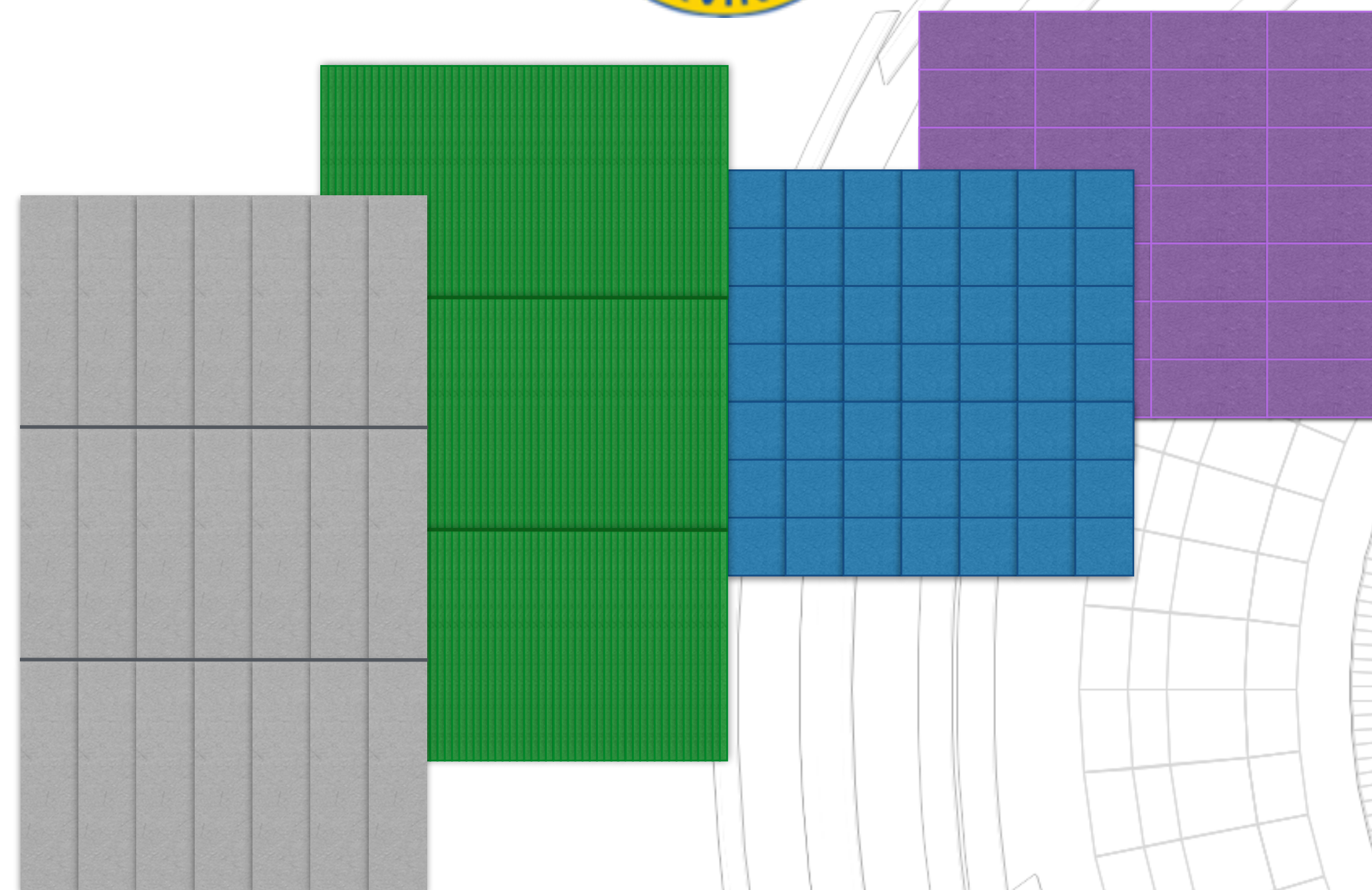


Uncertainties in the era of ML (For Particle and Astrophysics)

Aishik Ghosh

Aspen Centre for Physics

28 Mar 2023



Uncertainties, the bedrock of experimental science

Uncertainties, the bedrock of experimental science

$$m_H = 125.25 \pm 0.17 \text{ GeV}$$

Uncertainties, the bedrock of experimental science

$$m_H = 125.25 \pm 0.17 \text{ GeV}$$

Uncertainties, the bedrock of experimental science

$$m_H = 125.25 \pm 0.17 \text{ GeV}$$



How sure am I ? How can I reduce my uncertainty ?

Uncertainties, the bedrock of experimental science

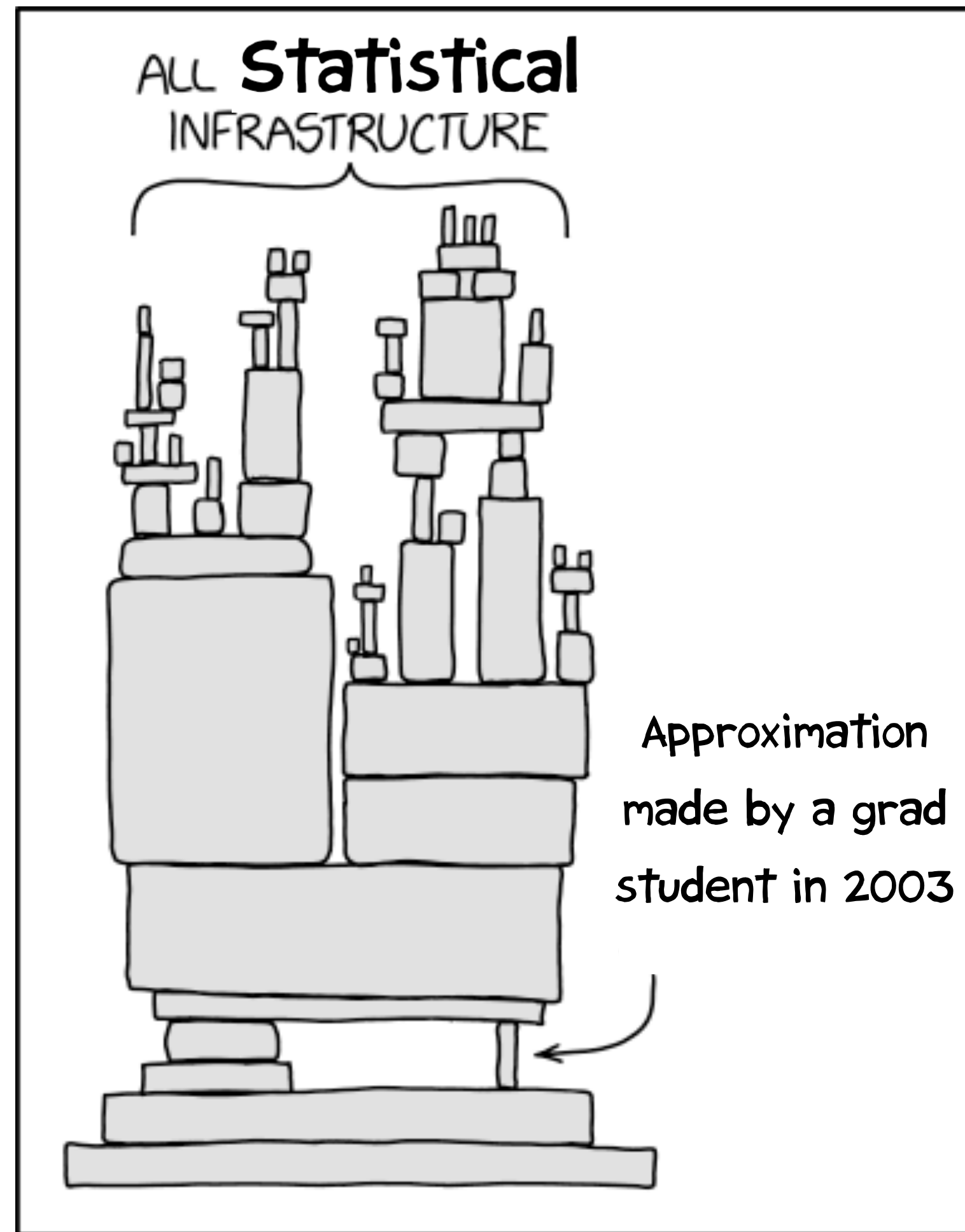
$$m_H = 125.25 \pm 0.17 \text{ GeV}$$

{statistical, detector systematic, theory systematic, epistemic,}



How sure am I ? How can I reduce my uncertainty ?

Nuisance Parameter Infrastructure



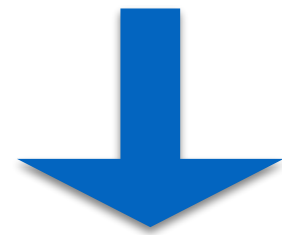
Time to re-examine
some of the
underlying pieces

Are they up to the
task of the precision era?

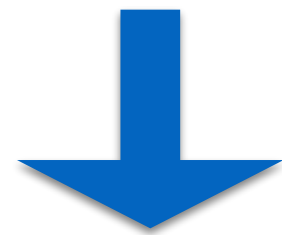
From Daniel Whiteson
Inspired by [XKCD](#)

Outline: A predictable evolution over ten years

Fear: Will ML exacerbate uncertainties in a way human-designed strategies naturally avoid ?



Solution: Find ML equivalents of uncertainty mitigation tricks we implicitly use in classical methods.
Understand good and bad ways to use ML



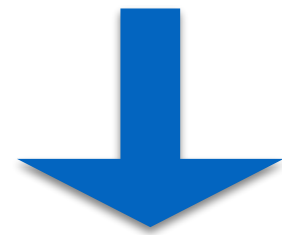
Opportunity: ML *for* uncertainty – Realising that ML unlocks completely new methods to tackle uncertainties in a way classical methods couldn't



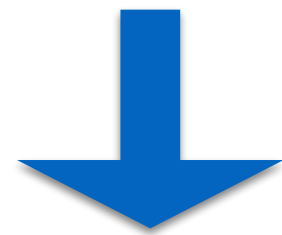
Revolution: Novel ML uncertainty quantification & mitigation methods have wider applications, also back-ported to traditional algorithms

Outline: A predictable evolution over ten years

Fear: Will ML exacerbate uncertainties in a way human-designed strategies naturally avoid ?



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*We are
here*



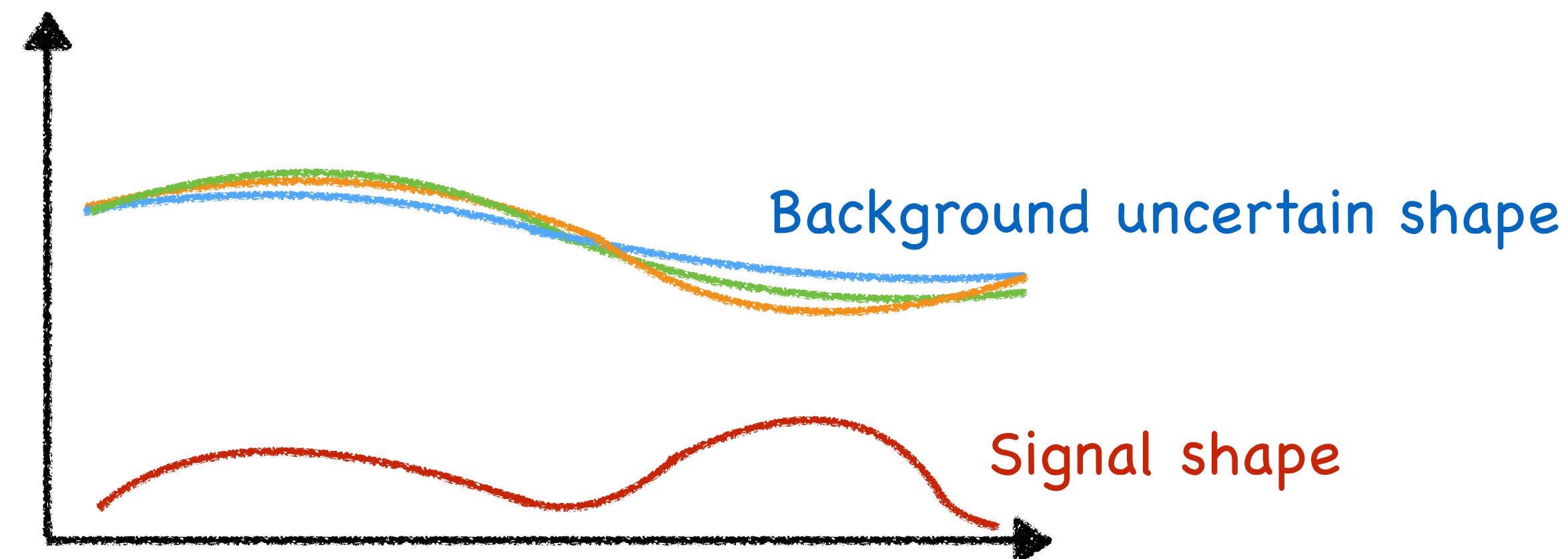
Revolution: Novel ML uncertainty quantification & mitigation methods have wider applications, also back-ported to traditional algorithms

Observable Sensitive to Nuisance Parameters

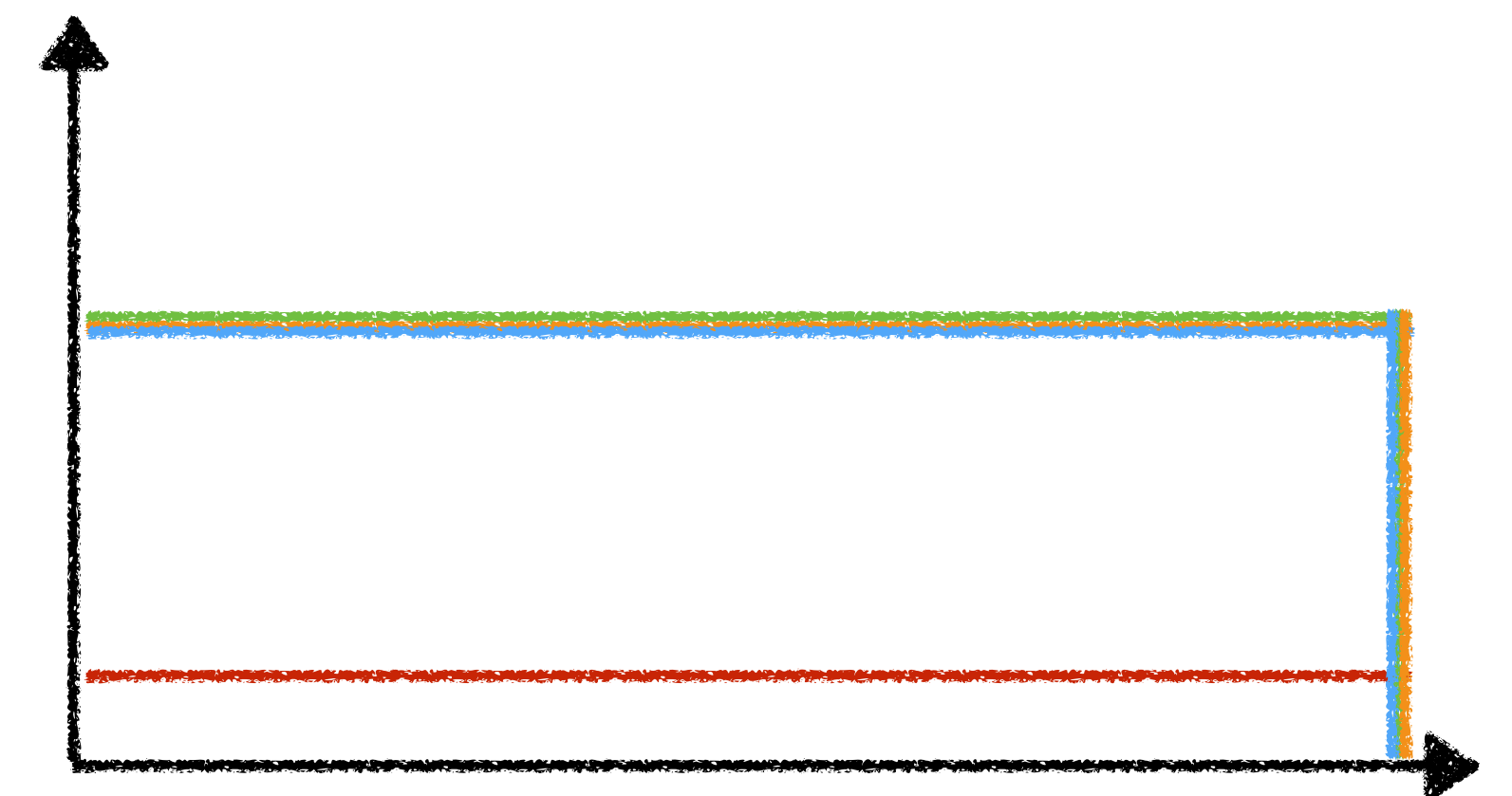
Traditionally, we reduce impact of NP by sacrificing something:

- Don't use observable
- Don't use phase space which is badly modelled by simulation
- Reduce sensitivity some other way

Infinite bin analysis, very sensitive to shape uncertainty



Single bin analysis, insensitive to shape uncertainty



ML equivalent problem: Domain Adaptation

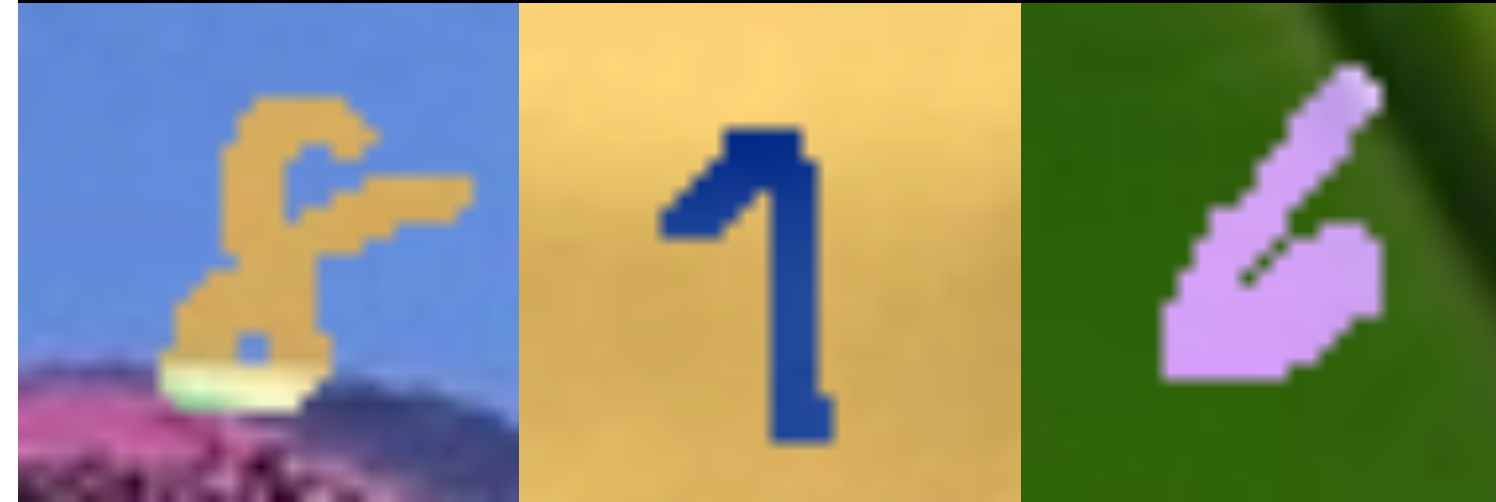
[arXiv:1505.07818](https://arxiv.org/abs/1505.07818)

MNIST

SOURCE

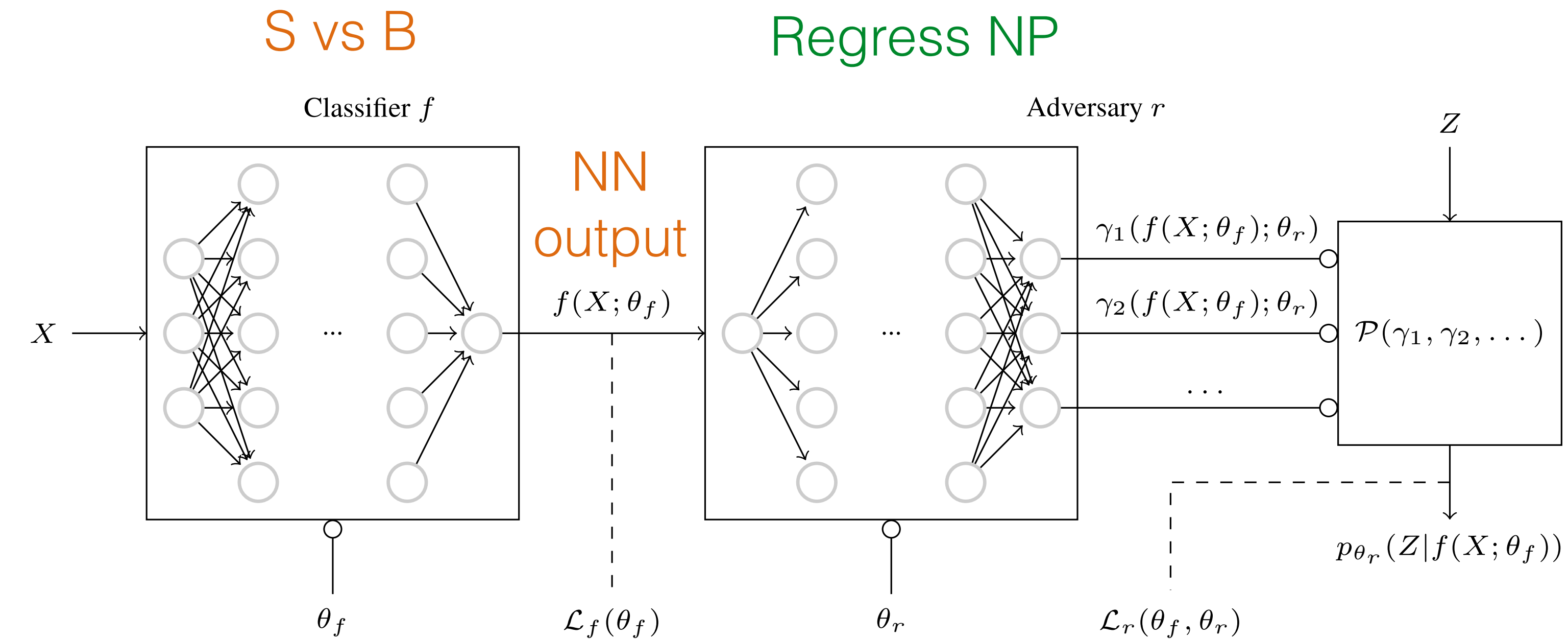


TARGET



MNIST-M

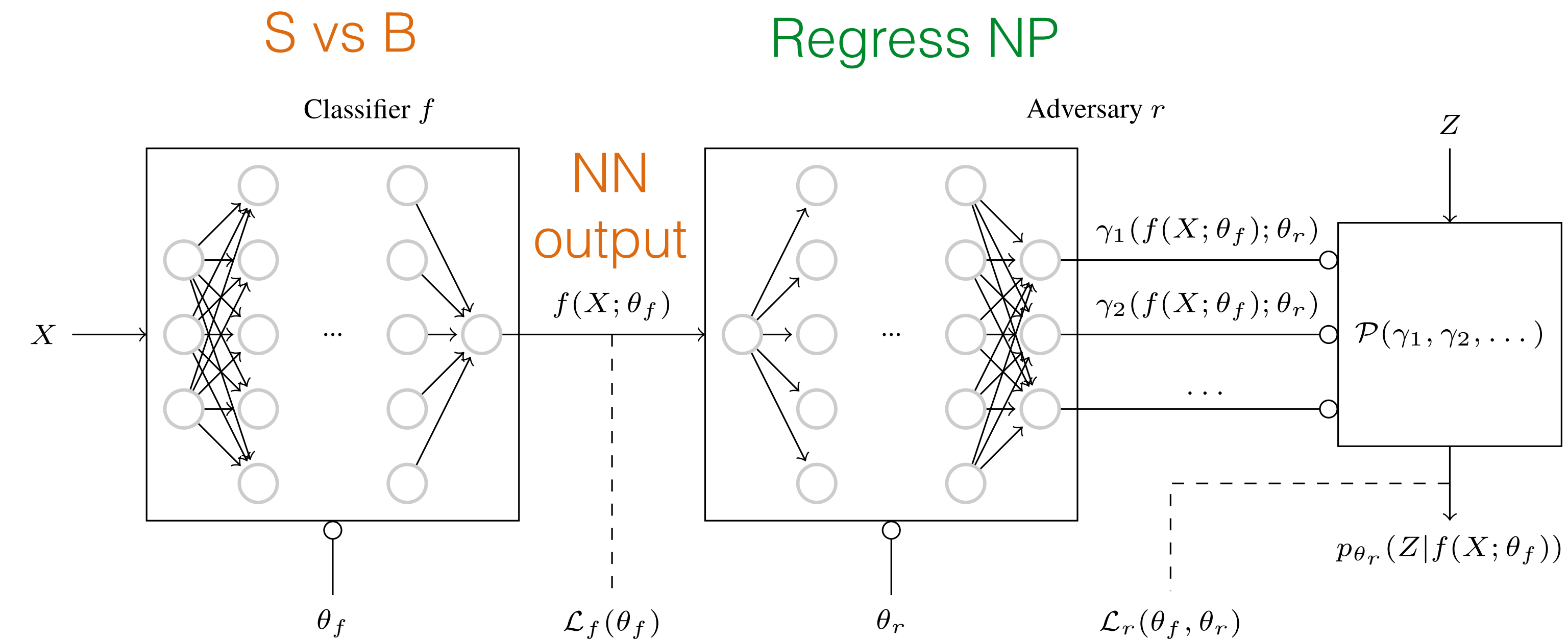
Adversarial decorrelation



[Learning to Pivot, Louppe et al.](#)

$$L_{Classifier} = L_{Classification} - \lambda \cdot L_{Adversary}$$

Adversarial decorrelation

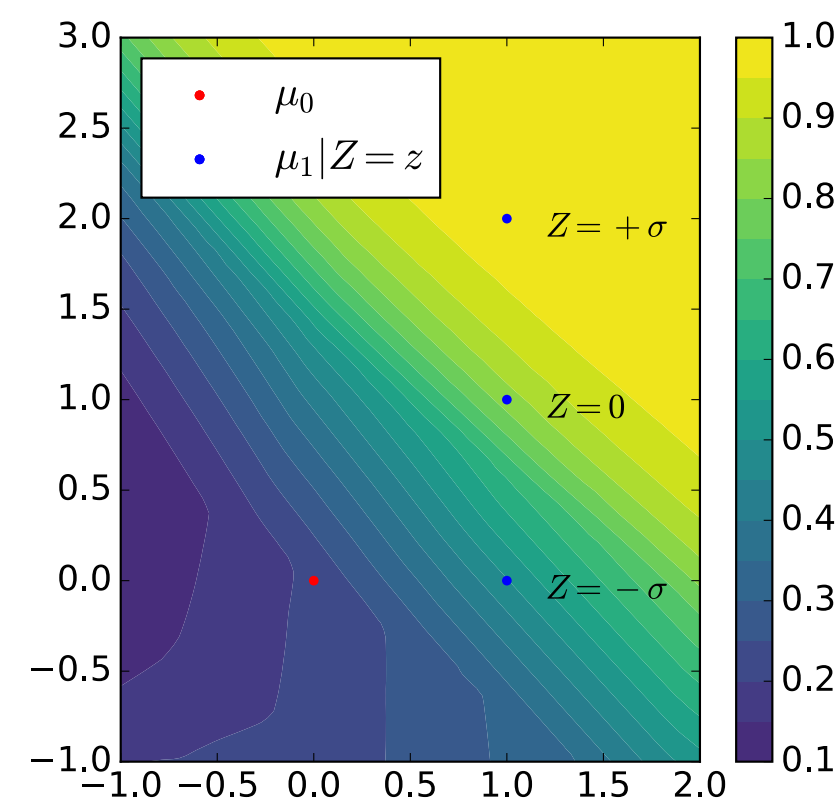
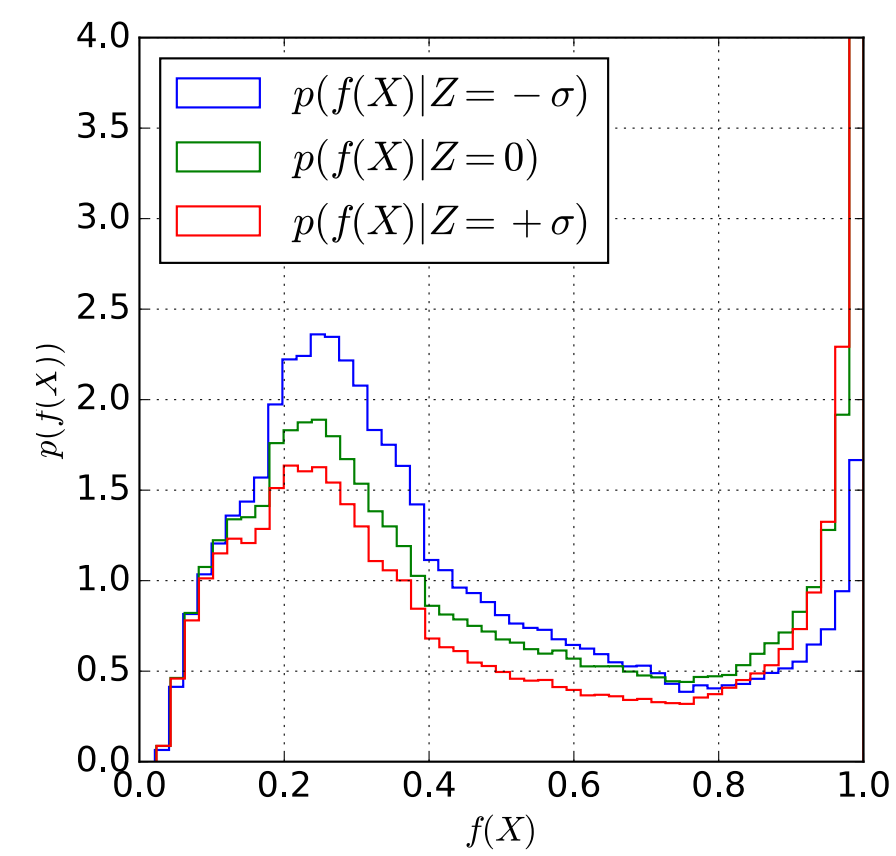


To fool the adversary, classifier output should be decorrelated to Z

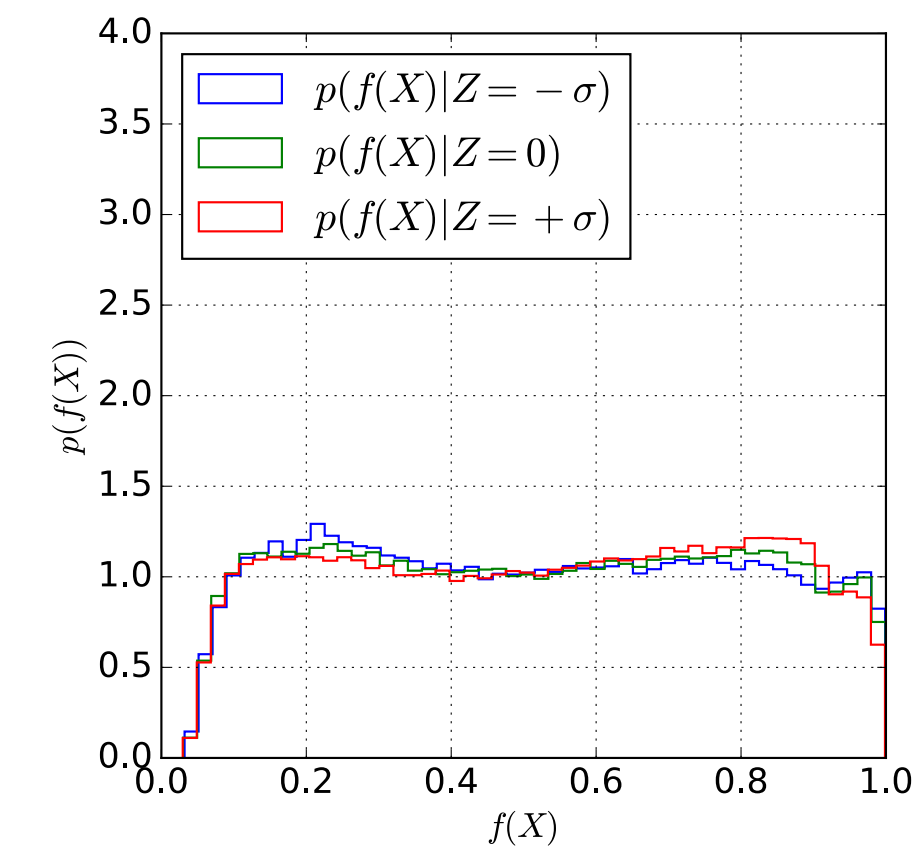
[Learning to Pivot, Louppe et al.](#)

$$L_{Classifier} = L_{Classification} - \lambda \cdot L_{Adversary}$$

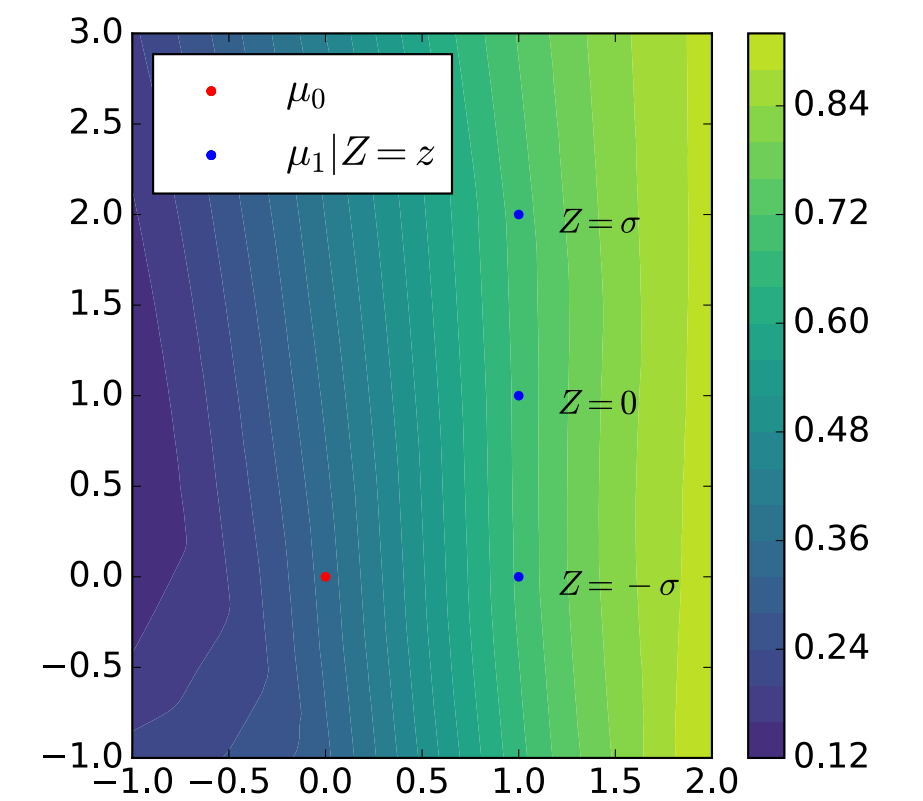
ML-Decorrelation Methods



Adversarial Decorrelation



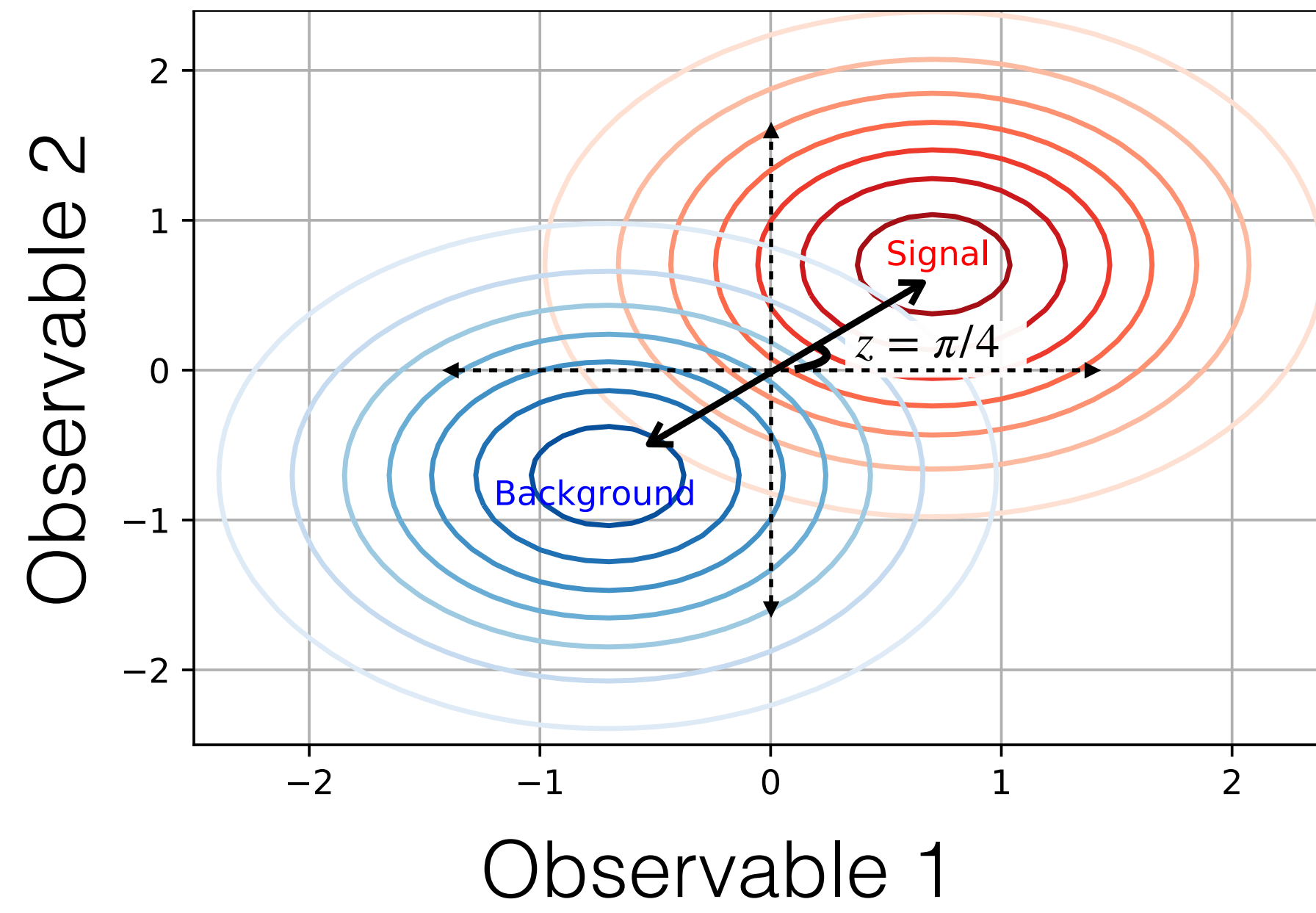
Classifier output for various values of Z



[Learning to Pivot, Louppe et al.](#)

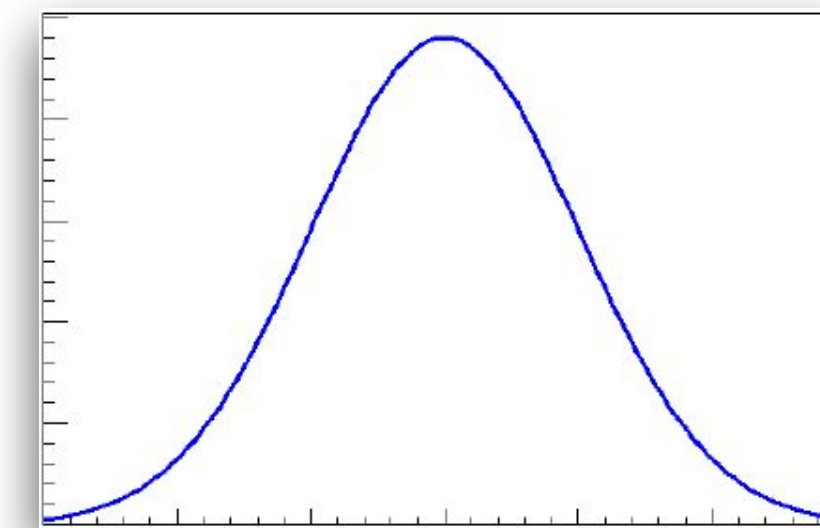
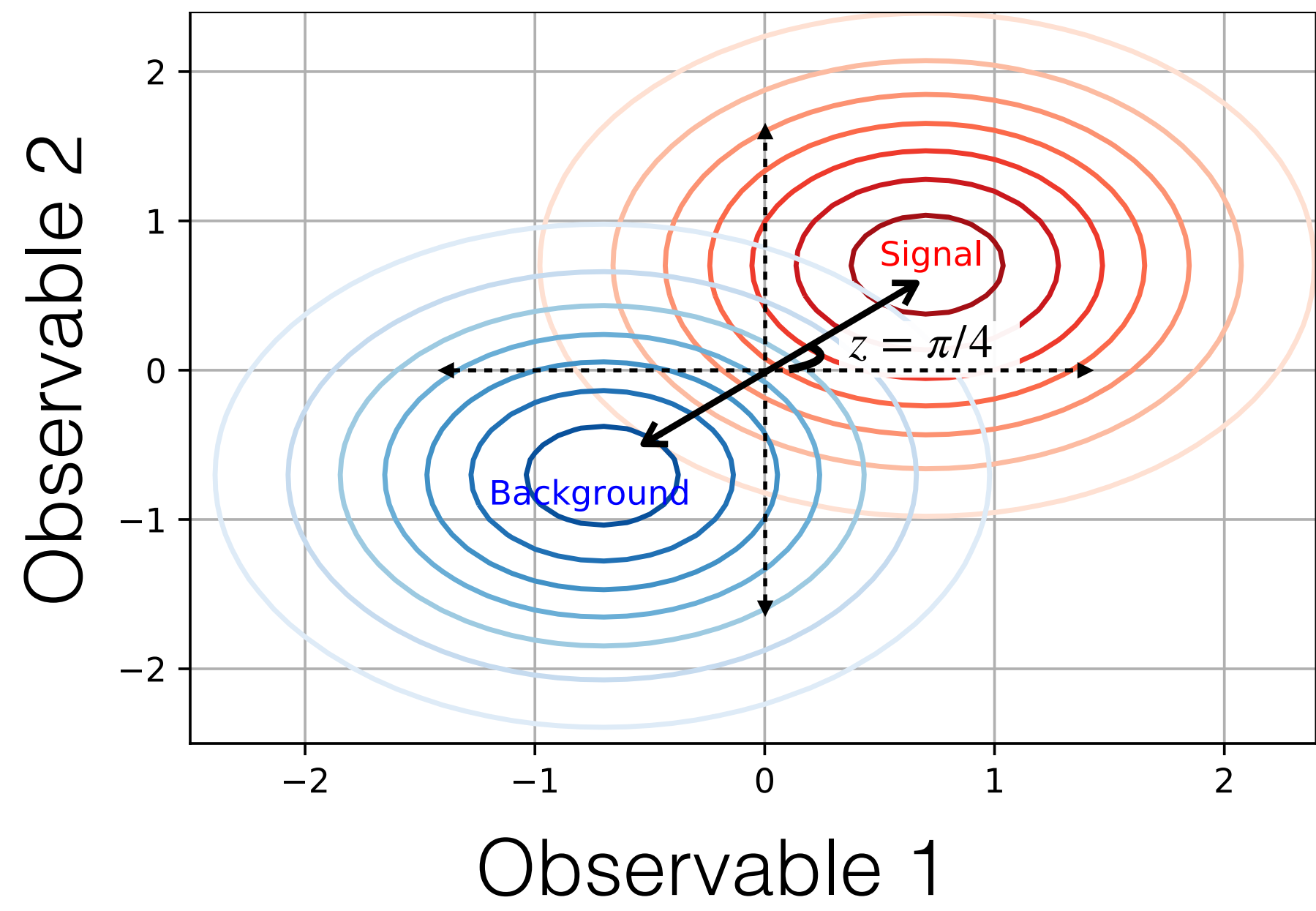
What if we could do better ?

What if we could do better ?

