



# 2019 papers by Stephen Parke



1. **“Scalar Nonstandard Interactions in Neutrino Oscillation”**  
S. F. Ge and S. J. Parke.  
arXiv:1812.08376 [hep-ph]  
DOI:10.1103/PhysRevLett.122.211801  
Phys. Rev. Lett. **122**, no. 21, 211801 (2019)  
IPMU18-0206, FERMILAB-PUB-18-487-T  
[INSPIRE-HEP entry](#)
2. **“Neutrino Oscillation Probabilities through the Looking Glass”**  
G. Barenboim, P. B. Denton, S. J. Parke and C. A. Ternes.  
arXiv:1902.00517 [hep-ph]  
DOI:10.1016/j.physletb.2019.03.002  
Phys. Lett. B **791**, 351 (2019)  
IFIC/19-07, FERMILAB-PUB-19-009-T  
[INSPIRE-HEP entry](#)
3. **“Simple and Precise Factorization of the Jarlskog Invariant for Neutrino Oscillations in Matter”**  
P. B. Denton and S. J. Parke.  
arXiv:1902.07185 [hep-ph]  
DOI:10.1103/PhysRevD.100.053004  
Phys. Rev. D **100**, no. 5, 053004 (2019)  
FERMILAB-PUB-19-072-T  
[INSPIRE-HEP entry](#)
4. **“Comment on Daya Bay’s Definition and Use of  $\Delta m_{ee}^2$ ”**  
S. J. Parke and R. Zukanovich-Funchal.  
arXiv:1903.00148 [hep-ex]  
FERMILAB-PUB-19-078-T  
[INSPIRE-HEP entry](#)
5. **“Sub-GeV Atmospheric Neutrinos and CP-Violation in DUNE”**  
K. J. Kelly, P. A. Machado, I. Martinez Soler, S. J. Parke and Y. F. Perez Gonzalez.  
arXiv:1904.02751 [hep-ph]  
DOI:10.1103/PhysRevLett.123.081801  
Phys. Rev. Lett. **123**, no. 8, 081801 (2019)  
FERMILAB-PUB-19-136-T, NUHEP-TH/19-03  
[INSPIRE-HEP entry](#)
6. **“Compact Perturbative Expressions for Oscillations with Sterile Neutrinos in Matter”**  
S. J. Parke and X. Zhang.  
arXiv:1905.01356 [hep-ph]  
FERMILAB-PUB-19-042-T  
[INSPIRE-HEP entry](#)
7. **“Constraint on the solar  $\Delta m^2$  using 4,000 days of short baseline reactor neutrino data”**  
A. Hernandez-Cabezudo, S. J. Parke and S. H. Seo.  
arXiv:1905.09479 [hep-ex]  
FERMILAB-PUB-19-190-T  
[INSPIRE-HEP entry](#)
8. **“Eigenvalues: the Rosetta Stone for Neutrino Oscillations in Matter”**  
P. B. Denton, S. J. Parke and X. Zhang.  
arXiv:1907.02534 [hep-ph]  
FERMILAB-PUB-19-326-T  
[INSPIRE-HEP entry](#)
9. **“Eigenvectors from Eigenvalues”**  
P. B. Denton, S. J. Parke, T. Tao and X. Zhang.  
arXiv:1908.03795 [math.RA]  
FERMILAB-PUB-19-377-T  
[INSPIRE-HEP entry](#)
10. **“Fibonacci Fast Convergence for Neutrino Oscillations in Matter”**  
P. B. Denton, S. J. Parke and X. Zhang.  
arXiv:1909.02009 [hep-ph]  
FERMILAB-PUB-19-462-T  
[INSPIRE-HEP entry](#)
11. **“Why matter effects matter for JUNO”**  
A. N. Khan, H. Nunokawa and S. J. Parke.  
arXiv:1910.12900 [hep-ph]  
FERMILAB-PUB-19-490-T  
[INSPIRE-HEP entry](#)



4 papers:



**3 & 3+**  
**Neutrino**  
**Flavor Transformations**  
**Matter/Vacuum**



4 papers:



**hep-ph:**

**Simple and Precise (~0.04%)  
Factorization of Jarlskog  
in Matter**





4 papers:

hep-ph:

Simple and Precise (~0.04%)  
Factorization of Jarlskog  
in Matter

hep-ex:

