

# Higgs CP violation at future colliders

Andrei Gritsan

Johns Hopkins University



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Energy Frontier: Higgs and BSM I Session  
Snowmass Summer Meeting, Seattle

# CP-violating H(125) Couplings

- CP-violating H(125) couplings

- tiny in the SM, excellent null-test

- well-defined stand-alone reference measurement

- potential baryogenesis connected to the Higgs sector

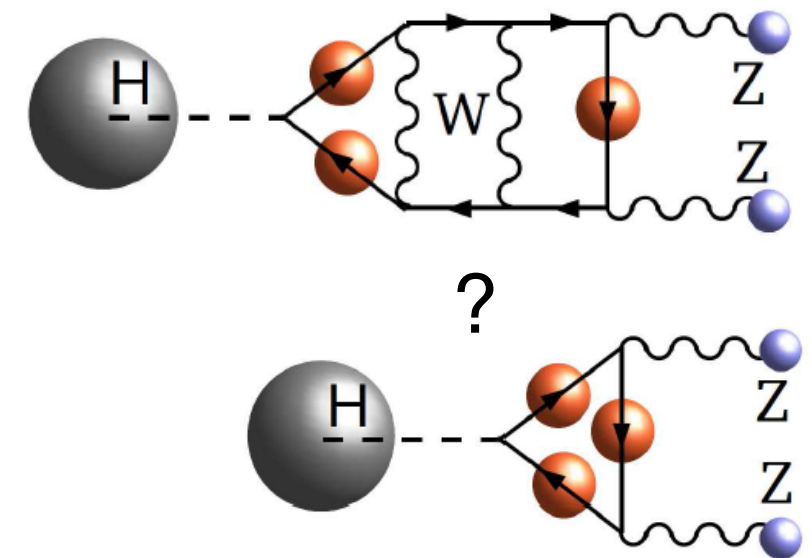
- $pp, e^+e^-, e^-p, \gamma\gamma, \mu^+\mu^- (\sqrt{s})$  have their unique features in  $CP$  of  $H(125)$

- complementarity to the EDM measurements and Flavor Physics

- Identify key reference measurements to compare facilities

- focus on direct H production

- connect to indirect (virtual, low-energy) probes



# Snowmass White Paper on Higgs CP

- Dedicated Snowmass White Paper: [arXiv:2205.07715](https://arxiv.org/abs/2205.07715)

Snowmass White Paper: Prospects of CP-violation measurements  
with the Higgs boson at future experiments

Editor: Andrei V. Gritsan,<sup>1</sup> Contributors: Henning Bahl,<sup>2</sup> Rahool Kumar Barman,<sup>3</sup> Ivanka Božović-Jelisavčić,<sup>4</sup> Jeffrey Davis,<sup>1</sup> Wouter Dekens,<sup>5</sup> Yanyan Gao,<sup>6</sup> Dorival Gonçalves,<sup>3</sup> Lucas S. Mandacarú Guerra,<sup>1</sup> Daniel Jeans,<sup>7</sup> Kyoungchul Kong,<sup>8</sup> Savvas Kyriacou,<sup>1</sup> Ren-Qi Pan,<sup>9</sup> Jeffrey Roskes,<sup>1</sup> Nhan V. Tran,<sup>10</sup> Natasa Vukašinović,<sup>4</sup> and Meng Xiao<sup>9</sup>

- Quick overview: [report in 2020](#) [report in 2021](#)

TABLE I: List of expected precision (at 68% C.L.) of  $CP$ -sensitive measurements of the parameters  $f_{CP}^{HX}$  defined in Eq. (2). Numerical values are given where reliable estimates are provided,  $\checkmark$  mark indicates that feasibility of such a measurement could be considered.

**Snowmass-2022**

Collider	$pp$	$pp$	$pp$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^-p$	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000		125	125	$\geq 500$	(theory)
$\mathcal{L}$ (fb <sup>-1</sup> )	300	3,000	20,000	250	350	500	1,000		250			
$HZZ/HWW$	$4 \cdot 10^{-5}$	$2.5 \cdot 10^{-6}$	$\checkmark$	$3.4 \cdot 10^{-4}$	$1.1 \cdot 10^{-4}$	$4 \cdot 10^{-5}$	$8 \cdot 10^{-6}$	$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$	$< 10^{-5}$
$H\gamma\gamma$	–	0.50	$\checkmark$	–	–	–	–	–	0.06	–	–	$< 10^{-2}$
$HZ\gamma$	–	$\sim 1$	$\checkmark$	–	–	–	–	–	–	–	–	$< 10^{-2}$
$Hgg$	0.12	0.011	$\checkmark$	–	–	–	–	–	–	–	–	$< 10^{-2}$
$Ht\bar{t}$	0.24	0.05	$\checkmark$	–	–	0.29	0.08	–	–	–	$\checkmark$	$< 10^{-2}$
$H\tau\tau$	0.07	0.008	$\checkmark$	0.01	0.01	0.02	0.06	–	$\checkmark$	$\checkmark$	$\checkmark$	$< 10^{-2}$
$H\mu\mu$	–	–	–	–	–	–	–	–	–	$\checkmark$	–	$< 10^{-2}$

<https://gitlab.cern.ch/snowmass21-ef01/higgs-cp>

# Starting Point: Snowmass-2013

- Start from Snowmass-2013, several developments in 9 years:
  - reliable **LHC results** on most measurements
  - more studies supporting **future proposals** (including White Papers)
  - phenomenological** development, EFT...
- Focus on: *CP* in *HZZ/HWW, HZγ, Hγγ, Hgg, Htt, Hττ, Hμμ*

Same parameters of interest  
as in Snowmass-2013  
[arXiv:1310.8361](https://arxiv.org/abs/1310.8361)

$$f_{\text{CP}}^{HX} \equiv \frac{\Gamma_{H \rightarrow X}^{\text{CP odd}}}{\Gamma_{H \rightarrow X}^{\text{CP odd}} + \Gamma_{H \rightarrow X}^{\text{CP even}}}$$

not enough studies

Collider	<i>pp</i>	<i>pp</i>	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$\gamma\gamma$	$\mu^+\mu^-$	target (theory)
E (GeV)	14,000	14,000	250	350	500	1,000	126	126	
$\mathcal{L}$ (fb <sup>-1</sup> )	300	3,000	250	350	500	1,000	250		
spin-2 <sub>m</sub> <sup>+</sup>	~10σ	≫10σ	>10σ	>10σ	>10σ	>10σ			>5σ
$VVH^\dagger$	0.07	0.02	✓	✓	✓	✓	✓	✓	< 10 <sup>-5</sup>
$VVH^\ddagger$	4·10 <sup>-4</sup>	1.2·10 <sup>-4</sup>	7·10 <sup>-4</sup>	1.1·10 <sup>-4</sup>	4·10 <sup>-5</sup>	8·10 <sup>-6</sup>	–	–	< 10 <sup>-5</sup>
$VVH^\diamond$	7·10 <sup>-4</sup>	1.3·10 <sup>-4</sup>	✓	✓	✓	✓	–	–	< 10 <sup>-5</sup>
$ggH$	0.50	0.16	–	–	–	–	–	–	< 10 <sup>-2</sup>
$\gamma\gamma H$	–	–	–	–	–	–	0.06	–	< 10 <sup>-2</sup>
$Z\gamma H$	–	✓	–	–	–	–	–	–	< 10 <sup>-2</sup>
$\tau\tau H$	✓	✓	0.01	0.01	0.02	0.06	✓	✓	< 10 <sup>-2</sup>
$ttH$	✓	✓	–	–	0.29	0.08	–	–	< 10 <sup>-2</sup>
$\mu\mu H$	–	–	–	–	–	–	–	✓	< 10 <sup>-2</sup>

<sup>†</sup> estimated in  $H \rightarrow ZZ^*$  decay mode

<sup>‡</sup> estimated in  $V^* \rightarrow HV$  production mode

<sup>◇</sup> estimated in  $V^*V^* \rightarrow H$  (VBF) production mode

Snowmass-2013



# General Comments

Collider	$pp$	$pp$	$pp$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^-p$	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	125	125	$\geq 500$	(theory)	
$\mathcal{L}$ ( $\text{fb}^{-1}$ )	300	3,000	20,000	250	350	500	1,000	250				

$pp$  LHC & HL-LHC - based on LHC

FCC-hh & SPPC expect  $\times 100$  ✓

$e^+e^-$  - keep lumi scenarios from 2013  
scaling to  $\times 10$  lumi available

$e^-p$  - limited to VBF production of H  
point to opportunity, no projection ✓

$\gamma\gamma$  - focus on unique  $H\gamma\gamma$  coupling  
no recent projections

$\mu\mu$  - focus on unique  $H\mu\mu$  coupling on-shell ✓  
associated H production at high energies

Collider	$pp$	$pp$	$pp$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^-p$	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000		125	125	$\geq 500$	(theory)
$\mathcal{L}$ ( $\text{fb}^{-1}$ )	300	3,000	20,000	250	350	500	1,000		250			
$HZZ/HWW$	$4 \cdot 10^{-5}$	$2.5 \cdot 10^{-6}$	✓	$3.4 \cdot 10^{-4}$	$1.1 \cdot 10^{-4}$	$4 \cdot 10^{-5}$	$8 \cdot 10^{-6}$	✓	✓	✓	✓	$< 10^{-5}$
$H\gamma\gamma$	—	0.50	✓	—	—	—	—	—	0.06	—	—	$< 10^{-2}$
$HZ\gamma$	—	$\sim 1$	✓	—	—	—	—	—	—	—	—	$< 10^{-2}$
$Hgg$	0.12	0.011	✓	—	—	—	—	—	—	—	—	$< 10^{-2}$
$Ht\bar{t}$	0.24	0.05	✓	—	—	0.29	0.08	—	—	—	✓	$< 10^{-2}$
$H\tau\tau$	0.07	0.008	✓	0.01	0.01	0.02	0.06	—	✓	✓	✓	$< 10^{-2}$
$H\mu\mu$	—	—	—	—	—	—	—	—	—	✓	—	$< 10^{-2}$

# Unique features of Facilities: $\gamma\gamma$ production

- **Photon collider** is unique with focus on  $H\gamma\gamma$  coupling

- photon beam polarization is critical for CP
- most interesting parameter:

$$\mathcal{A}_3 = \frac{|A_{||}|^2 - |A_{\perp}|^2}{|A_{||}|^2 + |A_{\perp}|^2} = \frac{2\mathcal{R}e(A_{--}^* A_{++})}{|A_{++}|^2 + |A_{--}|^2} = \frac{|a_2|^2 - |a_3|^2}{|a_2|^2 + |a_3|^2} = (1 - 2f_{CP})$$

Detecting and Studying Higgs Bosons at a Photon-Photon Collider: [arXiv:hep-ph/0110320](https://arxiv.org/abs/hep-ph/0110320)

- measure as asymmetry between  $||$  and  $\perp$  linear polarizations

for  $E_0 = 110$  GeV and  $\lambda = 1 \mu\text{m}$ :  $f_{CP} = \sin^2(\alpha^{\gamma\gamma}) \sim \pm 0.06$

at  $2.5 \cdot 10^{34} \times 10^7 = 250 \text{ fb}^{-1}$

Collider	$pp$	$pp$	$pp$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^-p$	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000		125	125	$\geq 500$	(theory)
$\mathcal{L}$ ( $\text{fb}^{-1}$ )	300	3,000	20,000	250	350	500	1,000		250			

