Beyond the Standard Model effects on neutrino flavor Experimental overview and prospects: High energies: neutrinos above the TeV scale To be published, ArXiv:2203.10811

> Teppei Katori King's College London Snowmass21 workshop, Seattle, July 24, 2022

> > 22/07/24



Beyond the Standard Model effects on Neutrino Flavor

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SNOWMASS WHITE PAPER: BEYOND THE STANDARD MODEL EFFECTS ON NEUTRINO FLAVOR

> SUBMITTED TO THE PROCEEDINGS OF THE US COMMUNITY STUDY ON THE FUTURE OF PARTICLE PHYSICS (SNOWMASS 2021)

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Beyond the Standard Model effects on Neutrino Flavor

Natural place to look for new physics

- 1. Longest propagation distance (> pc)
- 2. Direct highest energy particles (> 10TeV)
- 3. Quantum mixing

"Neutrino flavour effect" covers many topics in particle physics!

We want to discover any of these!

- Lorentz and CPT violation
- Long-range interaction
- Dark matter-neutrino interaction
- Dark energy-neutrino interaction
- Neutrino self-interaction
- Non-standard interaction
- Neutrino decay
- Neutrino decoherence
- Sterile neutrinos
- Extra dimension, etc





Astrophysical neutrino flavour physics

Natural place to look for new physics

- 1. Longest propagation distance (> pc)
- 2. Direct highest energy particles (> 10TeV)
- 3. Quantum mixing

Neutrino mixing (neutrino frontier)

Astrophysical Neutrino
Flavor PhysicsHighest energy
(energy frontier)Astrophysical
scale
(cosmic frontier)



Astrophysical neutrino flavour physics

Flavour information is sensitive to the leading order of new physics

$$H = H_{SM} + H_{BSM}$$
$$P = |H_{SM}|^2 + |H_{SM} \cdot H_{BSM}| + |H_{BSM}|^2 + \cdots$$

We need high statistics flavour data to look for new physics



Astrophysical neutrino flavour physics

Flavour information is sensitive to the leading order of new physics

$$H = H_{SM} + H_{BSM}$$

$$P = |H_{SM}|^2 + |H_{SM} \cdot H_{BSM}| + |H_{BSM}|^2 + \cdots$$

Standard neutrino Hamiltonian in vacuum

$$H_{SM} \sim \frac{m^2}{2E}$$

In highest energy, SM term is suppressed, BSM term becomes relatively larger

$$P = |H_{SM}|^2 + |H_{SM} \cdot H_{BSM}| + |H_{BSM}|^2 + \cdots$$

Higher-energy neutrinos have better sensitivity to new physics



Song et al, JCAP04(2021)054

Astrophysical neutrino flavour physics

The goal is to find

$$P \neq P_{SM}(\Delta m^2 \pm \delta \Delta m^2, \theta \pm \delta \theta)$$

Sensitivity is improved by better oscillation parameter measurements





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Song et al, JCAP04(2021)054

Astrophysical neutrino flavour physics

Astrophysical neutrino flavour simulation depends on astrophysical neutrino flavour assumption at the source

$$f_{\beta,\bigoplus} = \sum_{\beta}^{3} P_{\alpha \to \beta} (H_{SM, H_{BSM}}) \times f_{\alpha,S}$$

New physics sensitivity depends on astrophysical neutrino production model





IceCube, PRD104(2021)022002, ArXiv:2011:03560

Astrophysical neutrino flavour physics (2022)

IceCube data allows almost all astrophysical neutrino flavour ratio

- New physics limits have astrophysical neutrino production model dependencies

$$h_{eff} \sim \frac{1}{2E} U^{\dagger} M^{2} U + a_{\alpha\beta}^{(3)} - E c_{\alpha\beta}^{(4)} + E^{2} a_{\alpha\beta}^{(5)} - E^{3} c_{\alpha\beta}^{(6)} \cdots$$



06

Bayes Factor > 10

Bayes Factor > 31.6

0.8

Key

 $\mathbb{Re}(\overset{(3)}{a}_{\mu\tau})$ atm. limit (90%)

 $(0:0:)^{s}$

1.0

Summary

Astrophysical neutrino flavour physics is a cross-frontier topic.

