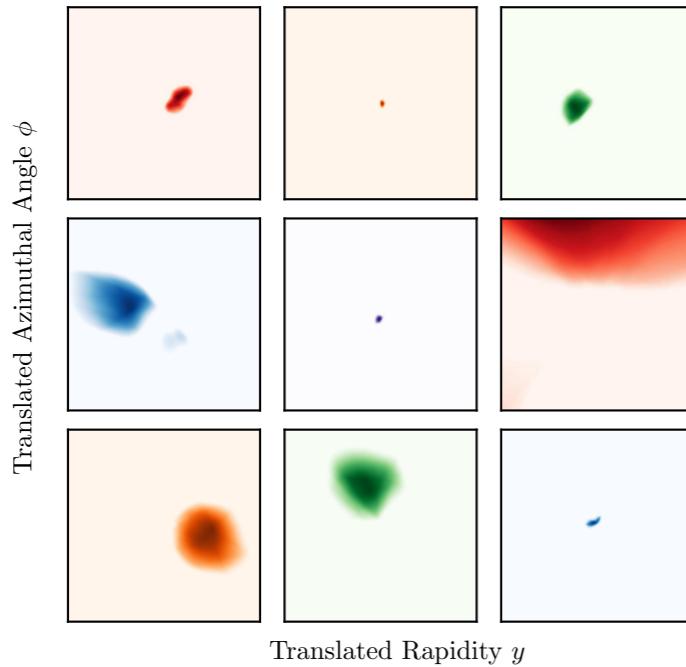


## EFNs: Dynamic Pixelation

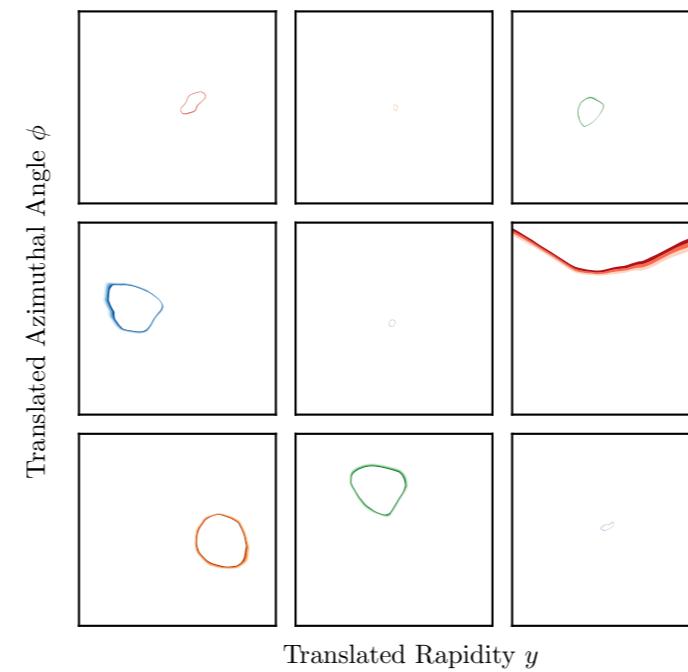


# Psychedelic Network Visualization

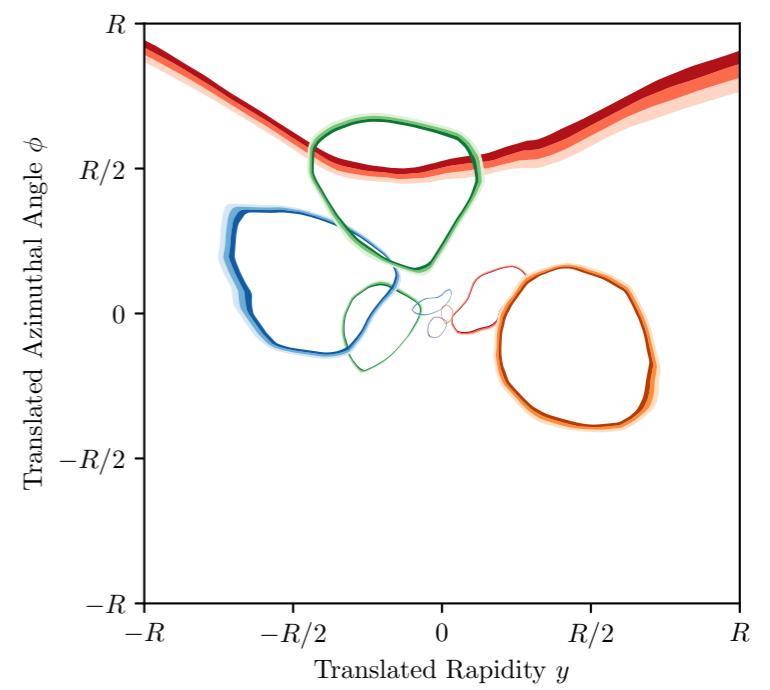
## Latent Filters



## 50% Contours

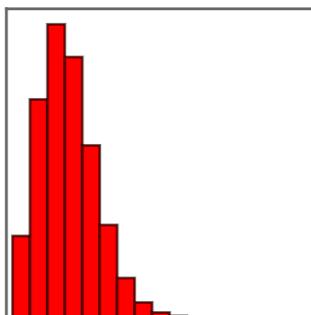


