

# Jet Pull

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**Simone Marzani**  
**Università di Genova & INFN Sezione di Genova**



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**Buffalo NY**



**in collaboration with Andrew Larkoski & Chang Wu**

**arXiv:1903.02275 & arXiv:19xx.zzzzz**

# Outline

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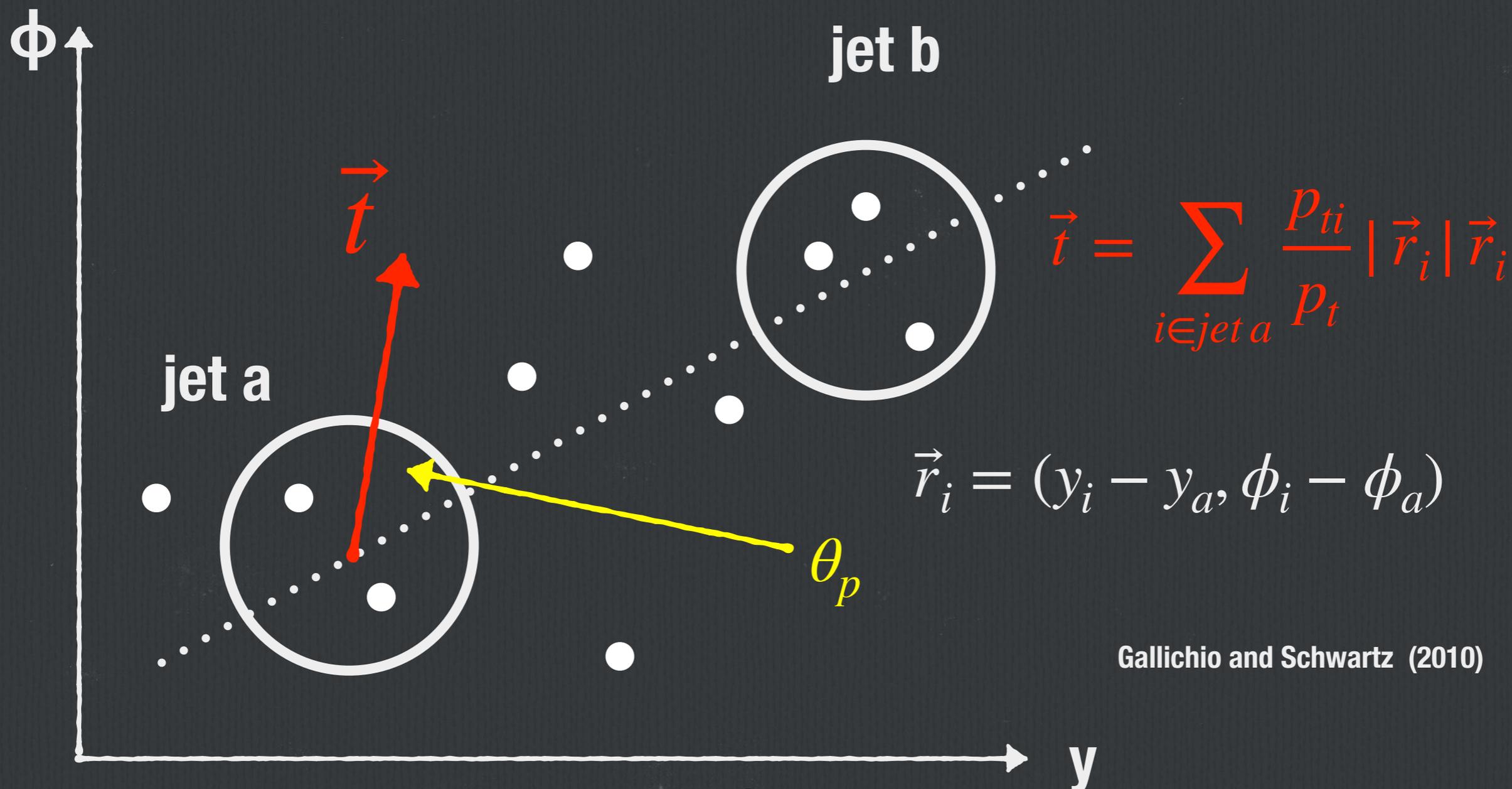
- **Probing colour flow with jet pull**
- **Theory predictions for the pull angle**
- **IRC safe projections of jet pull**
- **Conclusion and Outlook**

# Probing colour properties

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- one key aspect of the LHC physics program is the characterisation of (new) particle properties
- these include spin, CP properties and gauge charges
- in particular we would like to understand whether new particles carry colour charge
- a powerful way to extract this information is to study QCD radiation that accompanies the hard process
- this is often done with jet vetoes (central jet vetoes are a way of enhancing VBF against ggF Higgs production)
- jet shapes, which measure energy flow within a jet, are also sensitive to the colour flow of the jet environment

