

$$\Delta E = \frac{1}{2m_\chi} \left((m_\chi v)^2 - (m_\chi v - q)^2 \right) \leq vq - \frac{q^2}{2m_\chi}$$