Measurement of  $\Delta m_{21}^2$   
by Daya Bay/RENO

$$\Delta m_{21}^2 \leq \frac{1}{15} \Delta m_{ee}^2$$





4 papers:



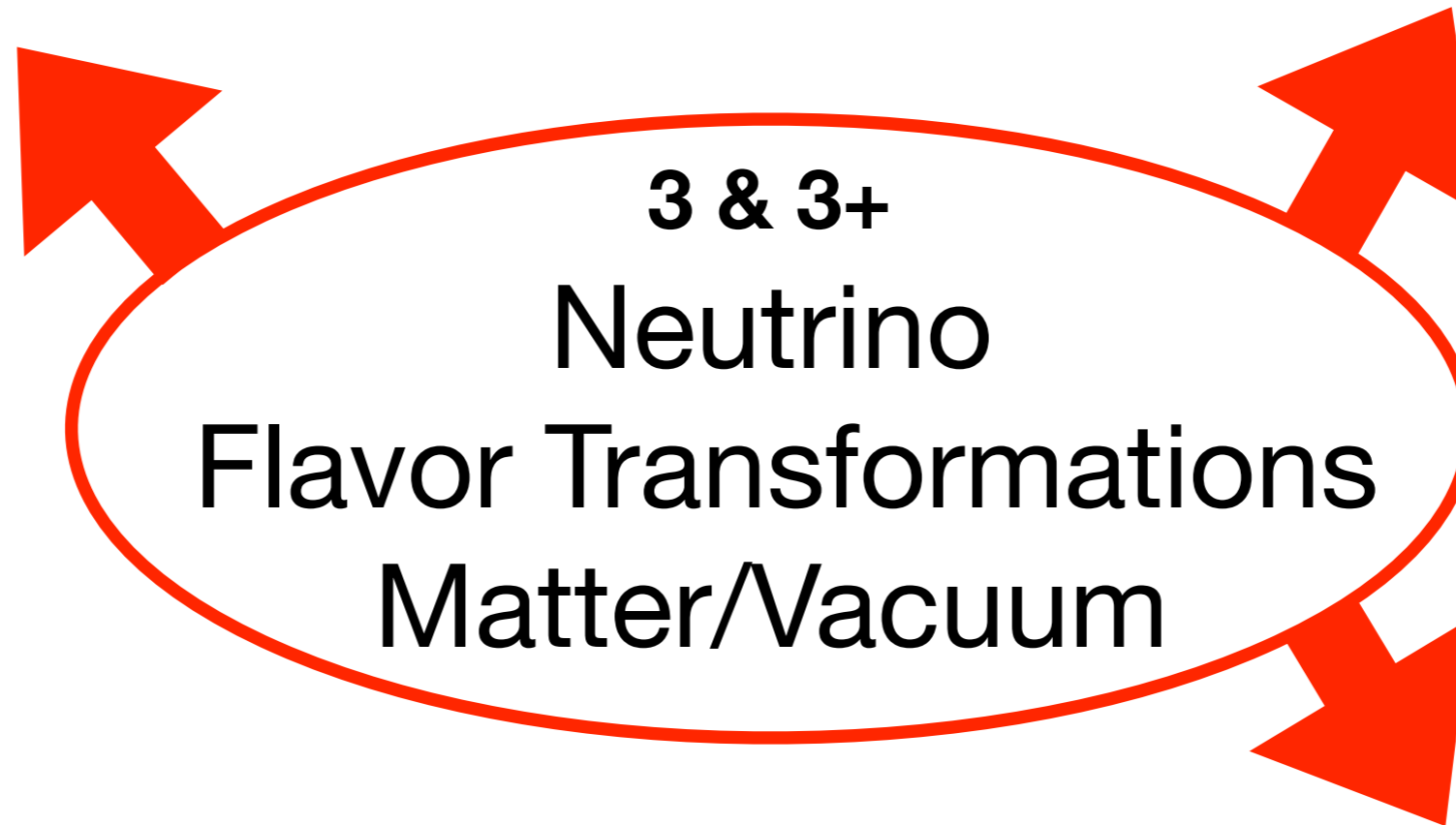
hep-ph:

Simple and Precise ( $\sim 0.04\%$ )  
Factorization of Jarlskog  
in Matter

hep-ex:

