## Sensitivity to Heavy Neutral Leptons With SAND detector at DUNE-ND

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## BEYOND STANDARD MODEL PHYSICS

* Why going beyond Standard Model?
- Observed Matter anti-matter asymmetry (BAU) requires BSM
- Dark matter (Bullet cluster, Galaxy rotation, GR lensing)
- Neutrino oscillation, CPV and neutrino masses
- SeeSaw models (low-SeeSaw, ...)



Muon neutrino oscillations, short range






* Pheno-Sensitivity


## . 6 years exposure, $1.1 \times 10^{21} \mathrm{NPOT} / 1 \mathrm{yr}$

- Small mixing between $\mathbf{N}_{2}$ and $\mathbf{N}_{3}$ due to BAU lower bound
- Detector's Geometry has been modified to fit with SAND transversally
- $\mathbf{D}_{\mathbf{s}}$ channel is dominant in this range. All $\mathbf{D}_{\mathbf{s}}$ channels has been covered
- Regarding the model parameters and simulation tools, the estimated Pheno-sensitivity is in the ballpark of the previous studies in the $\mathrm{D}_{\mathrm{s}}$ dominant region.
* Steps to Reconstruction

| Particle | Channel |
| :---: | :--- |
|  | $\rightarrow e N_{2,3}$ |
| $D_{s}$ | $\rightarrow \mu N_{2,3}$ |
|  | $\rightarrow \tau \nu_{\tau}$ |
|  | $\rightarrow \nu_{\tau} \mu N_{2,3}$ |
| $\tau$ | $\rightarrow \nu_{\mu} \mu N_{2,3}$ |
|  | $\rightarrow \rho N_{2,3}$ |

$$
\begin{array}{|cc|}
\hline \hline \text { Particle } & \text { Channel } \\
\hline N_{2,3} & \rightarrow \pi^{+} \mu^{-} \\
& \rightarrow \pi^{-} \mu^{+} \\
\hline
\end{array}
$$

- Mad-Dump output file is converted to a Genie-like output including a RooTracker tree
- Detector response: Running Edepsim
- Digitization
- Reconstruction: Existing Reco didn’t work for this particular event: Motivation for implementing a customized Kalman Filter



## DUNE Near Detector, SAND

## *SAND (System for on-Axis Neutrino Detection)

## - Detector tracker design inside KLOE magnet

- Tracker: ECAL + STT + Grain (LAr meniscus )
- Simulation tools: GEANT4 and FLUKA event generators





## Reconstruction, Kalman Filter

- Kalman Filter is an algorithm that determines the trajectory of a state vector of a dynamical system from a set of measurements taken at different times, taking into account gaussian fluctuations
- It proceeds progressively from one measurement to the next, improving the knowledge about the trajectory with each new measurement.
- There are three steps for Kalman Filter
- Predicting: an estimate is made for the next measurement from current knowledge of the state vector
- Filtering/Updating: Kalman Filter in Theory updates the state vector using the measurement
- Smoothing: recursive operation, step by step in the direction opposite to that of filter

Residuals

Predict

$$
\begin{array}{ll}
\tilde{x}_{k}^{k-1}=F_{k} \tilde{x}_{k-1} & \tilde{r}_{k}^{k-1}=m_{k}-H_{k} \tilde{x}_{k-1}^{k} \\
\tilde{C}_{k}^{k-1}=F_{k} C_{k-1} F_{k}^{T}+Q_{k} \quad(=\mathrm{MCS}) & \tilde{R}_{k}^{k-1}=V_{k}+H_{k} C_{k-1}^{k} H_{k}^{T}
\end{array}
$$

Update

$$
\begin{aligned}
& K_{k}=C_{k-1}^{k} H^{T}\left(V_{k}+H_{k} C_{k-1}^{k} H_{k}^{T}\right)^{-1} \\
& \tilde{x}_{k}=\tilde{x}_{k}^{k-1}+K_{k}\left(m_{k}-H_{k} \tilde{x}_{k-1}^{k}\right) \\
& C_{k}=\left(1-K_{k} H_{k}\right) C_{k-1}^{k}
\end{aligned}
$$

$$
\begin{gathered}
r_{k}=\left(1-K_{k} H_{k}\right) r_{k-1}^{k} \\
R_{k}=\left(1-K_{k} H_{k}\right) V_{k} \\
\chi_{k, F}^{2}=r_{k}^{T} R_{k}^{-1} r_{k}
\end{gathered}
$$

$$
\begin{aligned}
& X=\left(x, y, t_{x}, t_{y}, \frac{q}{P_{T}}\right) \\
& \frac{q}{P_{T}}\left[\frac{e}{G e V}\right]=\frac{1}{R \times 0.3 \times B}
\end{aligned}
$$