## Overlay

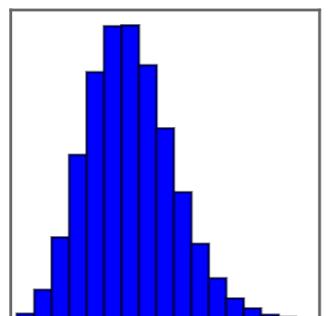


# Generation (Easy)

Jet Topics



Quark Jet

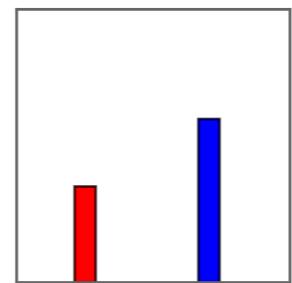


Gluon Jet

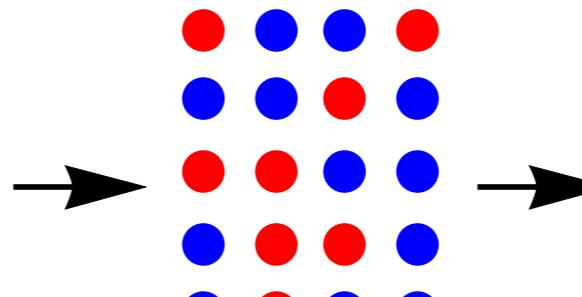
Mixed Jet Sample N

...