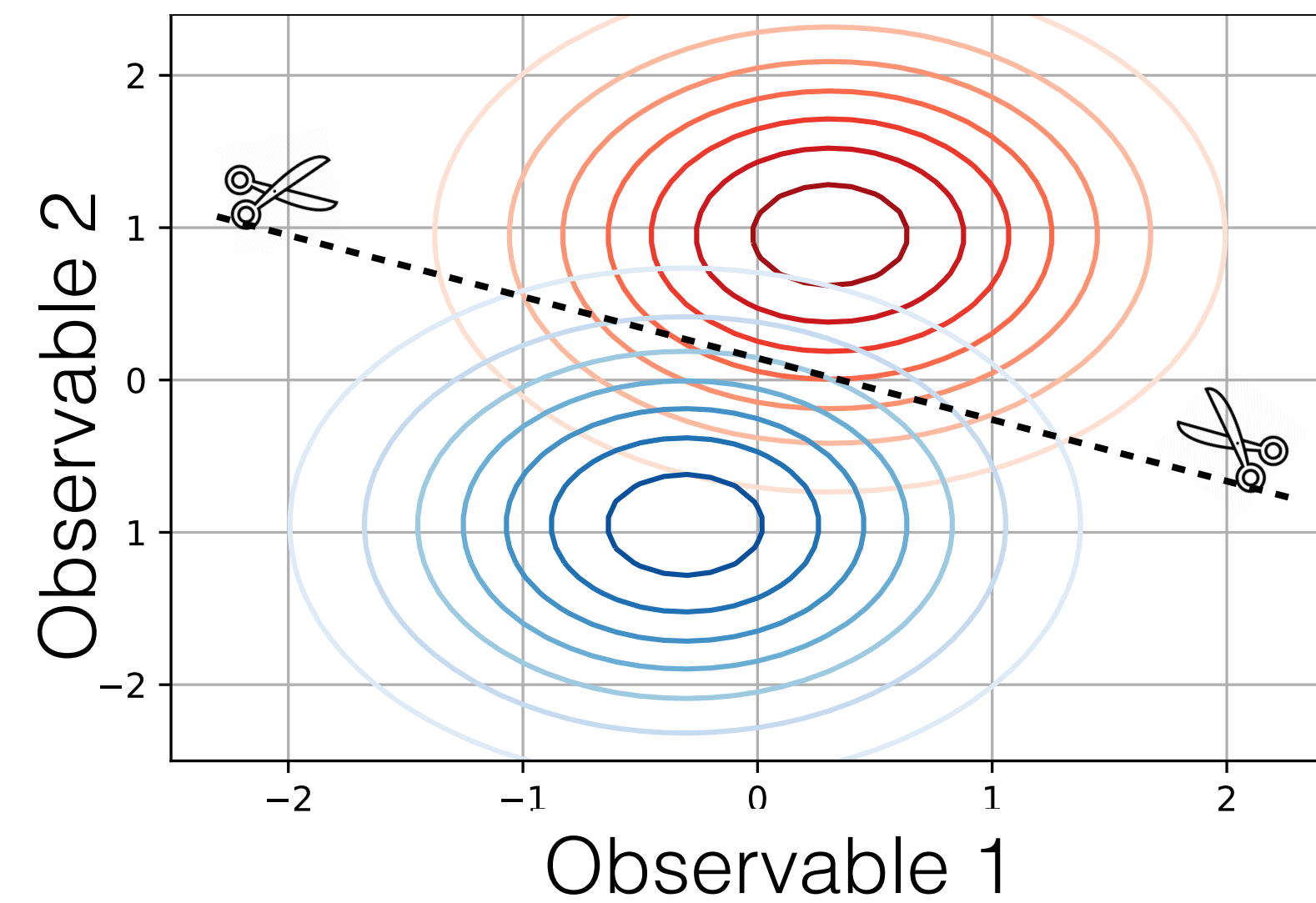
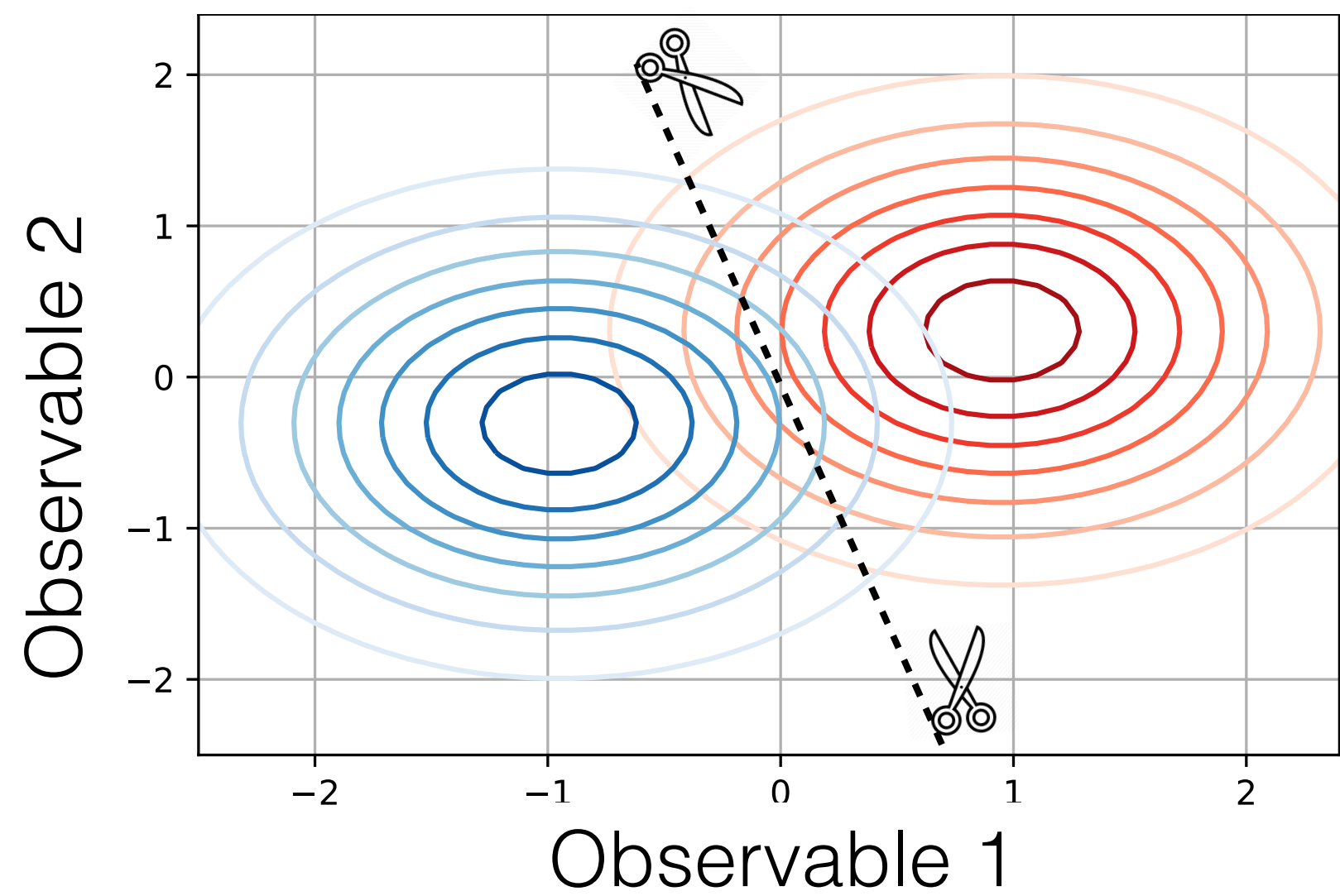


z = Nuisance Parameter

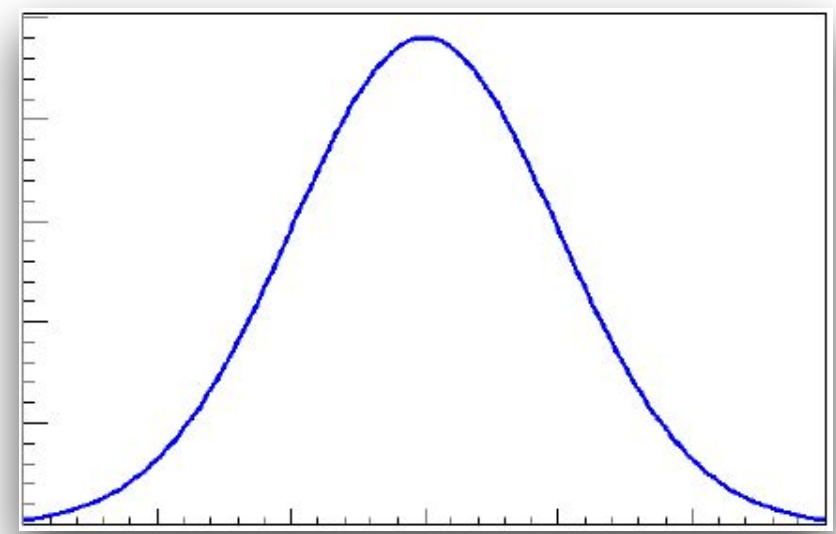
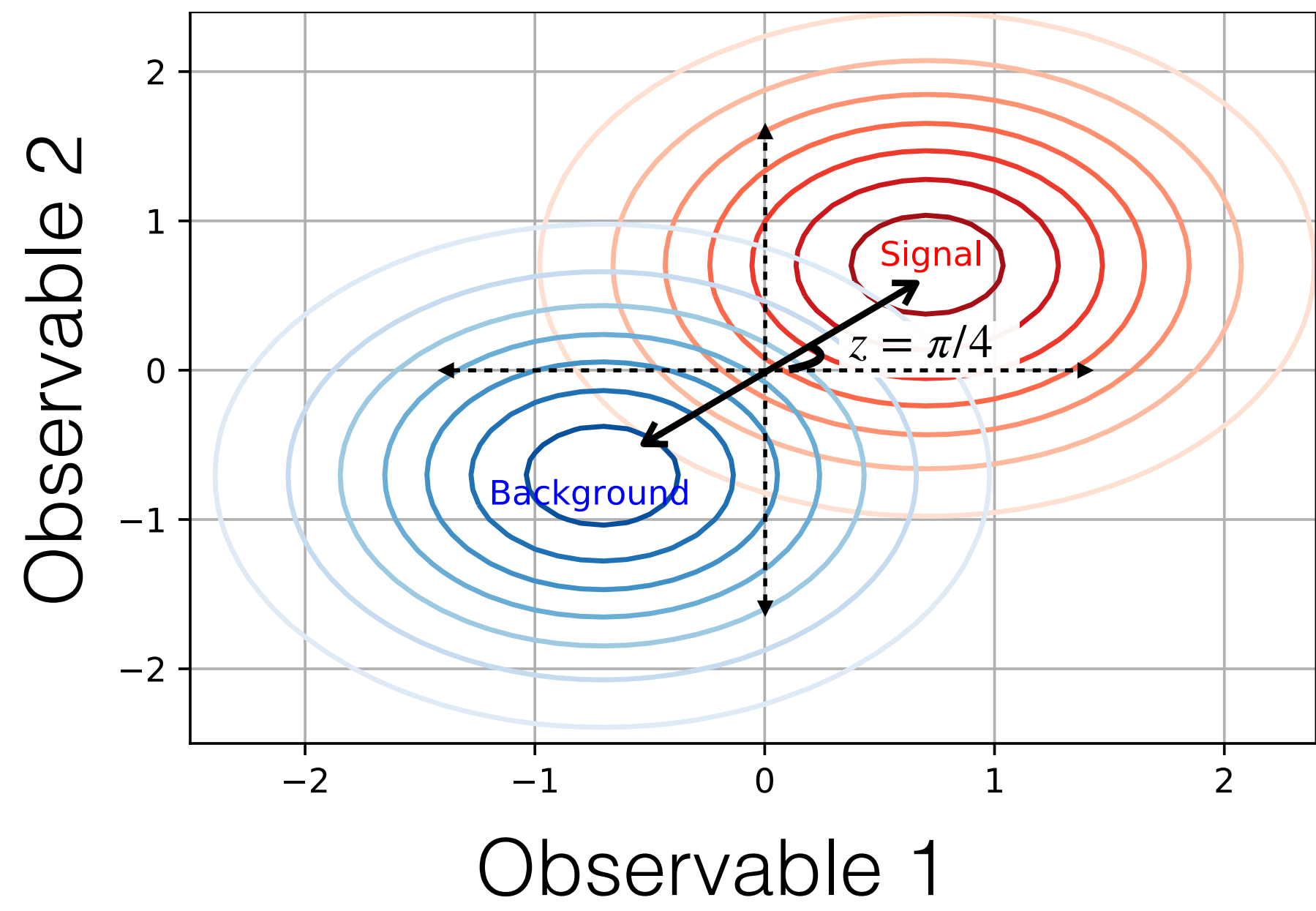
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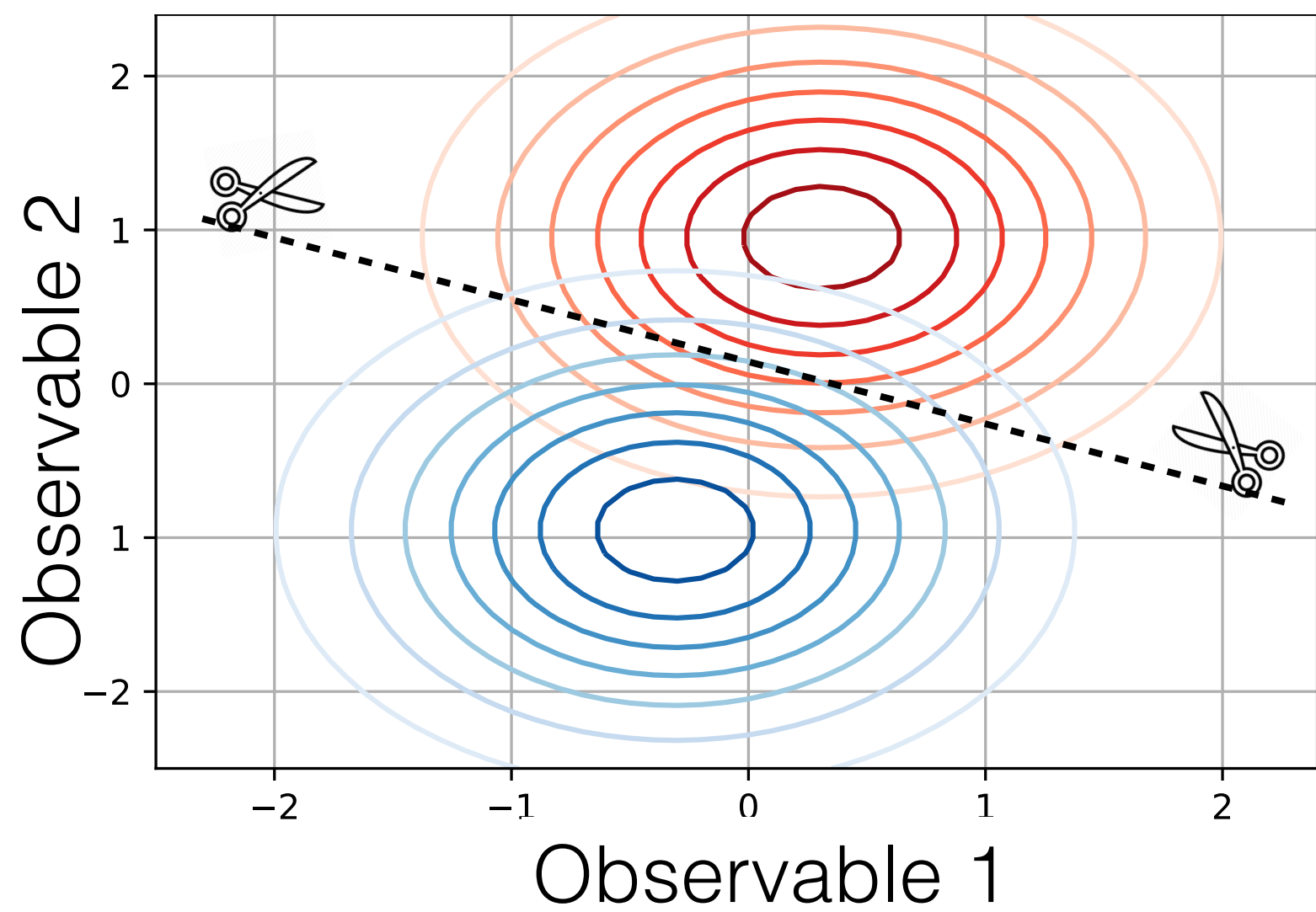
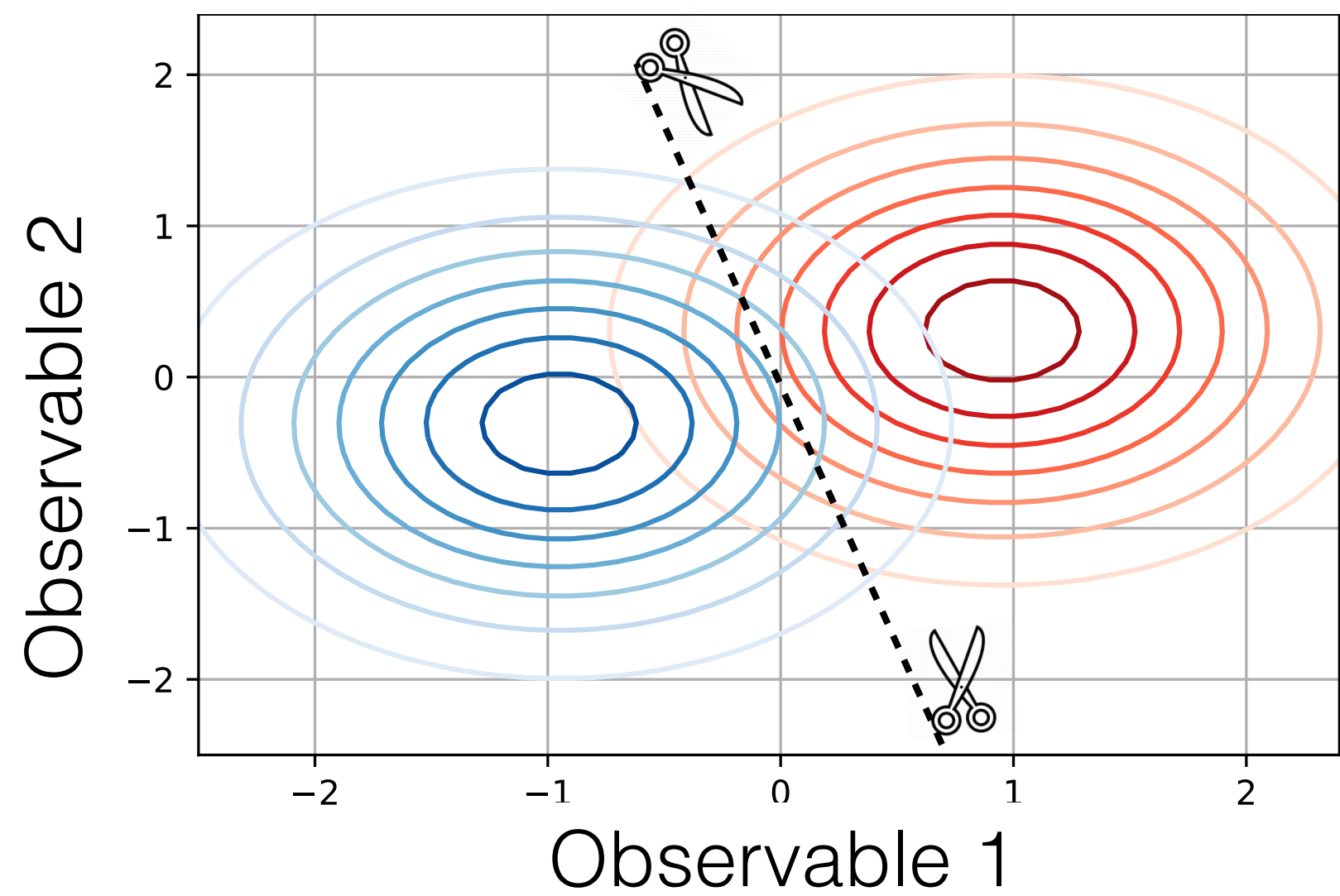
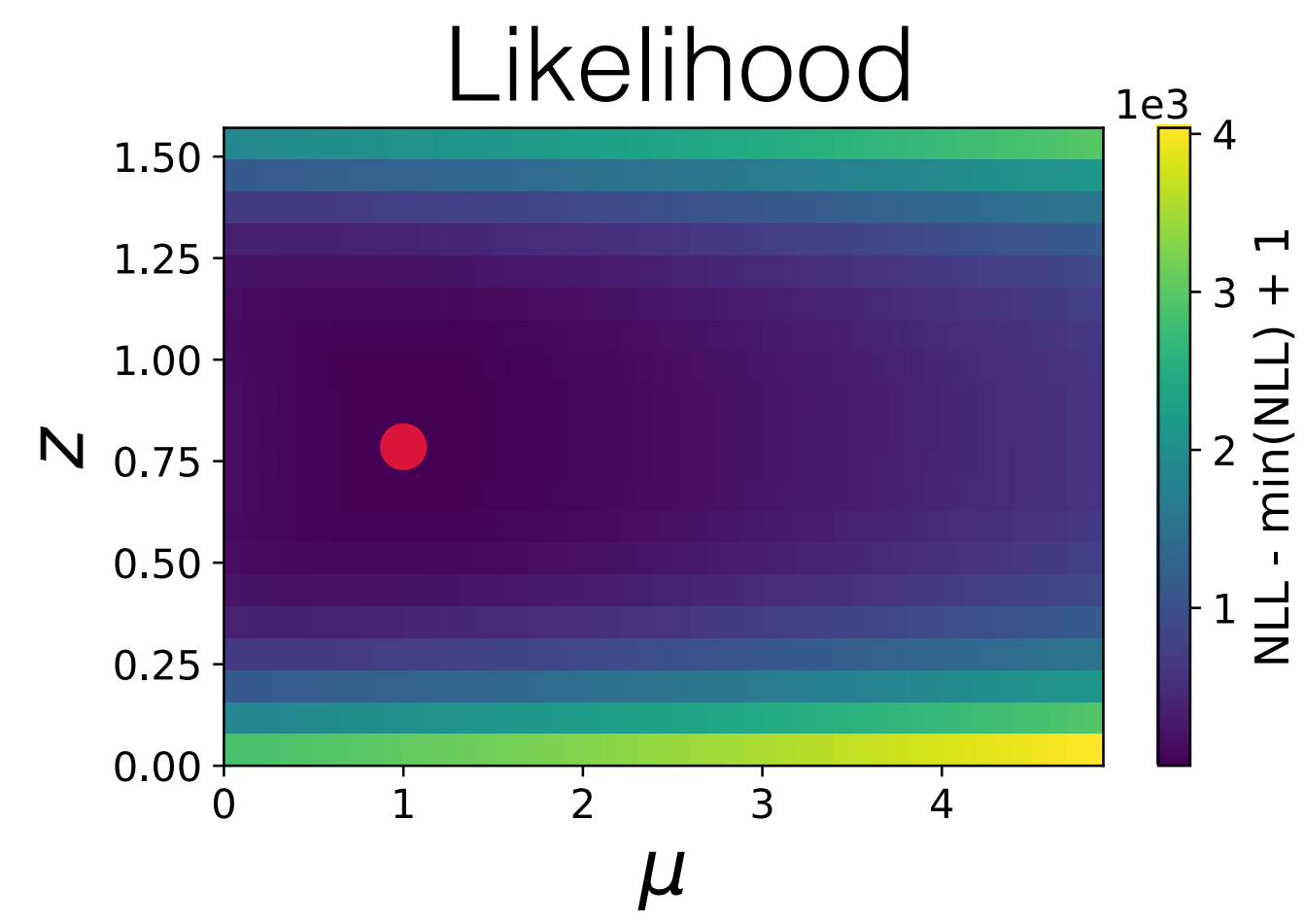
z = Nuisance Parameter
Prior



What if we could do better ?

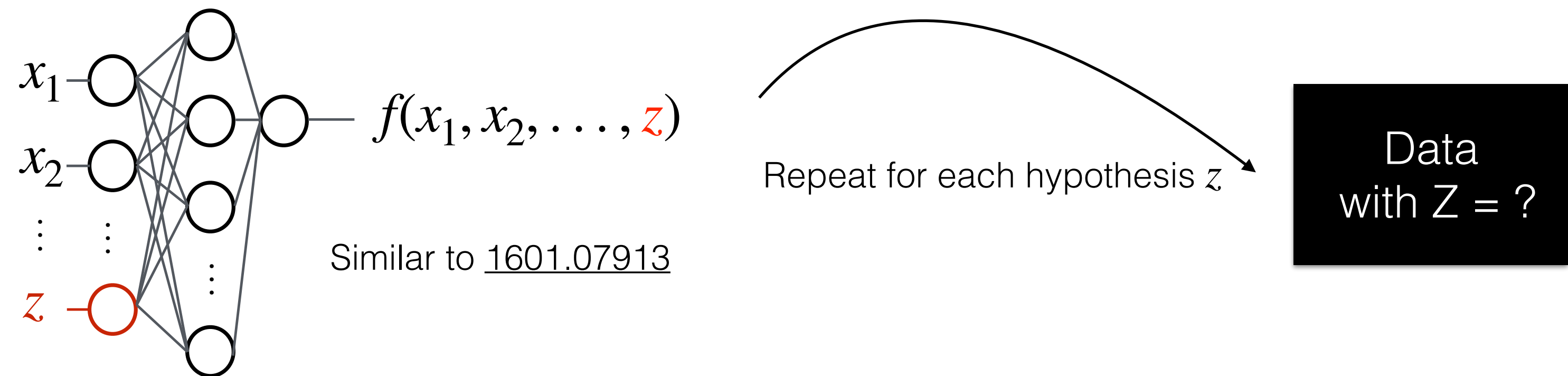


z = Nuisance Parameter
Prior



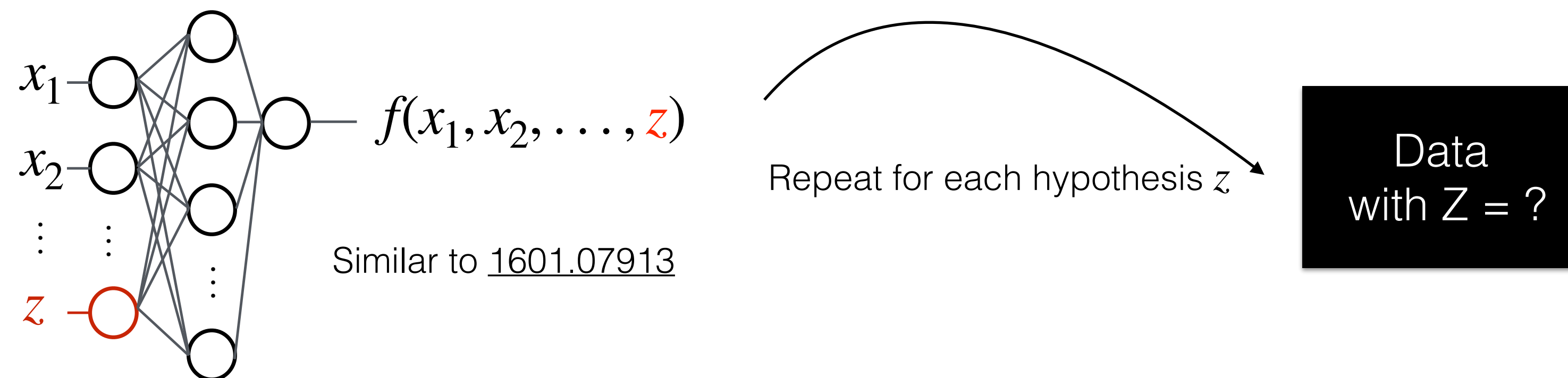
Opposite of decorrelation: Uncertainty-aware learning

- Propagate uncertainties through the classifier in an “uncertainty aware” way



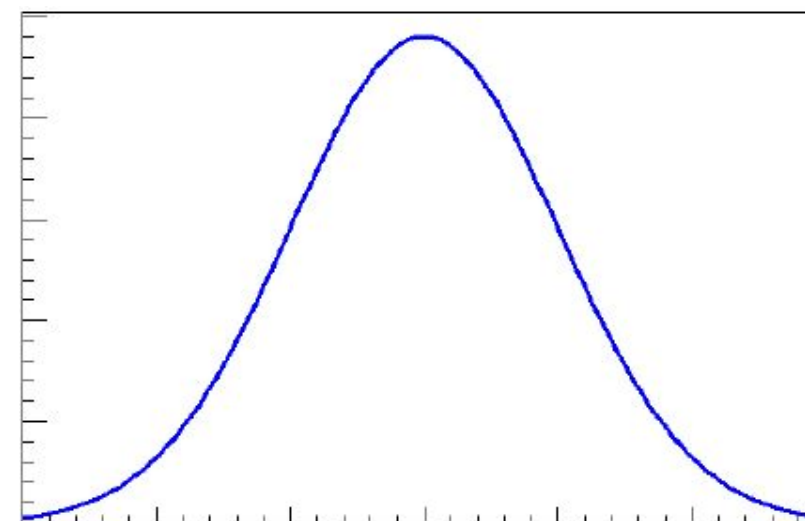
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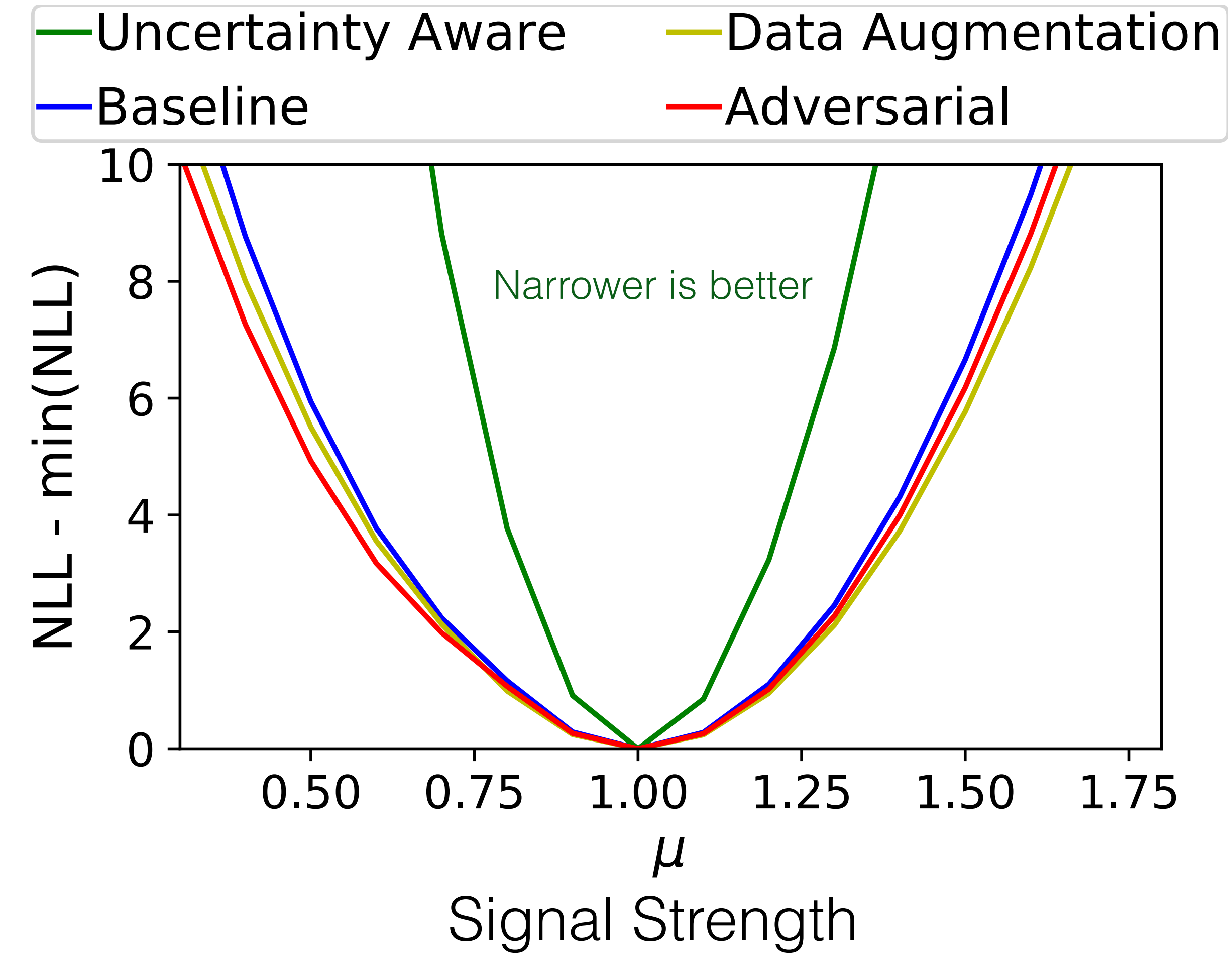


- Intuition: Allow the analysis technique to vary with Z
You always get the best classifier for each value of Z

- Profile Z + incorporate prior



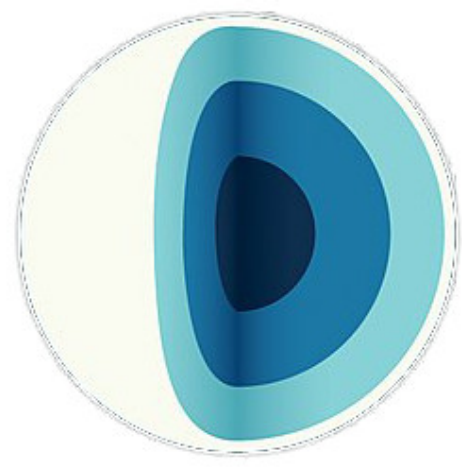
Better final measurements!



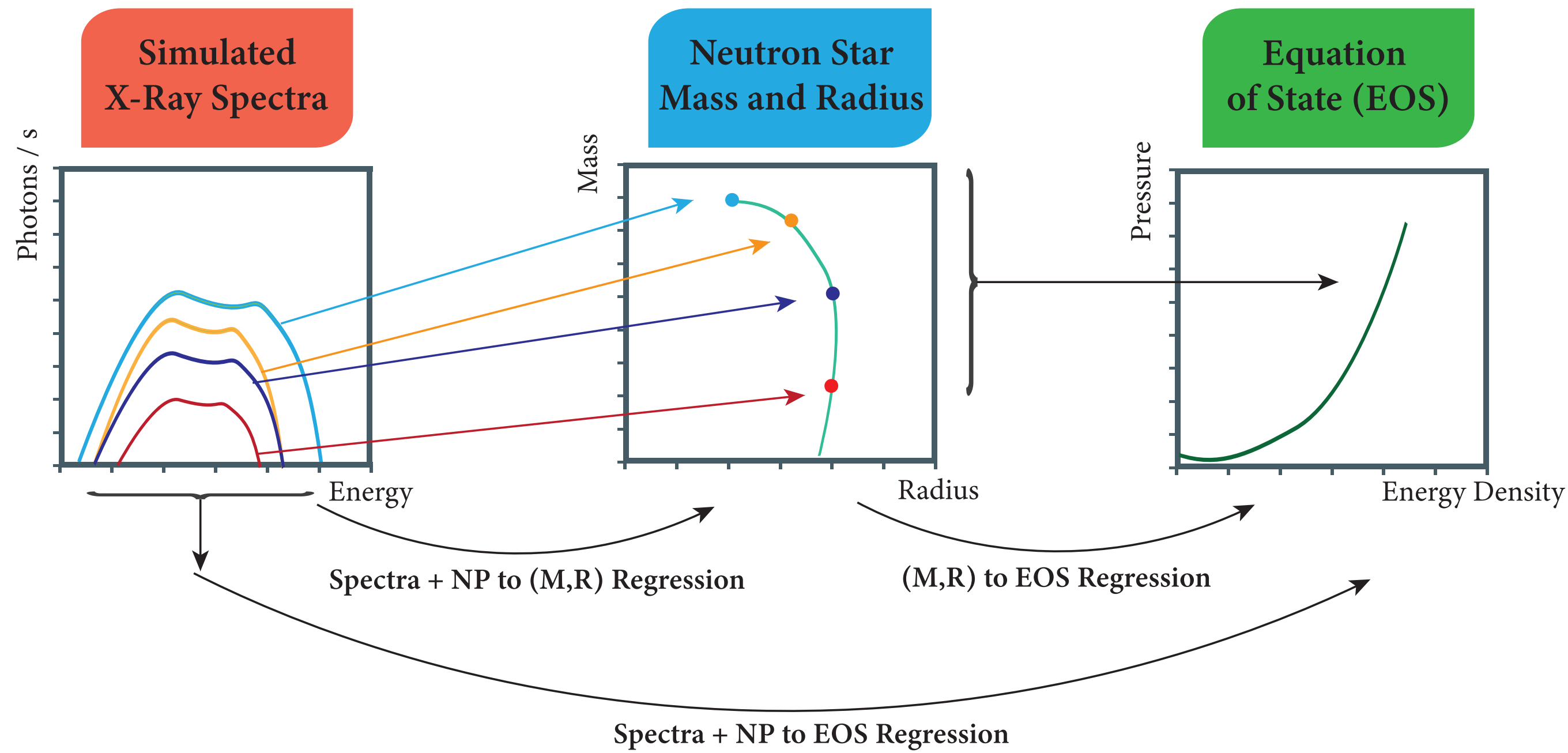
Narrower \Rightarrow Smaller [statistical + systematic] uncertainty on measurement

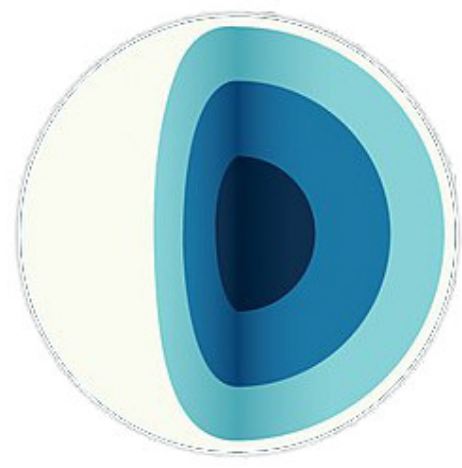
Practical for LHC analysis: Parameterise your main nuisance parameter but no need to train on all 100 NPs

An application in astrophysics

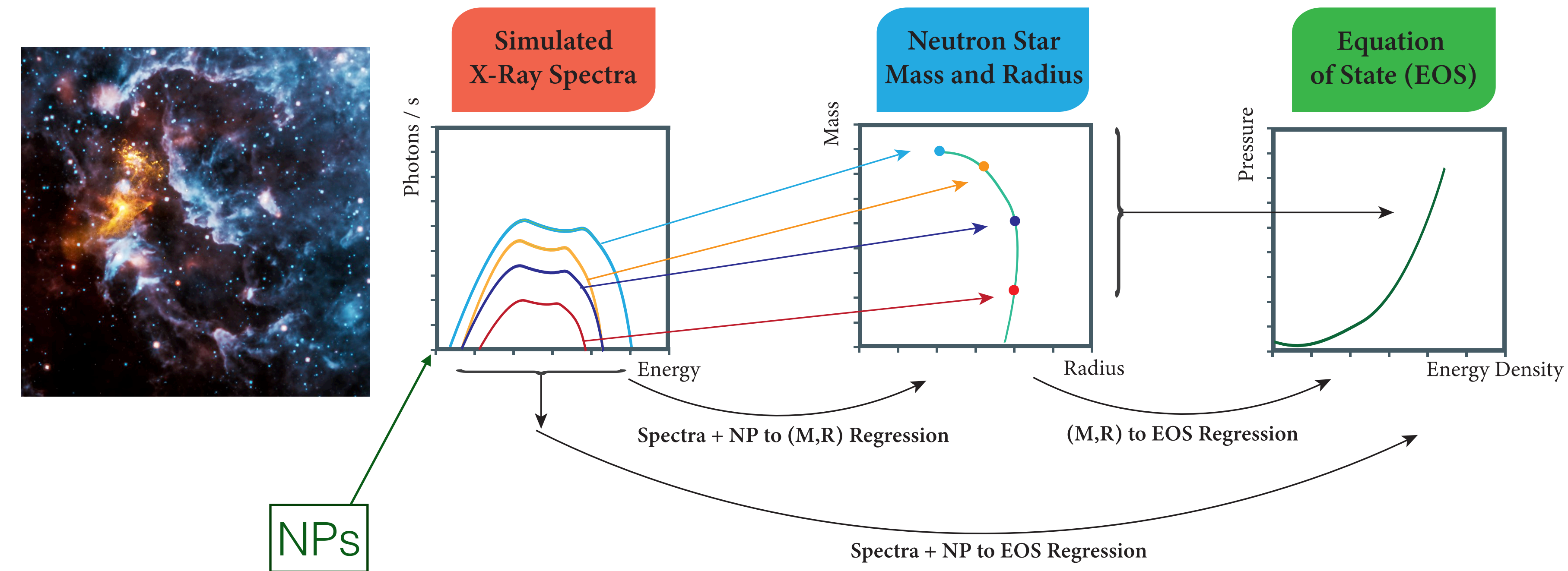


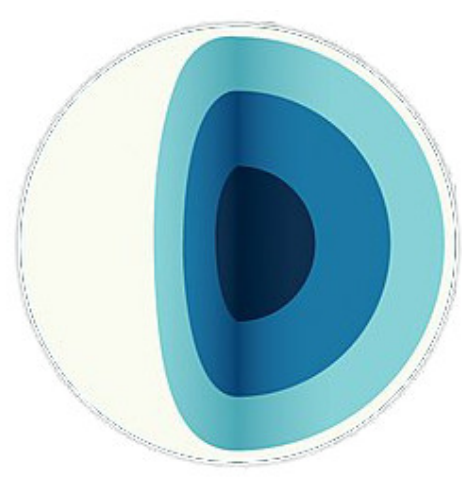
Application in Astrophysics: Full propagation of uncertainties





Application in Astrophysics: Full propagation of uncertainties

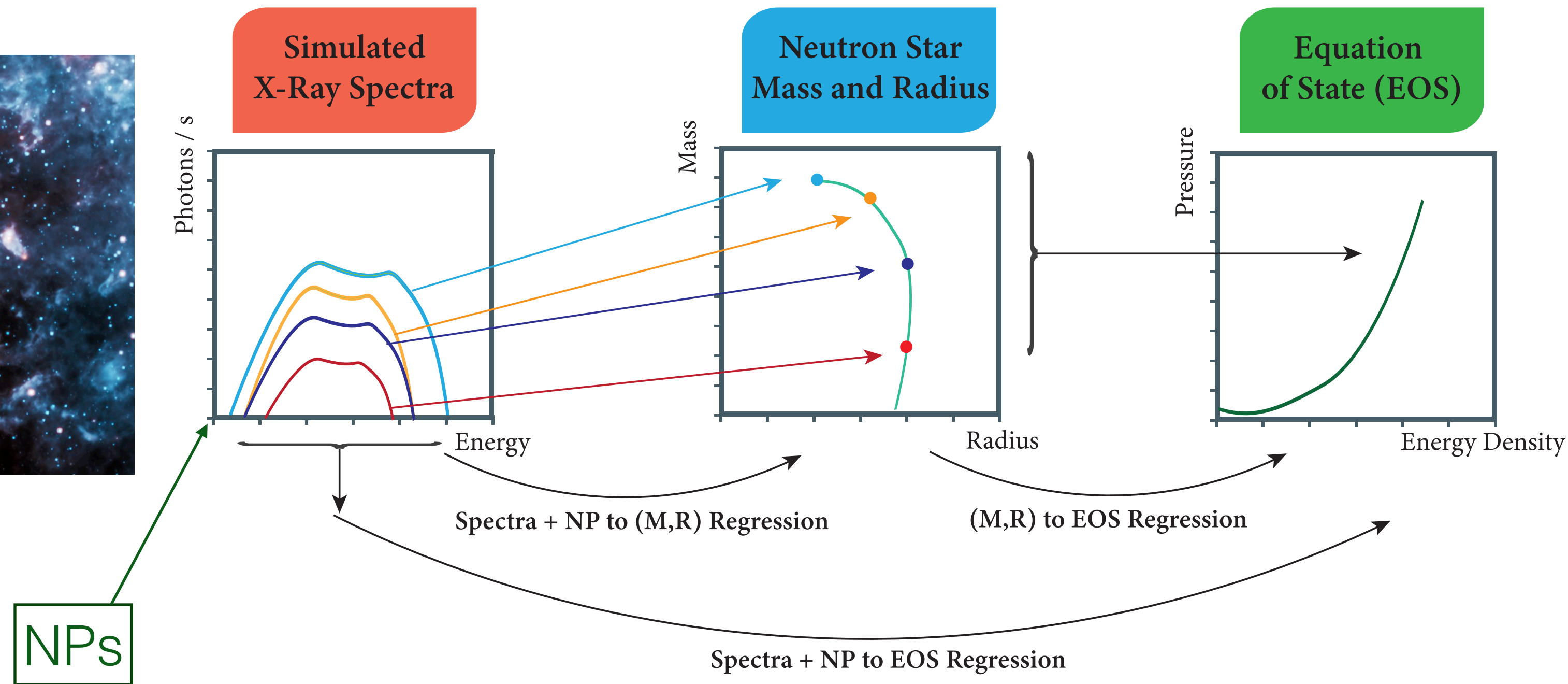
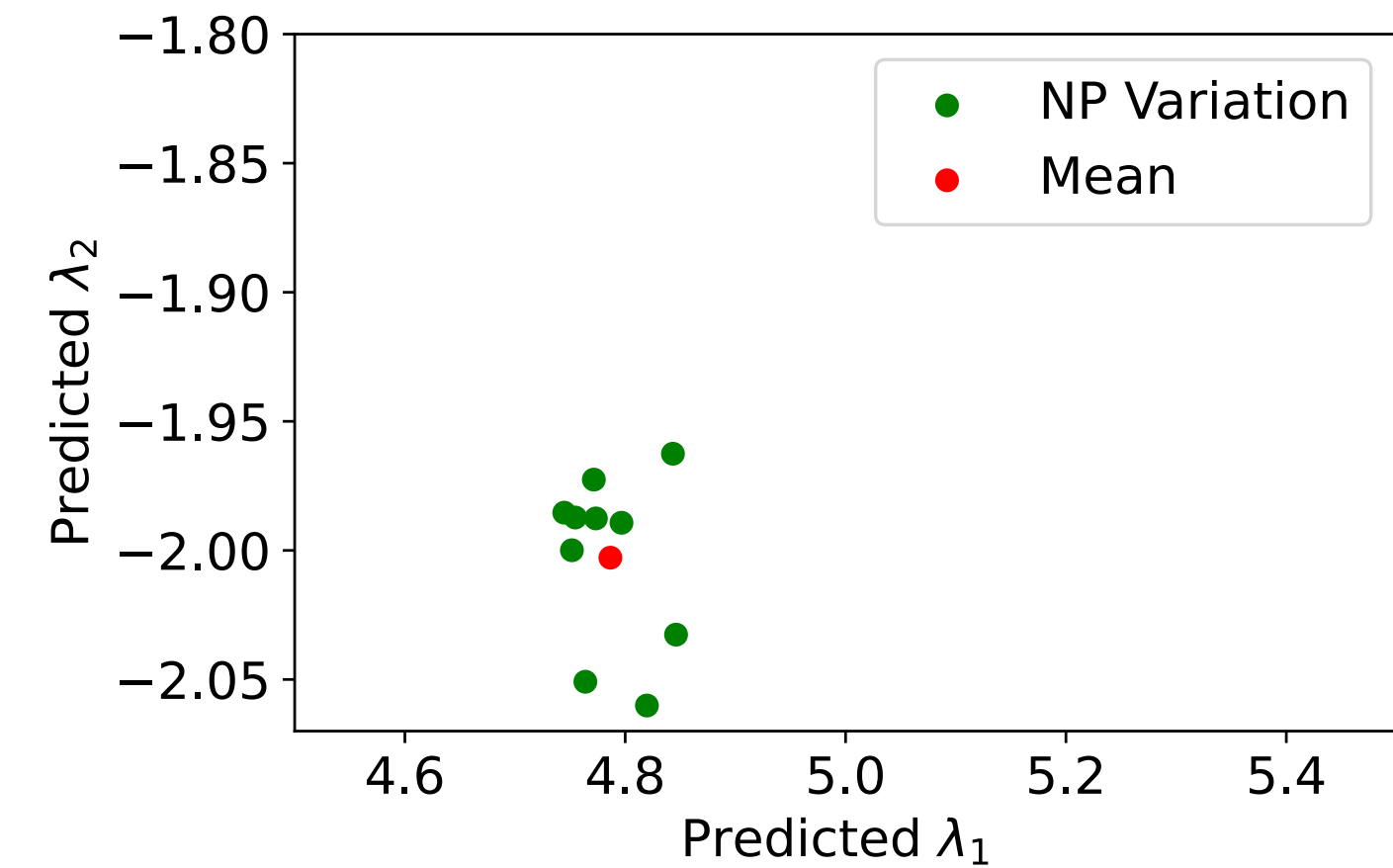
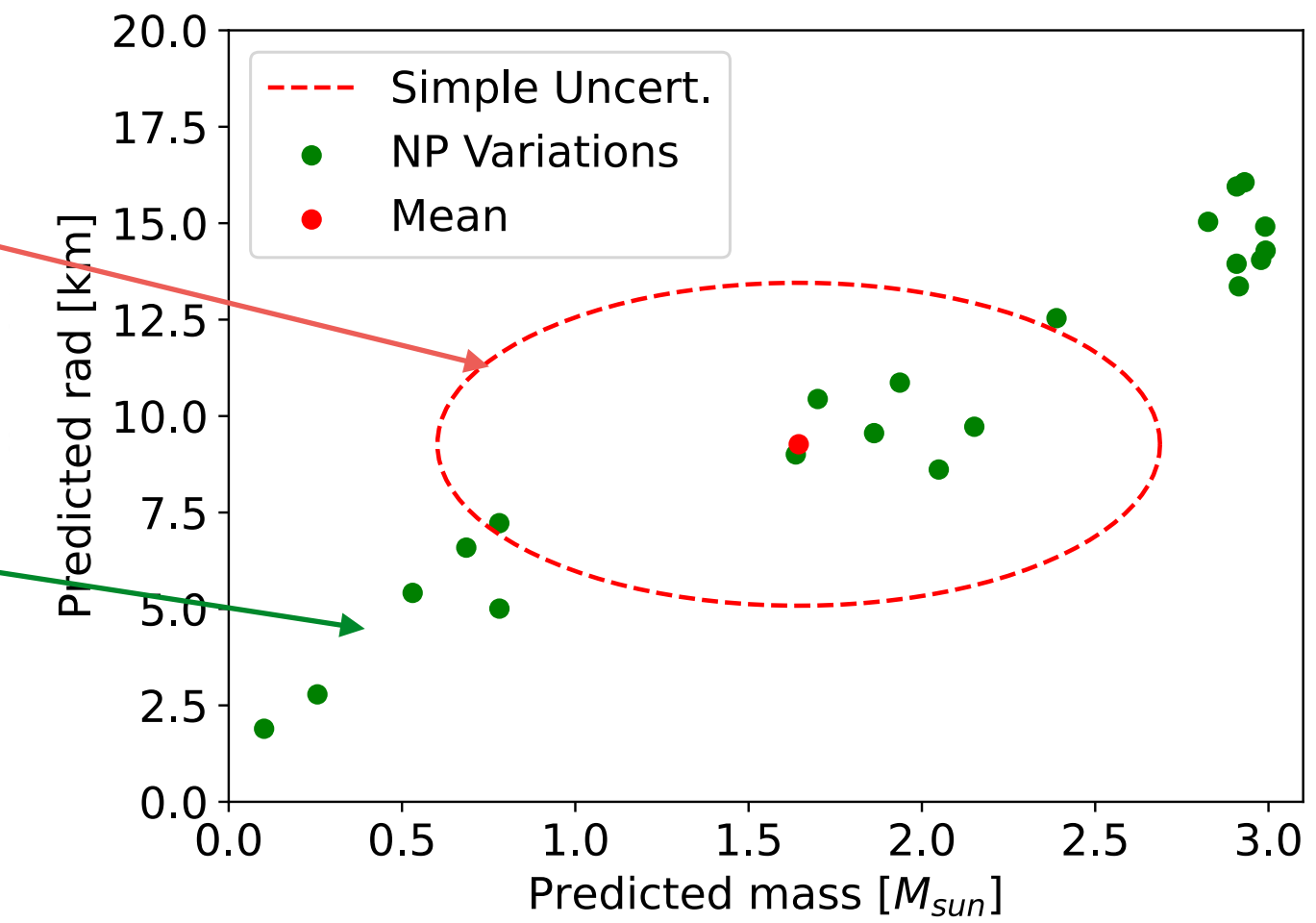


