

Enabling Precision EW Measurements at High Energy e<sup>+</sup>e<sup>-</sup> Colliders with in situ Center-of-Mass Energy Measurements Report on Lol **work** to EF04

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July 20, 2022

See previous report (s) to EF04 on ILC EW potential, ICHEP2020 talk, and Lol references for more details. Results are reported in the ILC Snowmass report.

 $\mathsf{Lol} = \mathsf{SNOWMASS21}\text{-}\mathsf{EF4}\text{-}\mathsf{EF0}\text{-}\mathsf{AF3}\text{-}\mathsf{AF0}\text{-}\mathsf{IF3}\text{-}\mathsf{IF5}\text{-}\mathsf{GrahamWilson}\text{-}119$ 

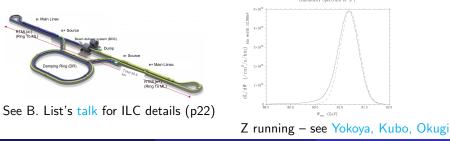
Focus is **ILC**, but relevant to any  $\rm e^+e^-$  collider. Eg.  $\rm C^3$ , HELEN, ReLiC, FCC-ee (so both linear and circular topologies).

# ILC

The ILC linear  $e^+e^-$  collider has been designed with an emphasis on an **initial-stage Higgs factory** that starts at  $\sqrt{s} = 250$  GeV and is **expandable in energy** to run at higher energies for pair production of top quarks and Higgs bosons, and potentially to 1 TeV and more.

**Particular strengths:** Longitudinally polarized electron and positron beams and higher energies. Many new measurement possibilities. Very complementary to those feasible with unpolarized & lower energy reach  $e^+e^-$  circular colliders.

The ILC is designed primarily to explore the 200 - 1000 GeV energy frontier regime. This has been the focus in making the case for the project. It is also capable of running at the **Z** and **WW** threshold.



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### Lol Questions

- An overarching question is how well can ILC running at lower √s, particularly near the Z-pole, perform statistically and systematically for measurements of PEW observables including those already explored at SLC/LEP?
- Would this offer significant advantages over only running at energies above ZH threshold?
- $\textbf{O} A related question is how such running with ILC compares statistically and systematically with other <math display="inline">e^+e^-$  collider concepts?

The circular approach now targets very high luminosity at low energy, but is therefore very large and more expensive, and if realized for  $e^+e^-$  would likely be on a longer time horizon than ILC. Also the new ReLiC linear collider concept has potential for very high luminosity too at all energies with polarized beams. For the different collider possibilities, whether one can really exploit the very large statistics and not be dominated by systematics is at the heart of these questions.

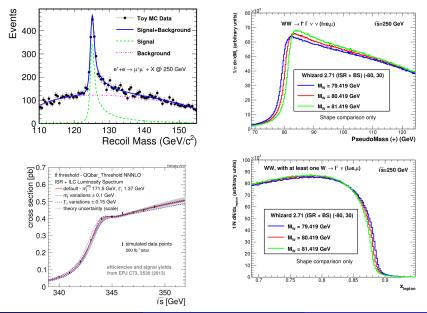
# Key Issue: Systematic control for the absolute scale of (**in collision...**) **center-of-mass energy** at **all** C-o-M energies

Studies were undertaken:

- to understand ILC capabilities for a precision measurement of the Z lineshape observables with a scan using polarized beams,
- **②** to further explore an experimental strategy for  $\sqrt{s}$  determination using di-leptons, and
- **③** to further explore  $M_{\rm W}$  capabilities synergistic with a concurrent Higgs program.

Focus of this talk: reporting progress on experimental issues associated with **center-of-mass energy** (item 2) which are a pre-requisite for getting the most out of a polarized Z scan (item 1) and underpin  $M_W$  prospects (item 3).

#### Example Physics Importance of $\sqrt{s}$ Knowledge



# ILC Physics Targets — Energy $(\sqrt{s})$ Requirements

#### Core Program

Observable	M <sub>H</sub>	$m_{ m t}$	$M_{ m W}$	M <sub>X</sub>
Method	Recoil mass	Scan	Reconstruction	Scan?
Best $\sqrt{s}$ [GeV]	250	350	250	Highest?
Current precision [MeV]	170	300	15*	-
Target precision [MeV]	10	20	2	?
$\sqrt{s}$ contribution [MeV]	3	6	0.6	?
$\sqrt{s}$ uncertainty goal [ppm]	100	200	10	100?

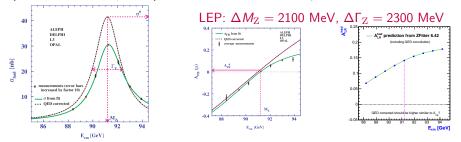
#### Ultimate Impact/Reach

Observable	$M_{ m W}$	Mz	$\Gamma_{\rm Z}$	$A_{ m LR}$
Method	Scan	Scan	Scan	Count/Scan
Best $\sqrt{s}$ [GeV]	161	91	91	91
Current precision	15**	2.1	2.3	$1.9 imes10^{-3}$
Target precision	2 MeV	0.2 MeV	0.11 MeV	$4.5 imes10^{-5}$
$\sqrt{s}$ contribution	0.8 MeV	0.2 MeV	small	$0.9 imes10^{-5}$
$\sqrt{s}$ uncertainty goal [ppm]	10	2	5**	5

\*(post CDF ...), \*\*(point-to-point most relevant)

# Polarized Beams Z Scan for Z LineShape and Asymmetries

Essentially, perform LEP/SLC-style measurements in all channels but also with  $\sqrt{s}$  dependence of the polarized asymmetries,  $A_{\text{LR}}$  and  $A_{FB,LR}^{f}$ , in addition to  $A_{FB}$ . (Also polarized  $\nu \overline{\nu} \gamma$  scan.) Not constrained to LEP-style scan points.

