



Muon $g - 2$ in 10 (ish) minutes

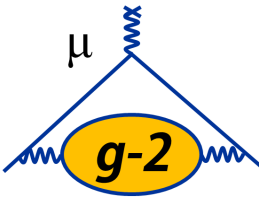
11 June 2019

New Perspectives 2019

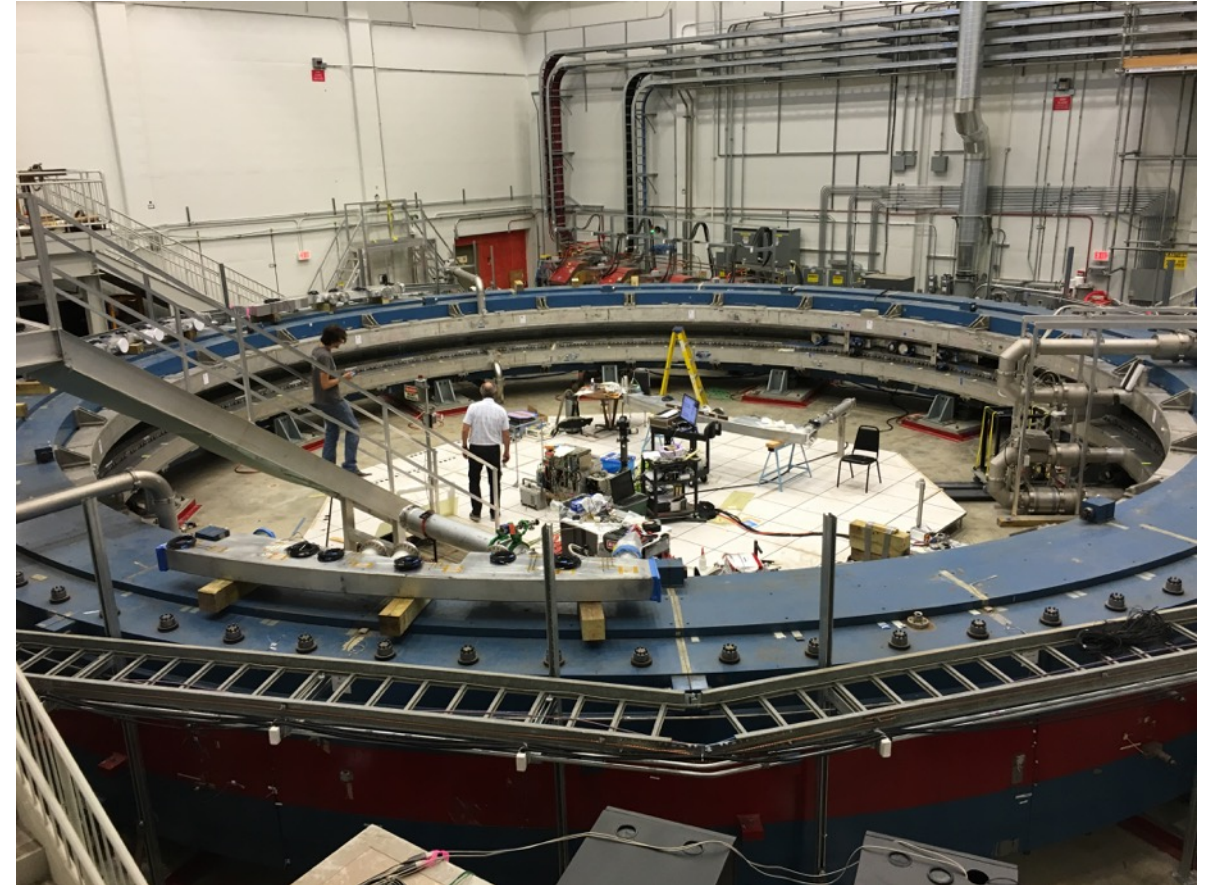
Jason Hempstead (on behalf of the Muon $g - 2$ collaboration)



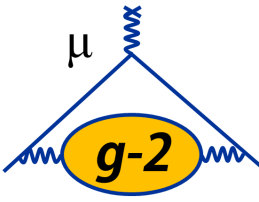
Outline



- The physics of $g_\mu - 2$
 - Magnetic dipole moments
 - Standard model calculation
 - Past experiments
- Fermilab E989
 - Experimental technique
 - Current status



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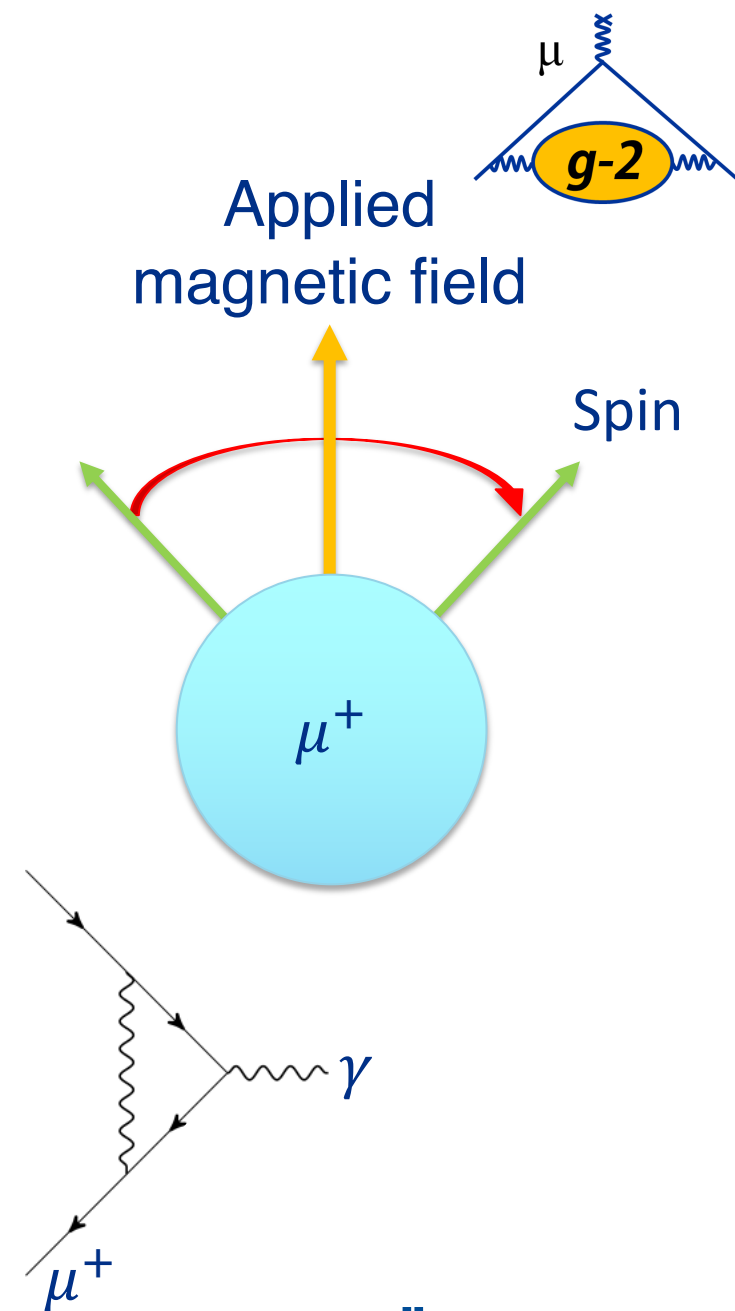
Magnetic dipole moment

- Spin will precess about an external field
 - At a rate dependent on the size of the magnetic moment

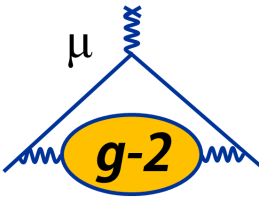
$$\begin{aligned}\frac{d\vec{s}}{dt} &= \vec{\mu} \times \vec{B} \\ &= \frac{gq}{2mc} \vec{s} \times \vec{B}\end{aligned}$$

- Dirac calculated $g = 2$
 - Later, Schwinger calculated a correction due to a photon loop in the vertex
- Define the “magnetic anomaly” – this is what we are measuring

$$a \equiv \frac{g - 2}{2}$$

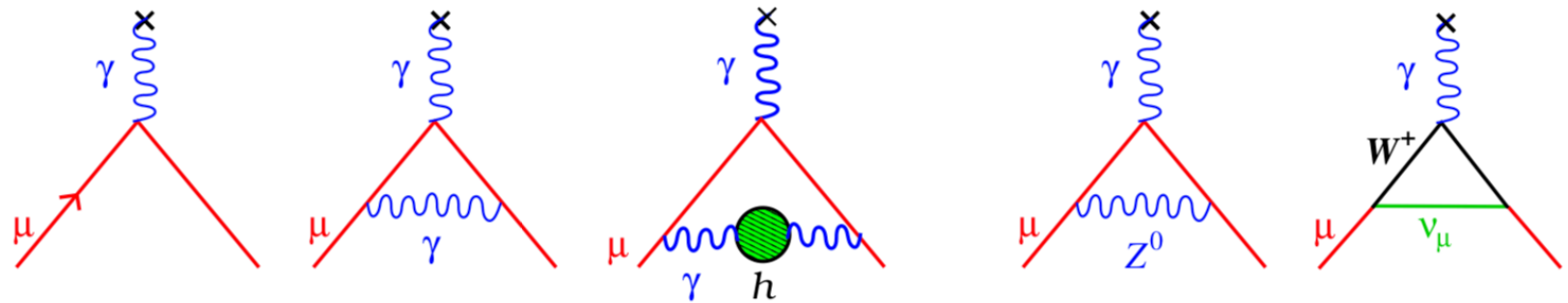


Standard model calculation

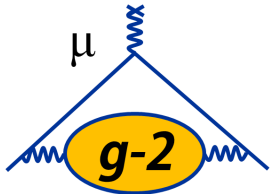


- Value of a_μ sensitive to all particles
 - New physics would show up in difference between SM calculation and measurement
- Calculation split into 4 categories, organized by what particles are loopy:
 - QED
 - Leptons and photons
 - Hadronic
 - Vacuum polarization (HVP)
 - Light-by-light (HLbL)
 - Weak
 - Higgs, Z, W

