Wakefield Acceleration in Nanostructures

Workshop on beam acceleration in crystals and nanostructures
and
Fermilab Colloquium
June 25, 2019

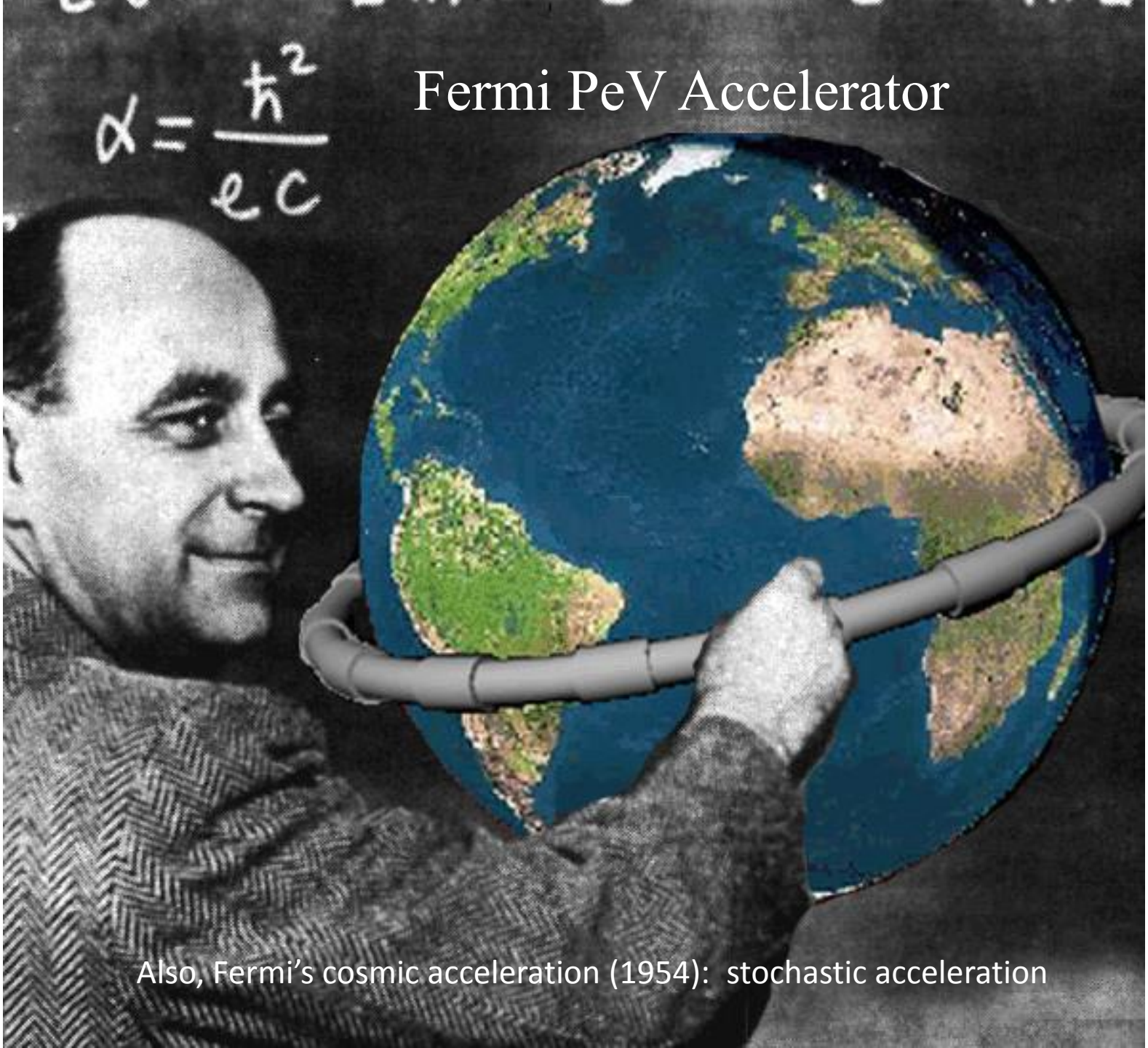
Toshi Tajima
UC Irvine

In dedication to the late Prof. Gaurang Yodh:
The last student of Enrico Fermi, at U. Chicago (PhD. 1955), passed away June 3, 2019

collaboration: G. Mourou, K. Nakajima, S. Hakimi, S. Bulanov, T. Ebisuzaki, X. Yan, M. Zhou, A. Chao, K. Abazajian, X. M. Zhang, D. Farinella, P. Taborek, F. Dollar, J. Wheeler, Y.M. Shin, V. Shiltsev, N. Naumova, W. J. Sha, J. C. Chanteloup, S. Nicks, D. Roa, A. Necas, C. Barty

- Introduction
- Fiber laser and ascent toward 100GeV and collider (and a tiny laser)
- Single-cycled laser and " TeV on a chip"
- Nature's favorite acceleration: cosmic wakefield
- Accelerator to our body

Fermi PeV Accelerator

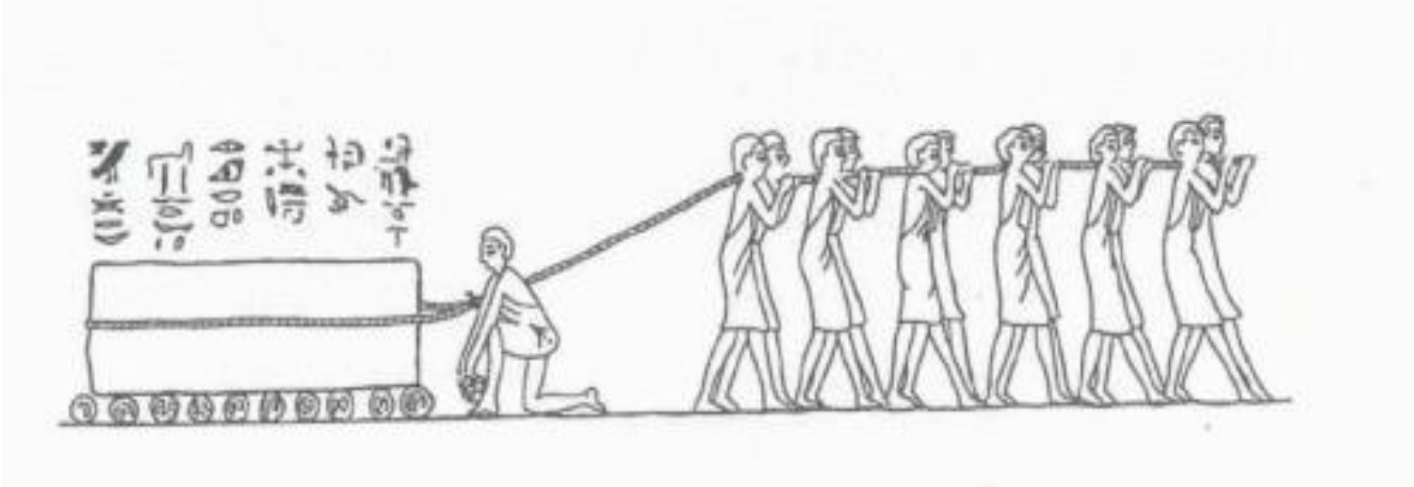


Also, Fermi's cosmic acceleration (1954): stochastic acceleration

Plasma accelerator driven by beam/pulse

Collective force ~N^2 (nonlinear ← linear force ~N)

Coherent and smooth structure (not stochastic)



Plasma accelerator driven by laser (coherent photons)

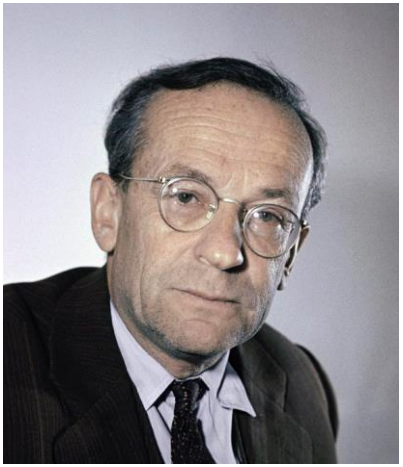
←[*Fermi*'s challenge for PeV accelerator]

compactification by 10^3 – 10^4 (even by 10^6) >> conventional accelerators

enabled by laser technology (intense ultrafast laser compression (Mourou et al.1985. 2013))

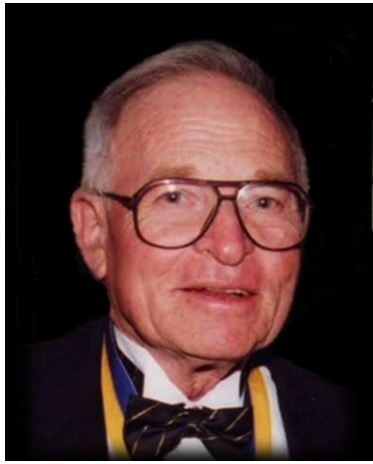
[particle beam-driven case: similar (if a bit lower)]

Acceleration by plasma wake waves: History



V. Veksler

Collective acceleration suggested:
Veksler (1956, CERN)
Driven by electron beam
(ion energy)~ (M/m)(electron energy)



N. Rostoker

Many experimental attempts of plasma acceleration (~60's -'70s, Rostoker's lab UCI included)
led to no such amplification
(ion energy)~ (2α+1)x(electron) **Mako-Tajima (UCI) analysis** (1978;1984)
sudden acceleration, ions untrapped,
electrons return, while some run away
→ #1 **gradual acceleration necessary**

J. Dawson

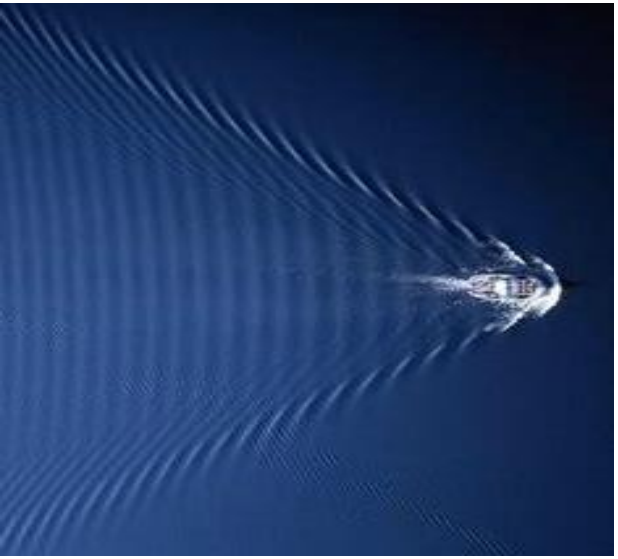
→ **Tajima-Dawson (1979, UCLA) wakefield**
#2 **electron acceleration** possible
with **trapping** **(with the Tajima-Dawson field)** with laser, more tolerant for sudden process

Target Normal Sheath Acceleration
laser-driven ion acceleration (LLNL,2000)
sudden acceleration, ions untrapped

Laser Wakefield (LWFA):

Wake phase velocity >> water movement speed
maintains **coherent** and **smooth** structure

Tsunami phase velocity becomes ~0,
causes **wavebreak** and **turbulence**

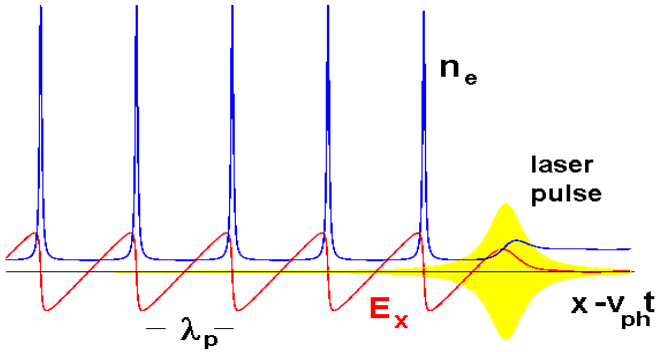


vs

Strong beam (of laser / particles) drives plasma waves to saturation amplitude: $E = m\omega v_{ph} / e$

No wave breaks and wake **peaks** at v≈c

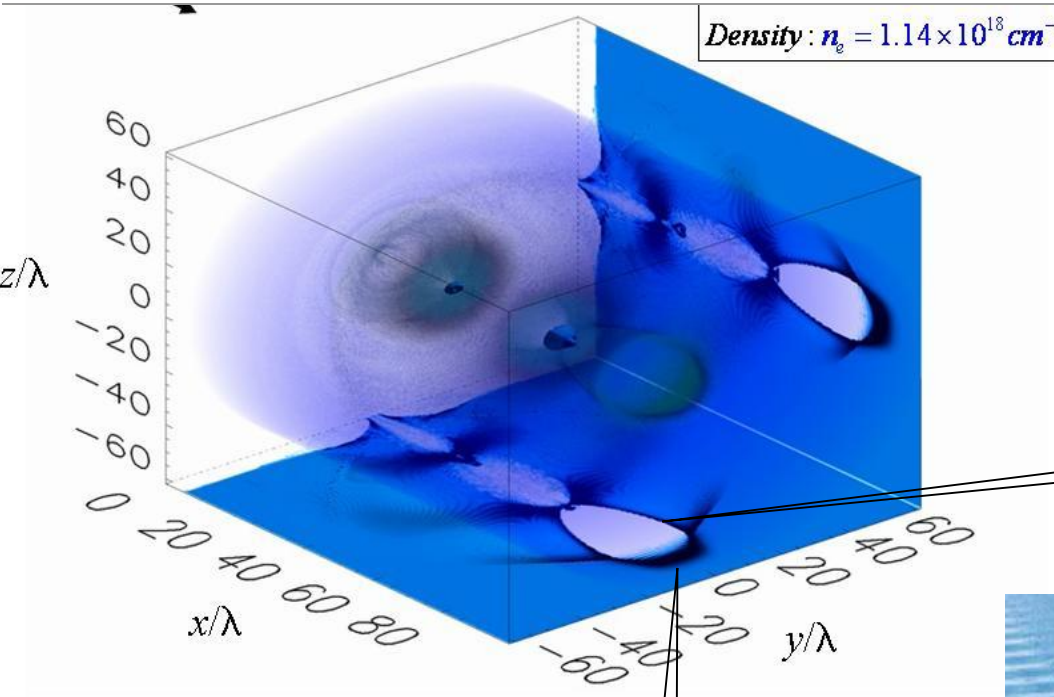
Wave **breaks** at v<c



← relativity regularizes (***relativistic coherence***)

Relativistic coherence enhances beyond the Tajima-Dawson field $E = m\omega_p c / e$ (~ GeV/cm)

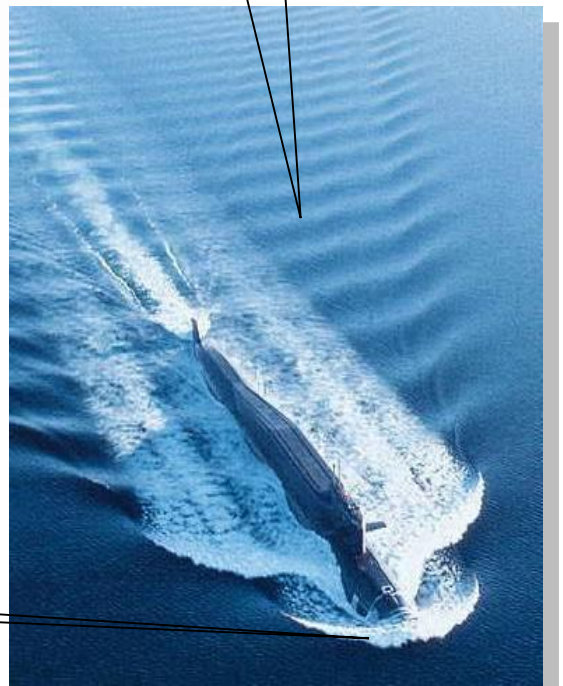
Laser-driven Bow and Wake



(Bulanov, Esirkepov)

Wakefield acceleration

Wake Wave



Bow Wave

Ponderomotive acceleration

The late Prof. Abdus Salam

At ICTP Summer School (1981),
Prof. Salam summoned me and discussed
about laser wakefield acceleration.

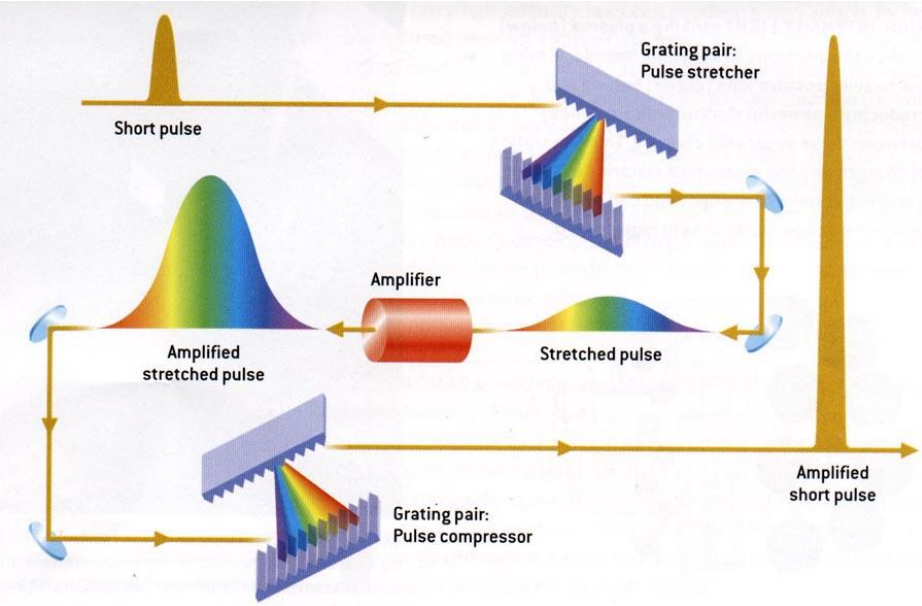
Salam: *'Scientists like me began feeling that we had less means to test our theory. However, with your laser acceleration, I am encouraged'.* (1981)

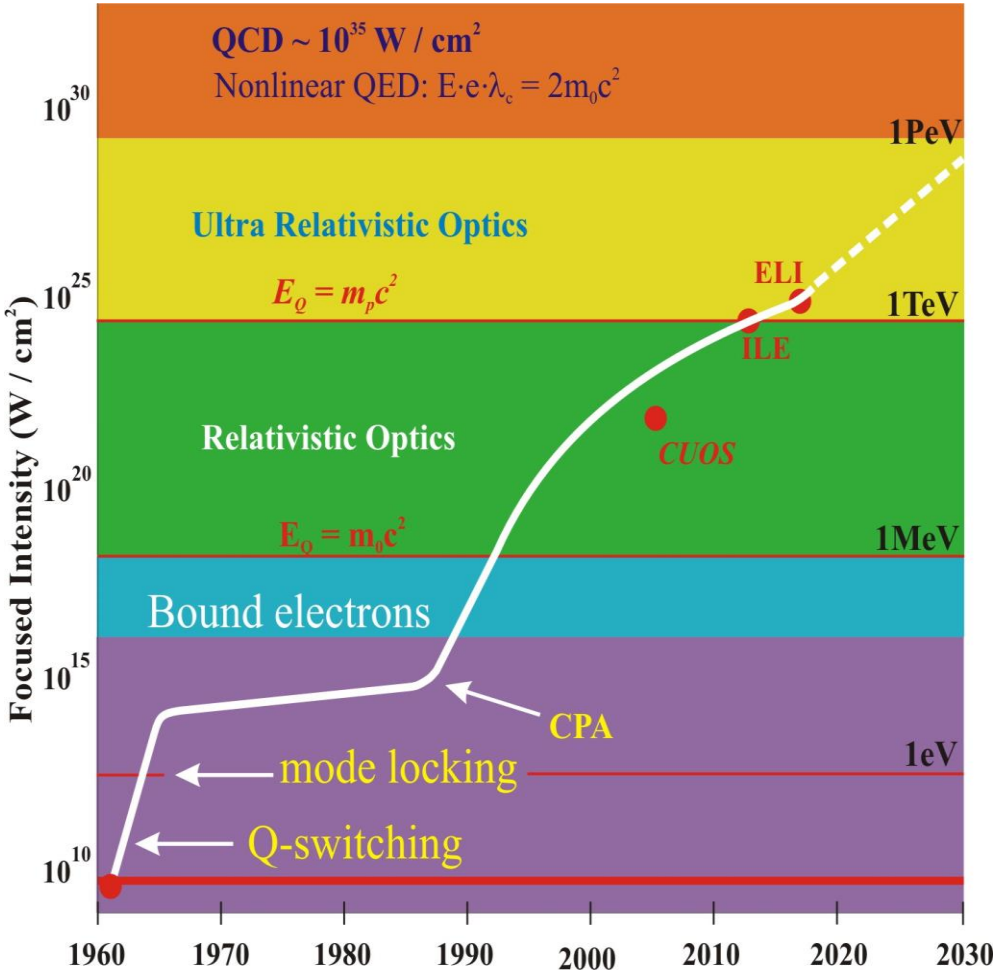
He organized the Oxford Workshop
on laser wakefield accelerator in 1982.