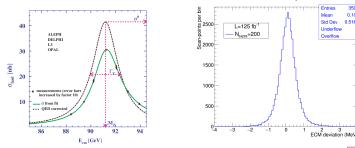


With 0.1 ab<sup>-1</sup> polarized scan around  $M_Z$ , find **statistical** uncertainties of 35 keV on  $M_Z$ , and 80 keV on  $\Gamma_Z$ , from LEP-style fit to  $(M_Z, \Gamma_Z, \sigma_{had}^0, R_e^0, R_{\mu}^0, R_{\tau}^0)$  using ZFITTER for QED convolution.

Exploiting this fully needs in-depth study of  $\sqrt{s}$  calibration systematics ILC  $\mathcal{L}$  is sufficient for  $M_Z$  to be systematics limited  $\Gamma_Z$  systematic uncertainty depends on  $\Delta(\sqrt{s}_+ - \sqrt{s}_-)$ , so expect  $\Delta\Gamma_Z \ll \Delta M_Z$ 

# Polarized Beams Z Scan for Z LineShape Study: WIP I

#### Initial line-shape study (all 4 channels). Use unpolarized cross-sections for now. ILC Z Lineshape Scan



Uses  $\sigma_{stat}/\sqrt{s}$  (%) = 0.25/ $\sqrt{N_{\mu\mu}} \oplus 0.8/\sqrt{N_{h}}$ 

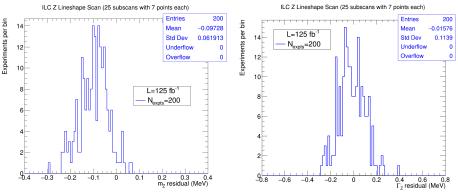
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- Scan has 7 nominal  $\sqrt{s}$  points, (peak,  $\pm \Delta$ ,  $\pm 2\Delta \pm 3\Delta$ ) with  $\Delta = 1.05$  GeV
- 25 scans of 5 fb<sup>-1</sup> per "experiment".  $7 \times 25 \times 4 = 700 \sigma_{tot}$  measurements.
- Assign luminosity per scan point in (2:1:2:1) ratio.  $(1 \text{ or } 0.5 \text{ fb}^{-1} \text{ each})$ .
- Do LEP-style fit to  $(M_Z, \Gamma_Z, \sigma_{had}^0, R_e^0, R_{\mu}^0, R_{\tau}^0)$  using ZFITTER
- Model center-of-mass energy systematics and int. lumi syst. of 0.064%.
- Each scan-point (175 per expt.) shifted from  $\sqrt{s}_{\text{nominal}}$  by a 100% correlated overall scale systematic (here +100 keV) and by stat. component driven by stat. uncertainty of  $\sqrt{s}$  measurement (typically 0.4 MeV/4.4 ppm).

# Polarized Beams Z Scan for Z LineShape Study: WIP II

Ensemble tests with 200 experiments.

Currently, fit the 700 measured cross-sections (actually occuring at shifted  $\sqrt{s}$ ) using assumed nominal  $\sqrt{s}$ . Ensemble mean  $\chi^2$  of 790 for 693 dof.



• As expected  $M_{\rm Z}$  biased down by assumed scale error (here +100 keV) with stat. error of 50–60 keV.

- $\bullet$  As expected  $\Gamma_{\rm Z}$  bias small with stat. dominated error of 100–120 keV.
- Such an experiment has 1.9B hadronic Zs.

# ILC $A_{\rm LR}$ Prospects from Z Running

Use 4 cross-section measurements ( $\sigma_{\pm\pm}$ ) to measure simultaneously:

$$m{A}_{
m LR}$$
,  $|m{P}(e^-)|$ ,  $|m{P}(e^+)|$ ,  $\sigma_u$ 

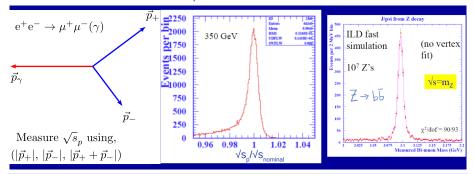
L (fb <sup>-1</sup> )	$N_Z^{ m had}$ (10 <sup>9</sup> )	$ P(e^-) $	$ P(e^+) $	$\Delta A_{ m LR}$ (stat.)	$\Delta A_{ m LR}$ (syst).
100	3.3	80%	30%	$4.3 imes10^{-5}$	$1.3 imes10^{-5}$
100	4.2	80%	60%	$2.4 imes10^{-5}$	$1.3 imes10^{-5}$
250	8.4	80%	30%	$2.7 imes10^{-5}$	$1.3 imes10^{-5}$
250	11	80%	60%	$1.5 imes10^{-5}$	$1.3 imes10^{-5}$

Estimated uncertainties on  $A_{\rm LR}$  for 4 different scenarios of Z-pole running with data-taking fractions in each helicity configuration (-+), (+-), (--), (++) chosen to minimize the statistical uncertainty on the asymmetry. The quoted statistical uncertainty includes Bhabha statistics for relative luminosity and Compton statistics for polarization differences. The systematic uncertainty assumes 5 ppm uncertainty on the absolute center-of-mass energy and a 1% understanding of beamstrahlung effects. Estimates assume data taken at a single center-of-mass energy (91.2 GeV).

Total uncertainty on  $A_{\rm LR}$  of  $4.5 \times 10^{-5}$  (scenario 1) to  $2.0 \times 10^{-5}$  (scenario 4). Corresponds to uncertainty on  $\sin^2 \theta_{\rm eff}^{\ell}$  of  $5.6 \times 10^{-6}$  (1) to  $2.5 \times 10^{-6}$  (4).

