

# SuSA and Mean-Field based models: Summary 2019



**Raúl González Jiménez**  
Grupo de Física Nuclear,  
IPARCOS,  
Universidad Complutense de Madrid



*NuSTEC meeting, December 12, 2019*

# *In collaboration with...*

## **SuSA and RMF**

Juan A. Caballero (Sevilla)

Guillermo D. Megias  
(Sevilla/Saclay/Tokyo)

Maria. B. Barbaro (Torino)  
A. De Pace (Torino)

T. William Donnelly (MIT)

Martin V. Ivanov (Sofia)  
Anton Antonov (Sofia)

J.E. Amaro (Granada)  
I. Ruiz-Simo (Granada)

Jose M. Udías (Madrid)

## **Ghent University**

Natalie Jachowicz

Alexis Nikolakopoulos

Nils Van Dessel

Kajetan Niewczas (Ghent/**Wroclaw**)


## **CEA Saclay**

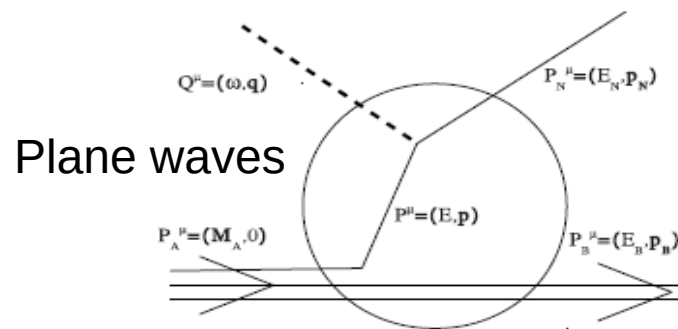
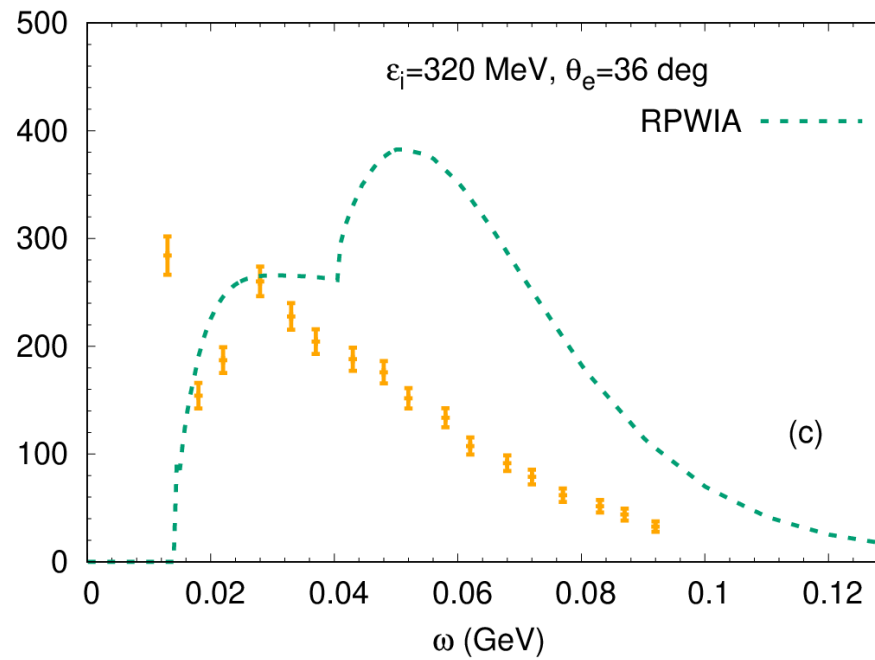
Stephen Dolan

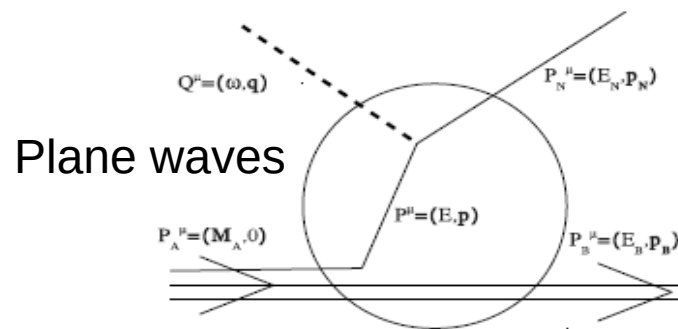
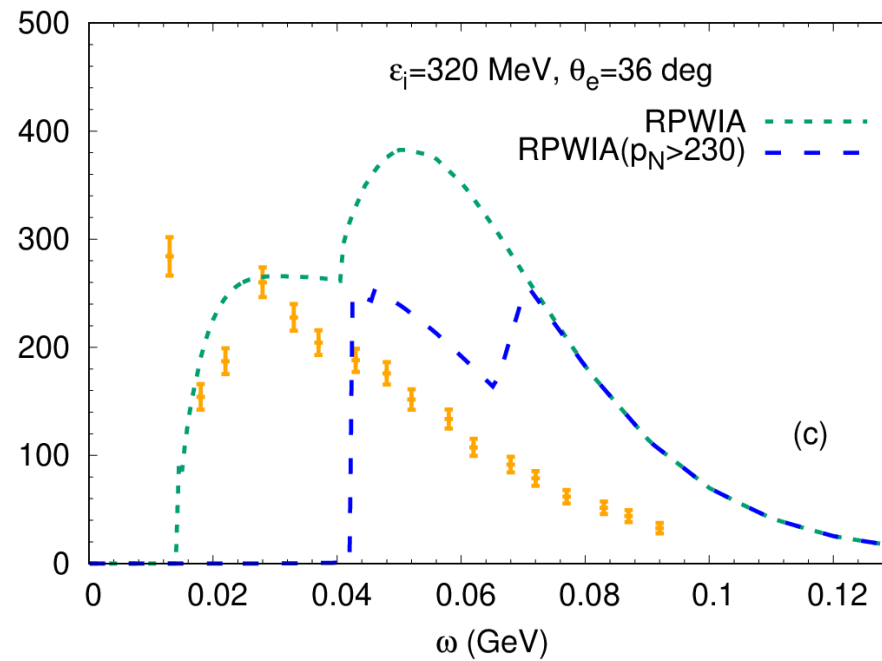
Sara Bolognesi

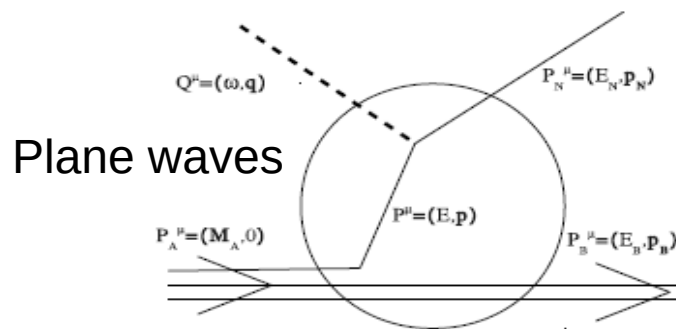
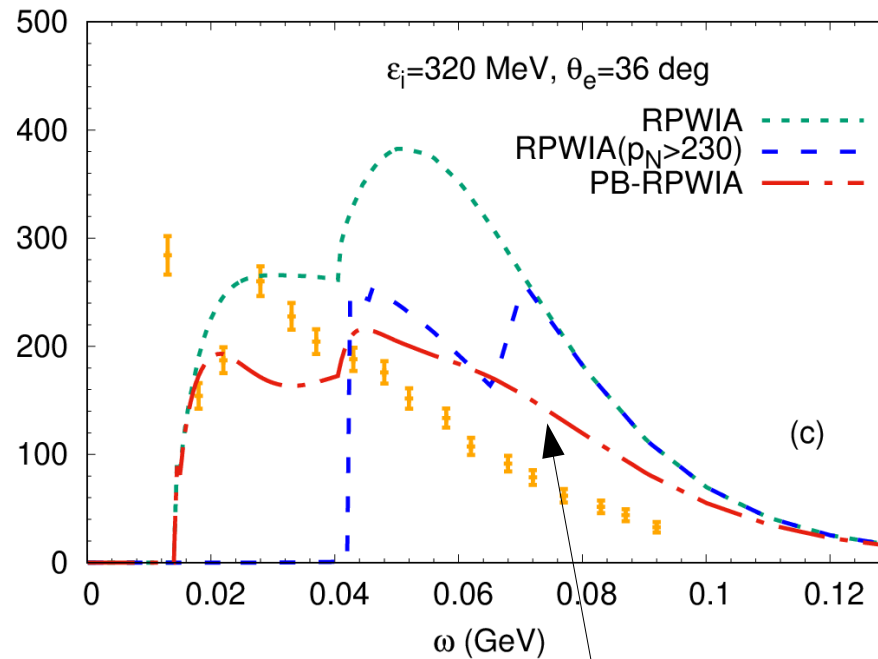
Vishvas Pandey (**Virginia Tech**)

**Nuclear effects in electron-nucleus and neutrino-nucleus scattering within a relativistic quantum mechanical framework**

R. González-Jiménez <sup>1,\*</sup> A. Nikolakopoulos,<sup>2,†</sup> N. Jachowicz,<sup>2,‡</sup> and J. M. Udías<sup>1,§</sup>

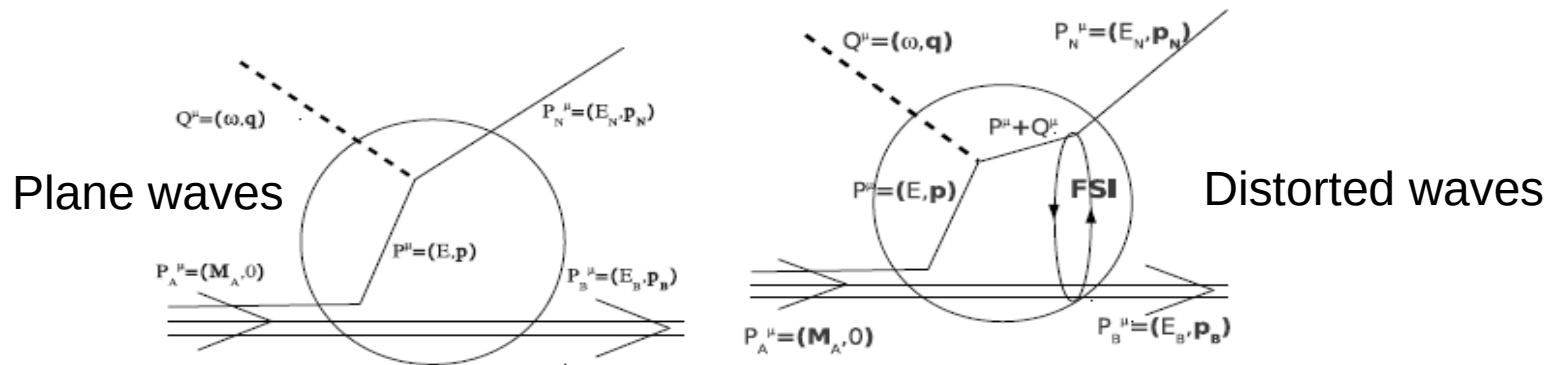
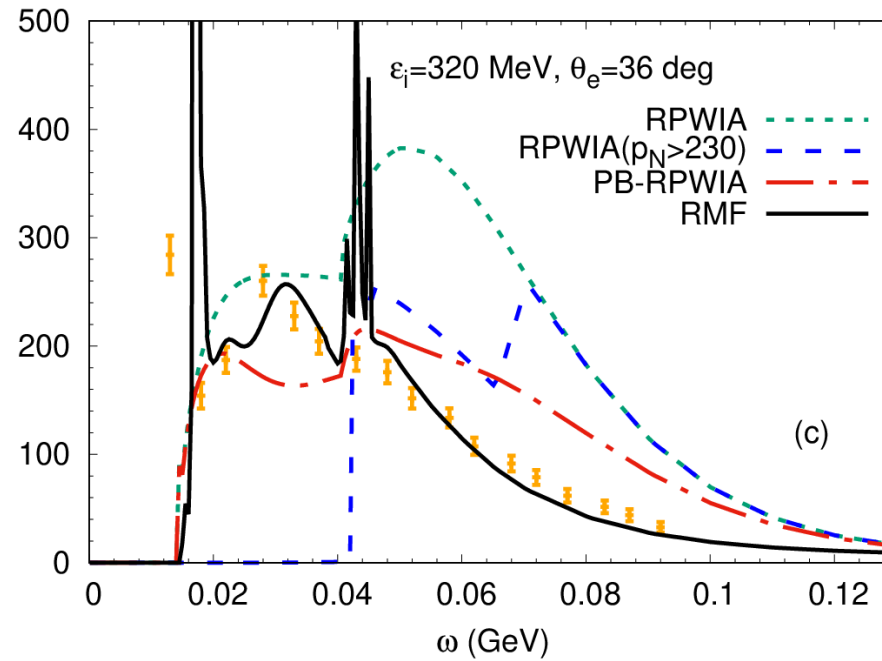
Inclusive electron scattering **at low  $q$ :**