Effort: many scientists over many years to realize his vision / dream
High field science: spawned

Ascent toward 100GeV and collier

Enabling technology: laser revolution



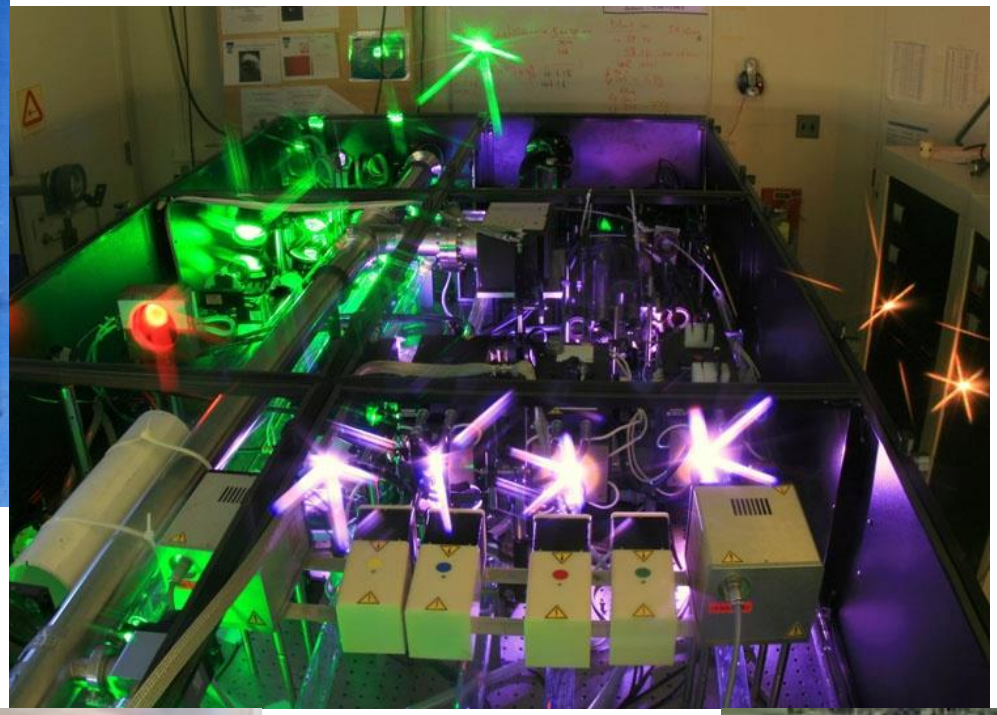


G. Mourou invented Chirped Pulse Amplification (1985)

Laser intensity exponentiated since,

to match the required intensity for Tajima-Dawson's LWFA (1979)

Demonstration, realization, and applications of laser wakefield accelerators



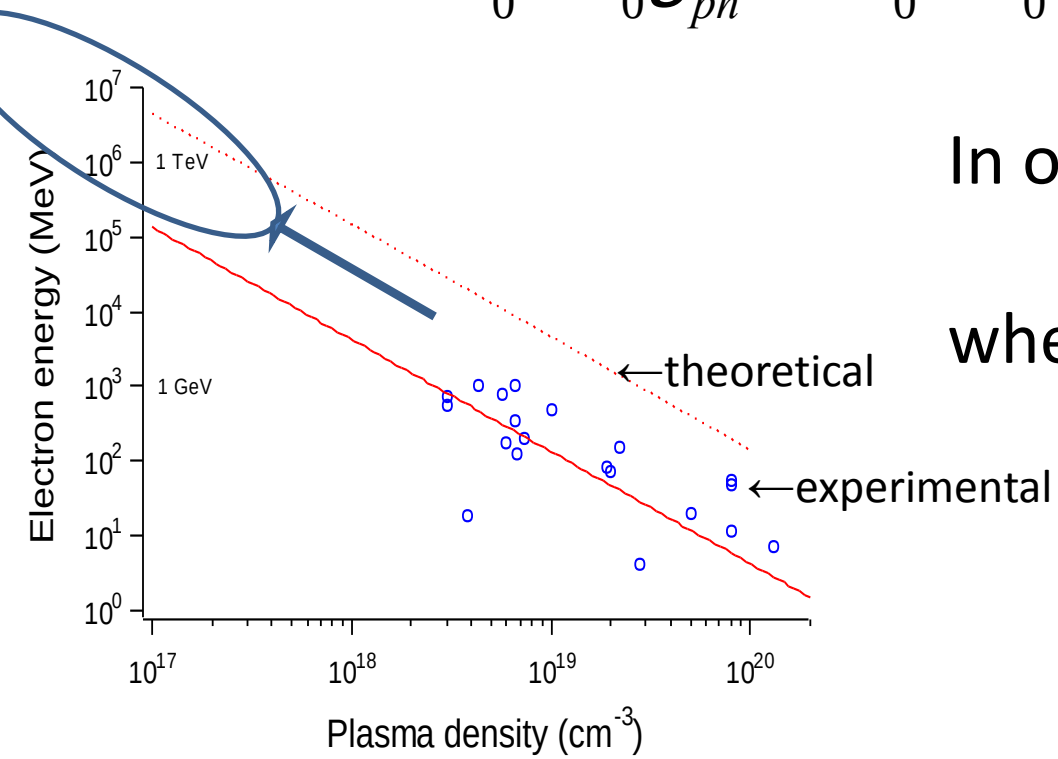
(Michigan)

4 GeV laser accelerator LBL

3GeV Synchrotron SOLEIL

Theory of wakefield toward extreme energy

$$\mathrm{D}E \approx 2m_0c^2a_0^2\gamma_{ph}^2 = 2m_0c^2a_0^2\left(\frac{n_{cr}}{n_e}\right),$$ (when 1D theory applies)



In order to avoid wavebreak,

$$a_0 < \gamma_{ph}^{1/2},$$

where

$$\gamma_{ph} = (n_{cr}/n_e)^{1/2}$$

n_{cr} =10^{21} (1eV photon)

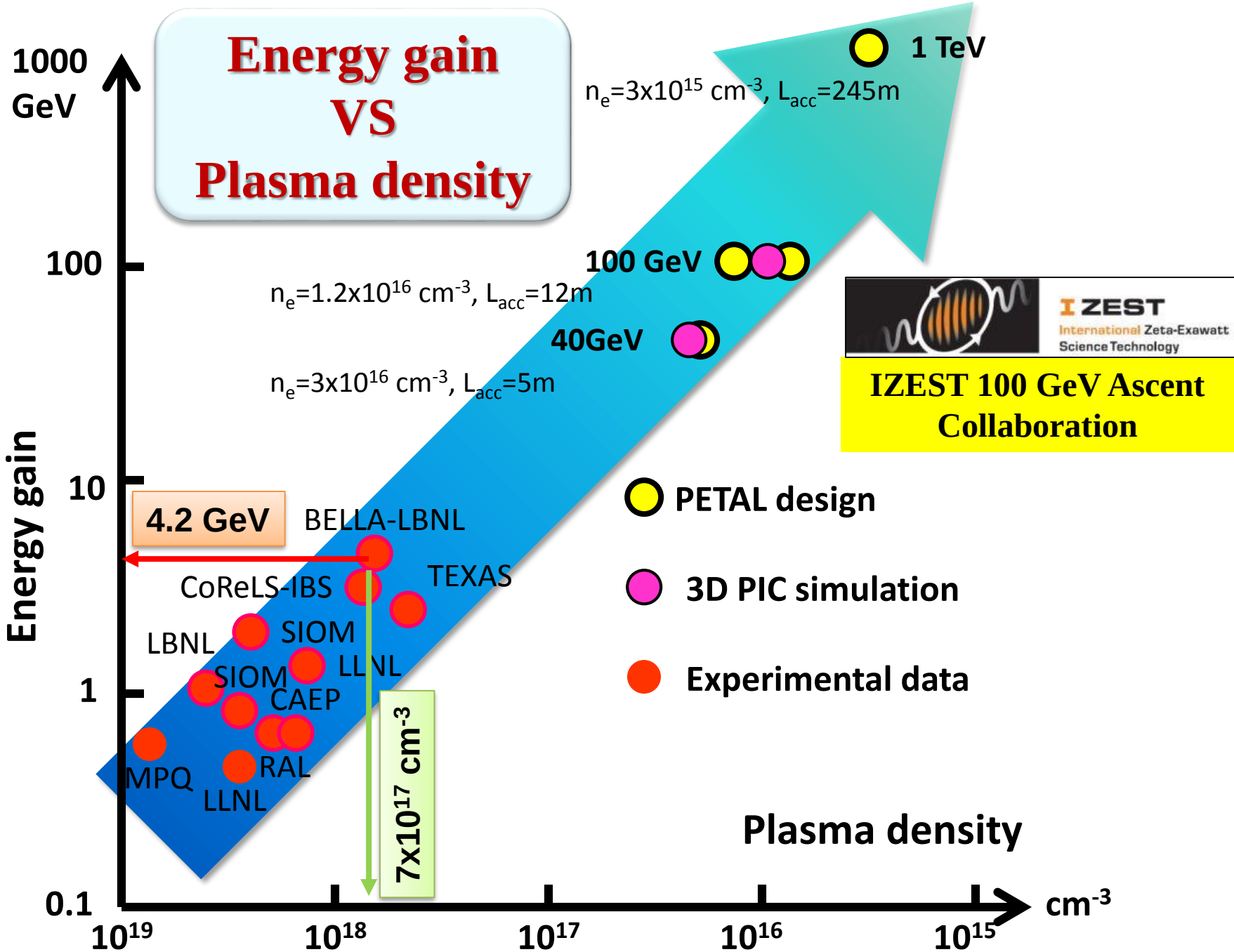
→ 10^{29} (10keV photon)

n_e = 10^{16} (gas) → 10^{23} (solid)

$$L_d = \frac{2}{\pi}\lambda_p a_0^2\left(\frac{n_{cr}}{n_e}\right), \qquad L_p = \frac{1}{3\pi}\lambda_p a_0\left(\frac{n_{cr}}{n_e}\right),$$

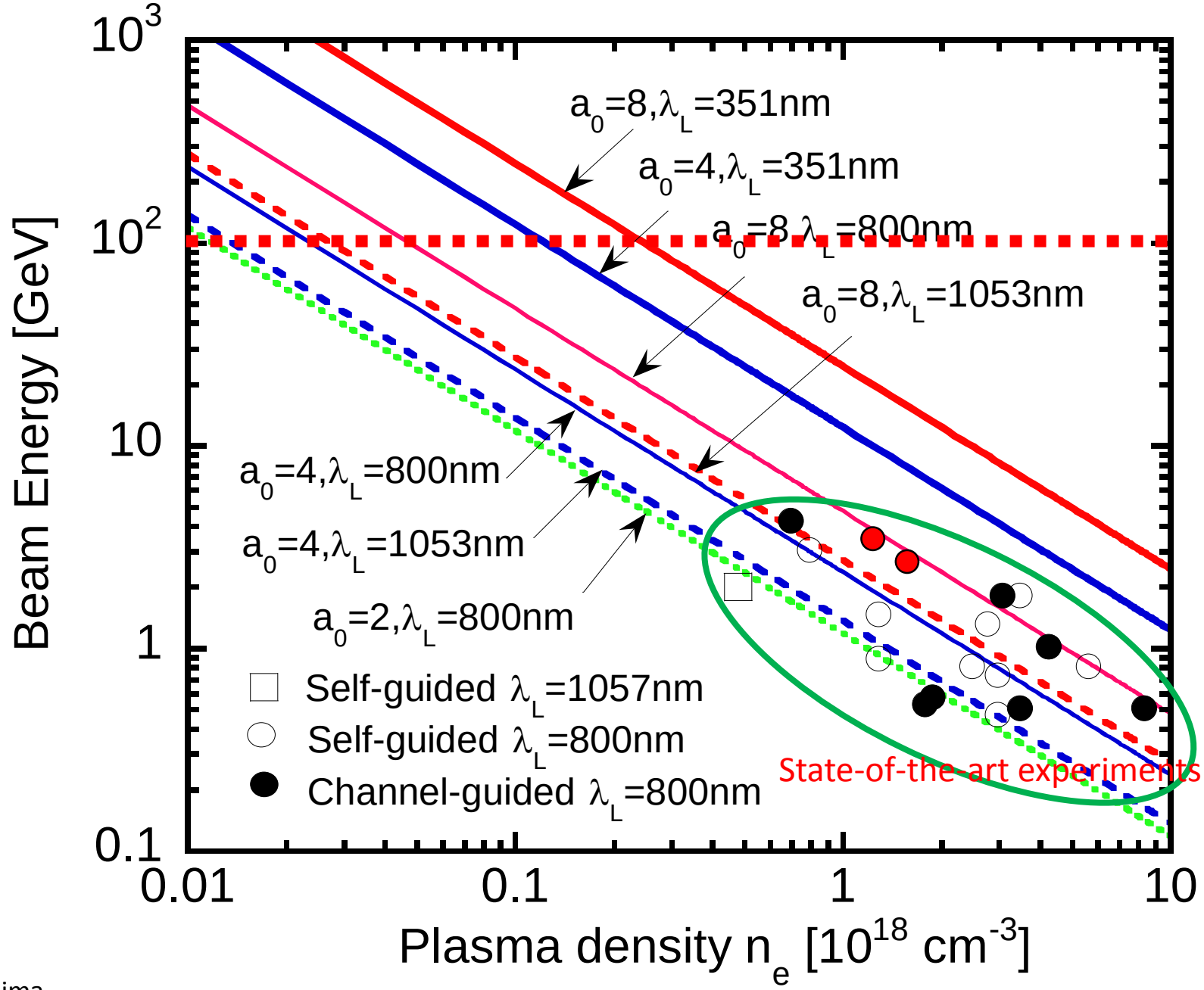
dephasing length

pump depletion length


Energy gain
VS
Plasma density
1000 GeV
100
10
1
0.1
Energy gain
1 TeV
n_e=3x10^{15} cm^{-3}, L_{acc}=245m
100 GeV
n_e=1.2x10^{16} cm^{-3}, L_{acc}=12m
40GeV
n_e=3x10^{16} cm^{-3}, L_{acc}=5m
IZEST
International Zeta-Exawatt Science Technology
IZEST 100 GeV Ascent Collaboration
4.2 GeV
BELLA-LBNL
TEXAS
CoReLS-IBS
LBNL
SIOM
SIOM
LLNL
CAEP
RAL
MPQ
LLNL
7x10^{17} cm^{-3}
PETAL design
3D PIC simulation
Experimental data
Plasma density
cm^{-3}
10^{19}
10^{18}
10^{17}
10^{16}
10^{15}