Kalman Filter, Toy MC
$B \bigcirc$




* Kalman Filter Procedure:
* Toy MC
- Toy MC starting with one single track, moved to multiple tracks, noise hits added
- Kalman Direction: Forward/Backward
- Measurements:
- Assuming uniform B field, 0.6 T, constant $\mathbf{\delta z}$ for the planes (ideal, zero thickness)
- RN generation with uniform distribution for initial position and initial momentum
- For each plane $\mathbf{X}, \mathbf{Y}$ according to analytic extrapolation, with $95 \%$ efficiency
- Smearing 0.1 mm for $\mathbf{X}$ and $\mathbf{Y}$
- Sequentially adding new information on each hits to get an optimal track
- Strategy:
- Prediction and Update (Filtering, Residual , $\mathrm{X}^{2}$ ): forward and backward, Smoothing
* Customized Kalman Filter General Assumption
- Prediction step is an analytical extrapolation
- Discreteness in z direction




## Kalman Filter, from Toy MC to Geant4 MC



Smoothing
Forward

* Preparation for Geant4 MC
- Mad-Dump: Genie-like output
- EdepSim (nd_hall_kloe_sttonly.gdml): Edep-Sim output
- Digitization (200 $\mu \mathrm{m}$ smearing): wire position added (to meet with Kalman Filter discrete process that goes in steps, e.g. zero uncertainty on z coordinate of the plane)
- X,Y hits are combined into an extrapolated measurement at the $z$ of the wire of the upstream plane of the module
* Kalman Filter Geant4 MC
- HNL sample 1 GeV mass $, D_{s} \rightarrow N_{2} \mu, \mathbf{U}_{\mu}: \mathbf{U}_{\mathbf{e}}: \mathbf{U}_{\tau} \sim \mathbf{1}: \mathbf{1 6}: \mathbf{3} . \mathbf{8}$
- Forward/Backward
- Customized Kalman Filter Assumptions
- Straw modules: XXYY or XXYYXX (present in this geometry)
- Uniform B field, 0.6 T
- Processing hits:

Separate measurement for $X$ and $Y$ are recombined to ( $X, Y$ ) referring to the $Z$ of the first straw layer of each module



Kalman Filter, Toy MC, Event Display




MC Truth Matching


* Dominant contributions to Invariant Mass (besides Momentum)
- Quality of the Vertex: < 1mm (most of statistics)
- Quality of the Reco final product angle: The final product angle resolution is around 30 [mrad] up to $25[\mathrm{GeV}]$
- MC truth Matching angle (preliminary):

Significant tail on the single particle angle resolution (currently cut by MC truth matching $\sim 20$ [mrad])



## Kalman Filter, GEANT4 MC

## * Features

- Backward Kalman direction implemented, in this case backward is more efficient: the initial hit is found easier and more precise (MCS not messing with the hits much)
- Multiple scattering has been added (changing the resolution by $0.1 \%$ )
- For better precision, external helical fit has been used (hits are coming from Kalman Filter, the used fit is the external one)


## * Items to have an eye on:

- Invariant Mass resolution
- Momentum resolution
- Kalman Filter parameters (Pull plots)
- Goodness of the fit ( $\mathrm{X}^{2}$ )


## * Procedure:

- Kalman Filter
- Forward/Backward Kalman and smoothing.
- External helical fit.
- Reco tracks:
A. Choosing either forward or backward as Reco tracks.
B. Matching the forward/backward Reco tracks ( $\geq 50 \%$ shared hits), choosing the right combo for the final Reco track collection
- Matching the Reco and the True
- Momentum resolution, invariant mass resolution, Pull plots


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Angle between $\mu$ and $\pi$, Reco vs True

particle1 $=\mu$, particle2 $=\pi$


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## Event Reconstruction

## * Kalman Event Reconstruction

## - For/Backward tracks

- The more apart the hits the better the track recognition
- Statistically, the backward Kalman is more efficient