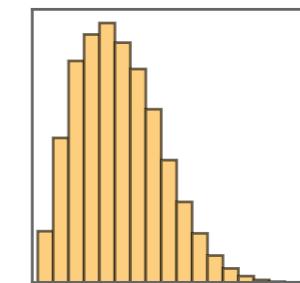
Mixed Jet Sample I



Jet Fractions



Mixed Data

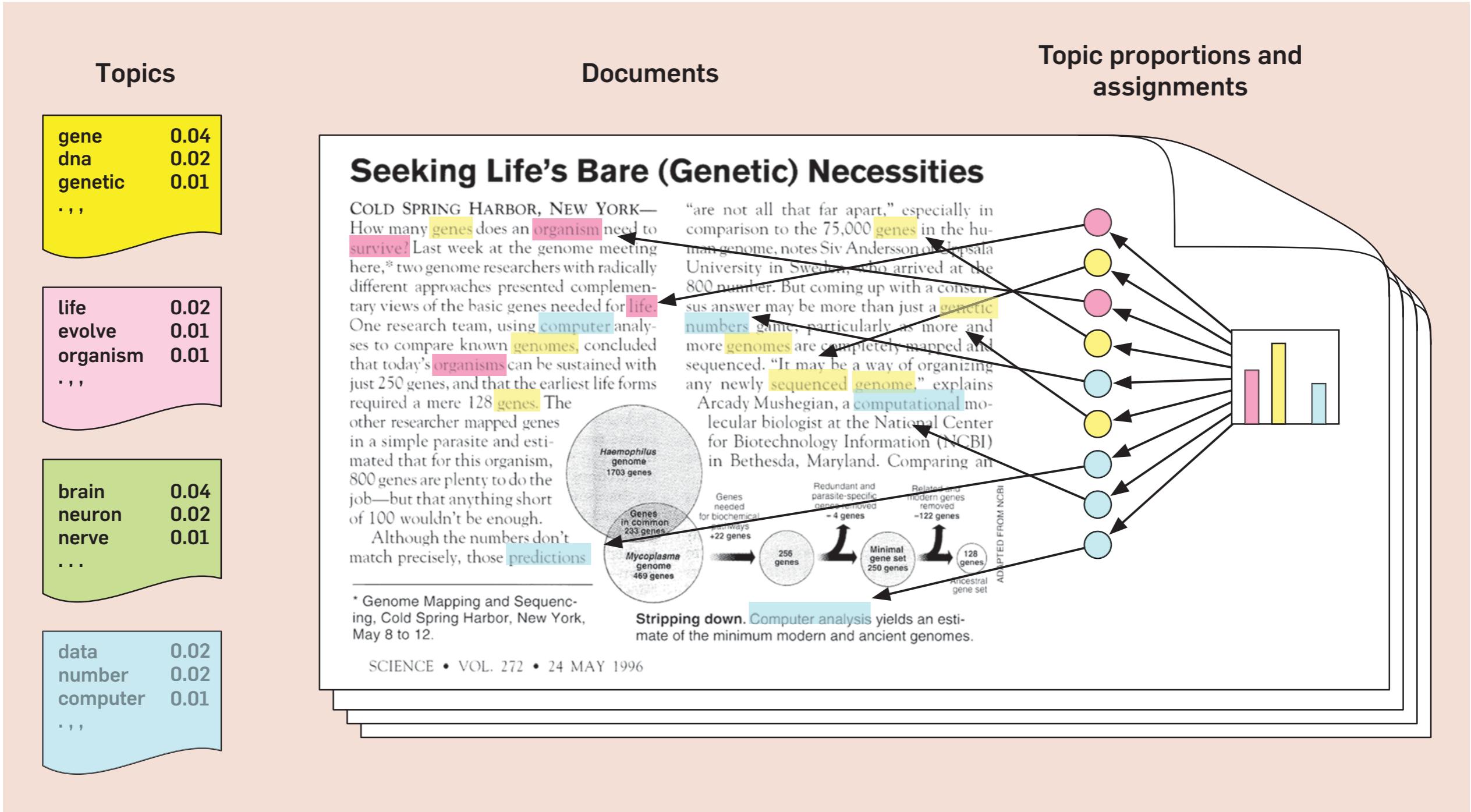


Histogram