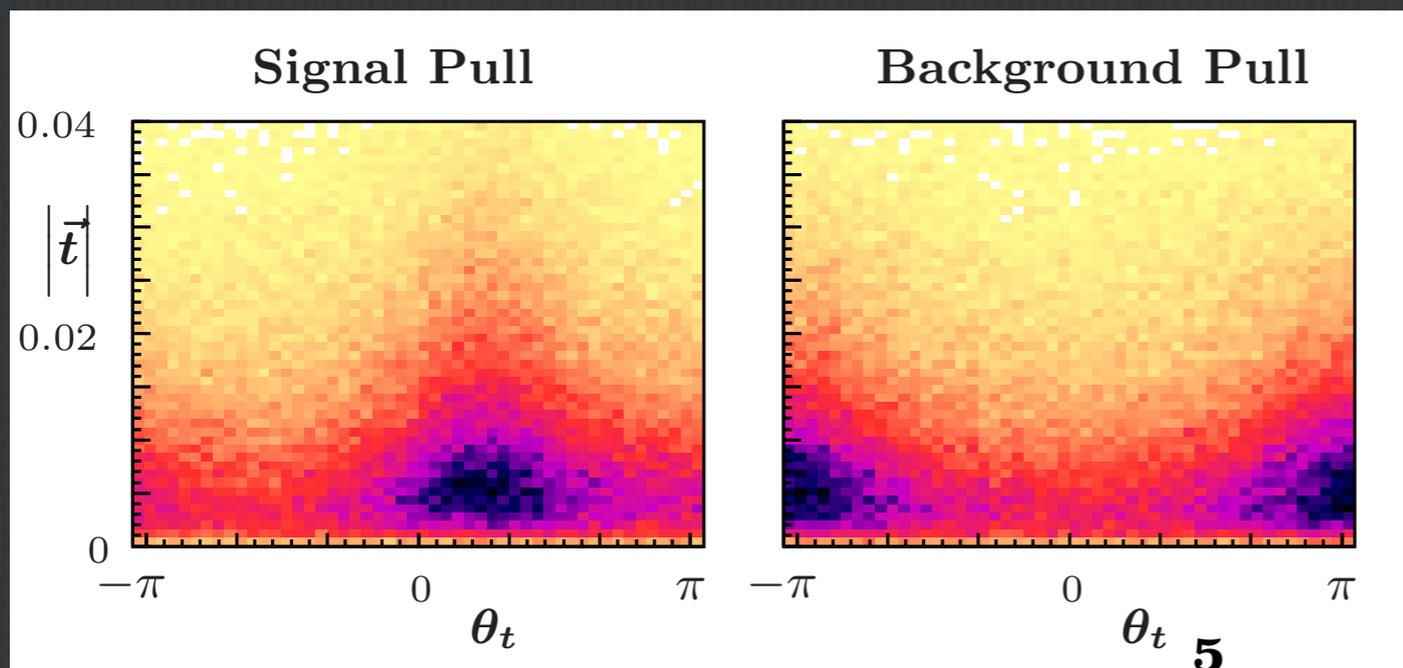
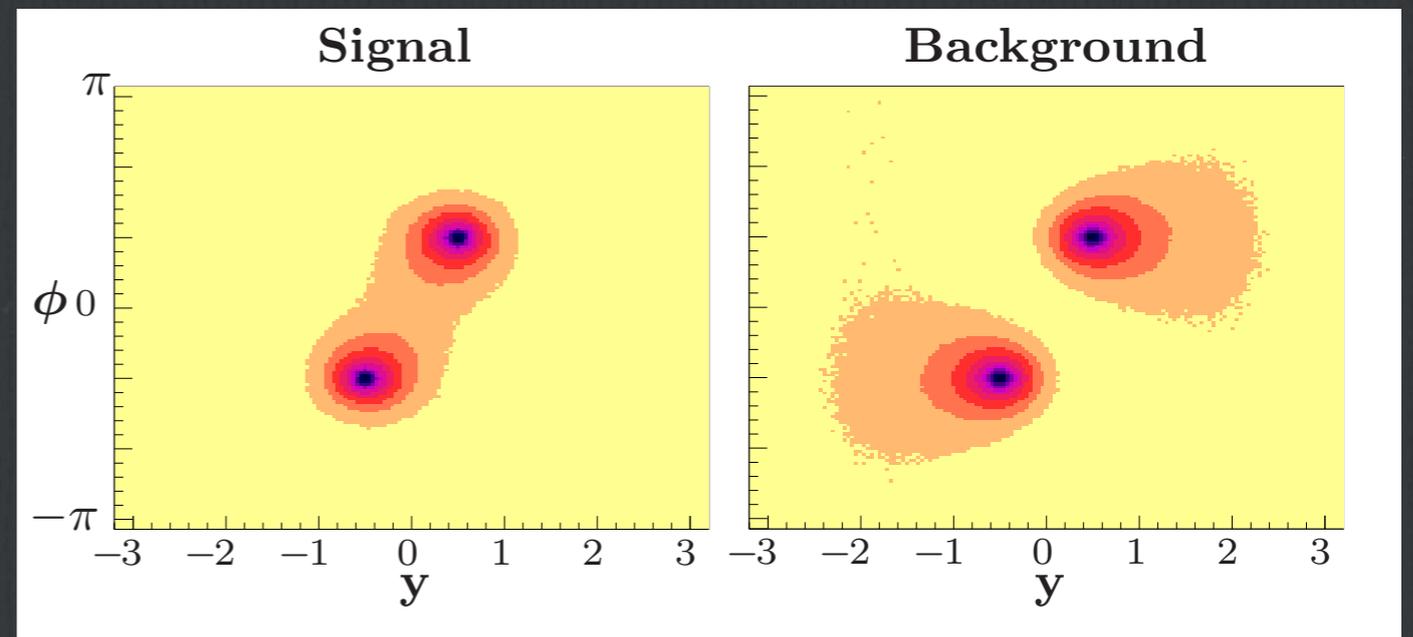
# Jet Pull



Gallichio and Schwartz (2010)

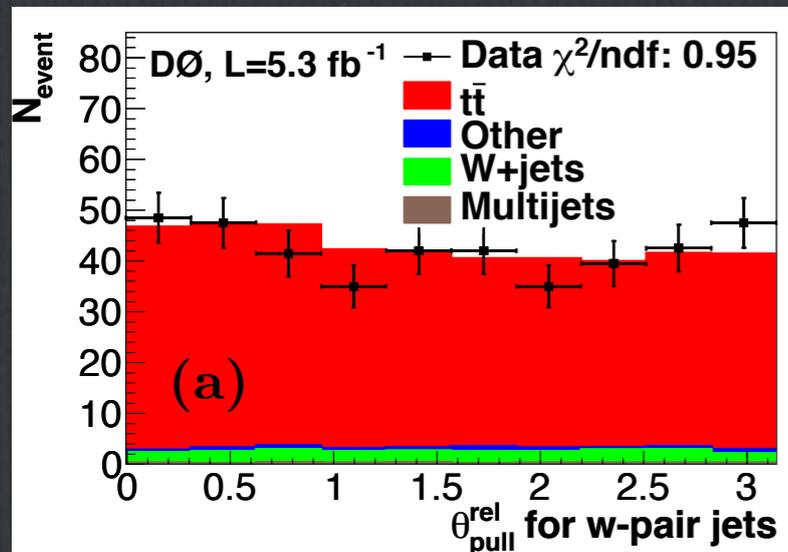
# $H \rightarrow bb$ vs $g \rightarrow bb$