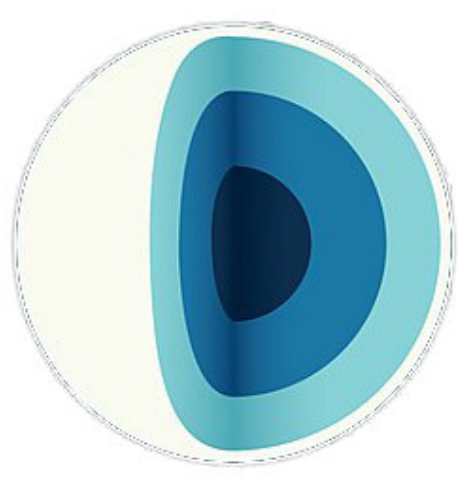


Application in Astrophysics: Full propagation of uncertainties

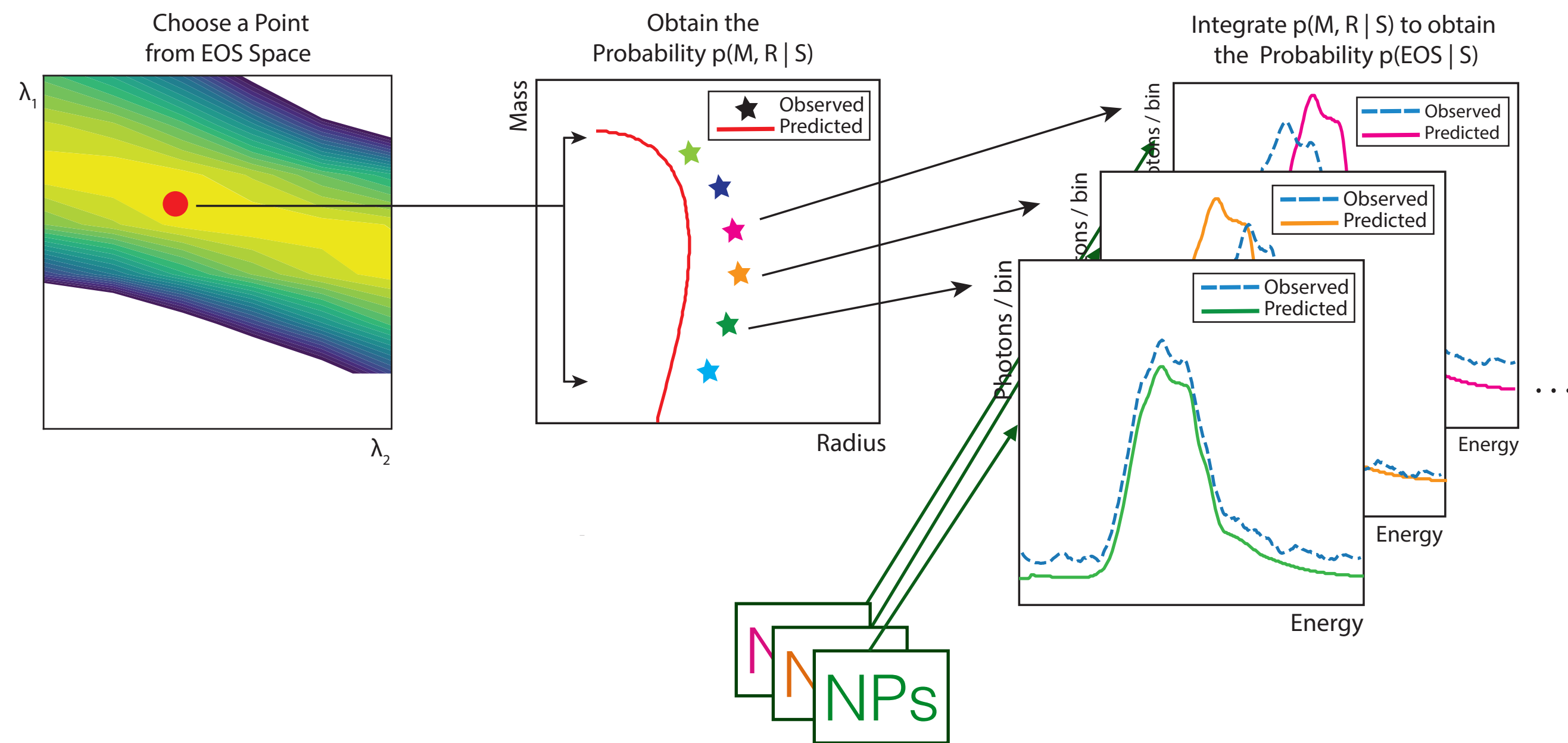
SOTA made a single point estimate + assumed uncorrelated Gaussian uncertainties

Real uncertainties look quite different





Learn forward process to access the likelihood



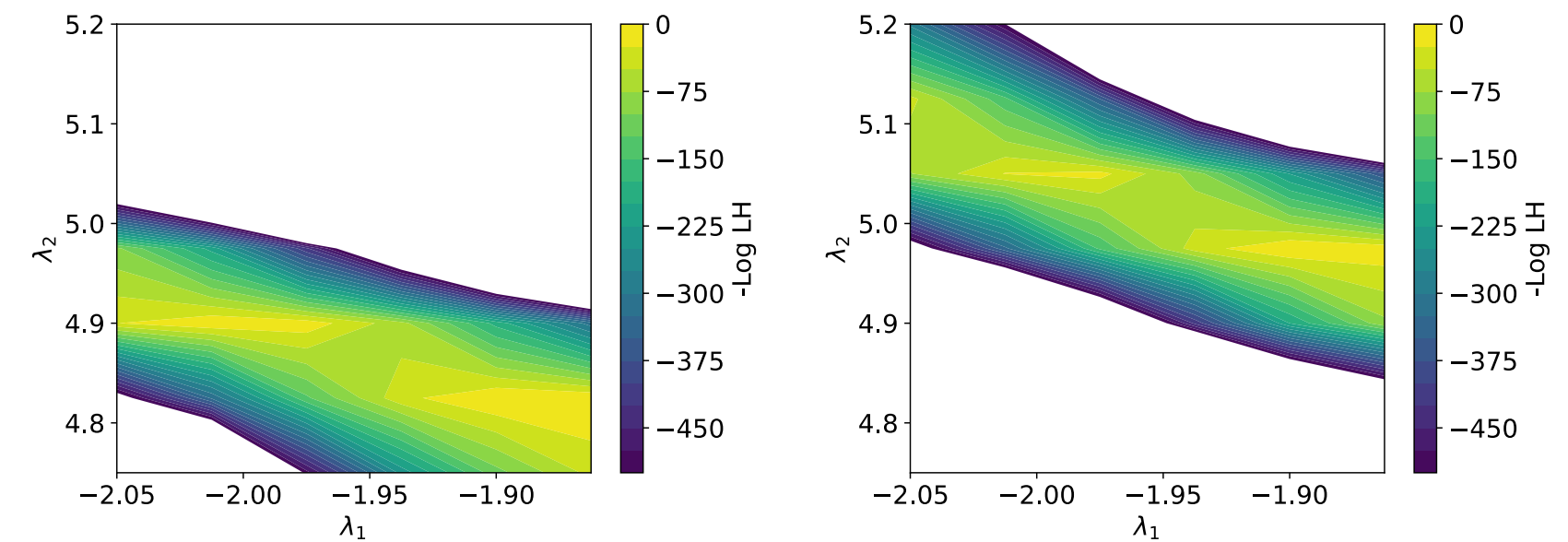
Deploy with ONNX Runtime to compute likelihoods on-the-fly



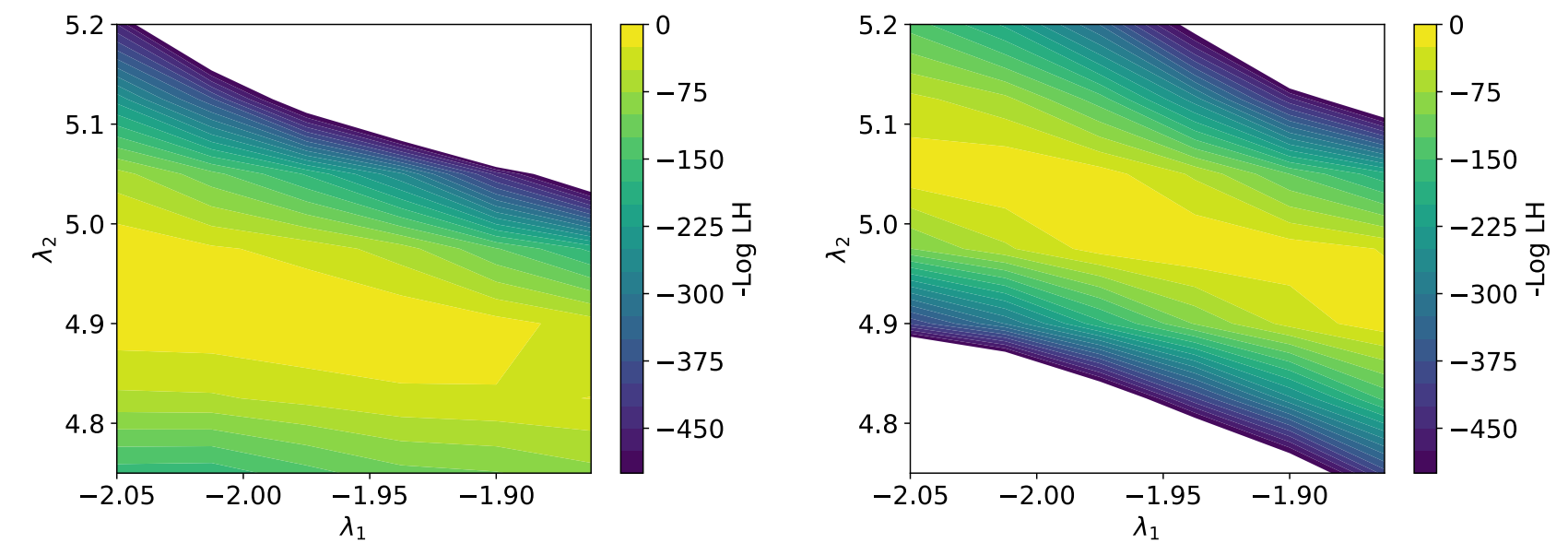
Nuisance
Priors:

EOS parameter
likelihoods:

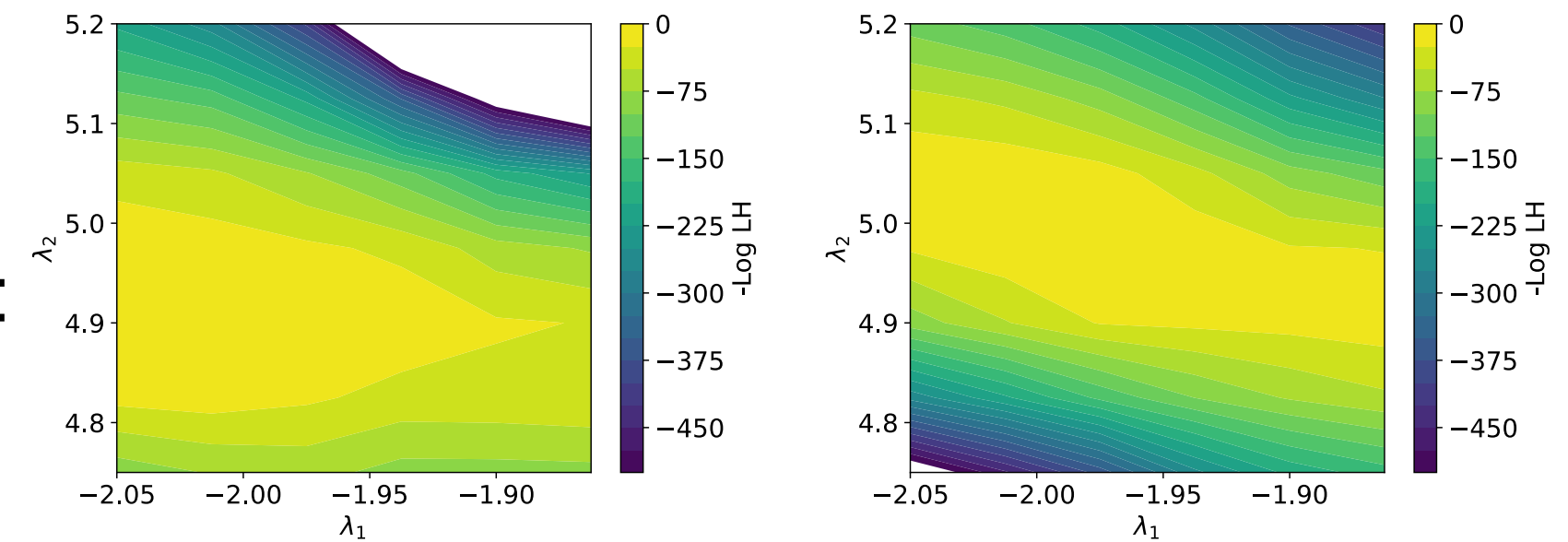
True:

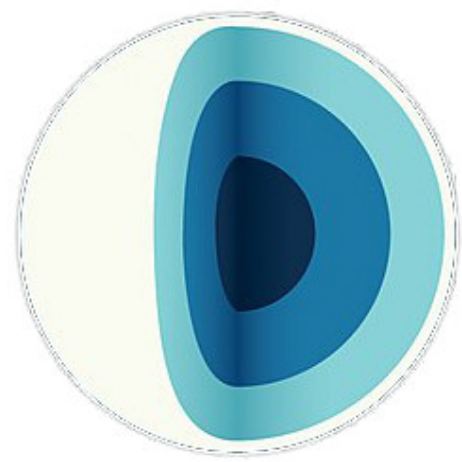


Tight:



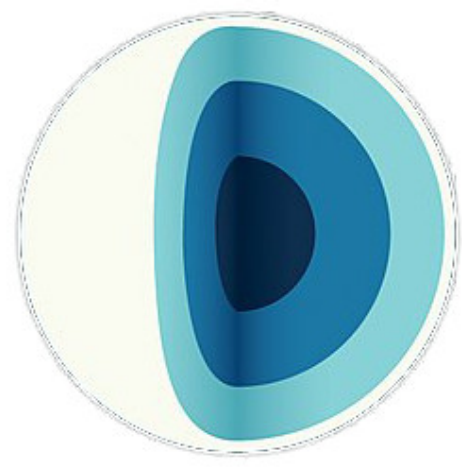
Loose:





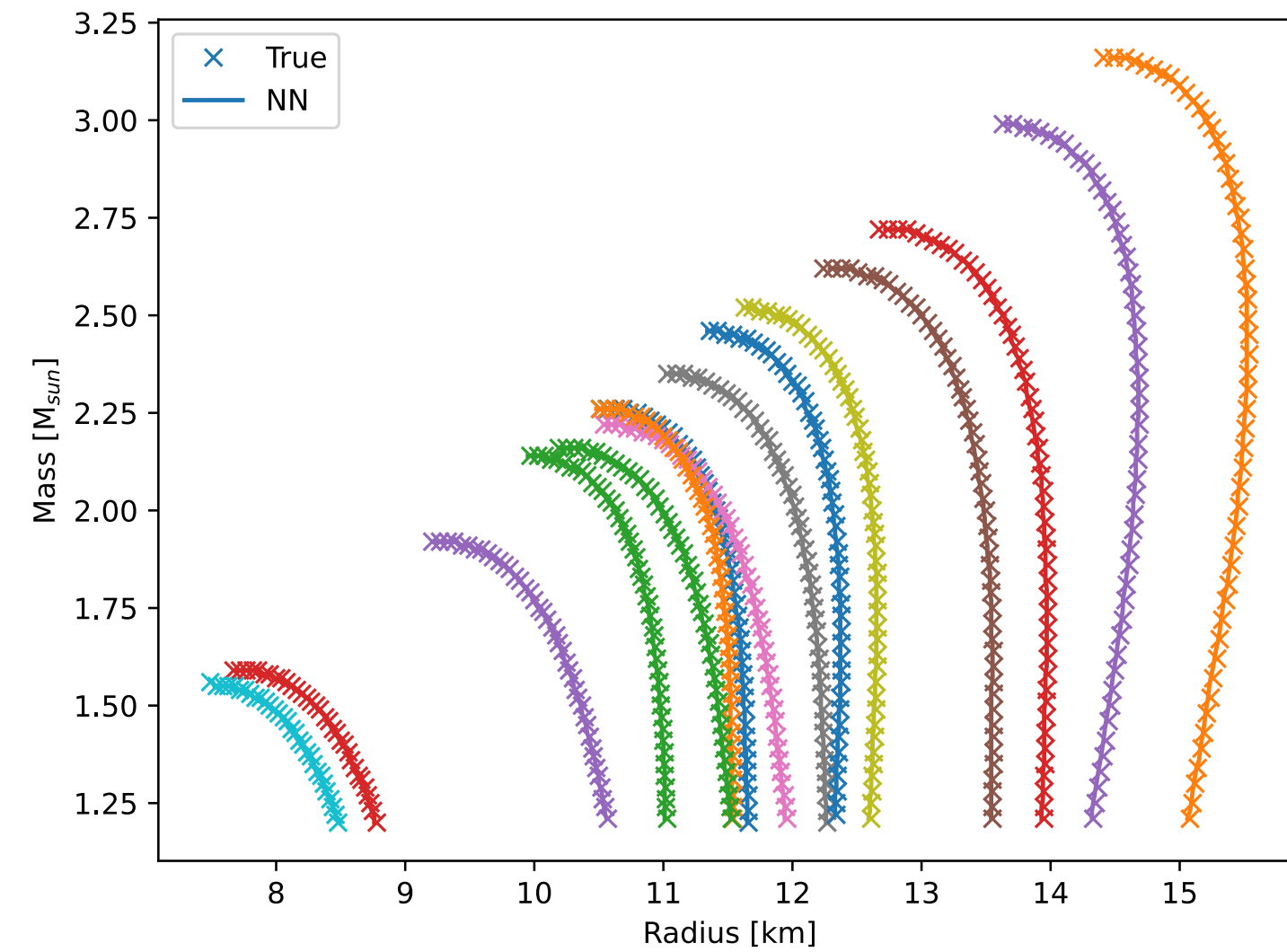
Forward process step-by-step

Intermediate steps remain interpretable physical quantities

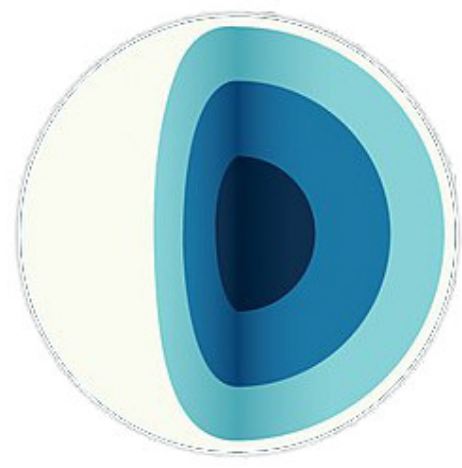


Forward process step-by-step

Intermediate steps remain interpretable physical quantities

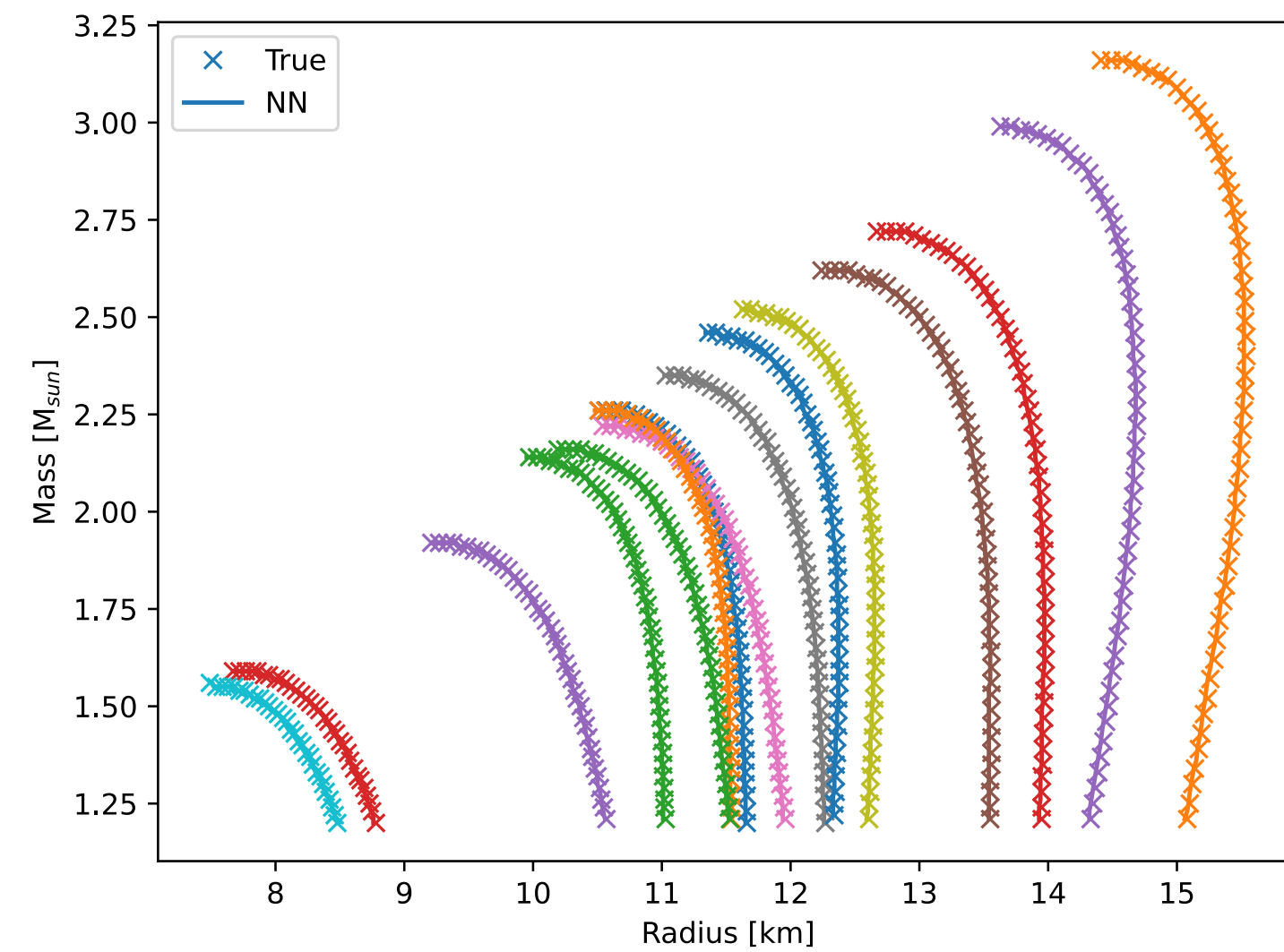


Learn EOS to M-R

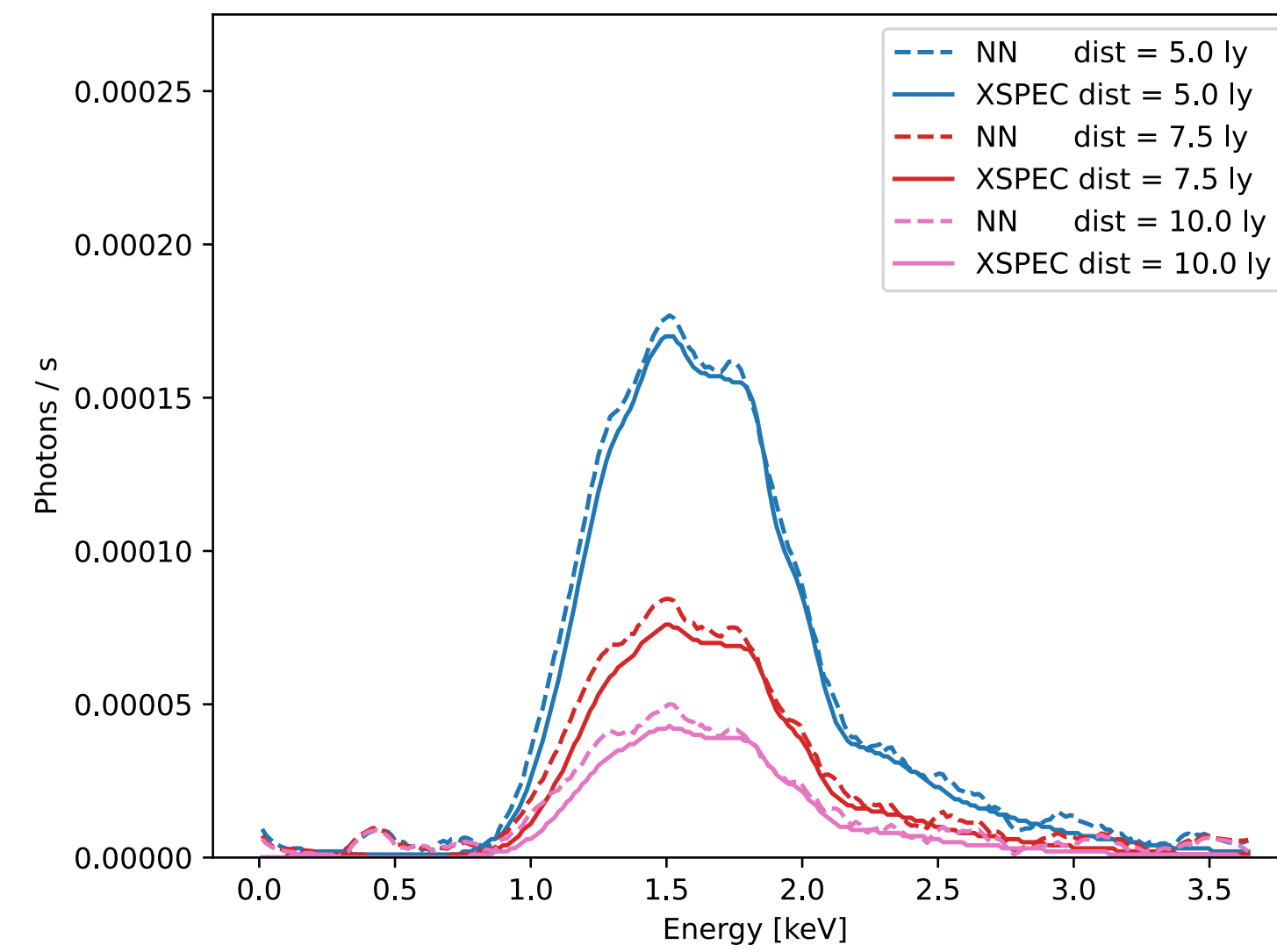


Forward process step-by-step

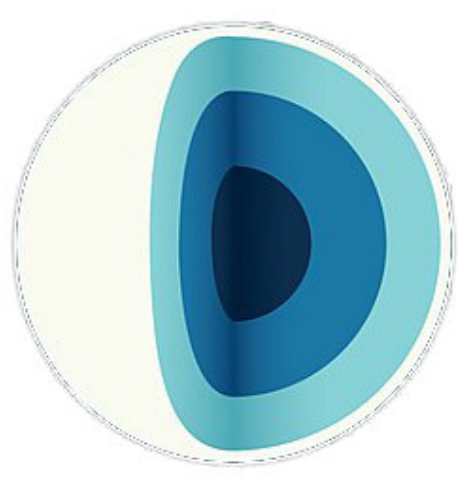
Intermediate steps remain interpretable physical quantities



Learn EOS to M-R



Learn {M,R,NPs} to Spectrum



Forward process step-by-step

Intermediate steps remain interpretable physical quantities

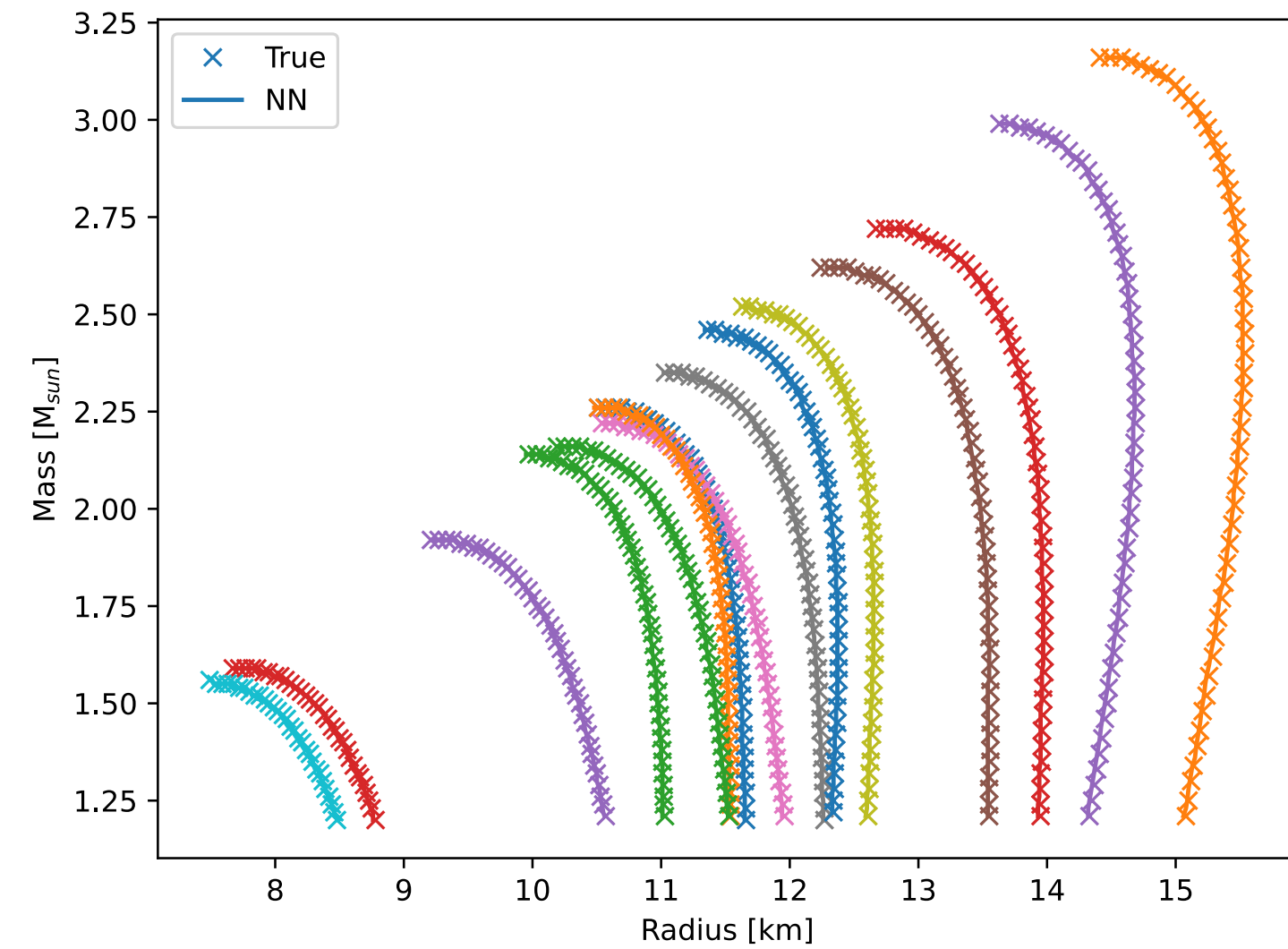
Nuisance
Priors:

M-R likelihoods:

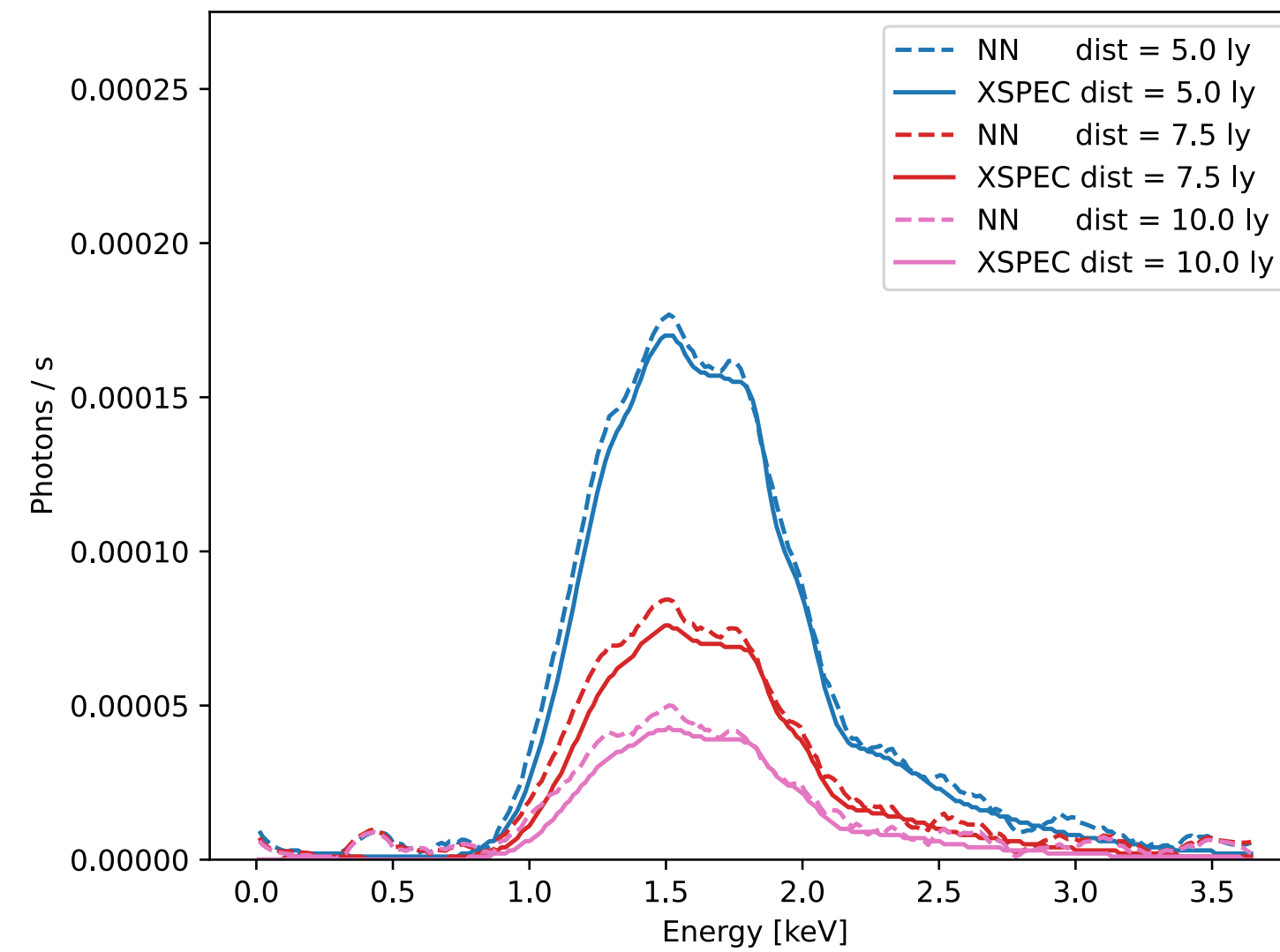
True:

Tight:

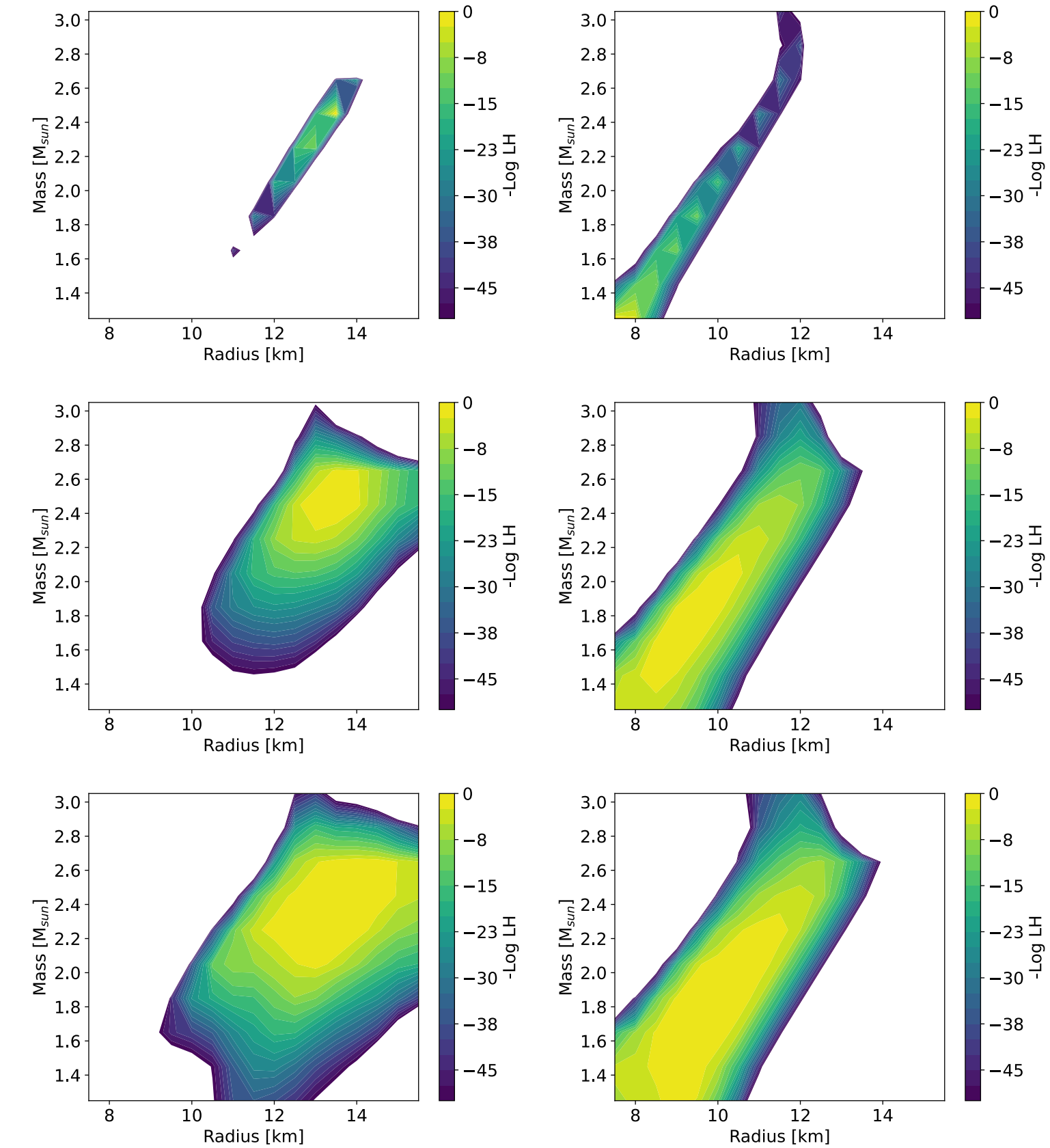
Loose:



Learn EOS to M-R



Learn {M,R,NPs} to Spectrum



Back to particle physics

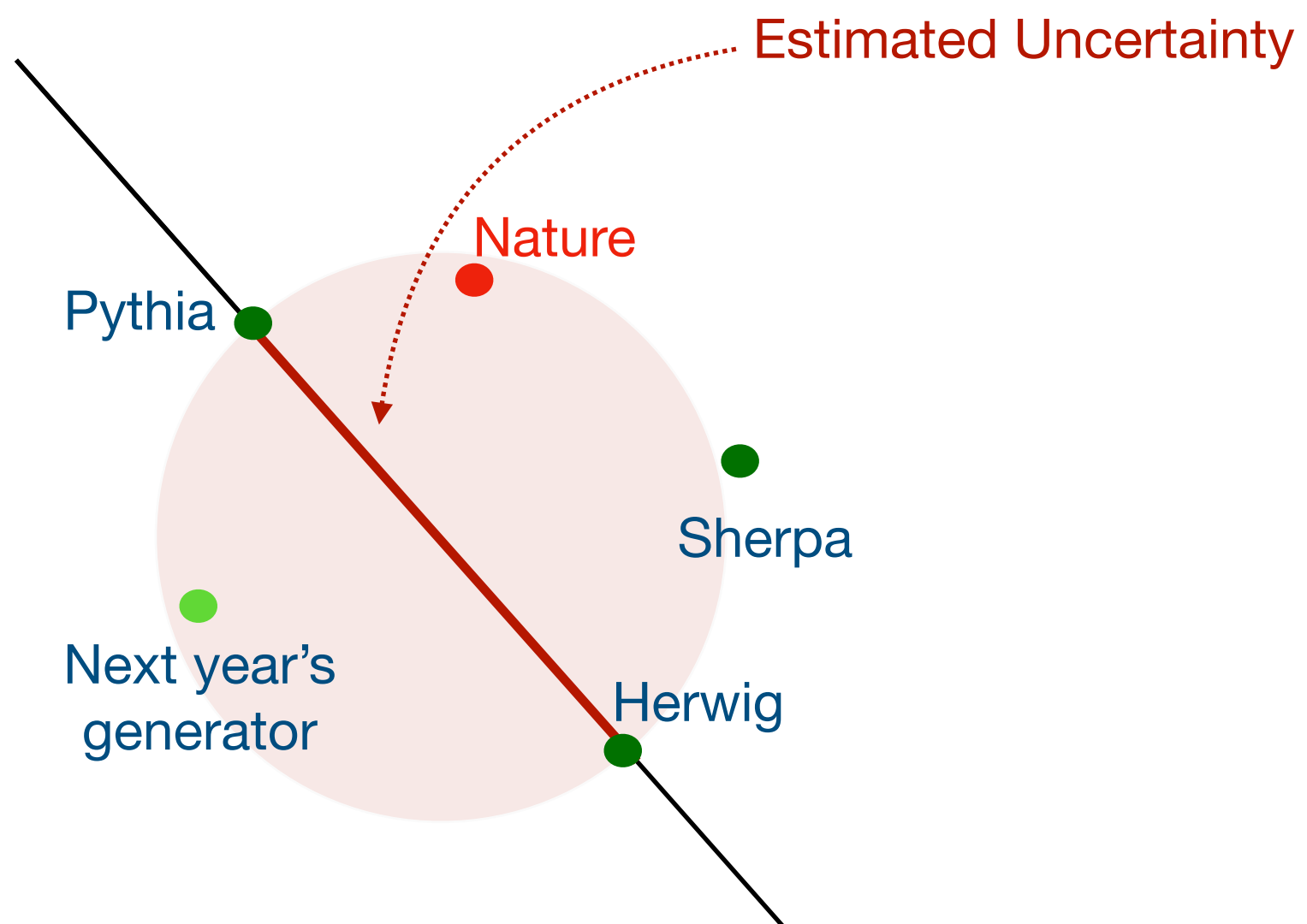
Back to particle physics

We also learnt what not to do ...