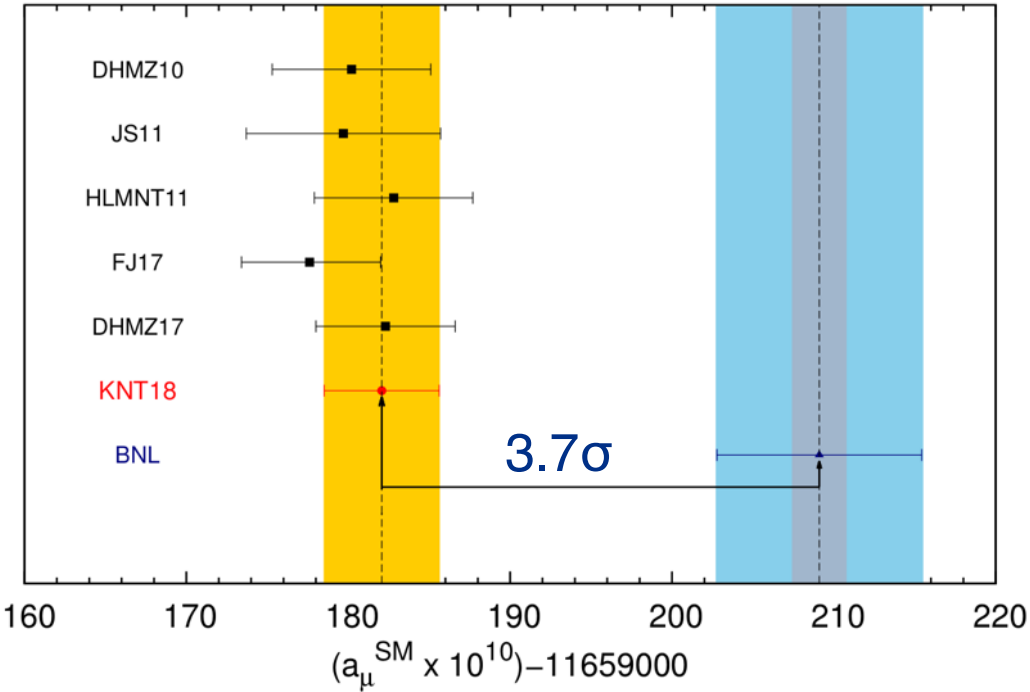
	Contribution ($\times 10^{10}$)	Error ($\times 10^{10}$)
QED	11 658 471.8971	0.007
Weak	15.36	0.10
HVP	684.68	2.42
HLbL	9.8	2.6
Total a_μ^{SM}	11 659 182.04	3.56



Brookhaven (BNL) E821 measurement

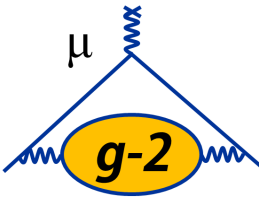


- Results of most recent measurement at Brookhaven E821 hint at something unknown...



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QED	11 658 471.8971	0.007
Weak	15.36	0.10
HVP	684.68	2.42
HLbL	9.8	2.6
Total a_μ^{SM}	11 659 182.04	3.56
a_μ^{BNL}	11 659 208.0	6.3
Δa_μ	25.96	7.24

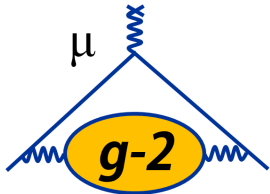
Outline



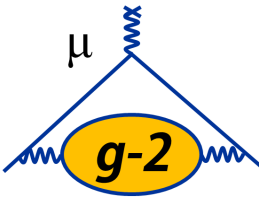
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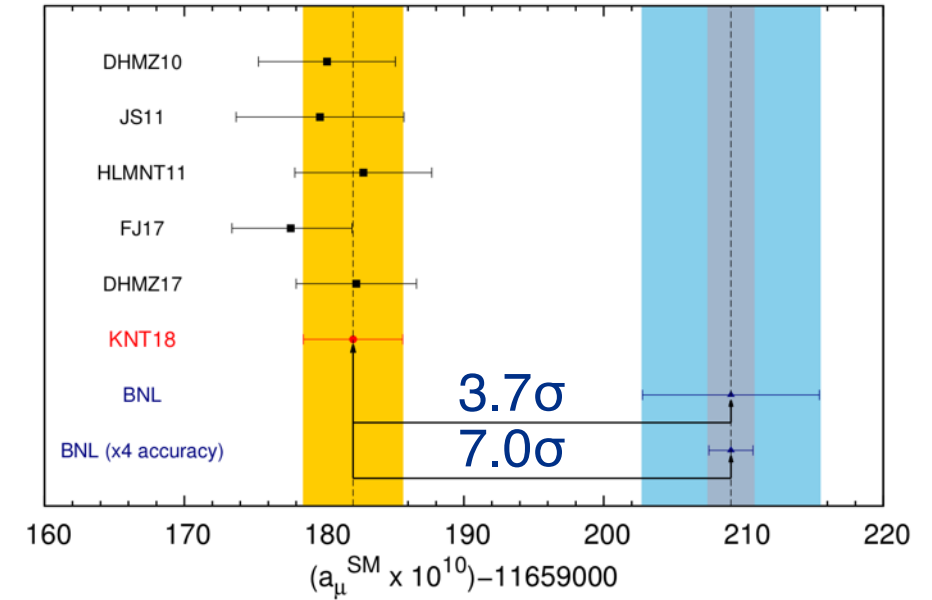
To resolve this...



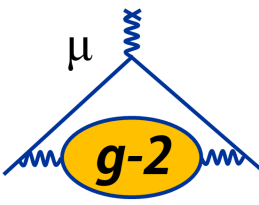
Fermilab E989



- 4x the precision of BNL
 - 540 parts per billion (ppb) \rightarrow 140 ppb
- 100 ppb statistical uncertainty
 - $\approx 10^{11}$ collected positrons
 - Roughly 21x the statistics taken at BNL
- 100 ppb systematic uncertainty
 - 70 ppb for magnetic field measurement
 - 70 ppb for spin precession frequency



Measuring a_μ with a storage ring

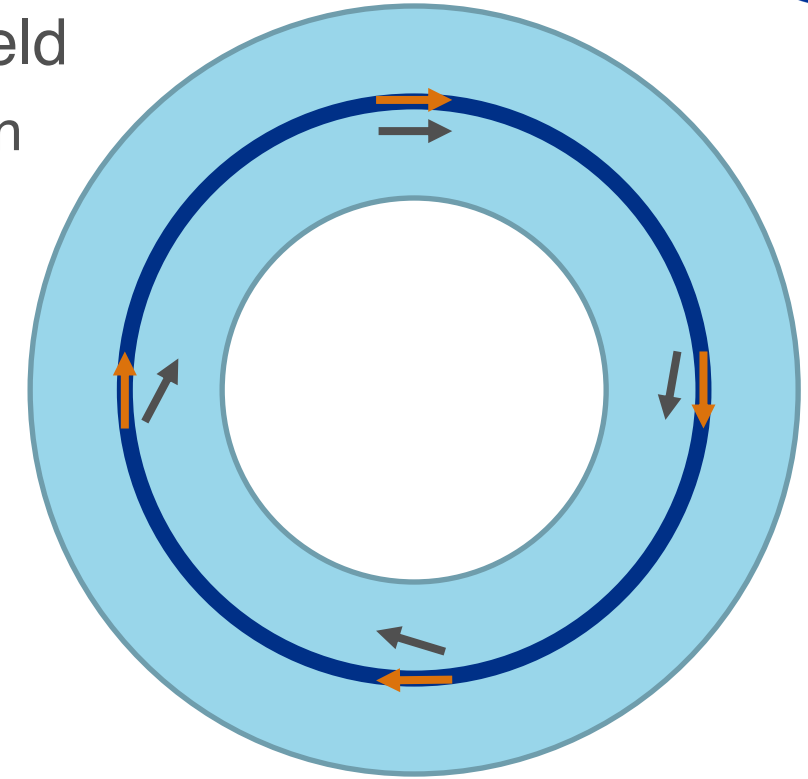


- Inject polarized muons into highly uniform 1.45 T field
 - High energy positrons preferentially emitted in direction of spin

$$\vec{\omega}_a = \vec{\omega}_s - \vec{\omega}_c = -\frac{e}{m} \left[\begin{array}{l} a_\mu \vec{B} \\ - a_\mu \frac{\gamma}{\gamma + 1} (\vec{\beta} \cdot \vec{B}) \vec{\beta} \\ - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \vec{\beta} \times \vec{E} \end{array} \right]$$

≈ 0 for motion transverse to magnetic field

≈ 0 for muons at “magic” momentum 3.1 GeV / c or $\gamma = 29.3$



Momentum vector 

Spin vector 

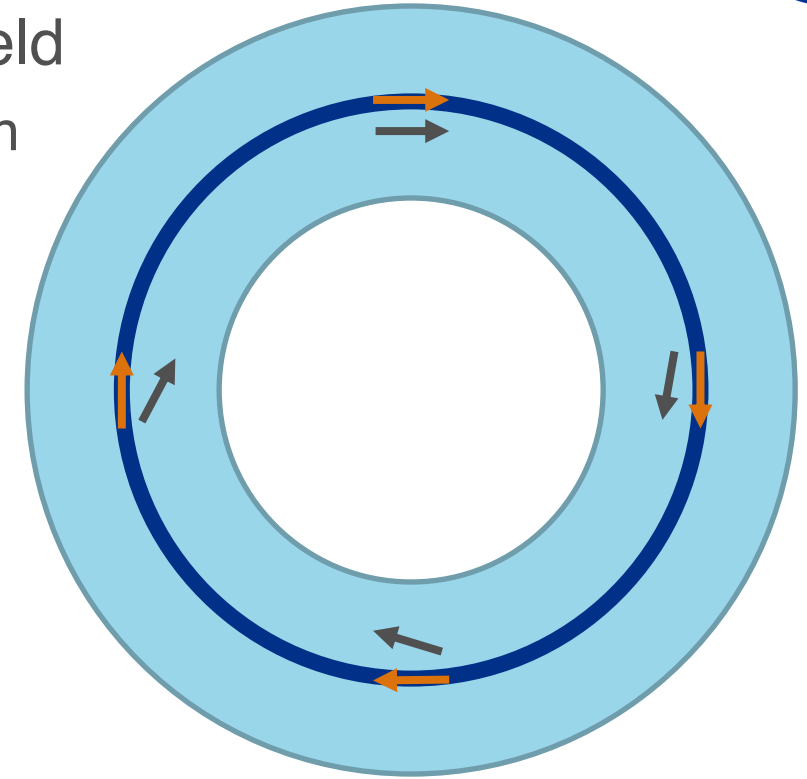
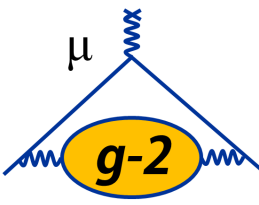
Measuring a_μ with a storage ring

