# Final Discussion

## Thank you for your participation...



...also to all our remote participants!

### Timeline for the White Paper

- Earliest possible release date for Fermilab g-2 measurement:
   15-20 December 2019
- Post the WP on arXiv by:1 Dec. 2019
- Deadline for finalizing individual WP chapters:

#### 1 Nov 2019

At this date the Overleaf chapters will be frozen.

Editorial board will release complete WP to authors for feedback on:
 15 Nov. 2019

will need to receive feedback from authors within a week

Experimental and theoretical inputs used in WP must be published by:
 15 Oct 2019

To make sure to be included in WP discussion, a paper to be posted in arXiv by same date.

## Note: The WP will be posted on arXiv in December, even if the Fermilab experiment's release date is delayed.

### White Paper Outline

- Executive Summary
- Introduction
- Chapter 1: data-driven HVP
- ♀ Chapter 2: lattice HVP
- ♀ Chapter 3: data-driven HLbL
- Chapter 4: lattice HLbL
- - T. Aoyama, T. Kinoshita, M. Nio
  - D. Stöckinger, H. Stöckinger-Kim
- Summary, Conclusions, and Outlook

### White Paper Structure

#### *Authorship*:

Contributors: open to participants in any of the workshops, and collaborators in group efforts, and of course everyone who is contributing to the writing of sections in the WP.

- Chapter authorship will be highlighted and described either in the introduction of the WP or in each WP chapter.
- Secutive Summary (about 1-2 pages)
- Introduction will follow and describe the process that lead to the WP.
- WP will be published in a journal. Possibilities include: PRD, EPJC, Phys. Reports,
- Expect follow-up WPs after the publication of the first one, with timelines to be coordinated with the experiments.

### Future Workshops

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in Japan, to be organized by Tsutomu Mibe and Shoji Hashimoto. probably at KEK, likely in first half of June, exact dates to be determined. (possible alternative dates early October)

#### **2021**:

Vera Gülpers, Antonin Portelli, and Thomas Teubner will apply to host workshop (with Vera as chair) at the Higgs Centre in Edinburgh, dates to be determined.

We hope to finalize and announce the dates for both workshops soon (before the end of 2019).

### **Dispersive HVP**

Status of the dispersive HVP WP chapter

- Presentations on status and recent developments of the experimental input data and the theoretical compilations, analyticity constraint, MC, MUonE
- Two intense and constructive discussion sessions (thanks to Dave for chairing the sessions, and to Martin for the comparison efforts):
- Ieading to agreement on procedures to overcome open questions and issues crucial for our WP chapter:
  - i. How can we achieve the major charge of the Theory Initiative, to come up with ``one conservative prediction"

➡ see extra slide by Bogdan: detailed procedure based on general philosophy (as brought up e.g. by Dave), to achieve a ``merging" of the two main data-driven predictions

no numbers yet, but simple enough to work on the short time-scale of WP v1, work will start immediately...

ii. Agreement on how to deal with the description of how different groups incorporate analyticity/unitarity constraints in the most important 2pi channel.

### **Dispersive HVP**

#### Proposal: conservative merging of model-independent HVP combination results

• Basic requirements for the *merging* procedure:

- *Conservative* (see tensions between experimental data and differences between combinations based on same datasets )

- Accounting for correlations between different channels (understood meaning of systematic uncertainties and identified 15 common ones, DHMZ since arXiv:1010.4180) Yields unavoidable increase of total uncertainty  $693.9 \pm 1.0 \pm 3.4 \pm 1.6 \pm 0.1_{\psi} \pm 0.7_{QCD}$ 

- Proposed *merging* procedure:
- <u>Central value</u>: simple average of the <u>DHMZ</u> and <u>KNT</u> sums of channels (the <u>DHMZ</u> and <u>KNT</u> central values are, by chance, very similar)

- Experimental uncertainties: in each channel/mass range use max(DHMZ, KNT) and see by how much to increase the corresponding DHMZ uncertainty (sq. difference); enhance the DHMZ *sum of channels (with correlations)* by these amounts (sq. sum)

Use |<u>DHMZ</u>(ch.)-<u>KNT</u>(ch.)| / 2 as extra systematic in each channel; independent between channels (sign of algebraic difference fluctuates for various channels)
o) ππ BABAR/KLOE systematic: max(DHMZ B./K. syst., |<u>DHMZ</u>(ππ)-<u>KNT</u>(ππ)| / 2) (stay conservative, but avoid double-counting the effect of this B./K. tension)
o) π<sup>+</sup>π<sup>-</sup>π<sup>0</sup>: do not include this systematic (difference understood: 1<sup>st</sup>/2<sup>nd</sup> order interp.)

### Lattice HVP WP ToC

- I. Introduction
  - A. The hadronic vacuum polarization
  - B. Calculating and integrating  $\Pi(q^2)$  to obtain  $a_{\mu}$
  - C.Time moments
  - D. Coordinate-space representation
  - E. Common issues
- II. Strategies
  - A. Connected light-quark contribution  $a_u^{\text{HLO}}(ud)$ 
    - 1. Statistical errors
    - 2. Finite volume effects and longdistance two-pion contributions
    - 3. Discretization and scale setting
    - 4. Chiral extrapolation/interpolation
  - B. Connected strange and charm contributions  $a_{\mu}^{\text{HLO}}(s)$ ,  $a_{\mu}^{\text{HLO}}(c)$ ,  $a_{\mu}^{\text{HLO}}(b)$
  - C. Disconnected term  $[a_{\mu}^{HLO} discussion]$
  - D. Strong and em IB contributions  $\delta a_{\mu}^{\mathrm{HLO}}$

- III. Comparisons
  - A. Comparison of total LO-HVP contribution
  - B. Flavor-by-flavor comparison
  - C. Toward lattice QCD consensus and permillevel precision

#### IV. Connections

- A. HVP from lattice QCD and the MUonE experiment
- B. HVP from tau decays
- C. Hadronic corrections to the running of  $\alpha$  and  $\sin^2\theta_W$
- V. Summary and conclusions
  - A. Current status
    - Combination of lattice HVP results
  - B. Expected progress in the next few years

### Data-driven HLbL

#### Summary of HLbL (as of May '19, very preliminary!)

Contributions to	<b>10</b> <sup>11</sup>	$\cdot  \pmb{a}_{\mu}^{ ext{HLbL}}$
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Pseudoscalar poles	$=93.8^{+4.0}_{-3.6}$
▶ pion box (kaon box $\sim -0.5$ )	= -15.9(2)
S-wave $\pi\pi$ rescattering	= -8(1)
• scalars and tensors with $M_R > 1$ GeV	$\sim -2(3)$
axial vectors	$\sim$ 8(3)
short-distance contribution	$\sim 10(10)$
entral value:	$85 \pm XX$
Incertainties added in quadrature:	<i>XX</i> = 12
Incertainties added linearly:	<i>XX</i> = 21

### Lattice HLbL

#### Whitepaper Outline

- 1. Introduction
- 2. HLbL on the Lattice
  - Approach to HLbL by RBC/UKQCD
  - Approach to HLbL by Mainz
- 3. Test case: HLbL scattering in QED
- 4. Pion-pole contribution
- 5. Cross-checks between RBC/UKQCD and Mainz
- 6. Results for physical pion mass
- 7. Additional cross-check: forward scattering amplitudes
- 8. Expected progress in next years
- 9. Summary of current knowledge from lattice