# $\sqrt{s}_p$ Method for Center-of-Mass Energy

#### Use dilepton momenta, with $\sqrt{s}_{p} \equiv E_{+} + E_{-} + |\vec{p}_{+-}|$ as $\sqrt{s}$ estimator.



Tie detector *p*-scale to particle masses (know  $J/\psi$ ,  $\pi^+$ , p to 1.9, 1.3, 0.006 ppm)

Measure  $<\sqrt{s}>$  and luminosity spectrum with same events. Expect statistical uncertainty of 1.0 ppm on *p*-scale per 1.2M  $J/\psi \rightarrow \mu^+\mu^-$  (4 × 10<sup>9</sup> hadronic Z's).

• excellent tracker momentum resolution - can resolve beam energy spread. • feasible for  $\mu^+\mu^-$  and  $e^+e^-$  (and ... 4l etc).

#### Introduction to Center-of-Mass Energy Issues

- Proposed  $\sqrt{s}_p$  method uses only the momenta of leptons in dilepton events.
- Critical issue for  $\sqrt{s_p}$  method: calibrating the tracker momentum scale.
- Can use  ${
  m K}^0_{
  m S}$ , A,  $J/\psi 
  ightarrow \mu^+\mu^-$  (mass known to 1.9 ppm).

For more details see studies of  $\sqrt{s_p}$  from ECFA LC2013, and of momentum-scale from AWLC 2014. Recent  $K_S^0$ ,  $\Lambda$  studies at LCWS 2021 – much higher precision feasible ... few **ppm** (not limited by parent mass knowledge or  $J/\psi$  statistics). More in depth talks on  $\sqrt{s}$ : ILC physics seminar and ILC MDI/BDS/Physics talk

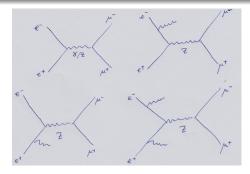
#### Today,

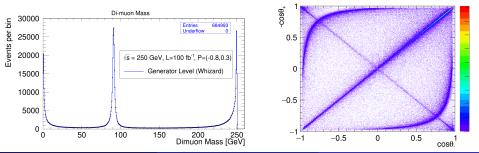
- Overview of the  $\sqrt{s_p}$  method prospects with  $\mu^+\mu^-$
- Brief overview of the "new" concept in recent tracker momentum scale studies (LCWS2021 talk).
- Bonus. Physics:  $M_Z$ . Beam knowledge: luminosity spectrum,  $dL/d\sqrt{s}$ .

#### Dimuons

Three main kinematic regimes.

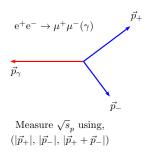
- Low mass,  $m_{\mu\mu} < 50$  GeV
- Medium mass, 50 < m<sub>µµ</sub> < 150 GeV</li>
- High mass,  $m_{\mu\mu} > 150$  GeV
  - Back-to-back events in the full energy peak.
  - Significant radiative return (ISR) to the Z and to low mass.





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# $\sqrt{s}_p$ Method in a Nutshell



Assuming,

- Equal beam energies,  $E_{\rm b}$
- The lab is the CM frame,  $(\sqrt{s} = 2 E_{\rm b}, \sum \vec{p_i} = 0)$
- The system recoiling against the dimuon is **massless**

$$\sqrt{s} = \sqrt{s}_p \equiv E_+ + E_- + |\vec{p}_+ + \vec{p}_-|$$

$$\sqrt{s}_{p} = \sqrt{p_{+}^{2} + m_{\mu}^{2}} + \sqrt{p_{-}^{2} + m_{\mu}^{2}} + |ec{p}_{+} + ec{p}_{-}|$$

#### An estimate of $\sqrt{s}$ using only the (precisely measurable) muon momenta

[Now,  $\sqrt{s}$  estimators previously extended to allow beam energy difference and crossing angle are extended to the general case with a massive recoil. Work in progress on applying constrained fits]

#### New approach to tracker momentum scale

See LCWS2021 talk for details. Use Armenteros-Podolanski kinematic construction for 2-body decays (AP).

- Explore AP method using mainly  $K_S^0 \to \pi^+\pi^-$ ,  $\Lambda \to p\pi^-$  (inspired by Rodríguez et al.). Much higher statistics than  $J/\psi$  alone.
- **(2)** If proven realistic, **enables precision Z program** (polarized lineshape scan)

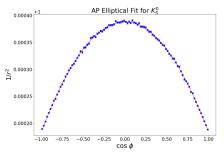
• Bonus: potential for large improvement in parent and child particle masses For a "V-decay",  $M^0 \rightarrow m_1^+ m_2^-$ , decompose the child particle lab momenta into components transverse and parallel to the parent momentum. The distribution of (child  $p_T$ ,  $\alpha \equiv \frac{p_L^+ - p_L^-}{p_L^+ + p_L^-}$ ) is a semi-ellipse with parameters relating the CM decay angle,  $\theta^*$ ,  $\beta$ , and the masses,  $(M, m_1, m_2)$ , that determine,  $p^*$ .

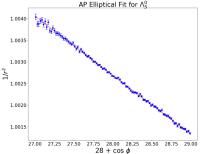
By obtaining sensitivity to both the parent and child masses, and positing improving ourselves the measurements of more ubiquitous parents ( $\rm K_S^0$  and  $\Lambda$ ), can obtain high sensitivity to the momentum scale

Proving the feasibility of sub-10 ppm momentum-scale uncertainty needs much work when typical existing experiments are at best at the 100 ppm level

#### Tracker momentum scale sensitivity estimate

Used sample of 250M hadronic Z's at  $\sqrt{s}=91.2$  GeV. Fit  $\rm K^0_S,\Lambda,\overline{\Lambda}$  in various momentum bins.