- Inject polarized muons into highly uniform 1.45 T field
 - High energy positrons preferentially emitted in direction of spin
- Record data in 700 μs “fills”
 - 10 (boosted) lifetimes of muon precession data

$$\vec{\omega}_a = \vec{\omega}_s - \vec{\omega}_c = -\frac{e}{m}a_\mu\vec{B}$$

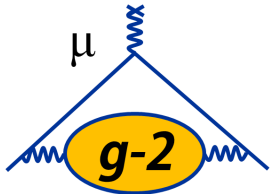
- Magnetic field measured in terms of the Larmor precession frequency of the free proton, ω_p

$$B = \frac{\omega_p}{\mu_p}$$



Momentum vector 
Spin vector 

Getting a number for $g_\mu - 2$

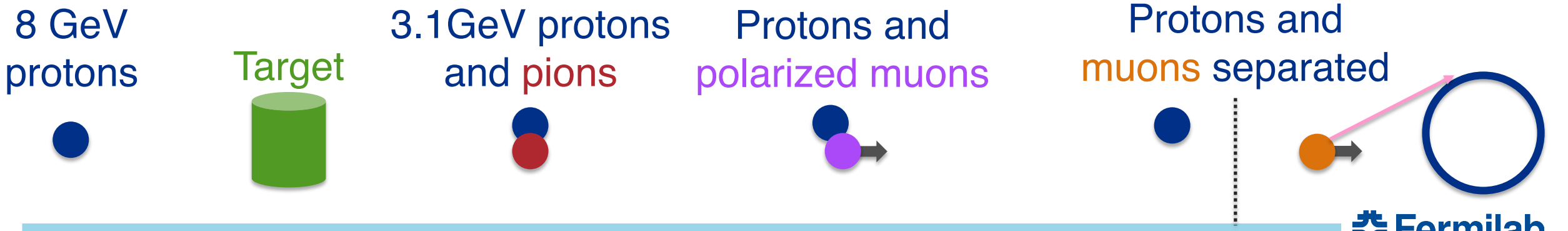
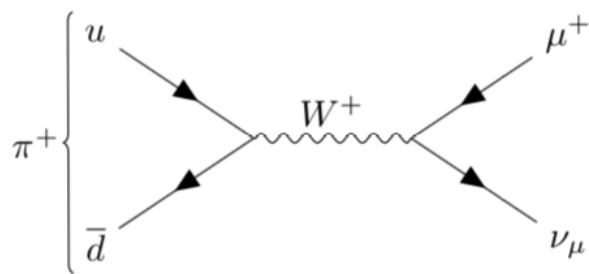
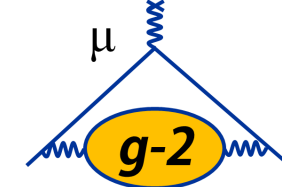


- Combination of constants measured very well

$$a_\mu = \frac{g_\mu - 2}{2} = \frac{\omega_a}{\tilde{\omega}_p} \frac{g_e}{2} \frac{\mu_p}{\mu_e} \frac{m_\mu}{m_e}$$

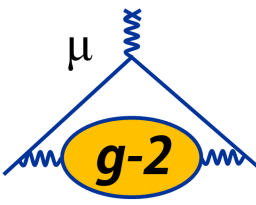
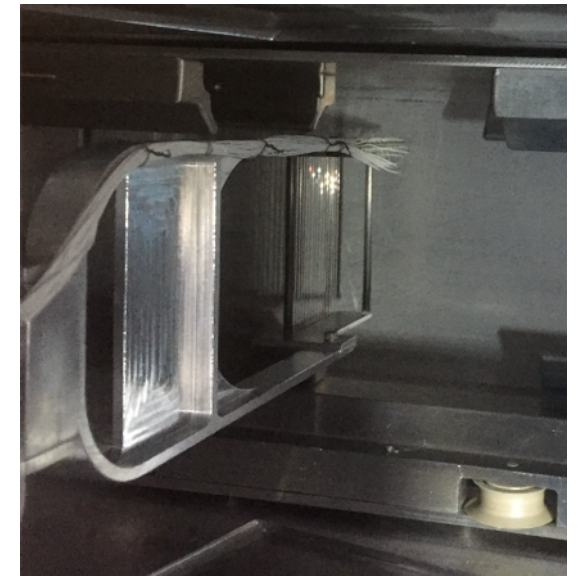
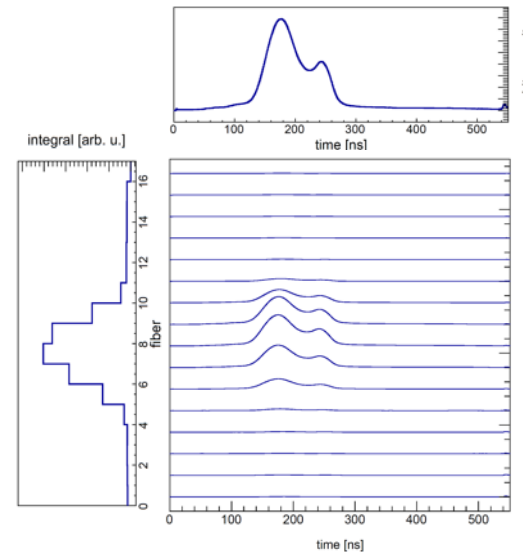
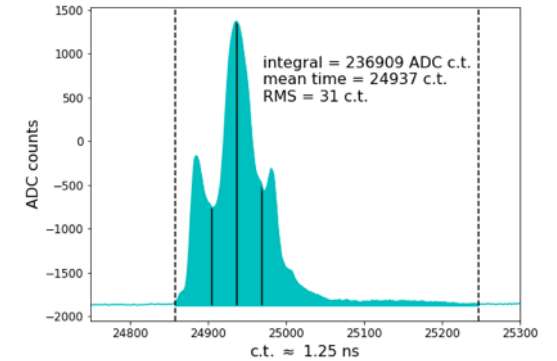
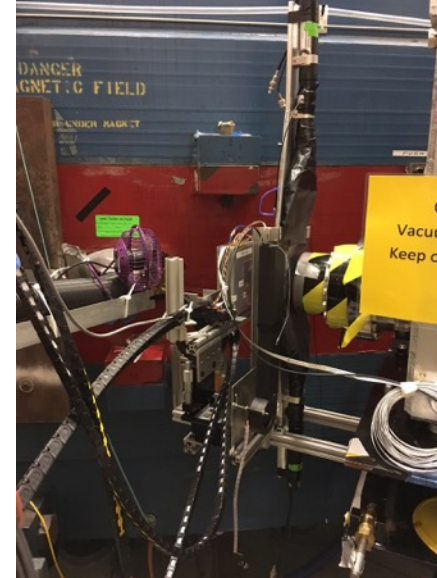
	Relative error (ppb)	Experiment
g_e	0.000 26	Quantum electron cyclotron. Hanneke et al. 2008.
μ_e/μ_p	3.0	Hydrogen spectroscopy. Winkler et al. 1972.
m_μ/m_e	22	Muonium hyperfine splitting. Liu et al. 1999.
$\omega_a/\tilde{\omega}_p$	140	Fermilab $g - 2$

Fermilab Muon $g - 2$ (E989)



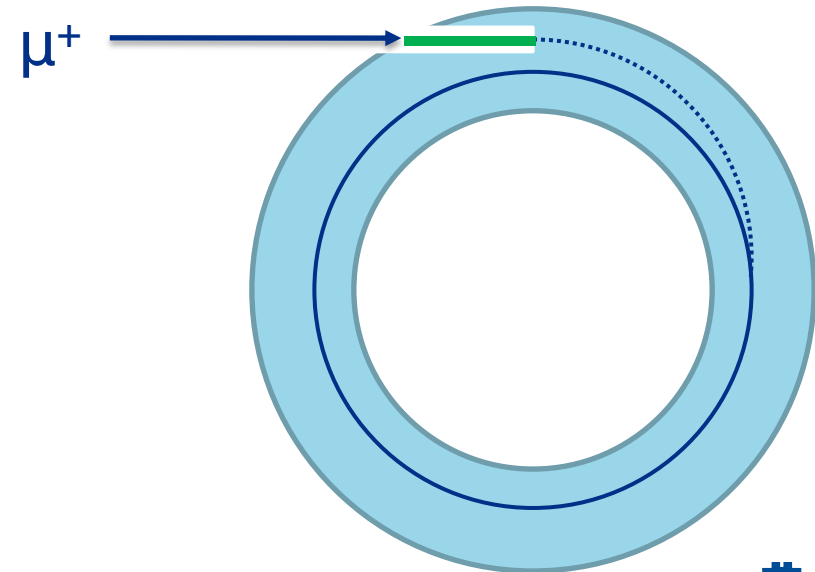
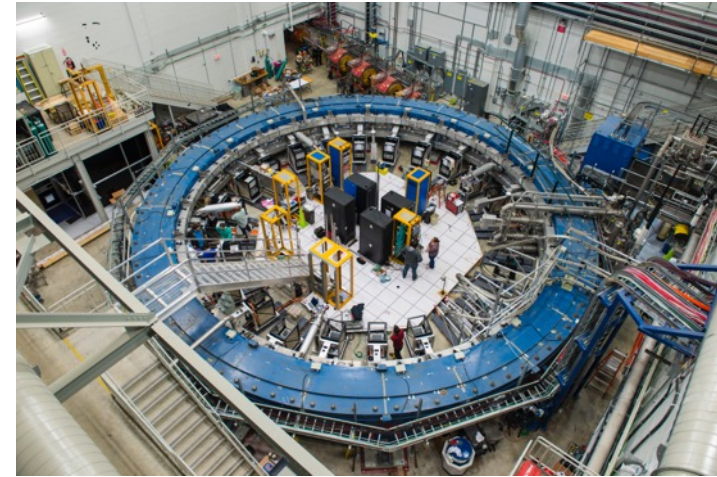
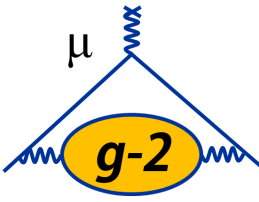
Understanding injection