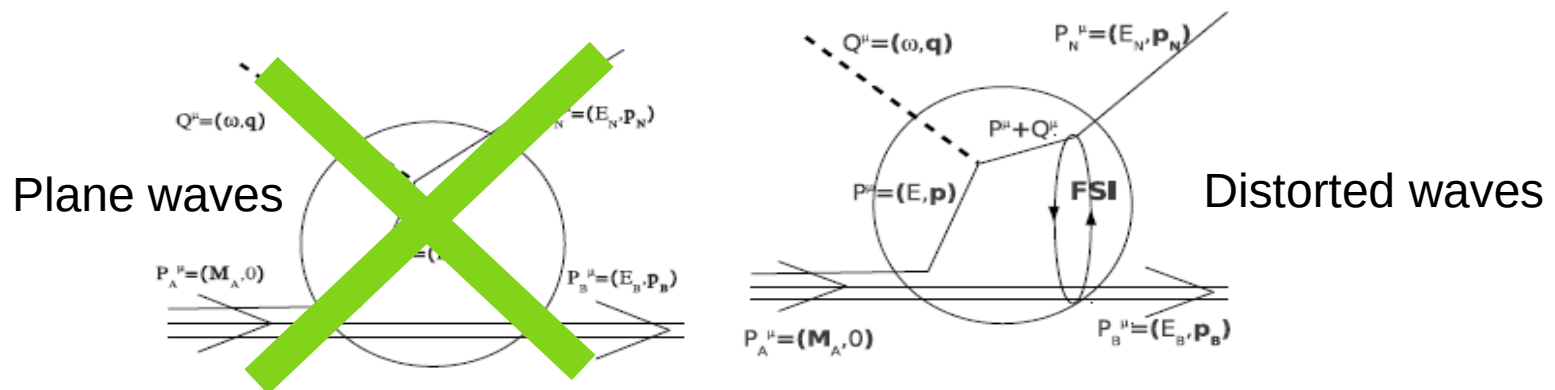
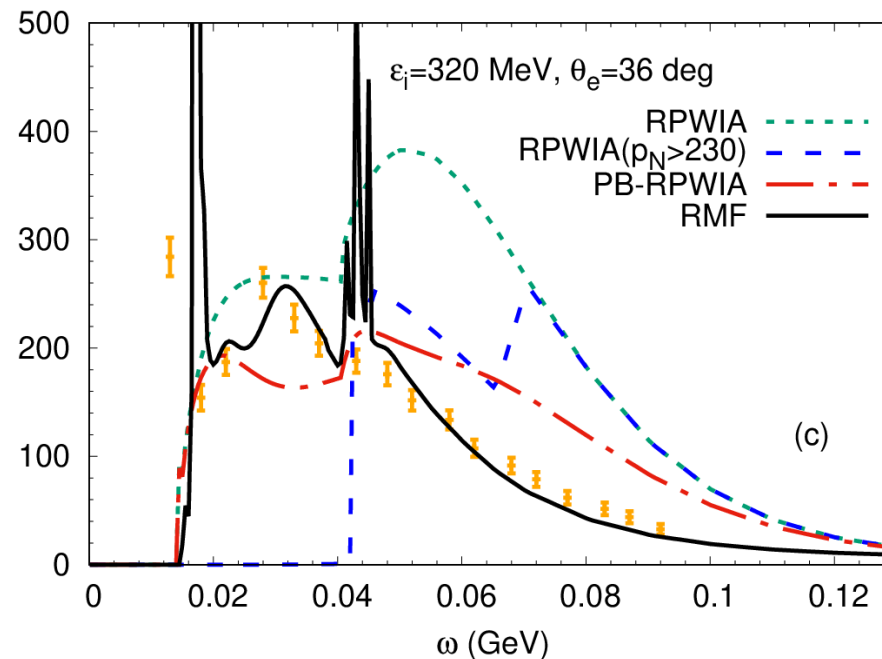
Inclusive electron scattering **at low  $q$ :**

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Orthogonalization

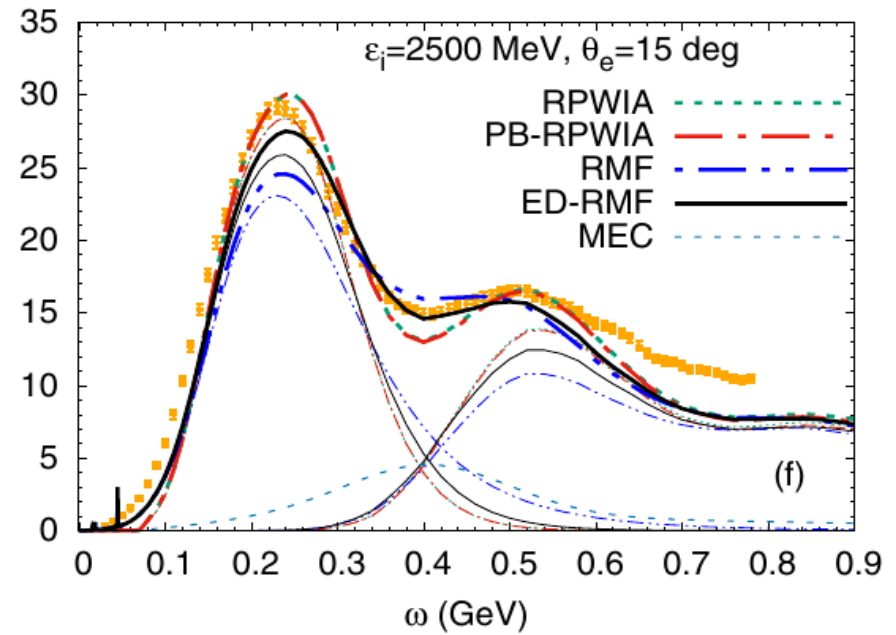
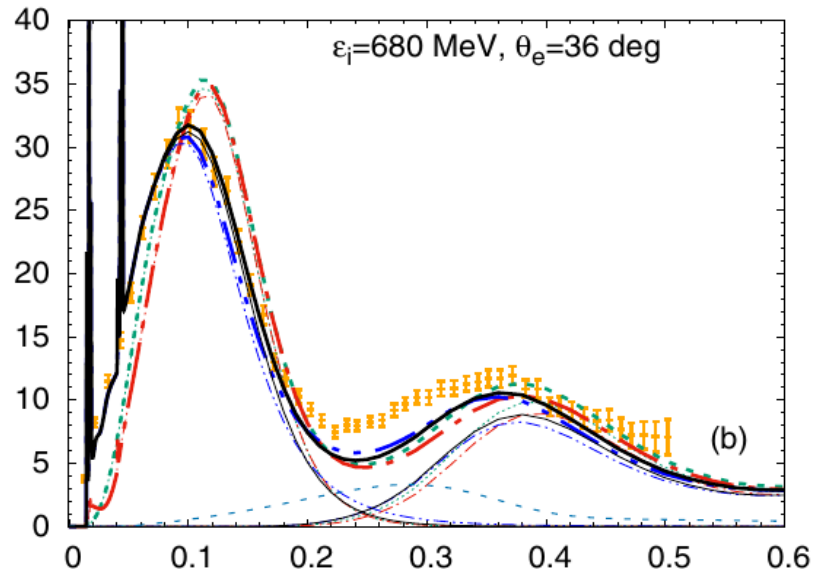
$$|\Psi^{s_N}(\mathbf{p}_N)\rangle = |\psi_{pw}^{s_N}(\mathbf{p}_N)\rangle - \sum_{\kappa, m_j} [C_{\kappa}^{m_j, s_N}(\mathbf{p}_N)]^\dagger |\psi_{\kappa}^{m_j}\rangle$$

Inclusive electron scattering **at low  $q$ :**

Inclusive electron scattering **at low  $q$ :**

When the outgoing nucleon has small momentum its wavelength is comparable to the distance between nucleons: **Quantum Mechanics is important !!**





**Distortion of the outgoing nucleon (= FSI in a Quantum Mechanical way)  
 Important at intermediate energies too !!!**

**Electron versus Muon Neutrino Induced Cross Sections in Charged Current  
Quasielastic Processes**

A. Nikolakopoulos,<sup>1,\*</sup> N. Jachowicz,<sup>1,†</sup> N. Van Dessel,<sup>1</sup> K. Niewczas,<sup>1,2</sup> R. González-Jiménez,<sup>3</sup> J. M. Udías,<sup>3</sup> and V. Pandey<sup>4</sup>

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For a given neutrino energy and scattering angle of the final lepton:

$$\frac{\nu_e \text{ QE cross section}}{\nu_\mu \text{ QE cross section}} = 1 \quad ???$$

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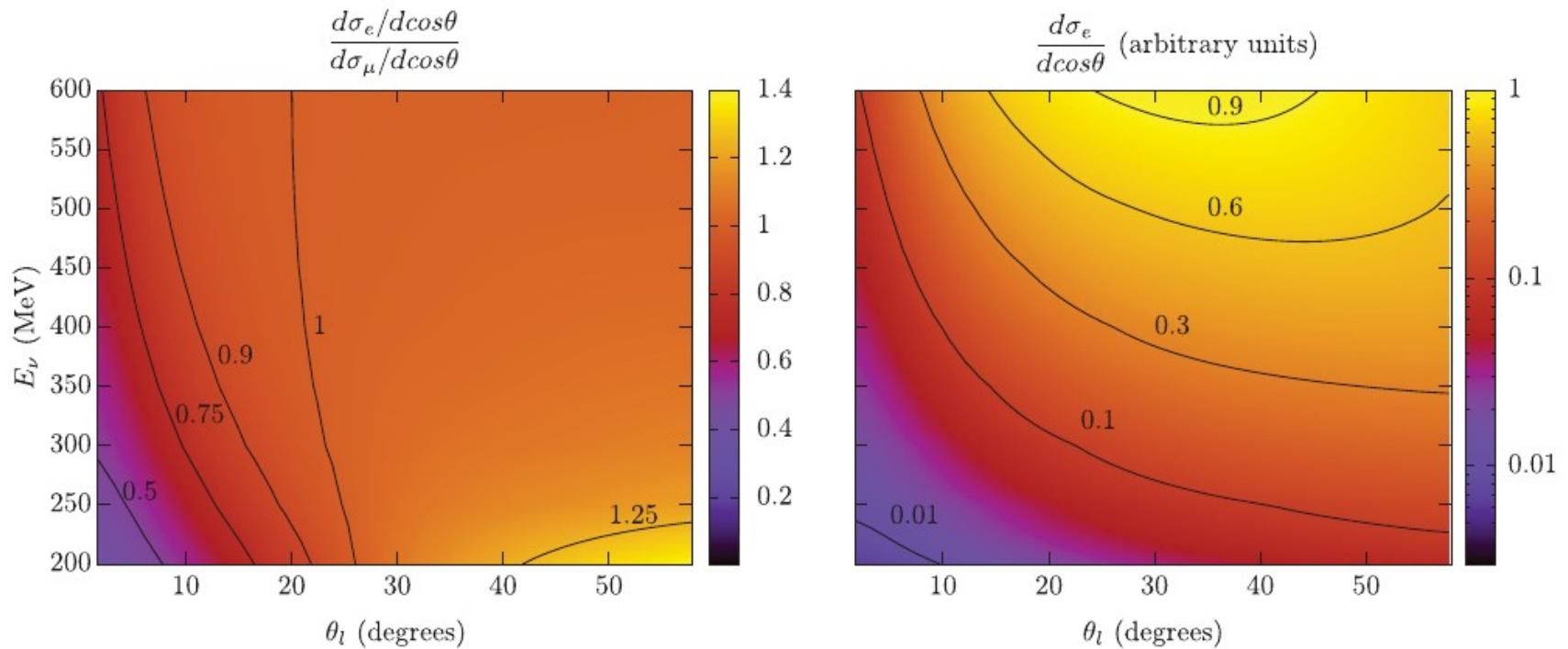


FIG. 4. Ratio of  $^{12}\text{C}$  cross sections as a function of incoming energy and lepton scattering angle, combined with relative strength of the cross section at the same kinematics (normalized such that the maximum in this kinematic region is 1). Results shown here were obtained within the CRPA approach, RMF ratios are very similar [30].