- Neutrino frontier, high-energy frontier, cosmic frontier

Very high discovery potential is supported by an interdisciplinary study

- Theory & experiment, particle physics & astrophysics



Summary

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High-precision oscillation measurement

Astrophysical Neutrino Flavor Physics

High statistics Astrophysical flavour data neutrino production model



Summary

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Neutrino telescopes

High-Energy (IceCube, ANTARES, KM3NeT, P-ONE, Baikal-GVD, etc) Ultra-high-energy (IceCube-Gen2, TAMBO, Trinity, RET-N, ARIANNA, RNO-G, GRAND, POEMMA, BEACON, PUEO, Trinity, EUSO-SPB2, Auger/GCOS, etc)

High-precision oscillation measurement

Oscillation experiments

Beam (T2K, NOvA, DUNE, Hyper-Kamiokande) Atmospheric (Super-Kamiokande, DUNE, Hyper-Kamiokande, IceCube-Upgrade, KM3NeT, INO) Reactor (JUNO), etc

Astrophysical Neutrino Flavor Physics

High statistics Astrophysical Te flavour data neutrino production model

Multi-messenger astronomy

Optics (Radio, infrared, VIS, UV, Xray, γ-ray) Comic rays (Auger, TA, GCOS, etc) Gravitational wave (LIGO, VARGO, KAGRA, LIGO-India, Einstein Telescope, LISA, etc)



Backup



Beyond the Standard Model effects on Neutrino Flavor

Fundamental physics with high-energy cosmic neutrinos today and in the future

- Natural place to look for new physics
- 1. Longest propagation distance (> pc)
- 2. Direct highest energy particles (> 10TeV)
- 3. Quantum mixing





Non-standard interactions

Atmospheric neutrinos cover ~100MeV - 20 TeV (conventional) coming from all direction (diffuse). However, direction is related to the propagation distance.

→ They are the highest energy particles (~20 TeV) with the longest baseline (12700km) propagating the high-density material (~13g/cm³) on Earth.



$$h_{eff} \sim \frac{1}{2E} M^2 + V_{CC}, \quad P_{\alpha\beta} = \left| \left\langle \nu_{\alpha} \left| U(h_{eff}, t) \right| \nu_{\beta} \right\rangle \right|^2$$
$$M^2 = \begin{pmatrix} m_{ee}^2 & m_{e\mu}^2 & m_{\tau e}^2 \\ \left(m_{e\mu}^2 \right)^* & m_{\mu\mu}^2 & m_{\mu\tau}^2 \\ \left(m_{\tau e}^2 \right)^* & \left(m_{\mu\tau}^2 \right)^* & m_{\tau\tau}^2 \end{pmatrix}, \quad V_{CC} = \begin{pmatrix} \sqrt{2}G_F n_e & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

Non-standard interaction limits in IceCube is order $\sim 10^{-25}$ GeV

cf) The highest precision hydrogen 1S-2S transition (PRL107(2011)203001) Fractional frequency uncertainty ~ $4x10^{-15} \rightarrow$ new physics sensitivity ~ 10^{-23} GeV



Flavor new physics search with effective operators

Standard Model Extension (SME) is an effective field theory to look for Lorentz violation

Standard Model New physics
$$L = i\bar{\psi}\gamma^{\mu}\partial_{\mu}\psi - m\bar{\psi}\psi + \bar{\psi}\gamma^{\mu}a_{\mu}\psi + \bar{\psi}\gamma^{\mu}c_{\mu\nu}\partial^{\nu}\psi \cdots$$

Effective Hamiltonian can be written from here



Astrophysical neutrino flavour sensitivity of dim-6 operator goes beyond the natural scale $c^{(6)} \sim \frac{1}{M_{Planck}^2} \sim 10^{-38} GeV^{-2}$, first time in any known scientific system



Flavor new physics search with effective operators

Neutrino oscillation formula is written with mixing matrix elements and eigenvalues

$$P_{\alpha \to \beta}(E,L) = 1 - 4\sum_{i>j} Re\left(V_{\alpha i}^* V_{\beta i}^* V_{\alpha j} V_{\beta j}\right) \sin^2\left(\frac{\lambda_i - \lambda_j}{2}L\right) + 2\sum_{i>j} Im\left(V_{\alpha i}^* V_{\beta i}^* V_{\alpha j} V_{\beta j}\right) \sin\left(\left(\lambda_i - \lambda_j\right)L\right)$$