$H\gamma\gamma$	—	0.50	✓	—	—	—	—	—	0.06	—	—	$< 10^{-2}$
$HZ\gamma$	—	$\sim 1$	✓	—	—	—	—	—	—	—	—	$< 10^{-2}$

# Unique features of Facilities: $\mu^+\mu^-$ production

- Muon collider is unique with focus on  $H\mu\mu$  coupling
  - muon beam transverse polarization is critical for CP
  - not many fermion couplings can be tested with polarization and CP
  - later we will discuss  $H\tau\tau$  and  $Htt$  (both 3rd family)
  - same transverse polarization  $\Rightarrow$  CP-even
  - opposite polarization  $\Rightarrow$  CP-odd

How Valuable is Polarization at a Muon Collider? A Test Case: Determining the CP Nature of a Higgs Boson:  
[arXiv:hep-ph/0003091](https://arxiv.org/abs/hep-ph/0003091)

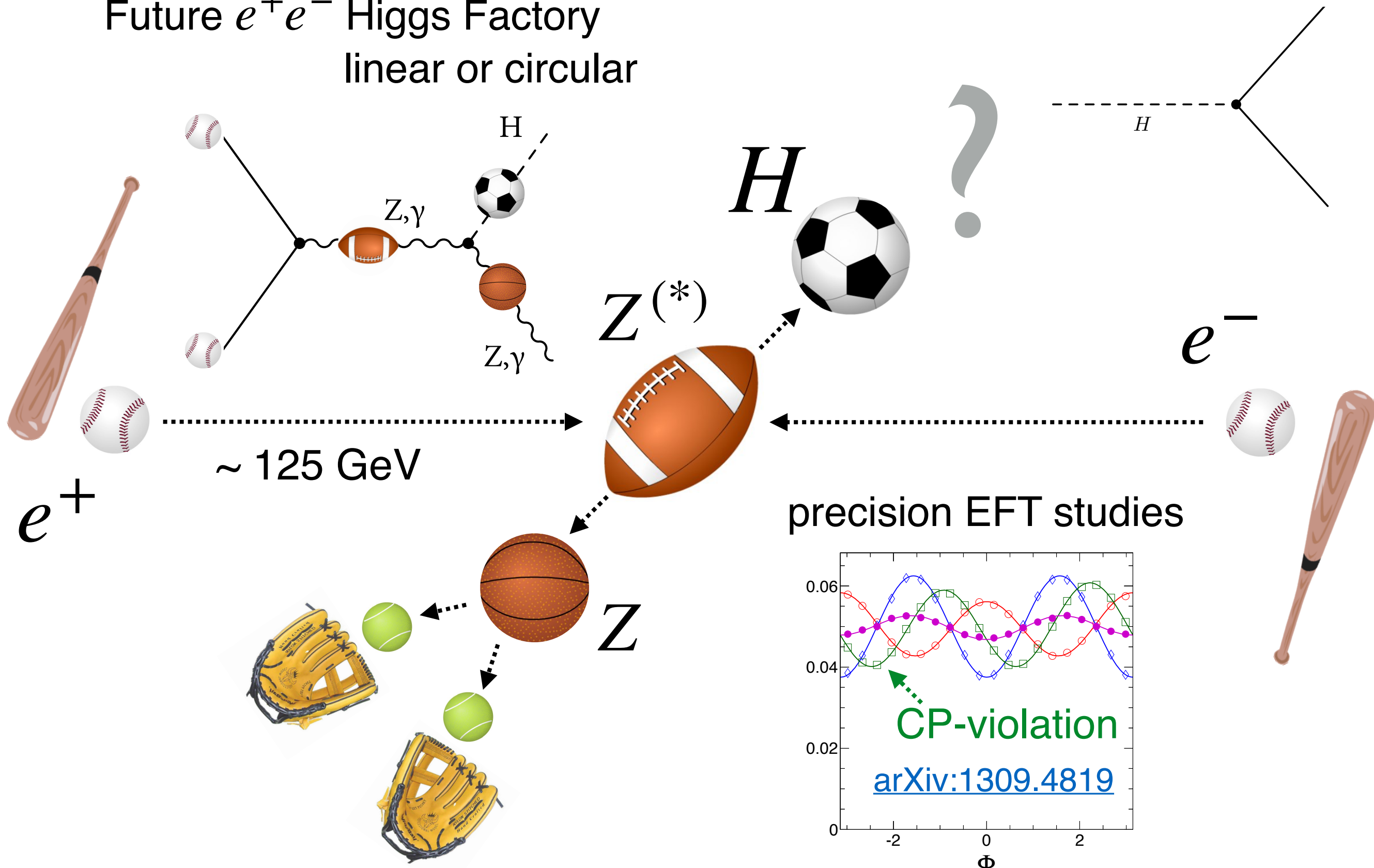
- Unique feature of the muon collider (CP in coupling to 2nd family)
  - though comes with a price of lumi, likely not a priority at first stage

Collider	$pp$	$pp$	$pp$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^-p$	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000		125	125	$\geq 500$	(theory)
$\mathcal{L}$ (fb $^{-1}$ )	300	3,000	20,000	250	350	500	1,000		250			
$H\mu\mu$	—	—	—	—	—	—	—	—	—	✓	—	$< 10^{-2}$

- High energy  $\mu^+\mu^-$ : associated production  $t\bar{t}H$ , VBF

# Unique features of Facilities: $e^+e^-$ production

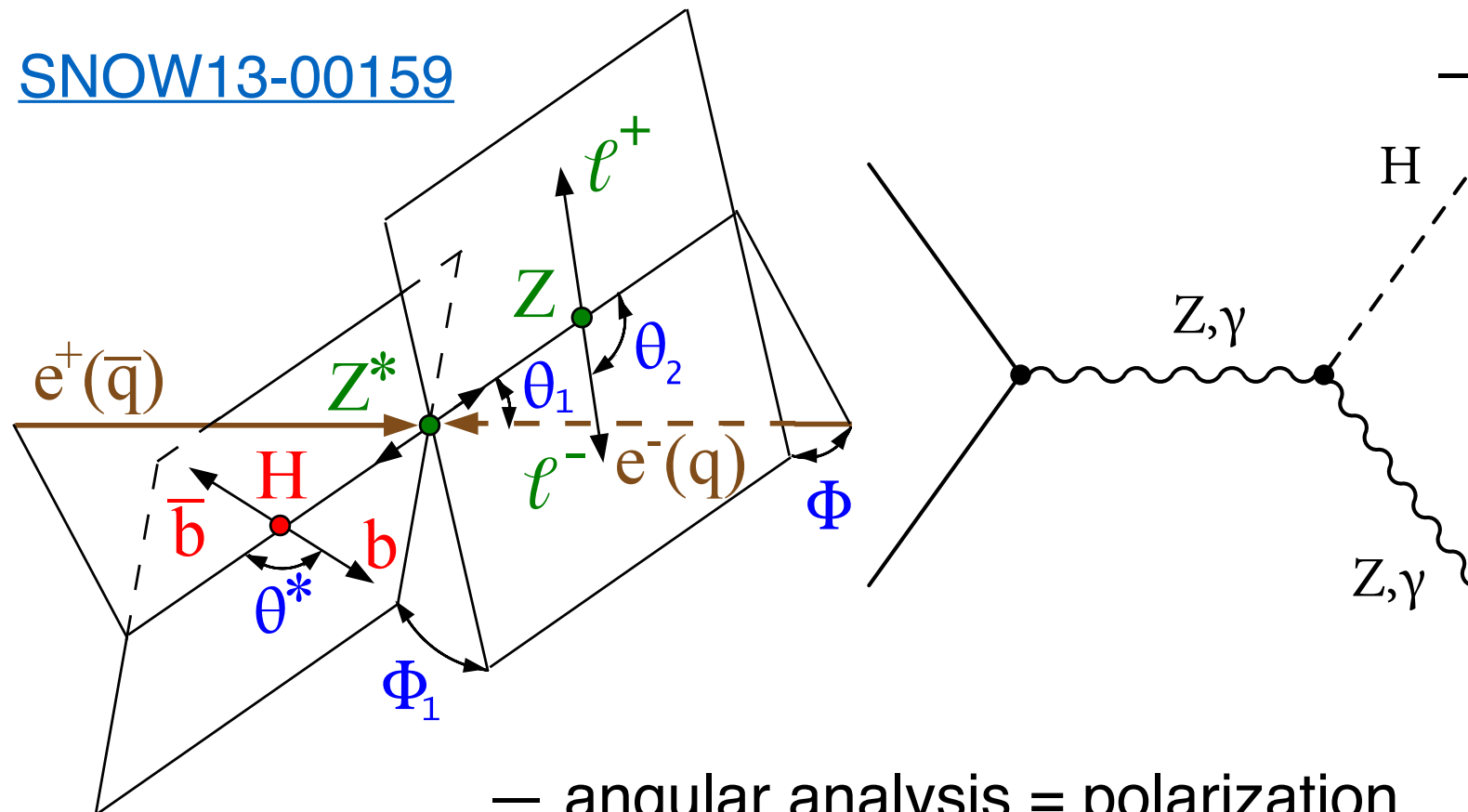
Future  $e^+e^-$  Higgs Factory  
linear or circular