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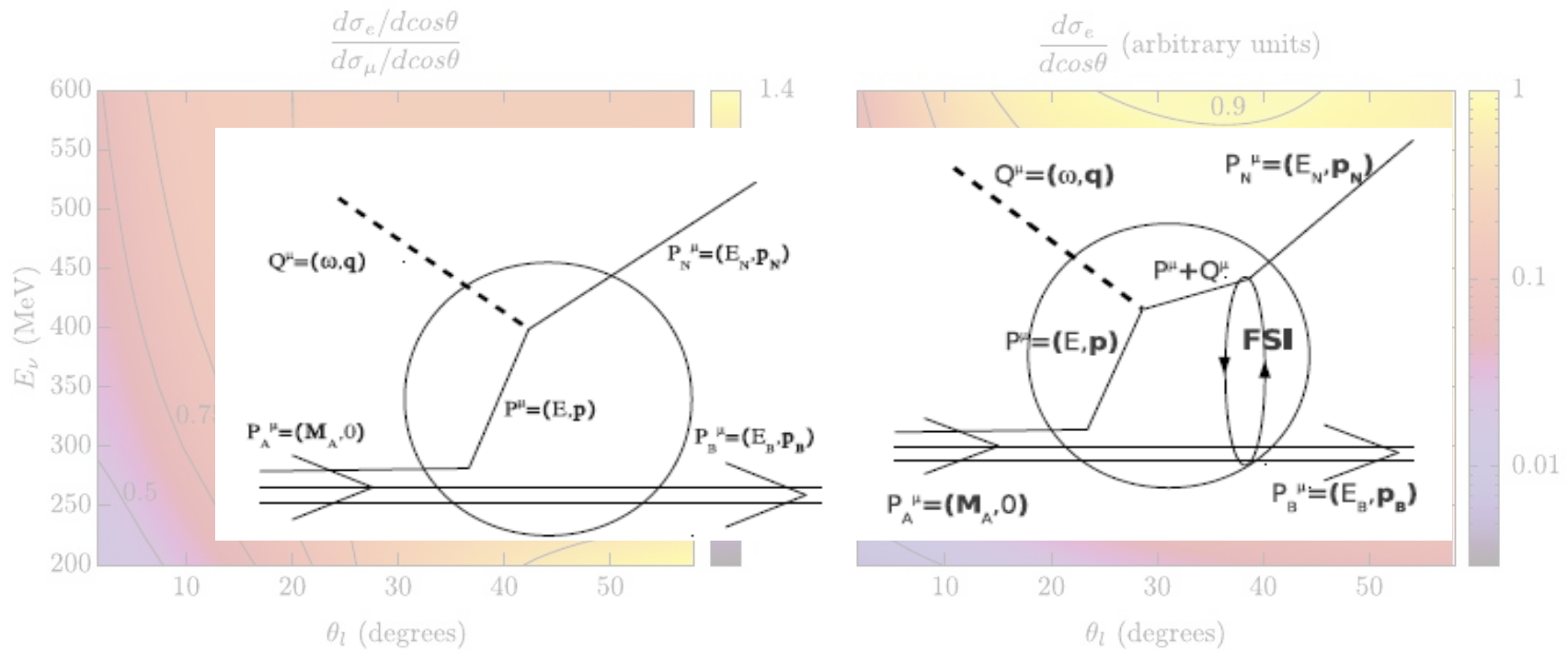


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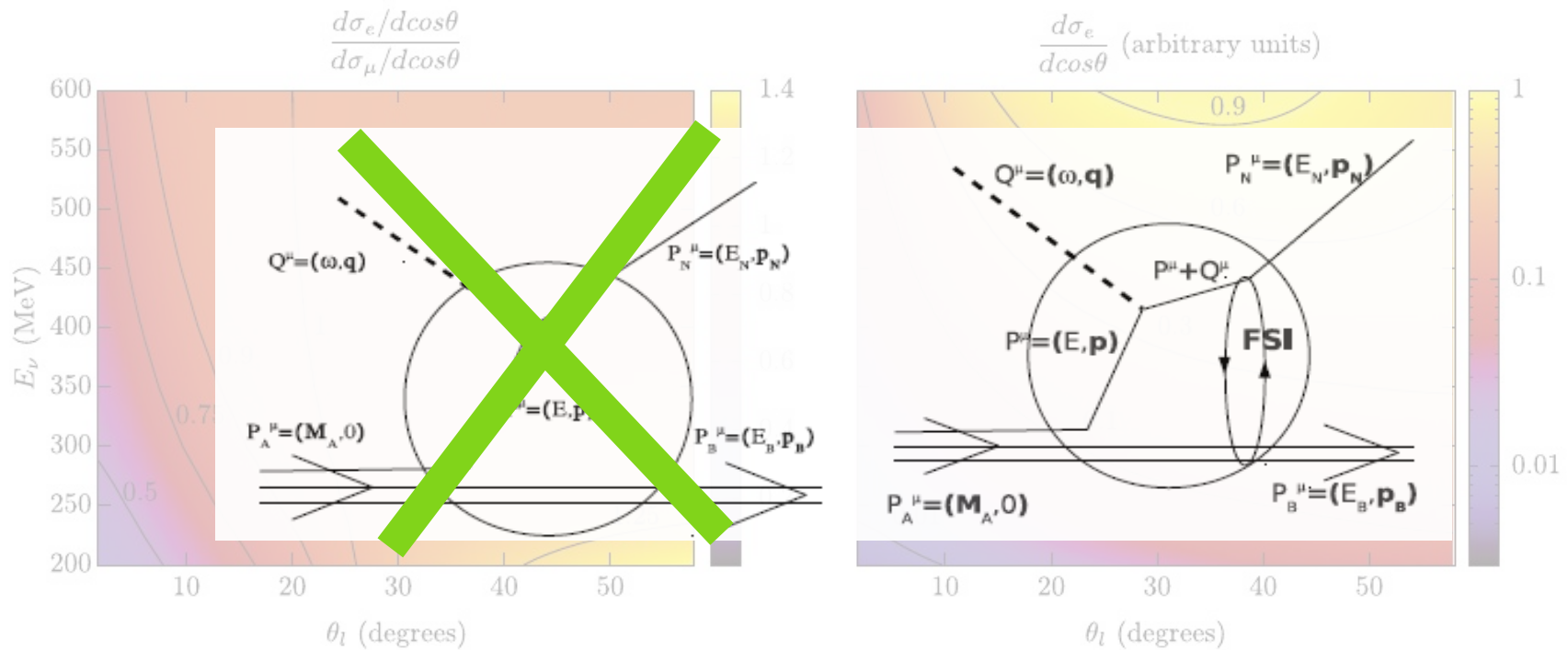


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**SuSAv2**

**SuSAv2-MEC**

**Analysis of the MINERvA antineutrino double-differential cross sections  
within the SuSav2 model including meson-exchange currents**

G. D. Megias

*Departamento de Física Atómica, Molecular y Nuclear, Universidad de Sevilla, 41080 Sevilla, Spain  
and IRFU, CEA, Université Paris-Saclay, 91191 Gif-sur-Yvette, France*

M. B. Barbaro

*Dipartimento di Fisica, Università di Torino and INFN, Sezione di Torino,  
Via P. Giuria 1, 10125 Torino, Italy*

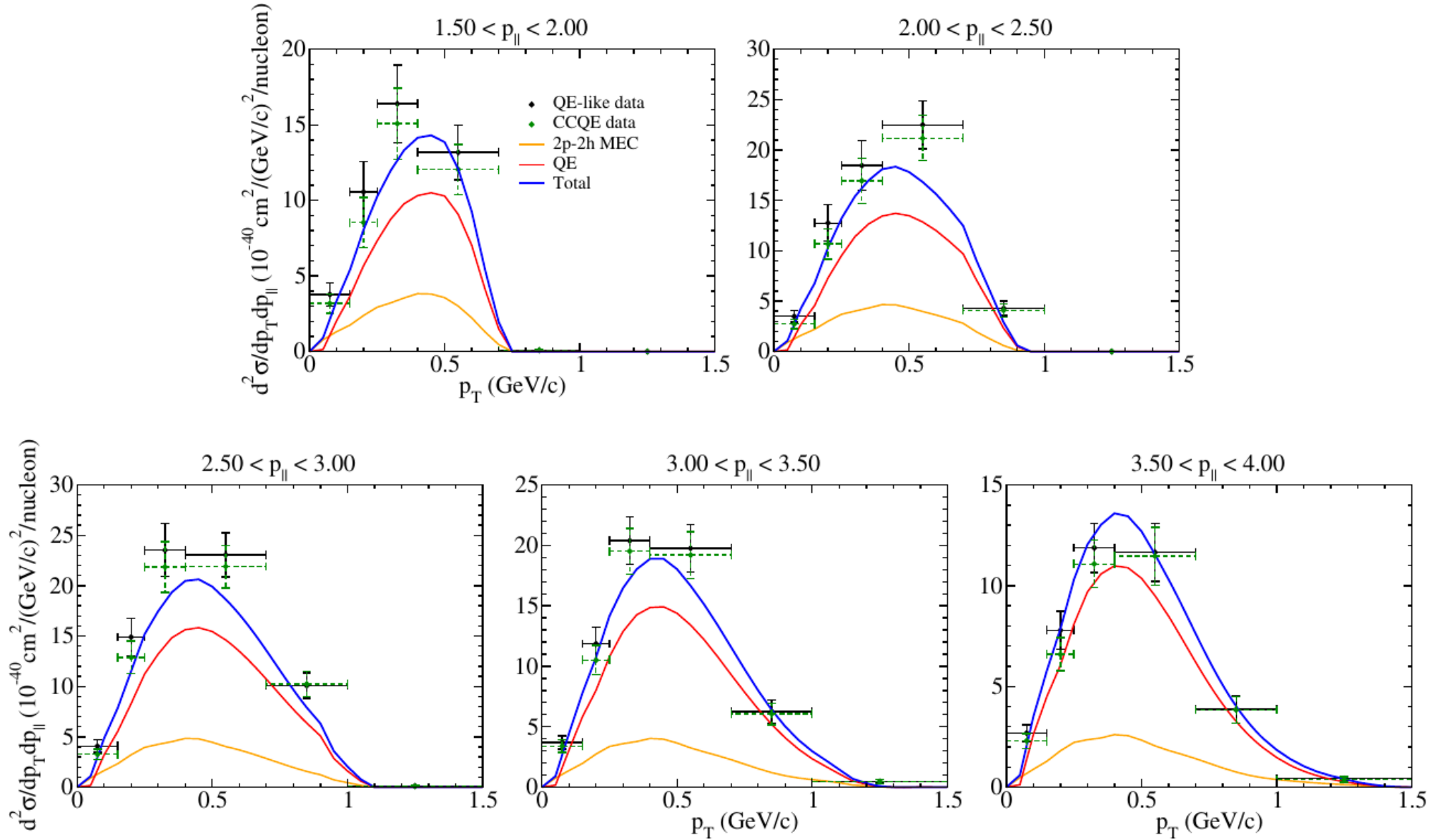
J. A. Caballero

*Departamento de Física Atómica, Molecular y Nuclear, Universidad de Sevilla, 41080 Sevilla, Spain*

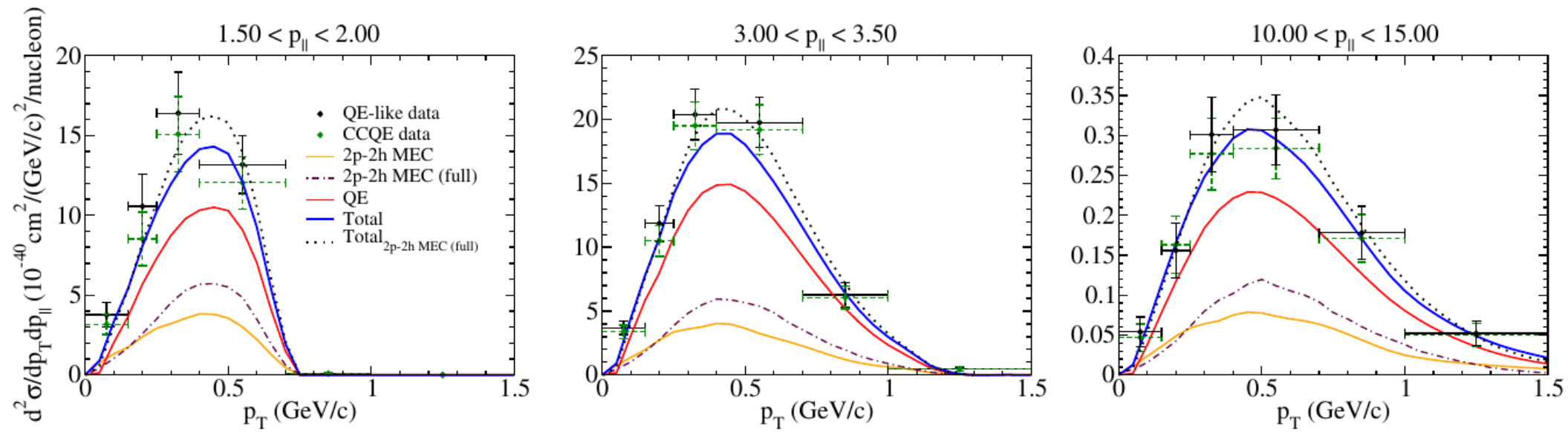
S. Dolan

*Ecole Polytechnique, IN2P3-CNRS, Laboratoire Leprince-Ringuet, 91120 Palaiseau, France  
and IRFU. CEA. Université Paris-Saclay. 91191 Gif-sur-Yvette. France*

# SuSAv2-MEC versus MINERvA nub 0ptions



Full propagator vs real propagator in the delta current.

