

arXiv:1912.08403

arXiv:2203.07668

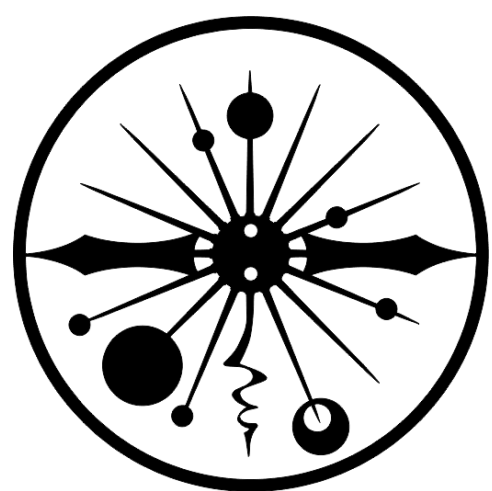
# Measuring the tau polarisation at ILC

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# Motivation

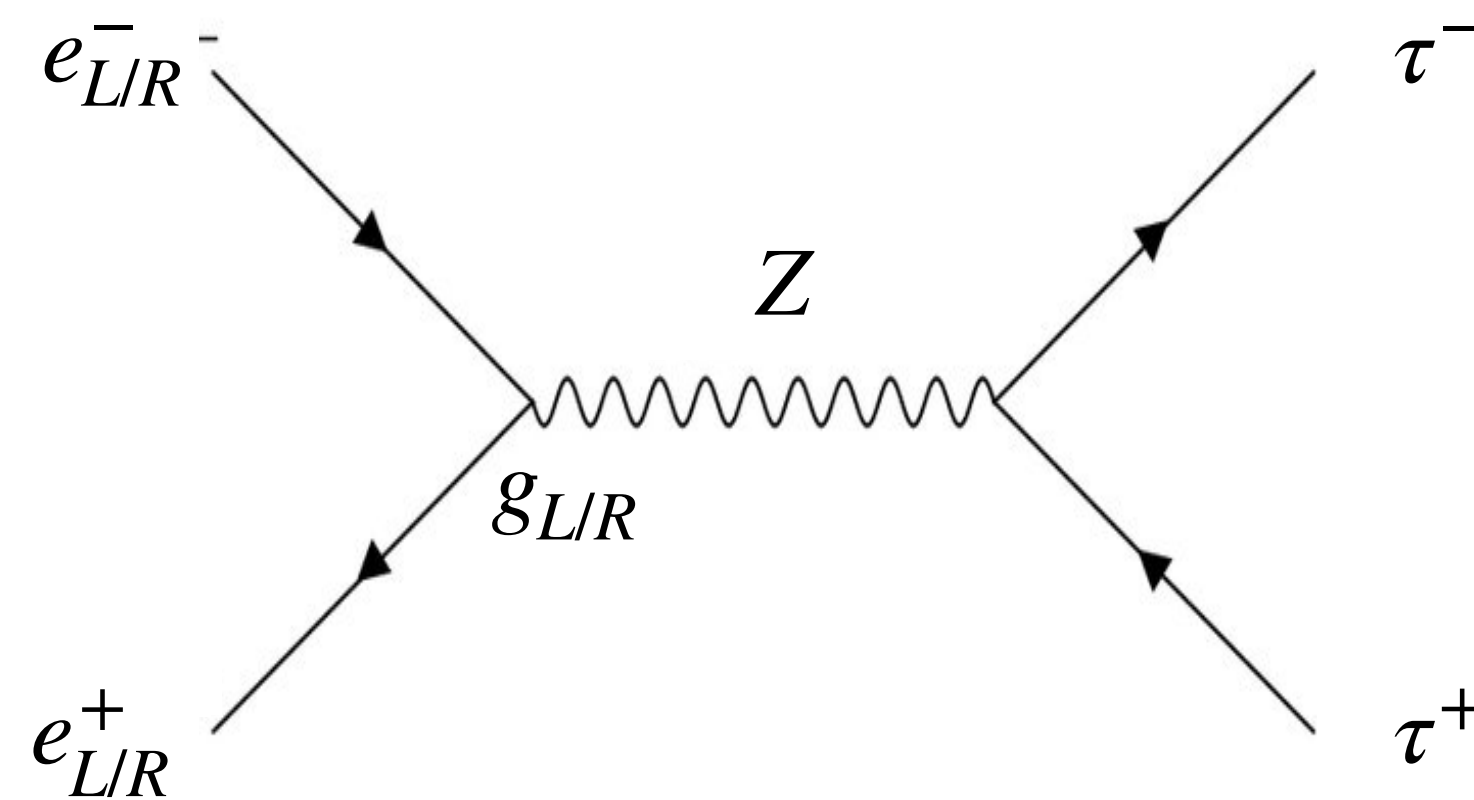
At the ILC, forward-backward asymmetry  $A_{FB} = \frac{3}{4} A_e \cdot A_f$  can be measured

Thanks to ILC's polarised beams,  $A_e$  can be measured  $\Rightarrow A_f$  can be extracted from  $A_{FB}$

By measuring  $A_{FB}$  precisely and looking for deviations from SM predictions, it is possible to search for new physics, such as heavy gauge boson  $Z'$

We can also directly measure  $A_\tau$  by using tau polarisation  $P(\tau)$

$$\frac{dP(\tau)}{d \cos \theta} = \frac{3}{8} A_\tau (1 + \cos^2 \theta) + \frac{3}{4} A_e \cos \theta$$



The aim of this study

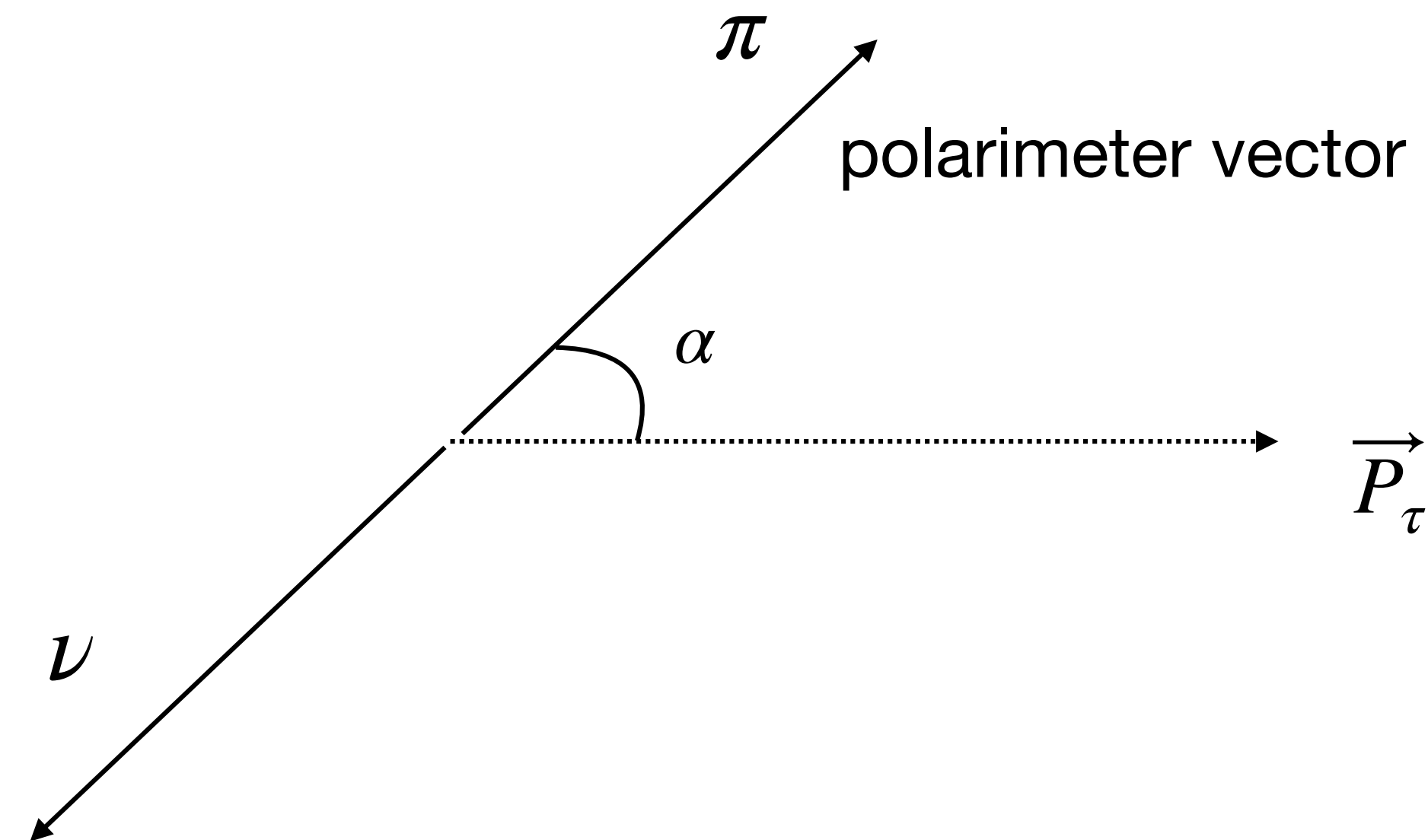
The reconstruction of tau spin orientation (“**Polarimeter**”) in order to measure polarisation to investigate new physics.

# Polarimeter

Reconstruction of tau polarisation  $P(\tau)$  depends on tau decay mode.

Polarimeter vectors of  $\tau \rightarrow \pi \nu$  in  $\tau$  rest frame

$$h(\tau^\pm \rightarrow \pi^\pm \nu) \propto p_{\pi^\pm}$$



Polarimeter vectors of  $\tau \rightarrow \rho \nu$  in  $\tau$  rest frame

$$h(\tau^\pm \rightarrow \pi^\pm \pi^0 \nu) \propto m_\tau (E_{\pi^\pm} - E_{\pi^0}) (p_{\pi^\pm} - p_{\pi^0}) + \frac{1}{2} (p_{\pi^\pm} + p_{\pi^0})^2 p_\nu$$

**“Polarimeter”**

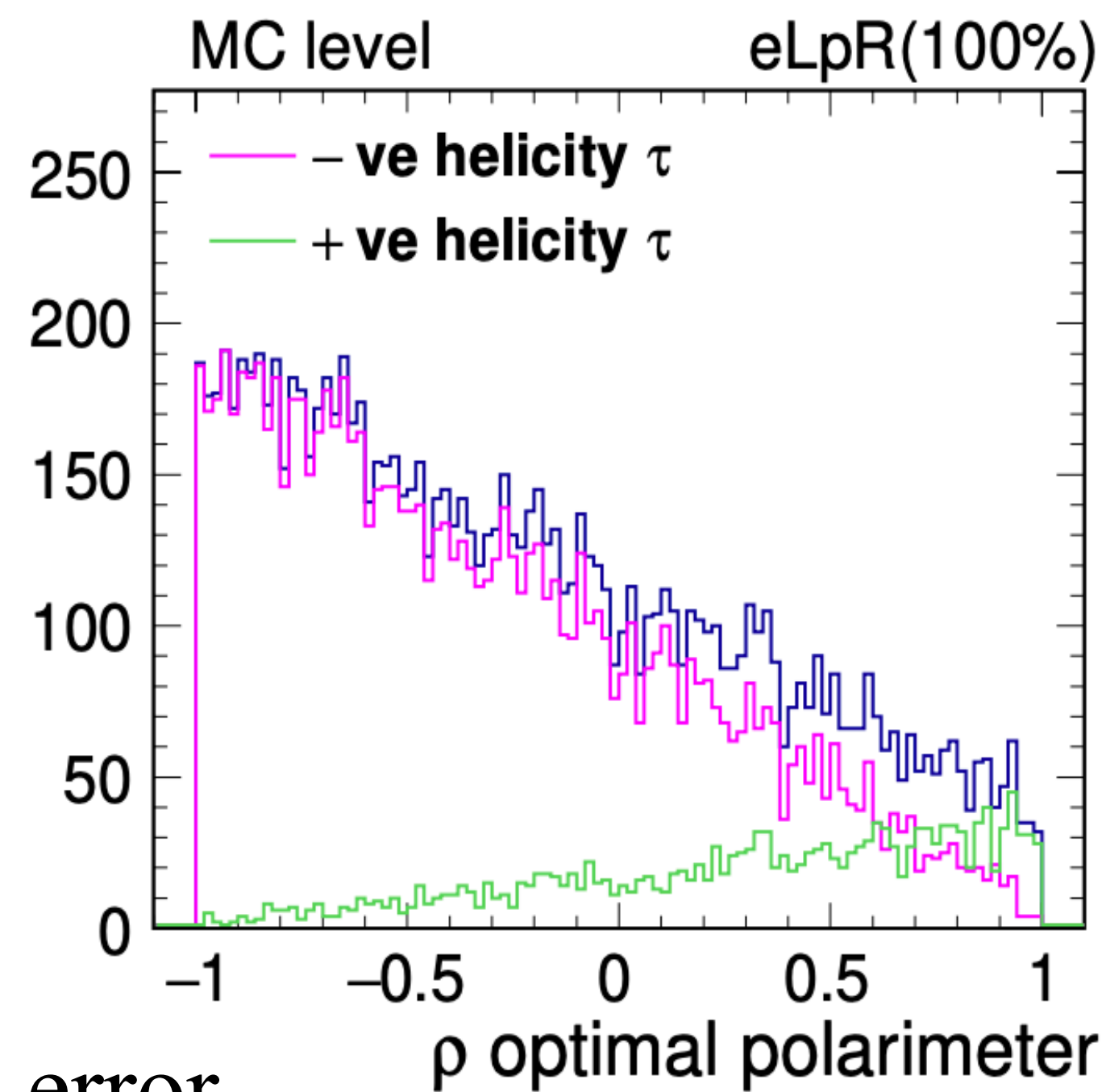
The cosine of the angle this polarimeter vector makes to the tau flight direction