- consider radiation pattern of a colour singlet (signal) vs colour octet (background)
- simulation shows dominant colour-connections:
- between the two b's for the singlet
- between each b and the initial-state for the background

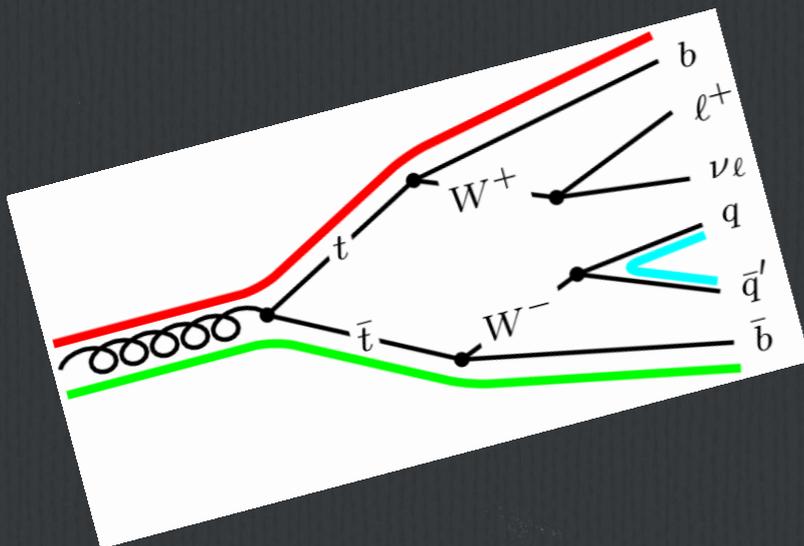


- pull angle shows much more sensitivity to colour flow than the pull magnitude

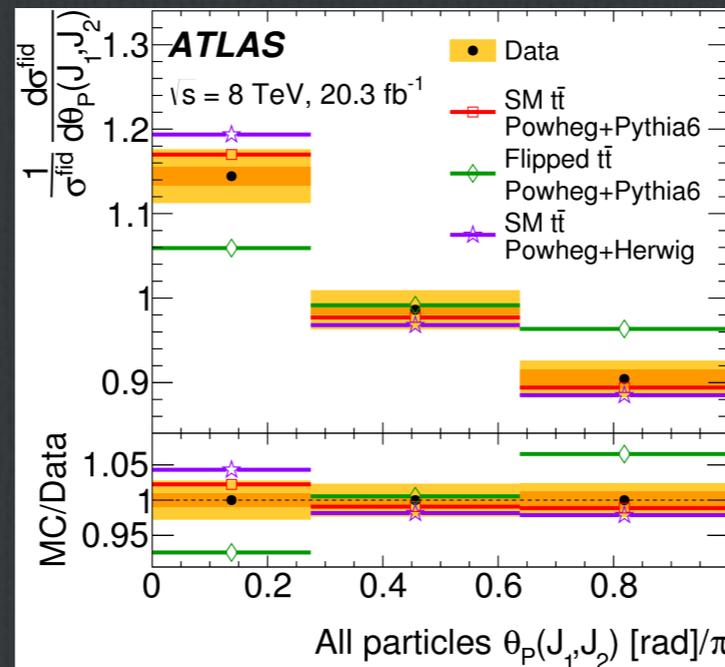
# Experimental measurements



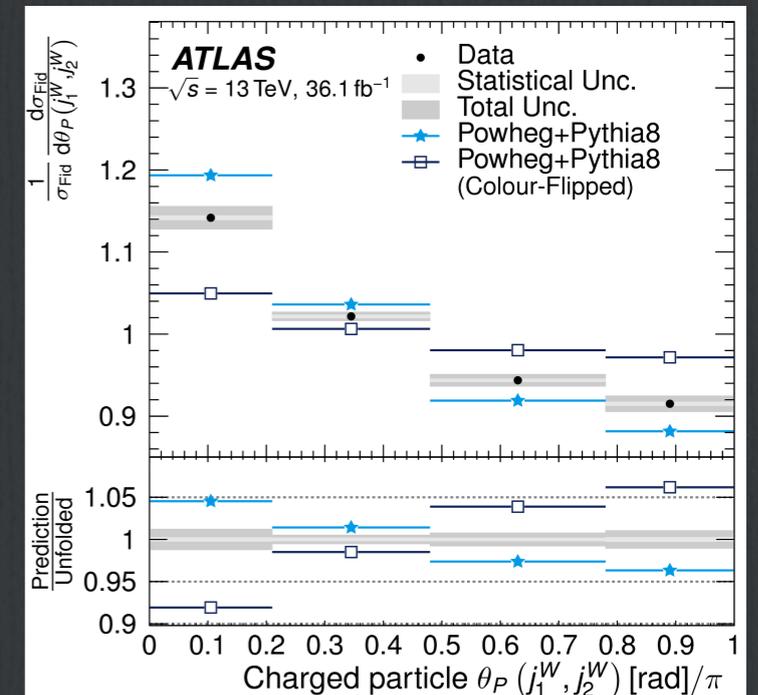
Phys.Rev. D83 (2011) 092002



- abundant production of top quarks offer nice lab for these studies
- pull angle can be measured on different types of colour connections