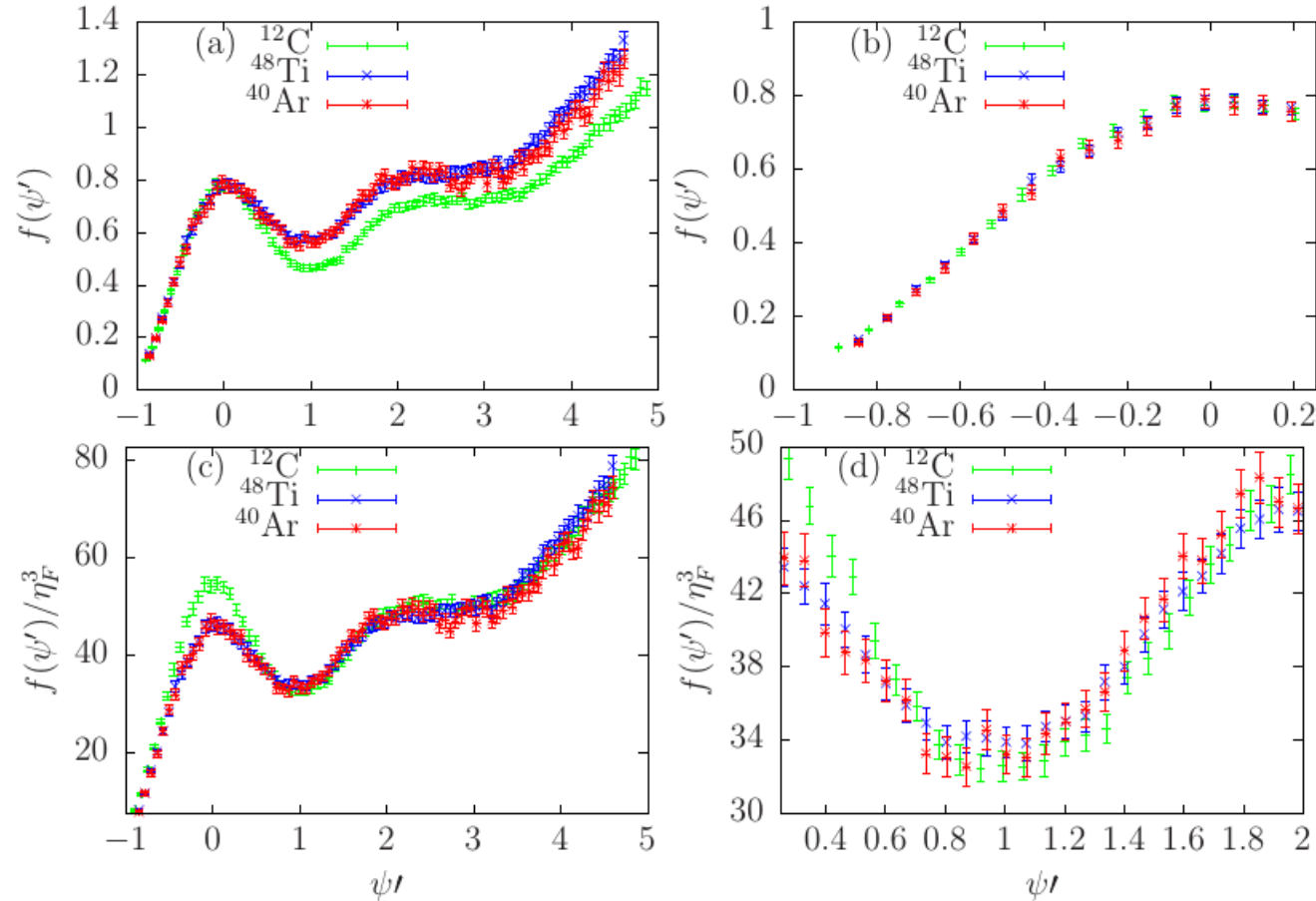


**Mean-field and two-body nuclear effects in inclusive electron scattering on argon, carbon, and titanium: The superscaling approach**

M. B. Barbaro,<sup>1</sup> J. A. Caballero,<sup>2</sup> A. De Pace,<sup>3</sup> T. W. Donnelly,<sup>4</sup> R. González-Jiménez,<sup>5</sup> and G. D. Megias<sup>2,6</sup>

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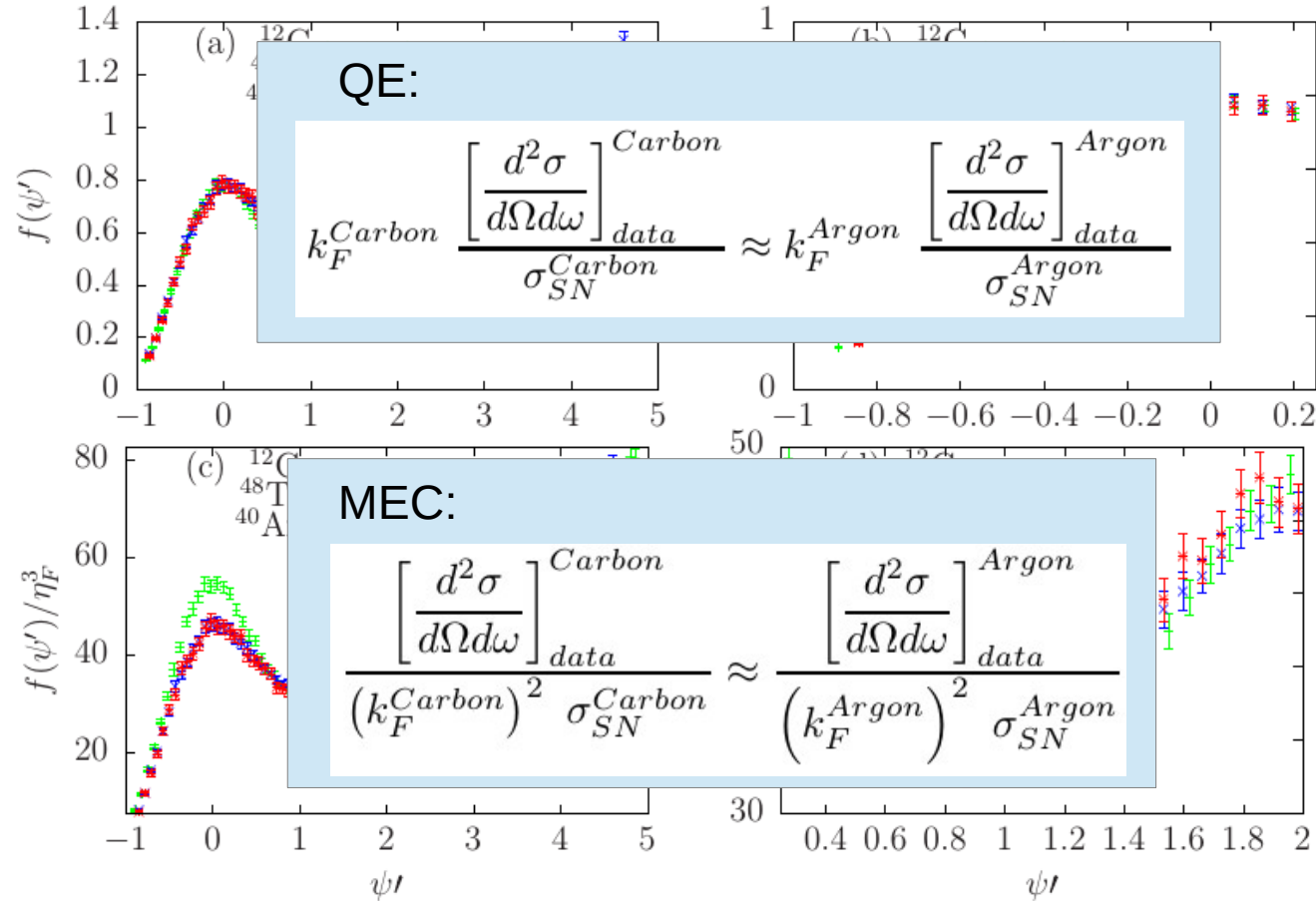
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The 2p2h response scales very differently from the quasielastic one, in full accord with what is predicted by the model.

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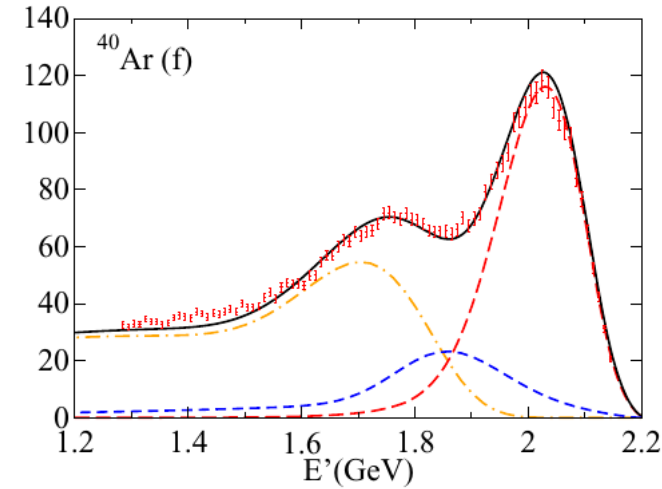
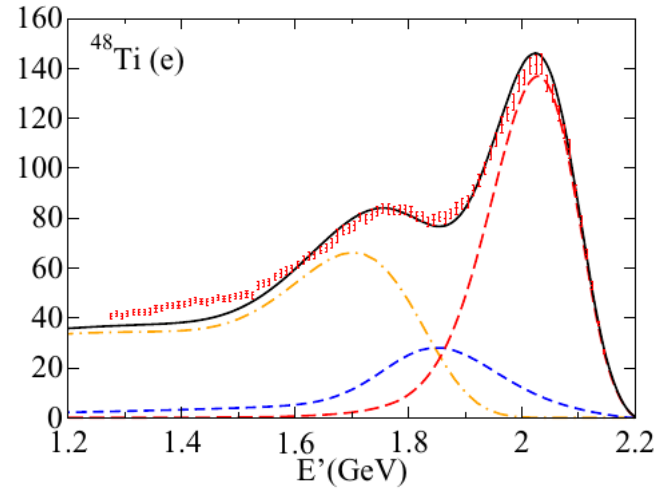
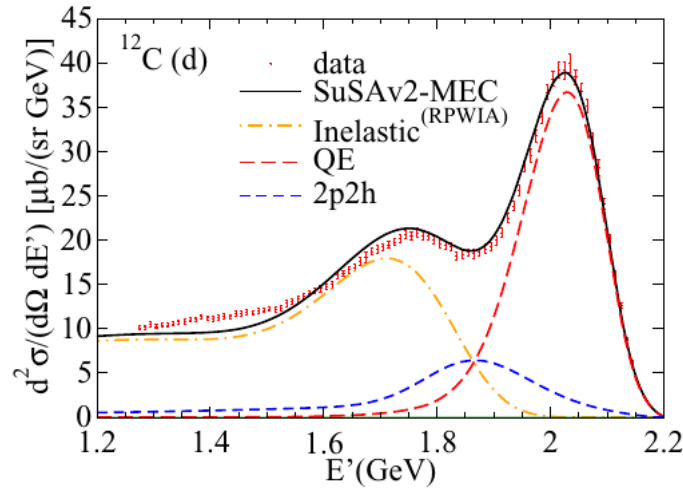
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Comparison with recent JLab data.

$E_i = 2222$  MeV,  
 $\theta_e = 15.541$  deg



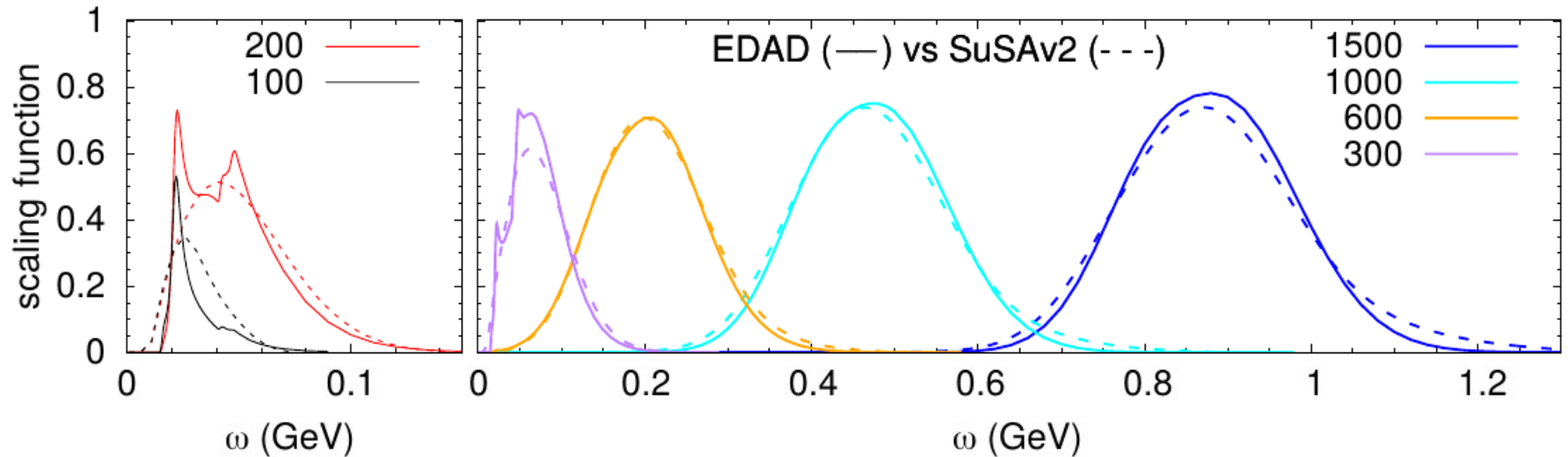


# Constraining the quasielastic response in inclusive lepton-nucleus scattering

R. González-Jiménez,<sup>1</sup> M.B. Barbaro,<sup>2</sup> J.A. Caballero,<sup>3</sup> T.W. Donnelly,<sup>4</sup>  
N. Jachowicz,<sup>5</sup> G.D. Megias,<sup>3,6</sup> K. Niewczas,<sup>7,5</sup> A. Nikolakopoulos,<sup>5</sup> and J.M. Udías<sup>1</sup>

