

$$\mathrm{Im}\,\Pi^{\mathrm{had}} = \frac{\alpha}{3} R(s) + \mathcal{O}(\alpha^2),$$