# Previous study

Extract polarimeter without using neutrino information

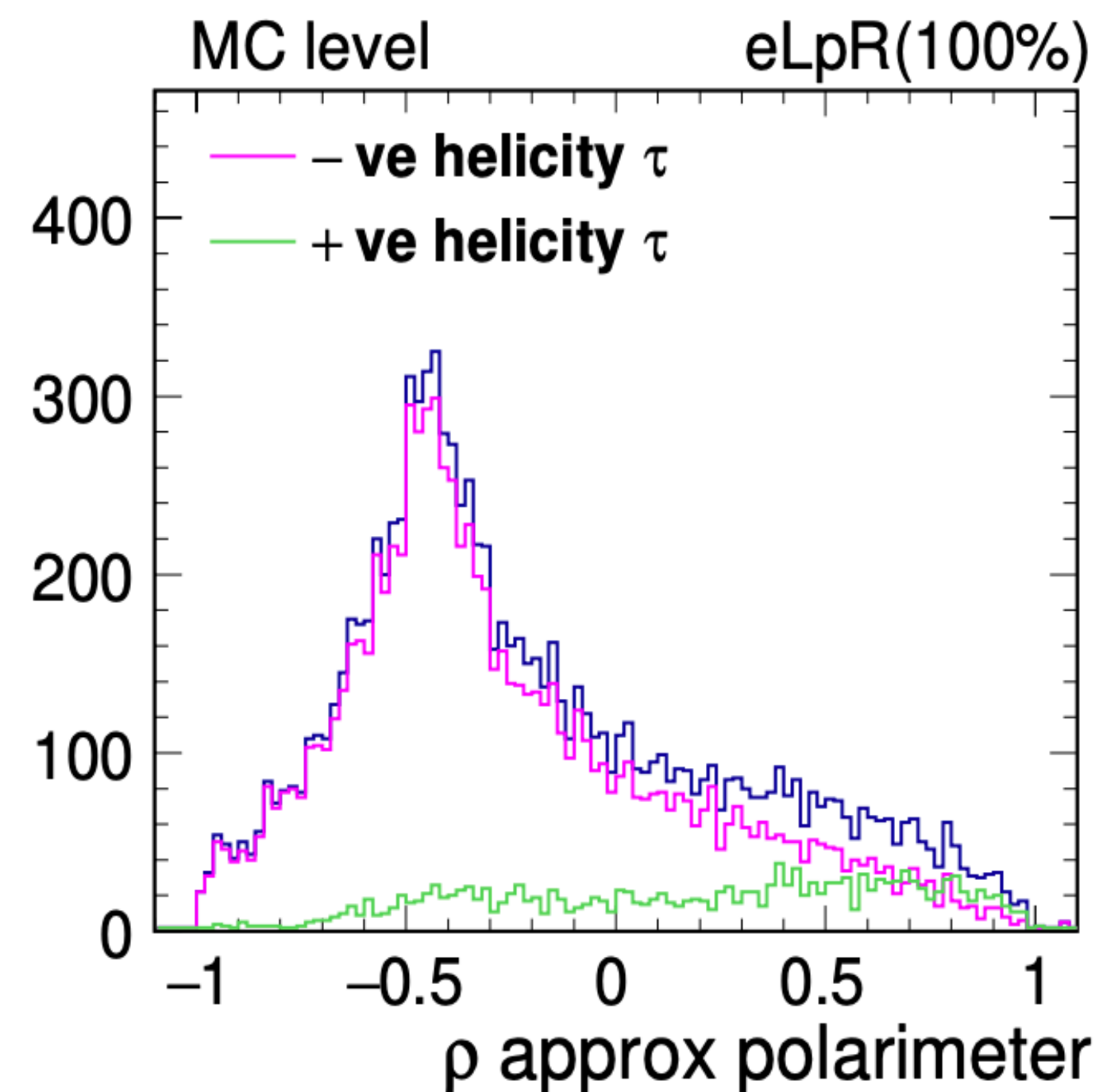
"Approximate" polarimeters based only on the momenta of visible tau decay products

"Optimal" polarimeters including the neutrino component



mean statistical error  
on tau polarisation

0.30 %



0.40 %

(  $E_{\text{CM}} = 500 \text{ GeV}$ ,  $\mathcal{L} = 1.6 \text{ ab}^{-1}$  )

[arXiv:1912.08403](https://arxiv.org/abs/1912.08403)

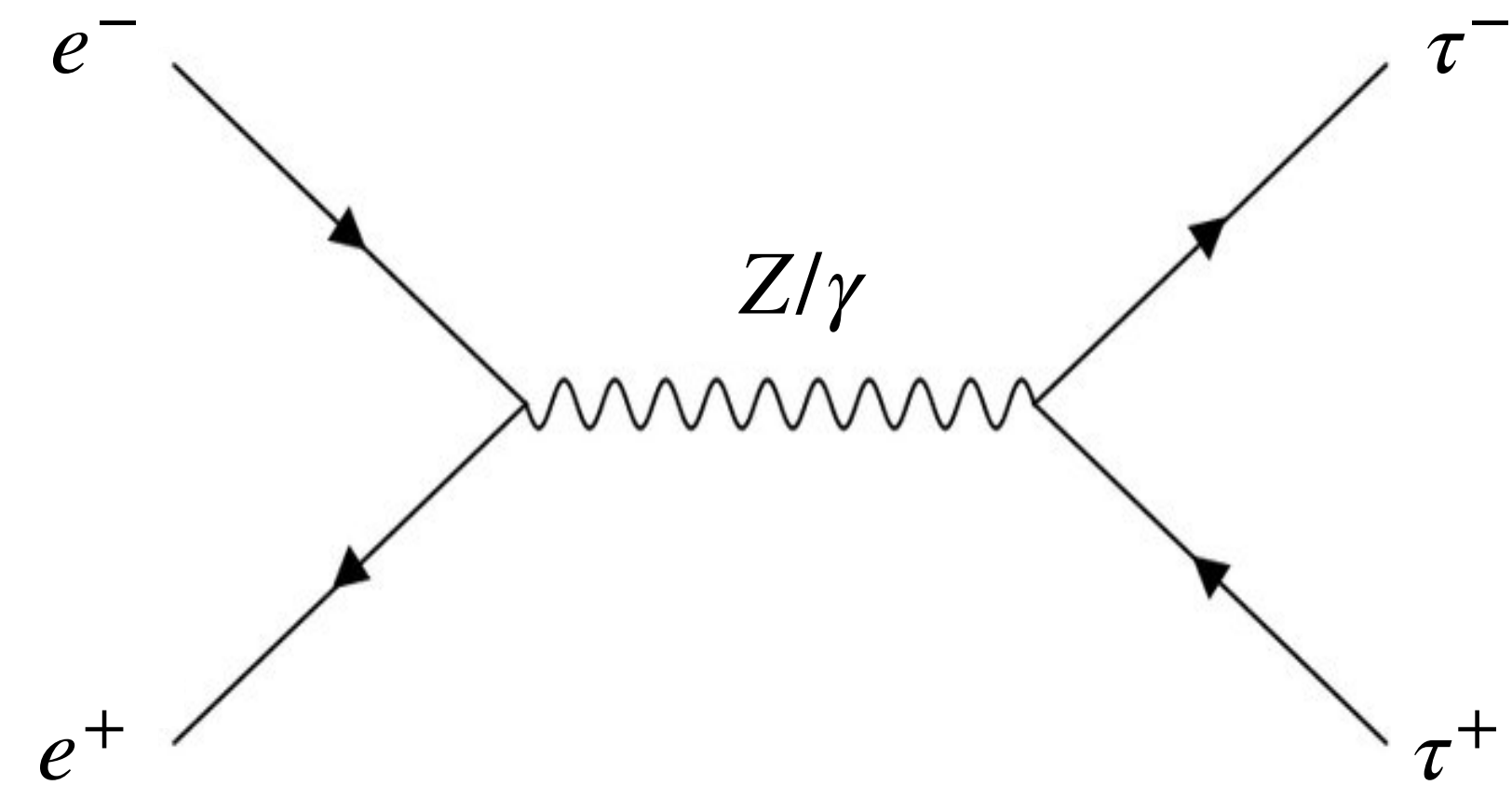
In this talk: reconstruct neutrino momentum  $\rightarrow$  optimal polarimeters

# Simulation setup

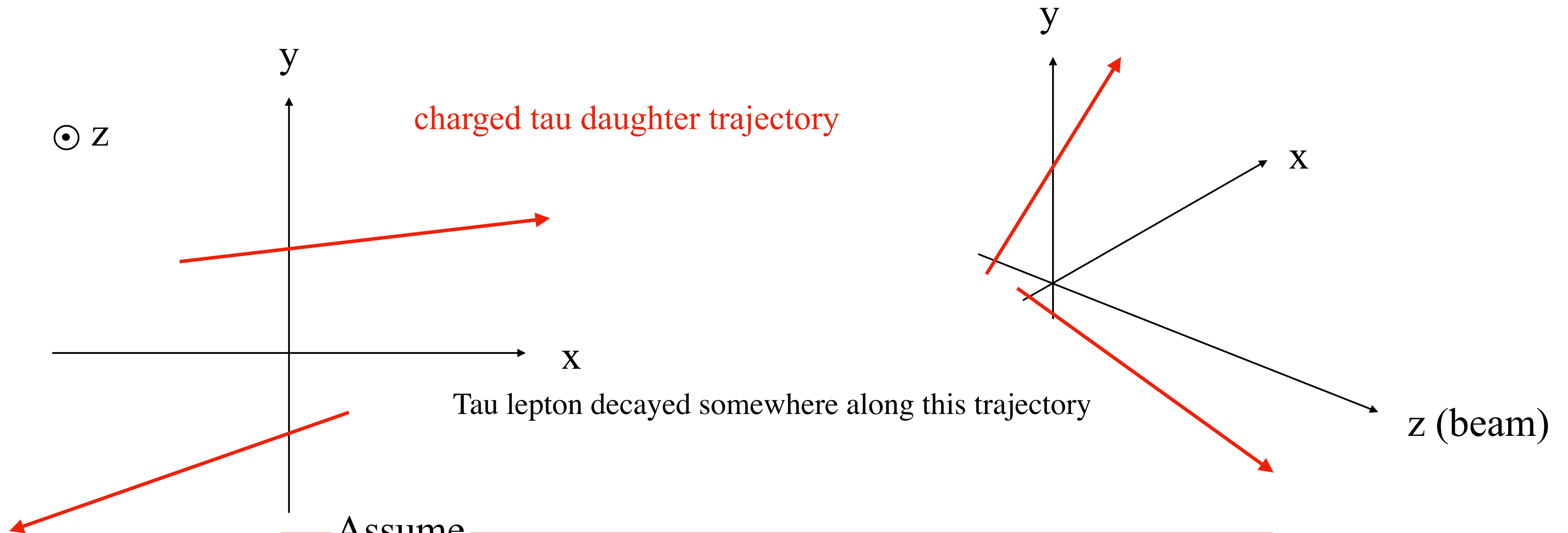
- Signal event sample with 100 %  $e_L^- e_R^+$  beam polarisations were generated using WHIZARD ver 2.8.5.
- The decay of the polarised tau was done using TAUOLA.
- MC truth information was used.

currently

- only look at
$$\tau \rightarrow \pi \nu \text{ (BR } \sim 10 \% )$$
$$\tau \rightarrow \rho \nu \text{ (BR } \sim 26 \% )$$