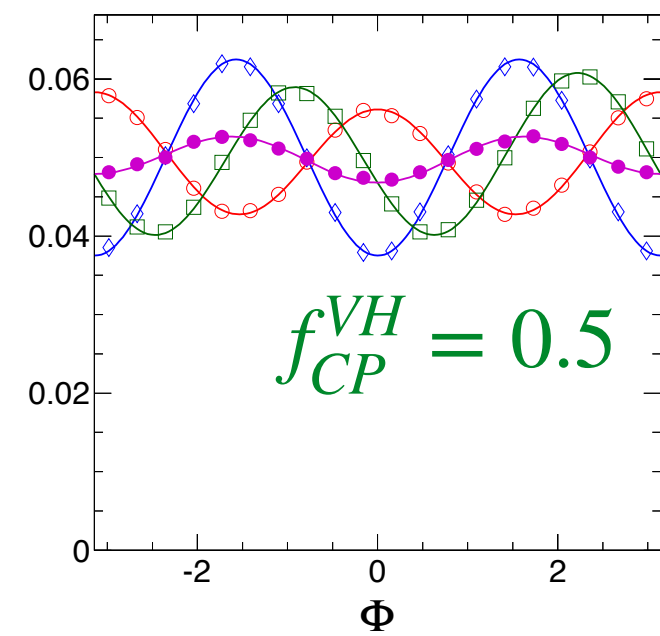
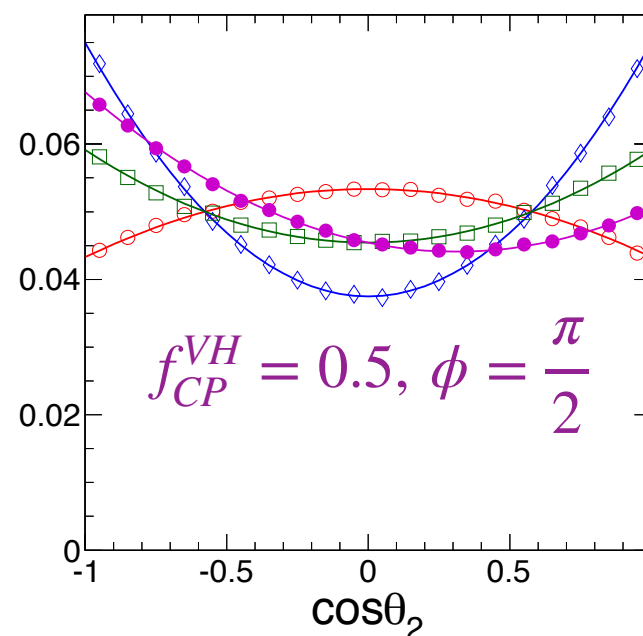
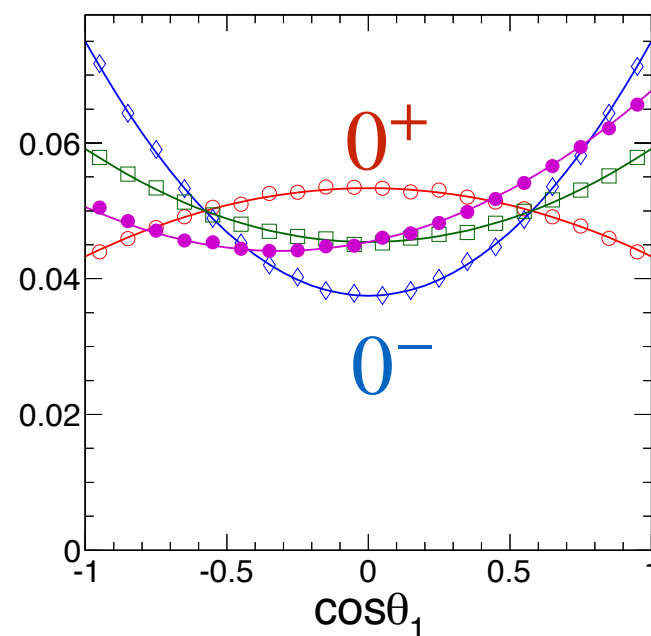
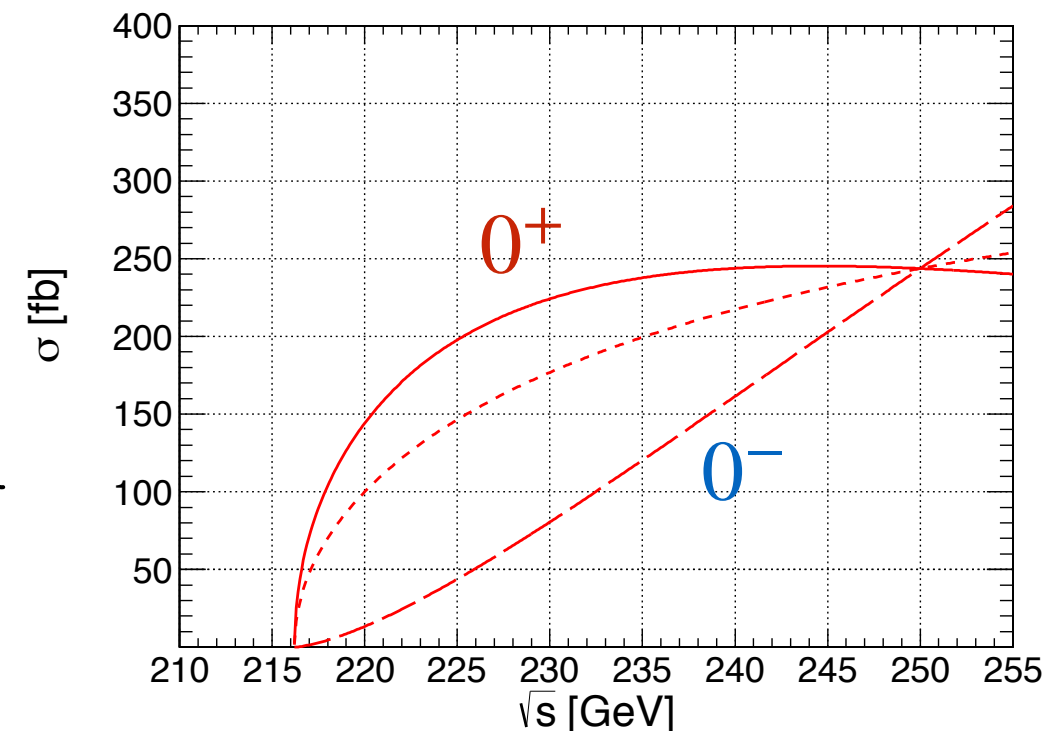
# Unique features of Facilities: $e^+e^-$ production

- $e^+e^-$  collider  $\rightarrow Z^* \rightarrow ZH \Rightarrow HZZ, HZ\gamma, H\gamma\gamma$  couplings

[SNOW13-00159](#)

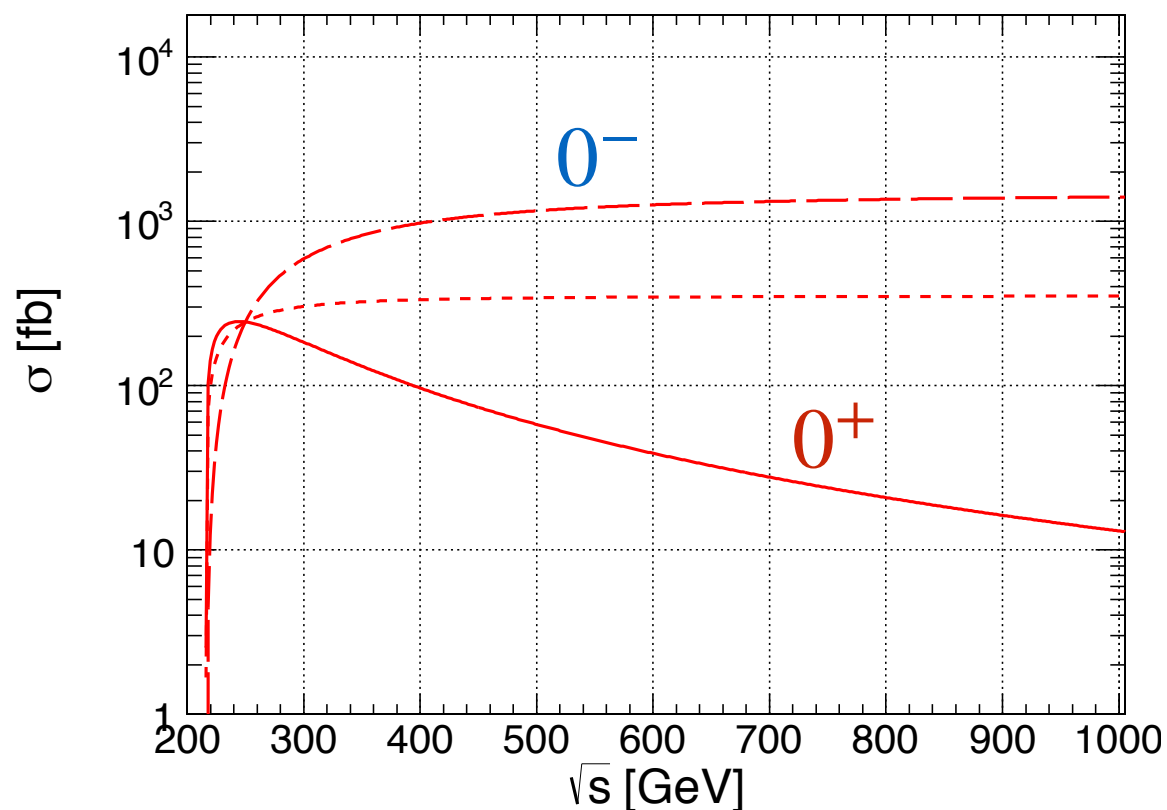


— threshold scan =  $q^2$  dependence



# $e^+e^-$ production at higher energies (LC)

- $e^+e^-$  collider  $\rightarrow Z^* \rightarrow ZH$
  - Scan  $q^2$  dependence of HVV
- $\Rightarrow$  increased sensitivity (no cutoff)



[SNOW13-00159](#)

- VBF  $e^+e^- \rightarrow \nu\bar{\nu}H$
- not much angular information  
 $q^2$ -dependence through  $p_T^H \dots$

- VBF  $e^+e^- \rightarrow e^+e^-H$

recent study ([ICHEP-2022](#))  
does not surpass  $e^+e^- \rightarrow Z^* \rightarrow ZH$   
at intermediate energies



# Unique features of Facilities: $e^+e^-$ production

- $e^+e^-$  collider  $\rightarrow Z^*/\gamma^* \rightarrow Z/\gamma^*H \Rightarrow HZZ, HZ\gamma, H\gamma\gamma$  couplings

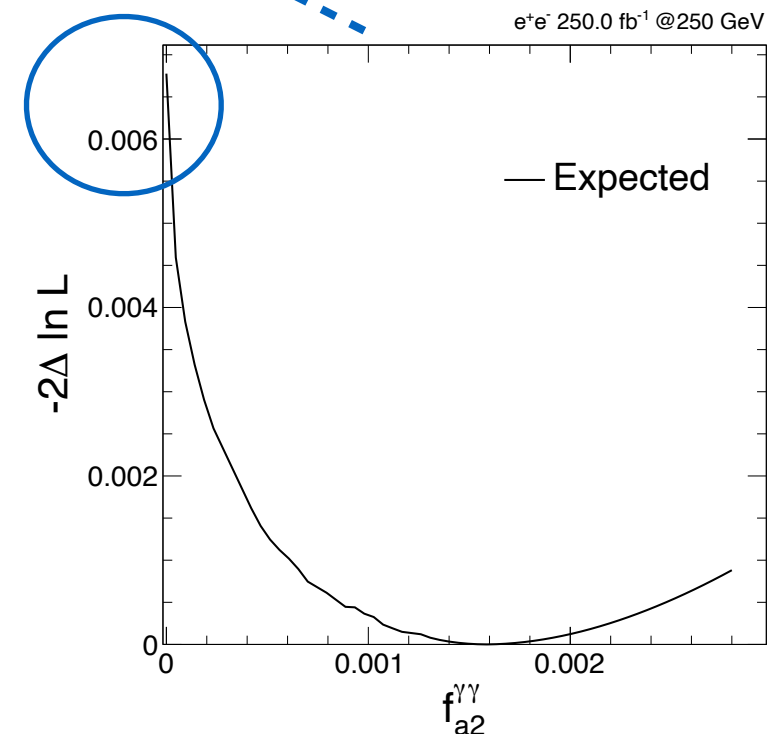
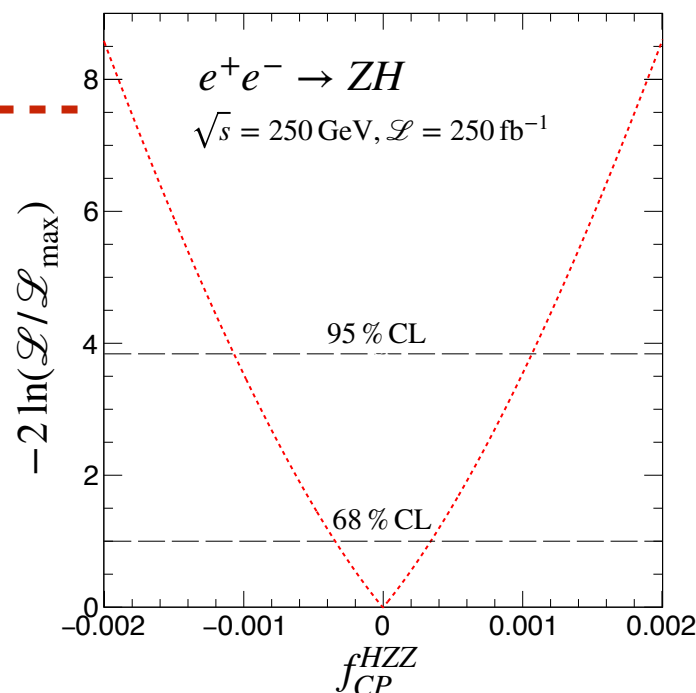
Collider	$pp$	$pp$	$pp$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^-p$	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000		125	125	$\geq 500$	(theory)
$\mathcal{L}$ (fb $^{-1}$ )	300	3,000	20,000	250	350	500	1,000		250			
$HZZ/HWW$	$4 \cdot 10^{-5}$	$2.5 \cdot 10^{-6}$	✓	$3.4 \cdot 10^{-4}$	$1.1 \cdot 10^{-4}$	$4 \cdot 10^{-5}$	$8 \cdot 10^{-6}$	✓	✓	✓	✓	$< 10^{-5}$
$H\gamma\gamma$	—	0.50	✓	—	—	—	—	—	0.06	—	—	$< 10^{-2}$
$HZ\gamma$	—	$\sim 1$	✓	—	—	—	—	—	—	—	—	$< 10^{-2}$