However, astrophysical neutrinos propagate $O(100Mpc) \rightarrow lost$ coherence

$$P_{\alpha \to \beta}(E, \infty) \sim 1 - 2 \sum_{i>j} Re\left(V_{\alpha i}^* V_{\beta i}^* V_{\alpha j} V_{\beta j}\right) = \sum_i |V_{\alpha i}|^2 |V_{\beta i}|^2$$

Astrophysical neutrino flux of flavour α at production is $\phi^p_{\alpha}(E) \sim \phi^P_{\alpha} \cdot E^{-\gamma}$. Since it's low statistics, we consider energy-averaged flavour composition β on Earth

$$\bar{\phi}_{\beta}^{\oplus} = \frac{1}{\Delta E} \int_{\Delta E} \sum_{\alpha} P_{\alpha \to \beta}(E, \infty) \, \phi_{\alpha}^{p}(E) dE$$

We take the fraction of this for each flavour.

$$f^{\oplus}_{\beta} = \frac{\bar{\phi}^{\oplus}_{\beta}}{\sum_{e,\mu,\tau} \bar{\phi}^{\oplus}_{\gamma}}$$



High-energy astrophysical neutrino flavour

High-energy particles (>60 TeV) propagating a long distance (>100 Mpc) - Neutrinos can probe new physics in the universe



IceCube, PRL114(2015)171102, Astro.J.809:98(2015), PRD99(2019)032004, ArXiv:2011:03560



HESE 7.5-yr flavor ratio (2018)





We are mainly testing scenarios where we assume astrophysical neutrino productions are dominated by ν_e or ν_μ

IceCube, Nature Physics 14 (2018) 961 Mewes, Nature 560 (2018) 316

Neutrino interferometry – Atmospheric neutrinos

dim.	method	type	sector	limits	ref.
3	CMB polarization	astrophysical	photon	$\sim 10^{-43} { m GeV}$	[6]
	He-Xe comagnetometer	tabletop	neutron	$\sim 10^{-34}~{ m GeV}$	[10]
	torsion pendulum	tabletop	electron	$\sim 10^{-31}~{ m GeV}$	[12]
	muon g-2	accelerator	muon	$\sim 10^{-24}~{ m GeV}$	[13]
	neutrino oscillation	$\operatorname{atmospheric}$	neutrino	$ \operatorname{Re}(\mathring{a}_{\mu\tau}^{(3)}) , \operatorname{Im}(\mathring{a}_{\mu\tau}^{(3)}) \stackrel{< 2.9 \times 10^{-24} \text{ GeV } (99\% \text{ C.L.})}{< 2.0 \times 10^{-24} \text{ GeV } (90\% \text{ C.L.})}$	this work
4	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-38}$	[7]
	Laser interferometer	LIGO	photon	$\sim 10^{-22}$	[8]
	Sapphire cavity oscillator	tabletop	photon	$\sim 10^{-18}$	[5]
	Ne-Rb-K comagnetometer	tabletop	neutron	$\sim 10^{-29}$	[11]
	trapped Ca ⁺ ion	tabletop	electron	$\sim 10^{-19}$	[14]
	neutrino oscillation	atmospheric	neutrino	$ \operatorname{Re}(\mathring{c}^{(4)}_{\mu\tau}) , \operatorname{Im}(\mathring{c}^{(4)}_{\mu\tau}) \stackrel{< 3.9 \times 10^{-28}}{< 2.7 \times 10^{-28}} (90\% \text{ C.L.}) \stackrel{< 0.1}{< 2.7 \times 10^{-28}}$	this work
5	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-34}~{ m GeV^{-1}}$	[7]
	ultra-high-energy cosmic ray	astrophysical	proton	$\sim 10^{-22}$ to 10^{-18} GeV ⁻¹	[9]
	neutrino oscillation	$\operatorname{atmospheric}$	neutrino	$\frac{\operatorname{Re}(\mathring{a}_{\mu\tau}^{(5)}) , \operatorname{Im}(\mathring{a}_{\mu\tau}^{(5)}) }{< 1.5 \times 10^{-32} \text{ GeV}^{-1} (99\% \text{ C.L.})} $	this work
6	GRB vacuum birefringene	astrophysical	photon	$\sim 10^{-31} { m GeV}^{-2}$	[7]
	ultra-high-energy cosmic ray	astrophysical	proton	$\sim 10^{-42}$ to 10^{-35} GeV ⁻²	[9]
	gravitational Cherenkov radiation	astrophysical	gravity	$\sim 10^{-31} { m GeV}^{-2}$	[15]
	neutrino oscillation	$\operatorname{atmospheric}$	neutrino	$\frac{ \hat{c}_{\mu\tau}^{(6)} }{ \mathbf{Im}(\hat{c}_{\mu\tau}^{(6)}) } \leq 1.5 \times 10^{-36} \text{ GeV}^{-2} (99\% \text{ C.L.}) \leq 9.1 \times 10^{-37} \text{ GeV}^{-2} (90\% \text{ C.L.})$	this work
7	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-28} { m GeV^{-3}}$	[7]
	neutrino oscillation	$\operatorname{atmospheric}$	neutrino	$\frac{\operatorname{Re}(\mathring{a}_{\mu\tau}^{(7)}) , \operatorname{Im}(\mathring{a}_{\mu\tau}^{(7)}) }{< 3.6 \times 10^{-41} \text{ GeV}^{-3} (99\% \text{ C.L.})} $	this work
8	gravitational Cherenkov radiation	astrophysical	gravity	$\sim 10^{-46} { m GeV^{-4}}$	[15]
	neutrino oscillation	$\operatorname{atmospheric}$	neutrino	$\frac{ \operatorname{Re}(\hat{c}_{\mu\tau}^{(8)}) }{ \operatorname{Im}(\hat{c}_{\mu\tau}^{(8)}) } \leq 5.2 \times 10^{-45} \text{ GeV}^{-4} (99\% \text{ C.L.}) \leq 1.4 \times 10^{-45} \text{ GeV}^{-4} (90\% \text{ C.L.})$	this work