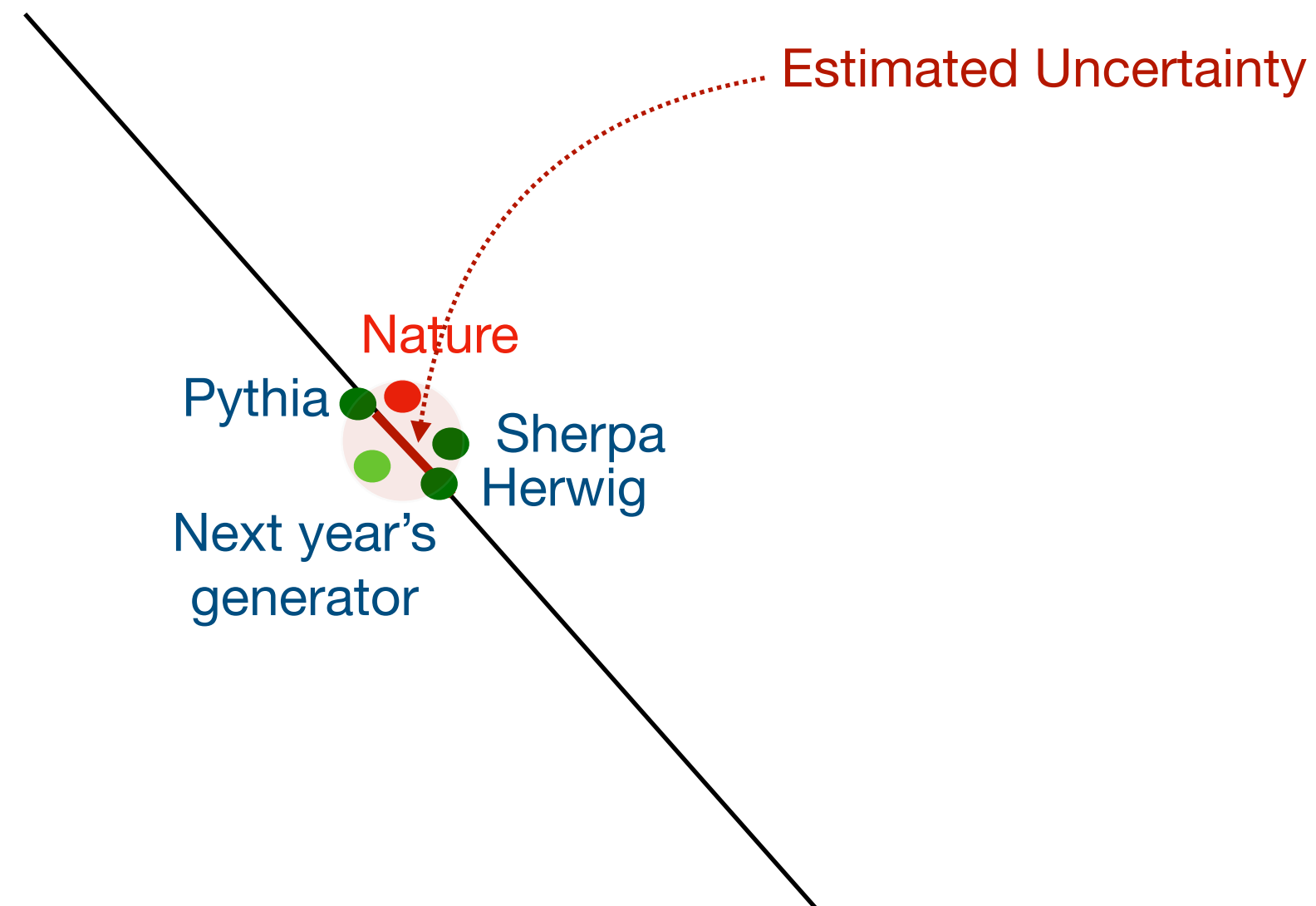
ML-decorrelating theory uncertainties

[EPJC:s10052.022.10012.w](#): **Aishik Ghosh**, Benjamin Nachman

Default



What you want with decorrelation

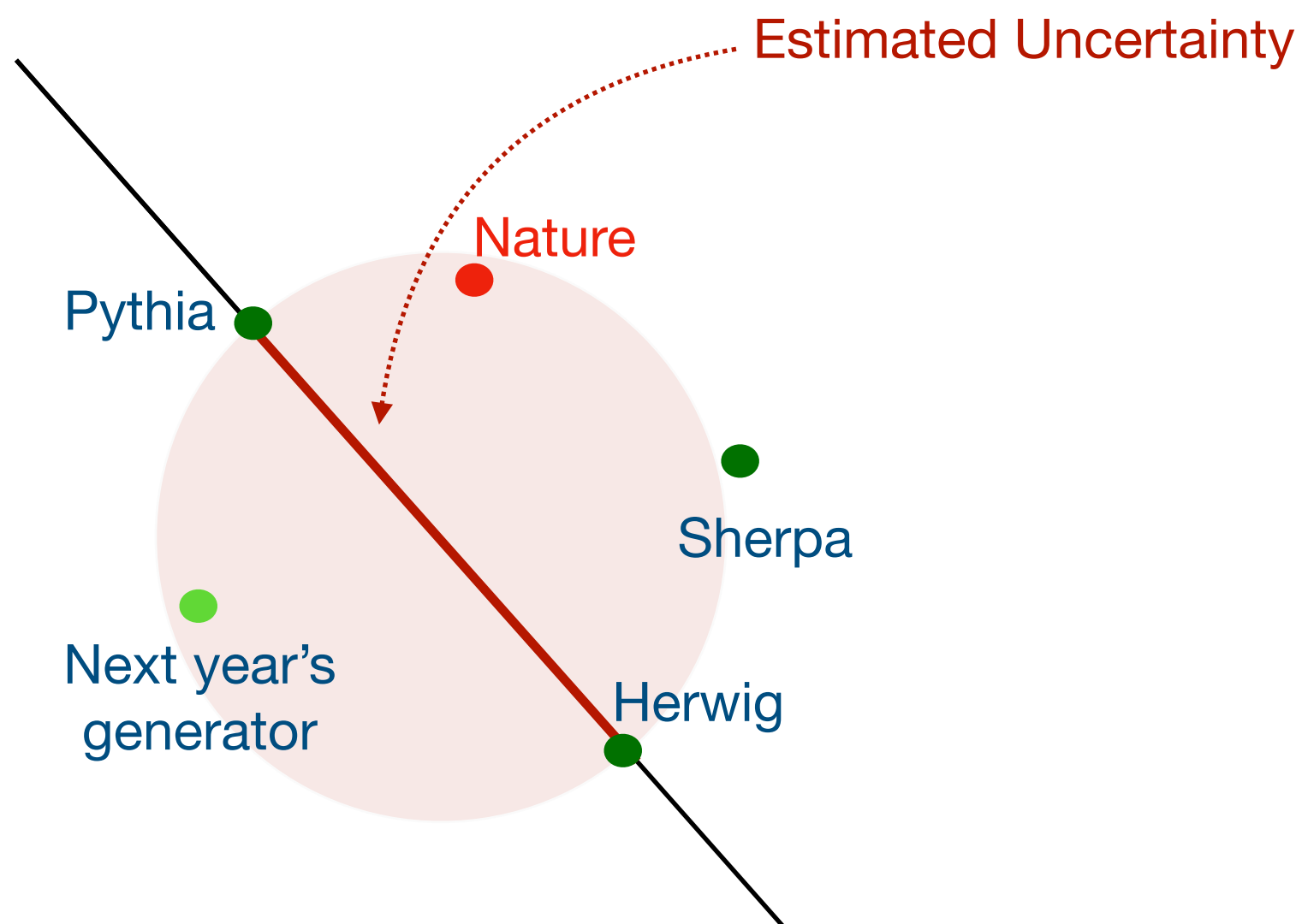


Instruction to ML: “Please shrink Pythia vs Herwig difference”

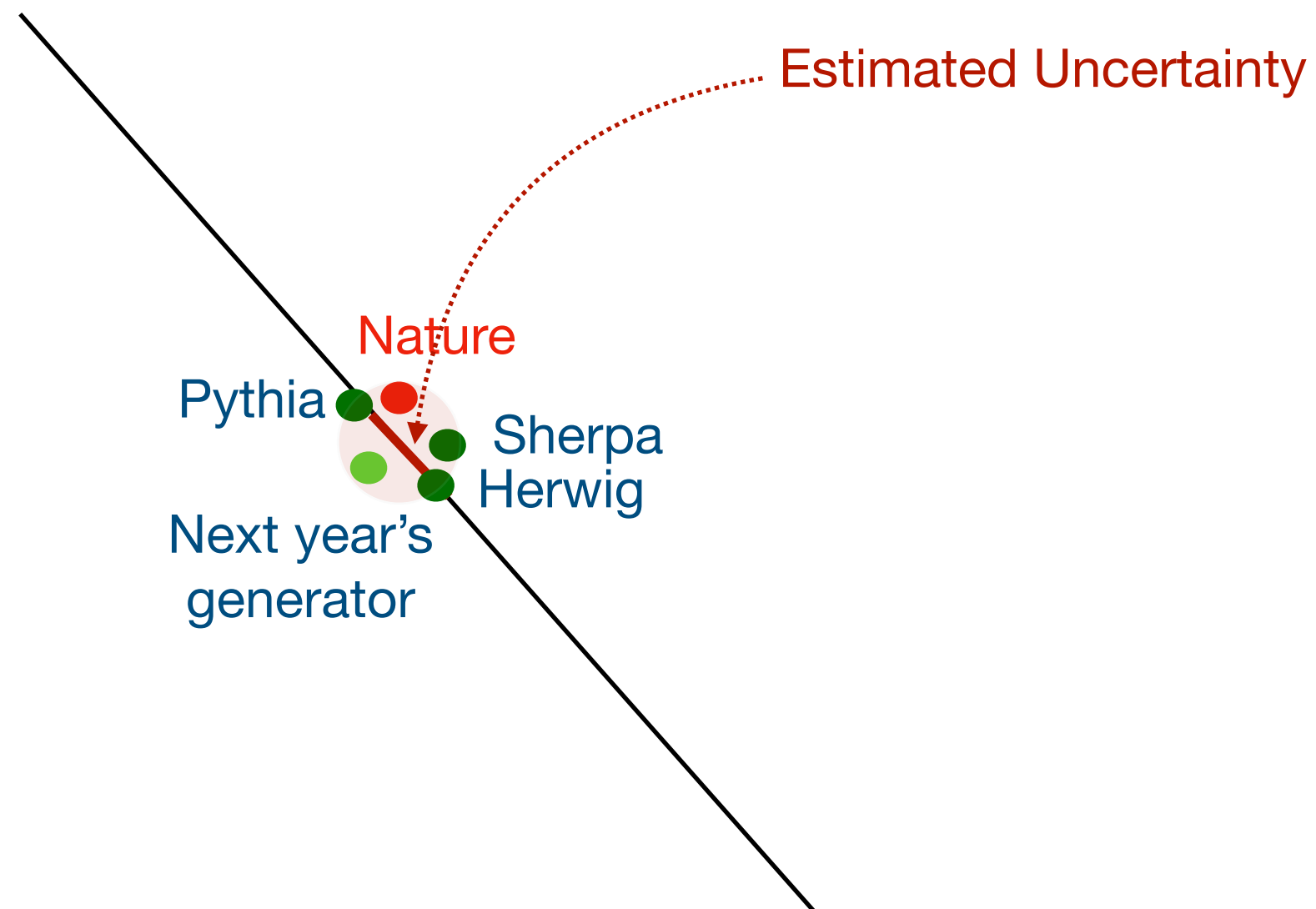
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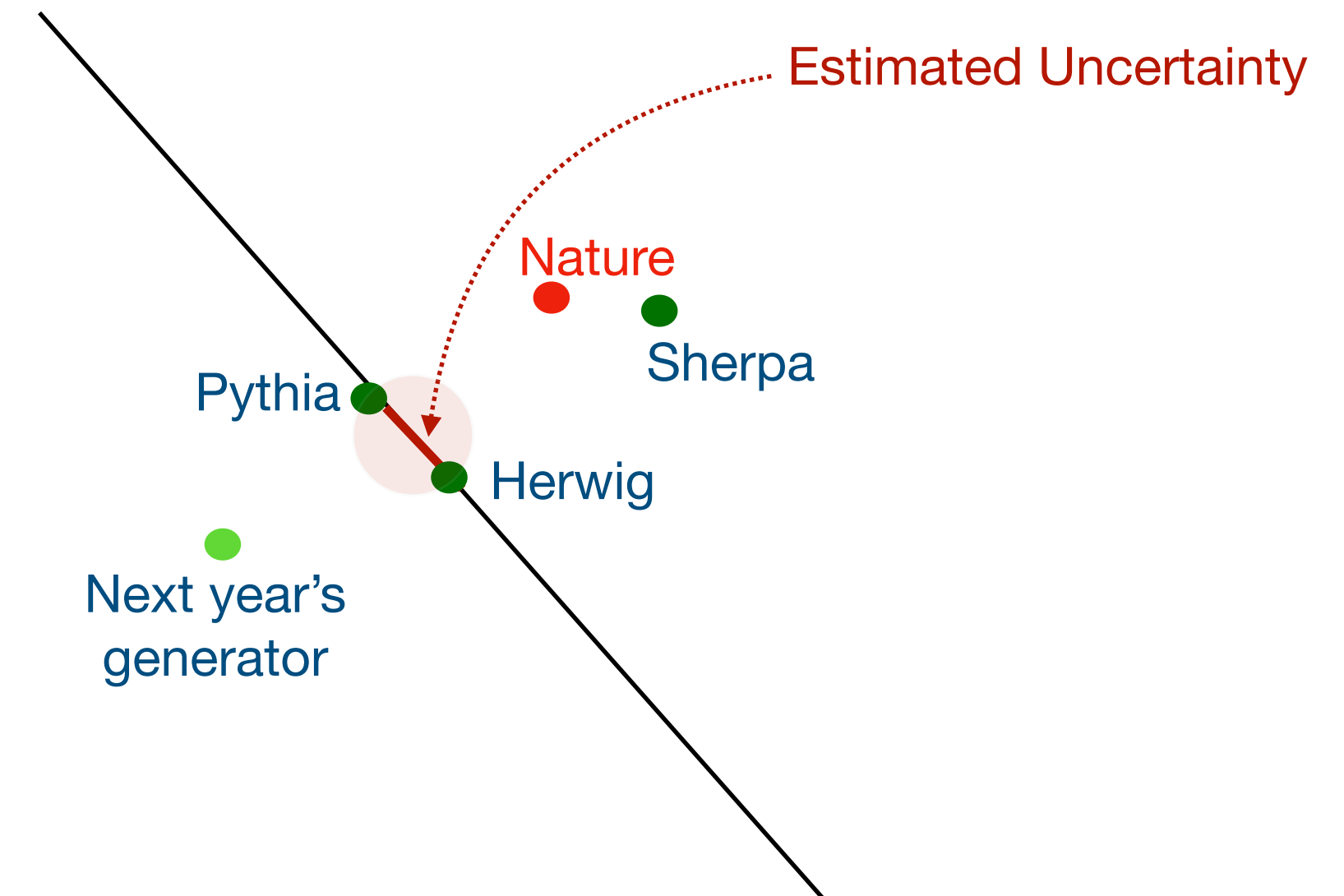
Default



What you want with decorrelation



What you get with decorrelation

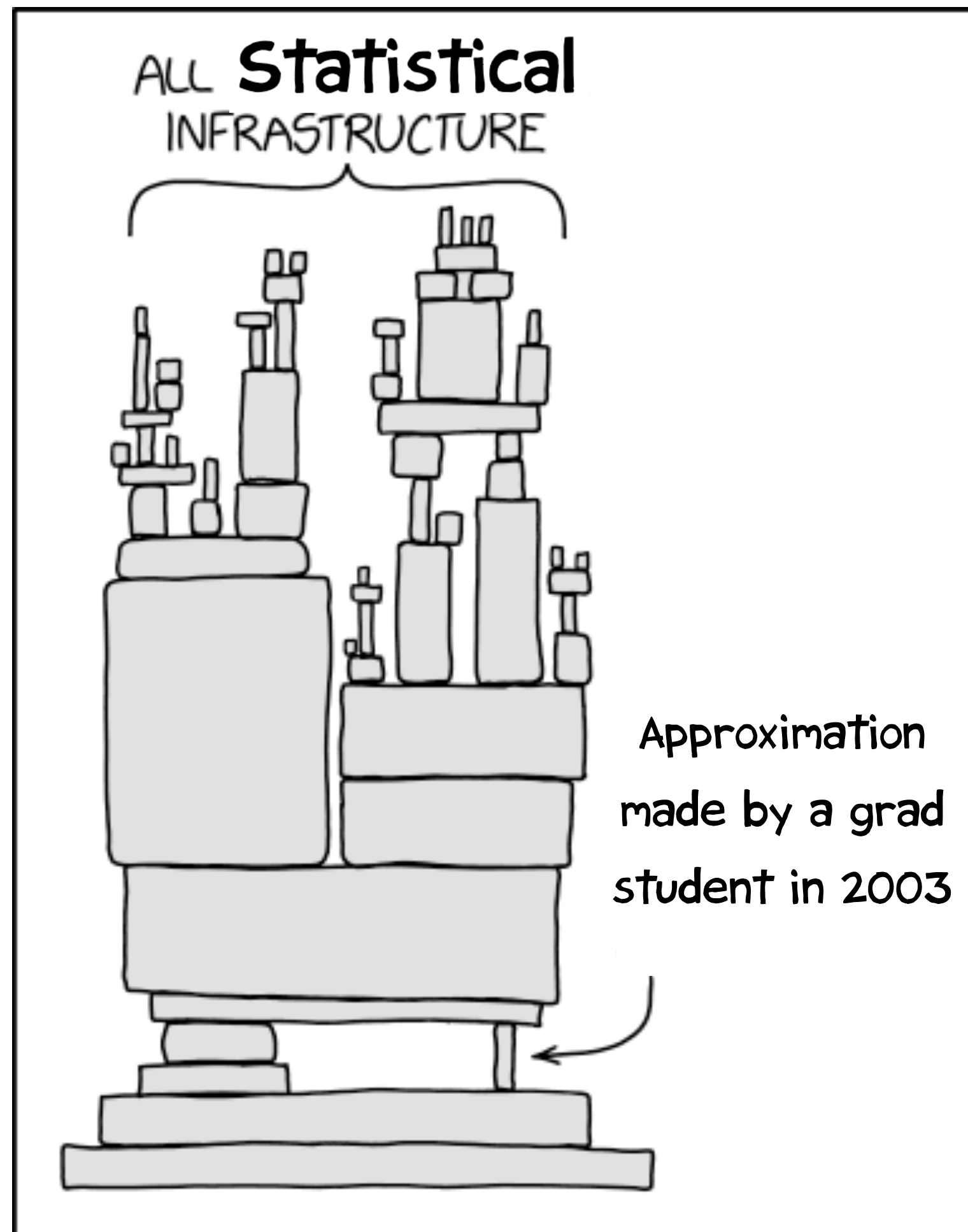


Instruction to ML: “Please shrink Pythia vs Herwig difference”

Model will learn to fool you !

ML methods don't often generalise the way you would hope

Theory uncertainties



From Daniel Whiteson

It's dangerous to use ML methods to mitigate theory uncertainties

But we continue to treat Δ_{theory} and Δ_{exp} on same footing in statistical fits

What even is their statistical behaviour?

Scale Uncertainties

Uncertainty of cross-section from truncating QFT series

Sensitivity to scale variation quantifies ‘uncertainty’

Scale Uncertainties

Up: $\mu_+ = 2 \mu_0$

$$\mu_0 = \frac{H_T}{2} = \frac{1}{2} \sum_{final\ state} \sqrt{m^2 + p_T^2}$$

Down: $\mu_- = \frac{1}{2} \mu_0$

Uncertainty of cross-section from truncating QFT series

Sensitivity to scale variation quantifies ‘uncertainty’

Questions

- How accurate are these scale uncertainties ?
- Is 1/2 to 2 a good range ?

Study pull distribution

$$t_{scale} = \frac{\sigma_{NLO} - \sigma_{LO}}{\Delta\sigma_{LO\ scale}}$$

Questions

- How accurate are these scale uncertainties ?
- Is 1/2 to 2 a good range ?

Madgraph paper

The automated computation of tree-level and next-to-leading order differential cross sections, and their matching to parton shower simulations

J. Alwall^a, R. Frederix^b, S. Frixione^b, V. Hirschi^c, F. Maltoni^d, O. Mattelaer^d, H.-S. Shao^e, T. Stelzer^f, P. Torrielli^g, M. Zaro^{h,i}

Study pull distribution

$$t_{scale} = \frac{\sigma_{NLO} - \sigma_{LO}}{\Delta\sigma_{LO\ scale}}$$

Process		Syntax	Cross section (pb)							
Vector boson +jets			LO 13 TeV				NLO 13 TeV			
a.1	$pp \rightarrow W^\pm$	p p > wpm	$1.375 \pm 0.002 \cdot 10^5$	+15.4%	+2.0%	$1.773 \pm 0.007 \cdot 10^5$	+5.2%	+1.9%		
a.2	$pp \rightarrow W^\pm j$	p p > wpm j	$2.045 \pm 0.001 \cdot 10^4$	-16.6%	-1.6%	$2.843 \pm 0.010 \cdot 10^4$	-9.4%	-1.6%		
a.3	$pp \rightarrow W^\pm jj$	p p > wpm j j	$6.805 \pm 0.015 \cdot 10^3$	+19.7%	+1.4%	$7.786 \pm 0.030 \cdot 10^3$	+5.9%	+1.3%		
a.4	$pp \rightarrow W^\pm jjj$	p p > wpm j j j	$1.821 \pm 0.002 \cdot 10^3$	-17.2%	-1.1%	$2.005 \pm 0.008 \cdot 10^3$	-8.0%	-1.1%		
				+24.5%	+0.8%		+2.4%	+0.9%		
				-18.6%	-0.7%		-6.0%	-0.8%		
				+41.0%	+0.5%		+0.9%	+0.6%		
				-27.1%	-0.5%		-6.7%	-0.5%		
a.5	$pp \rightarrow Z$	p p > z	$4.248 \pm 0.005 \cdot 10^4$	+14.6%	+2.0%	$5.410 \pm 0.022 \cdot 10^4$	+4.6%	+1.9%		
a.6	$pp \rightarrow Zj$	p p > z j	$7.209 \pm 0.005 \cdot 10^3$	-15.8%	-1.6%	$9.742 \pm 0.035 \cdot 10^3$	-8.6%	-1.5%		
a.7	$pp \rightarrow Zjj$	p p > z j j	$2.348 \pm 0.006 \cdot 10^3$	+19.3%	+1.2%	$2.665 \pm 0.010 \cdot 10^3$	+5.8%	+1.2%		
a.8	$pp \rightarrow Zjjj$	p p > z j j j	$6.314 \pm 0.008 \cdot 10^2$	-17.0%	-1.0%	$6.996 \pm 0.028 \cdot 10^2$	-7.8%	-1.0%		
				+24.3%	+0.6%		+2.5%	+0.7%		
				-18.5%	-0.6%		-6.0%	-0.7%		
				+40.8%	+0.5%		+1.1%	+0.5%		
				-27.0%	-0.5%		-6.8%	-0.5%		
a.9	$pp \rightarrow \gamma j$	p p > a j	$1.964 \pm 0.001 \cdot 10^4$	+31.2%	+1.7%	$5.218 \pm 0.025 \cdot 10^4$	+24.5%	+1.4%		
a.10	$pp \rightarrow \gamma jj$	p p > a j j	$7.815 \pm 0.008 \cdot 10^3$	-26.0%	-1.8%	$1.004 \pm 0.004 \cdot 10^4$	-21.4%	-1.6%		
				+32.8%	+0.9%		+5.9%	+0.8%		
				-24.2%	-1.2%		-10.9%	-1.2%		

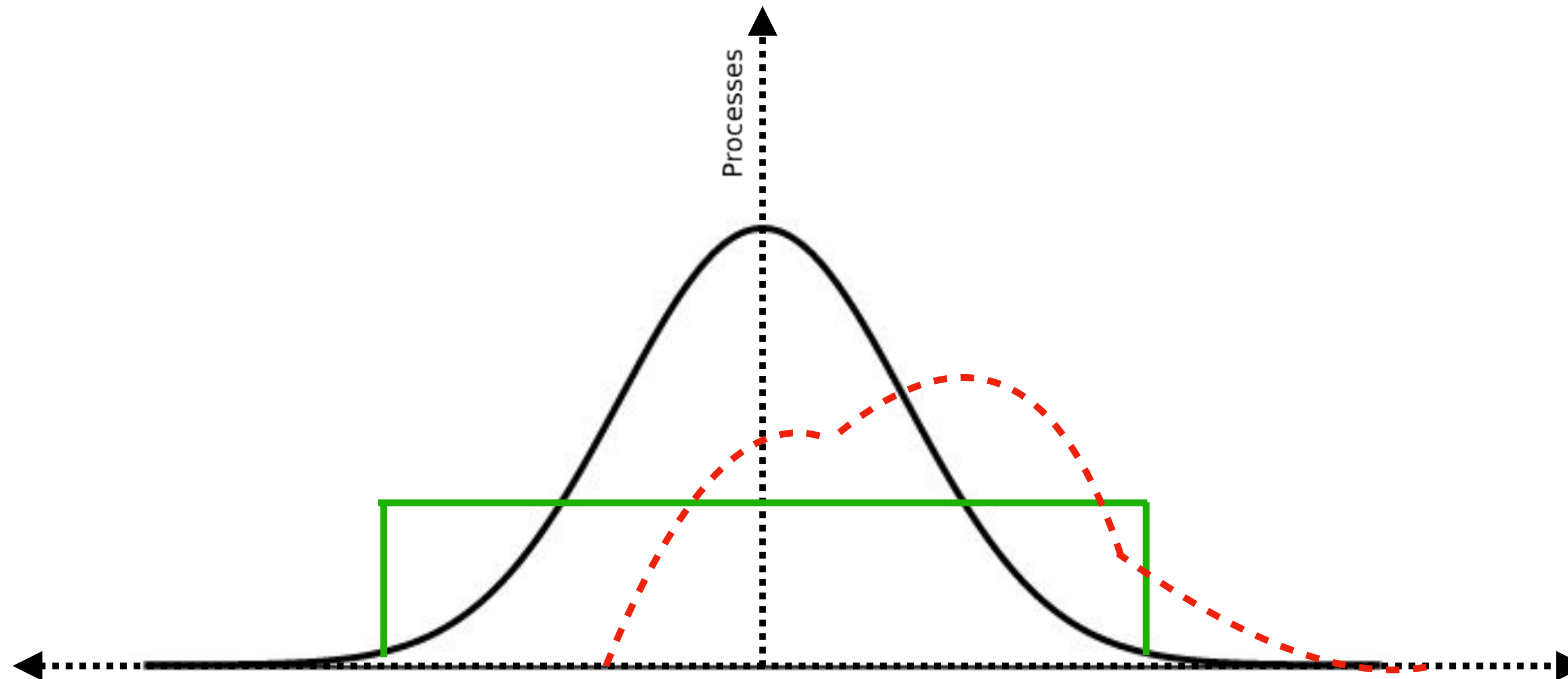
+127 more pp processes from 1405.0301!

(Not a random sampling)

Plot the pulls

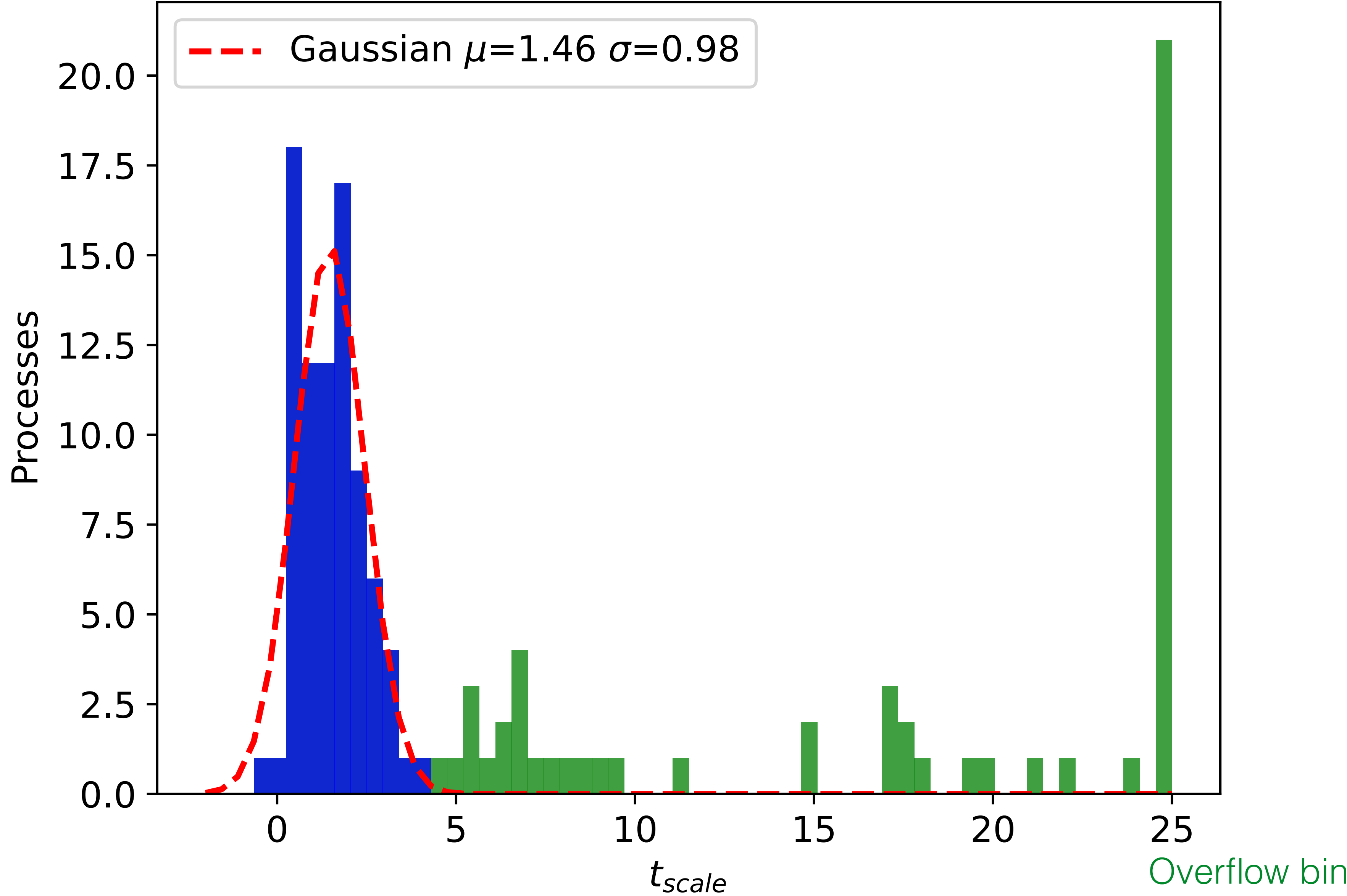
$$t_{scale} = \frac{\sigma_{NLO} - \sigma_{LO}}{\Delta\sigma_{LO\ scale}}$$

Which of these distributions do you expect?

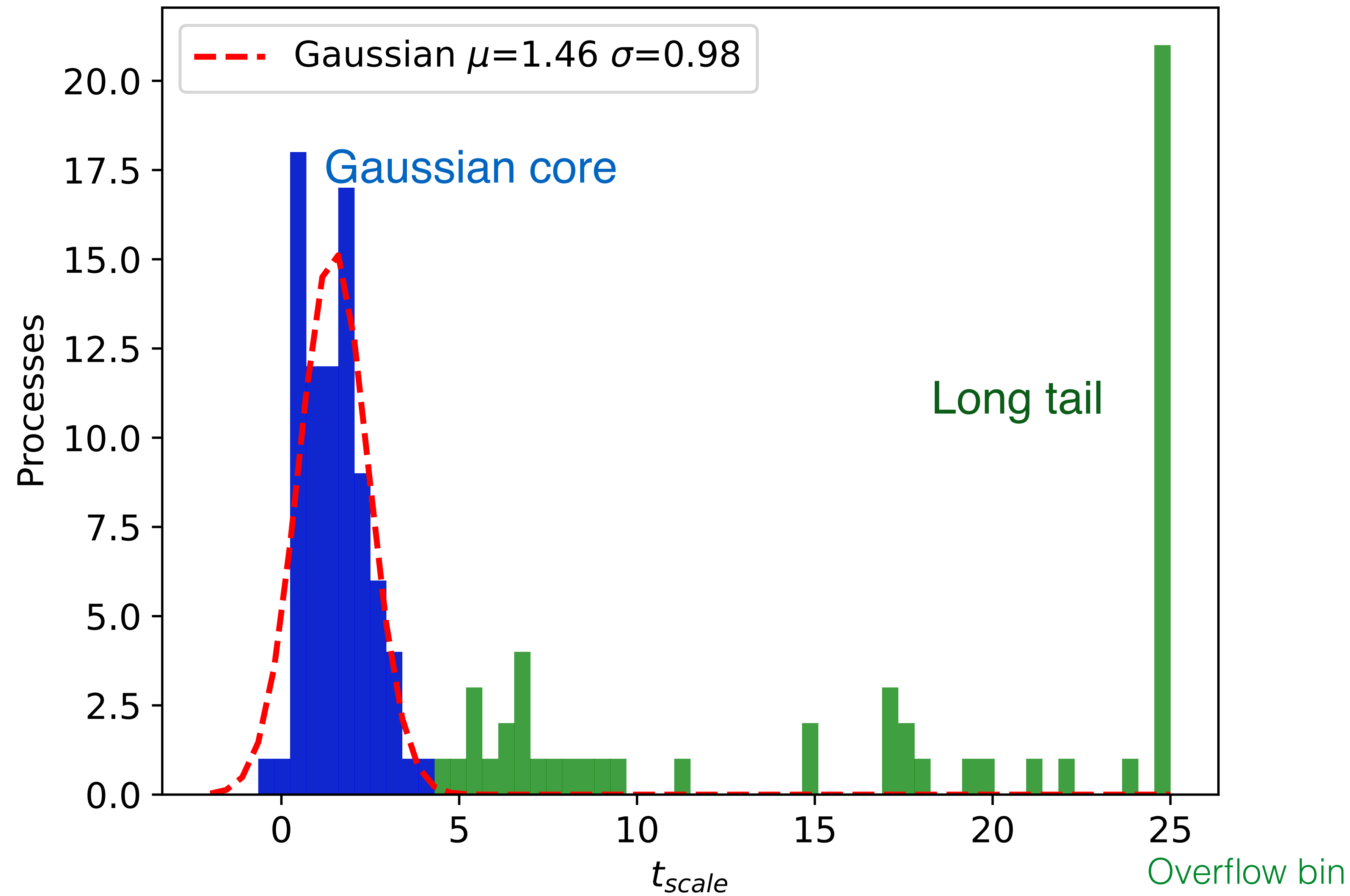


$$t_{scale} = \frac{\sigma_{NLO} - \sigma_{LO}}{\Delta\sigma_{LO\ scale}}$$

Pull distribution



Pull distribution



What processes populate the tail ?

Process	n_{part}	$\Delta\sigma/\sigma_0$	$\frac{\sigma_{\text{NLO}} - \sigma_0}{\Delta\sigma}$
p p > wpm	1	1.54×10^{-1}	1.84
p p > wpm j	2	1.97×10^{-1}	1.96
p p > wpm j j	3	2.45×10^{-1}	0.59
p p > wpm j j j	4	4.10×10^{-1}	0.25
p p > z	1	1.46×10^{-1}	1.87
p p > z j	2	1.93×10^{-1}	1.82
p p > z j j	3	2.43×10^{-1}	0.56
p p > z j j j	4	4.08×10^{-1}	0.27
p p > a j	2	3.12×10^{-1}	5.33
p p > a j j	3	3.28×10^{-1}	0.85
p p > w ⁺ w ⁻ wpm	3	1.00×10^{-3}	610.69
p p > z w ⁺ w ⁻	3	8.00×10^{-3}	92.39
p p > z z wpm	3	1.00×10^{-2}	85.00
p p > z z z	3	1.00×10^{-3}	302.75
p p > a w ⁺ w ⁻	3	1.90×10^{-2}	42.33
p p > a a wpm	3	4.40×10^{-2}	47.24
p p > a z wpm	3	1.00×10^{-3}	1244.49
p p > a z z	3	2.00×10^{-2}	17.24

QCD processes follow (an expected) pattern

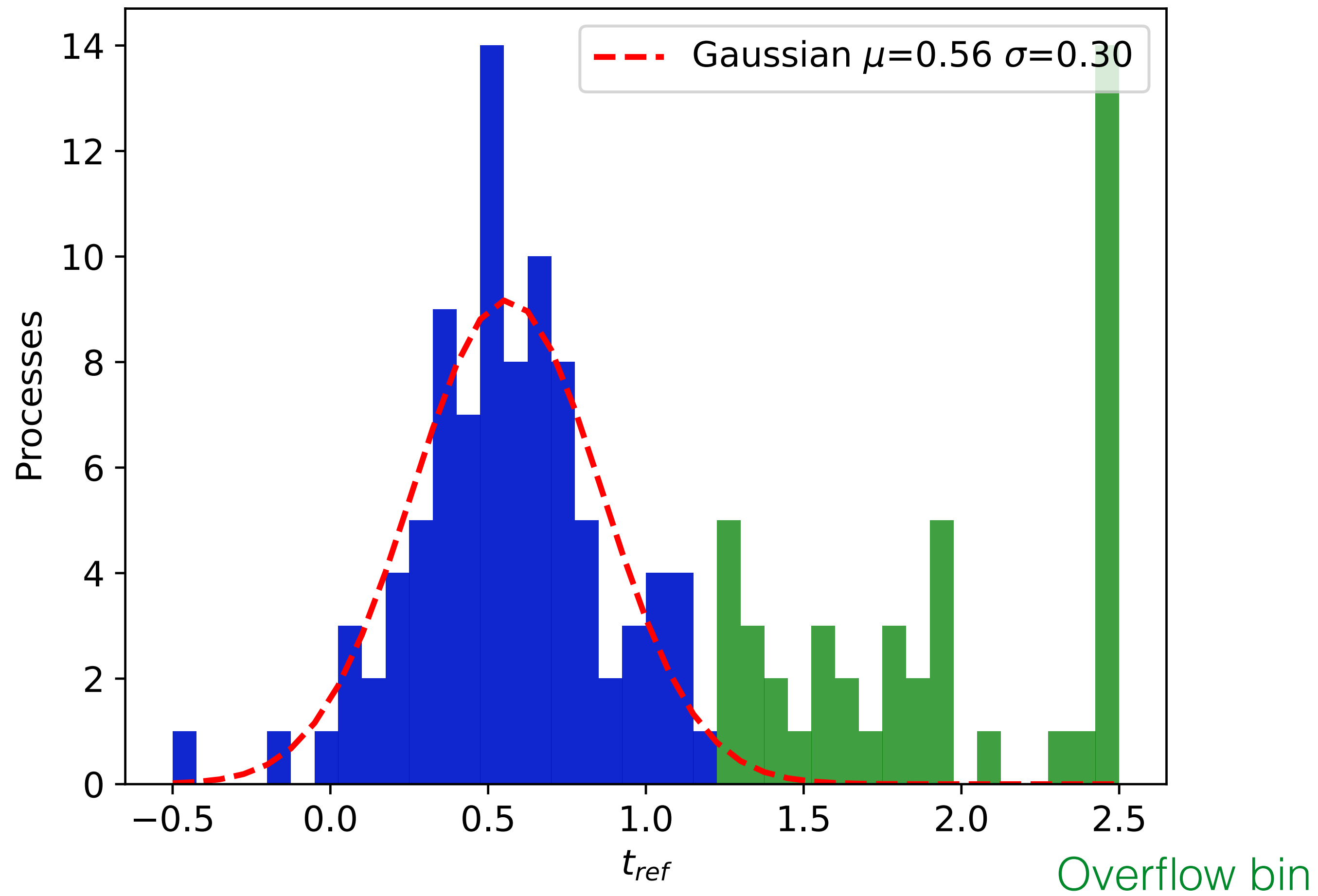
Process	$\frac{\Delta\sigma}{\sigma_0}$	n	$\frac{\Delta\sigma}{n\sigma_0}$
p p > j j	$+2.49 \times 10^{-1} \quad -1.88 \times 10^{-1}$	2	$+1.24 \times 10^{-1} \quad -9.40 \times 10^{-2}$
p p > b b	$+2.52 \times 10^{-1} \quad -1.89 \times 10^{-1}$	2	$+1.26 \times 10^{-1} \quad -9.45 \times 10^{-2}$
p p > t t	$+2.90 \times 10^{-1} \quad -2.11 \times 10^{-1}$	2	$+1.45 \times 10^{-1} \quad -1.06 \times 10^{-1}$
p p > j j j	$+4.38 \times 10^{-1} \quad -2.84 \times 10^{-1}$	3	$+1.46 \times 10^{-1} \quad -9.47 \times 10^{-2}$
p p > b b j	$+4.41 \times 10^{-1} \quad -2.85 \times 10^{-1}$	3	$+1.47 \times 10^{-1} \quad -9.50 \times 10^{-2}$
p p > t t j	$+4.51 \times 10^{-1} \quad -2.90 \times 10^{-1}$	3	$+1.50 \times 10^{-1} \quad -9.67 \times 10^{-2}$
p p > b b j j	$+6.18 \times 10^{-1} \quad -3.56 \times 10^{-1}$	4	$+1.54 \times 10^{-1} \quad -8.90 \times 10^{-2}$
p p > b b b b	$+6.17 \times 10^{-1} \quad -3.56 \times 10^{-1}$	4	$+1.54 \times 10^{-1} \quad -8.90 \times 10^{-2}$
p p > t t j j	$+6.14 \times 10^{-1} \quad -3.56 \times 10^{-1}$	4	$+1.53 \times 10^{-1} \quad -8.90 \times 10^{-2}$
p p > t t t t	$+6.38 \times 10^{-1} \quad -3.65 \times 10^{-1}$	4	$+1.60 \times 10^{-1} \quad -9.12 \times 10^{-2}$
p p > t t b b	$+6.21 \times 10^{-1} \quad -3.57 \times 10^{-1}$	4	$+1.55 \times 10^{-1} \quad -8.93 \times 10^{-2}$
average			$+1.47 \times 10^{-1} \quad -9.34 \times 10^{-2}$

Table 1: Scale dependence for LHC processes with only QCD particles in the final state. For each process, we report the relative scale uncertainty, the number of final state particles, and the per-particle relative scale uncertainty.

→ Tilman Plehn’s ‘reference process’ method

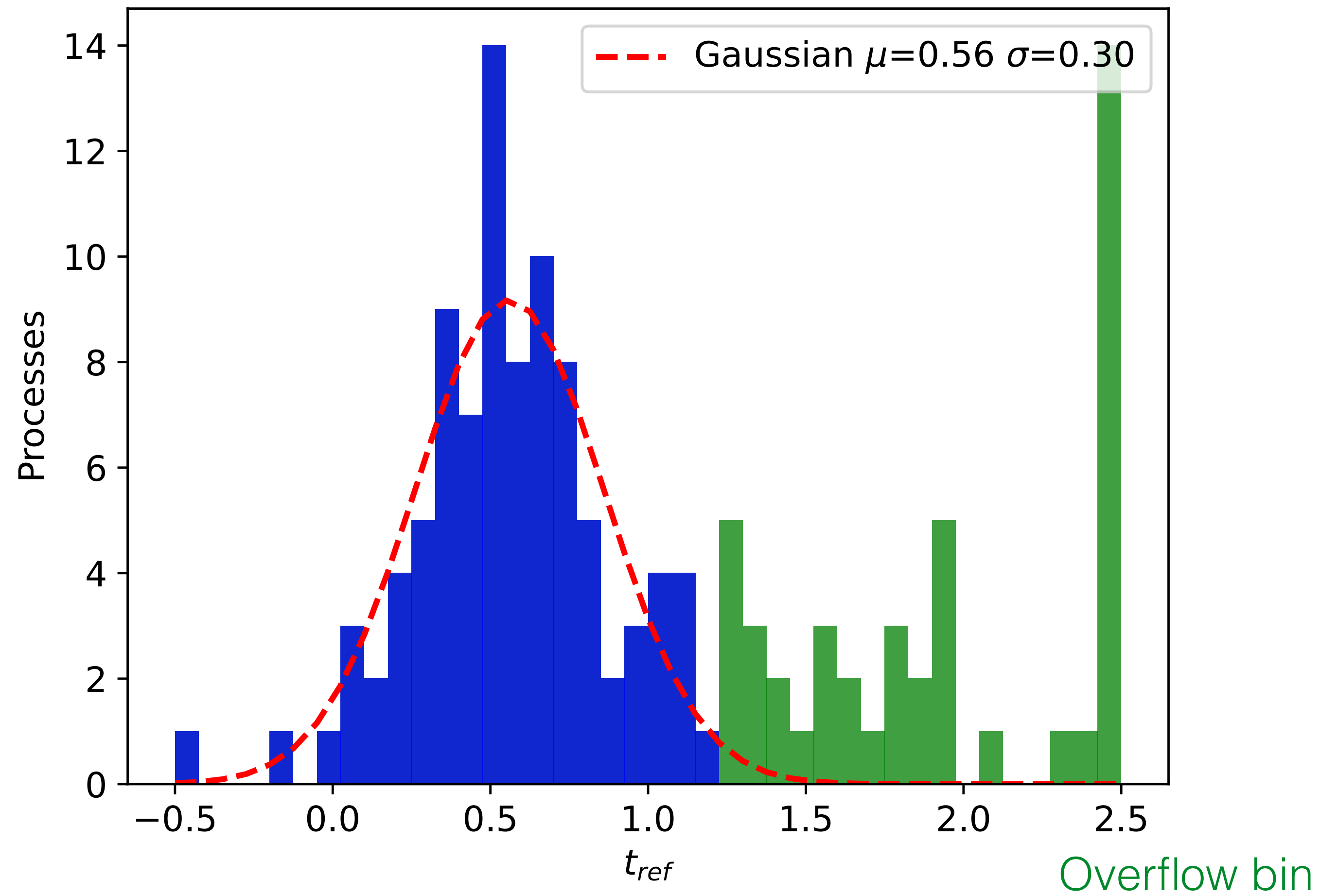
$$\frac{\Delta\sigma_{\text{ref}}}{\sigma_0} = n \times \left\langle \frac{\Delta\sigma}{n\sigma_0} \right\rangle_{\text{QCD}}.$$

Make correction in UQ for EW processes

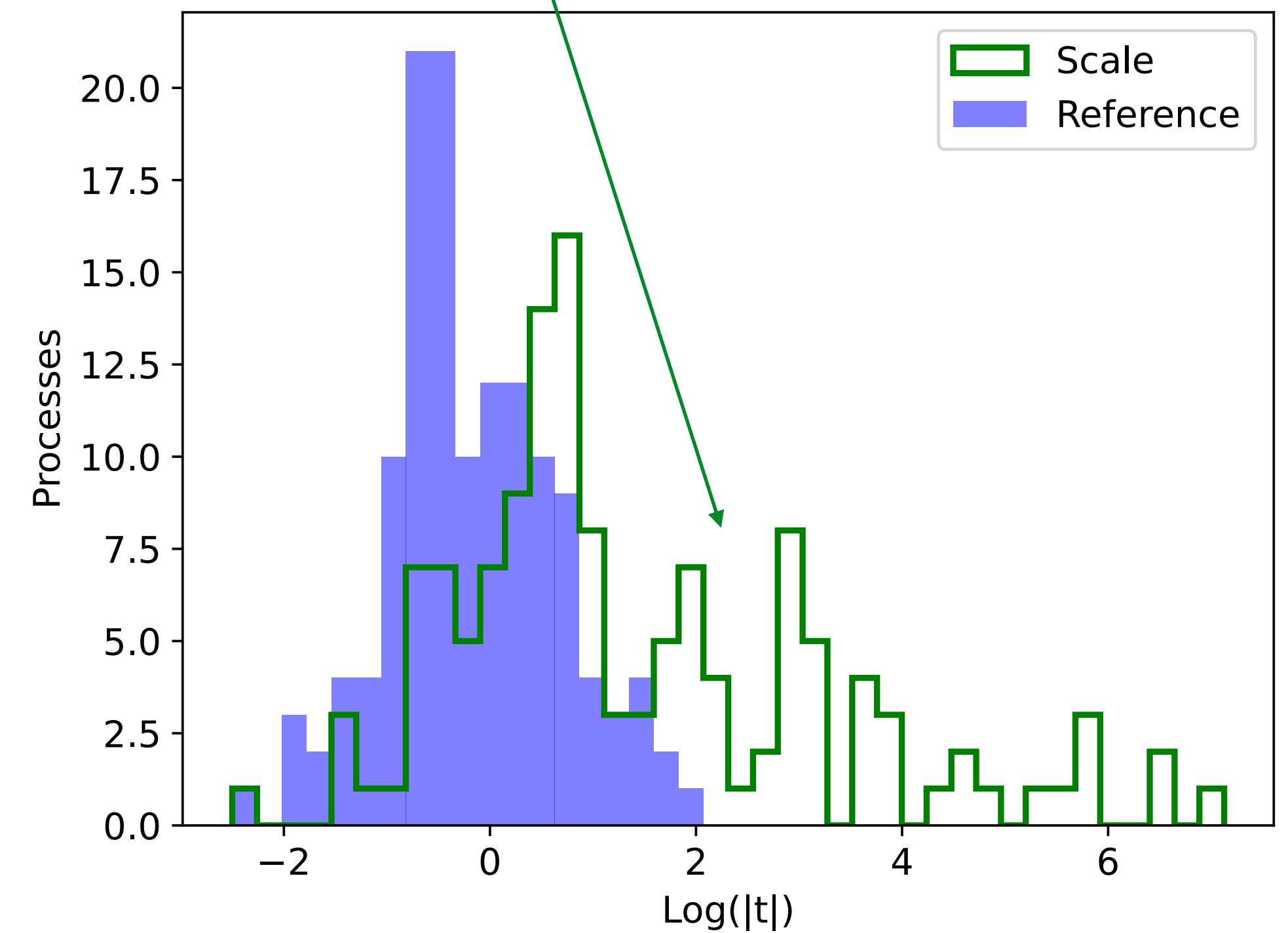


Much reduced tails

Make correction in UQ for EW processes



Much reduced tails



Leaves us wanting more ...

- Would be even more interesting to repeat study for NLO \rightarrow NNLO, differential distributions
- Can we use ML to automatically find patterns of failure ?
- Why did we find a Gaussian-ish core ?
- Impact: A new method for cross-checks within experiment collaborations

Snowmass Whitepaper: Recommendations for the future

- Common language for uncertainty between ML and Physics communities
- Funding to test ML UQ methods for physics
- Create benchmark datasets for uncertainty tests
- Develop and study interpretability methods

Snowmass Whitepaper: Recommendations for the future



Snowmass 2021: Summary of past work and future roadmap

- Common language for uncertainty between ML and Physics communities
- Funding to test ML UQ methods for physics
- Create benchmark datasets for uncertainty tests
- Develop and study interpretability methods

Conclusion

- ML more sensitive to simulation artefacts → building better uncertainty quantification tools
- ML lets us better propagate experimental uncertainties and build analyses optimised for all possibilities: HEP, Astro
- Solutions have wider use cases
 - Tractable likelihoods
 - Optimise true objective with differentiable programming [[Inferno](#), [NEOS](#)]
 - Uncertainty quantification of ML-simulators? [[Performance metrics](#), [Bayesian networks](#)]
 - Learn physics from machine: Mapping ML into a human-readable space [[CNN to EFPs](#)]

And more cool solutions to come !



Thank you!