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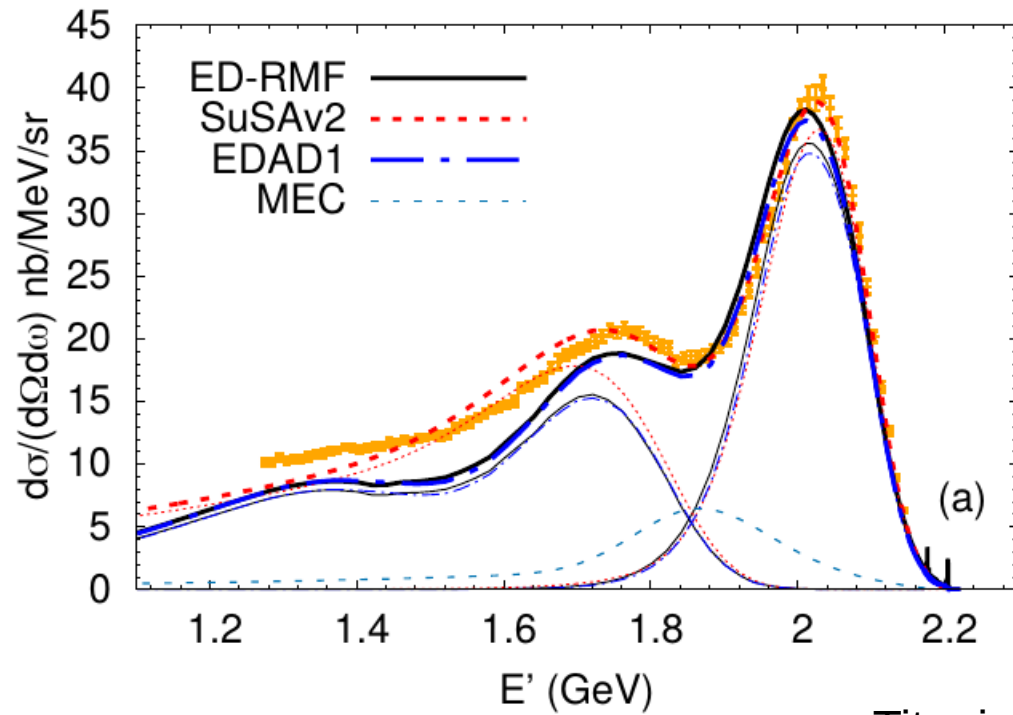
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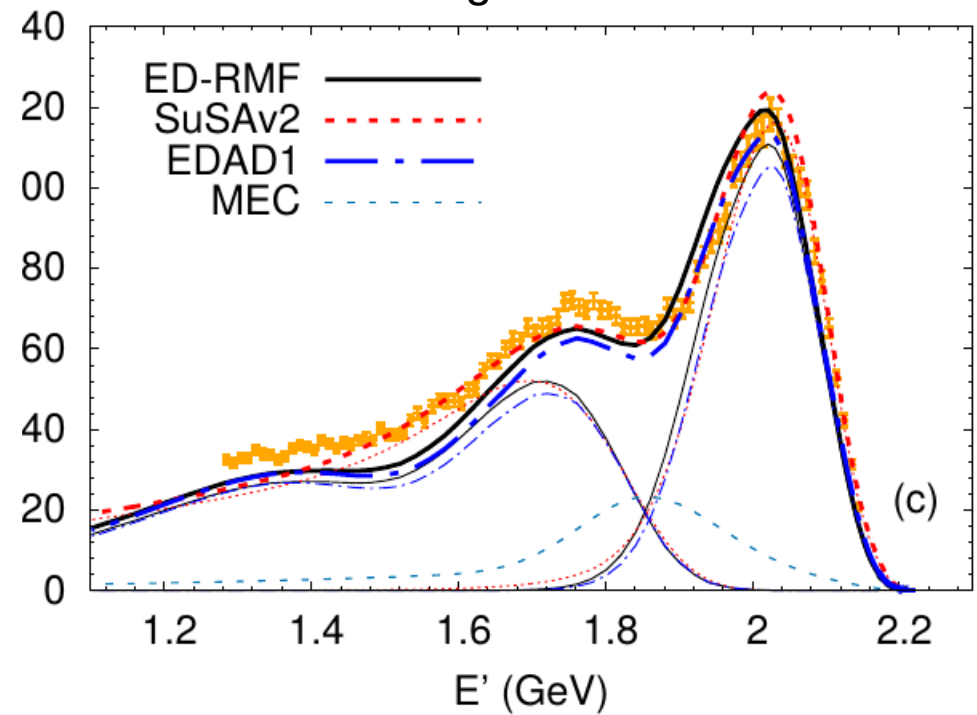
The SuSAv2 QE response is very similar to that from a model that solves the wave equation in presence of a real energy-dependent optical potential.

The coincidence between these two completely independent approaches, which satisfactorily agree with the inclusive data, reinforces the reliability of our predictions and sets constraints for the modeling of the QE response.

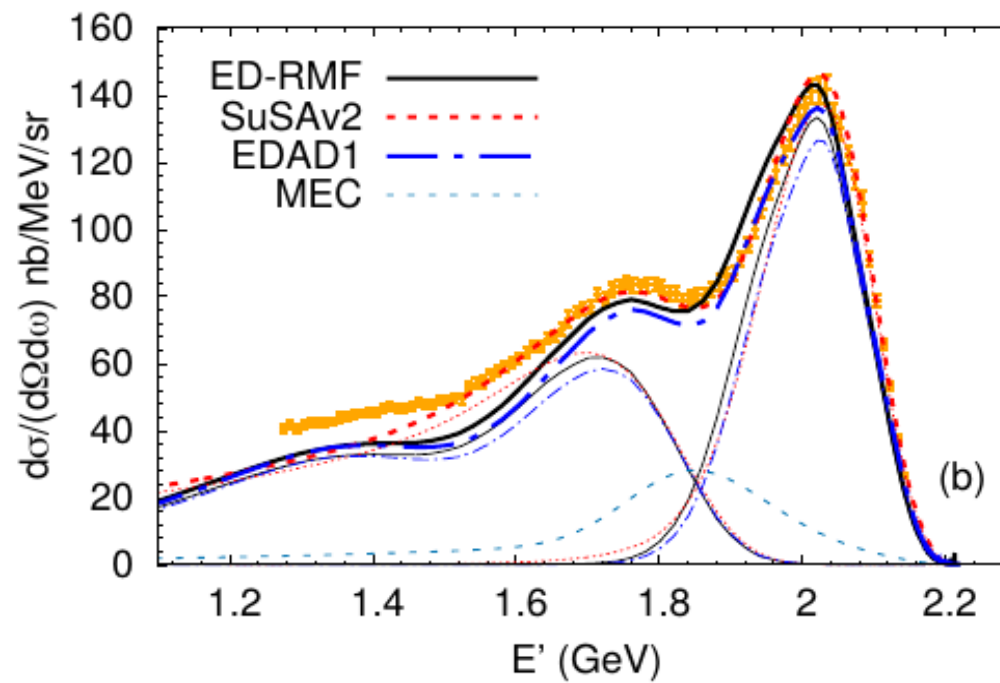
Carbon



Argon



Titanium



Recent JLab data.

$$E_i = 2222 \text{ MeV}$$

$$\theta_e = 15.541 \text{ deg}$$

# Implementation of the SuSAv2-MEC 1p1h and 2p2h models in GENIE and analysis of nuclear effects in T2K measurements

S. Dolan,<sup>1,2</sup> G.D. Megias,<sup>1,2</sup> and S. Bolognesi<sup>2</sup>

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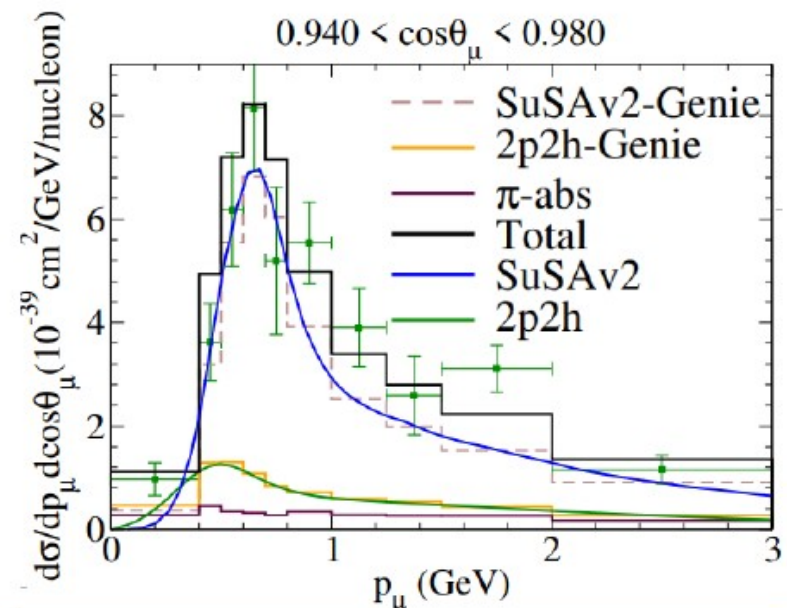
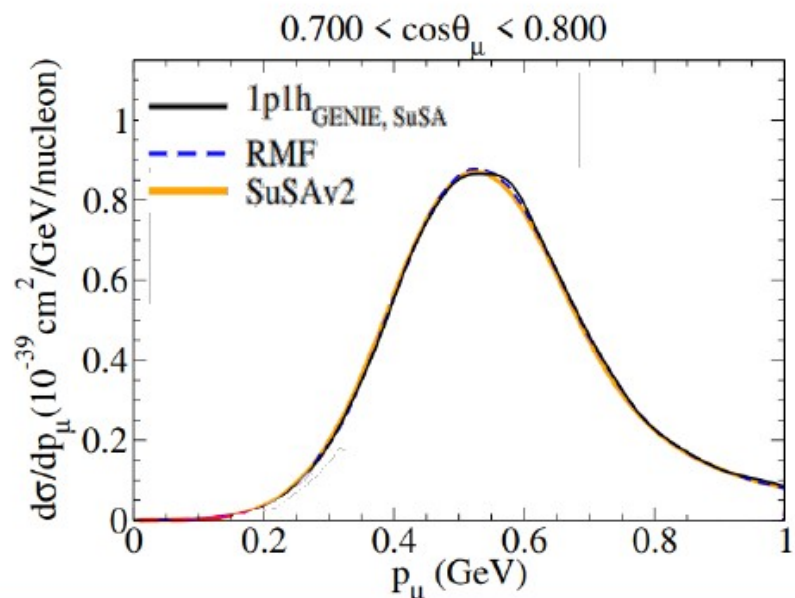
S. Dolan,<sup>1,2</sup> G.D. Megias,<sup>1,2</sup> and S. Bognesi<sup>2</sup>

## Overview

Based on: [arXiv:1905.08556](https://arxiv.org/abs/1905.08556)

Also: see Guillermo's talk before this

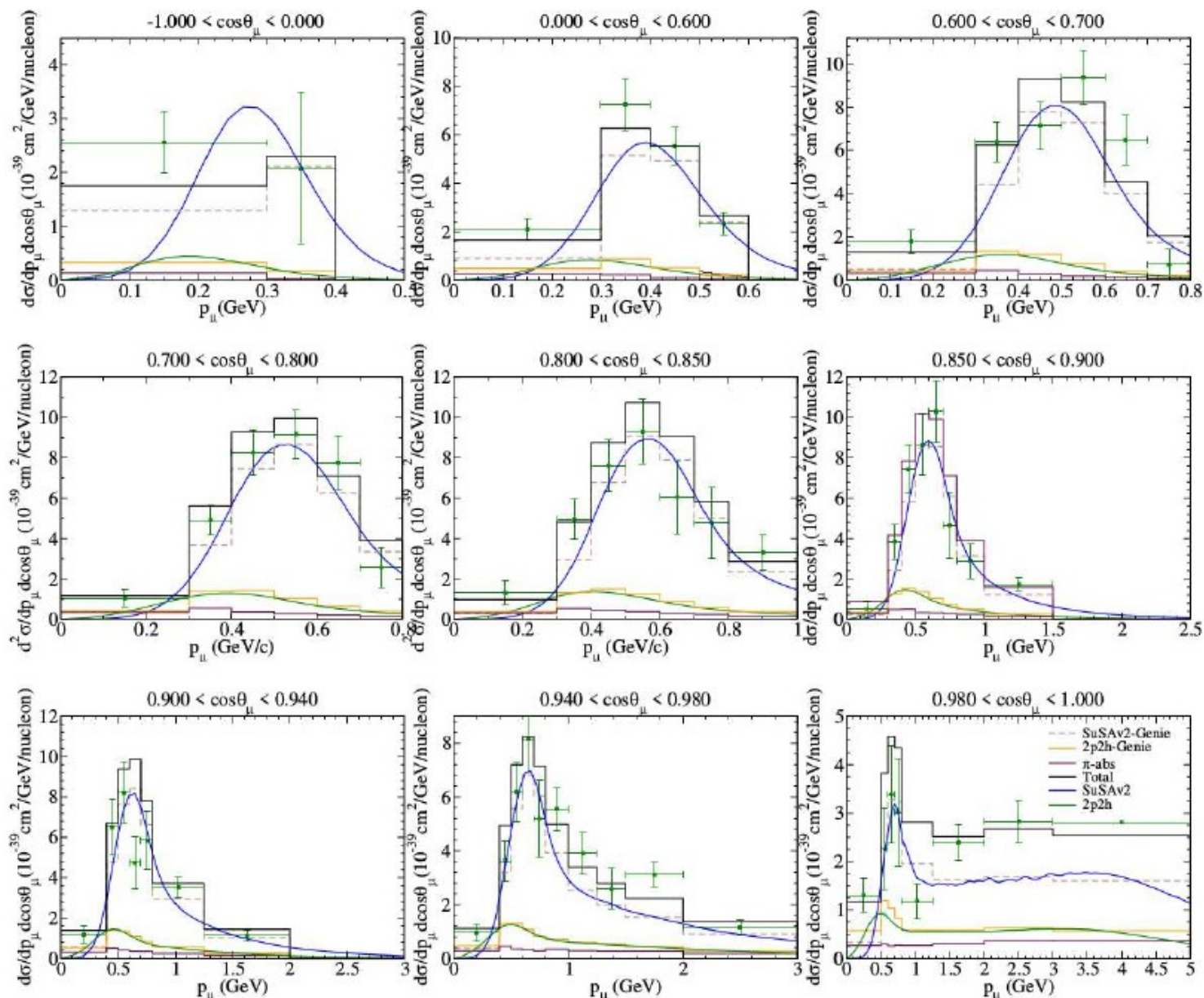
- Recently implemented the SuSAv2 1p1h and 2p2h models in GENIE using hadron tensors.
- Based on implementations of the Valencia 2p2h (NEUT/GENIE)
- Exactly reproduces the *inclusive* predictions of the models