- Beam entrance counters:
 - T0
 - Scintillating paddle coupled to 2 PMTs
 - Provides absolute injection time
 - Inflector Beam Monitoring System (IBMS)
 - Series of 3 detectors along beam path
 - Scintillating fibers coupled to silicon photomultipliers (SiPMs)
 - Spatial profile of beam

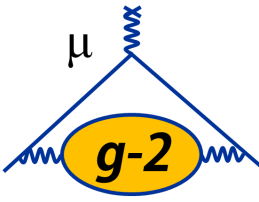


Storing muons to watch them precess

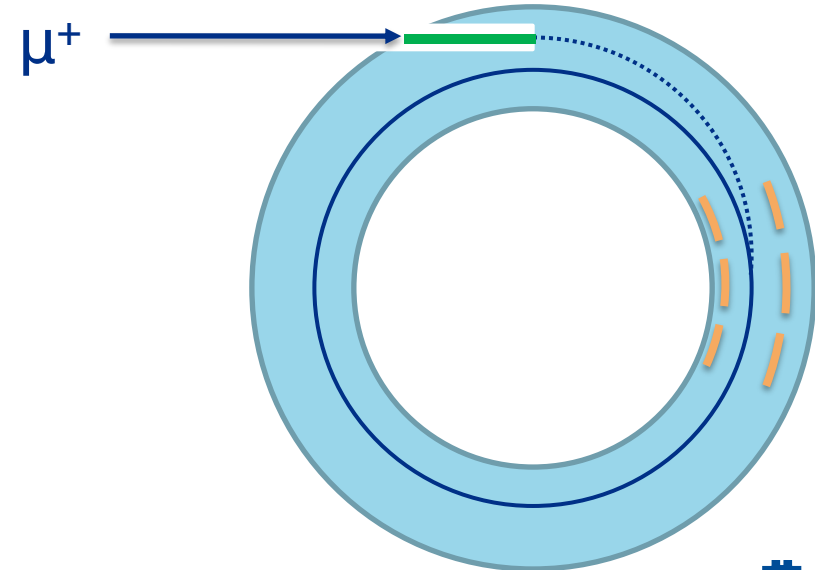
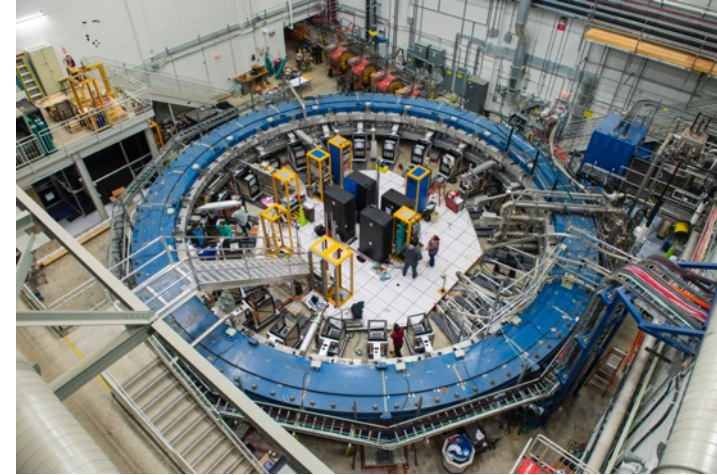
- Superconducting **inflector**
 - Cancels out magnetic field to allow injection



Storing muons to watch them precess

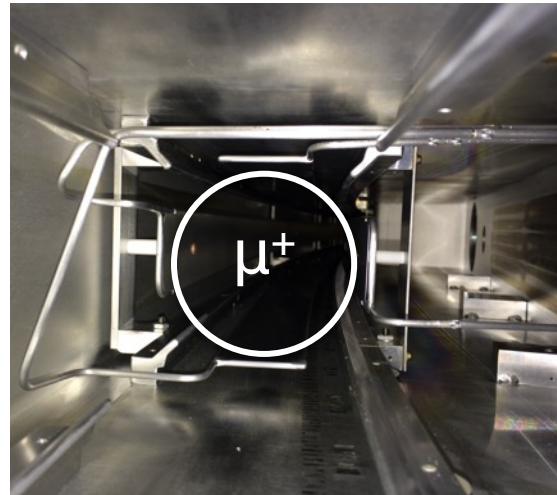
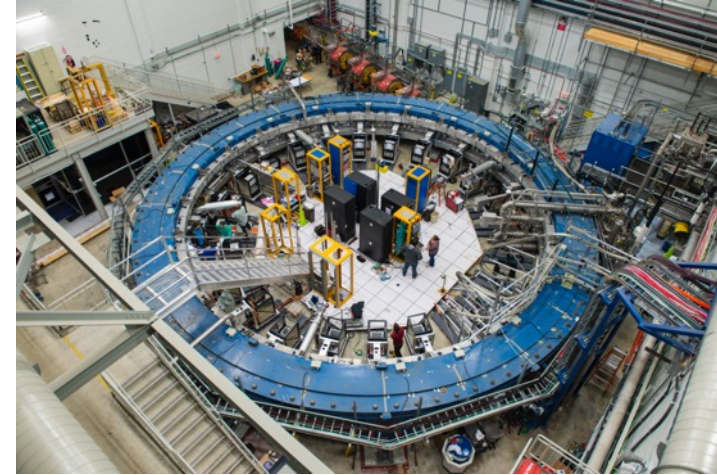
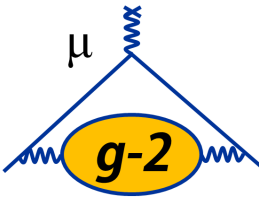


- Superconducting **inflector**
 - Cancels out magnetic field to allow injection
- Magnetic **kickers**
 - Deflect muons onto the proper orbit

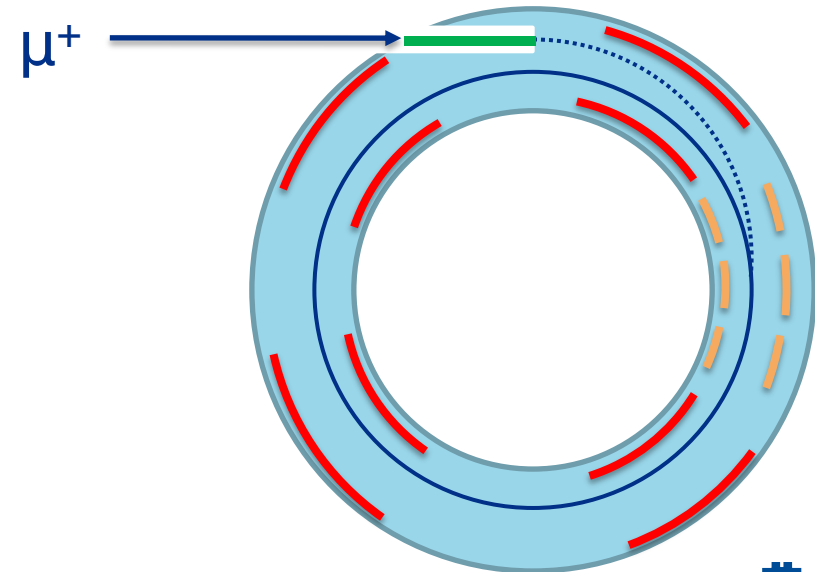


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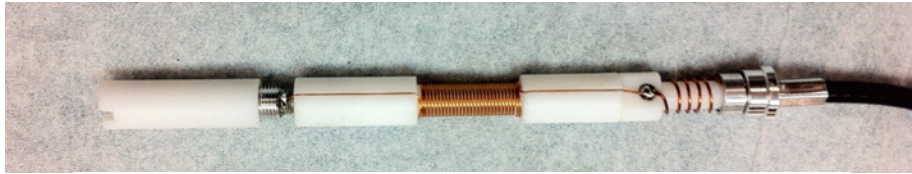
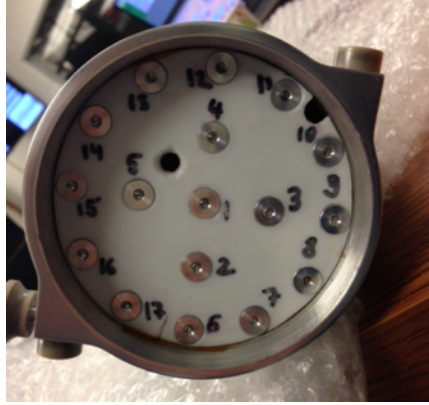
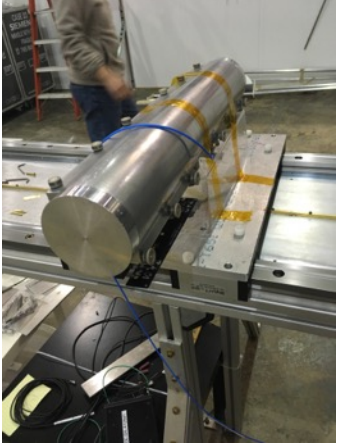
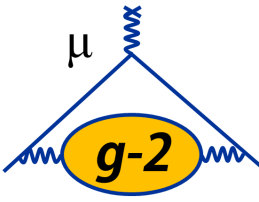
- Superconducting **inflector**
 - Cancels out magnetic field to allow injection
- Magnetic **kickers**
 - Deflect muons onto the proper orbit
- Electrostatic **quadrupoles**
 - Provide vertical focusing



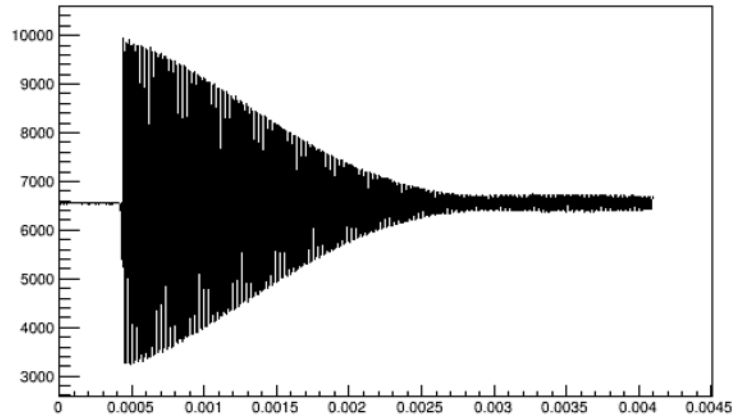
Cross-section of storage region



Measuring the magnetic field (ω_p)