- Image: 0.48 ppm
- 2 m<sub>Λ</sub>: 0.072 ppm

m<sub>π</sub>: 0.46 ppm

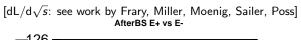
S<sub>p</sub>: 0.57 ppm

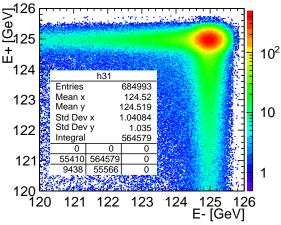
- Fit fixes proton mass
- Factors of (54, 75, 3) improvement over PDG for  $(K^0_S, \Lambda/\overline{\Lambda}, \pi^{\pm})$
- Momentum-scale to 2.5 ppm stat. per 10M hadronic Z, ILC Z run may have 400 such samples.

#### What do we really want to measure?

Ideally, the 2-d distribution of the absolute beam energies after beamstrahlung. From this we would know the distribution of both  $\sqrt{s}$  and the initial state momentum vector (especially the z component).

Now let's look at the related 1-d distributions  $(E_+, E_-, \sqrt{s}, p_z)$ with empirical fits.

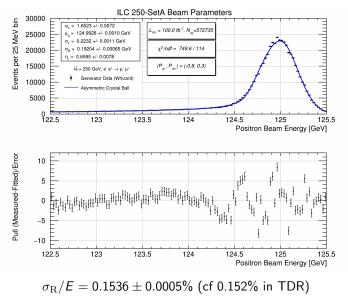




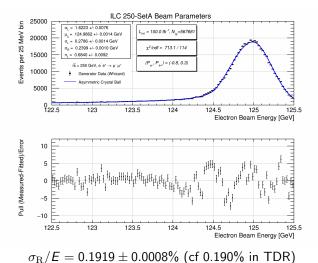
Whizard 250 GeV SetA  $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$  events

# Positron Beam Energy (After Beamstrahlung)

#### Initial fits used asymmetric Crystal Ball with 5 parameters.

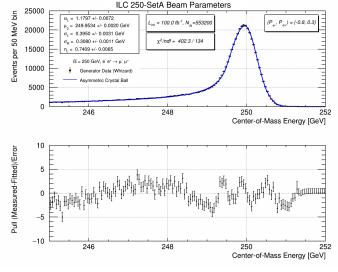


### Electron Beam Energy (After Beamstrahlung)



Note an undulator bypass could reduce this spread when one  $e^-$  cycle is used purely for  $e^+$  production.

### Center-of-Mass Energy (After Beamstrahlung)

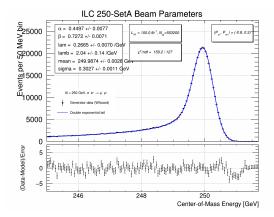


 $\sigma_{
m R}/\sqrt{s} = 0.1232 \pm 0.0004\%$  (cf 0.122% in TDR ( 0.190%  $\oplus$  0.152%)/2)

### Center-of-Mass Energy (After Beamstrahlung)

New analytical convolution fit (5 shape parameters): Use Eqn 9 from J-H. Cheng et al, arXiv:1603.04433.

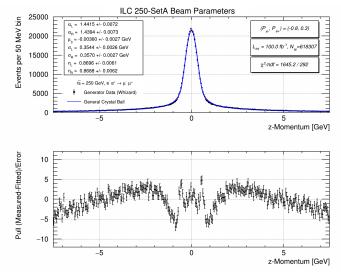
 $(\delta$ -function fraction $(\alpha)$  + double exponential tail), convolved with Gaussian



 $\sigma/\sqrt{s} = 0.1211 \pm 0.0004\%$  (cf 0.122% in TDR ( 0.190%  $\oplus$  0.152%)/2)

This fit is preferable to the asymmetric CB.

# z-Momentum of e<sup>+</sup>e<sup>-</sup> system (After Beamstrahlung)



 $\sigma/\sqrt{s} = 0.1416 \pm 0.0007\%$  (cf 0.122% from beam energy spread alone)

### Initial State Kinematics with Crossing Angle

Define the two beam energies (after beamstrahlung) as  $E_{\rm b}^-$  and  $E_{\rm b}^+$  for the electron beam and positron beam respectively.

Initial-state energy-momentum 4-vector (neglecting  $m_{\rm e}$ )

$$E = E_{\rm b}^- + E_{\rm b}^+$$

$$p_{\rm x} = (E_{\rm b}^- + E_{\rm b}^+)\sin(\alpha/2)$$

$$p_{\rm y} = 0$$

$$p_{\rm z} = (E_{\rm b}^- - E_{\rm b}^+)\cos(\alpha/2)$$

The corresponding center-of-mass energy is

$$\sqrt{s} = 2\sqrt{E_{\mathrm{b}}^{-}E_{\mathrm{b}}^{+}}\cos\left(lpha/2
ight)$$

Hence if  $\alpha$  is known (14 mrad for ILC), evaluation of the collision center-of-mass energy amounts to measuring the two beam energies. Introducing,

$$E_{
m ave} \equiv rac{E_{
m b}^- + E_{
m b}^+}{2} \ , \overline{\Delta E_{
m b}} \equiv rac{E_{
m b}^- - E_{
m b}^+}{2}$$

then with this notation,

$$\sqrt{s} = 2\sqrt{E_{
m ave}^2 - (\overline{\Delta E_{
m b}})^2}\cos{(lpha/2)}$$