## - Merged tracks

- Enhancing the InvarMass resolution
- Recovering the events failed in either of For/Backward process
- Saving the better reconstructed event
- Any risk of double counting is eliminated by the selection
- Preliminary Efficiency estimate
- Accepted tracks:
- Extrapolation of the track up to the exiting point, count the \# plane
- Number of planes = 6
- Single track efficiency $\sim 80 \%$
- Event (pair of tracks with a vertex<1mm) efficiency $\sim 60 \%$


SNOWMASS 2022

Momentum Resolution, A


## Resolution Comparison

Momentum Resolution, B

## Samples

A. Monochromatic, simple single muon: fixed point, fixed direction (horizontal)
B. My event-like muons (Cylindrical distribution, comparable angle to my sample)
C. HNL sample




## * Events Kinematic

- Heavy Neutrino: High P, mostly with low $\boldsymbol{\theta}$ : back to back (XY) 2-body decay
* Vertex quality
- Vertex residual cut $<1 \mathrm{~mm}$

* Treatment for Ghosts
- Opposite charges and tracks in opposite quadrants XY
- a angle in XY between the ghosts or the tracks
- Theta is the angle of HNL with respect to the $z$-axis
- Alpha is geometrically correlated with theta
- A cut can be made for selecting the tracks from ghosts: " $\alpha>2.9, \theta<0.02$ "
- Removes most of the ghosts contaminating the signal
- The remnant ghosts:
- No effect on the resolution (very symmetric events)
- Compensated by a correction factor


## * Particle ID

- Not necessary at this stage: Swapping $\pi-\mu$ has negligible effect on Invariant mass resolution

Event Selection





## * Acceptance

- Reconstructible fraction of the total number of generated signal
- Pre-selection FidVol
- Cubic fiducial cut at generation step enveloping the detector
- Reconstructible: Long tracks
- The extrapolation of the tracks to the detector walls must include 6 or more traversed planes
- Accepted Events: A = Reconstructible/generated
* Efficiency
- Signal candidate: Track pair with opposite charge forming the invariant mass
- $\varepsilon 4=4$ track events/Accepted events
- $\varepsilon=$ Selected signal candidates/Accepted events
- $g=$ physical tracks/ghost tracks

| - $\varepsilon=$ Selected signal candidates/Accepted events <br> - $g=$ physical tracks/ghost tracks |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Acceptance and Efficiency |  |  |  |  |  |  |
| Channel | Mass[GeV/c ${ }^{2}$ ] | Total Number of Event | A\% | $\epsilon_{4} \%$ | $\epsilon \%$ | g\% |
|  | 1.7 | 168186 | 53 | 58 | 42 | 27 |
|  | 1.6 | 217118 | 55 | 57 | 43 | 26 |
|  | 1.5 | 212892 | 47 | 57 | 43 | 27 |
|  | 1.4 | 181300 | 62 | 35 | 26 | 26 |
|  | 1.3 | 197050 | $62^{\circ}$ | 57 | 43 | 28 |
|  | 1.2 | 186388 | 48 | 57 | 43 | 29 |
|  | 1.1 | 170394 | 55 | 56 | 41 | 30 |
| $D_{s} \rightarrow \mu N_{2}$ | 1.0 | 154438 | 62 | 56 | 42 | 31 |
|  | 0.9 | 136468 | 63 | 57 | 41 | 32 |
|  | 0.8 | 119364 | 52 | 57 | 39 | 34 |
|  | 0.7 | 92088 | 63 | 58 | 38 | 37 |
|  | 0.6 | 92598 | 60 | 60 | 35 | 42 |
|  | 0.5 | 85674 | 40 | 61 | 33 | 52 |
|  | 0.4 | 80514 | 56 | 62 | 27 | 64 |
|  | 0.3 | 76914 | 60 | 63 | 18 | 92 |


(a)

(c)

(e)

True Vertex

(b)

Accepted True Vertex

(d)

(f)

* Generic Background
- Neutrino interaction from the beam for 6 yrs of exposure
- Single beam spill, $\mathrm{T}=1.2 \mathrm{~s} \equiv 7.5 \times 10^{13} \mathrm{POT}$ within the full body of detector: Number of $v$ interactions $\sim 1.3 \times 10^{10}$
* Computationally Affordable Background Generation
- First approximation:
- v CC interactions only inside SAND inner tracker (STT)
- Interaction inside STT is 0.74 for one single spill: $117 \times 10^{6} \mathrm{v}$ CC interactions for 6 yrs of exposure
- Second Approximation (High statistic only at generation level):
- Most dangerous final state to the signal: $\pi \mu$
- Cherry picking the final state -> choosing events with final state single $\pi$ ( $\sim 30 \%$ of total events)
- $30 \times 10^{6}$ vCC interactions for 6 yrs of exposure
- Simulation and reconstruction steps the same as for the signal
- Background invariant mass distribution mimicking the signal (2ph+2g tracks) $\rightarrow 11$ candidates for 6 yrs of exposure
- Background Modeling
- Uniform or exponential p.d.f.
* Subdominant Background Event Topology and selection "handles"