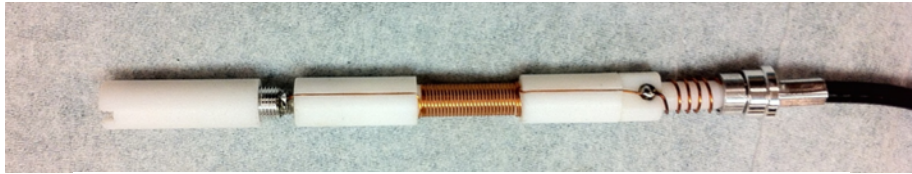
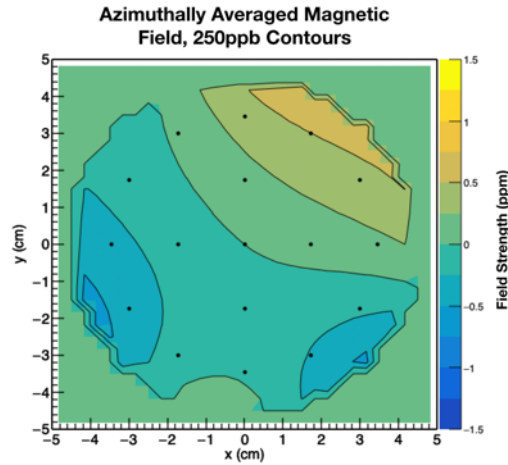
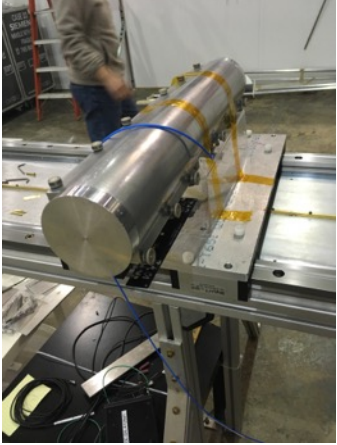
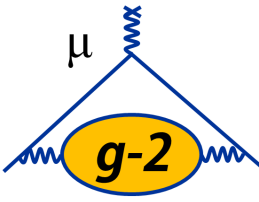


Event_000_probe_082 Starting at 1518398574387325000 with time interval 1.000000 microsec

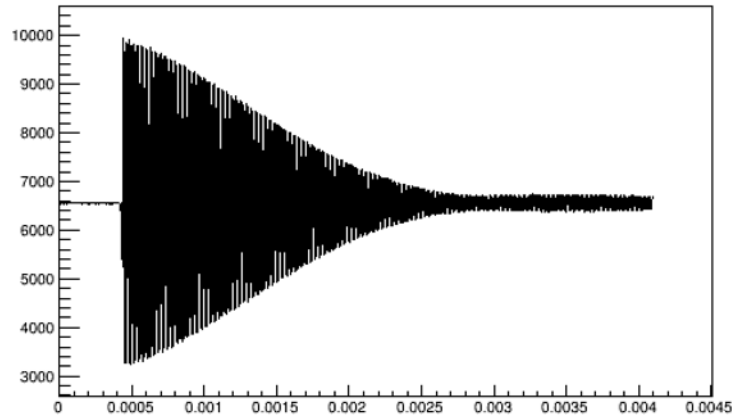


- Nuclear magnetic resonance (NMR) probes (x17) on a trolley to survey the muon storage region periodically
 - When no beam present
 - Measures Larmor precession of the protons in petroleum jelly samples
- 378 additional probes outside the storage region to monitor continuously
- Very well understood water sample to calibrate the trolley probes

Measuring the magnetic field (ω_p)



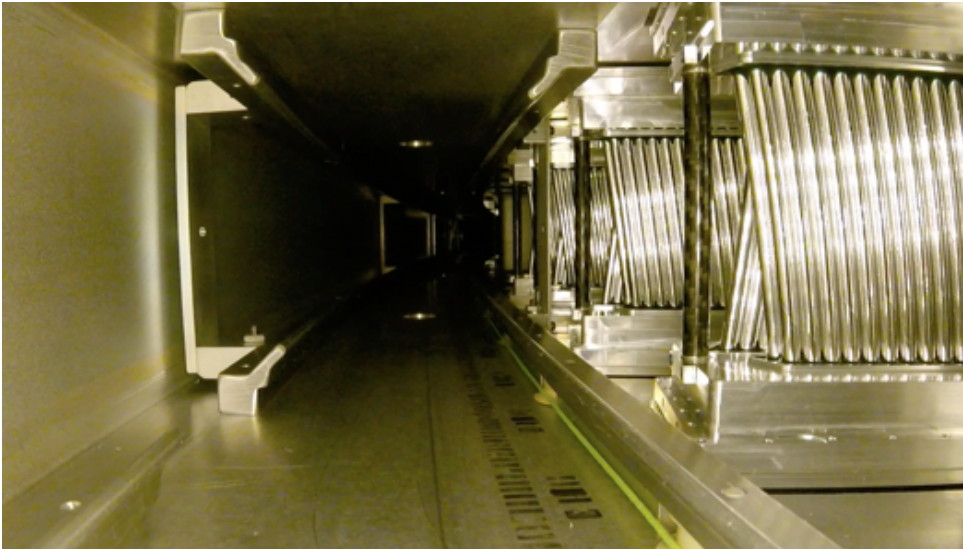
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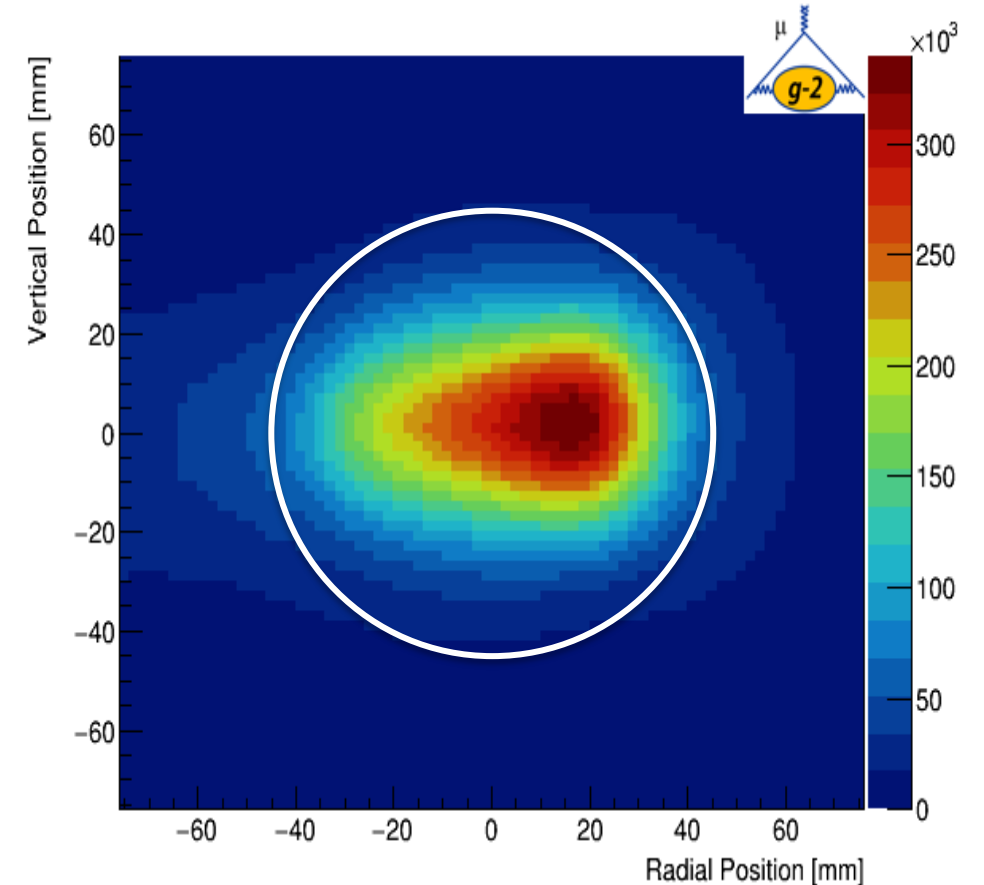
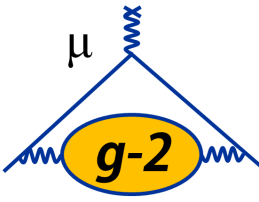
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Measuring beam distribution

- 2 stations of straw tracking detectors
 - Extrapolate positron tracks to decay position
- Provide information about location of beam
 - $\omega_p \rightarrow \tilde{\omega}_p$

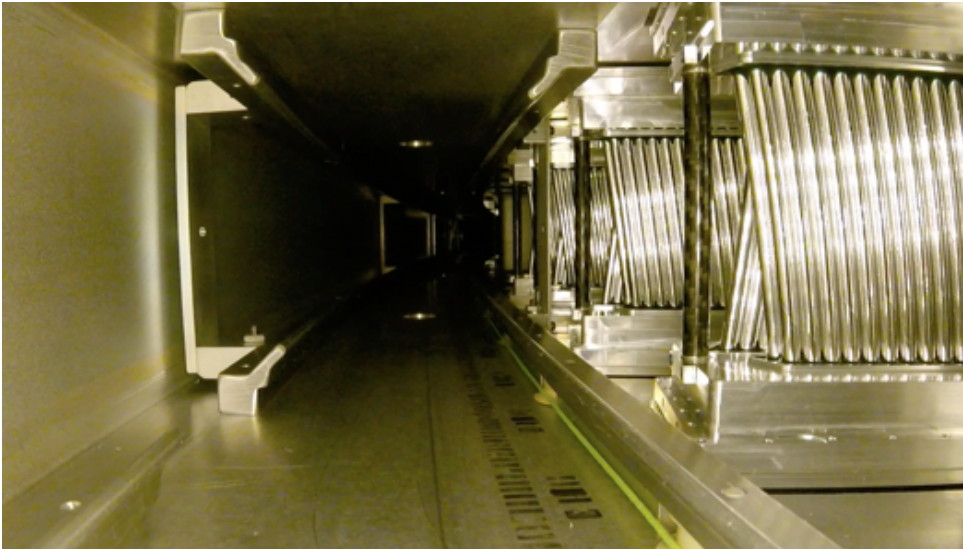


G. Lukicov. High precision track-based alignment of the tracking detector of the g-2 experiment (poster). Fermilab Users Meeting 2019.