# $\tau$ reconstruction method

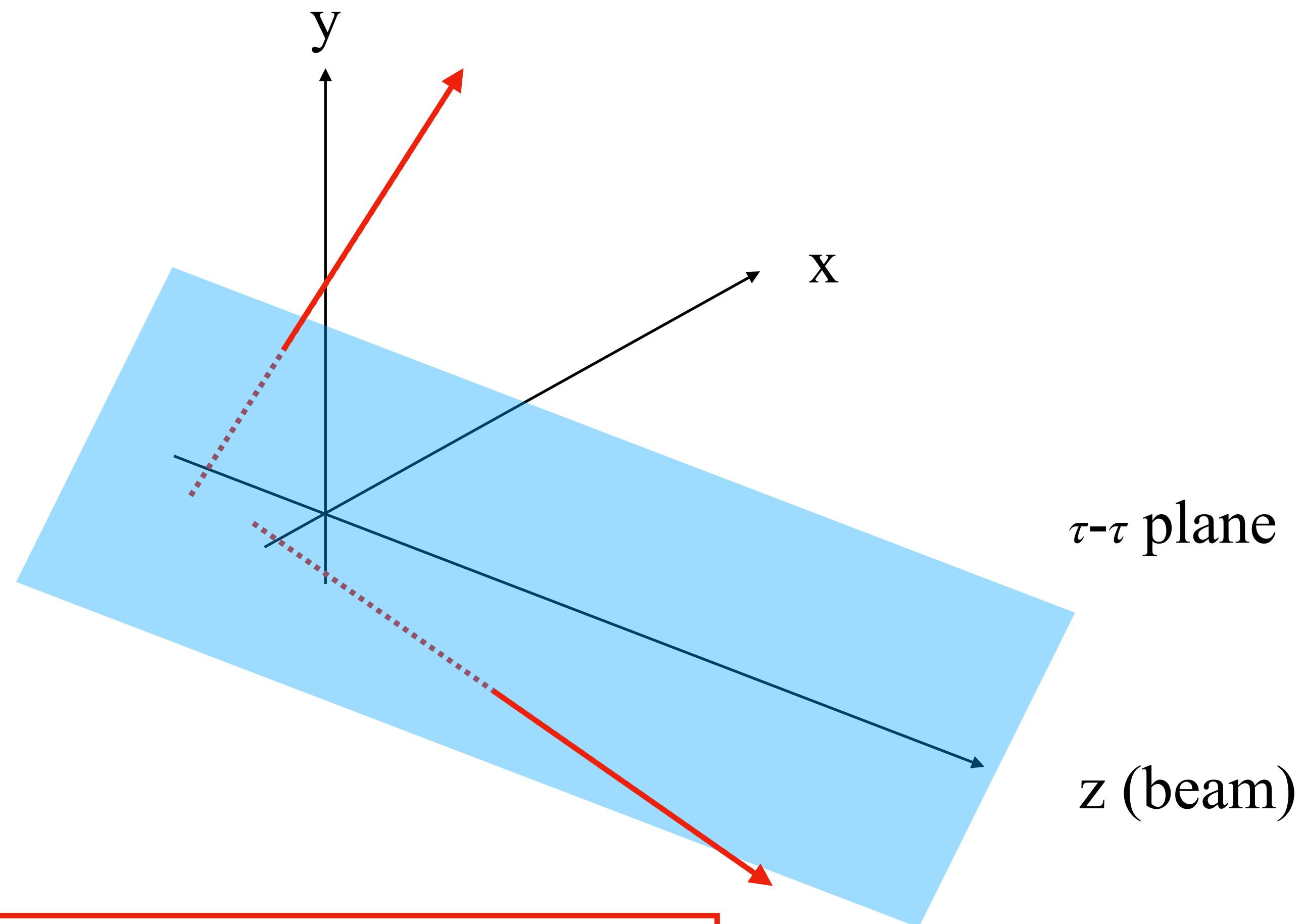
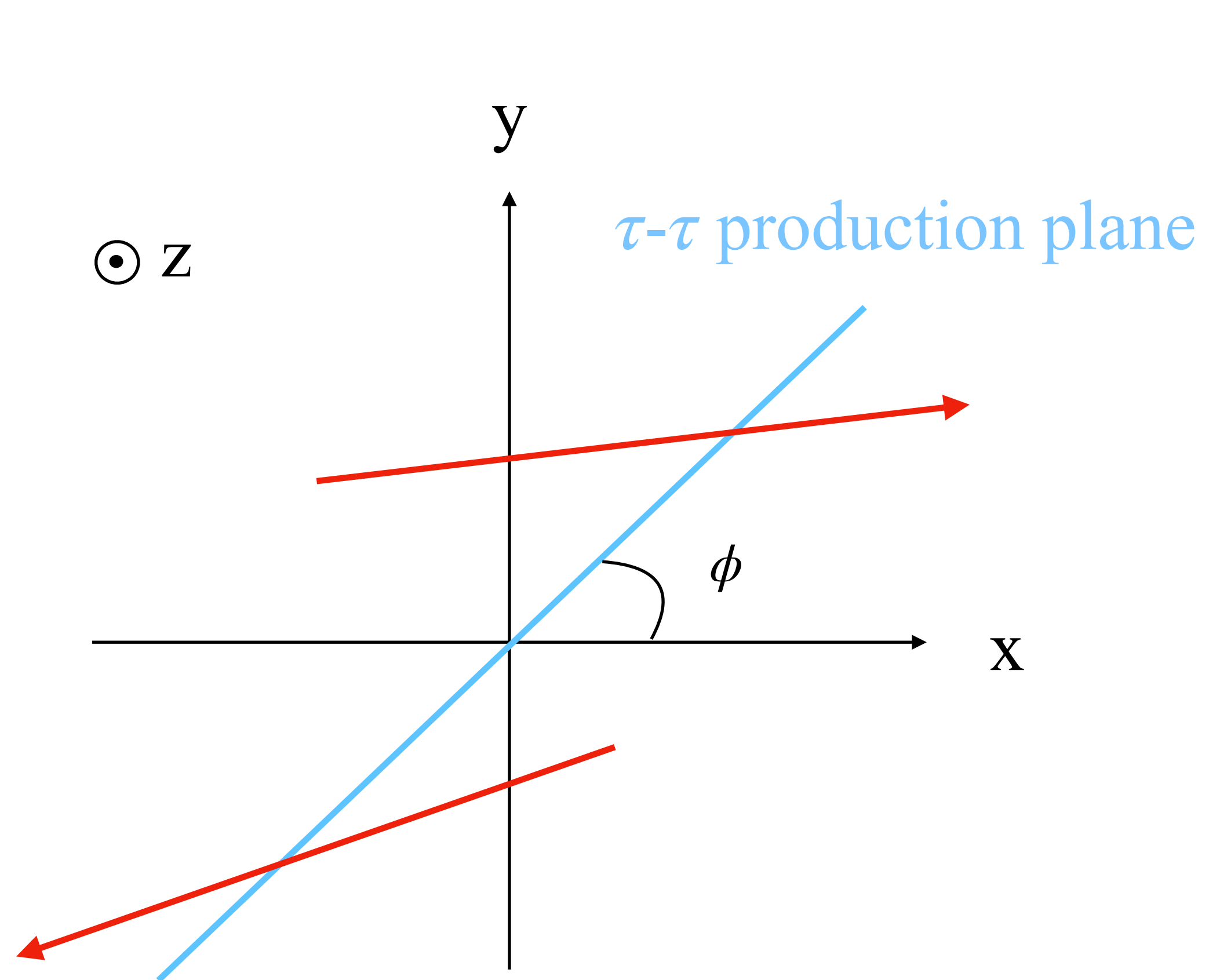


## Assume

- Two taus are produced along the beam line ( $x = y = 0$ ),
- Two taus are back-to-back in  $x$ - $y$  plane,  
— any ISR photons have negligible  $p_T$
- Charged particle travels approximately in a straight line near IP.



# $\tau$ reconstruction method

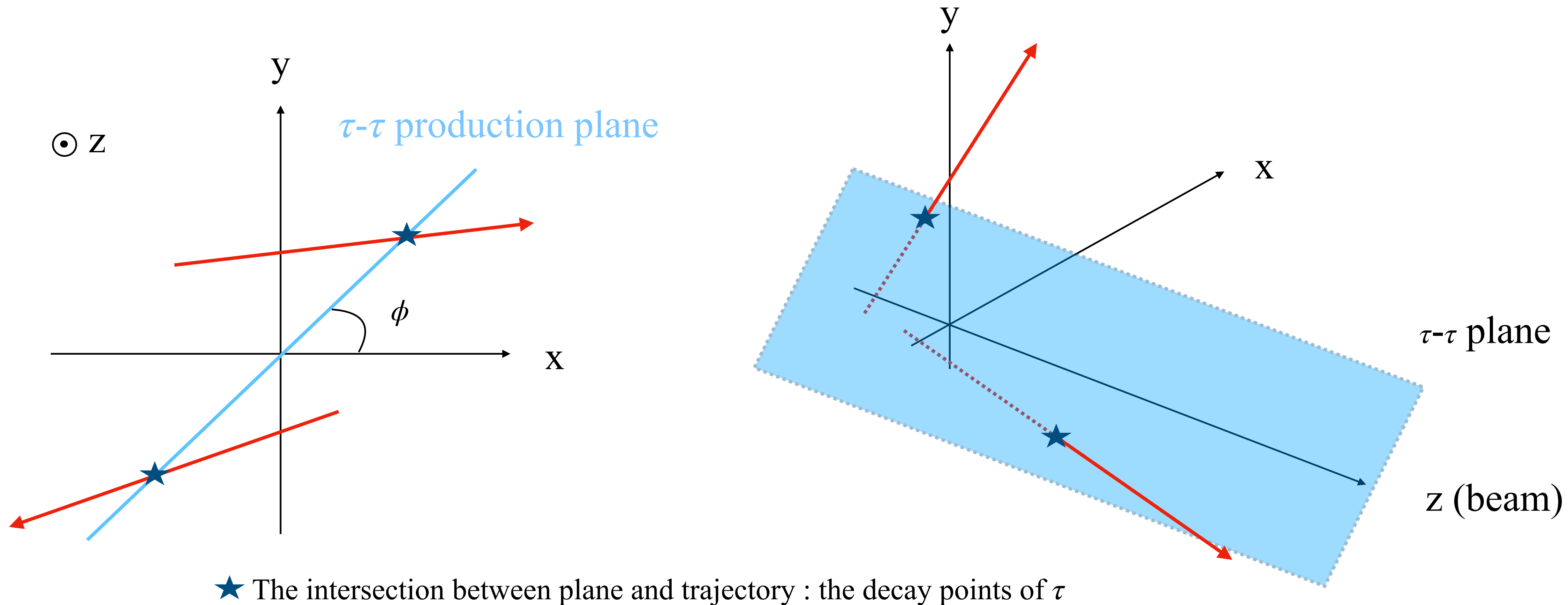


## Assume

- Primary interaction occurs along the beam line( $x = y = 0$ ),
- Two taus are back-to-back in  $x$ - $y$  plane,
- Charged particle travels approximately in a straight line near IP.

- Two tau momenta lie in a plane containing  $z$ -axis, at some azimuthal angle  $\phi$

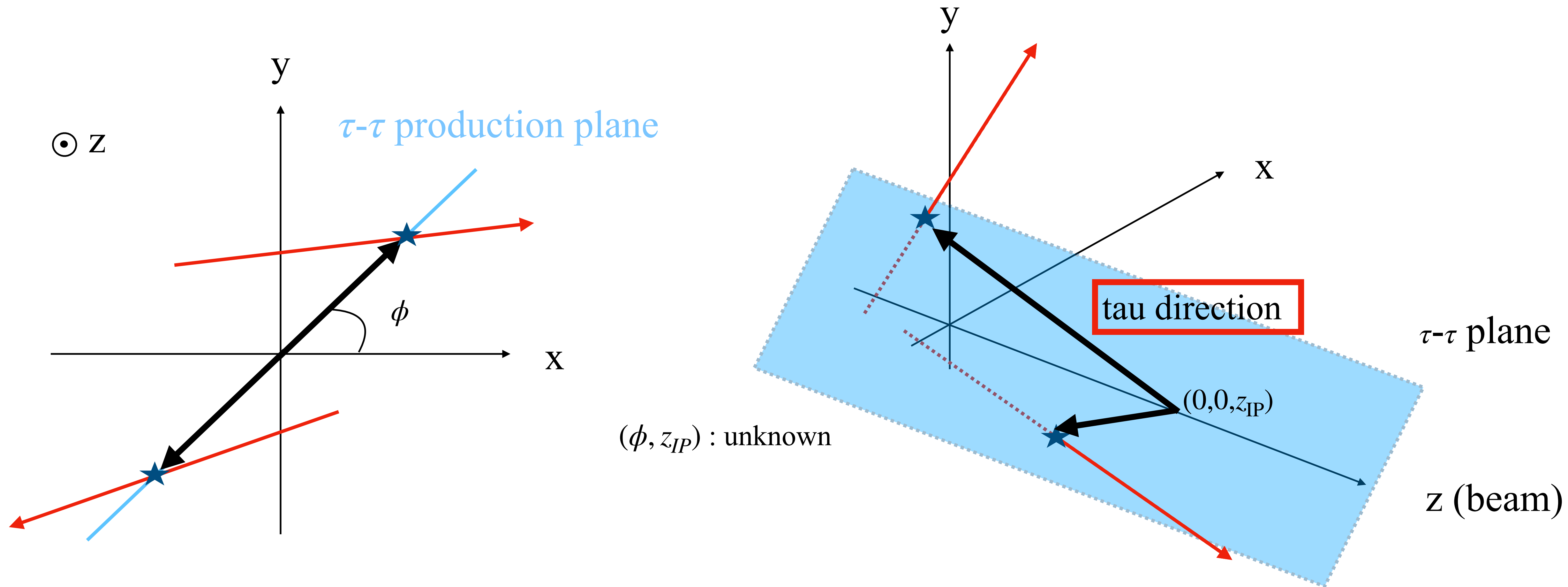
# $\tau$ reconstruction method



For a plane with azimuthal angle  $\phi$ ,  
the intersection of trajectories with this plane can be calculated.



# $\tau$ reconstruction method



then choice of  $z_{IP}$  gives direction of tau momenta

$\Rightarrow$  How can we choose  $\phi, z_{IP}$  ?

# $\tau$ reconstruction method

## Unknown

- neutrino 3-momentum  $\times 2$
- ISR momentum
- $z_{IP}$

## Constraints

- 4-momentum conservation
- tau mass  $\times 2$
- Decay point on **trajectory**  $\times 2$

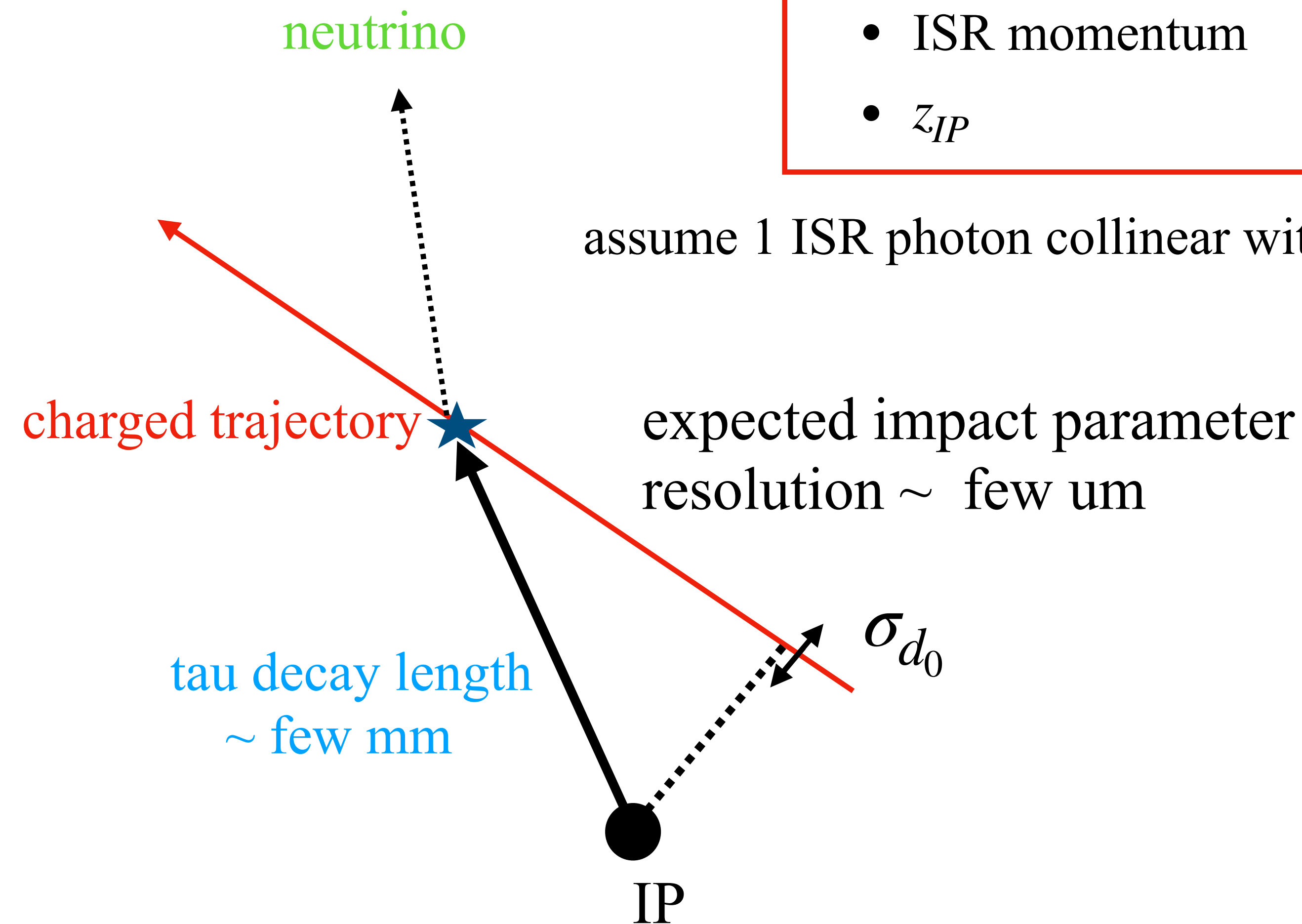
assume 1 ISR photon collinear with beam and each other