Appendix B: Recent updates of the studies at an electron-positron collider

see also [arXiv:2203.11707](https://arxiv.org/abs/2203.11707)  
in agreement

Contributed by Lucas S. Mandacarú Guerra and Savvas Kyriacou.

E (GeV)	$\mathcal{L}$ (fb $^{-1}$ )	$f_{CP}^{HVV}$
250	250	$3.4 \cdot 10^{-4}$
250	2,500	$3.9 \cdot 10^{-5}$
350	350	$1.2 \cdot 10^{-4}$
350	3,500	$2.9 \cdot 10^{-5}$
500	500	$4.3 \cdot 10^{-5}$
500	5,000	$1.3 \cdot 10^{-5}$
1,000	1,000	$1.0 \cdot 10^{-5}$
1,000	10,000	$3.0 \cdot 10^{-6}$

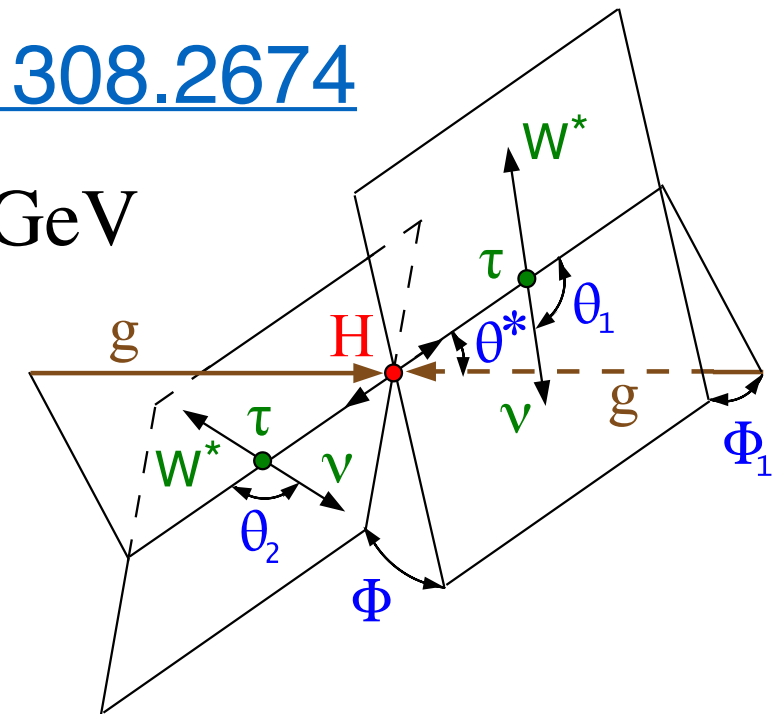


# Fermion couplings at an $e^+e^-$ collider

- $e^+e^-$  pheno studies at Snowmass-2013: [arXiv:1308.2674](https://arxiv.org/abs/1308.2674)

- $H \rightarrow \tau\tau$  the only CP in  $Hff$  at  $e^+e^-$   $\sqrt{s} < 500$  GeV
- reach  $f_{CP} \sim 0.008$  ( $\alpha \sim 5^\circ$ ) at  $e^+e^-$  ref. lumi

note: worse at higher  $\sqrt{s}$  : no vertex in  $e^+e^- \rightarrow \nu\bar{\nu}H$



- **Linear collider**  $e^+e^- \rightarrow t\bar{t}H$

cross section dependence studied of  $0^+$  vs.  $0^-$  at [Snowmass-2013](https://arxiv.org/abs/1308.2674)

recent similar study in [arXiv:1807.02441](https://arxiv.org/abs/1807.02441)

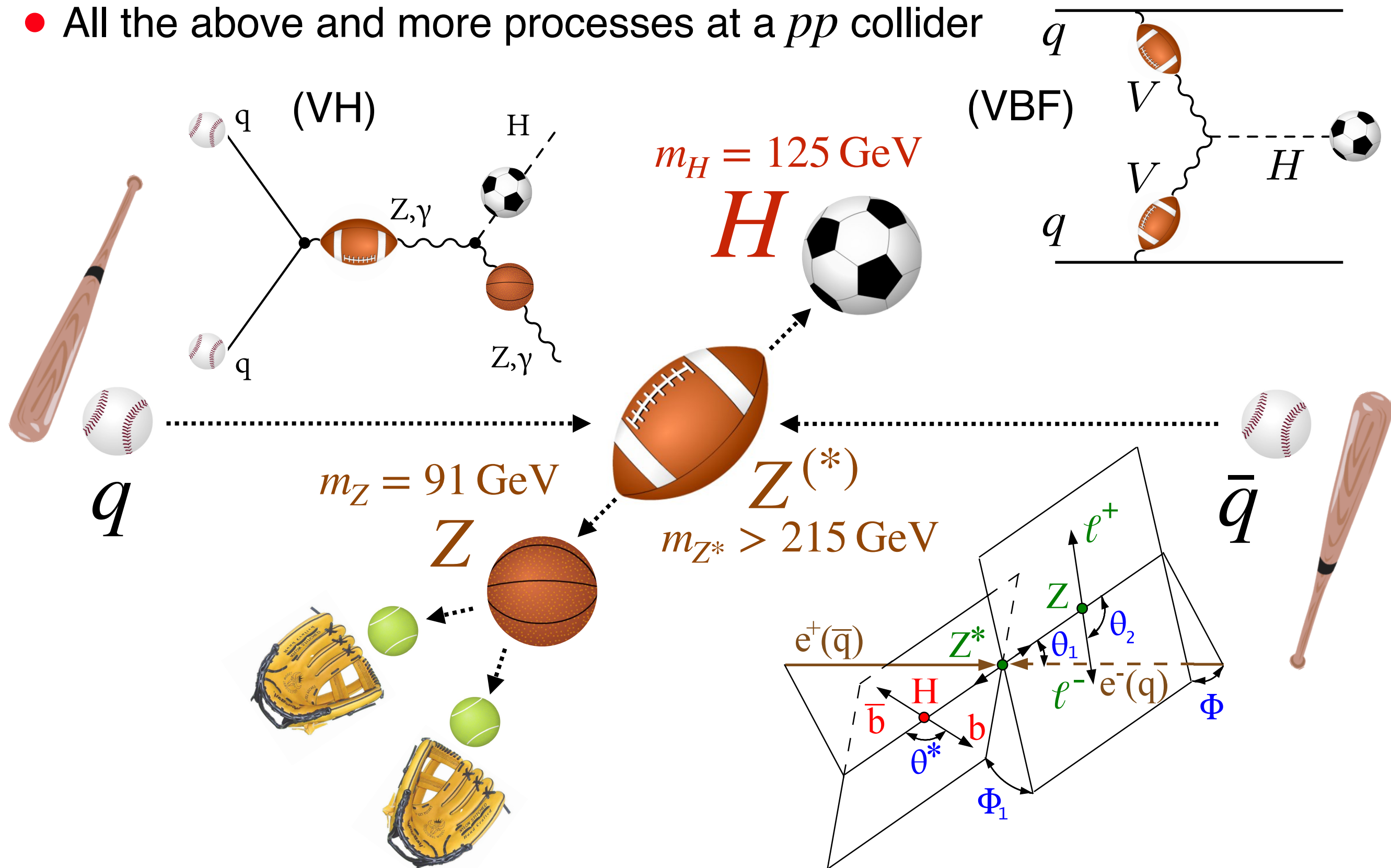
need dedicated  $CP$ -sensitive study (see LHC studies)

from Snowmass-2013

Collider	$pp$	$pp$	$pp$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^-p$	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	125	125	$\geq 500$		(theory)
$\mathcal{L}$ ( $\text{fb}^{-1}$ )	300	3,000	20,000	250	350	500	1,000	250				
$Ht\bar{t}$	0.24	0.05	✓	–	–	0.29	0.08	–	–	–	✓	$< 10^{-2}$
$H\tau\tau$	0.07	0.008	✓	0.01	0.01	0.02	0.06	–	✓	✓	✓	$< 10^{-2}$
$H\mu\mu$	–	–	–	–	–	–	–	–	–	✓	–	$< 10^{-2}$

# Unique features of Facilities: $pp$ production

- All the above and more processes at a  $pp$  collider



# Unique features of Facilities: $pp$ production

- $pp \rightarrow V^* \rightarrow VH \Rightarrow HWW, HZZ, HZ\gamma, H\gamma\gamma, Hgg$  couplings