K. Nakajima

1 ω → 3ω; 10times energy; 30times shorter



K. Nakajima

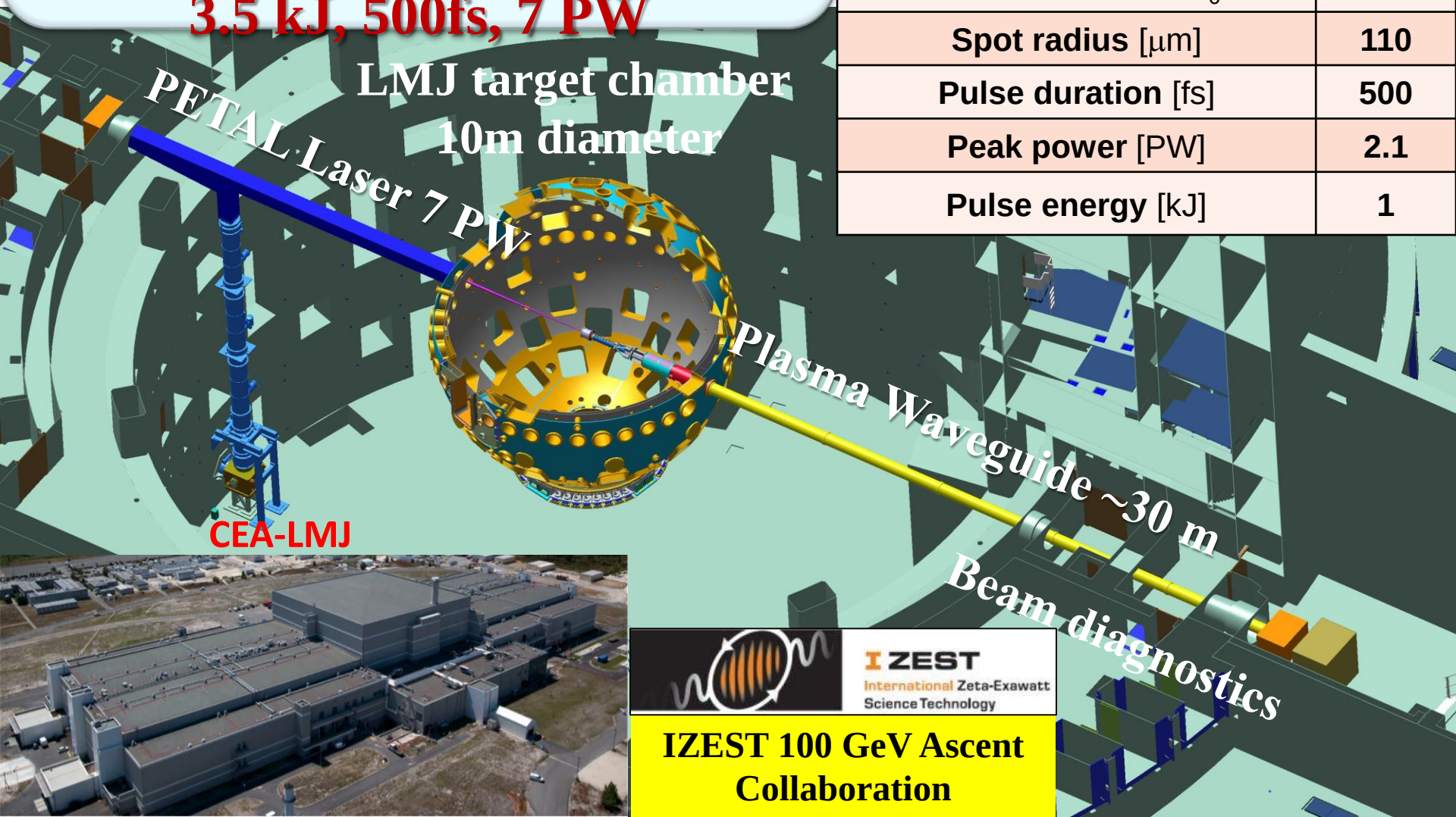
IZEST 100 GeV Ascent Plan

K. Nakajima
at CEA-Bordeaux

PETAL laser

3.5 kJ, 500fs, 7 PW

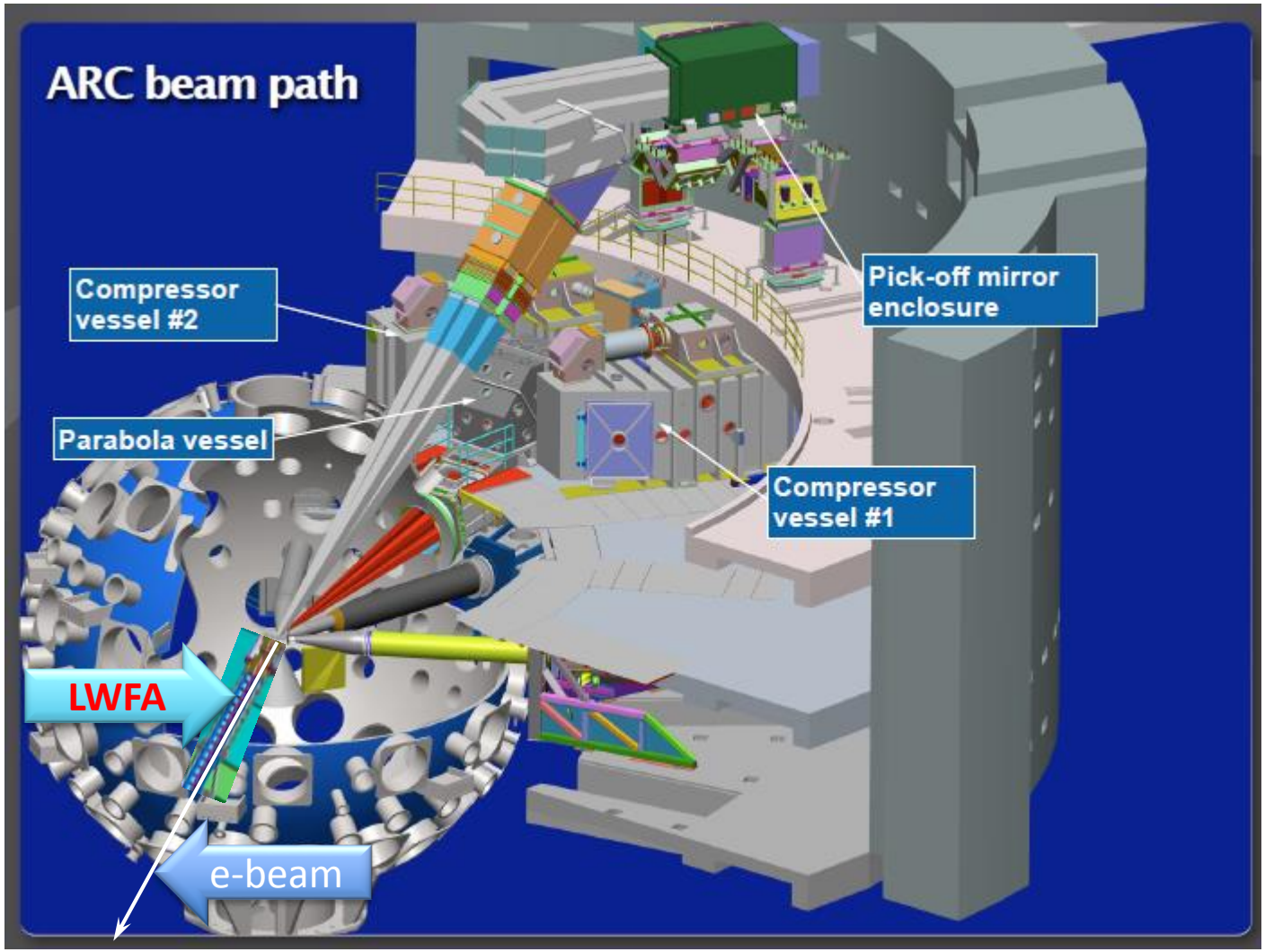
Experiment parameters	
Energy gain [GeV]	100
Plasma density [10^{15} cm^{-3}]	12
Accelerator length [m]	12
Normalized field a_0	3
Spot radius [μm]	110
Pulse duration [fs]	500
Peak power [PW]	2.1
Pulse energy [kJ]	1



IZEST
International Zeta-Exawatt Science Technology

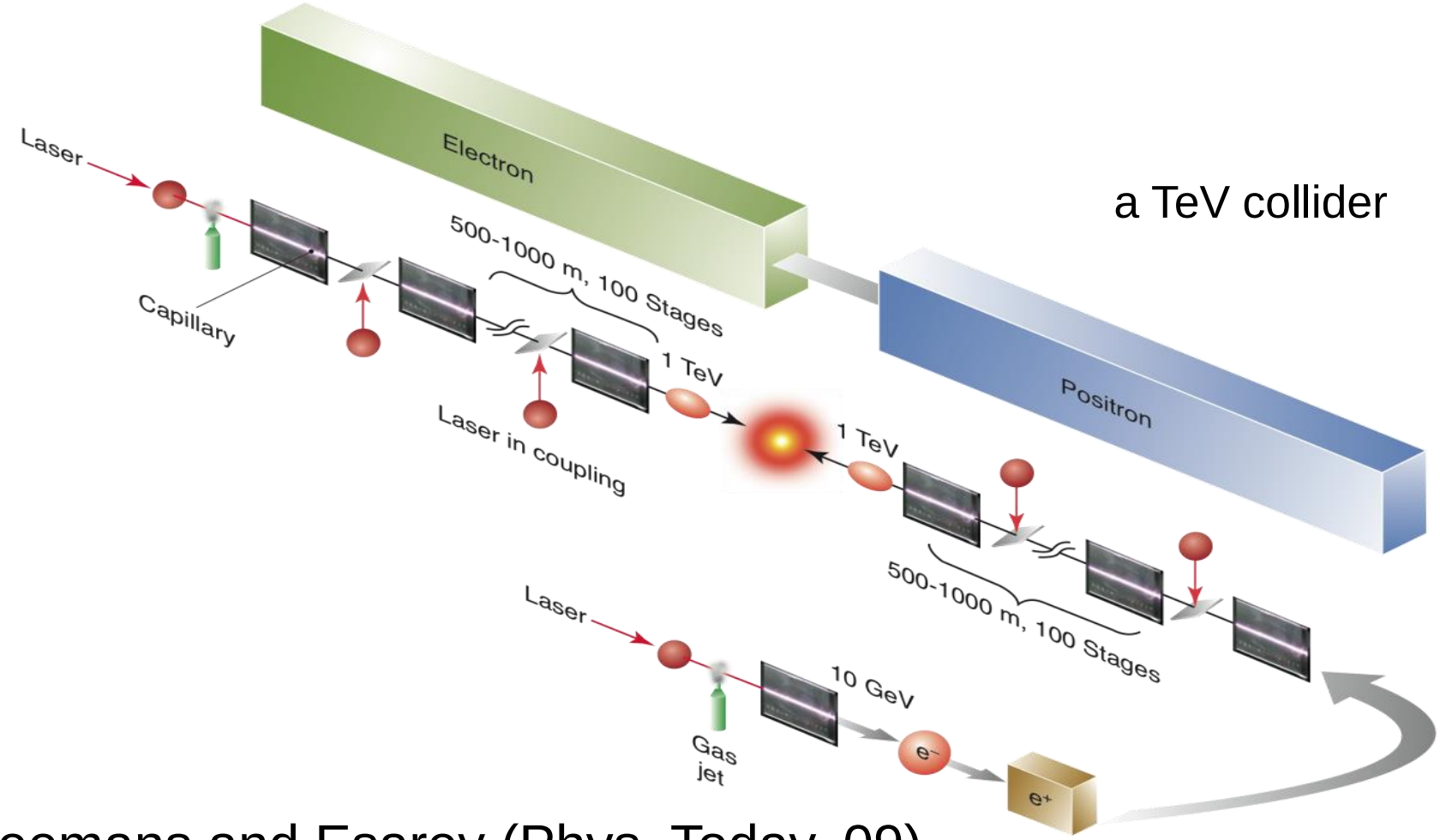
IZEST 100 GeV Ascent Collaboration

100 GeV UV LWFA experiment at ARC



by courtesy of C.P.J. Barty

Laser driven collider concept



a TeV collider

Leemans and Esarey (Phys. Today, 09)

ICFA-ICUIL Joint Task Force on Laser Acceleration(Darmstadt,10)

Density scalings of LWFA for collider

Accelerating field E_z	$\propto n_e^{1/2}$
Focusing constant K	$\propto n_e^{1/2}$
Stage length L_{stage}	$\propto n_e^{-3/2}$
Energy gain per stage W_{stage}	$\propto n_e^{-1}$
Number of stages N_{stage}	$\propto n_e$
Total linac length L_{total}	$\propto n_e^{-1/2}$
Number of particles per bunch N_b	$\propto n_e^{-1/2}$
Laser pulse duration τ_L	$\propto n_e^{-1/2}$
Laser peak power P_L	$\propto n_e^{-1}$
Laser energy per stage U_L	$\propto n_e^{-3/2}$
Radiation loss $\Delta\gamma$	$\propto n_e^{1/2}$
Radiative energy spread σ_γ/γ_f	$\propto n_e^{1/2}$
Initial normalized emittance ε_{n0}	$\propto n_e^{-1/2}$
Collision frequency f_c	$\propto n_e$
Beam power P_b	$\propto n_e^{1/2}$
Average laser power P_{avg}	$\propto n_e^{-1/2}$
Wall plug power P_{wall}	$\propto n_e^{1/2}$

(Nakajima, PR STAB, 2011)

10^{18} /cc (conventional) → 10^{16} /cc

ICFA-ICUIL Joint Task Force
on laser acceleration (Darmstadt, 2010)

W. Leemans, Chair

Case	1 TeV	10 TeV (Scenario I)	10 TeV (Scenario II)
Energy per beam (TeV)	0.5	5	5
Luminosity (10^{34} cm^{-2}s^{-1})	1.2	71.4	71.4
Electrons per bunch ($\times 10^9$)	4	4	1.3
Bunch repetition rate (kHz)	13	17	170
Horizontal emittance $\gamma\varepsilon_x$ (nm-rad)	700	200	200
Vertical emittance $\gamma\varepsilon_y$ (nm-rad)	700	200	200
β* (mm)	0.2	0.2	0.2
Horizontal beam size at IP σ^*_x (nm)	12	2	2
Vertical beam size at IP σ^*_y (nm)	12	2	2
Luminosity enhancement factor	1.04	1.35	1.2
Bunch length σ_z (μm)	1	1	1
Beamstrahlung parameter ϒ	148	8980	2800
Beamstrahlung photons per electron n_γ	1.68	3.67	2.4
Beamstrahlung energy loss δ_E (%)	30.4	48	32
Accelerating gradient (GV/m)	10	10	10
Average beam power (MW)	4.2	54	170
Wall plug to beam efficiency (%)	10	10	10
One linac length (km)	0.1	1.0	0.3

Collider subgroup
List of parameters
(W. Chou)

Table 1
Collider parameters

JTF Report #2

Case	1 TeV	10 TeV (Scenario I)	10 TeV (Scenario II)
Wavelength (μm)	1	1	1
Pulse energy/stage (J)	32	32	1
Pulse length (fs)	56	56	18
Repetition rate (kHz)	13	17	170
Peak power (TW)	240	240	24
Average laser power/stage (MW)	0.42	0.54	0.17
Energy gain/stage (GeV)	10	10	1
Stage length [LPA + in-coupling] (m)	2	2	0.06
Number of stages (one linac)	50	500	5000
Total laser power (MW)	42	540	1700
Total wall power (MW)	84	1080	3400
Laser to beam efficiency (%) [laser to wake 50% + wake to beam 40%]	20	20	20
Wall plug to laser efficiency (%)	50	50	50
Laser spot rms radius (μm)	69	69	22
Laser intensity (W/cm^2)	3×10^{18}	3×10^{18}	3×10^{18}
Laser strength parameter a_0	1.5	1.5	1.5
Plasma density (cm^{-3}), with tapering	10^{17}	10^{17}	10^{18}
Plasma wavelength (μm)	105	105	33

Collider subgroup
List of parameters
(W. Chou)

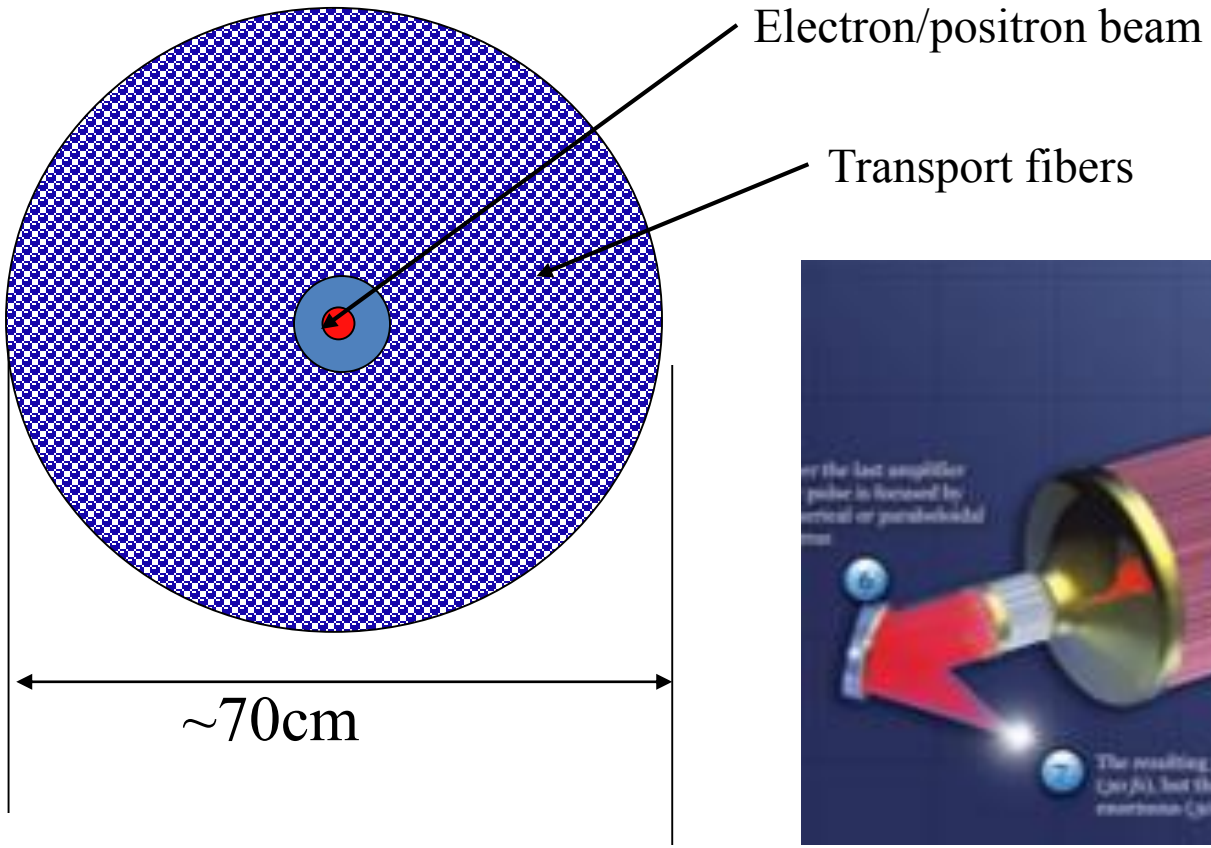
Table 2
Laser parameters

JTF Report #3: Comparison of Choices

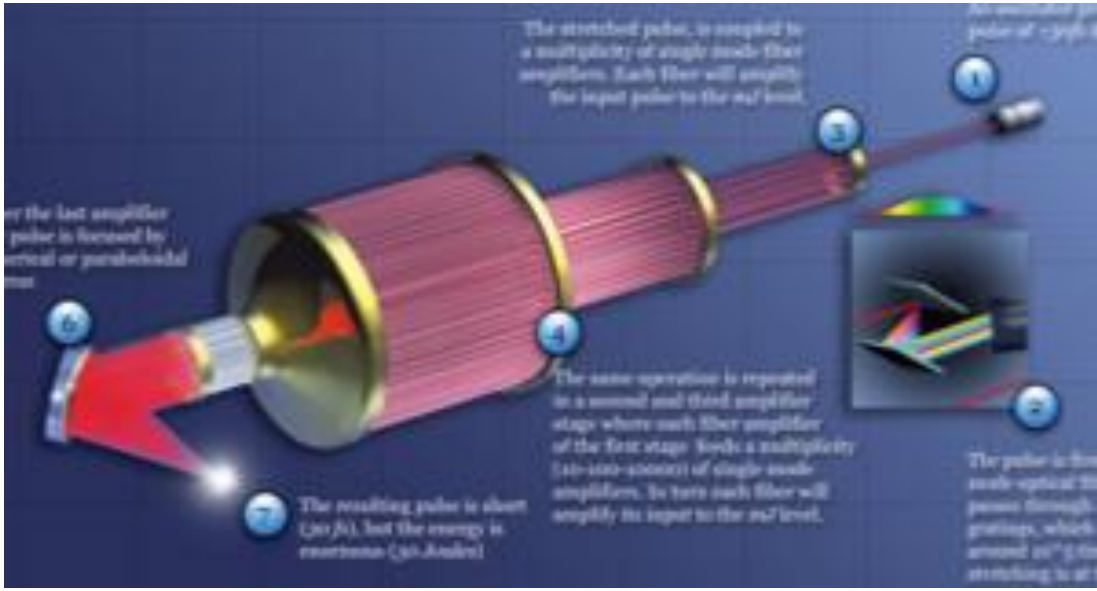
Accelerator	Beam	Beam energy (GeV)	Beam power (MW)	Efficiency AC to beam	Note on AC power
PSI Cyclotron	H+	0.59	1.3	0.18	RF + magnets
SNS Linac	H^-	0.92	1.0	0.07	RF + cryo + cooling
TESLA (23.4 MV/m)	e^+/e^-	250 × 2	23	0.24	RF + cryo + cooling
ILC (31.5 MV/m)	e^+/e^-	250 × 2	21	0.16	RF + cryo + cooling
CLIC	e^+/e^-	1500 × 2	29.4	0.09	RF + cooling
LPA	e^+/e^-	500 × 2	8.4	0.10	Laser + plasma

CAN Laser:

Need to Phase
32 J/1mJ/fiber~ 3×10^4 Phased Fibers!