For choice of  $z_{IP}$ ,  $\phi$

we can calculate tau 4-momenta  $P_\tau$

the invariant mass of the missing (neutrino) momentum for each tau can be calculated

$$P_\nu = P_\tau - P_{vis}$$

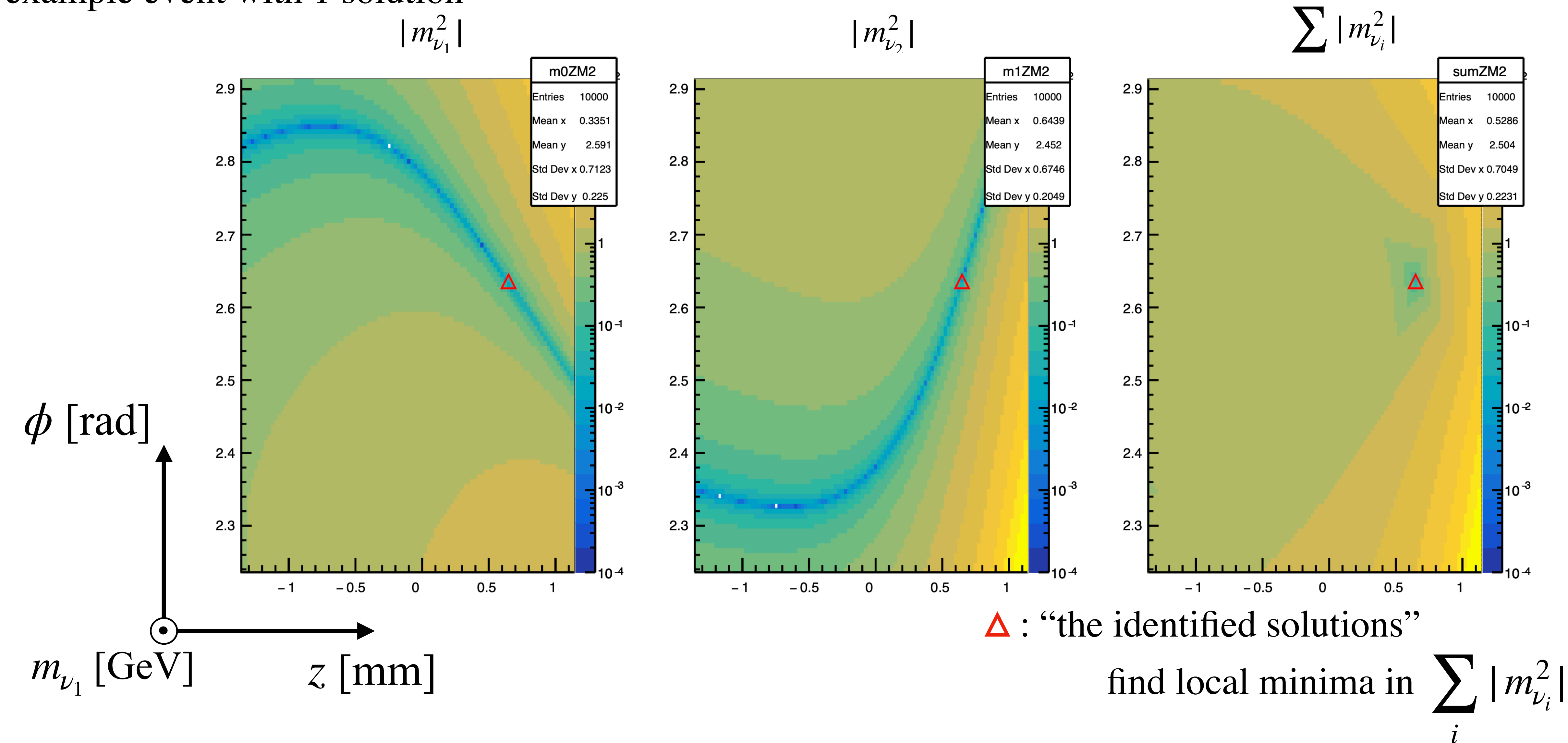


We choose the values of  $z$  and  $\phi$  which result in neutrino masses closest to zero

# Find solutions

We choose the values of  $z$  and  $\phi$  which result in neutrino masses closest to zero

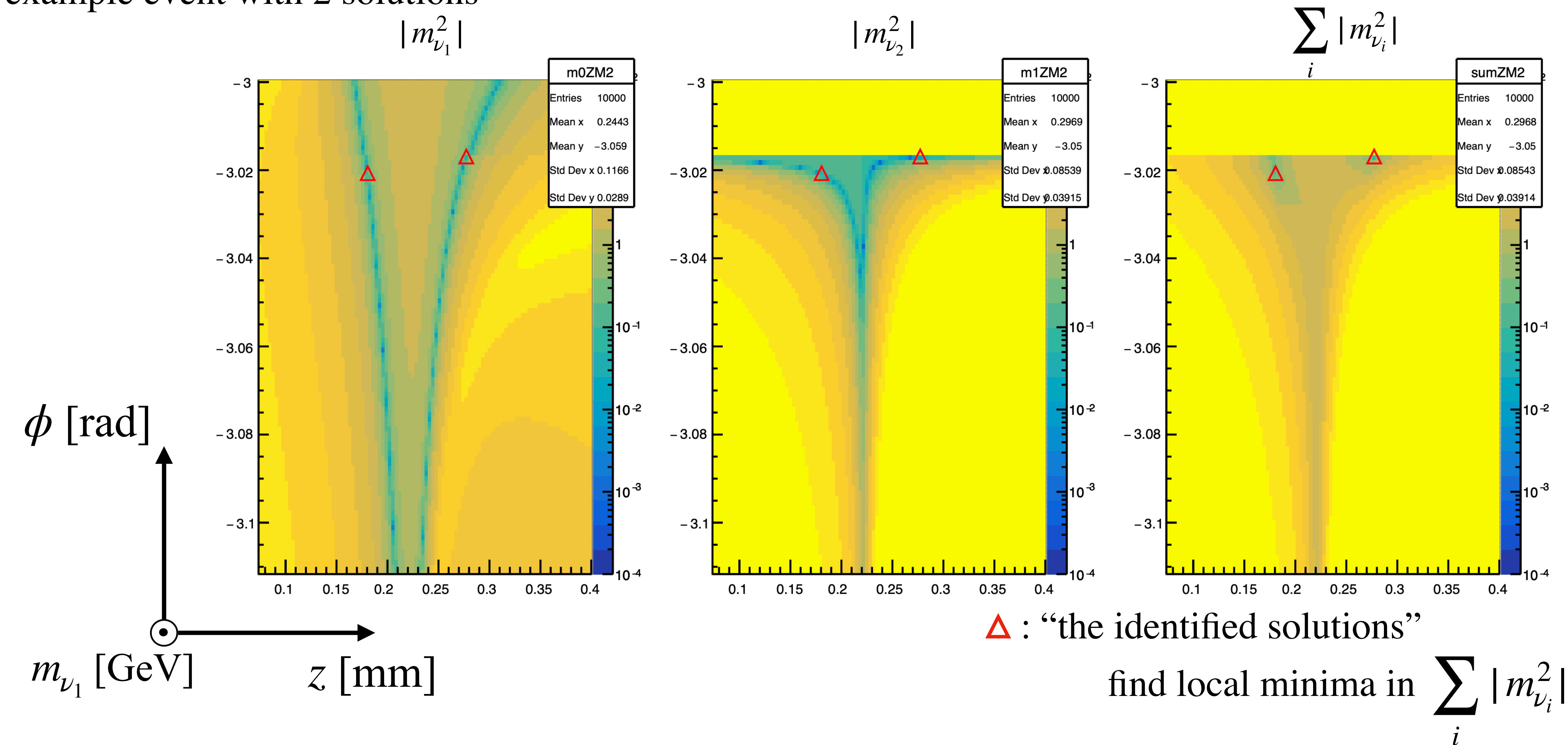
example event with 1 solution



# Find solutions

We choose the values of  $z$  and  $\phi$  which result in neutrino masses closest to zero

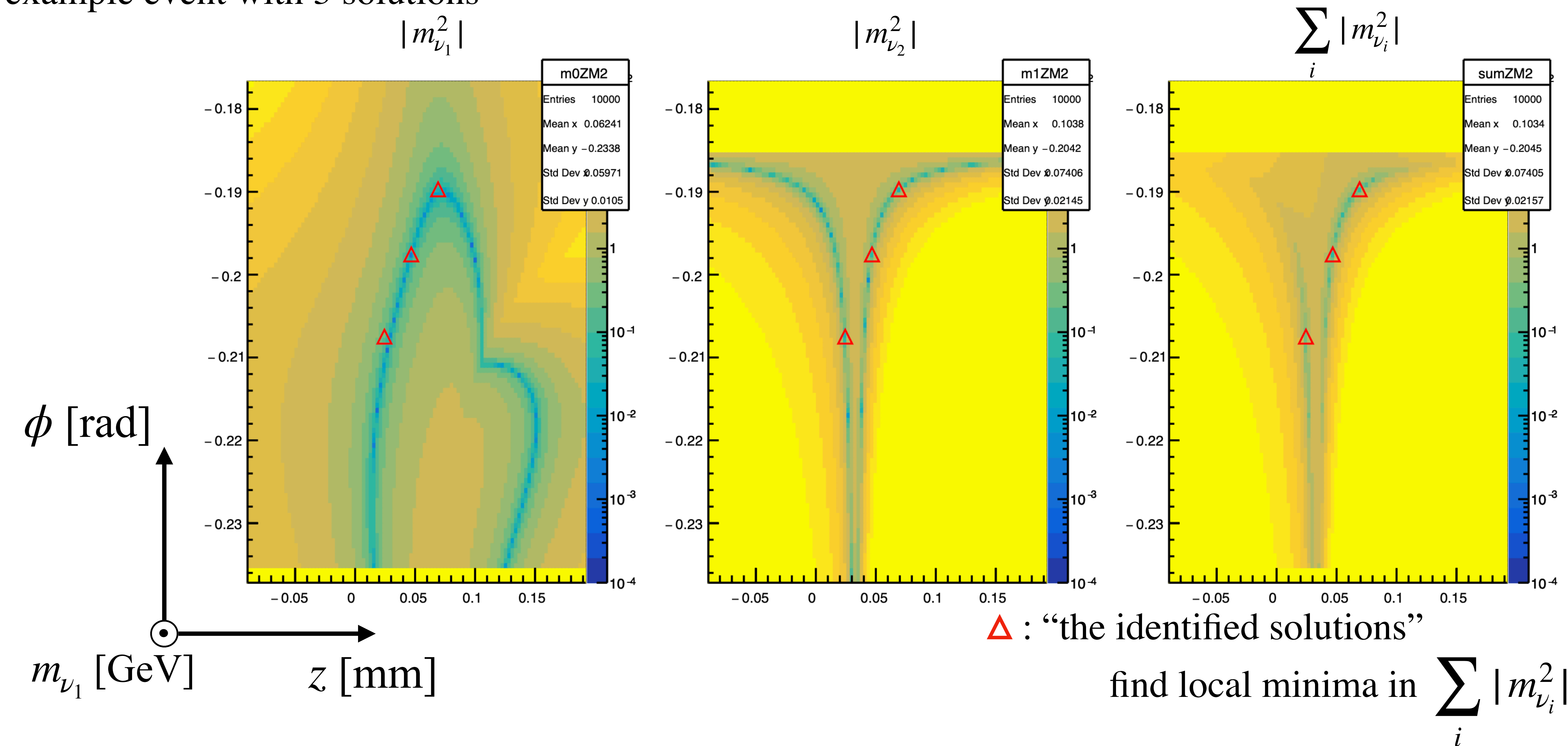
example event with 2 solutions



# Find solutions

We choose the values of  $z$  and  $\phi$  which result in neutrino masses closest to zero