### Final State Kinematics and Equating to Initial State

Let's look at the final state of the  $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$  process. Denote the  $\mu^+$  as particle 1, the  $\mu^-$  as particle 2, and the rest-of-the event (RoE) as system 3. We can write this final-state system 4-vector as

$$(E_1 + E_2 + E_3, \ \vec{p_1} + \vec{p_2} + \vec{p_3})$$

Applying  $(E, \vec{p})$  conservation we obtain,

$$E_1 + E_2 + \sqrt{p_3^2 + M_3^2} = 2 E_{\text{ave}}$$
 (1)

$$\vec{p_1} + \vec{p_2} + \vec{p_3} = (2 \ E_{\text{ave}} \sin(\alpha/2), 0, 2 \ \overline{\Delta E_{\text{b}}} \cos(\alpha/2)) \equiv \vec{p_{\text{initial}}}$$
(2)

The RoE is often not fully detected and needs to be inferred using  $(E, \vec{p})$  conservation. We have 4 equations and 6 unknowns:

the 3 components of the RoE momentum  $(\vec{p}_3)$ ,  $E_{\rm ave}$ ,  $\overline{\Delta E_{\rm b}}$ , and  $M_3$ . **Our approach is to solve for**  $E_{\rm ave}$  **for various assumptions on**  $(\overline{\Delta E_{\rm b}}, M_3)$ . Specifically we then focus on using the simplifying assumptions of the original  $\sqrt{s_p}$  method that  $M_3 = 0$  and  $\overline{\Delta E_{\rm b}} = 0$ . Note: latter is often a poor assumption for the  $p_z$  conservation component on an event-to-event basis.

# The Averaged Beam Energy Quadratic

This approach results in a quadratic equation in  $E_{\text{ave}}$ ,  $(AE_{\text{ave}}^2 + BE_{\text{ave}} + C = 0)$ , with coefficients of

$$A = \cos^2(\alpha/2)$$
$$B = -E_{12} + p_{12}^x \sin(\alpha/2)$$
$$C = (M_{12}^2 - M_3^2)/4 + p_{12}^z \overline{\Delta E_b} \cos(\alpha/2) - \overline{\Delta E_b}^2 \cos^2(\alpha/2)$$

Based on this, there are a number of cases of interest to solve for  $E_{\text{ave}}$ :

• Zero crossing angle, 
$$\alpha = 0$$
,  $\overline{\Delta E_{\rm b}} = 0$ ,  $M_3 = 0$ .

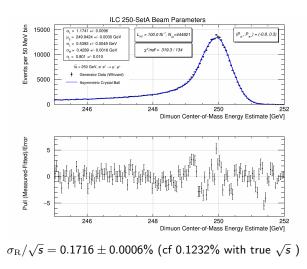
2 Crossing angle and 
$$\overline{\Delta E_{\rm b}} = 0$$
,  $M_3 = 0$ .

• Crossing angle and  $\overline{\Delta E_{\rm b}}$  non-zero,  $M_3 = 0$ .

- Crossing angle and  $M_3$  non-zero,  $\overline{\Delta E_{\rm b}} = 0$ .
- Crossing angle and  $\overline{\Delta E_{\rm b}}$  and  $M_3$  non-zero.

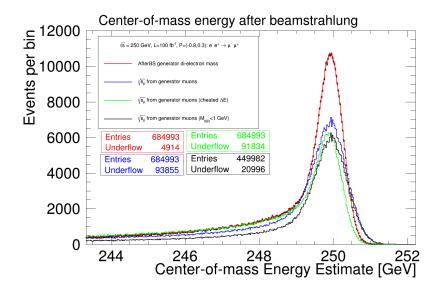
The original formula,  $\sqrt{s} = E_1 + E_2 + |\vec{p}_{12}|$ , arises trivially in the first case. In the rest of this talk the  $\sqrt{s}$  estimate from the largest positive solution of the second case is what I now mean by  $\sqrt{s}_p$ . Obviously it is also a purely muon momentum dependent quantity.

# Dimuon Estimate of Center-of-Mass Energy (After BS)



- This is the generator-level  $\sqrt{s_p}$  calculated from the 2 muons
- Why so broad? Why fewer events?
- Because some events violate the assumptions that  $\overline{\Delta E_{\rm b}} = 0$  and  $M_3 = 0$
- The former is no surprise given the *p<sub>z</sub>* distribution
- The latter is associated with events with 2 or more non-collinear ISR/FSR photons

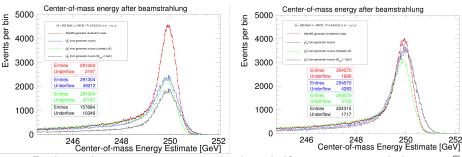
# Comparisons (After BS)



# What's Going On?

 $50 < m_{\mu\mu}^{
m gen} < 150~{
m GeV}$ 

 $m^{
m gen}_{\mu\mu} > 150 \,\, {
m GeV}$ 

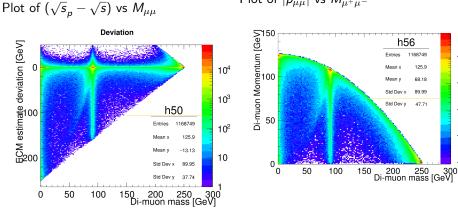


- For lower dimuon mass events, only about half are reconstructed close to  $\sqrt{s}$
- Most higher dimuon mass events reconstructed close to the original  $\sqrt{s}$

#### Conclusion

Lower dimuon mass events are more likely to violate the assumptions.