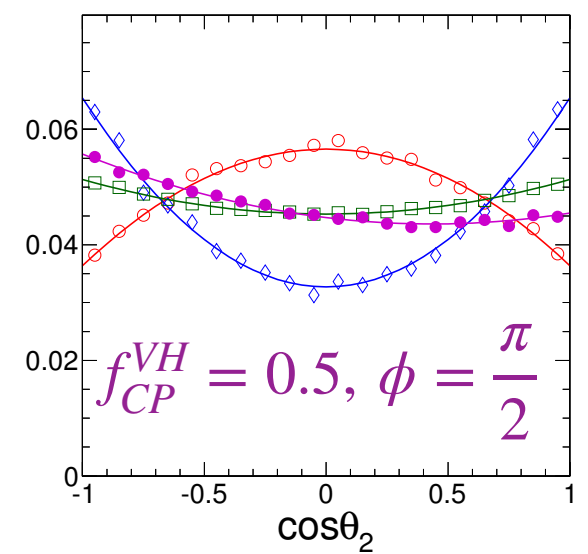
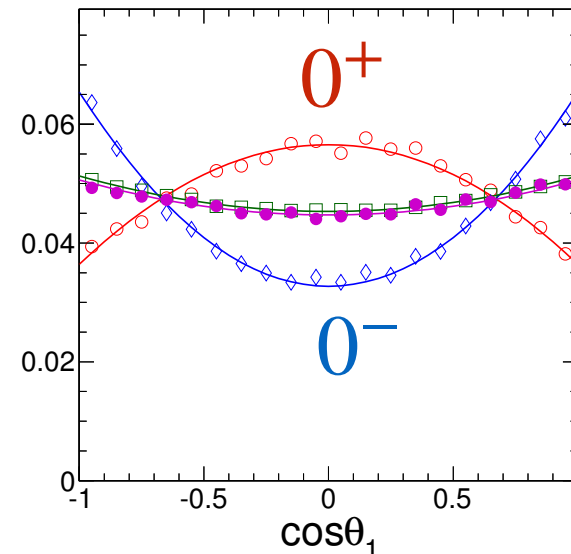
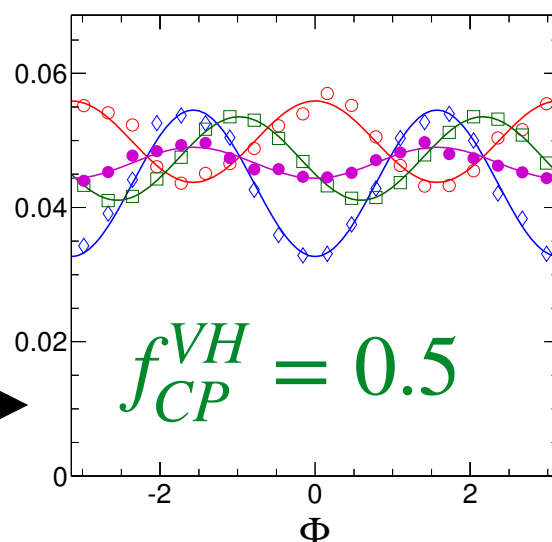
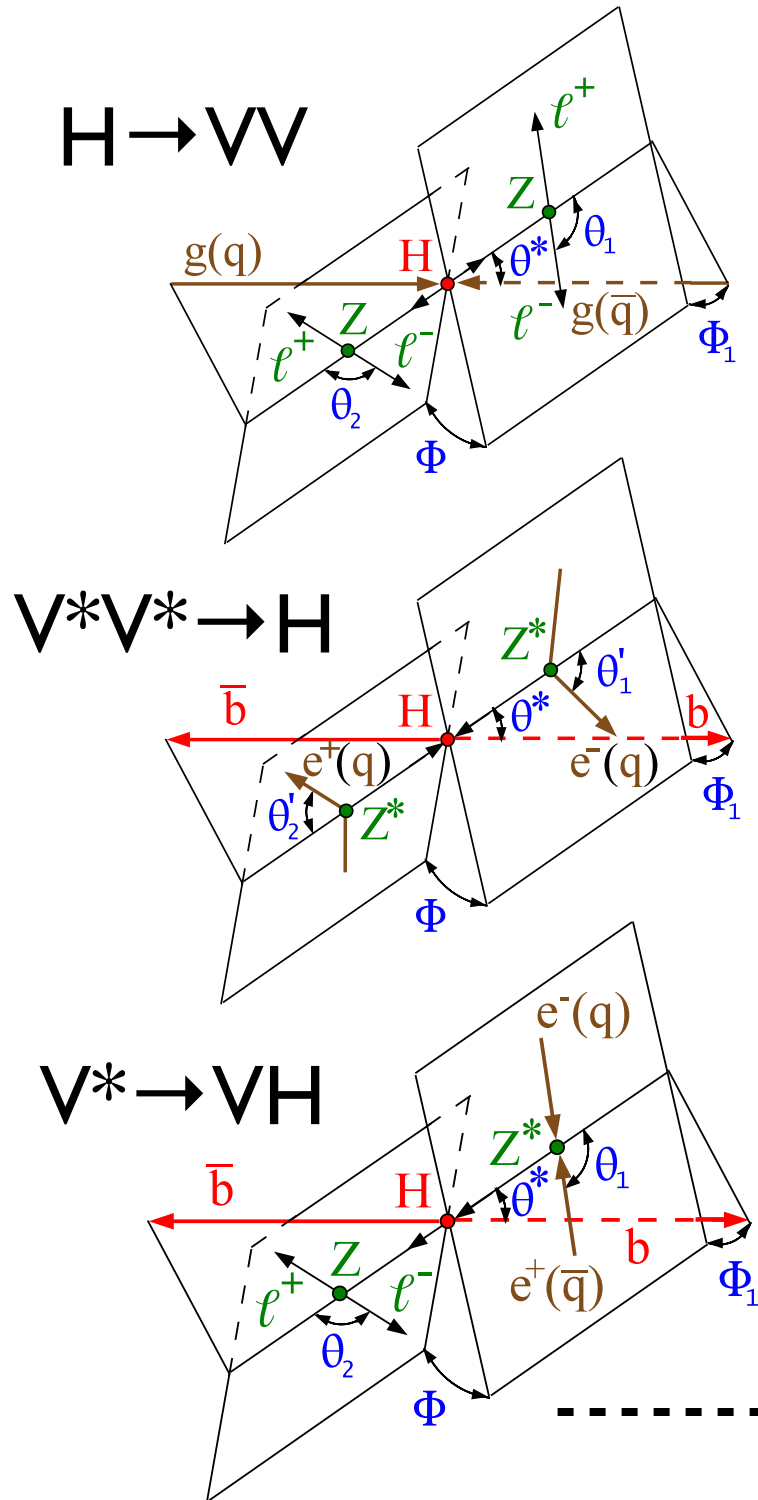
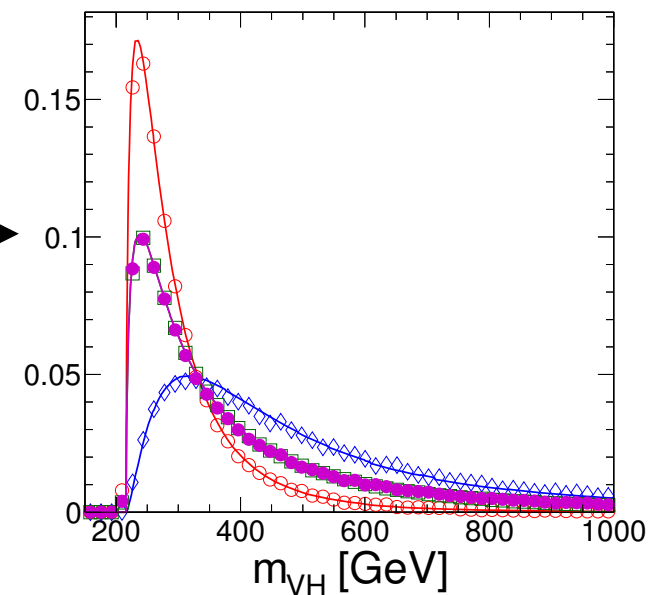
also VBF  $V^*V^* \rightarrow H$  and decay  $H \rightarrow VV$

$pp$  unique  $gg \rightarrow H$

benefit from LHC experience

- scan of  $q^2$ -dependence
- polarization measurement

[SNOW13-00159](#)

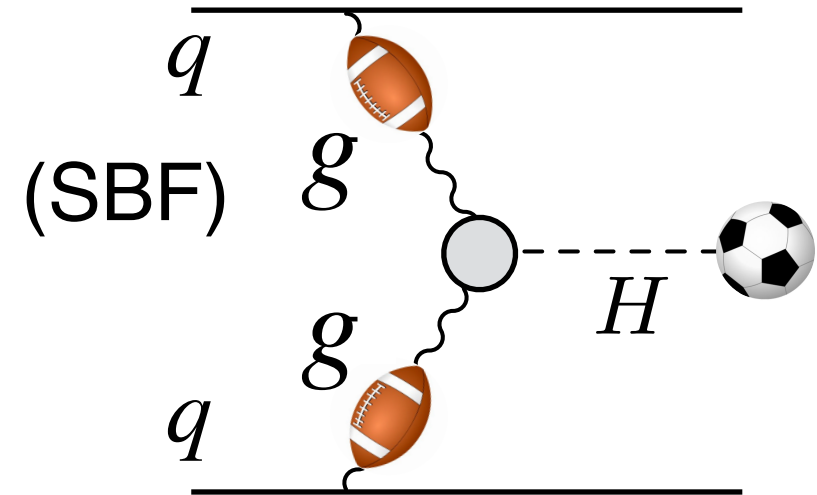


# Gluon fusion in $pp$ production

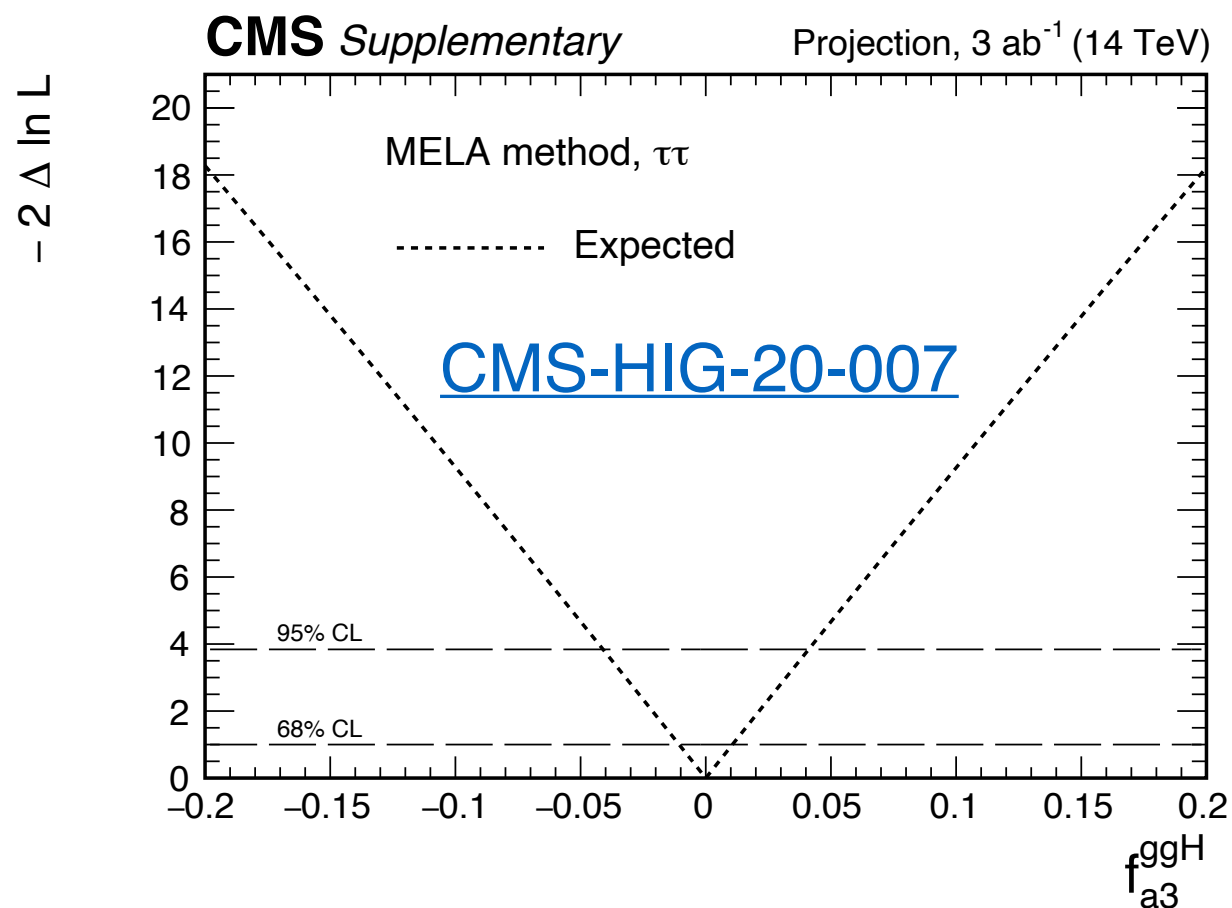
- $pp$  is unique to measure  $Hgg$  coupling

BSM loop (point-like) or SM fermion loop

$$a_2^{gg} = -\alpha_s \kappa_Q / (6\pi) \quad \& \quad a_3^{gg} = -\alpha_s \tilde{\kappa}_Q / (4\pi)$$



- Update Snowmass-2013 ([pheno](#)) with recent LHC (mutual benefit):



Collider	$pp$	$pp$	$pp$
E (GeV)	14,000	14,000	100,000
$\mathcal{L}$ ( $\text{fb}^{-1}$ )	300	3,000	20,000
$Hgg$	0.12	0.011	✓

benefit from multiple H decay modes

# $H\gamma\gamma, HZ\gamma$ in $pp$ production

- $CP$  in photon couplings appear challenging at all colliders

poor precision in VBF and  $VH$

Appendix A: Recent updates of the studies at a hadron collider

Contributed by Jeffrey Davis, Savvas Kyriacou, and Jeffrey Roskes.