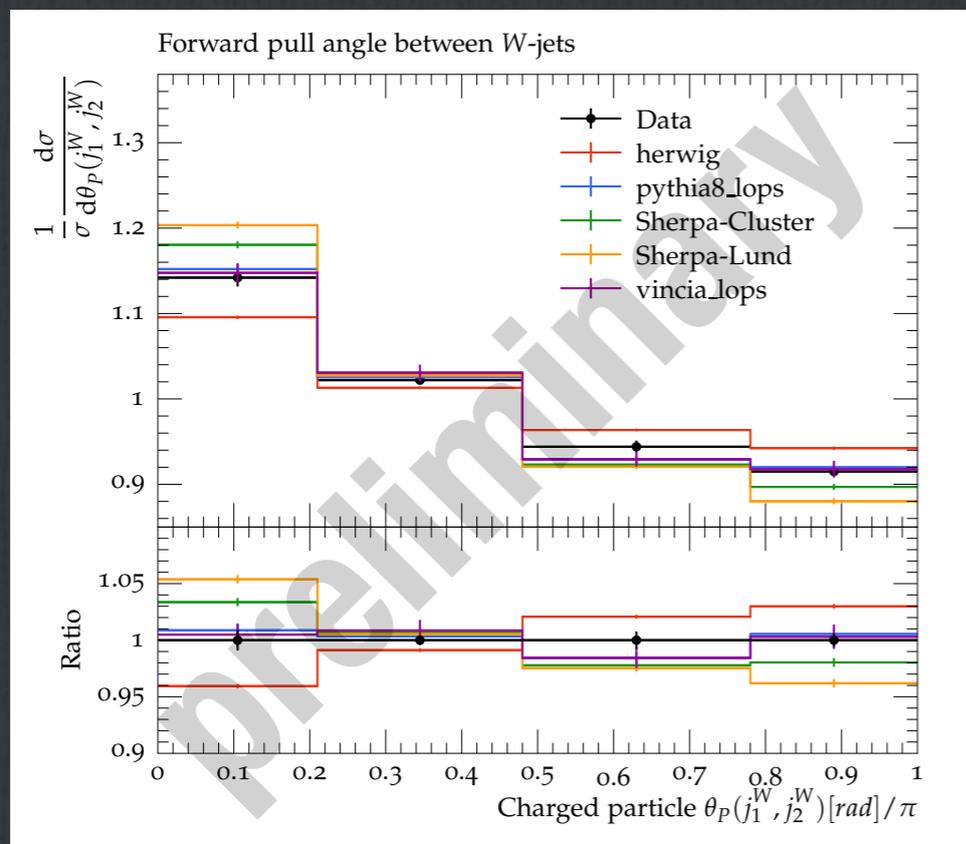
Phys. Lett. B750 (2015) 475



Eur. Phys. J. C 78 (2018)

**CMS ???**

# Les Houches studies



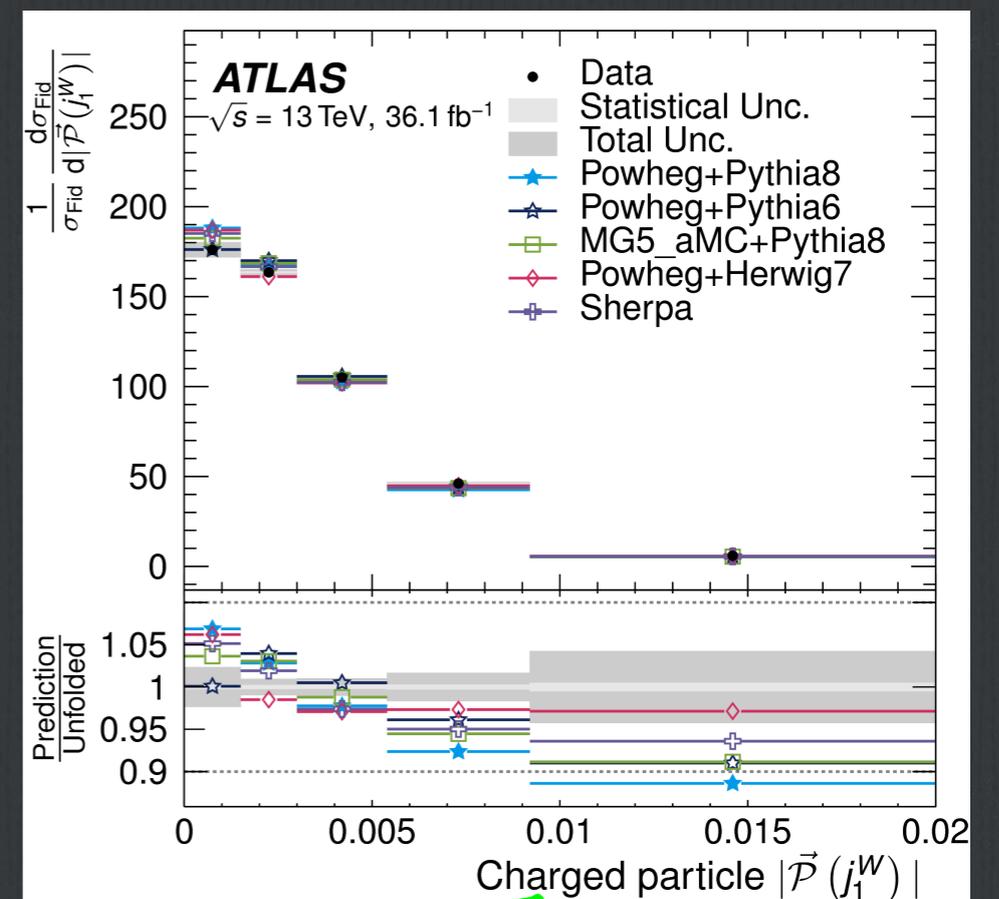
courtesy of Helen Brooks

- astonishing precision of 13 TeV data allows for stringent test of different MC tools
- on-going study started at LH 19 aimed at understanding this observable better
- intricate interplay of different ingredients:
  - spread in parton shower modelling is comparable (if not bigger) than spread due to non-perturbative contributions

- we hope to achieve a clearer picture for the proceedings!