Measurement of  $\Delta m_{21}^2$   
by Daya Bay/RENO

$$\Delta m_{21}^2 \leq \frac{1}{15} \Delta m_{ee}^2$$



hep-ph:

New simple relationship  
between eigenvalues,  $\widehat{m^2}_i$ ,  
and mixing angles,  $\widehat{\theta}_{jk}$ , in matter;  
(Rosetta)



4 papers:

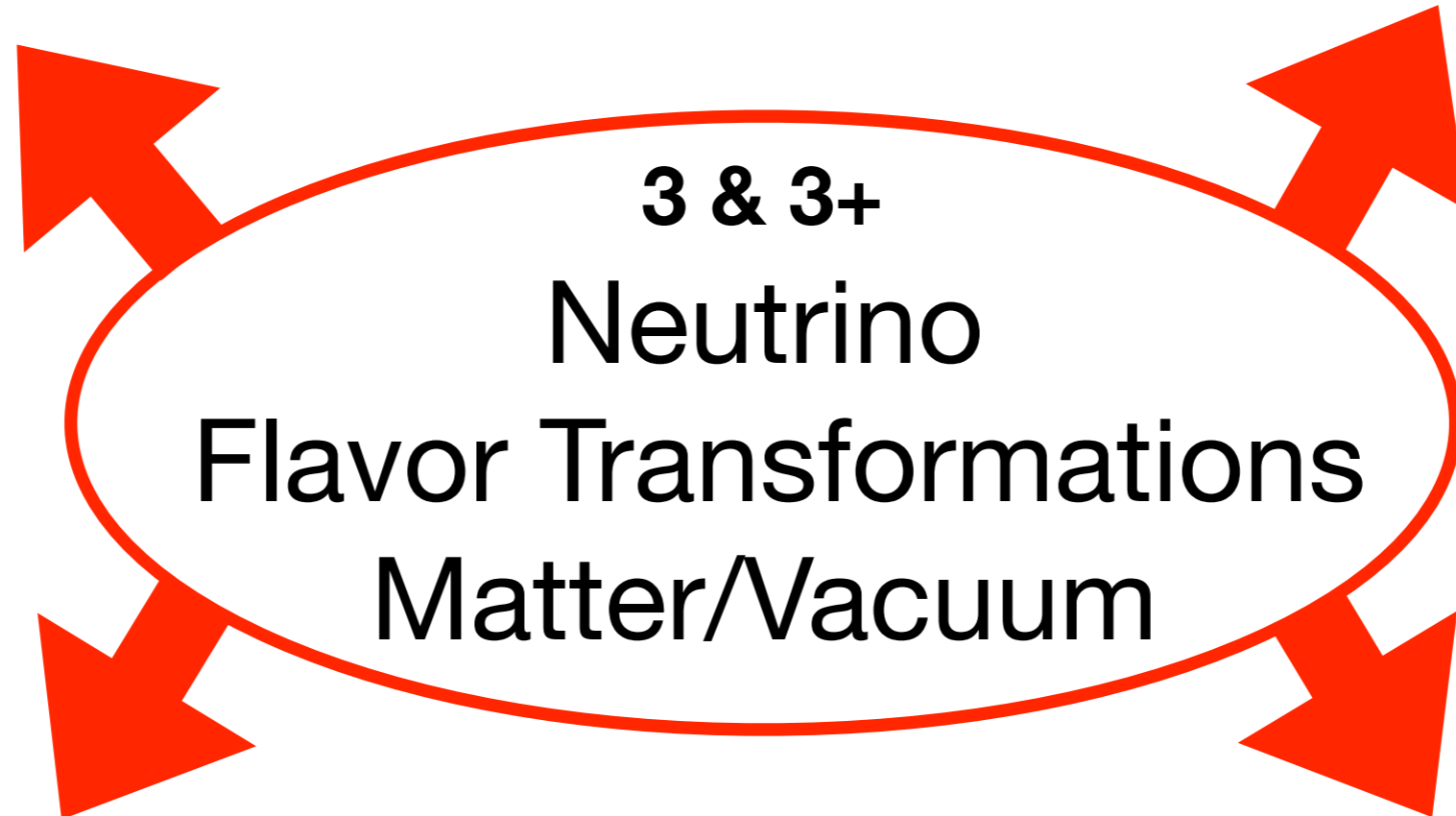
hep-ph:

Simple and Precise (~0.04%)  
Factorization of Jarlskog  
in Matter

hep-ex:

Measurement of  $\Delta m_{21}^2$   
by Daya Bay/RENO

$$\Delta m_{21}^2 \leq \frac{1}{15} \Delta m_{ee}^2$$

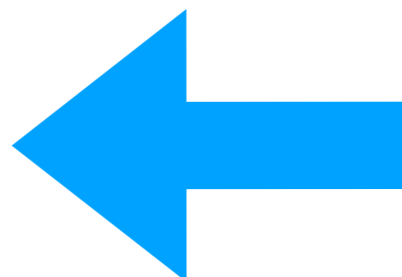


math.RA

generalized and proven  
for an arbitrary NxN Hermitian matrix  
with the mathematician T. Tao

hep-ph:

New simple relationship  
between eigenvalues,  $\widehat{m^2}_i$ ,  
and mixing angles,  $\widehat{\theta}_{jk}$ , in matter;  
(Rosetta)





# Generalization to nxn:

- Let  $H$  be an  $n \times n$  Hermitian matrix with eigenvalues  $\lambda_i(H)$  and eigenvectors  $v_i$
- Let  $h_j$  be the  $(n-1) \times (n-1)$  Hermitian matrix from  $H$  with  $j$ -th row and  $j$ -th column deleted with eigenvalues  $\lambda_i(h_j)$

(  $h_j$  principal minor of  $H$  )

$$|v_{i,j}|^2 = \frac{\prod_{k=1}^{n-1} (\lambda_i(H) - \lambda_k(h_j))}{\prod_{k=1, k \neq i}^n (\lambda_i(H) - \lambda_k(H))}$$

- **Phase information** is a more complicated expression.
- **Numerator** is characteristic function for  $h_j$  evaluated at  $\lambda_i(H)$
- **Normalized**  $\sum_i |v_{i,j}|^2 = 1 = \sum_j |v_{i,j}|^2$

Peter Denton, SP, Terrence Tao, Xining Zhang: [arXiv:1908.03759](https://arxiv.org/abs/1908.03759) [math.RA]