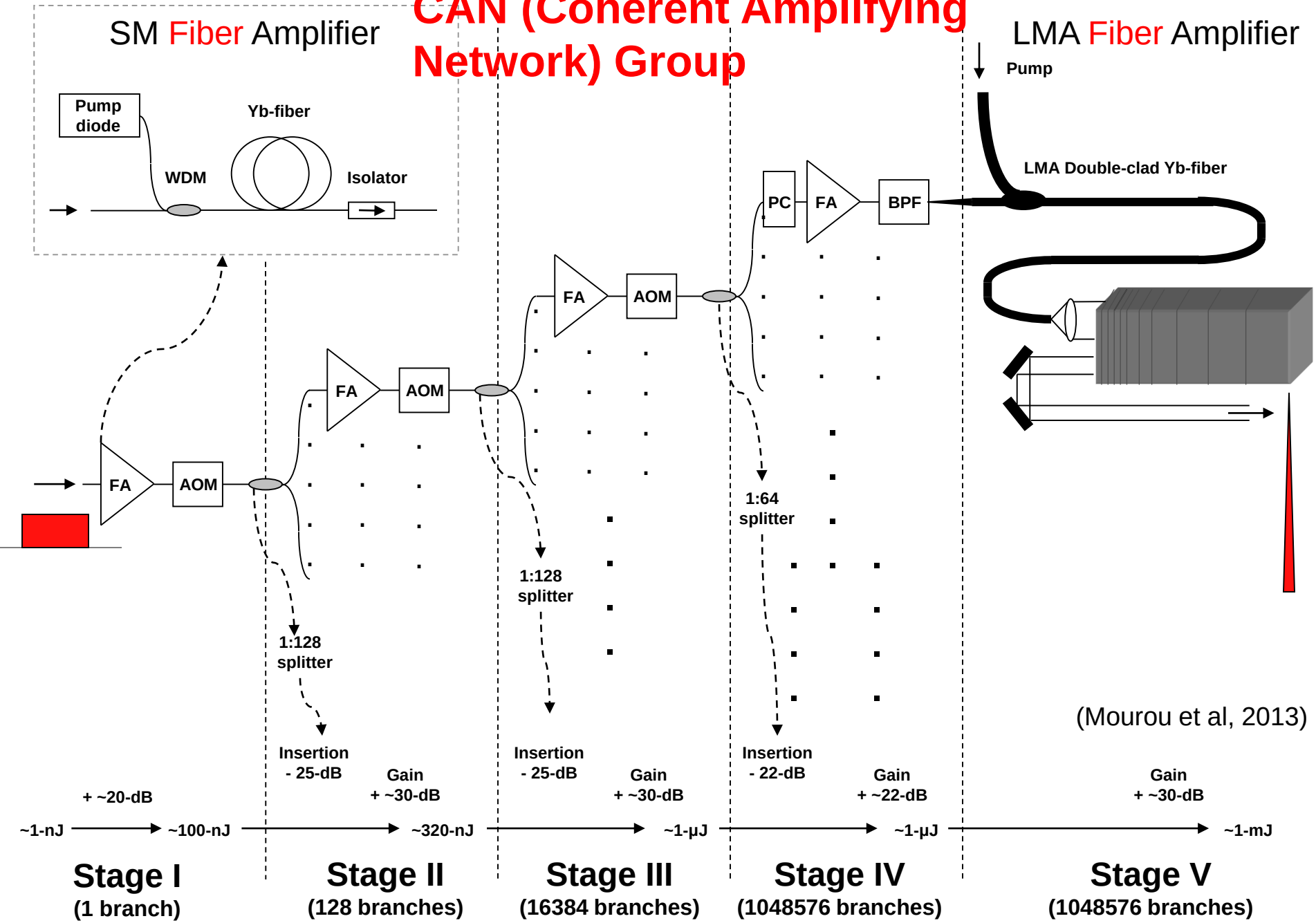


G. Mourou: patent (2009)
Mourou, Brockesby, Tajima, Limpert (2013)



Length of a fiber ~2m Total fiber length~ 5 10^4km

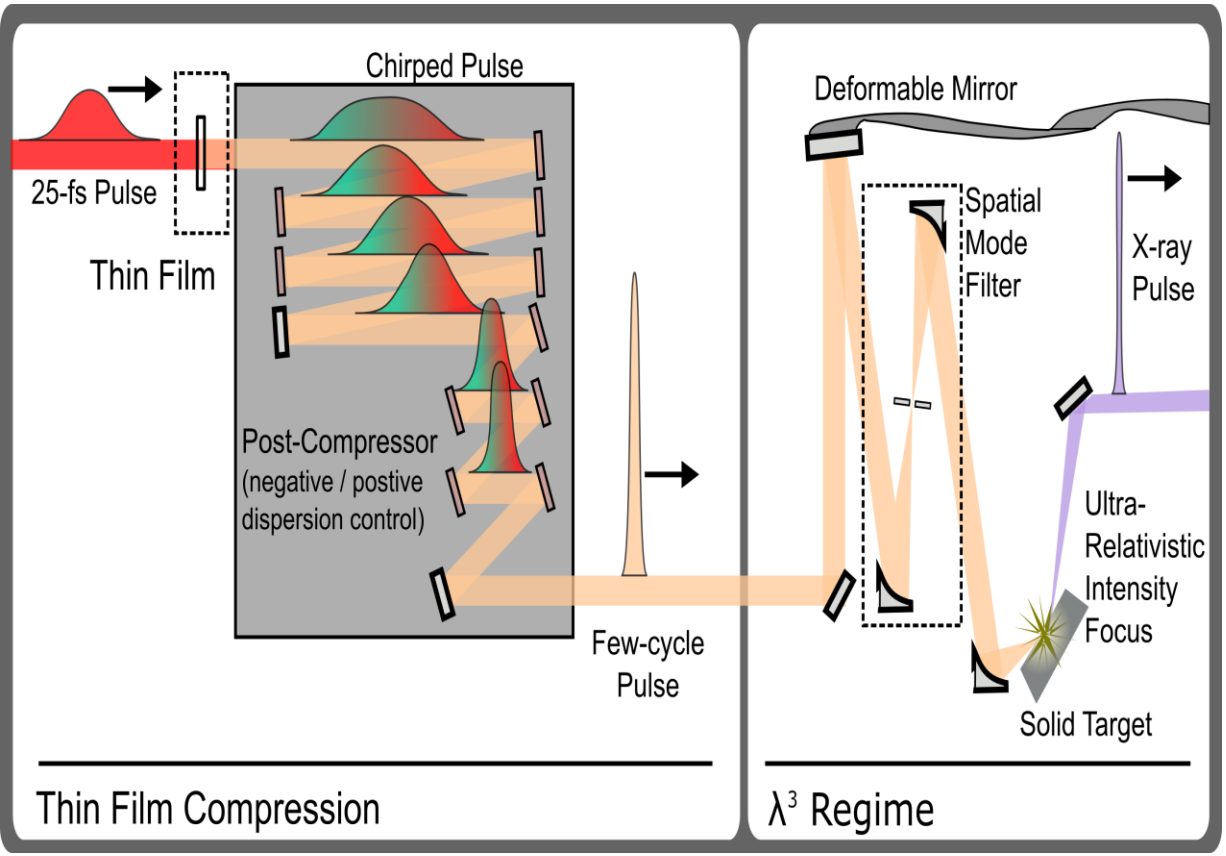
CAN (Coherent Amplifying Network) Group

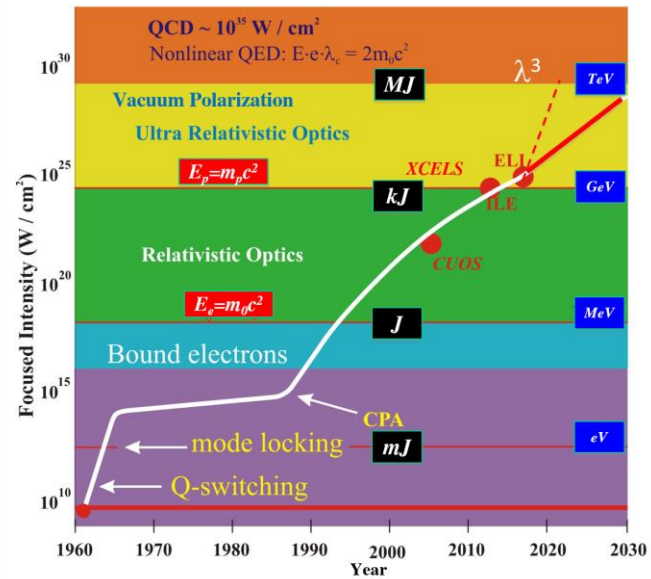


(Mourou et al, 2013)

Single-cycled laser and “TeV on a chip”

Thin film compression and single-cycle optical and X-ray lasers





G. Mourou et al. (2013)

X-ray LWFA in crystal suggested

X-ray Laser Wakefield Accelerator in crystal:

LWFA pump-depletion length:

$$L_{acc} \sim a_X\,(c/\omega_p)\,(\omega_X/\omega_p)^2, \qquad (a_X = eE_X/mc\omega_X)$$

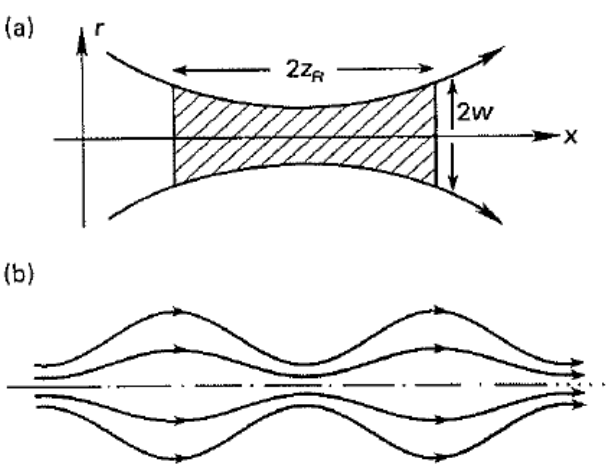
LWFA energy gain

$$\varepsilon_X = 2a_X^2\, mc^2 (n_{cr}/n_e),$$

Here, $n_{cr} = 10^{29}$, $n_e = 10^{23}$, $a_X \sim 30$ (pancake laser pulse with the Schwinger intensity, with focal radius assumed the same as optical laser radius. Could be greater if we further focus by optics, or nonlinearity, or if we not limit the intensity at Schwinger. see below)

The vacuum self-focus power threshold

$$P_{cr} = (45/14)\, c\, E_S^2\, \lambda^2\, \alpha^{-1}, \qquad (E_S: \text{Schwinger field})$$



Schwinger fiber acceleration in vacuum:

(no surface, no breakdown)

Vacuum photon dispersion relation with focus

$$\omega = c\,\sqrt{(k_z^2 + \langle k_{perp}^2 \rangle)},$$

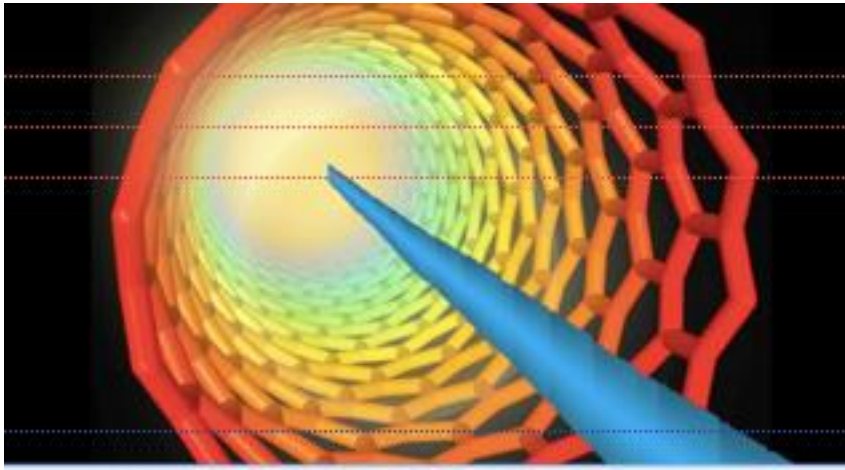
The vacuum dispersion relation with fiber self-modulation

$$\omega / (k_z + k_s) = c, \qquad (k_s = 2\pi / s)$$

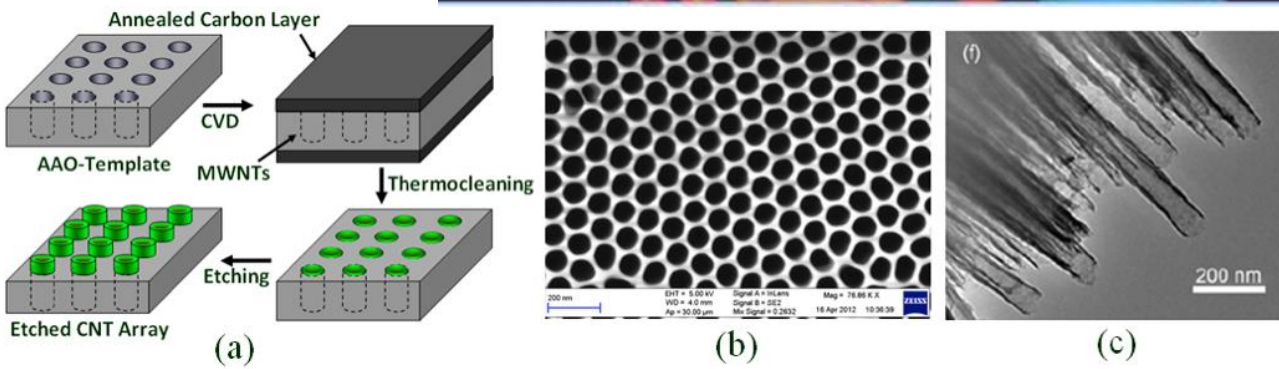
(Tajima and Cavenago, PRL, 1987)

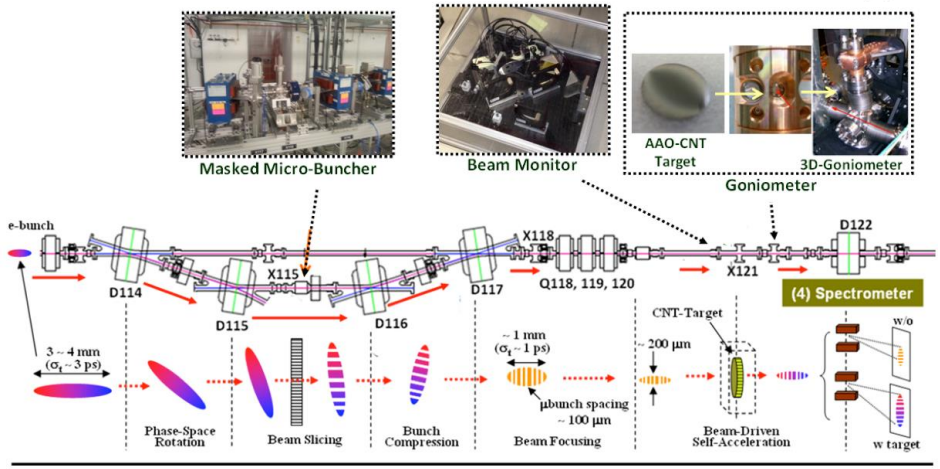
Wakefield acceleration in porous nanomaterials

Carbon nanotube with
Particle beam / X-ray pulse



Porous nanomaterial





Collaboration (2015) with Fermilab / NIU
Y. Shin et al.

Earlier works of X-ray crystal acceleration

-X-ray optics and fields (Tajima et al. PRL,1987)

-**Nanocrystal hole** for particle propagation (Newberger, Tajima, et al. 1989, AAC; PR,..)

-particle transport in the crystal (Tajima et al. 1990, PA)

APPLICATION OF NOVEL MATERIAL IN CRYSTAL ACCELERATOR CONCEPTS

B. Newberger, T. Tajima, The University of Texas at Austin, Austin, Texas 78712
F. R. Huson, W. Mackay, Texas Accelerator Center, The Woodlands, Texas
B. C. Covington, J. R. Payne, Z. G. Zou, Sam Houston State University, Huntsville, Texas
N. K. Mahale, S. Ohnuma, University of Houston, Houston, Texas 77004

; which incorporate regular macroscopic features
on the underlying crystal lattice are of potential
ne application to crystal accelerators and coherent
urces. We have recently begun an investigation of
aterial, porous Si, in which pores of radii up to a
attice spacings are etched through finite volumes
rystal. The potential reduction of losses to parti-
anneled along the pores makes this a very inter-
ial in crystal accelerators for relativistic, positively
icles. Our results on material properties which are
this context will be presented. The consequences
ransport will be discussed.

and $k = v_0/m_I c^2$, v_0, is the "spring constant of th
channel well. Its specific form depends on the mo
construct the continuum potential of a string of aton
purposes it suffices to take a typical value of 2×10^1
is the multiple scattering velocity space "diffusion"
We have used[10]

$$D = z\pi r_e^2 N Z_{\mathrm{val}} \left(\frac{m_e}{m_I}\right)^2 L_R,$$

where r_E is the classical electron radius, Z_{val} is t
of valence electrons, and N is the number density
tal. Logarithmic dependencies on particle energy
neglected throughout; L_R is a constant with a ty

Particle Accelerators, 1990, Vol. 32, pp. 235–240
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BEAM TRANSPORT IN THE CRYSTAL X-RAY ACCELERATOR

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Abstract A Fokker-Planck model of charged particle transport in crystal channels which includes the effect of strong accelerating gradients has been developed[1] for application to

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Crystal X-Ray Accelerator

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(Received 18 November 1986)

An ultimate linac structure is realized by an appropriate crystal lattice (superlattice) that serves as a "soft" irised waveguide for x rays. High-energy ($\simeq$40 keV) x rays are injected into the crystal at the Bragg angle to cause Bormann anomalous transmission, yielding slow-wave accelerating fields. Particles (e.g., muons) are channeled along the crystal axis.