Known unknowns

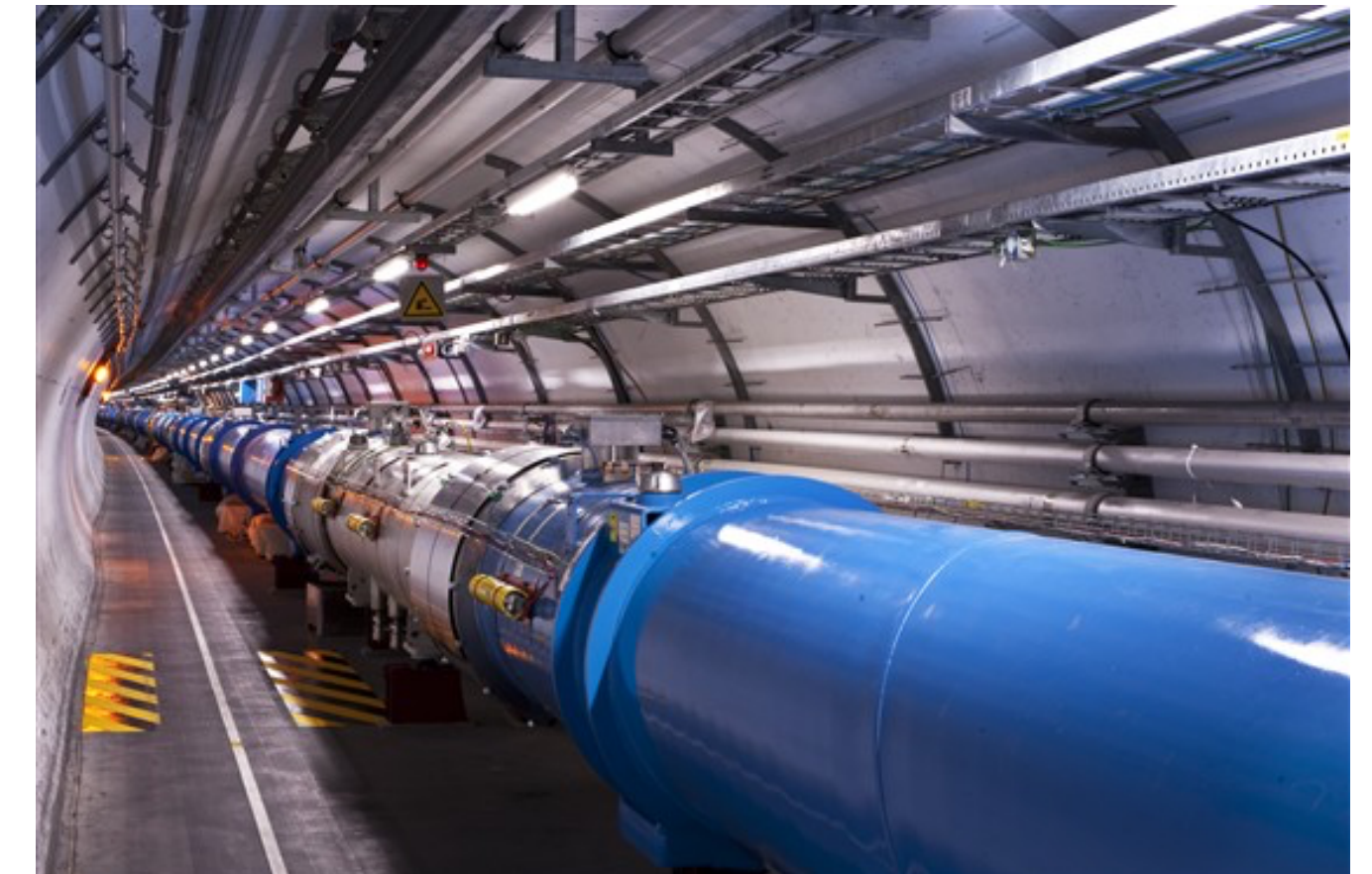
Simulation using Standard Model of particle physics



Detector state in sim: $Z=1$

Train ML models on simulation, apply on data

Unlabelled data from LHC



Detector state in data: $Z = ?$

Systematic differences lead to systematic uncertainties

Make correction in UQ for EW processes

Process	n_{part}	$\Delta\sigma/\sigma_0$	$\frac{\sigma_{\text{NLO}}-\sigma_0}{\Delta\sigma}$	$\Delta\sigma_{\text{ref}}/\sigma_0$	$\frac{\sigma_{\text{NLO}}-\sigma_0}{\Delta\sigma_{\text{ref}}}$
p p > wpm	1	1.54×10^{-1}	1.84	1.47×10^{-1}	1.92
p p > wpm j	2	1.97×10^{-1}	1.96	2.94×10^{-1}	1.31
p p > wpm j j	3	2.45×10^{-1}	0.59	4.41×10^{-1}	0.33
p p > wpm j j j	4	4.10×10^{-1}	0.25	5.88×10^{-1}	0.18
p p > z	1	1.46×10^{-1}	1.87	1.47×10^{-1}	1.86
p p > z j	2	1.93×10^{-1}	1.82	2.94×10^{-1}	1.19
p p > z j j	3	2.43×10^{-1}	0.56	4.41×10^{-1}	0.31
p p > z j j j	4	4.08×10^{-1}	0.27	5.88×10^{-1}	0.19
p p > a j	2	3.12×10^{-1}	5.33	2.94×10^{-1}	5.66
p p > a j j	3	3.28×10^{-1}	0.85	4.41×10^{-1}	0.63
p p > w+ w- wpm	3	1.00×10^{-3}	610.69	4.41×10^{-1}	1.39
p p > z w+ w-	3	8.00×10^{-3}	92.39	4.41×10^{-1}	1.68
p p > z z wpm	3	1.00×10^{-2}	85.00	4.41×10^{-1}	1.93
p p > z z z	3	1.00×10^{-3}	302.75	4.41×10^{-1}	0.69
p p > a w+ w-	3	1.90×10^{-2}	42.33	4.41×10^{-1}	1.82
p p > a a wpm	3	4.40×10^{-2}	47.24	4.41×10^{-1}	4.72
p p > a z wpm	3	1.00×10^{-3}	1244.49	4.41×10^{-1}	2.82
p p > a z z	3	2.00×10^{-2}	17.24	4.41×10^{-1}	0.78

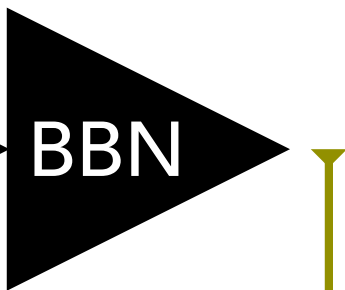
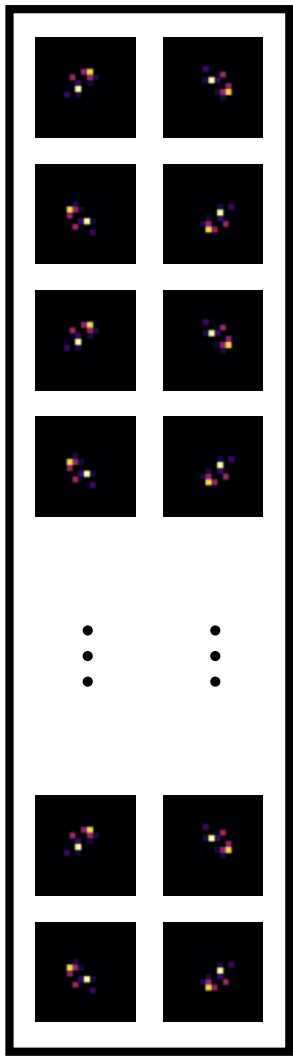
Surviving tails

Process	n_{part}	$\Delta\sigma/\sigma_0$	$\frac{\sigma_{\text{NLO}}-\sigma_0}{\Delta\sigma}$	$\Delta\sigma_{\text{ref}}/\sigma_0$	$\frac{\sigma_{\text{NLO}}-\sigma_0}{\Delta\sigma_{\text{ref}}}$
p p > h	1	3.48×10^{-1}	3.02	1.47×10^{-1}	7.15

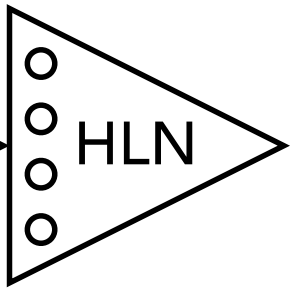
Large corrections loop-induced 2->1 process

Mapping machine-learned physics into a human-readable space

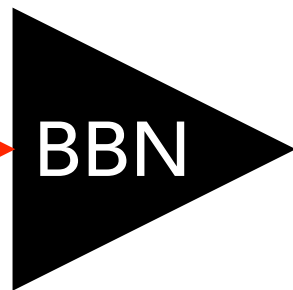
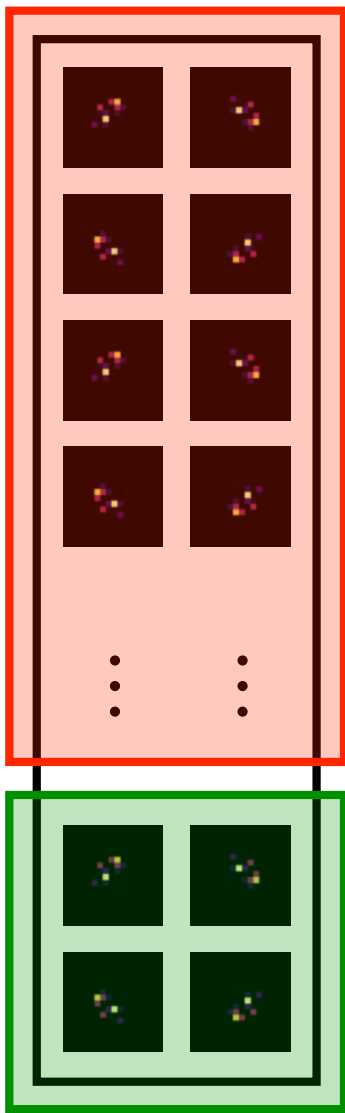
Signal/Background Pairs



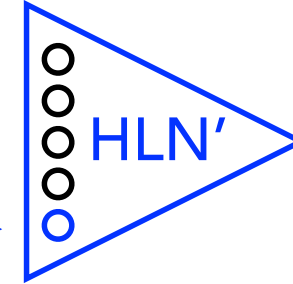
Same
Decision
Ordering?



No



Maximize
Decision
Ordering



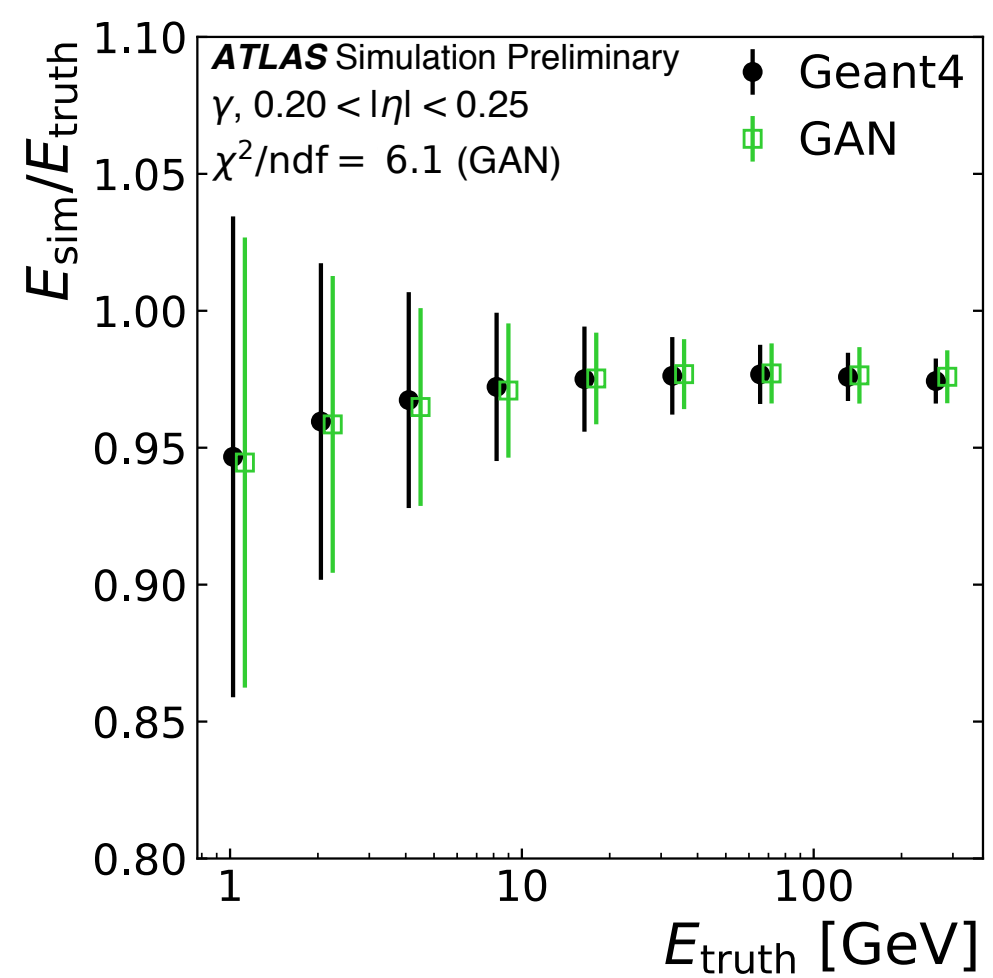
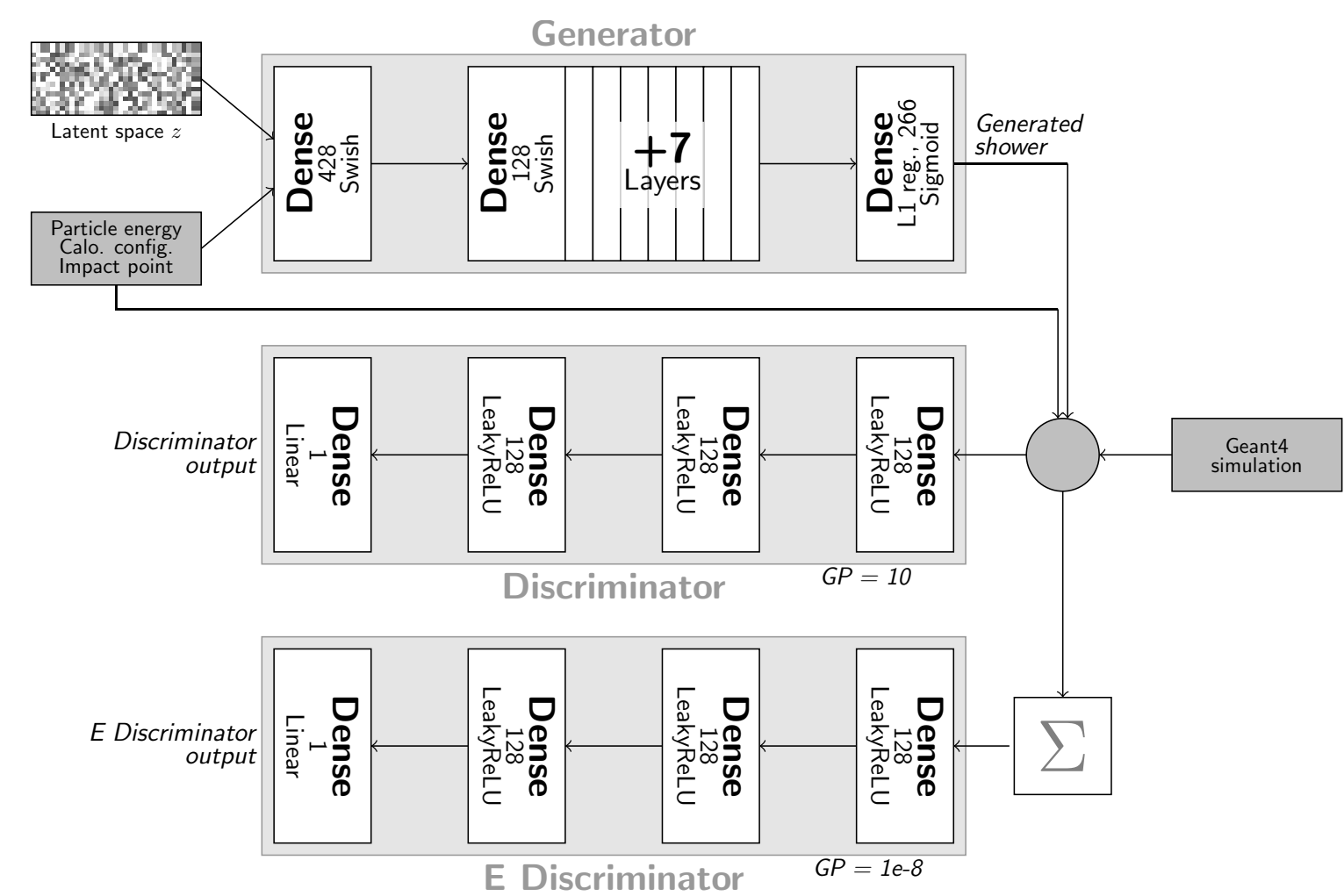
*Black-Box
Guided
Search*

Rank	EFP	κ	β	Chrom #	ADO[EFP, CNN] _{X₆}	AUC[EFP]	ADO[6HL + EFP, CNN] _{X_{all}}	AUC[6HL + EFP]
1		2	$\frac{1}{2}$	3	0.6207	0.8031	0.9714	0.9528 ± 0.0003
2		2	$\frac{1}{2}$	3	0.6205	0.8203	0.9714	0.9524
3		0	—	1	0.6205	0.6737	0.9715	0.9525
4		2	$\frac{1}{2}$	3	0.6199	0.8301	0.9715	0.9527
5		2	$\frac{1}{2}$	3	0.6197	0.8290	0.9714	0.9527
6		2	$\frac{1}{2}$	3	0.6196	0.8251	0.9715	0.9522
7		0	$\frac{1}{2}$	2	0.6187	0.7511	0.9715	0.9526
8		2	$\frac{1}{2}$	3	0.6184	0.8257	0.9712	0.9527
9		2	$\frac{1}{2}$	3	0.6182	0.8090	0.9714	0.9527
10		2	$\frac{1}{2}$	3	0.6180	0.8314	0.9714	0.9526
60		0	1	2	0.6163	0.7194	0.9715	0.9525
341		—1	$\frac{1}{2}$	4	0.6142	0.6286	0.9714	0.9509
589		0	2	2	0.6109	0.7579	0.9714	0.9523
3106		—1	—	1	0.5891	0.5882	0.9714	0.9510
3519		$\frac{1}{2}$	$\frac{1}{2}$	2	0.5664	0.7698	0.9715	0.9524
3521		$\frac{1}{2}$	—	1	0.5663	0.7093	0.9714	0.9522
5531		1	2	1	0.5290	0.7454	0.9714	0.9507
5554		1	$\frac{1}{2}$	2	0.5279	0.8210	0.9713	0.9505
5610		2	—	1	0.5245	0.7117	0.9714	0.9507
5657		1	1	3	0.5224	0.8257	0.9712	0.9506
5793		1	1	2	0.5191	0.8640	0.9714	0.9505
6052		1	2	3	0.5153	0.8500	0.9716	0.9504
7438		1	2	2	0.5011	0.8835	0.9716	0.9506

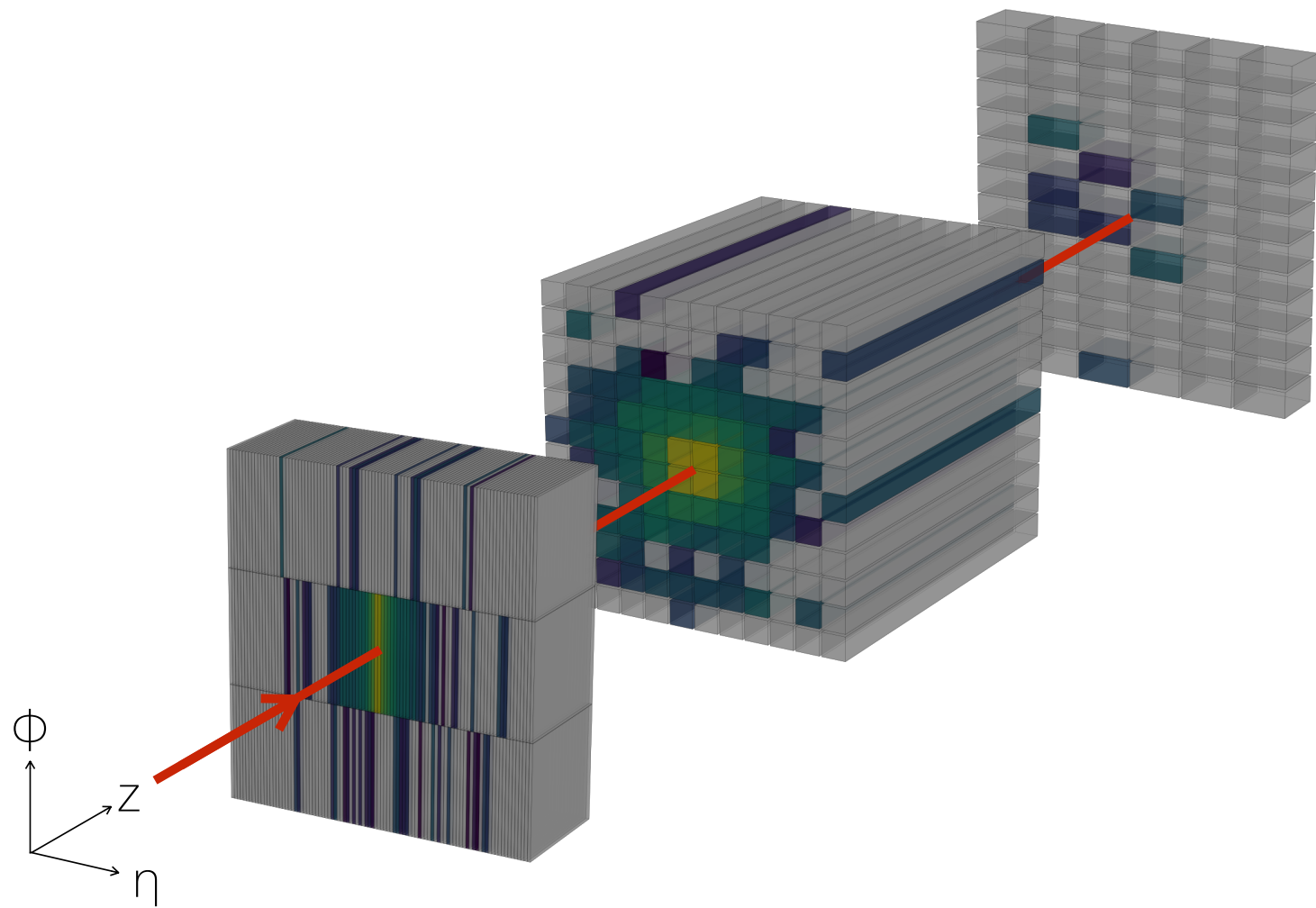
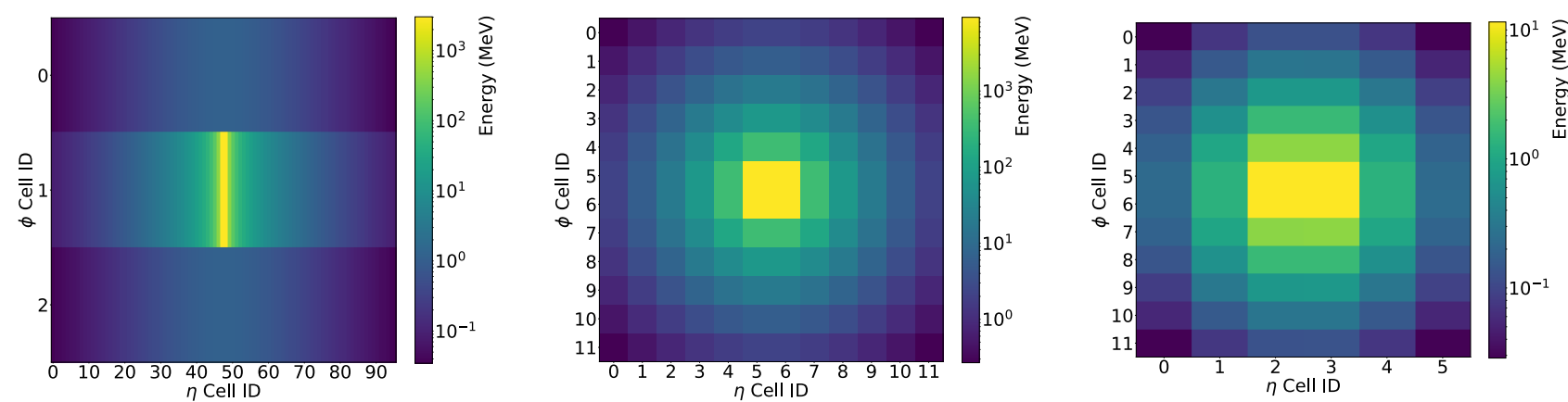
Performance Metrics for Generative Models

Generative Models for Simulation

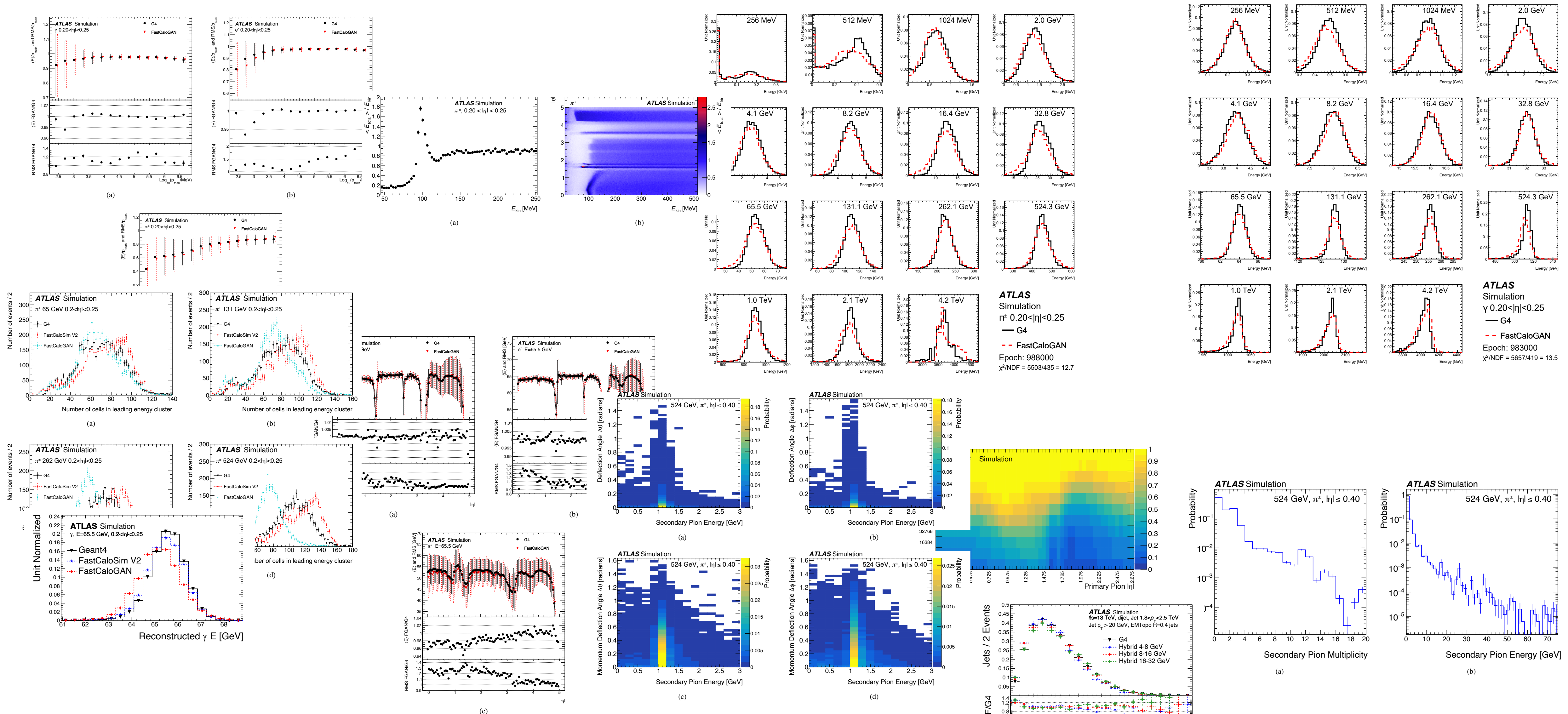
[Ghosh, ATLAS Collaboration, 2019](#)



[Paganini et al.](#)



Evaluating Fast Calo Simulators



Can we automatise the evaluation ?

[Krause and Shih, 2021](#)

5.4 Classifier metrics

In much of the GAN literature (see e.g. [8]), a common metric is to train classifiers to distinguish between different categories of data (e.g. e^+ vs. π^+), and to see if there is any difference in classifier performance when real data and generated data are interchanged. For example, one might train a classifier on e^+ vs. π^+ GEANT4 images, and compare this to a classifier trained on e^+ vs. π^+ GAN images. If the classifier trained on real images performs similarly to the classifier trained on generated images, then this is evidence that the generated images are approximating the real images well. One can repeat this test for different combinations of real and generated data.

The ultimate test of whether $p_{\text{generated}}(x) = p_{\text{data}}(x)$ would be a direct binary classifier between real and generated images of the *same* type. If the generated and true probability

Can we automatise the evaluation ?

[Krause and Shih, 2021](#)

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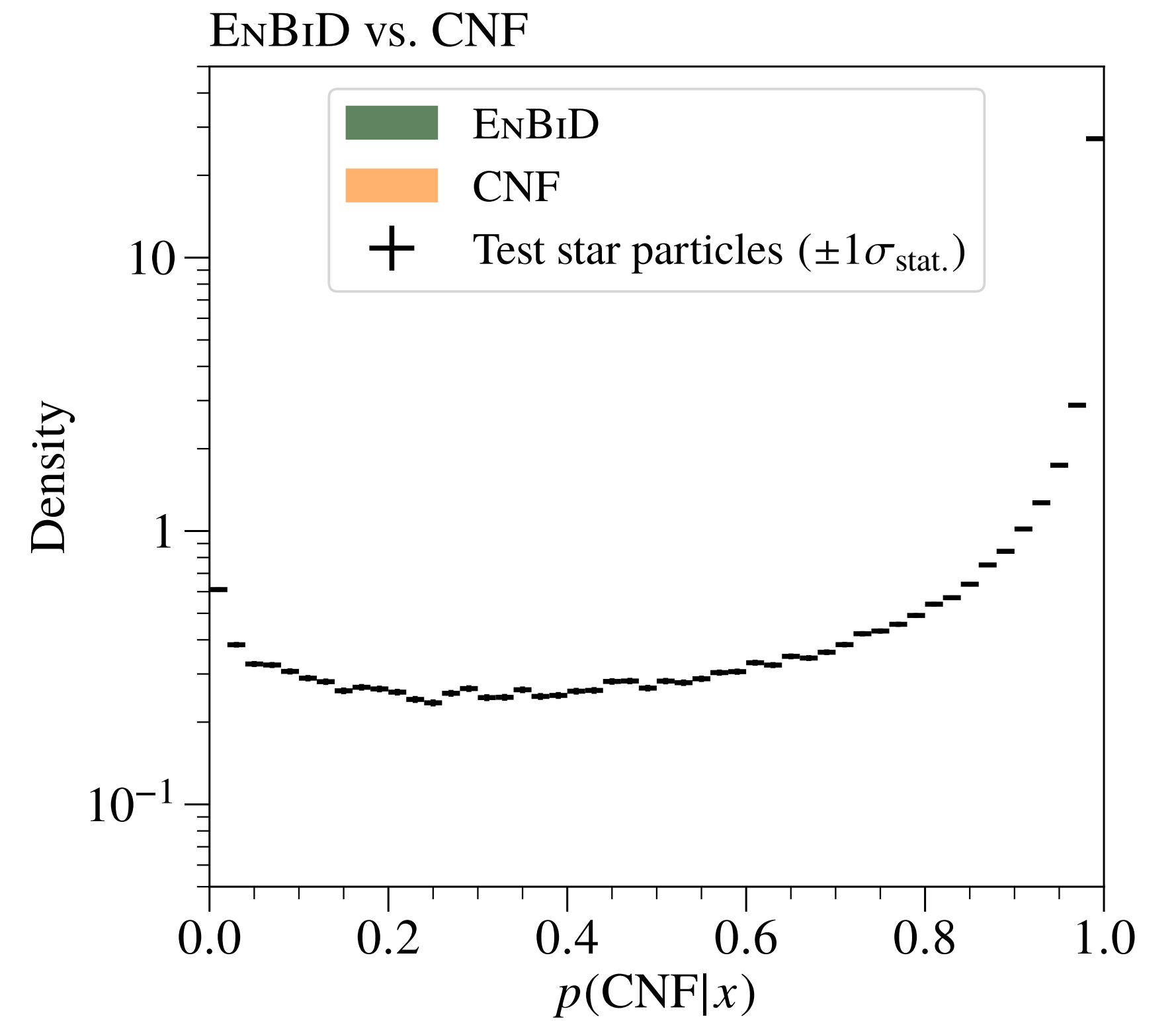
Classify Geant4 vs generated and use AUC as single metric

Another classifier test

[Lim et al, 2022](#)

Compare two generative models:



Classify generative model1 vs model2, check if test dataset agrees better with one or the other



A comparison of metrics

On the Evaluation of Generative Models in High Energy Physics

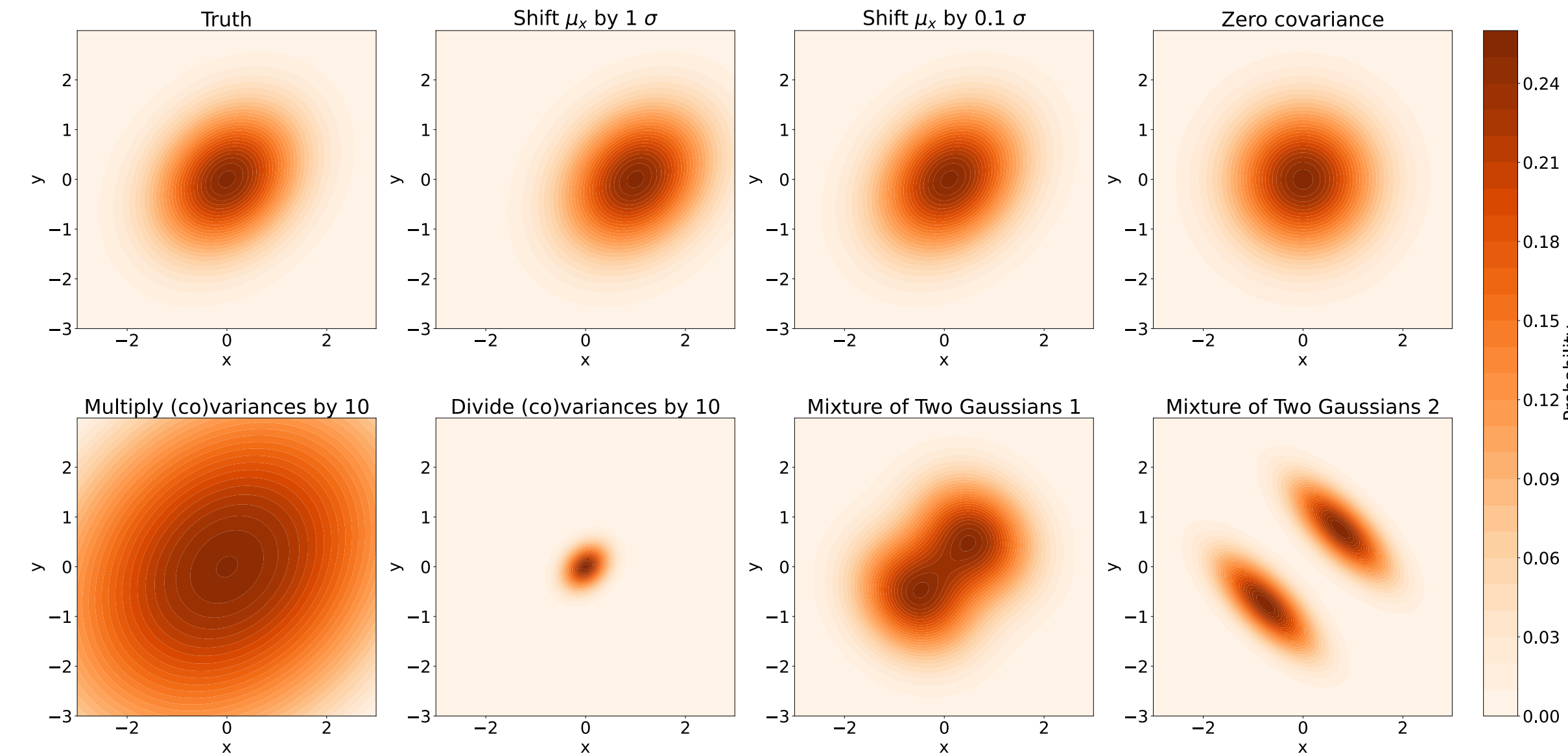
Raghav Kansal ^{*}, Anni Li , and Javier Duarte 
University of California San Diego, La Jolla, CA 92093, USA

Nadezda Chernyavskaya , Maurizio Pierini 
European Center for Nuclear Research (CERN), 1211 Geneva 23, Switzerland

Breno Orzari , Thiago Tomei 
Universidade Estadual Paulista, São Paulo/SP, CEP 01049-010, Brazil

(Dated: November 21, 2022)

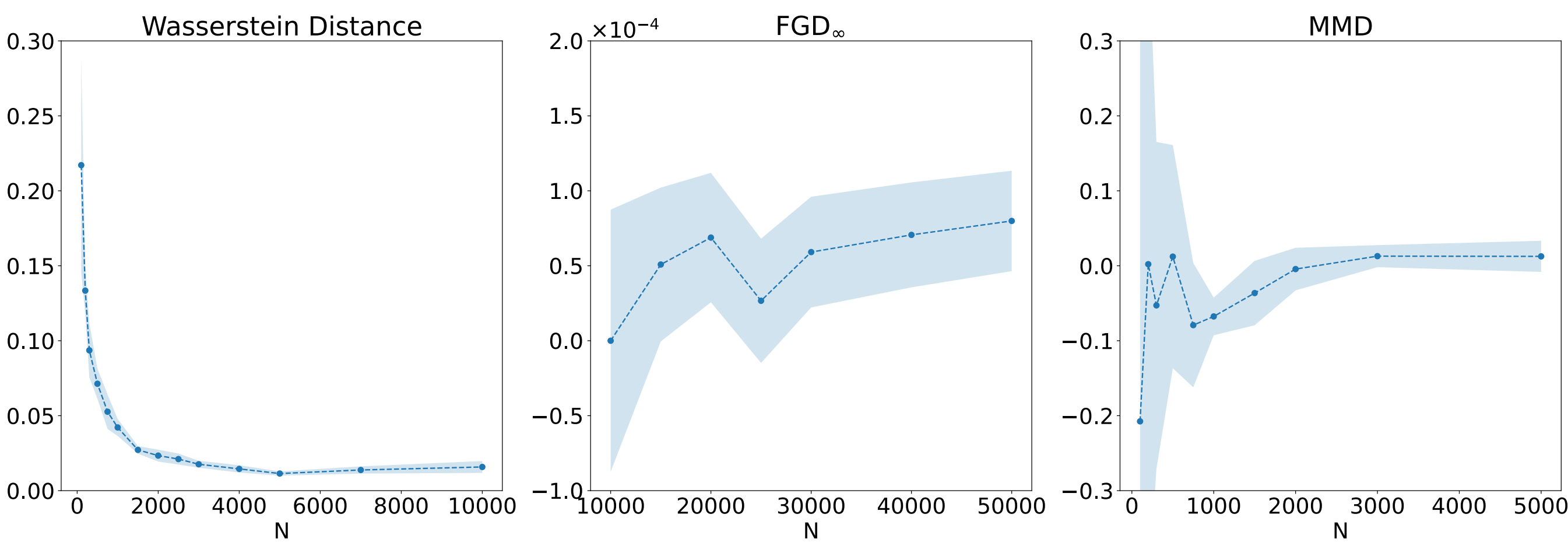
[Kansal et al, 2022](#)



Detailed comparison on Gaussian toys where you have full control

Application on jet dataset with hand designed distortions

Gaussian Study



- FGD_∞ , MMD unbiased
- W too expensive for large N

Metric	Truth	Shift μ_x by 1σ	Shift μ_x by 0.1σ	Zero covariance	Multiply (co)variances by 10	Divide (co)variances by 10	Mixture of Two Gaussians 1	Mixture of Two Gaussians 2
Wasserstein	0.016 ± 0.004	1.14 ± 0.02	0.043 ± 0.008	0.077 ± 0.006	9.8 ± 0.1	0.97 ± 0.01	0.036 ± 0.003	0.191 ± 0.005
$FGD_\infty \times 10^3$	0.08 ± 0.03	1011 ± 1	11.0 ± 0.1	32.3 ± 0.2	9400 ± 8	935.1 ± 0.7	0.07 ± 0.03	0.03 ± 0.03
MMD	0.01 ± 0.02	16.4 ± 0.9	0.07 ± 0.04	0.40 ± 0.08	$19k \pm 1k$	4.3 ± 0.1	0.06 ± 0.02	0.35 ± 0.03
Precision	0.972 ± 0.005	0.91 ± 0.01	0.976 ± 0.004	0.969 ± 0.006	0.34 ± 0.01	1.0 ± 0.0	0.975 ± 0.003	0.9976 ± 0.0007
Recall	0.997 ± 0.001	0.992 ± 0.003	0.997 ± 0.001	0.9976 ± 0.0006	0.998 ± 0.001	0.58 ± 0.02	0.996 ± 0.001	0.9970 ± 0.0009
Density	3.23 ± 0.06	2.48 ± 0.08	3.19 ± 0.07	3.1 ± 0.1	0.60 ± 0.02	5.7 ± 0.3	2.99 ± 0.09	0.989 ± 0.009
Coverage	0.876 ± 0.002	0.780 ± 0.006	0.872 ± 0.005	0.872 ± 0.004	0.60 ± 0.01	0.406 ± 0.008	0.871 ± 0.002	0.956 ± 0.006

FGD_∞ most promising
(but no sensitivity to higher moments, requires extrapolation)

Jet Study

[Kansal et al, 2022](#)

Metric	Truth	Smeared	Shifted	Removing tail	Particle features smeared	Particle η^{rel} smeared	Particle $p_{\text{T}}^{\text{rel}}$ smeared	Particle $p_{\text{T}}^{\text{rel}}$ shifted
$W_1^M \times 10^3$	0.28 ± 0.05	2.1 ± 0.2	6.0 ± 0.3	0.6 ± 0.2	1.7 ± 0.2	0.9 ± 0.3	0.5 ± 0.2	5.8 ± 0.2
Wasserstein EFP	0.02 ± 0.01	0.09 ± 0.05	0.10 ± 0.02	0.016 ± 0.007	0.19 ± 0.08	0.03 ± 0.01	0.03 ± 0.02	0.06 ± 0.02
FGD $_{\infty}$ EFP $\times 10^3$	0.01 ± 0.02	21.5 ± 0.3	26.8 ± 0.3	2.31 ± 0.07	23.4 ± 0.3	3.59 ± 0.09	2.29 ± 0.05	28.9 ± 0.2
MMD EFP $\times 10^3$	-0.006 ± 0.005	0.17 ± 0.06	0.9 ± 0.1	0.03 ± 0.02	0.35 ± 0.09	0.08 ± 0.05	0.01 ± 0.02	1.8 ± 0.1
Precision EFP	0.9 ± 0.1	0.94 ± 0.04	0.978 ± 0.005	0.88 ± 0.08	0.7 ± 0.1	0.94 ± 0.06	0.7 ± 0.1	0.79 ± 0.09
Recall EFP	0.9 ± 0.1	0.88 ± 0.07	0.97 ± 0.01	0.92 ± 0.06	0.83 ± 0.05	0.92 ± 0.07	0.8 ± 0.1	0.8 ± 0.1
Wasserstein PN	1.65 ± 0.06	1.7 ± 0.1	2.4 ± 0.4	1.71 ± 0.08	4.5 ± 0.1	1.79 ± 0.05	4.0 ± 0.4	7.6 ± 0.2
FGD $_{\infty}$ PN $\times 10^3$	0.8 ± 0.7	40 ± 2	193 ± 9	5.0 ± 0.9	1250 ± 10	20 ± 1	1230 ± 10	3640 ± 10
MMD PN $\times 10^3$	-2 ± 2	4 ± 8	80 ± 10	-1 ± 4	500 ± 100	3 ± 2	560 ± 60	1100 ± 40
Precision PN	0.68 ± 0.07	0.64 ± 0.04	0.71 ± 0.06	0.73 ± 0.03	0.09 ± 0.04	0.75 ± 0.08	0.08 ± 0.04	0.39 ± 0.08
Recall PN	0.70 ± 0.05	0.61 ± 0.04	0.61 ± 0.08	0.73 ± 0.06	0.014 ± 0.009	0.7 ± 0.1	0.01 ± 0.01	0.57 ± 0.09
Classifier LLF AUC	0.50	0.52	0.54	0.50	0.97	0.81	0.93	0.99
Classifier HLF AUC	0.50	0.53	0.55	0.50	0.84	0.64	0.74	0.92

- FGD_{∞} on EFPs does quite well in these tests
- Would be interesting to see it used and stress tested !

Bayesian Generative Models

Bayesian Generative Models

[Butter et al.](#)

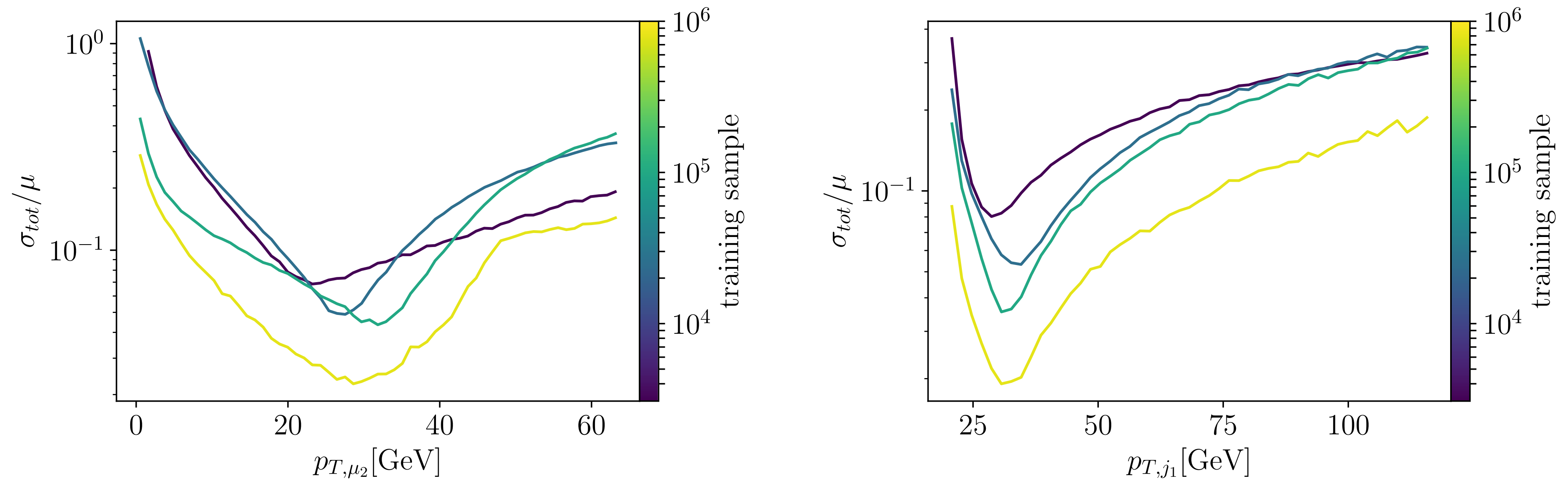


Figure 12: Relative uncertainty from the BINN for the $Z + 1$ jet sample, as a function of the size of the training sample.

Other uncertainty methods

Differentiable Programming: Optimise your final objective directly

[Simpson et al.](#)

Following Inferno [[de Castro et al.](#)]

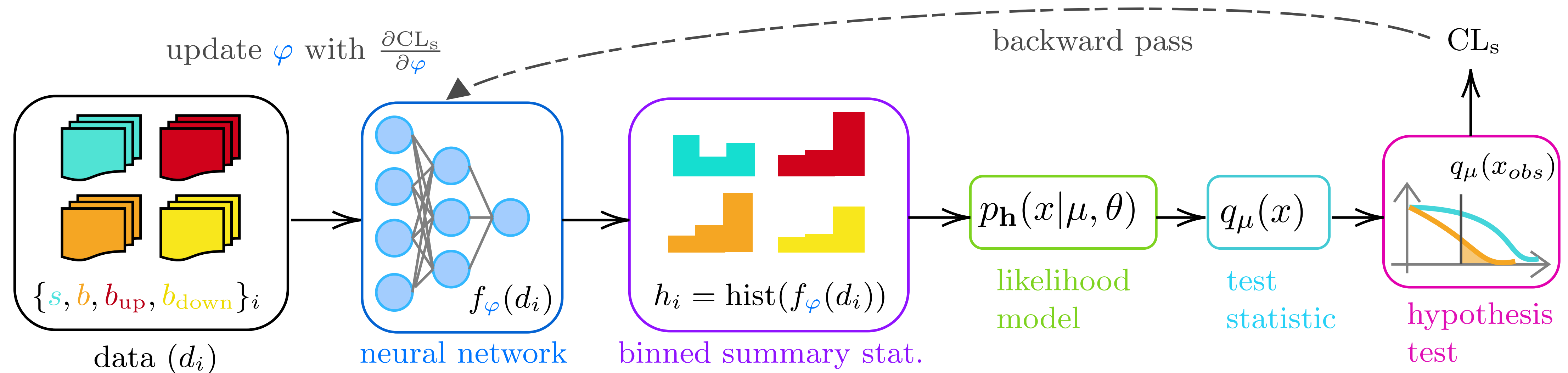


Figure 1. The pipeline for **neos**. The dashed line indicating the backward pass involves updating the weights φ of the neural network via gradient descent.