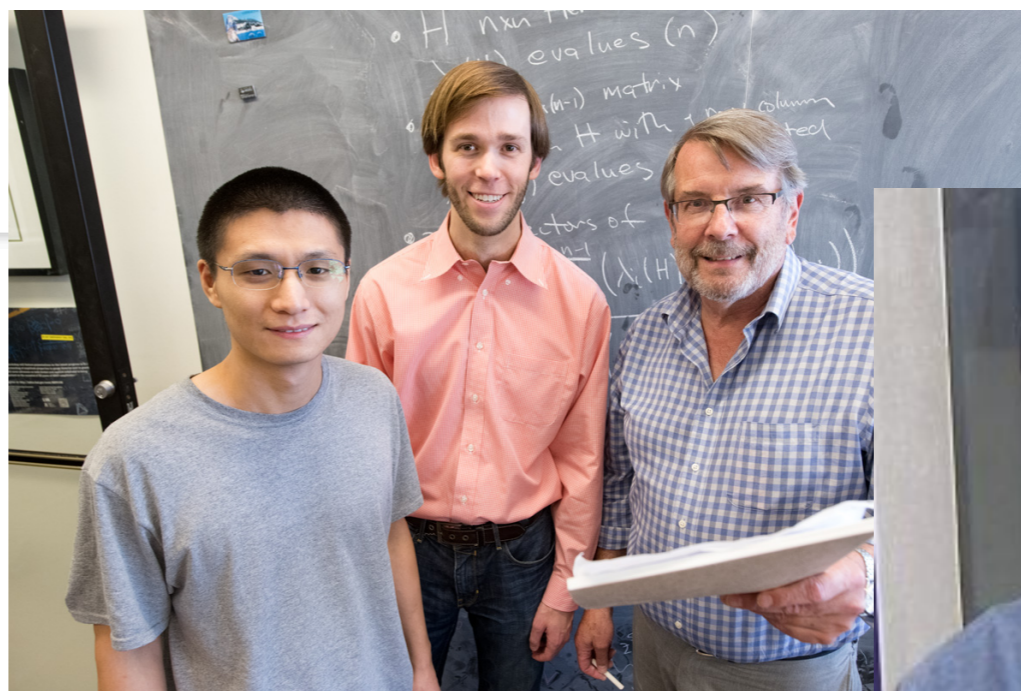


# Neutrinos Lead to Unexpected Discovery in Basic Math

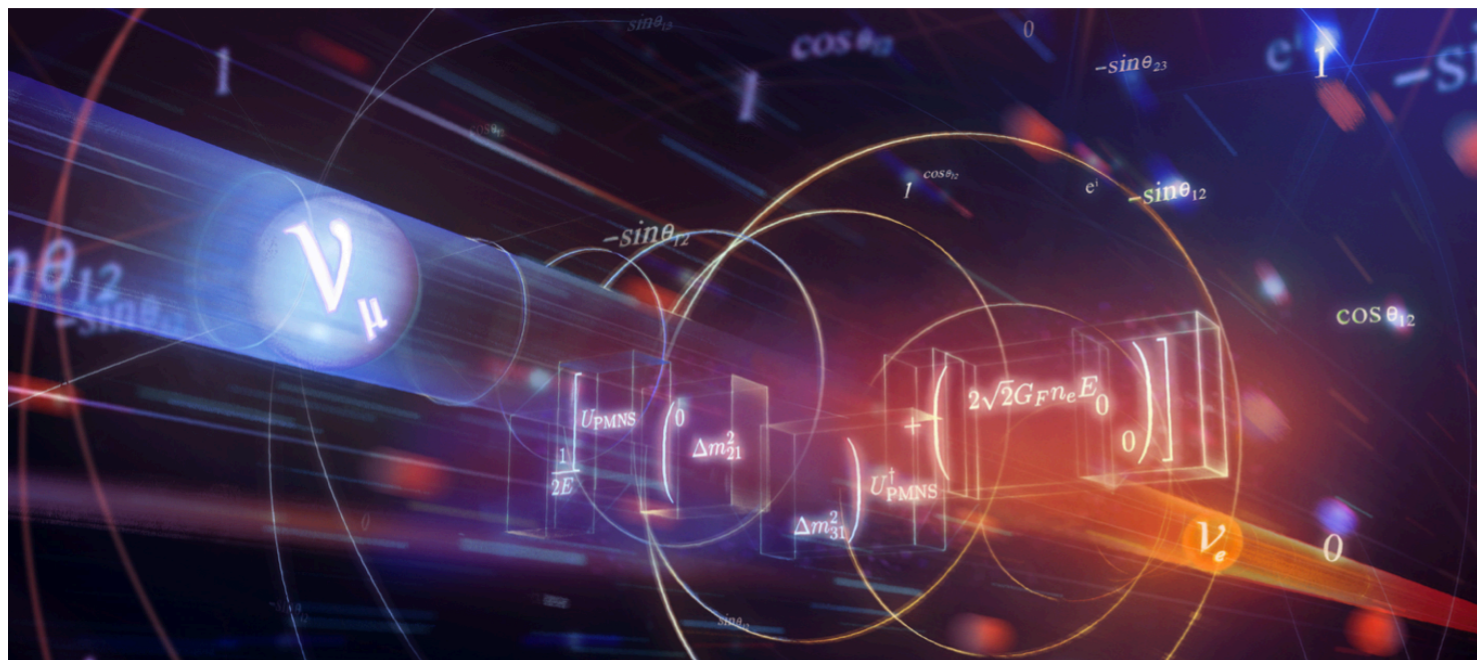
By NATALIE WOLCHOVER

November 13, 2019

Three physicists wanted to calculate how neutrinos change. They ended up discovering an unexpected relationship between some of the most ubiquitous objects in math.