# Can we make firmer theory predictions?

- besides MC study we can try and understand jet pull with analytic calculations
- we aim at a description that matches together fixed-order and resummed prediction
- let's look at next-to-leading log (NLL)
- pull magnitude (or any component of the pull vector) is IRC safe:
- if two emissions  $p_1, p_2$  become collinear, we are only sensitive to  $p_1 + p_2$
- if emission  $p_1$  becomes soft  $p_{t1} \rightarrow 0$  and it does not contribute to the magnitude
- we can calculate this distribution in perturbation theory!



not quite IRC safe!

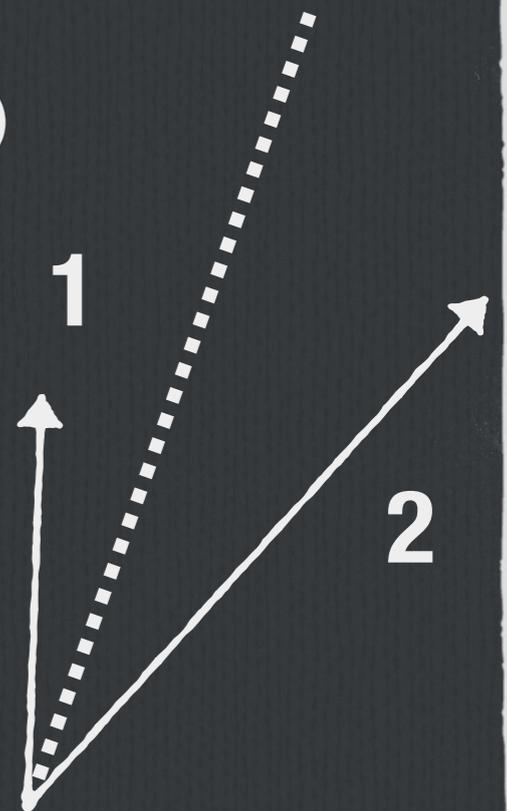
# Resummation of the pull magnitude

- we consider the resummation of the magnitude of a 2-D vector:

$$t = |\vec{t}| = \left| \sum_{i \in \text{jet } a} \frac{p_{ti}}{p_t} |\vec{r}_i| \vec{r}_i \right|$$

- situation very similar to well-known  $Q_T$  resummation (but in the final state)
- we work in a conjugate Fourier space
- on the other hand, its scaling properties are similar to the jet mass

$$\begin{aligned} t &= |\vec{t}_1 + \vec{t}_2| \simeq |z(1-z)^2 - (1-z)z^2| \theta_{12}^2 \\ &= |z(1-z)(1-2z)| \theta_{12}^2 \end{aligned}$$



# NLL resummation

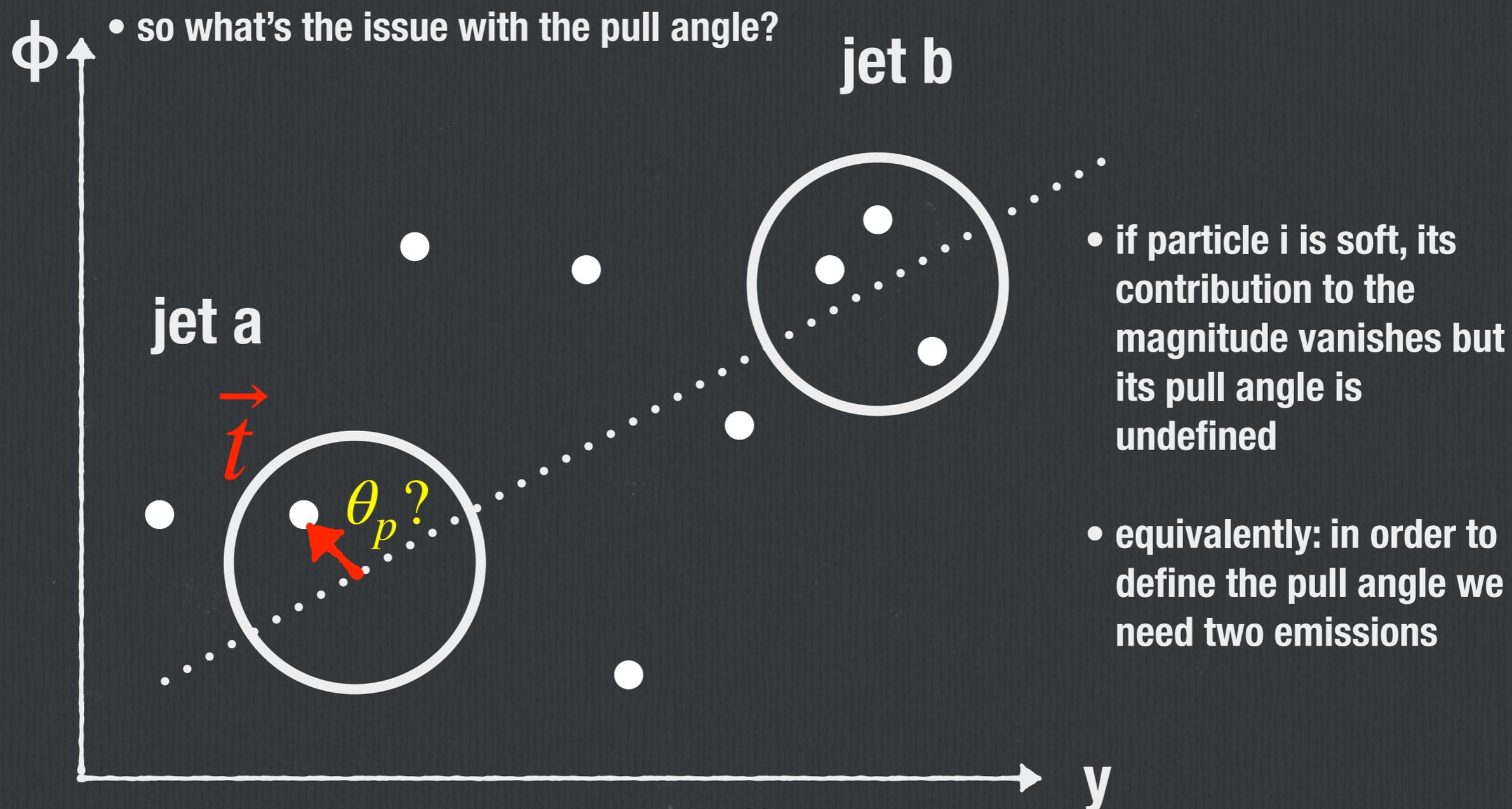
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- in the collinear limit, i.e. up to term of  $O(R^2)$  the all-order behaviour is