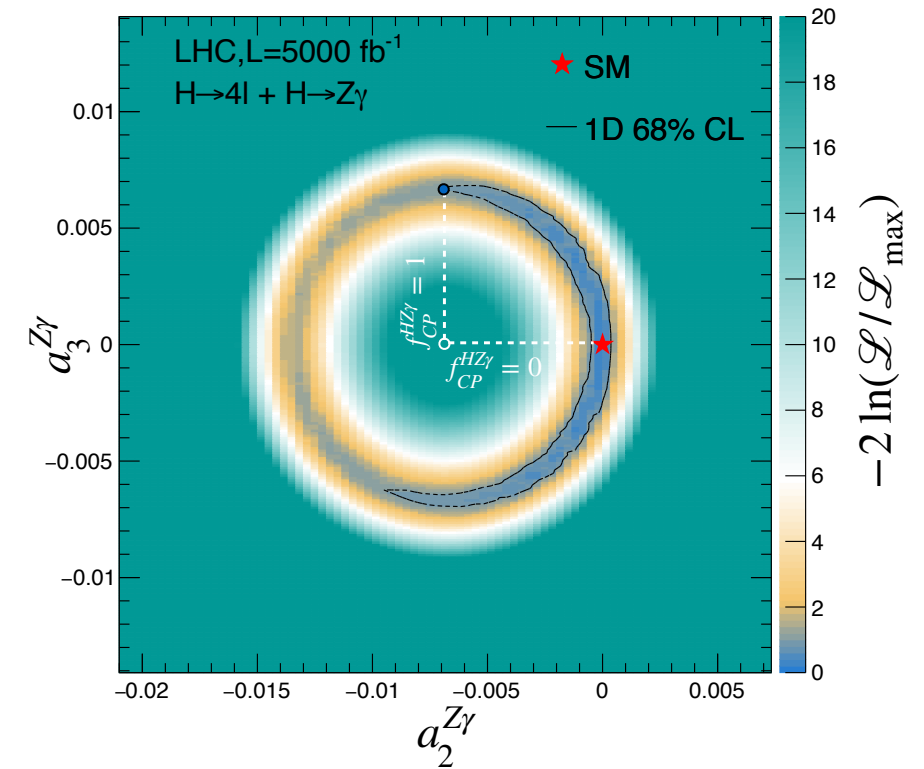
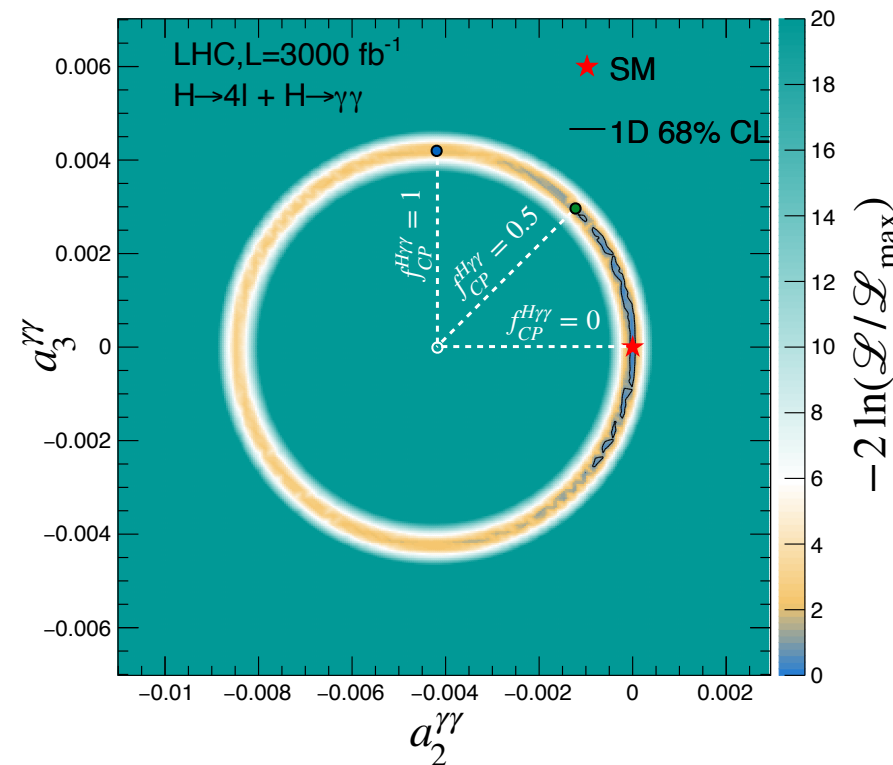
$$H \rightarrow \gamma\gamma(Z\gamma)$$

constrain  $(a_2^{V\gamma})^2 + (a_3^{V\gamma})^2$

$$H \rightarrow \gamma^*\gamma^*(Z\gamma^*) \rightarrow 4\ell$$

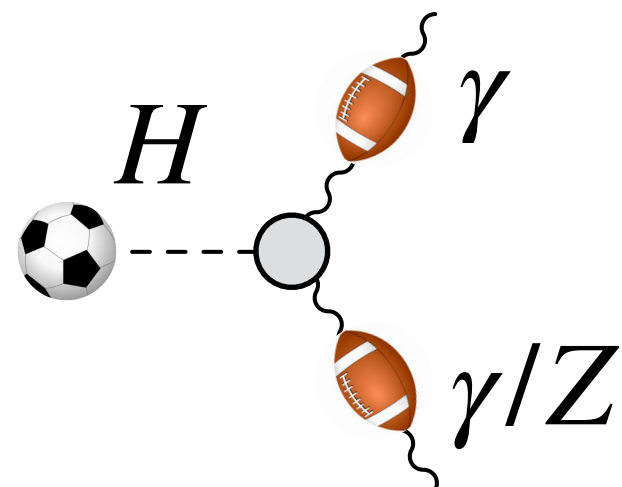
resolve  $a_2^{V\gamma}/a_3^{V\gamma}$

expect good constraints  
at  $pp$  100 TeV



Collider	$pp$	$pp$	$pp$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^-p$	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	125	125	$\geq 500$		(theory)
$\mathcal{L}$ ( $\text{fb}^{-1}$ )	300	3,000	20,000	250	350	500	1,000	250				

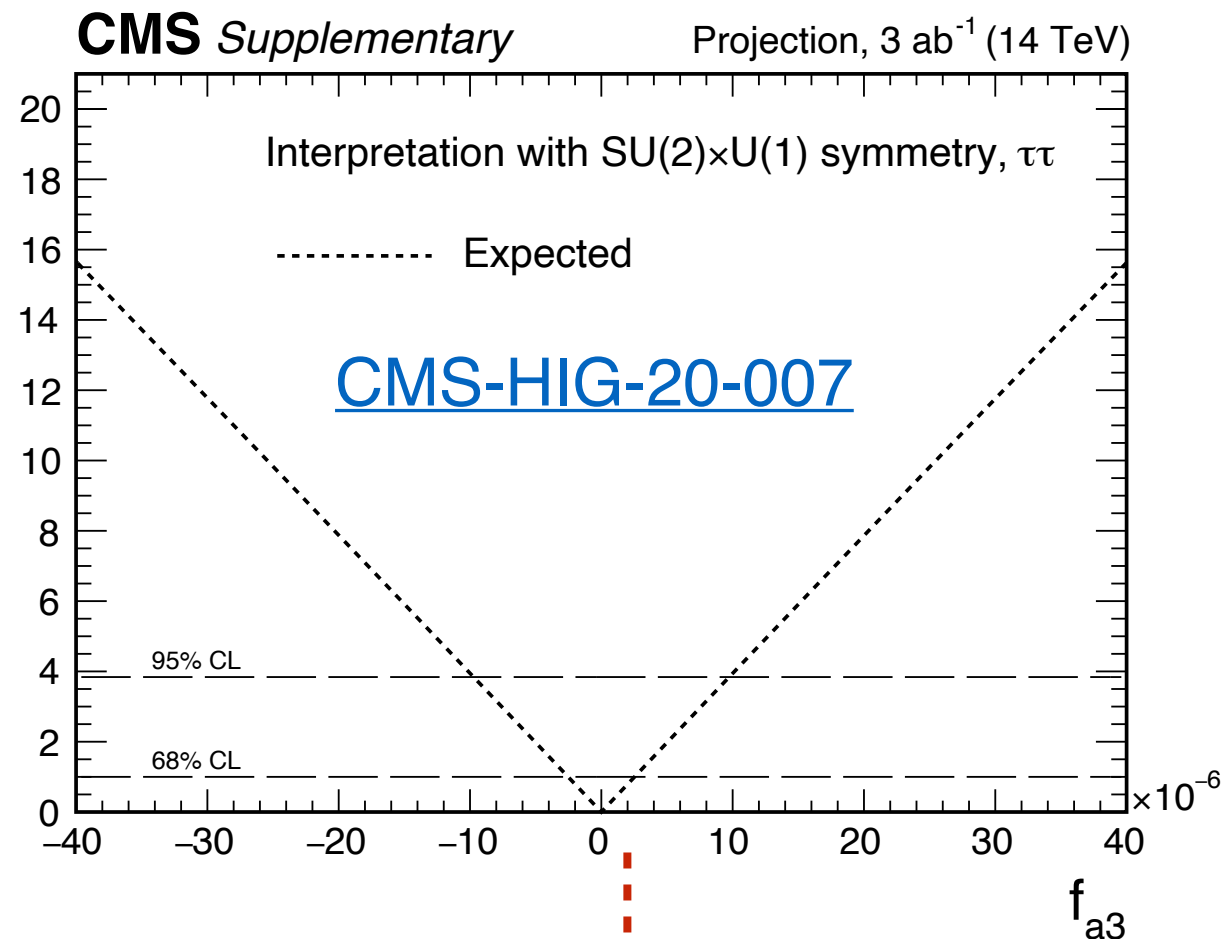
$H\gamma\gamma$	—	0.50	$< 0.05$ (?)	—	—	—	—	—	0.06	—	—	$< 10^{-2}$
$HZ\gamma$	—	$\sim 1$	$< 0.05$ (?)	—	—	—	—	—	—	—	—	$< 10^{-2}$