←

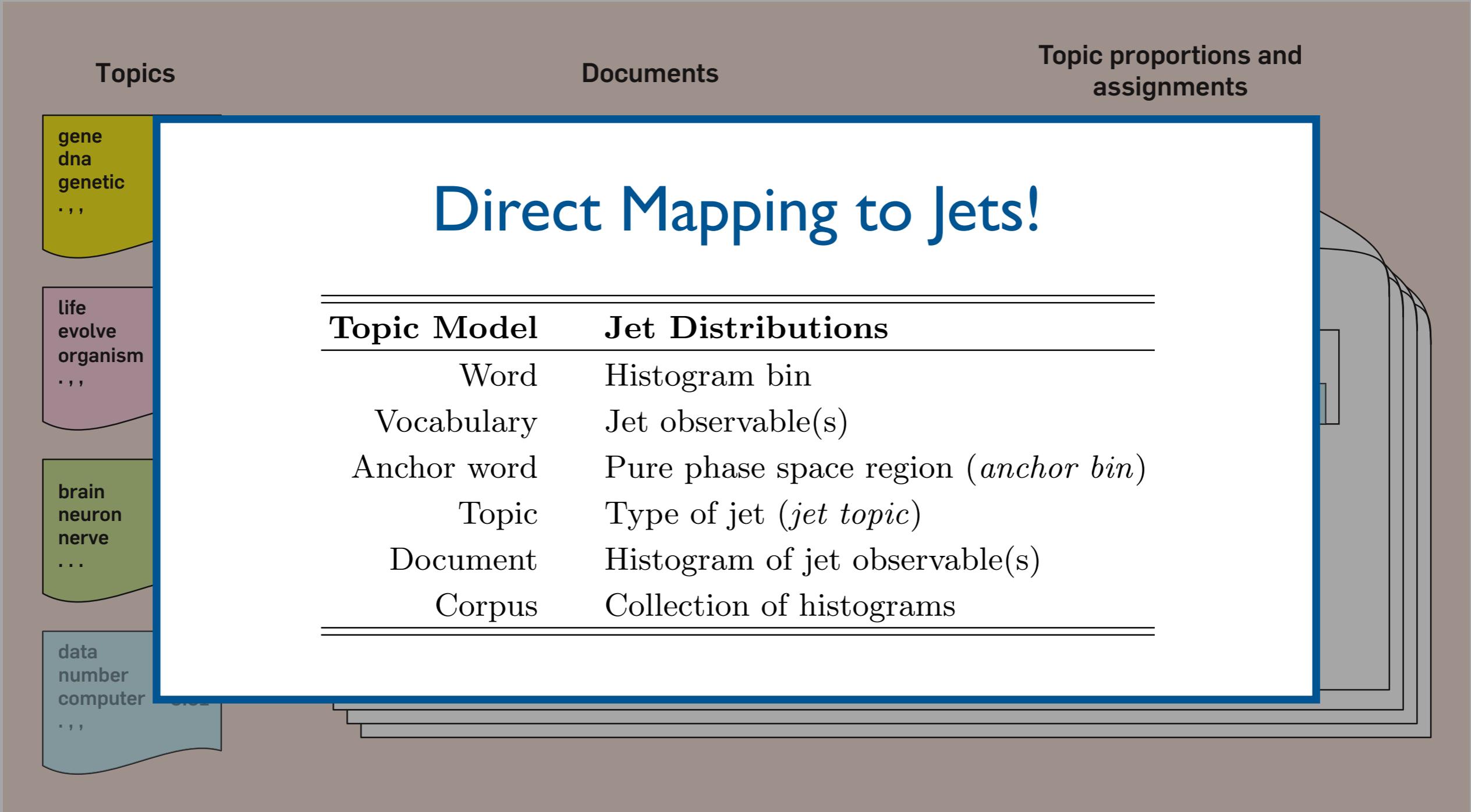
# Demixing (Impossible?)

# Topic Modeling



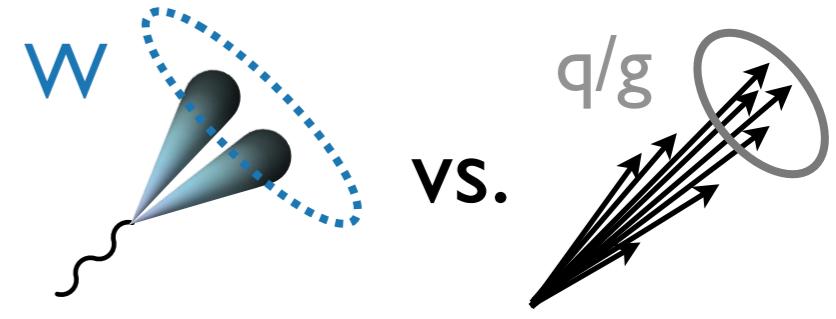
[Blei, 2012]