$$\frac{1}{\sigma_0} \frac{d\sigma}{dt} = \int_0^\infty db b J_0(bt) \exp [L f_1(\lambda) + f_{2c}(\lambda)] S_{ng}(\lambda)$$
$$\lambda = \alpha_s \beta_0 \log \left( b \frac{e^{\gamma_E}}{2} \right)$$

- remarkably, the  $f_1$  and  $f_{2c}$  have the same function have the same functional form as for the jet mass distribution
- $S_{ng}$  accounts for non-global logarithms, not investigated yet

# Pull angle: IRC un-safety



# aside: Sudakov safety

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- we know of other observables that suffers from similar problems (ratio of angularities, soft-drop momentum balance)
- we can make sense of these observables if we are able to resolve the singularities with the help of a (safe) companion variable
- we say that the IRC unsafe variable  $u$  is Sudakov safe if there exists an IRC safe observable  $s$  such that

$$p(u) = \int ds p(u | s) p(s)$$

- $p(s)$  must be calculated to all-orders in order to (Sudakov) suppress the  $s=0$  singularity

Larkoski, Thaler (2013)  
Larkoski, SM, Thaler (2015)

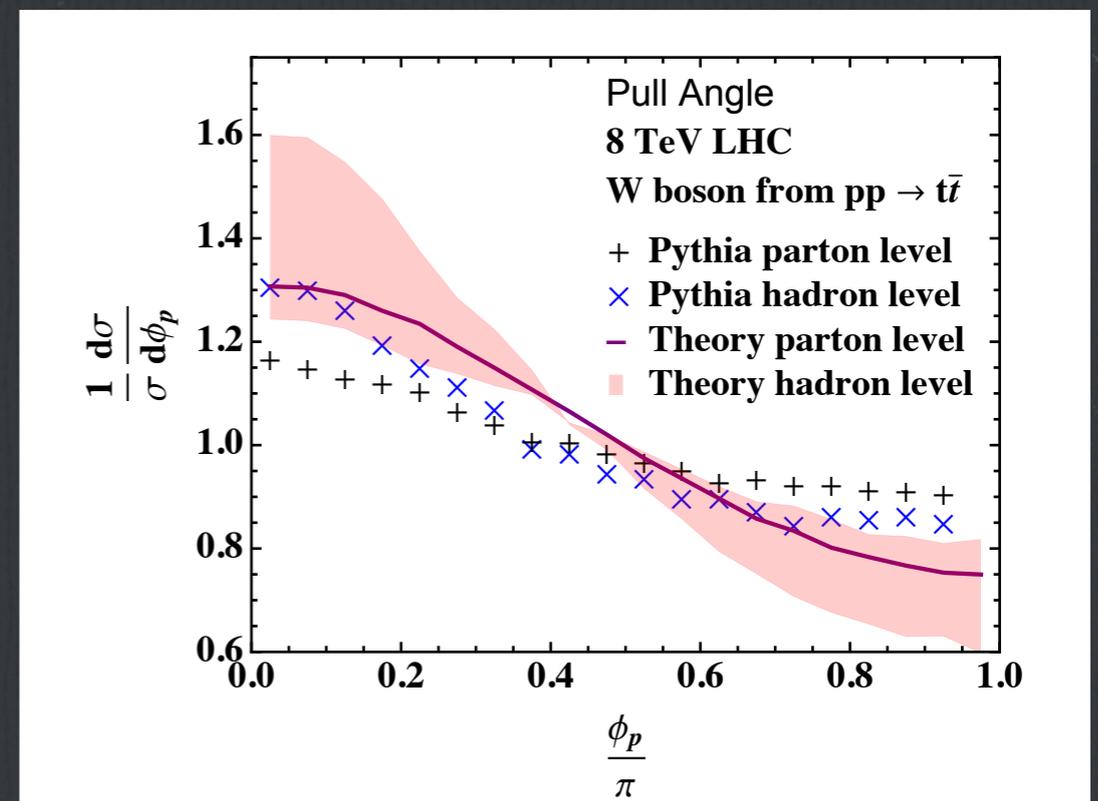
# Perturbative calculation

- our natural candidate for the safe companion is the pull magnitude itself
- thus we can write (apologies but in our paper we call the pull angle  $\phi_p$  rather than  $\theta_p$ )

$$\frac{1}{\sigma} \frac{d\sigma}{d\phi_p} = \int dt p(\phi_p | t) p^{res}(t)$$

computed at fixed-order

resummed at NLL in the collinear limit  
(but with no non-global logs at the moment)