Unfolding with nuisance parameters

[Chan and Nachman arXiv:2302.05390](#)

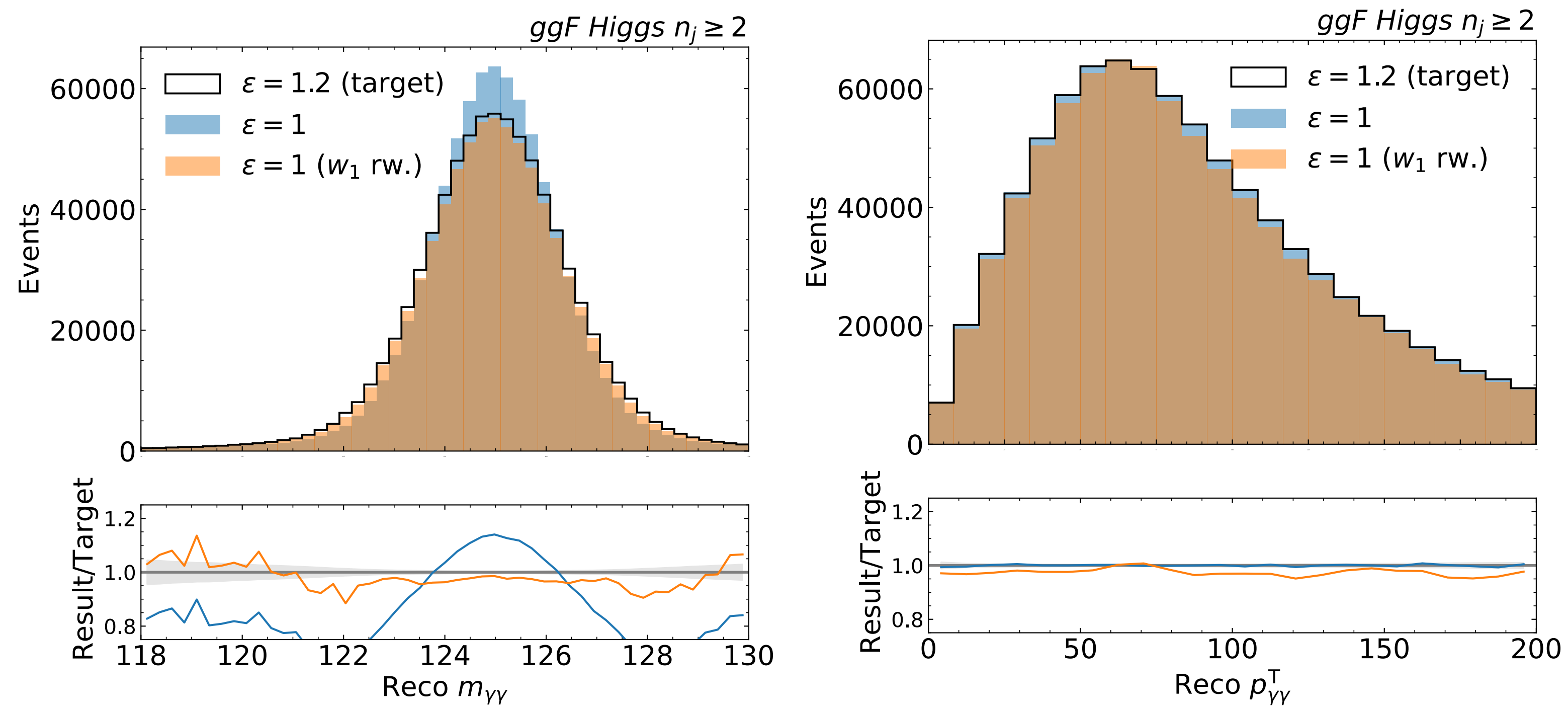
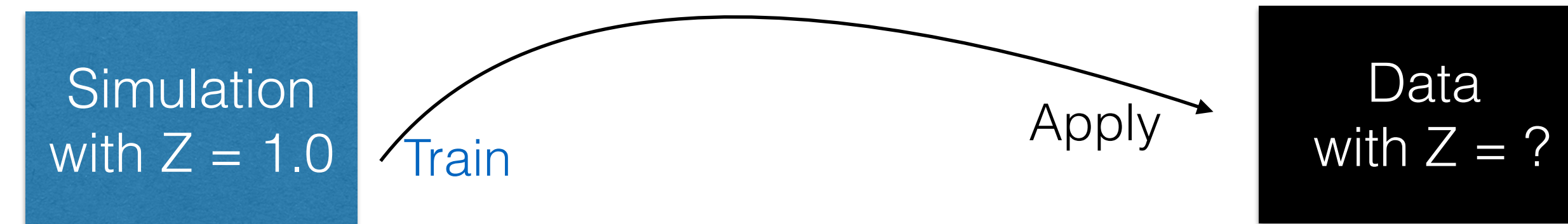


FIG. 6. Higgs boson cross section: the nominal detector-level spectra $m_{\gamma\gamma}$ (left) and $p_{\gamma\gamma}^T$ (right) with $\epsilon_\gamma = 1$ reweighted by the trained w_1 conditioned at $\epsilon_\gamma = 1.2$ and compared to the spectra with $\epsilon_\gamma = 1.2$.

More on uncertainty-aware networks

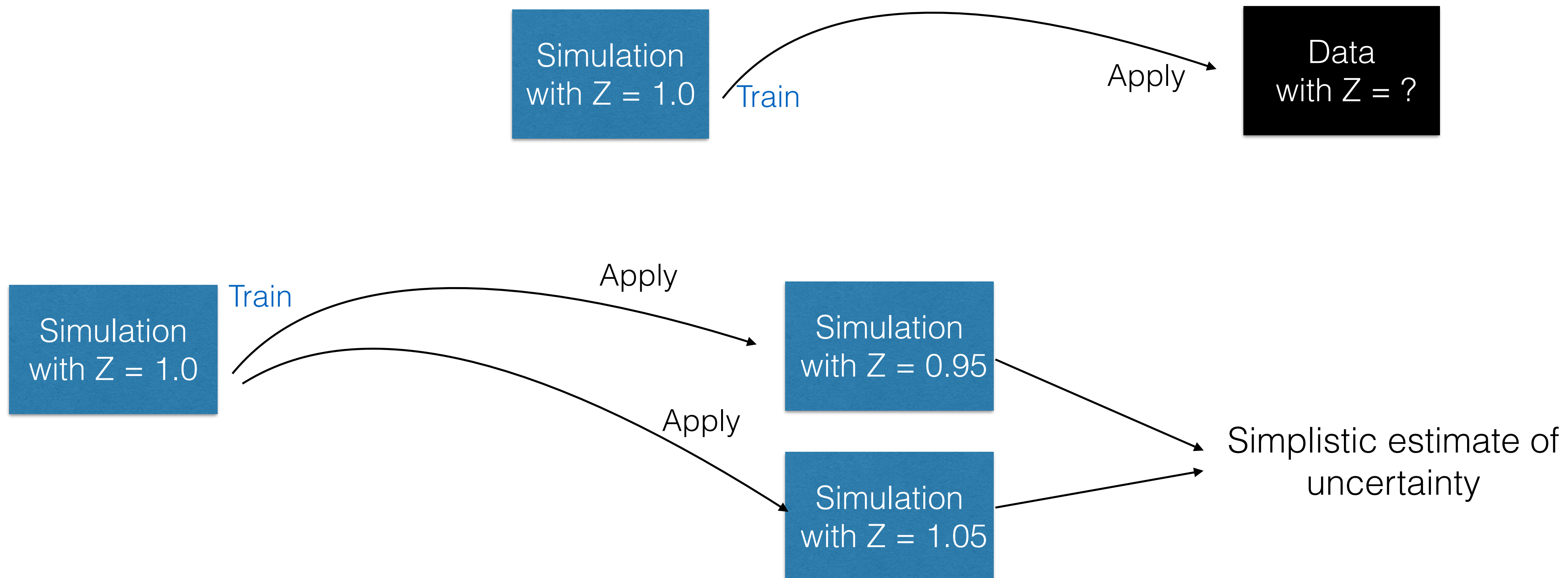
Baseline Approach to Uncertainty Quantification

Train AI classifier on nominal data (assume detector state $Z=1$) and estimate uncertainties using alternate simulations



Baseline Approach to Uncertainty Quantification

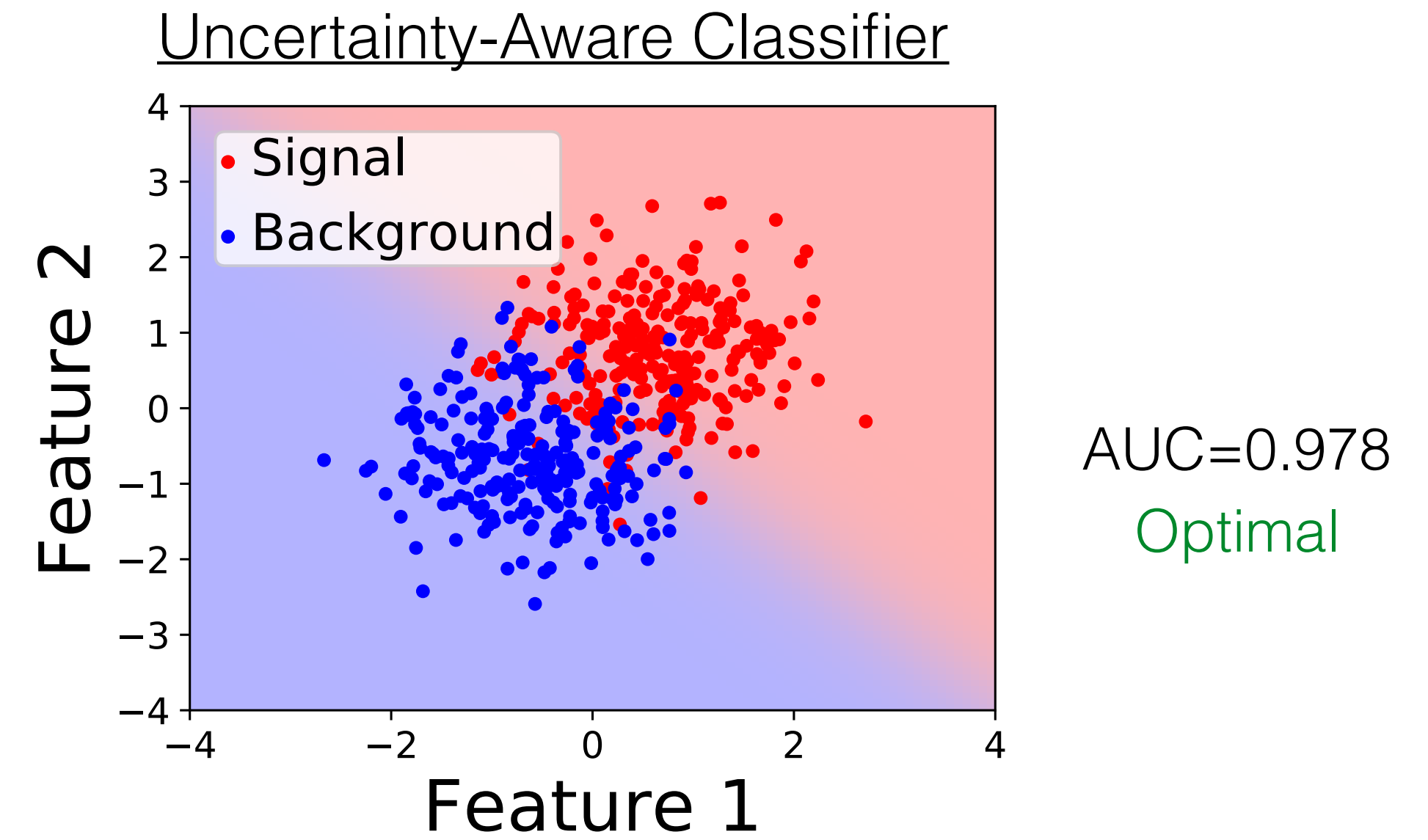
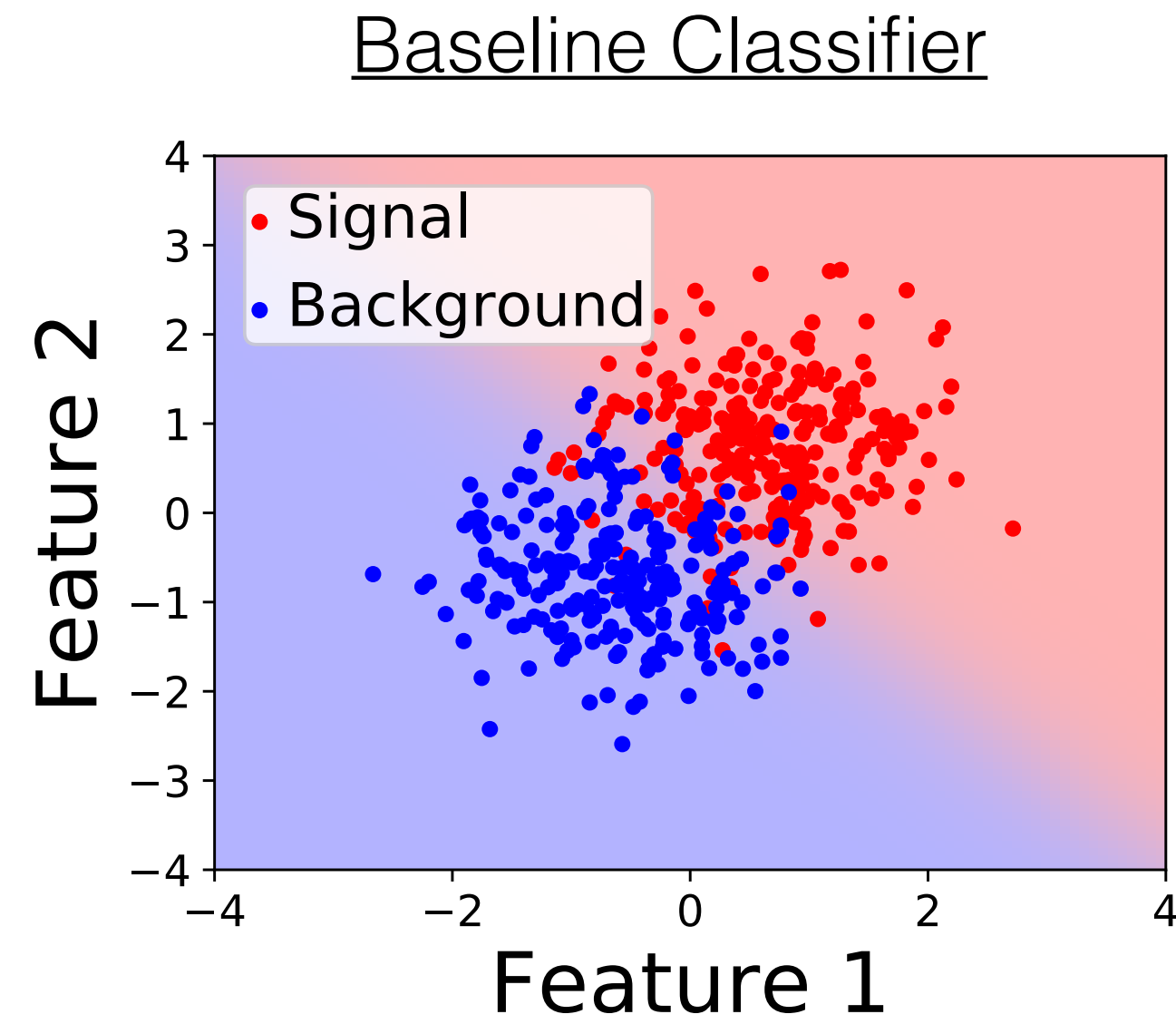
Train AI classifier on nominal data (assume detector state $Z=1$) and estimate uncertainties using alternate simulations



Full statistical treatment → Expensive 'Profile Likelihood'

Nominal and Systematic Up Examples

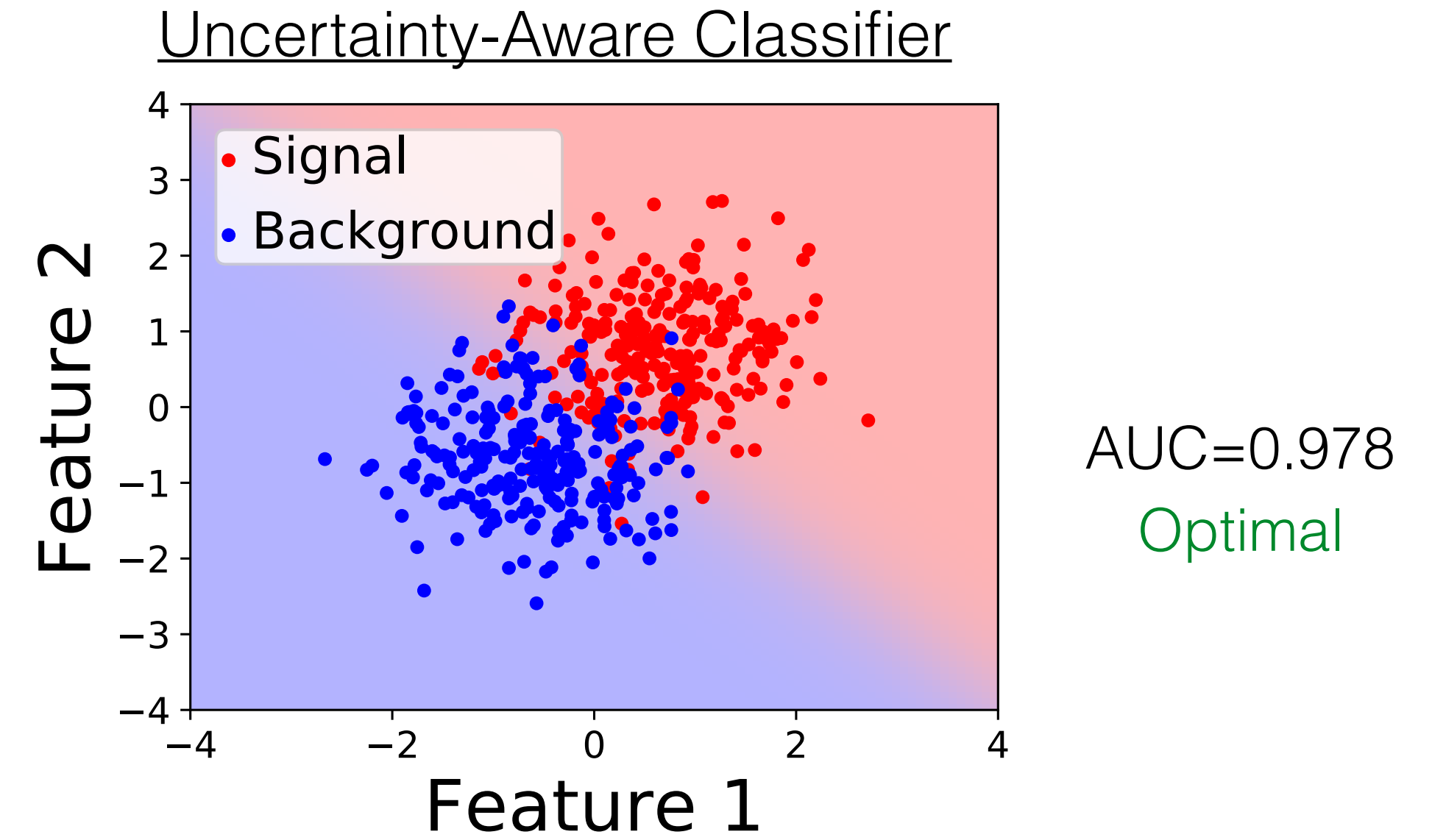
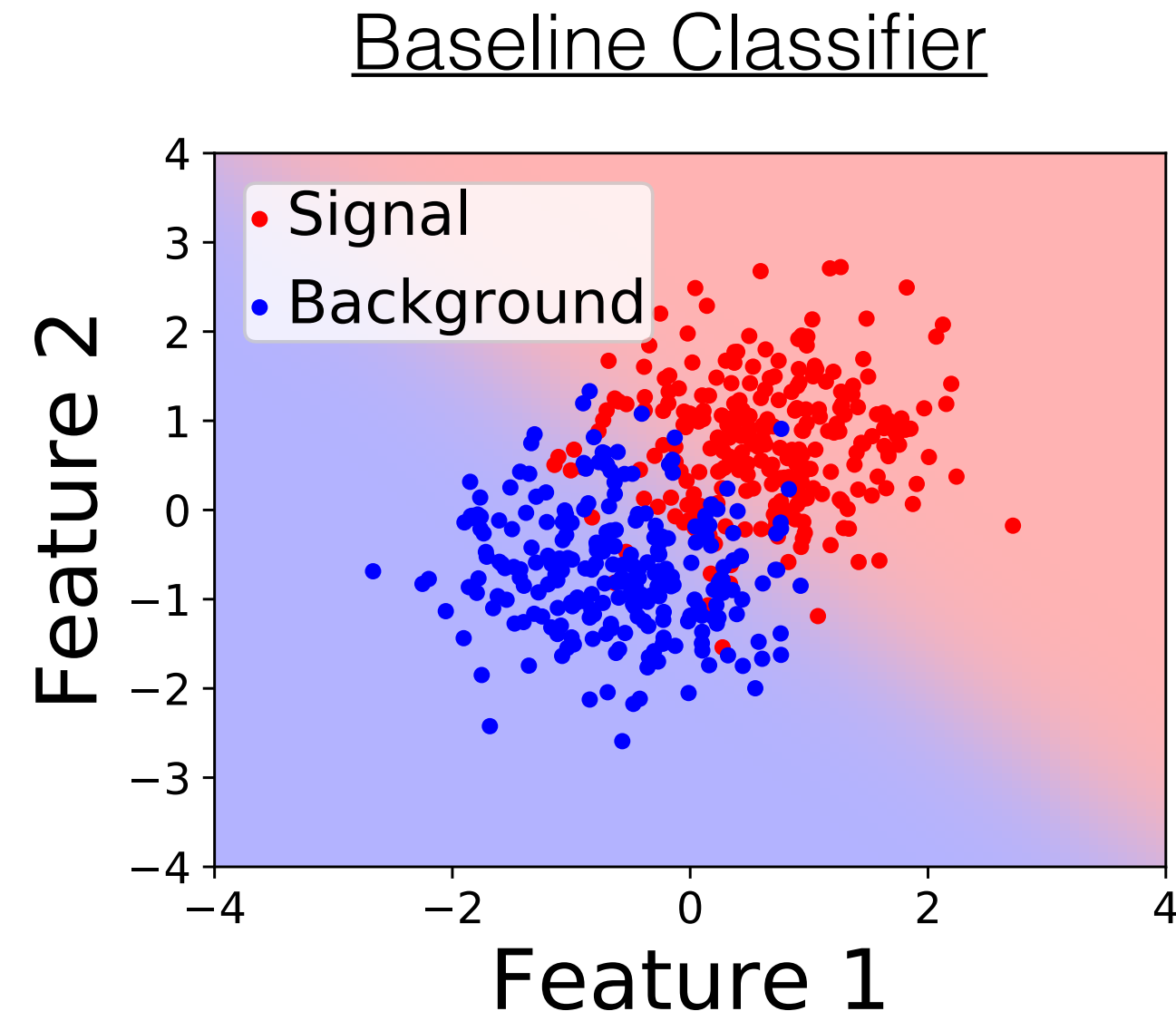
Nominal “Data”



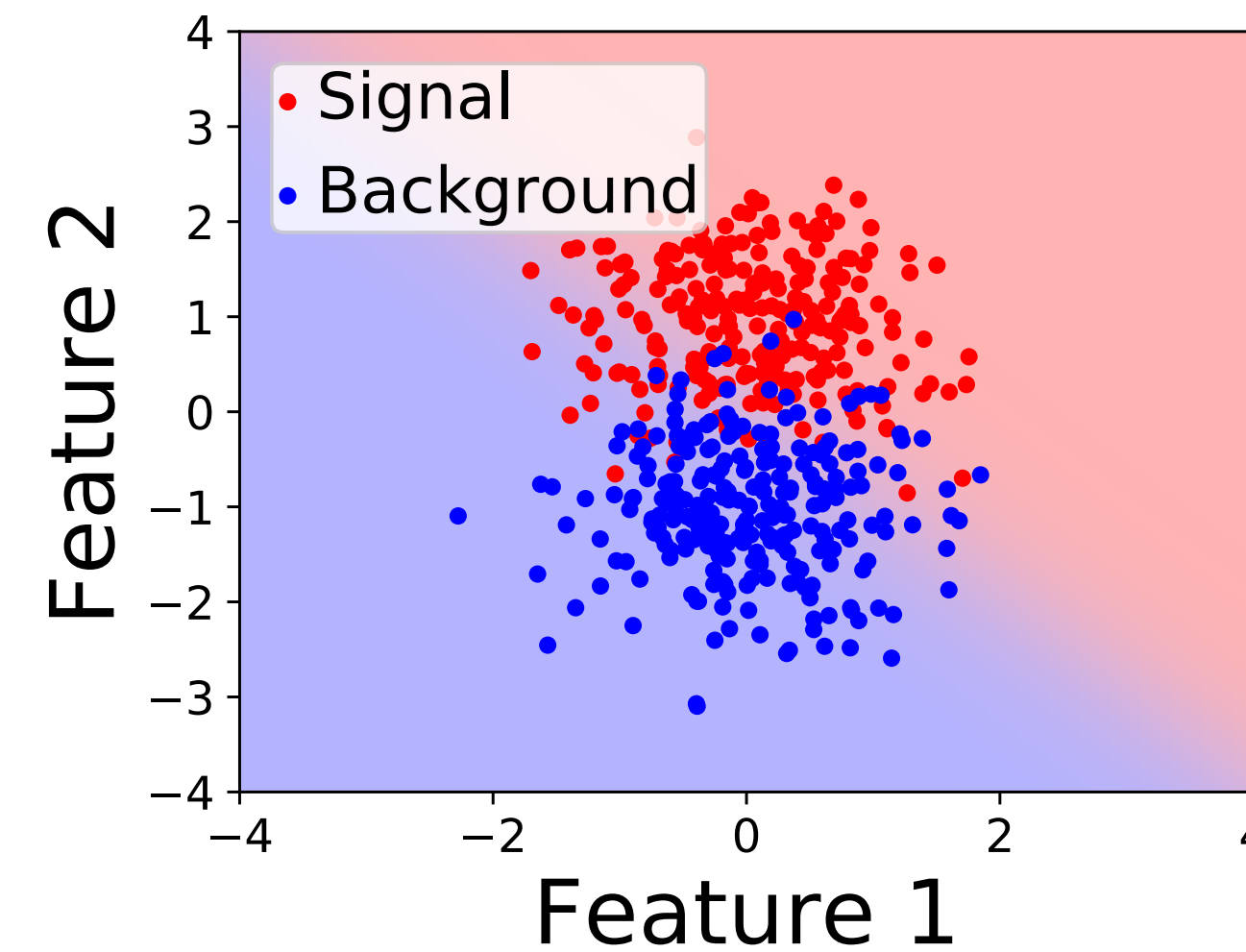
SystUp “Data”

Nominal and Systematic Up Examples

Nominal "Data"

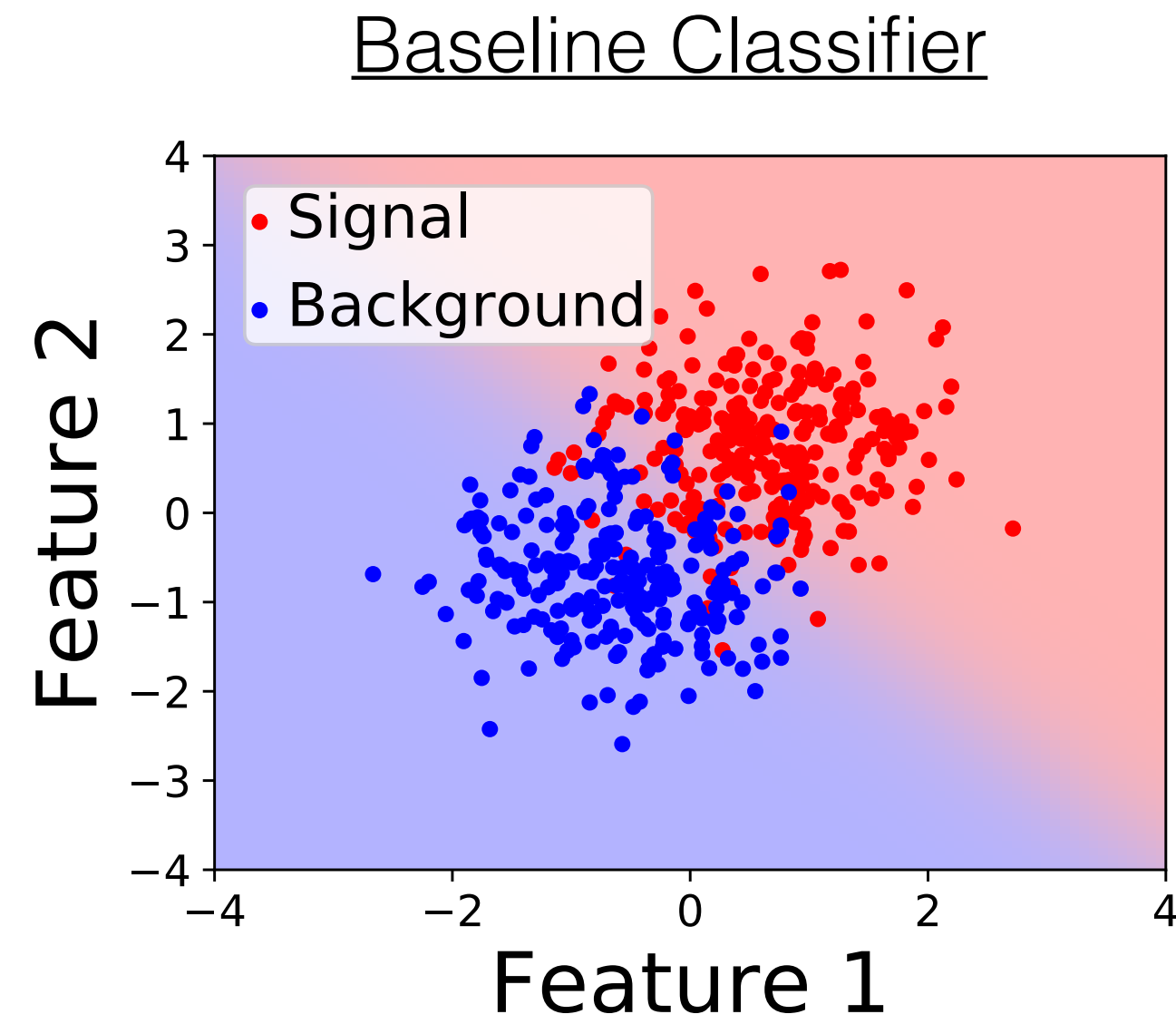


SystUp "Data"

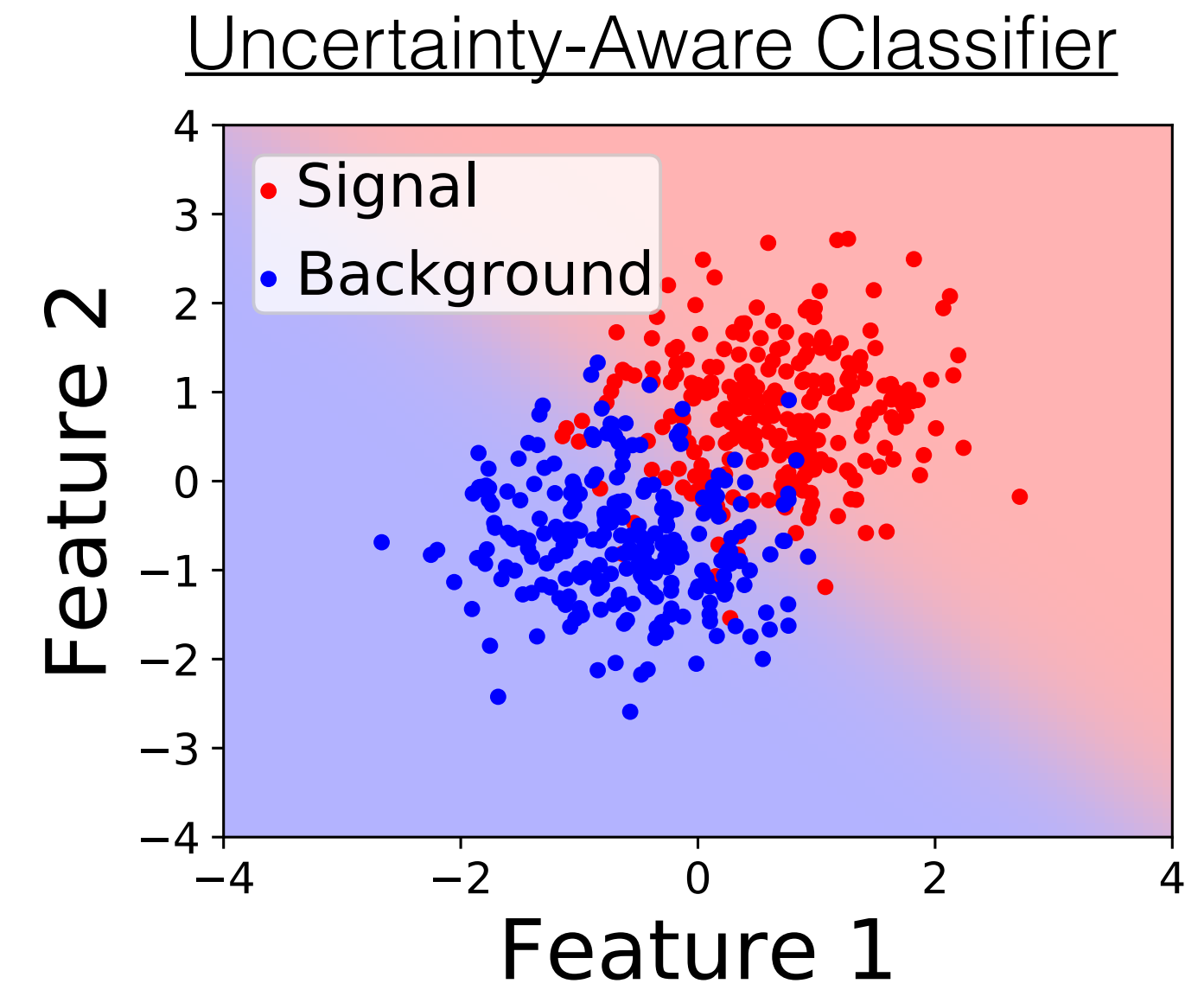


Nominal and Systematic Up Examples

Nominal "Data"

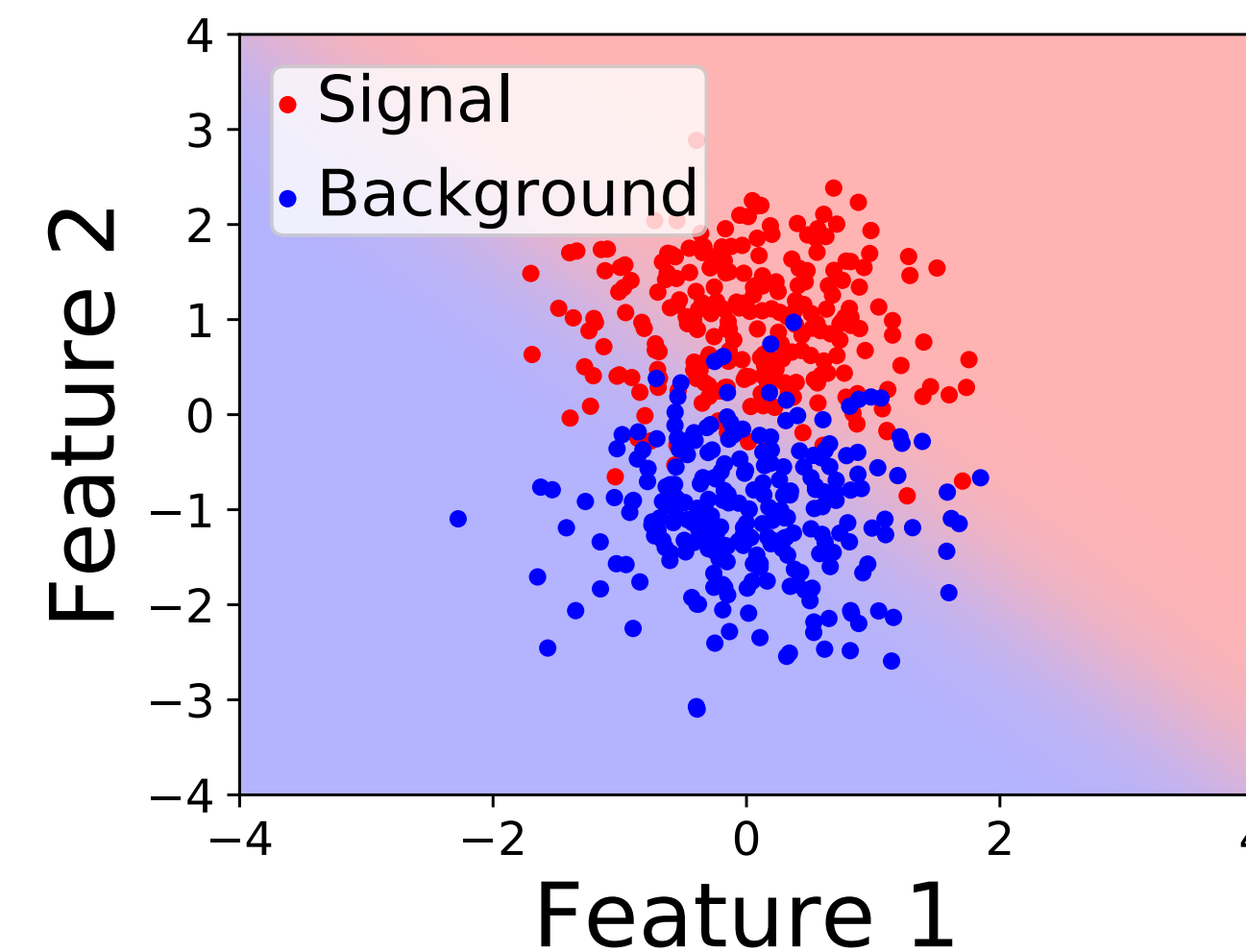


AUC=0.978
Optimal

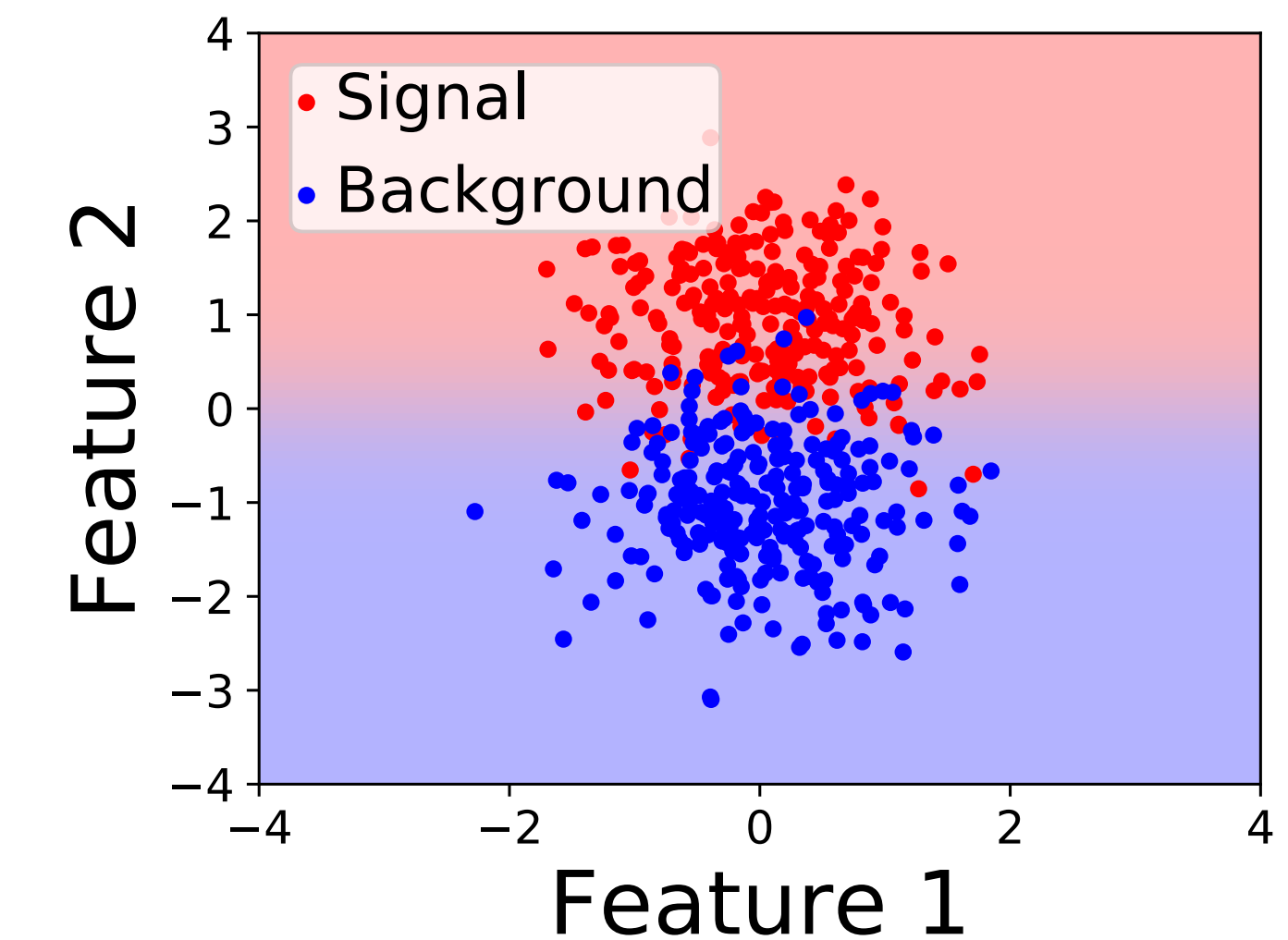


AUC=0.978
Optimal

SystUp "Data"



AUC=0.924
Sub-Optimal

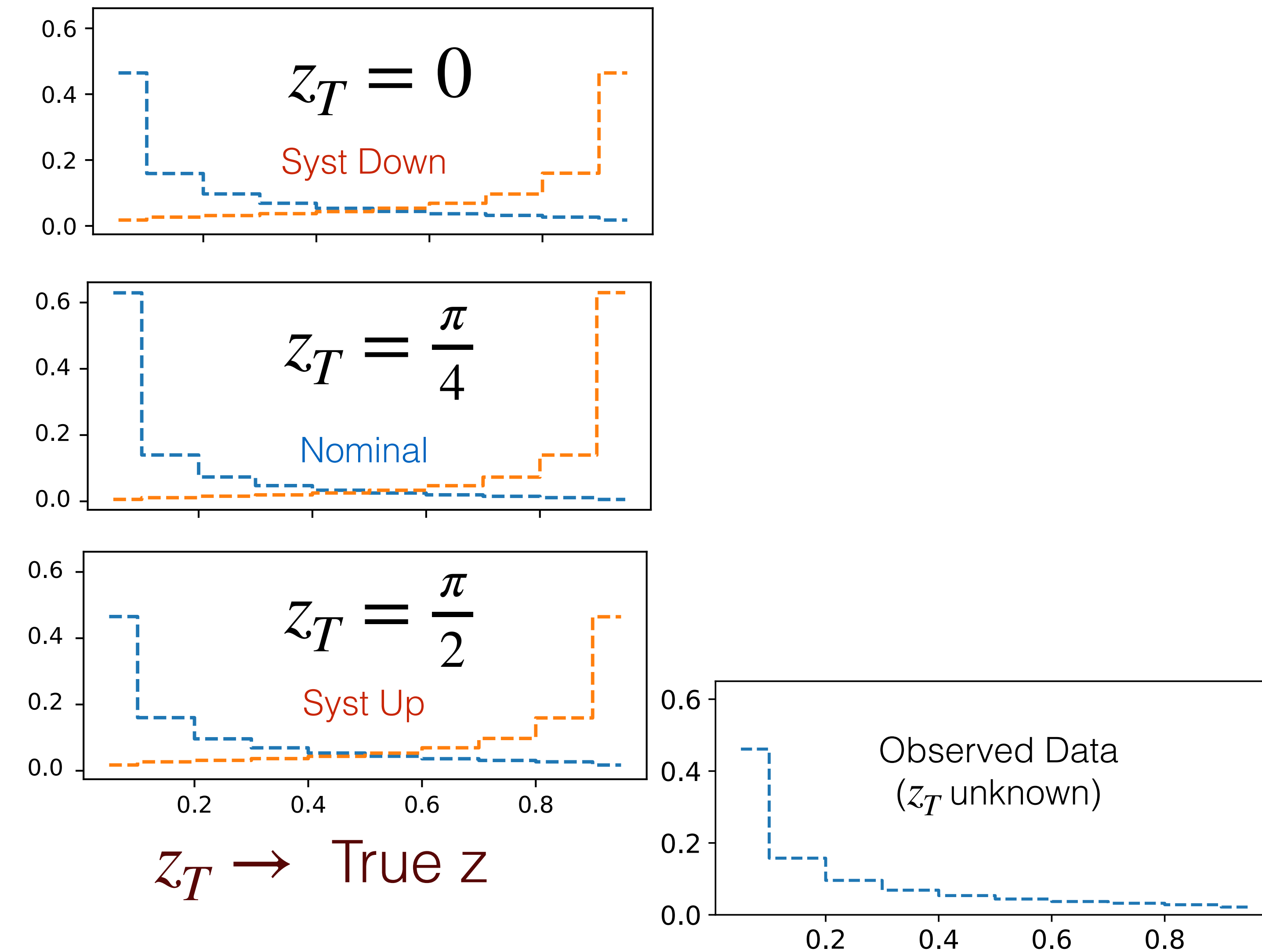


AUC=0.978
Optimal

Uncer-Aware Classifier is able to rotate its decision function based on Z while the Baseline Classifier decision function remains frozen⁴⁹