# SuSAv2-MEC implementation in GENIE: Validation plots (T2K CC0 $\pi$ )

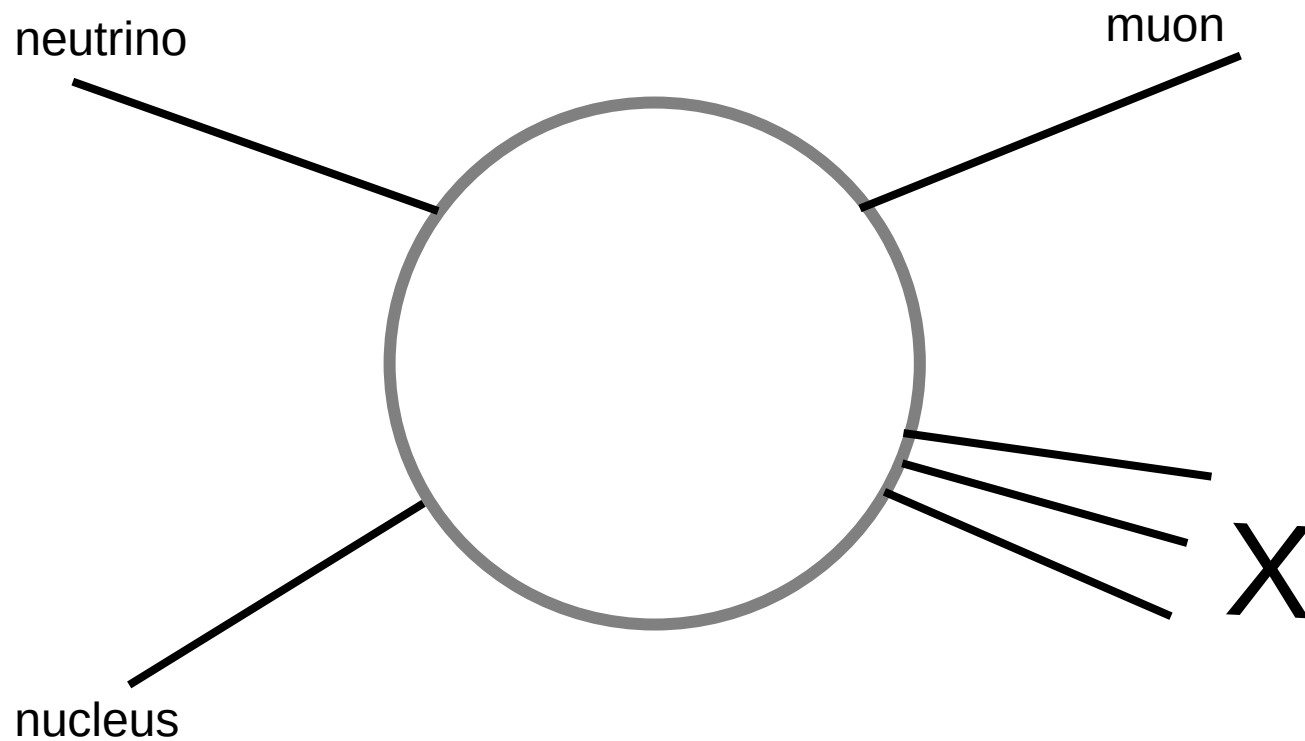
T2K CC0 $\pi$   $\nu_\mu$ - $^{12}\text{C}$  data vs. SuSAv2-MEC<sub>GENIE</sub>

$\chi^2 = 255.8$  (67 bins)



What do we need?

# Inclusive cross section?





# Inclusive cross section?

Many models are good for the inclusive xs (at typical QE kinematics).

**Realistic spectral function model for charged-current quasielastic-like neutrino and antineutrino scattering cross sections on  $^{12}\text{C}$**

M. V. Ivanov and A. N. Antonov

*Institute for Nuclear Research and Nuclear Energy, Bulgarian Academy of Sciences, Sofia 1784, Bulgaria*

G. D. Megias and J. A. Caballero

*Departamento de Física Atómica, Molecular y Nuclear, Universidad de Sevilla, 41080 Sevilla, Spain*

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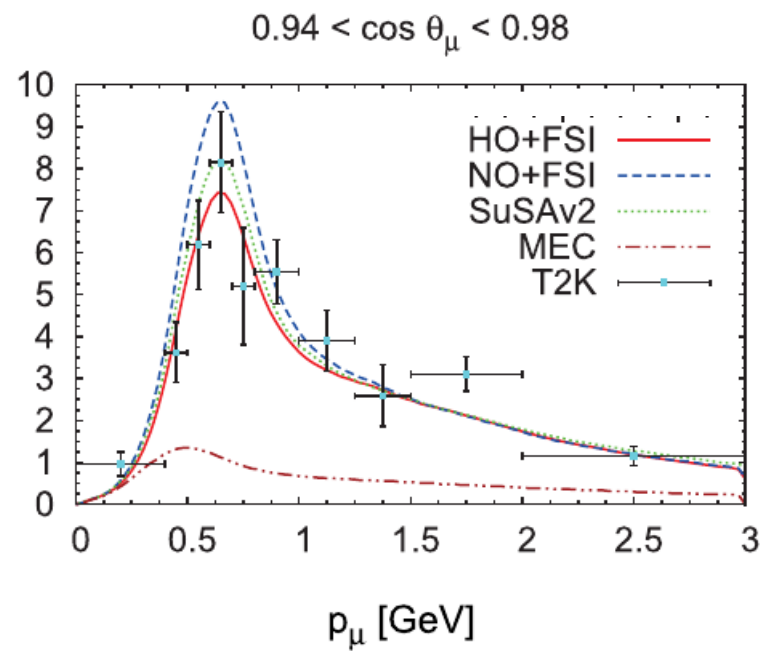
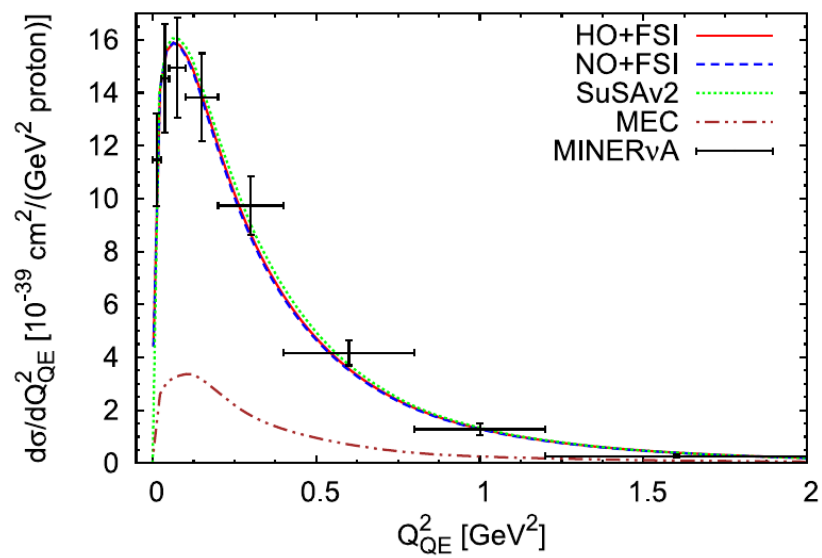
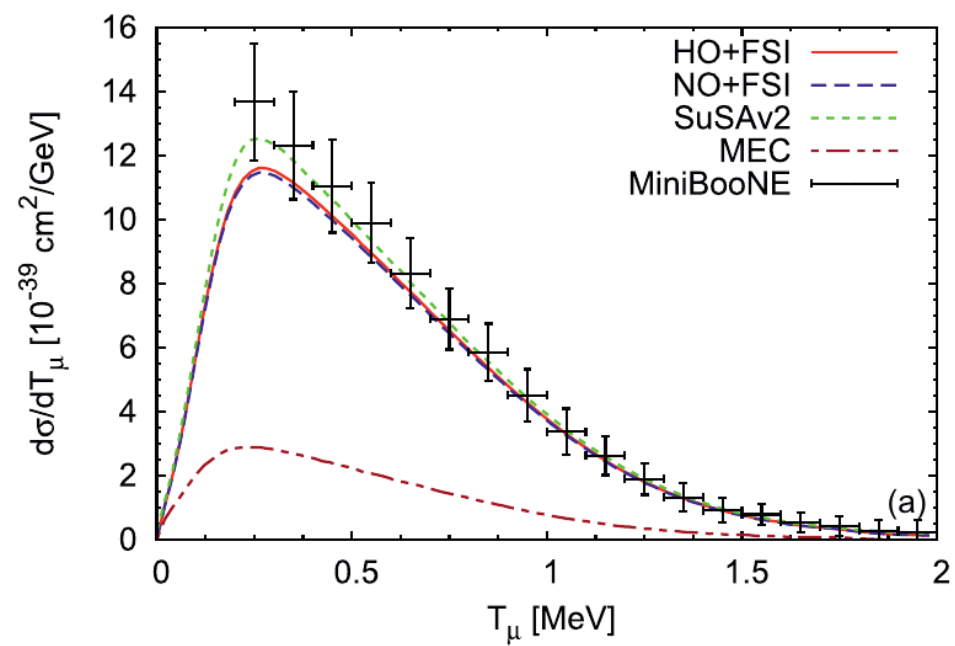
*Departamento de Física Atómica, Molecular y Nuclear, and Instituto de Física Teórica y Computacional Carlos I, Universidad de Granada, Granada 18071, Spain*

T. W. Donnelly

*Center for Theoretical Physics, Laboratory for Nuclear Science and Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA*

J. M. Udías

*Grupo de Física Nuclear, Departamento de Estructura de la Materia, Física Aplicada y Electrónica and UPARCOS, Universidad Complutense de Madrid, CEI Moncloa, 28040 Madrid, Spain*



# Inclusive cross section?

Many models are good for the inclusive xs (at typical QE kinematics).

**SuSAv2+MEC is the state of the art among the inclusive models:**

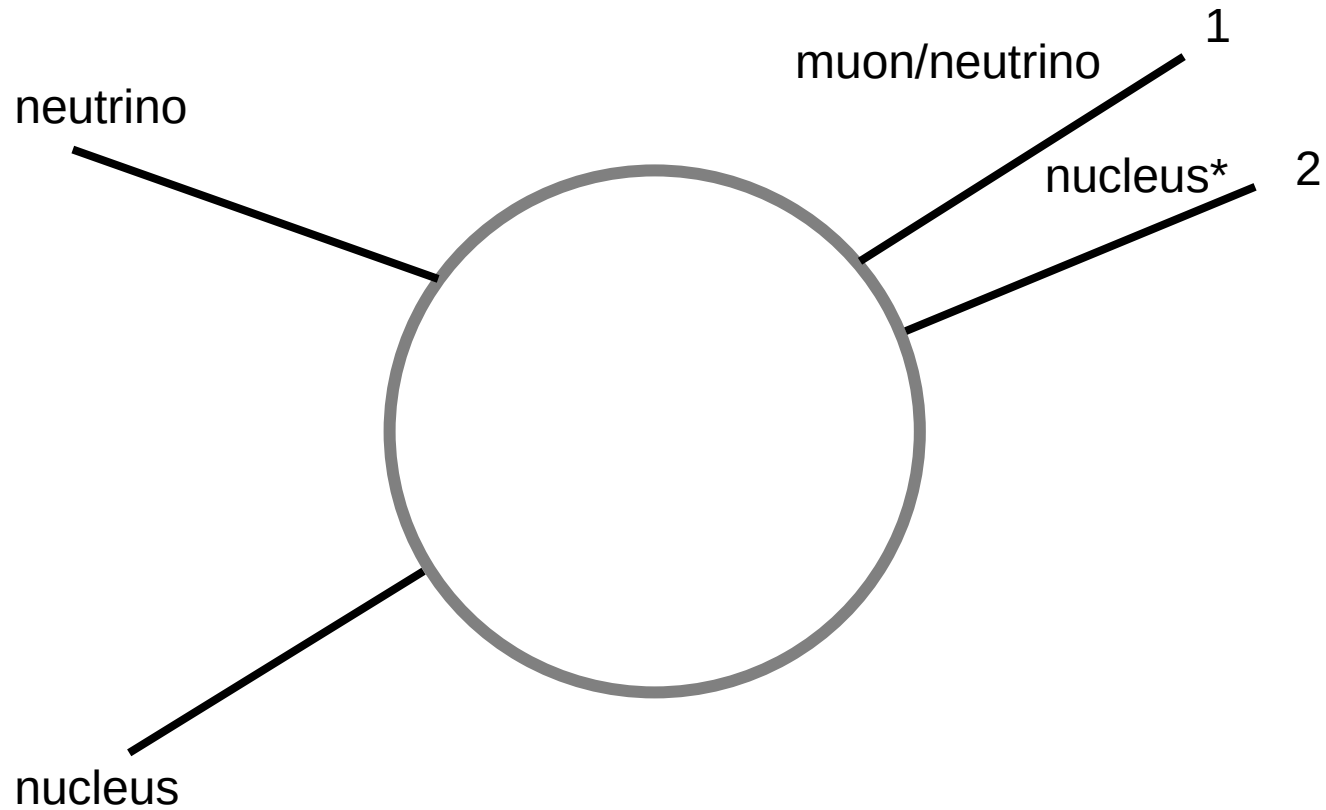
- + Extensively tested against electron and neutrino scattering data:  
systematically on the data.
- + **Fully relativistic.**
- + Extremely efficient from computational point of view.
- + **For neutrino interactions, it needs to be extended to the DIS region.**
- + **Not suppose to work at very low  $q$ , but a few things could be done.**

What do we need?