# Non-perturbative effects

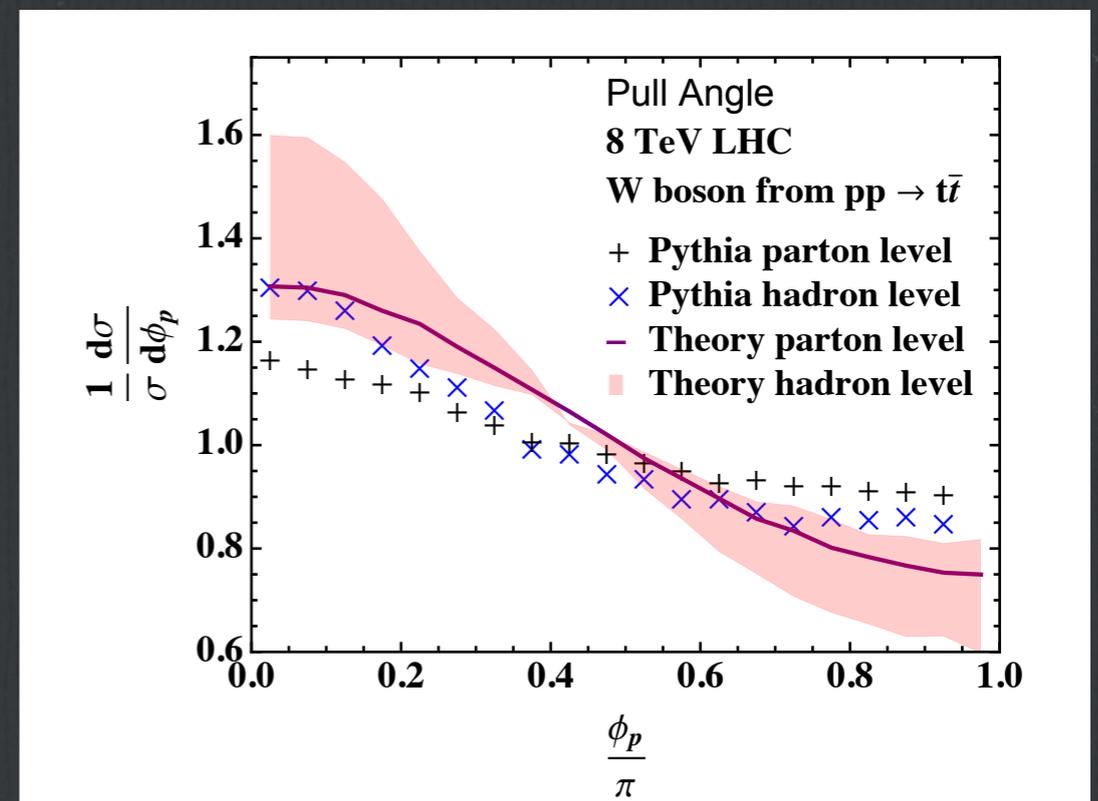
- for IRC safe observable we can make relatively strong statements about the scaling of non-perturbative corrections
- for Sudakov safe observable we don't have such luxury
- we make some rough estimate

$$p_{np}(t, \phi_p) \propto \tanh\left(\frac{1}{a\phi_p(2\pi - \phi_p)}\right) \delta\left(t - \frac{\Omega}{E_J}\right)$$