example event with 3 solutions

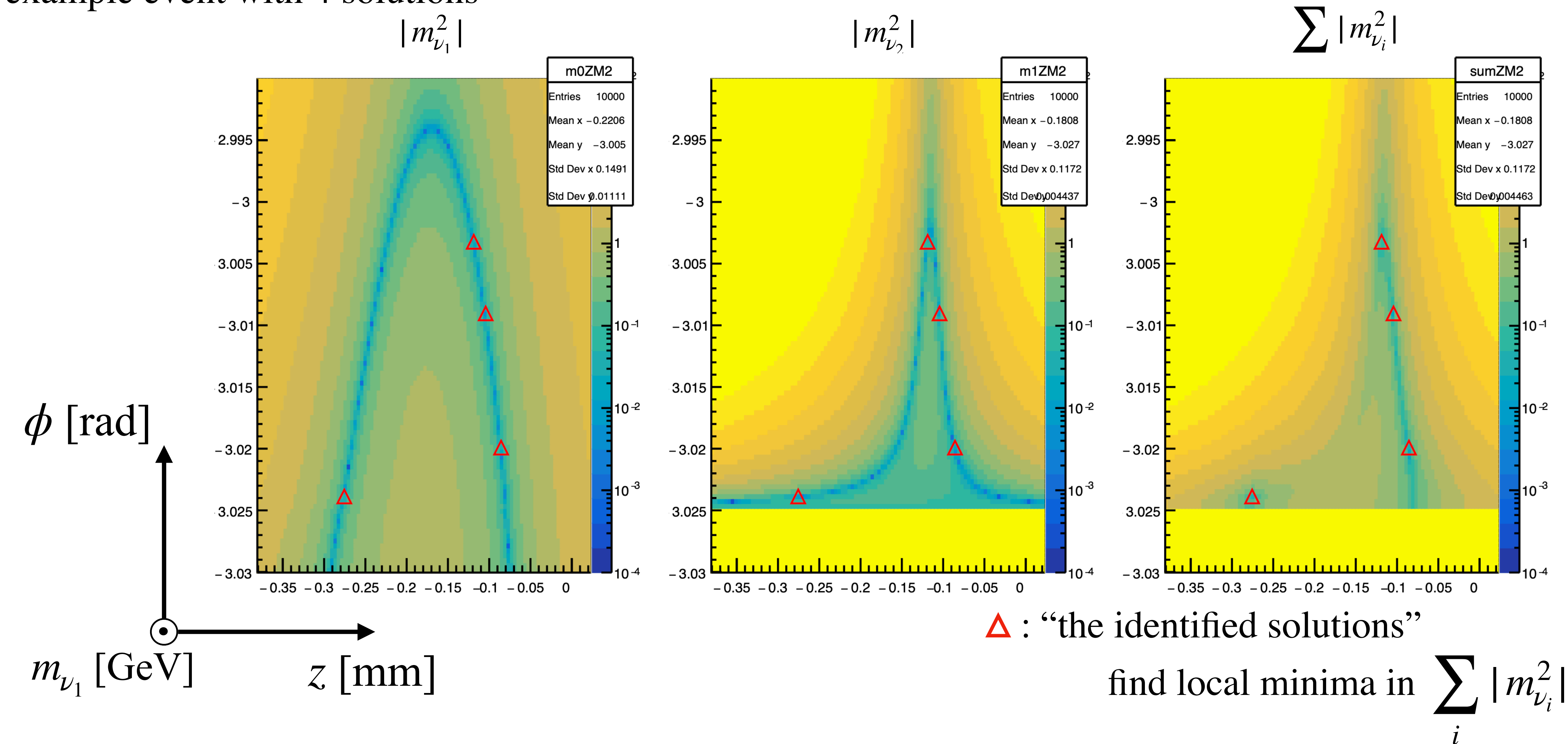




# Find solutions

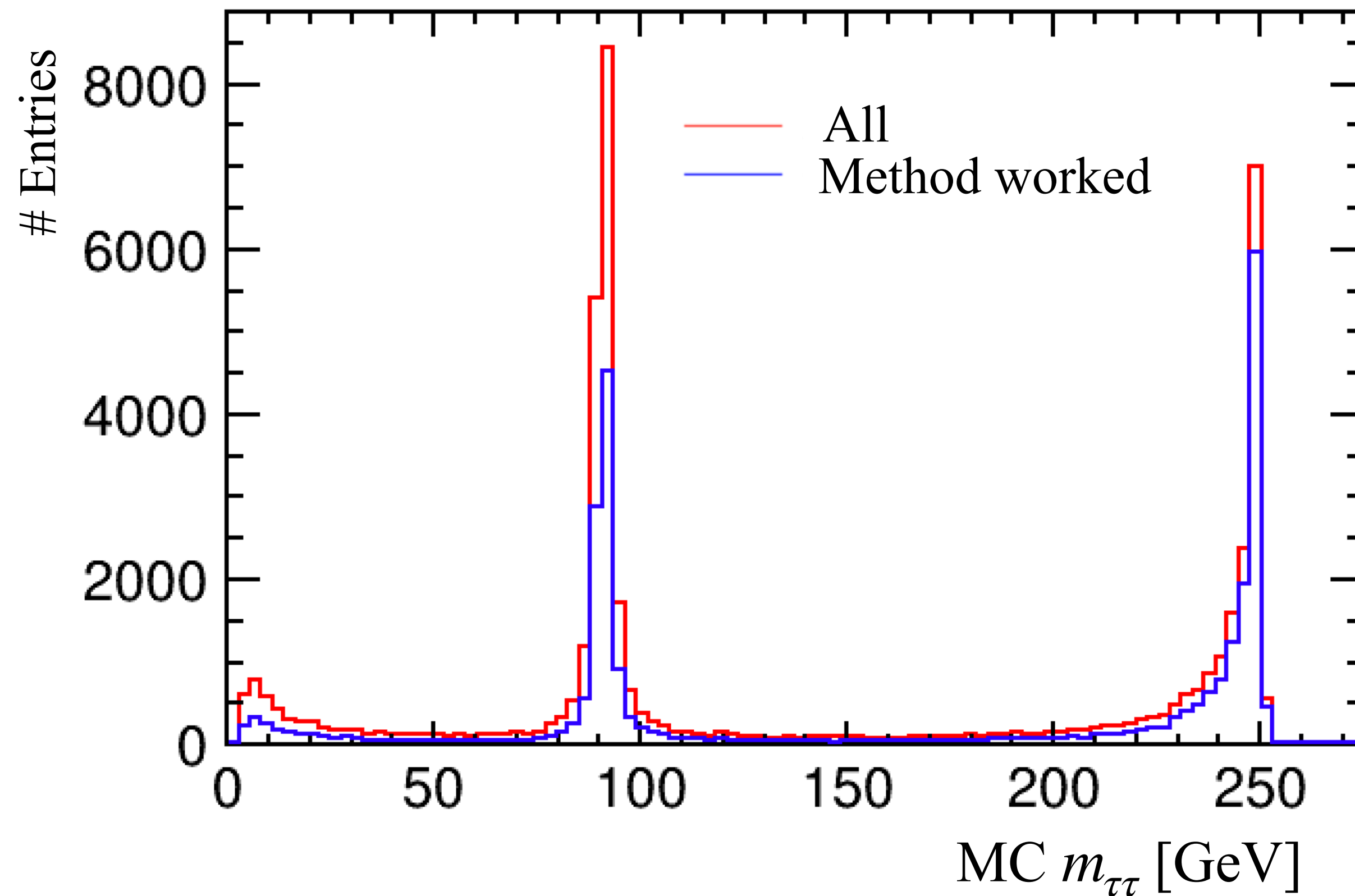
We choose the values of  $z$  and  $\phi$  which result in neutrino masses closest to zero

example event with 4 solutions

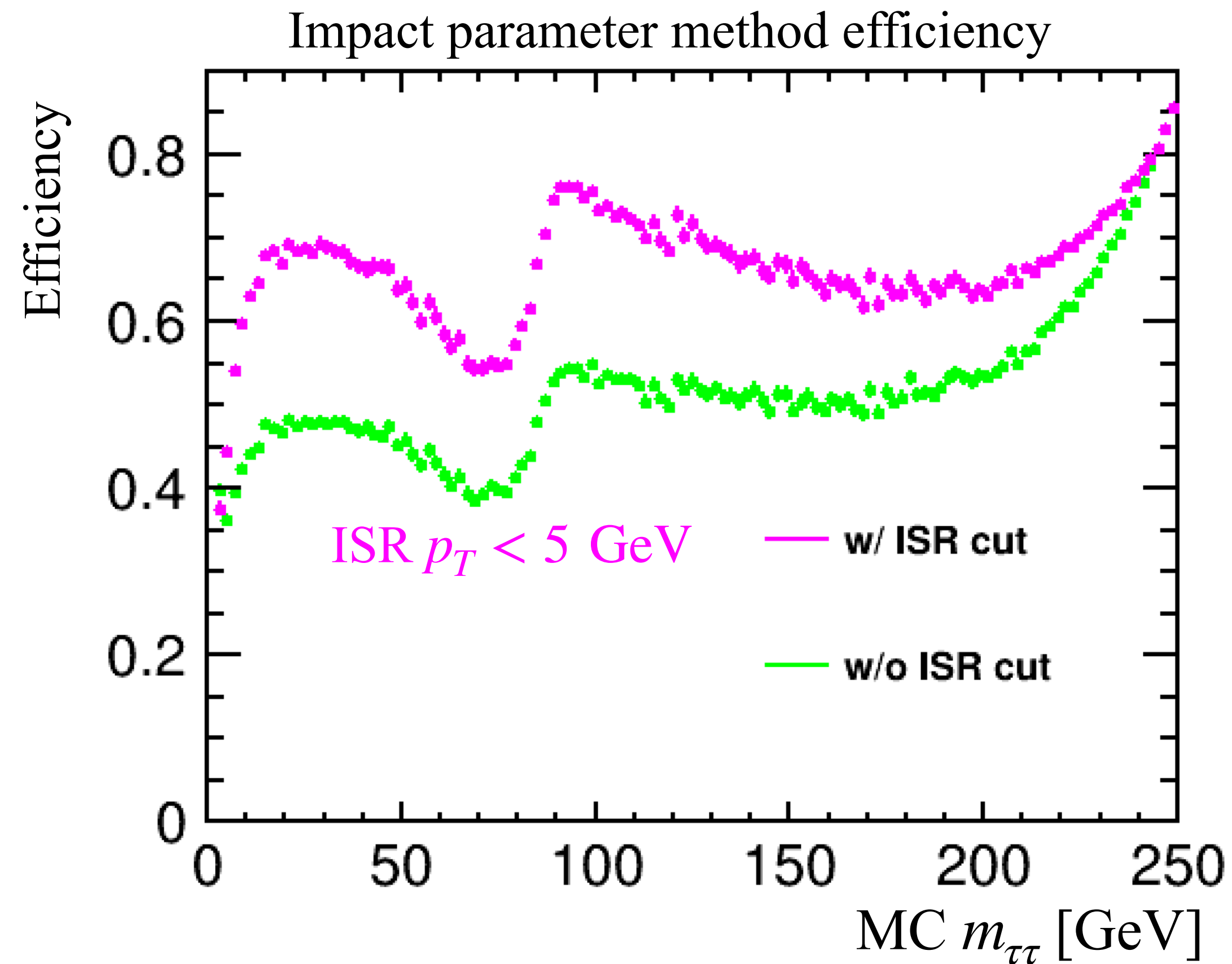




# Method efficiency



Method worked : at least 1 solution is found

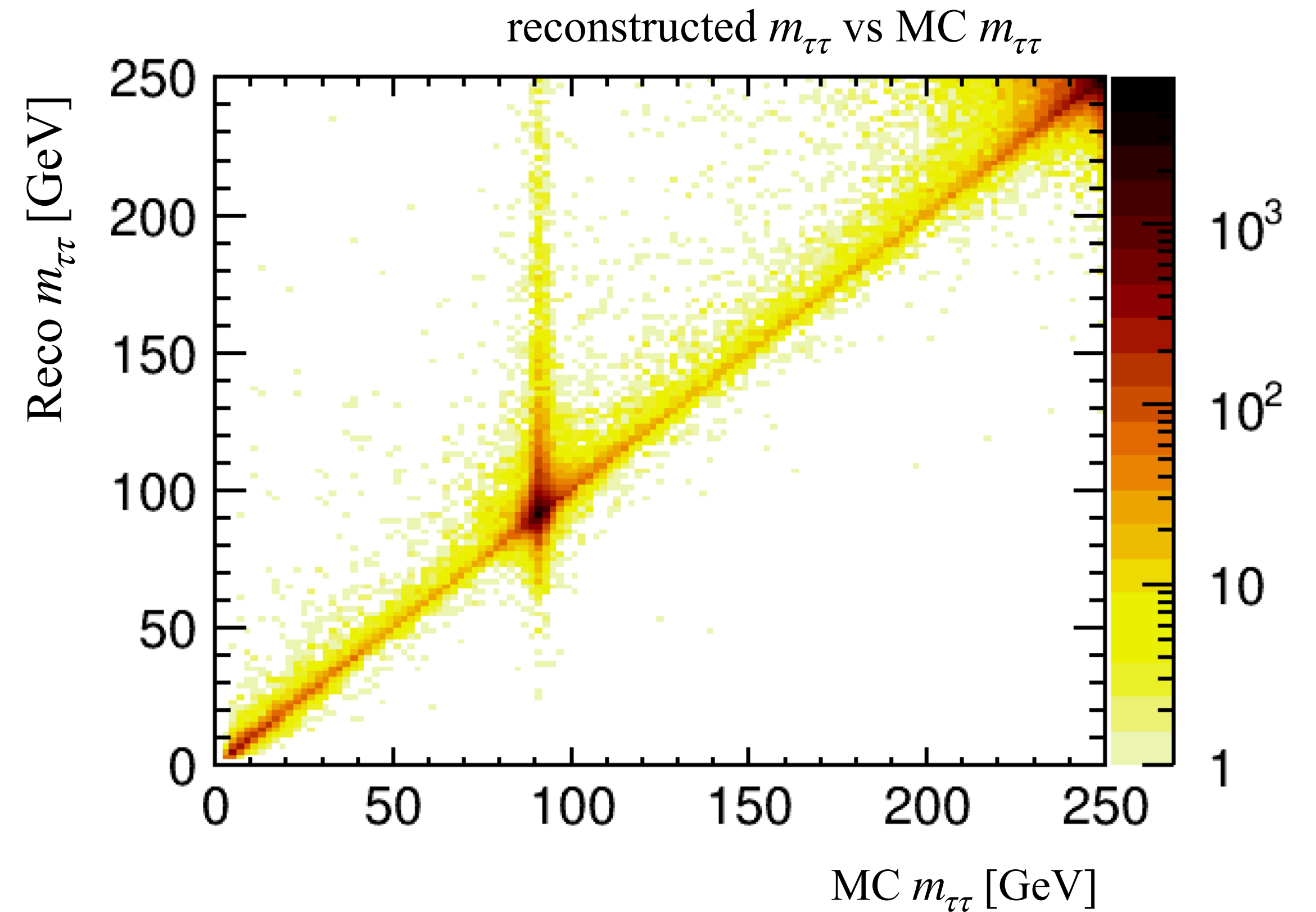
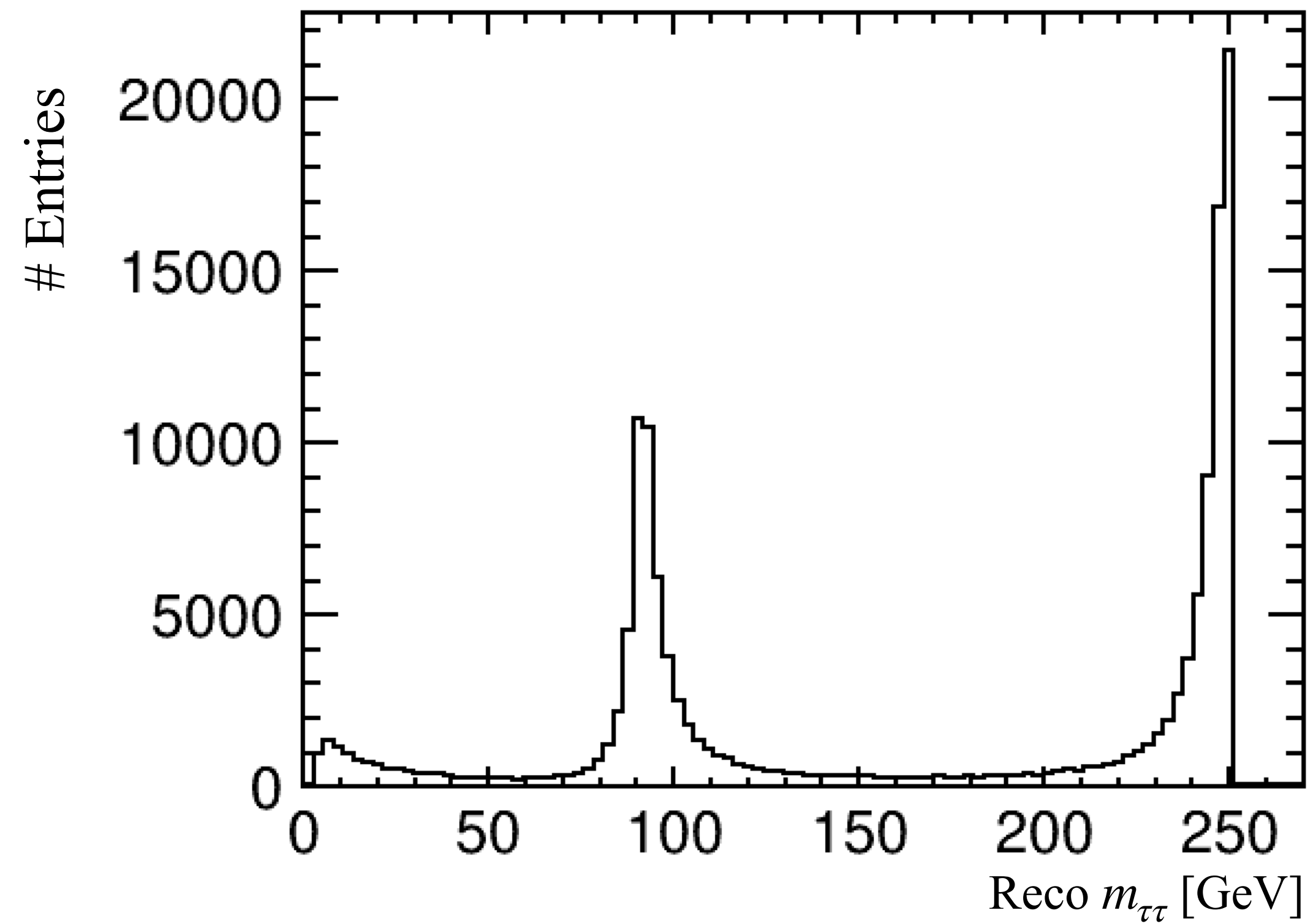