PACS numbers: 52.75.Di, 41.80.−y, 61.80.Mk

An approach to the attainment of ever higher energies by extrapolating the linac to higher accelerating fields, higher frequencies, and finer structures is prompted by several considerations, including the luminosity requirement which demands the radius of the colliding-beam spot be proportionately small at high energies: $a_0 = \pi^{-1/2}\hbar c(fN)^{-1/2}P\epsilon^{-2}$, where f, N, P, and ϵ are the duty cycle, total number of events, beam power, and beam energy, respectively. This approach, however, encounters a physical barrier when the photon energy becomes of the order $\hbar\omega = \hbar\omega_p \simeq mc^2\alpha^2 \simeq 30$ eV (α = the fine-structure constant), corresponding to wavelength (scale length) $\lambda \simeq 500$ Å. The metallic wall begins to absorb the photon strongly, where ω_p is the plasma frequency corresponding to the crystal electron density. In addition, since the wall becomes not perfectly conducting for $\hbar\omega \gtrsim mc^2\alpha^2$, the longitudinal component of fields becomes small and the photon goes almost straight into the wall (a soft-wall regime). As the photon energy $\hbar\omega$ much exceeds $mc^2\alpha^2$ and becomes $\gtrsim mc^2\alpha$, however, the metal now ceases to be opaque. The mean free path of the photon is given by Bethe-Bloch theory as $l_i = (3/2^8\pi) \times a_B^{-2}\alpha^{-1}n^{-1}(\hbar\omega/Z_{\mathrm{eff}}^2\mathcal{R})^{7/2}$, where a_B is the Bohr radius, n the electron density, Z_{eff} the effective charge of the lattice ion, and $\mathcal{R}$ the Rydberg energy.

In the present concept the photon energy is taken at the hard x-ray range of $\hbar\omega = mc^2\alpha$ and the linac structure is replaced by a crystal structure, e.g., silicon or GaAs-AlAs. (A similar bold endeavor was apparently undertaken by Hofstadter already in 1968.[1]) Here the crystal axis provides the channel through which accelerated particles propagate with minimum scattering (channeling[2]) and the x rays are transmitted via the Bormann effect (anomalous transmission[3,4]) when the x rays (wavelength λ) are injected in the xz plane with a

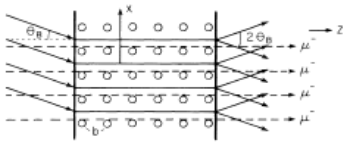
where b is the transverse lattice constant and later a the longitudinal lattice constant ($a \simeq b$) (see Fig. 1). The row of lattice ions (perhaps with inner-shell electrons) constitutes the "waveguide" wall for x rays, while they also act as periodic irises to generate slow waves. A superlattice[5] such as $Ge_cSi_{1-c}S_i$ (in which the relative concentration c ranges from 0 to 1 over 100 Å or longer in the longitudinal z direction) brings in an additional freedom in the crystal structure and provides a small Brillouin wave number $k_s = 2\pi/s$ with s being the periodicity length. We demand that the x-ray light in the crystal channel walls becomes a slow wave and satisfies the high-energy acceleration condition

$$\omega/(k_z + k_s) = c, \tag{2}$$

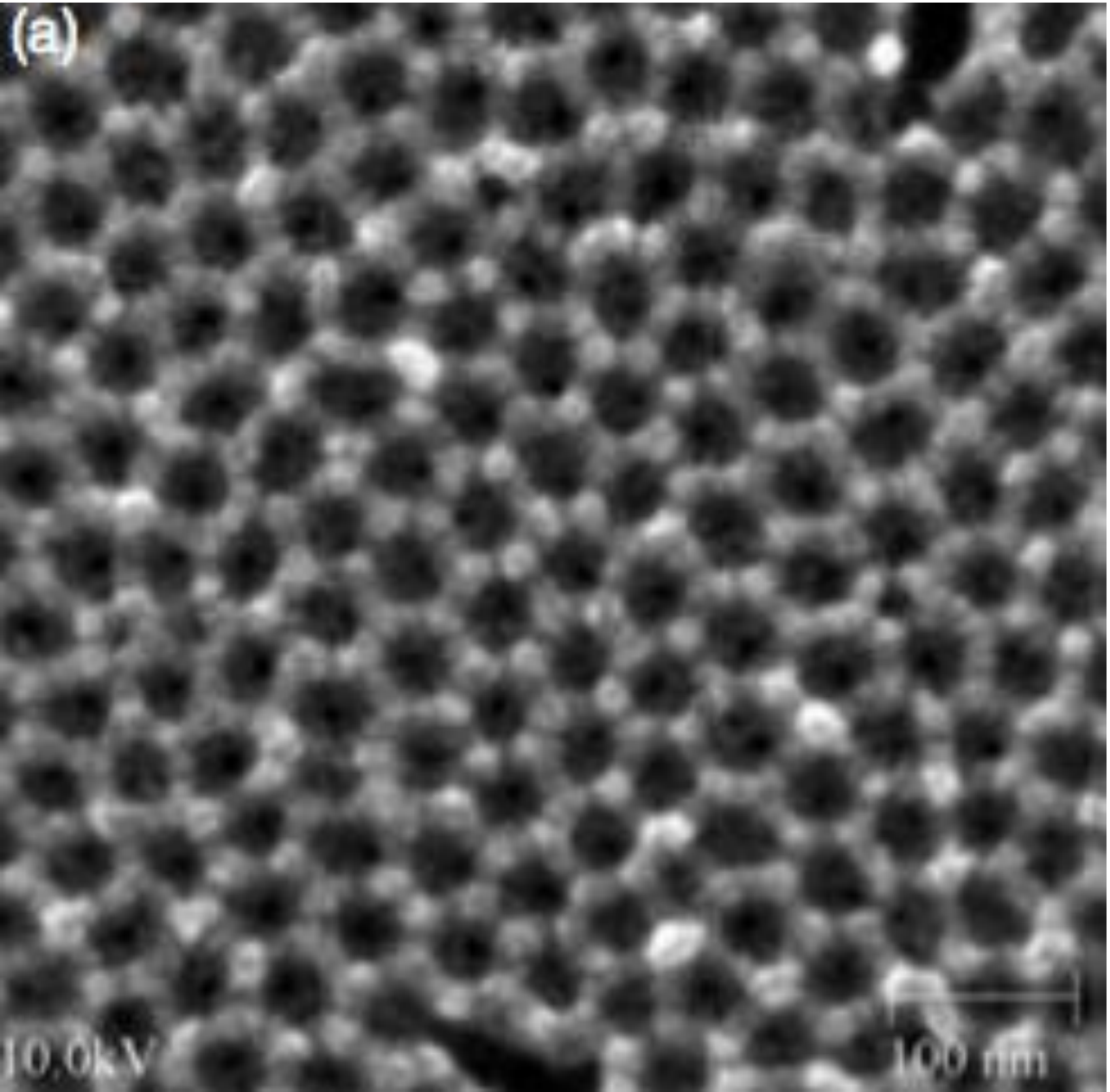
where ω and k_z are the light frequency and longitudinal wave number.

The energy loss of moving particles in matter is due to ionization, bremsstrahlung, and nuclear collisions. We can show[6] that a channeled high-energy particle moving fast in the z direction oscillates in the xy plane according to the Hamiltonian

$$H = \frac{1}{2m}(p_x^2 + p_y^2) + V(x,y), \tag{3}$$

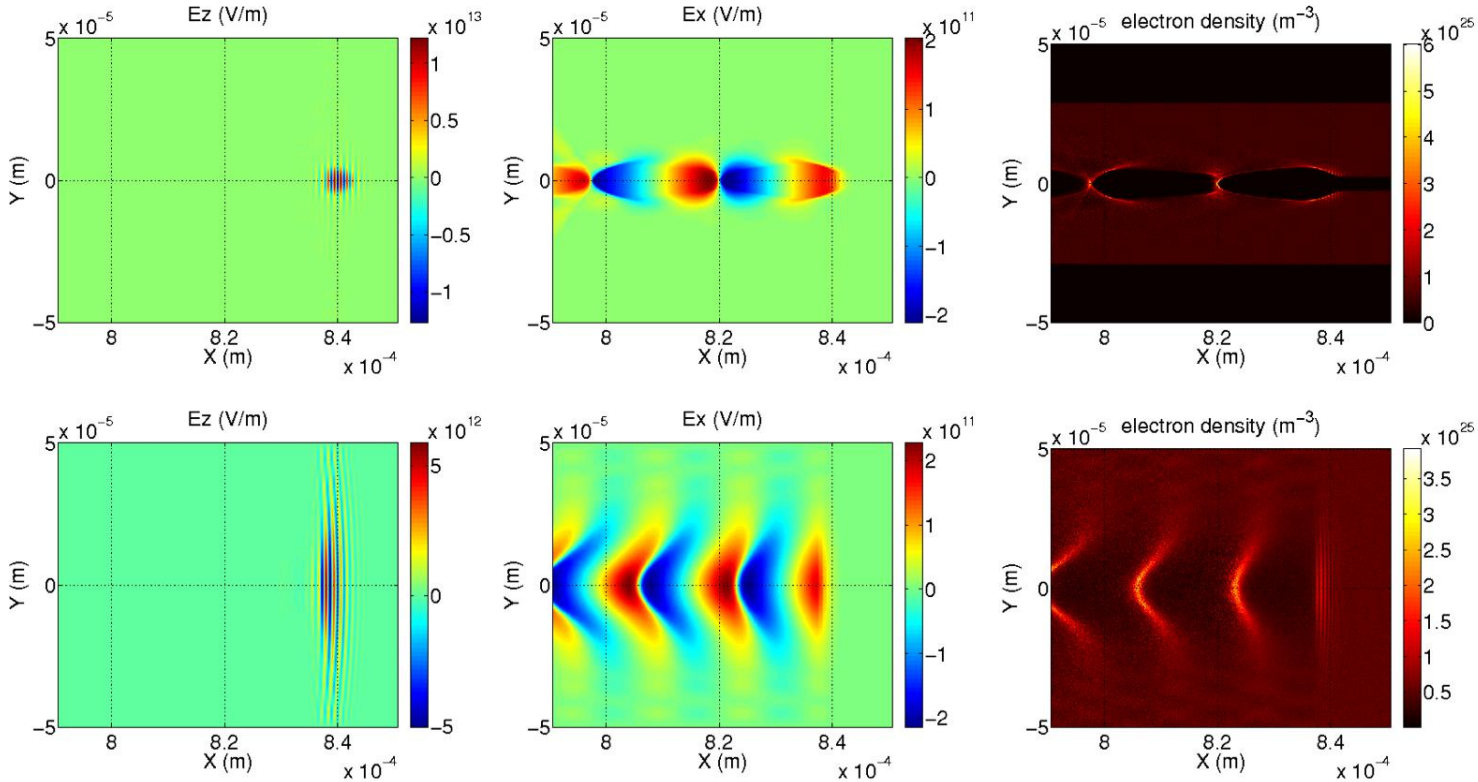


Porous Nanomaterial



Porous alimina on Si substrate
Nanotech. **15**, 833 (2004)

X-ray LWFA in a tube vs. uniform solid



in nanotube

in uniform solid

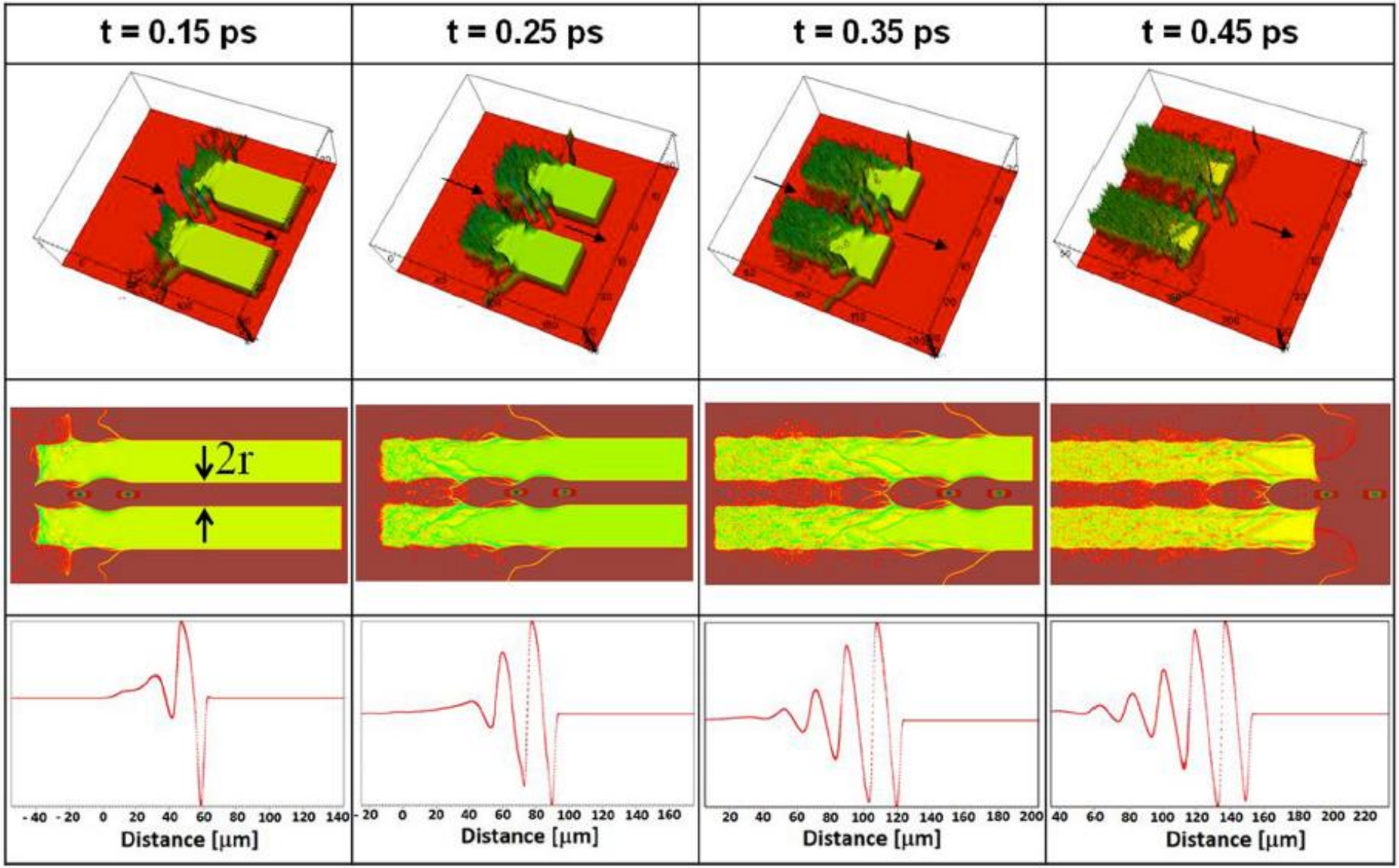
A few-cycled 1keV X-ray pulse (a_0 ~ O(1)), causing 10TeV/m wakefield in the tube

more strongly confined in the tube

cf: uniform solid

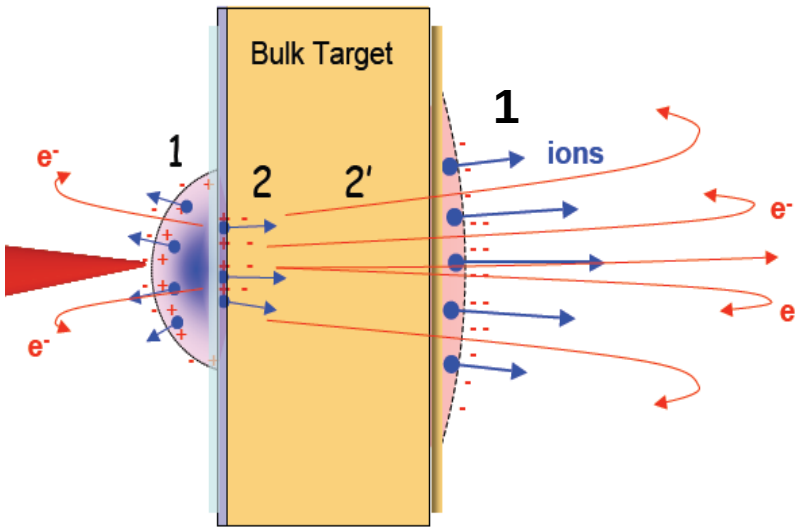
X. Zhang (2016)