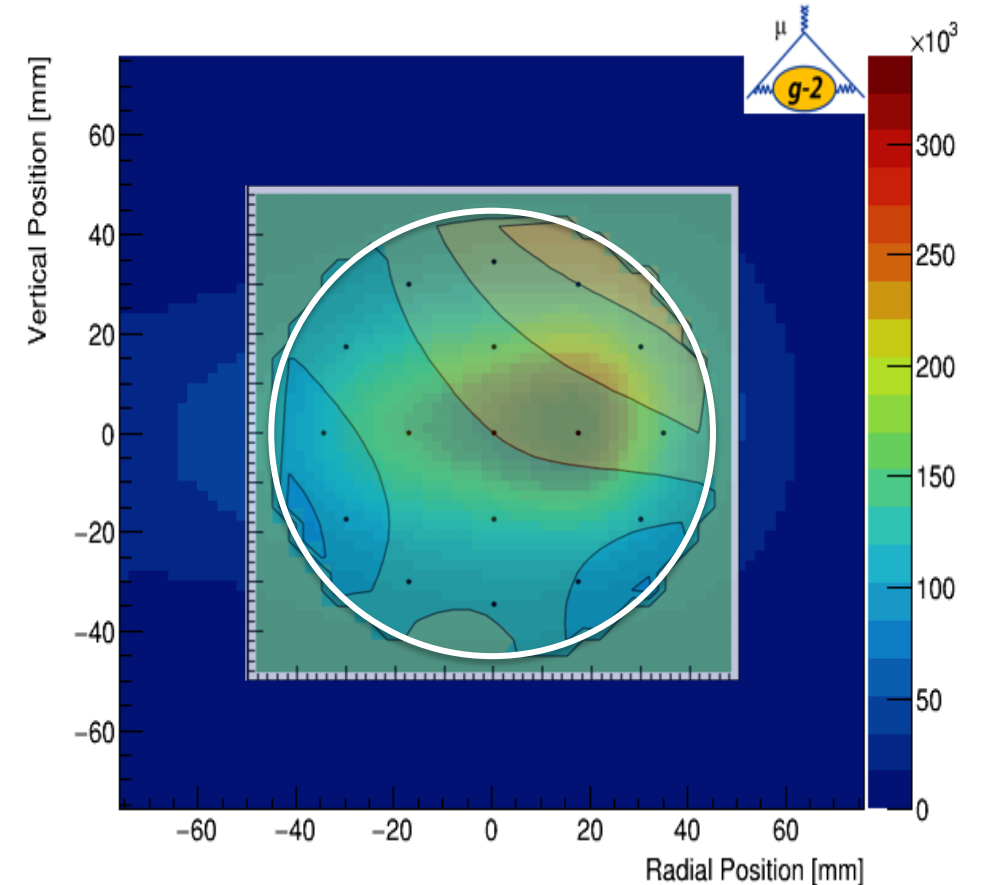
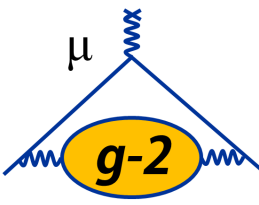


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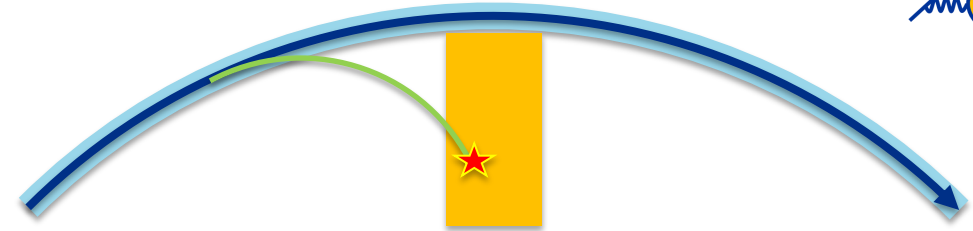
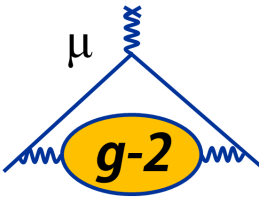


G. Lukicov. High precision track-based alignment of the tracking detector of the g-2 experiment (poster). Fermilab Users Meeting 2019.



Measuring the precession frequency (ω_a)

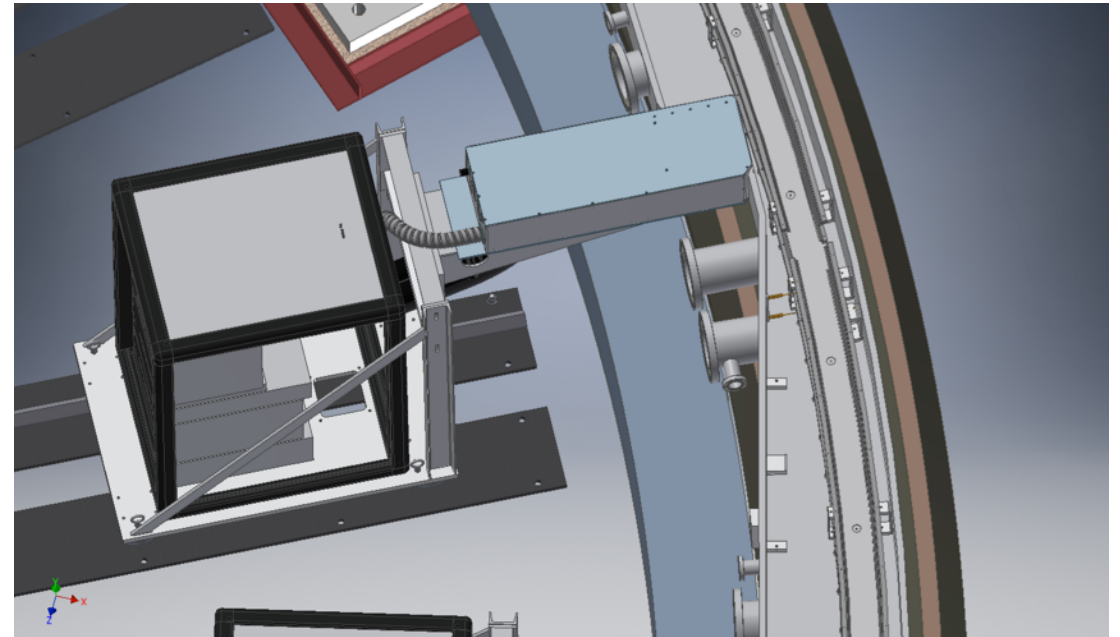
- Use electromagnetic calorimeters
 - 24 equally spaced around ring
 - Each is a 9x6 grid of lead fluoride (PbF_2) crystals read out individually by SiPMs



Decay positron curling inward from the muon storage orbit to strike a calorimeter



J. Hempstead. Preparing the Muon $g - 2$ calorimeters for Run 2 (poster). Fermilab Users Meeting 2019.

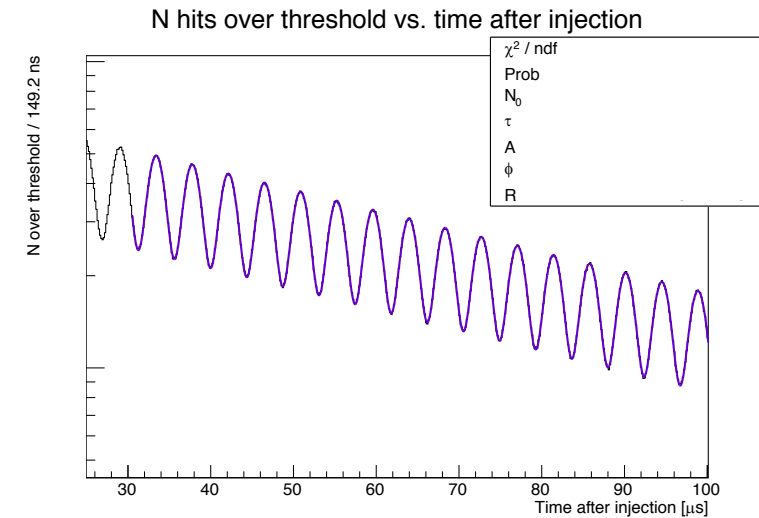
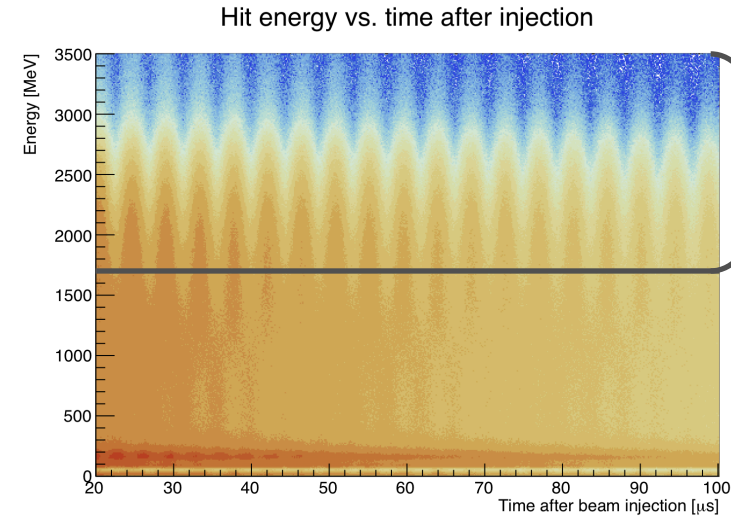
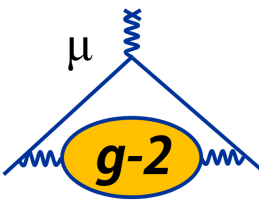


Measuring the precession frequency (ω_a)