Impact parameter method efficiency is  $> 80\%$  for events with  $m_{\tau\tau} \sim 250$  GeV

# Comparison with MC

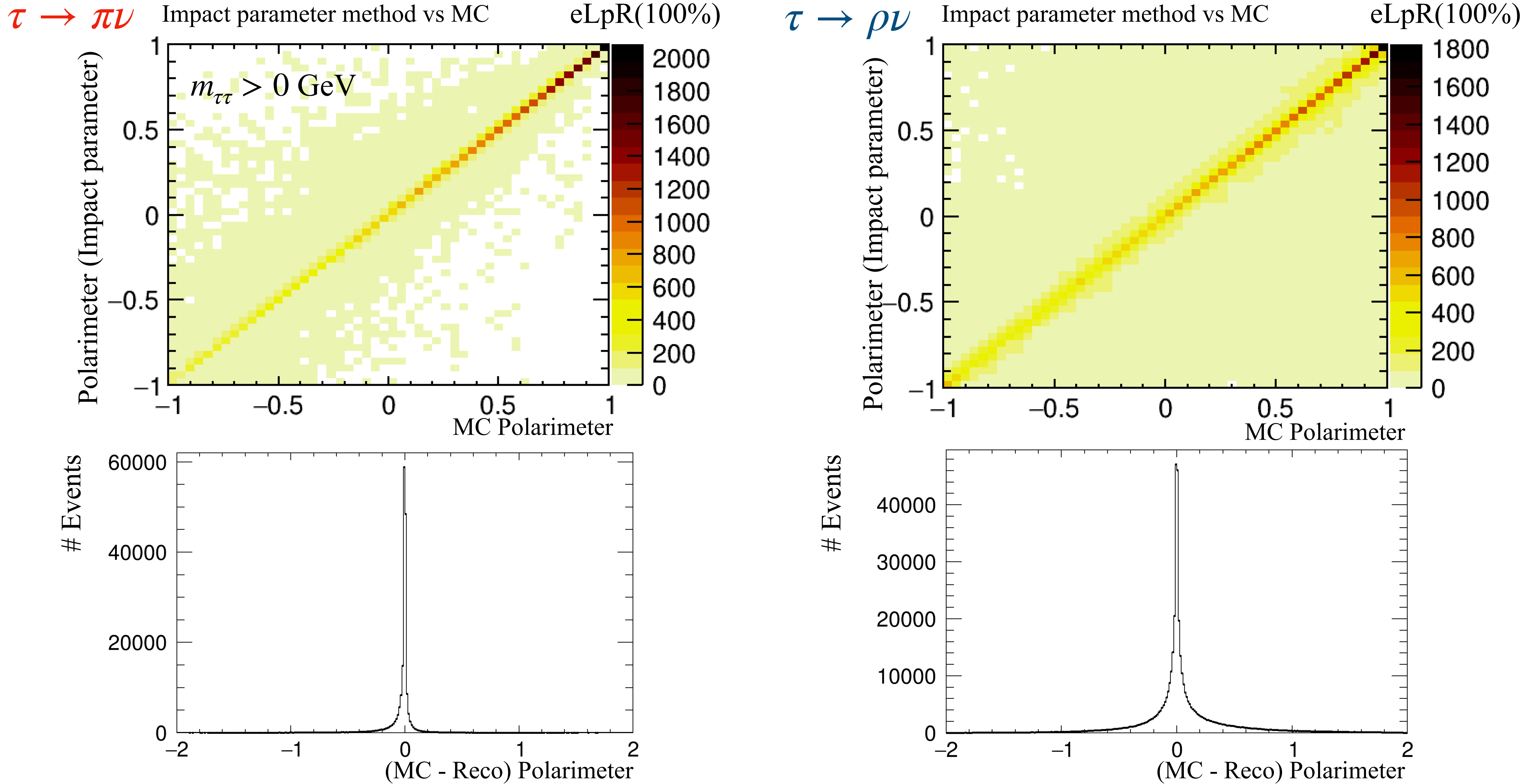
Reconstructed  $m_{\tau\tau}$  based on Impact parameter method solutions

weighted combination of all solutions



Reasonable agreement between MC and reconstructed  $m_{\tau\tau}$

# Polarimeter



Polarimeter using reconstructed  $\nu$  is in reasonable agreement with MC one.

# Summary

- Full reconstruction of  $e^+e^- \rightarrow \tau^+\tau^-$  using impact parameter was investigated.
- For events with  $m_{\tau\tau} \sim 250$  GeV, impact parameter method efficiency is  $> 80\%$ .  
 $m_{\tau\tau} \sim 91$  GeV  $\sim 70\%$
- Polarimeters were reconstructed in the  $\tau \rightarrow \pi\nu$  and  $\tau \rightarrow \rho\nu$  decay modes.
- Reasonable agreement between MC truth polarimeter and the one from “Impact parameter method” for both  $\tau \rightarrow \pi\nu$  and  $\tau \rightarrow \rho\nu$  decay were found.

# Future plan

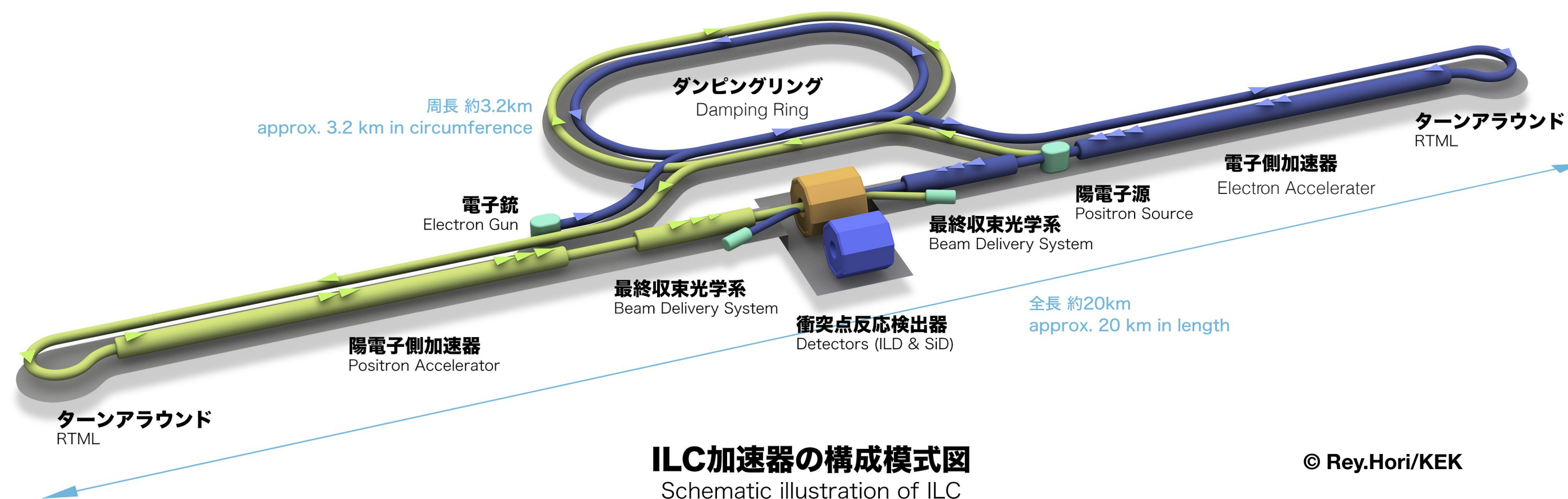
- Understand the structure of the method's efficiency around the  $Z$  peak.
- Investigate the effect of full detector simulation and reconstruction.
- Quantify the precision with which the tau polarisation can be measured at ILC-250.
- Investigate search for new physics by using the tau polarisation.





# Introduction

## International Linear Collider (ILC)



linear electron-positron collider

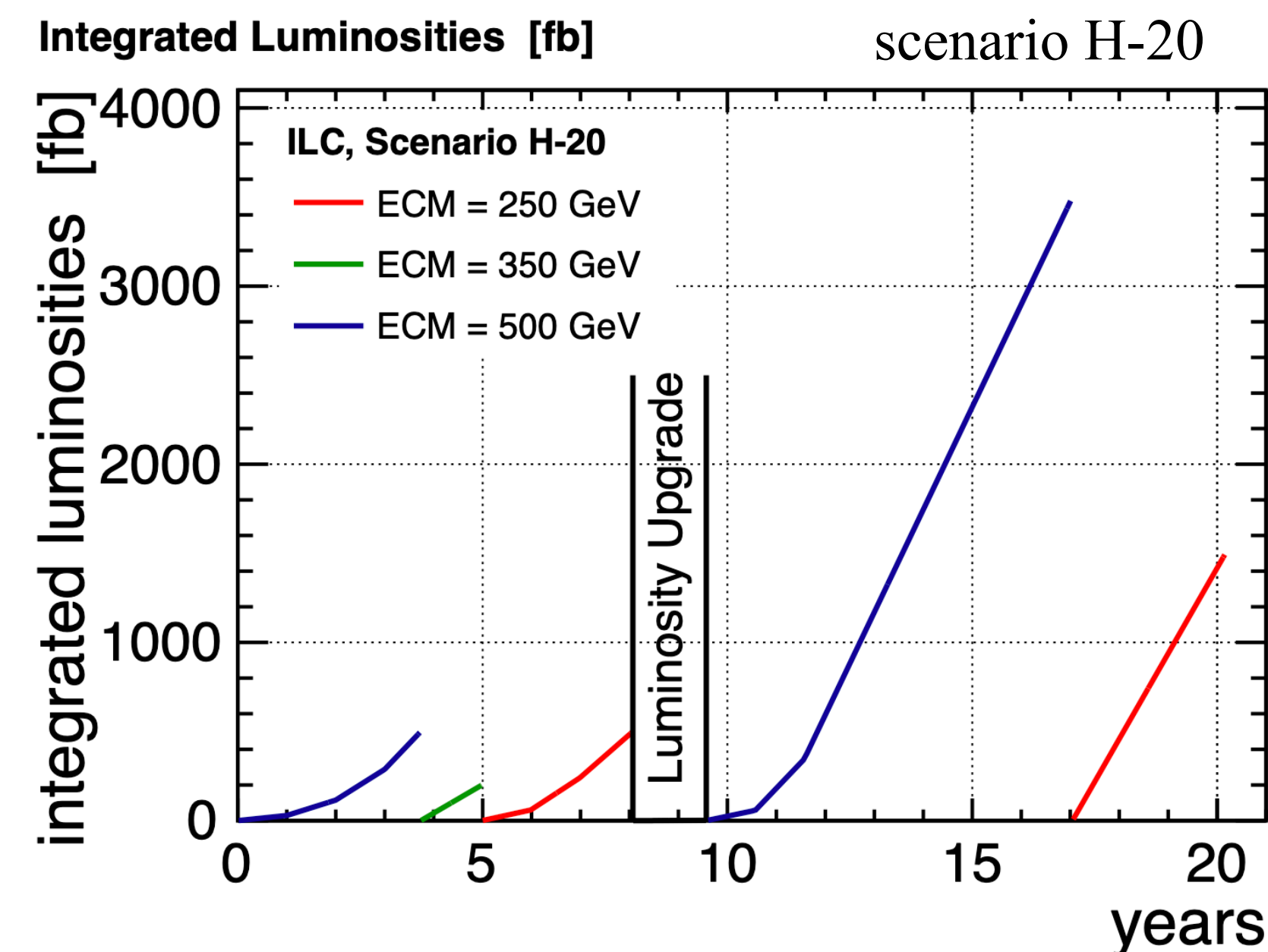
centre-of-mass energy : 250 GeV — 500 GeV

integrated luminosities: 2  $\text{ab}^{-1}$  — 4  $\text{ab}^{-1}$

beam polarisation:  $(e^-, e^+) = (\pm 80\%, \pm 30\%)$

### The aim of ILC experiment

- Precision measurement of the Higgs boson and top quark
- Discovery of physics beyond the Standard Model
  - search for candidates for dark matter



The transverse momenta  $p_T$  of the two taus are assumed to be equal to conserve the event's transverse momentum. The magnitudes of the total tau momenta are then given by  $p_i = p_T / \sin \theta_i$ , and the  $z$  momenta by  $p_{z,i} = p_T / \tan \theta_i$ .