Information about the hadrons?

Initial State

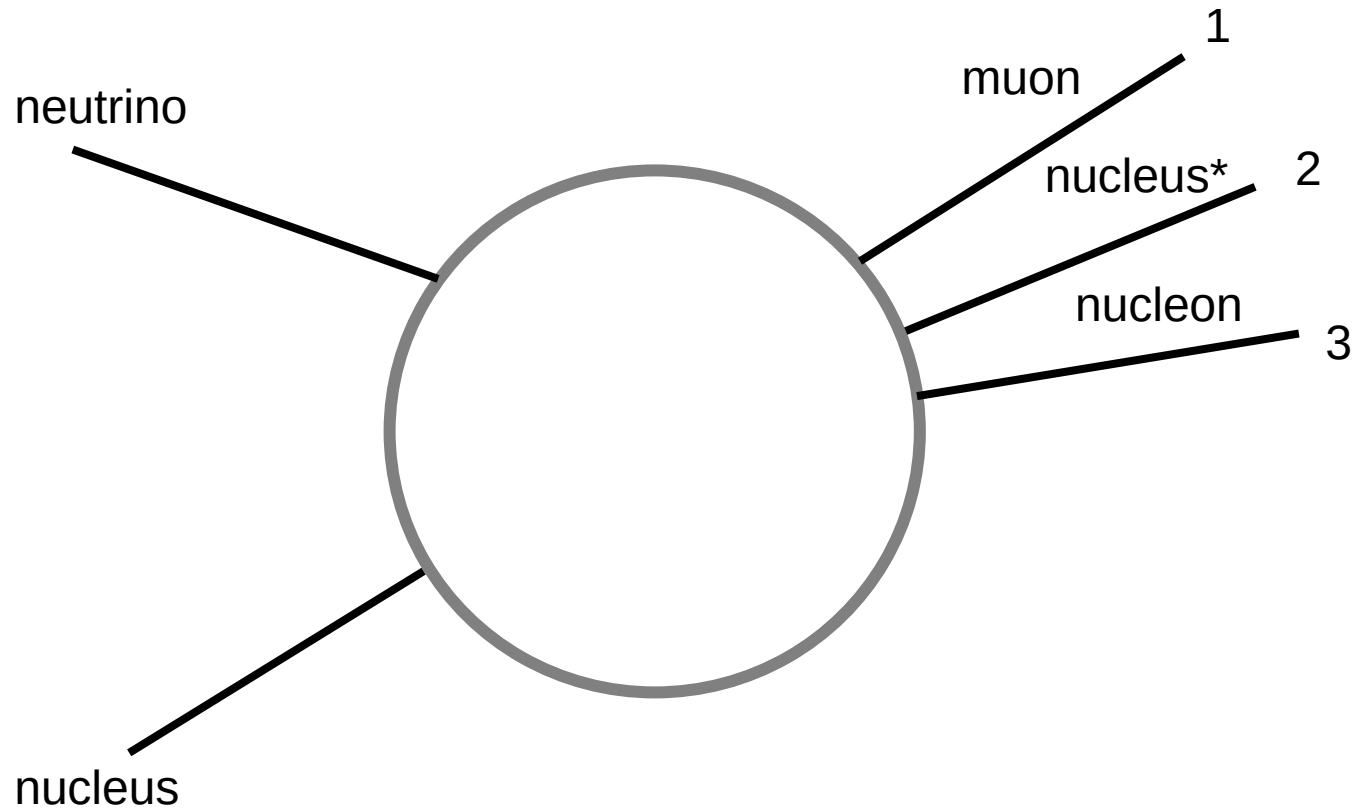
Final State



Elastic scattering  
(difficult)

Initial State

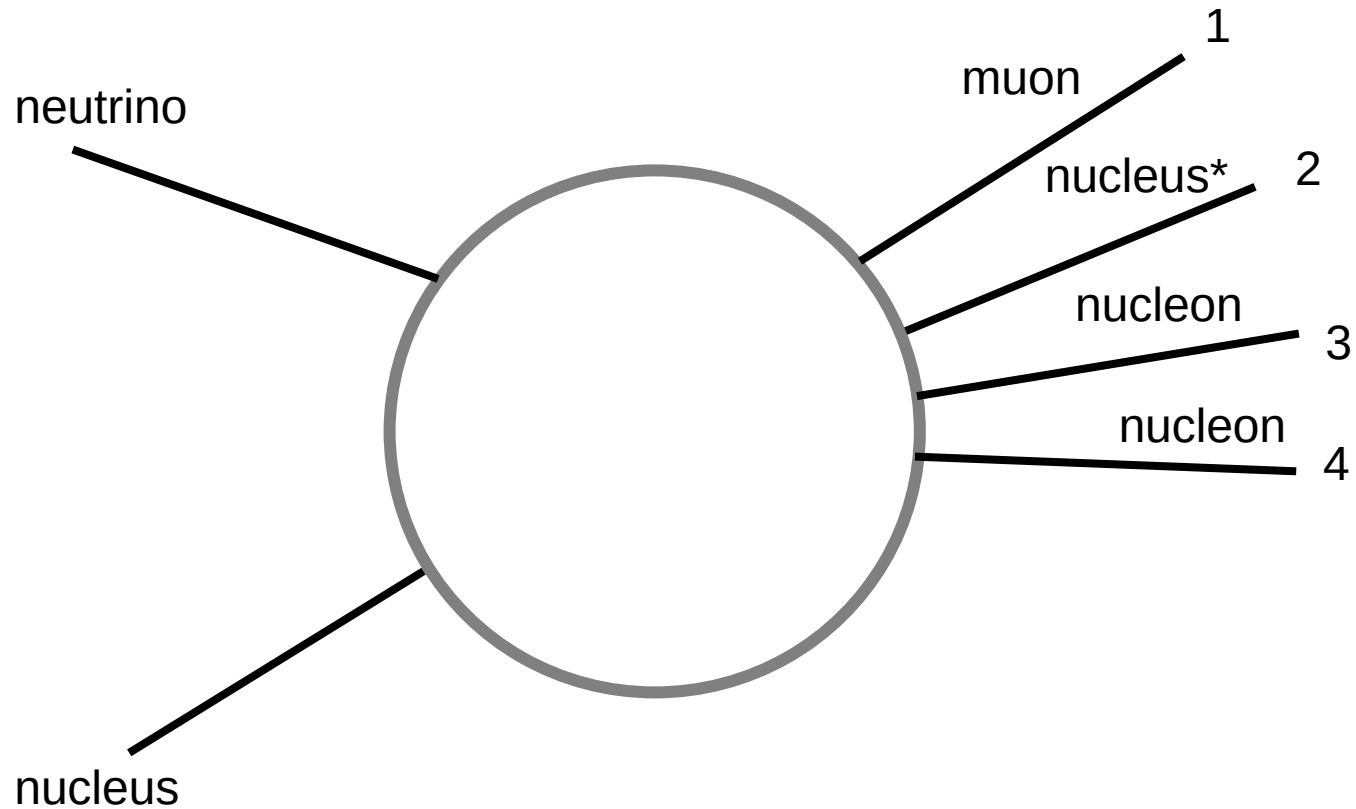
Final State



Quasielastic scattering  
(difficult)

Initial State

Final State

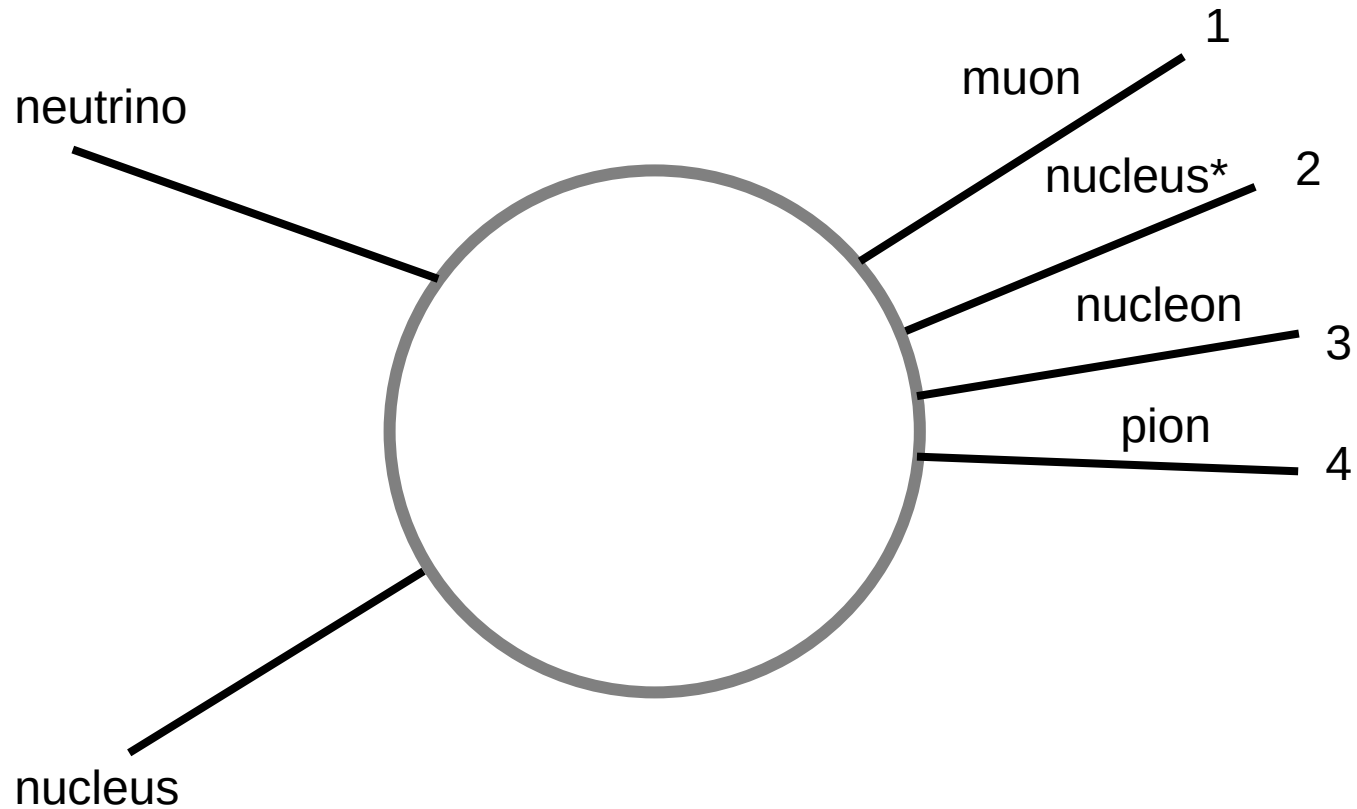


2N knockout  
(extremely difficult)



Initial State

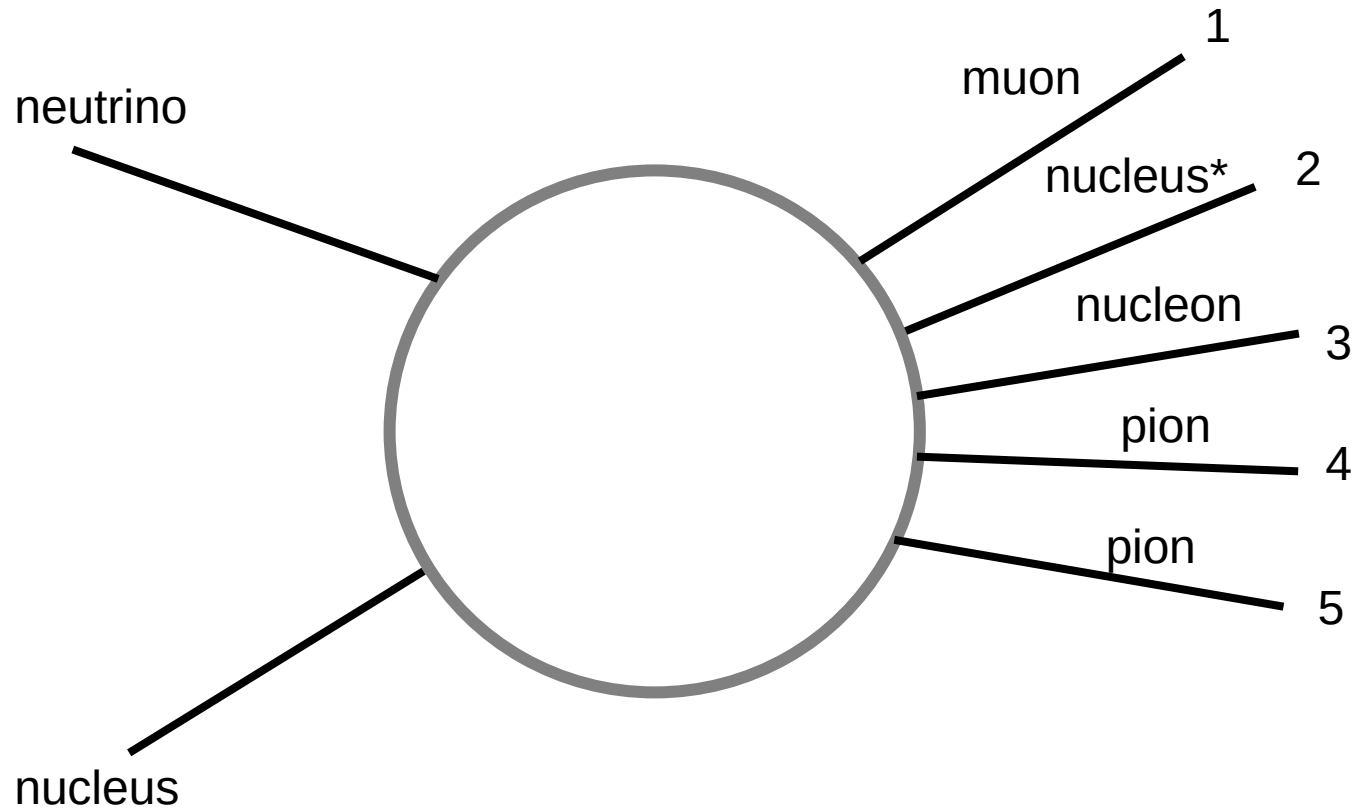
Final State



Single-pion production  
(extremely difficult)