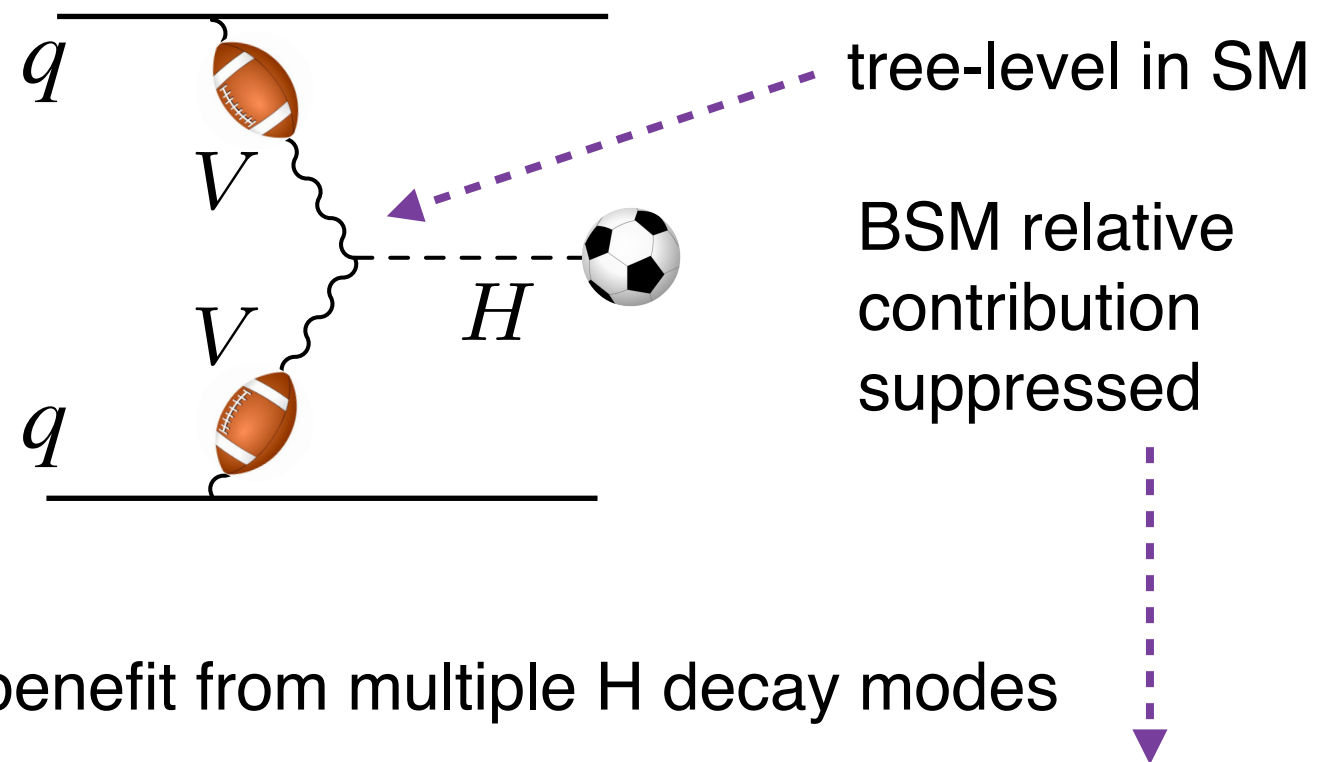
# $HZZ, HWW$ in $pp$ production

- Update Snowmass-2013 ([pheno](#)) with recent LHC (mutual benefit):



mostly VBF topology ( $VH$  similar)

$H \rightarrow VV$  not as sensitive due to low  $q^2$



Collider	$pp$	$pp$	$pp$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^-p$	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	125	125	$\geq 500$		(theory)
$\mathcal{L}$ ( $\text{fb}^{-1}$ )	300	3,000	20,000	250	350	500	1,000	250				
$HZZ/HWW$	$4 \cdot 10^{-5}$	$2.5 \cdot 10^{-6}$	✓	$3.4 \cdot 10^{-4}$	$1.1 \cdot 10^{-4}$	$4 \cdot 10^{-5}$	$8 \cdot 10^{-6}$	✓	✓	✓	✓	$< 10^{-5}$

$\sim 10^{-8} (?)$

# Fermion couplings: $t\bar{t}H$ at $pp$

- Very first test of CP in  $Hff$  in 2020:

- $t\bar{t}H$  spin-off from Snowmass-2013 ([arXiv:1606.03107](https://arxiv.org/abs/1606.03107))

pheno projection agreement with CMS/ATLAS

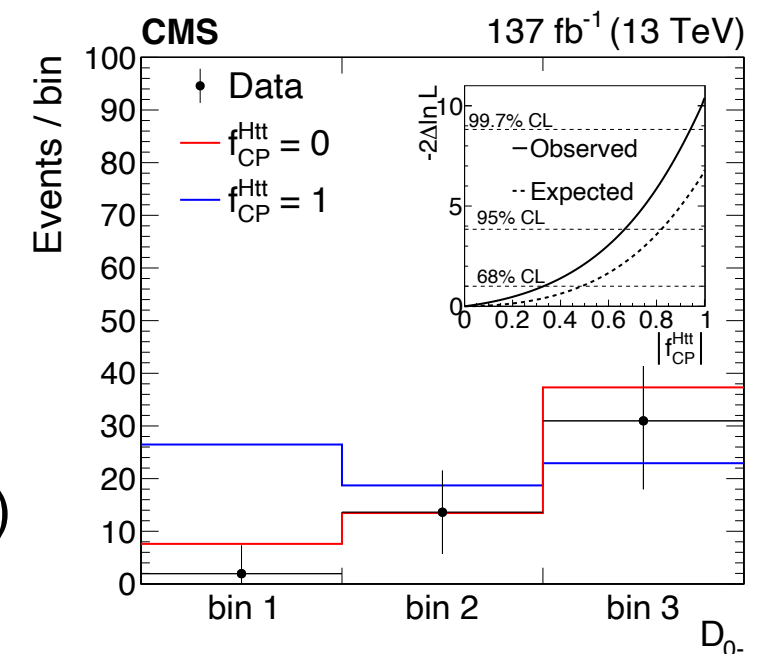
no sensitivity to  $2\text{Re}\left(A_{\text{CP even}}A_{\text{CP odd}}^*\right)$  (semi-leptonic, hadronic)

- need di-lepton channel for CP interf: [arXiv:1507.07926](https://arxiv.org/abs/1507.07926)

- reach  $f_{\text{CP}} \sim 0.05$  ( $\alpha \sim 13^\circ$ ) at HL-LHC [arXiv:2110.07635](https://arxiv.org/abs/2110.07635)

pheno projection with di-leptonic, semi-leptonic, hadronic  $t\bar{t}$  decay

- similar in  $tH$ ; no sensitivity to  $b\bar{b}H$ , or other light  $q$



CMS [arXiv:2003.10866](https://arxiv.org/abs/2003.10866)

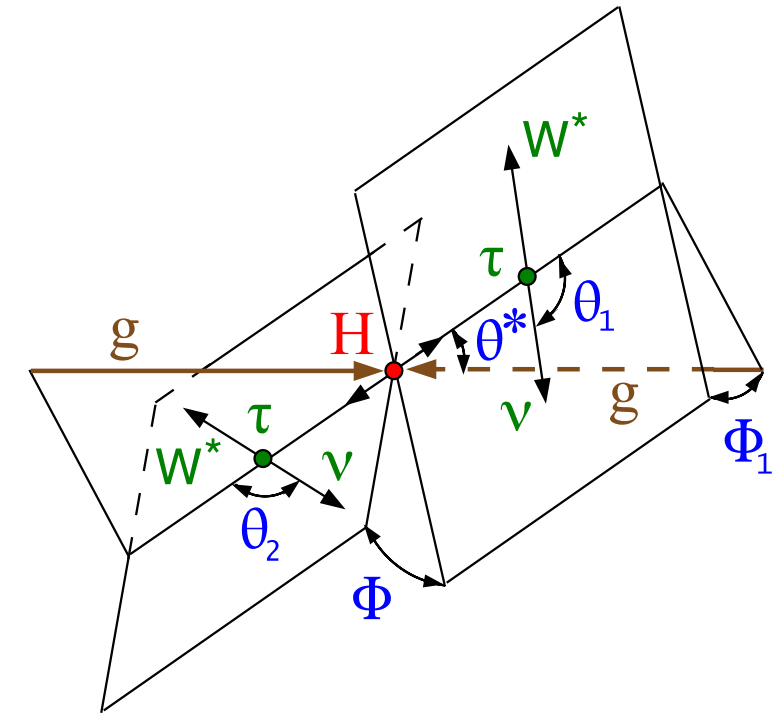
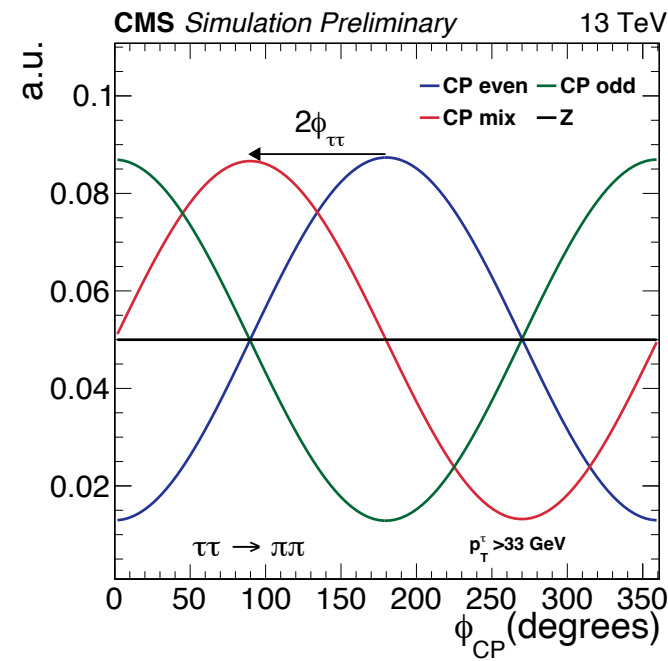
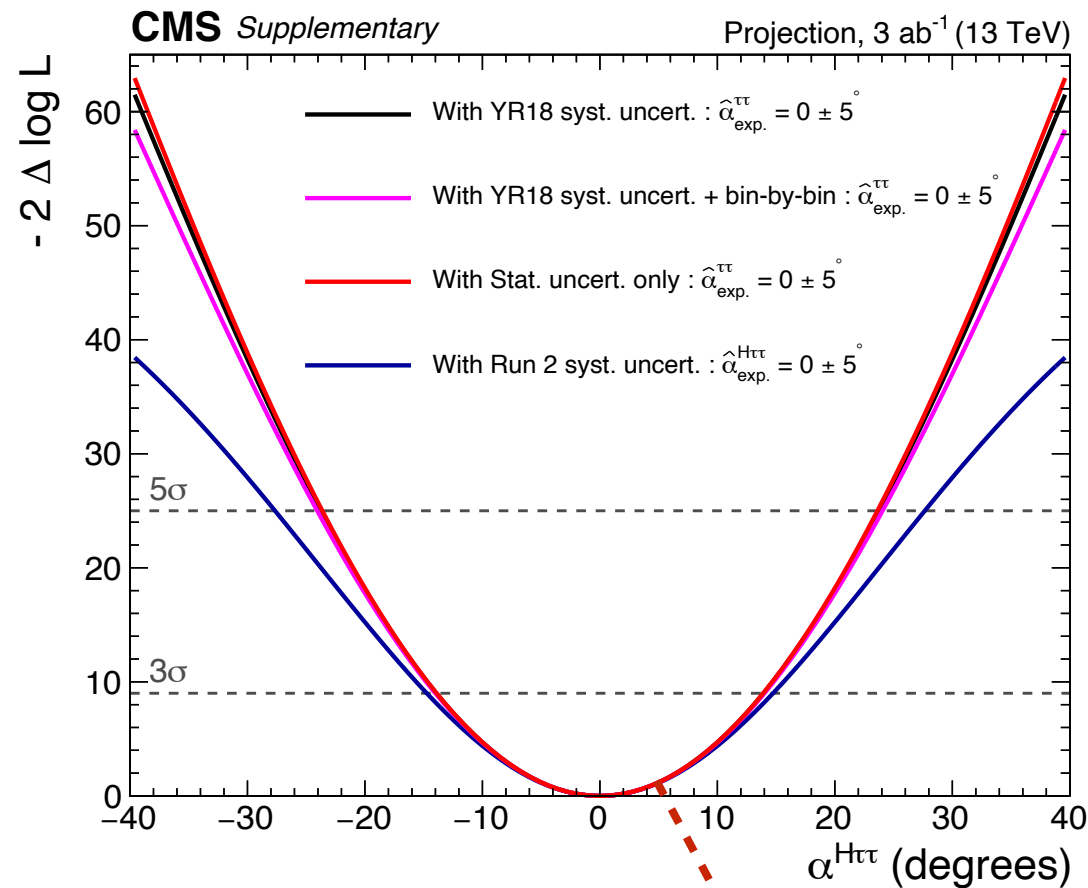
ATLAS [arXiv:2004.04545](https://arxiv.org/abs/2004.04545)