# Topic Modeling



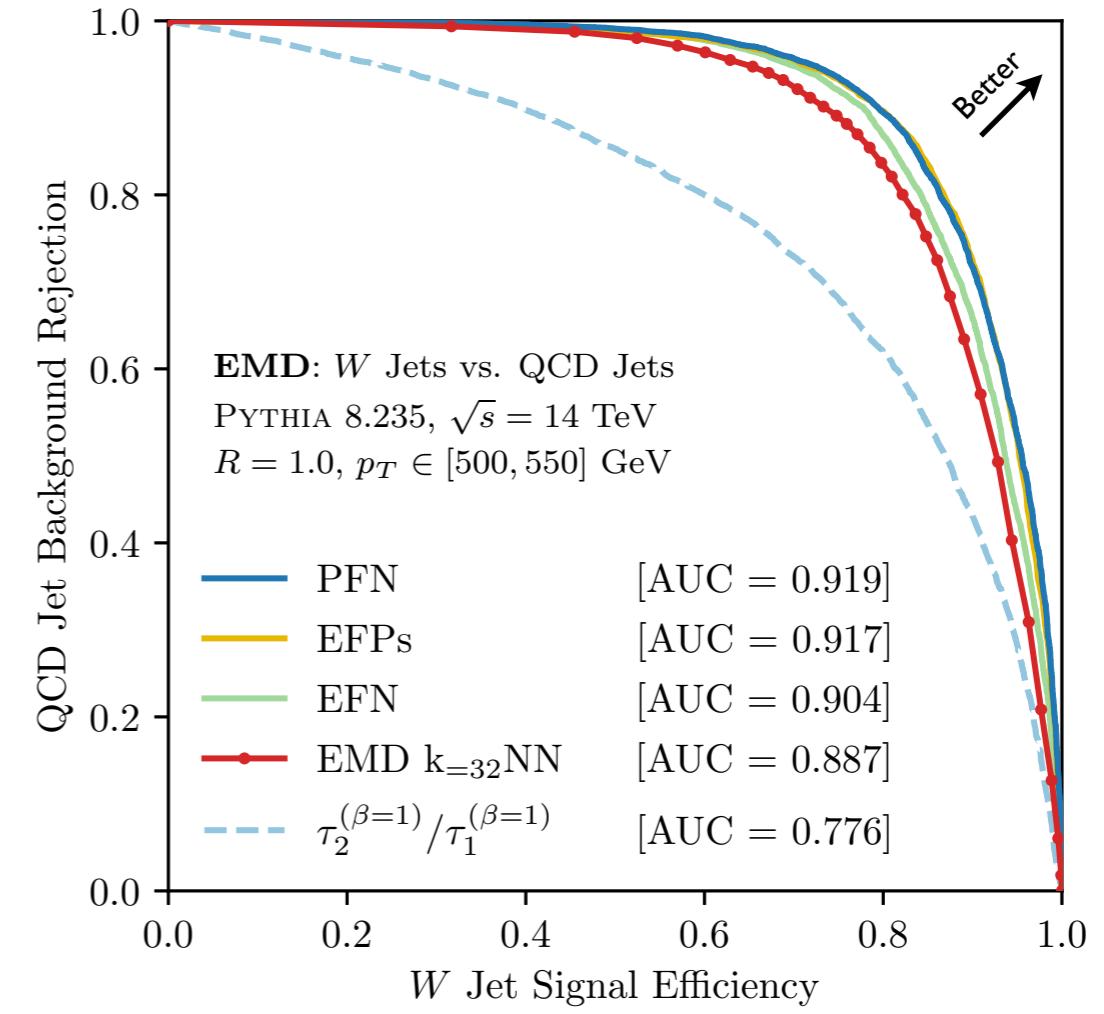