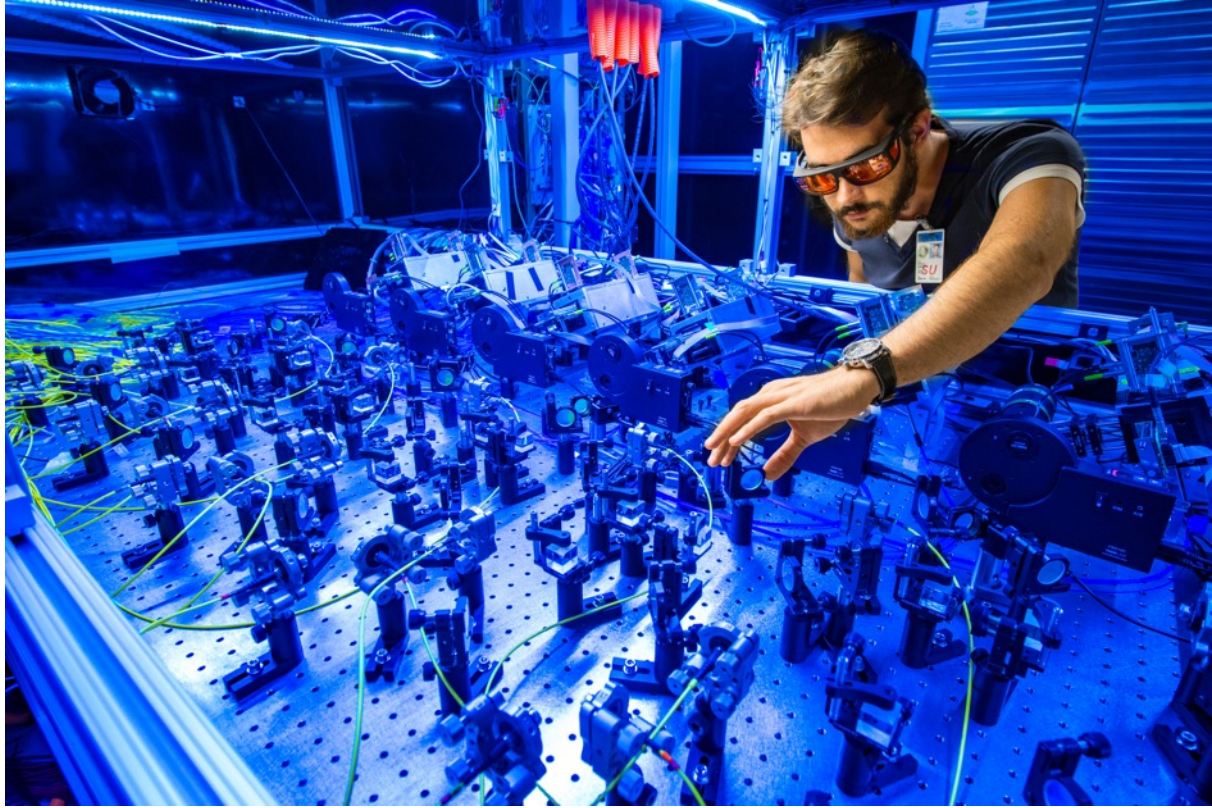
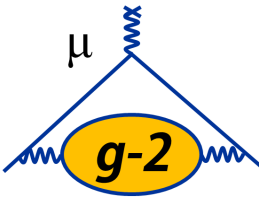
- Use electromagnetic calorimeters
 - 24 equally spaced around ring
 - Each is a 9x6 grid of lead fluoride (PbF_2) crystals read out individually by SiPMs
- $\omega_a = \omega_S - \omega_C$ is imprinted in the number of positrons in a given direction
 - Cut on positron energy
- Fit using

$$N(t) = N_0 \exp(-t/\gamma\tau_\mu) [1 + A \cos(\omega_a t - \phi)]$$

M. Bhattacharya. Pileup Systematic Studies in the Fermilab Muon g-2 Experiment. New Perspectives 2019.



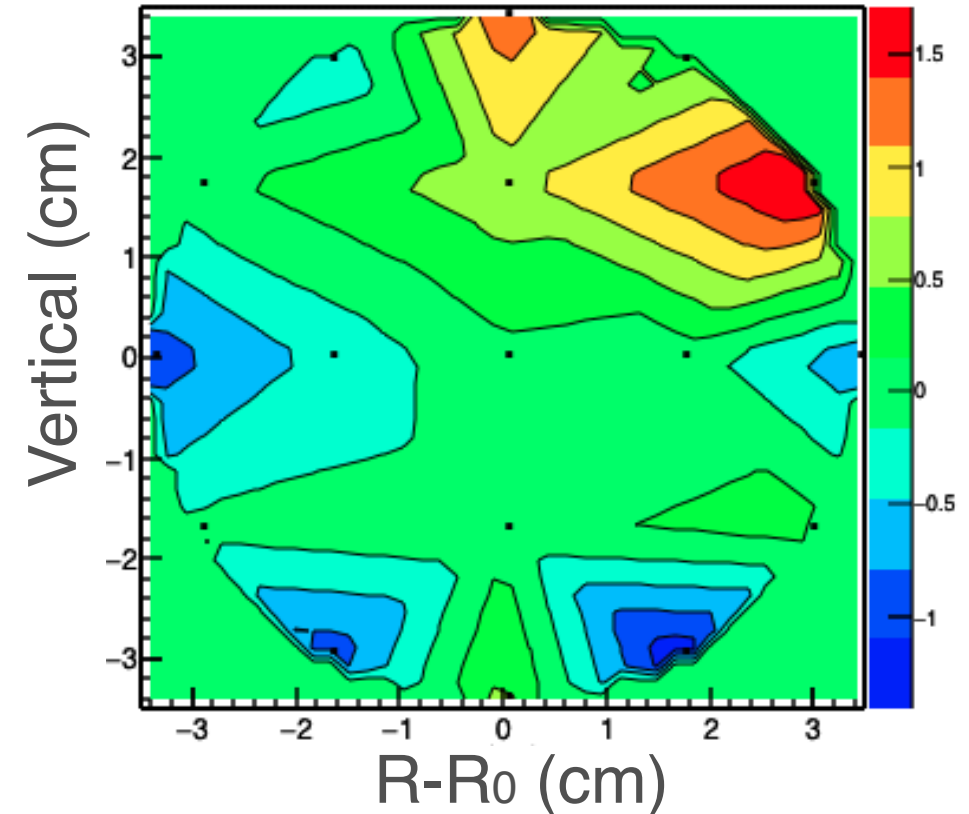
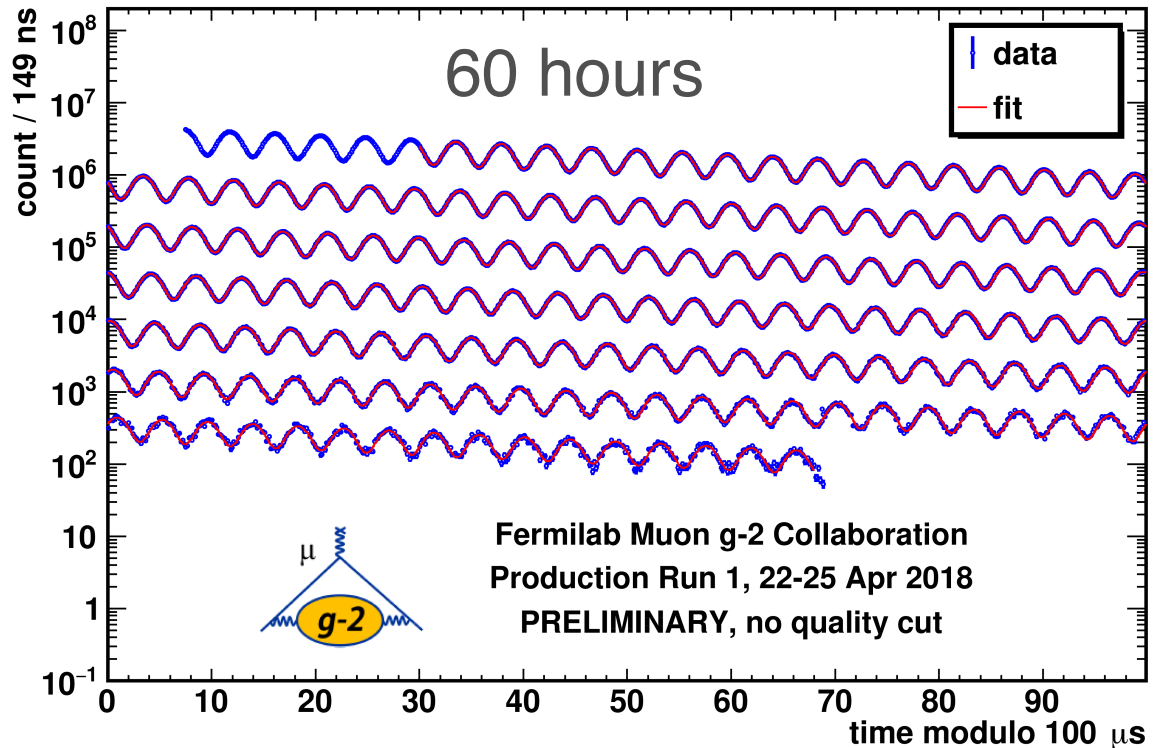
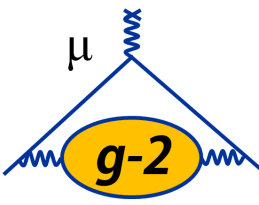
Laser system



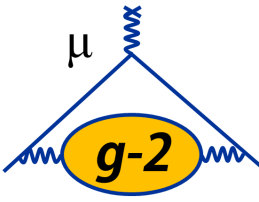
- Track and correct gain of individual channels in calorimeters
- Timing alignment of individual channels
 - Synchronization laser pulse at the beginning of every fill

Current status

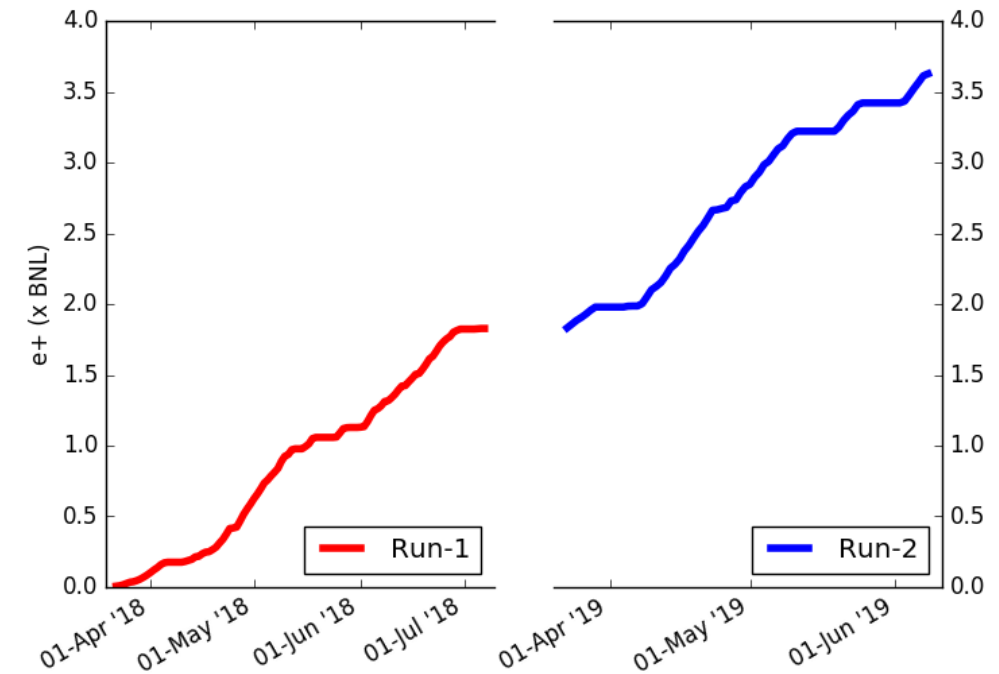
- Run 1 analysis underway
 - About 1.4x the statistics of the E821 result (in ω_a fit)
 - Magnetic field uniformity about 2x better