Collider	$pp$	$pp$	$pp$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^-p$	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	125	125	$\geq 500$		(theory)
$\mathcal{L}$ ( $\text{fb}^{-1}$ )	300	3,000	20,000	250	350	500	1,000	250				
$Ht\bar{t}$	0.24	0.05	✓	—	—	0.29	0.08	—	—	—	✓	$< 10^{-2}$

# Decay: $H \rightarrow \tau^+ \tau^-$ at $pp$

- Very first test of  $CP$  in  $H\tau\tau$  in 2020

CMS: [CMS-HIG-20-006](#)



$pp$  pheno studies at Snowmass-2013: [arXiv:1308.1094](#)

— reach  $f_{CP} \sim 0.008$  ( $\alpha \sim 5^\circ$ ) at HL-LHC [CMS-HIG-20-006](#)

Collider	$pp$	$pp$	$pp$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^-p$	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	125	125	$\geq 500$		(theory)
$\mathcal{L}$ ( $\text{fb}^{-1}$ )	300	3,000	20,000	250	350	500	1,000	250				
$H\tau\tau$	0.07	0.008	✓	0.01	0.01	0.02	0.06	—	✓	✓	✓	$< 10^{-2}$

# Overview of Higgs CP at Colliders

- Now cover all couplings at  $pp$  and  $e^+e^-$  colliders:

new numerical estimates for the first time (since 2013)

*pp* 100 TeV would be the best by  $\times 100$ , but more distant ...

new entries (since 2013)

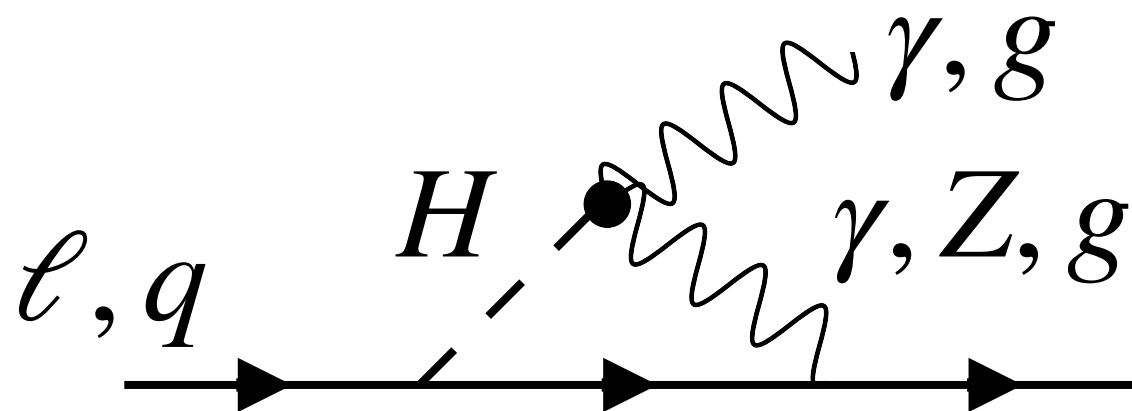
Collider	$pp$	$pp$	$pp$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^-p$	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target (theory)
E (GeV)	14,000	14,000	100,000	250	350	500	1,000		125	125	$\geq 500$	
$\mathcal{L}$ ( $\text{fb}^{-1}$ )	300	3,000	20,000	250	350	500	1,000		250			
$HZZ/HWW$	$4 \cdot 10^{-5}$	$2.5 \cdot 10^{-6}$	✓	$3.4 \cdot 10^{-4}$	$1.1 \cdot 10^{-4}$	$4 \cdot 10^{-5}$	$8 \cdot 10^{-6}$	✓	✓	✓	✓	$< 10^{-5}$
$H\gamma\gamma$	—	0.50	✓	—	—	—	—	—	0.06	—	—	$< 10^{-2}$
$HZ\gamma$	—	$\sim 1$	✓	—	—	—	—	—	—	—	—	$< 10^{-2}$
$Hgg$	0.12	0.011	✓	—	—	—	—	—	—	—	—	$< 10^{-2}$
$Ht\bar{t}$	0.24	0.05	✓	—	—	0.29	0.08	—	—	—	✓	$< 10^{-2}$
$H\tau\tau$	0.07	0.008	✓	0.01	0.01	0.02	0.06	—	✓	✓	✓	$< 10^{-2}$
$H\mu\mu$	—	—	—	—	—	—	—	—	—	✓	—	$< 10^{-2}$

revised numerical estimates

new dedicated studies show not enough precision

# Higgs $CP$ from EDM

- Electric Dipole Moment (EDM) of electron  $d_e < 1.1 \times 10^{-29} e \text{ cm}$
- atoms/molecules  $d_n < 1.8 \times 10^{-26} e \text{ cm}$
- $d_e^{\text{SM}} \sim 10^{-38} e \text{ cm}$



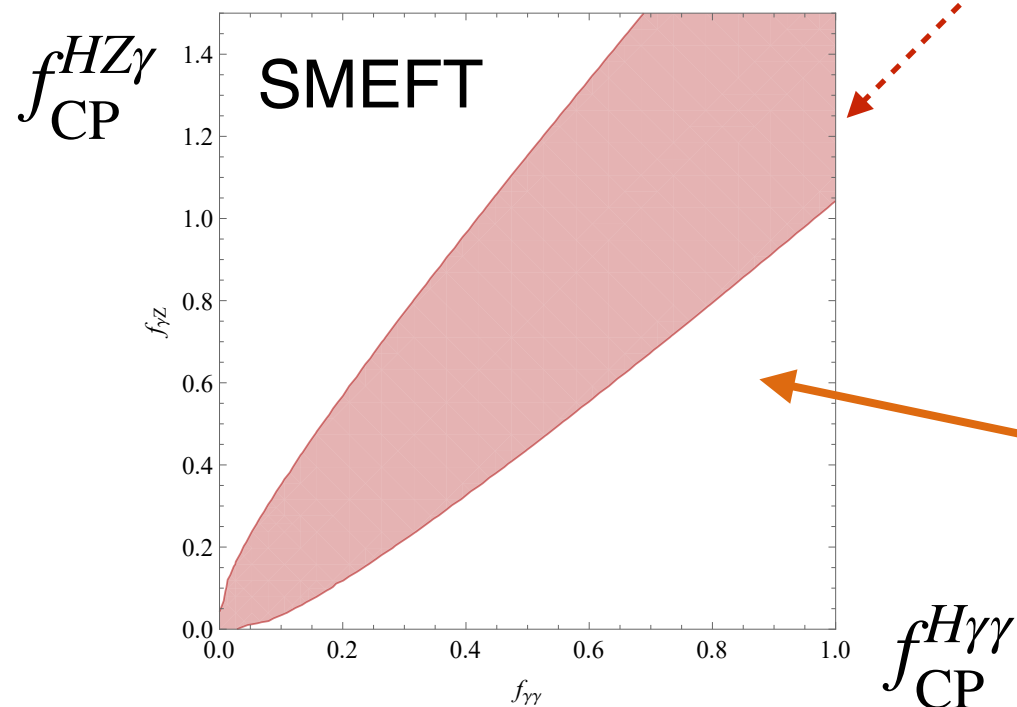
expect  $\times 10^{-2}$  in  $\sim 10$  years [arXiv:2203.08103](https://arxiv.org/abs/2203.08103)

Appendix C: EDM constraints

*Contributed by Wouter Dekens.*

$HX$ coupling	$Hgg$	$H\gamma\gamma$	$HZ\gamma$	$HZZ$	$Ht\bar{t}$	$Hu\bar{u}$	$Hdd$	$H\tau\tau$	$H\mu\mu$	$Hee$
$f_{CP}^{HX} / (1 - f_{CP}^{HX}) <$	0.12	$2.4 \cdot 10^{-8}$	$4.4 \cdot 10^{-8}$	$1.2 \cdot 10^{-13}$	$4.3 \cdot 10^{-7}$	0.72	0.039	$2.2 \cdot 10^{-2}$	36	$1.1 \cdot 10^{-6}$

only EDM



— assuming  $CP$ -even SM coupling to 1st family

— assuming one  $CP$ -odd coupling at a time

lost tight constraints with 3 couplings already

$$f_{CP}^{H\gamma\gamma}, f_{CP}^{HZ\gamma}, f_{CP}^{HZZ}$$

# Summary on Higgs $CP$

- Higgs  $CP$  is a good reference measurement for Snowmass-2022
  - Snowmass-2013 was already a good starting point
- Reached several conclusions on colliders:
  - $pp$  reach full spectrum of Higgs  $CP$ , except  $H\mu\mu$
  - $e^+e^-$  comparable to HL-LHC in Higgs  $CP$ , except  $Hgg$
  - $\gamma\gamma$  at 125 GeV + polarize unique  $CP$  in  $H\gamma\gamma$
  - $\mu^+\mu^-$  at 125 GeV + polarize unique  $CP$  in  $H\mu\mu$  (2nd family)
  - $e^-p$  allow  $CP$  in VBF
  - $pp$  at 100 TeV the furthest reach, including  $CP$  in  $HV\gamma$
- EDM constraints on Higgs  $CP$ 
  - strongest, but assuming one  $CP$ -odd coupling at a time
  - assuming  $CP$ -even SM coupling to 1st family

$HWW, HZZ$   
 $HZ\gamma, H\gamma\gamma, Hgg$   
 $Htt, H\tau\tau, H\mu\mu$