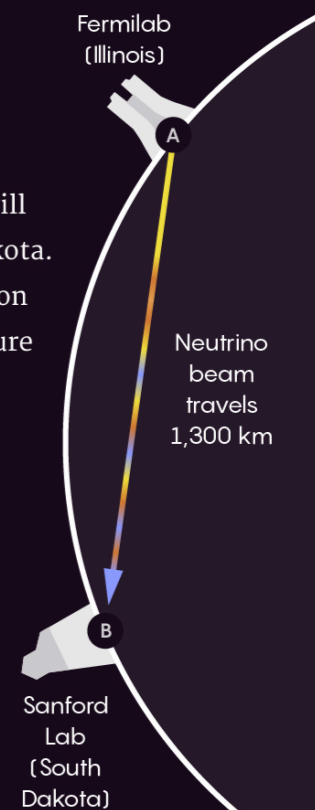
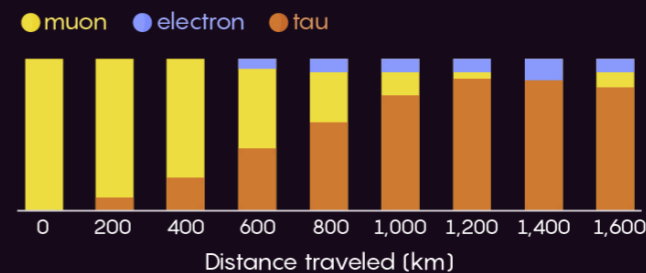
<https://paw.princeton.edu/article/mind-mathematician>



## The Neutrino Express

Neutrinos are ephemeral in more ways than one. They pass straight through matter, and they also change their type, or "flavor," as they move. In the DUNE experiment, now under construction, a fire hose of muon neutrinos (and antineutrinos) will be shot through the earth from Illinois to South Dakota. During the journey, many will transform into electron neutrinos (and antineutrinos). Physicists will measure the rates of change in the hopes of learning why the universe has more matter than antimatter.

### PROBABILITY OF DETECTING NEUTRINO FLAVOR





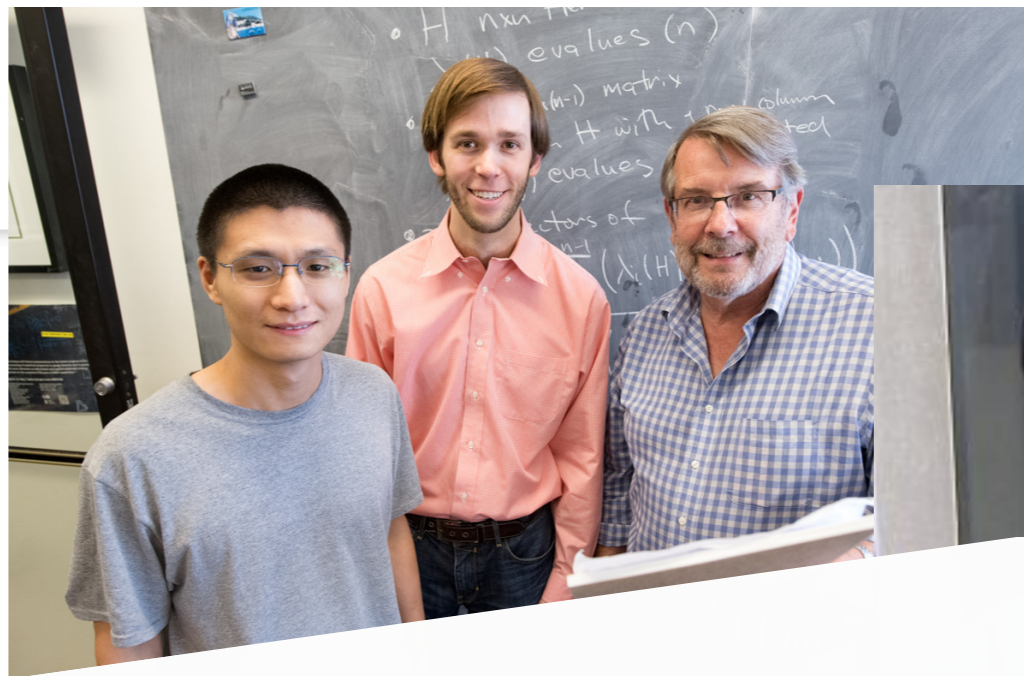


# Neutrinos Lead to Unexpected Discovery in Basic Math

By NATALIE WOLCHOVER

November 13, 2019

Three physicists wanted to calculate... ended up...



mathematician

FermiNews article 9/23/2019

From: Nigel S. Lockyer lockyer@fnal.gov  
Subject: Congratulations  
Date: September 27, 2019 at 5:39 PM  
To: Stephen Parke parke@fnal.gov  
Cc: Joseph Lykken lykken@fnal.gov

Stephen,

Read the article on your linear algebra discovery. Very impressive. Connected to neutrinos no less.

Nigel