Beam-driven wakefield on a chip



Y. Shin (2014)

Laser-driven ion acceleration mechanisms

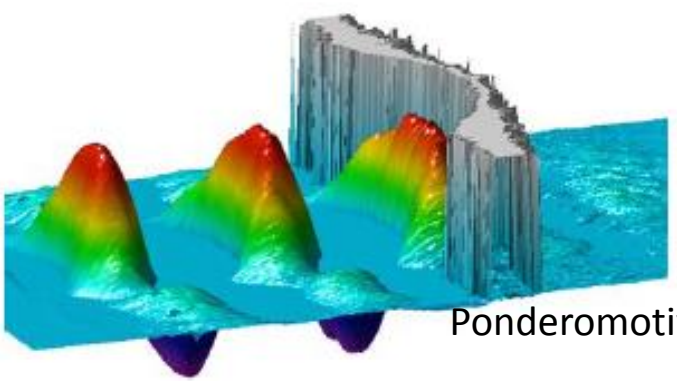


***E*~TV/m**

1)TNSA

micron thick targets

incoherent process



Ponderomotive acceleration

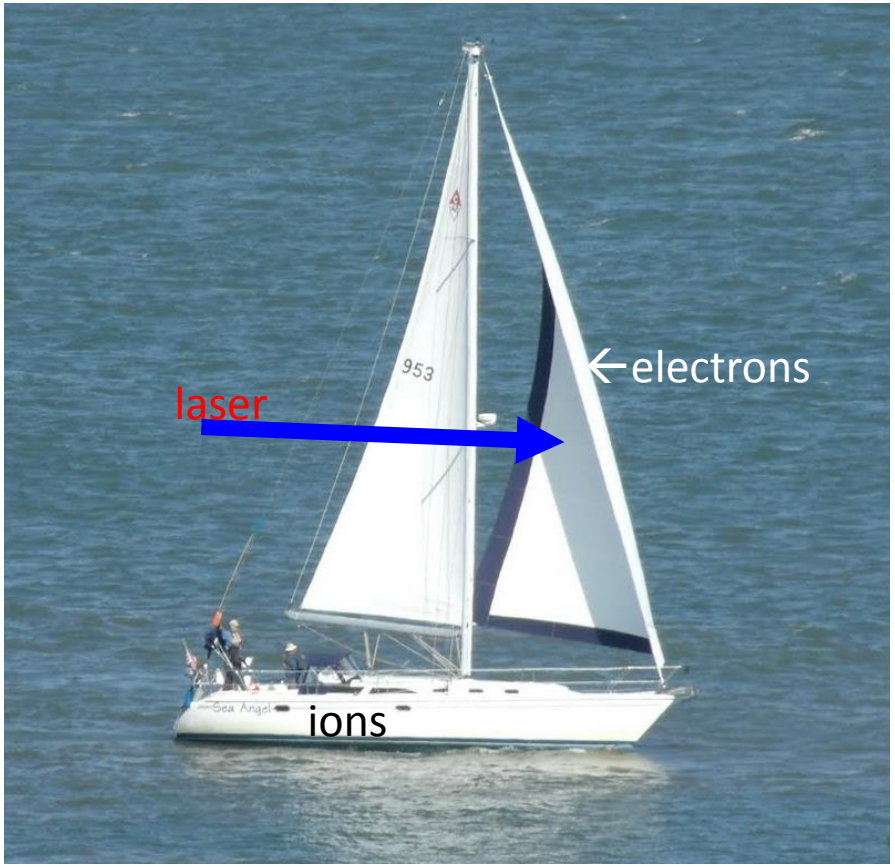
2)RPA

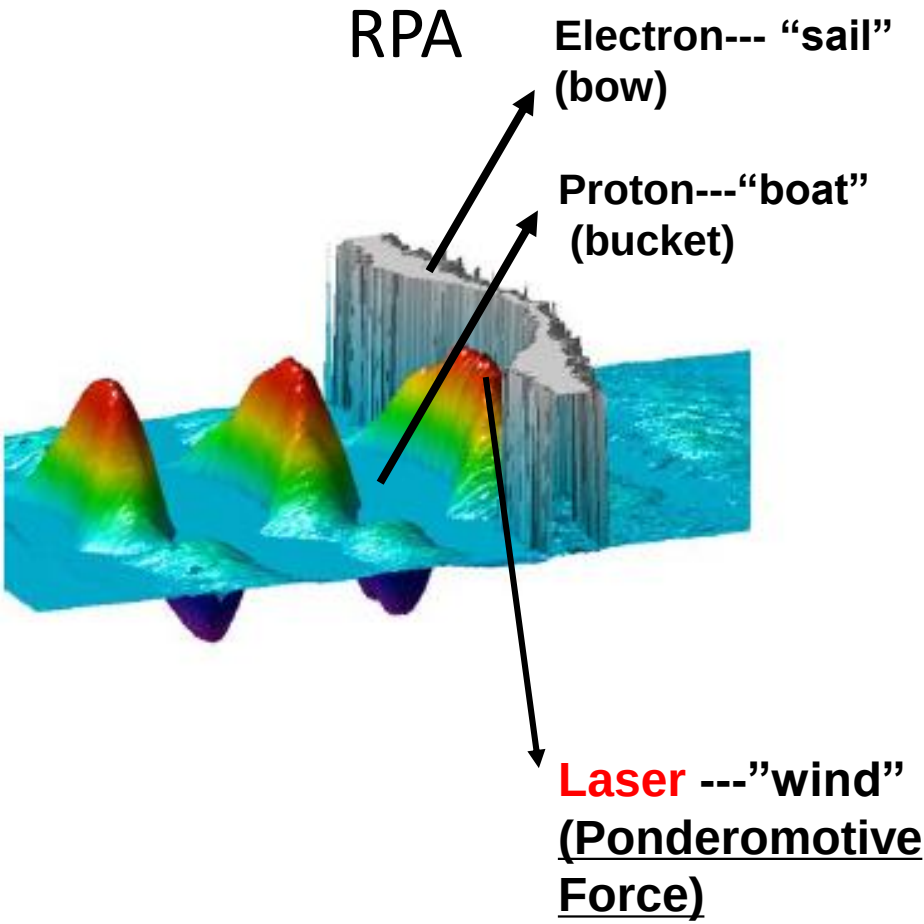
nanotargets

can be coherent

X. Q. Yan (2010)

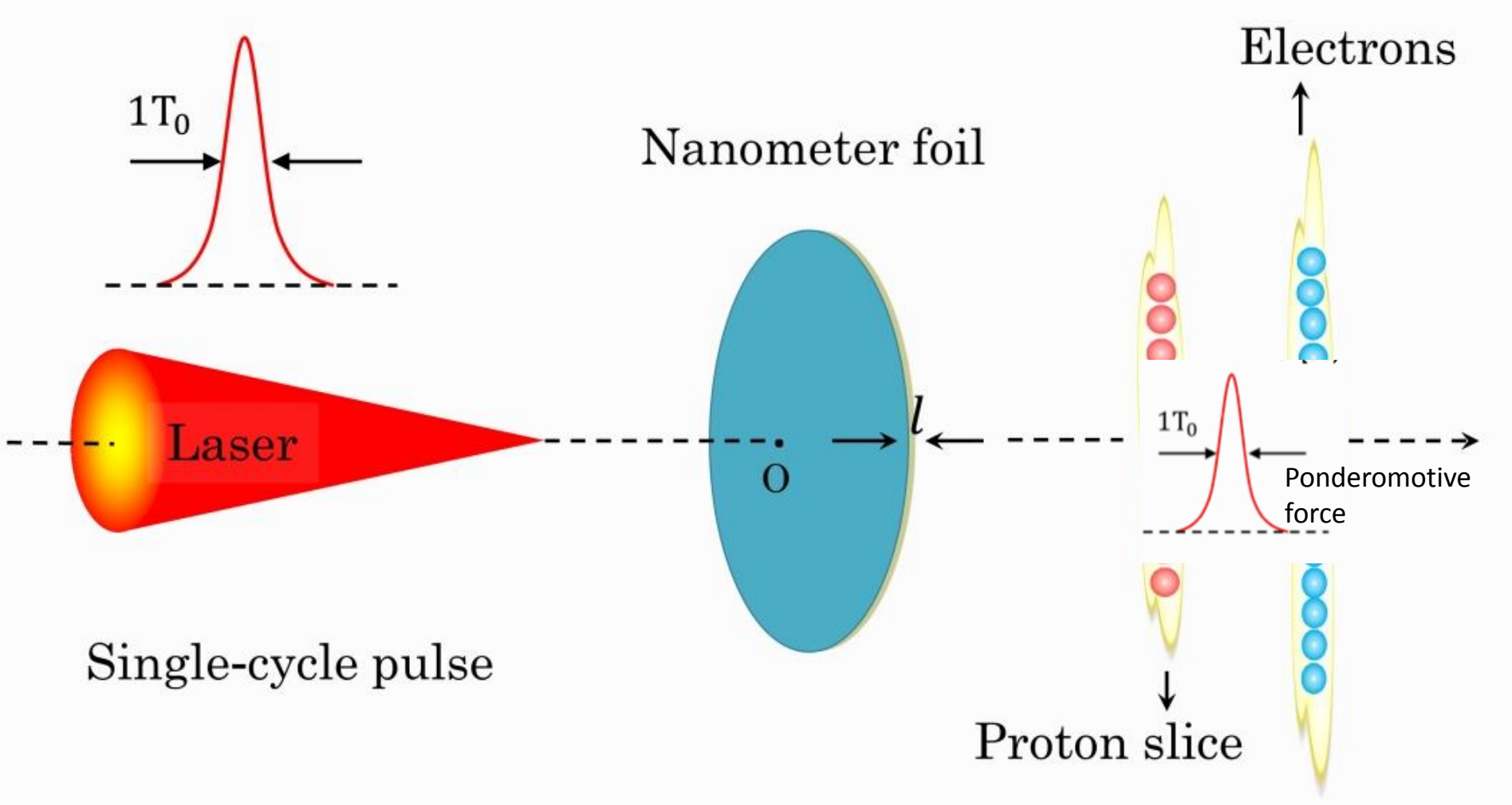
RPA (Radiation Pressure Acceleration)





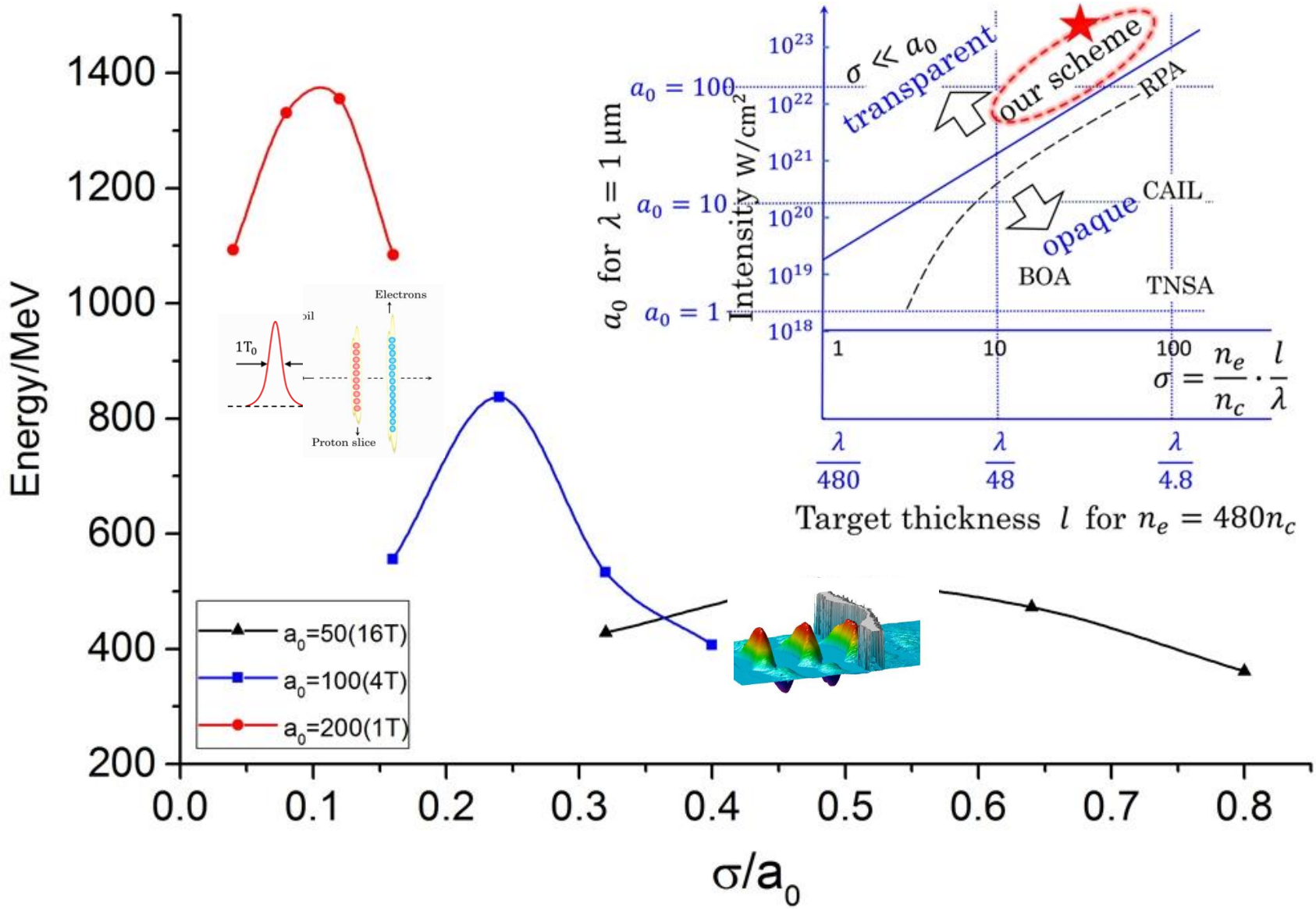
Esirkepov et al. (2004)
X. Yan (2010)

single-cycle pulse ion acceleration regime



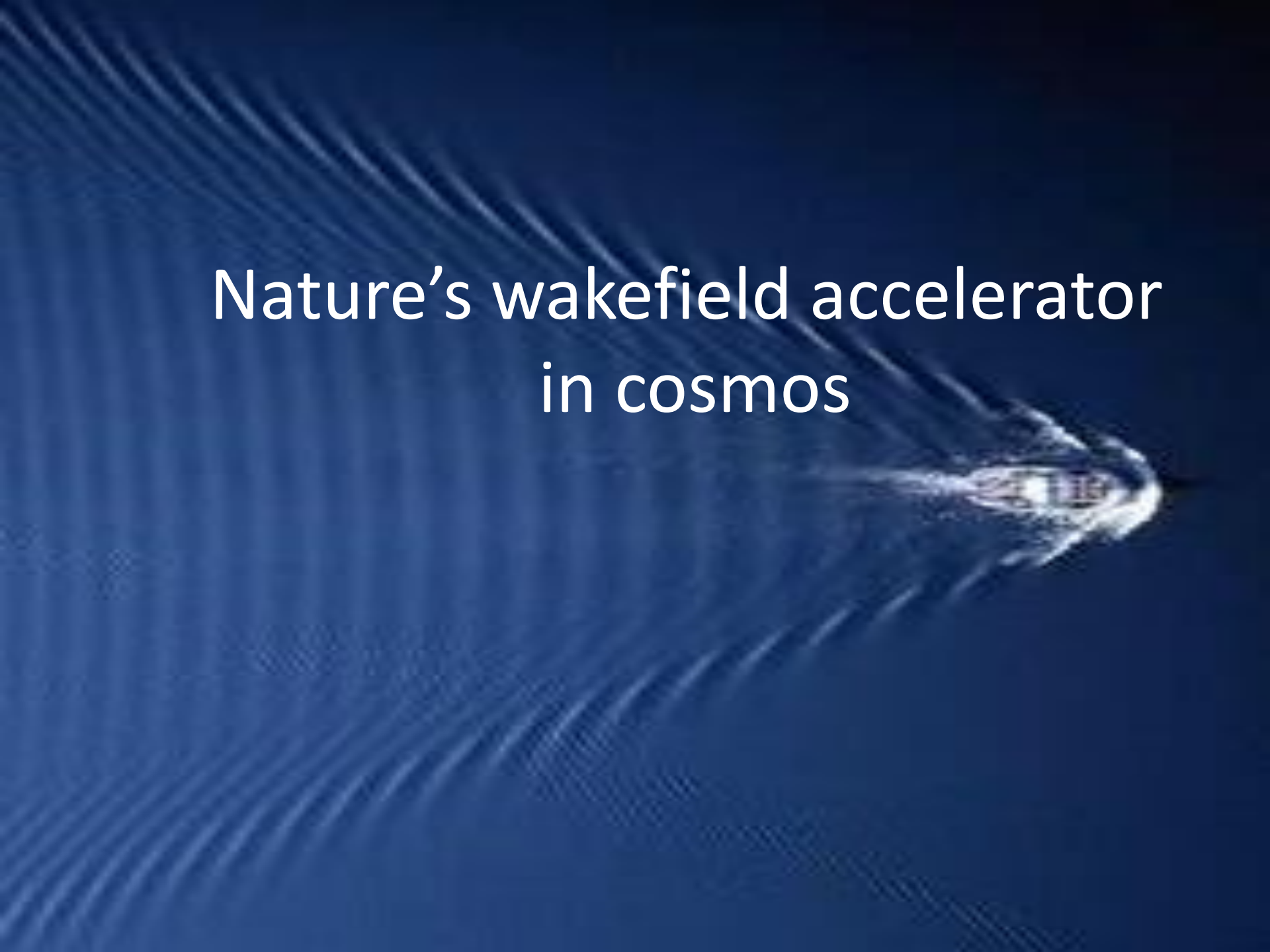
M. Zhou (2016)

Laser-driven ion acceleration: TNSA, RPA and our regime



M.Zhou, X.Yan, T. Tajima, and G.Mourou, (2015)

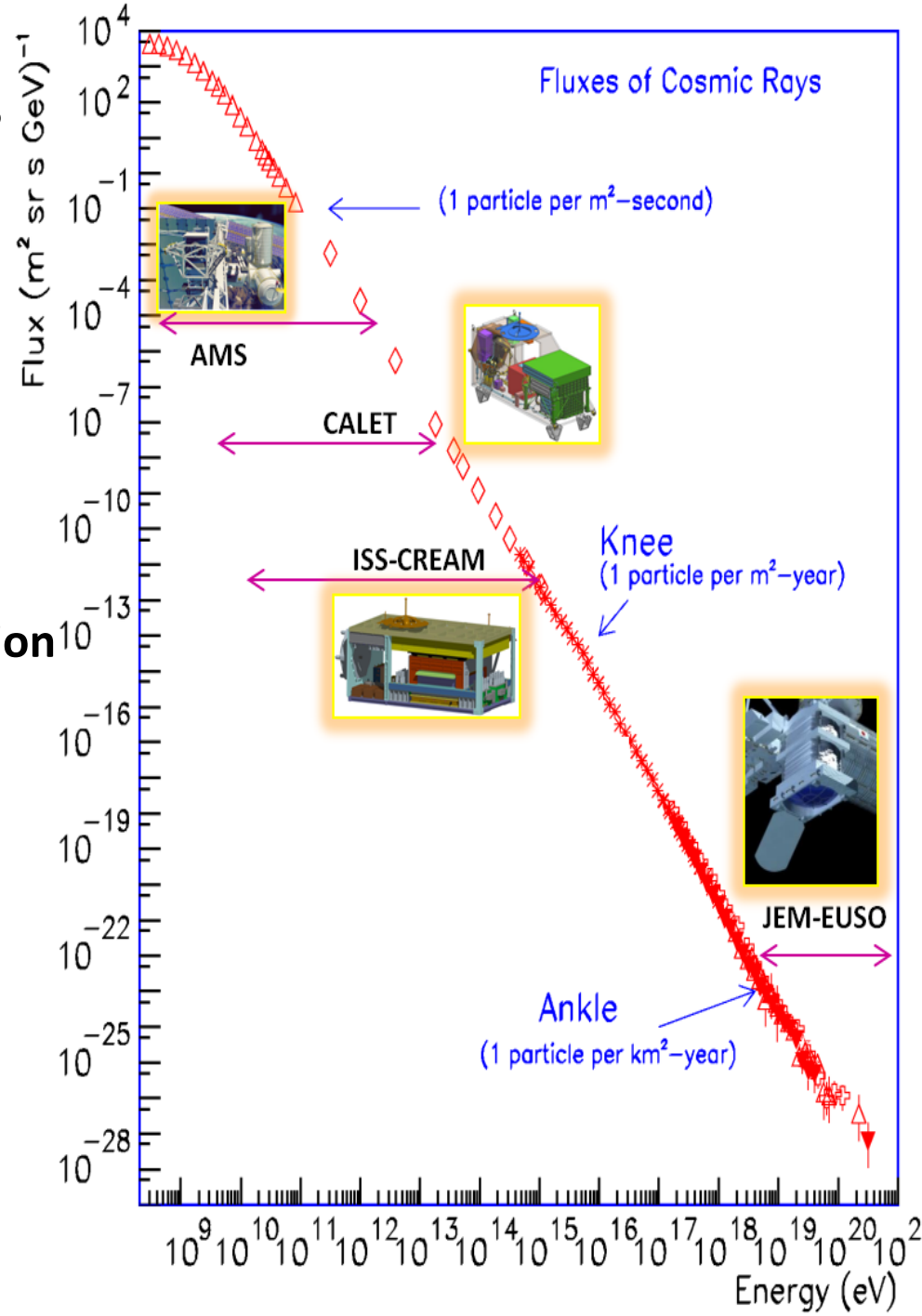
Nature’s wakefield accelerator in cosmos