TABLE I: Comparison of attainable best limits of SME coefficients in various fields.



IceCube atmospheric neutrino limit, $c^{(6)} < 10^{-36} GeV^{-2}$ This is close to the target signal region, $c^{(6)} \sim 10^{-38} GeV^{-2}$

Neutrino interferometry – Atmospheric neutrinos

Strong limits on many parameters but they depend on the source flavour assumptions.

Substantial limits for $\tau \tau \xi$ parameters are obtained through quantum Zeno effect

dim coefficient limit (BF> 10)

 $2 \times 10^{-26} \text{ GeV}$

 2×10^{-31}

 $2 \times 10^{-37} \text{ GeV}^{-1}$

 $3\times 10^{-42}~{\rm GeV^{-2}}$

 $3 \times 10^{-47} \text{ GeV}^{-3}$

 $2\times 10^{-52}~{\rm GeV^{-4}}$

 $\operatorname{Re}(\mathring{a}_{\tau\tau}^{(3)})$

 $\operatorname{Re}(\mathring{c}_{\tau\tau}^{(4)})$

 $\operatorname{Re}(\mathring{a}_{\tau\tau}^{(5)})$

 $\operatorname{Re}(\mathring{c}_{\tau\tau}^{(6)})$

 $\operatorname{Re}(\mathring{a}_{\tau\tau}^{(7)})$

Re ($\mathring{c}_{\tau\tau}^{(8)}$)





3

4

5

6

7

8

Neutrino flavor ratio ($v_e : v_\mu : v_\tau$)



Neutrino flavor ratio ($v_e : v_\mu : v_\tau$)



Neutrino flavor ratio ($v_e : v_\mu : v_\tau$)



Neutrino flavor ratio ($v_e : v_u : v_\tau$)

Astrophysical neutrino production mechanism is not known \rightarrow production flavour ratio is not known 0.01.0

Flavour ratio on Earth is different due to mixing by neutrino masses

All possible flavour ratio is confined in a small space

e.g.) New physics just below the limit can produce any flavour ratio