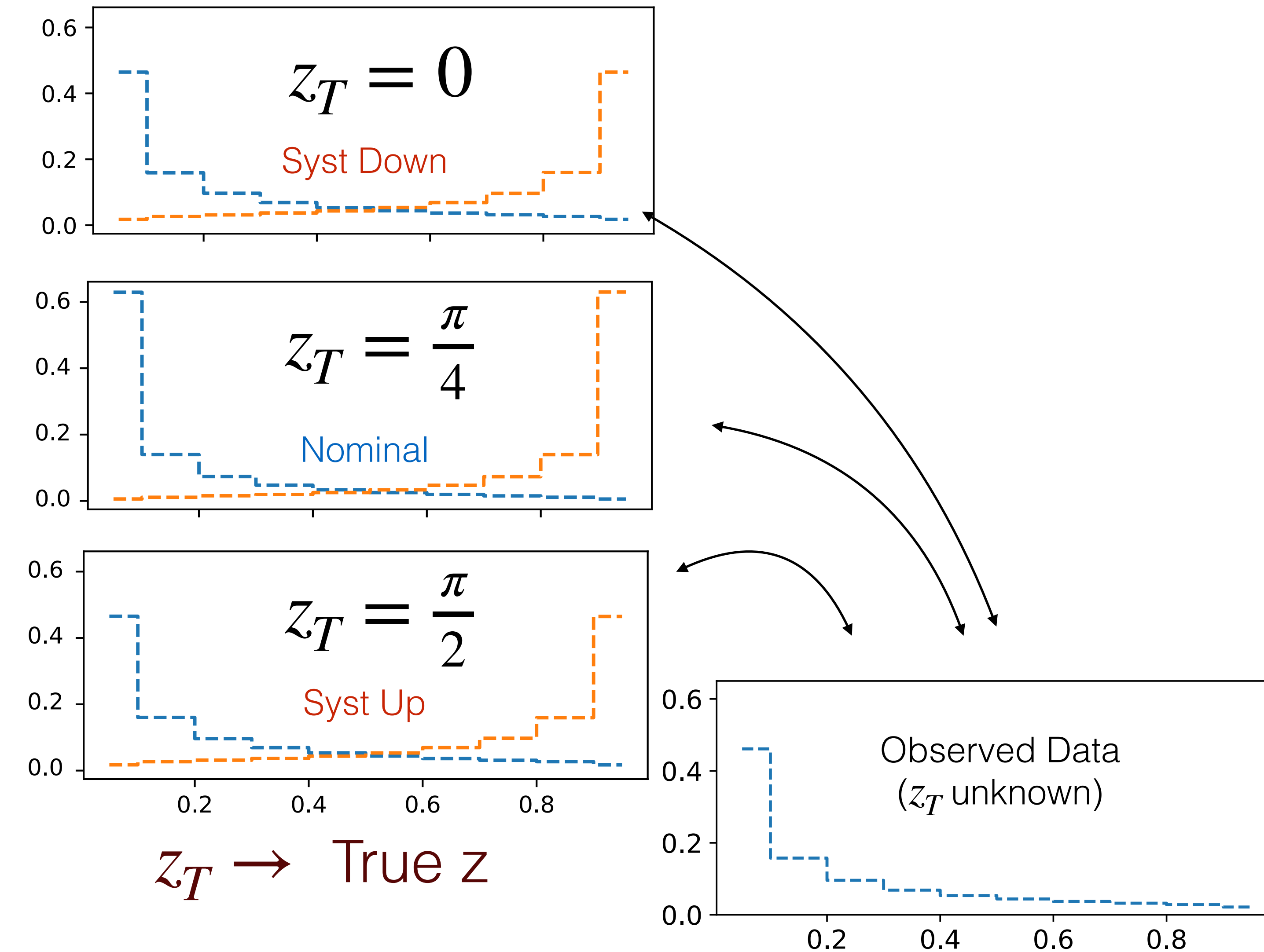
Scan the 2D Likelihood space in Z vs μ

Template **Baseline Classifier** Score Histograms for various Z



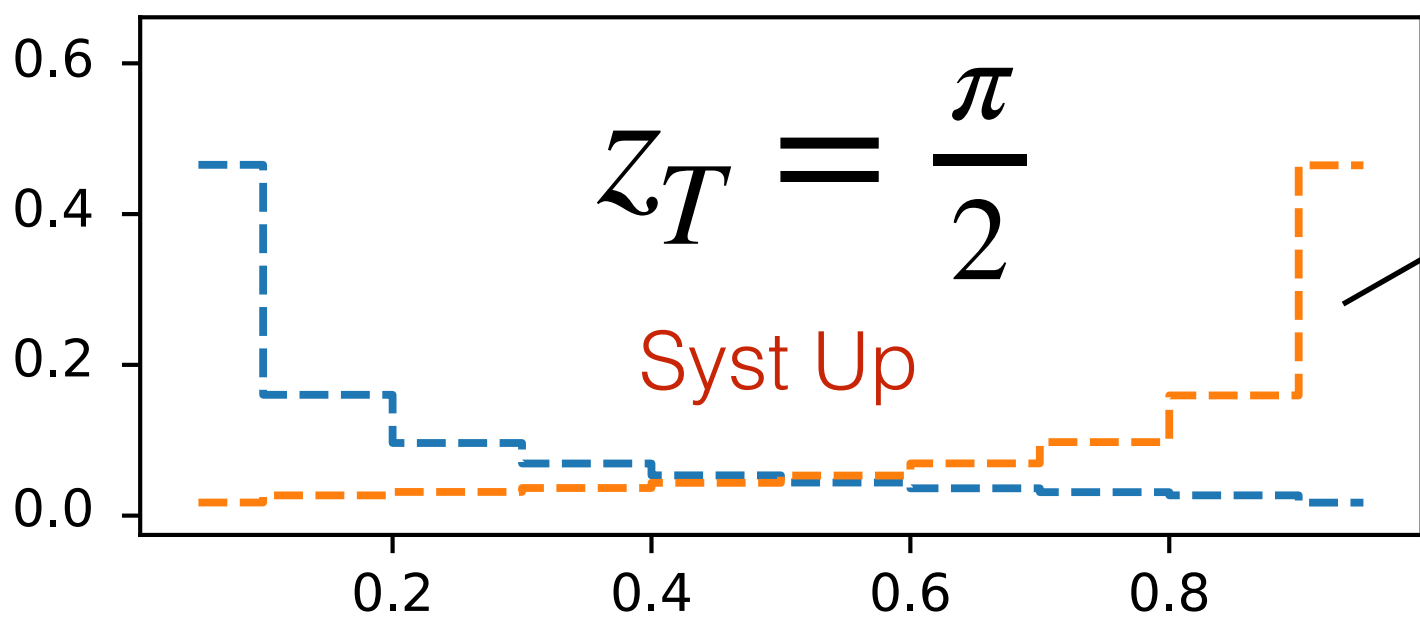
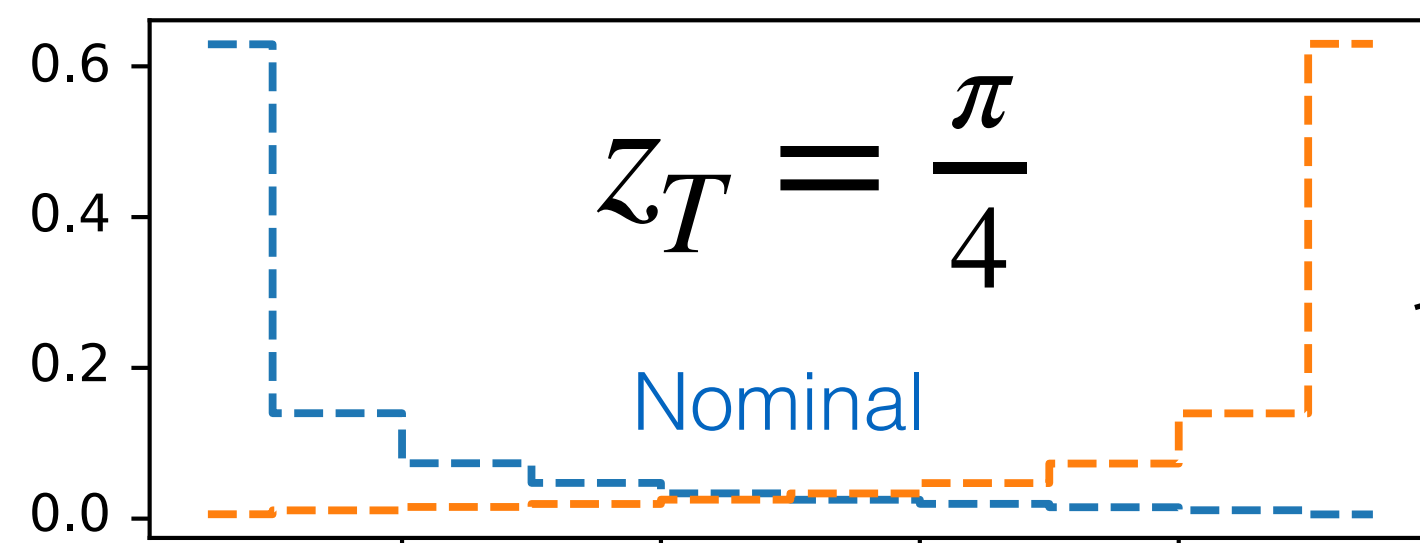
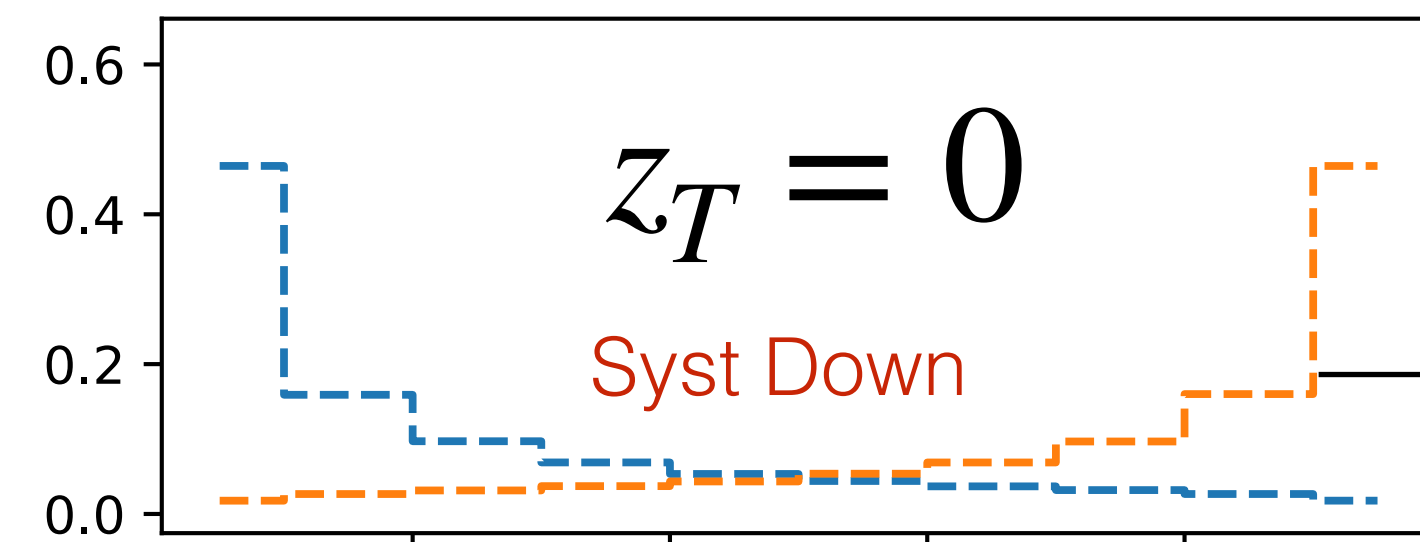
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Template **Baseline Classifier** Score Histograms for various Z

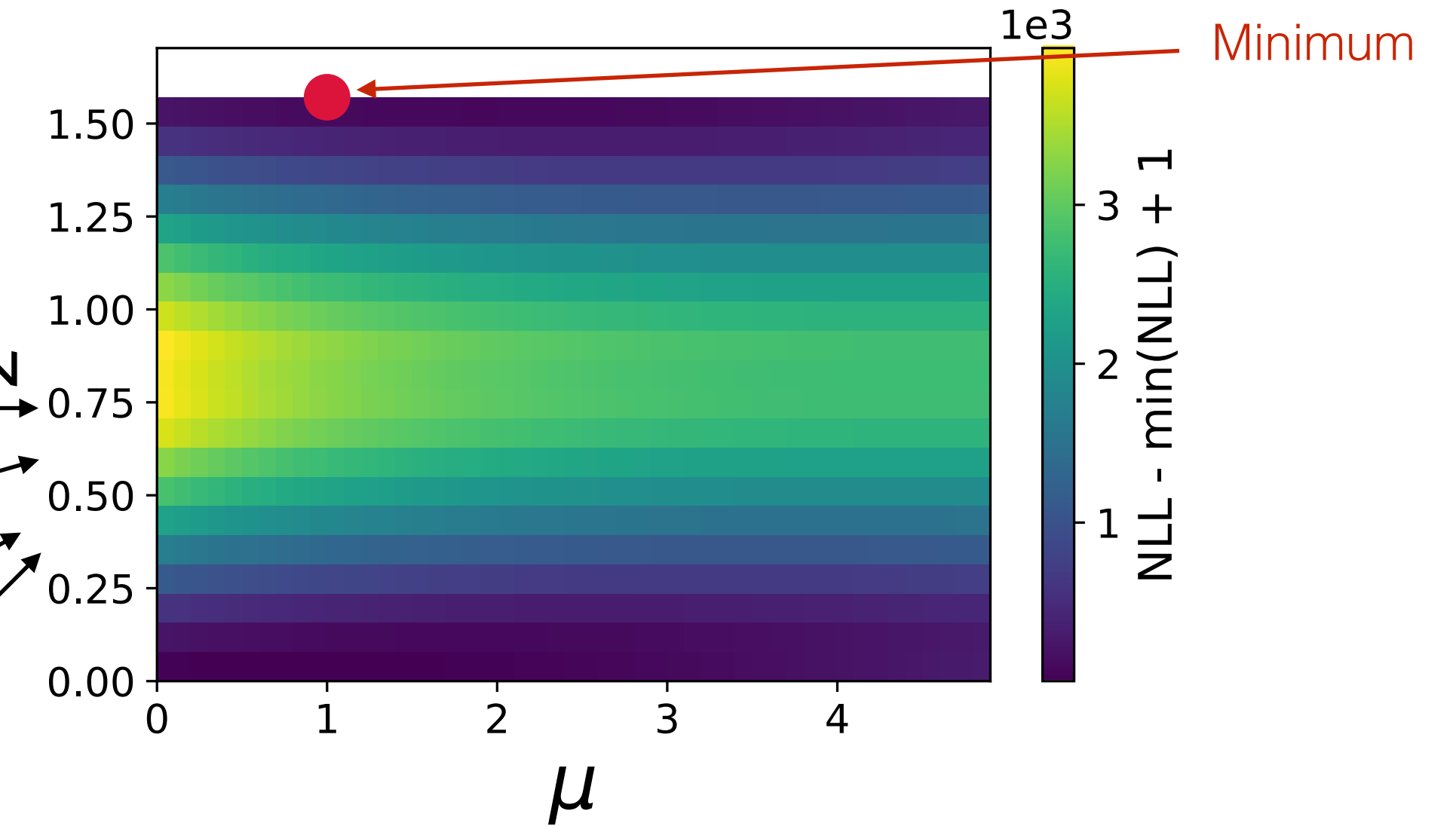
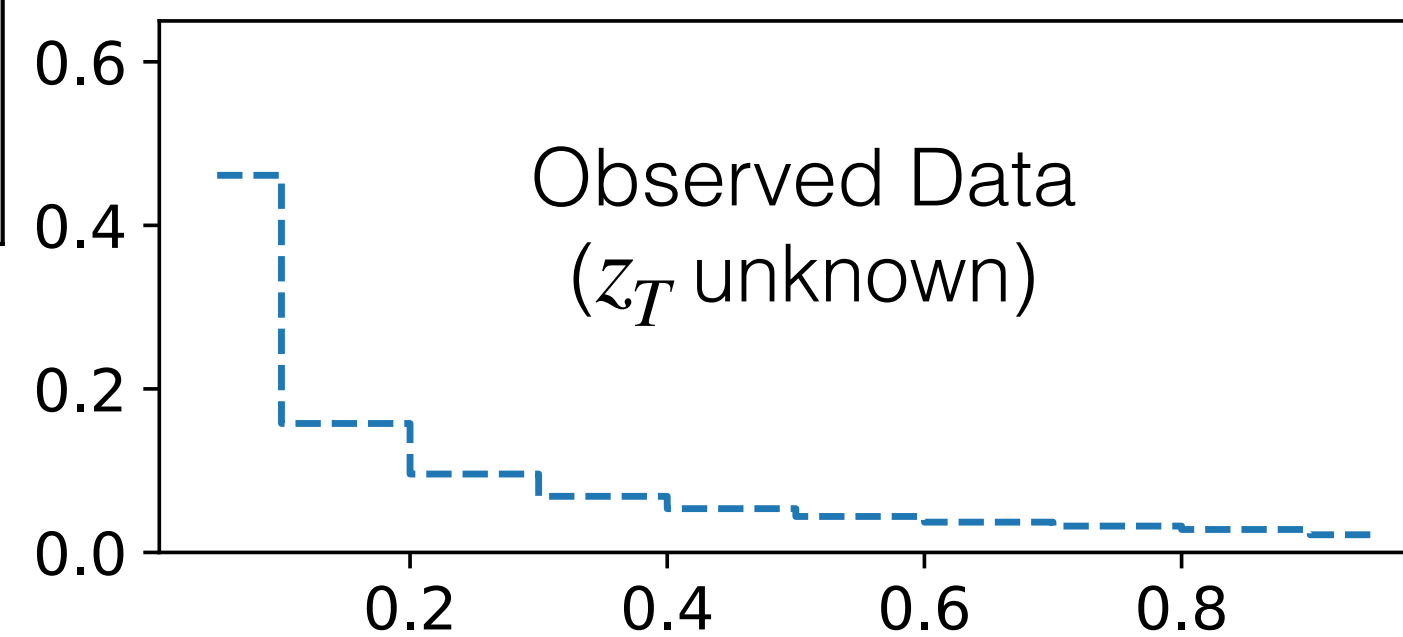


Scan the 2D Likelihood space in Z vs μ

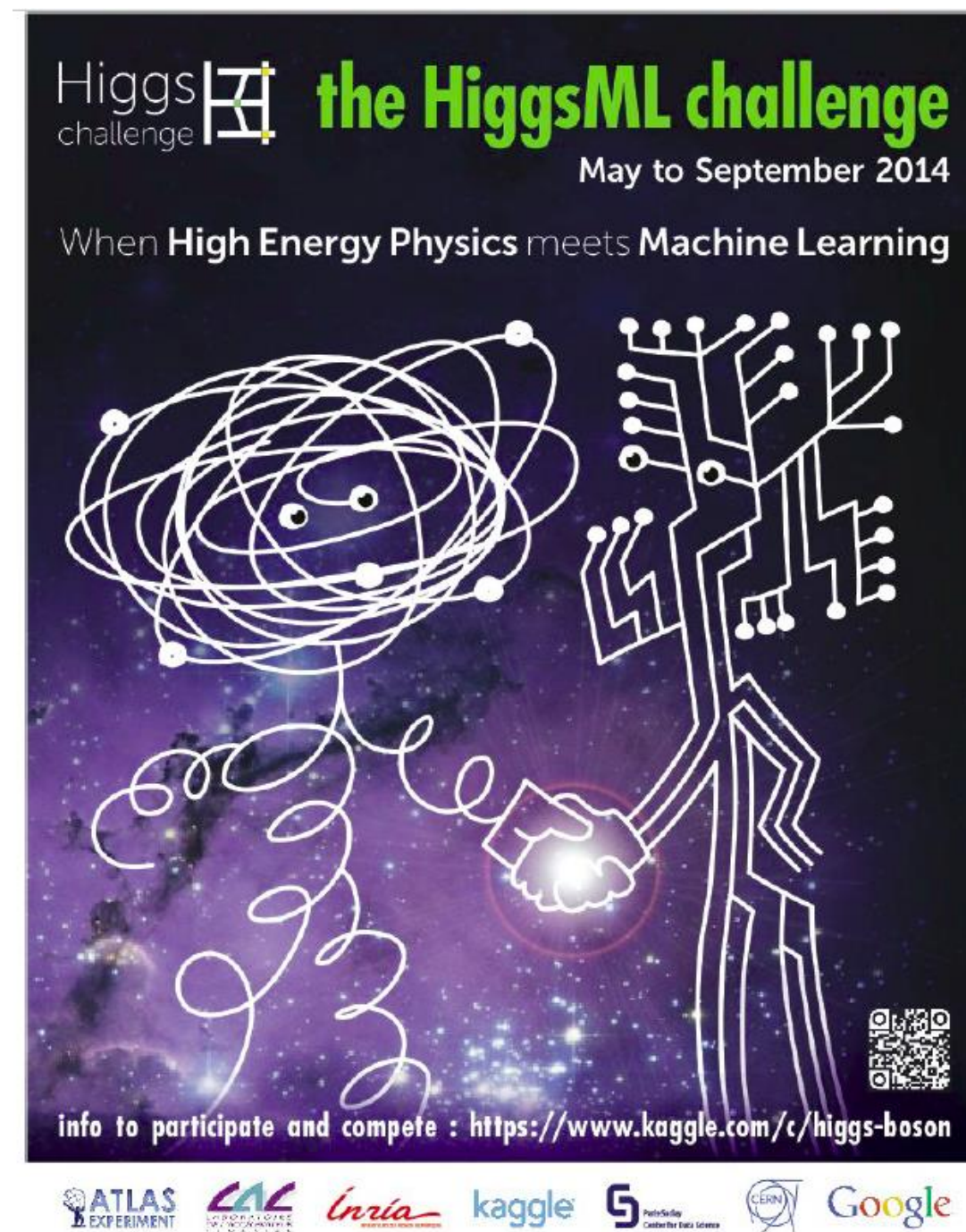
Template **Baseline Classifier** Score Histograms for various Z



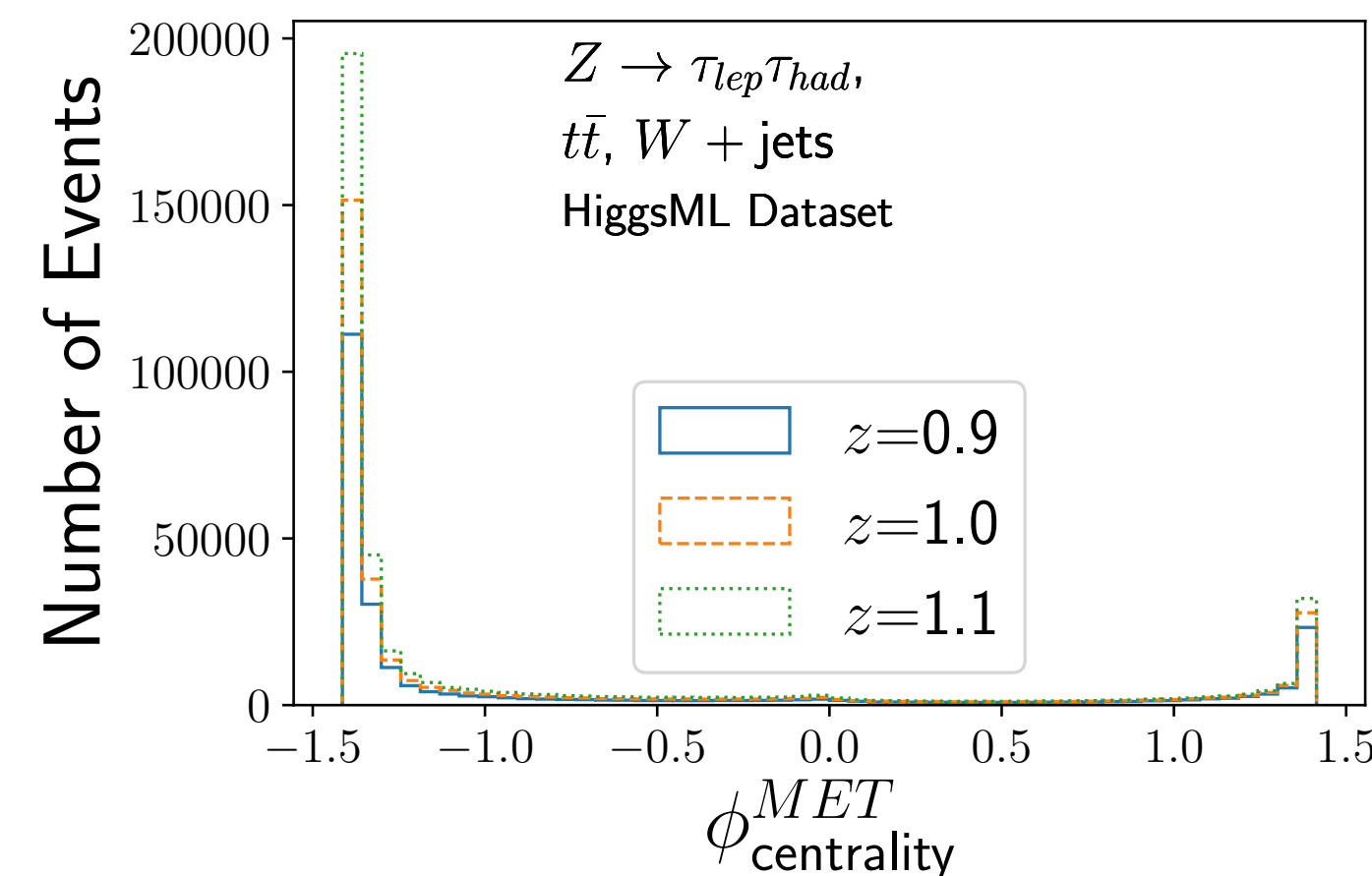
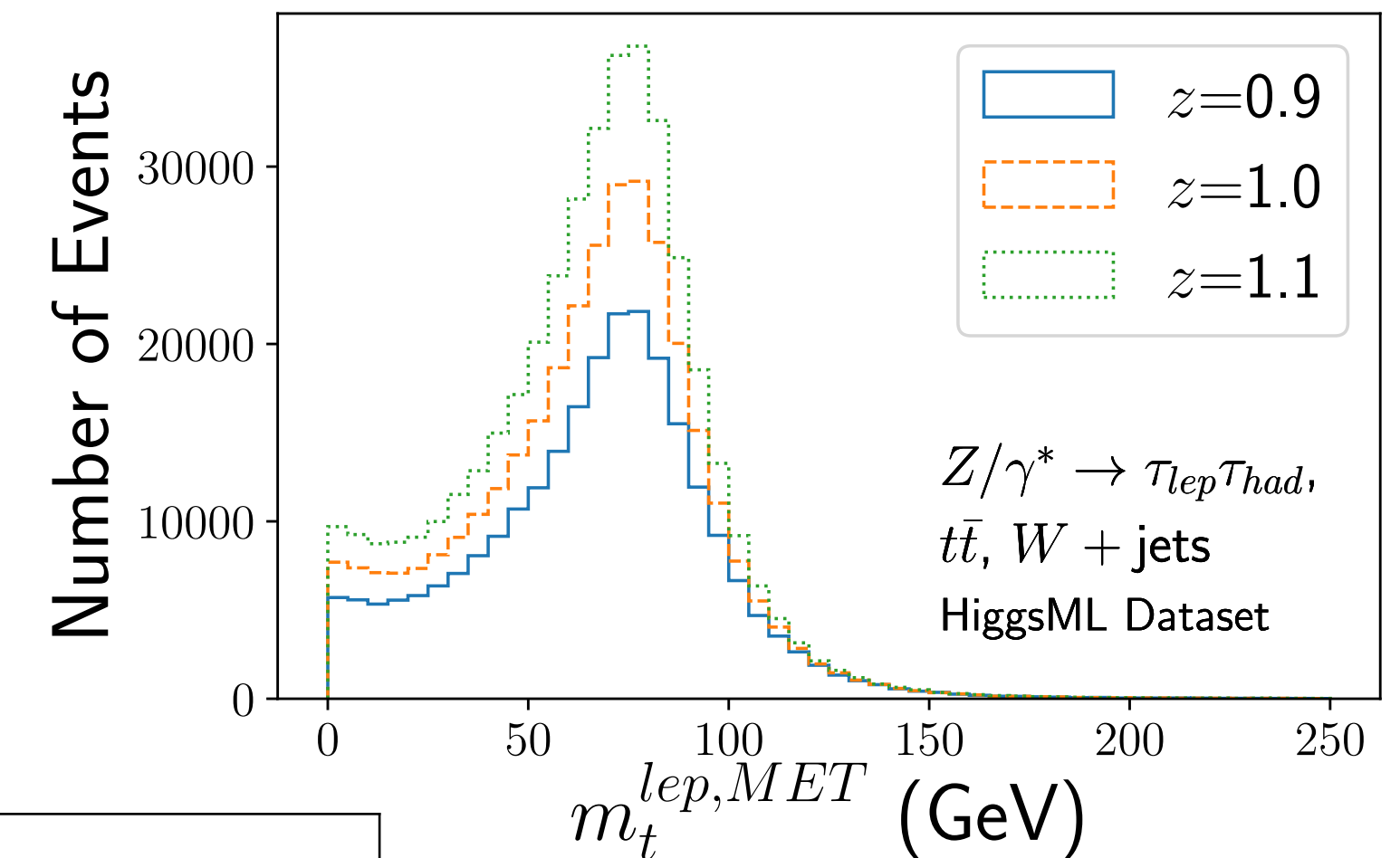
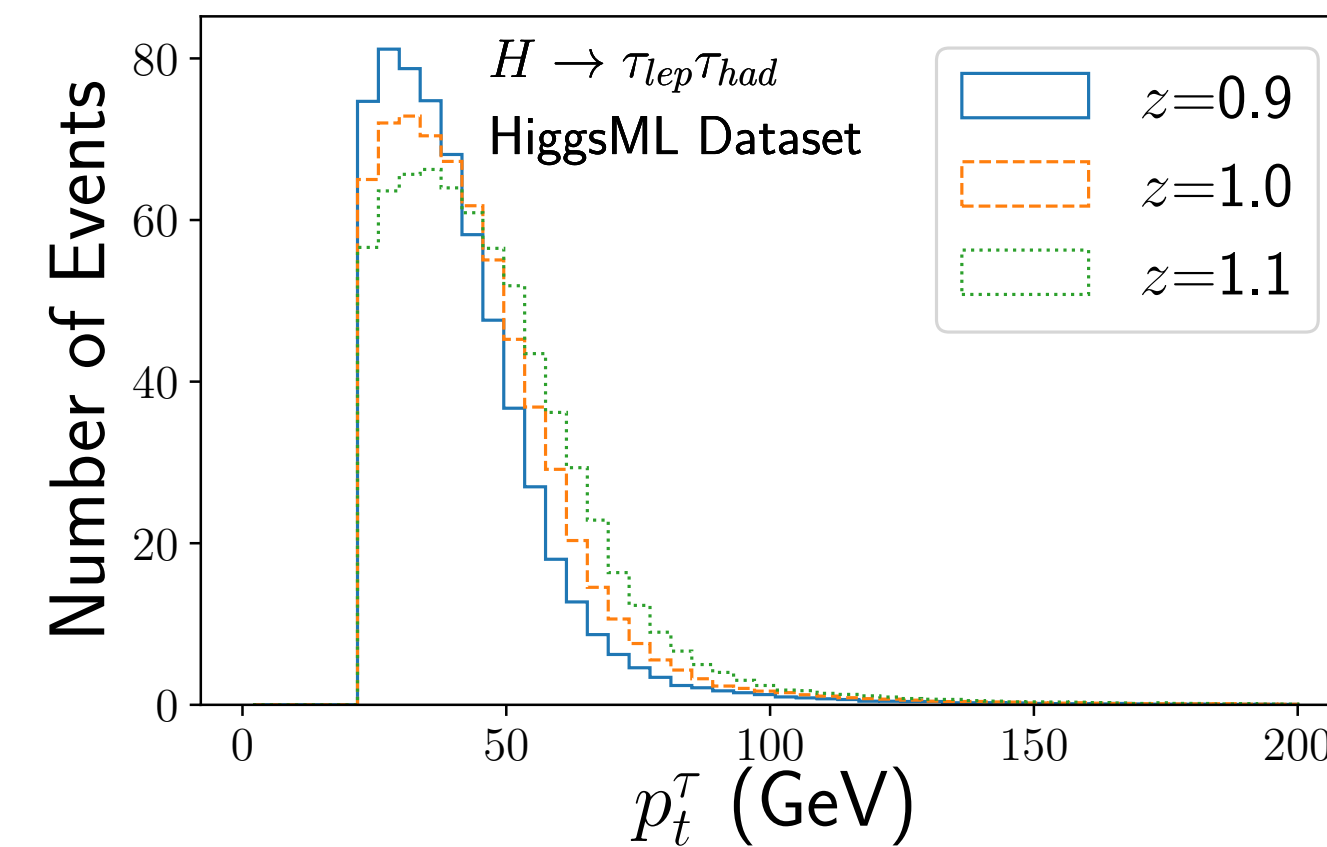
$z_T \rightarrow$ True z



Physics Data: HiggsML + Tau Energy Scale (TES) Uncertainty

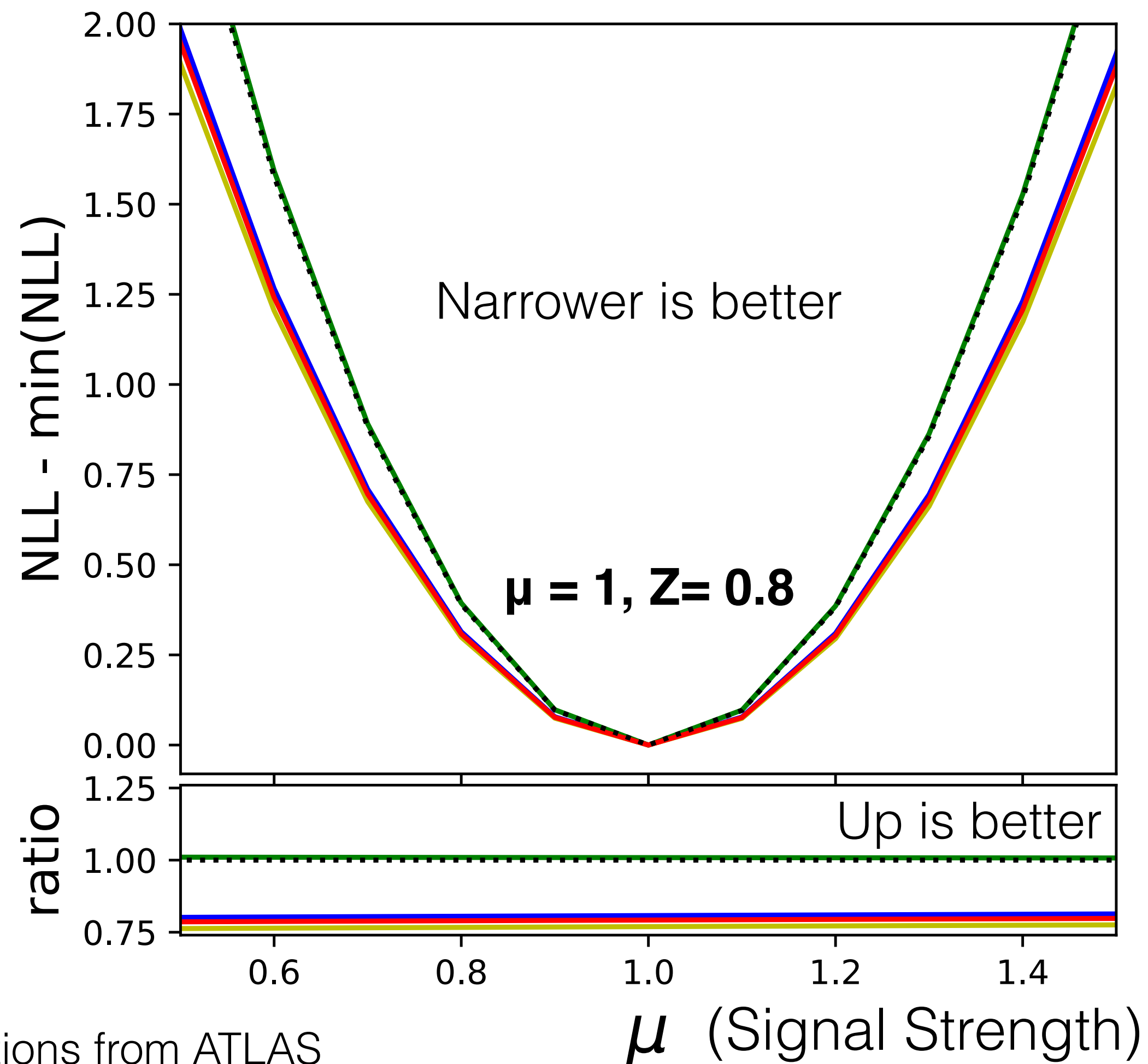


Parameter of Interest is Higgs signal strength μ , and
TES is the nuisance parameter Z



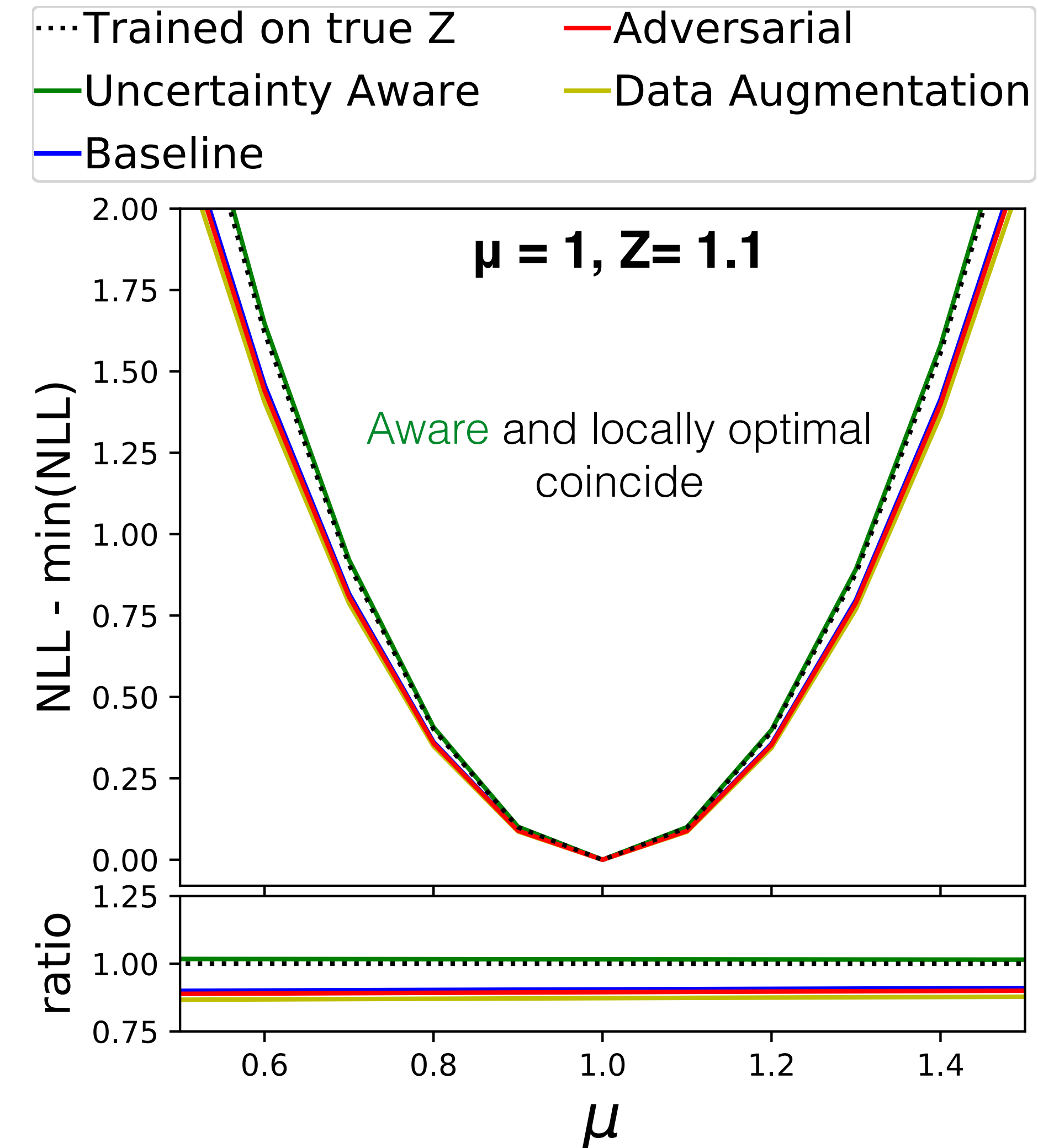
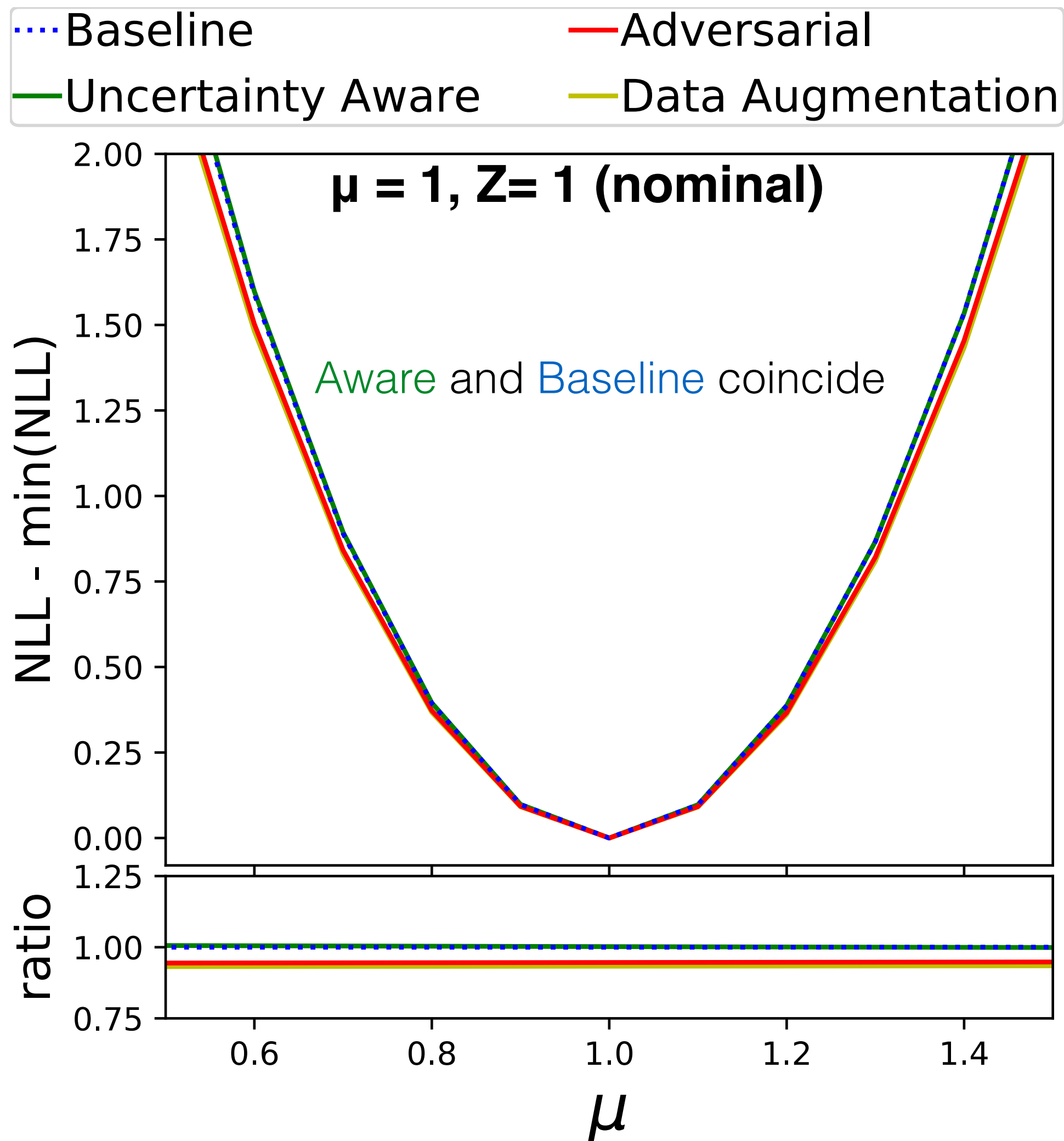
Physics Data: HiggsML + Tau Energy Scale (TES) Uncertainty

···· Trained on true Z — Adversarial
— Uncertainty Aware — Data Augmentation
— Baseline



Uncertainty-Aware coincides with classifier trained on true Z
⇒ Can't get much better than that!

Test performance for “observed” data at nominal and above nominal Z



In every case the **Aware Classifier** is as good as the optimal one, no other technique matches its performance everywhere

Idea fascinating also to ML researchers !

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- ML researchers assume i.i.d
- This technique exploits correlations between samples – a different paradigm
- Interesting applications outside of physics

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[arXiv:2007.02931](https://arxiv.org/abs/2007.02931)

Idea fascinating also to ML researchers !

- ML researchers assume i.i.d
- This technique exploits correlations between samples – a different paradigm
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For my handwriting this is '2', for yours it might be 'a'
ARM: Adapt to the individual + classify



ERM → 2
ARM → a

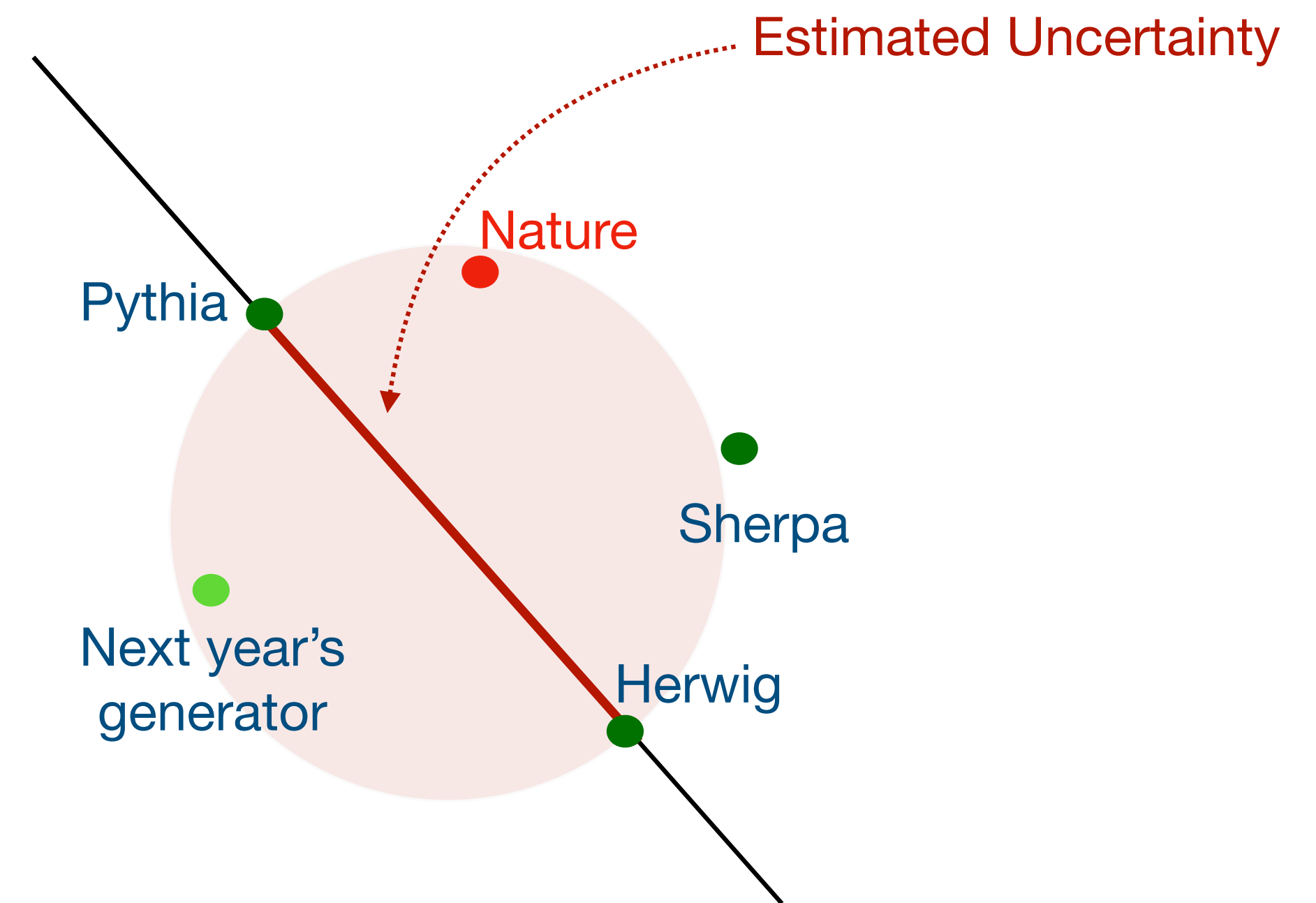
[arXiv:2007.02931](https://arxiv.org/abs/2007.02931)

Theory Uncertainties

What are they ?