Ultrahigh Energy Cosmic Rays (UHECR)

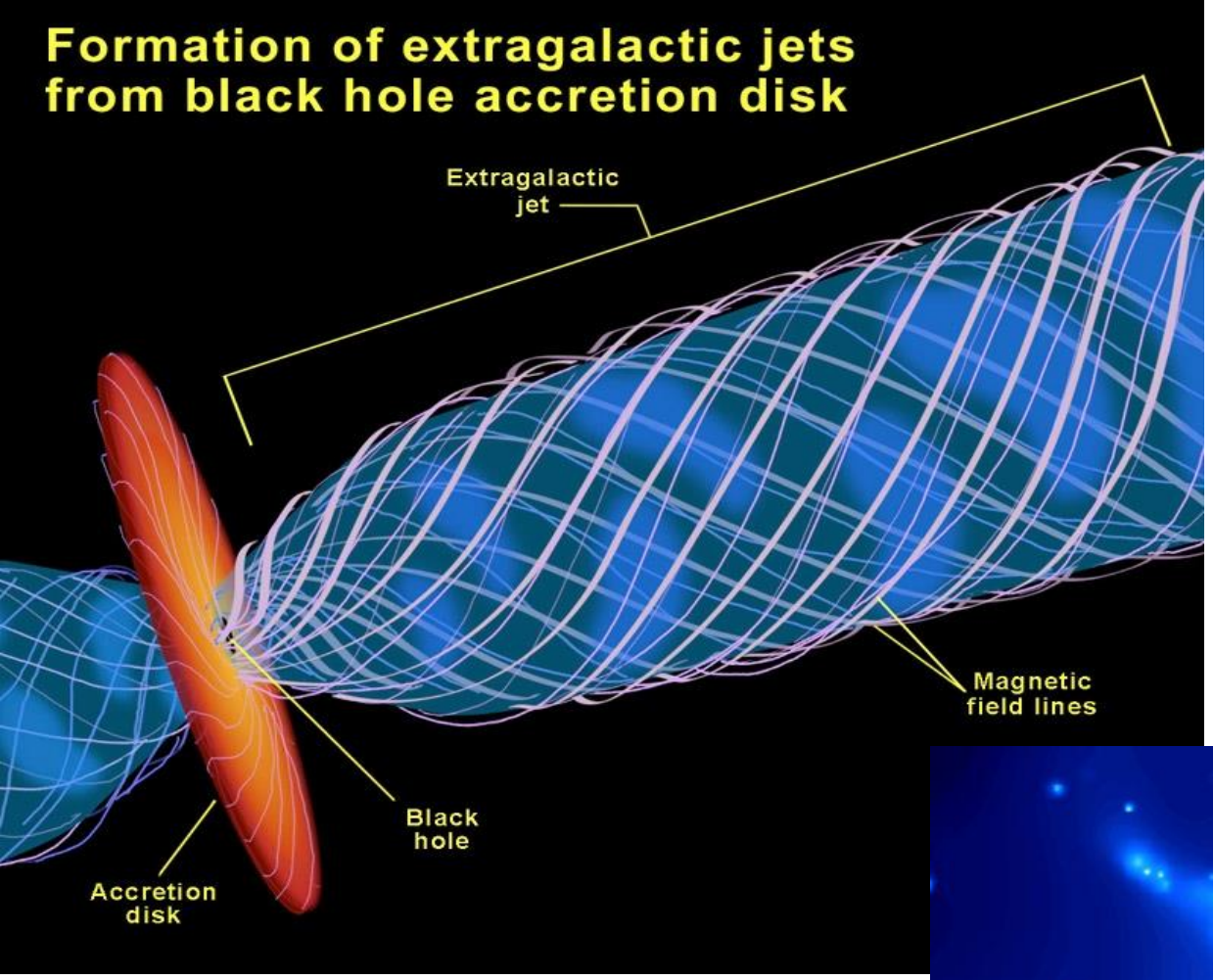
<u>Fermi mechanism</u> runs out of steam
- beyond 10^{19} eV
- due to synchrotron radiation

<u>Wakefield acceleration</u>
- comes in rescue
- prompt, intense, linear acceleration
- small synchrotron radiation
- radiation damping effects?



Cen A

- Distance : 3.4Mpc
- Radio Galaxy
  - Nearest
  - Brightest radio source
- Elliptical Galaxy
- Black hole at the center w/ relativistic jets



Fermi's **'Stochastic Acceleration'**
(large synchrotron radiation loss)

↓

Coherent wakefield acceleration
(no limitation of the energy)

Nature's LWFA : Blazar jets

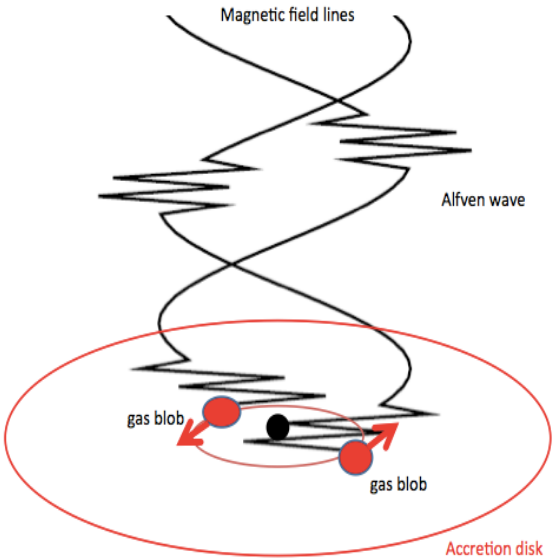
extreme high energy cosmic rays (~10^{21} eV)

episodic γ-ray bursts observed

consistent with LWFA theory

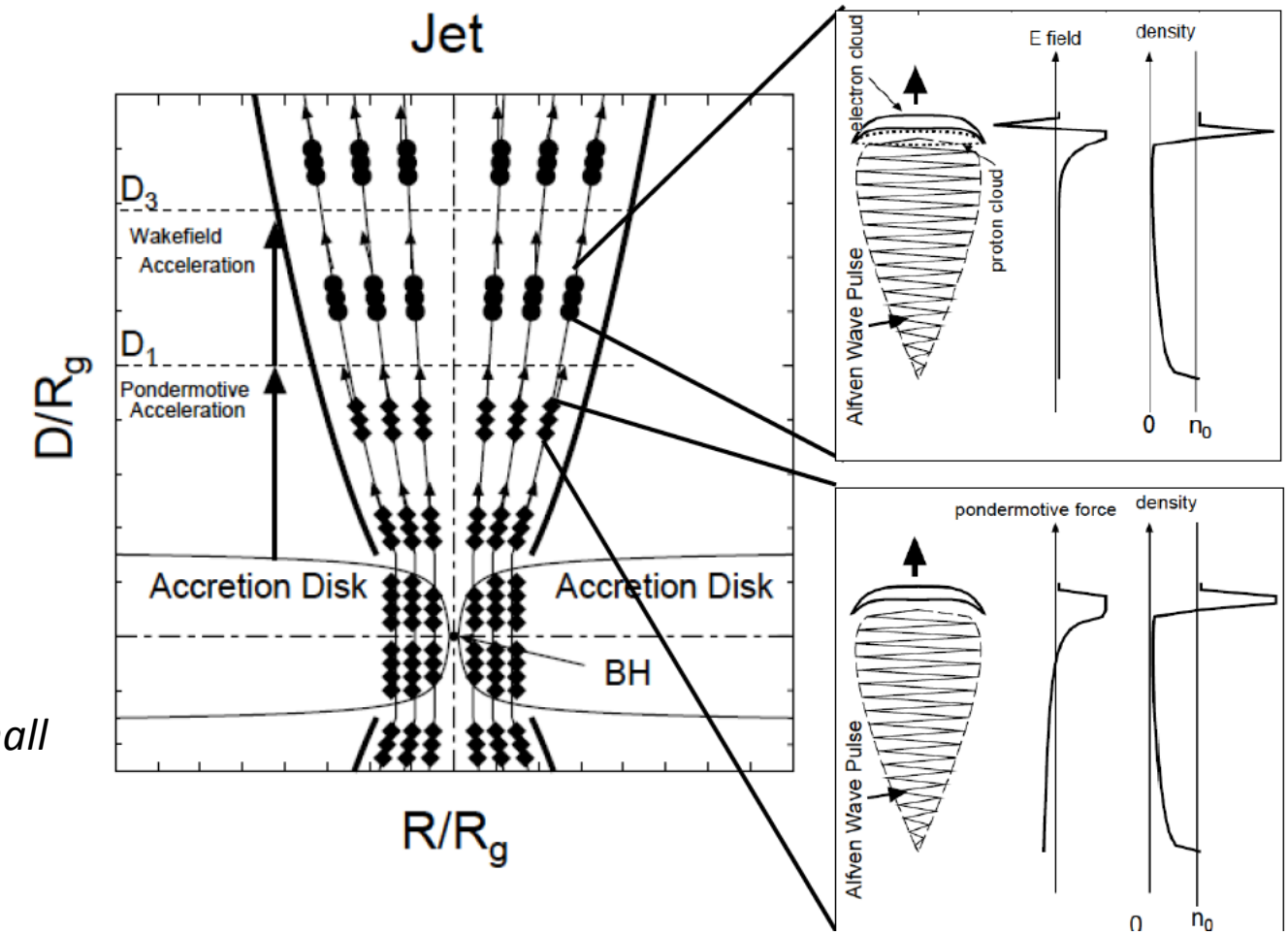
Ebisuzaki-Tajima (2014)

Astrophysical wakefield acceleration: Superintense Alfven Shock in the Blackhole Accretion Disk toward ZeV Cosmic Rays ($a_0 \sim 10^6$ -10^{10}, large spatial scale)



$a_0 = eE_0 / mc\omega_0 >> 1$

E_0: modest
ω_0 : extremely small



Ebisuzaki and Tajima, Astropart. Phys.(2014)

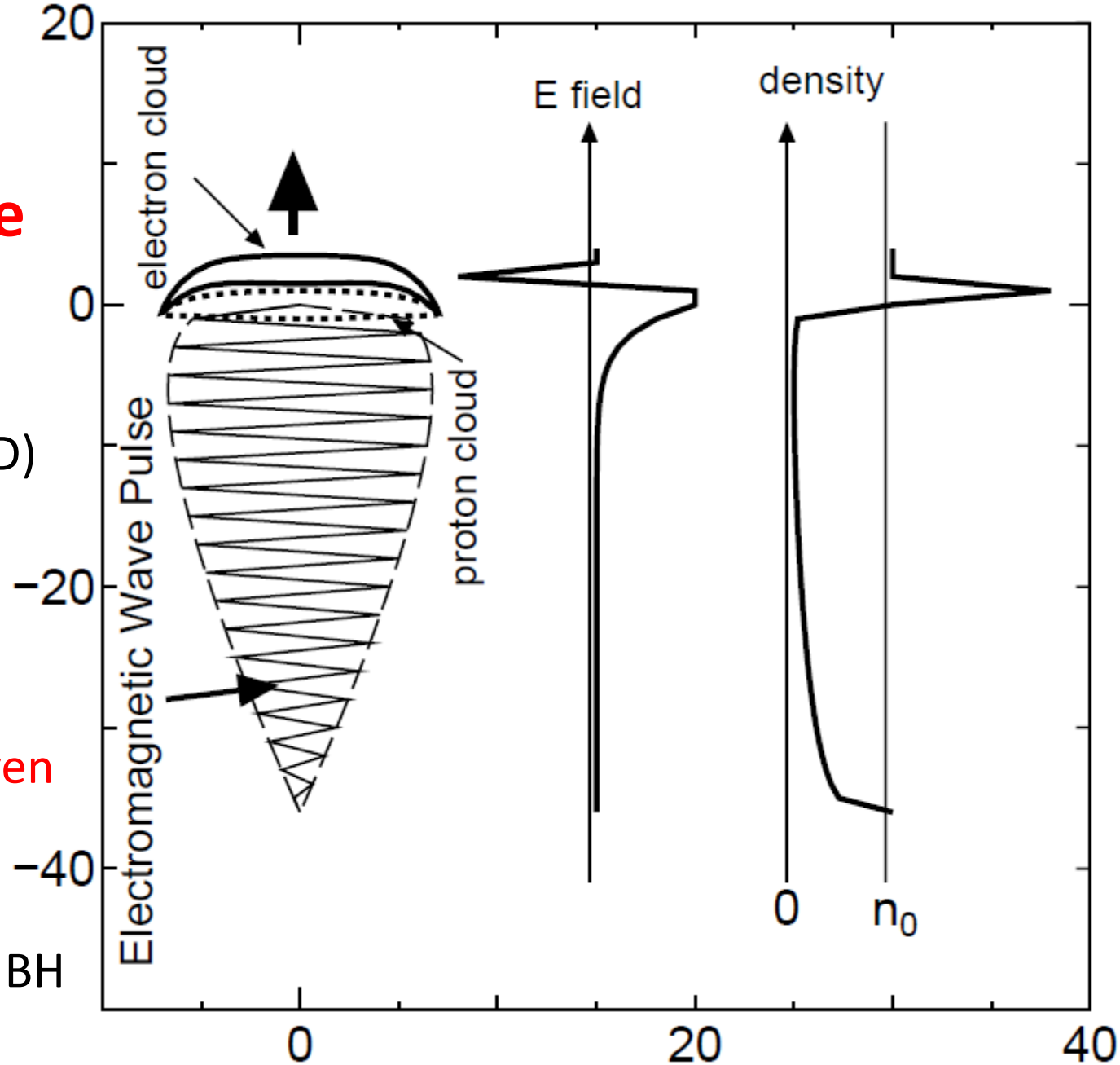
Phys.Rev. STAB, **18**, 024401 (2015).

Wakefield vs. Ponderomotive Acceleration

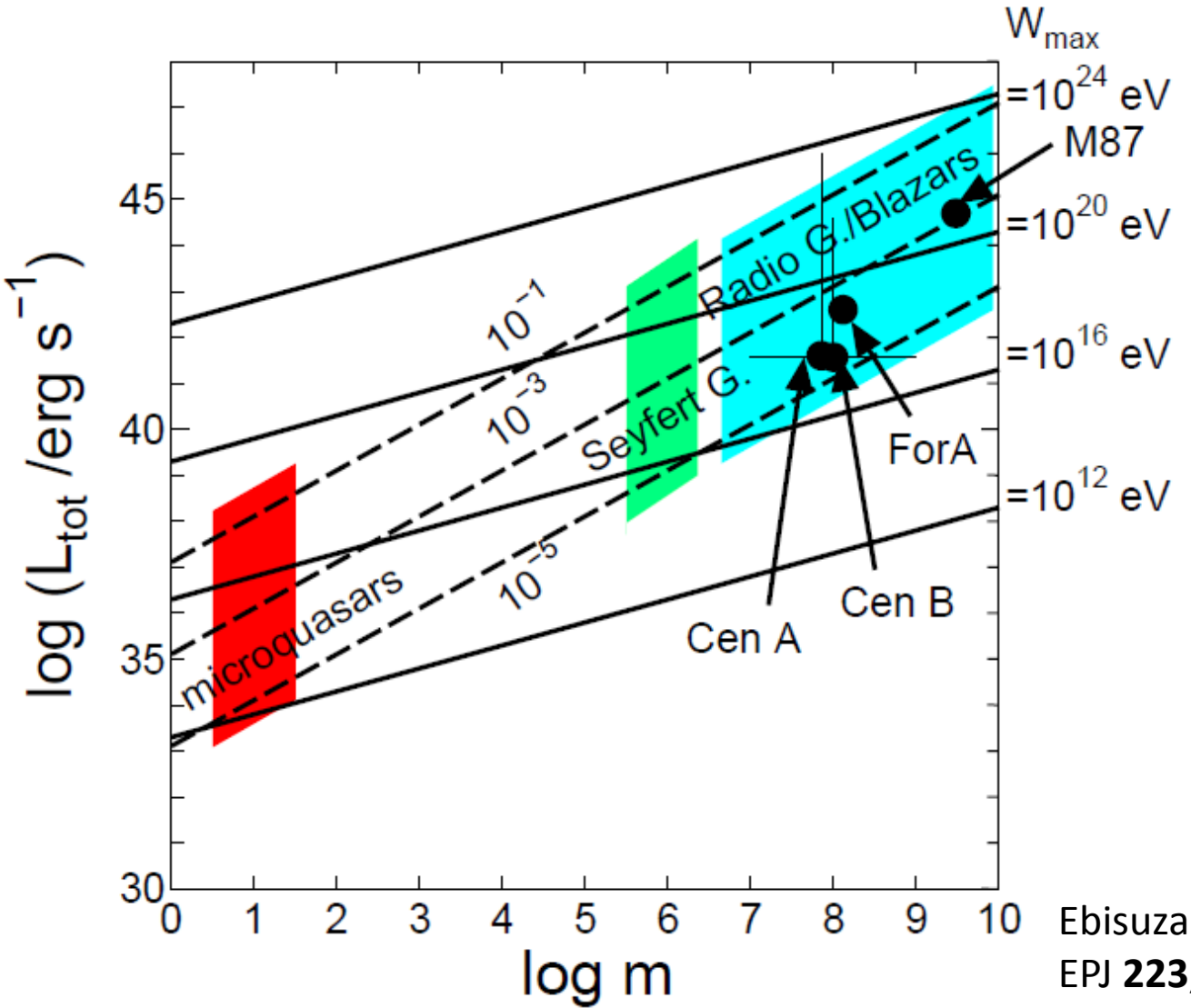
wavebreak (1D or 2D)
in higher a_0
→ wakefield
less important