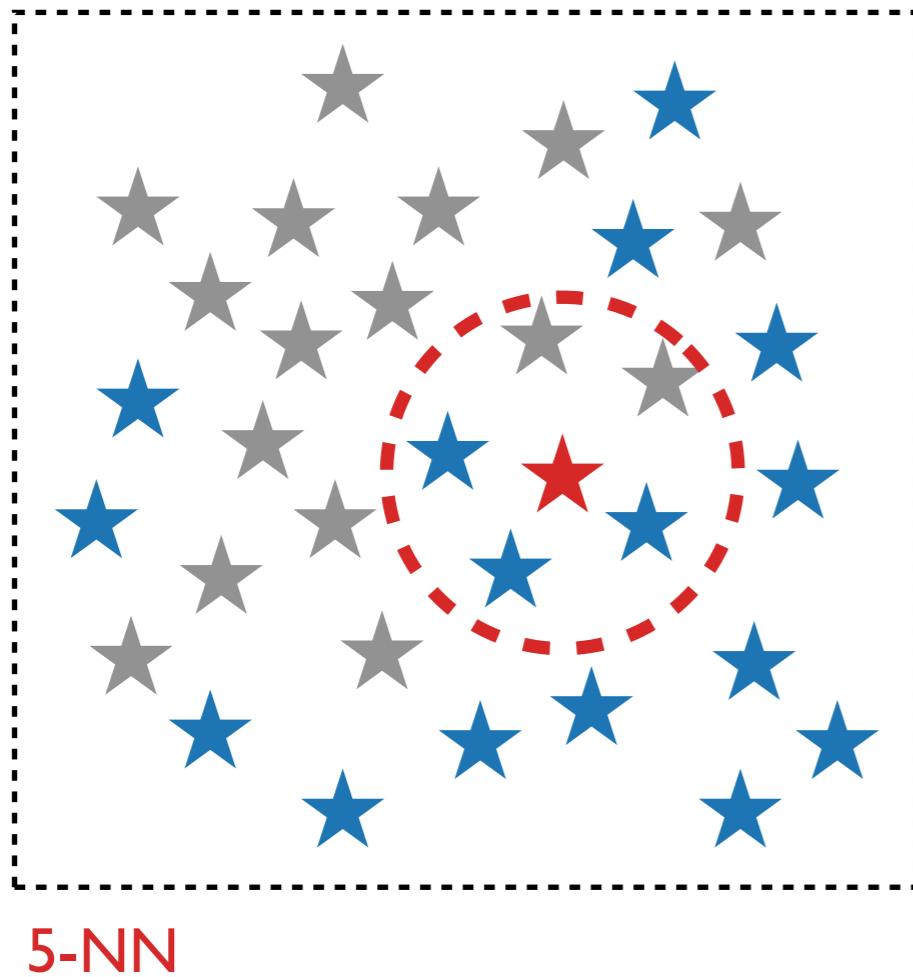
[Blei, 2012]