Theory uncertainties often describe our lack of understanding / ability to calculate

No statistical origin for them (such as auxiliary measurement)



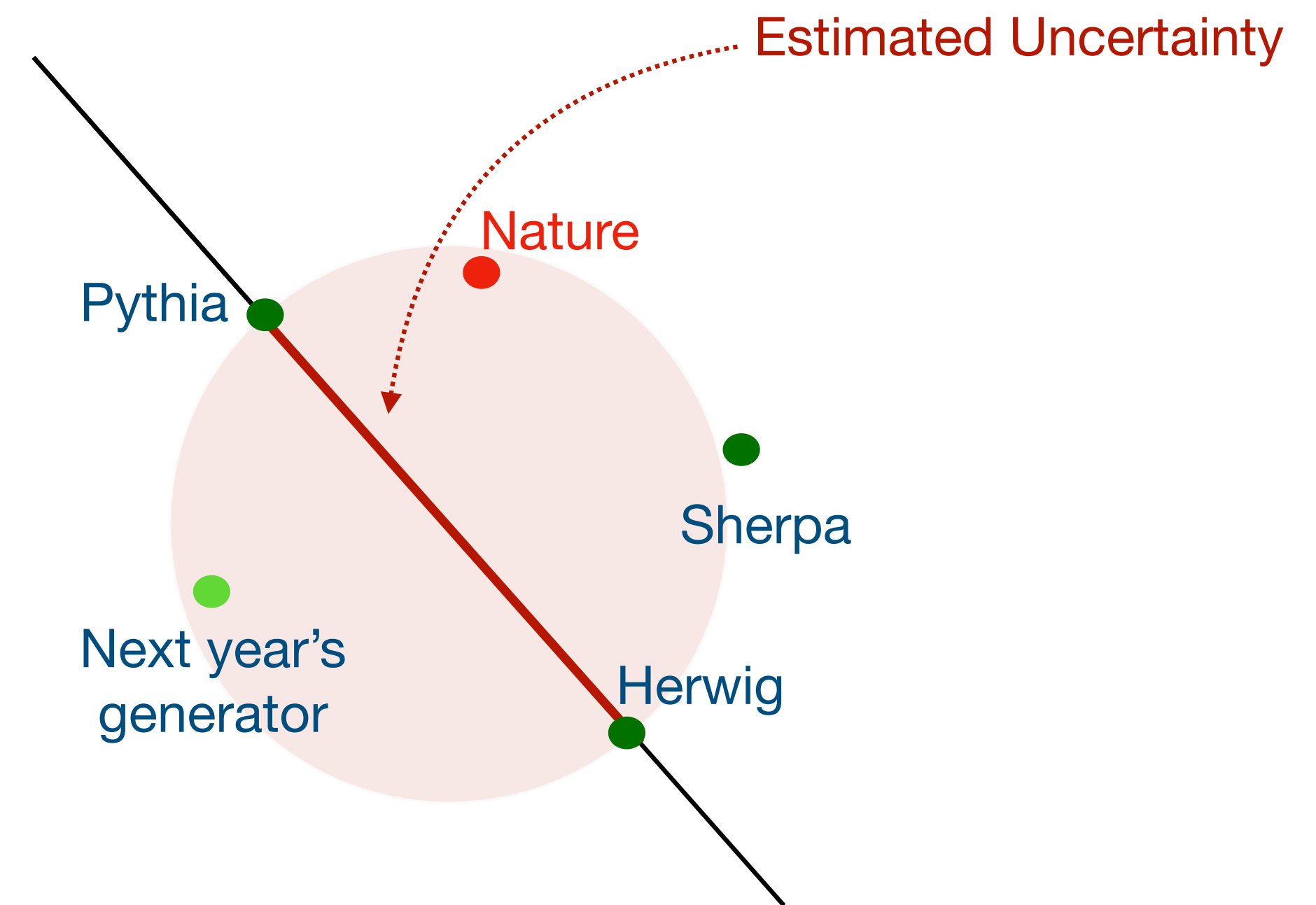
What are they ?

Theory uncertainties often describe our lack of understanding / ability to calculate

No statistical origin for them (such as auxiliary measurement)

Eg. Hadronisation:

- Few **different packages** to simulate it
- None are correct!
- Use difference in performance of your data analysis algorithm on **Pythia** simulator vs **Herwig** simulator **ad-hoc estimate of uncertainty**



Goodhart's Law

When a measure becomes a target, it ceases to be a good measure

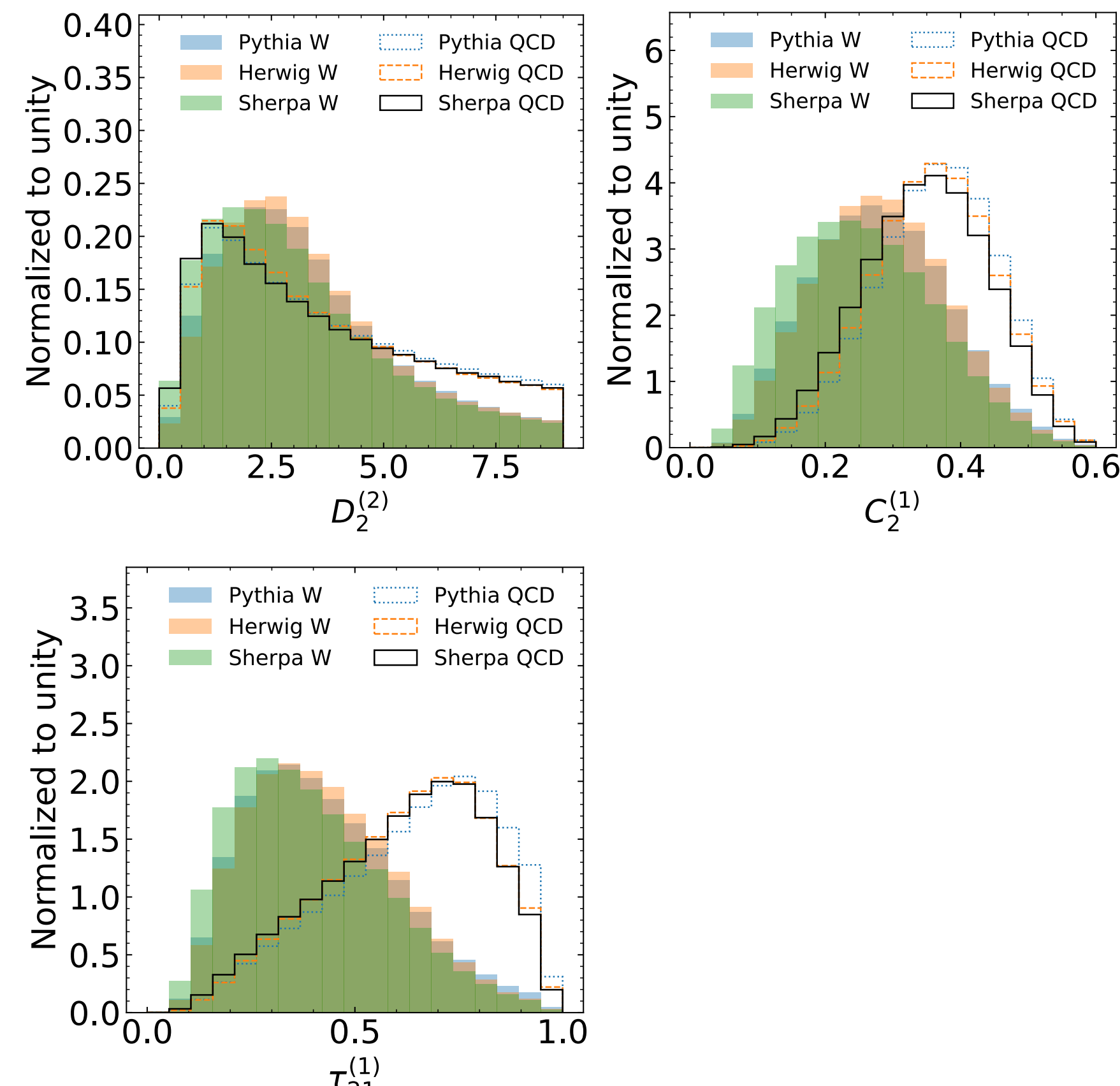
=> Dangerous to optimise proxy metrics of uncertainty

Case Study 1: Two-point uncertainty (fragmentation modelling)

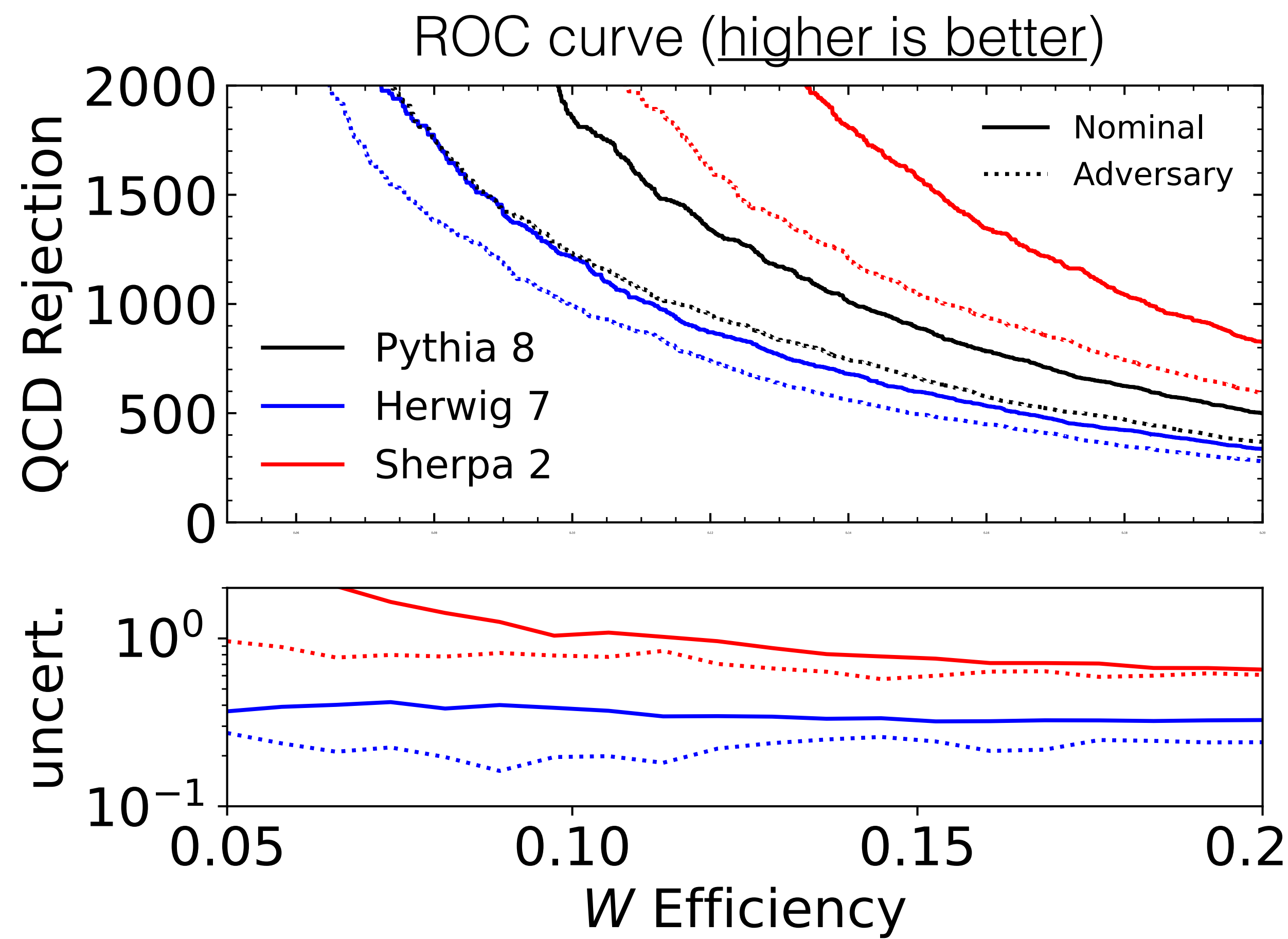
Goal: W jets vs QCD jets

Decorrelation: Reduce difference in performance on **Herwig** vs Pythia

Cross-check: Test uncertainty estimate from {**Herwig** vs Pythia} using **Sherpa**



Case Study 1: Two-point uncertainty - Result

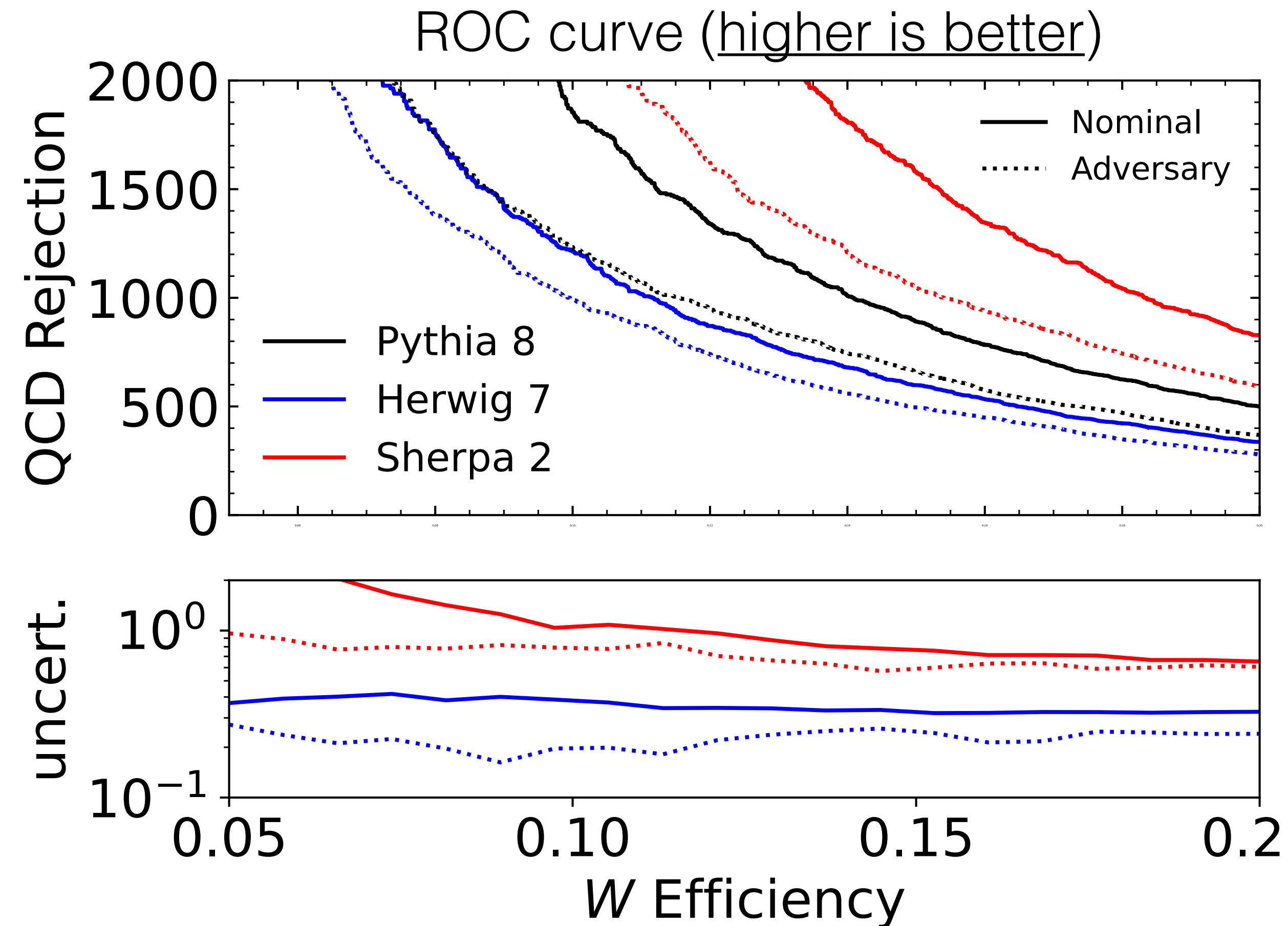


Case Study 1: Two-point uncertainty - Result

Adversary successfully sacrifices separation power in order to reduce difference in performance between **Herwig** and Pythia

Cross-check with **Sherpa** reveals uncertainty severely underestimated by usual **Herwig** vs Pythia comparison

In an typical LHC analysis, a cross-check with third generator rarely performed, similar to prior work suggesting decorrelation for theory uncertainties

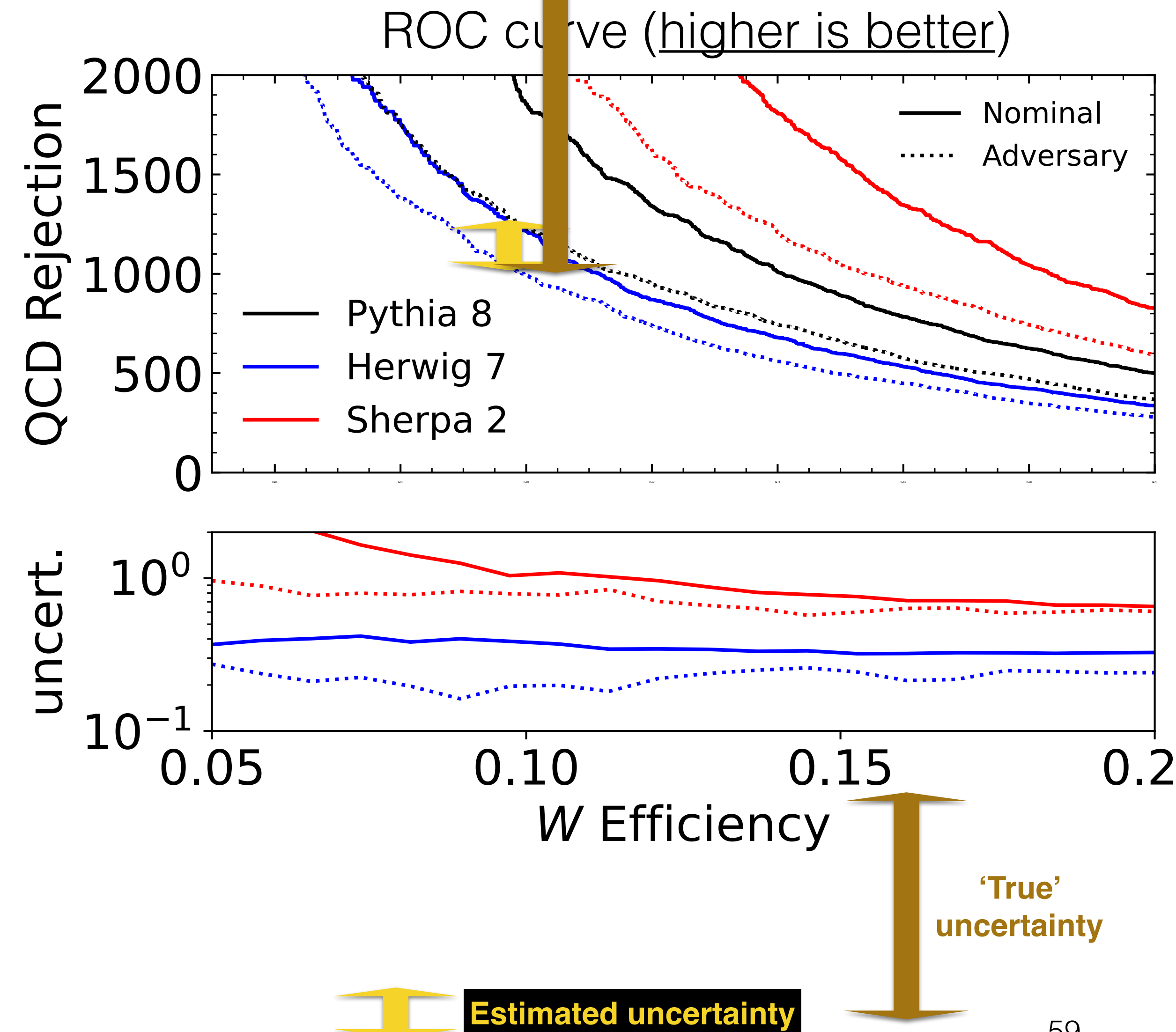


Case Study 1: Two-point uncertainty - Result

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Case Study 2: Higher-order corrections

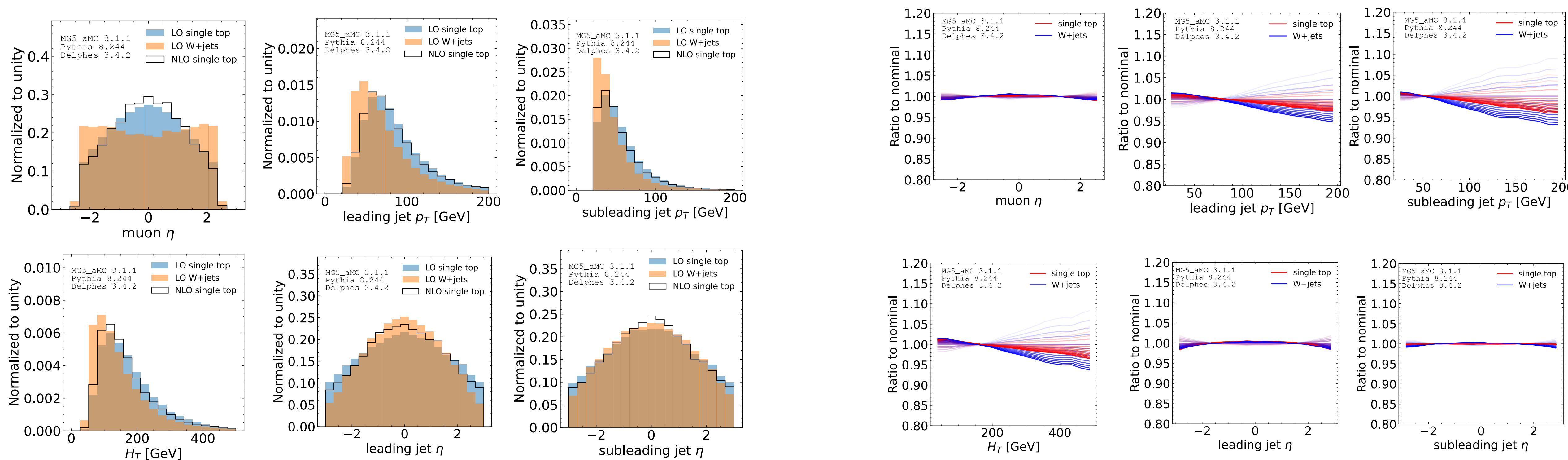
- We can't calculate QFT to infinite order
- Artefact of truncation of series: Varying certain unphysical scales changes predictions
- Uncertainty quantification: Vary scales (renormalization scale, factorisation scale) between $1/2$ to 2 in MC, see change in prediction

Scale uncertainty – Problem Setup

Goal: Single top vs W+Jets

Decorrelation: Reduce difference in performance on scale variations at LO

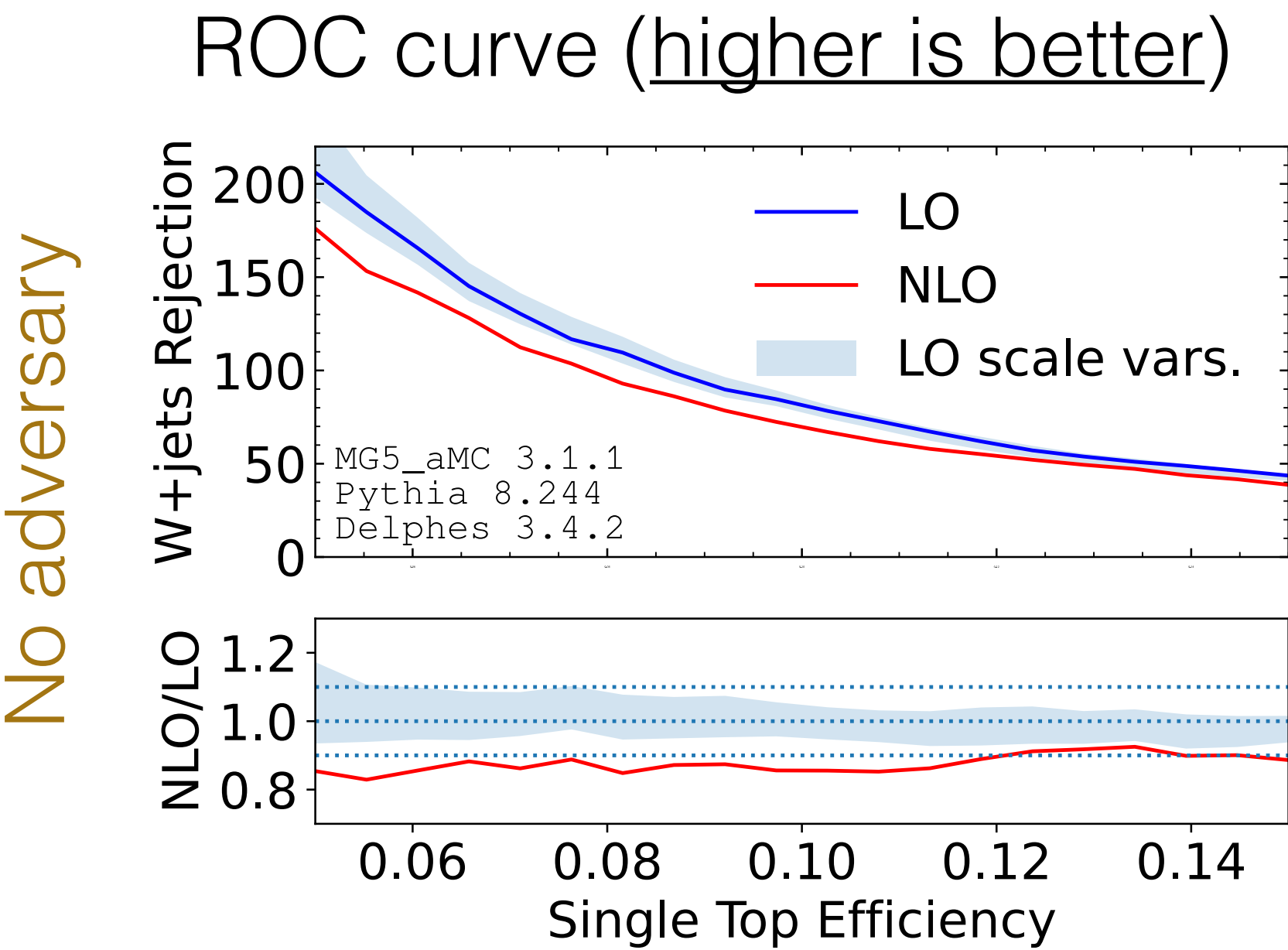
Cross-check: Test uncertainty estimate from {scale variations at LO} using NLO



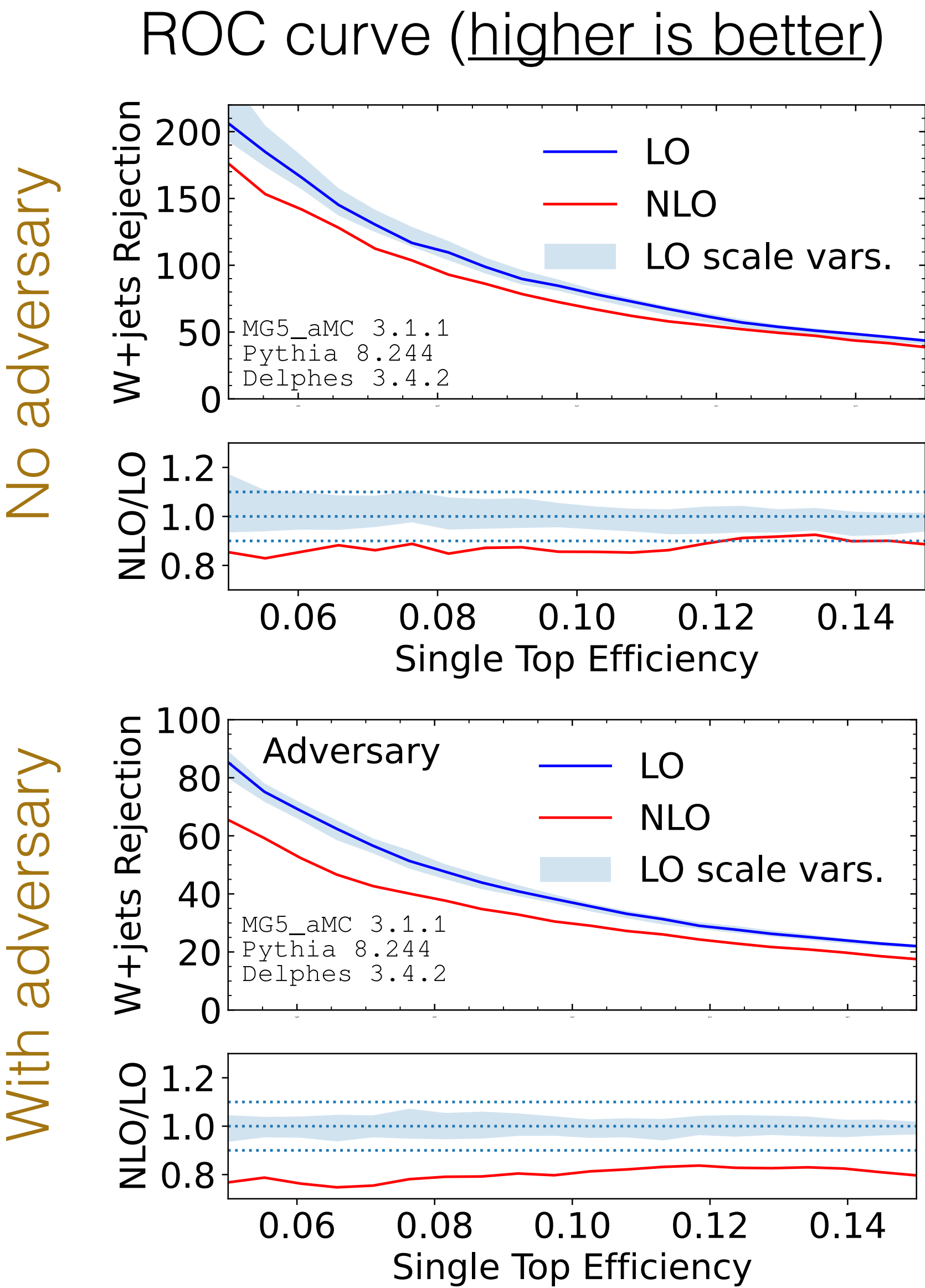
NLO vs LO

Factorisation scale variations going from 1/2 to 2

Case Study 2: Continuous uncertainty - Result



Case Study 2: Continuous uncertainty - Result



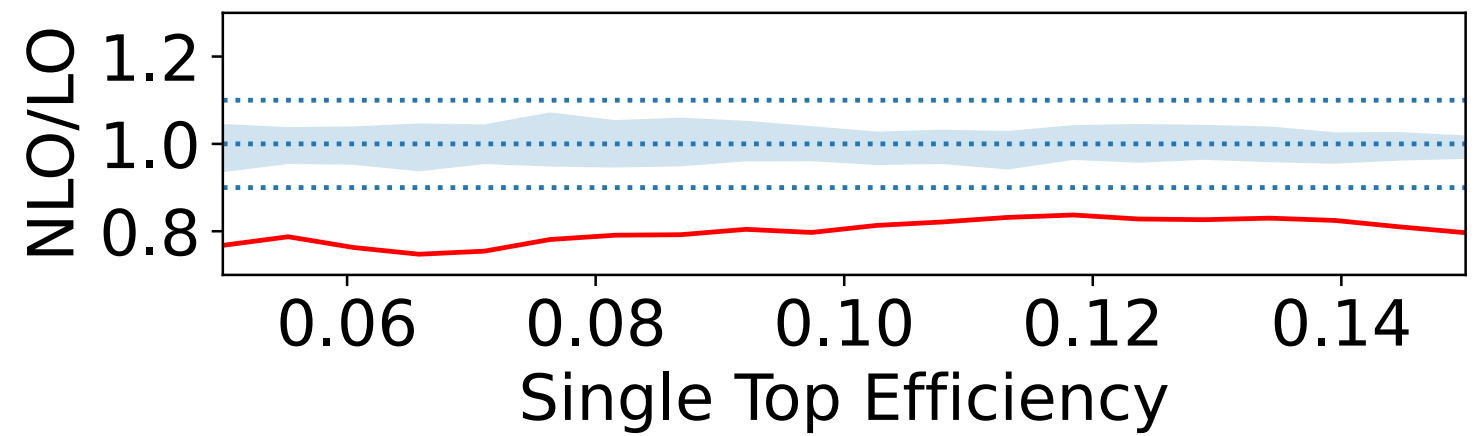
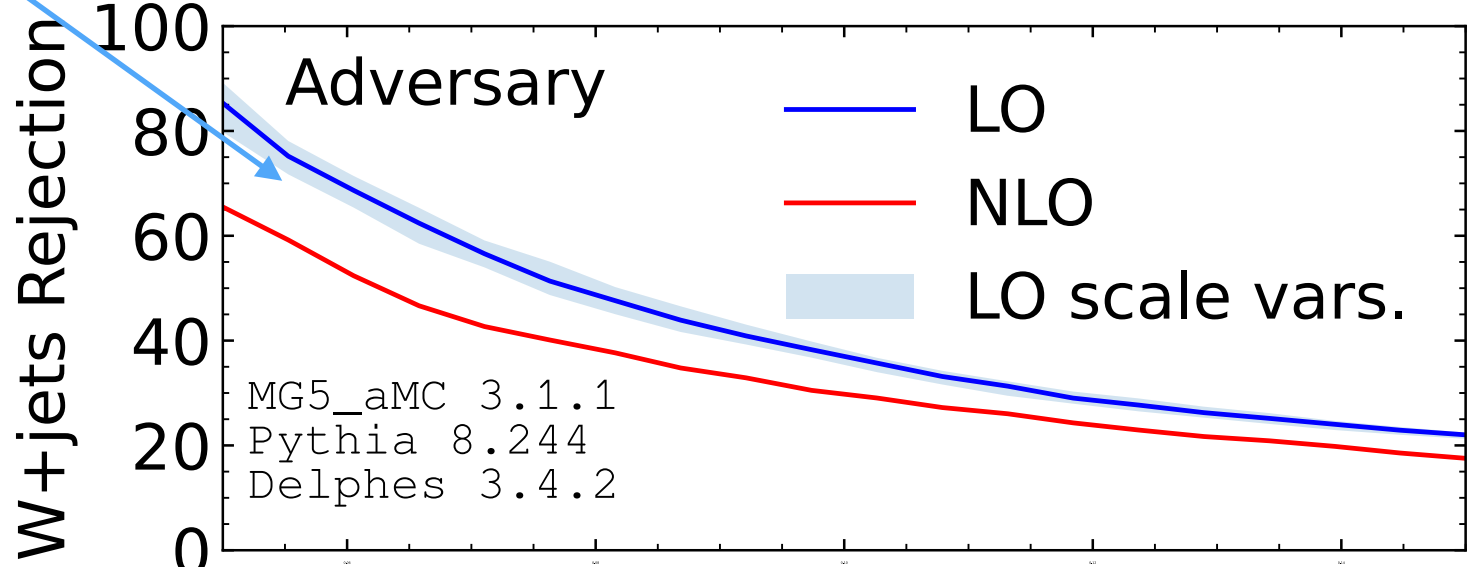
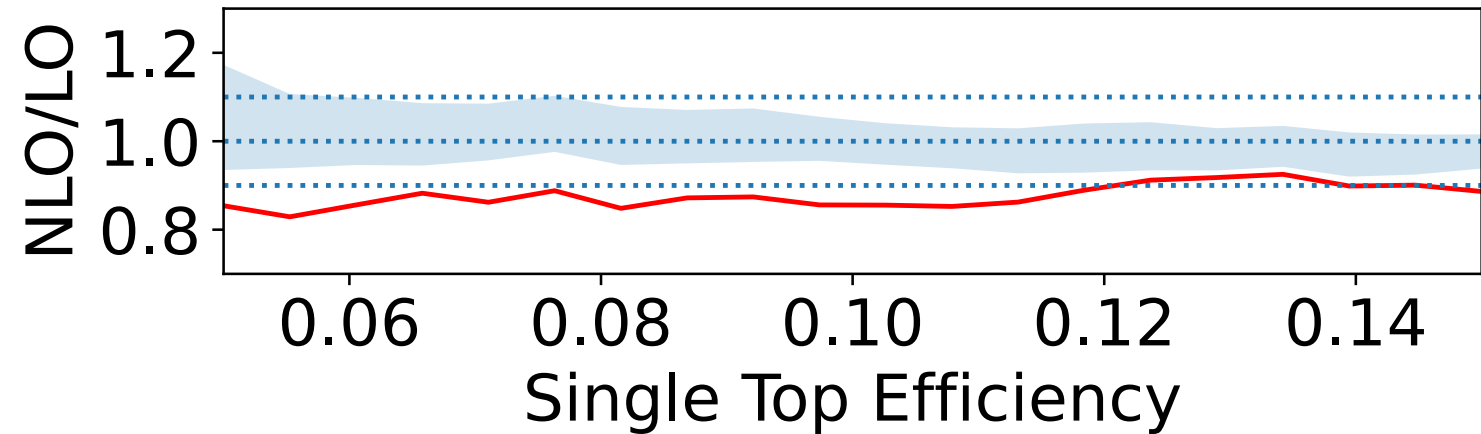
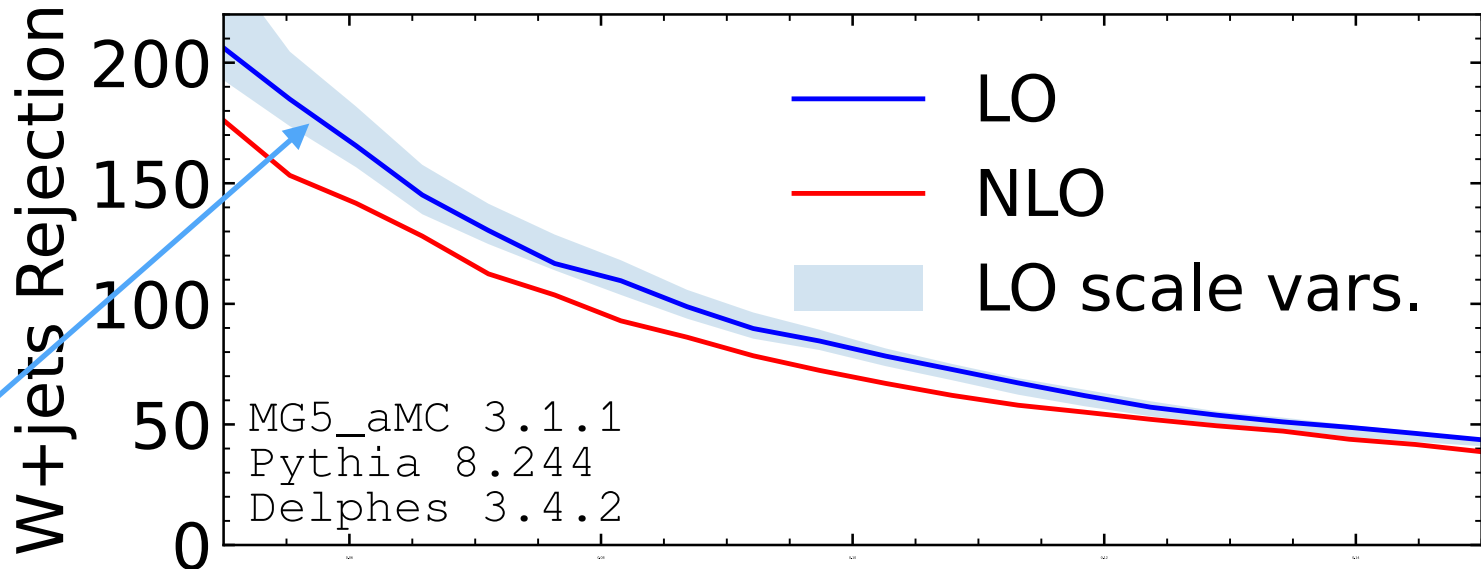
Case Study 2: Continuous uncertainty - Result

Decorrelation:
Only the **error bars**
shrink, not the actual
distance to **NLO**

No adversary

With adversary

ROC curve (higher is better)



Case Study 2: Continuous uncertainty - Result

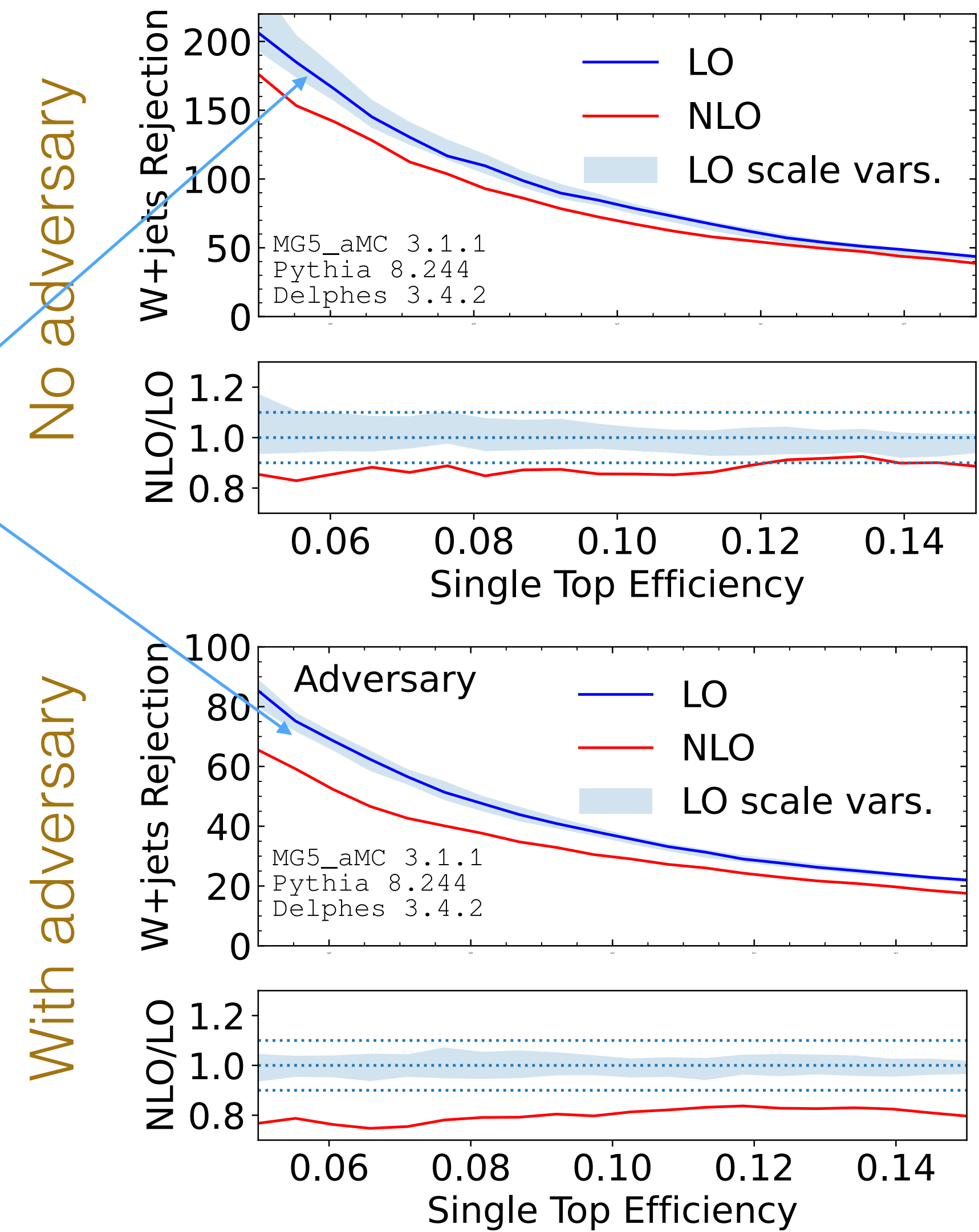
Adversary successfully **sacrifices**
separation power in order to reduce
difference in performance between **scale**
variations

Cross-check with **NLO** reveals **uncertainty**
severely underestimated by decorrelation
approach

In an typical LHC analysis, a cross-check
with higher-order usually unavailable

Decorrelation:
Only the **error bars**
shrink, not the actual
distance to **NLO**

ROC curve (higher is better)



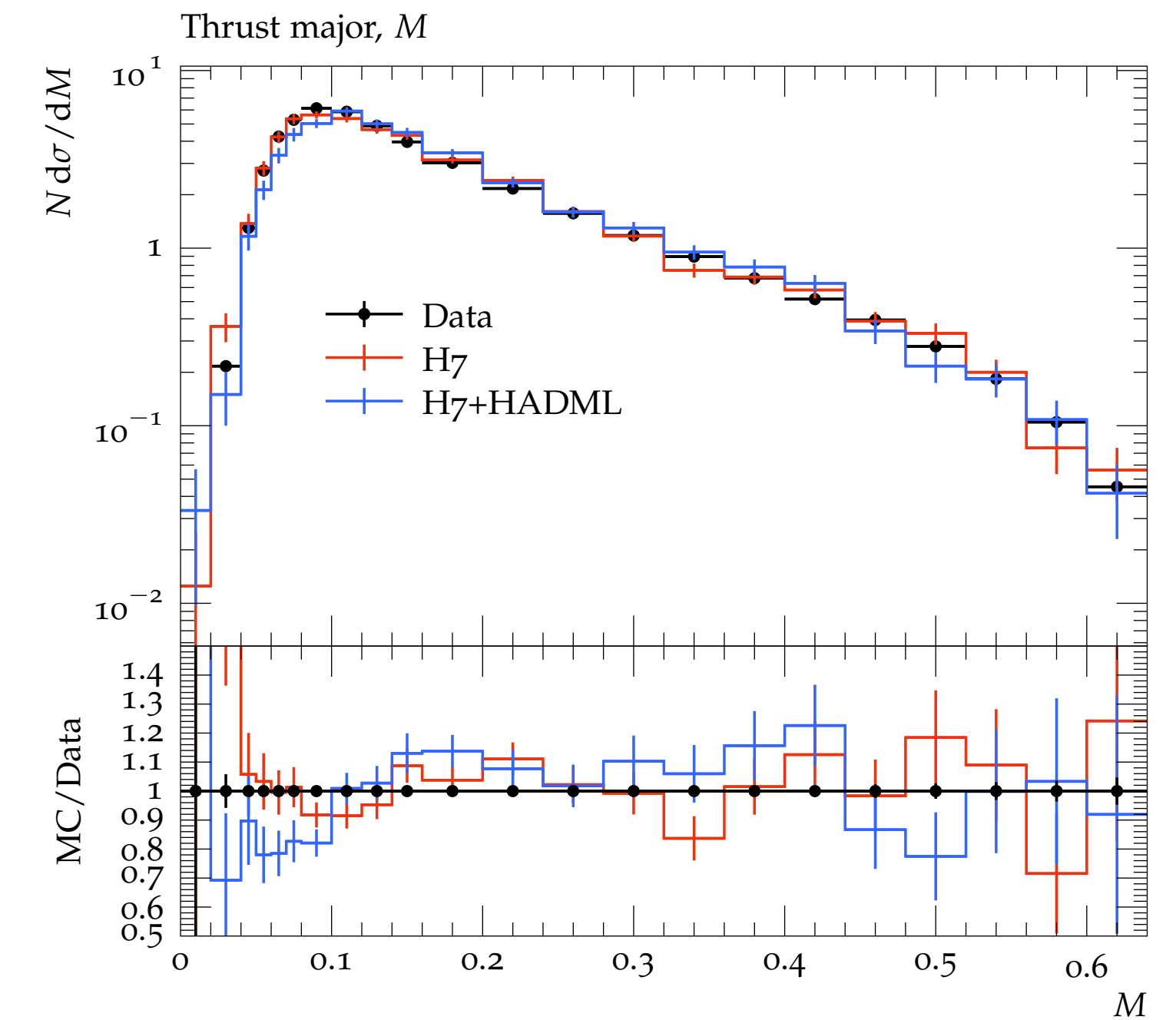
Universe is a perfect simulator

[PRD.106.096020](#): **Aishik Ghosh**, Xiangyang Ju, Benjamin Nachman, and Andrzej Siodmok

Universe is a perfect simulator

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Bypass theory, can we learn hadronization directly from data ?



Overconstraining NP

From [W. Verkerke](#):

Our modelling of NPs might be over-simplified

- If you assume one NP – chances are that your physics Likelihood will exploit this oversimplified JES model to overconstrain JES for high p_T jets!