Ponderomotive-driven
Acceleration more
robust (a_0>>1)

a_0 ~ $10^{6\text{-}10}$ in AGN BH



Comic ray acceleration and γ-ray emission: Summary



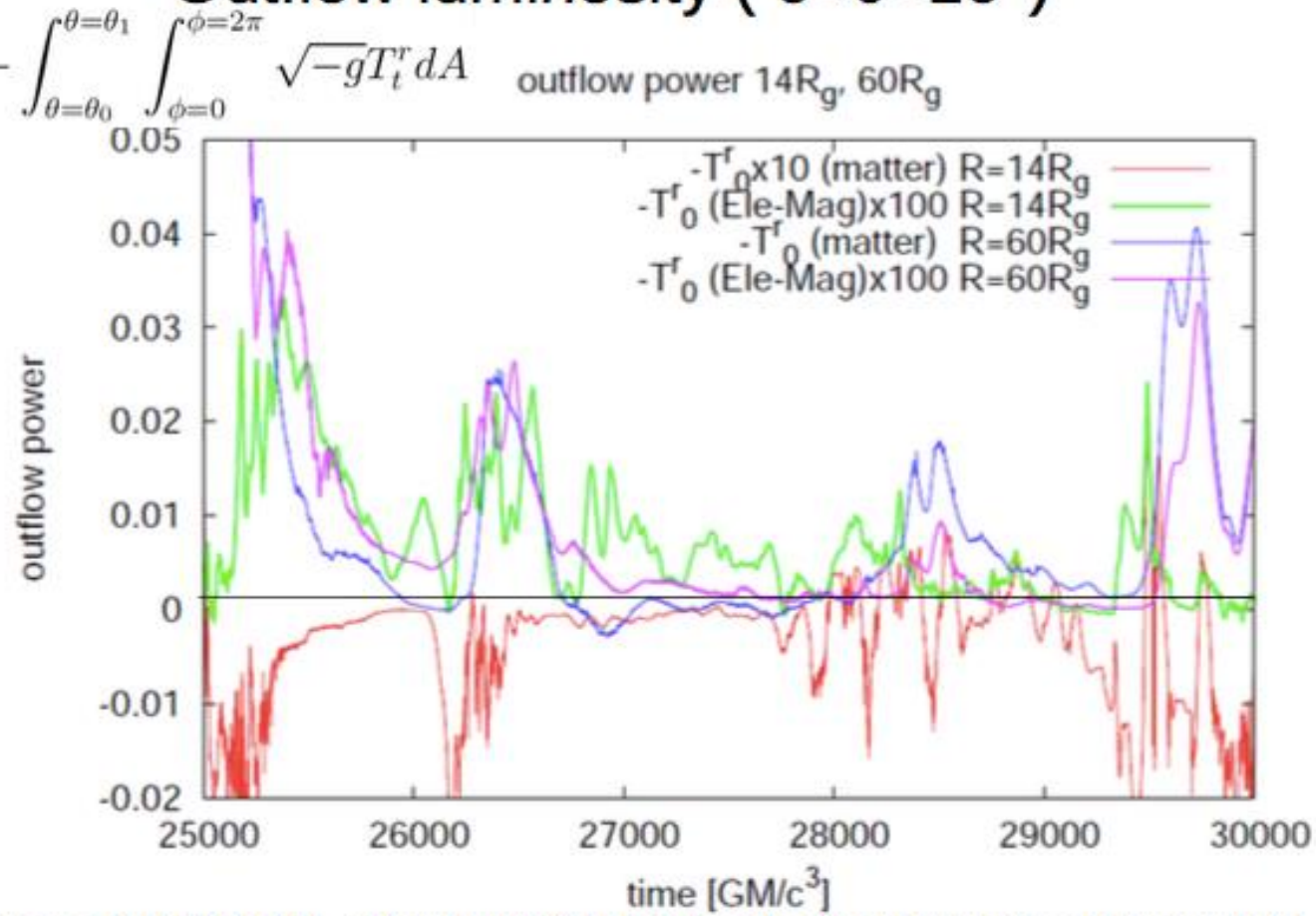
Ebisuzaki, Tajima
EPJ **223**, 1113(2014)

General Relativistic MHD simulation of accretion disk + jets

Outflow luminosity (0<θ<10°)

$$E_{\rm dot} = -\int_{\theta=\theta_0}^{\theta=\theta_1}\int_{\phi=0}^{\phi=2\pi}\sqrt{-g}T^r_t\,dA$$

θ_0=0
θ_1=10



Short time variavilitry (Δt~a few tensGM/c³) in electromagnetic components (green and pink) : Good agreement with Ebisuzaki & Tajima(2014) $t_{var} \sim M$

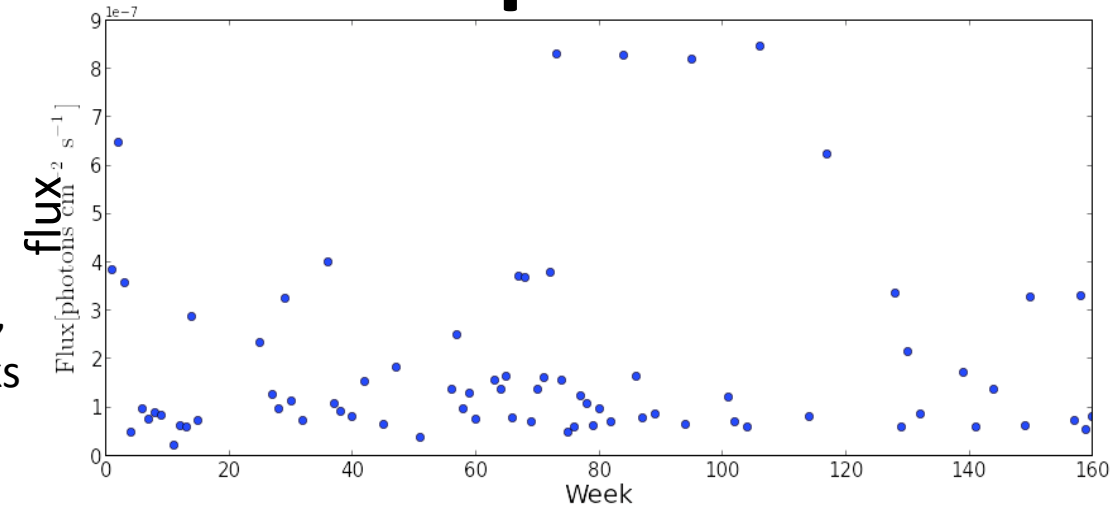
=> possible origine for flares in blazars,

strong Alfven wave mode => Application t wake field acc. for UHECRs

A. Mizuta, T. Ebisuzaki (2018)

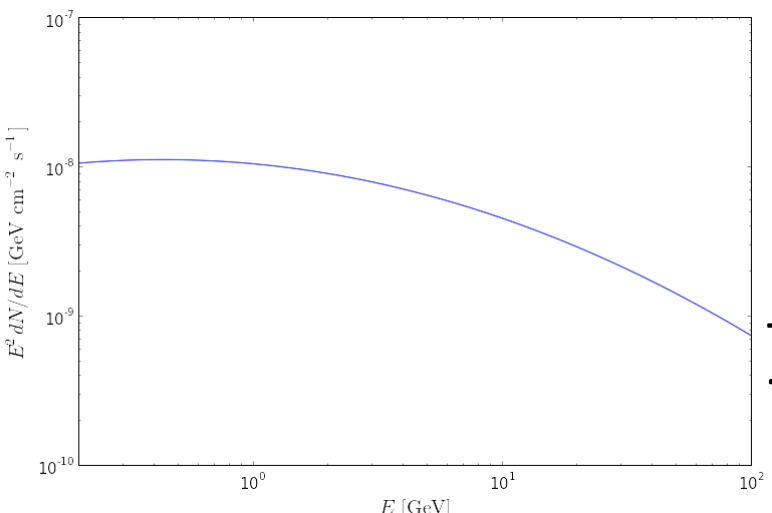
Blazar shows anti-correlation between γ burst flux and spectral index

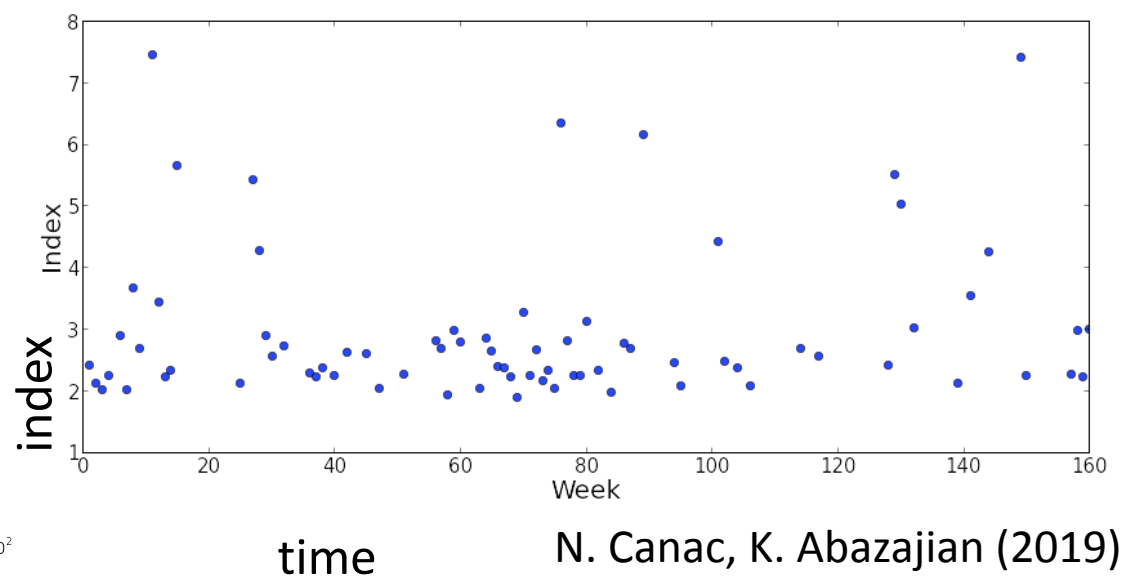
Blazar: AO0235+164
M ~ 10^8 M_{Sun}



Rise time < week (less than a unit),
Period between bursts ~> 10 weeks
Spectral index => 2
(~ Ebisuzaki/Tajima theory)

→ all quantitatively consistent with Wakefield theory



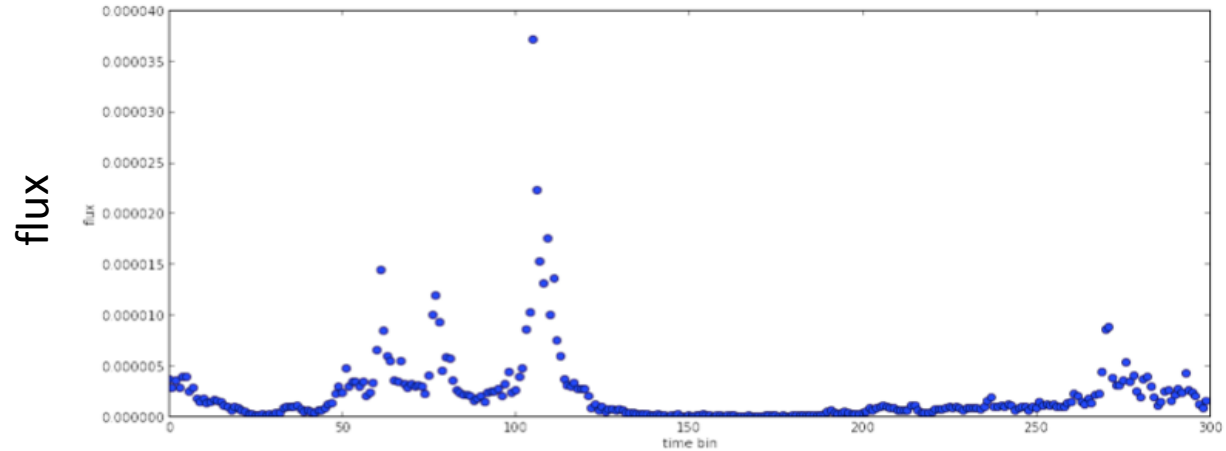


N. Canac, K. Abazajian (2019)

Again, Anti-correlation even in a bigger blazar

Blazar: 3C454.3

$M \sim 10^9 M_{Sun}$

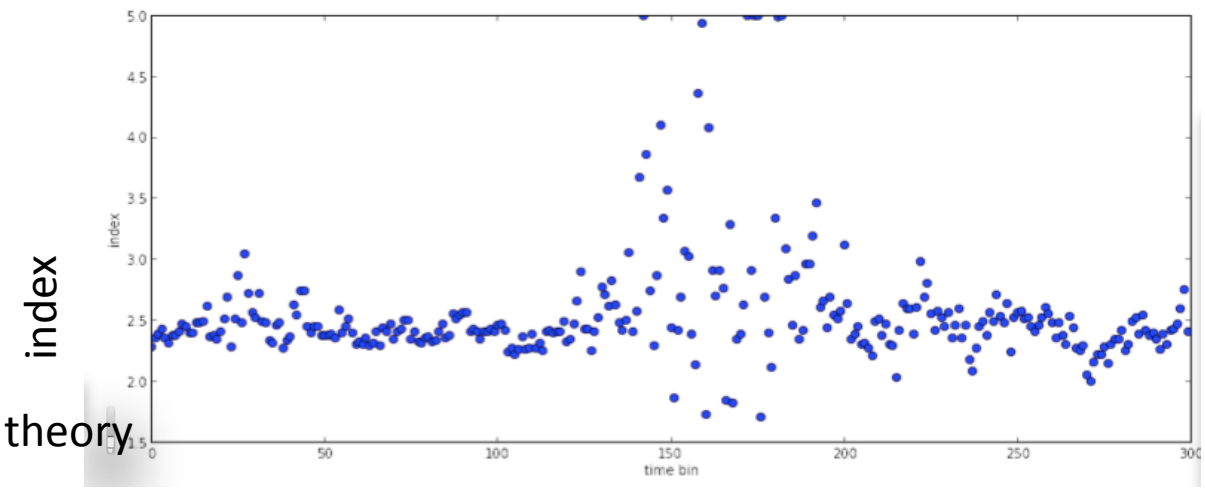


Same anti-correlation as AO0235+164

The rise time and burst periods a lot longer (by an order of magnitude)

Quantitative agreement and **<u>correct scaling</u>** with Blazar mass with (broader sense of) Wakefield theory (Ebisuzaki/Tajima)

period ~ *M* ; luminosity ~*M*

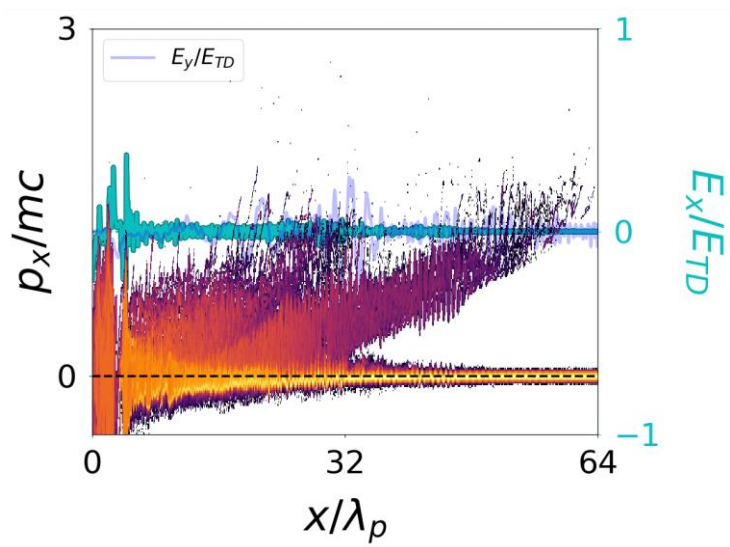


time

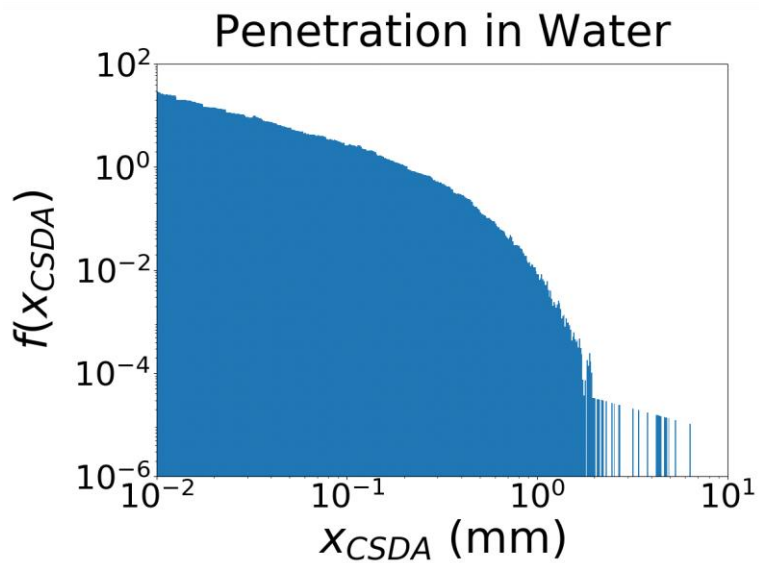
N. Canac, K. Abazajian (2019)

High density wakefields for medicine

- Micron accelerator in endoscope by fiber laser
- Density ~ 10^{21} cm^{-3} nanomaterials target
- Theranostics



Critical density wakefield acceleration



Nicks et al. (2019)

Conclusions

- Demonstrated: ultrafast pulses, coherent collective (robust) wakefield (GeV/cm) excitable.
- Thin-Film Compression (TFC)
- Single-cycled laser → single-cycled X-ray laser
- Wakefield in nanostructure (TeV/cm): accessible
- Wakefield acceleration: Nature's accelerators favored for EHECR, gamma ray bursts from Blazars
- Applications: LWFA endoscopic radiation therapy (ESRT) ← **μm** accelerator ← fiber laser

Thank you!
Y.Shin