### 2d Generator Level Plots



Most events consistent with  $M_3 \approx 0$ 

Plot of  $|p_{\mu\mu}|$  vs  $M_{\mu^+\mu^-}$ 

In most events,  $\sqrt{s_p}$ , is a reasonable estimator. But also can be off by a lot. WIP on identifying problematic events (eg. kinematic fits). It may be feasible to find alternative estimators/methods in those cases, or at least reject them.

 $10^{4}$ 

 $10^{3}$ 

 $10^{2}$ 

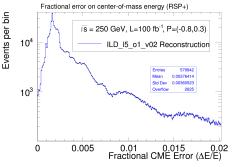
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### Event Selection Requirements

Currently rather simple.

Use latest full ILD simulation/reconstruction at 250 GeV.

- Require exactly two identified muons
- Opposite sign pair
- Require uncertainty on estimated  $\sqrt{s}_p$  of the event of less than 0.8% based on propagating track-based error matrices
- Categorize reconstruction quality as gold (<0.15%), silver ([0.15, 0.30]%), bronze ([0.30, 0.80]%)
- $\bullet\,$  Require the two muons pass a vertex fit with p-value >1 %



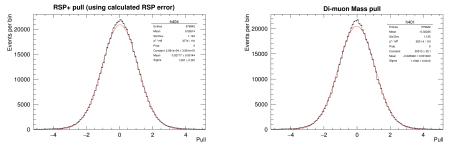
Selection efficiencies for (80%/30%) beam polarizations:

- $\varepsilon_{-+} = 69.77 \pm 0.06$  %
- $\varepsilon_{+-} = 67.35 \pm 0.06$  %
- $\varepsilon_{--}=69.47\pm0.05$  %
- $\varepsilon_{++} = 67.72 \pm 0.06$  %

Backgrounds not yet studied in detail,  $(\tau^+\tau^- \text{ is small:} 0.15\%, \text{ of no import for the } \sqrt{s} \text{ peak region}).$ 

### **Dimuon Pull Distributions**

- Pull  $\equiv$  (meas true)/error.
- Track-based estimates of the errors on both the  $\sqrt{s_p}$  quantity (left) and the di-muon mass (right) agree well with the modeled uncertainties for reconstructed dimuon events.



- In both cases the fitted rms over this range is about 10% larger than ideal. Central range well described. Suspect tails should be non-Gaussian given the non-Gaussian tails of multiple scattering.
- In practice this is rather encouraging

### Vertex Fit: Exploit ILC nanobeams

Given that the track errors are well modeled and the 2 muons should originate from a common vertex consistent with the interaction point, we can perform:

- Vertex Fit: Constrain the two tracks to a common point in 3-d
- Beam-spot Constrained Vertex Fit

The ILC beam-spot size is  $(\sigma_x,\sigma_y)=(515,7.7)$  nm,  $\sigma_z=0.202$  mm

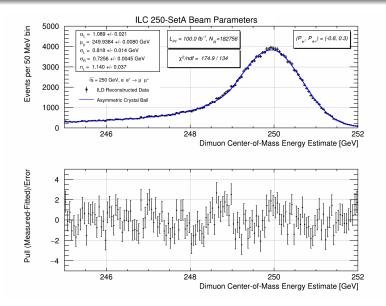
- Vertex fit along same lines as AWLC2014 talk has been re-implemented using the fully simulated data
- Also have explored beam-spot constraints

What good is this?

- Residual background rejection (eg.  $\tau^+\tau^-$  reduced by factor of 20)
- Additional handle for rejecting or deweighting mis-measured events
- Some modest improvement in precision of di-muon kinematic quantities
- $\bullet$  Also useful for  ${\rm H} \to \mu^+ \mu^-$  and for ZH recoil
- Interaction point measurement ( $O(1\mu m)$  resolution per event) can be used to correlate with ( $E_-, E_+$ ) for understanding beamstrahlung

Note: simulated data does not currently simulate the transverse beam-spot ellipse nor the beam energy- $z_{\rm vtx}$  correlations.

# Example: Silver Quality Dimuon PFOs (After BS)



Gold and bronze quality fits are in the backup slides.

# Strategy for Absolute $\sqrt{s}$ and Estimate of Precision

#### **Prior Estimation Method**

• Guesstimate how well the peak position of the Gaussian can be measured using the observed  $\sqrt{s}_p$  distributions in bins of fractional error

#### **Current Thinking**

- The luminosity spectrum and absolute center-of-mass energy are the same problem or at least very related. How well one can determine the absolute scale depends on knowledge of the shape (input also from Bhabhas).
- Beam energy spread likely to be well constrained by spectrometer data
- Likely need either a convolution fit (CF) or a reweighting fit
- Work is in progress on a CF by parametrizing the underlying  $(E_-, E_+)$  distribution, and modeling quantities related to  $\sqrt{s}$  and  $p_z$  after convolving with detector resolution (and ISR, FSR and cross-section effects)

#### **Current Estimation Method**

- Use estimates of the statistical error on  $\mu_0$  for 5-parameter Crystal Ball fits to fully simulated data with the 4 shape parameters fixed to their best fit values.
- Fits are done in the 3 resolution categories.
- Next slide has these estimates

$L_{ m int}$ [ab <sup>-1</sup> ]	Poln [%]	Gold	Silver	Bronze	G+S+B
0.9	-80, +30	6.5	3.1	8.5	2.7
0.9	+80, -30	7.7	3.4	9.6	3.0
0.1	-80, -30	26	12.1	33	10.4
0.1	+80, +30	29	13.0	41	11.4
2.0	—	4.8	2.2	6.2	1.9

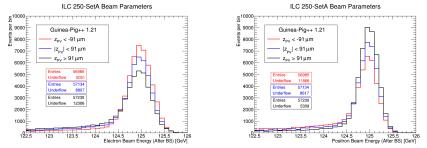
Fractional errors on  $\mu_0$  parameter (mode of peak) when fitting with 5-parameter Crystal Ball function with all 4 shape parameters fixed to their best-fit values.