Current status

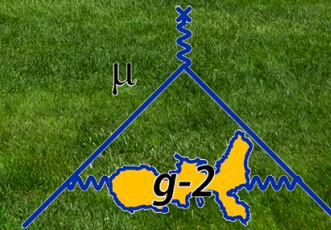
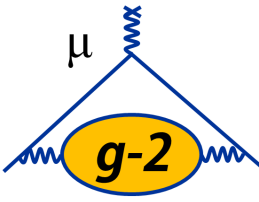


- Run 1 analysis underway
 - About 1.4x the statistics of the E821 result (in ω_a fit)
 - Magnetic field uniformity about 2x better
- Run 2 in progress
 - Currently collected $\sim 1.8x$ the statistics of E821
 - Improved stability of run conditions



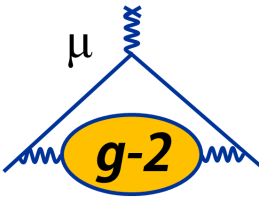
S. Ganguly. Muon g-2: Measuring the anomalous magnetic dipole moment of a muon to high precision. Fermilab Users Meeting 2019.

Thanks!



Back-up

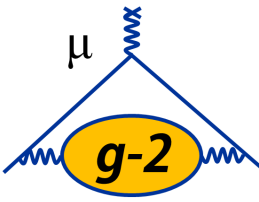
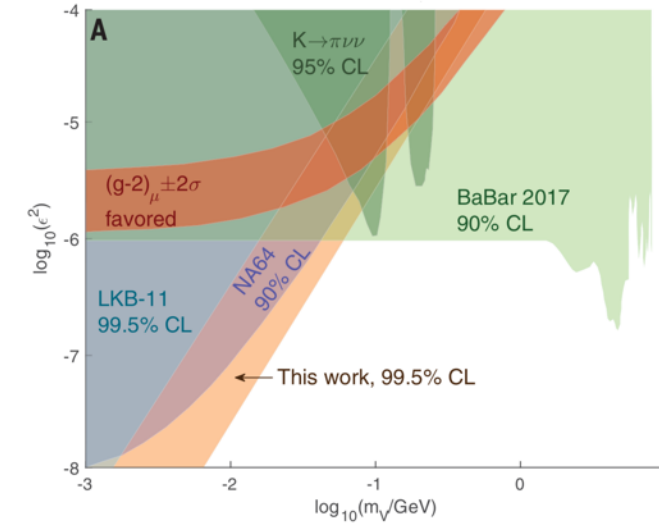
Various sources



- P. A. M. Dirac. The Quantum Theory of the Electron. 1928.
- B. Lee Roberts. The History of the Muon ($g - 2$) Experiments. 2018.
- A. Keshavarzi, D. Nomura, and T. Teubner. The muon $g - 2$ and $\alpha(M_Z^2)$: a new data-based analysis. 2018.
- G. W. Bennett et al. Final report of the E821 muon anomalous magnetic moment measurement at BNL. 2006.
- A. T. Fienberg. Measuring the Precession Frequency in the E989 Muon $g - 2$ Experiment. 2019.
- P. J. Mohr, D. B. Newell, and B. N. Taylor. CODATA Recommended Values of the Fundamental Physical Constants: 2014. 2016.
- D. Hanneke, S. Fogwell, and G. Gabrielse. New Measurement of the Electron Magnetic Moment and the Fine Structure Constant. 2008.
- P. F. Winkler et al. Magnetic Moment of the Proton in Bohr Magnetons. 1972.
- W. Liu et al. High Precision Measurements of the Ground State Hyperfine Structure Interval of Muonium and of the Muon Magnetic Moment. 1999.
- J. Grange et al. Muon ($g-2$) Technical Design Report. 2015.
- D. Stratakis et al. Accelerator performance analysis of the Fermilab Muon Campus. 2017.
- R. Osofsky. Magnetic Field Status of the Muon $g-2$ Experiment. New Perspectives 2018.
- J. D. Jackson. Classical Electrodynamics, Third Edition. 1998.
- Photos from Fermilab and Wikipedia

Potential new physics?

- SUSY
 - Still no sign at the LHC
- Dark photon
 - Almost completely ruled out by various experiments

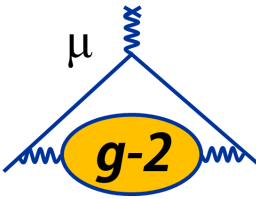
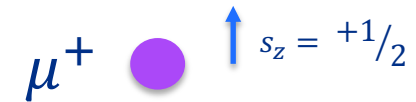
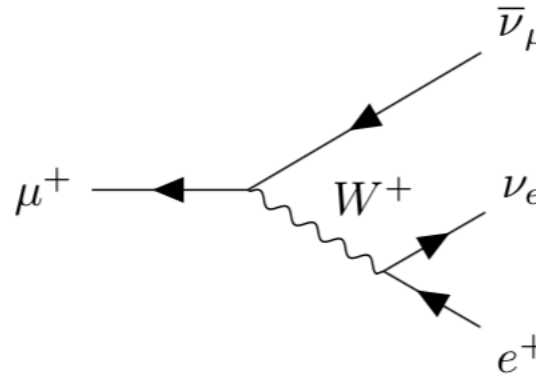
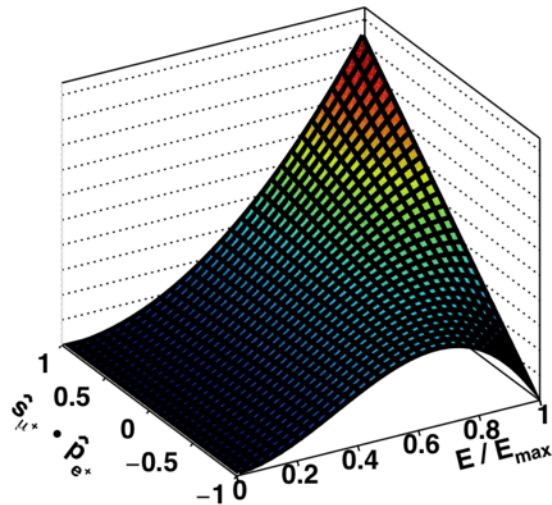


$$\begin{aligned}
 & \text{Diagram 1: } g = 2 \left(1 + \dots \right) \\
 & \text{Diagram 2: } + .00116 \dots \\
 & \text{Diagram 3: } + .00000006951 \dots \\
 & \text{Diagram 4: } + .000000001536 \\
 & \text{Diagram 5: } + ?)
 \end{aligned}$$

- Parker et al. Measurement of the fine-structure constant as a test of the Standard Model. 2018.
- B. Lee Roberts. The History of the Muon ($g - 2$) Experiments. 2018.

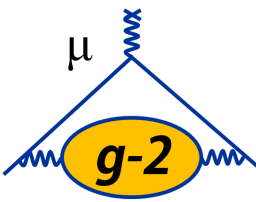
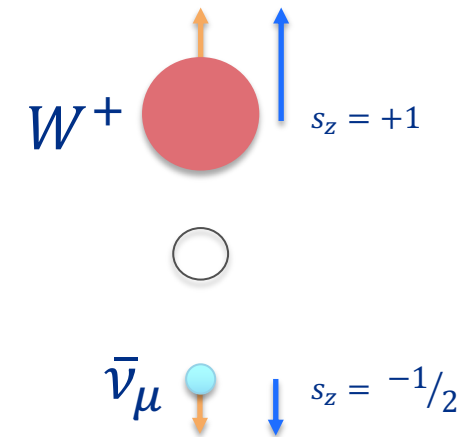
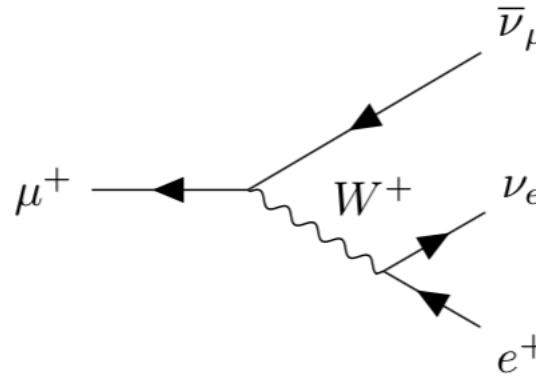
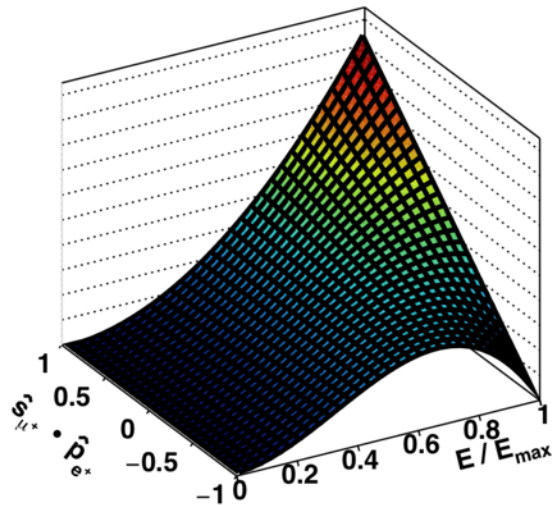
Measurement technique

- Apply a magnetic field
 - Muons' spins rotate
- Count decay positrons
 - Preferentially emitted in the direction of the muon's spin
 - Relies on parity violation in the weak decay



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