$$\Omega \simeq \Lambda_{QCD}, \quad 0 \leq a \leq 0.25$$

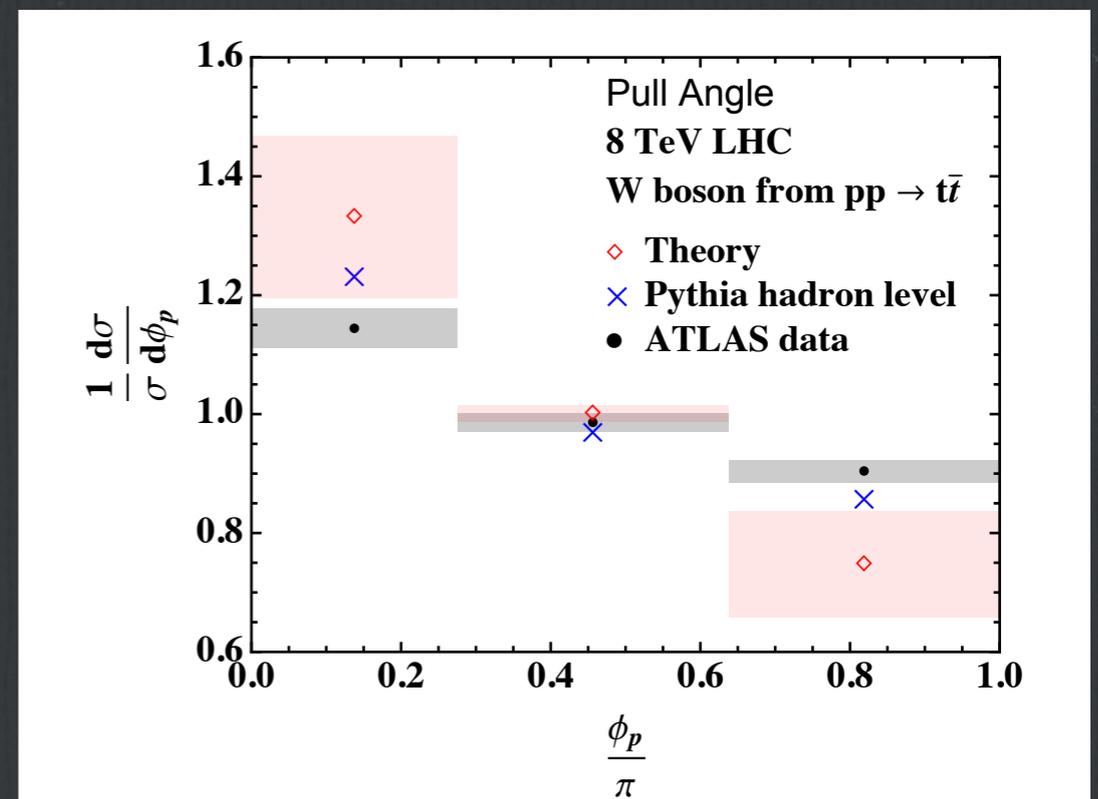
uniform to peaked in  $\phi_p=0$

$$P_{tot} = P_{np} \otimes P_{pert}$$

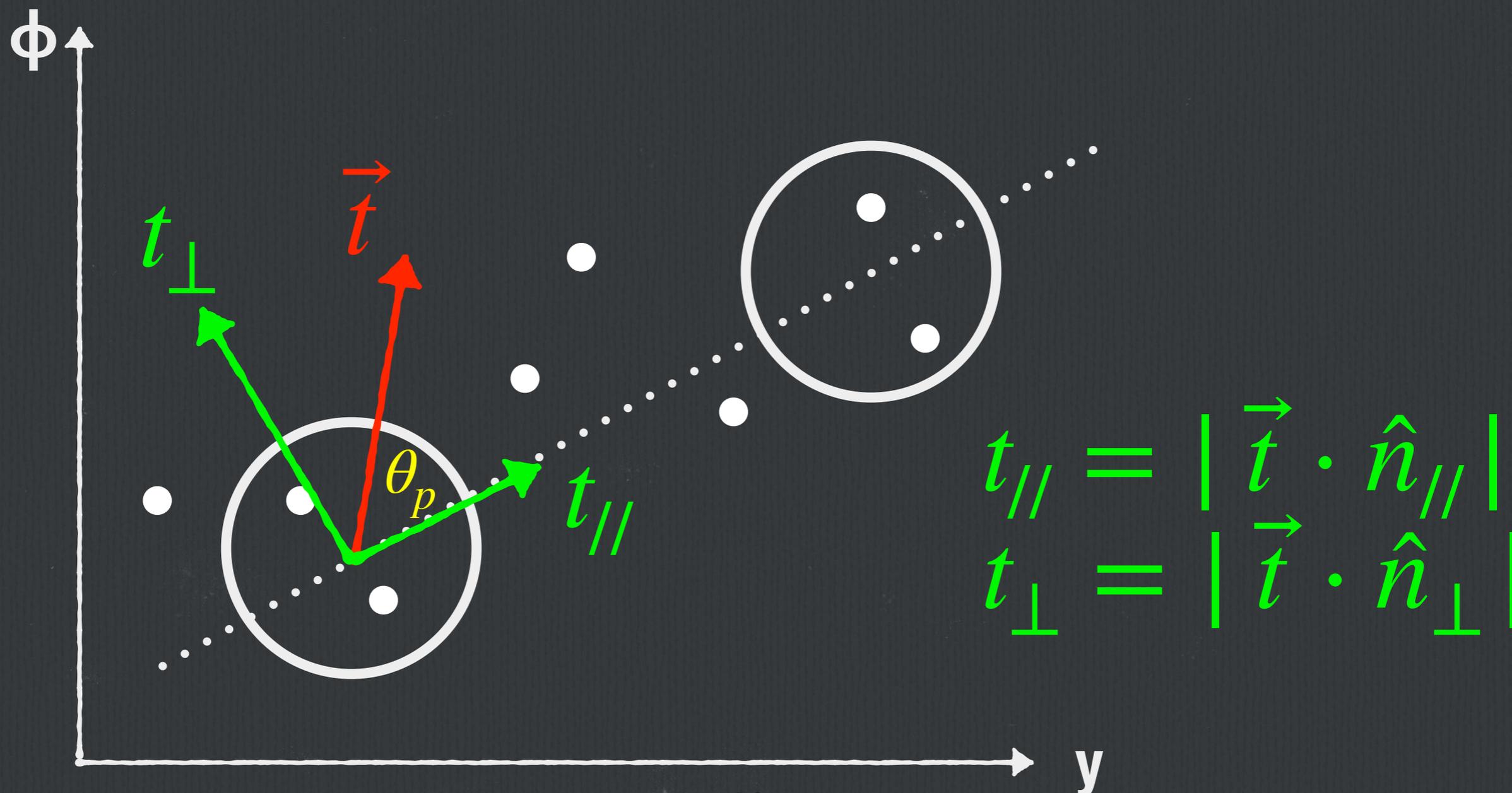


# Comparison to the data

- we can now compare to the Run I measurement by the ATLAS collaboration
  - our calculation is in fair agreement with the data (similar to the Monte Carlo prediction)
  - however it suffers from large theory uncertainties
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- perturbative uncertainties: Sudakov safe observables do not admit standard expansion in terms of Feynman diagrams: we have to combine fixed-order and resummed ingredients (and several questions remain open)
  - non-pert. uncertainties: lack of IRC safety prevents us from clearly separating perturbative and non-perturbative regions



# Safe uses of jet pull



# NLL resummation

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- the new variables  $t_{//}$  and  $t_{\perp}$  are IRC safe: we can combine fixed-order and resummed prediction in the standard way
- their resummation is relatively straightforward
- it closely follows the formalism develop for analogous projections of  $Q_T$  i.e.  $a_T$  (and  $\phi^*$ )

Banfi, Dasgupta  
and Duran Delgado (2010)

$$\frac{1}{\sigma_0} \frac{d\sigma^{collinear}}{dt_{\perp}} = \frac{1}{\pi} \int_0^{\infty} db \cos(bt_{\perp}) \exp [Lf_1(\lambda) + f_{2c}(\lambda)]$$

# Towards phenomenology

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- in order achieve full NLL resummation we will have to include
- soft radiation at wide angle (through an expansion in powers of the jet radius)
- non-global logarithms
- notice that soft radiation is crucial (this is what we want to probe) but does depend on the jet environment
- we have to specify the process and the event selection, e.g.

$$pp \rightarrow W(\rightarrow qq') + jet$$

- and measure the pull between the W subjets

# Conclusions & Outlook

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- jet pull is an interesting observable to probe colour flow in LHC events
- pull angle distributions measured by D0 and ATLAS: fair agreement with MC but small experimental uncertainties expose shortcomings of simulations
- theory analysis possible but conclusions are not very firm because of IRC unsafely
- this can be alleviated by looking at safe projections of the jet pull vector (work in progress)

**THANK YOU VERY MUCH!**