Conservation of energy gives  $E_{\tau,1} + E_{\tau,2} + E_{ISR} = E_{CM}$ , where  $E_{\tau,1(2)}$  is the energy of tau 1(2),  $E_{ISR}$  the energy carried by ISR photons, and  $E_{CM}$  the centre-of-mass energy. If we assume a single ISR photon collinear with the beam, then momentum conservation in the  $z$  directions gives  $E_{ISR} = |p_{z,1} + p_{z,2}|$ . We then write

$$\begin{aligned} E_{CM} &= E_{\tau,1} + E_{\tau,2} + E_{ISR} \\ &= \sqrt{p_1^2 + m_\tau^2} + \sqrt{p_2^2 + m_\tau^2} + |p_{z,1} + p_{z,2}| \\ &\approx p_1 \left[ 1 + \frac{m_\tau^2}{2 p_1^2} \right] + p_2 \left[ 1 + \frac{m_\tau^2}{2 p_2^2} \right] + |p_{z,1} + p_{z,2}| \end{aligned}$$

when we consider the limit  $p_i \gg m_\tau$ . Rewriting in terms of  $p_T$  and  $\theta_{1,2}$

$$\begin{aligned} 0 \approx & p_T^2 (|\cot \theta_1 + \cot \theta_2| + \csc \theta_1 + \csc \theta_2) \\ & - p_T E_{CM} \\ & + \frac{1}{2} m_\tau^2 (\sin \theta_1 + \sin \theta_2) \end{aligned}$$

which is a quadratic equation in  $p_T$ , with solutions

$$p_T \approx \frac{E_{CM}}{2A} \left( 1 \pm \sqrt{1 - 4AC \frac{m_\tau^2}{E_{CM}^2}} \right),$$

$$A = |\cot \theta_1 + \cot \theta_2| + \csc \theta_1 + \csc \theta_2$$

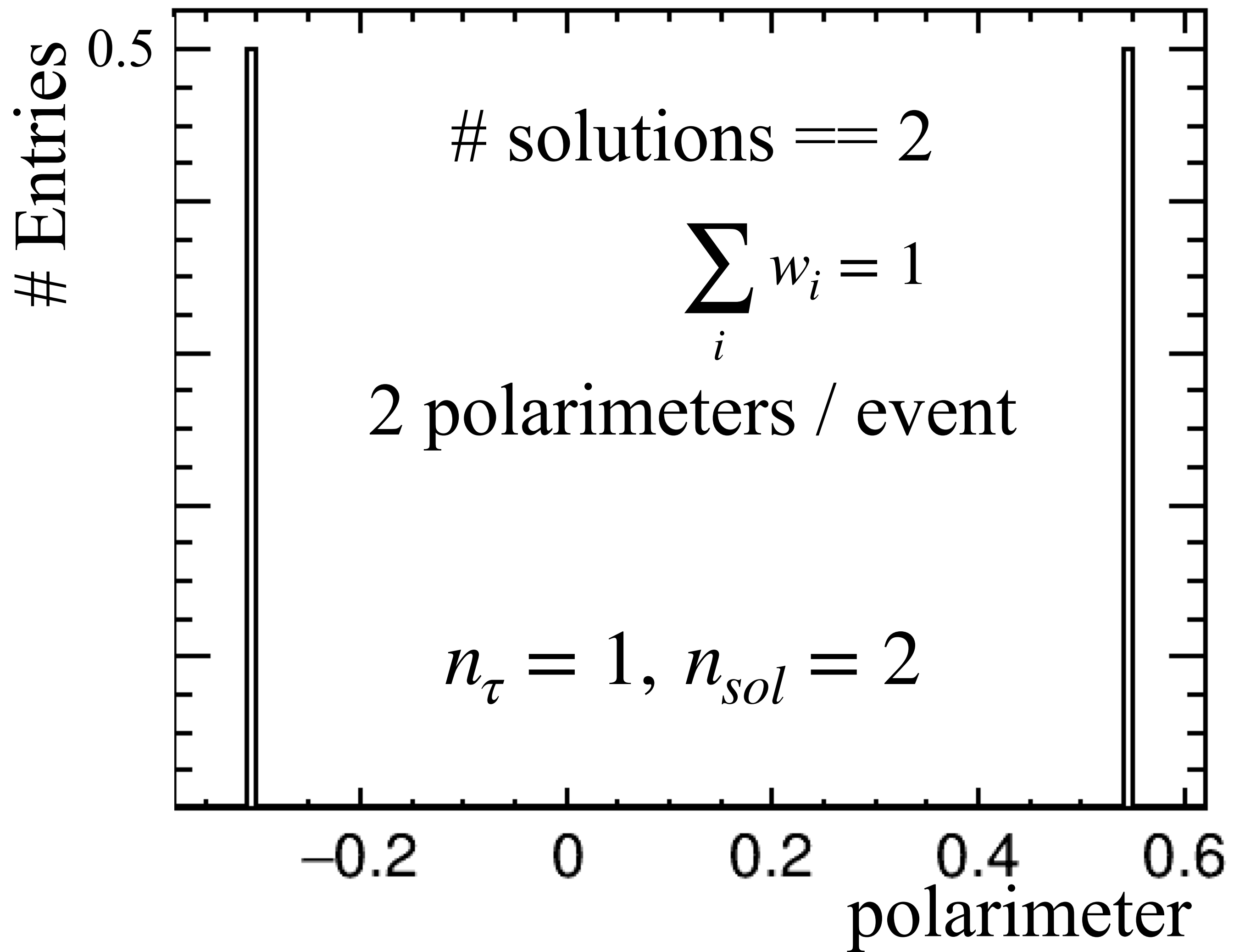
$$C = \frac{1}{2} (\sin \theta_1 + \sin \theta_2).$$

If each tau has several solutions,  
 apply equal weight

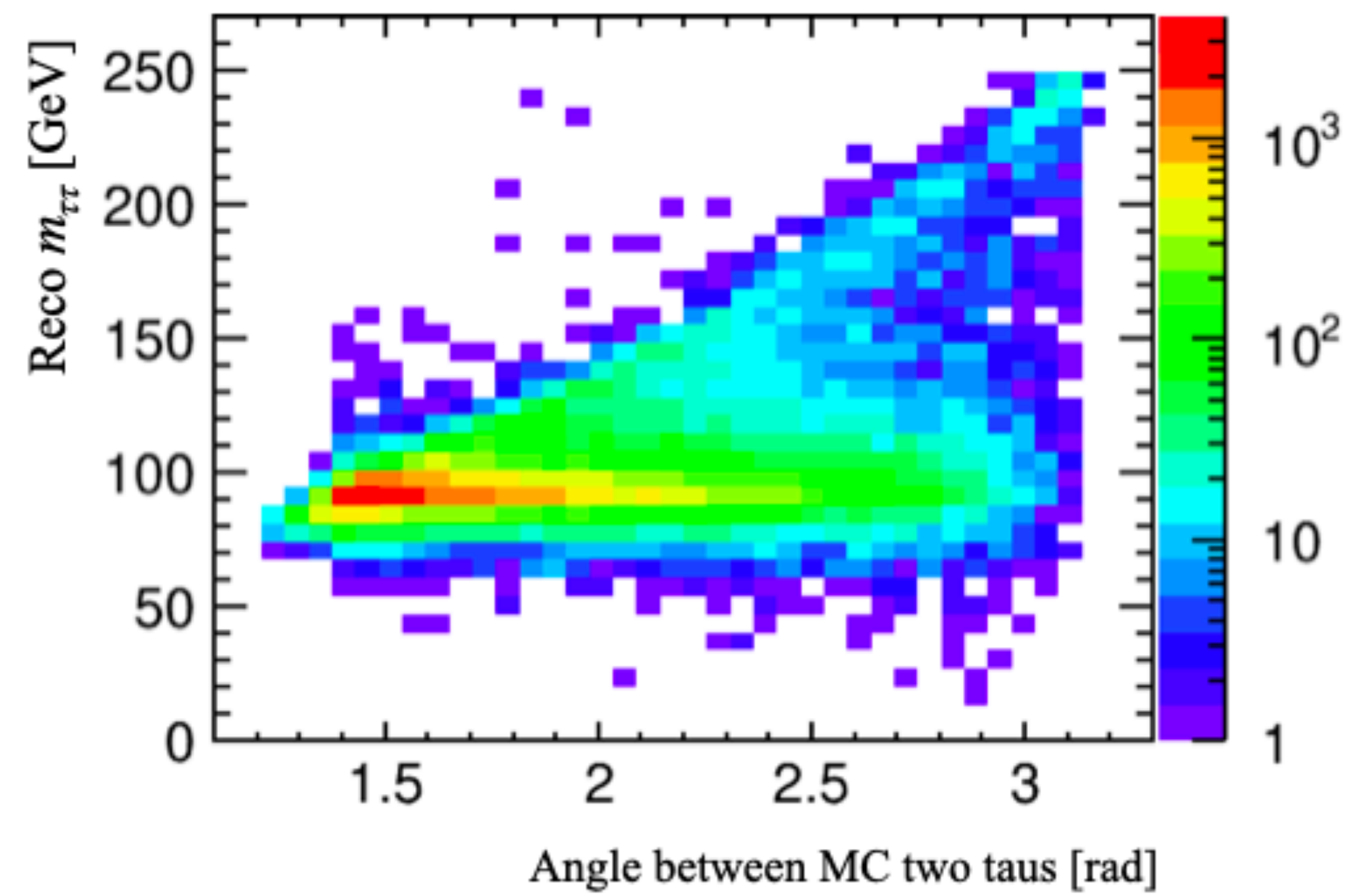
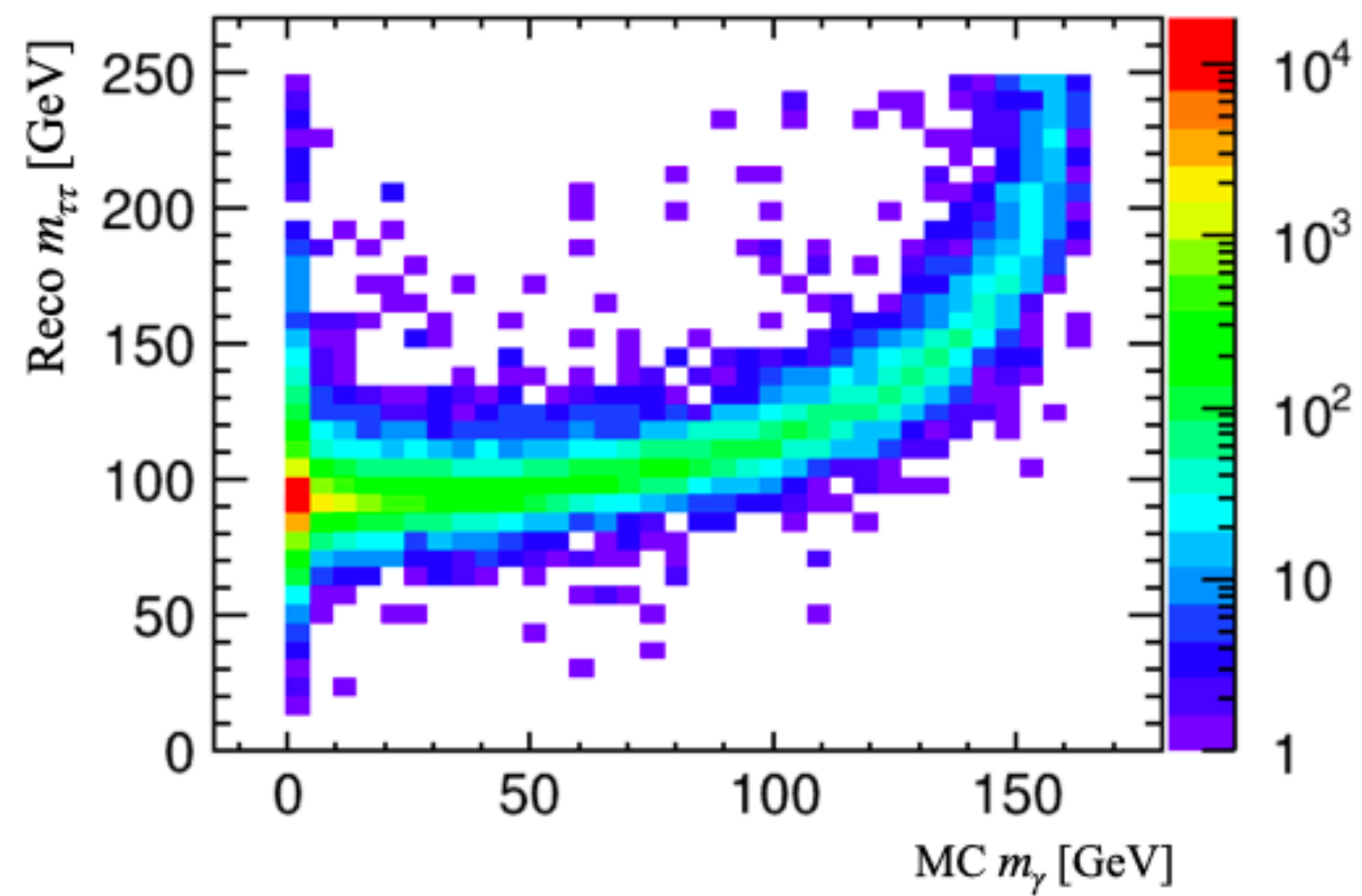
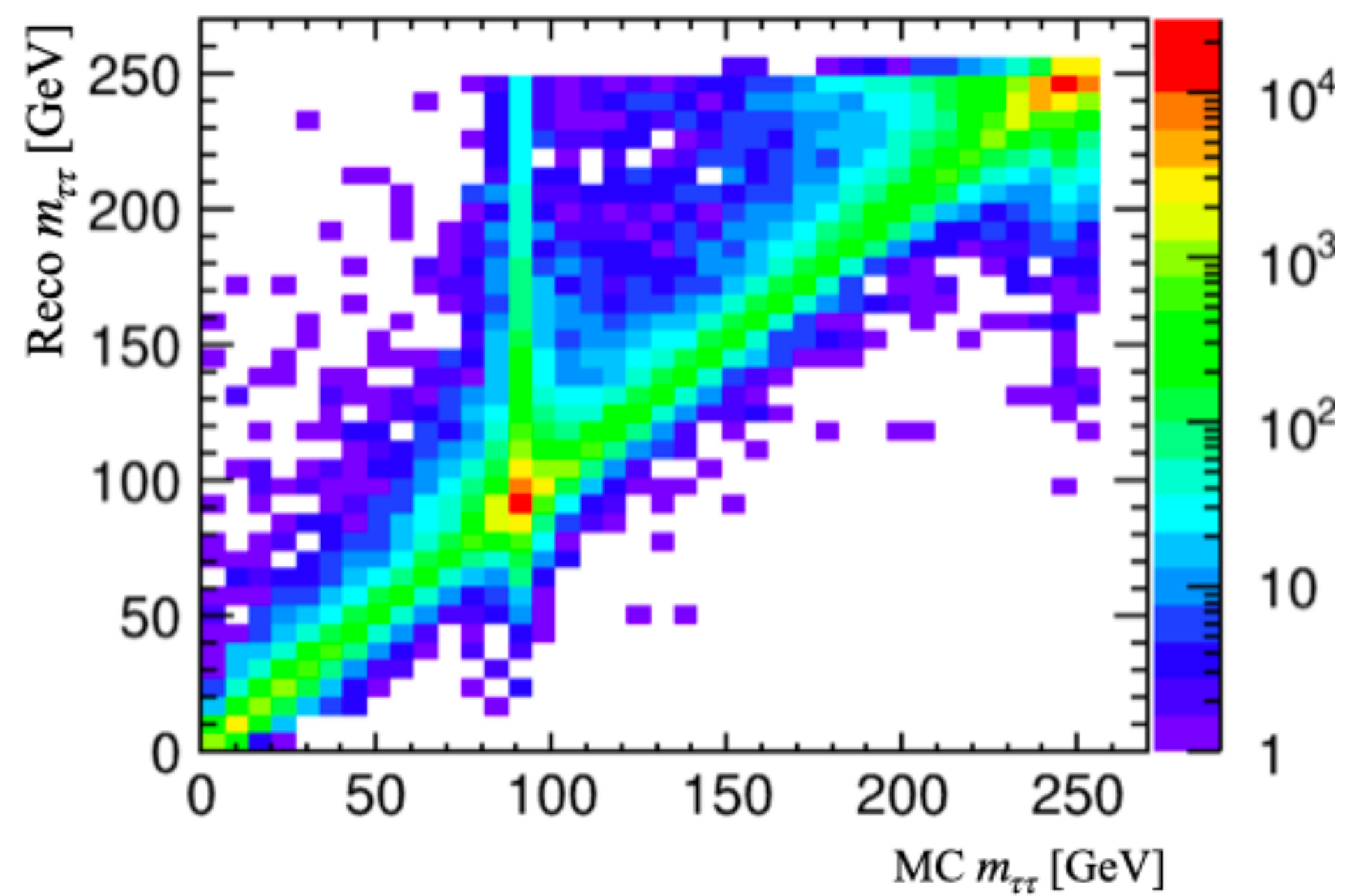
$$\text{weight } w = \frac{1}{n_{\tau} \cdot n_{sol}}$$

