

$$Q = Q_0 + \frac{1}{2\pi} \langle \Delta \phi \rangle = Q_0 + \frac{3}{16\pi} g a^2$$