# Revisiting Jet Classification



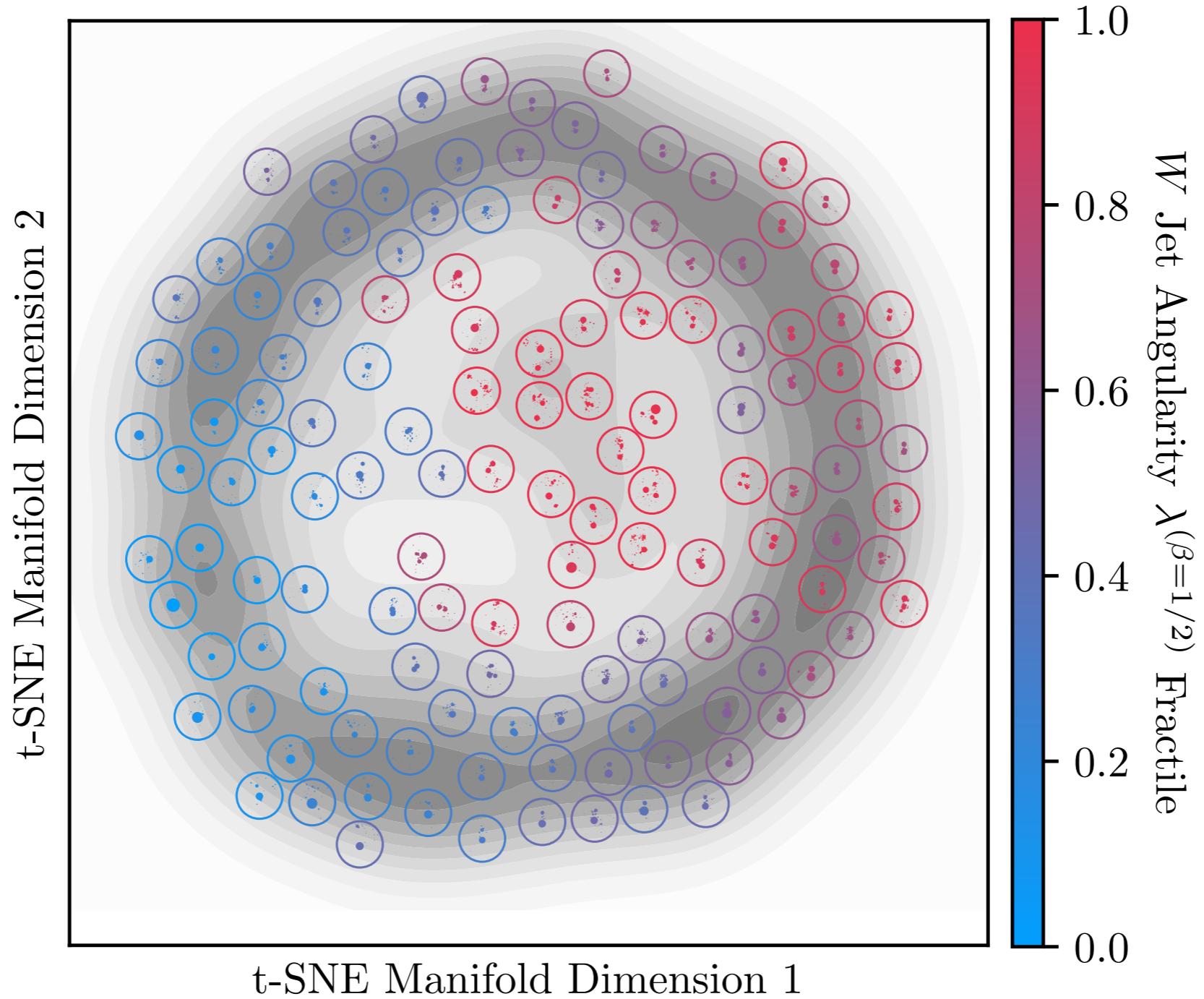
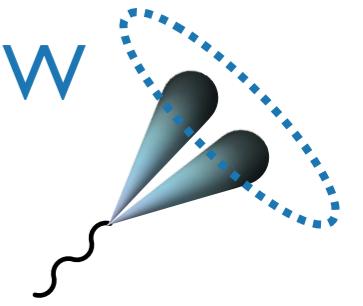
Estimate jet label by **k nearest neighbors** in training data

Approaches performance of **modern machine learning**



[Komiske, Metodiev, JDT, [1902.02346](#);  
comparison to JDT, Van Tilburg, [1011.2268](#), [1108.2701](#); Komiske, Metodiev, JDT, [1712.07124](#), [1810.05165](#)]

# The Space of Boosted W Bosons



[Komiske, Metodiev, JDT, [1902.02346](#)]