1. Accidental vertex

- Vertex resolution
- Invariant Mass

2. Outside vertex

- Vertex resolution either/or Invariant Mass


## Background



ECAL



## \# v-CC interactions Background: single n final state



| Detector element | Mass [t] | FHC | RHC |
| :---: | :---: | :---: | :---: |
| Magnet | 511 | 68.9 | 36.6 |
| ECAL | 100 | 13.5 | 7.2 |
| LAr+STT | 8.2 | 1.1 | 0.59 |
| STT fiducial volume | 5.5 | 0.74 | 0.39 |
| Total | 619.2 | 83.5 | 44.39 |

https://indico.cern.ch/event/806612/attachments/1813045/2962023/A Near Detector for DUNE.pdf

Signal Modeling

## * Signal Model (RooFit):

- Two-sided Hypatia distribution as signal p.d.f:
- Hyperbolic core of a crystal-ball-like G function and two tails
- Model the invariant mass distribution with generic tails
- Fitting the signal with Hypatia gives a much better parametrization





HNL Signal $\left(m_{\mathrm{HNL}}=1.0\right)$


HNL Signal $\left(\mathrm{m}_{\mathrm{HNL}}=1.7\right)$


## Final Sensitivity

## * Combining parameters in Pheno-sensitivity with statistical analysis of the Signal and Background

- Signal Model:

Hypatia p.d.f. $\longrightarrow$ model the invariant mass distribution with generic tails

- Background Model:

Exponential or Flat p.d.f. $\rightarrow$ model the most dangerous background

- CLs Calculation (RooStats):
- Inference calculation using frequentist approach based on likelihood ratio
- Generating toy MC samples ( 100 toys)
- $N_{s} \rightarrow \mathrm{U}^{2}: \mathrm{N}_{\mathrm{s}}$ is not imposed to 1 but to the number of events is corresponding to $95 \% \mathrm{CL}$, taking into account $\mathrm{A}, \varepsilon$ and g





## * Summary

- Sensitivity to Heavy Neutral Lepton has been investigated: Pheno+Detector simulation
- Theory framework: vMSM
- Lagrangian conversion: FynRules+Mathematica
- Simulation Tools: Pythia8, Mad-Dump
- Pheno-sensitivity for three benchmark couplings and
for 6 yrs of exposure $\sim 10^{-8}-10^{-9}$
- Traget detector: SAND
- Reconstruction Tool: Kalman Filter
- Efficiency for single track: $\sim 80 \%$, track pair: $\sim 60 \%$
- Signal modeling: Two-sided Hypatia p.d.f.
- Most dangerous Background: $v_{\mu} C C+\pi$
- Background Modeling: Uniform and exponential p.d.f.
- 11 candidates from background for 6 yrs of exposure
- Final Sensitivity for vMSM, coupling model II, degraded by factor $\sim 3$ from Pheno-Sensitivity
* Outlook
- Pheno: Adding more channels, HNL production/decay
- Simulation: More realistic picture adding pile up
- Reconstruction: Optimization of Kalman Filter

Summary and Outlook


* Comments on Kalman Filter
- Each implementation of KF is unique with its challenges
- Customized for this work: working decently for high momentum
- Pattern recognition, an external fit is used due to better results
- Geometry dependent (implemented for full STT geometry)
- The Efficiency is $\sim 80 \%$, meets the need of this work
- It can be optimized to be used for any geometry and generic neutrino interaction event.
* Comments on Final Sensitivity
- The final sensitivity calculation has been demonstrated within vMSM and for benchmark II
- The final sensitivity for Majorana HNLs shows a factor $\sim 3$ degradation with respect to the Pheno, thanks to reconstruction efficiency and low background
- Room for improvement through optimization, but no big difference is expected
- In higher mass region the sensitivity worsens due to the larger invariant mass resolution