Initial State

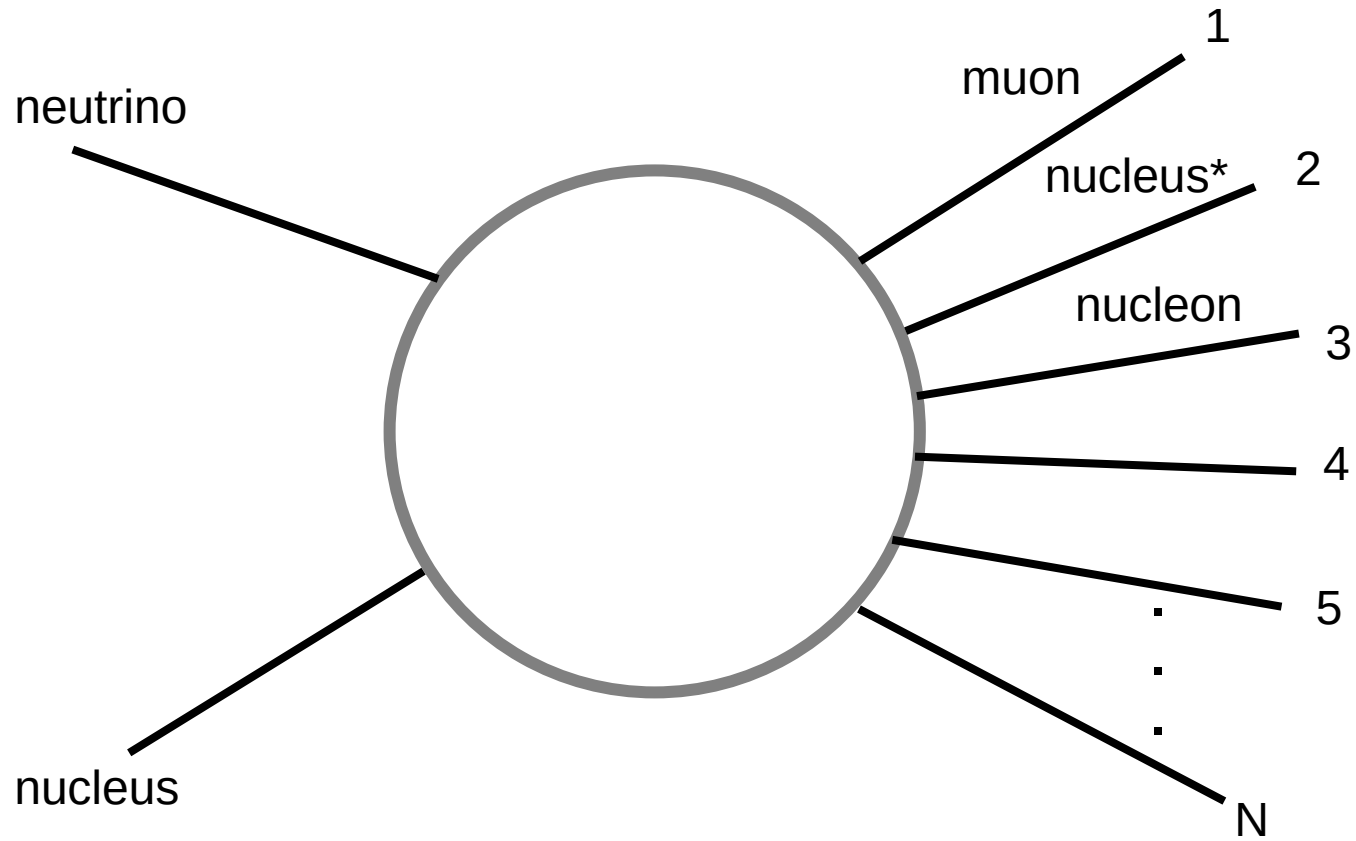
Final State



Two-pion production  
(impossible?)

Initial State

Final State



Impossible

# **Problem:**

**We are not able to model with accuracy any of the non-inclusive cross sections.**

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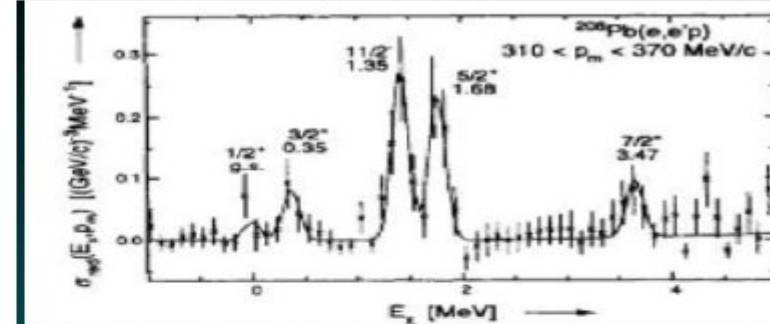
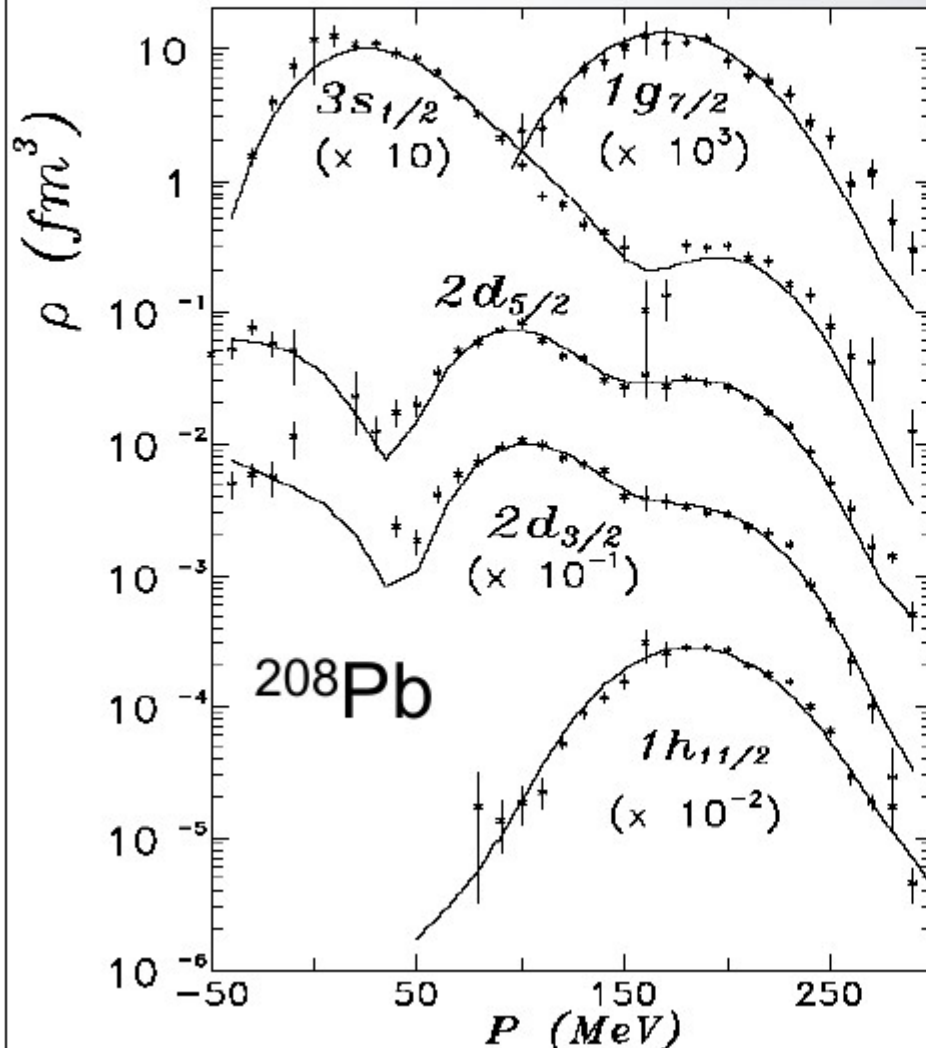
One exception:

**Exclusive**  $A(e,e'p)A-1$  in a narrow missing energy window (= one nucleon knock out from the outer shells)

# Exclusive $A(e,e'p)A-1$ in a narrow missing energy window (outer shells)



The RMF yields good agreement with exclusive  
(e,e'p) data JM Udias et al., PRC48, 2731 (1993), PRC51 3246 (1995)



Reasonably good agreement  
with data under exclusive  
kinematics  
spectroscopic factors are now a  
free parameter, fitted to data.  
RMF tend to imply larger  
spectroscopic factors.

	$3s_{1/2}$	$2d_{3/2}$	$1h_{11/2}$	$2d_{5/2}$	$1g_{7/2}$
Non rel. (Ref. [41])	50 %	53 %	42 %	44 %	19 %
Non rel. (Ref. [42])	55 %	57 %	58 %	54 %	26 %
Rel. (Refs. [40, 6])	70 %	72 %	64 %	60 %	30 %

## Conclusions and Outlook:

- + Modeling all reaction channels with high precision is (and will be) impossible.
- + Actually, we can describe very well only one channel: QE scattering with only one nucleon in the final state and small missing energy left in the residual nucleus,  $E_m < 20$  MeV.
  - ++ For such events, the **neutrino energy could be reconstructed with few percent accuracy.**  
(Van Orden and Donnelly, arXiv:1908.00932)
- + We are working on this.

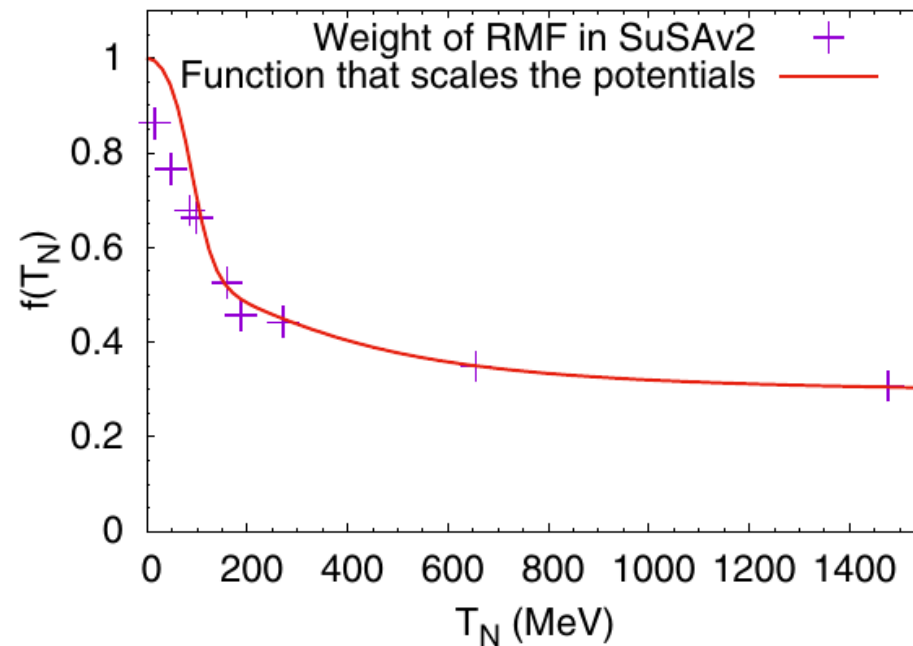
Back up slides



We have presented a **real energy-dependent potential** that can be used in a large energy range:

- + For low energies of the outgoing nucleons it is identical to RMF potential, thus: orthogonality, current conservation and dispersion relations are fulfilled.

- + The phenomenology suggests that for high energies of the outgoing nucleon the potential should become softer.



**New energy-dependent potential = RMF potential  $\times$   $f(T_N)$**

# Superscaling Approach

## Scaling phenomenon - definition

It happens when the inclusive cross section can be written as the product of a *single-nucleon* cross section times a specific function (*scaling function*) that depends on only one variable (*scaling variable*)

$$\star \frac{d\sigma^{(ee')}}{d\Omega_e d\omega} = \sigma_{Mott}(v_L R^L + v_T R^T), \quad R^{L,T} \text{ nuclear responses.}$$

$$\star \sigma_{SN} = \sigma_{Mott}(v_L \mathcal{R}^L + v_T \mathcal{R}^T), \quad \mathcal{R}^{L,T} \text{ single-nucleon responses.}$$

$$\frac{d\sigma^{(ee')}}{d\Omega_e d\omega} / \sigma_{SN} = F(q, \omega) \xrightarrow{q \rightarrow \infty} F(\Psi)$$

***Most of the models based on IA present scaling at some level.***

The scaling function incorporates itself all nuclear information.

## Scaling phenomenon