Also the  $e^+e^-$  channel should be used. The additional benefit of the much larger statistics from more forward Bhabhas is offset by the poorer track momentum resolution at forward angles.

# Beamstrahlung / z-Vertex Effects Explained

Divide interactions in 3 equi-probability parts according to  $z_{PV}$ . Preferentially

- **0**  $e^+e^-$  collisions occurring more on the initial  $e^-$  side (z < 0)
- 2  $e^+e^-$  collisions mostly central
- **③**  $e^+e^-$  collisions preferentially on the initial  $e^+$  side (z > 0)

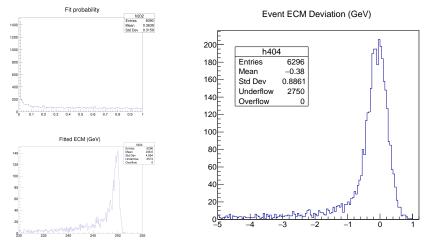


The beamstrahlung tail grows and the peak shrinks for  $e^-$  as z increases, and, for  $e^+$  as z decreases. In both cases, the largest beamstrahlung tail occurs when the interacting  $e^-$  or  $e^+$  has on average traversed more of the opposing bunch.

Thus both  $\sqrt{s}$  and  $p_z = E_- - E_+$  distributions depend on z. Likely needs to be taken into account for  $\sqrt{s}$ ,  $dL/d\sqrt{s}$ , Higgs recoil, kinematic fits ...

## Kinematic Fit Approach: Hot Off The Press

Test whether events consistent with  $e^+e^- \rightarrow \mu^+\mu^-$  (with no photons) by fitting for  $E_{ave}$  and  $\overline{\Delta E_b}$  as unmeasured parameters. (4C/2U/2dof)



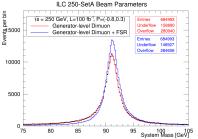
Plots require  $p_{\rm fit} > 0.05$  (26% of all events). See backup for details. Use 0.15% momentum resolution. Peak width is 0.3 GeV (same as energy spread).

## Measuring $M_Z$ using $m_{\mu^+\mu^-}$ with high energy running

Look at  $\sqrt{s} = 250$  GeV running with latest beam parameters and full simulation

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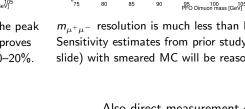
2000

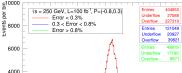


Adding in FSR photon(s) reduces the peak width to be consistent with  $\Gamma_{Z}$ . Improves statistical sensitivity on mode by 10-20%.

Main systematics:

- momentum-scale
- In FSR modeling/treatment
- Electron *p*-scale in the  $e^+e^-$  channel





ILC 250-SetA Beam Parameters

 $m_{\mu^+\mu^-}$  resolution is much less than  $\Gamma_{\rm Z}$ . Sensitivity estimates from prior study (next slide) with smeared MC will be reasonable.

#### Also direct measurement of $\Gamma_{\rm Z}$ ?

## Measuring $M_{\rm Z}$ from $m_{\mu^+\mu^-}$

Revisited old study of  $\sqrt{s_p}$  at  $\sqrt{s} = 250$ , 350, 500, 1000 GeV. Used smeared MC. Fitted  $m_{\mu^+\mu^-} \in [75, 105]$  GeV with sum of two Voigtians. Statistical uncertainties on the peak parameter,  $M_Z$ , scaled to full ILC program using simulations with TDR beam parameters

Statis	tical uncerta	ainties for $\mu^+\mu^-$ channel				
	$\sqrt{s}$ [GeV]	$L_{ m int}$ [ab $^{-1}$ ]	Poln [%]	Sharing [%]	$\Delta M_{ m Z}$ [MeV]	
	250	2.0	80/30	(45,45,5,5)	1.20	
	350	0.2	80/30	(67.5,22.5,5,5)	5.99	
	500	4.0	80/30	(40,40,10,10)	2.55	
	1000	8.0	80/20	(40,40,10,10)	5.75	
	All	14.2	_	_	1.05	

- Current PDG uncertainty on  $M_{\rm Z}$  is 2.1 MeV
- FSR makes effective Breit-Wigner width larger and shifts the peak
- $\bullet\,$  Treatment of FSR and especially inclusion of  $e^+e^-$  channel should decrease stat. uncertainty to 0.7 MeV
- Sensitivity dominated by  $\sqrt{s}=250~{\rm GeV}$  running
- Main systematic tracker p-scale. Target at most 2.5 ppm in this context.

## **Concluding Remarks**

Lol had 3 main thrusts

- New study on **polarized Z-scan**. While anchored in old studies of "Giga-Z" much broader in scope and ambition. Potential measurement of  $\sin^2 \theta_{\rm eff}^{\ell}$  to  $2.5 \times 10^{-6}$  using  $A_{\rm LR}$ .
- Further exploration based on existing studies of center-of-mass energy calibration using di-leptons. Significant progress in this area.
- Further exploration based on existing studies and LEP2-style W mass measurements using WW production. Much room for additional work and collaboration. See also recent talk with focus on M<sub>W</sub>.

In all cases welcome further collaboration.

- $\bullet\,$  KU graduate student, Justin Anguiano, worked on some of the WW aspects of  $M_{\rm W}$  2011.12451
- Collaborating with others including Jenny List and Michael Peskin.
- KU graduate student, Brendon Madison, has been working on several aspects of the center-of-mass energy studies.