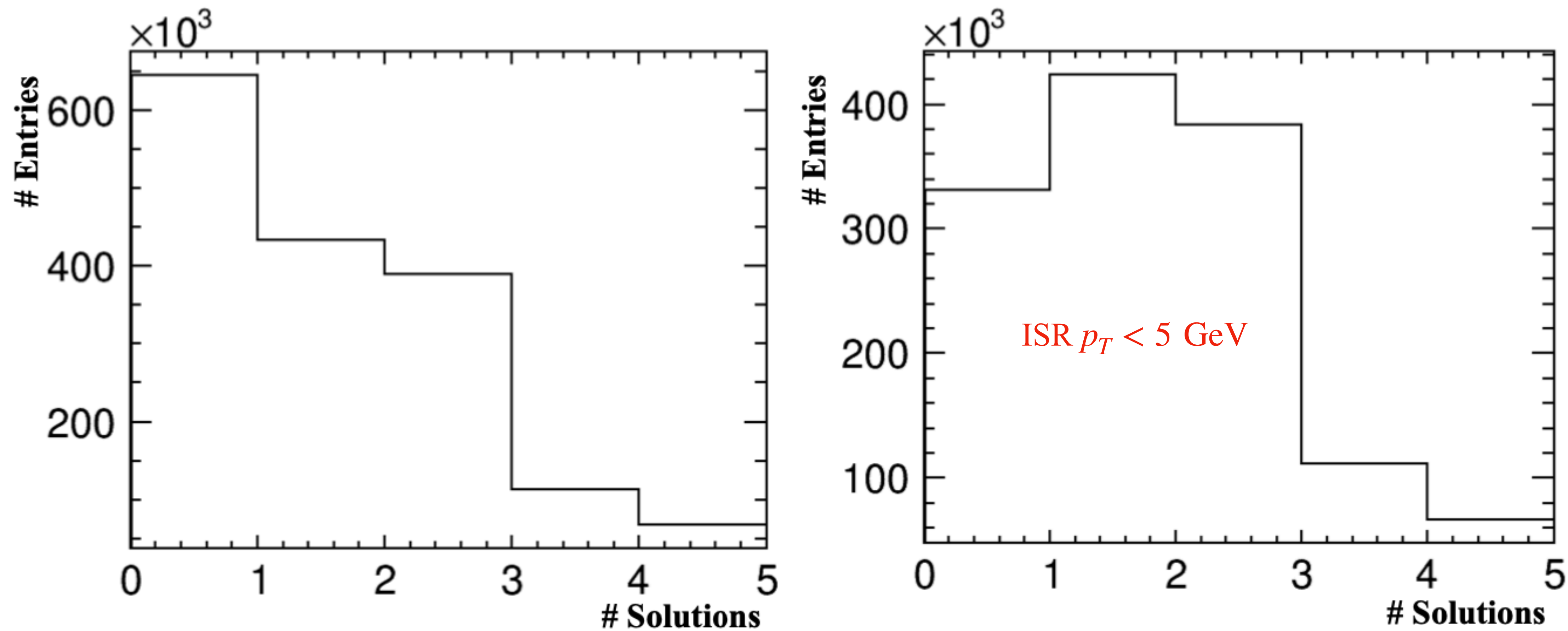
cf.

two taus have a polarimeter : each tau has one solution =>  $n_{\tau} = 2, n_{sol} = 1$   
 two solutions =>  $n_{\tau} = 2, n_{sol} = 2$





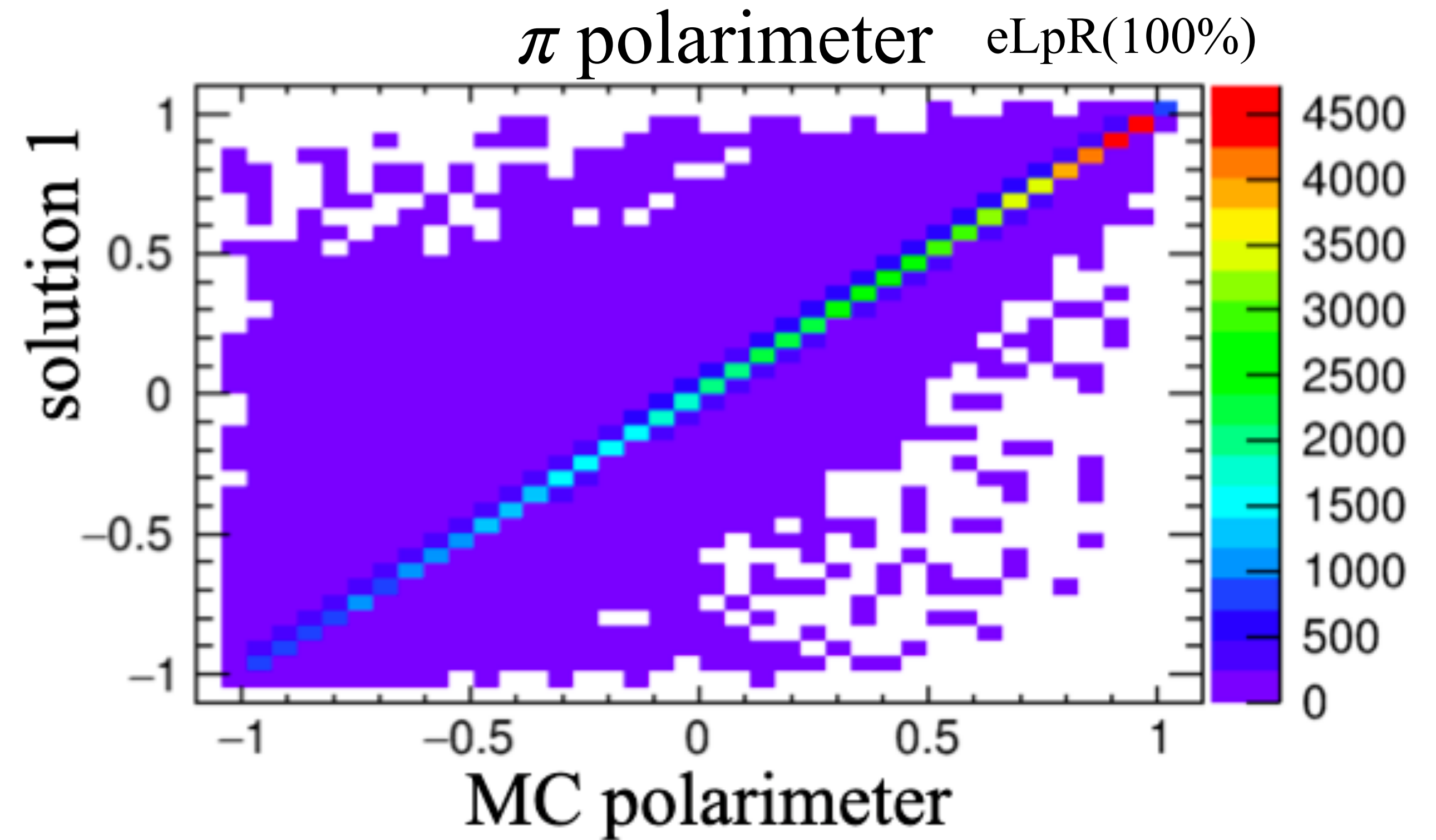
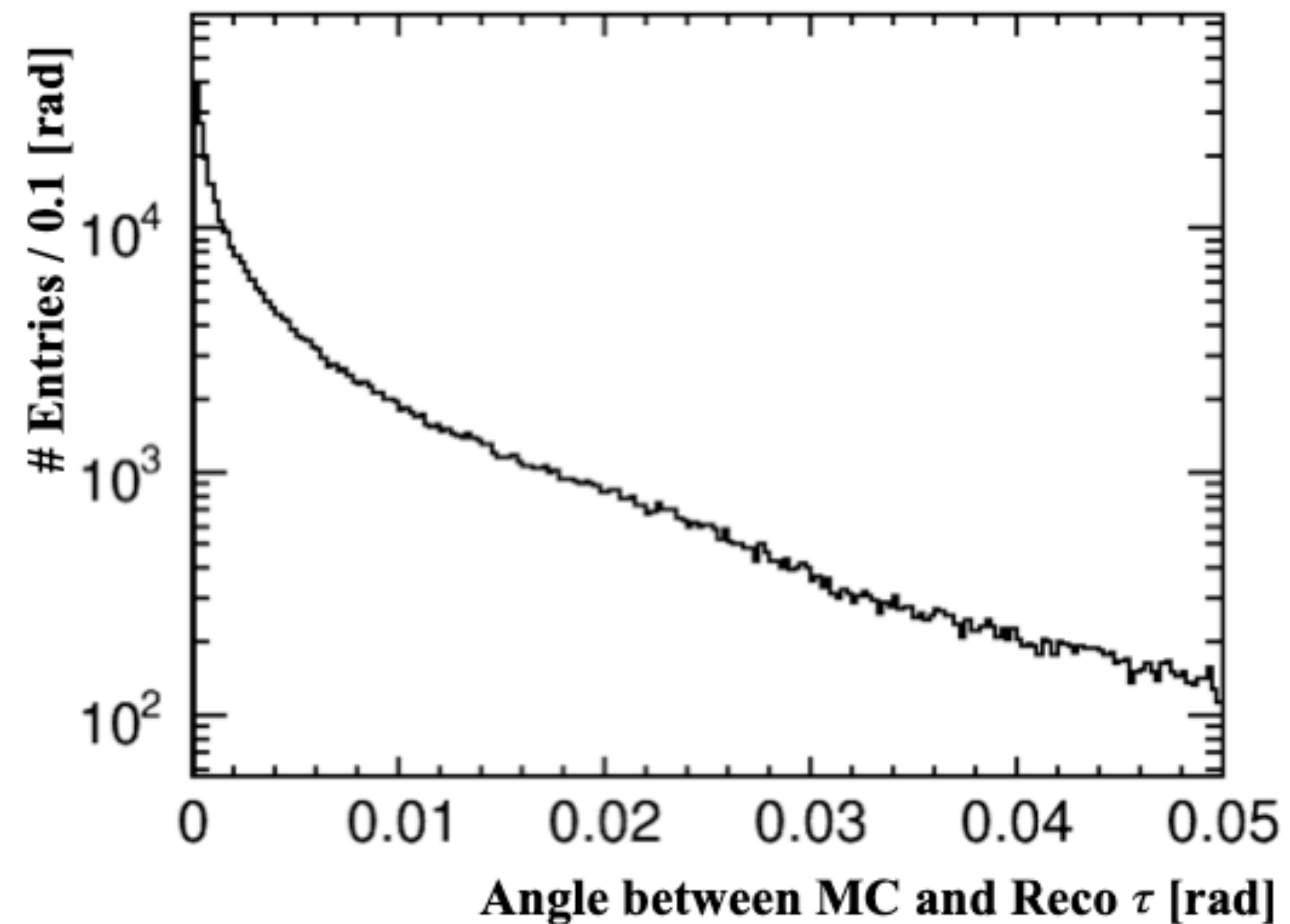
reconstructed  $m_{\tau\tau}$  vs MC  $m_{\tau\tau}$ 



The number of solutions, in all  $e^-e^+ \rightarrow \tau^-\tau^+$  events (left) and those with small ( $< 5$  GeV)



# Comparison with MC



The reconstructed direction is typically within a few mrad of the true direction.

reasonable agreement between MC and reconstructed tau