### Progress

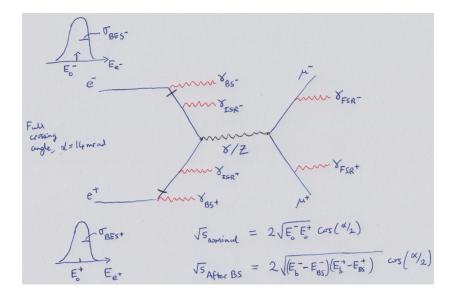
- New high precision method for momentum-scale using especially  ${\rm K}^0_{\rm S}$  and A. Promises 2.5 ppm uncertainty per 10M hadronic Zs.
- $\bullet\,$  More detailed investigation of dimuons for  $\sqrt{s}$  and  $dL/d\sqrt{s}$  reconstruction
- Measurement of  $M_{\rm Z}$  using dimuon mass for  $\sqrt{s}\gg M_{\rm Z}$  to 1.0 MeV dominated by  $\sqrt{s}=250~{\rm GeV}$  data

### Conclusions

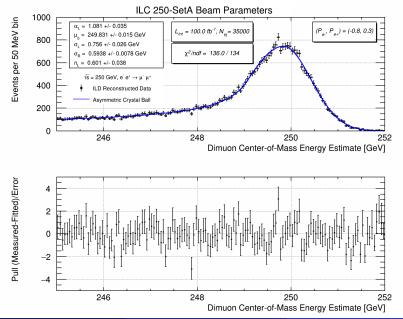
- Tracking detectors designed for ILC have the potential to measure beam energy related quantities with precision similar to the intrinsic energy spread using dimuon events (and also wide-angle Bhabha events)
- At  $\sqrt{s} = 250$  GeV, dimuon estimate of 2 ppm precision on  $\sqrt{s}$ . More than sufficient (10 ppm needed) to not limit measurements such as  $M_{\rm W}$ .
- $\bullet\,$  Potential to improve  $M_{\rm Z}$  by a factor of three using 250 GeV di-lepton data
- Applying the same  $\sqrt{s}$  techniques to running at the Z-pole enables a high precision electroweak measurement program for ILC that takes advantage of absolute center-of-mass energy scale knowledge

# Backup Slides

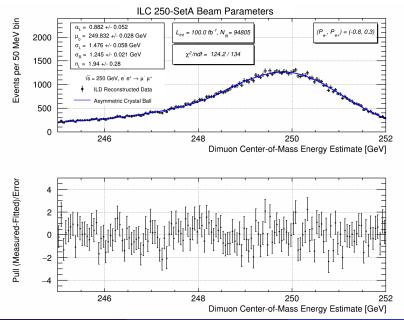
# Returning to $\sqrt{s_p}$ and Adding More Realism



## Gold Quality Dimuon PFOs (After BS)

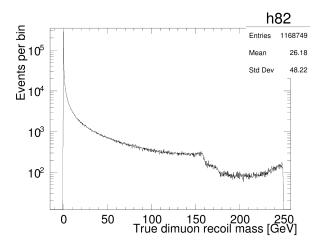


## Bronze Quality Dimuon PFOs (After BS)



## Recoil Mass (at generator level)

Distribution of  $M_3$ .



Events in the tails will be from multiple non-collinear radiation (example ISR from both beams)

Graham W. Wilson (University of Kansas)

## Kinematic Fits for $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$

Inspired by revisiting some of the LEP2 techniques for  $M_{\rm W}$  measurement, one can also cast the whole problem as a constrained fit problem. Promises to be very useful in event selection, hypothesis identification, and parameter measurement, but needs excellent object calibration and measurement uncertainties.

#### Two body fits

Test the hypothesis of  $e^+e^- \rightarrow \mu^+\mu^-$  with no additional photons.

- Specify  $E_{\rm ave}$  and  $\overline{\Delta E_{\rm b}}$  and fit with the 4 constraints of (E,p) conservation. (4C/4dof fit)
- **2** \* Fit for  $E_{\rm ave}$  and  $\overline{\Delta E_{\rm b}}$  as unmeasured fit parameters with the 4 constraints. (4C/2U/2dof fit).

Initial test implementation uses easily adaptable constrained fitting code of V. Blobel with toy MC based smearing and uncertainties.

- Find 10.7% of events satisfy the 2-body hypothesis ( $p_{\rm fit} > 0.01$ ) IF the correct  $E_{\rm ave}$  and  $\overline{\Delta E_{\rm b}}$  are specified (Fit 1). For these events,  $M_{\mu\mu}$  is synonymous with  $\sqrt{s}$ .
- Solution Find 26% of events satisfy fit 2 ( $p_{\rm fit} > 0.05$ ). Note often the fitted  $\sqrt{s}$  is near  $M_Z$  ... with large  $|\overline{\Delta E_{\rm b}}|$ .

#### Three particle collinear ISR fits

Test the  $e^+e^- \rightarrow \mu^+\mu^-\gamma$  hypothesis where the  $\gamma$  is an undetected ISR photon collinear with one of the beams with z-hemisphere signed energy,  $E_{\rm ISR}$ .

- Specify  $E_{\text{ave}}$ ,  $\overline{\Delta E_{\text{b}}}$ ,  $E_{\text{ISR}}$  and fit with 4 constraints. (4C/4dof fit)
- Specify E<sub>ave</sub> and <u>AE<sub>b</sub></u>. Fit E<sub>ISR</sub> as unmeasured parameter and fit with 4 constraints. (4C/1U/3dof fit)
- Fit for  $E_{\text{ave}}$ ,  $\overline{\Delta E_{\text{b}}}$ ,  $E_{\text{ISR}}$  as unmeasured fit parameters with the 4 constraints. (4C/3U/1dof fit).